

Tearing, Reconnection, and Energy Dissipation in Plasma Turbulence

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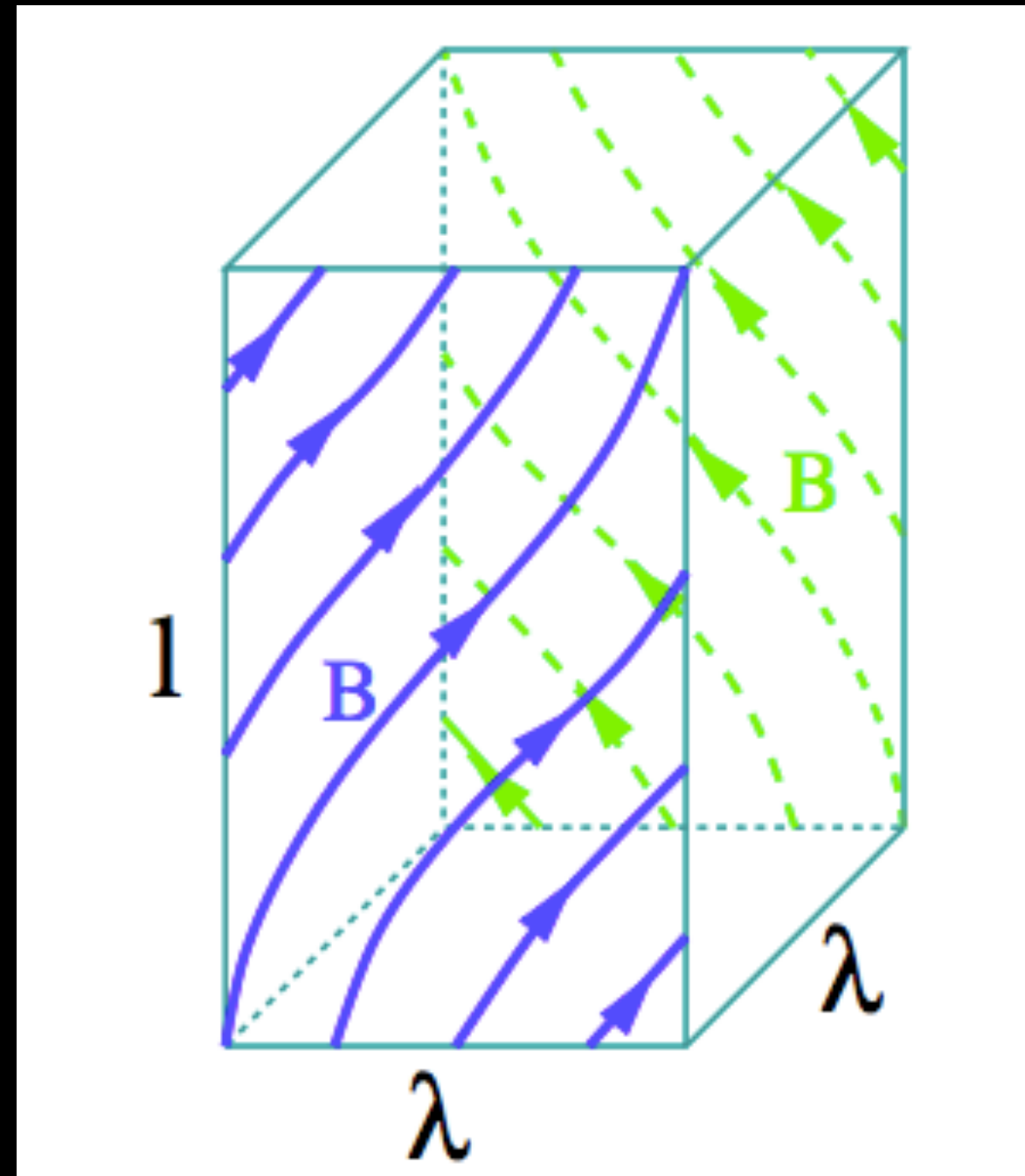


*Connecting Micro and Macro Scales:
Acceleration, Reconnection, and
Dissipation in Astrophysical Plasmas*
KITP, September 2019

- Understanding of magnetic turbulence in plasmas has matured greatly over the last decade or so.
- A prominent unsolved question remains that of how energy dissipates in turbulence. This is essential to understanding observations.
- Magnetic reconnection has long been suggested to play an important role in turbulence.
- Reconnection is essentially an energy dissipation/conversion mechanism, so an assessment of whether indeed it is active in turbulence is critical.
- Goal of this talk is to examine this question analytically.
- Details in Loureiro & Boldyrev, arXiv:1907.09610

Models of MHD turbulence

MHD turbulent eddies are not isotropic

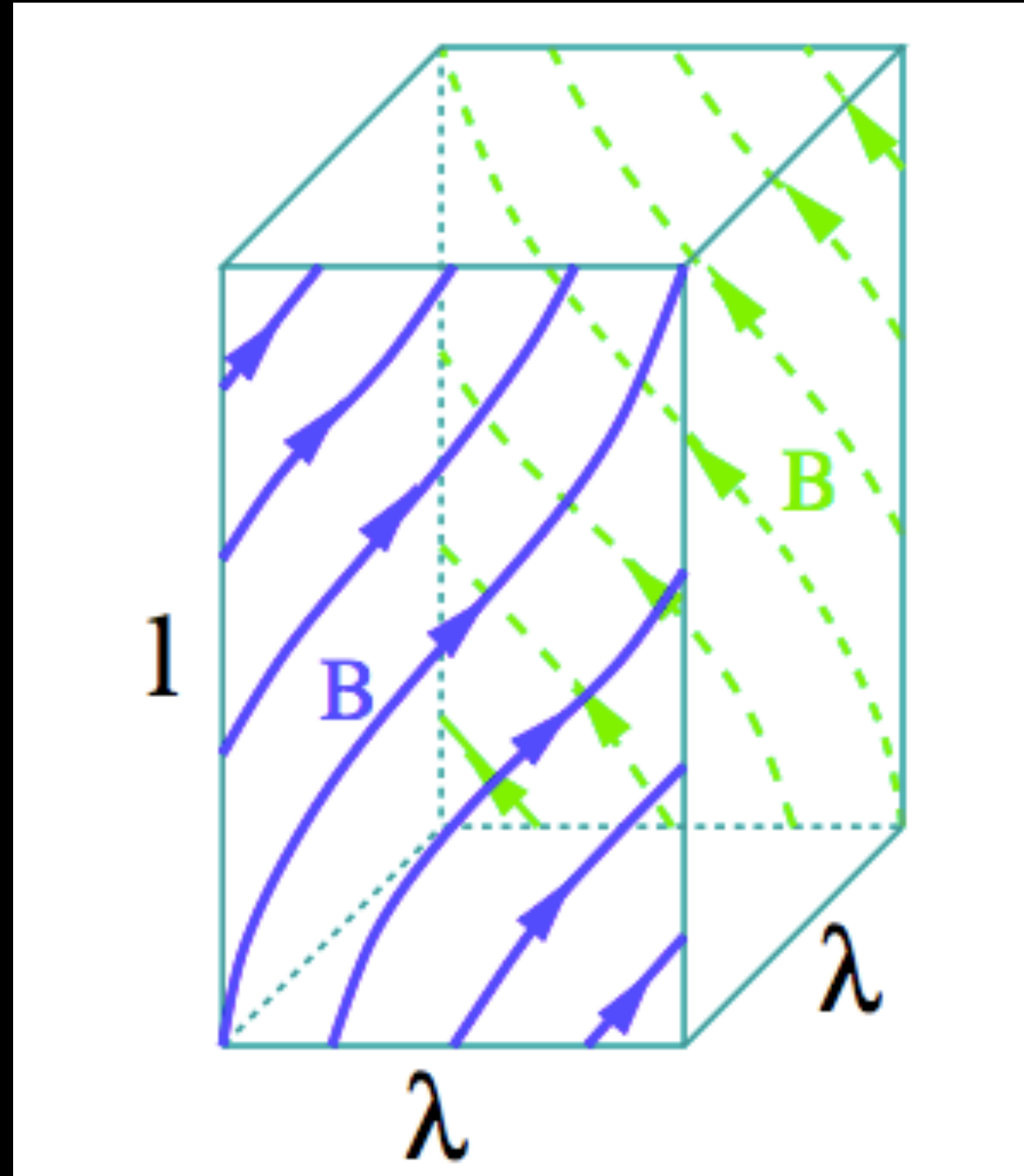


Goldreich-Sridhar (GS95): eddies' dimension perpendicular to the background field are comparable; become filaments at small scales. (key idea: critical balance).

$$E(k) \sim k^{-5/3}$$

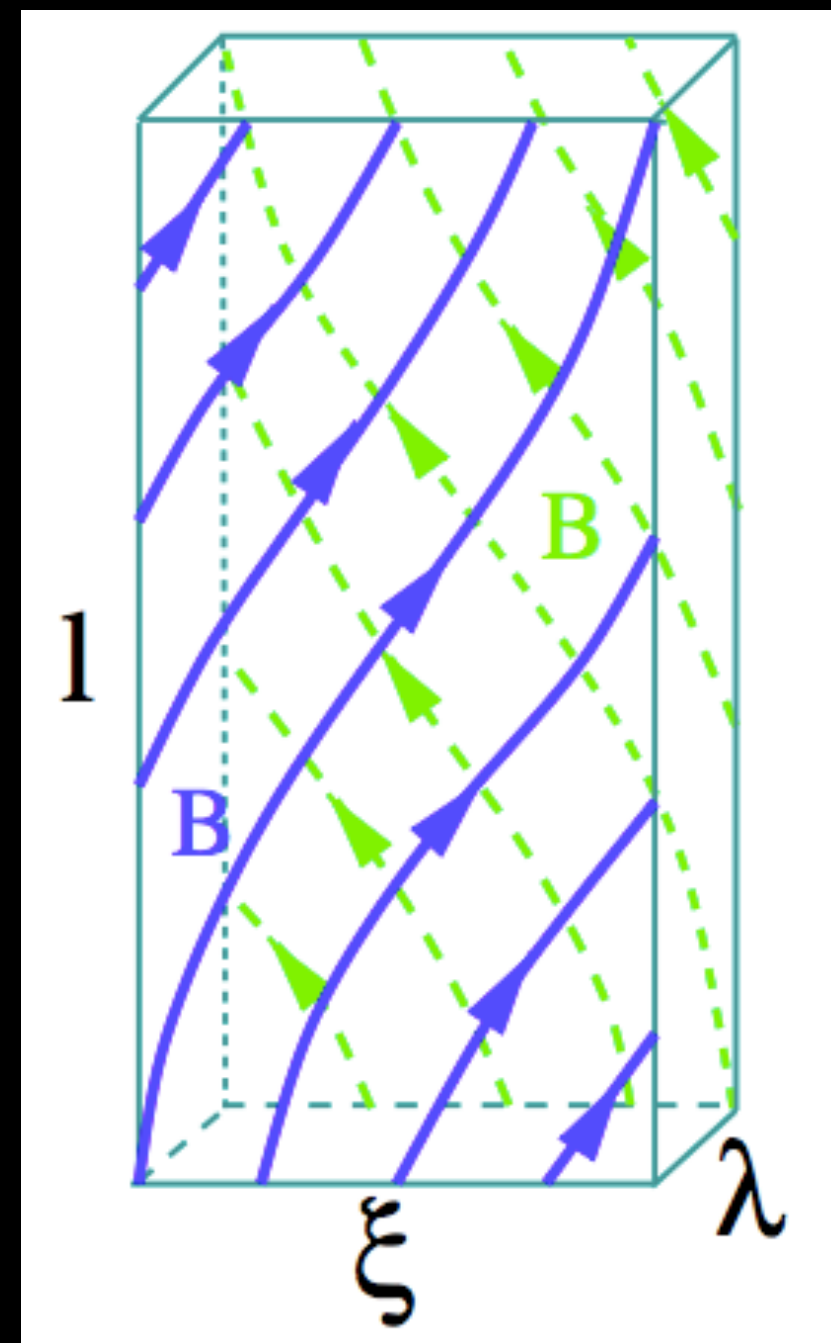
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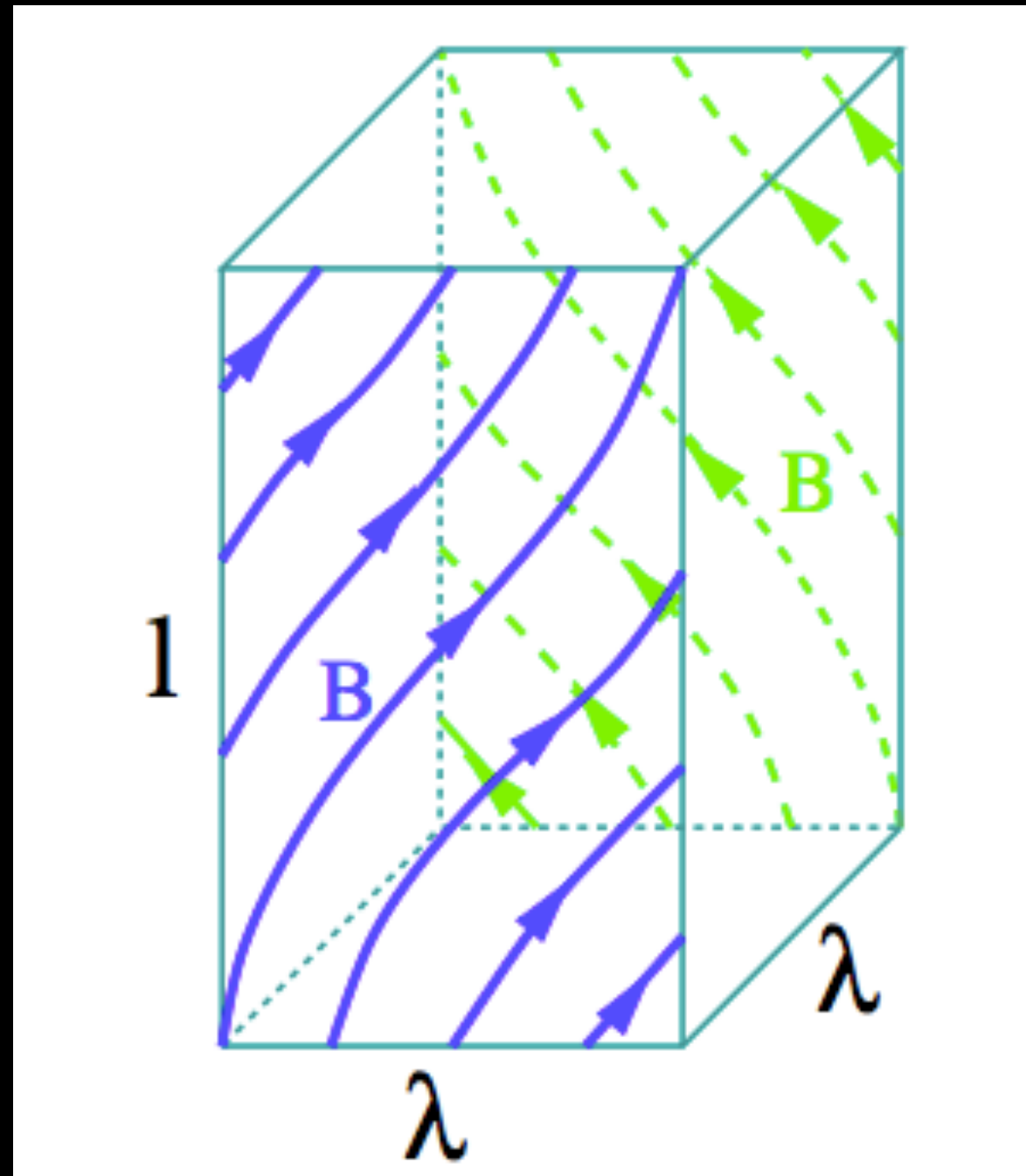


Boldyrev '06, Chandran+'15, Mallet & Schekochihin '17: eddies fully anisotropic; $\xi/\lambda \gg 1$; become high-aspect ratio current sheets at small scales. (key idea: critical balance + dynamic alignment).

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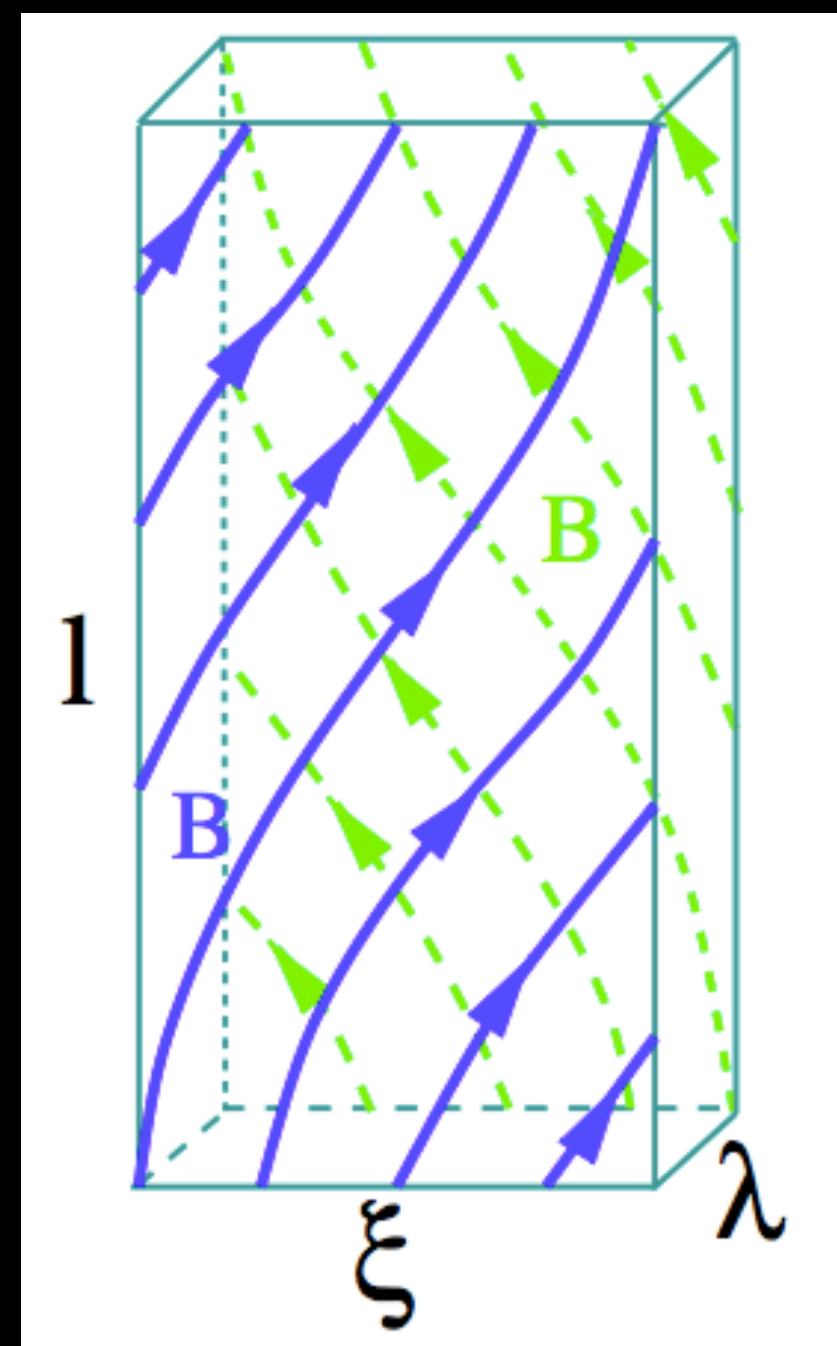
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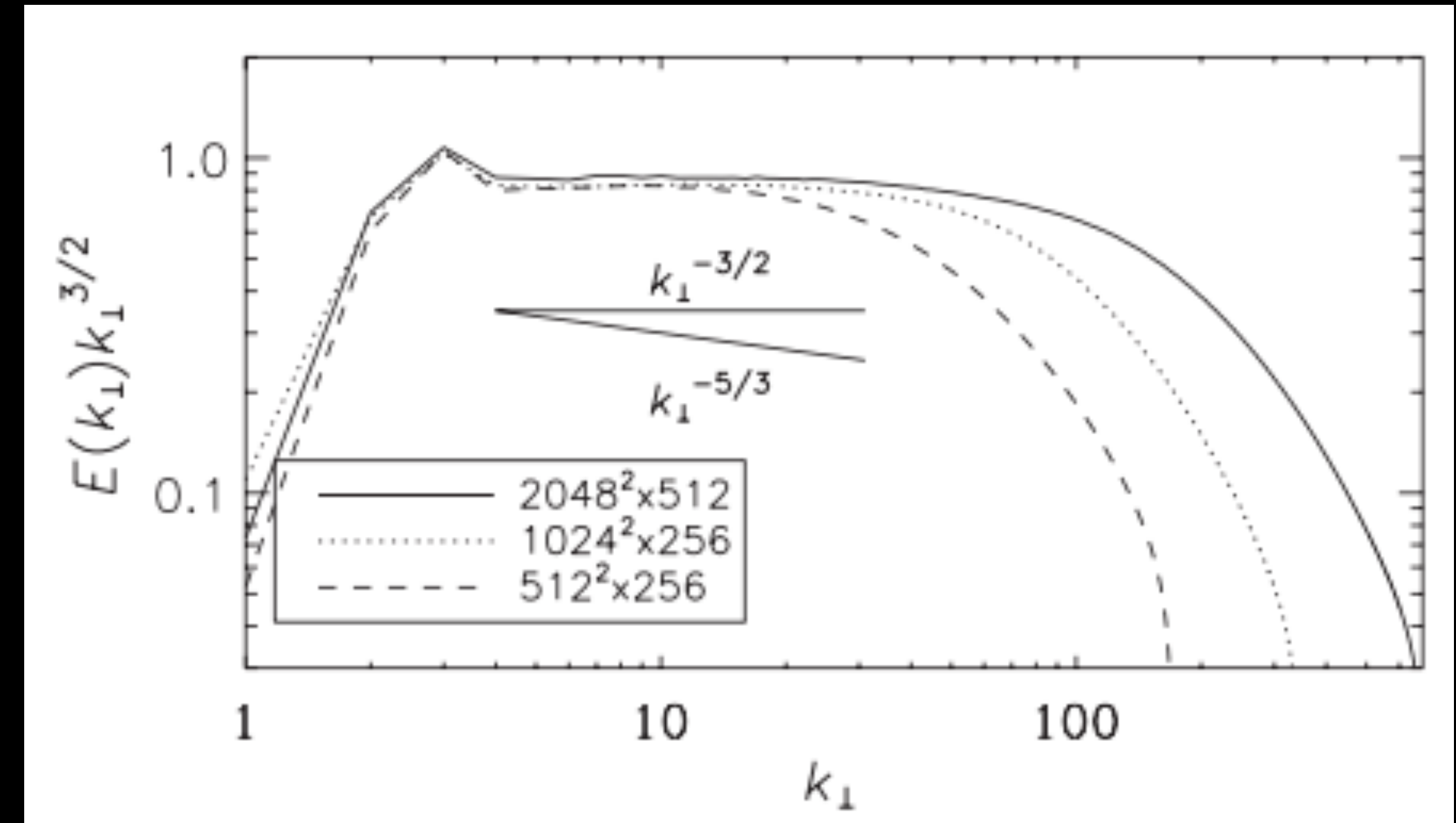
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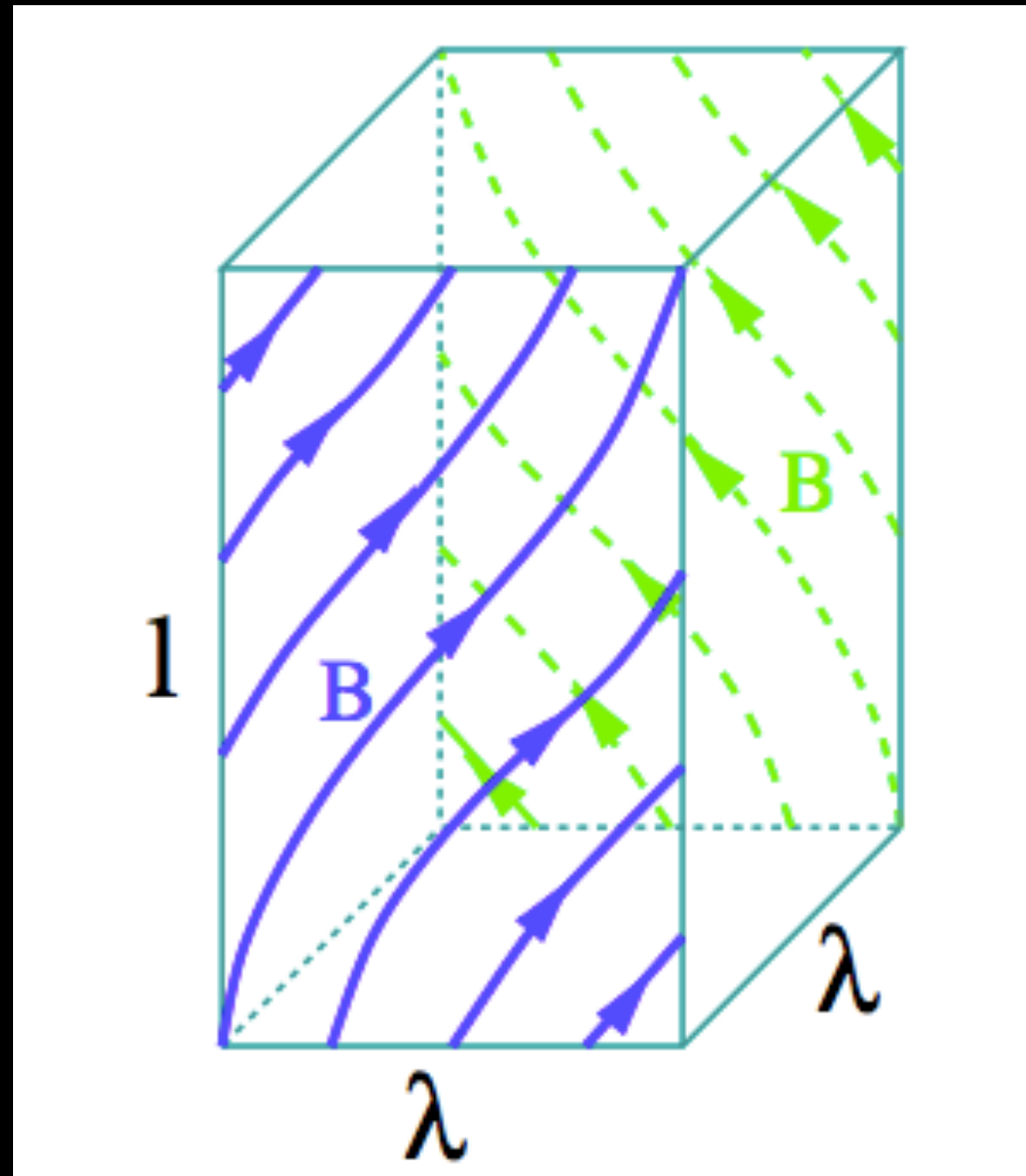
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Magnetic energy spectrum. Perez et al., PRX '12

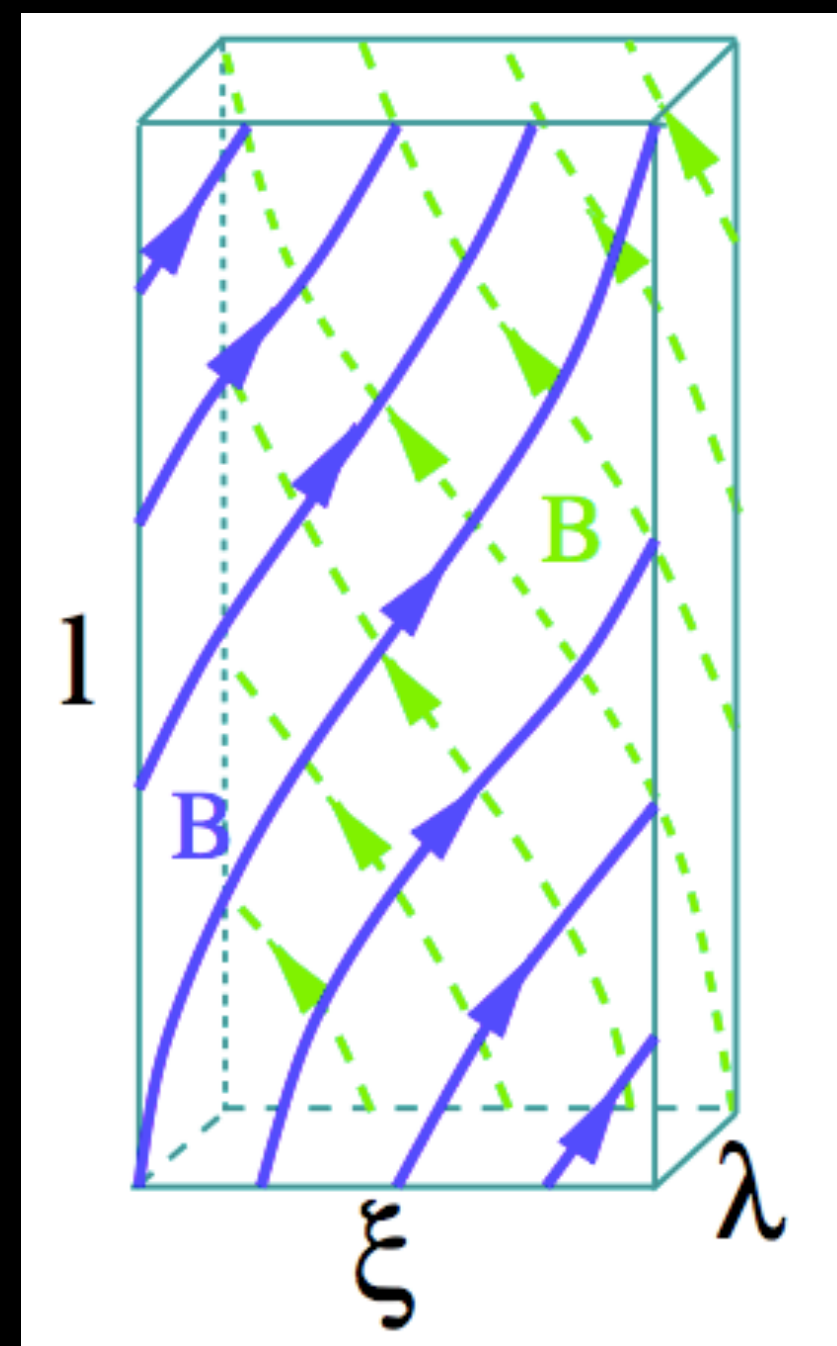
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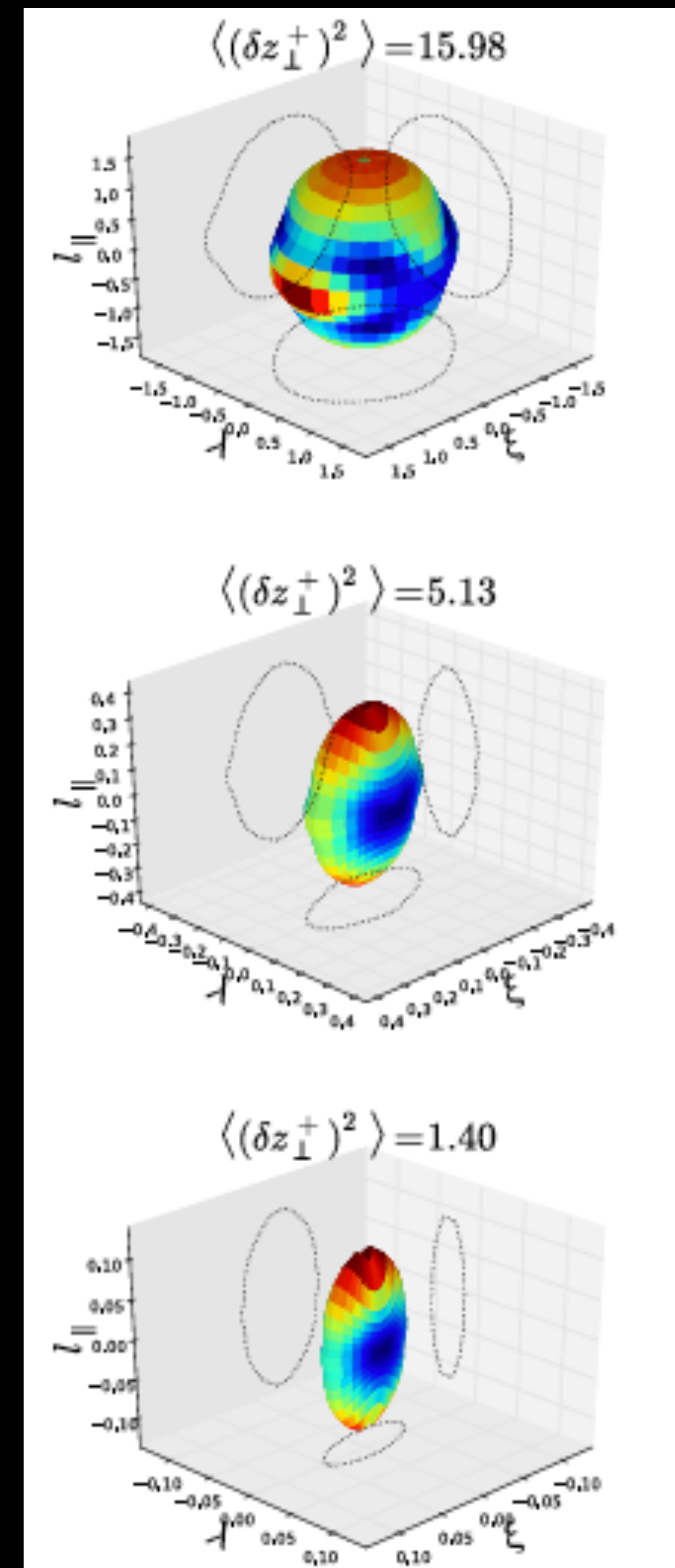
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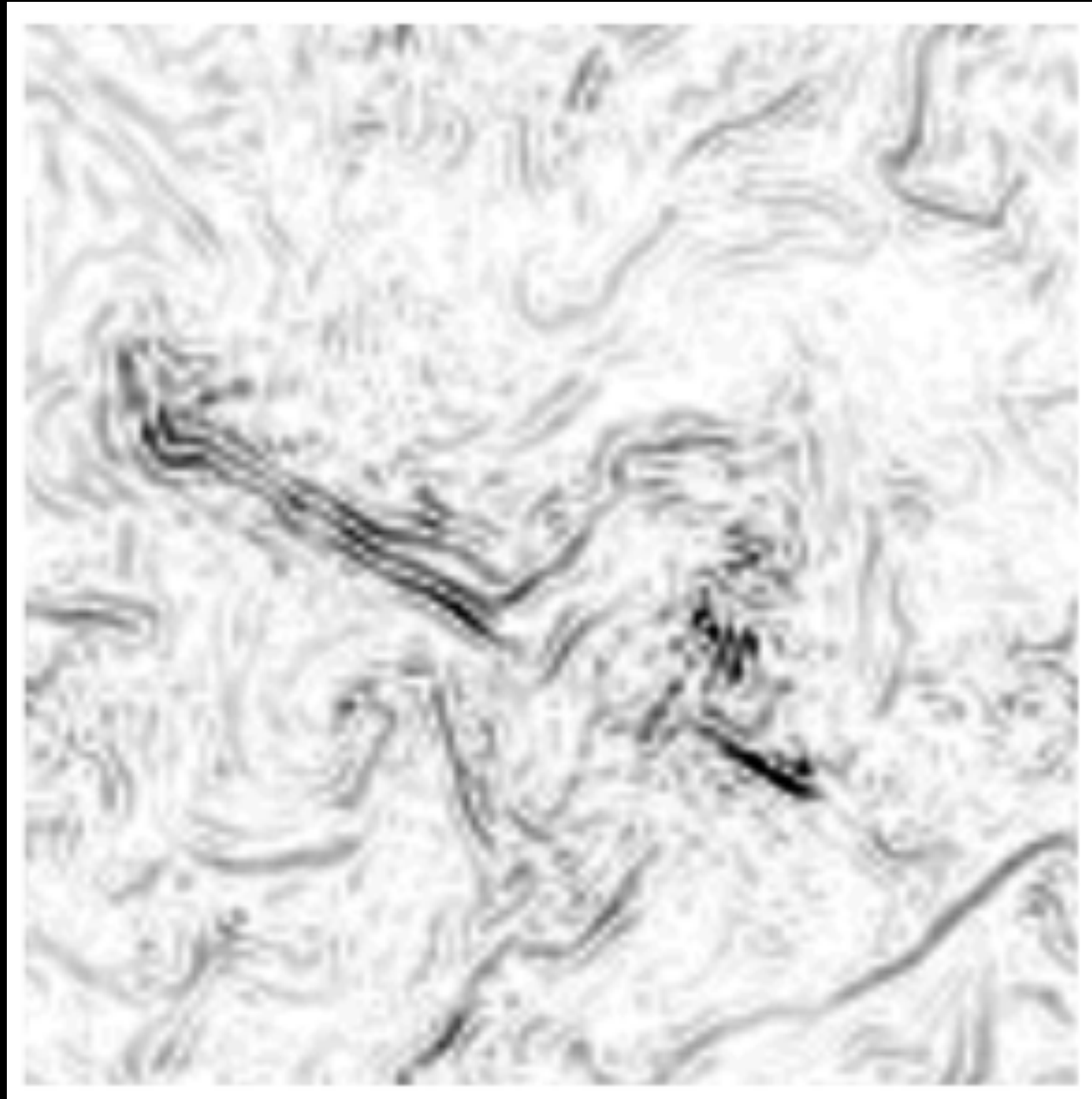
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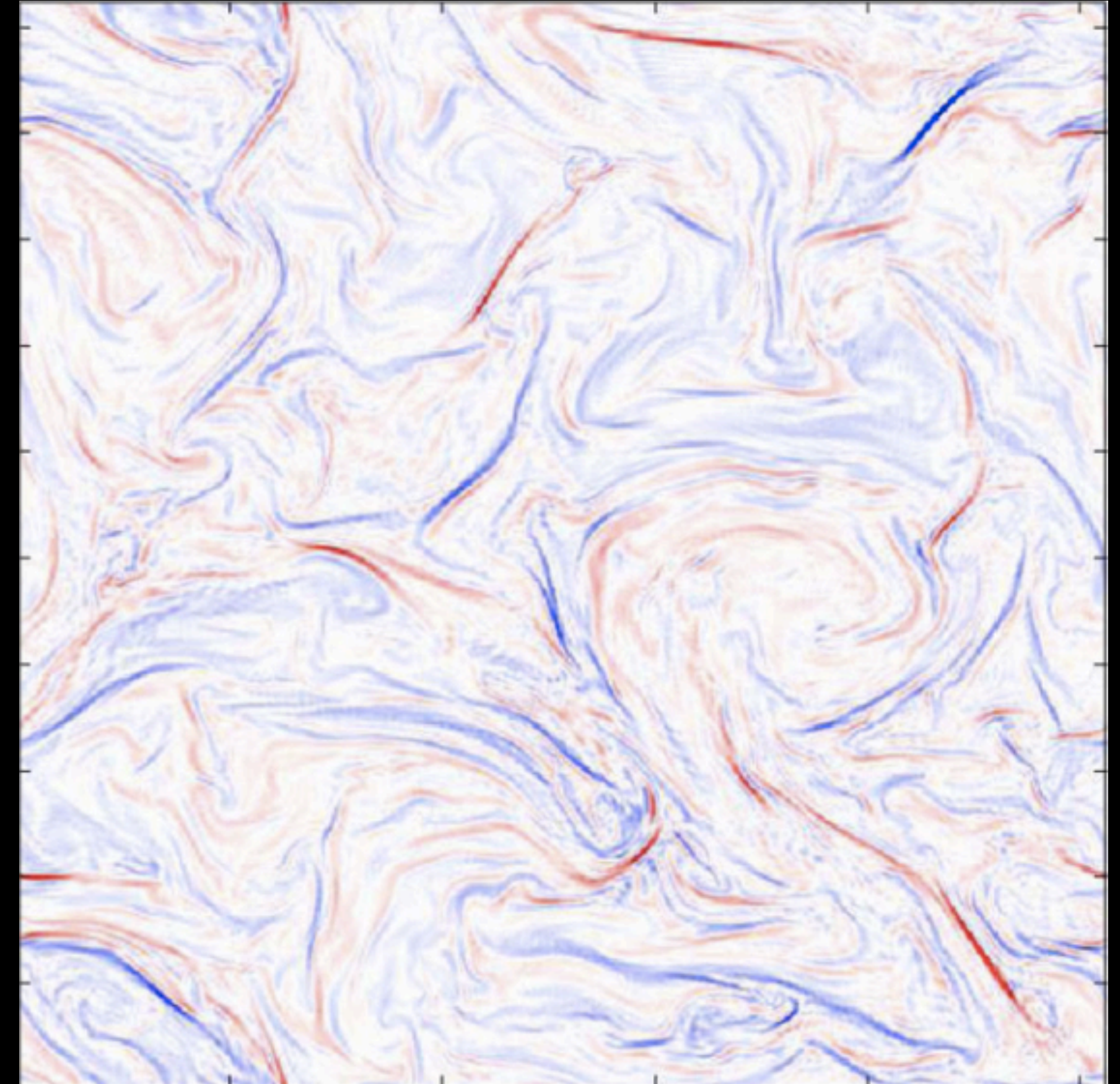
Mallet+ '16

Current sheet formation is predicted and observed

MHD turbulence simulations show abundant evidence for current sheet formation



Maron & Goldreich, ApJ '01

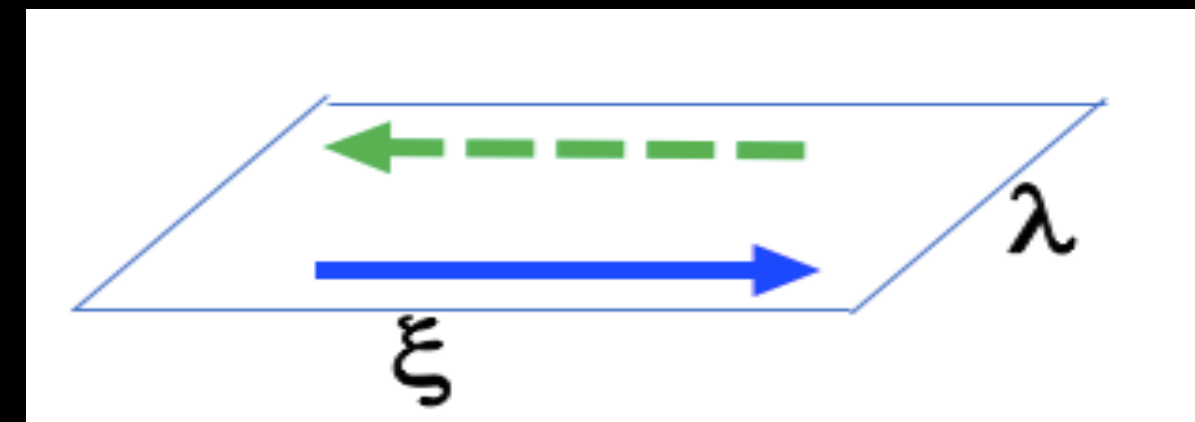
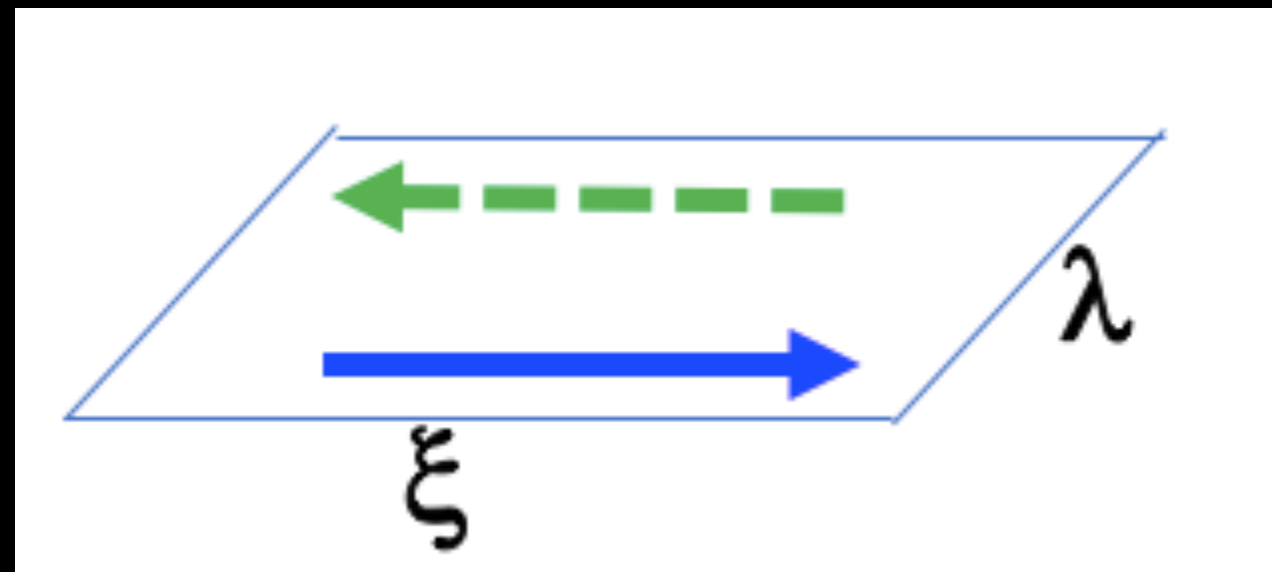


Zhdankin *et al.*, ApJ '13

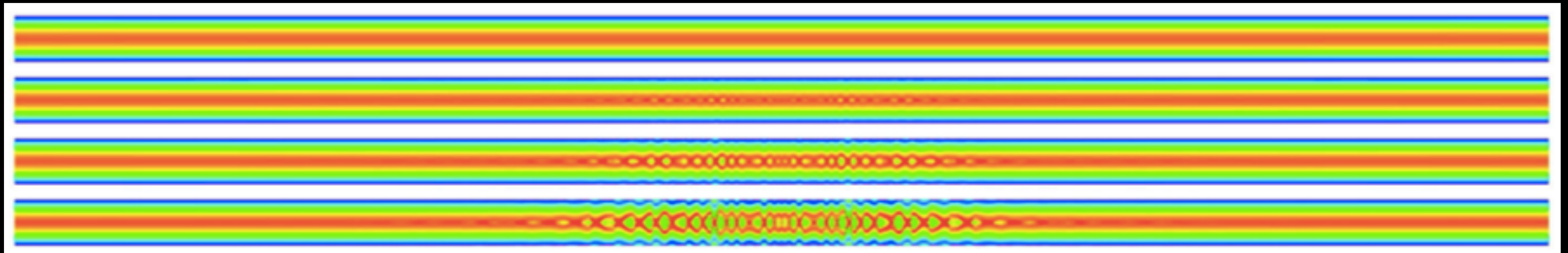
Strongly anisotropic current sheets are unstable

Current sheet anisotropy is limited by the tearing instability

- Eddy anisotropy in the field-perpendicular plane is predicted to increase as eddies get smaller



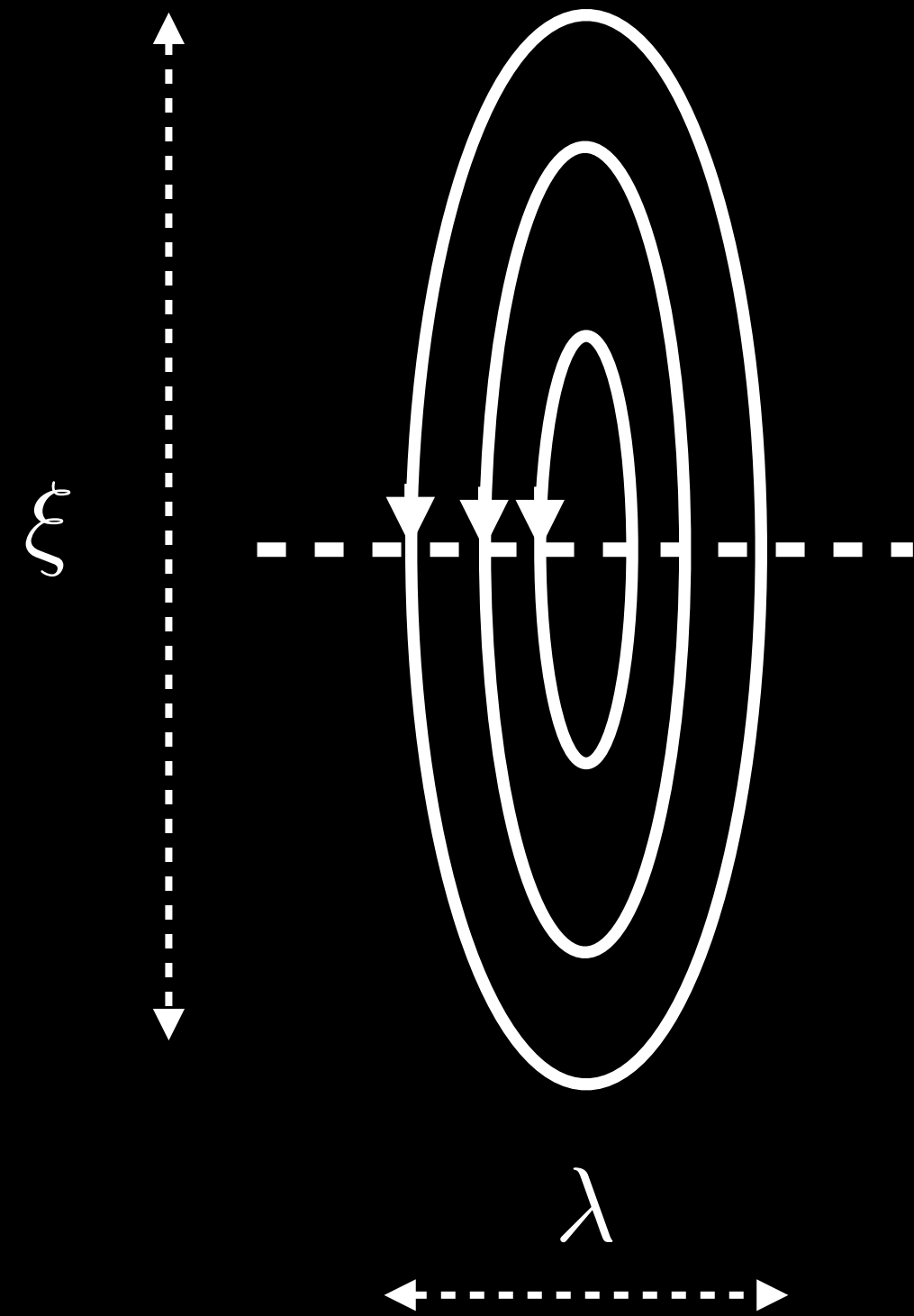
- At the dissipation scale, eddies' perpendicular aspect ratio would be the same as for a Sweet-Parker current sheet
- Cannot happen: Sweet-Parker sheets are super-Alfvénically unstable (Loureiro, Schekochihin & Cowley, 2007)



Samtaney et al., 2009

Dynamic tearing onset in the inertial range

Matching the turbulence and tearing instability timescales



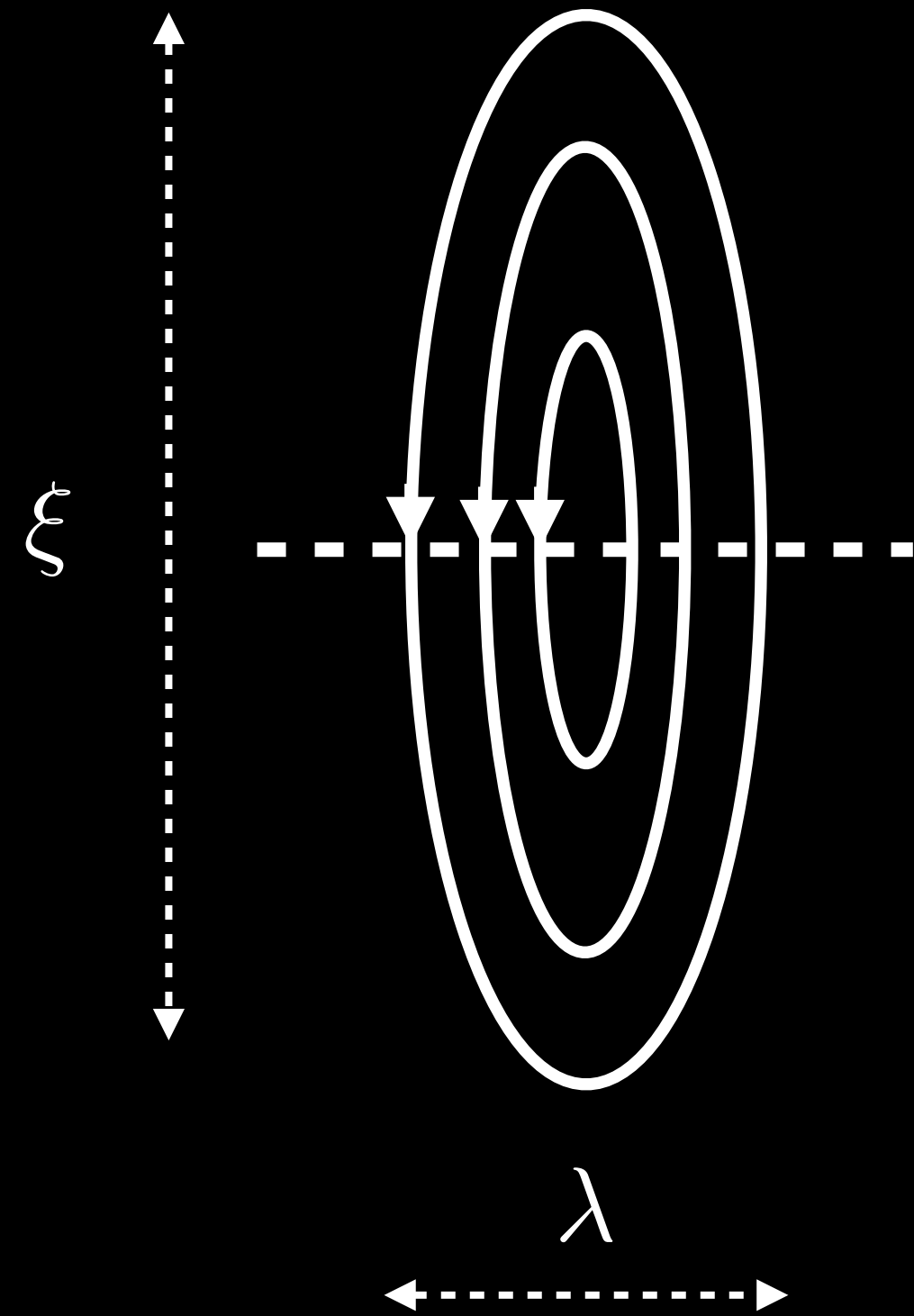
Loureiro & Boldyrev, PRL 2017

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Mallet *et al.*, MNRAS 2017

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- At what scale does the *eddy turnover time* become comparable to the *tearing mode growth time* in the eddy?

$$\gamma_t(\lambda)\tau_{nl}(\lambda) \sim 1$$

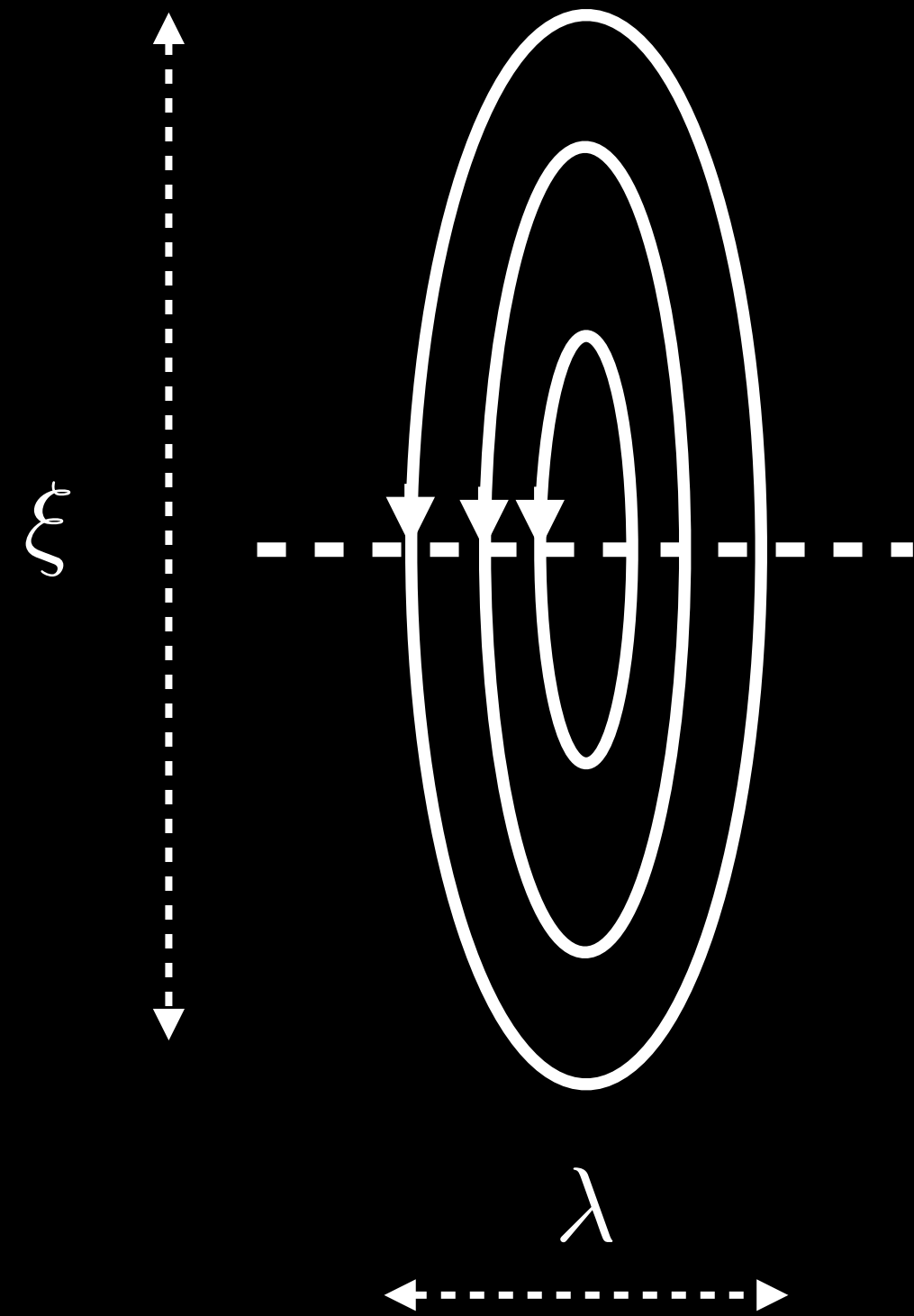
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- At what scale does the *eddy turnover time* become comparable to the *tearing mode growth time* in the eddy?

$$\gamma_t(\lambda)\tau_{nl}(\lambda) \sim 1$$

- This leads to the prediction of a *critical scale* below which tearing is faster than turbulence:

$$\lambda_{cr}/L \sim S_L^{-4/7}$$

Loureiro & Boldyrev, PRL 2017

Boldyrev & Loureiro, ApJ 2017

Mallet *et al.*, MNRAS 2017

Spectrum

Prediction of the existence of a new, sub-inertial range



- Spectrum can be computed from enforcing constant energy flux: $\gamma_{nl} V_{A,\lambda}^2 = \epsilon$

where $\epsilon \sim V_{A,0}^3 / L_0$ is the constant rate of energy cascade over scales.

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- We assume that when the tearing mode becomes nonlinear, it sets the timescale of the eddy:

$$\gamma_{nl} \sim \gamma_{\text{tear}}$$

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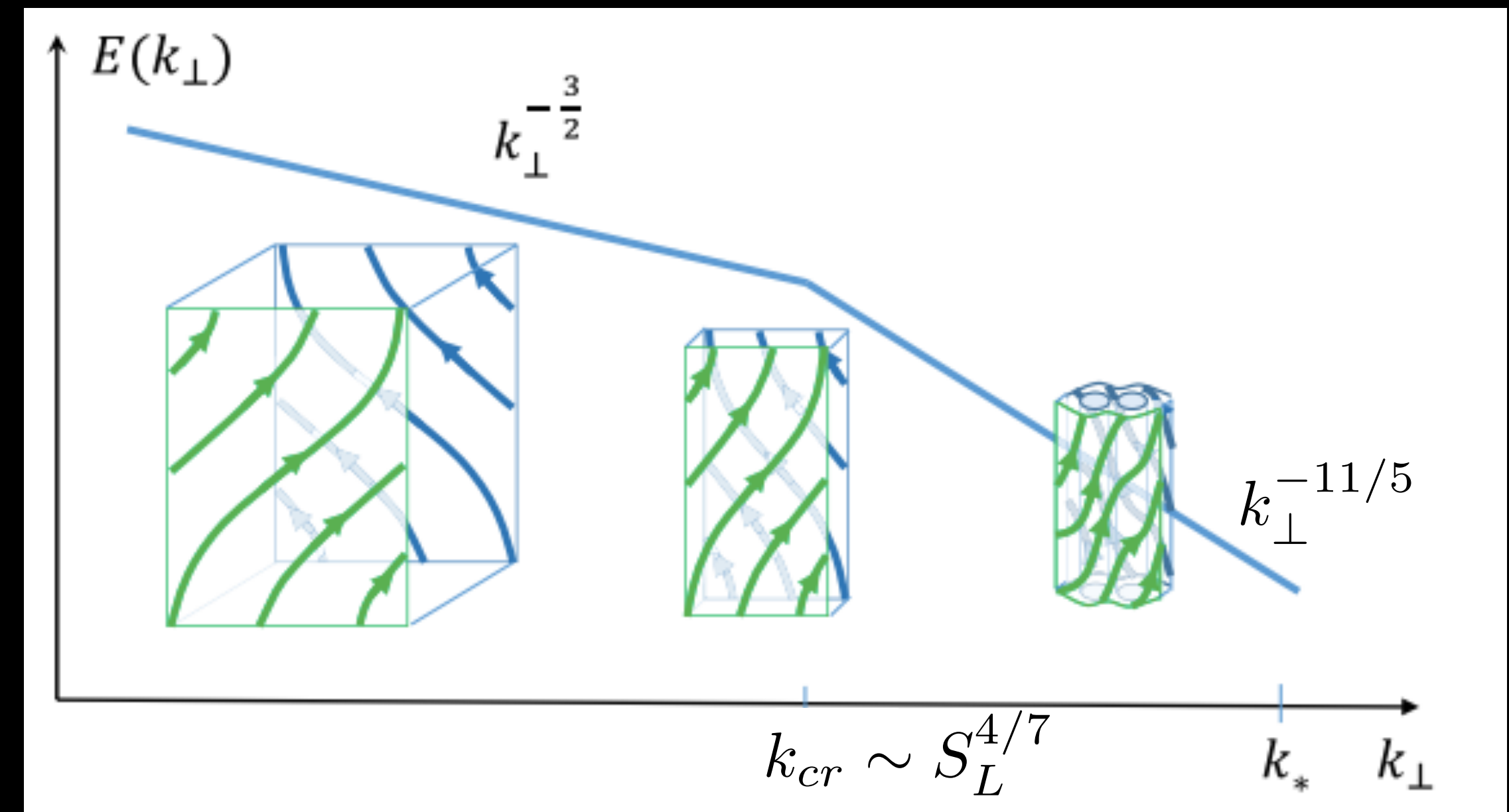
- Obtain:

$$E(k_{\perp}) dk_{\perp} \sim \epsilon^{4/5} \eta^{-2/5} k_{\perp}^{-11/5} dk_{\perp}$$

(or $E(k_{\perp}) \sim k_{\perp}^{-19/9}$)

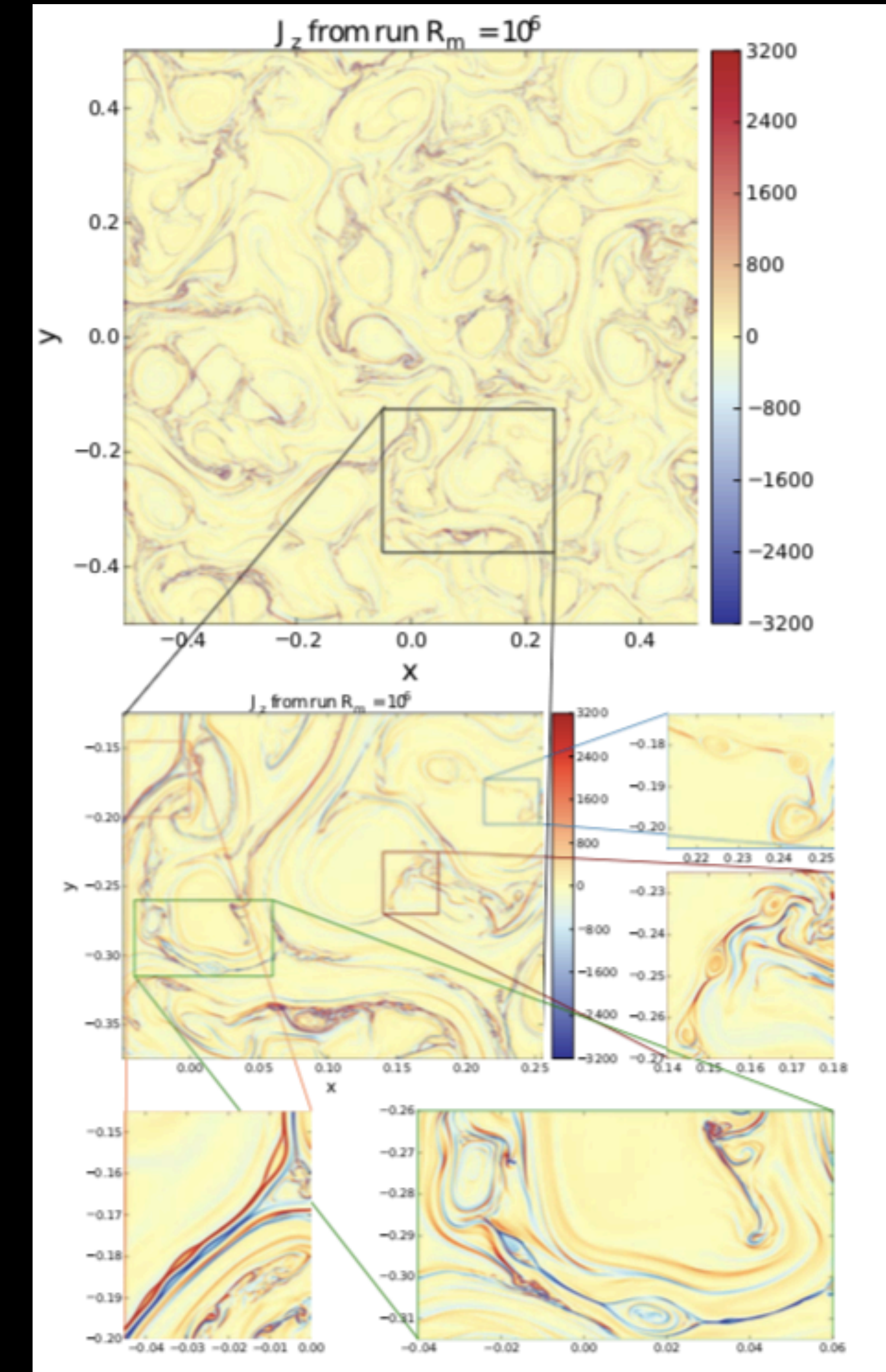
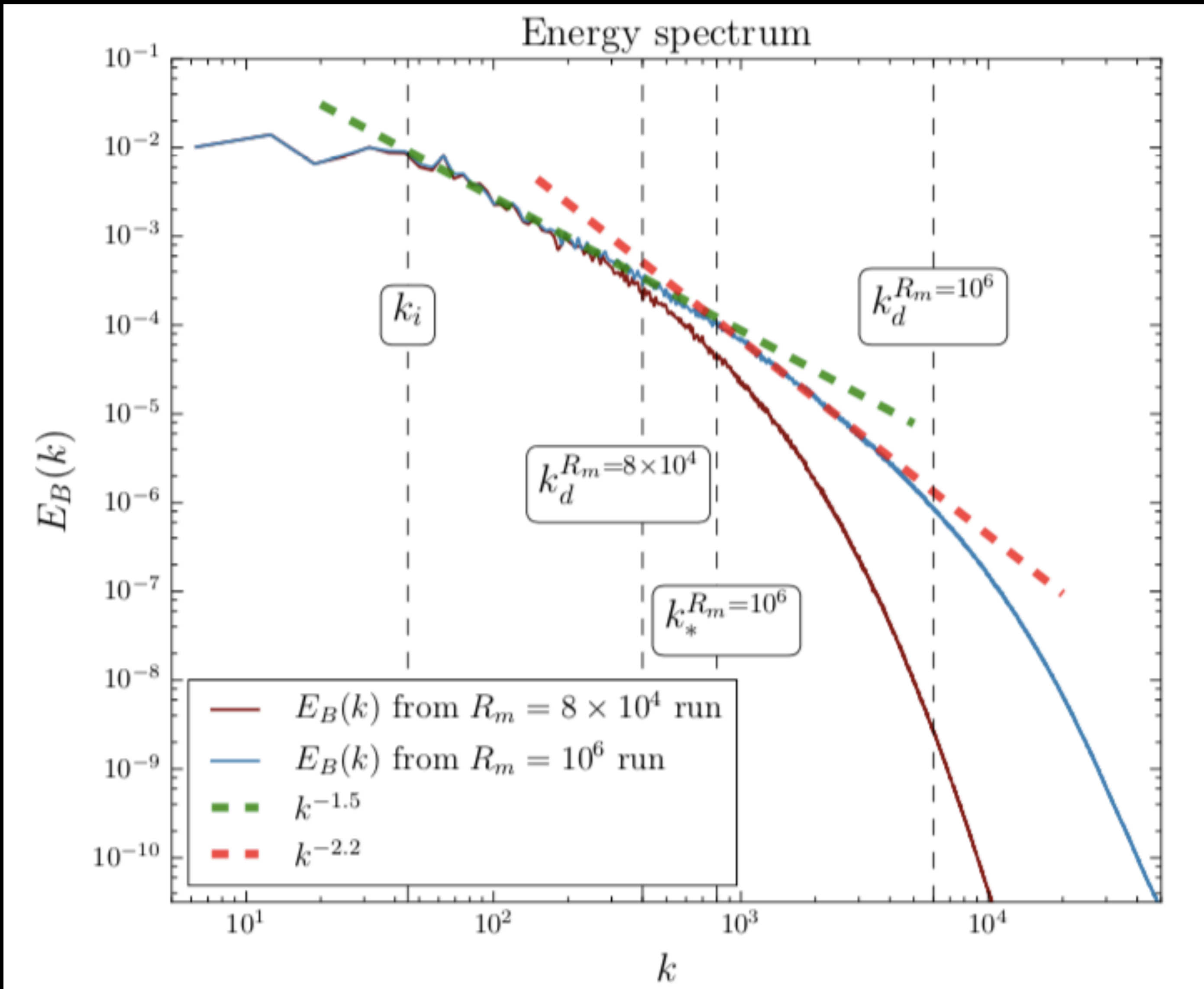
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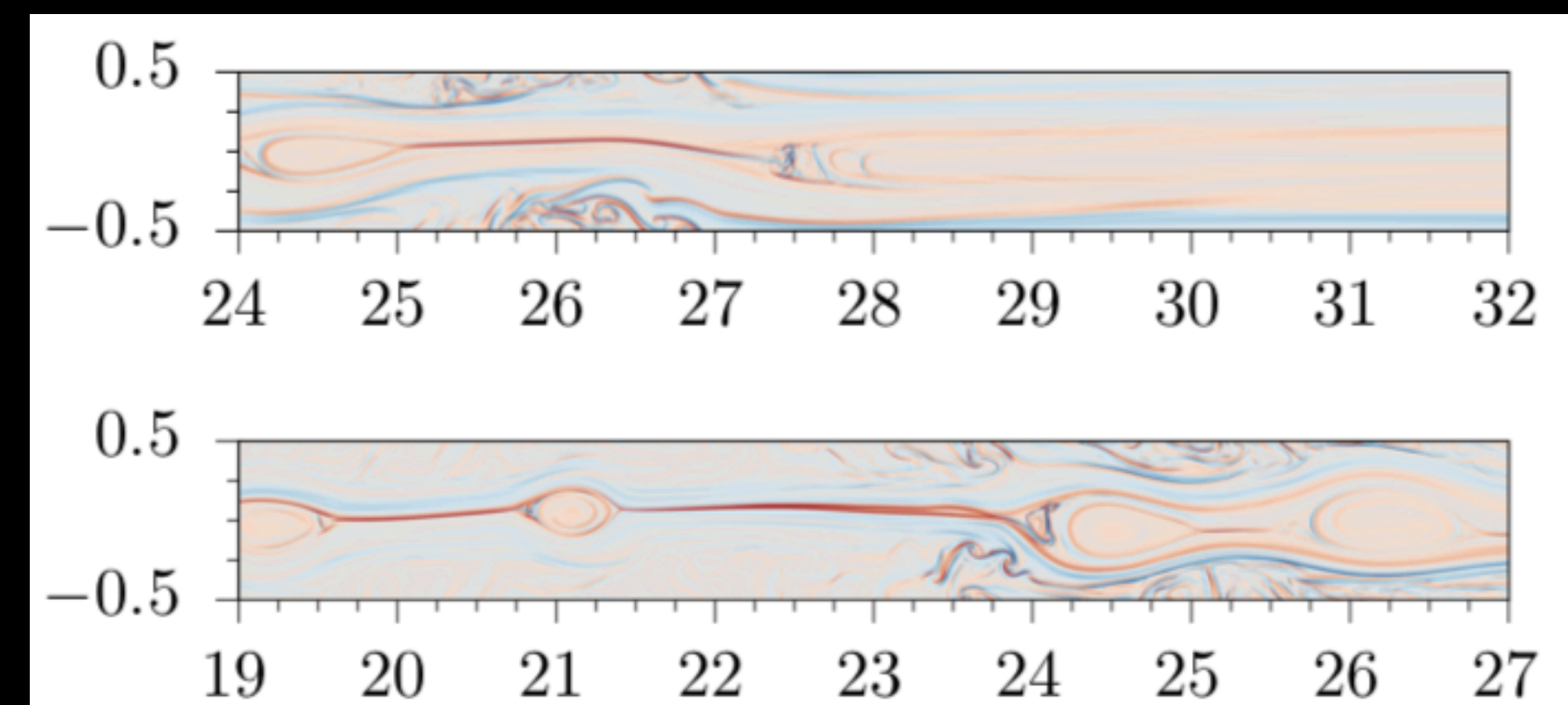
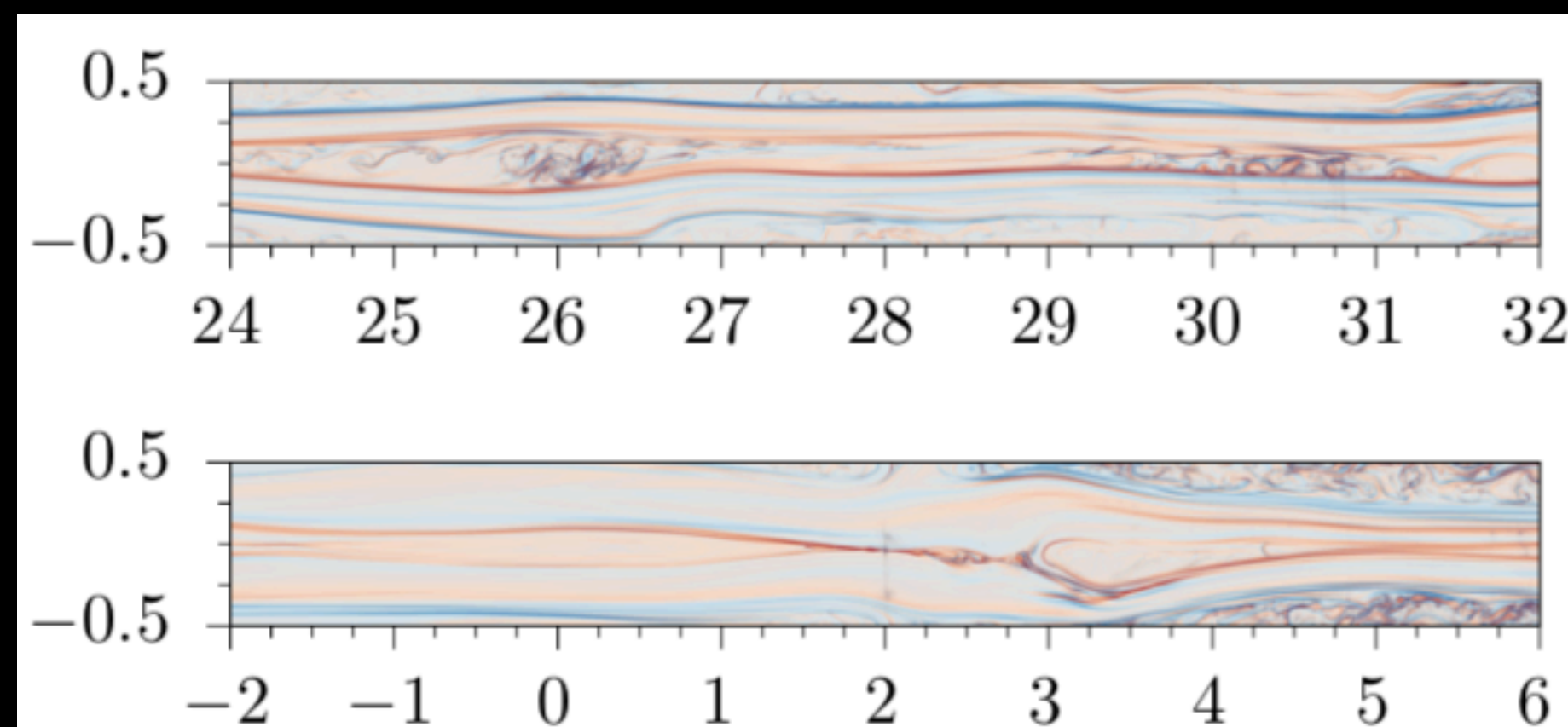
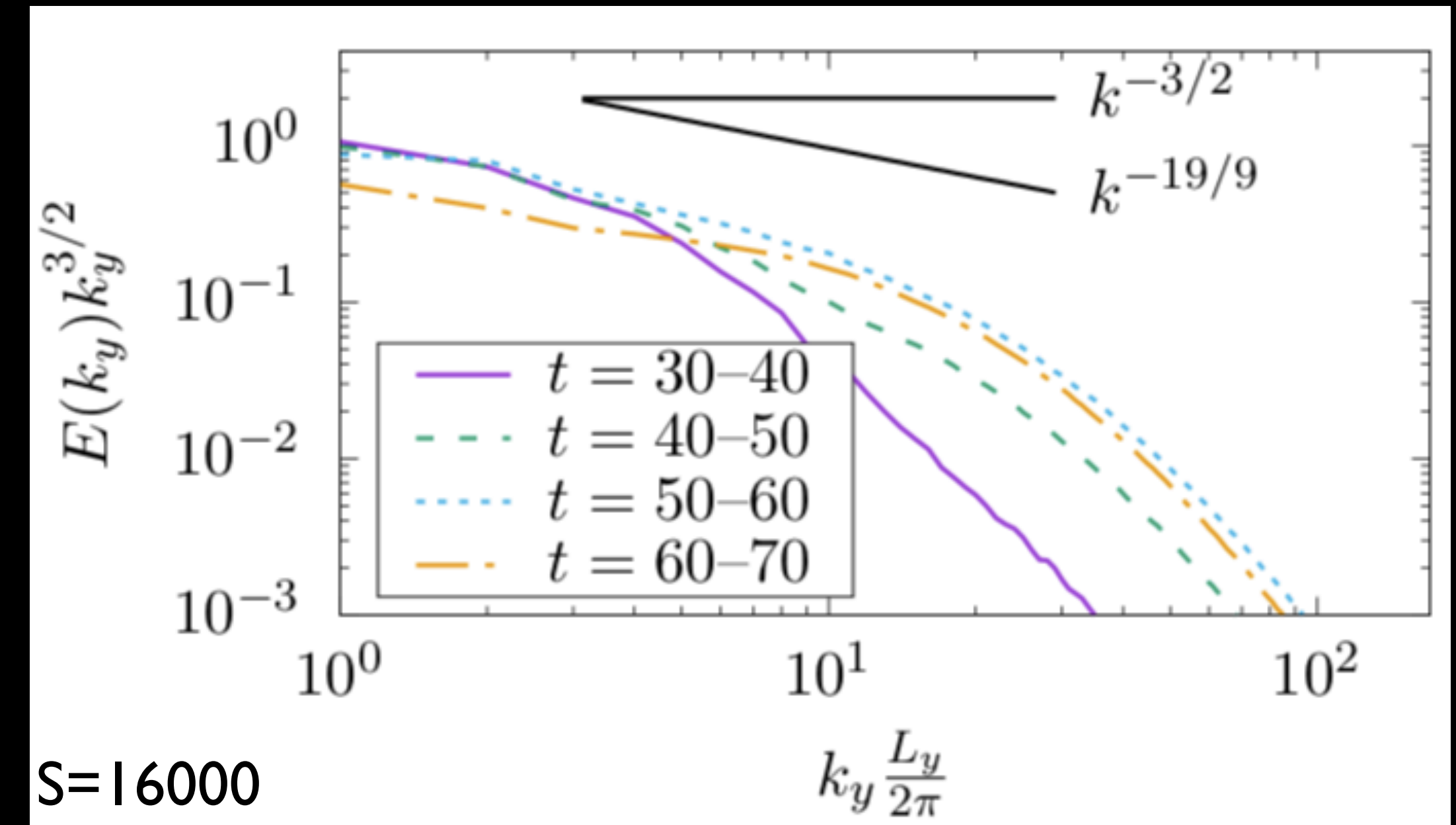
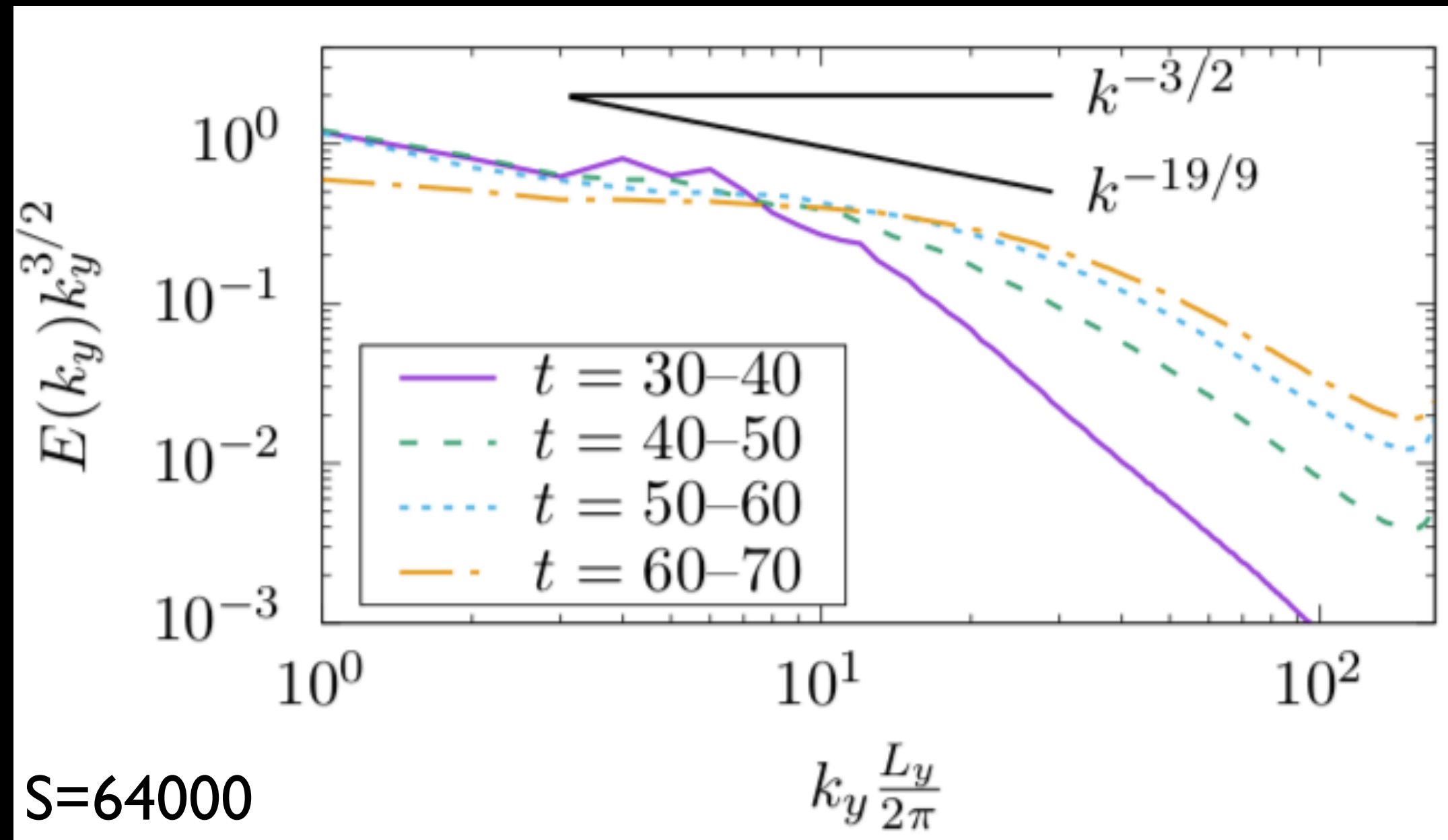
Numerical support for tearing in MHD turbulence

Simulations seem consistent with these predictions



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Extension to the kinetic regime

Collisionless tearing in MHD-scale eddies



- In many realistic plasmas, collisions are so infrequent that the tearing mode in a MHD-scale eddy will trigger kinetic effects:

$$\lambda \gg \rho_i \gg \delta \sim d_e$$

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- Different cases can be analyzed, depending on electron beta.

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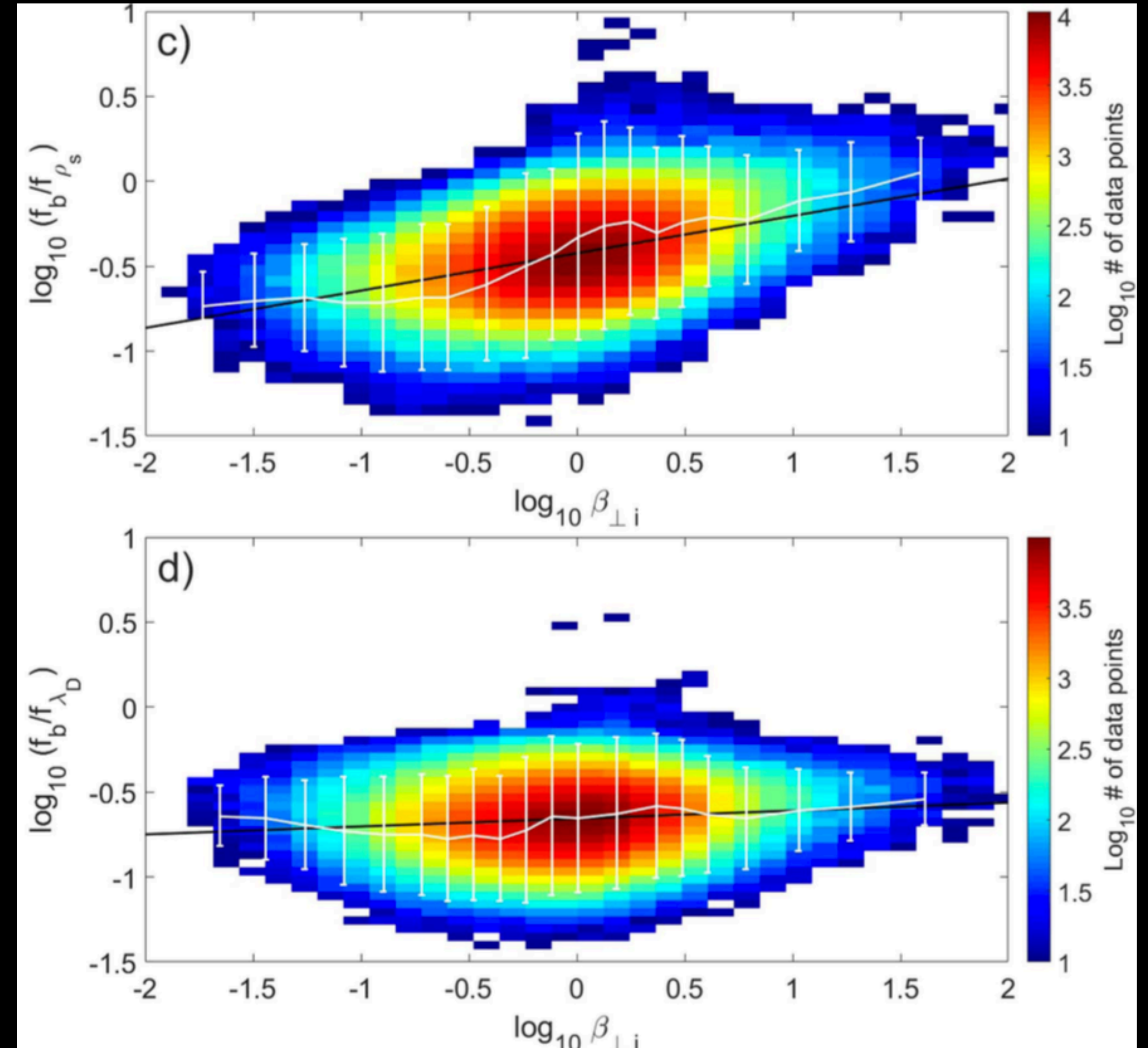
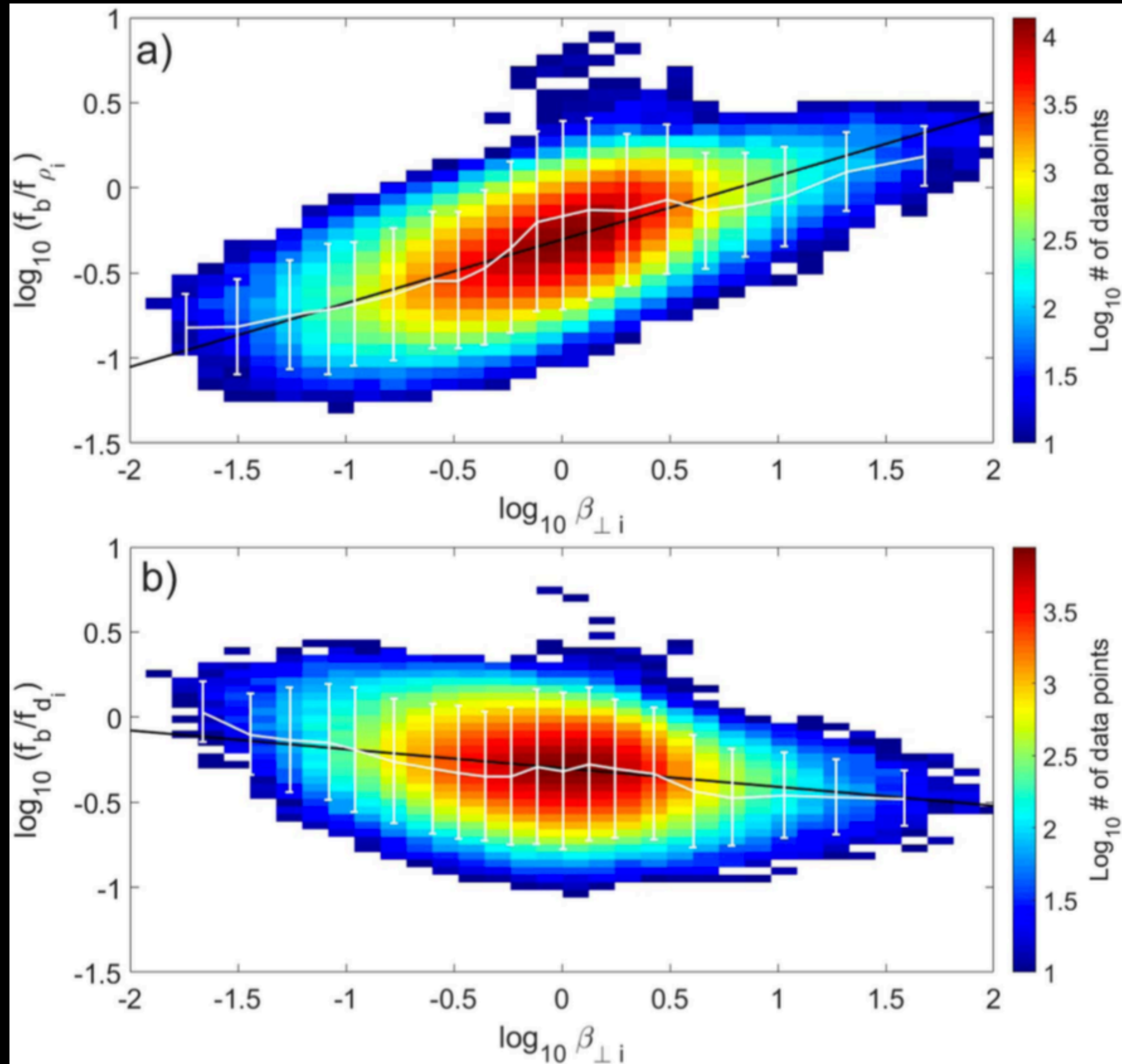
- This can be handled with kinetic tearing mode theory (reconnection is caused by electron inertia, instead of collisions).
- Different cases can be analyzed, depending on electron beta.
- Invariably, obtain spectra that scale as

$$E(k_{\perp}) \propto k_{\perp}^{-3} \quad \text{or} \quad E(k_{\perp}) \propto k_{\perp}^{-8/3}$$

depending on what shape is assumed for the tearing magnetic field (tanh or sine).

Evidence for tearing onset in SW turbulence

Analysis of SW data shows evidence of a tearing-induced spectral break for low electron beta



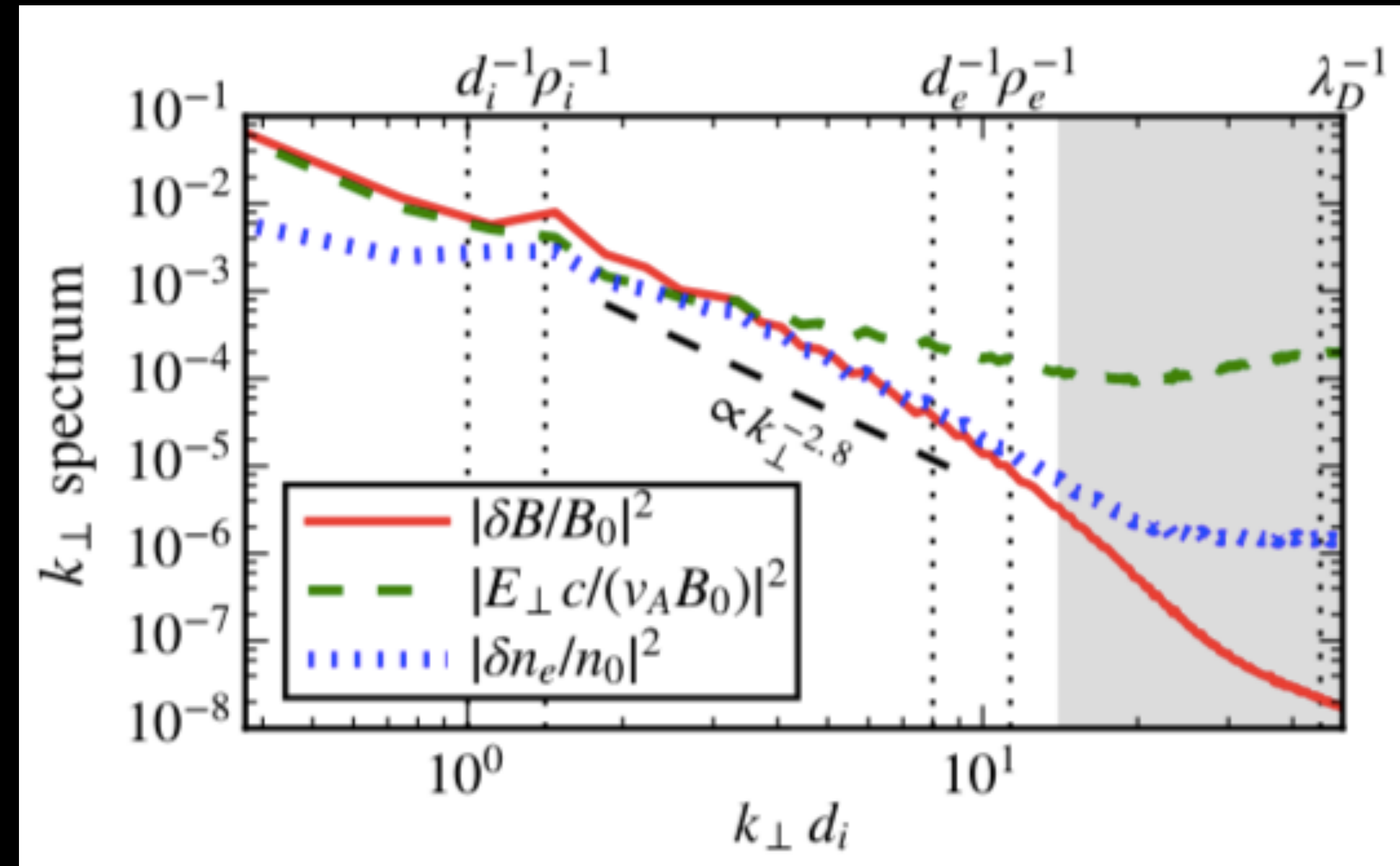
Tearing in the kinetic turbulence range

Collisionless tearing at sub-Larmor radius scales



- Can we extend these ideas to the kinetic turbulent range, i.e.,

$$\lambda \ll \max(\rho_i, \rho_s)$$



D. Groselj *et al.*, PRL '18

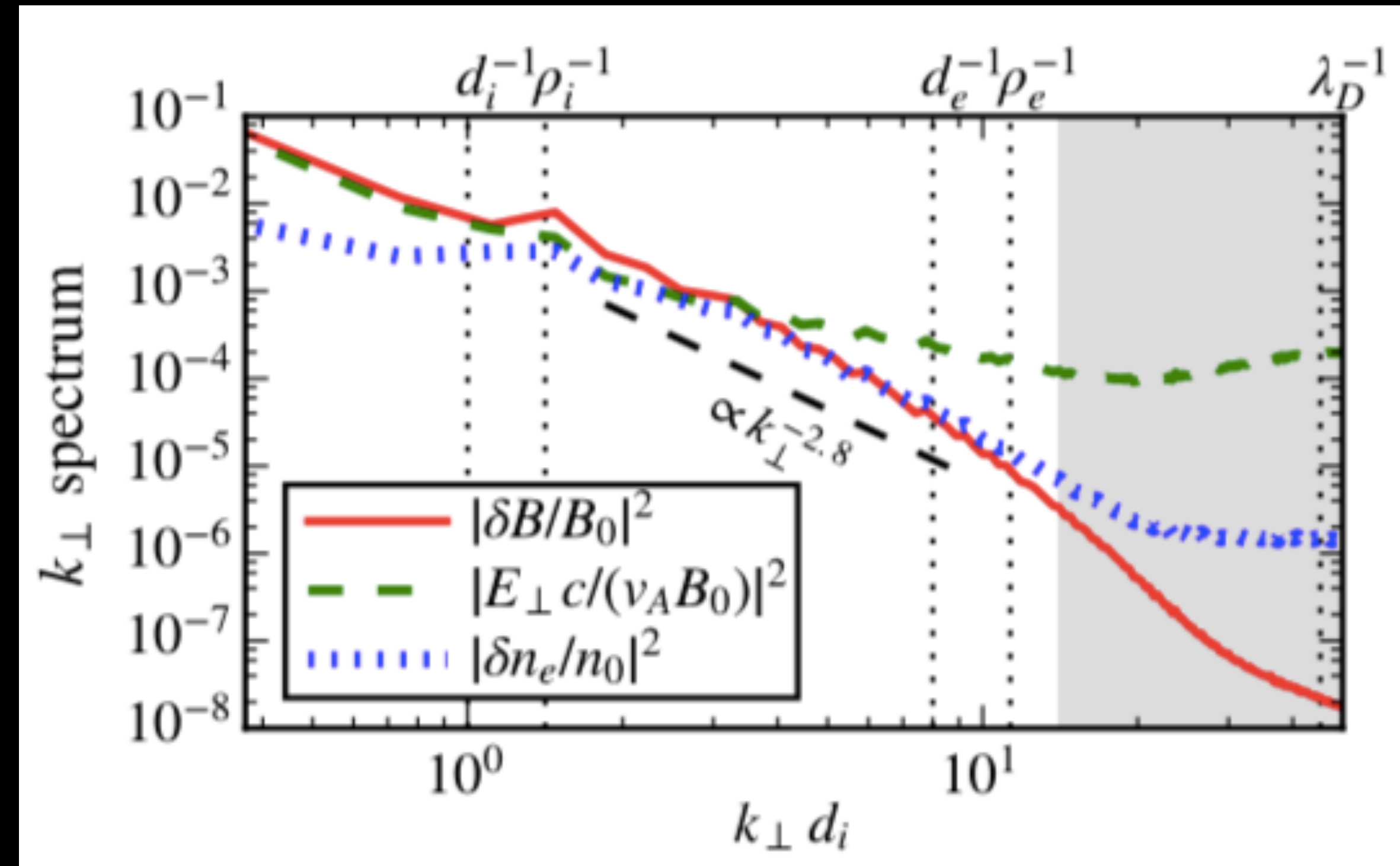
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- Uncertain: no theory to describe the eddy aspect ratio, etc.
- Numerical simulations do suggest ubiquitous current sheet presence at these scales.
- Cannot estimate the critical scale for the transition to the tearing range – this requires knowing what the eddies look like.



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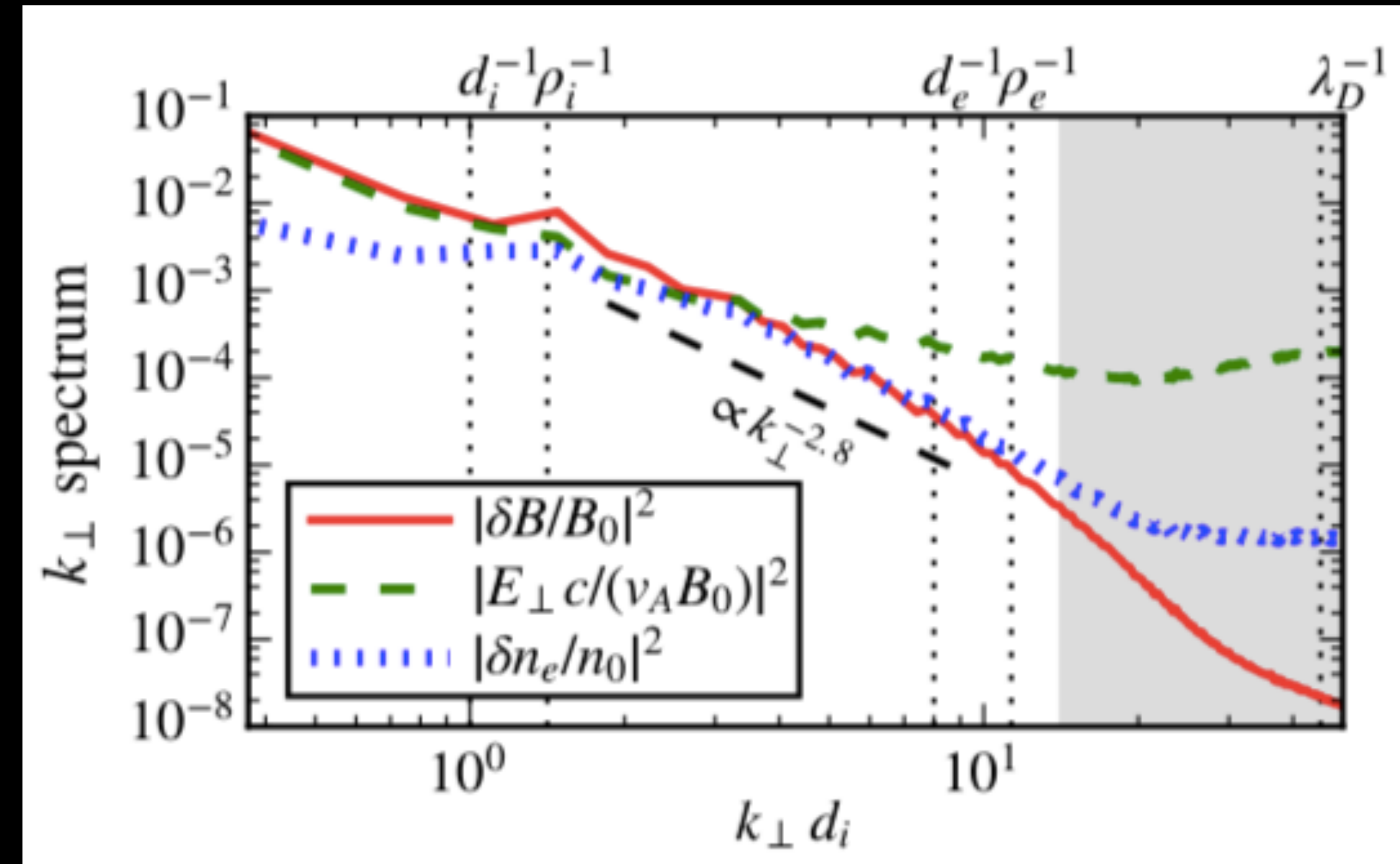
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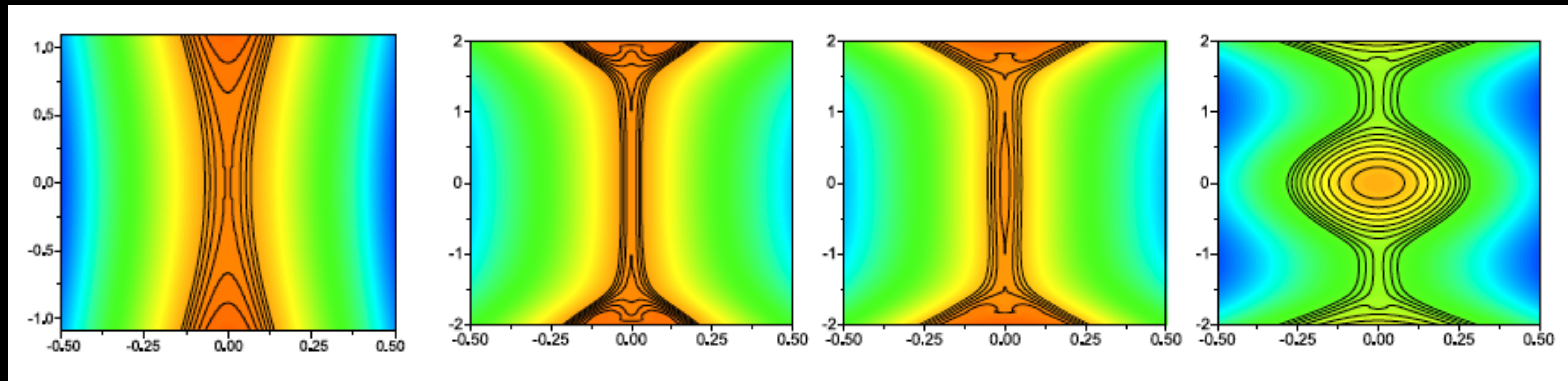
- But can estimate the spectrum given expression for the tearing mode growth rate at those scales. Again, we obtain:

$$E(k_{\perp}) \propto k_{\perp}^{-3} \quad \text{or} \quad E(k_{\perp}) \propto k_{\perp}^{-8/3}$$

Nonlinear Tearing-Mode Evolution

Recap of how MHD tearing proceeds in the absence of turbulence

- When the (most unstable) tearing mode becomes nonlinear, it continues to grow exponentially at the linear growth rate (the Waelbroeck collapse)
- *In the absence of background turbulence*, the collapse leads to the formation of a current sheet: of the Sweet-Parker (SP) kind, if $S < S_{cr} \sim 10^4$, or of the plasmoid-unstable kind, otherwise.
- If SP, the rate remains the same. If plasmoid-dominated, rate becomes $\sim S_{cr}^{-1/2} \sim 0.01$ (Uzdensky *et al.*, '10)

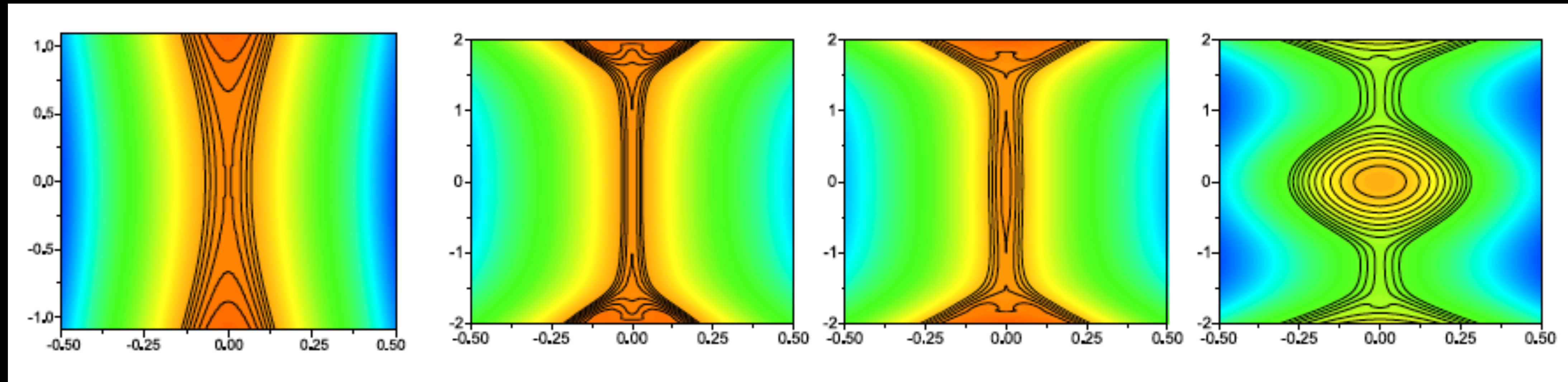


Loureiro *et al.* '05

- Collisionless tearing is similar, except rate becomes 0.1 (e.g., Comisso & Bhattacharjee '16, Cassak '17).

Nonlinear Tearing-Mode Evolution

Recap of how MHD tearing proceeds in the absence of turbulence



- What we usually call *reconnection* is the *advanced or the post-collapse stage*: more precisely, it is when the rate changes to 0.01 in the MHD plasmoid case, or 0.1 in the collisionless case.
- Crucially, **it is only in this (late nonlinear) stage of the tearing mode that significant amounts of flux are reconnected, and significant (~50%) amounts of energy are dissipated/converted.**

Tearing vs. Reconnection: enter turbulence

Tearing onset does not guarantee eddy will fully reconnect



Tearing vs. Reconnection: enter turbulence



Tearing onset does not guarantee eddy will fully reconnect

- The X-point collapse is a **global** (i.e., at the scale of the eddy) nonlinear rearrangement (i.e., it's a loss of equilibrium); the eddy is forced (by the nonlinearities causing the collapse) to adjust its evolution rate to the tearing rate.

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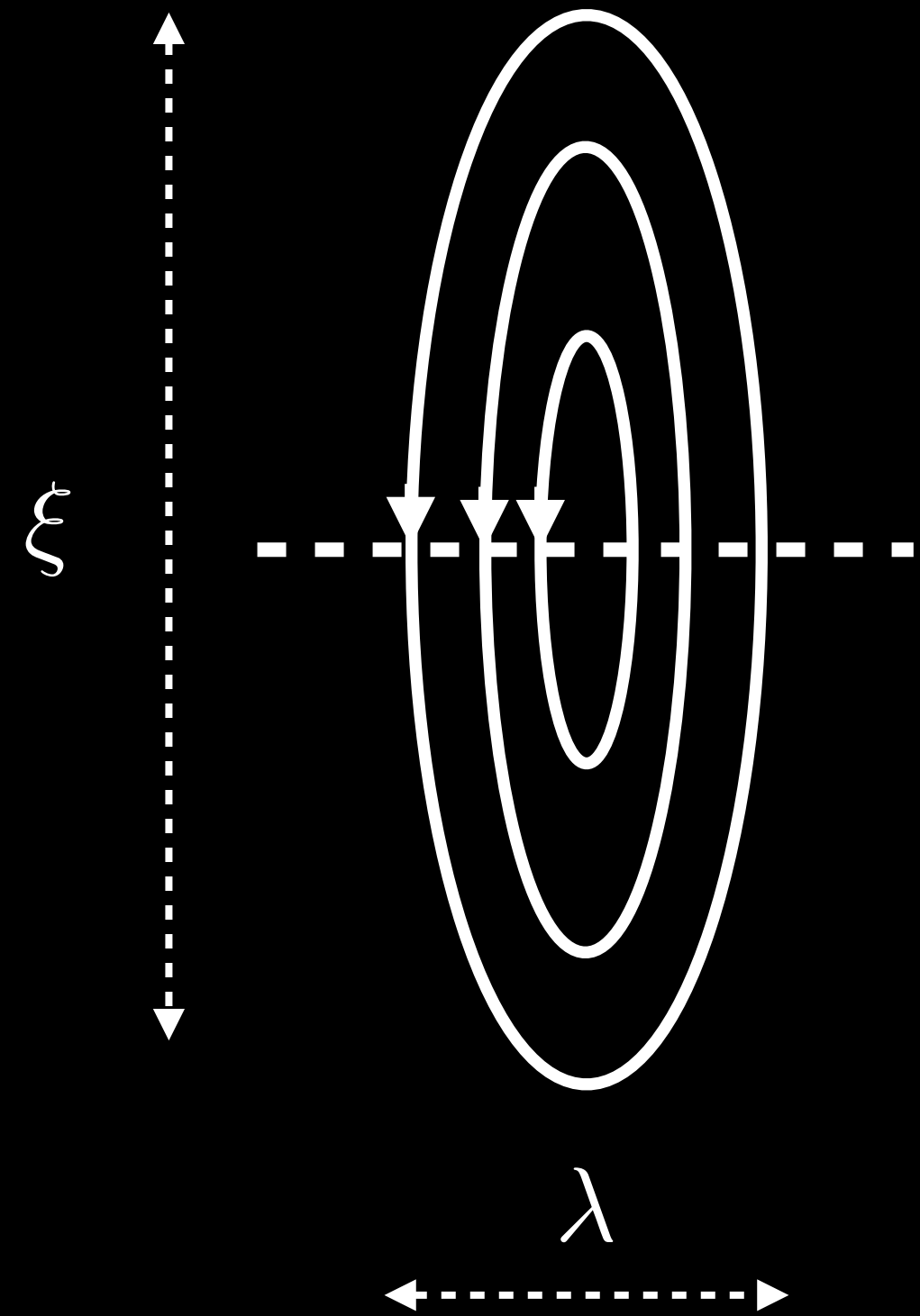


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- All we can say is that there is a finite (order 1) probability that the collapse will last long enough to transition to the reconnection stage proper (and an order 1 probability that it won't)
- **If it does transition to the reconnection stage, will there be time to reconnect significant amounts of flux (and dissipate significant amounts of energy) in the lifetime of the eddy?**

Reconnecting the flux in an eddy

How long does it take to reconnect the flux in an eddy?



$$\psi_\lambda = B_\xi(\lambda)\lambda \quad (\text{reconnectable}) \text{ flux contained in eddy.}$$

$$\tau_{rec} = \mathcal{R}^{-1} \tau_{A,\lambda} \quad \text{where} \quad \tau_{A,\lambda} = \lambda/v_{A,\lambda}$$

\mathcal{R} is the (dimensionless) reconnection rate.

$$\text{In MHD,} \quad \mathcal{R} \sim S_\xi^{-1/2} \quad \text{if} \quad S_\xi \lesssim S_{cr} \approx 10^4$$

$$\mathcal{R} \sim S_{cr}^{-1/2} \approx 0.01 \quad \text{if} \quad S_\xi > S_{cr} \quad (\text{the plasmoid regime})$$

$$\text{In collisionless plasmas,} \quad \mathcal{R} \sim 0.1$$

Can full eddy reconnection happen?

Criterion for reconnection to have time to occur

- A typical eddy at scales $\lambda \ll \lambda_{cr}$ exists for a time of order γ_t^{-1}
- It has a finite probability of reaching the deep nonlinear stage, whereupon it may transition to the reconnection regime.

• If

$$\gamma_t \tau_{rec} \ll 1$$

then the *reconnection time is much shorter than the eddy turnover time*, and it is thus expected that full reconnection will occur. Observable consequence should be a steepening of the spectrum.

- *Otherwise, reconnection is slower*, and the eddy will cease to exist without significant reconnection having taken place.

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- Now need to work out this condition in the MHD and in the collisionless regimes.

Reconnection in MHD turbulence

Criterion for reconnection to have time to occur



Criterion for reconnection to have time to occur

- Tearing becomes relevant below the scale $\lambda_{cr}/L \sim S_L^{-4/7}$
- The eddy turn over rate becomes the tearing mode rate $\gamma_t \sim \tau_{A,\lambda}^{-1} (\lambda v_{A,\lambda}/\eta)^{-1/2}$
where $v_{A,\lambda} \sim \varepsilon^{2/5} \eta^{-1/5} \lambda^{3/5}$ with $\varepsilon = V_{A,0}^3/L$

Reconnection in MHD turbulence



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- So: $\gamma_t \tau_{rec} \ll 1 \implies \lambda/L \gg \mathcal{R}^{-5/4} S_L^{-3/4}$

- This is valid only if $\lambda_{cr} \gg \lambda \gg \lambda_{diss}$ where $\lambda_{diss} \sim S_L^{-3/4} L$

- The first inequality yields $S_L \gg \mathcal{R}^{-7} \sim S_{cr}^{7/2} \sim 10^{14}$

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Impossible to simulate.

Implication is that MHD simulations may be severely underestimating reconnection-driven dissipation.

- Collisionless plasma: electron inertia (not resistivity) breaks the frozen flux. Now $\mathcal{R} \sim 0.1$
- Consider first the case when the tearing onset happens above the ion kinetic scales: $\lambda_{cr} > \rho_i, \rho_s, d_i$
- Low beta case as an example.
- Tearing mode onset scale is $\lambda_{cr}/L \sim (d_e/L)^{4/9}(\rho_s/L)^{4/9}$. Below that scale we have $\gamma_t \sim v_{A,\lambda} d_e \rho_s / \lambda^3$

In this case, we find: $\gamma_t \tau_{rec} \ll 1 \implies \lambda \gg \mathcal{R}^{-1/2} (d_e \rho_s)^{1/2}$

Valid if $\lambda_{cr} \gg \lambda \gg \rho_s \implies \mathcal{R} \ll \frac{d_e}{\rho_s} \ll \mathcal{R}^9 \left(\frac{L}{\rho_s} \right)^2$

Reconnection in collisionless turbulence

Reconnection at fluid scales



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- Valid if $\lambda_{cr} \gg \lambda \gg \rho_s \implies \mathcal{R} \ll \frac{d_e}{\rho_s} \ll \mathcal{R}^9 \left(\frac{L}{\rho_s} \right)^2$

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- Valid if $\lambda_{cr} \gg \lambda \gg \rho_s \implies \mathcal{R} \ll \frac{d_e}{\rho_s} \ll \mathcal{R}^9 \left(\frac{L}{\rho_s} \right)^2$
- The left inequality may not hold in the pristine SW: it requires $\beta_e \ll 2(m_e/m_i)\mathcal{R}^{-2} \approx 0.1$ which may be too low.
- But the solar corona should observe both of these conditions (and fall in this case of collisionless reconnection at fluid scales).
- The right inequality places spectacular demands on computer simulations...

- Now consider the case when tearing onset is at sub-ion scales. As an example, take a plasma where $\beta_i \sim 1 \gg \beta_e$ (so-called inertial kinetic-Alfvén turbulence).

- From Boldyrev & Loureiro '19, we have
$$\gamma_t \sim \frac{v_{Ae,\lambda}}{\lambda} \left(\frac{d_e}{\lambda} \right)^2$$

- Therefore, we find:
$$\gamma_t \tau_{rec} \ll 1 \Rightarrow \frac{\lambda}{d_e} \gg \mathcal{R}^{-1/2} \sim 3$$

- This is interestingly consistent with Phan *et al.* '18 observations of 'electron-only' reconnection events in the Earth's magnetosheath: reports of reconnection on current sheets $\sim 4d_e$ wide.

– We don't know λ_{cr} for this case, so cannot compute the upper validity limit for this result.

– The lower bound is that $\lambda/d_e \gg 1$, which is marginally satisfied.

– Unlike previous cases, this condition may be easily satisfied in simulations.

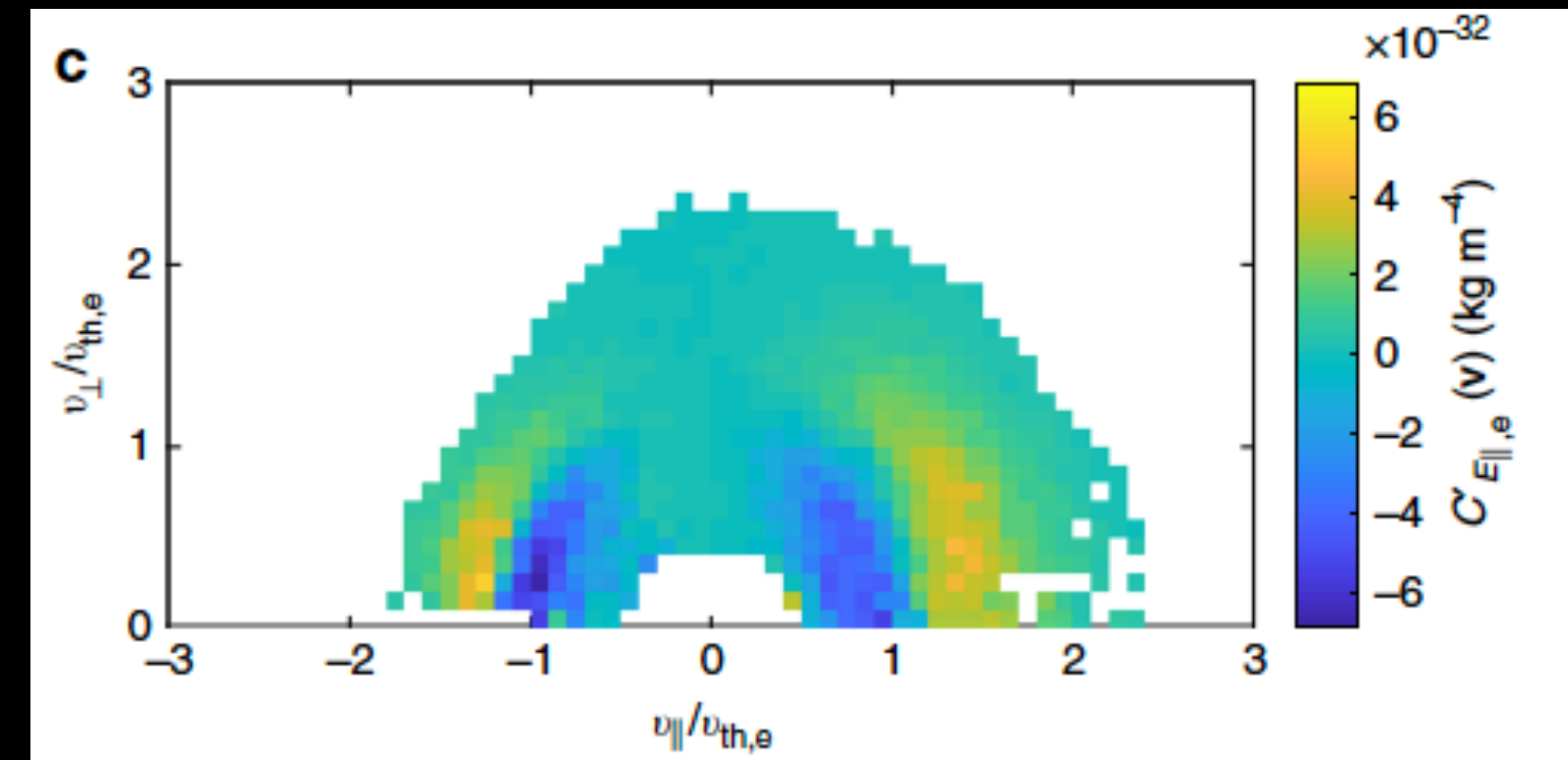
Reconnection at kinetic scales in collisionless turbulence

Consistence with observations



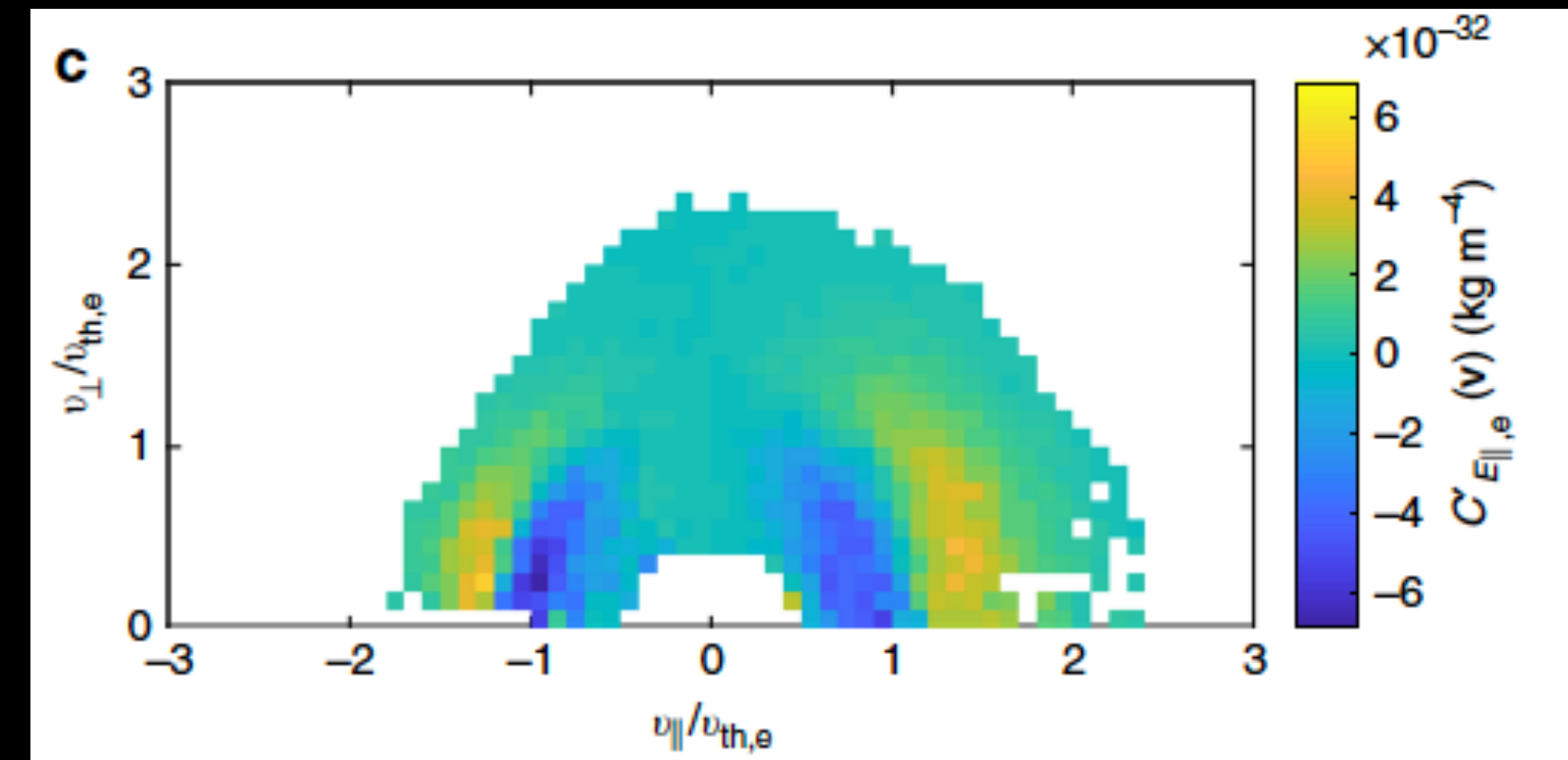
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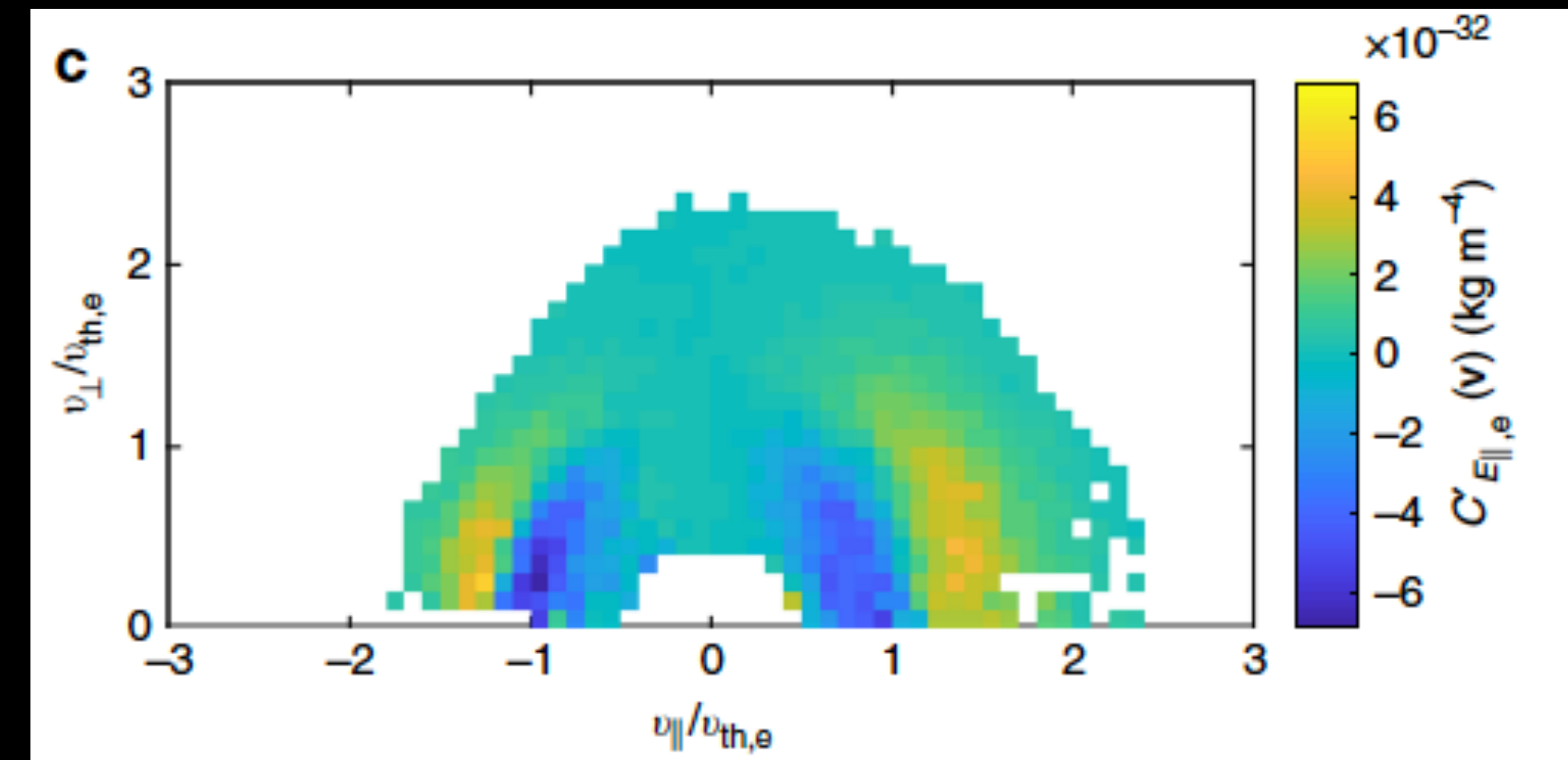
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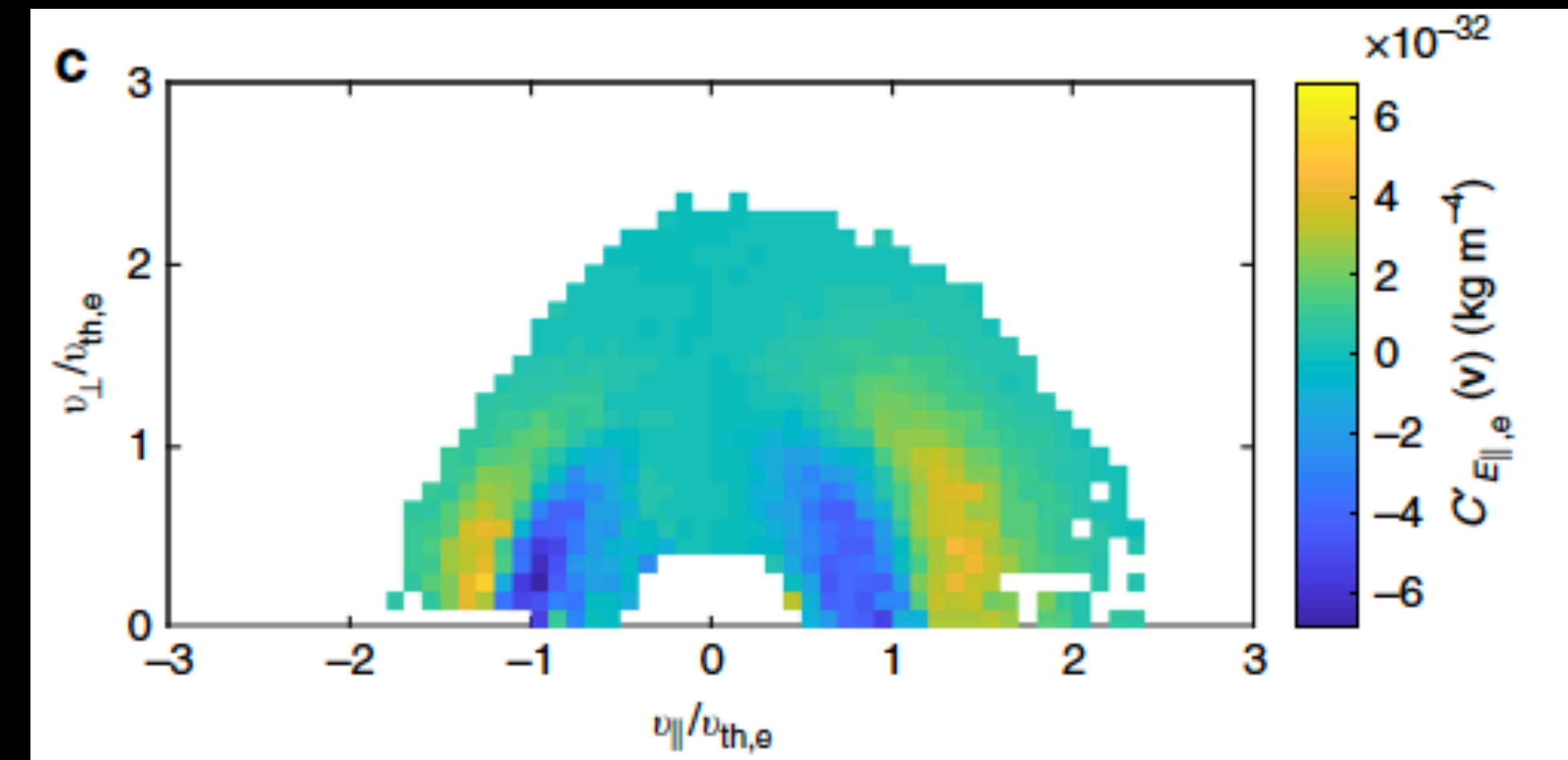
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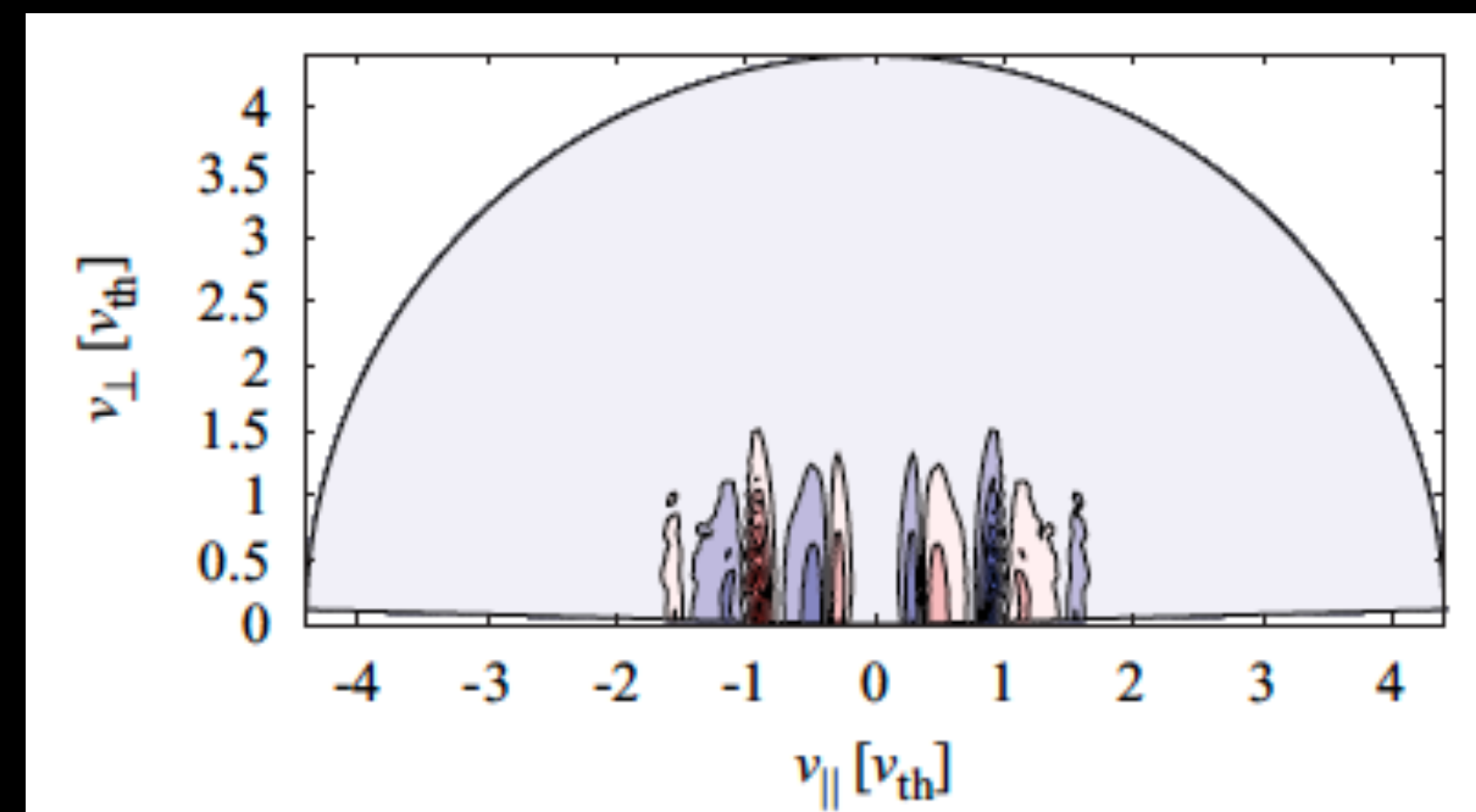
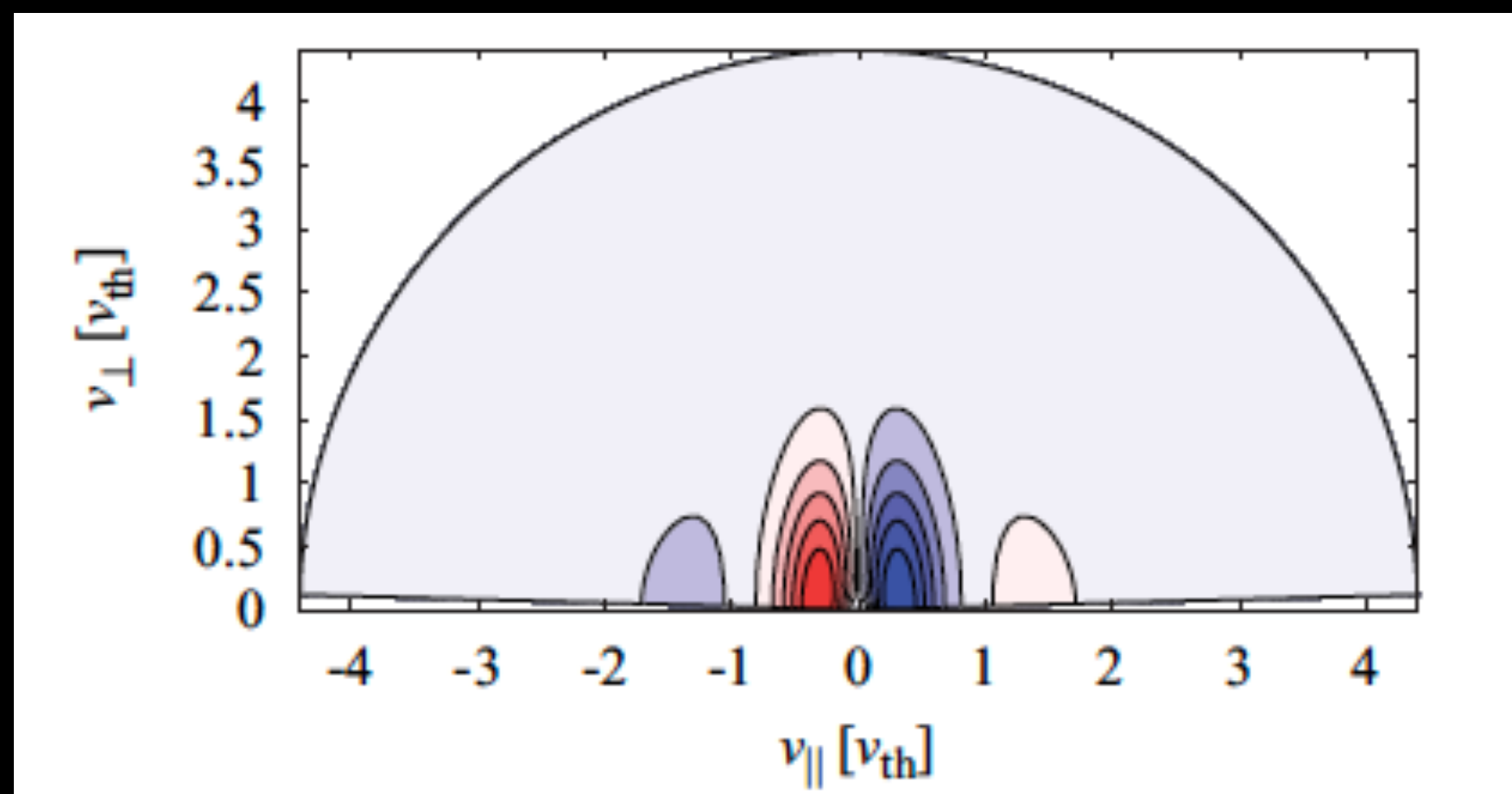


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Chen et al. 2019



Numata & Loureiro 2015

1. If current understanding of MHD turbulence is correct, tearing mode has to become important:

- Eddies become current sheets of progressively larger aspect ratios at small scales
- Therefore, they are progressively more unstable to the tearing mode
- Can compute the scale at which reconnection becomes important. This marks the onset of a new, sub-inertial range whose spectrum is $k_{\perp}^{-11/5}$ or $k_{\perp}^{-19/9}$
- These ideas can be extended to the kinetic (collisionless) regime. In all cases, we obtain spectra that scale as $k_{\perp}^{-8/3}$ or k_{\perp}^{-3} in good agreement with observations and simulations.

2. The onset of tearing does not automatically guarantee that the eddy will reconnect.

- Fundamentally, that's because the reconnection rate is different from the tearing rate; reconnection can only happen if it is *faster* than tearing.
- The conditions for reconnection to happen are *very demanding*
- *We may be significantly underestimating reconnection-driven energy dissipation/conversion in some simulations*