

New insight on Jupiter's inner structure from seismic measurements

Patrick Gaulme, François-Xavier Schmider, Jean Gay, Tristan Guillot^{1,2}, Cédric Jacob

A&A **504**, A130 (2011)



¹ Observatoire de la Côte d'Azur, CNRS, Nice

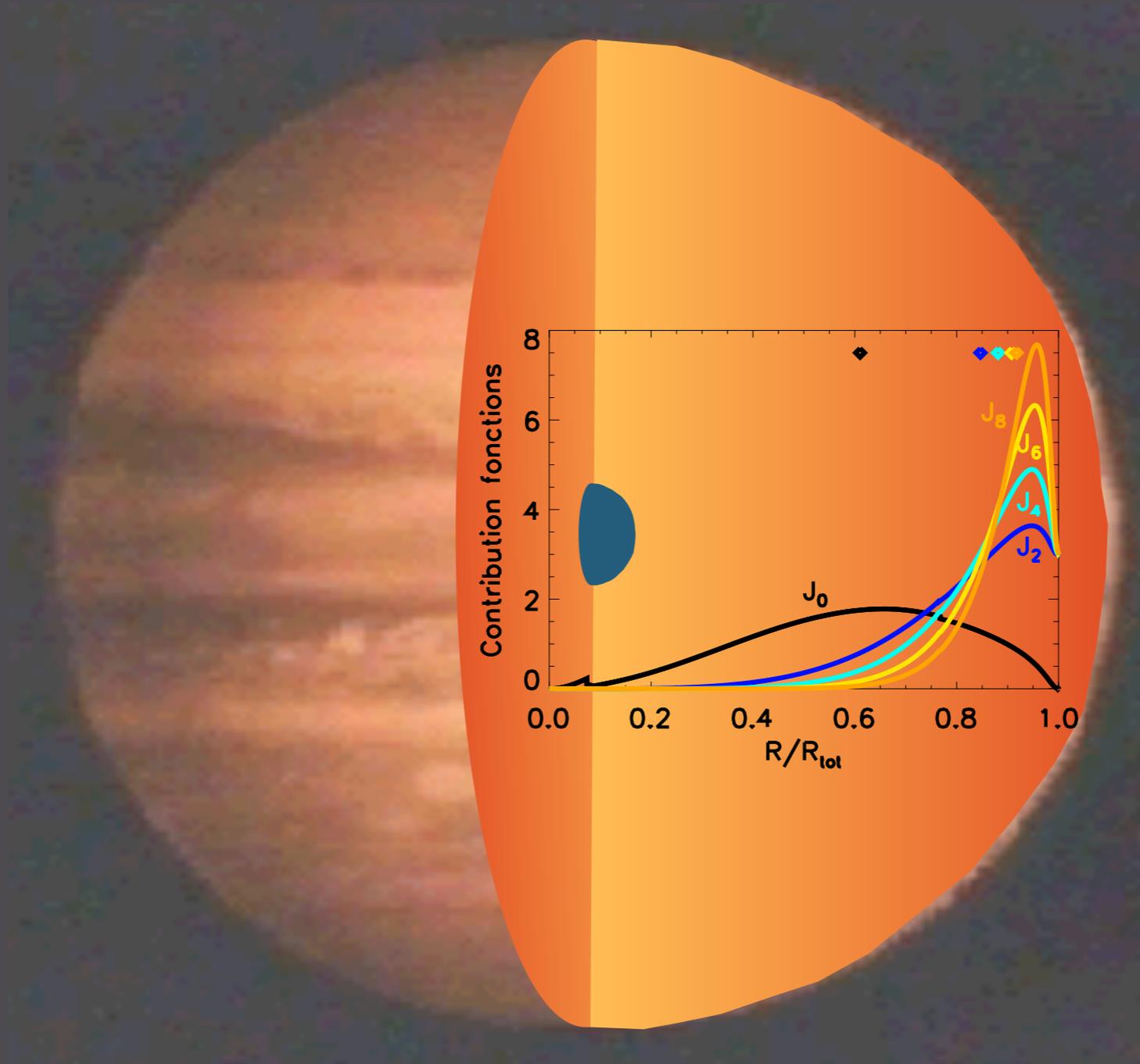
² UCSC, Santa Cruz, USA (Fulbright visiting prof)

Probing deep...

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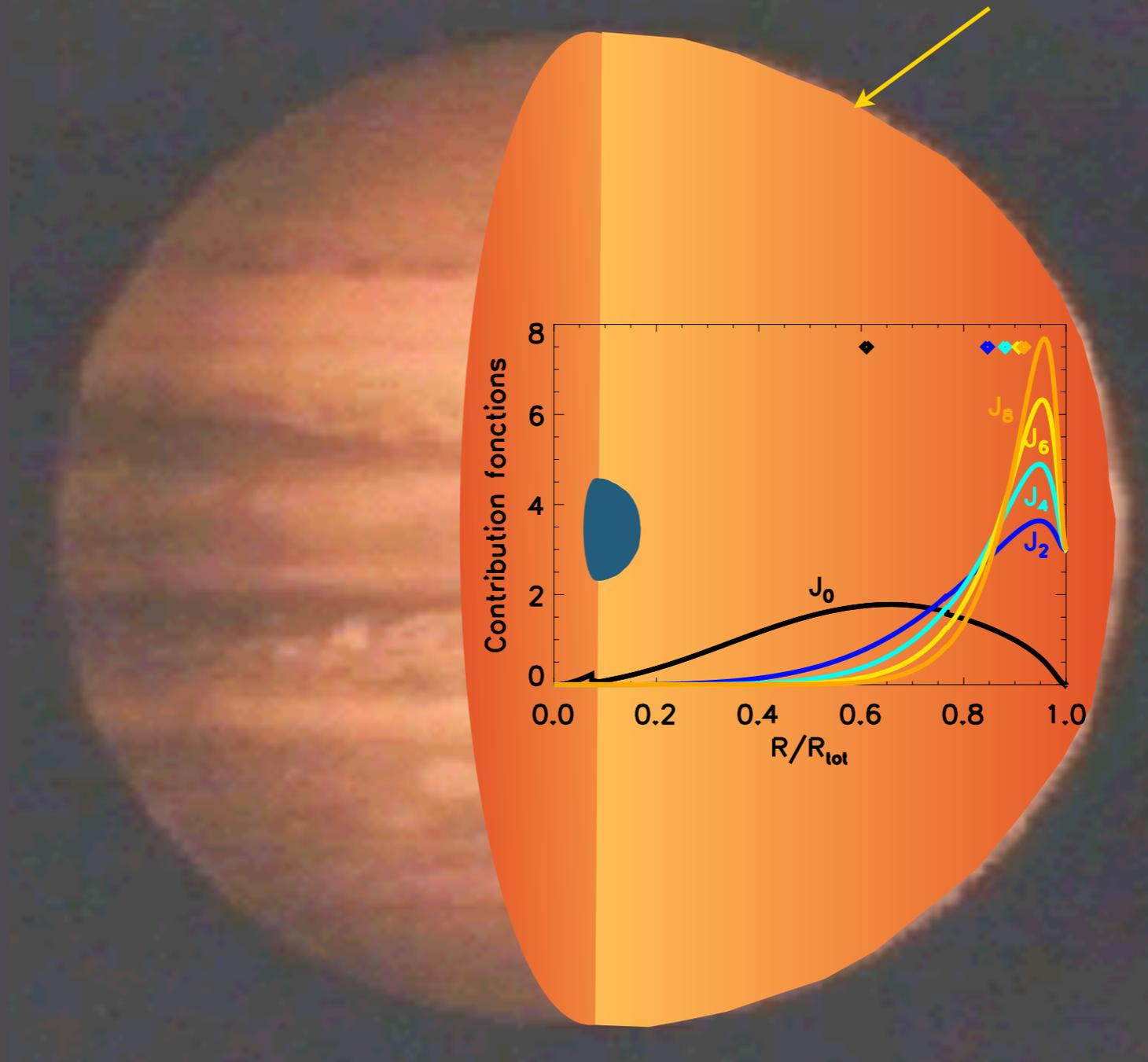


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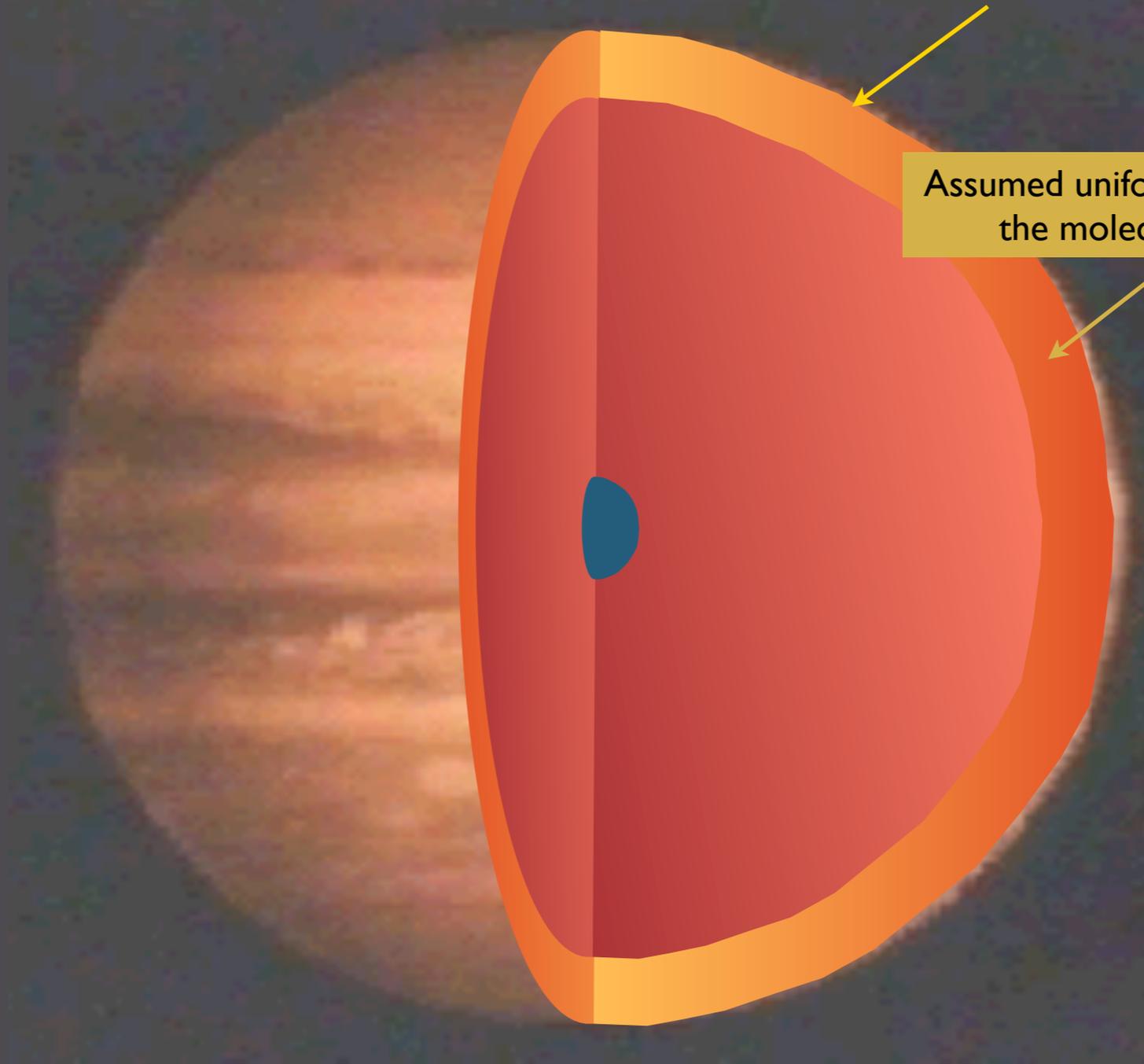
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skin-deep measurement of the composition



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Assumed uniform composition in
the molecular envelope

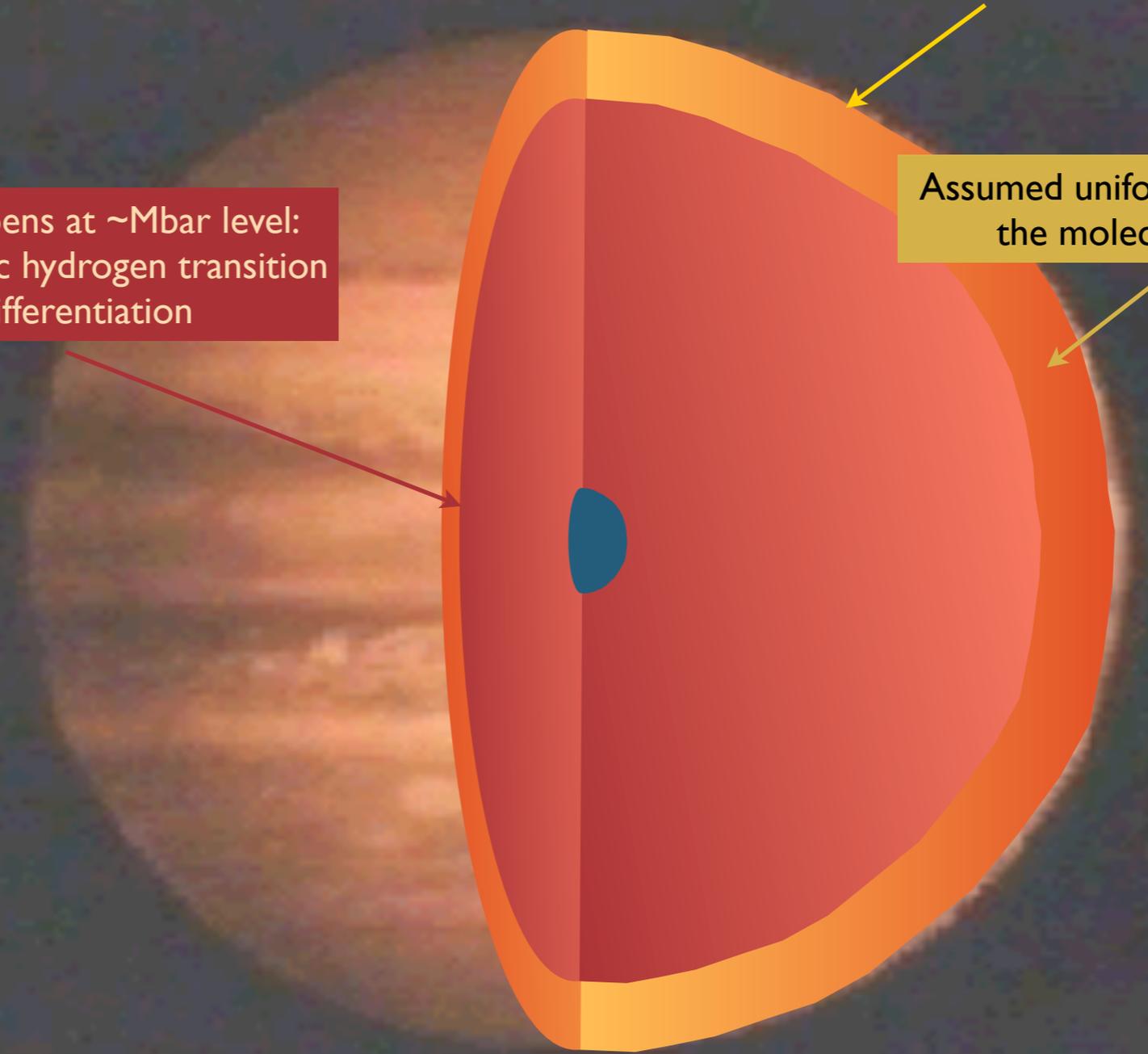


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Something happens at ~Mbar level:
molecular/metallic hydrogen transition
helium differentiation

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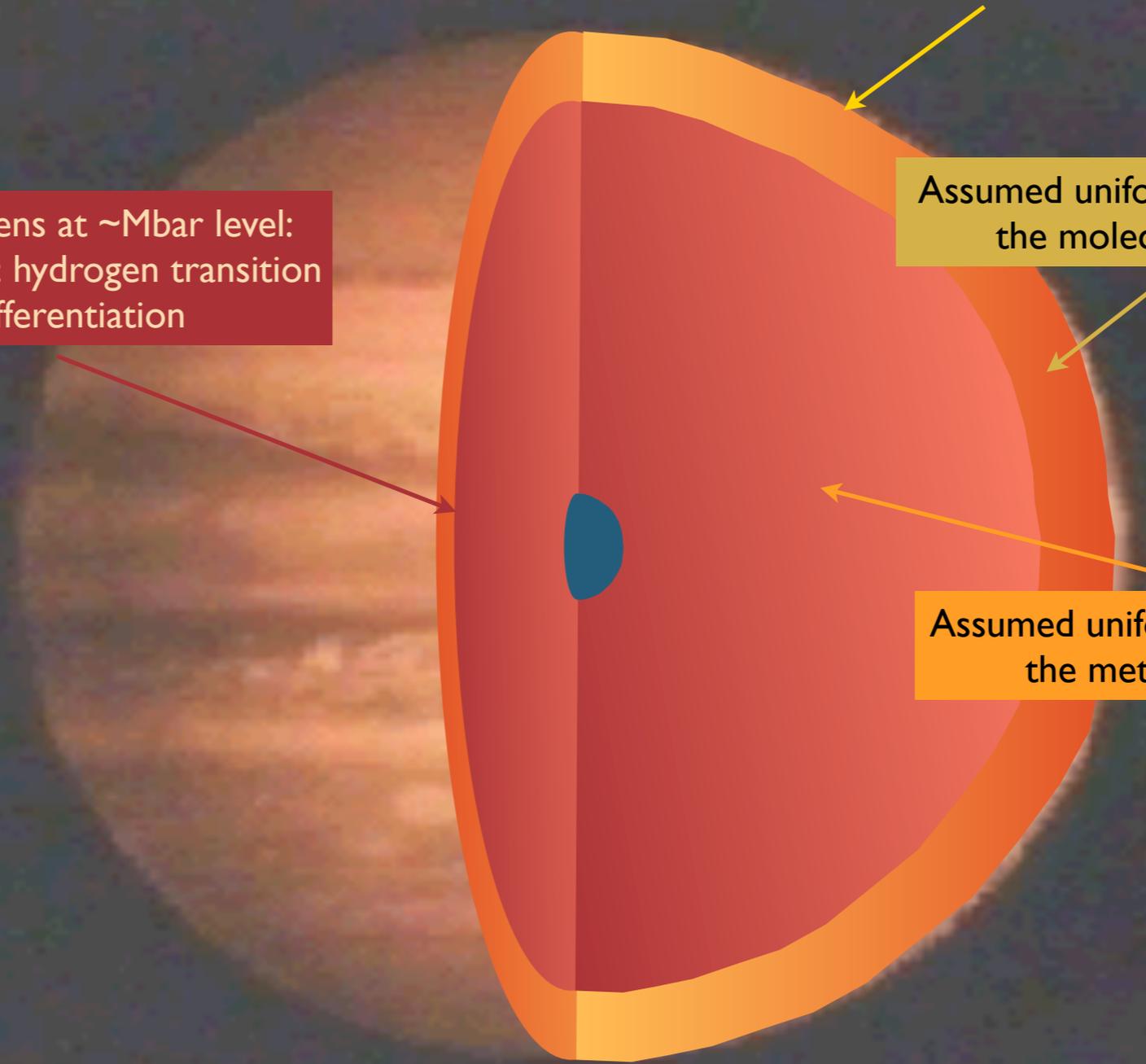
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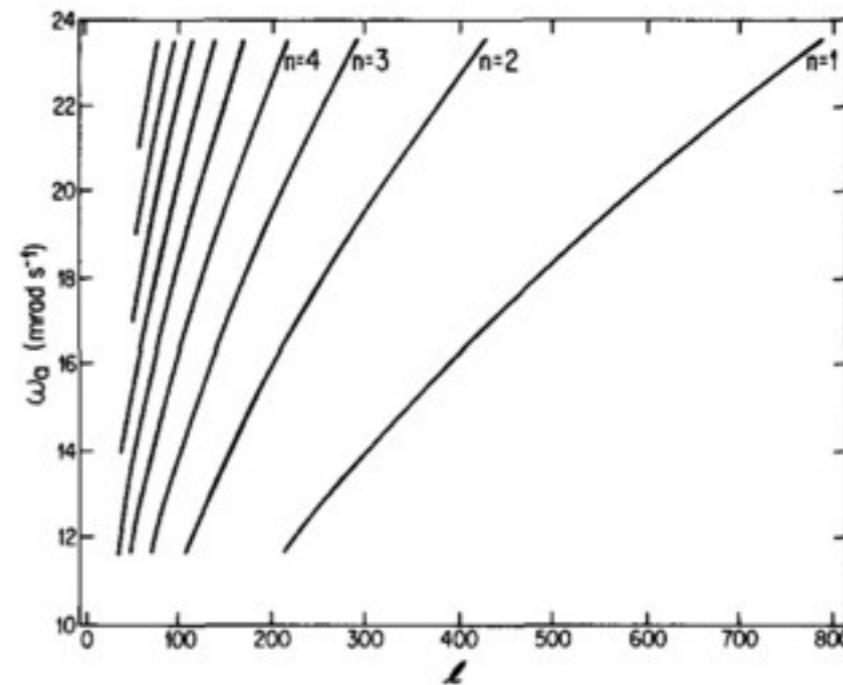
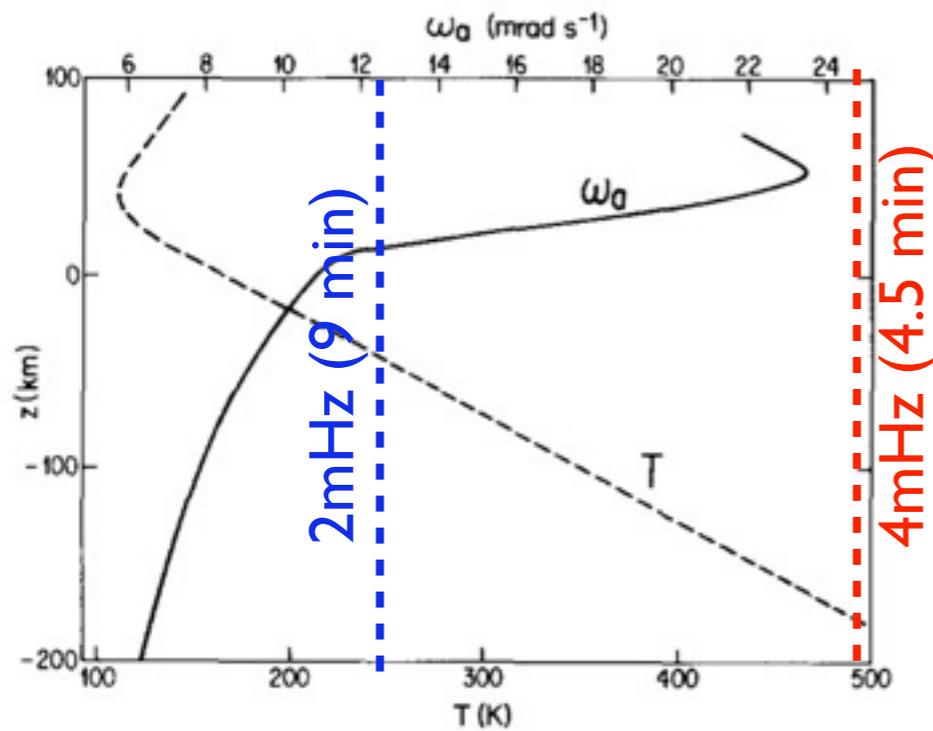
Assumed uniform composition in
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A central dense core is generally
needed to fit the measured
gravity field

Theoretical bases

Vorontsov et al. (1976) and subsequent work: identification of free oscillation modes

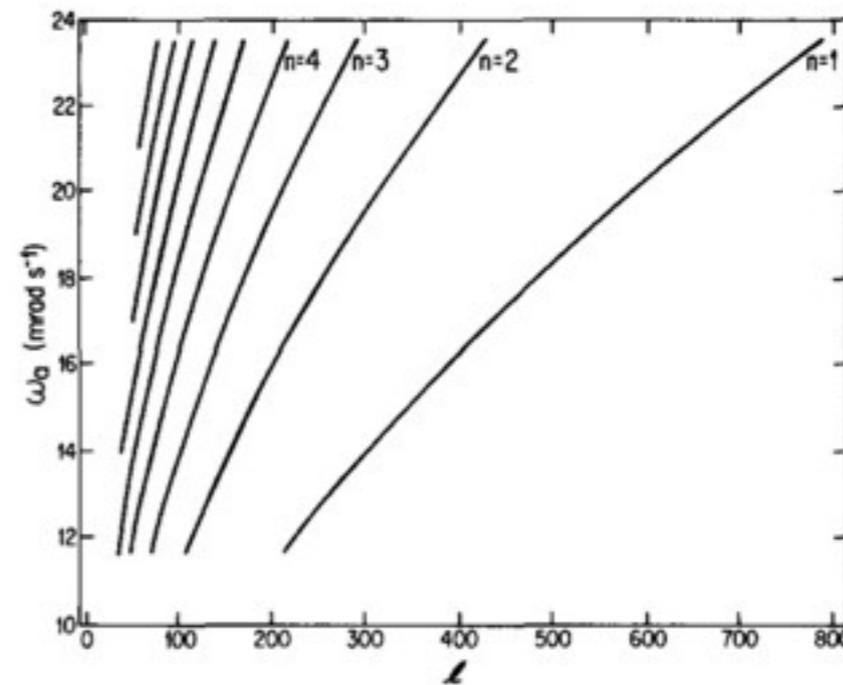
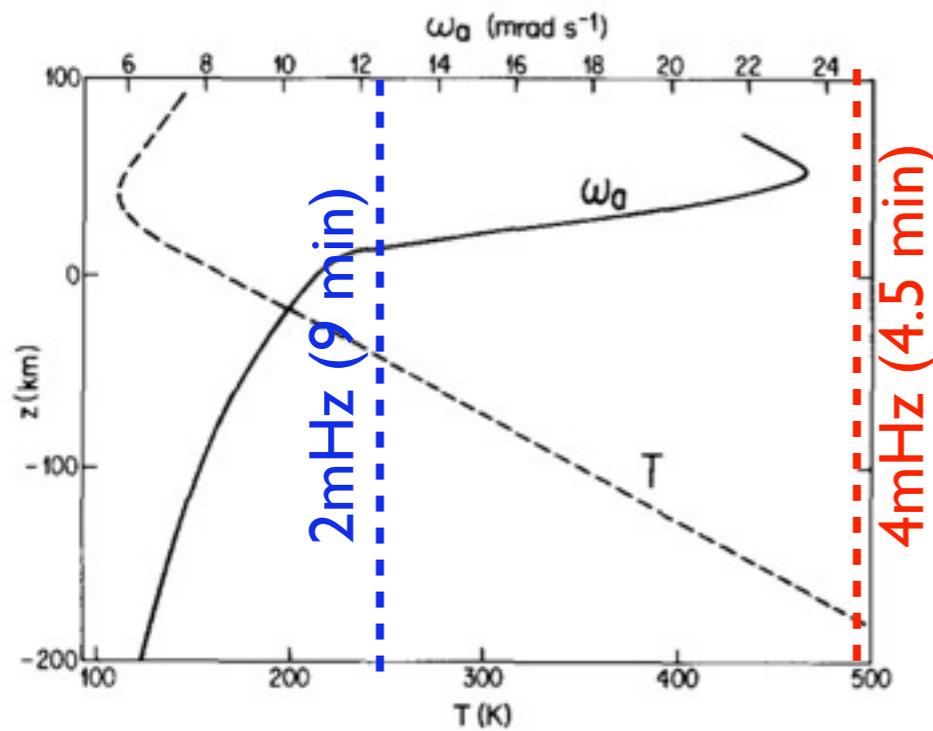
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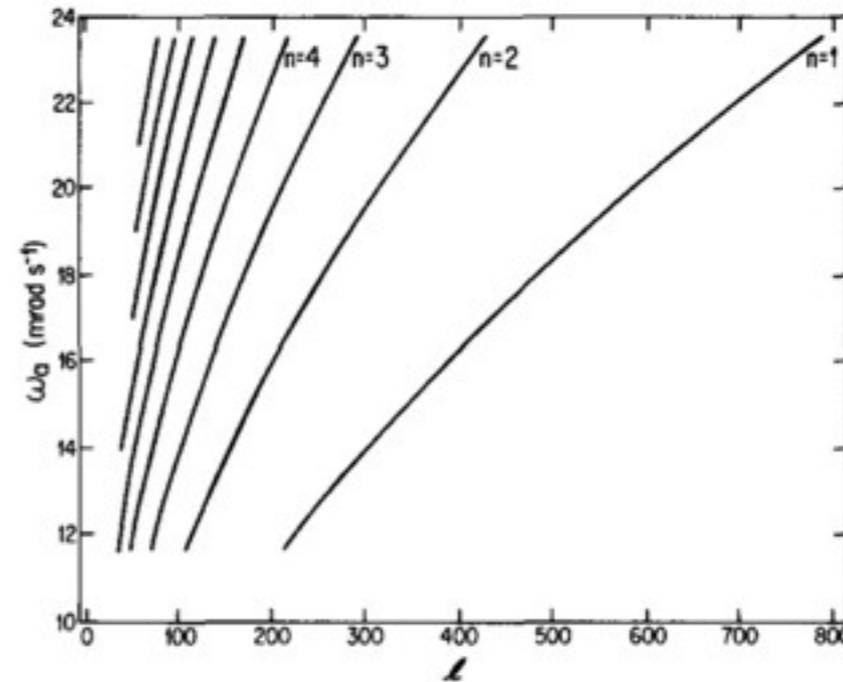
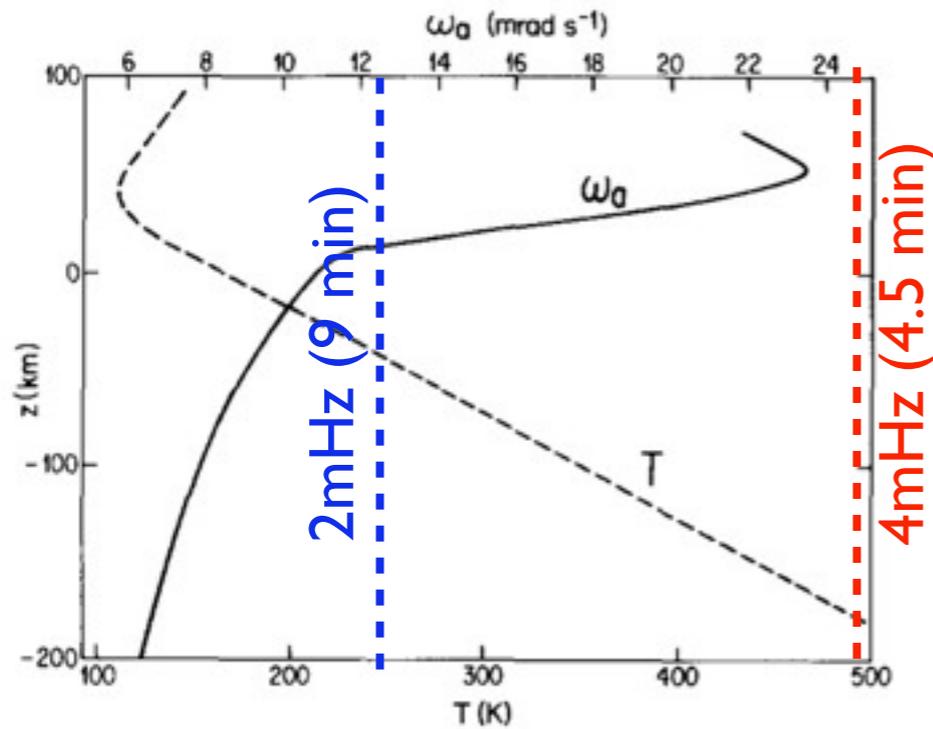


For eddy (or convective) velocities between 10 and 80 m sec^{-1} and length scales on the order of a scale height ($\sim 20 \text{ km}$ at the 1-bar level), the periods of turbulent motions match well with the standing wave periods (4.5–9 min).

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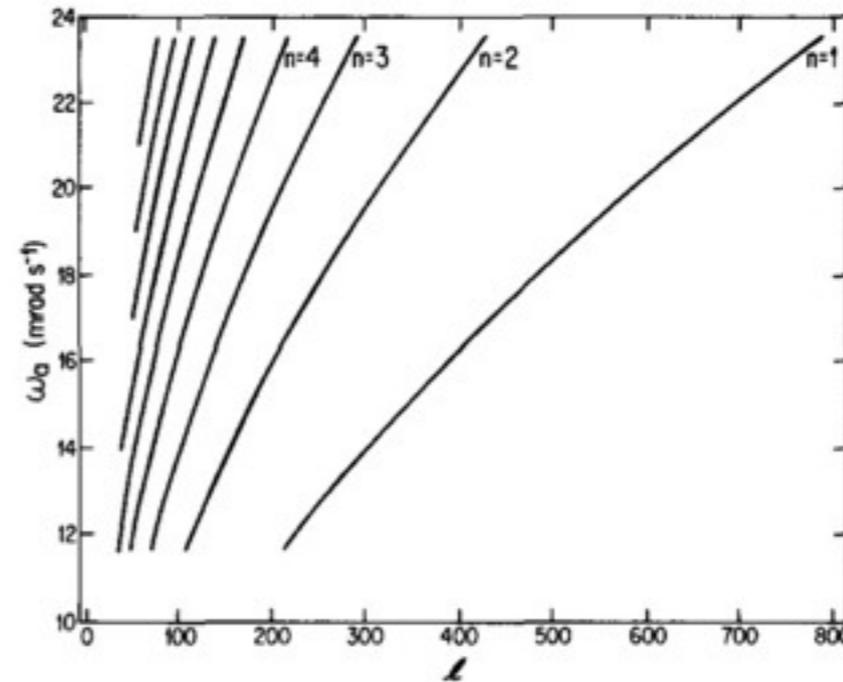
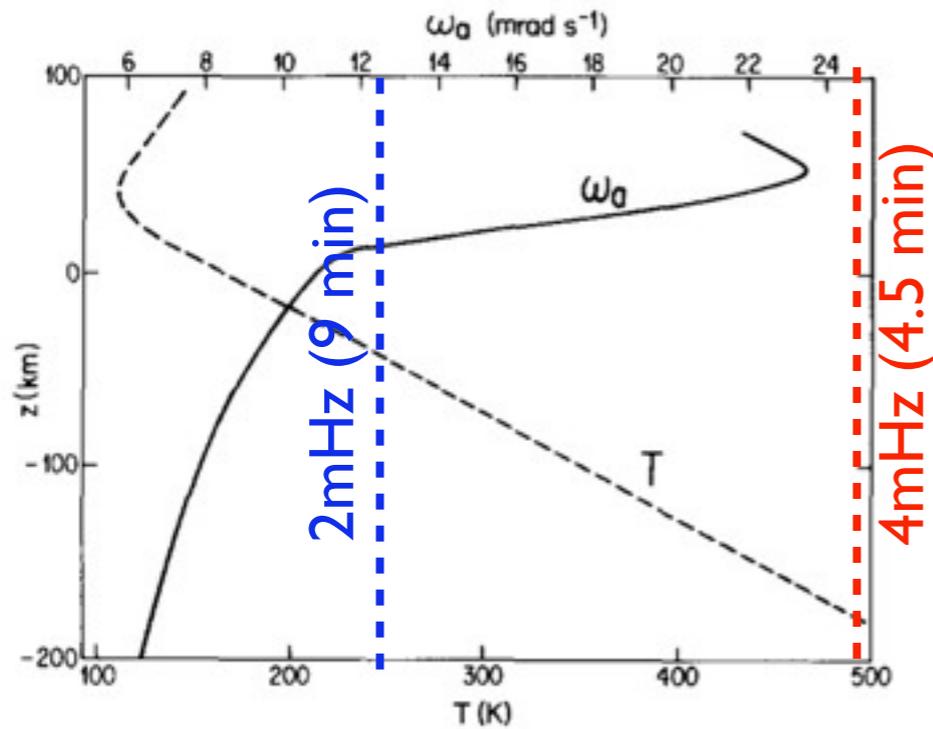
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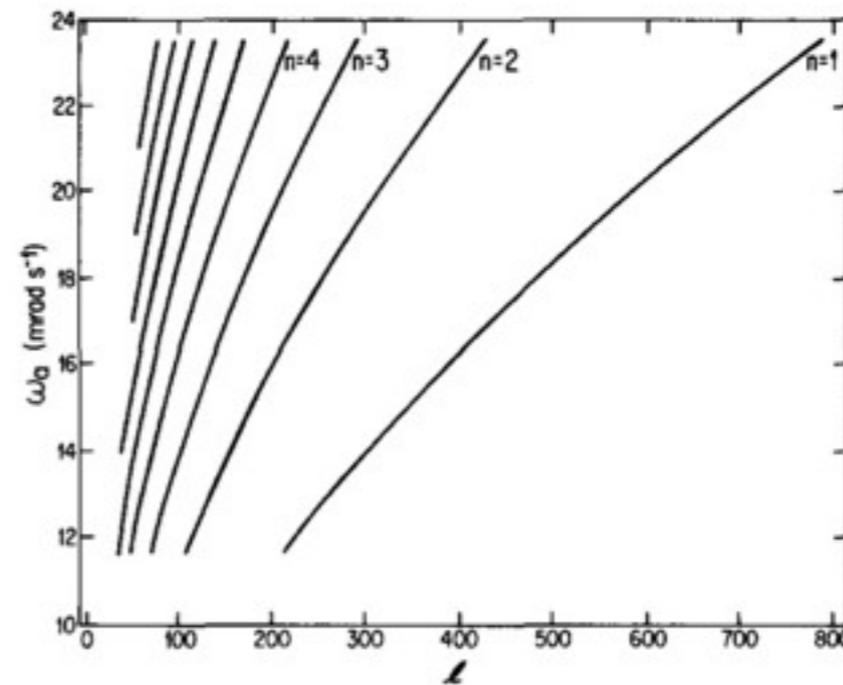
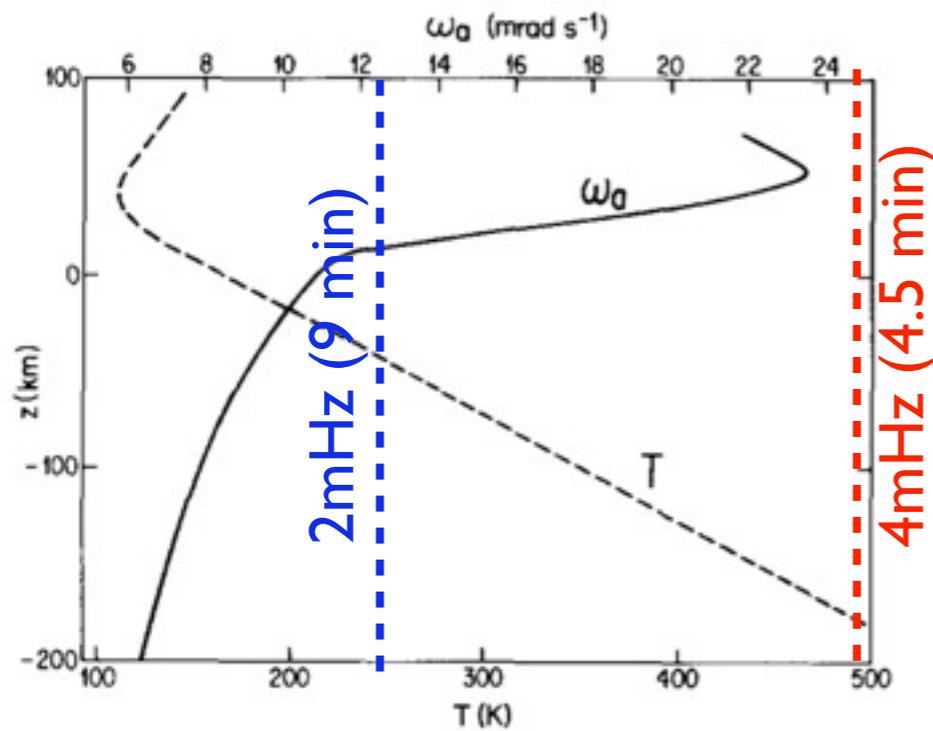
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$$\Rightarrow u_0 \sim 0.5 \text{ m/s}$$

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 - $T_{\text{lifetime}} \sim T_{\text{mode}} (F_w / \epsilon F_{\text{tot}}) \sim 10 \text{ mn} (25000 / (13600 \times 1\%)) \sim 1.3 \text{ days}$

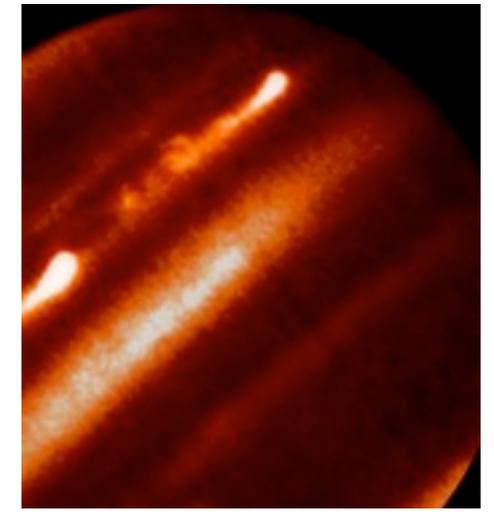
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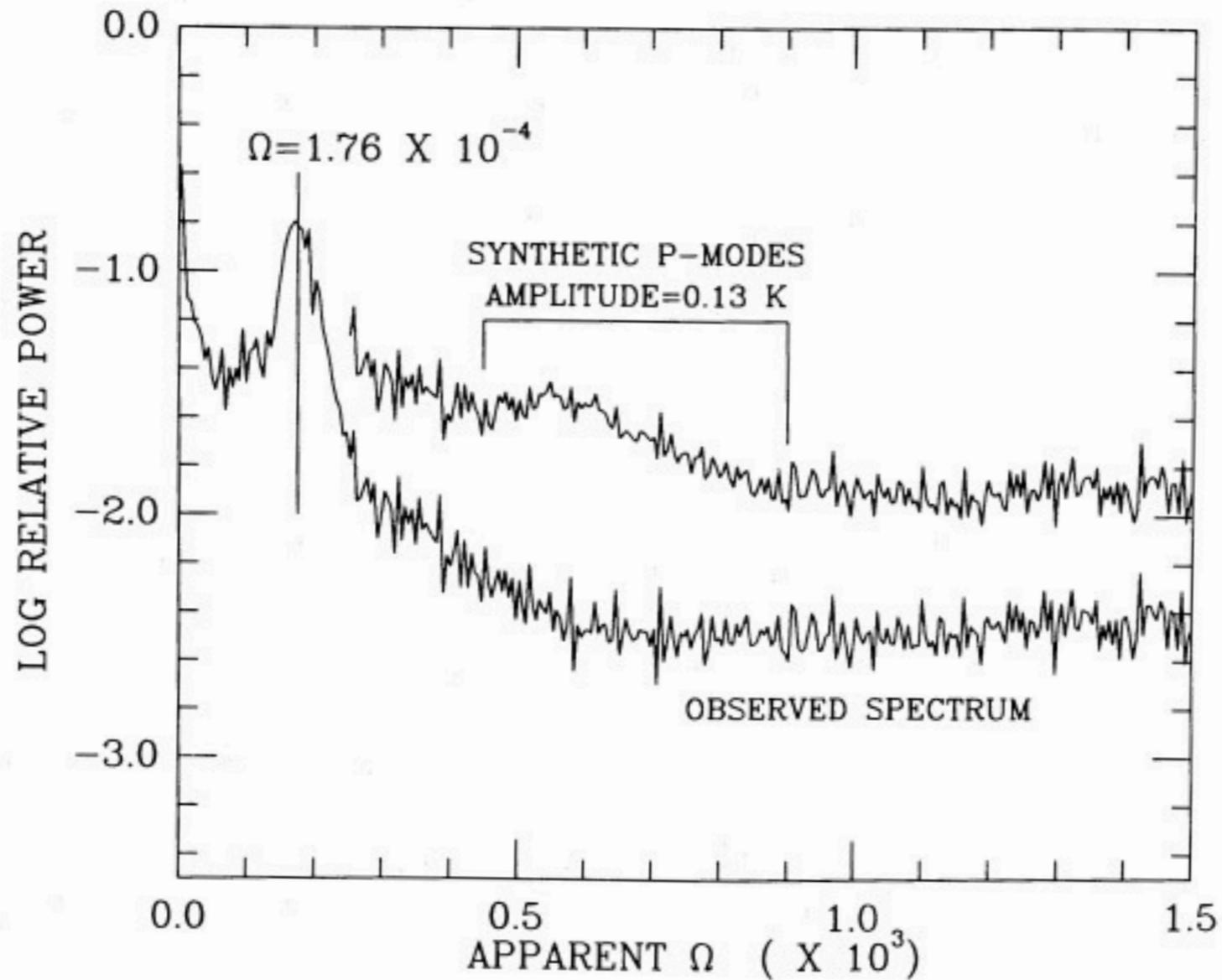
Bercovici & Schubert (1987): Trapped high degree acoustic waves (form + excitation)

Standing acoustic waves, with periods between about 4.5 and 9 min, may be trapped in a wave duct beneath Jupiter's tropopause. Detection of these oscillations by observations of Doppler shifting of infrared and ultraviolet absorption lines would offer a new and important method for probing the giant planet's deep atmosphere and interior. Information would be revealed on Jupiter's thermal and density structure and the depth to which its zonal winds penetrate. Standing oscillations in the molecular hydrogen envelope are modeled and their theoretical eigenfrequencies are presented as they might appear in actual data analysis. Several forcing functions for wave generation are considered. These include coupling with turbulent and convective motions, thermal overstability due to radiative transfer, effects of wave propagation in a saturated atmosphere, and consequences of *ortho*- to *para*hydrogen conversion. Although the forcing mechanisms couple well with the acoustic waves, allowing for possible maintenance of the oscillations, the contribution they make to velocity amplitudes is very small, between 1.0 and 0.1 m sec⁻¹. This implies that the Doppler shifting caused by the waves may be unresolvable except, perhaps, by methods of superposing time records of oscillations to enhance acoustic signals and diminish random noise. © 1987 Academic Press, Inc.

IR Observation



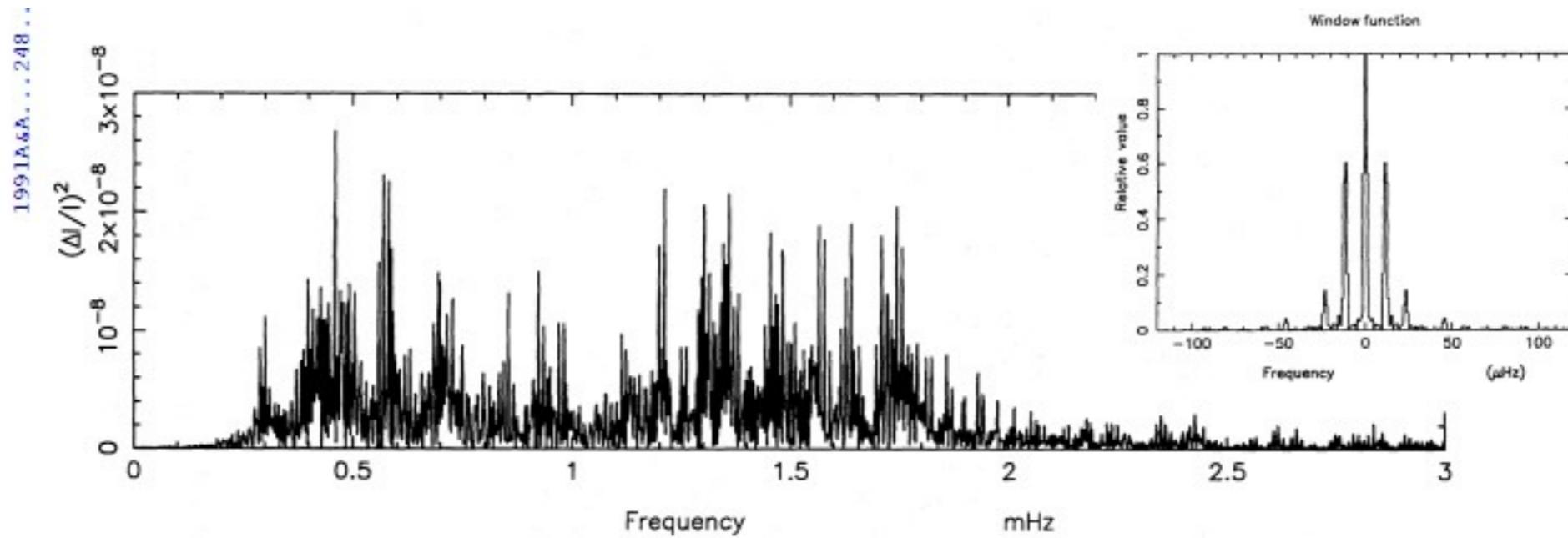
IRTF



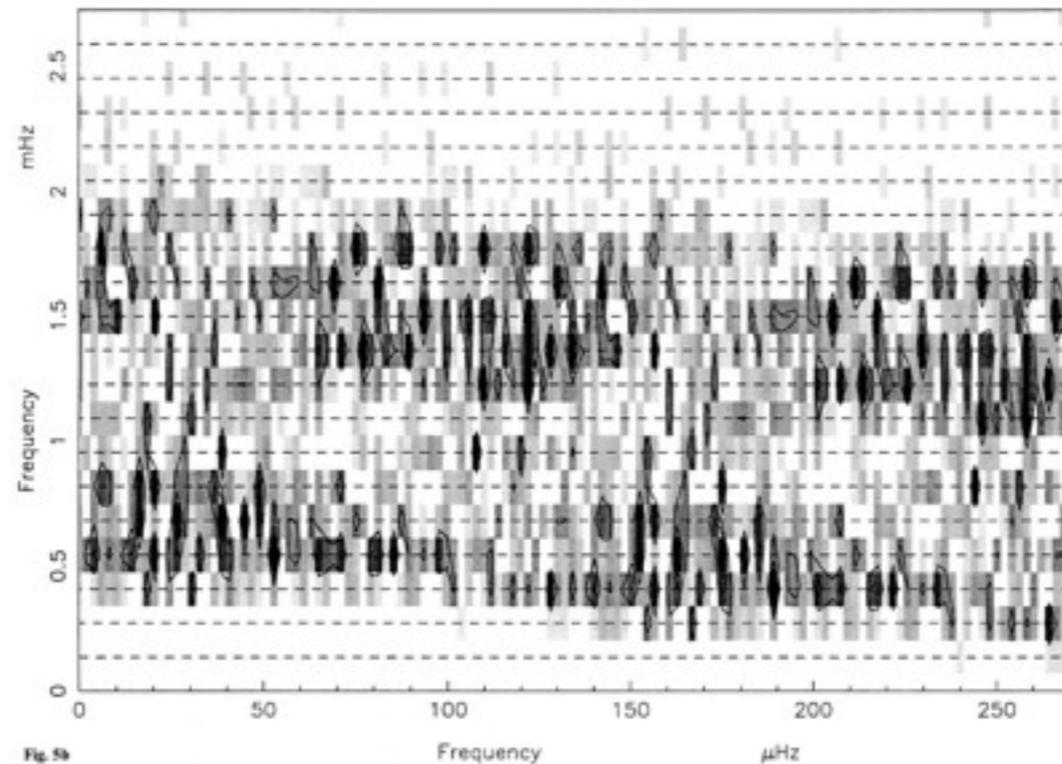
Deming et al. (1989)

No oscillation at the 0.07K level, equivalent to ~ 1 m/s velocity

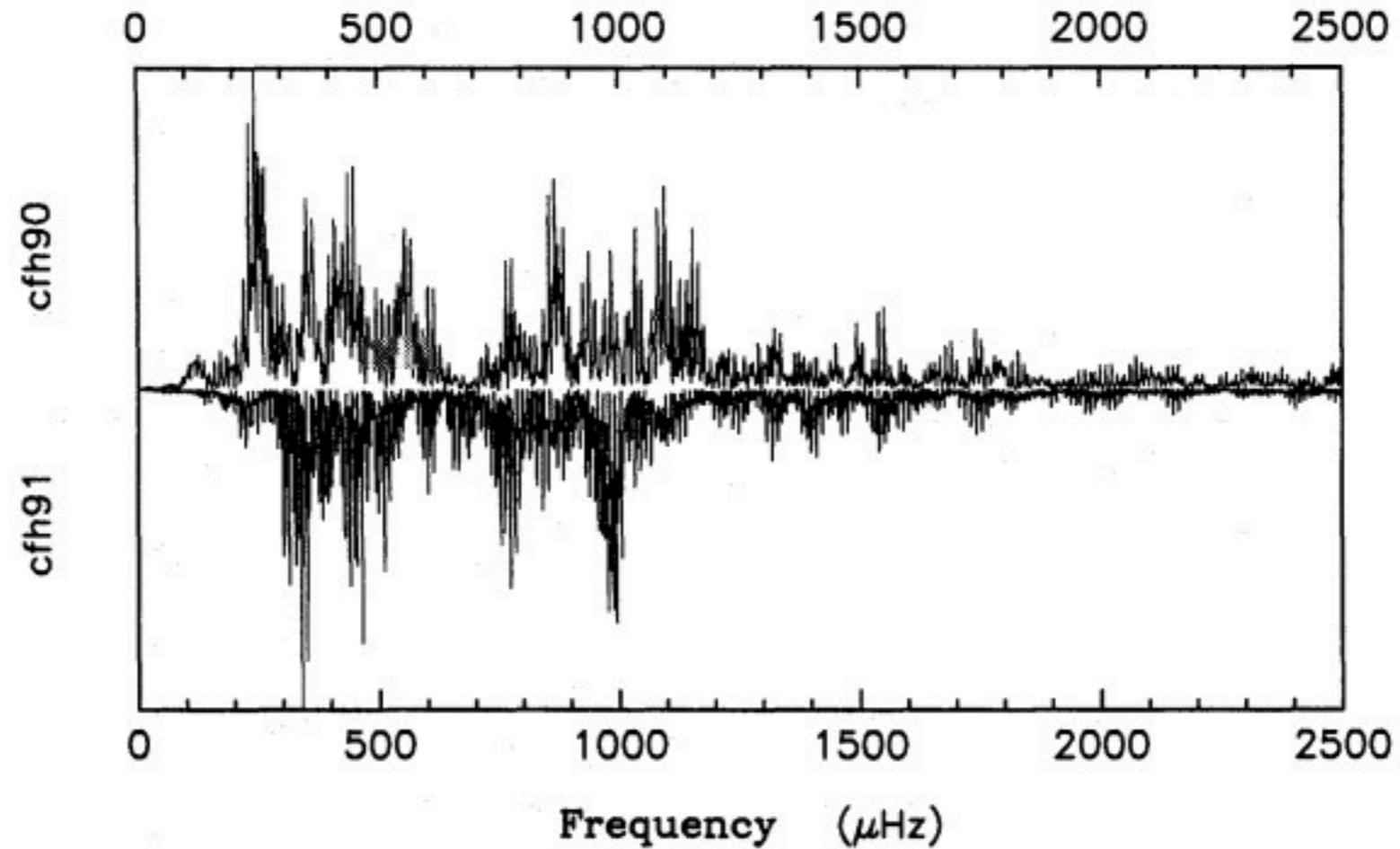
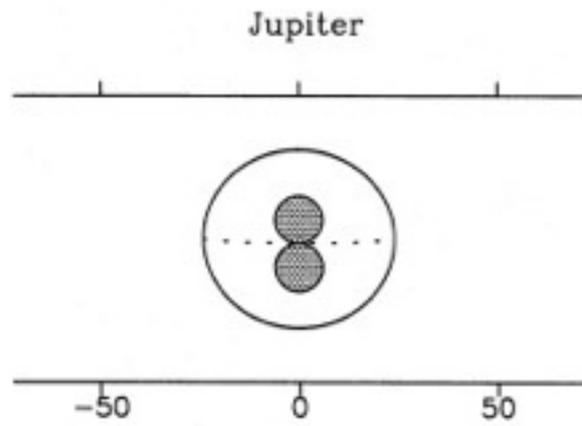
Doppler shift observations



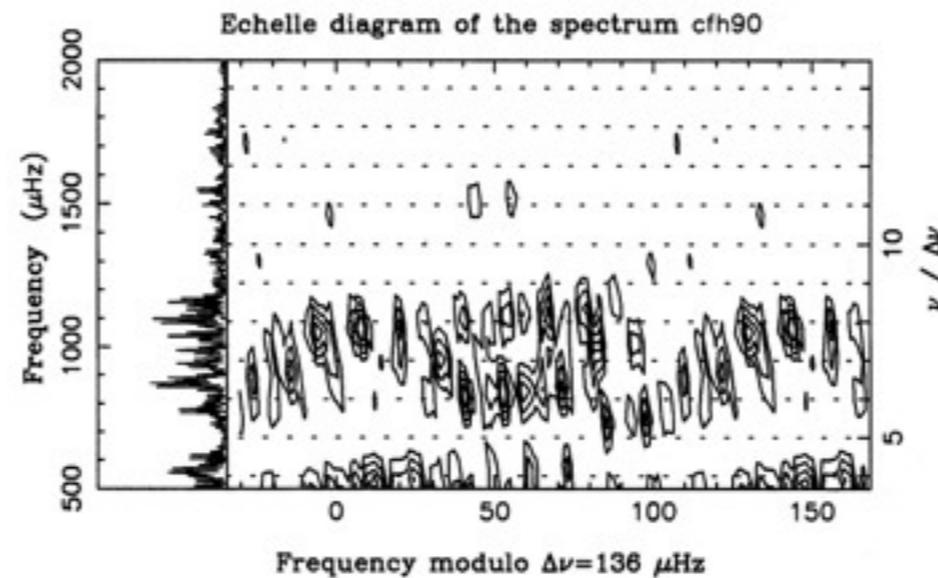
Schmider et al. (1991)



Fourier Transform Spectrometer Observations



Mosser et al. (1993)



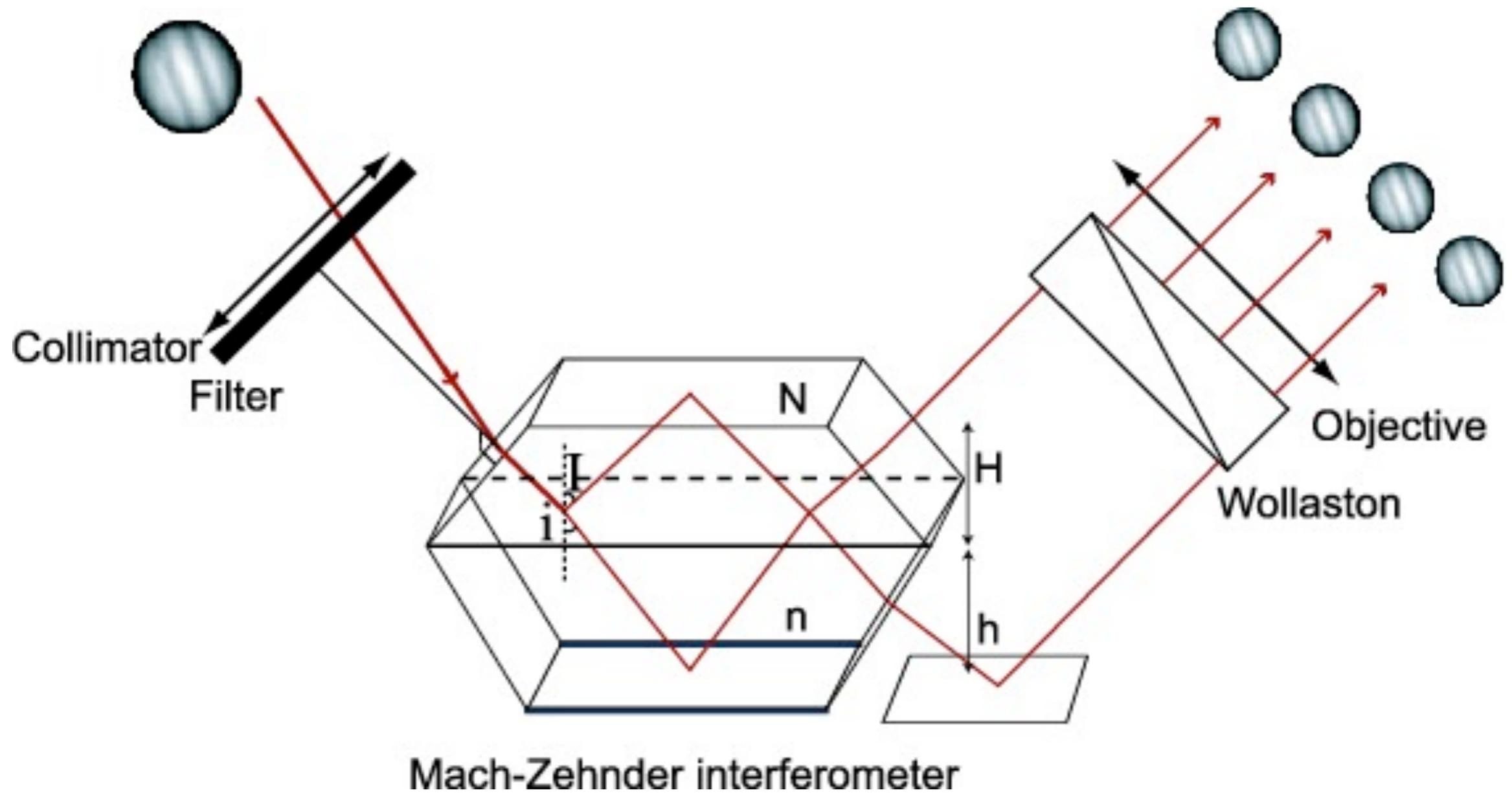
Other works

- **Marley & Porco (1992)**: Resonance of f-modes, possible gaps in Saturn's rings
- **Provost et al. (1993)**: Asymptotic calculation with jovian core
- **Lee (1993)**: Non-perturbative approach including rotation
- **Mosser et al. (1994)**: Link with the observables
- **Gudkova et al. (1995)**: Influence of the troposphere & core, inverse problem
- **Lederer & Marley (1995)**: Power spectrum contaminated by albedo features at $f < 700$ mHz, but not above

SYMPA

Seismographic Imaging Interferometer for Monitoring of Planetary Atmospheres

Magnesium triplet: 517nm

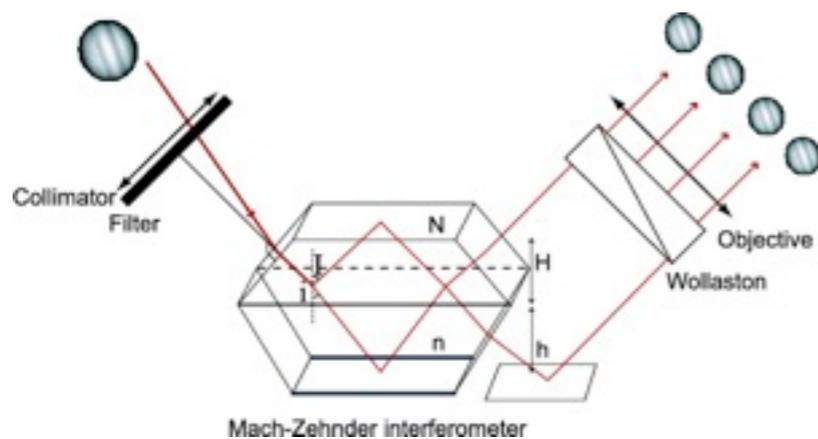


Schmider et al. A&A (2007)
Gaulme et al. A&A (2008)

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fringe contrast

$$I_1(x, y) = \frac{I_0(x, y)}{4} [1 - \gamma \cos \phi(x, y)]$$

$$I_2(x, y) = \frac{I_0(x, y)}{4} [1 - \gamma \sin \phi(x, y)]$$

$$I_3(x, y) = \frac{I_0(x, y)}{4} [1 + \gamma \cos \phi(x, y)]$$

$$I_4(x, y) = \frac{I_0(x, y)}{4} [1 + \gamma \sin \phi(x, y)]$$

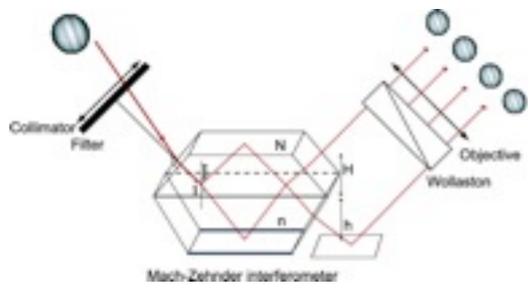
wave phase map: $\phi(x, y) = 2\pi\sigma_0\Delta(x, y) \left(1 + \frac{v_D}{c}\right)$

$$U = \frac{I_1 - I_3}{I_1 + I_3} \propto \gamma \cos \phi$$

$$V = \frac{I_2 - I_4}{I_2 + I_4} \propto \gamma \sin \phi$$

$$Z = U + iV \propto \gamma e^{i\phi}$$

$$Z_{J,\text{flat}} = Z_{\text{jup}} \times Z_0^* \times Z_{J,\text{rot}}^* Z_{E,\text{rot}}^* \times Z_{E/J}^* \times Z_{J/S}^* \\ \propto \exp\left(i4\pi\sigma_0\Delta\frac{v_{\text{osc}}}{c}\right)$$



SYMPA

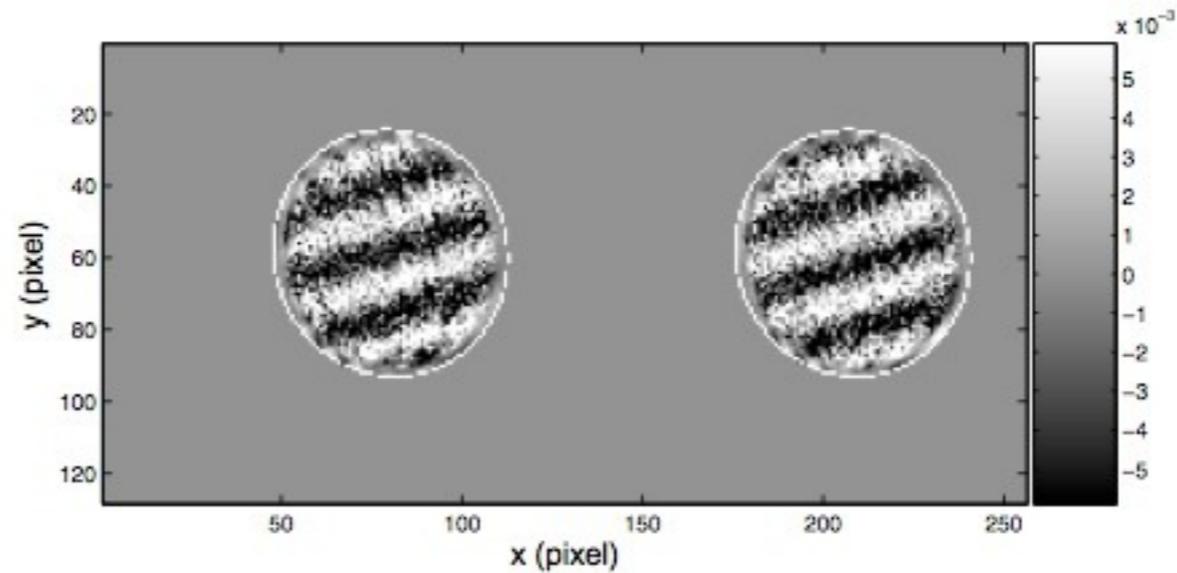
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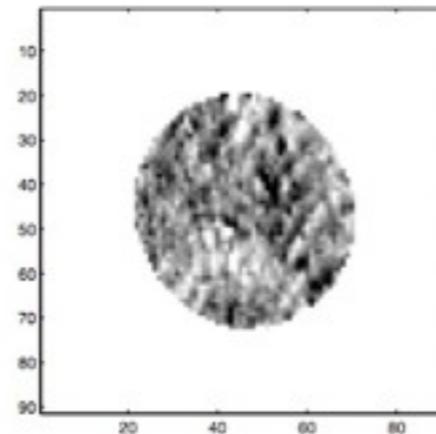
$$\propto \exp\left(i4\pi\sigma_0\Delta\frac{v_{osc}}{c}\right)$$

Jupiter's rotation:

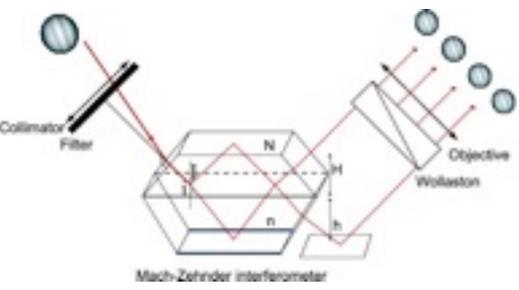
$$Z_{j,rot} = Z_{jup} \times Z_0^*$$



Final velocity map
(averaged over 5 mins):

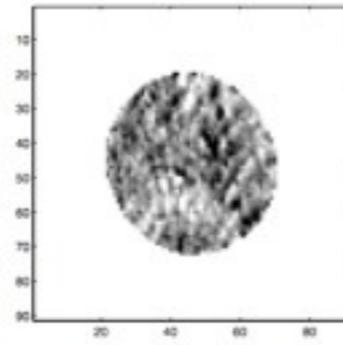


Gaulme et al. A&A (2008)

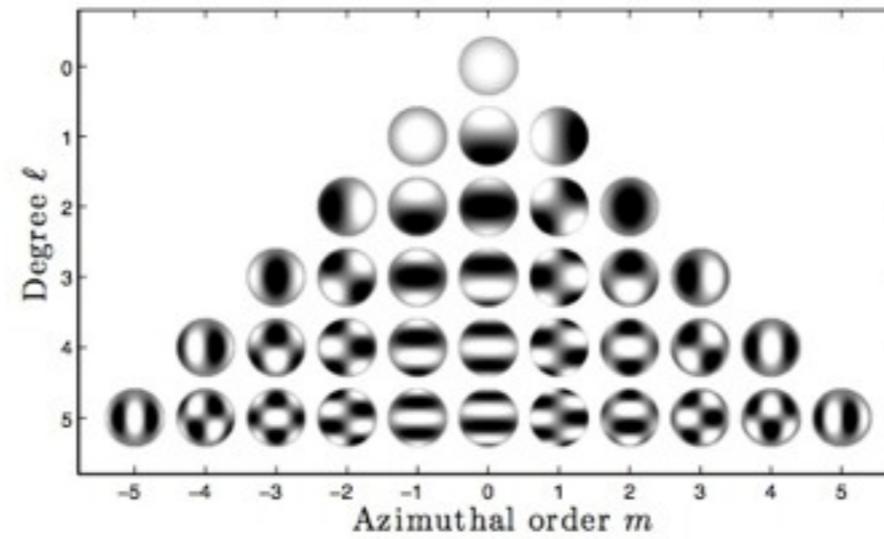


SYMPA: data analysis

velocity map

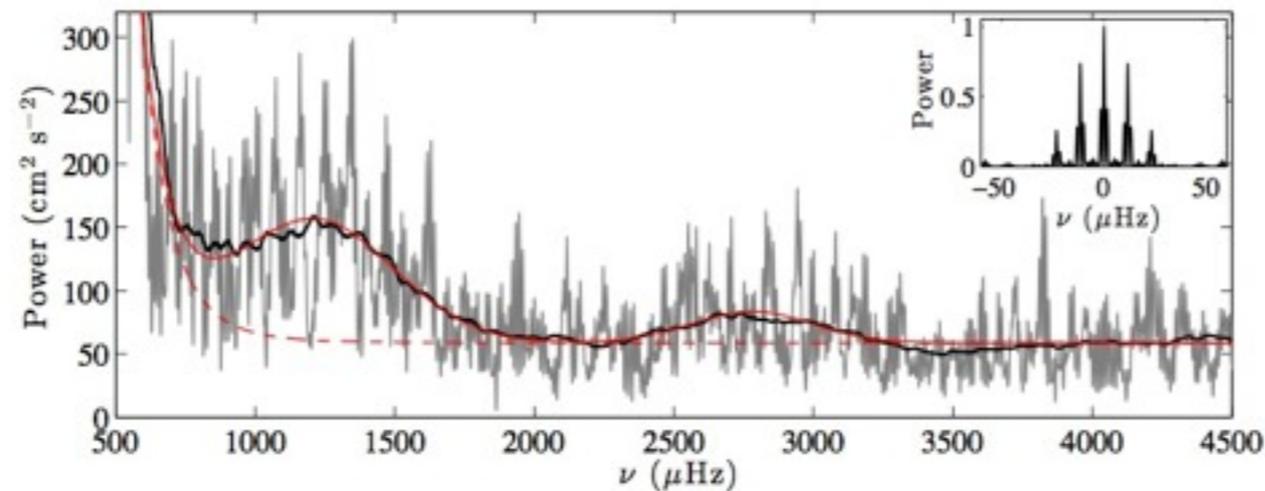


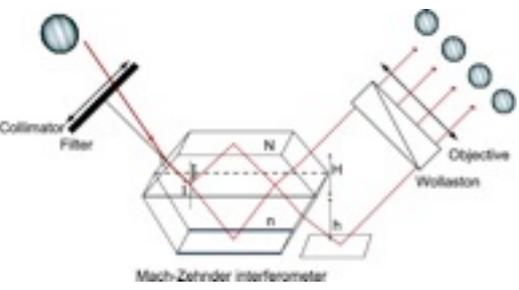
Y_{lm} basis:



Sum of the time series $l,m=1,0$ & $l,+/-1$

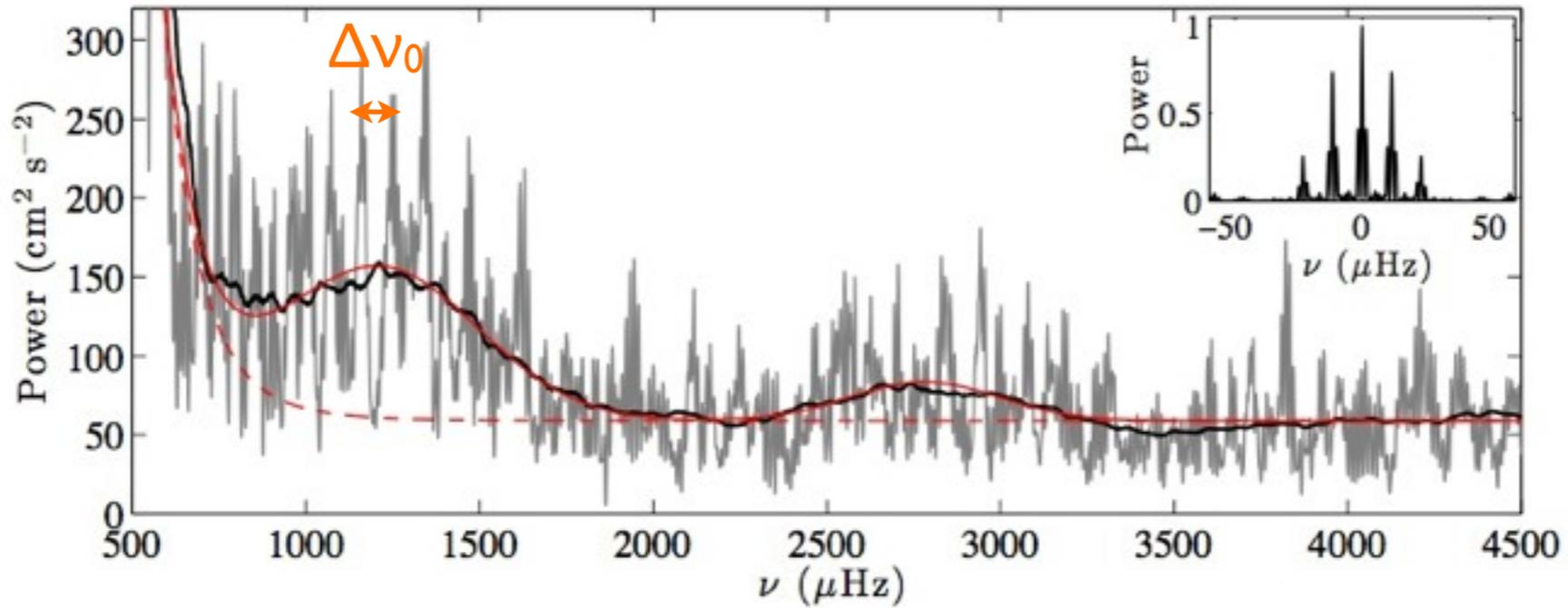
Power spectrum:





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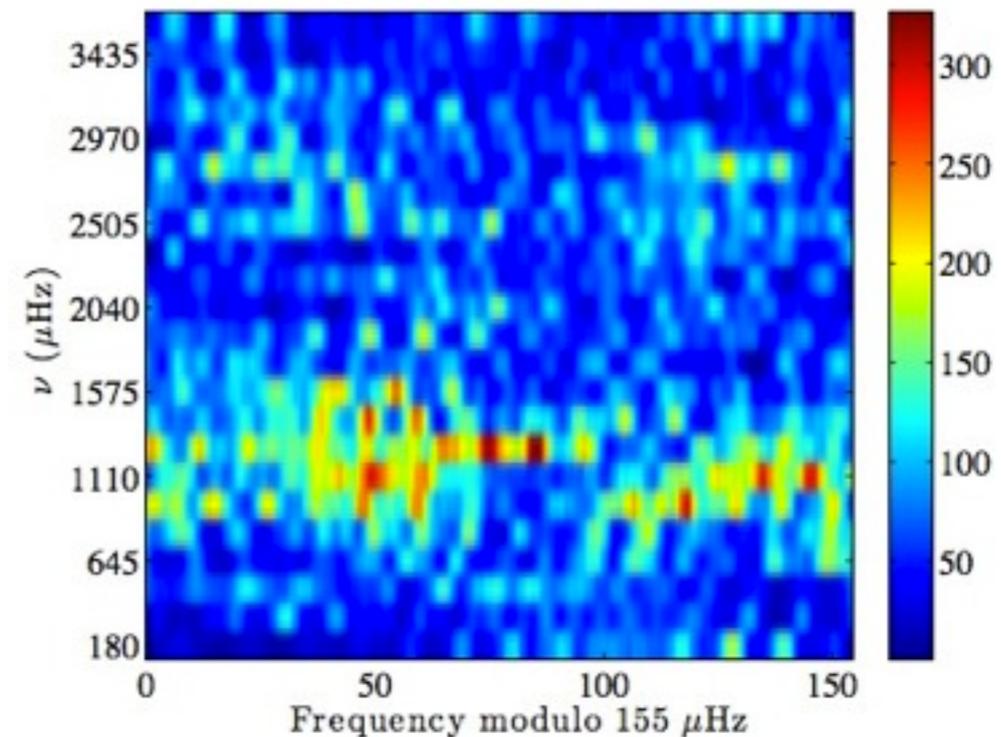
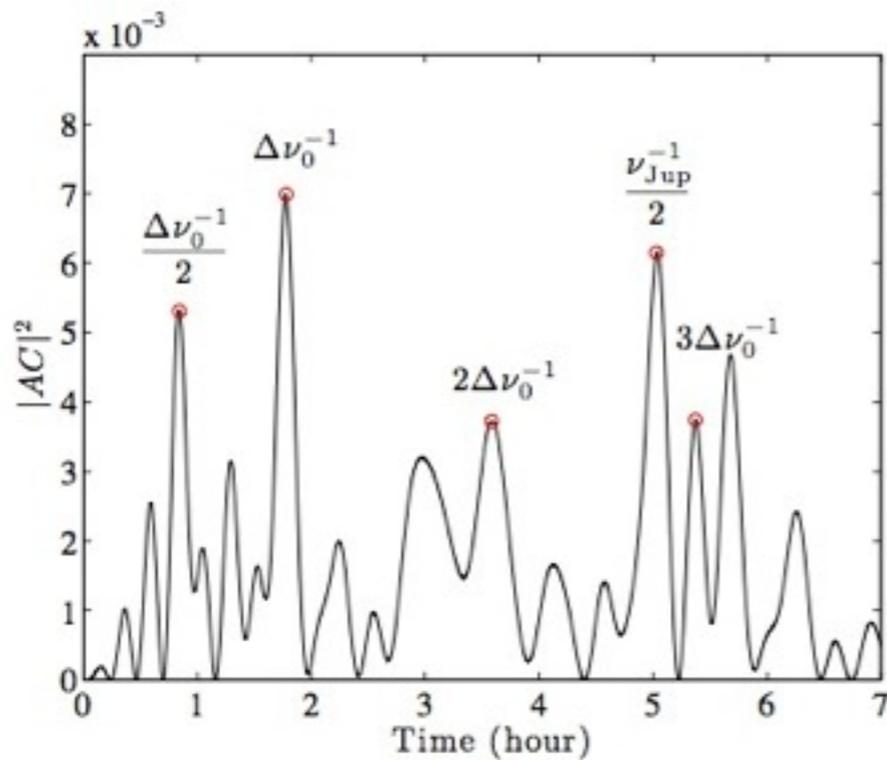
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Power spectrum of the power spectrum:

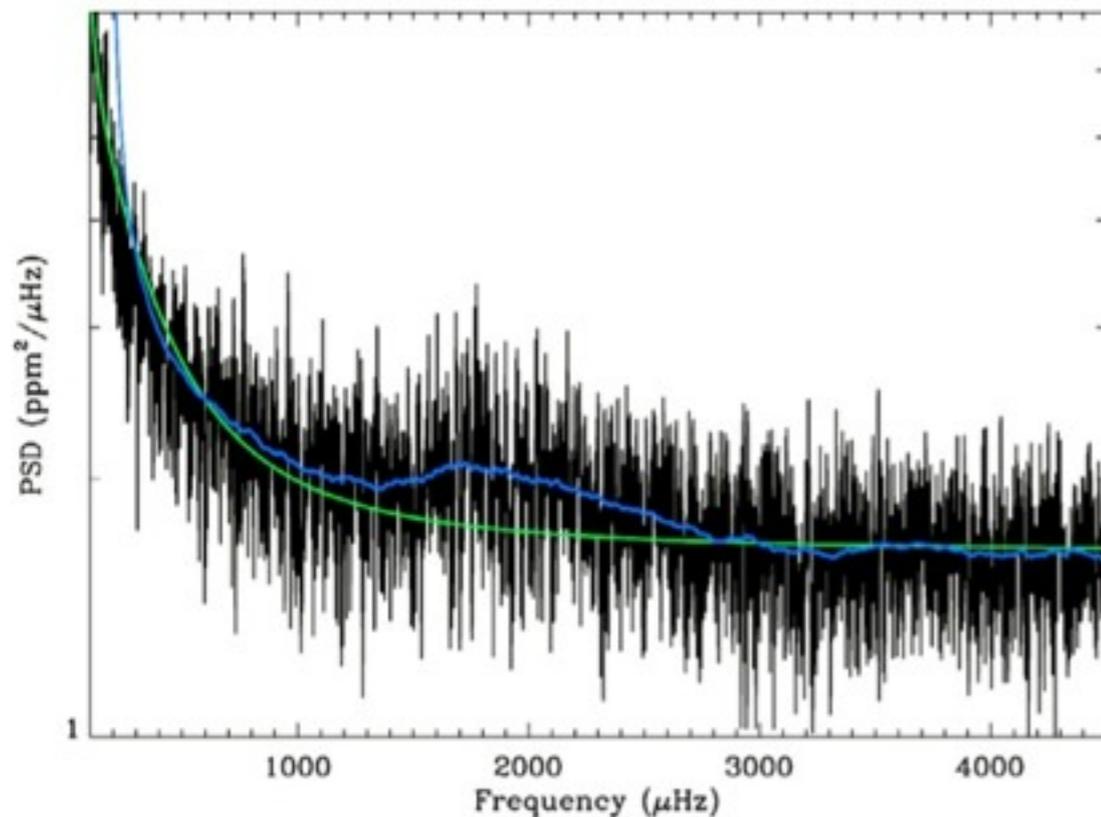
Gaulme et al. A&A (2011)

Echelle diagram

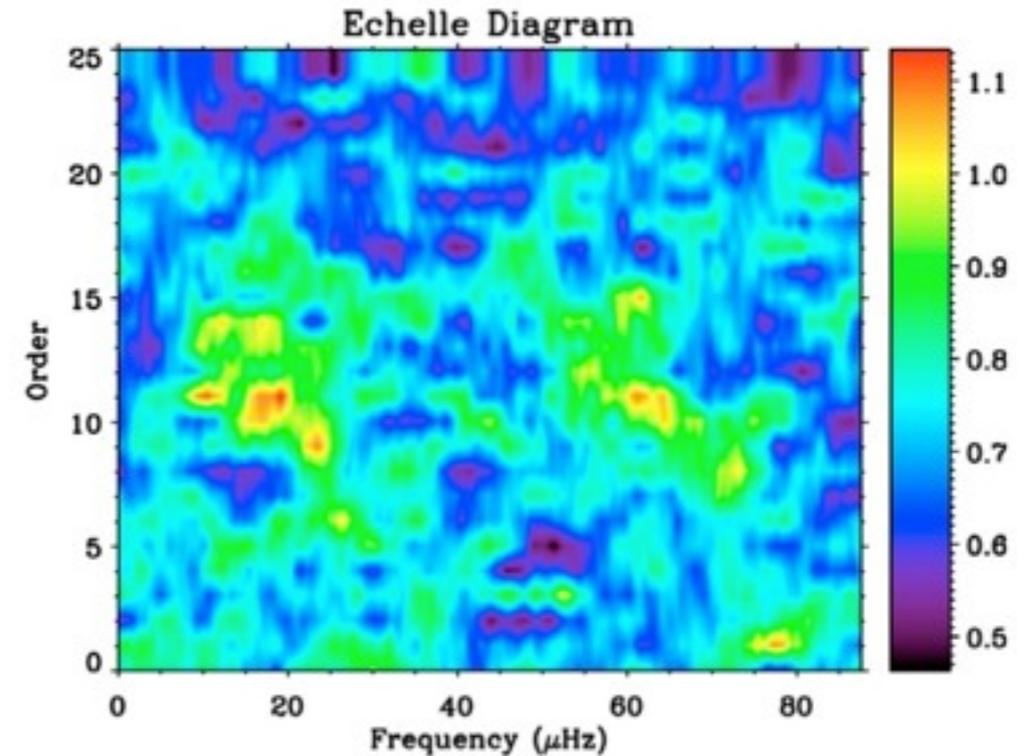


Analysis of a CoRoT lightcurve

Power spectrum
of HD 181906:



Echelle diagram

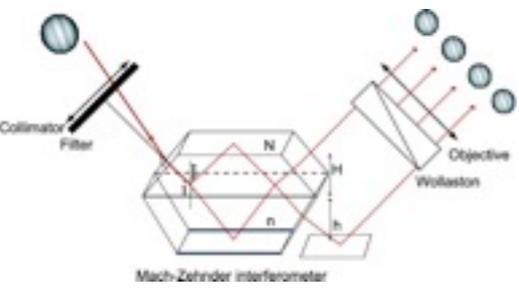


$$\Delta\nu = 87.5 \pm 2.6 \mu\text{Hz}$$

Comparison with other stars

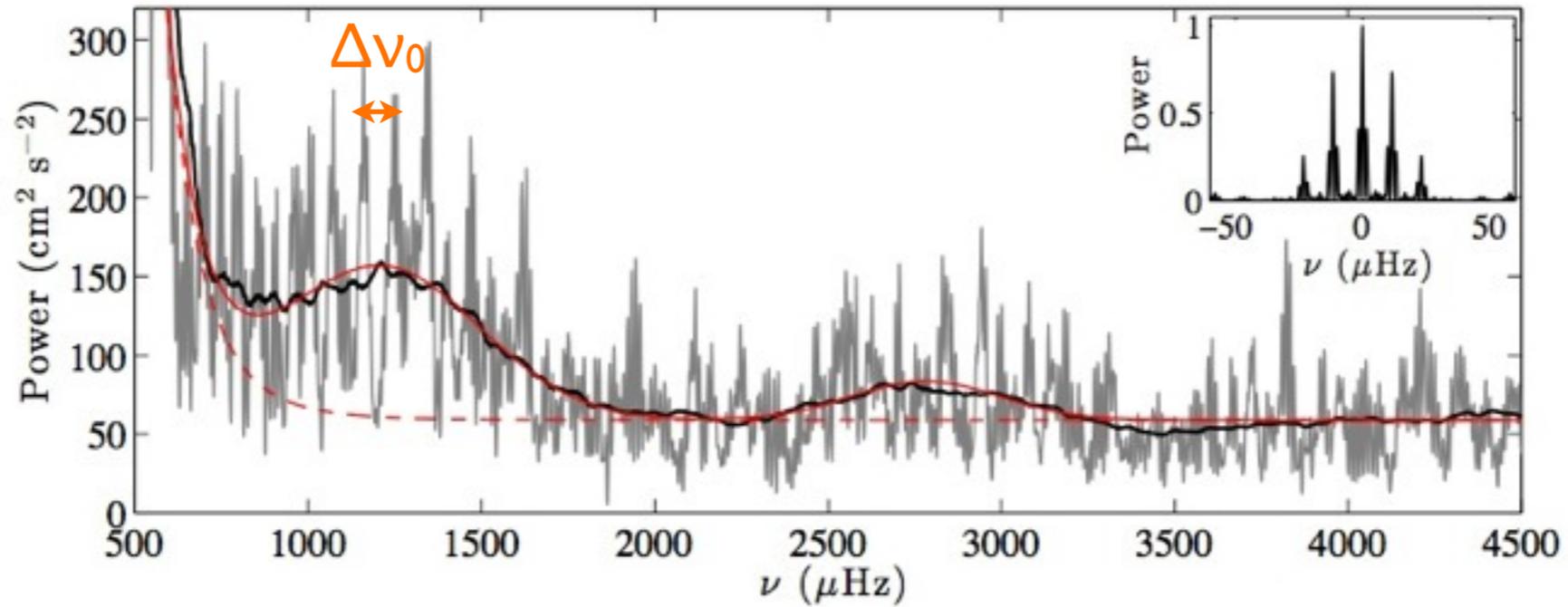
| Stars | HD 181906 this paper | HD 49933 Appourchaux et al. (2008) | HD 181420 Barban et al. (2009) | HD 175726 Mosser et al. (2009b) | Procyon Arentoft et al. (2008) |
|--------------------|-------------------------------|---------------------------------------|-----------------------------------|------------------------------------|-----------------------------------|
| Spectral type | F8 | F5 | F2 | F9/G0 | F5 |
| T_{eff} | 6300 ± 150 K | 6780 ± 130 K | 6580 ± 105 K | 6000 ± 100 K | 6514 ± 27 K |
| [Fe/H] | -0.11 ± 0.14 dex | -0.37 dex | 0.00 ± 0.06 dex | -0.22 ± 0.1 dex | -0.05 dex |
| $v \sin i$ | 10 ± 1 km s ⁻¹ | $9.5 - 10.9$ km s ⁻¹ | 18 ± 1 km s ⁻¹ | 13.5 ± 0.5 km s ⁻¹ | 3.16 ± 0.5 km s ⁻¹ |
| $\Delta\nu$ | 87.5 ± 2.6 μHz | 85.9 ± 0.15 μHz | ~ 75 μHz | ~ 97 μHz | ~ 55 μHz |
| ν_{max} | 1900 μHz | 1760 μHz | 1500 μHz | 2000 μHz | 900 μHz |
| A_{max} | 3.26 ± 0.42 ppm | 4.02 ± 0.57 ppm | 3.82 ± 0.40 ppm | ~ 1.7 ppm | ~ 8.5 ppm |

Garcia et al. (2009)



SYMPA: data analysis

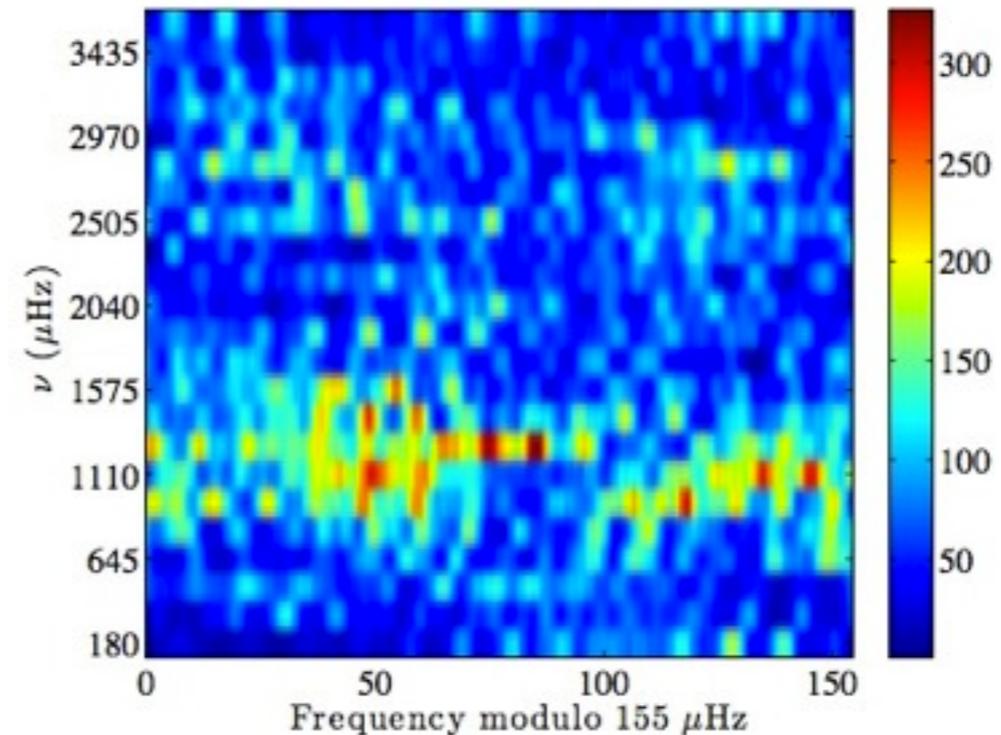
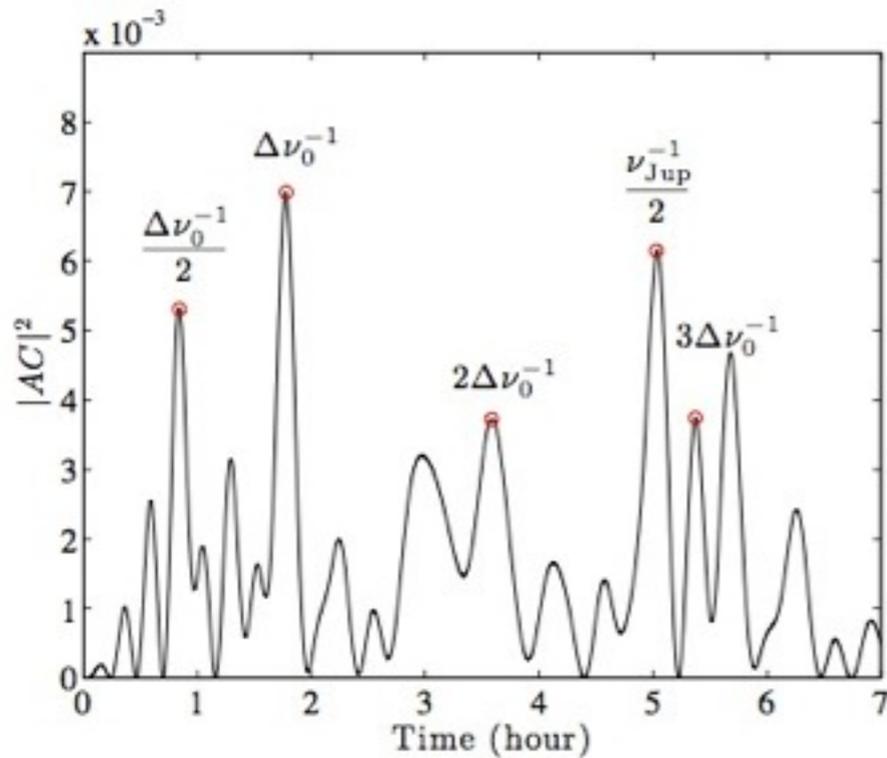
Power spectrum:

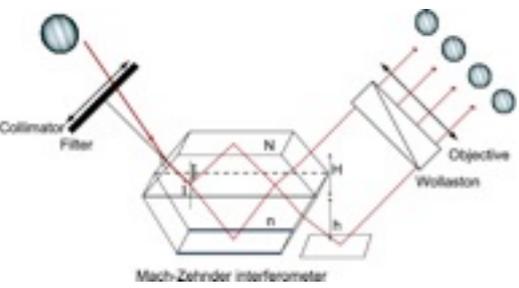


Power spectrum of the power spectrum:

Gaulme et al. A&A (2011)

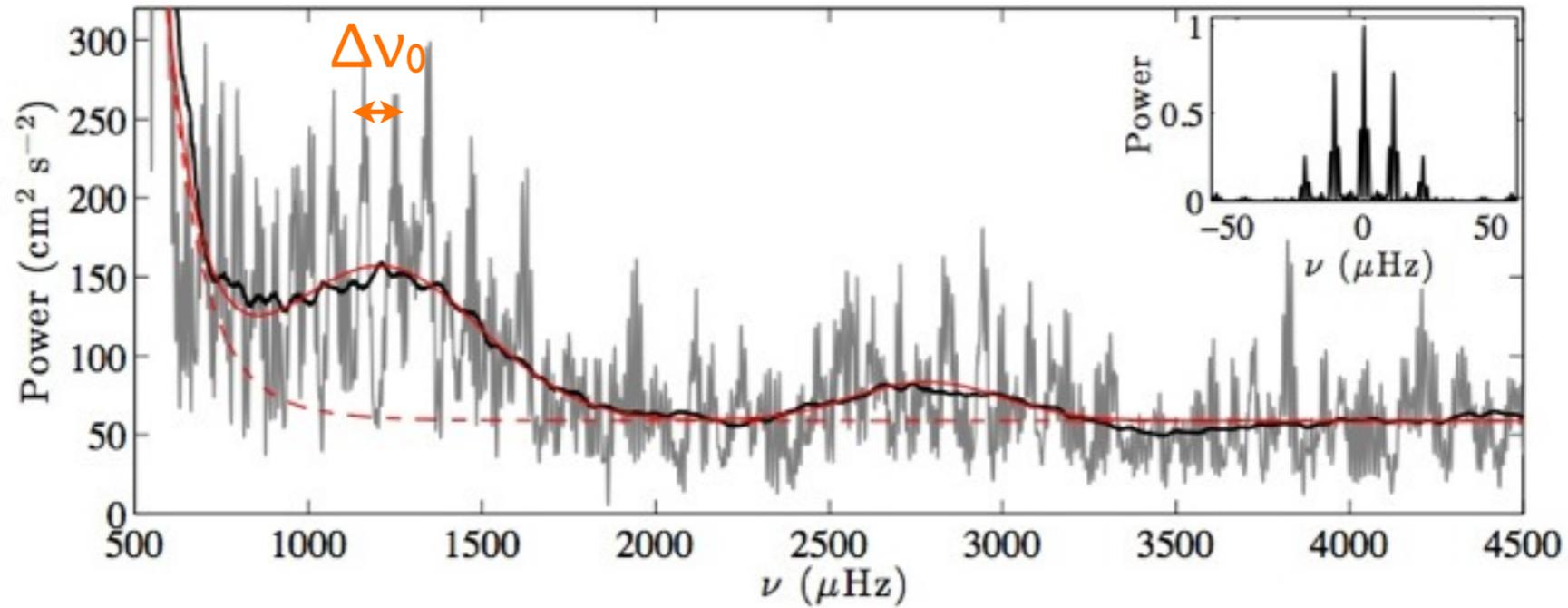
Echelle diagram





SYMPA: data analysis

Power spectrum:



Frequencies & amplitudes
of the peaks:

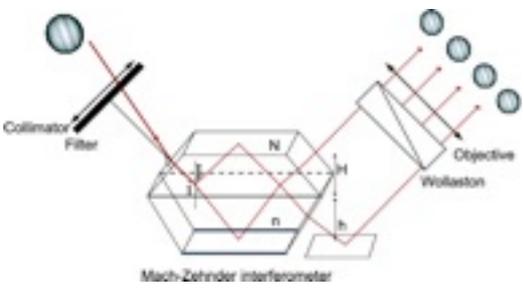
Gaulme et al. A&A (2011)

Oscillation frequencies

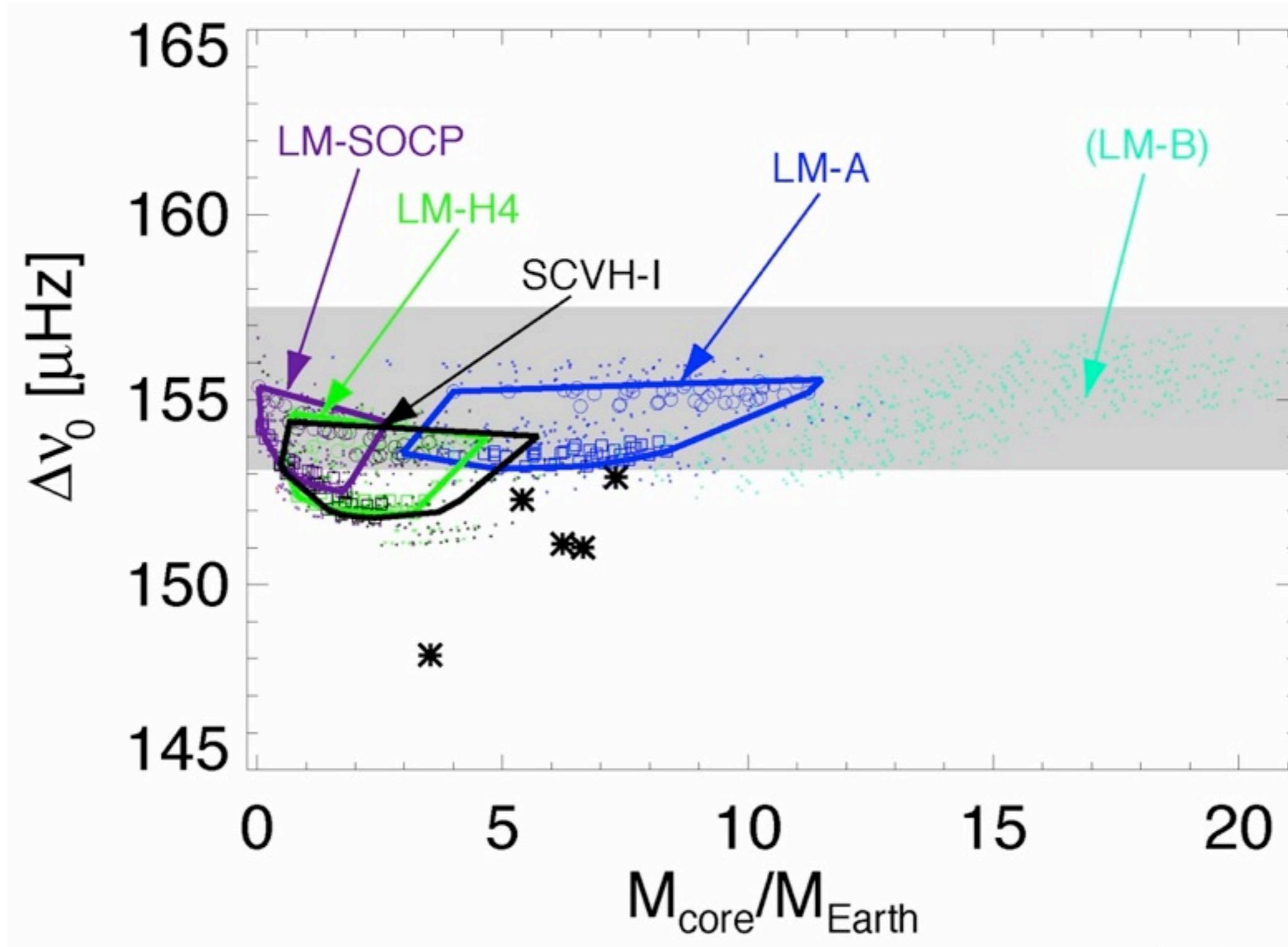
| ν μHz | Velocity cm s^{-1} | Error cm s^{-1} | ν μHz | Velocity cm s^{-1} | Error cm s^{-1} |
|-------------------------|--------------------------------|-----------------------------|-------------------------|--------------------------------|-----------------------------|
| 792 | 44.0 | -6.2/+3.9 | 1478 | 46.4 | -6.5/+4.1 |
| 854 | 46.7 | -6.6/+4.2 | 1533 | 37.3 | -5.3/+3.3 |
| 915 | 34.1 | -4.8/+3.0 | 1615 | 40.9 | -5.8/+3.7 |
| 970 | 48.7 | -6.9/+4.4 | 1753 | 33.0 | -4.6/+2.9 |
| 1011 | 51.4 | -7.2/+4.6 | 1939 | 32.0 | -4.4/+2.8 |
| 1066 | 45.7 | -6.4/+4.1 | 2110 | 30.1 | -4.2/+2.7 |
| 1094 | 42.4 | -6.0/+3.8 | 2535 | 30.3 | -4.3/+2.7 |
| 1162 | 54.1 | -7.6/+4.8 | 2714 | 30.6 | -4.3/+2.7 |
| 1245 | 53.8 | -7.6/+4.8 | 2837 | 36.2 | -5.1/+3.2 |
| 1341 | 51.5 | -7.3/+4.6 | 2947 | 41.1 | -5.8/+3.7 |
| 1410 | 40.7 | -5.7/+3.6 | 3071 | 30.7 | -4.3/+2.7 |

$$\nu_{\text{max}} = 1213 \pm 50 \mu\text{Hz}$$

$$\Delta\nu_0 = 155.3 \pm 2.2 \mu\text{Hz.}$$



SYMPA & interior models



What is next?

- Juno's arrival at Jupiter in 2016
 - Accurate gravity field measurements (up to J10 and beyond)
 - Accurate mapping of the magnetic field
 - Constraints on the deep water abundance (radiometry)
- JUICE: an ESA mission to the Jupiter-system
 - Proposal for an on-board sismometer called DSI-ECHOES (PI: F-X Schmider)
- Future ground-based observations
 - Jupiter is becoming a good target again for Northern hemisphere observations