

# *Potential Barrier Effects in Two-Photon Ionization and High-Order Harmonic Generation in the XUV Regime*

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# Outline

## ■ **Potential Barrier Effects in Multiphoton Ionization**

- *Background on Potential Barriers in Photoionization*
- *Calculation of Two-Photon Generalized Cross Sections*
- *Intermediate State Potential Barrier Effects*
- *Final State Potential Barrier Effects*

## ■ **Potential Barrier Effects in HHG**

- *New Formulation for Harmonic Generation*
- *Closed Form Analytic Formula for HHG Near the Cutoff*
- *Potential Barrier Effects in HHG from Xe*
- *Potential Barrier Effects in HHG from Transition Metal Ions*

## ■ **Concluding Remarks**

# **Potential Barrier Effects in Multiphoton Ionization Processes**

**Liang-Wen Pi and Anthony F. Starace**

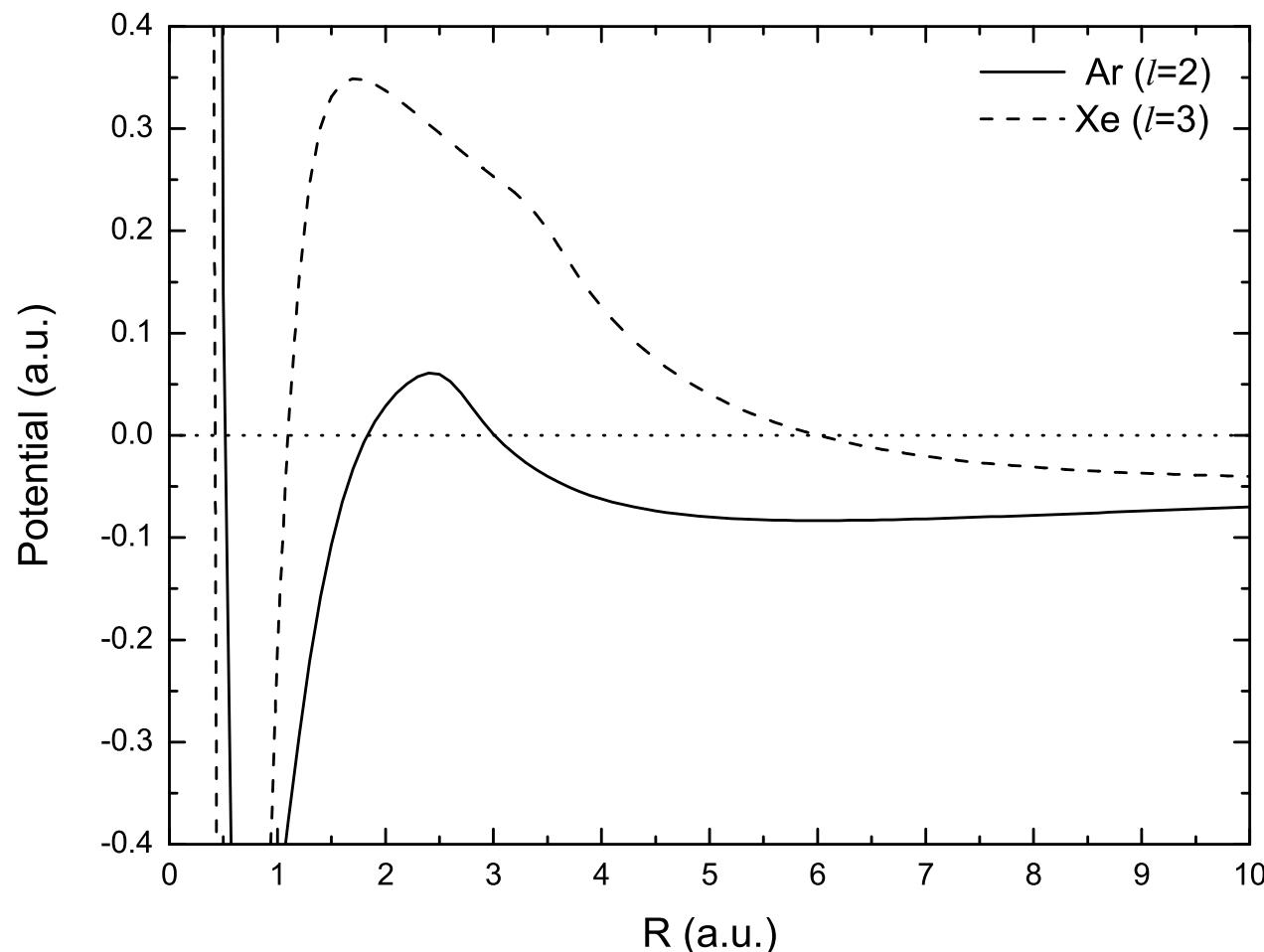
*Department of Physics & Astronomy  
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**Reference:** *Manuscript in preparation*

# Potential Barrier Effects



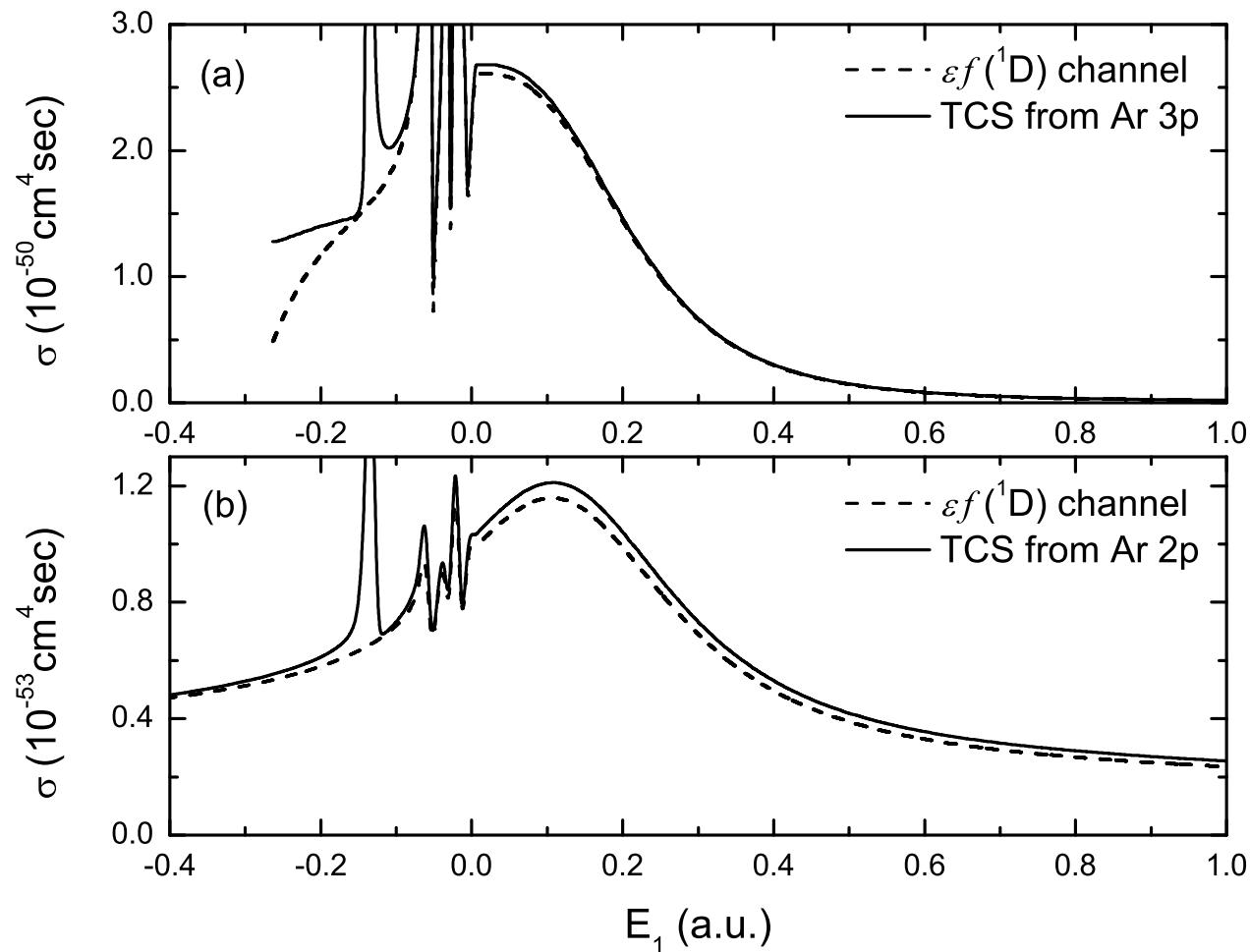
- Effective potential for Ar ( $l=2$ ) and Xe ( $l=3$ )



# Potential Barrier Effects

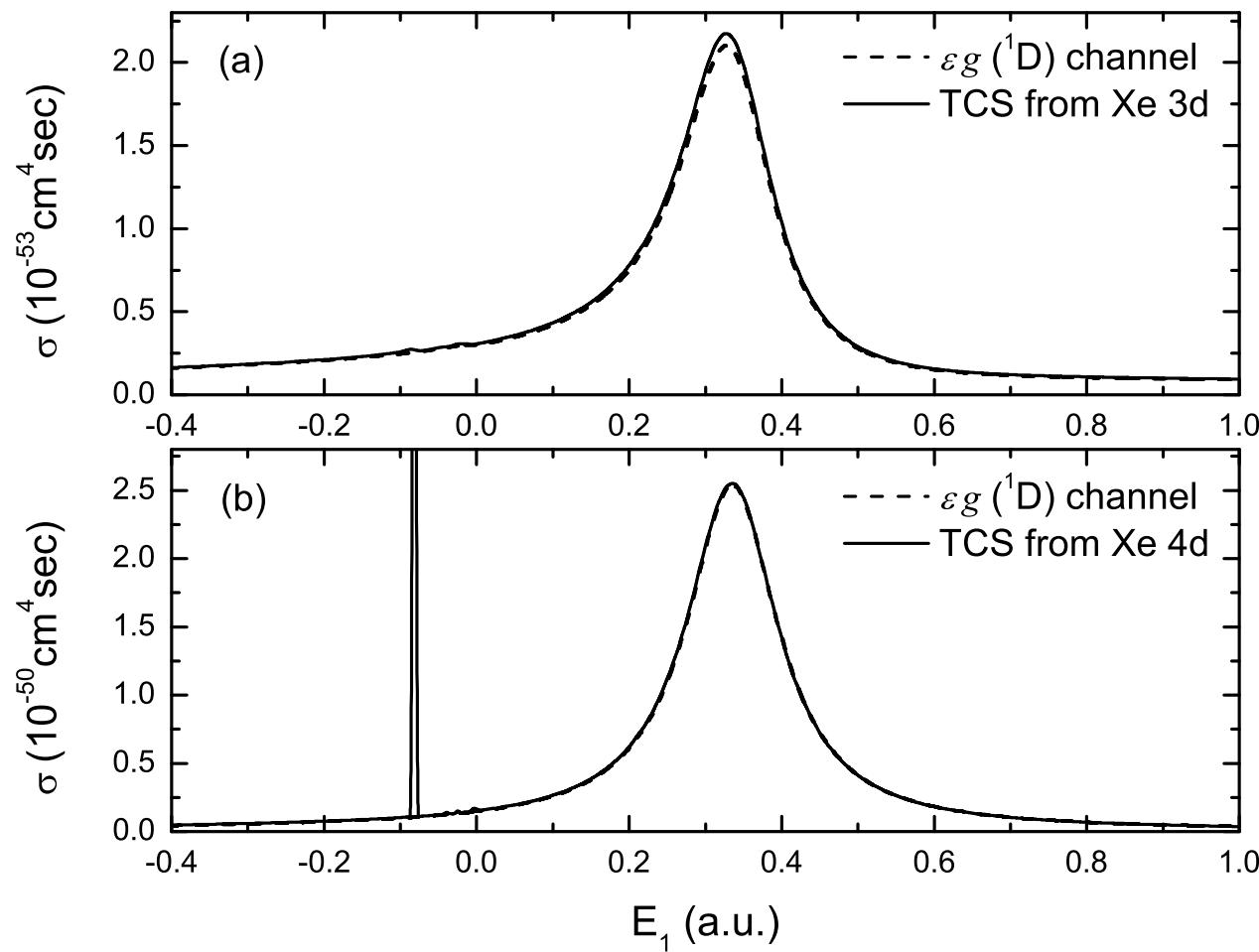


- Generalized cross sections for two-photon ionization of the Ar 2p- and 3p-subshells



# Potential Barrier Effects

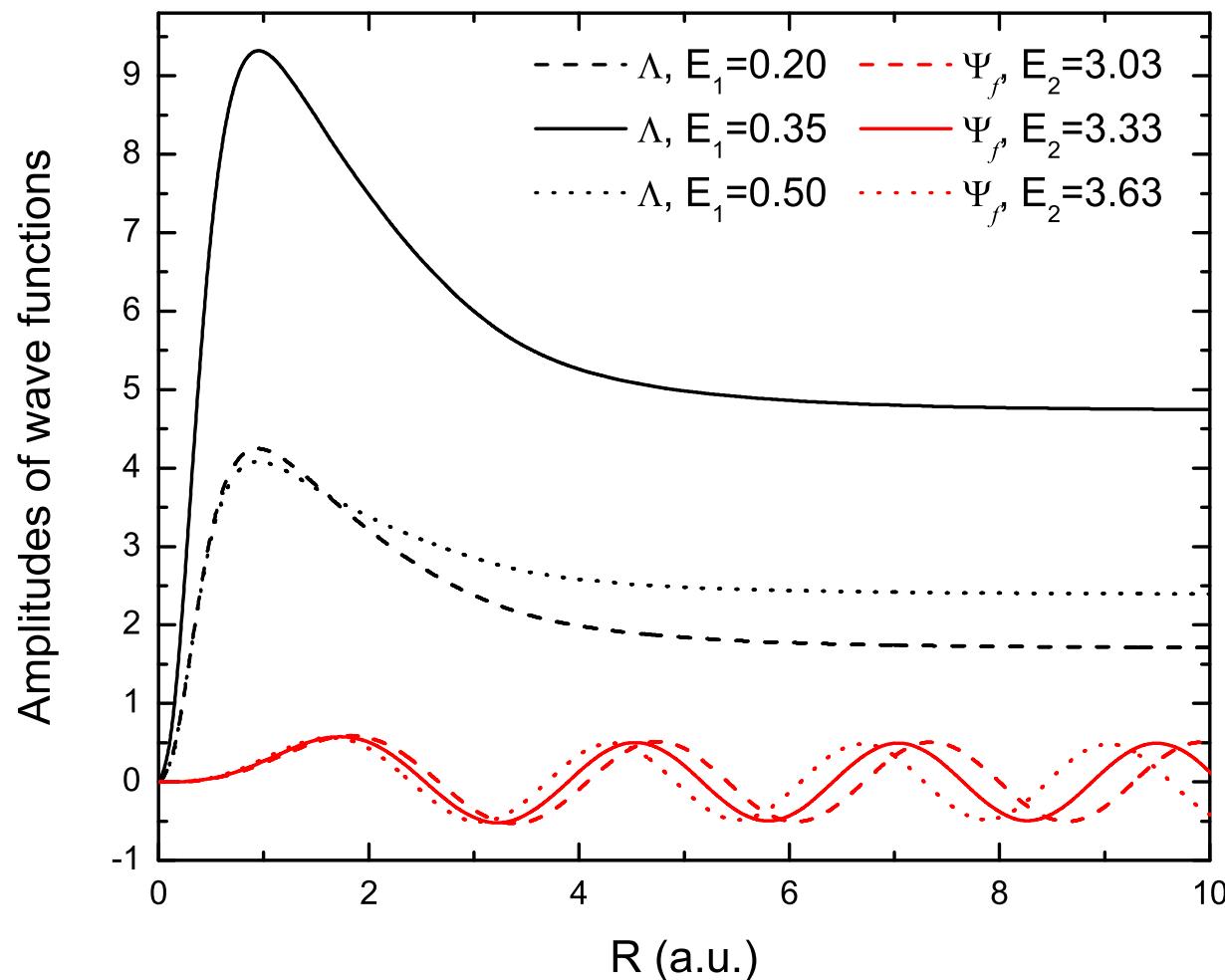
- Generalized cross sections for two-photon ionization of the Xe 3d- and 4d-subshells



# Potential Barrier Effects



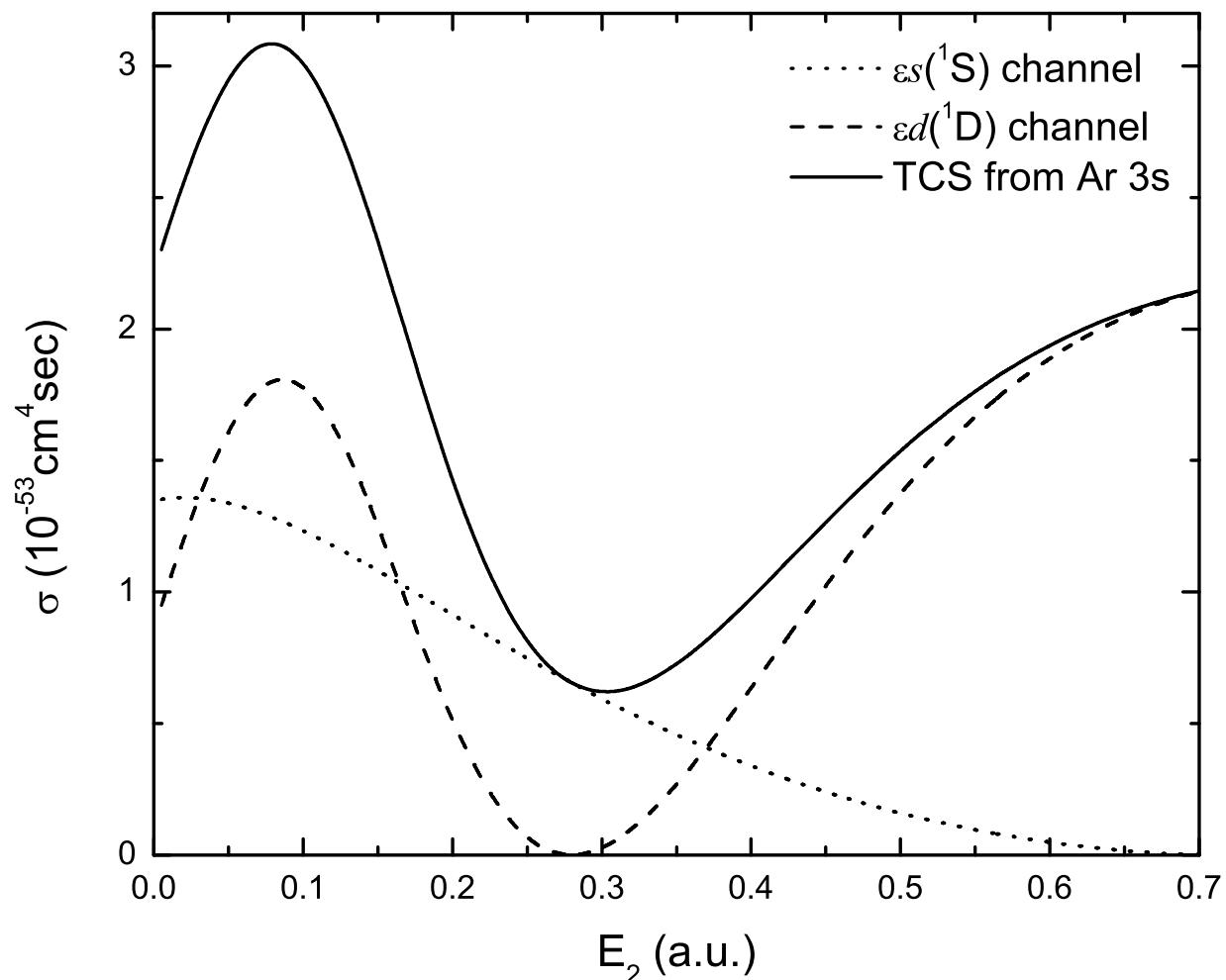
- Amplitudes of the intermediate state  $\Lambda$  and the final state  $\Psi$  for 2-photon ionization of  $Xe\ 4d$



# Potential Barrier Effects



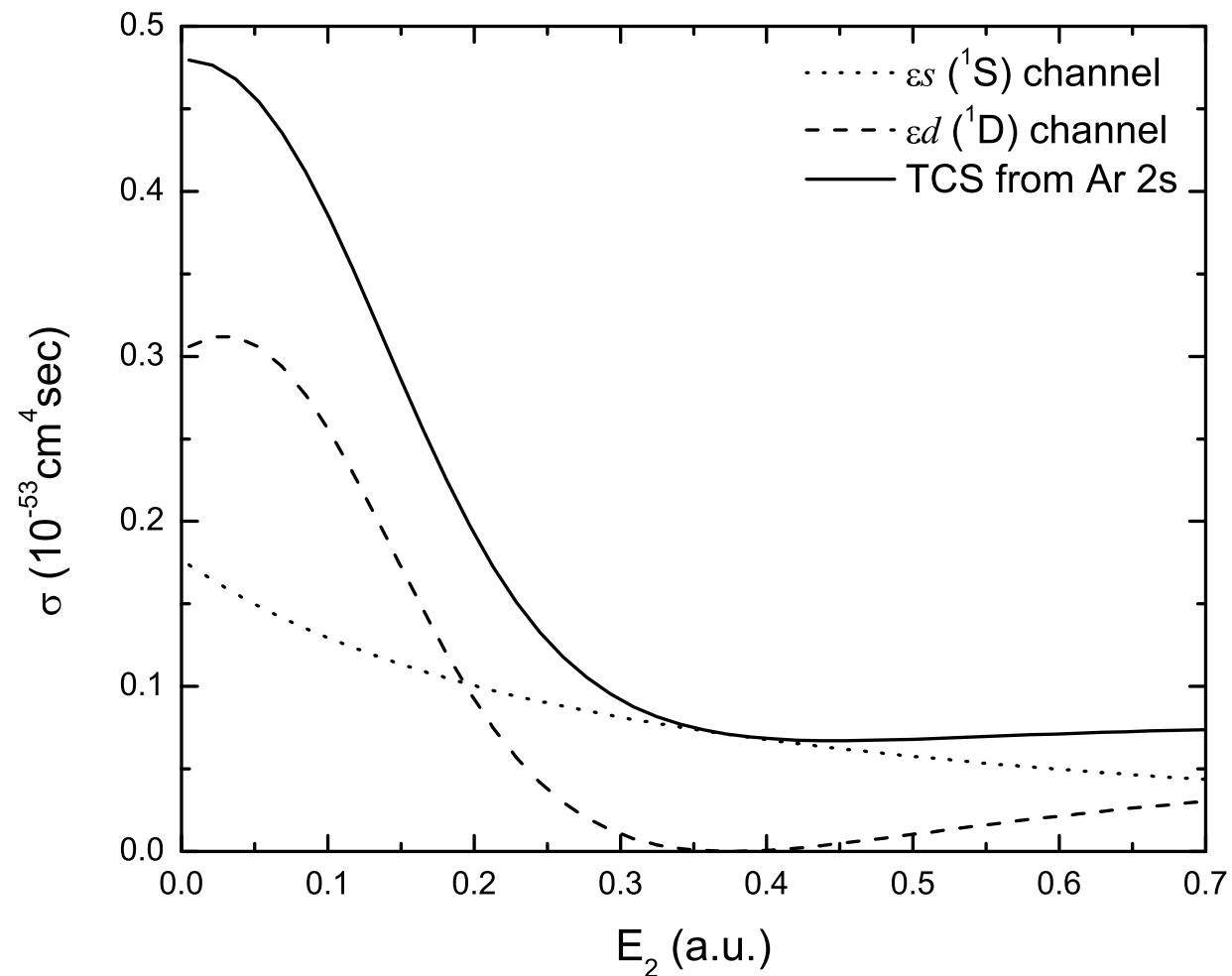
- Generalized cross section for two-photon ionization of the Ar 3s-subshell



# Potential Barrier Effects



- Generalized cross section for two-photon ionization of the Ar 2s-subshell



# *Potential Barrier Effects in High Harmonic Generation*

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**References:** M.V. Frolov *et al.*, *Phys. Rev. A* **82**, XXXXXX (2010), in press.

M.V. Frolov *et al.*, *Phys. Rev. Lett.* **102**, 243901 (2009).

# Key HHG References



## References

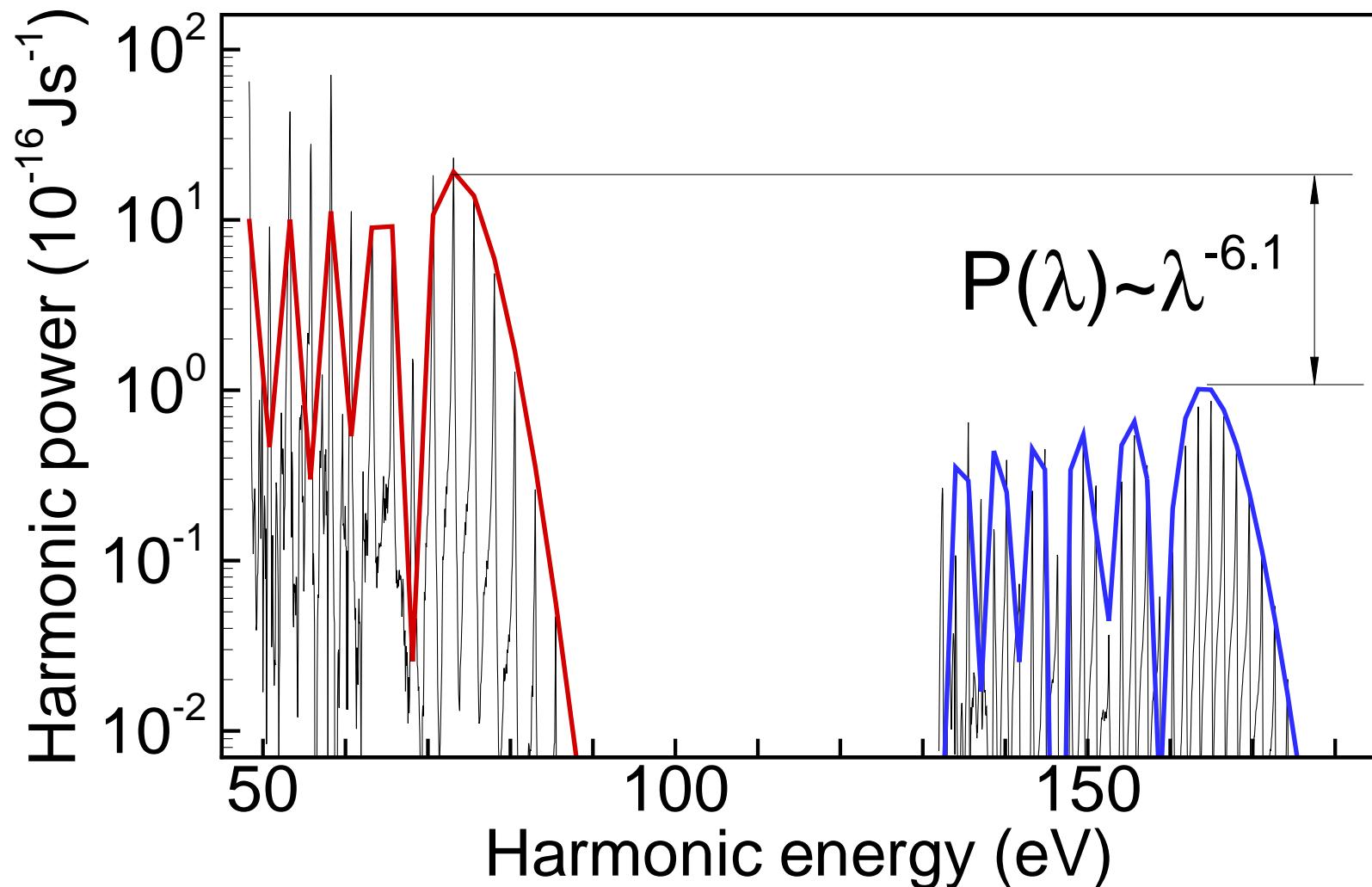
- [1] M.V. Frolov, A.V. Flegel, N.L. Manakov, and A.F. Starace, *Phys. Rev. A* **75**, 063407 (2007) **[General Formulation]**
- [2] M.V. Frolov, A.V. Flegel, N.L. Manakov, and A.F. Starace, *Phys. Rev. A* **75**, 063408 (2007) **[Application to TDER model]**
- [3] M.V. Frolov, N.L. Manakov, T.S. Sarantseva and A.F. Starace, *J. Phys. B* **42**, 035601 (2009) **[Analytic HHG Formula for TDER model]**
- [4] M.V. Frolov, N. L. Manakov, T.S. Sarantseva, M.Yu. Emelin, M.Yu. Ryabikin and A.F. Starace, *Phys. Rev. Lett.* **102**, 243901 (2009) **[Analytic HHG Formula for neutral atoms; potential barrier effects seen in Xe]**
- [5] M.V. Frolov, N.L. Manakov and A.F. Starace, *Phys. Rev. A* **82** (in press) (2010)  
**[Resonant HHG for transition metal ions Cr+ and Mn+]**

# Comparison of $\mathcal{H}\mathcal{H}G$ for $\mathcal{H}$ -Atom



$\lambda = 1.0 \mu\text{m}$  (left) and  $\lambda = 1.6 \mu\text{m}$  (right),  $I = 2 \times 10^{14} \text{W/cm}^2$ .

*Thick Lines: Analytic Formula Results; Thin Lines: TDSE Results.*



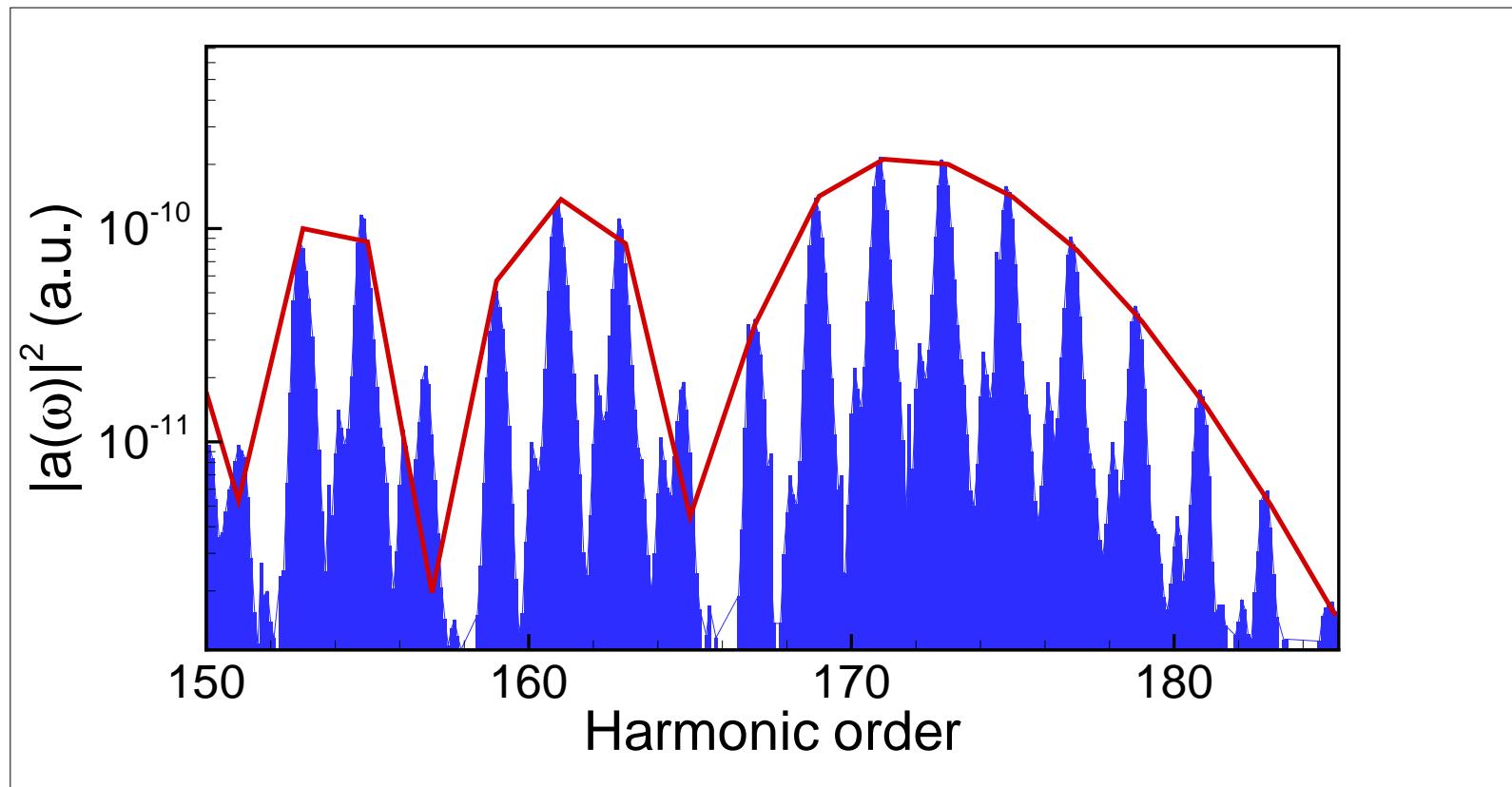
# Comparison of $\mathcal{H}\mathcal{H}G$ for $\mathcal{H}$ -Atom



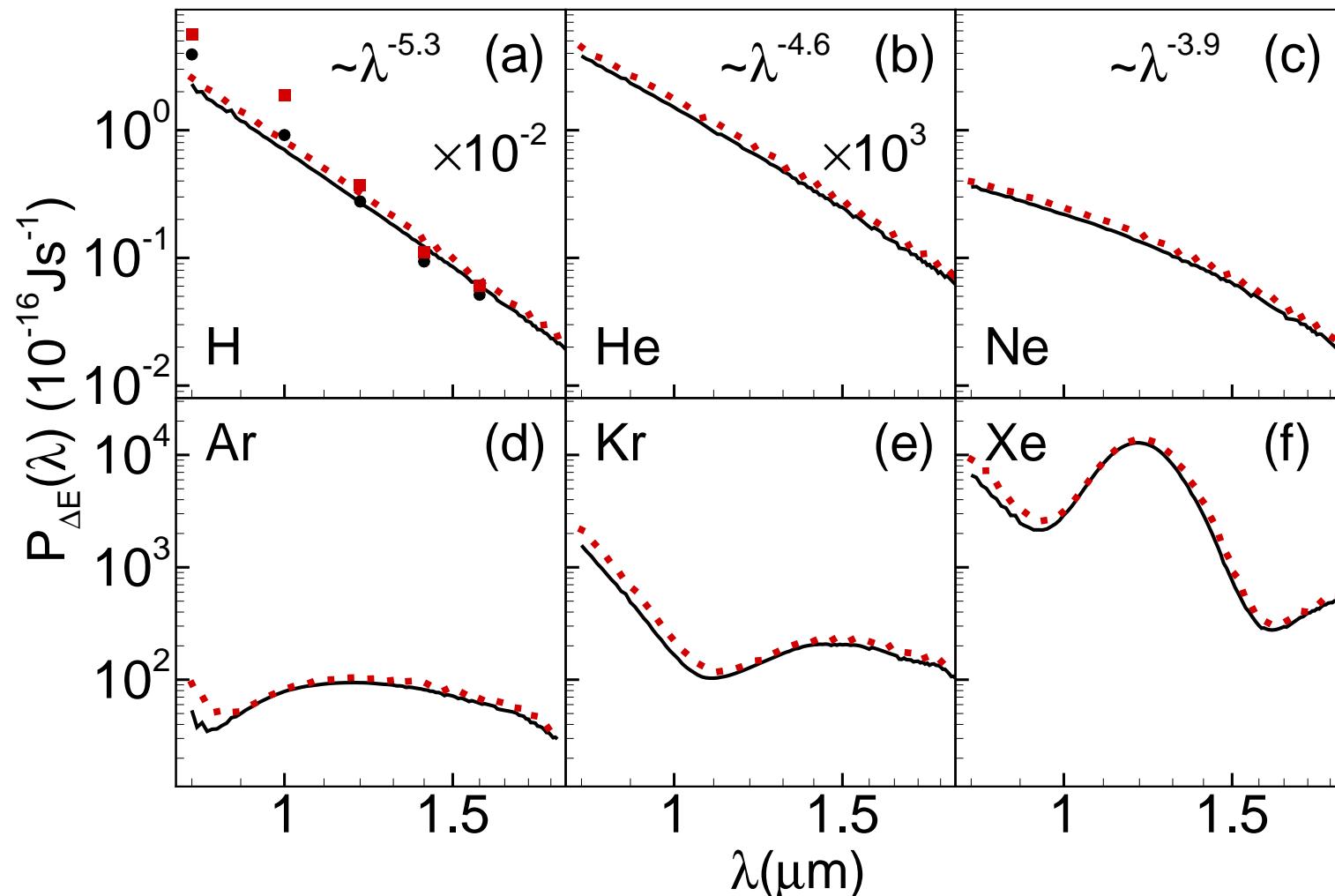
*Thin Lines:* J.A. Pérez-Hernández *et al.*, *Opt Exp* **17**, 9891

(2009) TDSE results for  $\lambda = 1.6 \mu\text{m}$ ,  $I = 1.6 \times 10^{14} \text{W/cm}^2$

*Thick Lines:* Present Analytic Formula Results



Harmonic power,  $P_{\Delta E}(\lambda)$ , vs.  $\lambda$  for H and rare gases  
 with  $I = 2 \times 10^{14}$  W/cm<sup>2</sup> and  
 $\Delta E = 20$  eV (solid lines) and 30 eV (dotted lines)



# Cr Plasma HHG Spectra



PHYSICAL REVIEW A 75, 063806 (2007)

## Systematic investigation of resonance-induced single-harmonic enhancement in the extreme-ultraviolet range

R. A. Ganeev,<sup>1,2,\*</sup> L. B. Elouga Bom,<sup>1</sup> J.-C. Kieffer,<sup>1</sup> and T. Ozaki<sup>1</sup>

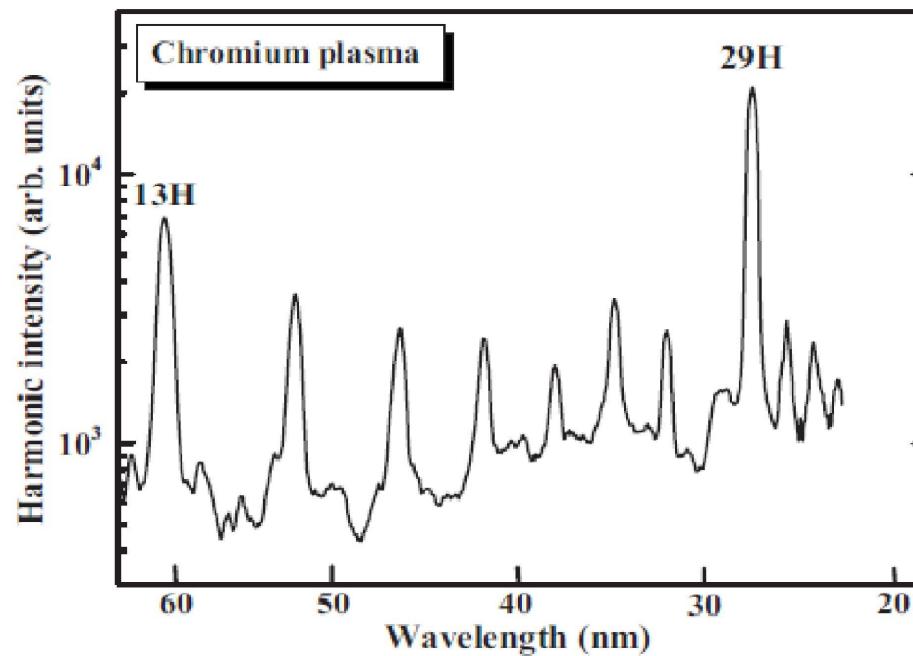
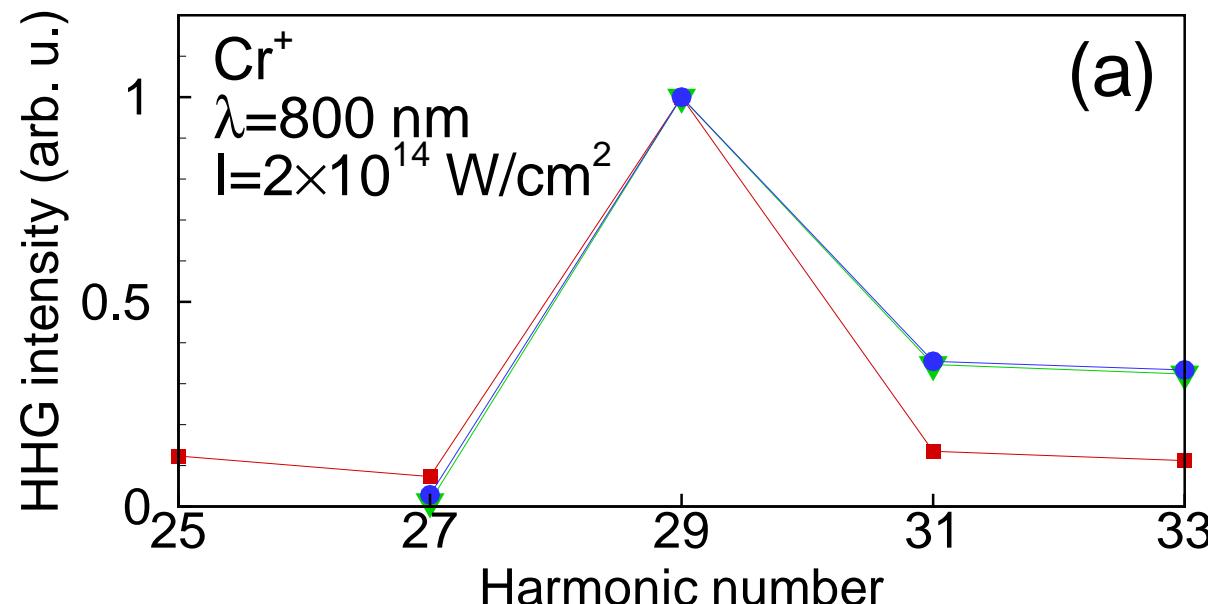


FIG. 4. Harmonic spectra from Cr plasma in the case of 800 nm, 35 fs chirp-free main pulses.



**Figure 1:** HHG spectra of Cr<sup>+</sup> for  $\lambda = 800\text{nm}$ . Squares (red): Ganeev *et al.* results [Phys. Rev. A **75**, 063806 (2007)]. Circles (blue): present results for  $\beta = 0$ . Triangles (green): present results for Cr<sup>+</sup> with the asymmetry parameter  $\beta \neq 0$ .

### Physics of recombination:

- (i): Cr<sup>++</sup>3p<sup>6</sup>3d<sup>4</sup>(<sup>5</sup>D)+ $\epsilon\ell \rightarrow$  Cr<sup>+</sup>3p<sup>5</sup>(<sup>2</sup>P)3d<sup>6</sup>(<sup>5</sup>D)(<sup>6</sup>P)
- (ii): Cr<sup>+</sup>3p<sup>5</sup>(<sup>2</sup>P)3d<sup>6</sup>(<sup>5</sup>D)(<sup>6</sup>P) → Cr<sup>+</sup>3p<sup>6</sup>3d<sup>5</sup>(<sup>6</sup>S) +  $\gamma$ .