

# Physics of Stellar Winds from Hot, Luminous Massive Stars

**Stan Owocki**

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- **Radiatively driven winds of hot stars (OB, WR, LBV)**

- High  $V_{\infty} (\sim 3 V_{\text{esc}} = 2000-3000 \text{ km/s}) \gg V_{\text{sound}} \sim 10 \text{ km/s}$
- High  $\dot{M} (10^{-4} - 10^{-8} M_{\text{sun}}/\text{yr})$
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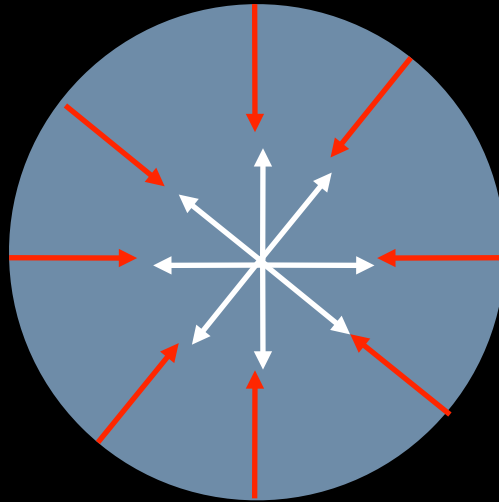
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# Radiative force vs. gravity

Radiative  
Force

$$g_{rad} = \int_0^\infty d\nu \frac{\kappa_\nu F_\nu}{c}$$



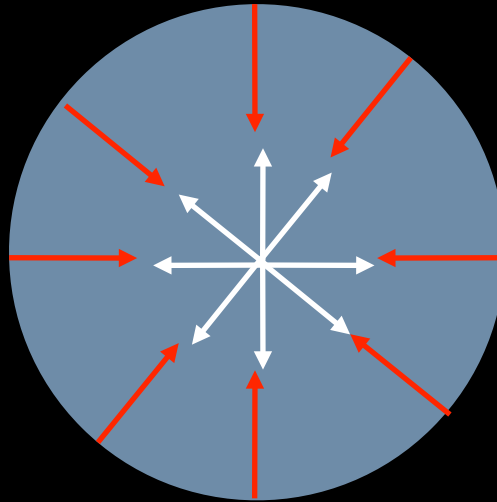
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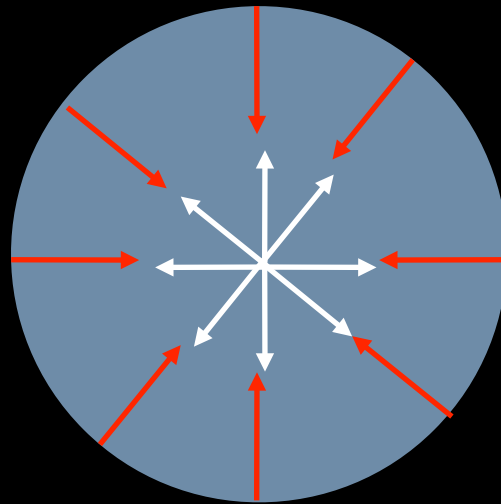
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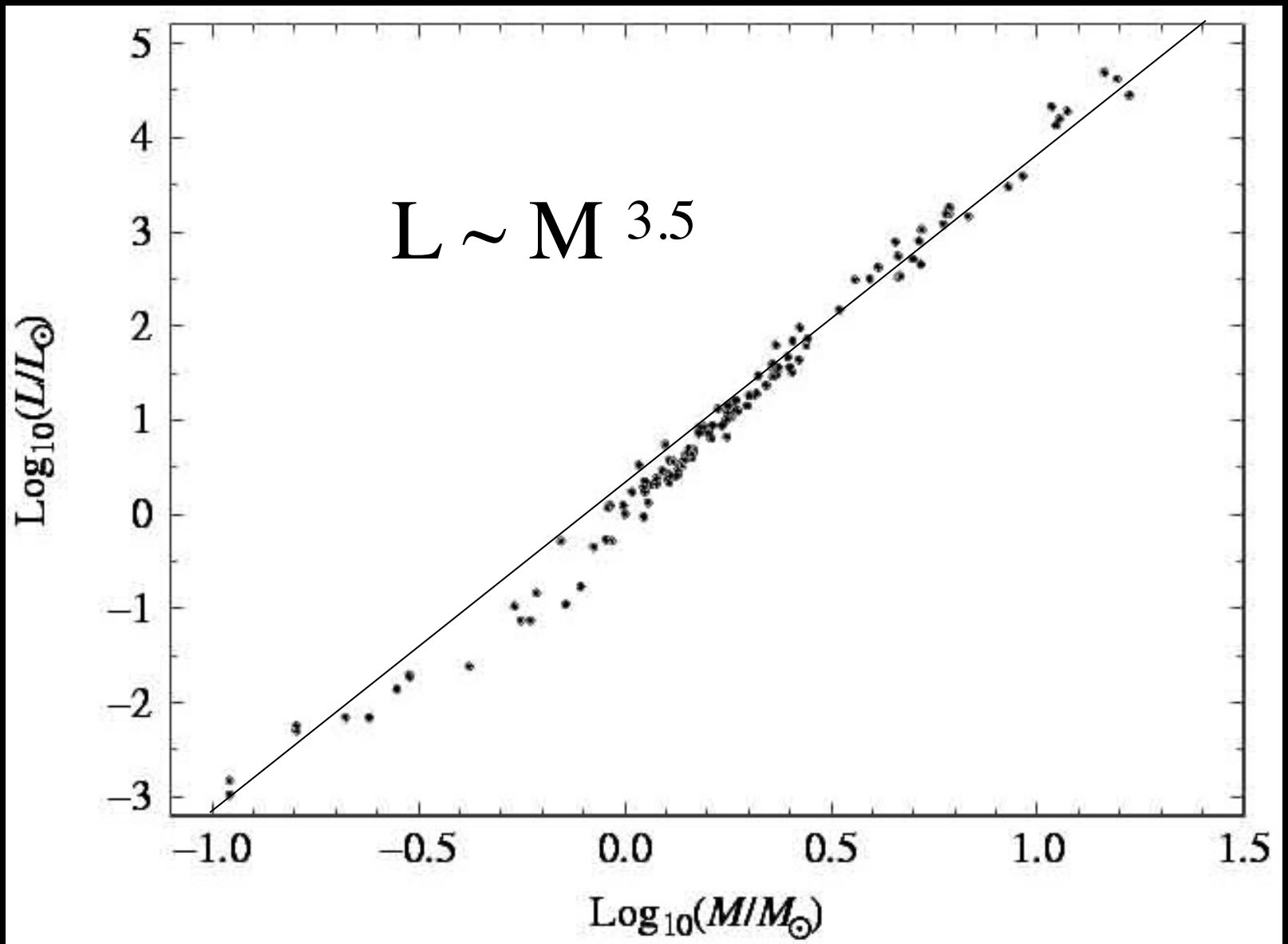
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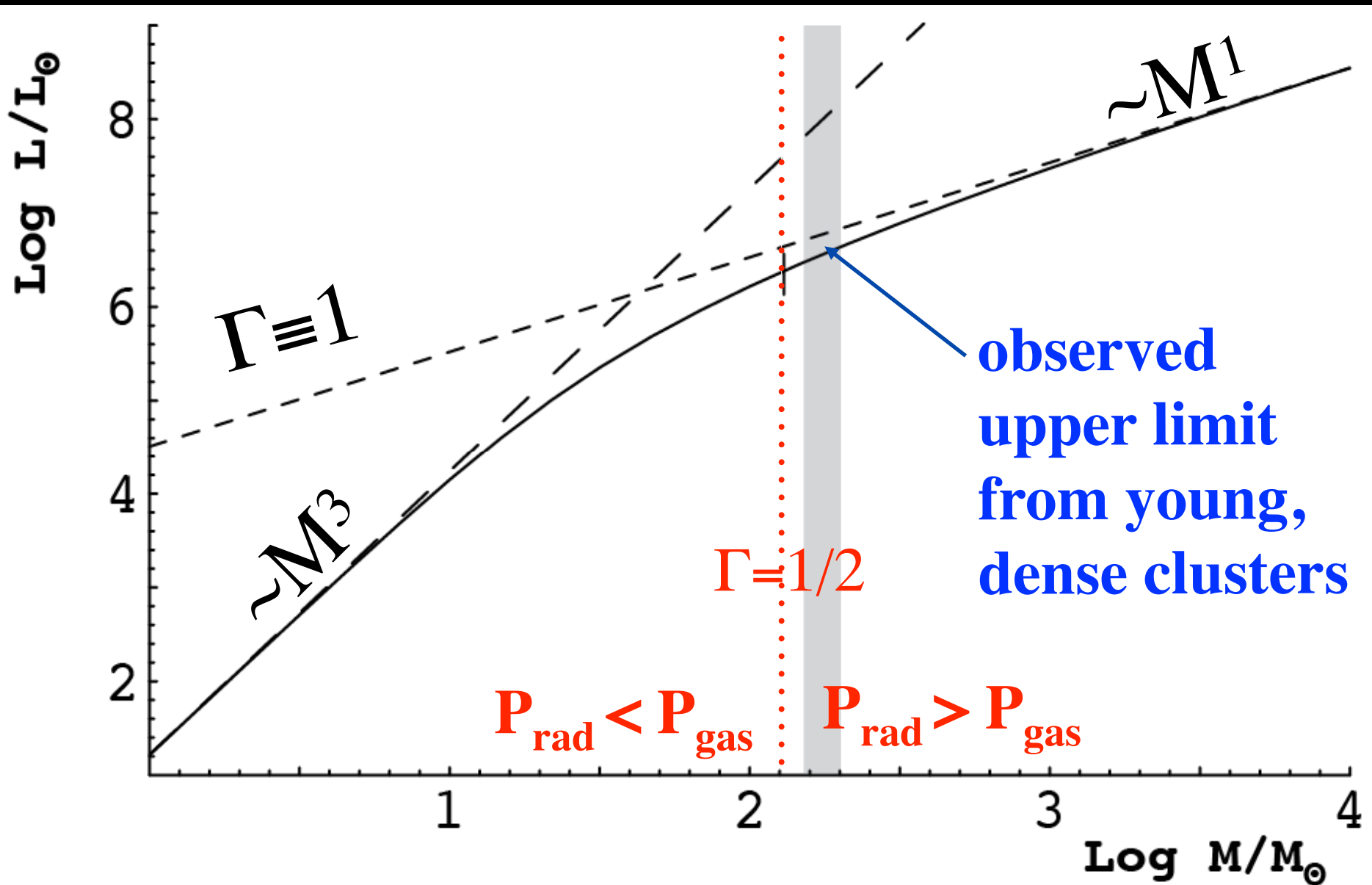
$$\Gamma_e \equiv \frac{g_e}{g} = \frac{\kappa_e L / 4\pi r^2 c}{GM / r^2} = \frac{\kappa_e L}{4\pi GM c}$$

$$\Gamma \approx 2 \times 10^{-5} \frac{L / L_\odot}{M / M_\odot} \frac{\overline{\kappa_F}}{\kappa_e}$$

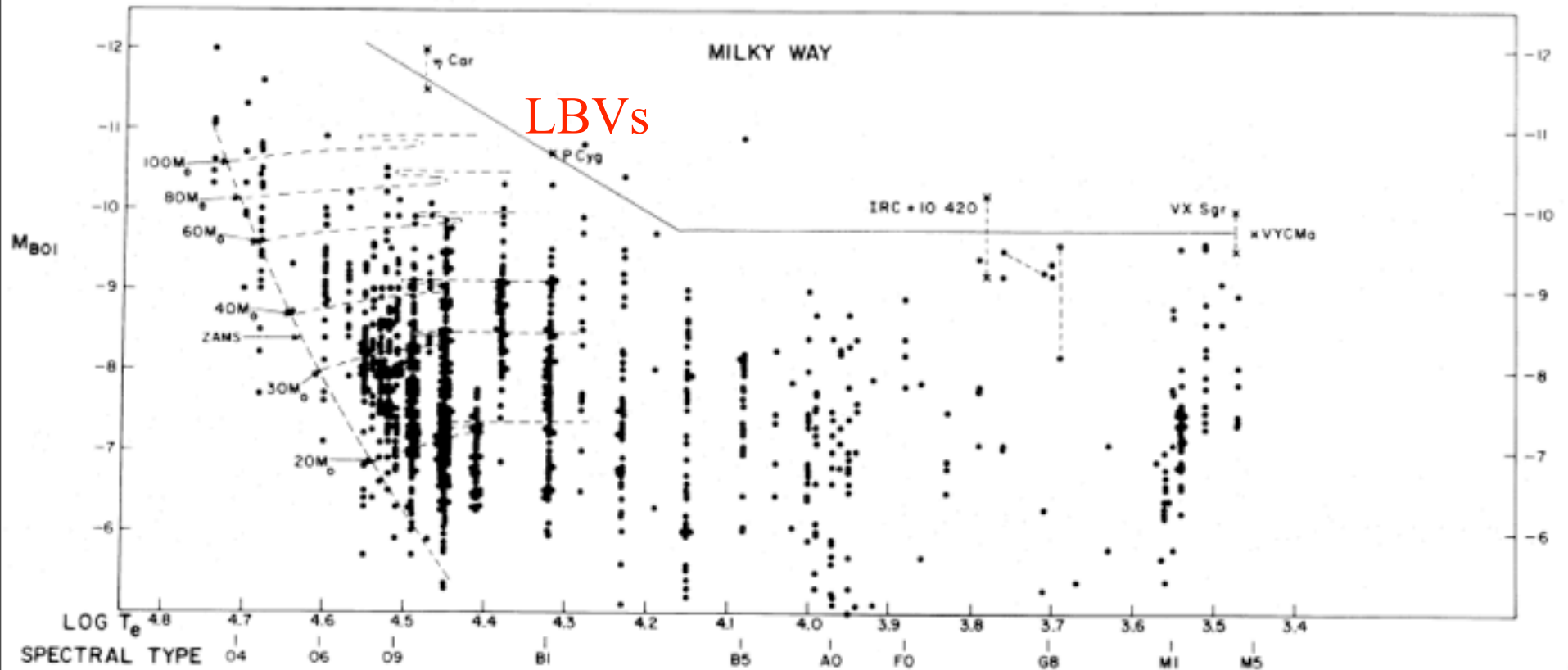
# Stellar Luminosity vs. Mass



# Eddington Standard Model (n=3 Polytrope)

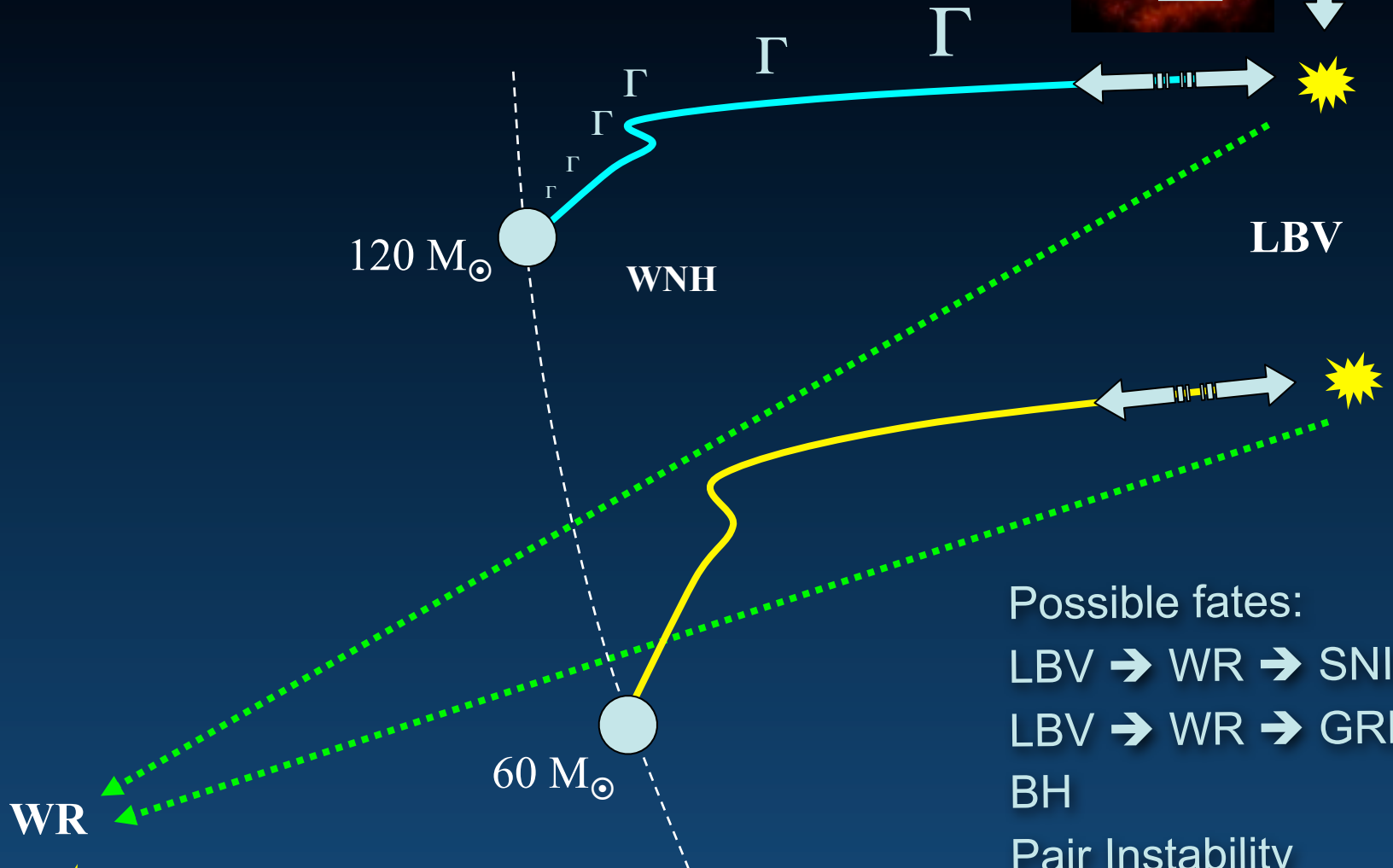


# Humphreys-Davidson Limit



# Mass loss and stellar evolution:

## Luminous Blue Variable (LBV) winds/eruptions



**WR**  
Ib/c  
GRBs?

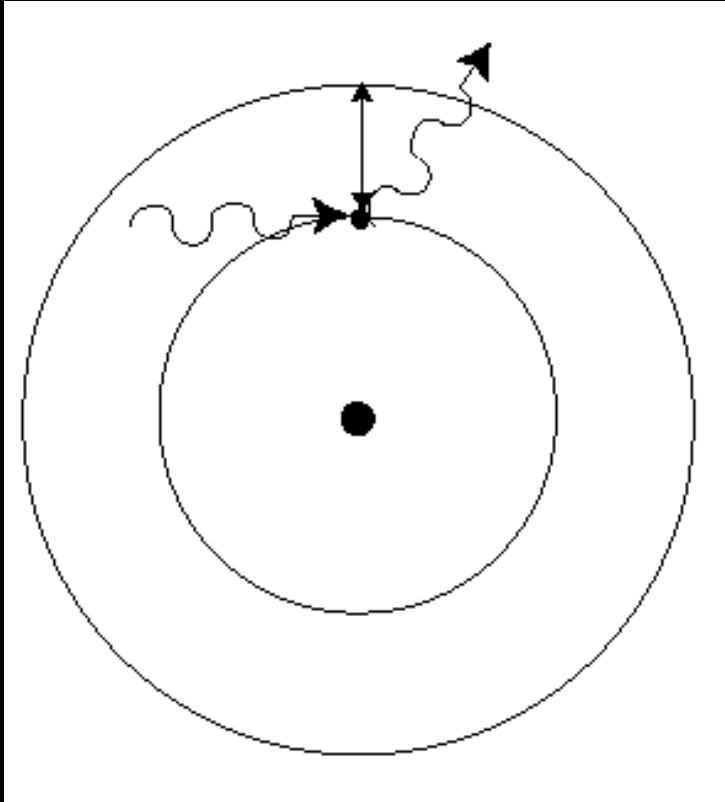
- Possible fates:  
LBV → WR → SNIbc  
LBV → WR → GRB  
BH  
Pair Instability  
Type II

# Line-Driven Stellar Winds

- For normal (sub-Eddington stars) wind is driven is by **line** scattering of light by electrons **bound** to **metal ions**
- This has some key differences from **free** electron scattering...

# Driving by **Line-Opacity**

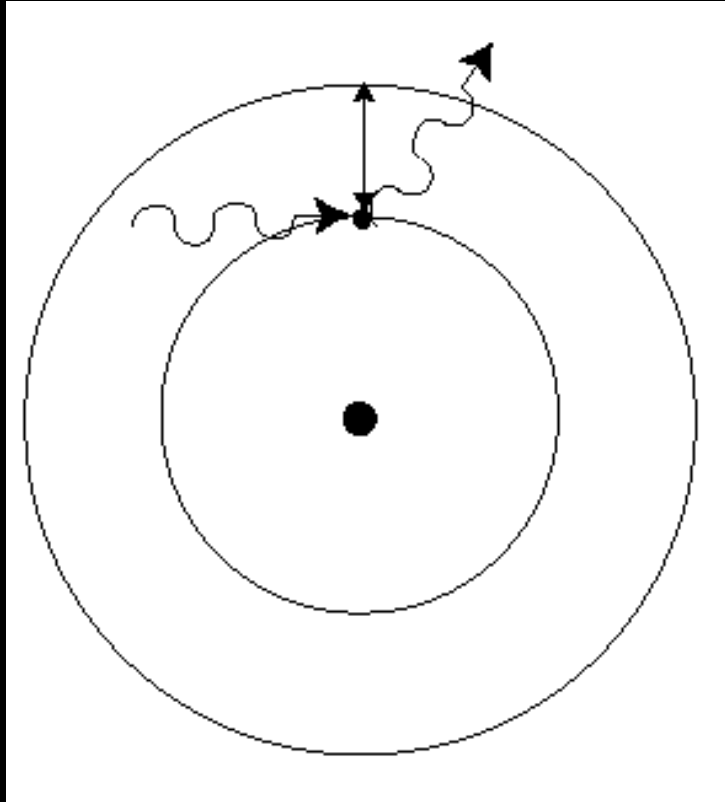
Optically **thin**



$$\Gamma_{thin} \sim Q\Gamma_e \sim 1000\Gamma_e$$

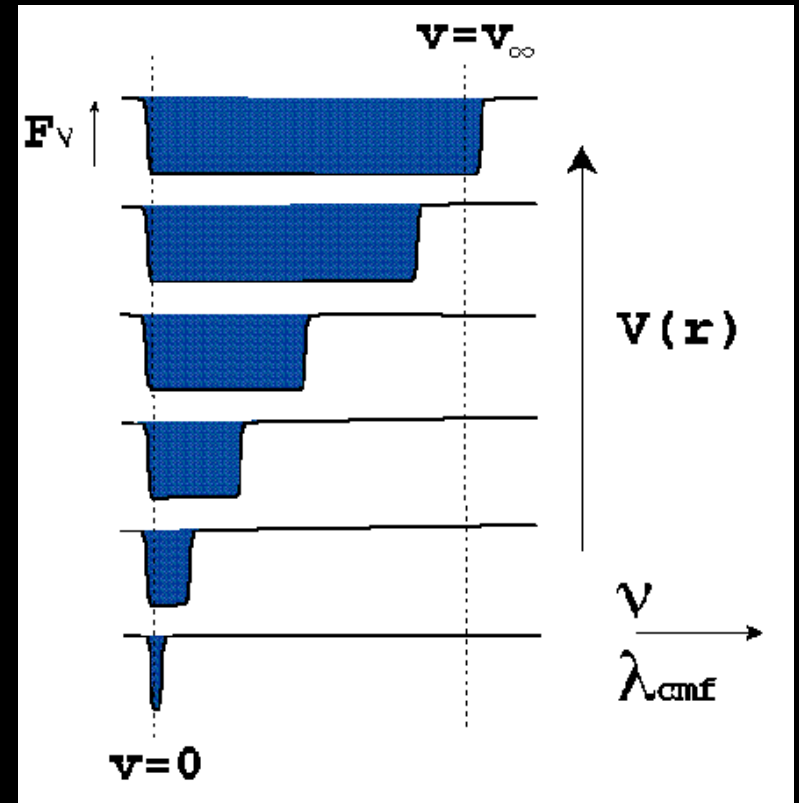
# Driving by **Line-Opacity**

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Optically **thick**



$$\Gamma_{thick} \sim \frac{Q\Gamma_e}{\tau} \sim \frac{1}{\rho} \frac{dv}{dr}$$



# CAK model of steady-state wind

Equation of motion:

$$v v' \approx - \frac{GM(1-\Gamma)}{r^2} + \frac{\bar{Q}L}{r^2} \left( \frac{r^2 v v'}{\dot{M}\bar{Q}} \right)^\alpha$$

**inertia**                      **gravity**                      **CAK line-force**

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$0 < \alpha < 1$   
CAK ensemble of  
thick & thin lines

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$g_{\text{CAK}} \approx$  gravity

Mass loss rate

$$\dot{M} \approx \frac{L}{c^2} \left( \frac{\bar{Q}\Gamma}{1-\Gamma} \right)^{\frac{1}{\alpha}-1}$$

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Velocity law

$$v(r) \approx v_\infty (1 - R_* / r)^\beta \quad \beta \approx 0.8$$

$\sim v_{\text{esc}}$

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$\sim v_{\text{esc}}$

**Wind-Momentum  
Luminosity law**

$$\dot{M} v_\infty \sim \bar{Q}^{-1+1/\alpha} L^{1/\alpha}$$

$$\sim Z^{0.6} L^{1.7}$$

$$\alpha \approx 0.6$$

$$\bar{Q} \sim Z$$

**How are such winds  
affected by (rapid)  
stellar rotation?**

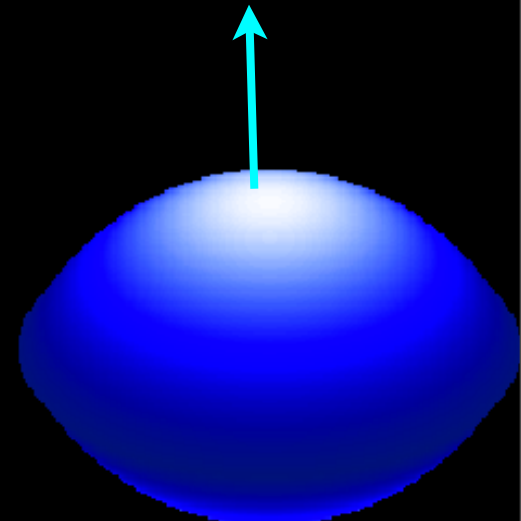
# Gravity Darkening

$$F(\theta) \sim g_{eff}(\theta)$$

$$\dot{M} \sim F(\theta)$$

$$V_{\infty} \sim \sqrt{g(\theta)}$$

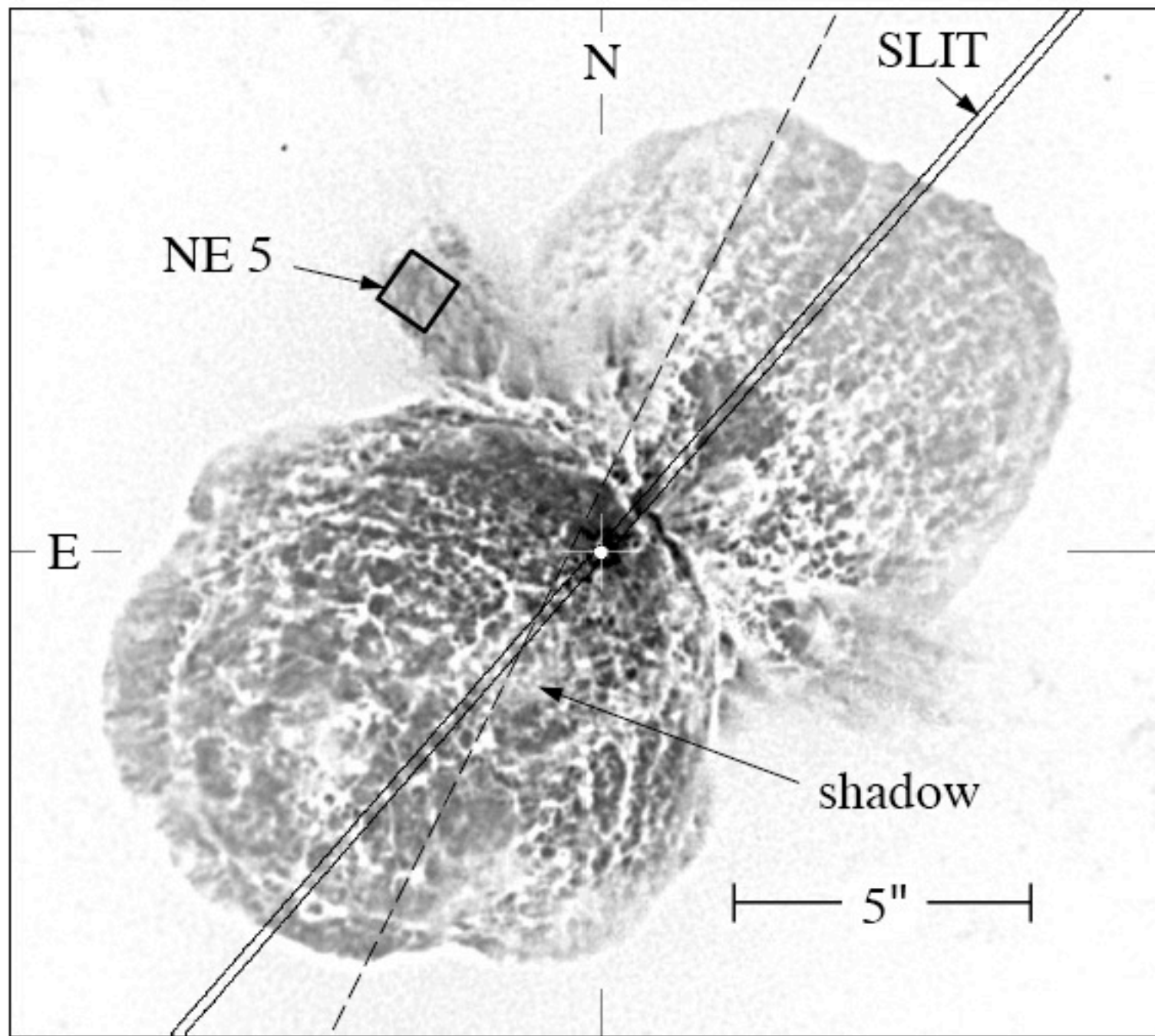
higher at pole!

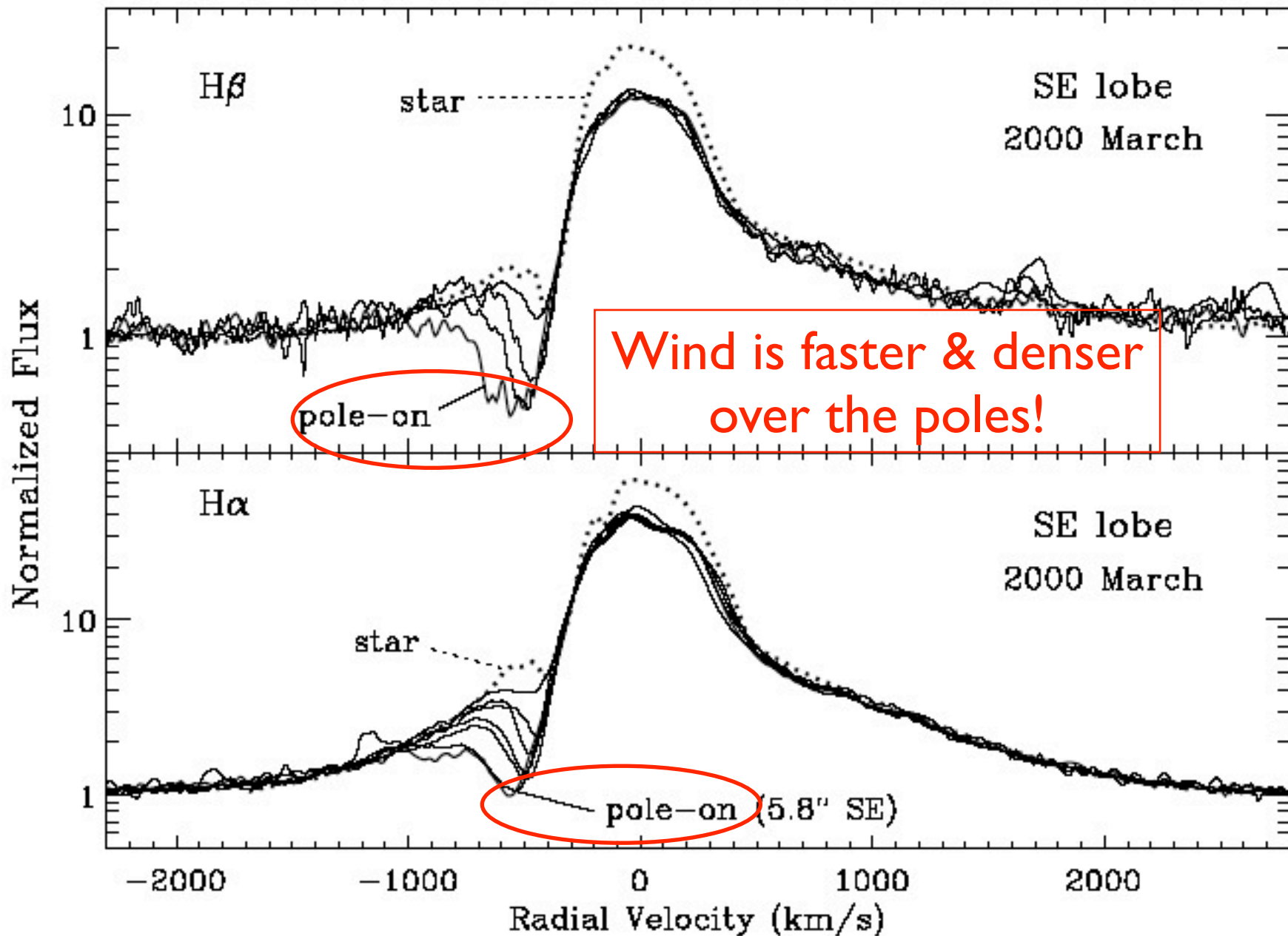


increasing stellar rotation









**How are winds affected by a  
(large-scale)  
stellar magnetic field?**

# MiMeS

## Magnetism in Massive Stars

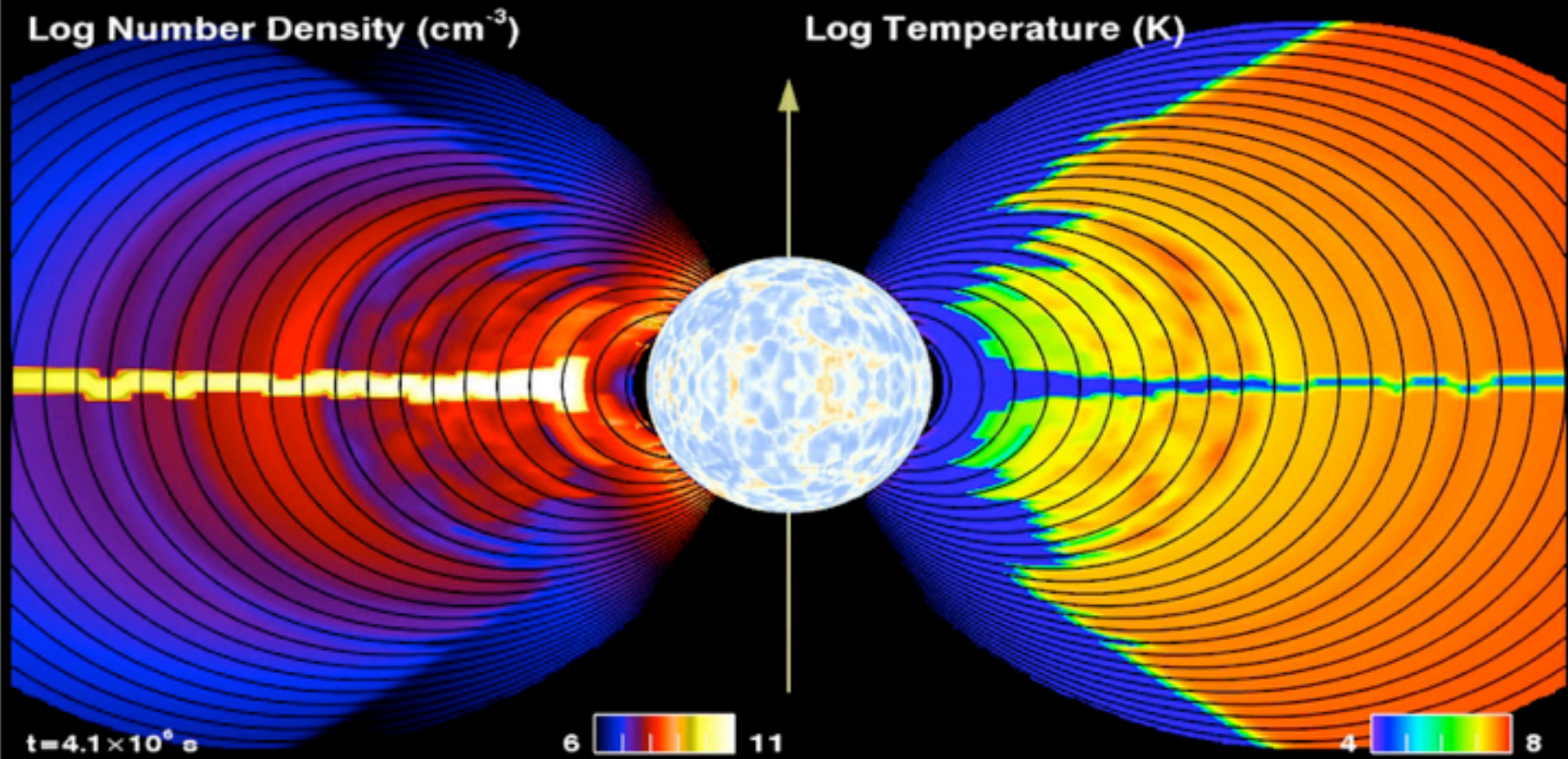
P.I.: Gregg A. Wade, Royal Military College  
50+ Co-Is, 2008-2012, CFHT Allocation: 640 hours



[http://www.physics.queensu.ca/~wade/mimes/  
MiMeS Magnetism in Massive Stars.html](http://www.physics.queensu.ca/~wade/mimes/MiMeS_Magnetism_in_Massive_Stars.html)

# Rigid Field - Hydro Dynamics for $\eta_* \gg 1$

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# RRM model for $\sigma$ Ori E

EM +B-field

photometry

$$B_* \sim 10^4 \text{ G}$$

$$\Rightarrow \eta_* \sim 10^6 !$$

$$\text{tilt} \sim 55^\circ$$

H $\alpha$

polarimetry



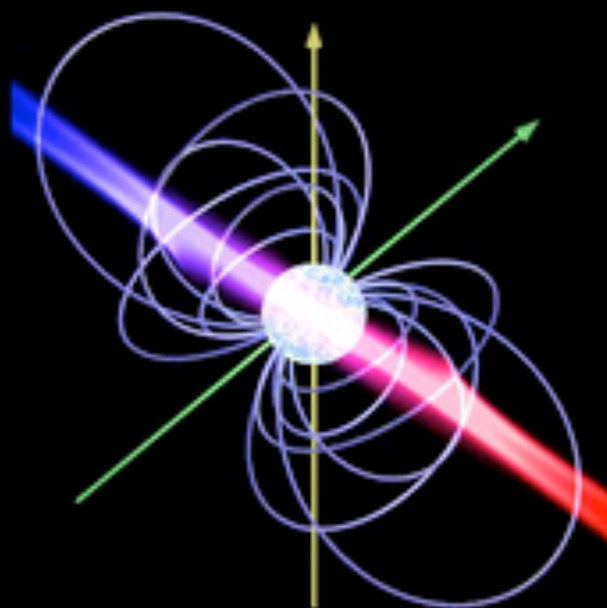
# RRM mode! for $\sigma$ Ori E

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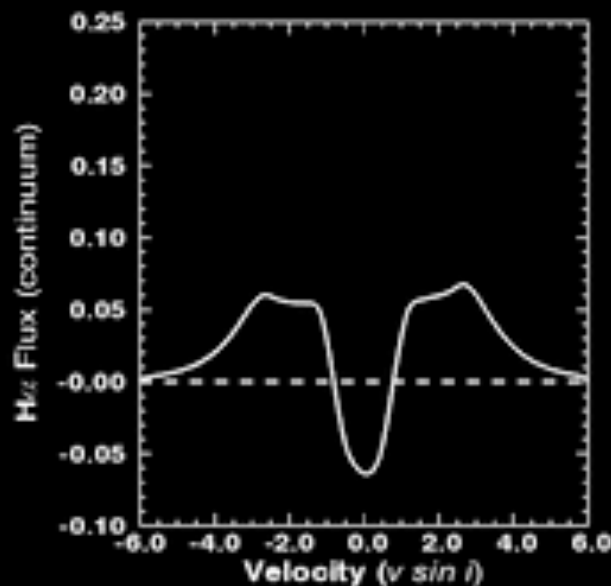
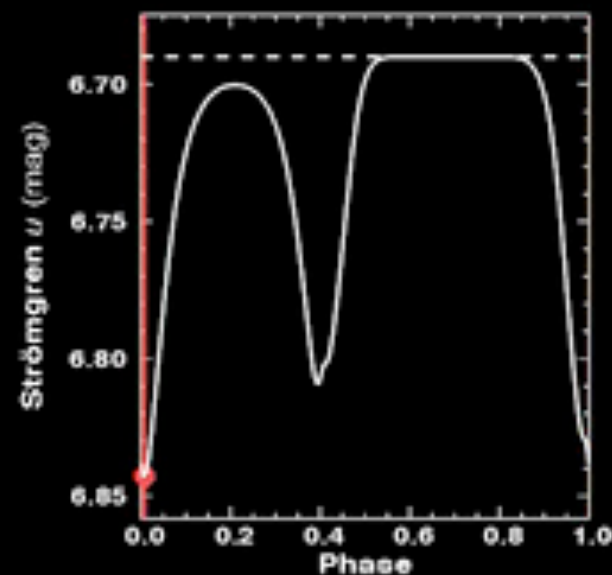
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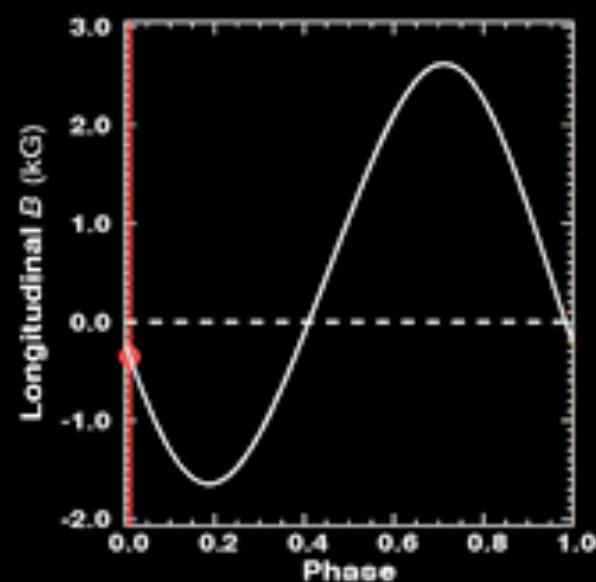
EM +B-field



photometry



$H\alpha$



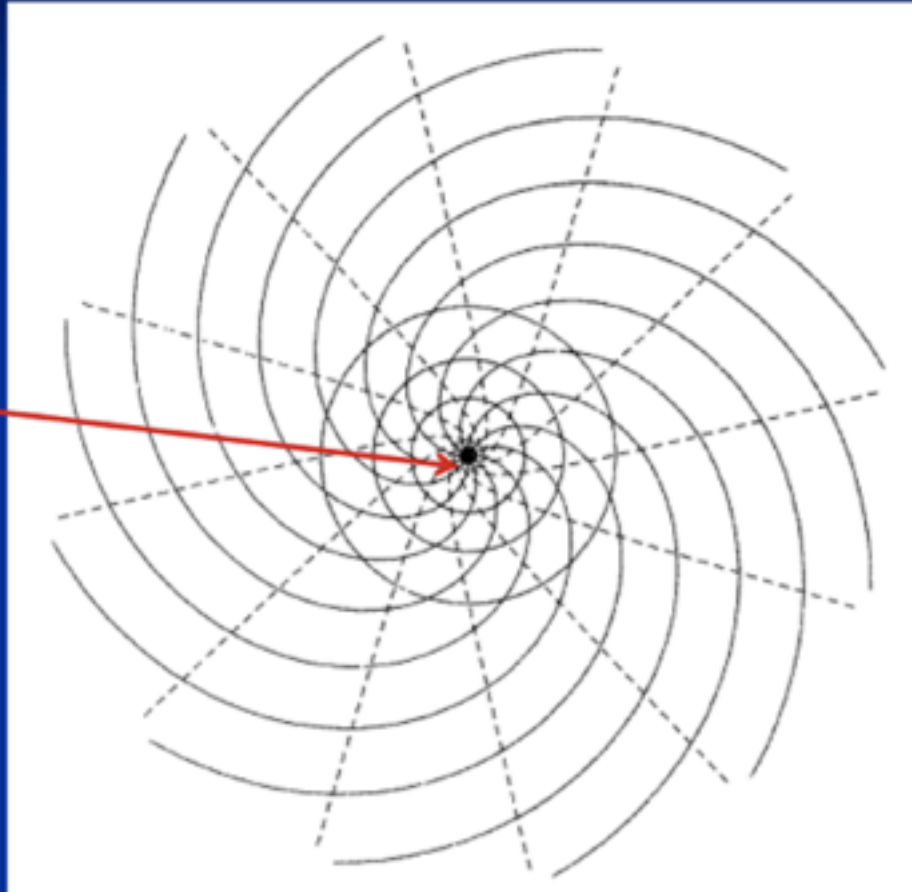
polarimetry



# Angular Momentum Loss & Spindown

Weber and Davis (1967)

Monopole field at solar surface



$$\dot{J} = \frac{2}{3} \dot{M} \Omega R_A^2$$

# Stellar spindown time

Table 1. Estimated spin-down time for selected known magnetic stars.

Star <sup>a</sup>	$M/M_{\odot}$	$R_*/R_{\odot}$	P (d)	$k$	$\dot{M}$ ( $10^{-9} M_{\odot} \text{ yr}^{-1}$ )	$v_{\infty}$ (1000 km s <sup>-1</sup> )	$B_p$ (kG)	$\eta_*$	$\tau_{\text{spin}}$ (Myr)
$\theta^1$ Ori C <sup>1</sup>	40	8	15.4	0.28	400	2.5	1.1	15.7	8
HD191612 <sup>2</sup>	40	18	538	0.17	6100	2.5	1.6	7.6	0.4
$\zeta$ Cas <sup>3</sup>	8	5.9	5.37	0.1	0.3	0.8	0.34	3200	65.2
$\sigma$ Ori E <sup>4</sup>	8.9	5.3	1.2	0.1	2.4	1.46	9.6	$1.4 \times 10^5$	1.4
$\rho$ Leo <sup>5</sup>	22	35	7-47	0.12	630	1.1	0.24	20	1.1

$$\tau_{\text{spin}} \approx \tau_{\text{mass}} \frac{\frac{3}{2} k}{\sqrt{\eta_*}} \quad \eta_* \equiv \frac{B_*^2 R_*^2}{\dot{M} V_{\infty}}$$

$$\approx 11 \text{ Myr} \frac{k_{-1}}{B_{\text{kG}}} \frac{M_*}{R_*} \sqrt{\frac{V_8}{\dot{M}_{-9}}}$$

## DISCOVERY OF ROTATIONAL BRAKING IN THE MAGNETIC HELIUM-STRONG STAR SIGMA ORIONIS E

R. H. D. TOWNSEND<sup>1</sup>, M. E. OKSALA<sup>2</sup>, D. H. COHEN<sup>3</sup>, S. P. OWOCKI<sup>2</sup>, AND A. UD-DOULA<sup>4</sup>

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<sup>2</sup> Bartol Research Institute, Department of Physics and Astronomy, University of Delaware, Newark, DE 19716, USA

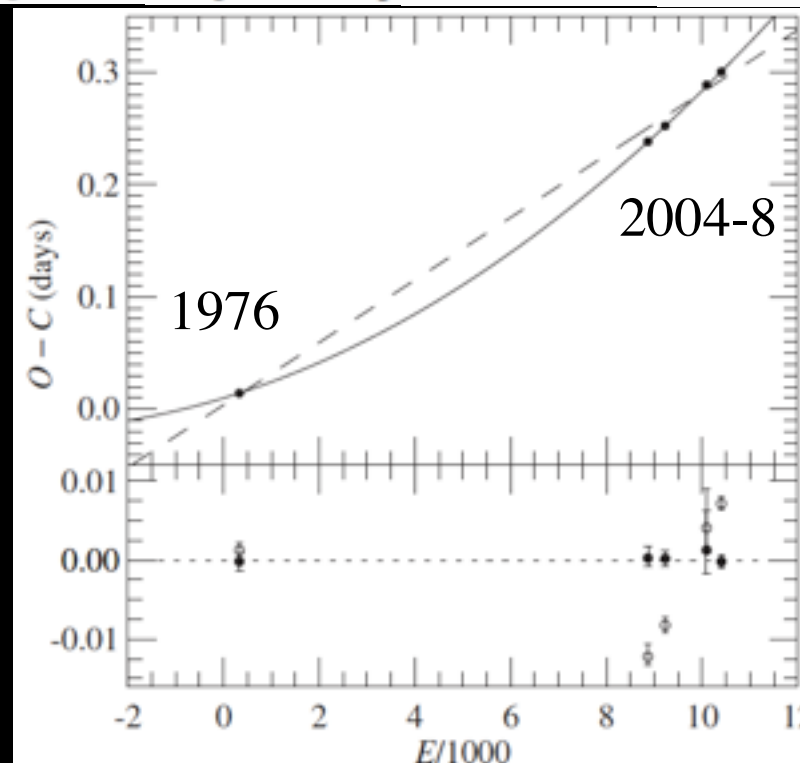
<sup>3</sup> Department of Physics and Astronomy, Swarthmore College, Swarthmore, PA 19081, USA

<sup>4</sup> Penn State Worthington Scranton, 120 Ridge View Drive, Dunmore, PA 18512, USA

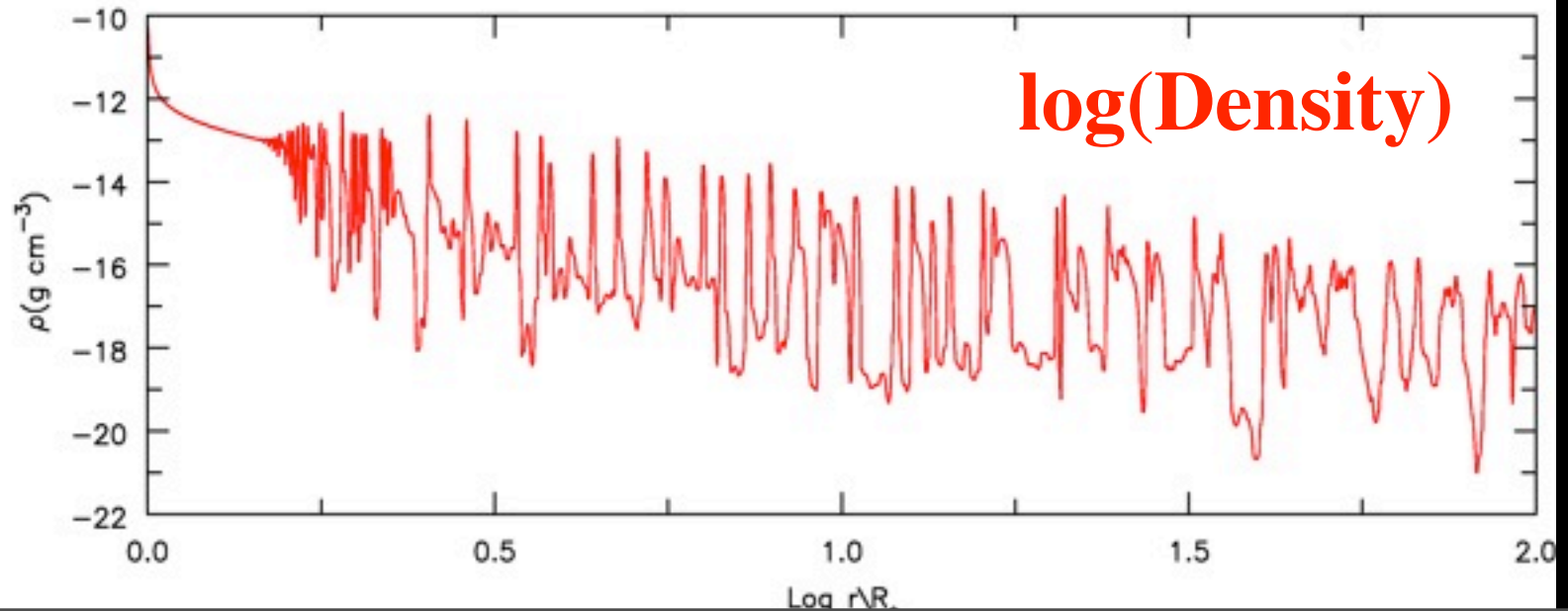
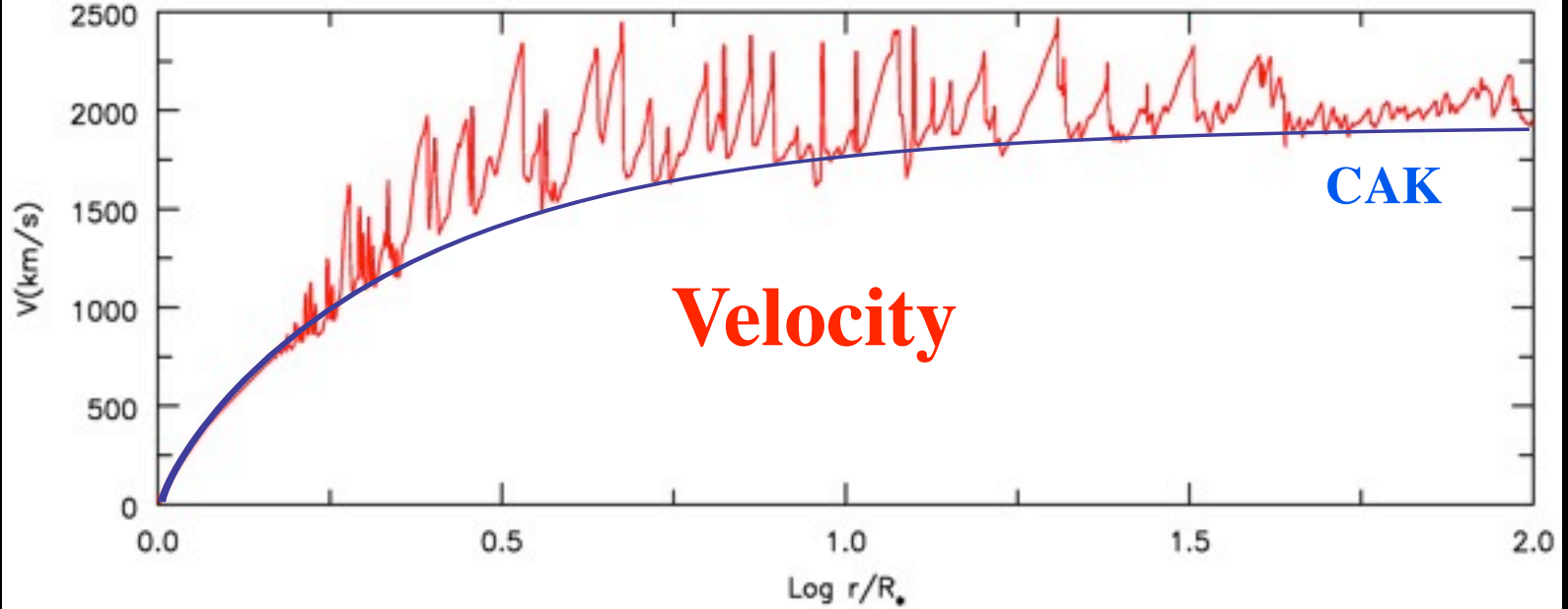
Received 2010 March 12; accepted 2010 April 14; published 2010 April 26

### ABSTRACT

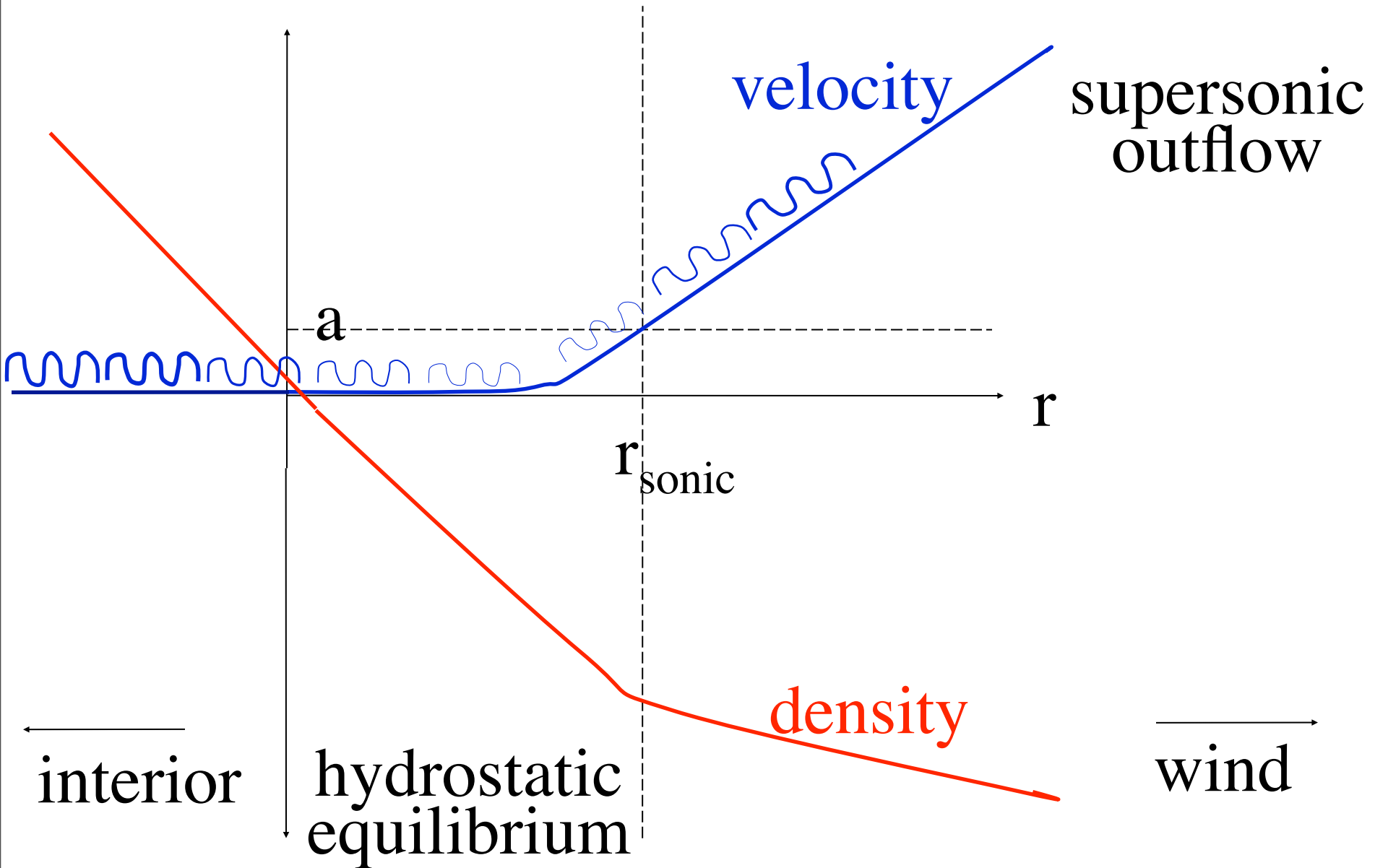
We present new *U*-band photometry of the magnetic helium-strong star  $\sigma$  Ori E, obtained over 2004–2009 using the SMARTS 0.9 m telescope at Cerro Tololo Inter-American Observatory. When combined with historical measurements, these data constrain the evolution of the star's 1.19 day rotation period over the past three decades. We are able to rule out a constant period at the  $p_{\text{null}} = 0.05\%$  level, and instead find that the data are well described ( $p_{\text{null}} = 99.3\%$ ) by a period increasing linearly at a rate of 77 ms per year. This corresponds to a characteristic spin-down time of 1.34 Myr, in good agreement with theoretical predictions based on magnetohydrodynamical simulations of angular momentum loss from magnetic massive stars. We therefore conclude that the observations are consistent with  $\sigma$  Ori E undergoing rotational braking due to its magnetized line-driven wind.



# Line-driving intrinsically unstable at small-scales



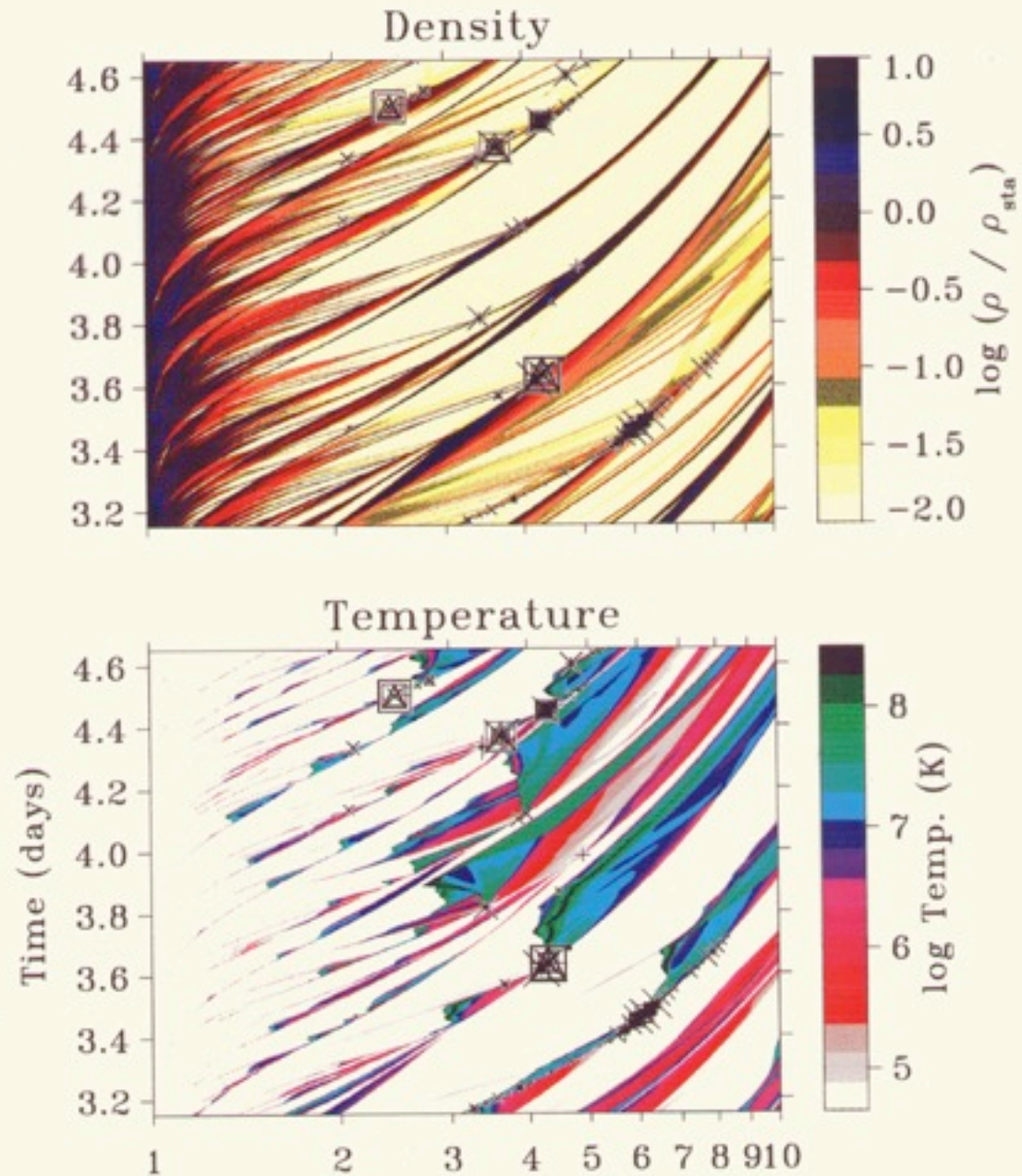
# Wave leakage through sonic point



# Turbulence-seeded clump collisions

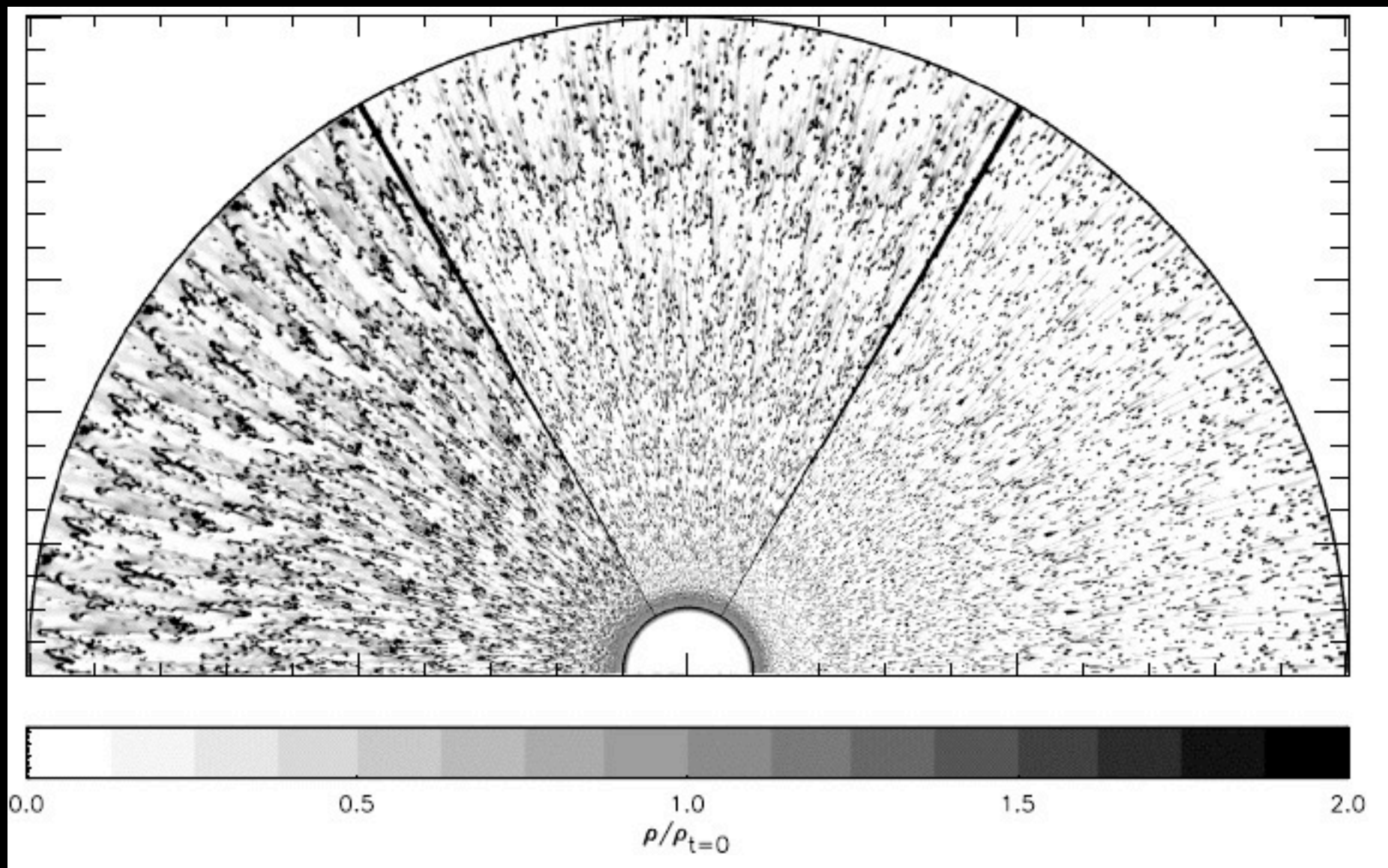
Enhances  $V_{\text{disp}}$   
and thus X-ray  
emission

Feldmeier et al.  
1997





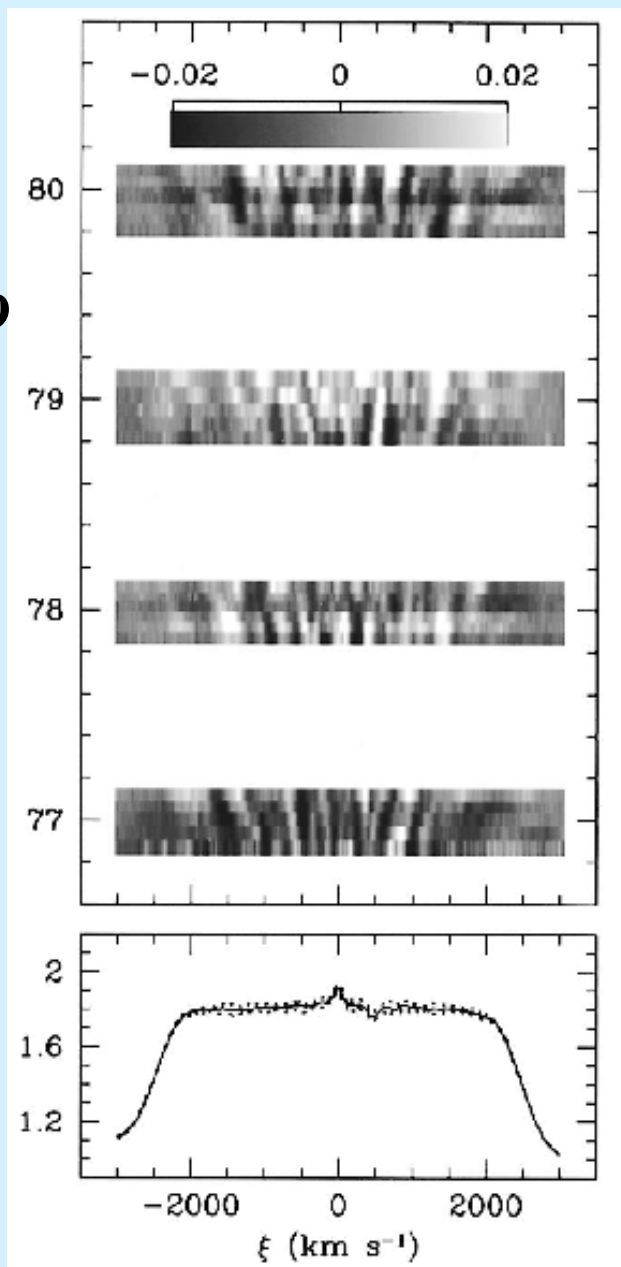
In 2D sims, RT instabilities break shells into clumps



Dessart & Owocki 2005

# WR Star Emission Profile Variability

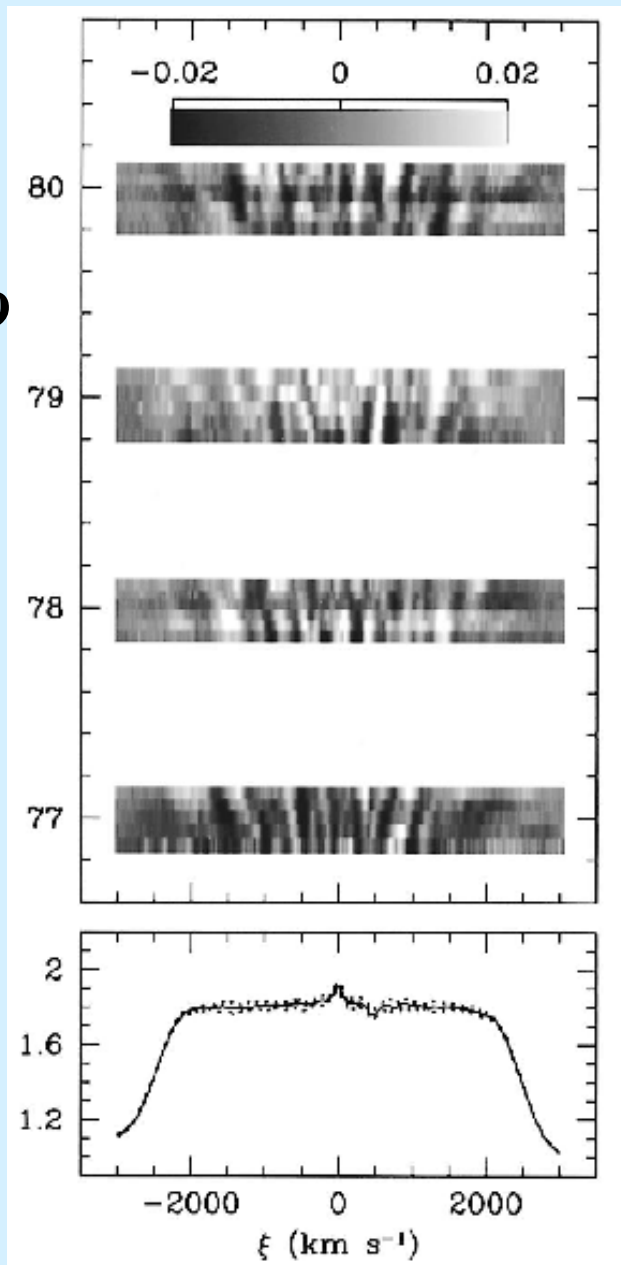
**WR 140**  
**Lepine &**  
**Moffat 1999**





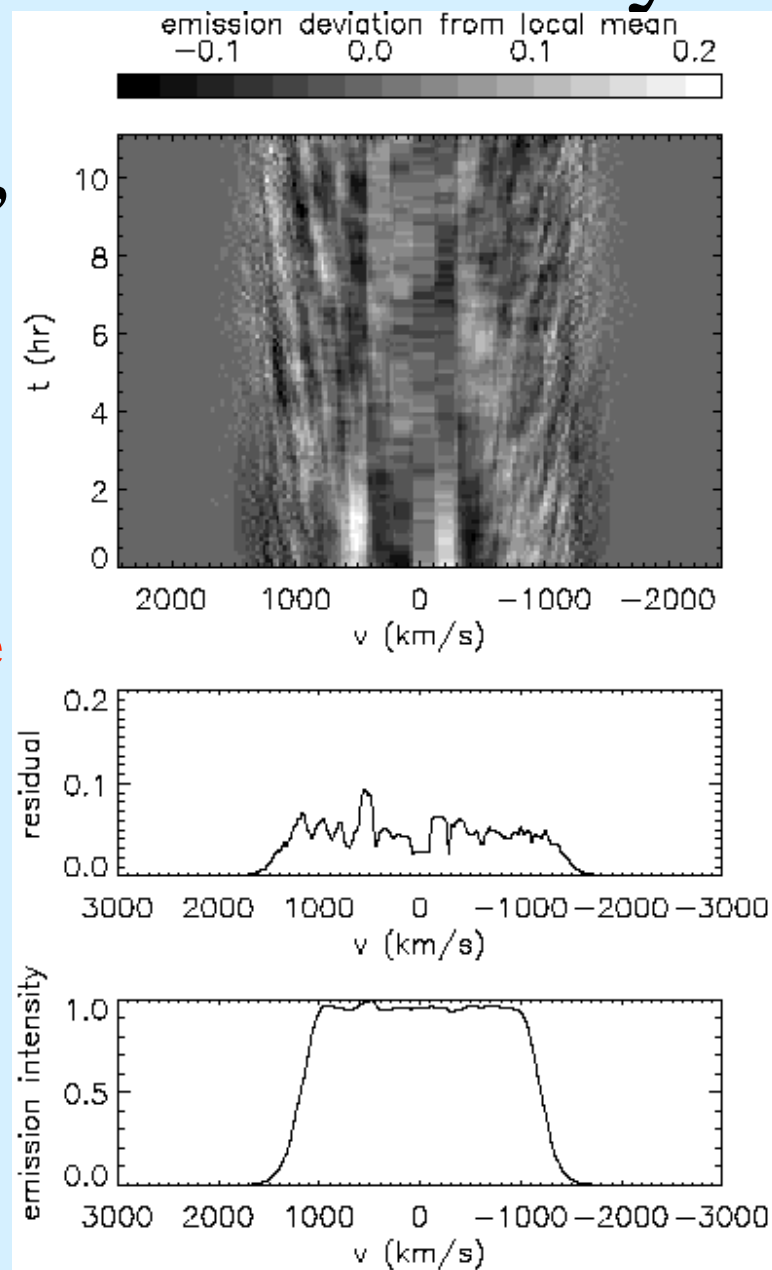
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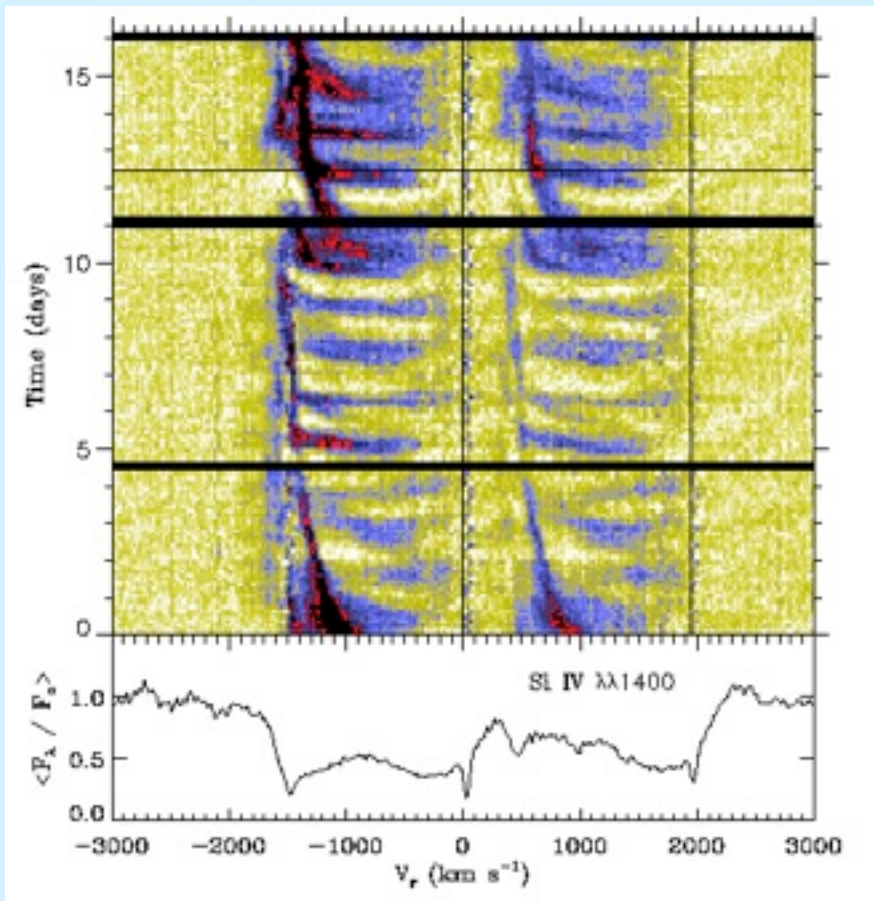


**3D**  
**“patch”**  
**model**  
**Dessart &**  
**Owocki**  
**2002**

**patch size**  
**~3 deg**

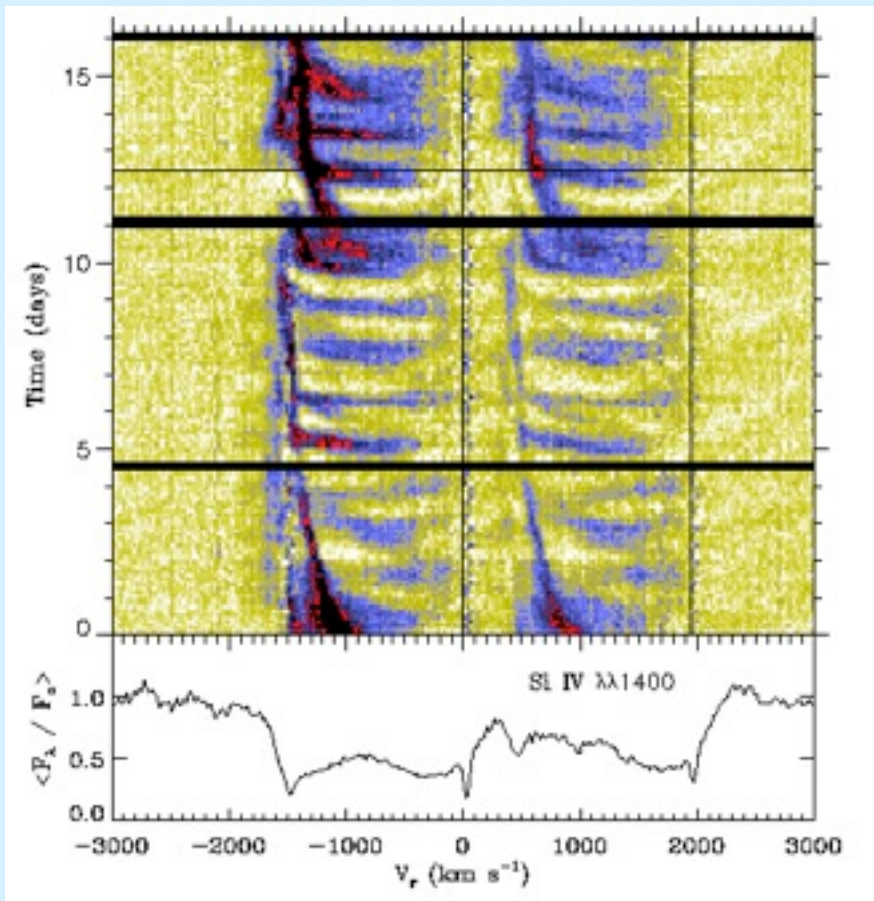


# Discrete Absorption Components: evidence for **large-scale** wind structure

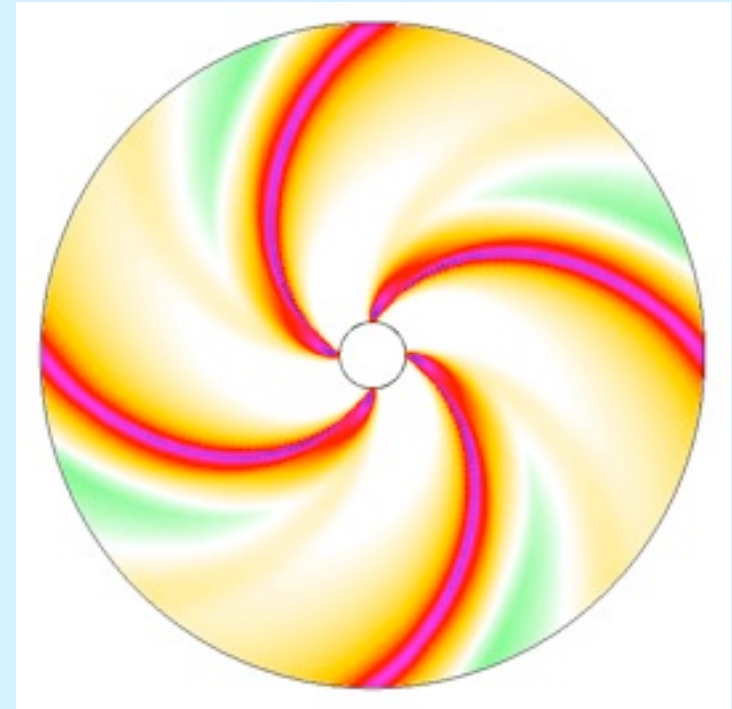


Monitoring campaigns of P-Cygni lines formed in hot-star winds often show **modulation** at periods comparable to the stellar rotation period.

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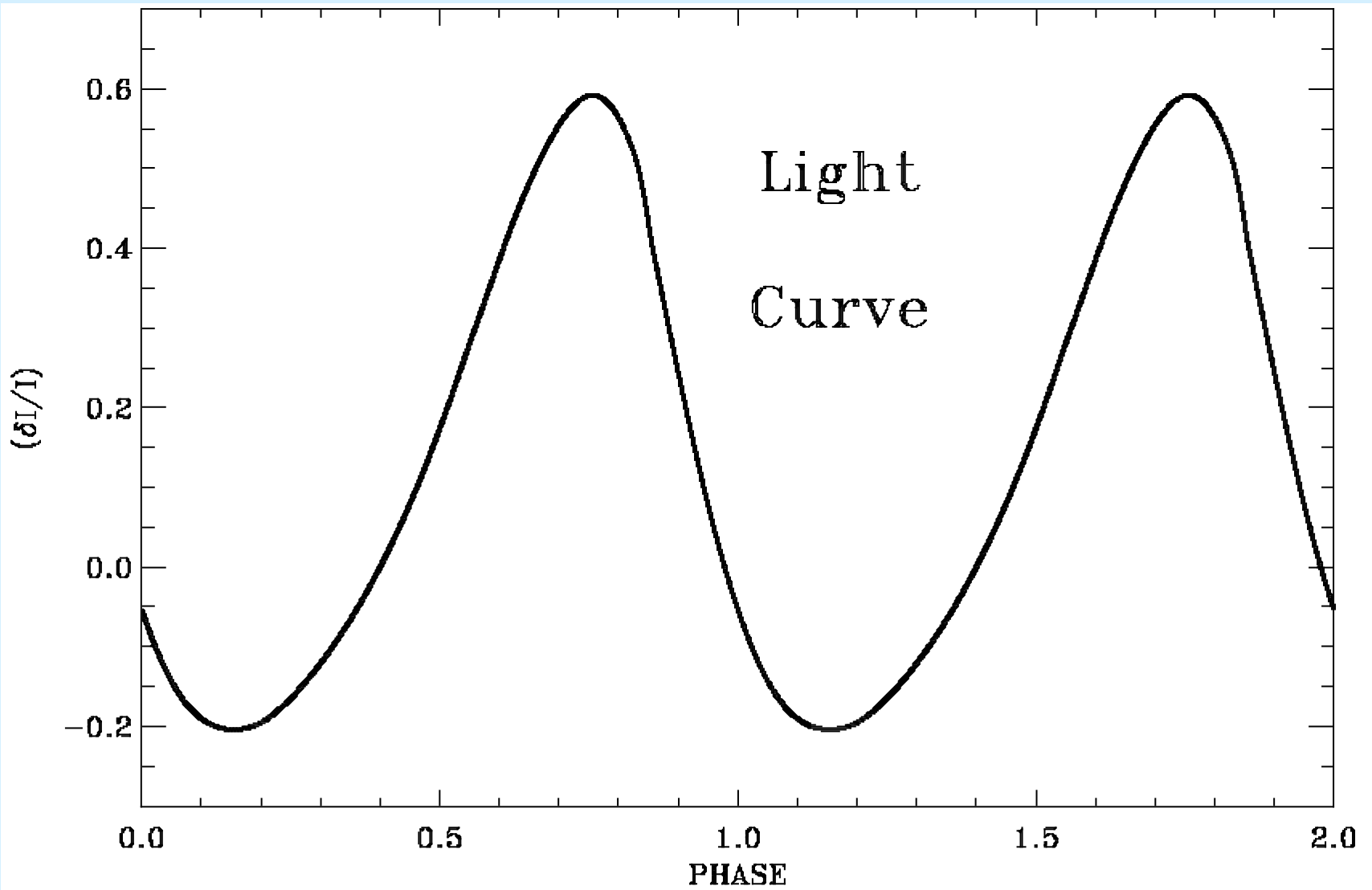
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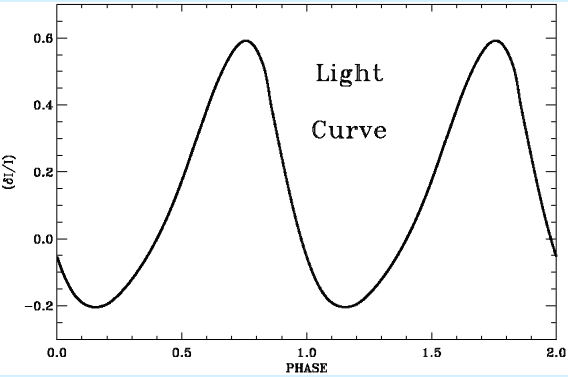
**Radiation hydrodynamics**  
simulation of CIRs in a hot-star wind

These may stem from large-scale surface structure that induces spiral wind variation analogous to solar **Corotating Interaction Regions**.

# Radial pulsations in BW Vul

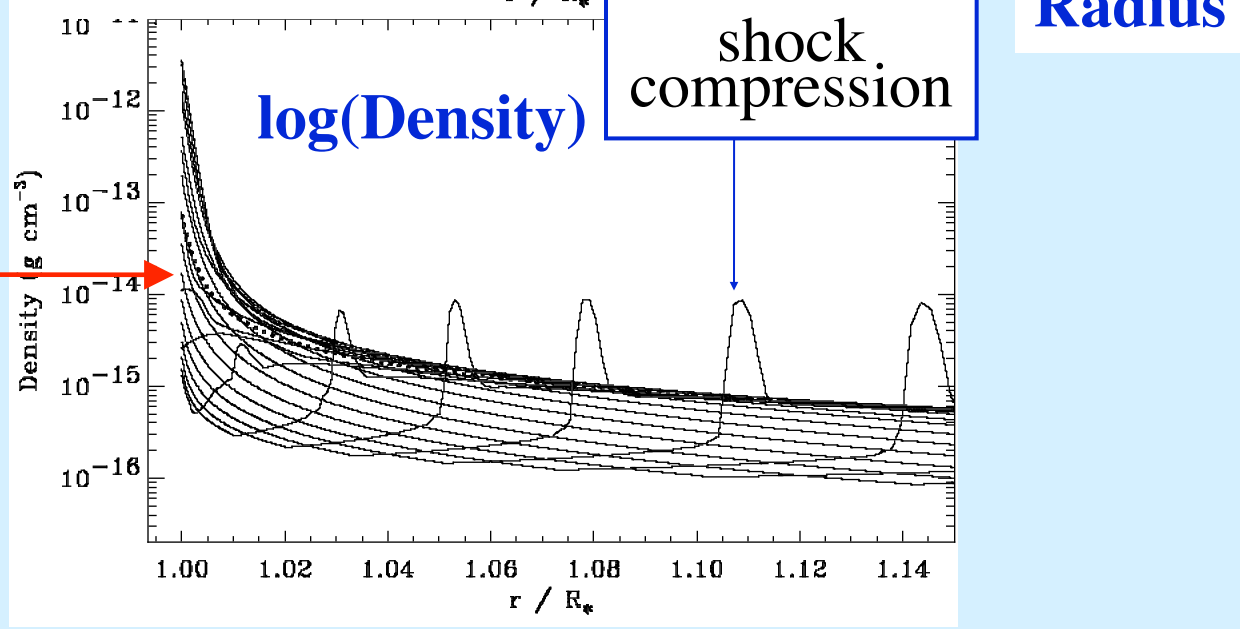
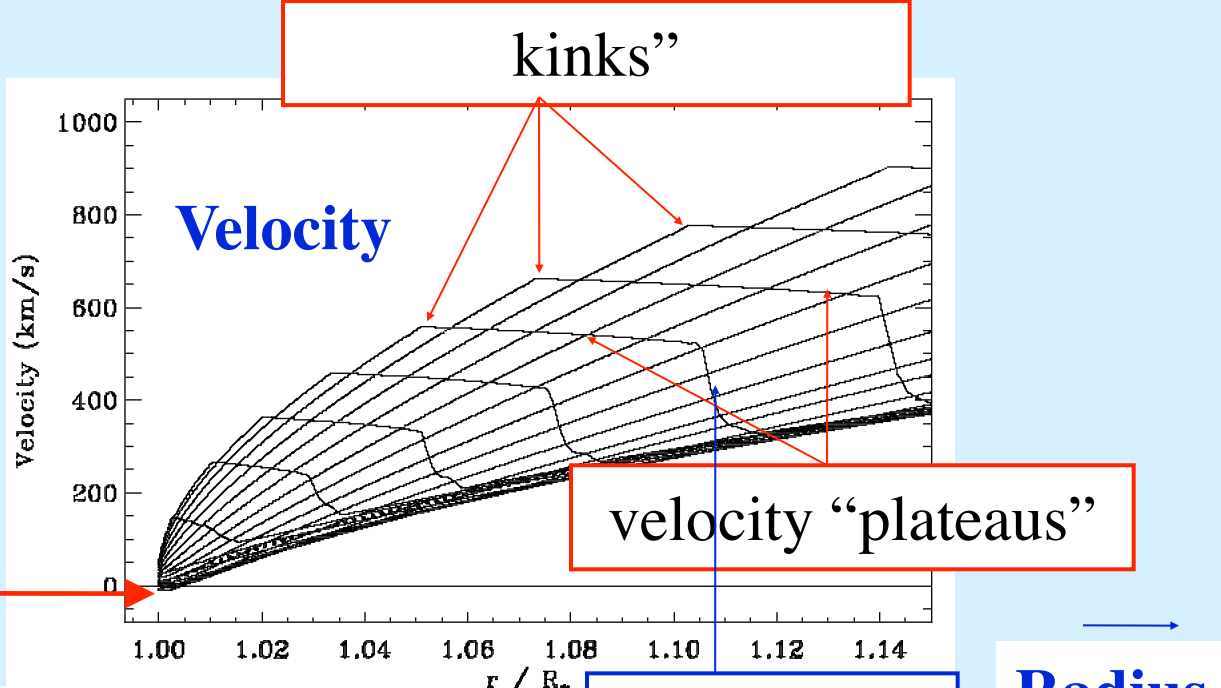


# Wind variations from base perturbations in density and brightness

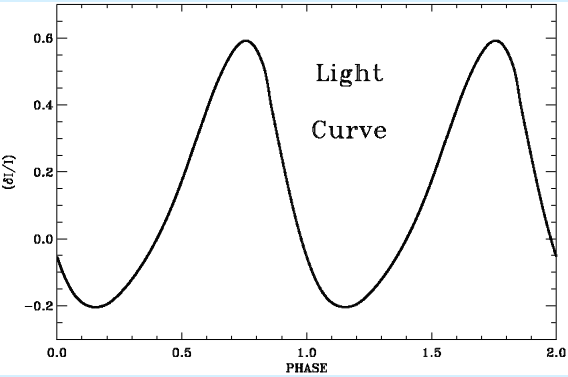


radiative driving modulated by brightness variations

wind base perturbed by  $\delta\rho/\rho \sim 50$

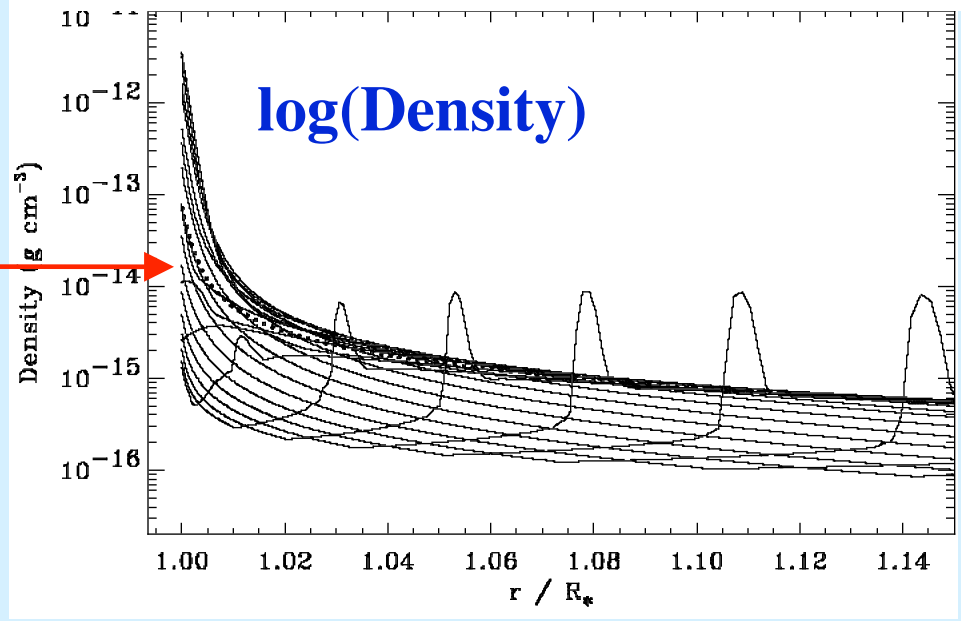
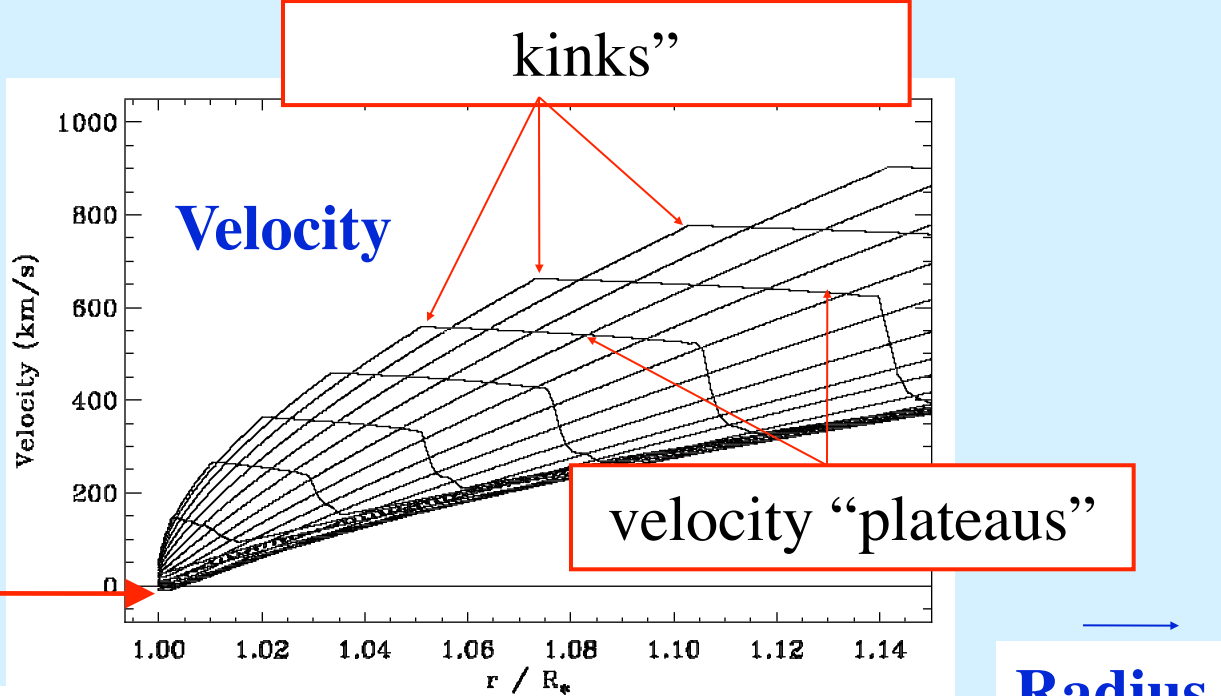


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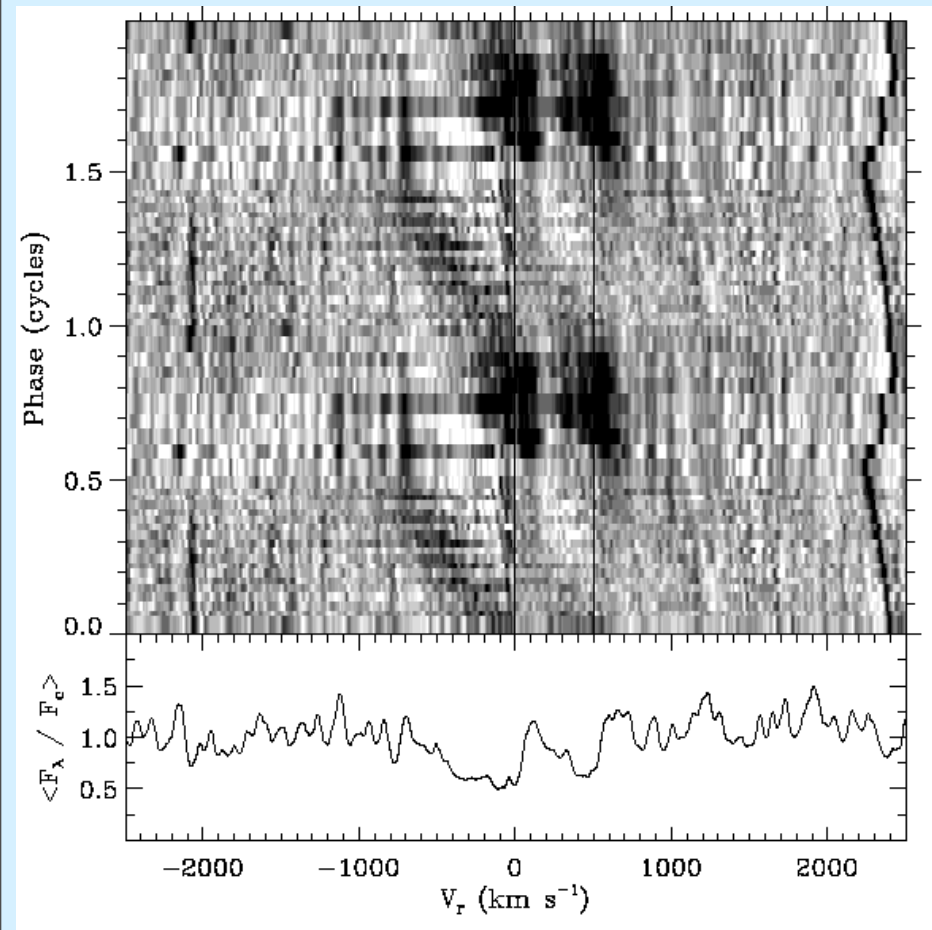
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# Dynamic spectra

C IV

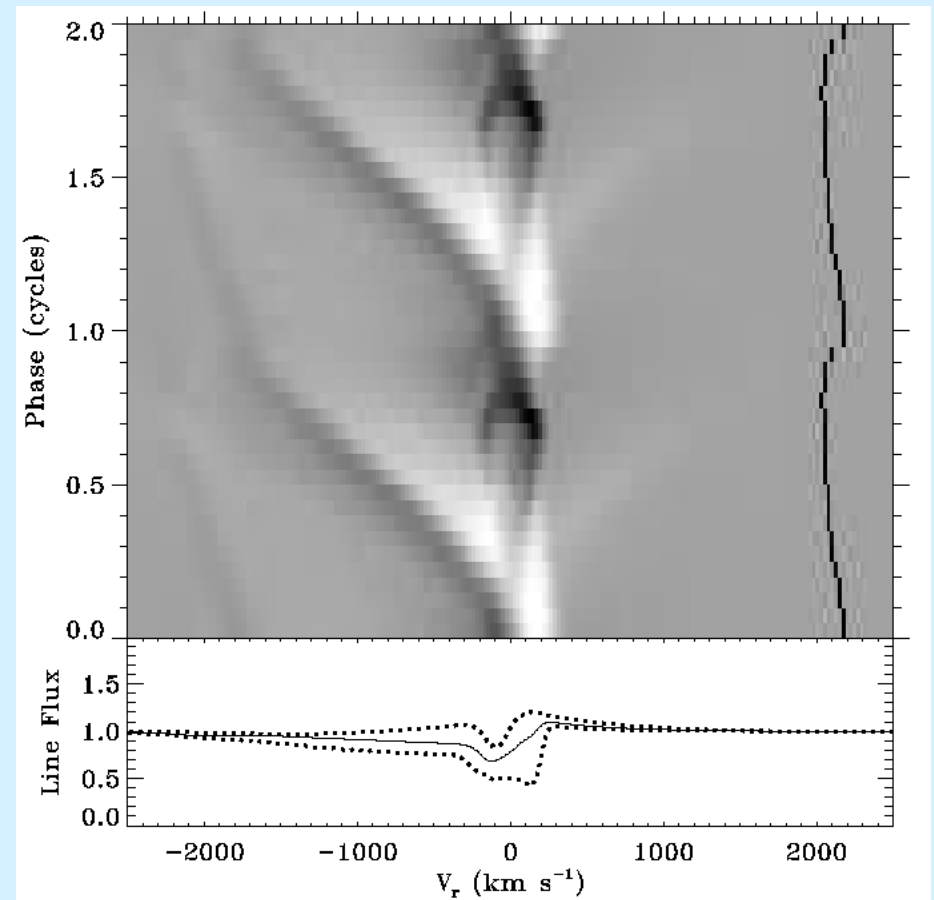
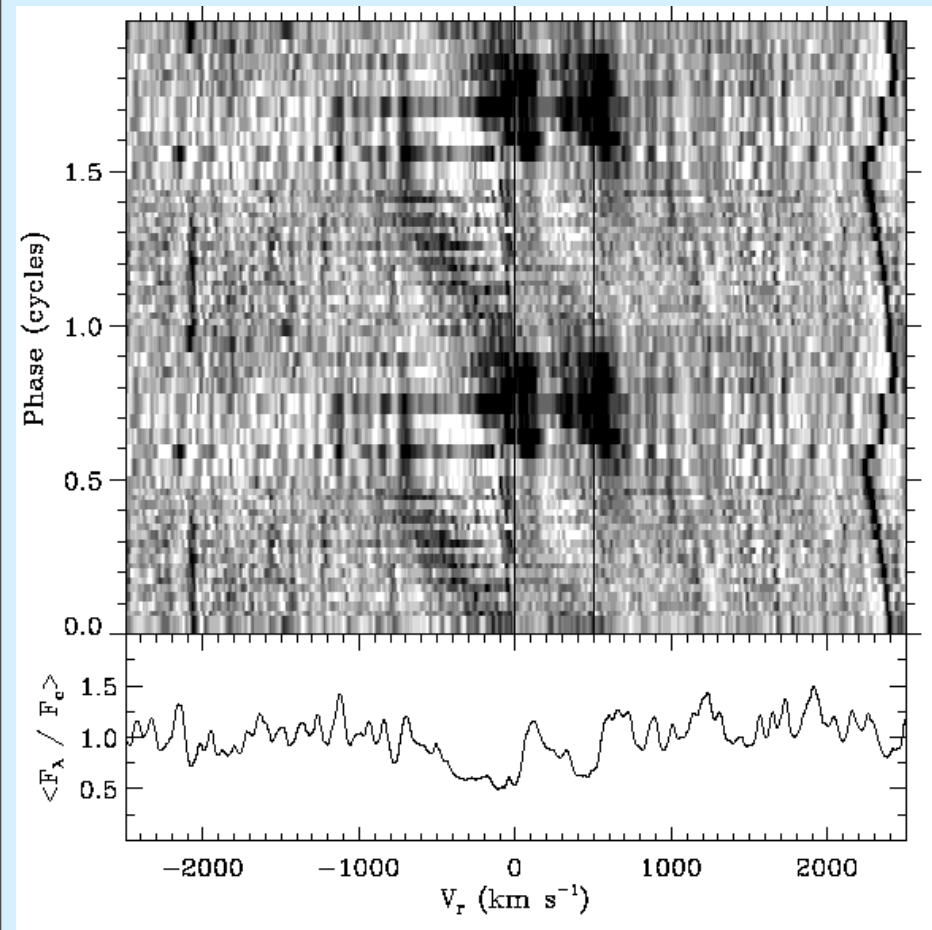




# Dynamic spectra

C IV

Model line





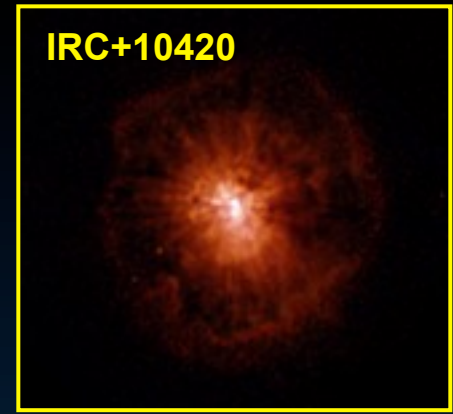
## Massive, Luminous stars:

Several  $M_{\odot}$  of circumstellar matter resulting from brief eruptions, expanding at about 50-600 km/s.

VY CMa



IRC+10420



P Cygni

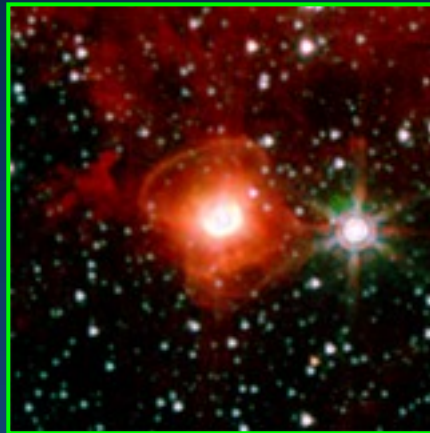


Pistol Star (Figer et al. 1999)



SN1987A

(courtesy P. Challis)



HD 168625

(Smith 2007)



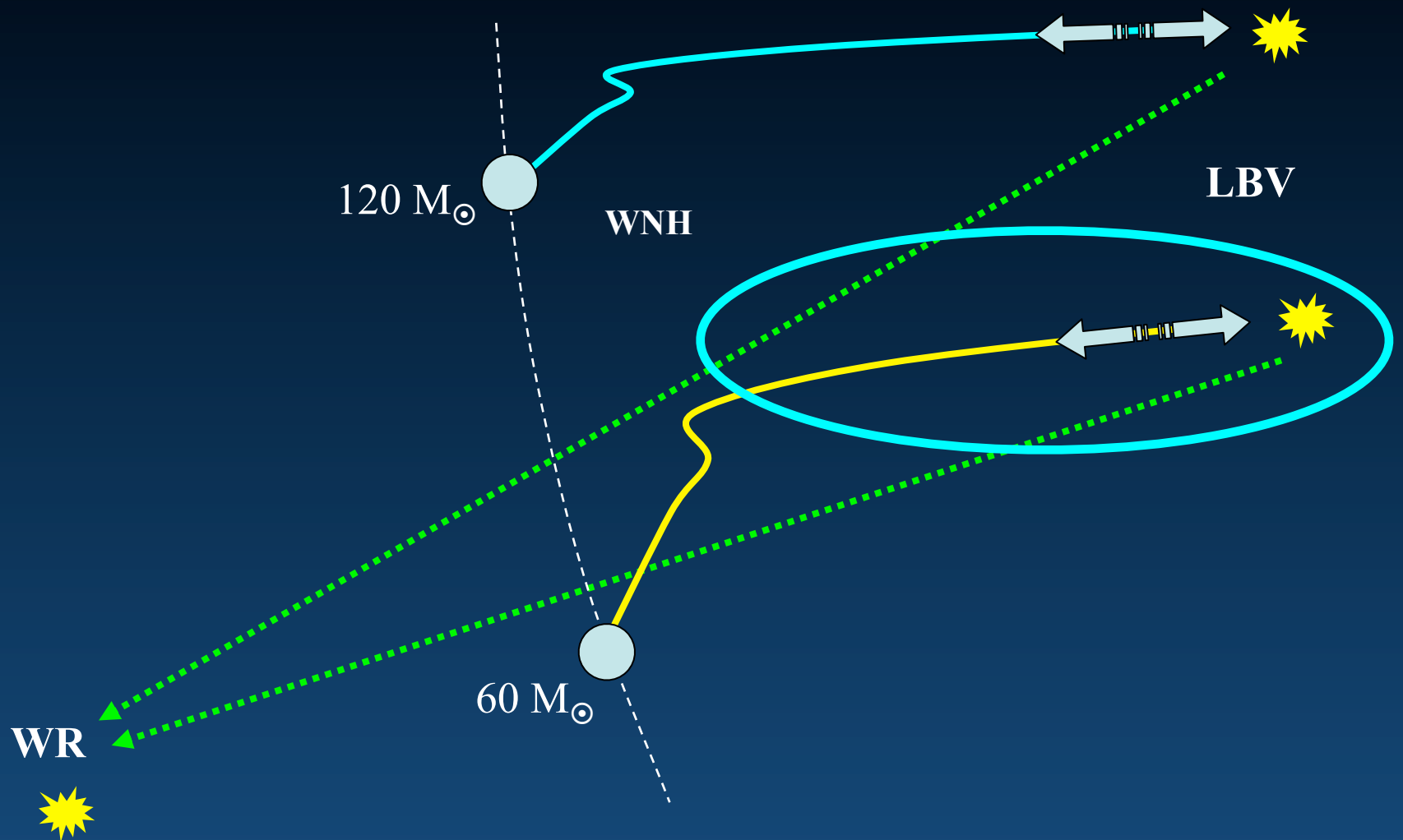
Sher 25

(Brandner et al. 1997)

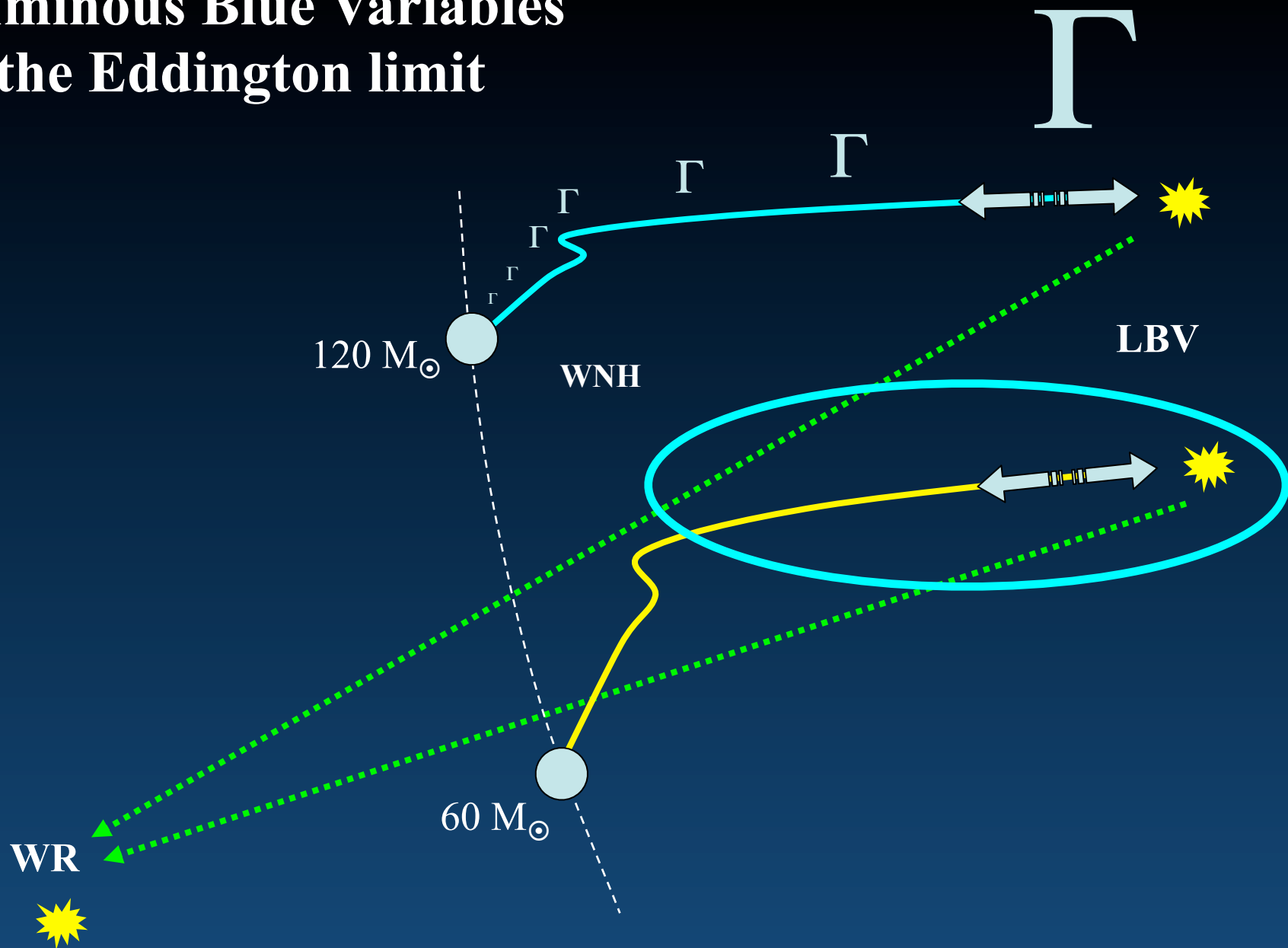


Eta Car

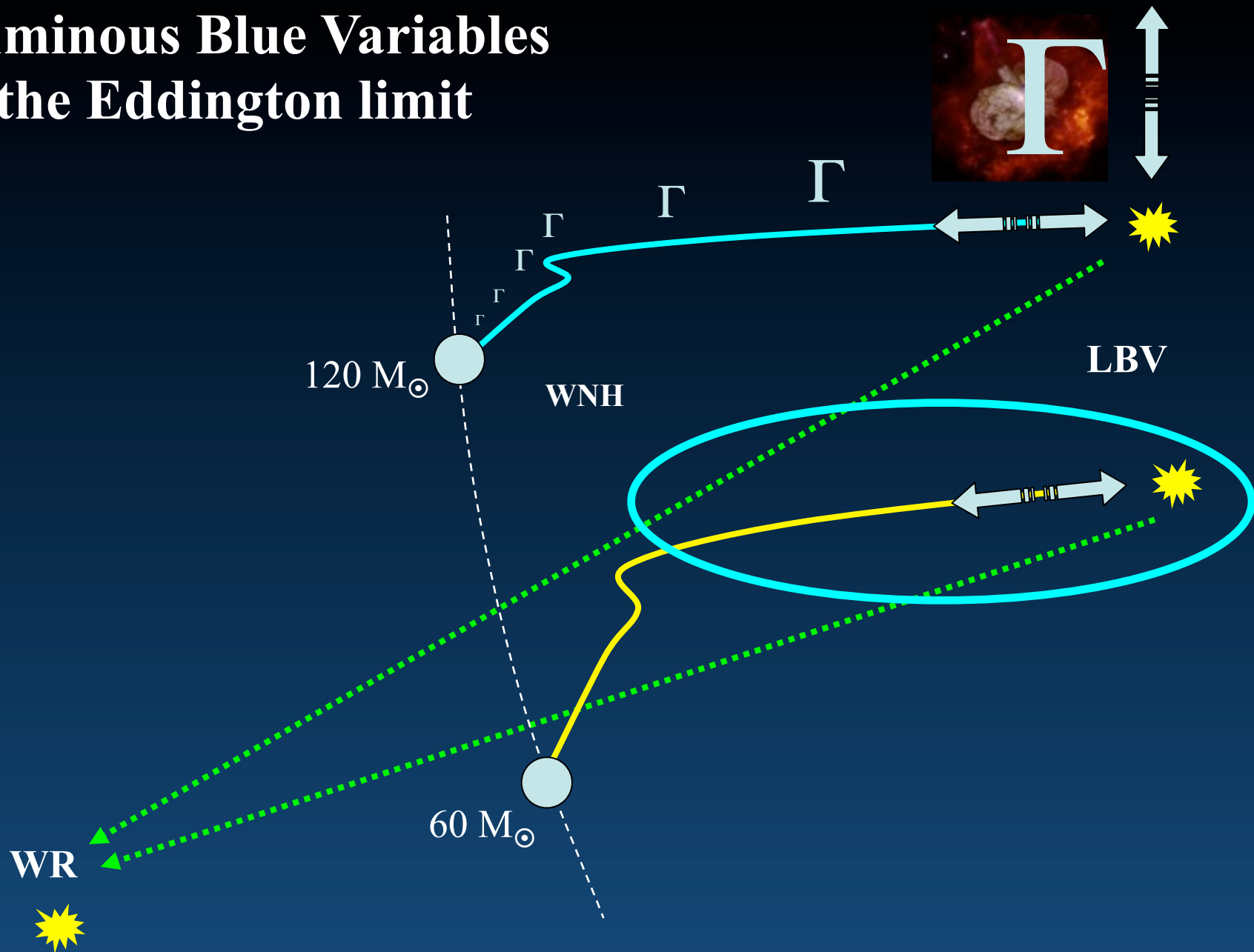
# Luminous Blue Variables & the Eddington limit



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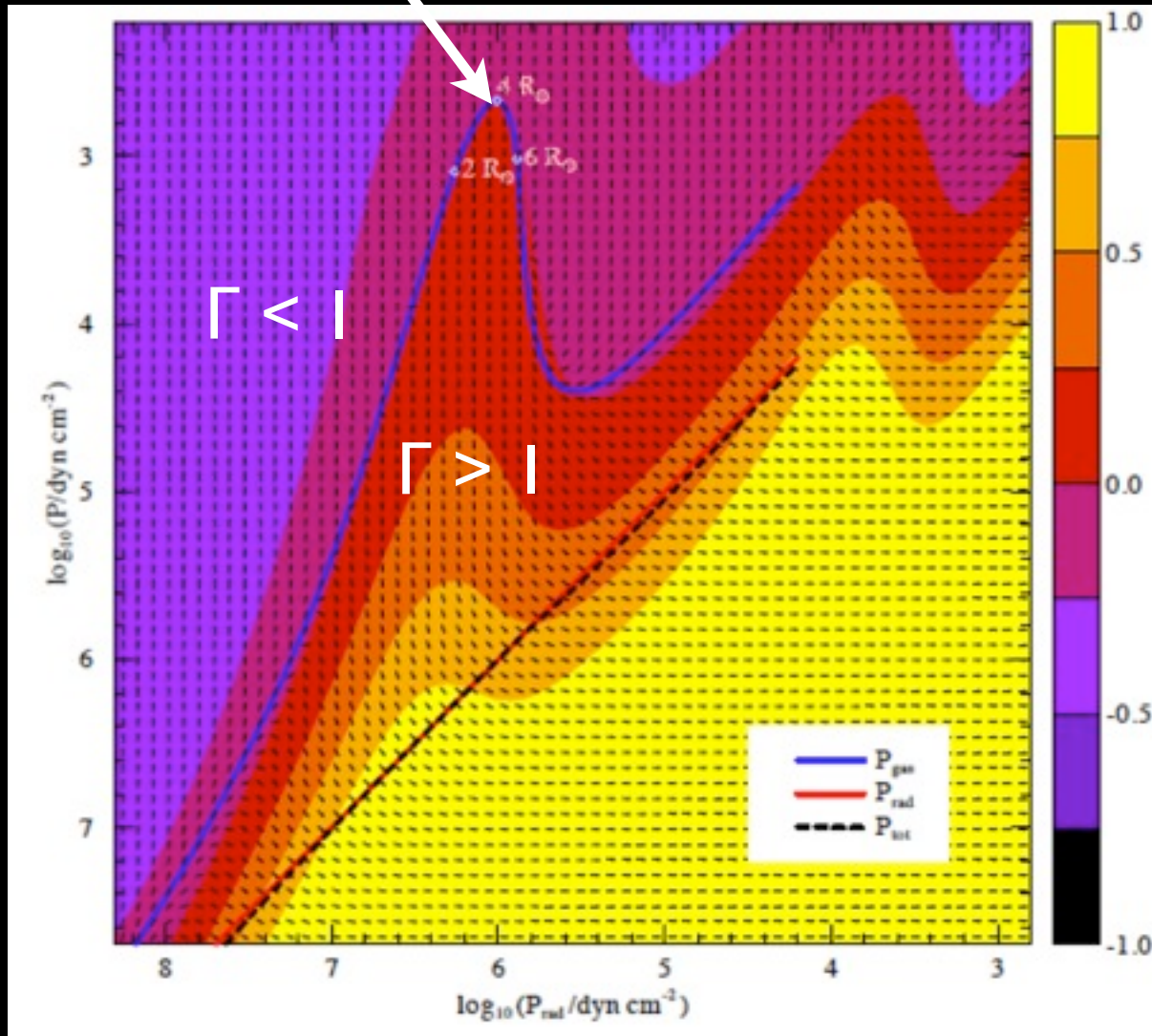


# Luminous Blue Variables & the Eddington limit



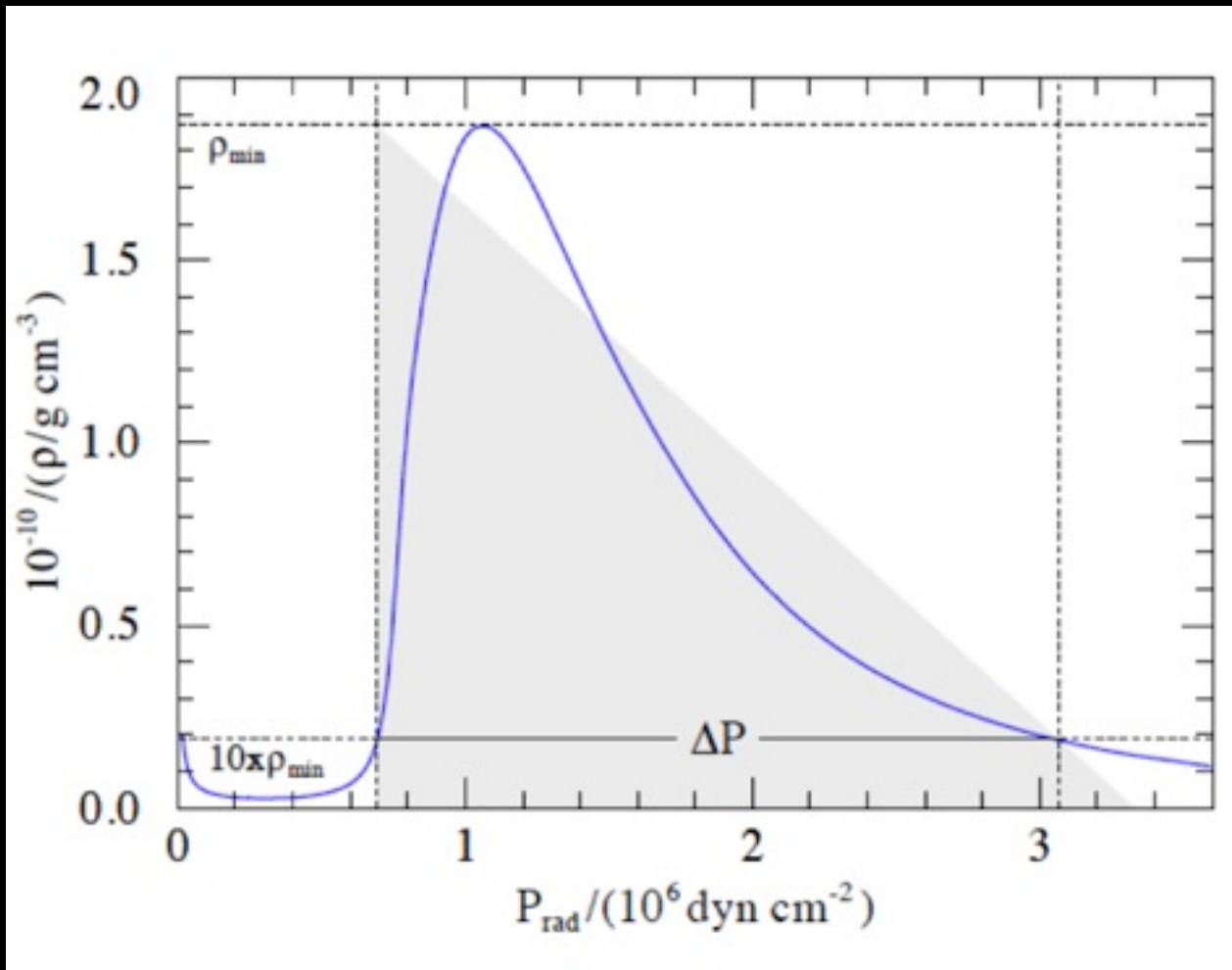
# Fe-bump can inflate envelope

$P_{\text{gas}}$



$P_{\text{rad}}$

$R_{out}$  ←  $R_{in}$



$1 / \rho_{min}(\Gamma, Z)$

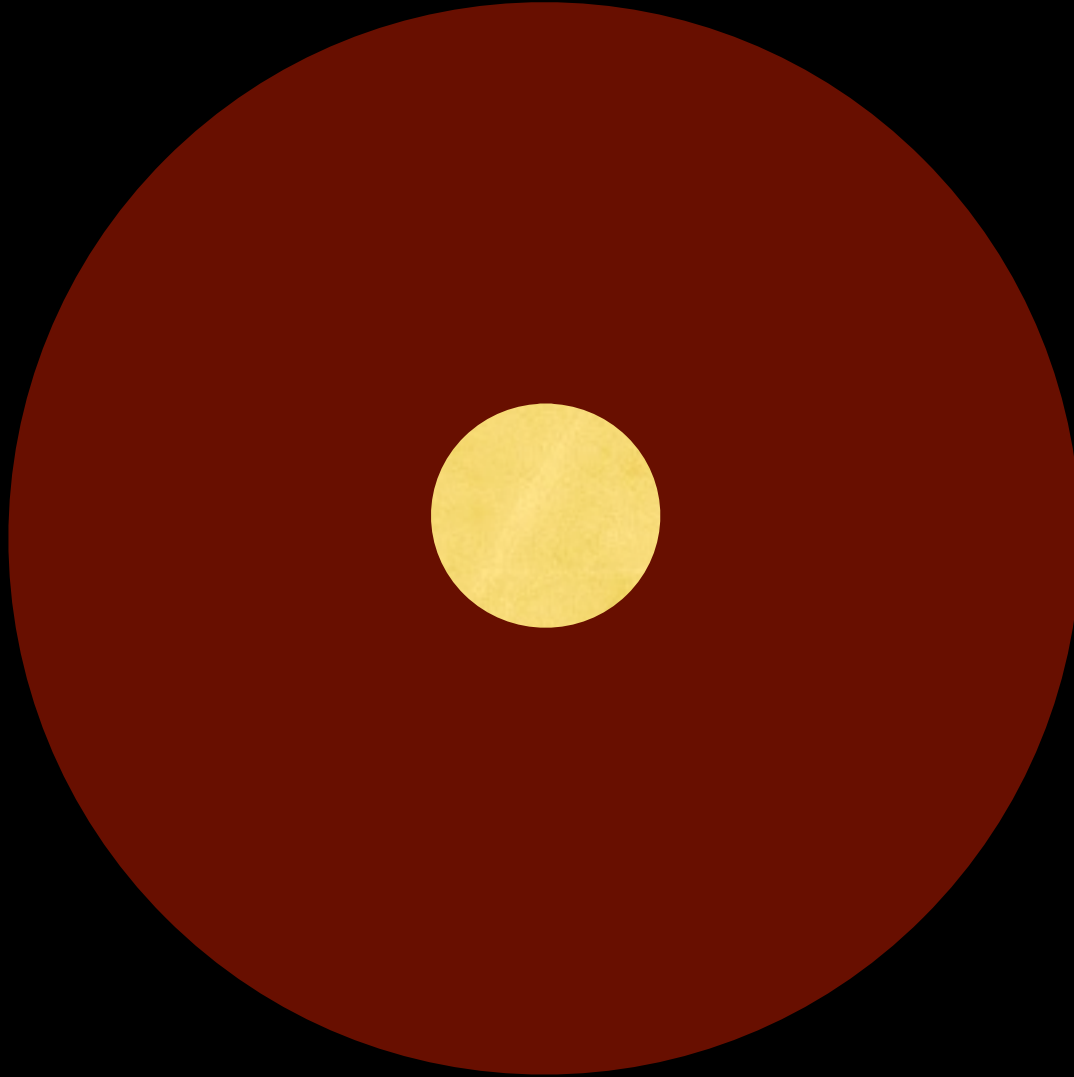
$$\frac{R_{out}}{R_{in}} = \frac{1}{1 - W}$$

$$W \simeq \frac{R_{in}}{GM} \frac{\Delta P}{2\rho_{min}}$$

# Envelope Inflation-Dissipation Cycle

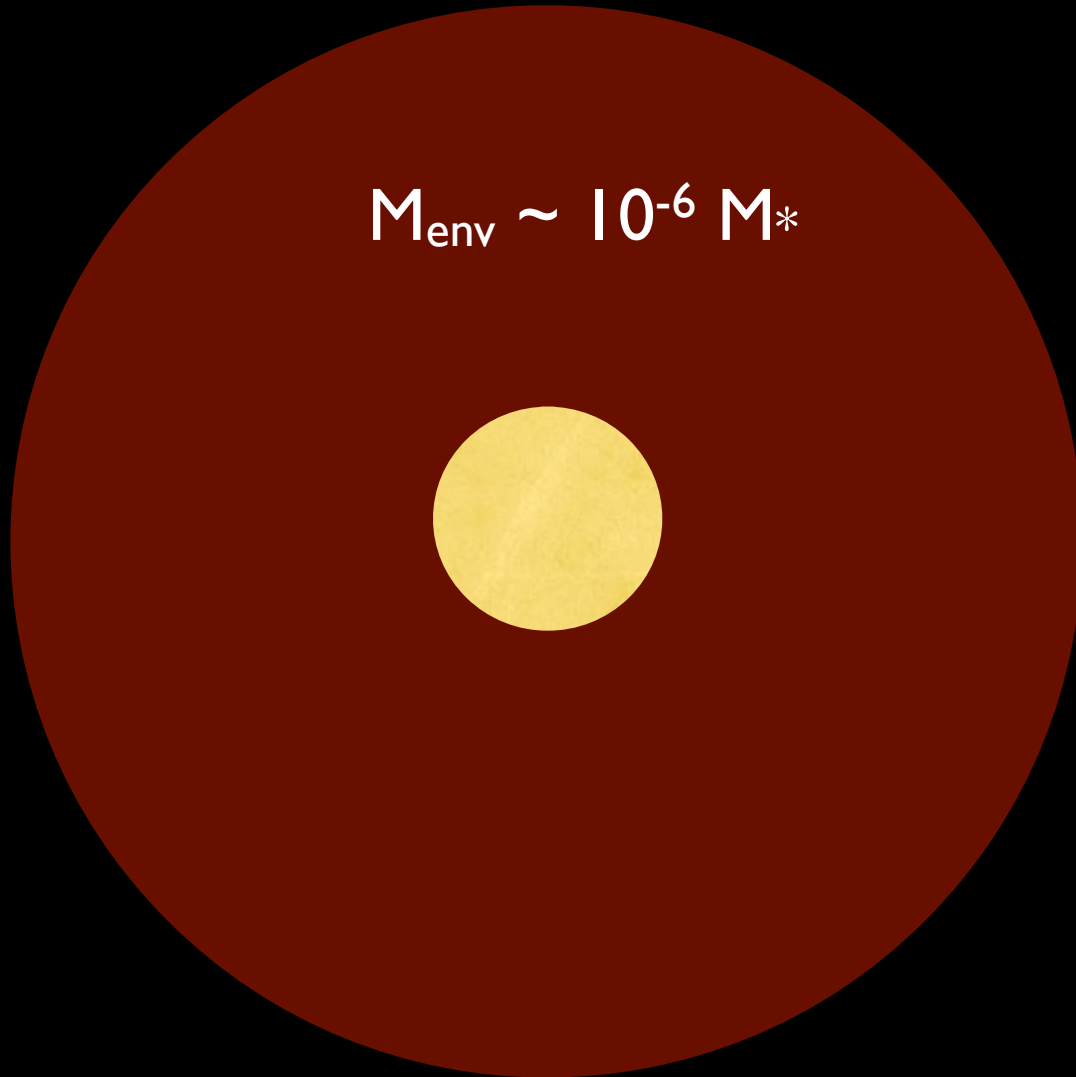


# Envelope Inflation-Dissipation Cycle

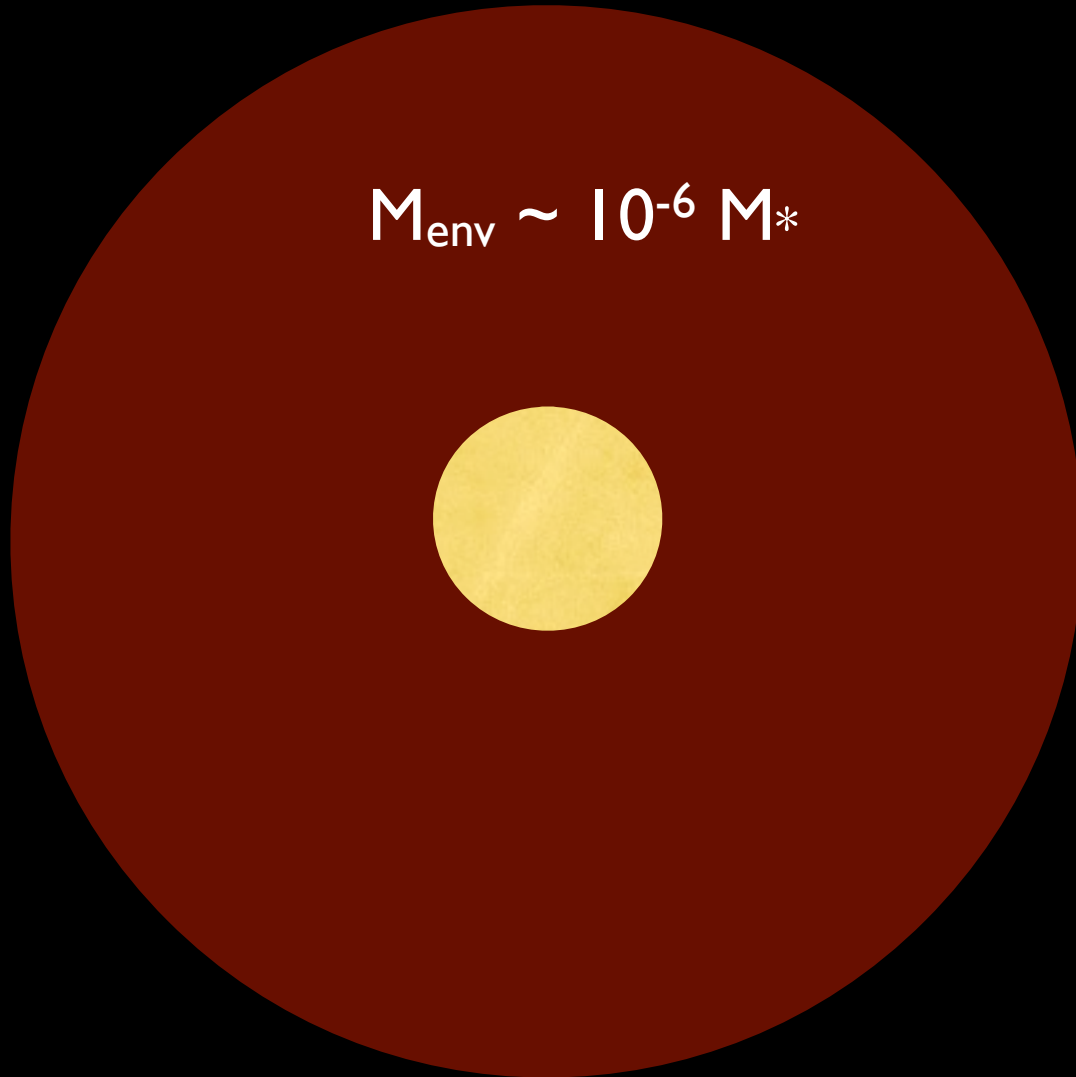




# Envelope Inflation-Dissipation Cycle



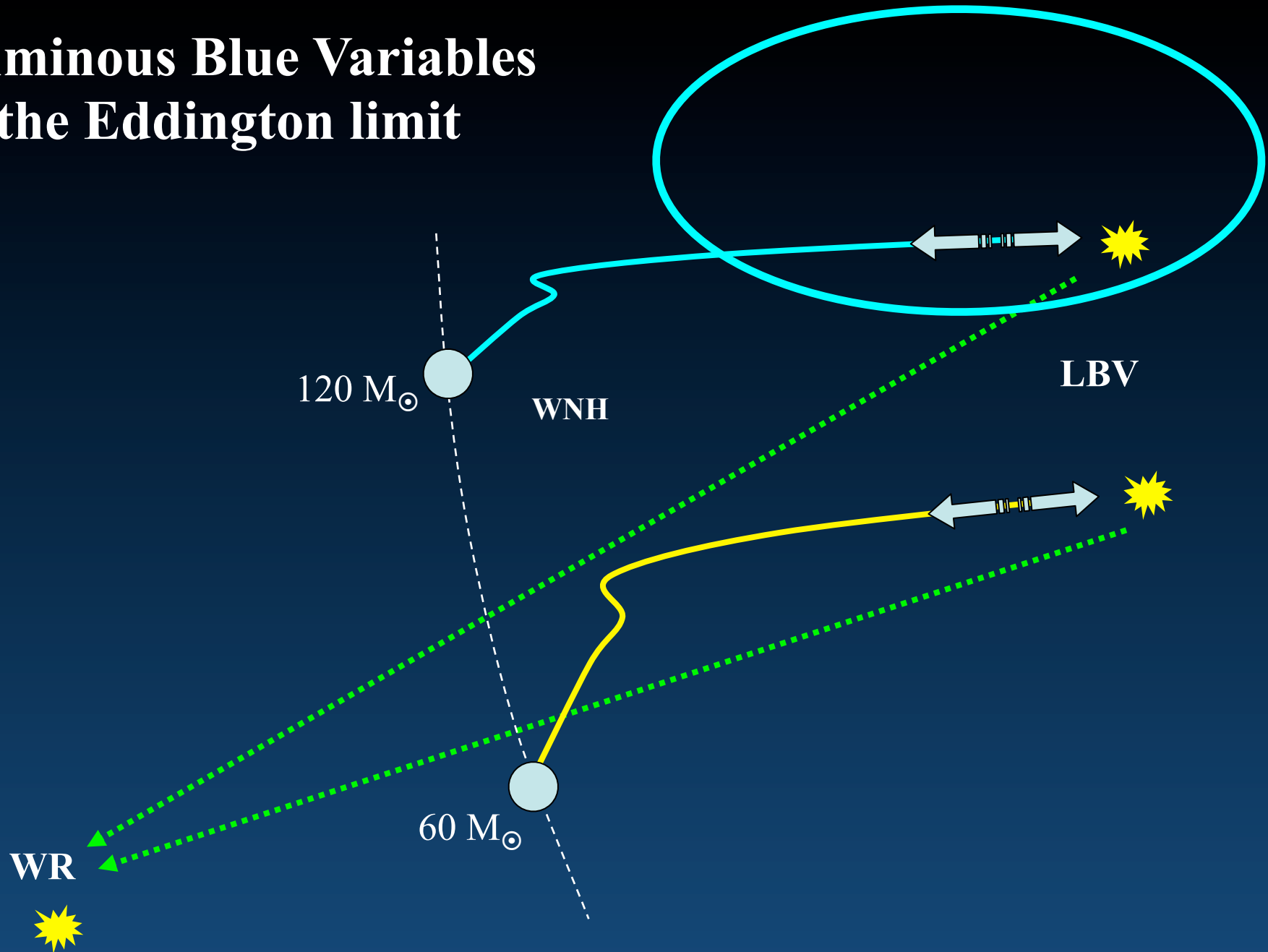
# Envelope Inflation-Dissipation Cycle



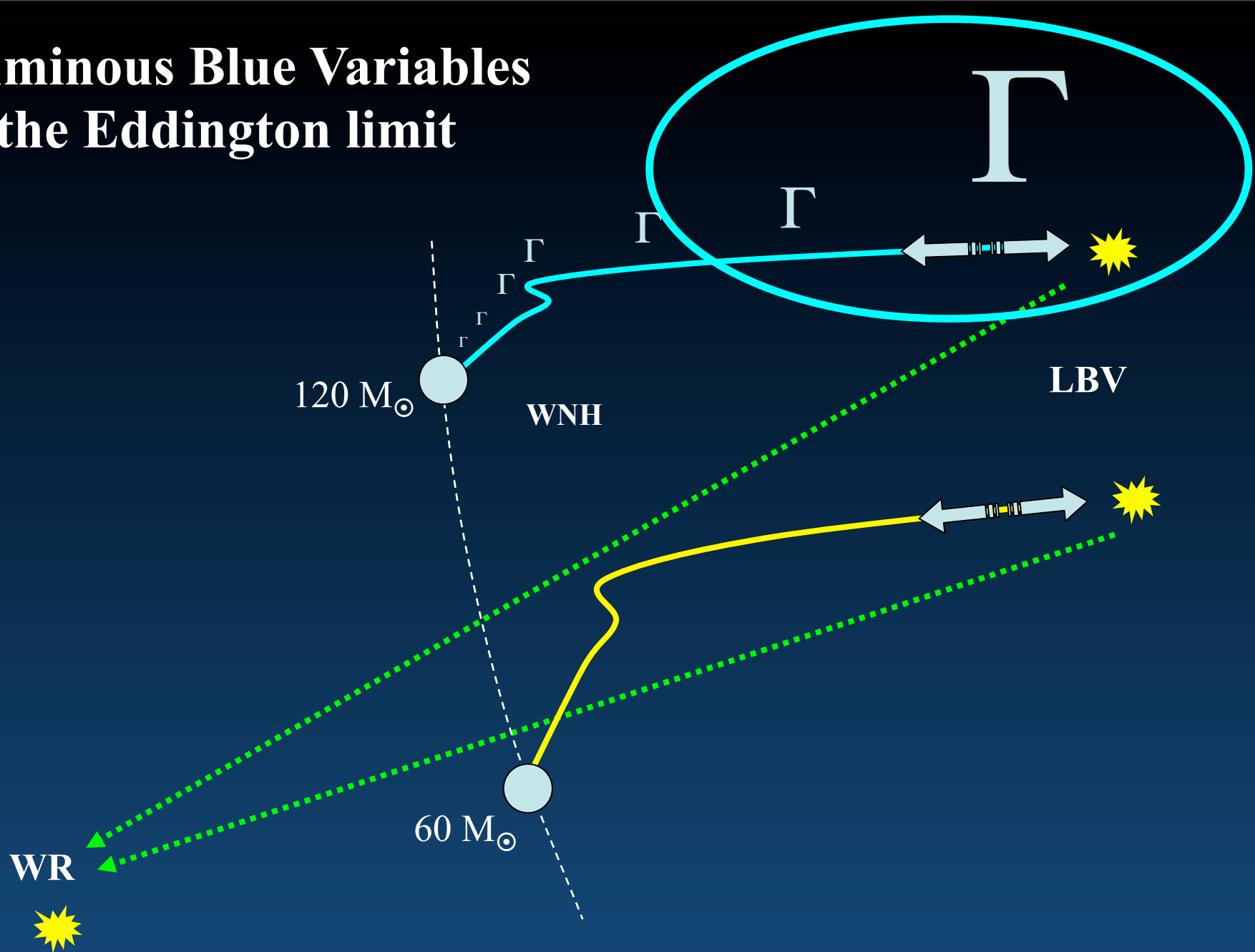
$$M_{\text{env}} \sim 10^{-6} M_*$$

$$T \downarrow \Rightarrow \kappa \uparrow \Rightarrow \dot{M} \uparrow$$

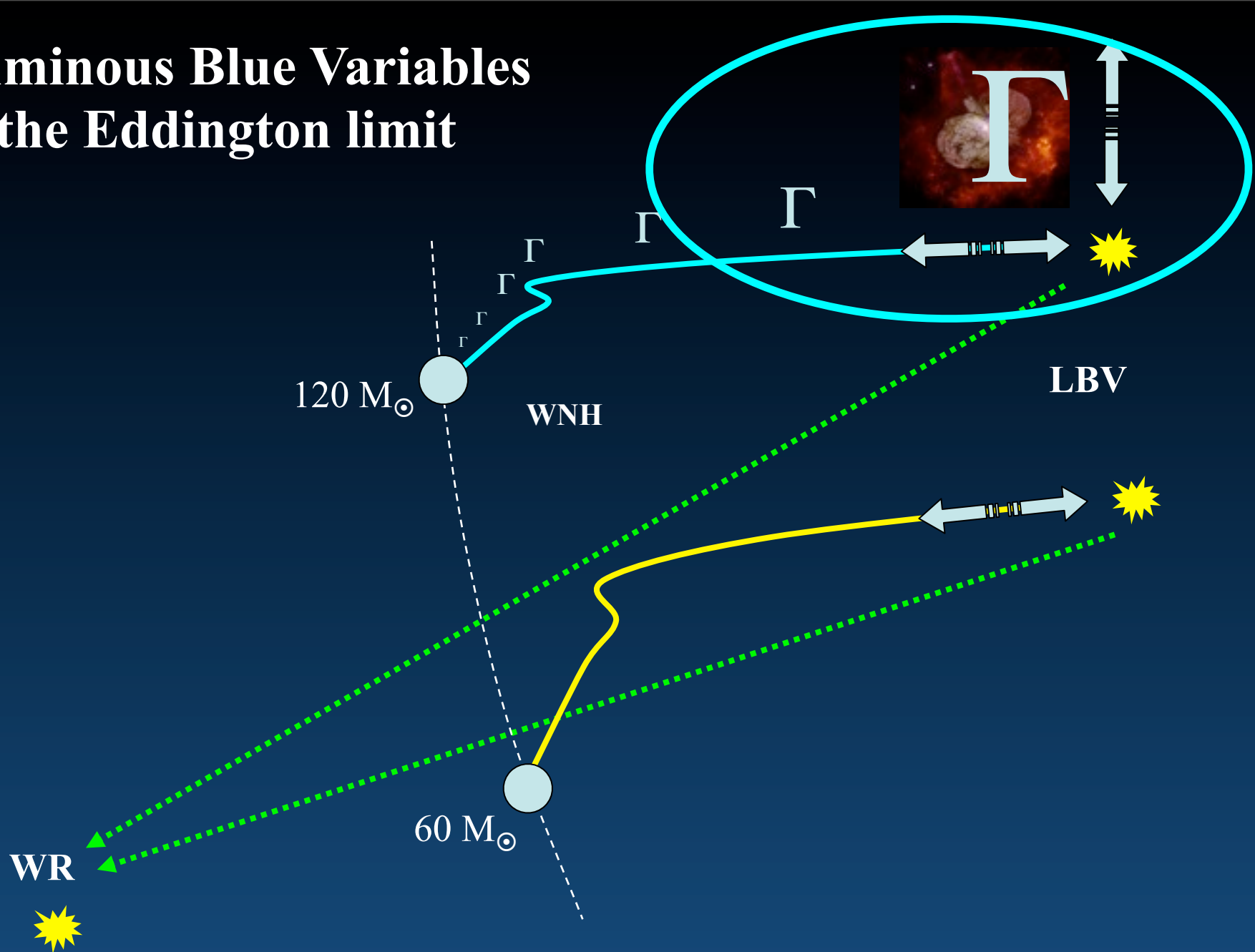
# Luminous Blue Variables & the Eddington limit



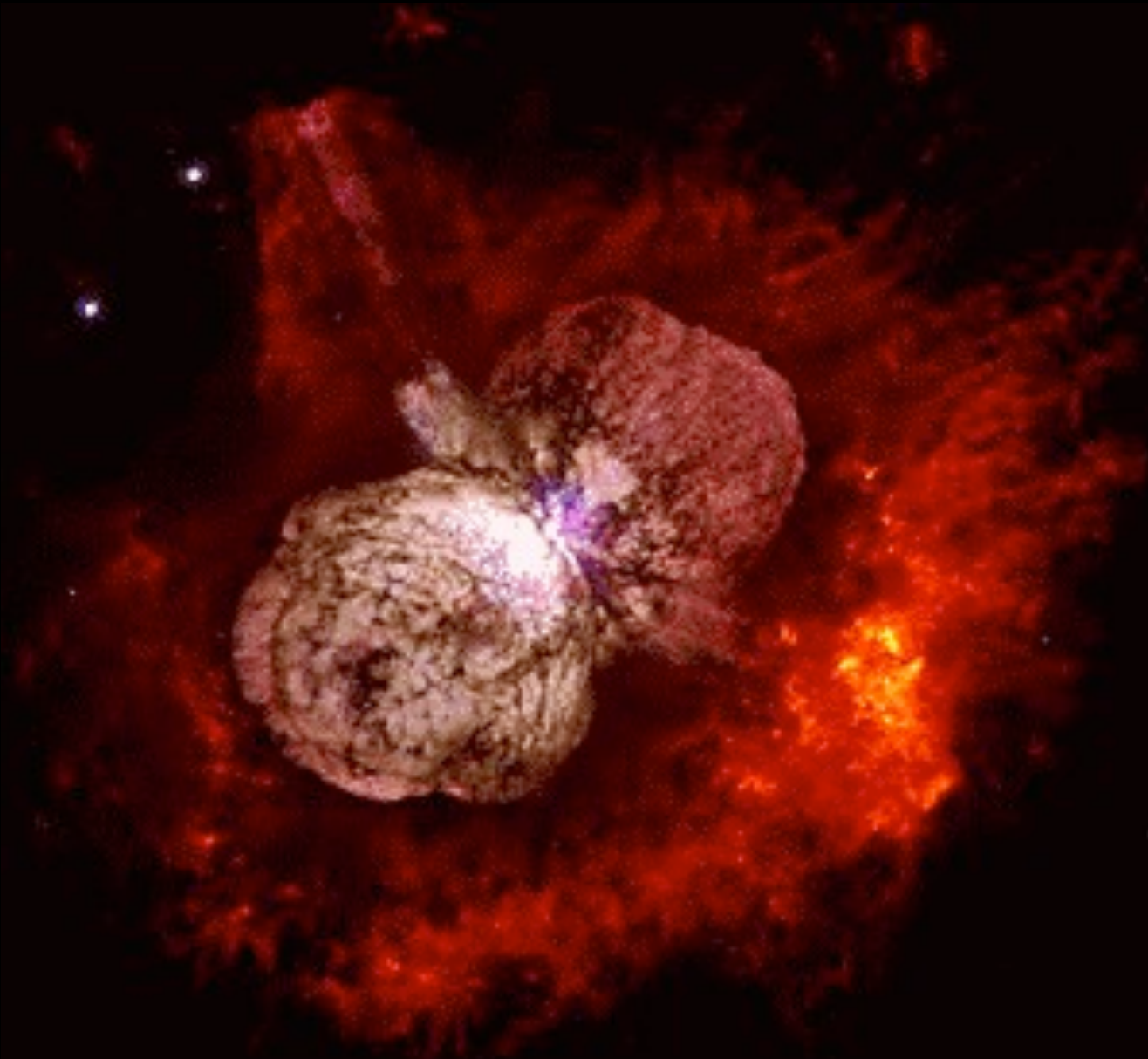
# Luminous Blue Variables & the Eddington limit



# Luminous Blue Variables & the Eddington limit



# Eta Carinae



# Eta Car's Extreme Properties

Present day:

$$L_{rad} \approx 5 \times 10^6 L_{\odot}$$
$$\approx L_{\text{Edd}}$$

$$\dot{M} \approx 10^{-3} M_{\odot}/\text{yr}$$

$$V_{\infty} \approx 600 \text{ km/s}$$

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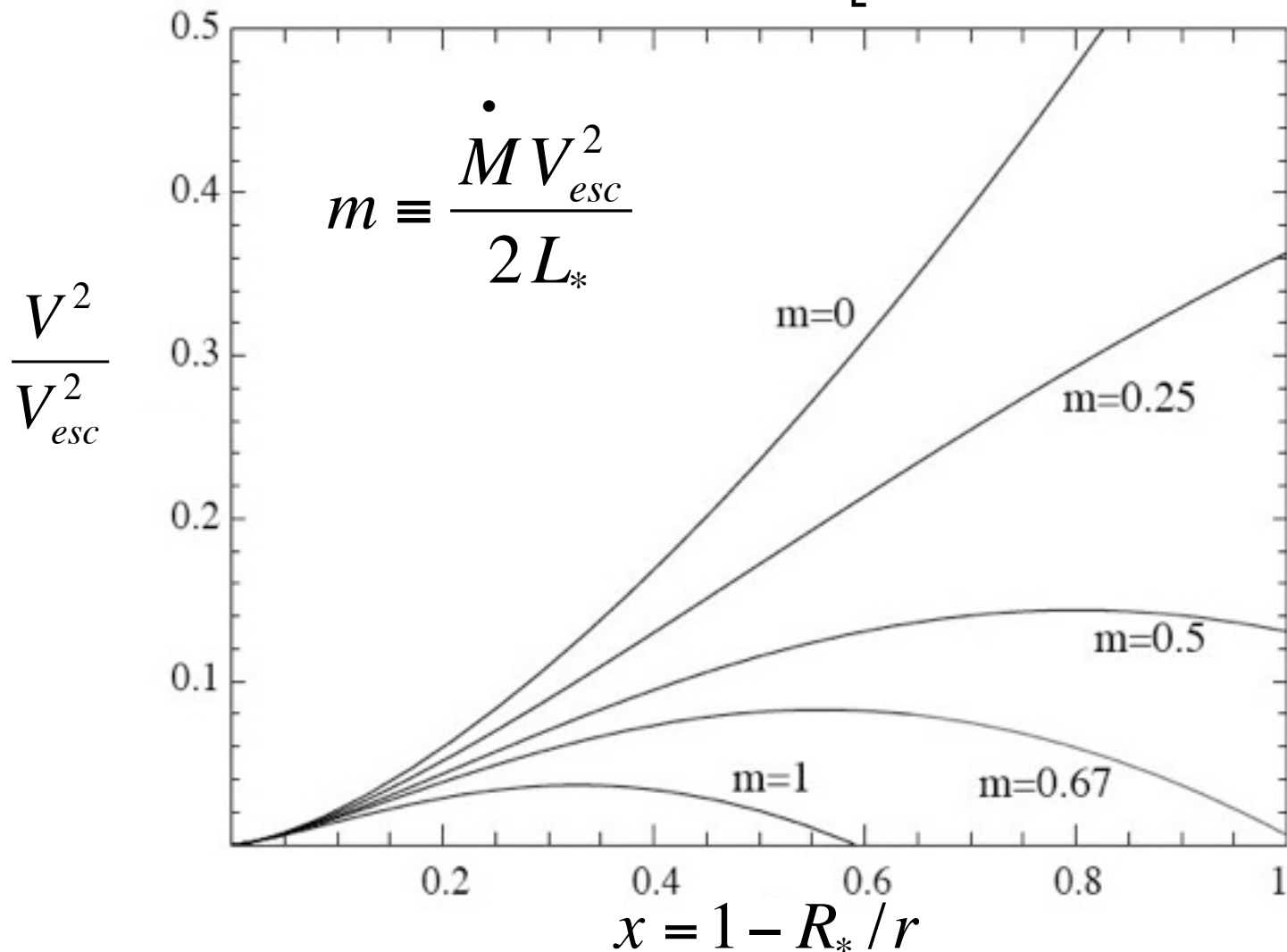
$$\approx L_{kin} = \dot{M} v_{\infty}^2 / 2$$

=> Mass loss is energy or “photon-tiring” limited

# Stagnation of photon-tired outflow

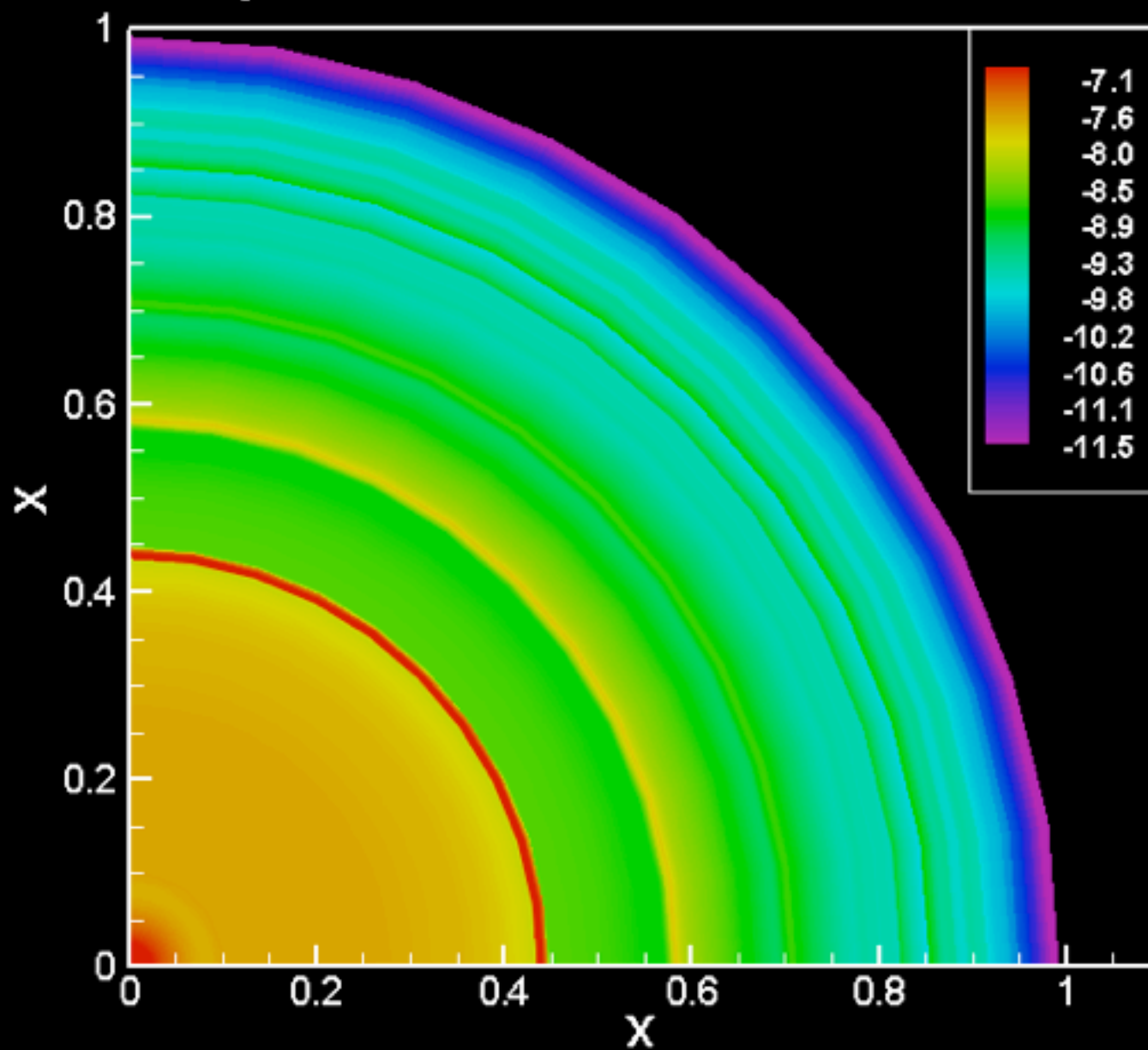
$$\frac{\kappa}{\kappa_{Edd}} = 1 + \sqrt{x}$$

$$L(r) = L_* - \dot{M} \left[ \frac{V^2}{2} + \frac{GM}{R} - \frac{GM}{r} \right]$$

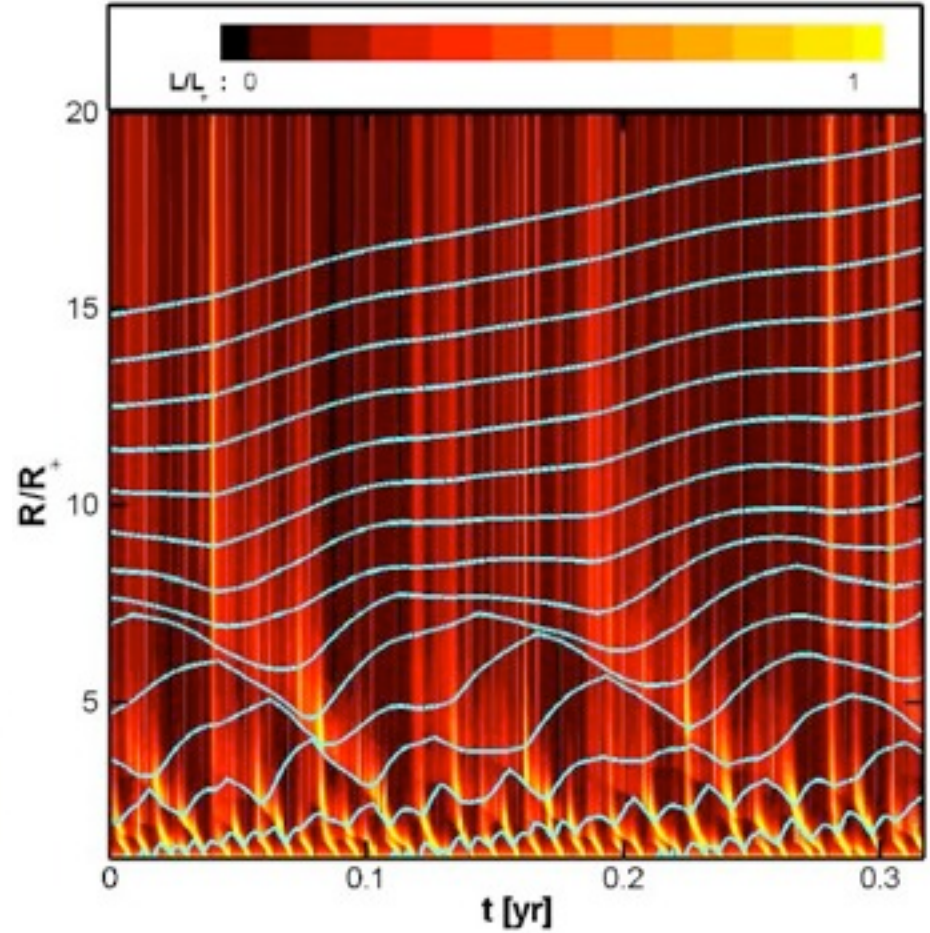
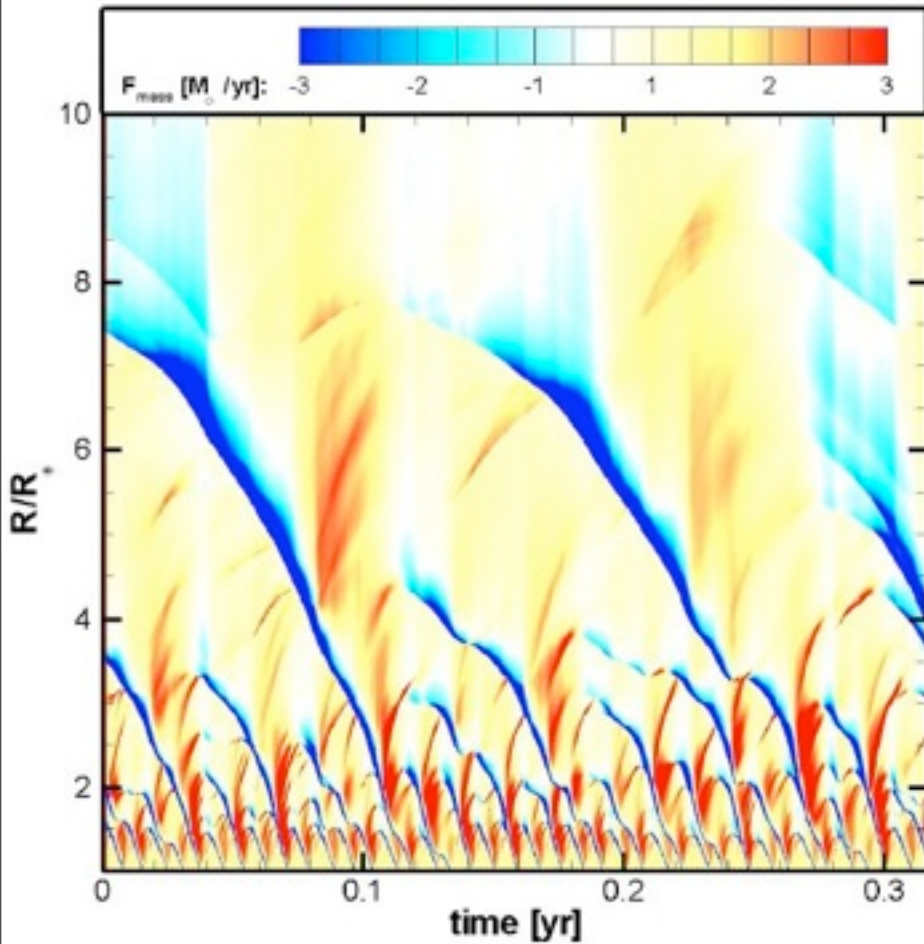




Density after 0.0000E+00 seconds



# Photon Tiring & Flow Stagnation

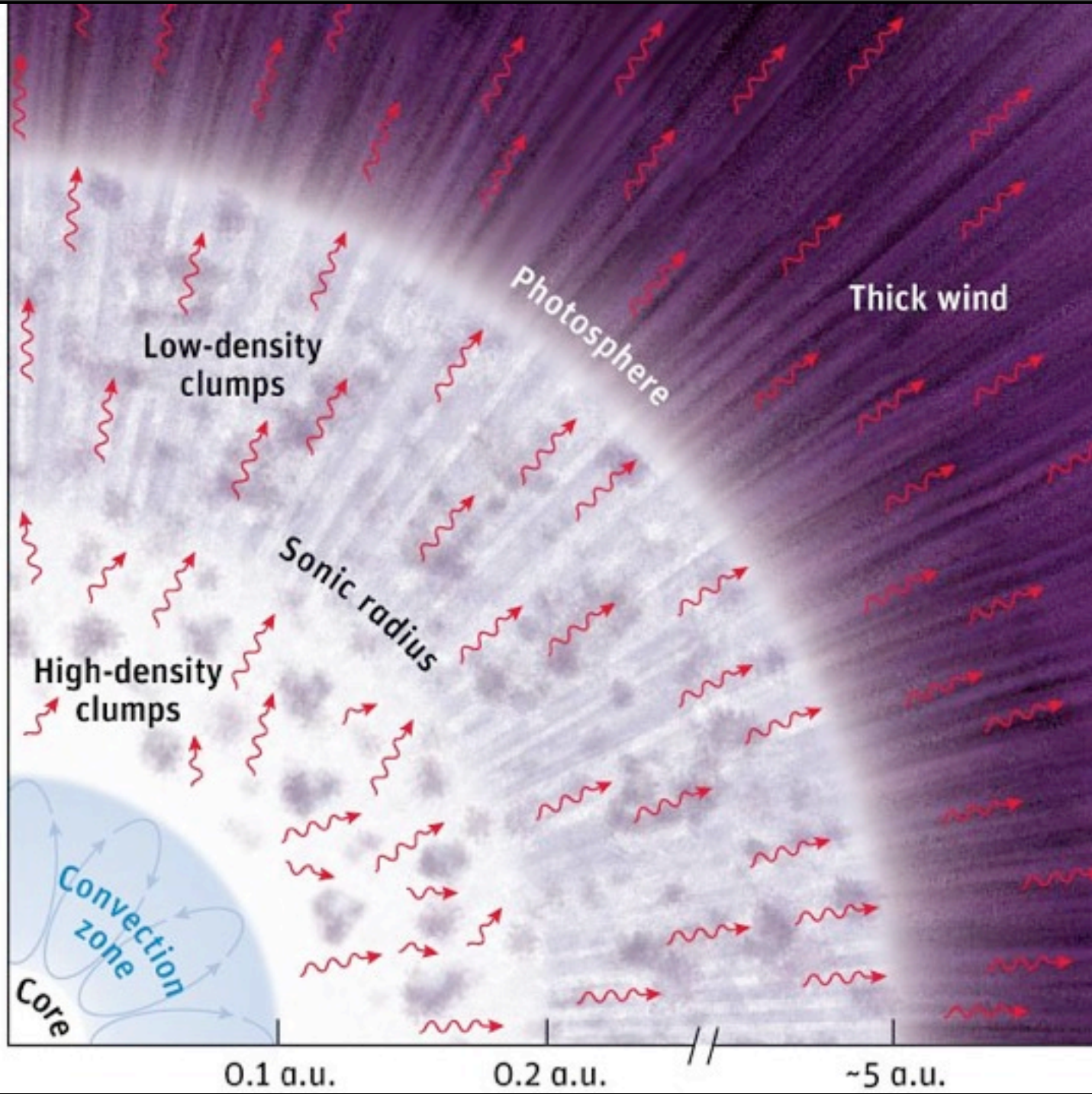


# Fluidized Bed



Spiegel 2006





# Summary

- Massive star winds driven by line-scattering
- Strong Line-deshadowing instability
  - small-scale clumping & embedded soft X-rays
- Large-scale structure from NRP or bright spots
- Rapid rotation  $\Rightarrow$  faster denser polar wind
- Eddington limit  $\Rightarrow$  LBV & Eruptions
  
- Wind magnetic channeling + rotation
  - centrifugally supported magnetospheres
- Magnetic spindown over 1 Myr