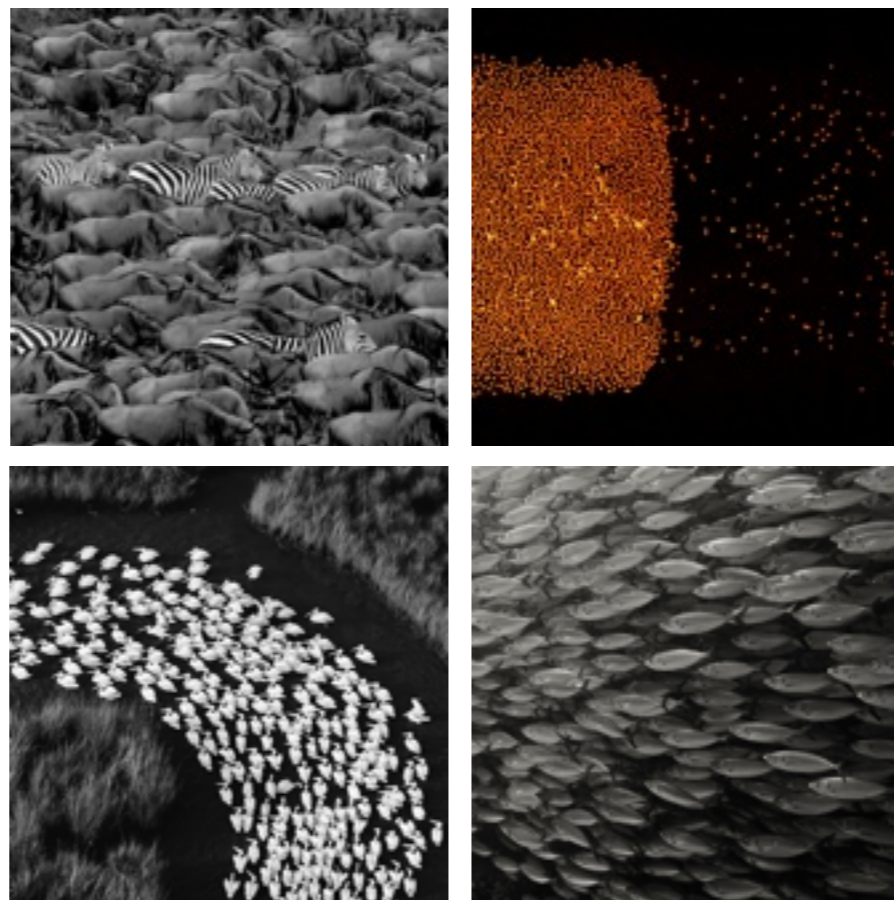


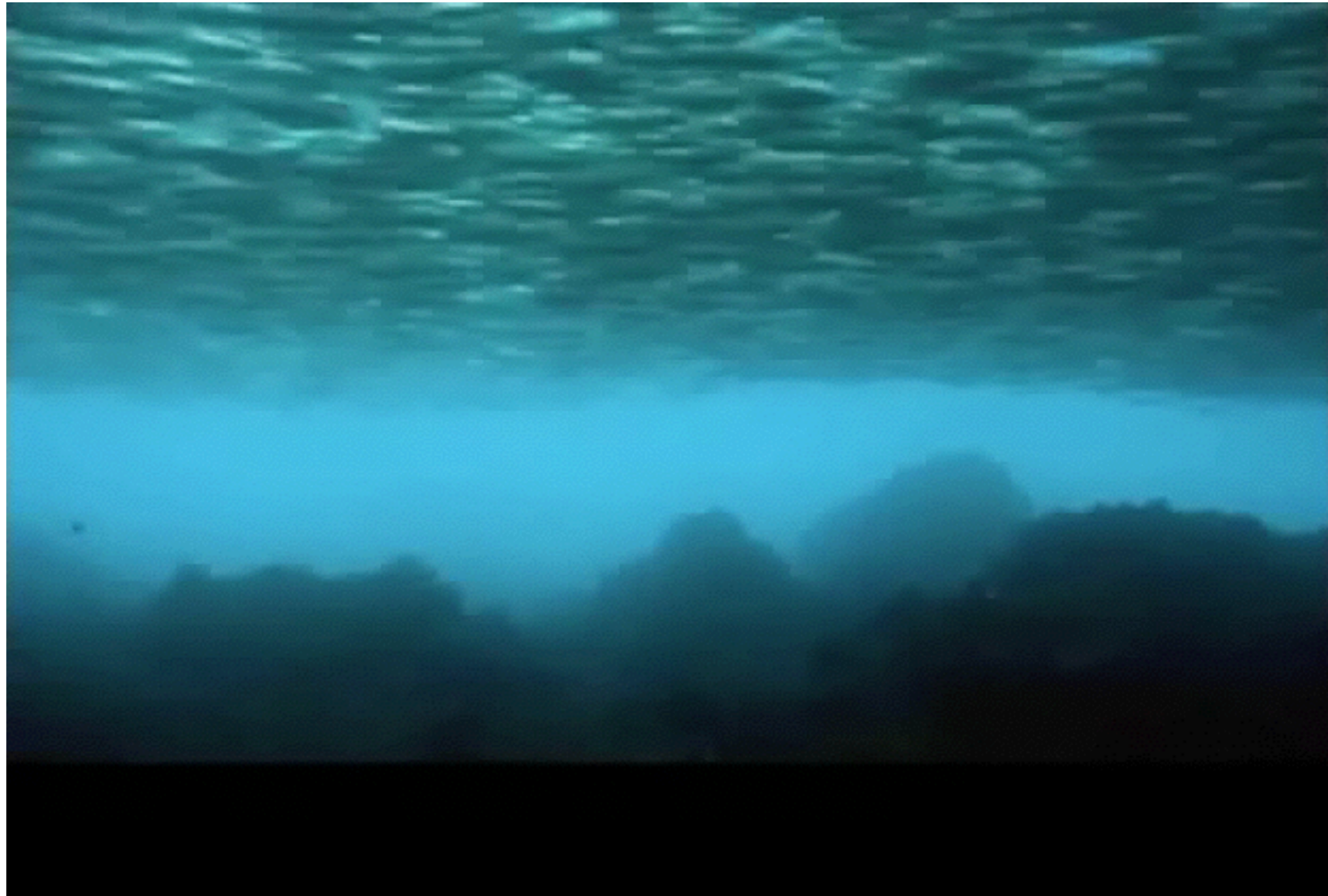
Collective Motion in Populations of Colloidal Bots



Denis Bartolo

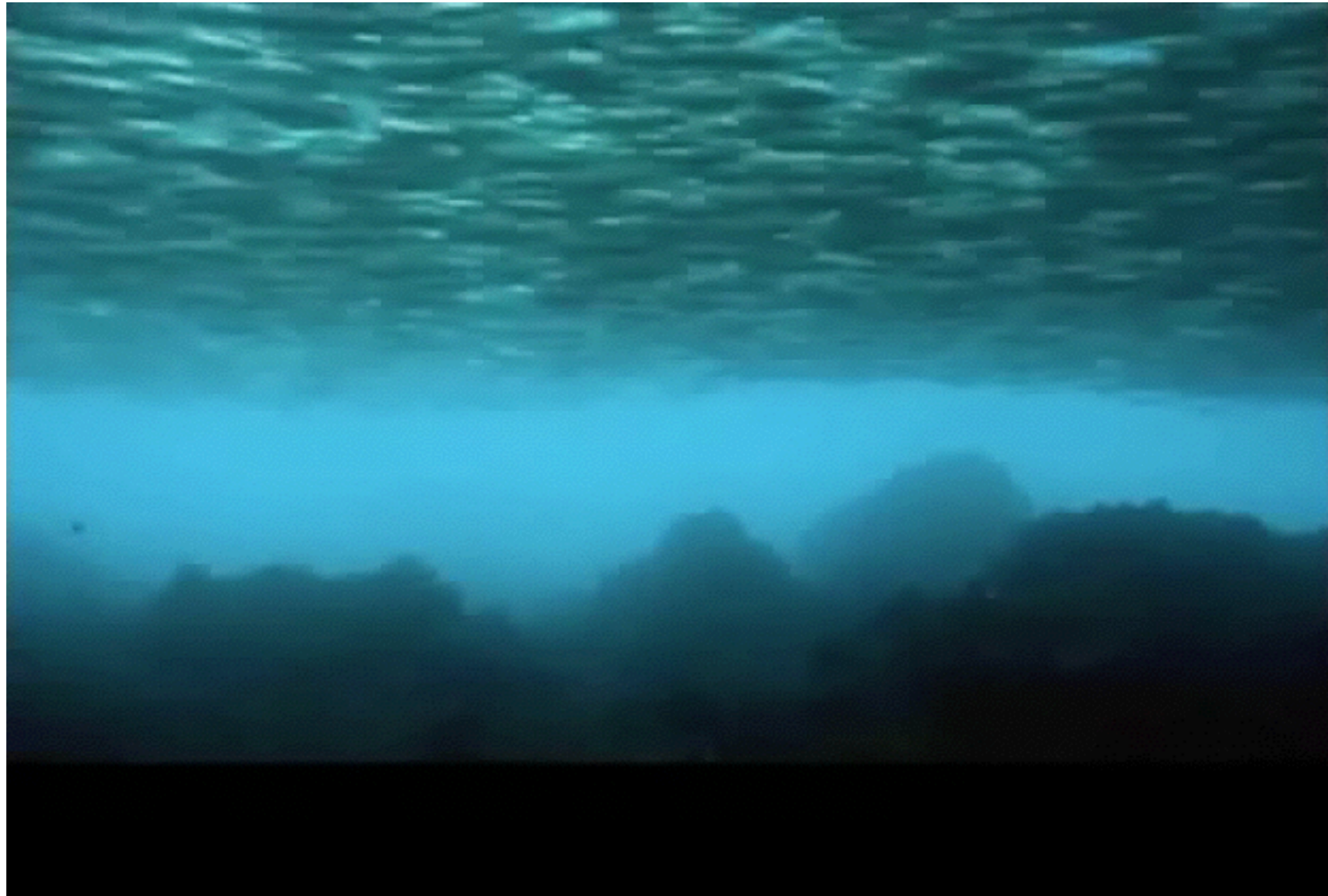
Antoine Bricard (PhD), Jean-Baptiste Caussin (PhD), Nicolas Desreumaux (PhD), Olivier Dauchot (EC2M, ESPCI)

Coherent directed motion



Sardines: 7km-long school

Coherent directed motion



Sardines: 7km-long school

Coherent directed motion



Locusts: 14km-long swarm

Coherent directed motion

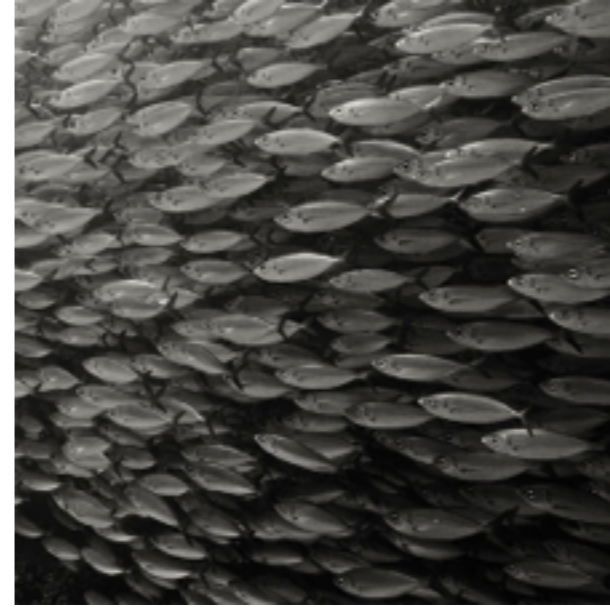


Locusts: 14km-long swarm

Similar large-scale behavior



National geographic



Steve Dunleavy



National geographic

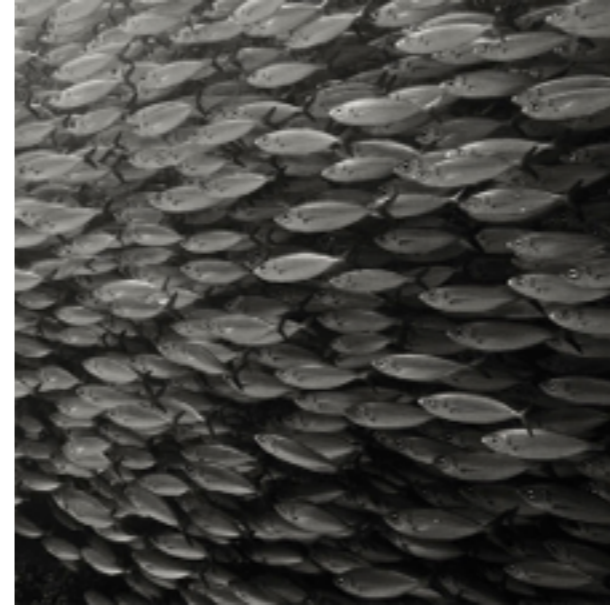


National geographic

Different interactions at the individual level



National geographic



Steve Dunleavy



National geographic

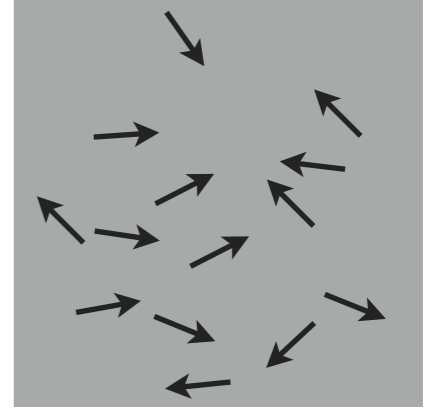
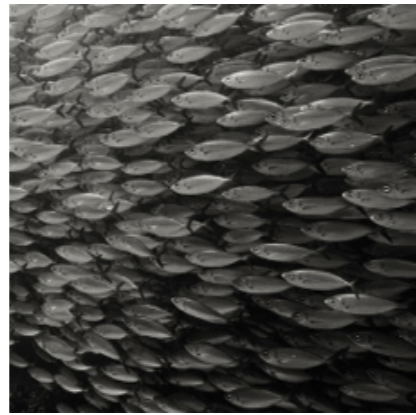


National geographic

Coherent directed motion

Physicists' comfort zone

Flocking



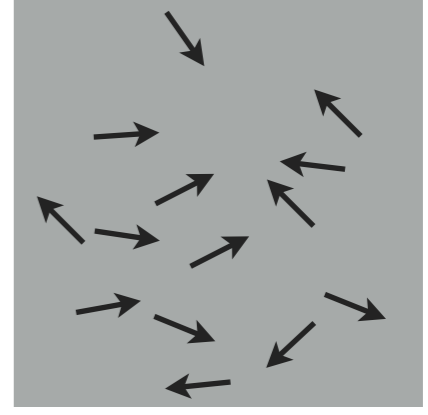
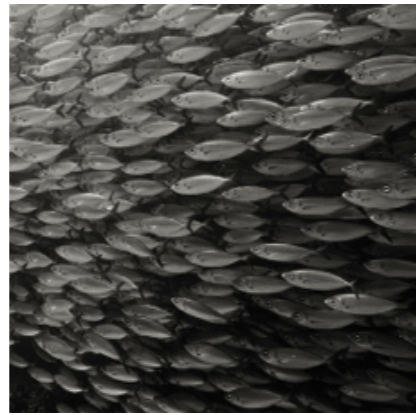
\mathbf{V}_i

Emergence of directed motion?
How is the rotational symmetry broken?

\mathbf{r}_i

Self-organization into “localized” groups?
How is the translational symmetry broken?

Flocking



\mathbf{V}_i

Emergence of directed motion?
How is the rotational symmetry broken?

\mathbf{r}_i

Self-organization into “localized” groups?
How is the translational symmetry broken?

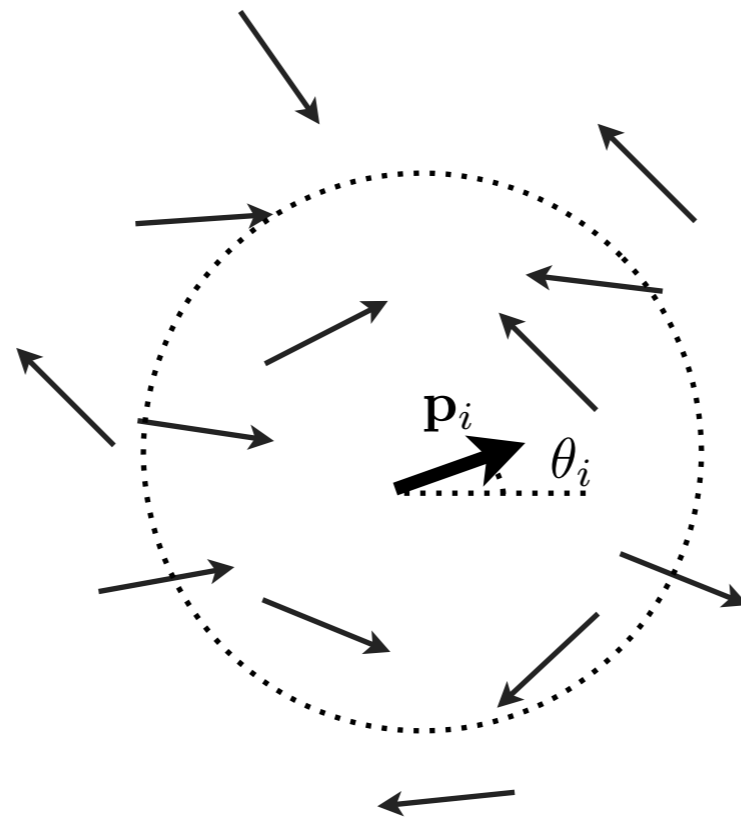
Vicsek model(s)

Self-propelled

$$\mathbf{v}_i = v_0 \mathbf{p}_i$$

Polar/Alignment interaction

$$\theta_i(t+1) = \langle \theta_i(t) \rangle_R + \xi_i(t)$$



Polar active matter

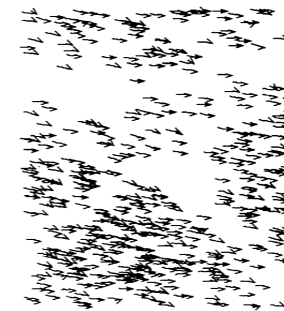
Hallmarks of polar active matter

1

Disordered gas



✓ Polar liquid



Disordered

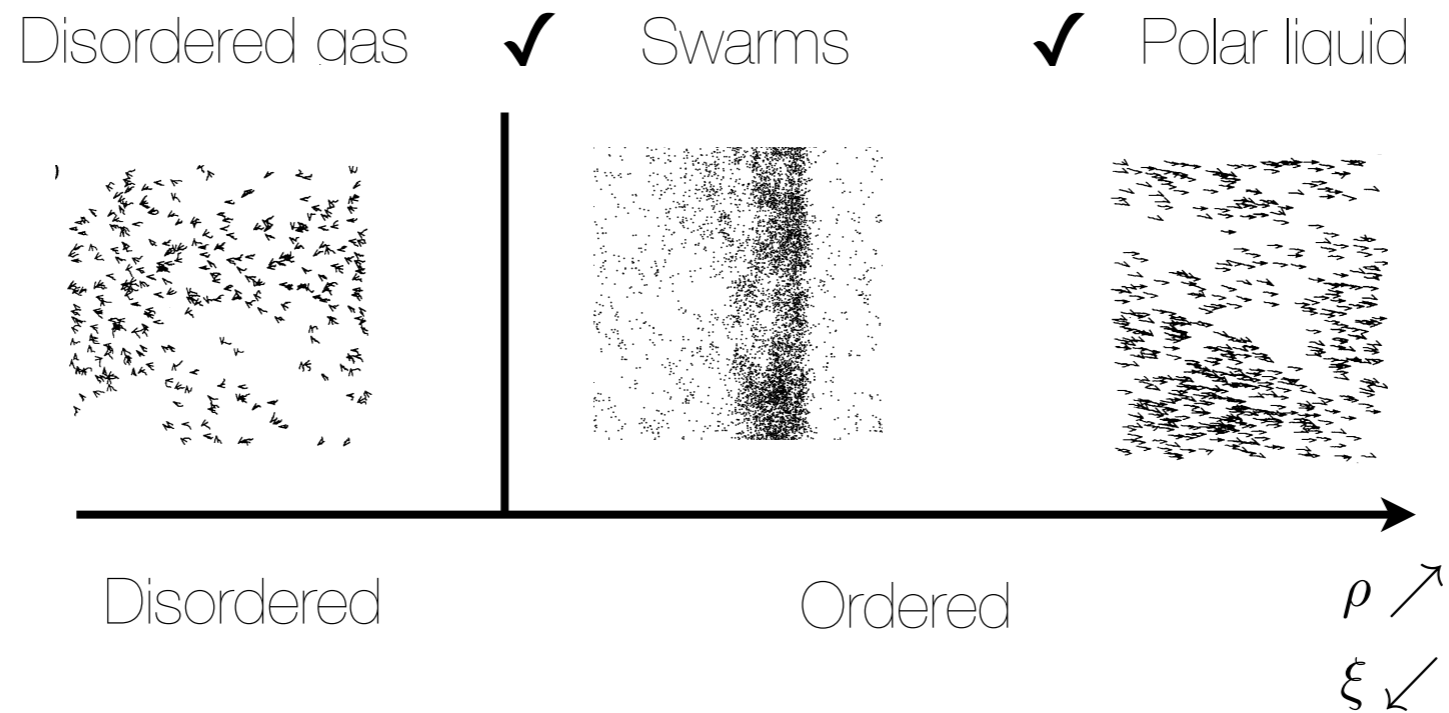
Ordered

ρ ↗

ξ ↘

Hallmarks of polar active matter

1

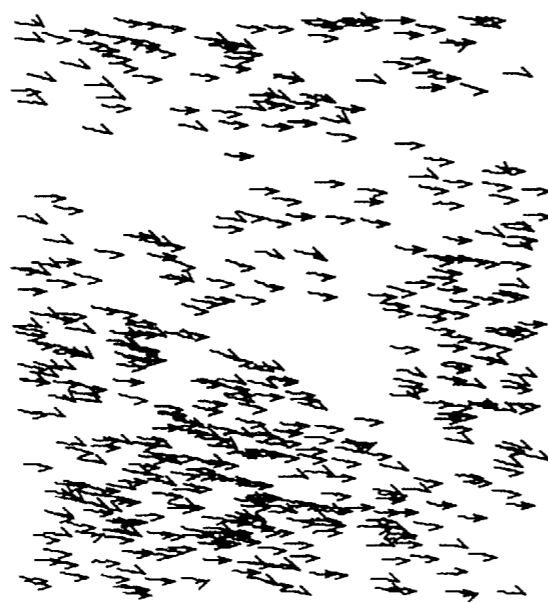


Hallmarks of polar active matter

1



2



Giant Number Fluctuations

$$\Delta N \sim \langle N \rangle^\alpha$$
$$\alpha > 1$$

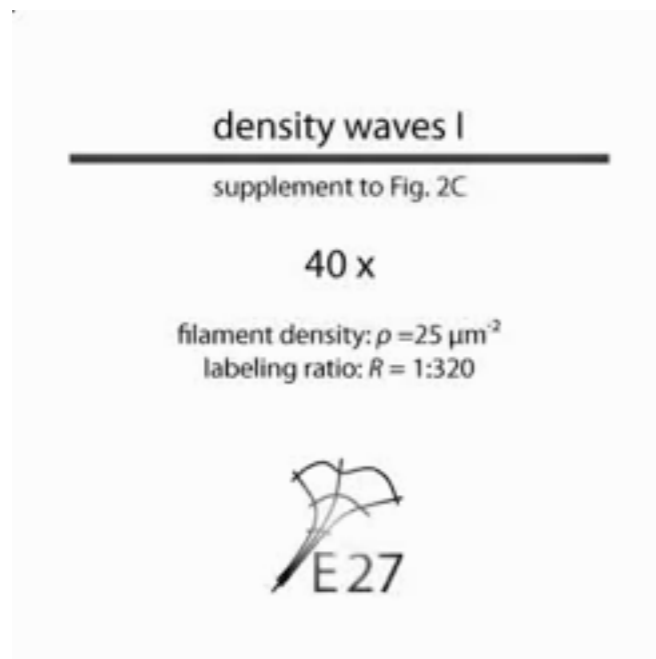
The hallmarks of active matter

3

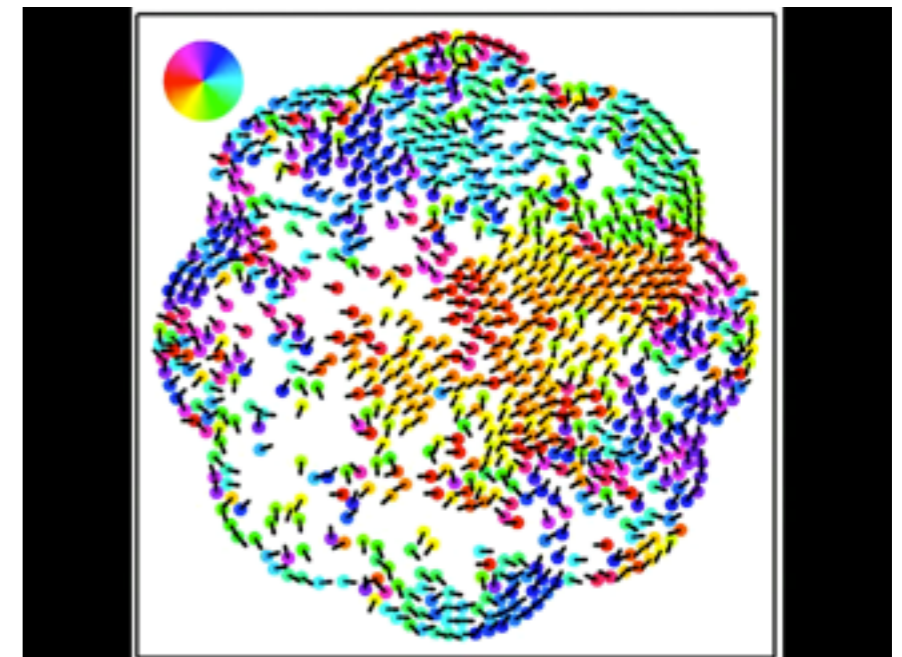
$$N_{\text{Theories}} \gg N_{\text{Experiments}}$$

The hallmarks of active matter

3 $N_{\text{Theories}} \gg N_{\text{Experiments}}$



Baush's group Nature 2010

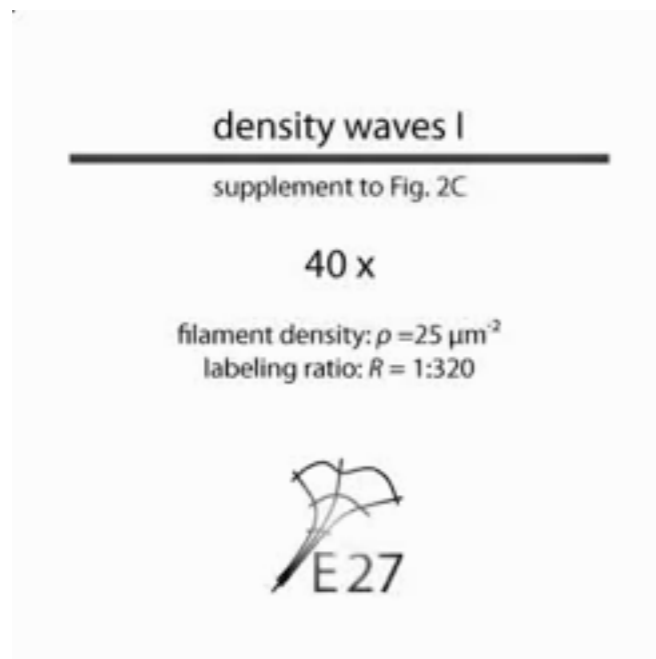


Dauchot's group PRL 2010

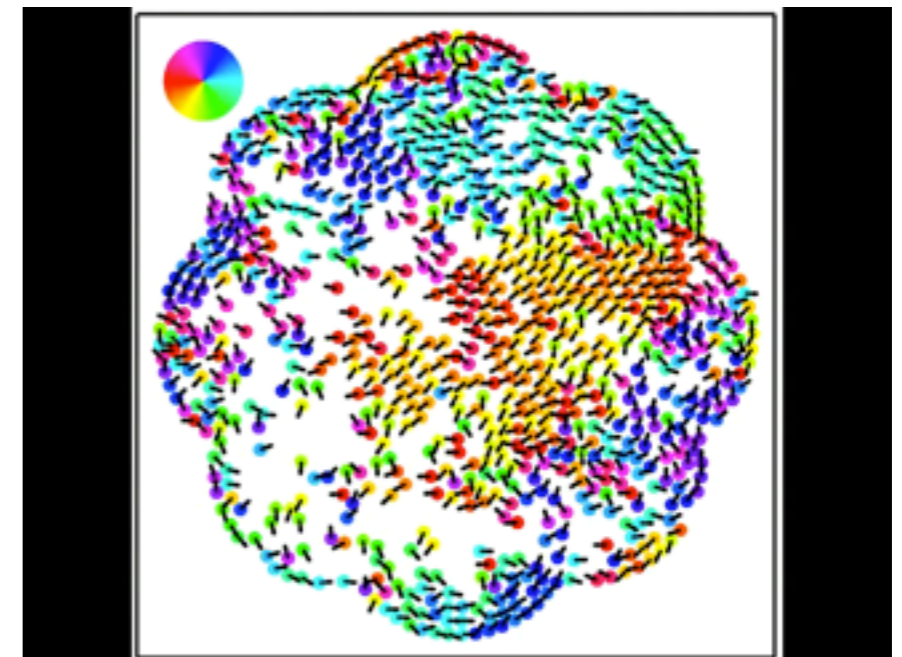
The hallmarks of active matter

3 $N_{\text{Theories}} \gg N_{\text{Experiments}}$

~0 model system until 2010



Baush's group Nature 2010



Dauchot's group PRL 2010

Polar-liquid phase?

Large-scale population dynamics

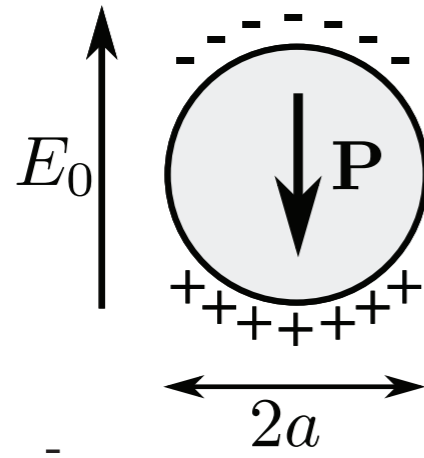
Requirements

- $N \gg \gg 1$ Small (Paris: 12 000 €/m²)
- Quantitative measurements (tracking)
- Known polar interactions

Self-propelled particles: 1st trick

Quincke Rotation

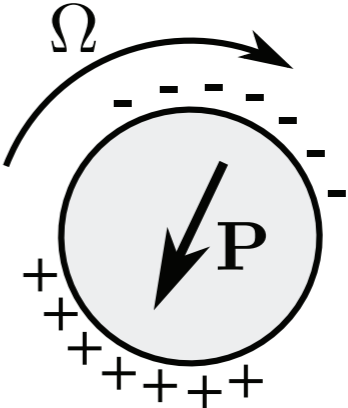
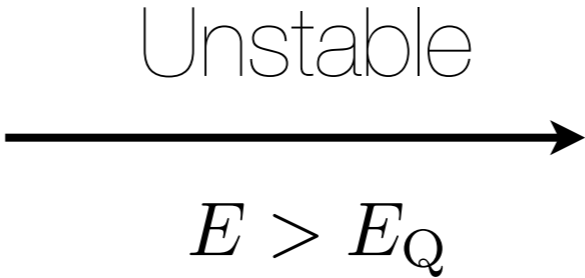
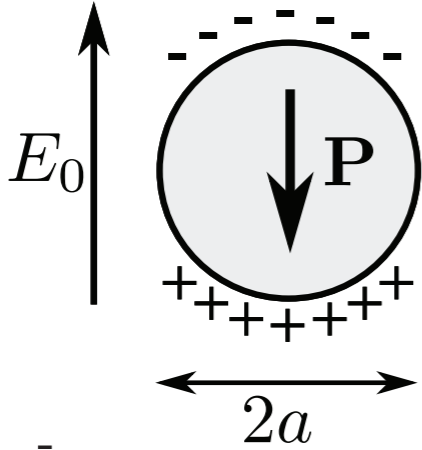
G. Quincke, Ann. Phys. Chem. **59**, 417 (1896).



Self-propelled particles: 1st trick

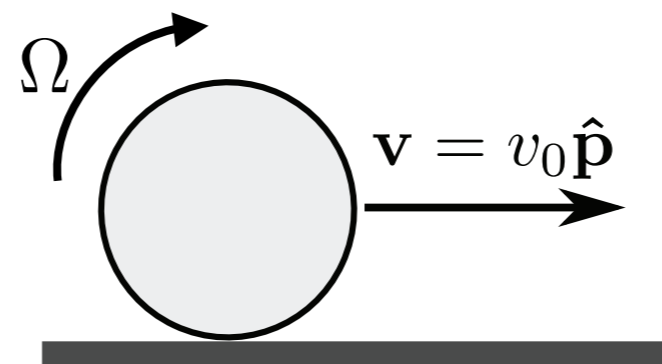
Quincke Rotation

G. Quincke, Ann. Phys. Chem. **59**, 417 (1896).

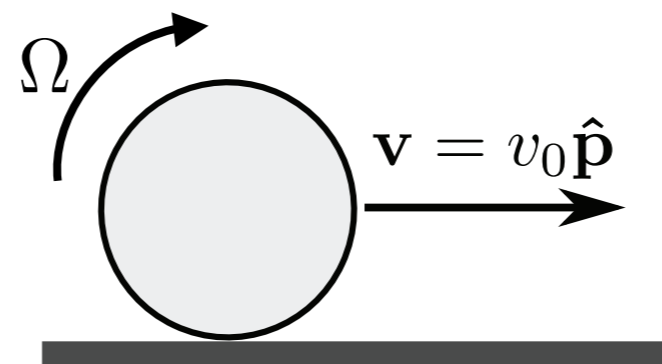


$$\boldsymbol{\Omega} \sim \mathbf{P} \times \mathbf{E}$$

Self-propelled particles: 2nd trick



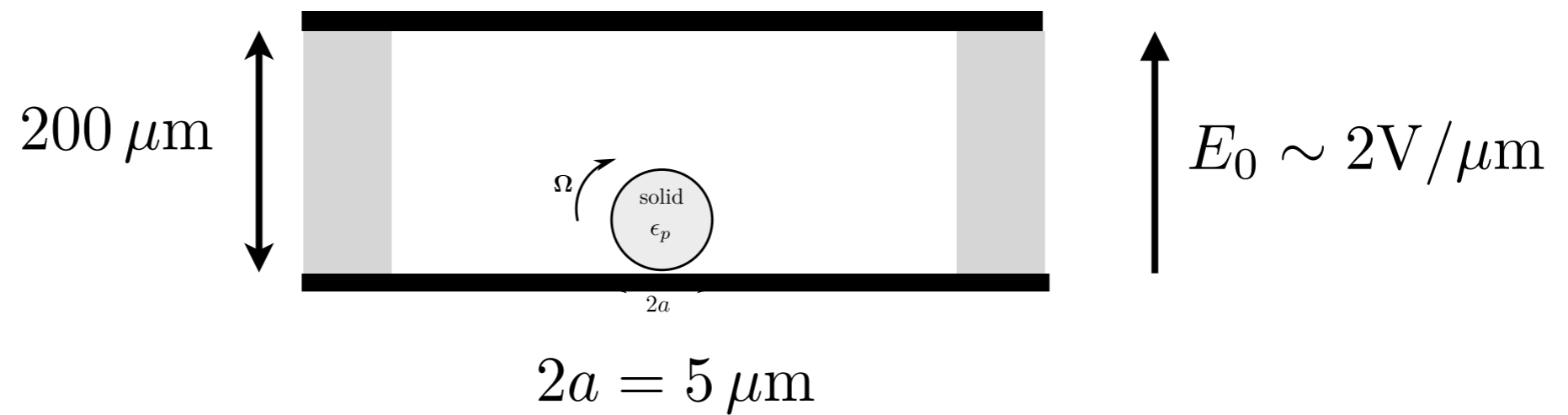
Self-propelled particles: 2nd trick



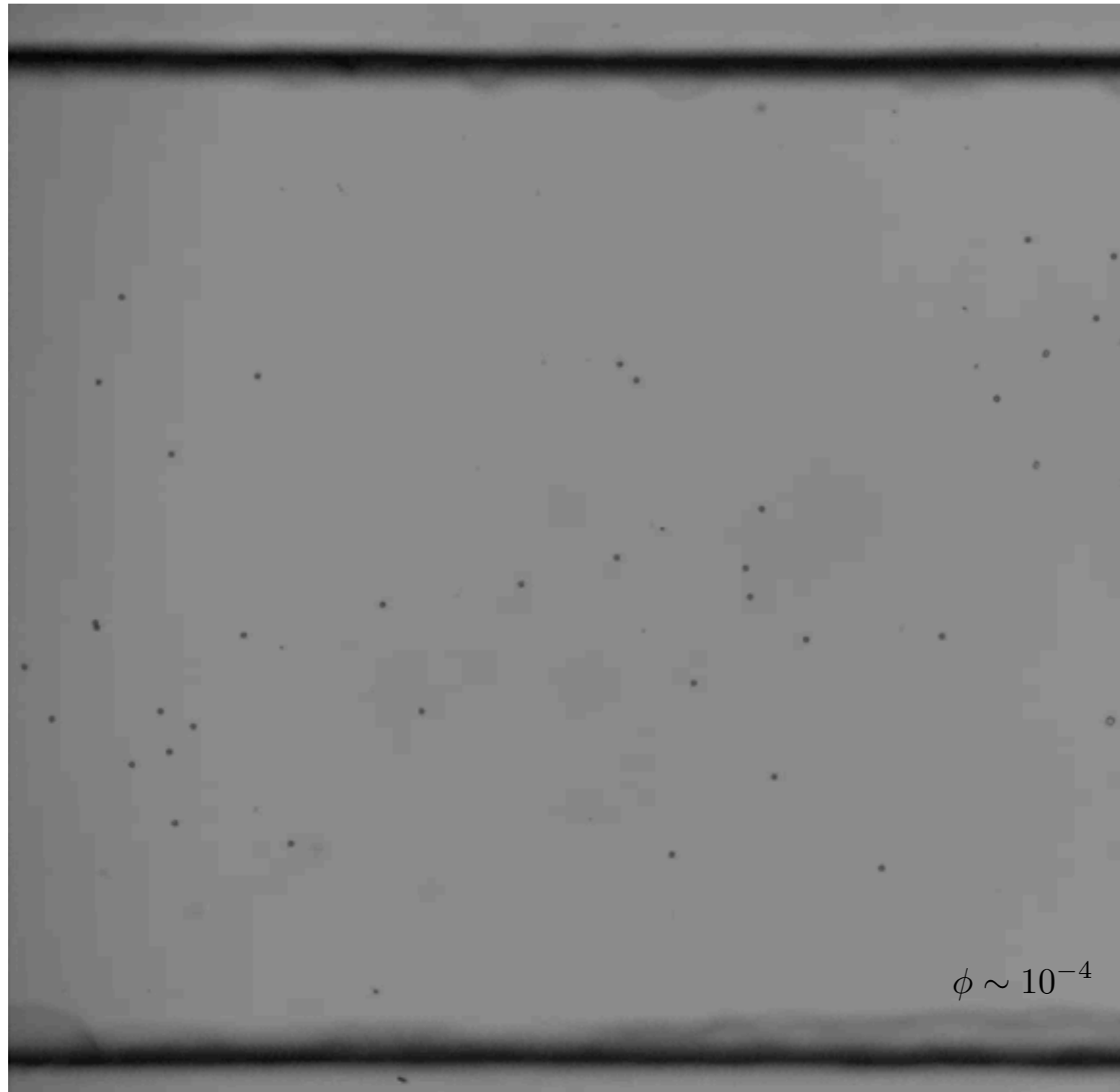
Self-propelled colloids

PMMA colloids
Hexadecane oil+AOT salt

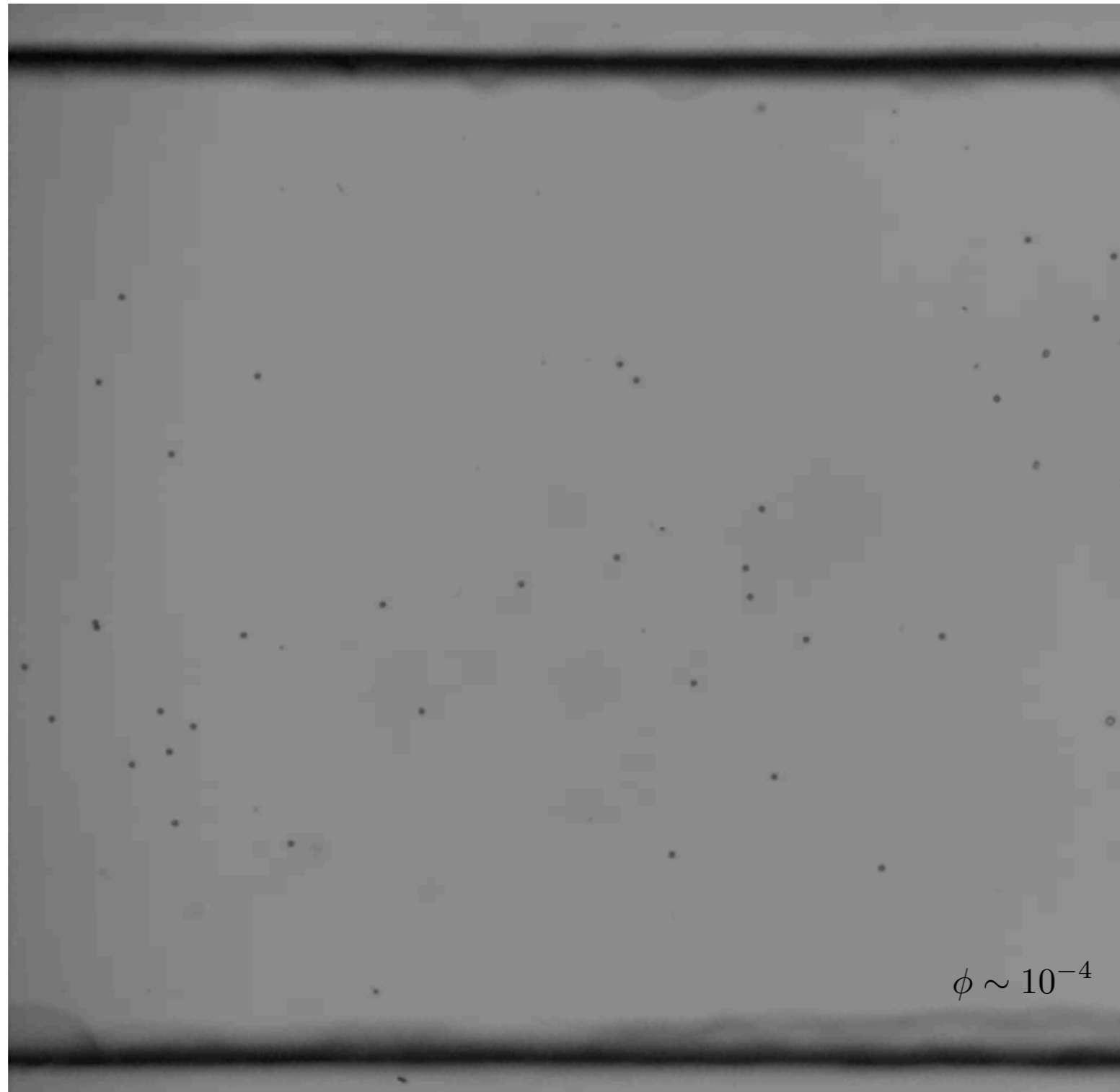
Microfluidic channel:
ITO coated glass



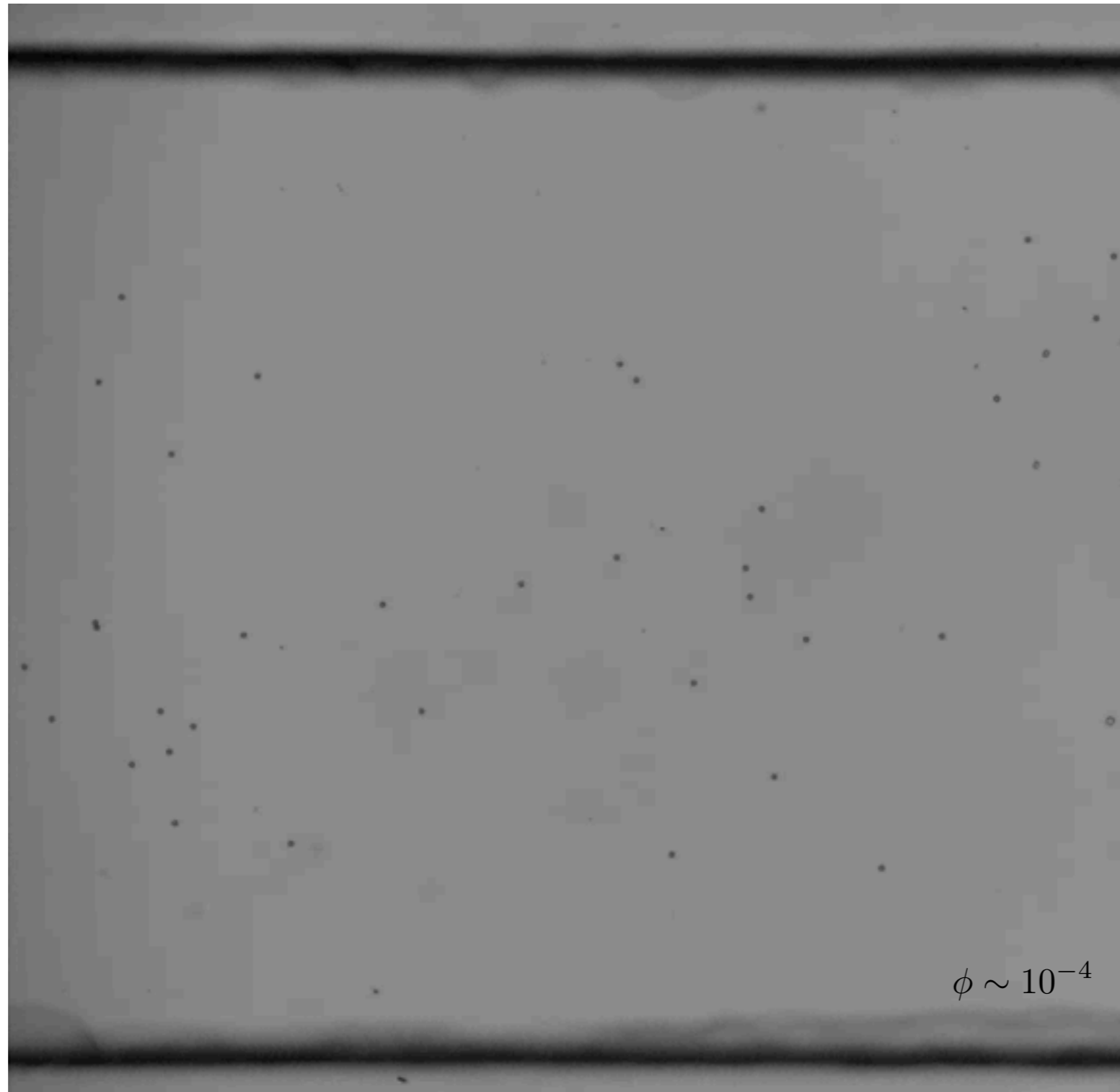
Colloidal rolling robots



Colloidal rolling robots

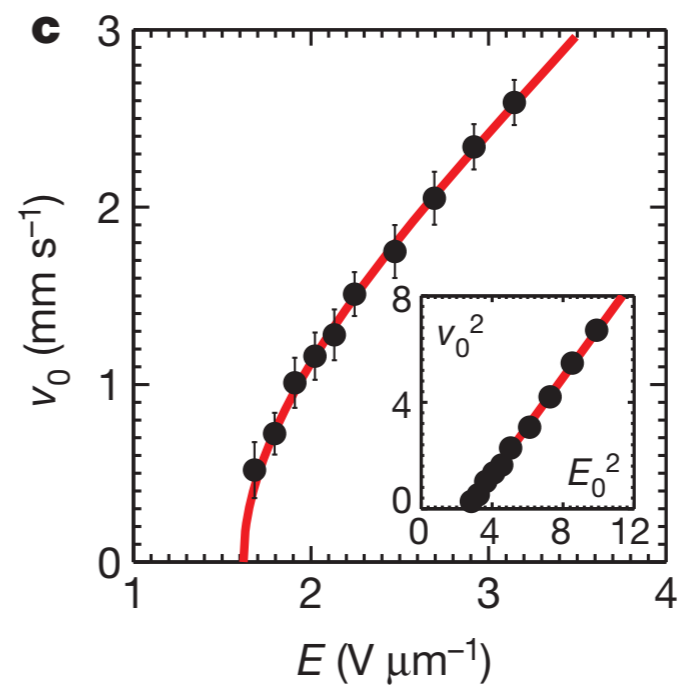
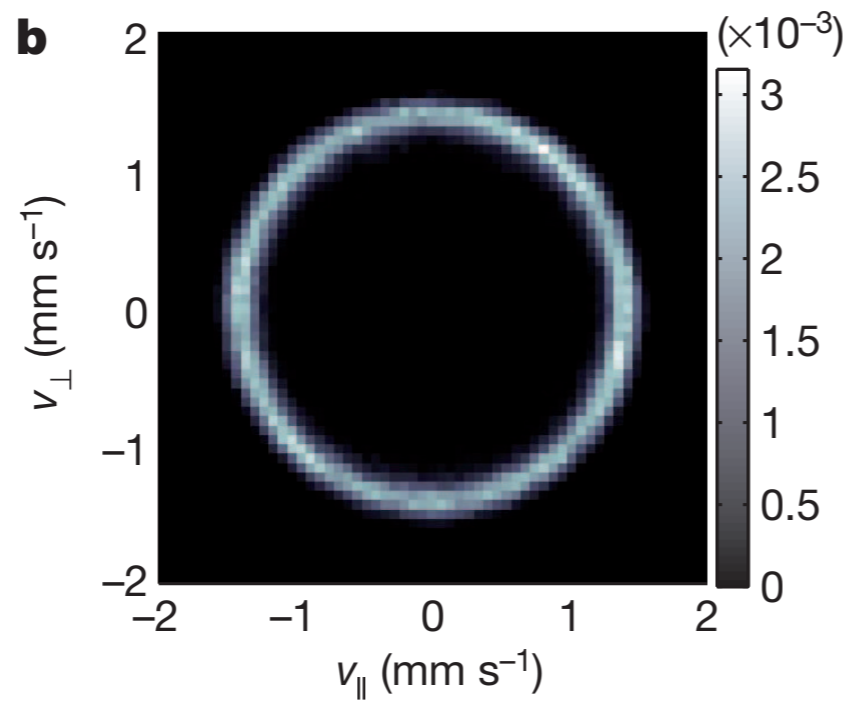


Colloidal rolling robots



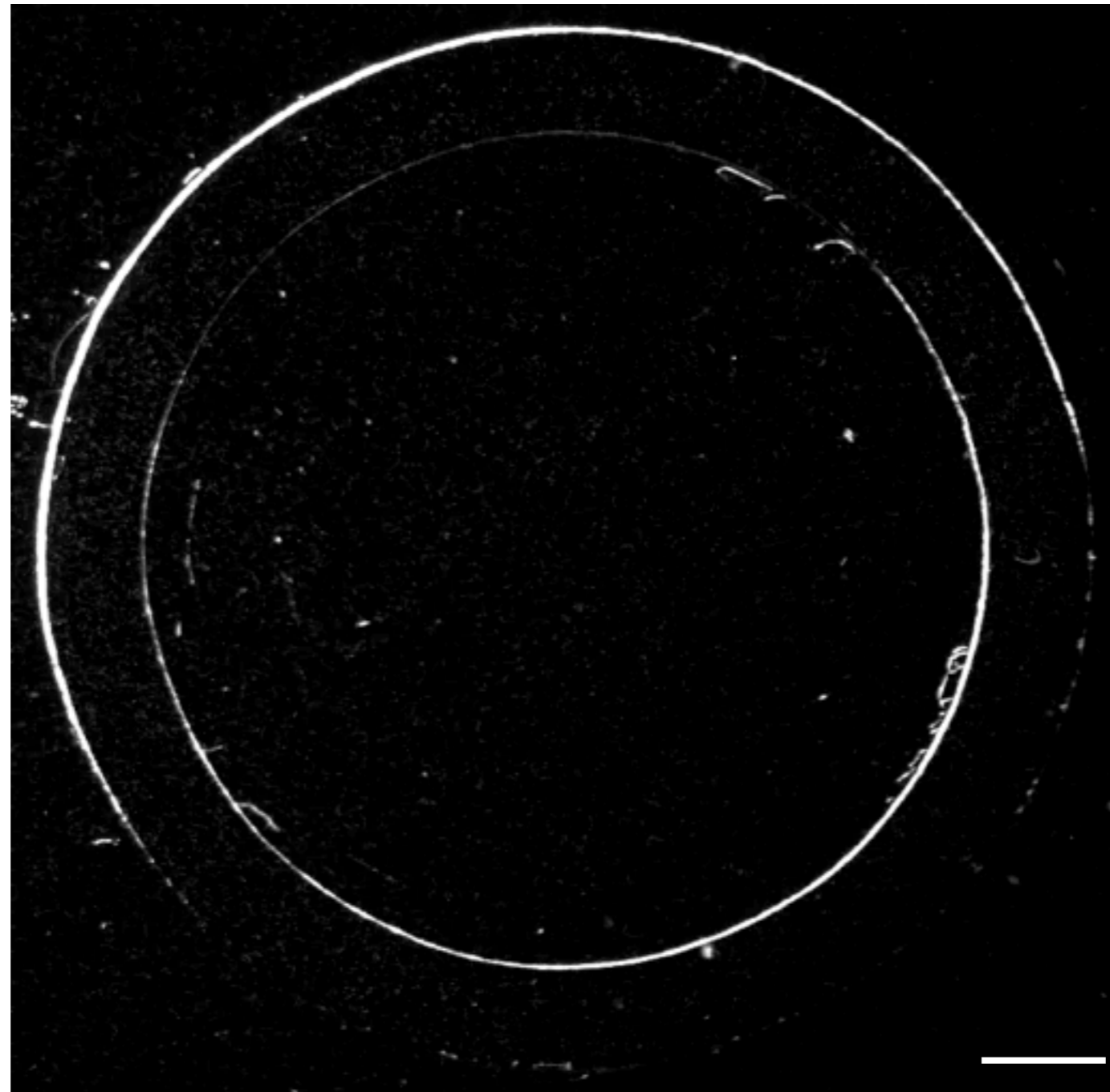
$$v_0 = 1.5 \text{ mm/s}$$

Self-propulsion: isotropic and tunable



Collective motion?

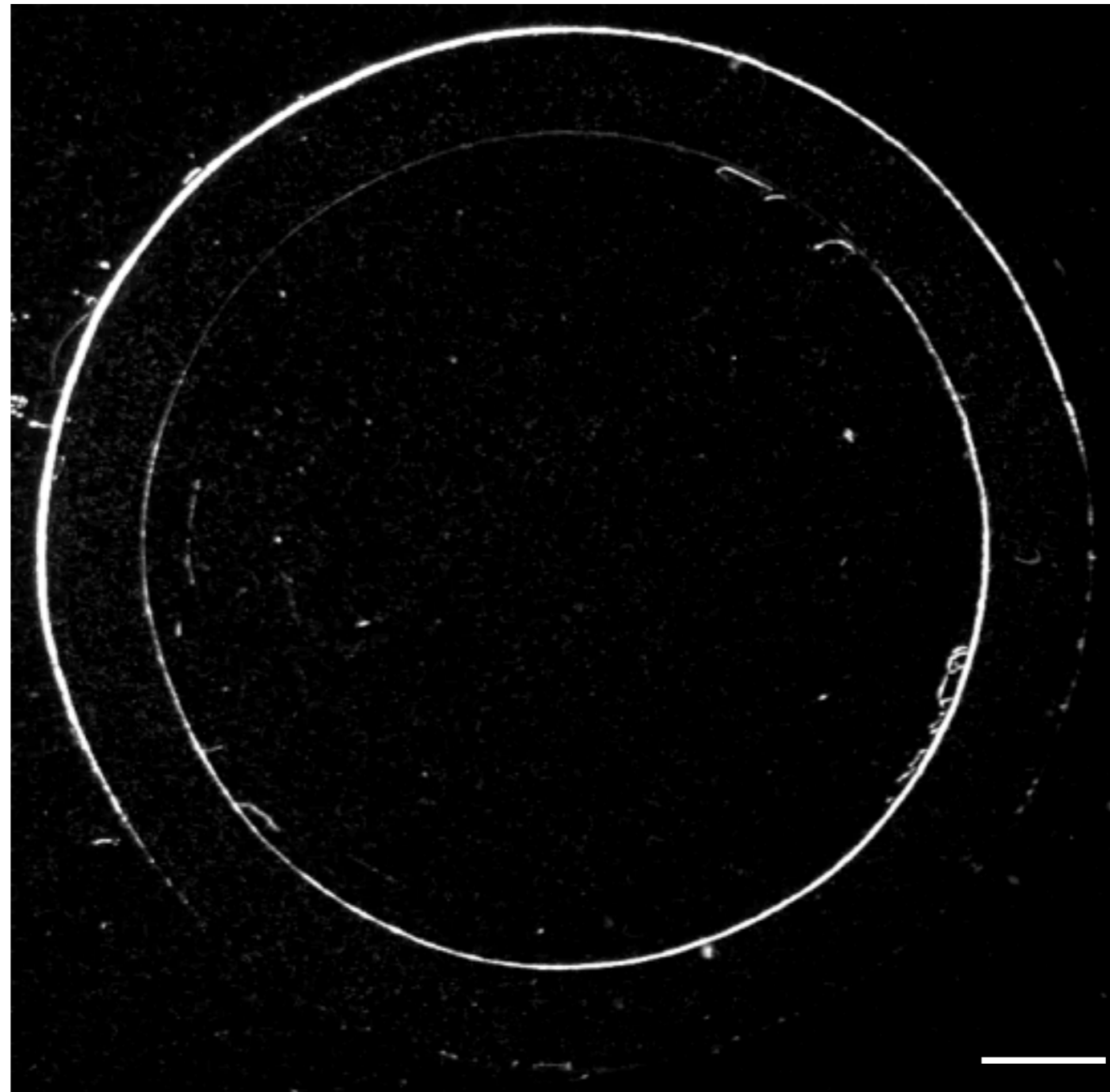
Periodic boundary conditions



1 mm

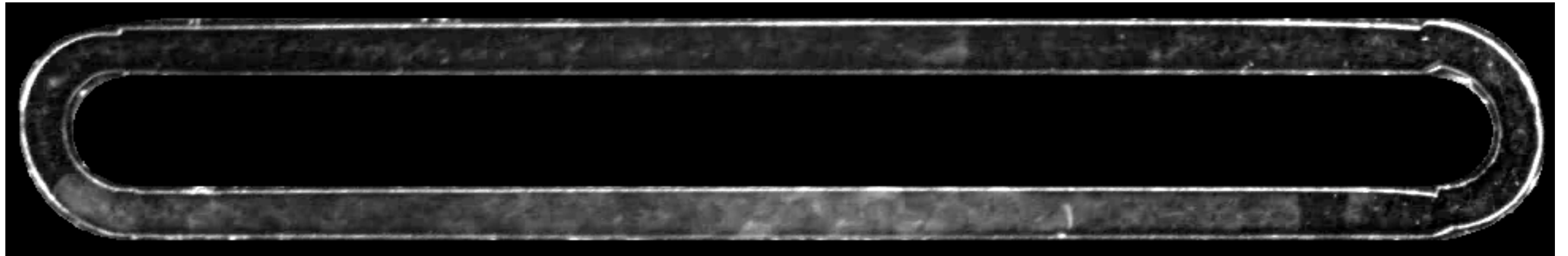
Collective motion?

Periodic boundary conditions



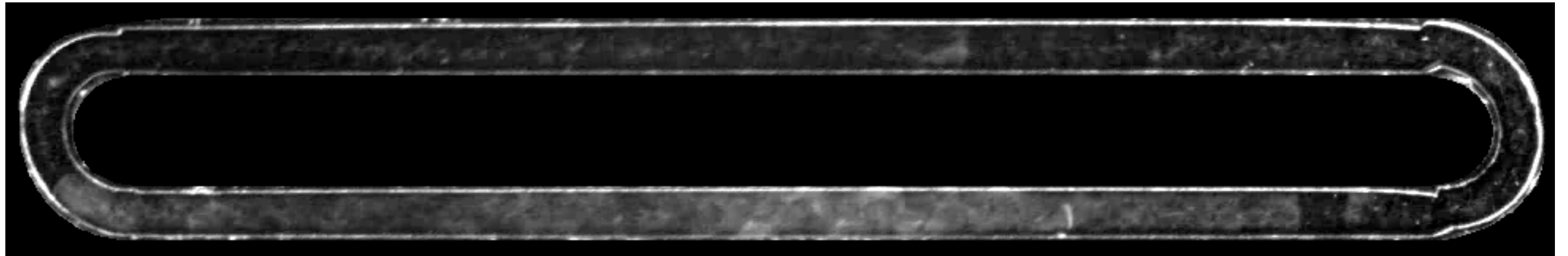
1 mm

Flocking



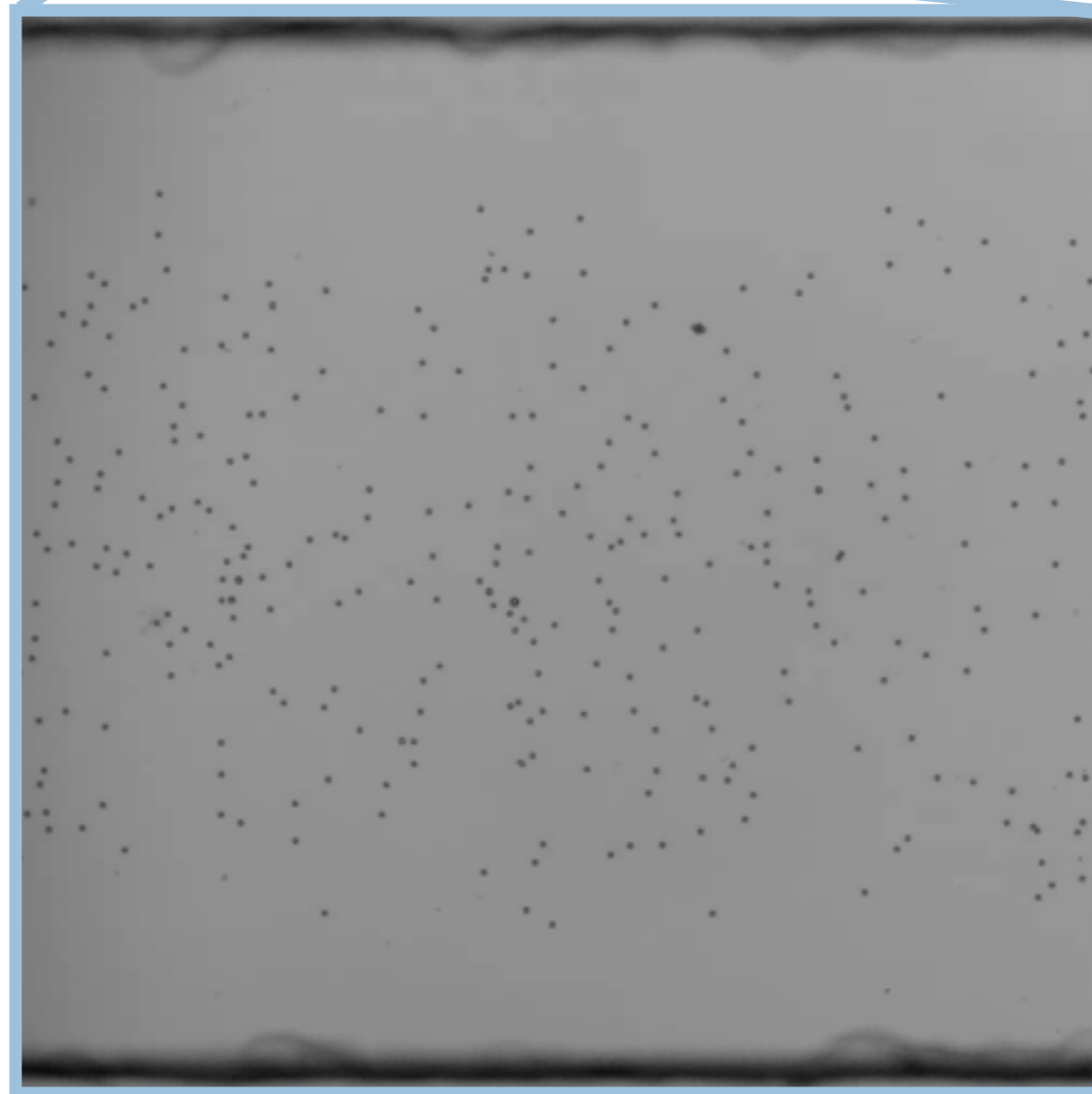
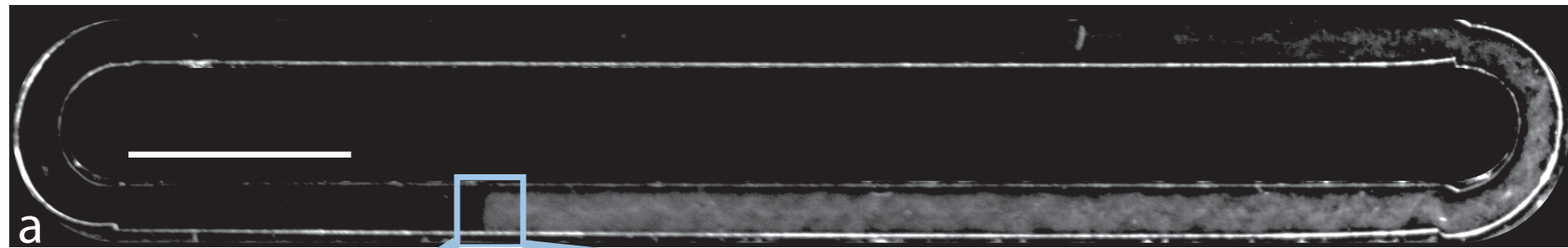
$$\phi \sim 10^{-2}$$

Flocking



$$\phi \sim 10^{-2}$$

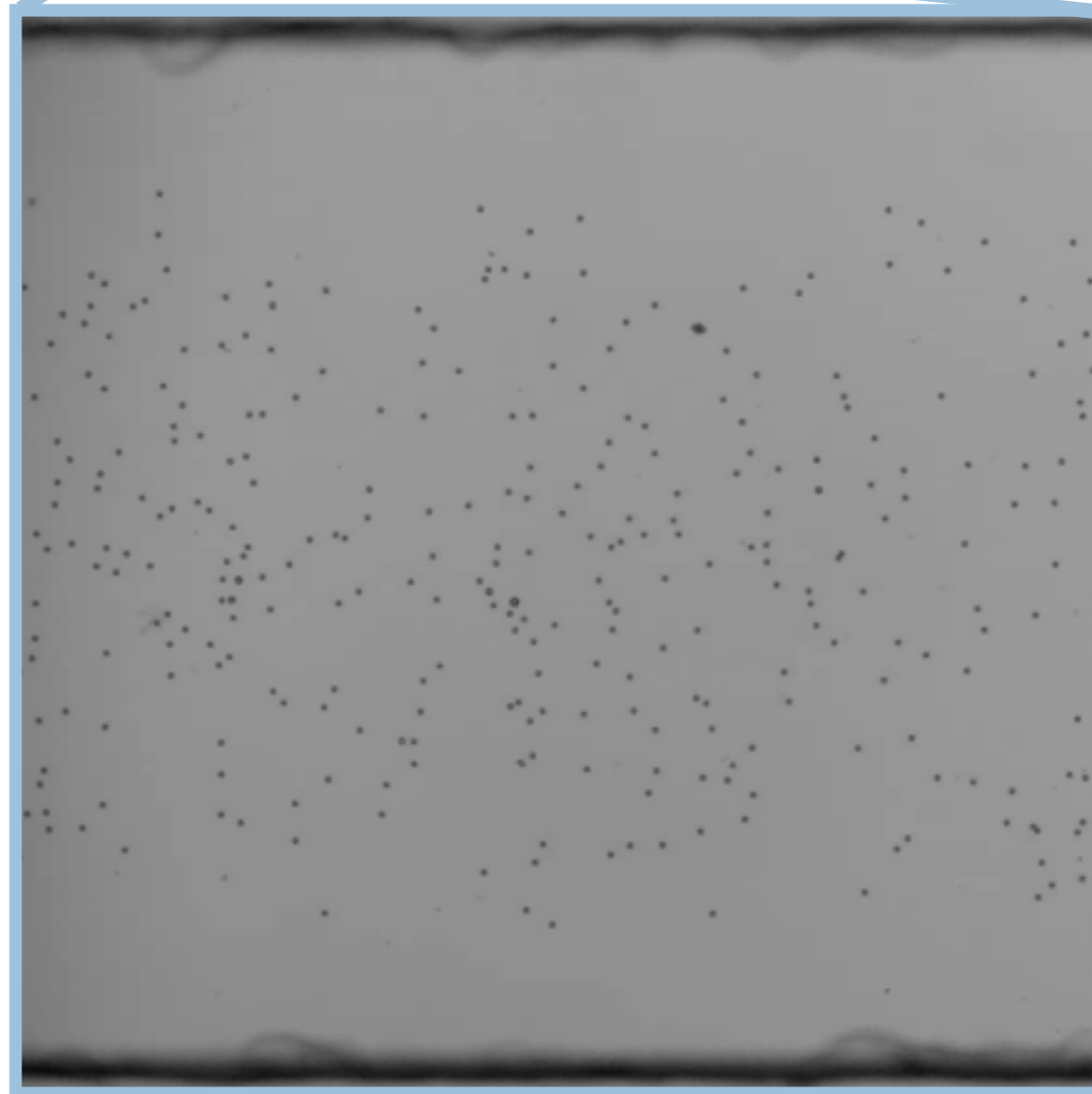
Flocking



Flocking

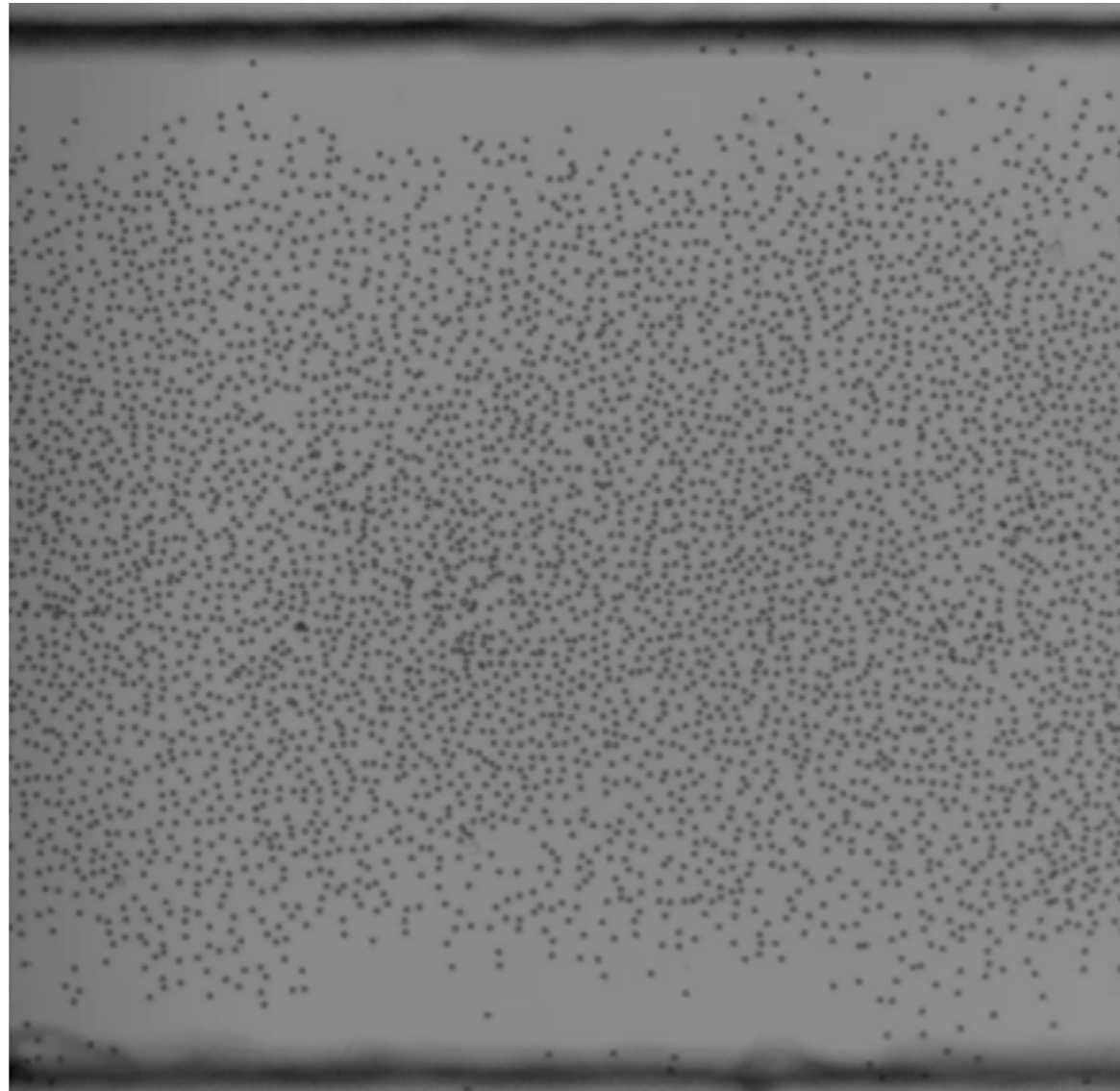


$$\phi \sim 10^{-2}$$



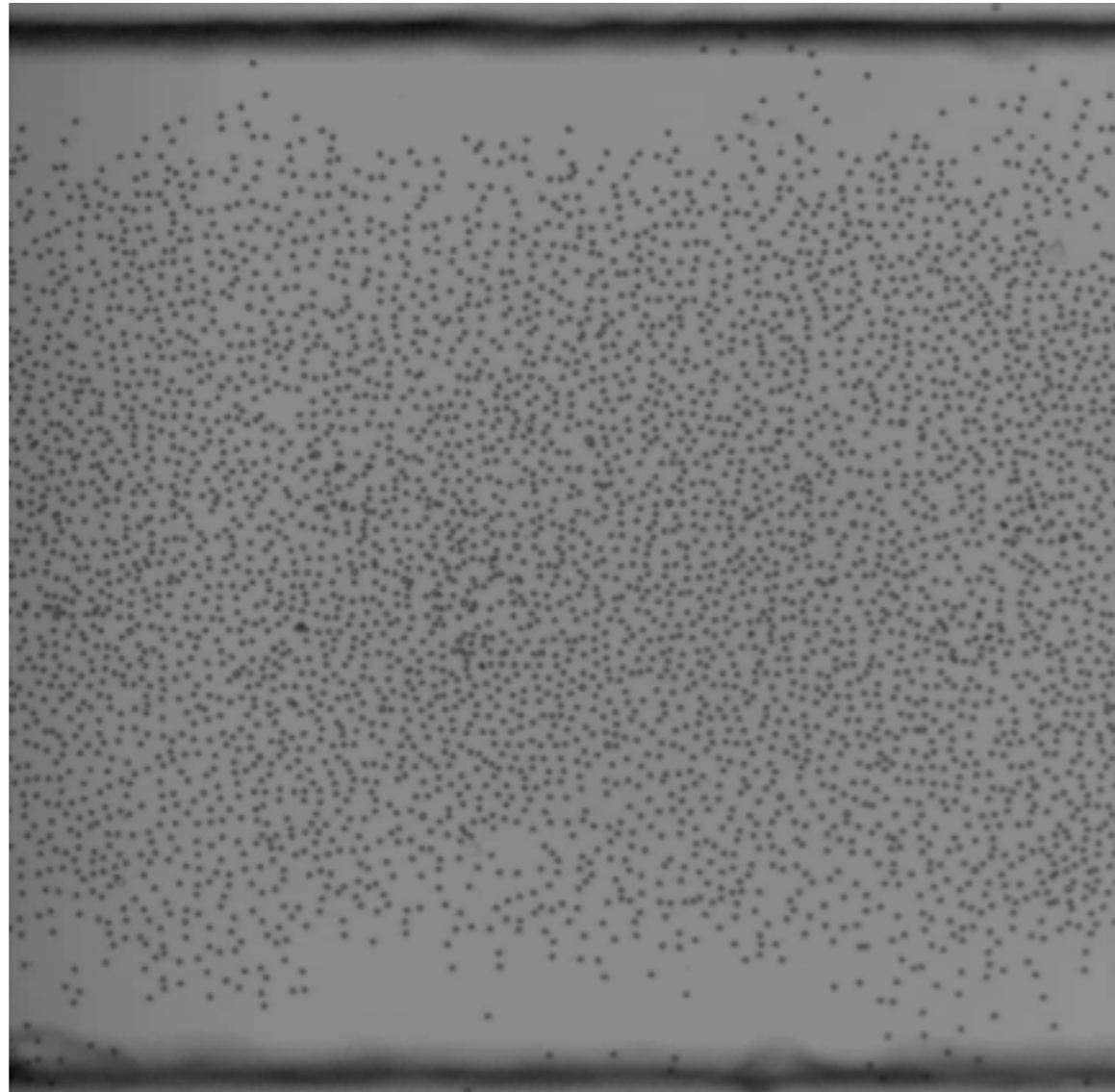
$$\phi \sim 10^{-2}$$

Polar-liquid phase



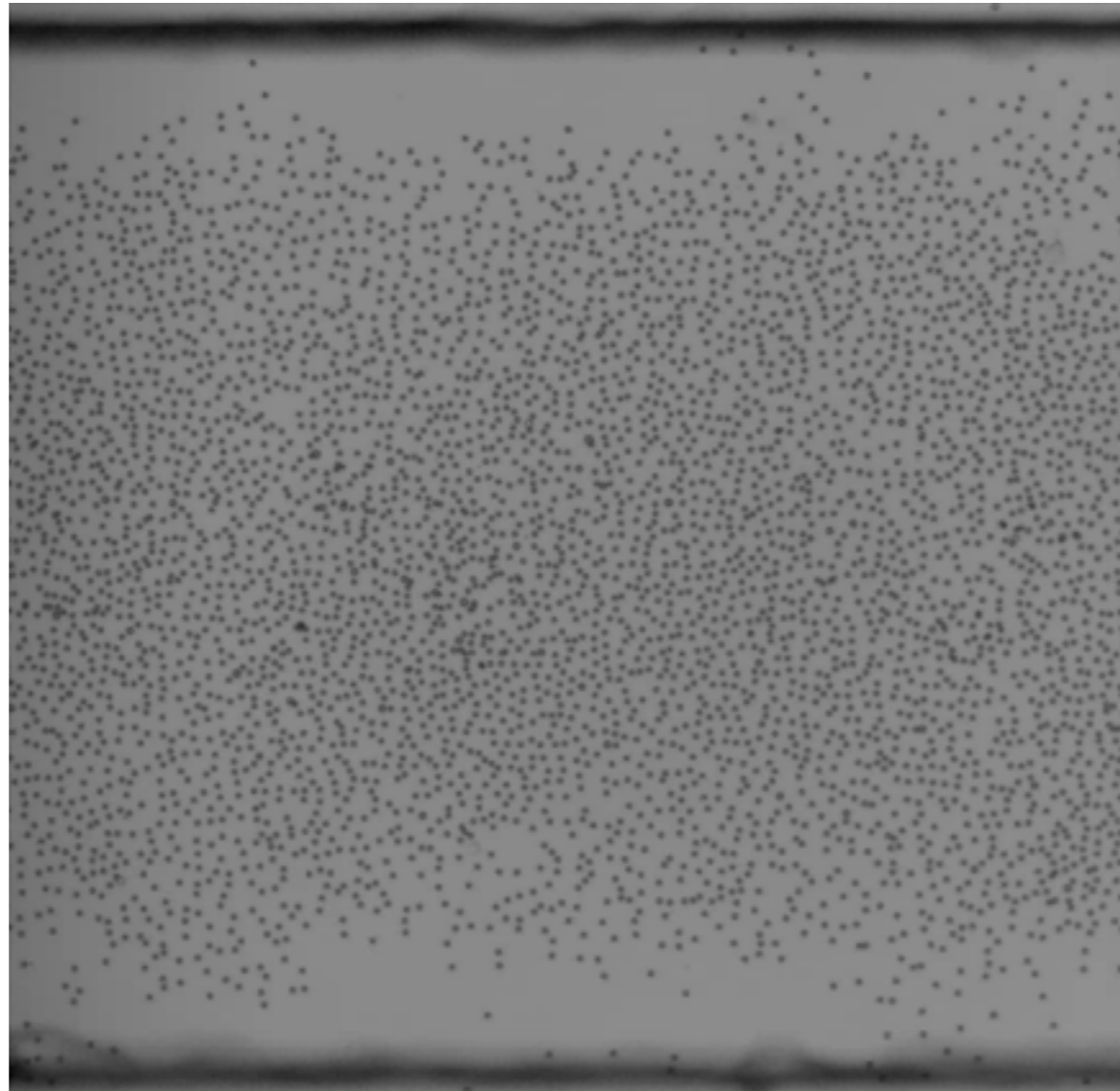
$$\phi \sim 1.8 \times 10^{-1}$$

Polar-liquid phase



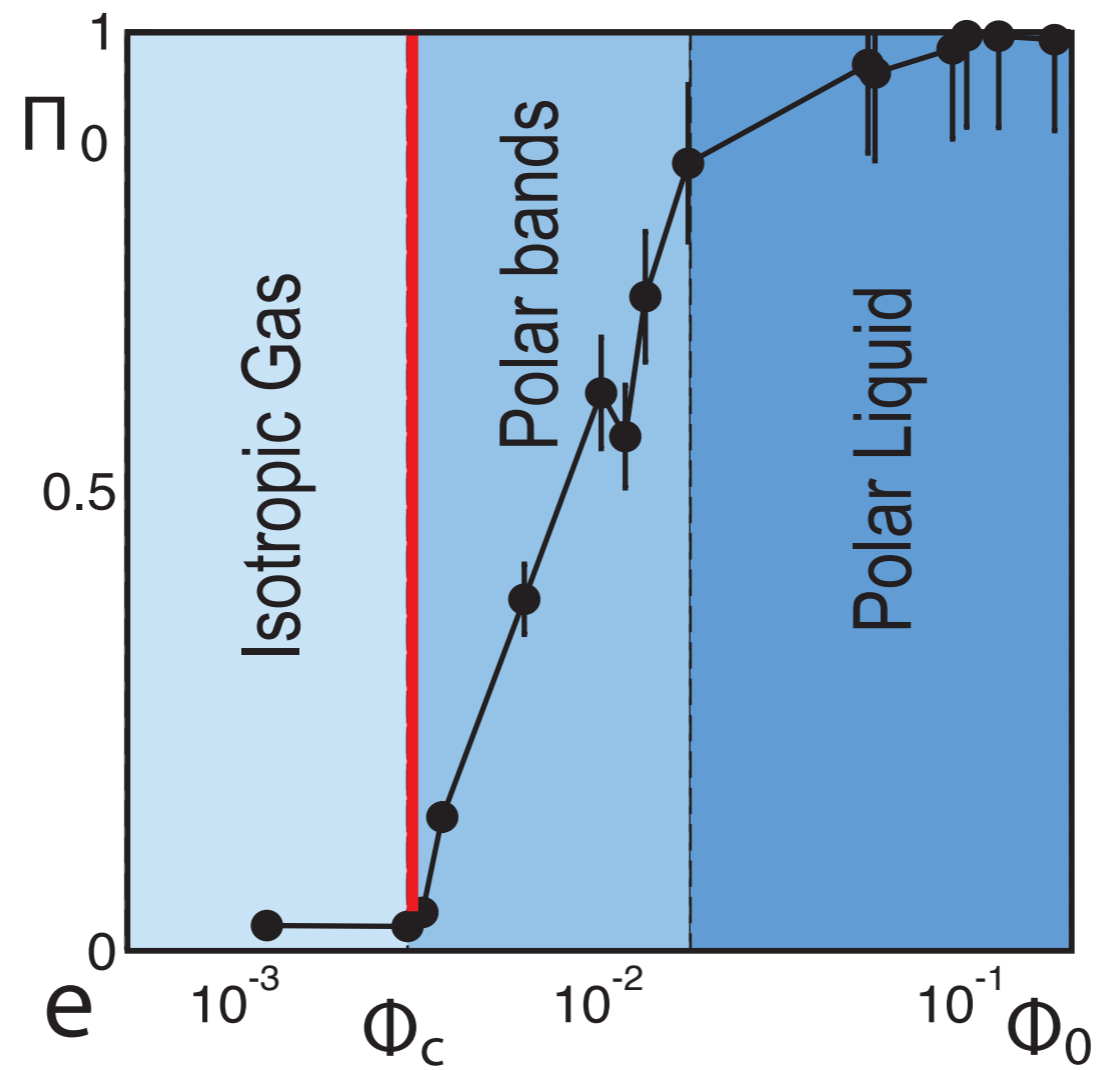
$$\phi \sim 1.8 \times 10^{-1}$$

Polar-liquid phase



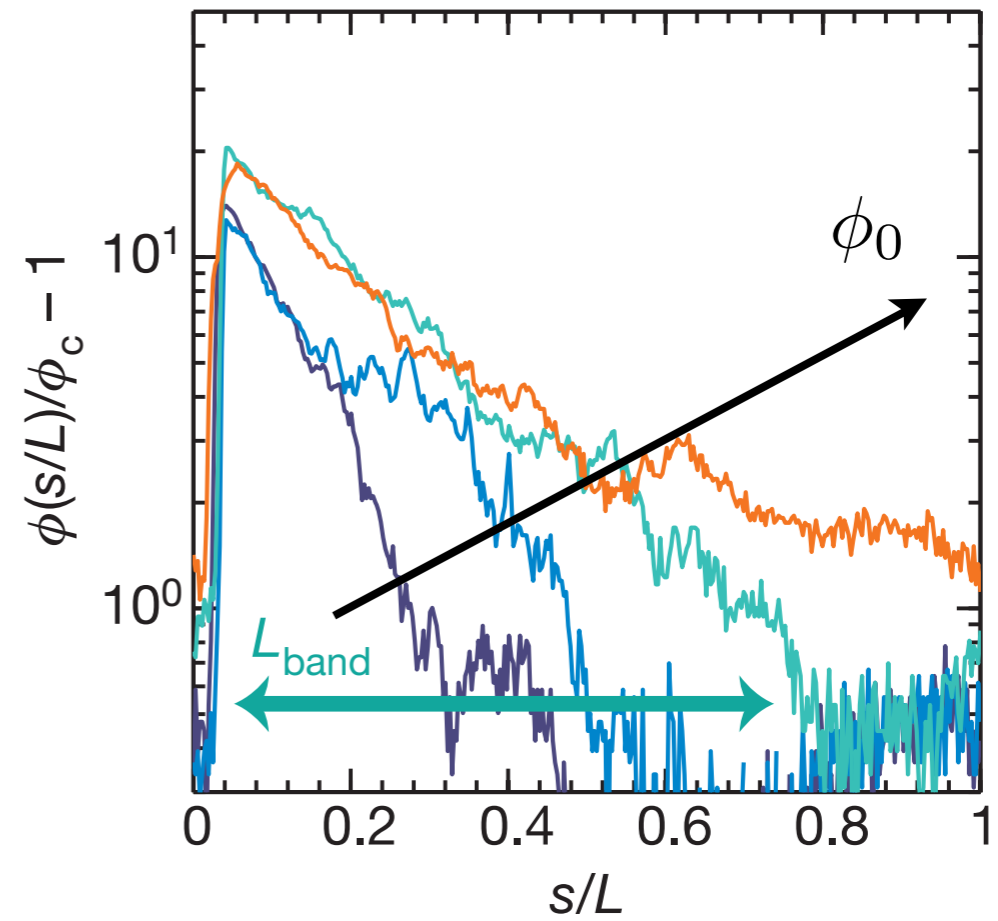
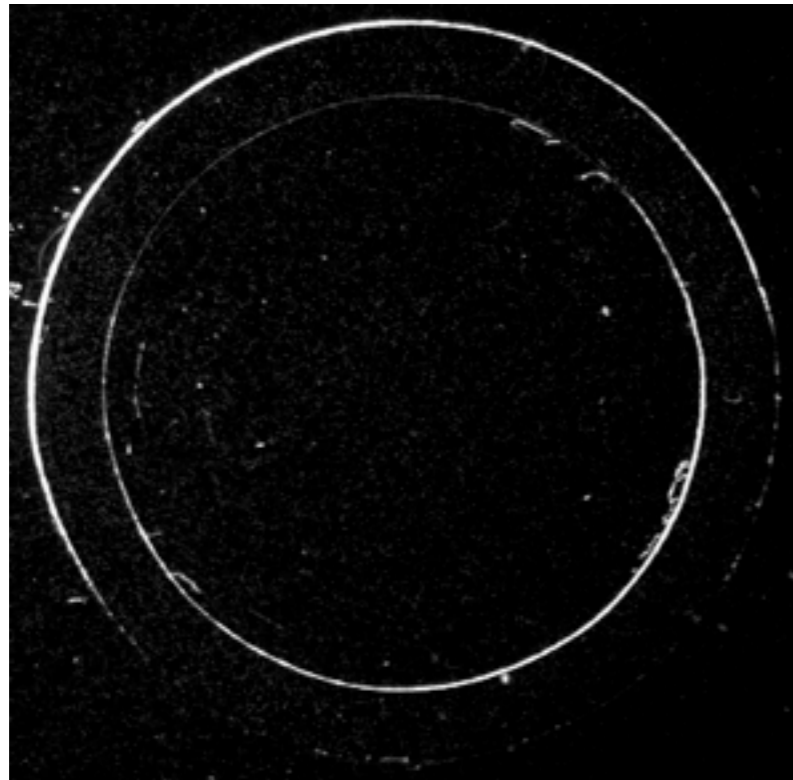
$$\phi \sim 1.8 \times 10^{-1}$$

Phase behavior



Does NOT depend on the field amplitude

Colloidal swarms: Polar bands

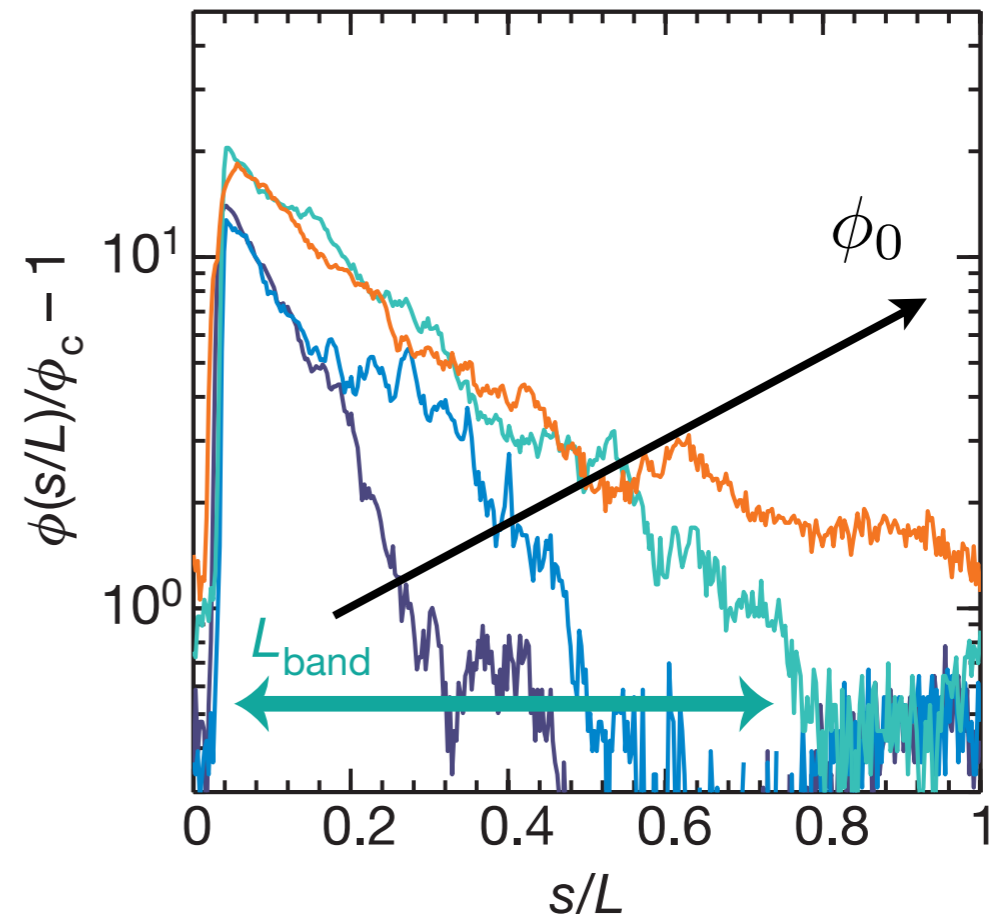
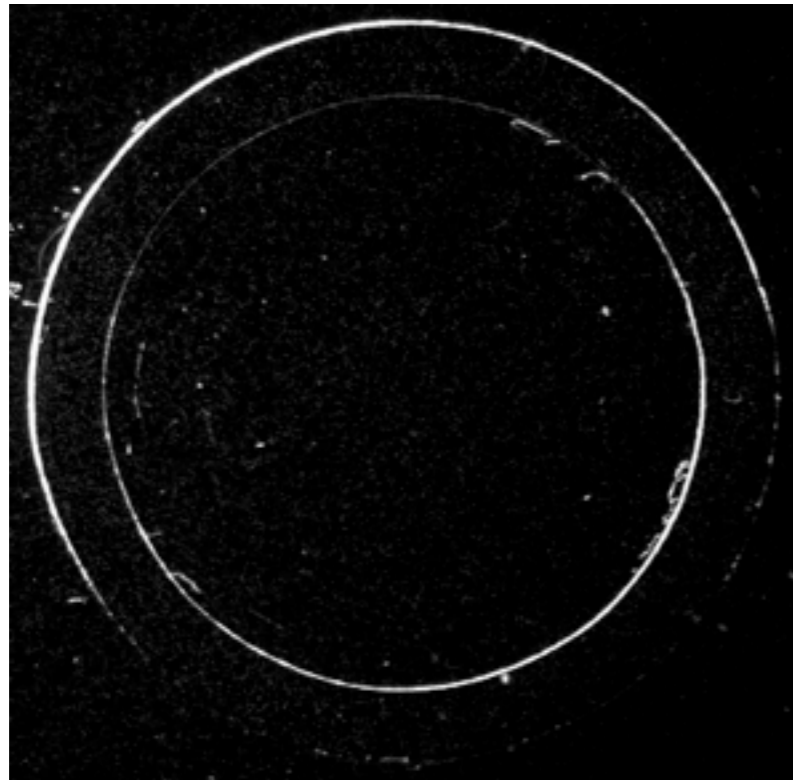


Exponential tail

$$\phi_\infty \sim \phi_c$$

$$L_{\text{band}} \nearrow \quad \phi_0 \nearrow$$

Colloidal swarms: Polar bands

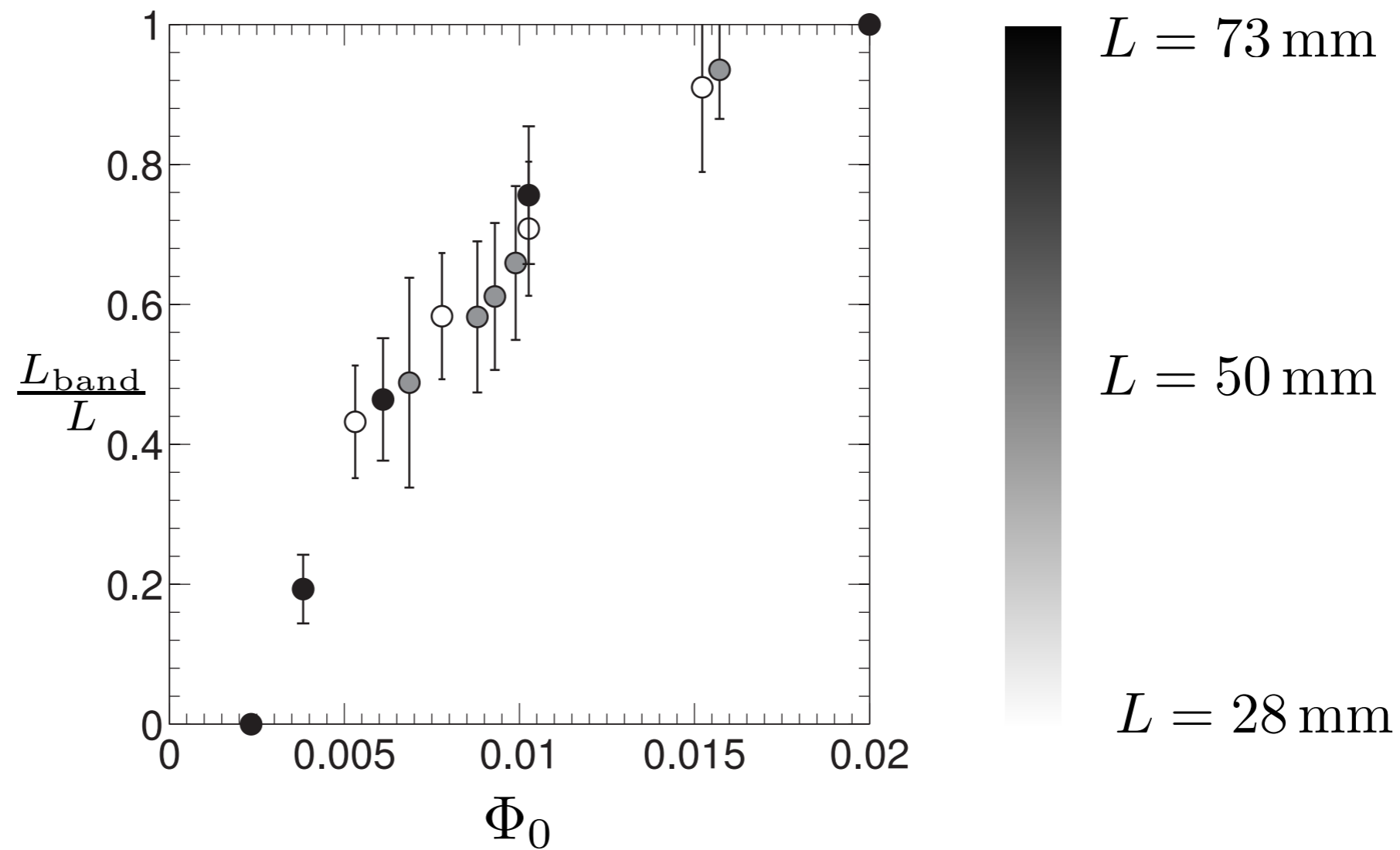


Exponential tail

$$\phi_\infty \sim \phi_c$$

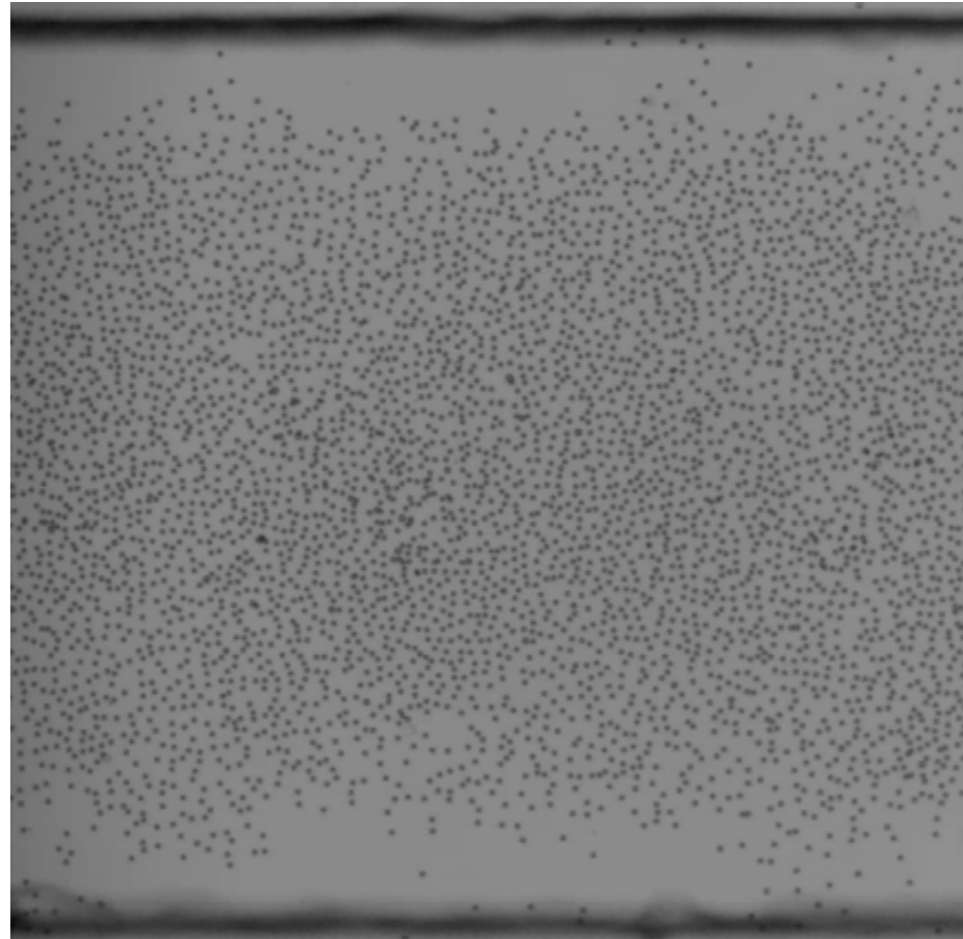
$$L_{\text{band}} \nearrow \quad \phi_0 \nearrow$$

No intrinsic length scale



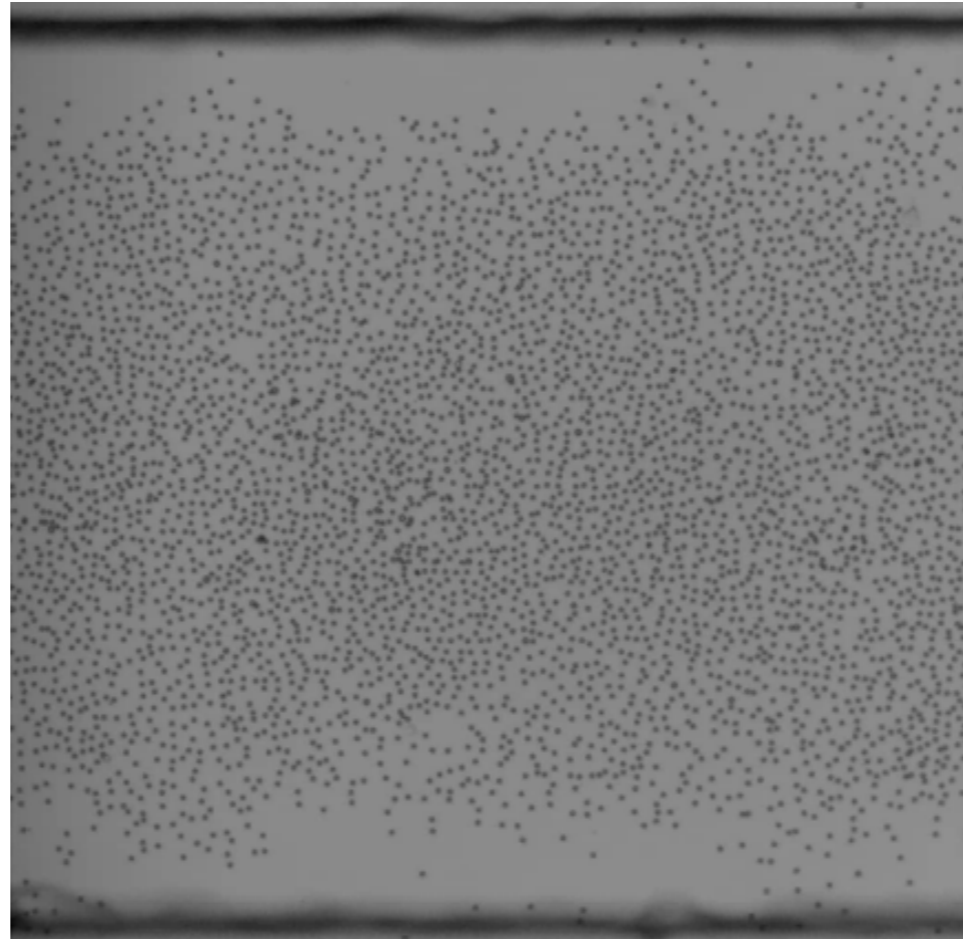
« Phase coexistence »

Polar liquid



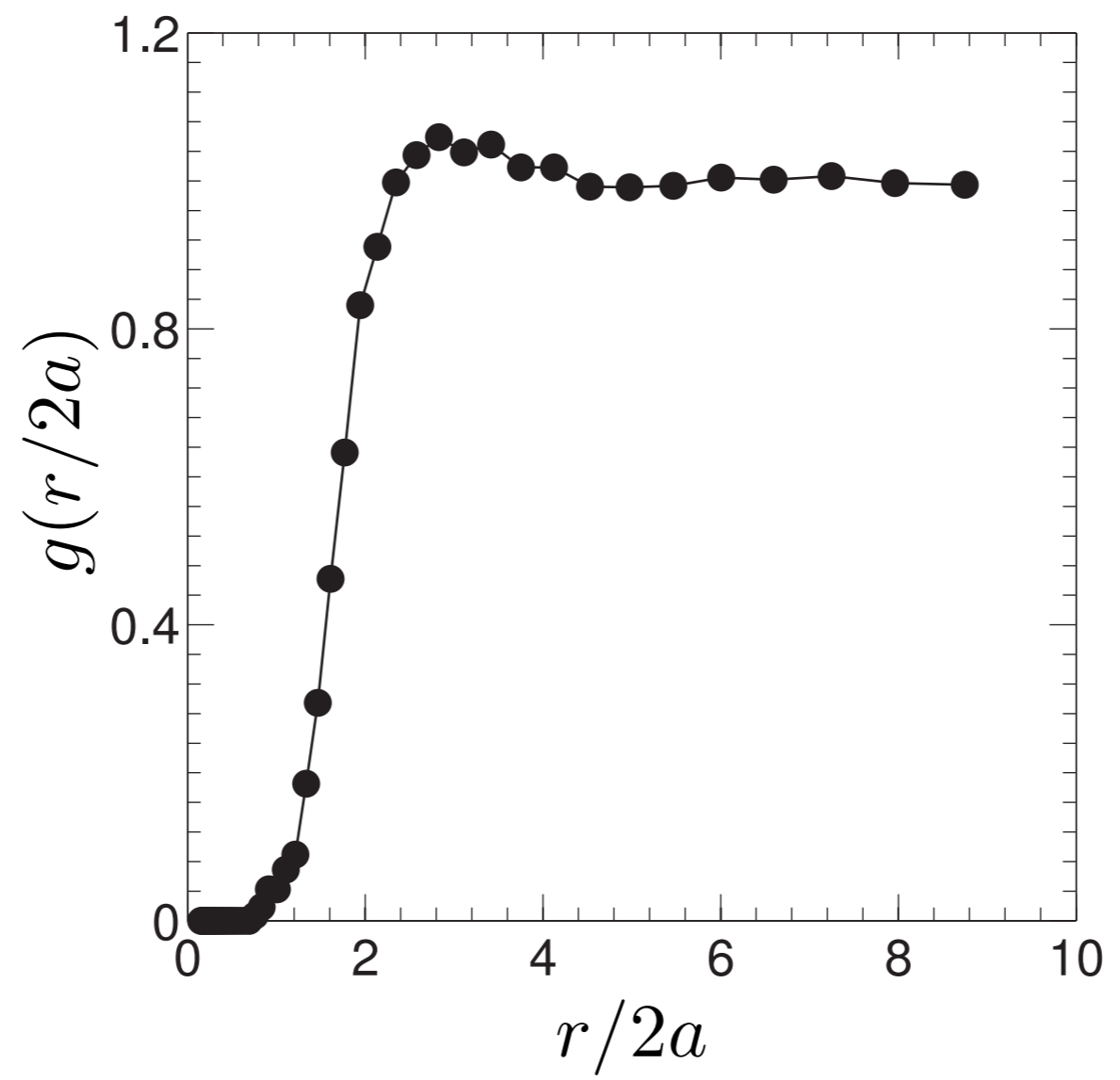
Spontaneously flowing liquid

Polar liquid



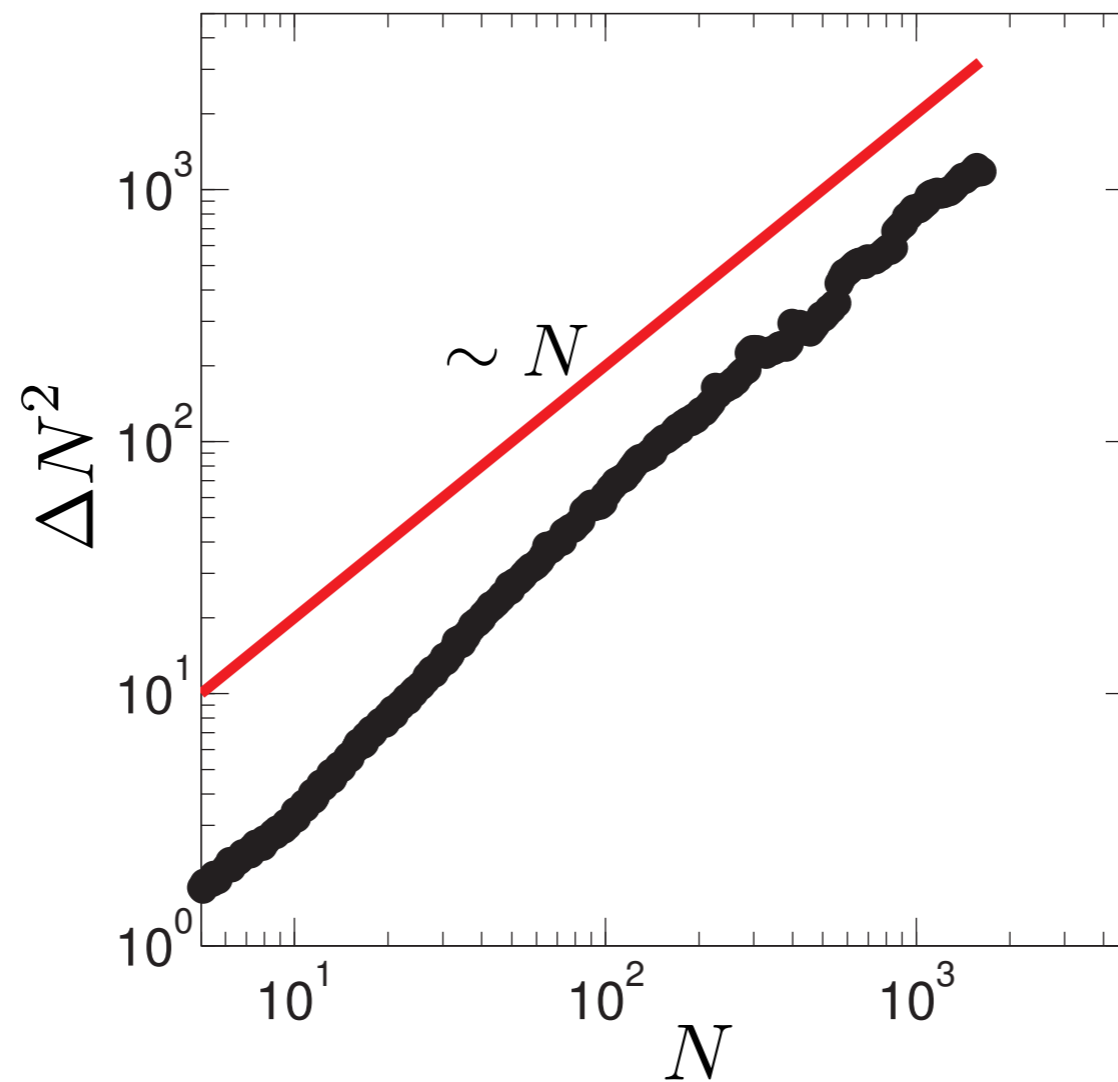
Spontaneously flowing liquid

Polar liquid: Structure



Weakly correlated "liquid"

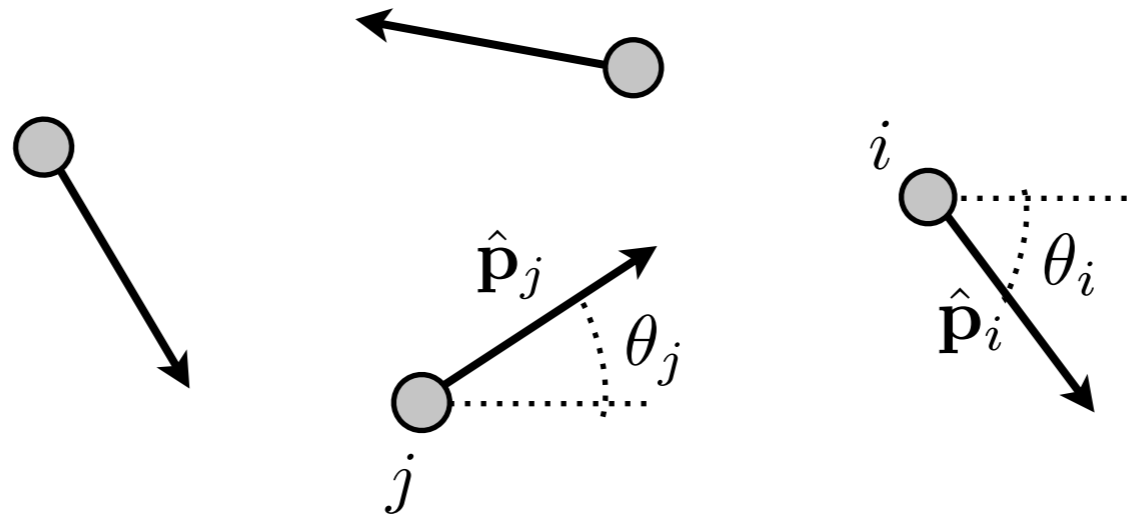
Polar liquid: Density fluctuations



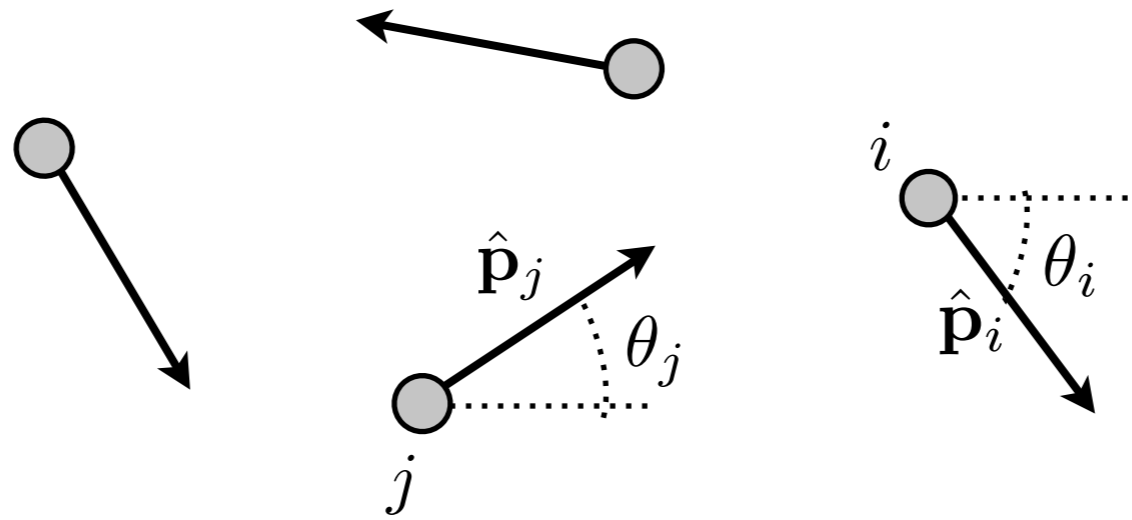
No Giant-Number Fluctuations !

Equations of motion

- Stokes equation
- + Maxwell equation
- + outstanding student



Equations of motion



$$\dot{\mathbf{r}}_j = v_0 \hat{\mathbf{p}}_j$$

constant speed

$$\dot{\theta}_j = -\frac{\partial}{\partial \theta_j} \sum_{i \neq j} \mathcal{H}_{\text{eff}}(\mathbf{r}_j - \mathbf{r}_i, \hat{\mathbf{p}}_i, \hat{\mathbf{p}}_j) + \xi_j(t)$$

effective potential interaction

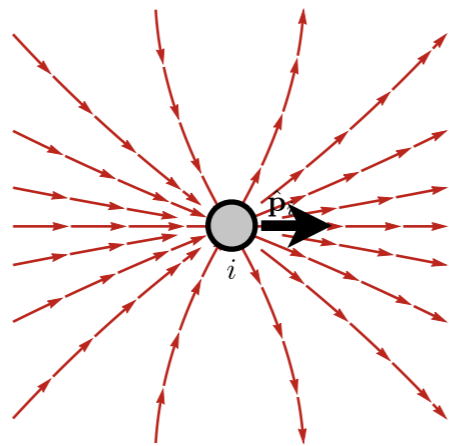
Hydrodynamics does matter

$$\dot{\mathbf{r}}_j = v_0 \hat{\mathbf{p}}_j$$

$$\dot{\theta}_j = -\frac{\partial}{\partial \theta_j} \sum_{i \neq j} \mathcal{H}_{\text{eff}}(\mathbf{r}_j - \mathbf{r}_i, \hat{\mathbf{p}}_i, \hat{\mathbf{p}}_j) + \xi_j(t)$$

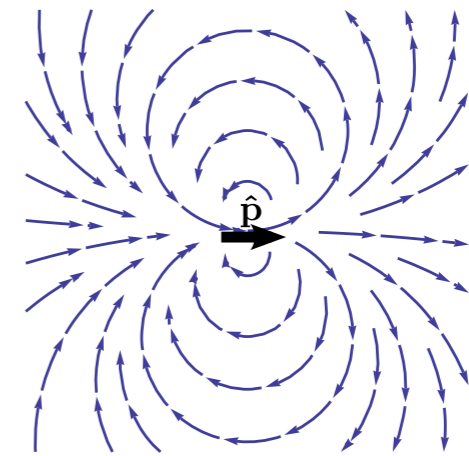
Alignment interactions

$$\mathcal{H}_{\text{eff}}(\mathbf{r}, \hat{\mathbf{p}}_i, \hat{\mathbf{p}}_j) = -A(r) \hat{\mathbf{p}}_i \cdot \hat{\mathbf{p}}_j - B(r) \hat{\mathbf{r}} \cdot \hat{\mathbf{p}}_j - C(r) \hat{\mathbf{p}}_i \cdot (2\hat{\mathbf{r}}\hat{\mathbf{r}} - \mathbf{I}) \cdot \hat{\mathbf{p}}_j$$



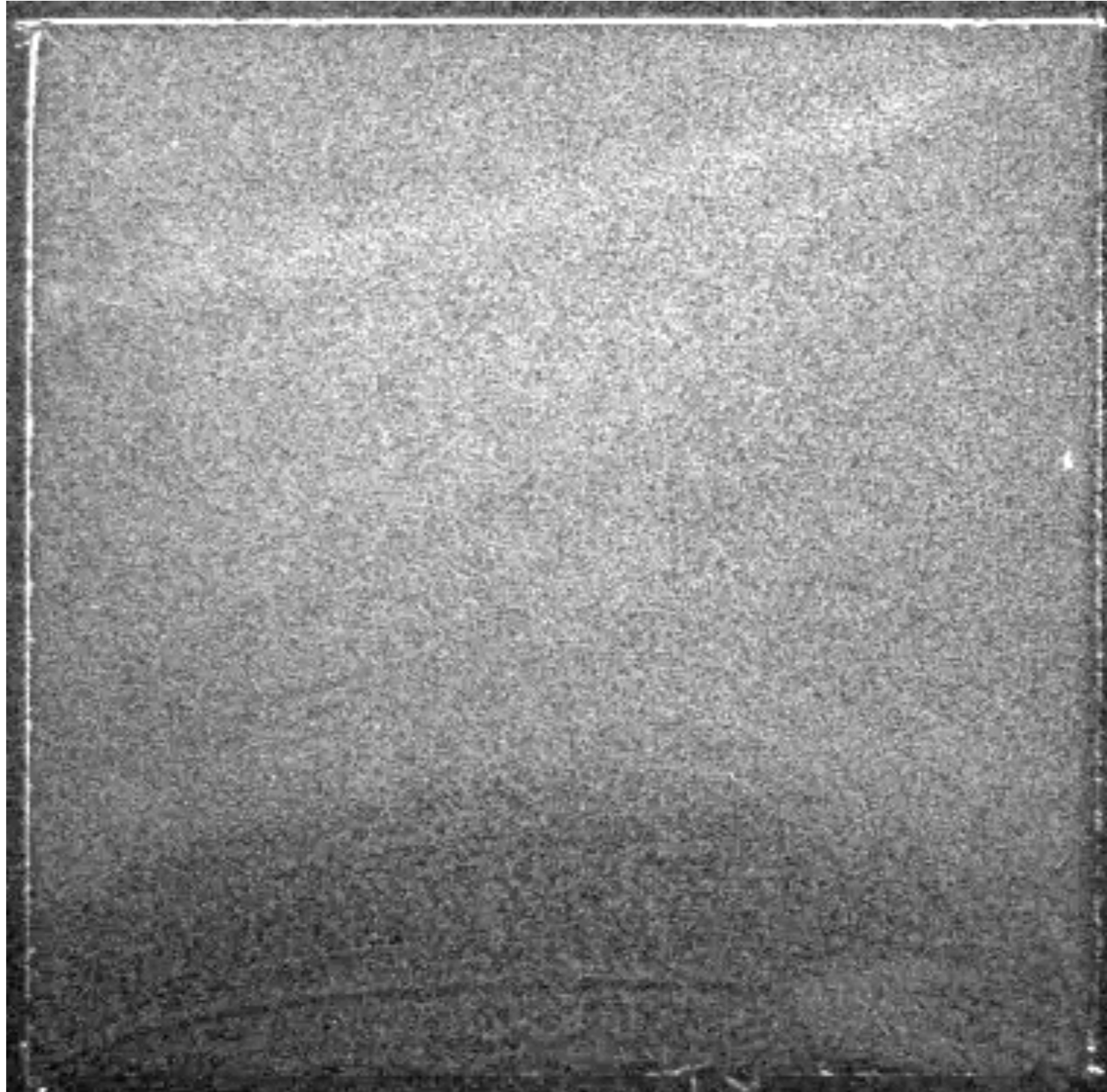
Suppression of the giant number fluctuations

$$\mathcal{H}_{\text{eff}}(\mathbf{r}, \hat{\mathbf{p}}_i, \hat{\mathbf{p}}_j) = -A(r) \hat{\mathbf{p}}_i \cdot \hat{\mathbf{p}}_j - B(r) \hat{\mathbf{r}} \cdot \hat{\mathbf{p}}_j - C(r) \hat{\mathbf{p}}_i \cdot (2\hat{\mathbf{r}}\hat{\mathbf{r}} - \mathbf{I}) \cdot \hat{\mathbf{p}}_j$$

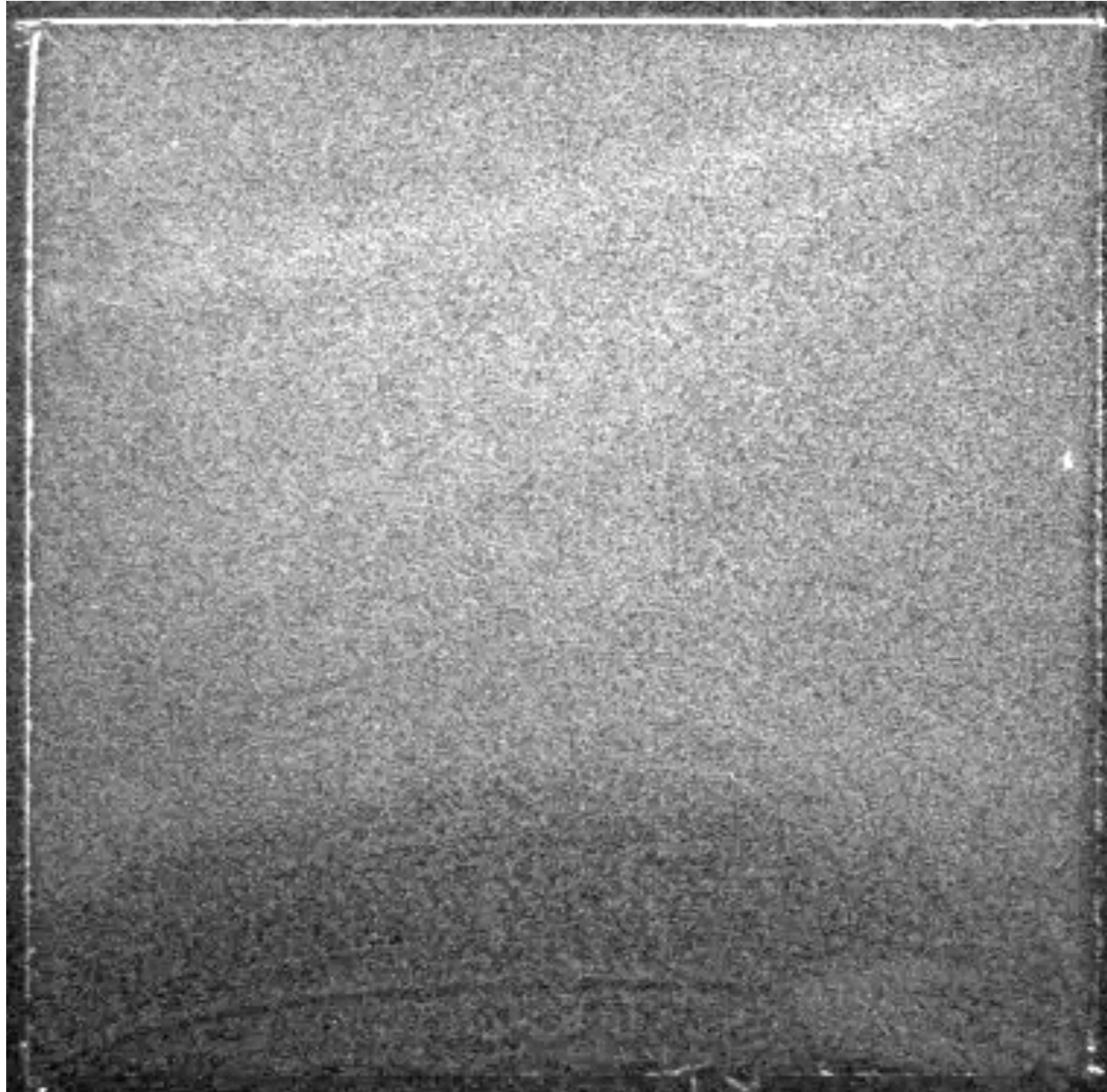


Damping of the splay modes

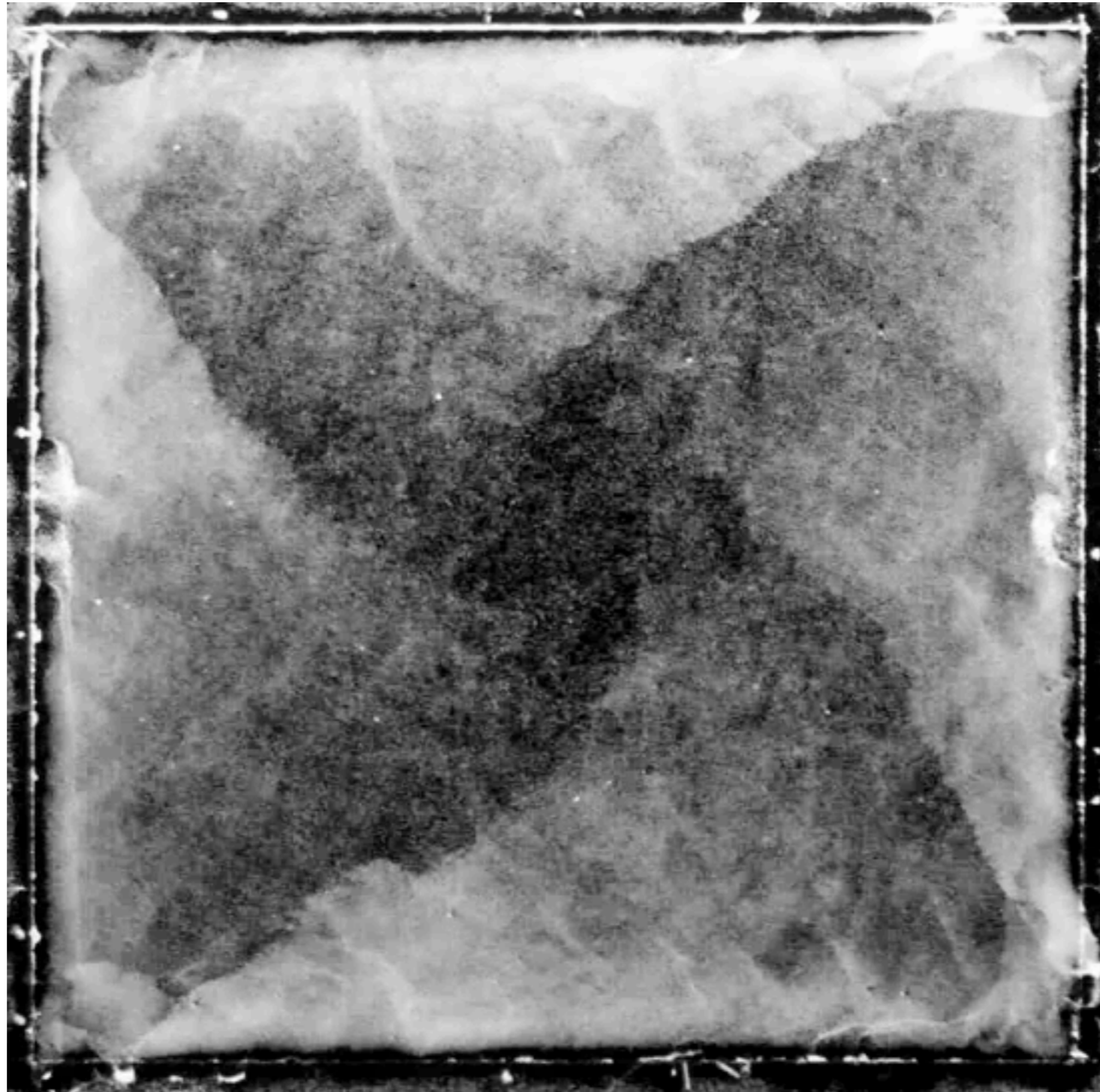
Destroying the polar liquid phase



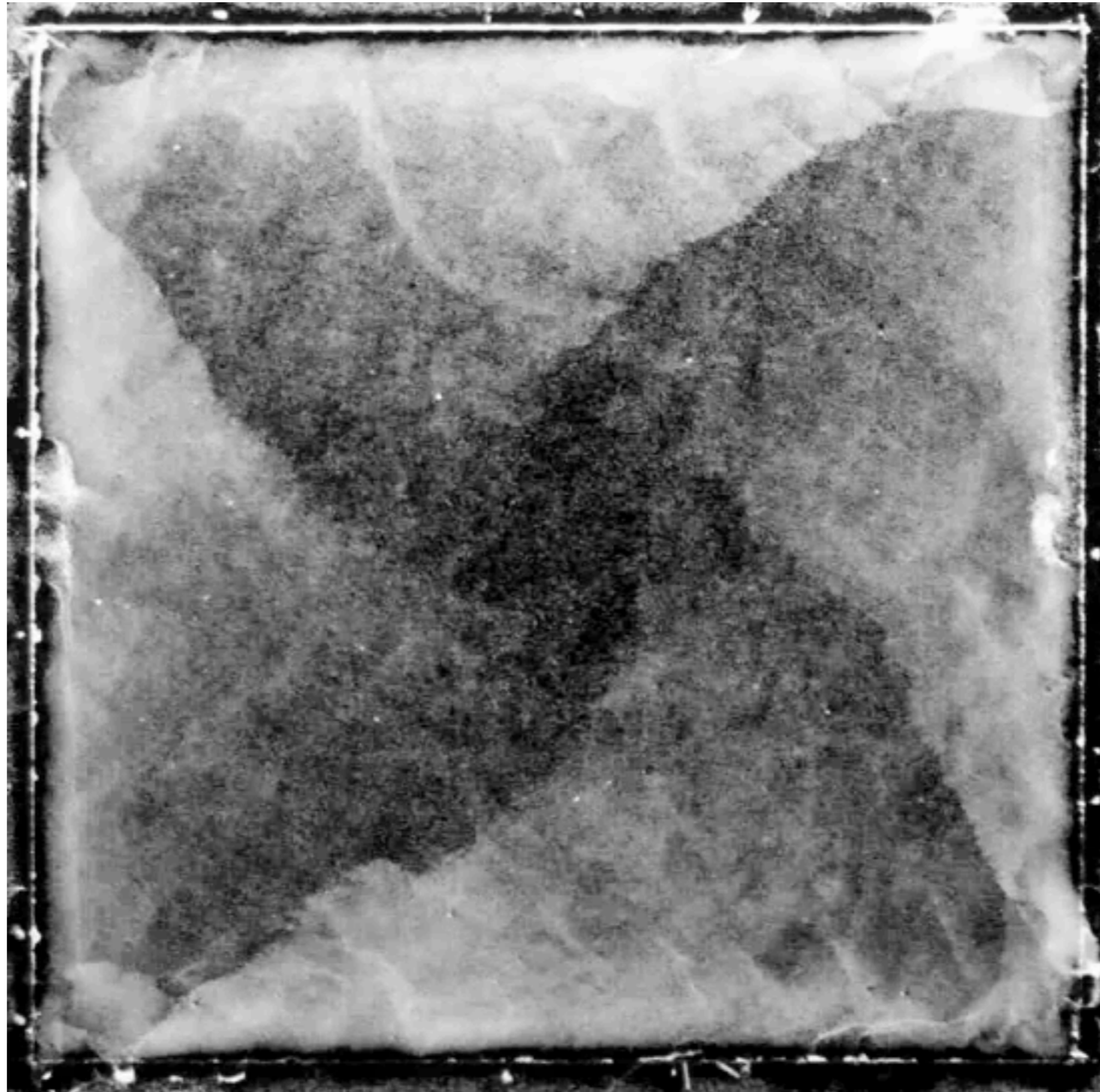
Destroying the polar liquid phase



Destroying the polar liquid phase



Destroying the polar liquid phase



with

Antoine Bricard

(Experiments)

Jean-Baptiste Caussin

(Theory)

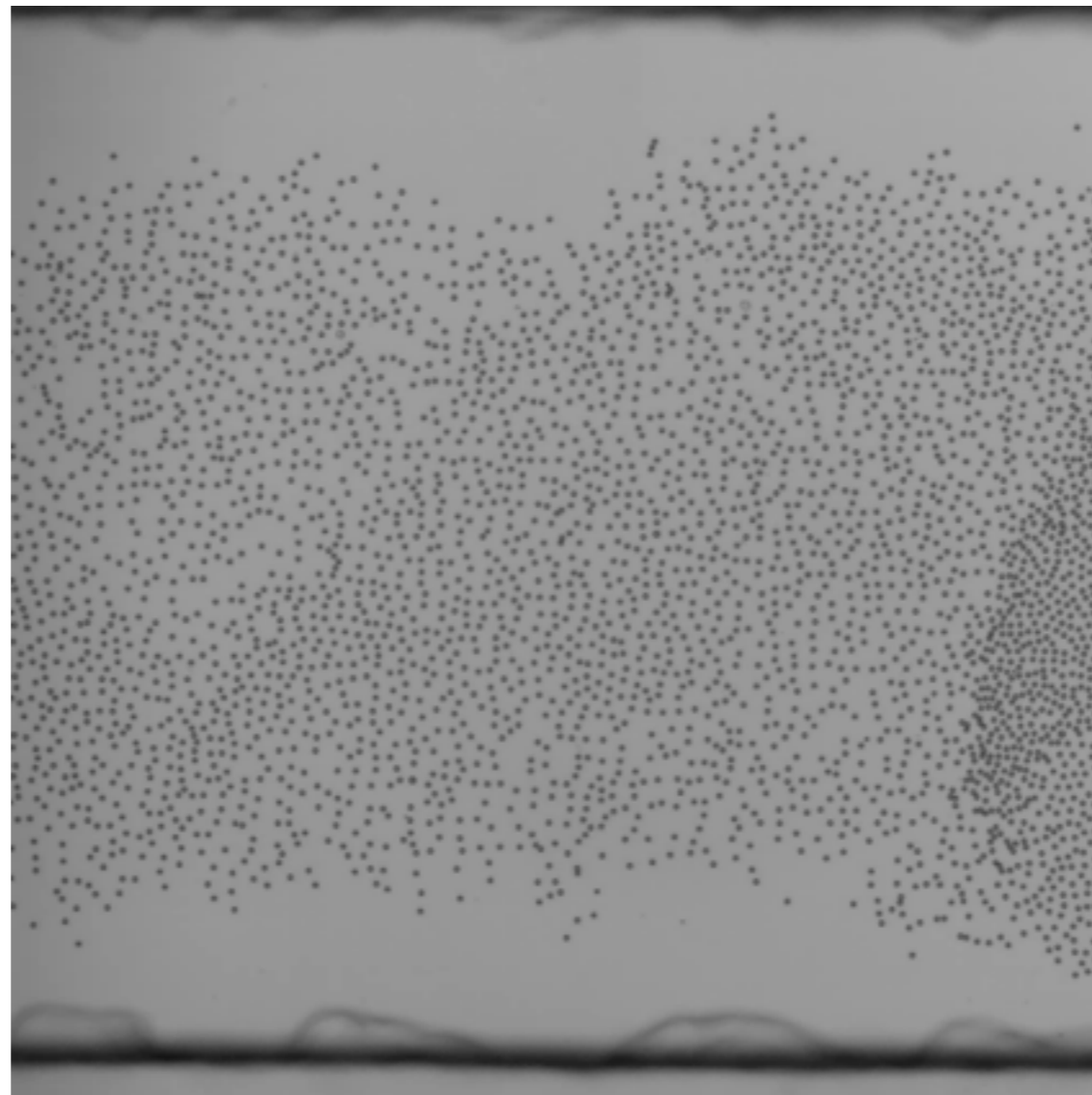
Nicolas Desreumaux

(Experiments)

&

Olivier Dauchot

(EC2M, ESPCI)



with

Antoine Bricard

(Experiments)

Jean-Baptiste Caussin

(Theory)

Nicolas Desreumaux

(Experiments)

&

Olivier Dauchot

(EC2M, ESPCI)

