# Living clusters and crystals from low-density suspensions of active colloids

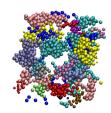






Universidad Complutense de Madrid KITP, 13Th of February 2014

#### Outline



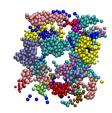
✓ Active colloids

✓ Self-assembly of active colloids

✓ What happens in a bacteria & polymer mixture?

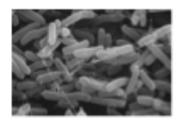
✓ Can we make living clusters of active colloids in low concentrated suspensions?

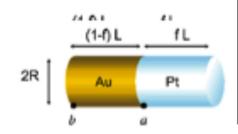


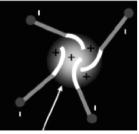


active colloids: absorb energy from their surroundings or from an internal fuel and dissipate it while moving around

examples: living bacteria, self-propelled colloids, synthetic centrosomes







Ramaswamy (2004) & Marchetti (2013)

a suspension of active colloids is driven out of equilibrium by its active nature

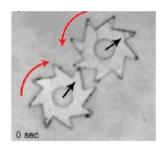


#### Why?

#### Technologically relevant

active colloids can be used to self-assemble novel smart materials, that could perform tasks such as

produce energy



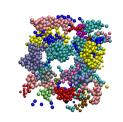
perform directional motion
Di LeonardoPNAS (2009)

"Fundamentally" relevant

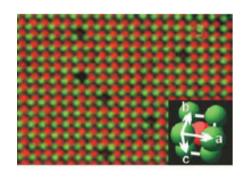
Sokolov PNAS (2009)

the Physics of a suspension of intrinsically out of equilibrium systems still needs to be fully understood

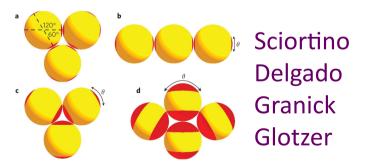
# Self-assembly in Soft Matter (passive colloids)



#### Oppositely charged colloids

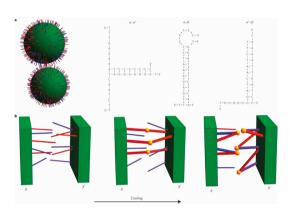


Leunissen, Dijkstra,
van Blaaderen
Patchy colloids

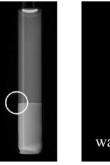


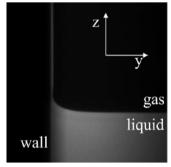
DNA-coated colloids

Frenkel&Eiser Pine&Chaikin



#### Colloid&Polymer mixture

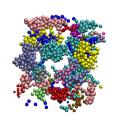




Aarts & Lekkerkerker

What happens in a suspension of active colloids?





#### The team:

University of Edinburgh



Wilson Poon





Mike Cates

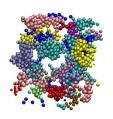
Davide Marenduzzo

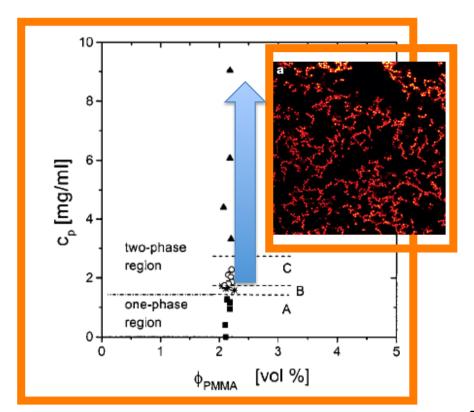


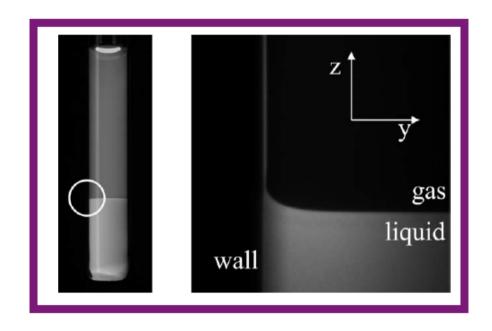
Columbia University

Angelo Cacciuto





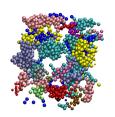


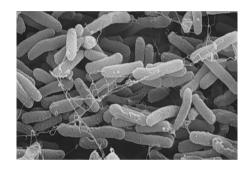


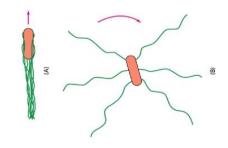
Asakura, Oosawa, Vrij (1954, 1976) Lekkerker (1992, 2002) Dijkstra (1999)

Aarts (2006)

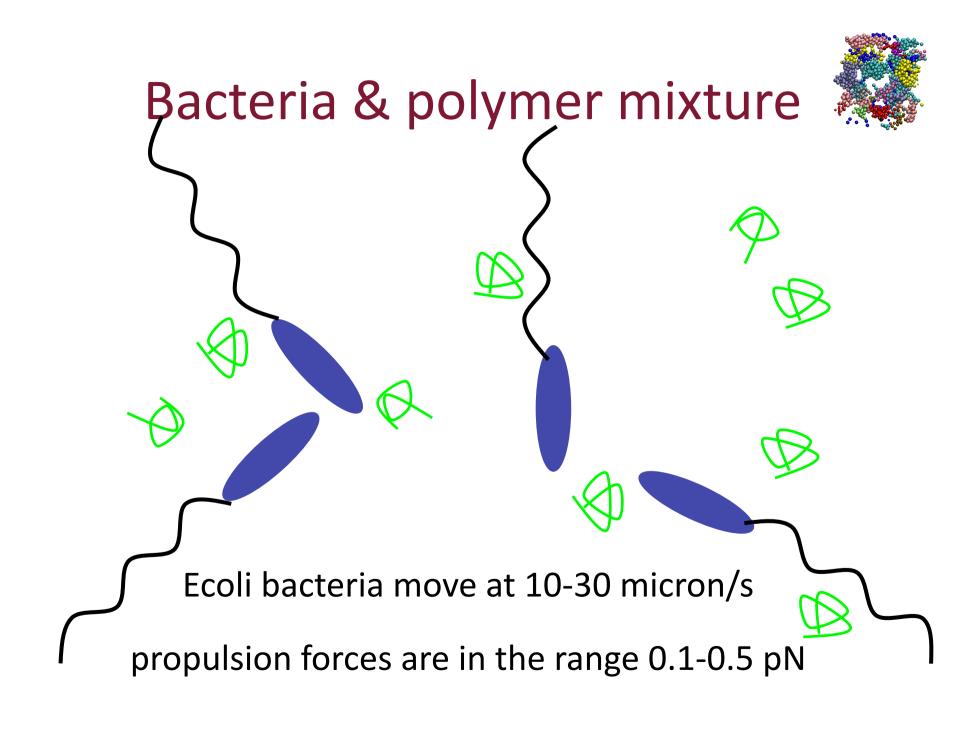
## Bacteria & polymer mixture



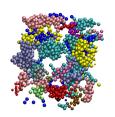


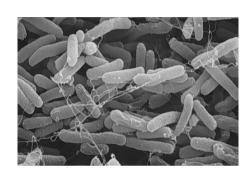


Bacteria swim (self-propel) due to the presence of flagella

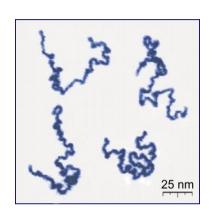


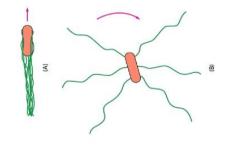




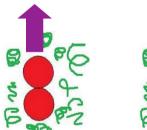


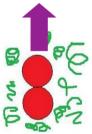






bacteria swim (self-propel) due to the presence of flagella

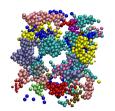


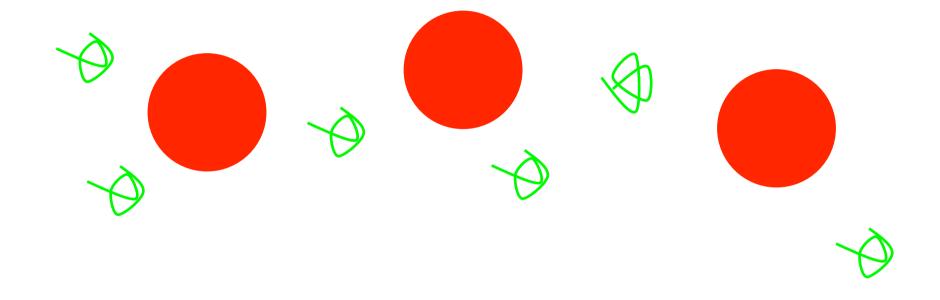


polymers lead to depletion attraction between non-motile bacteria

Schwarz-Linek, Soft Matter(2010)

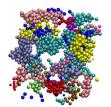
### Bacteria & polymer mixture

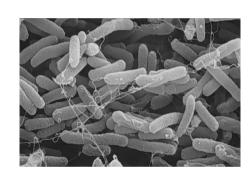




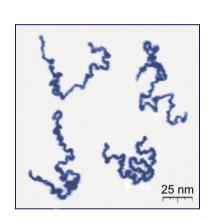
in a colloid-polymer mixture depletion forces are  $^{\sim}$  k $_{\rm B}$ T/giration radius ( $^{\sim}$ 10-100 nm) so in the range of 0.05-0.5 pN





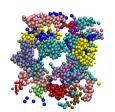






competition between propulsion and attraction





experiments

**Ecoli** 



**NaPSS** 

simulations

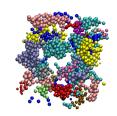
self-propelled hard dumbbells



short-range attractions

competition between propulsion and attraction





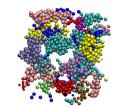
experiments

Non-motile Ecoli (alive, no flagella)

Motile Ecoli (alive, swimming)







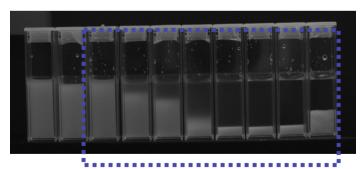
# Phase separation experiments

Non-motile Ecoli (alive, no Motile Ecoli (alive, flagella)

swimming)

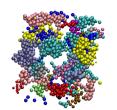






2 hours: phase separation

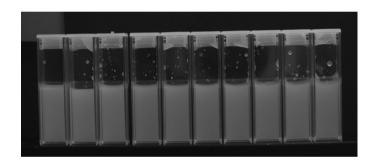
if NaPSS > 0.2 wt %



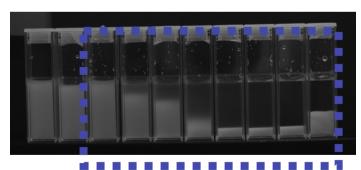
# Phase separation experiments

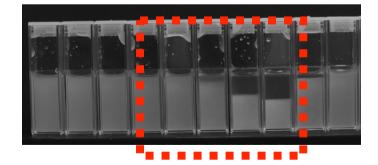
Non-motile Ecoli (alive, no flagella)

Motile Ecoli (alive, swimming)







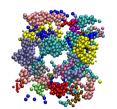


2 hours: phase separation

if NaPSS > 0.2 wt %

2 hours: phase separation

if NaPSS > 0.4 wt %



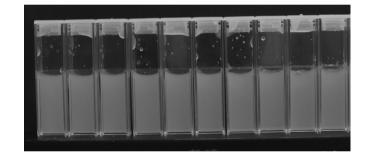
### Phase separation

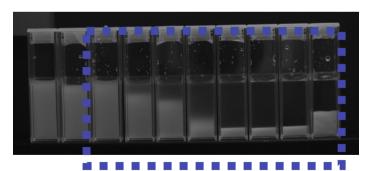
experiments

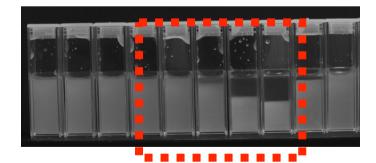
Non-motile Ecoli (alive, no flagella)

Motile Ecoli (alive, swimming)







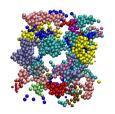


2 hours: phase separation

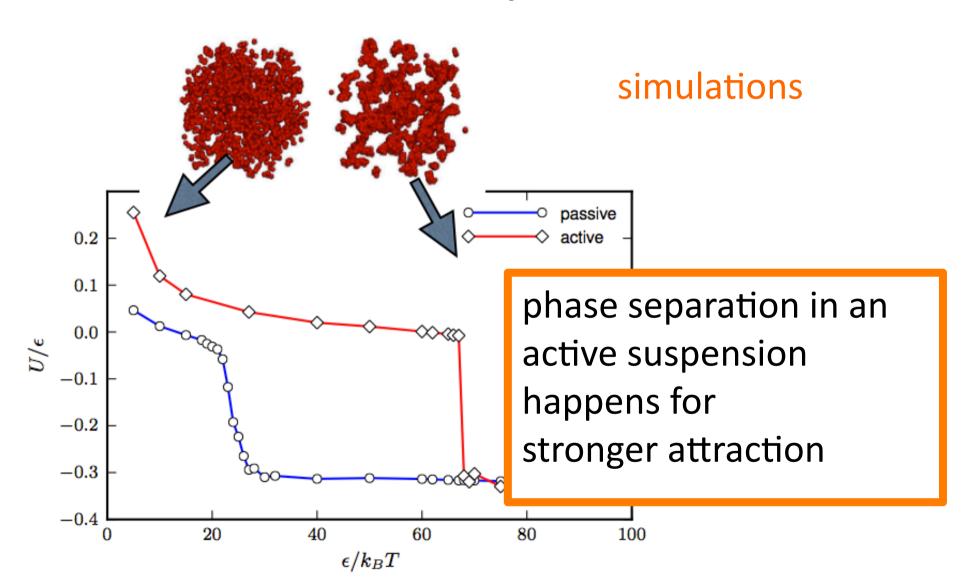
this corresponds to a

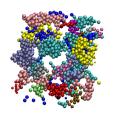
if NaPSS > 0.2 wt %

stronger depletion attraction

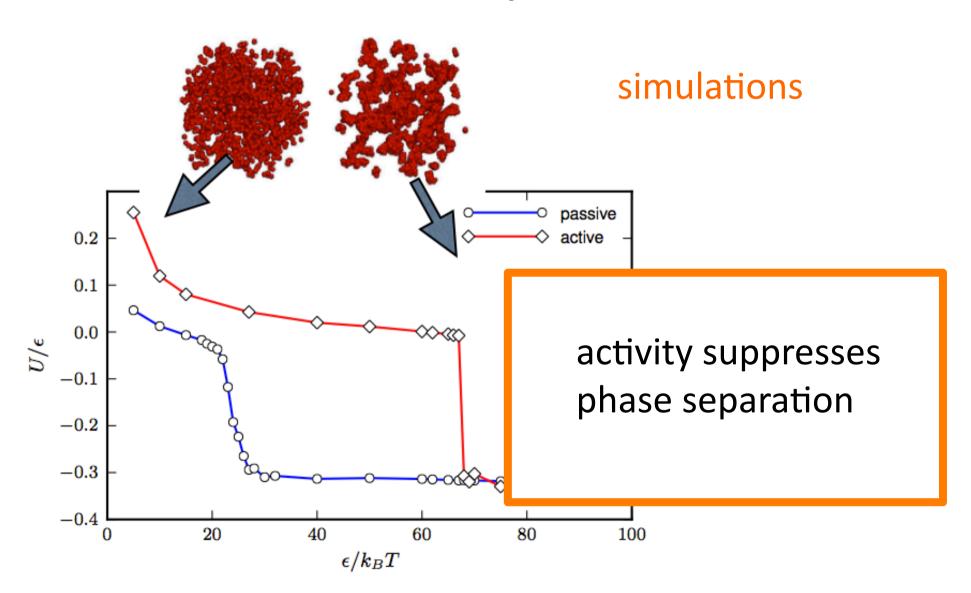


### Phase separation



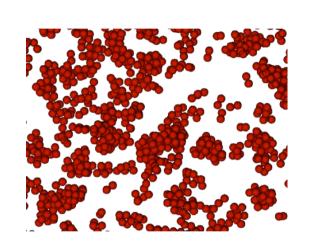


### Phase separation





#### transient clusters



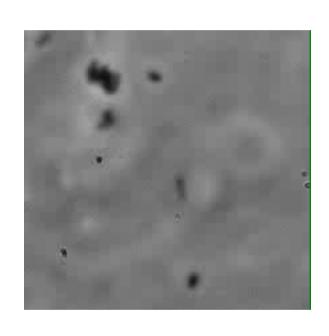


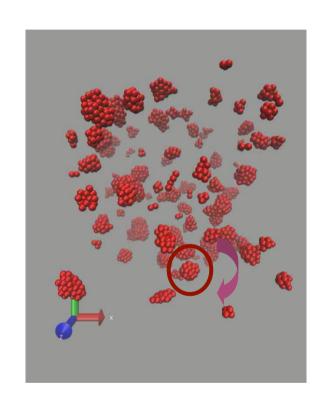


finite-size clusters of variable size (simulations)

small clusters (flagella of external bacteria may screen interactions) (experiments)

# Self-assembly of nano-rotors



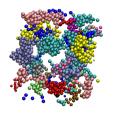


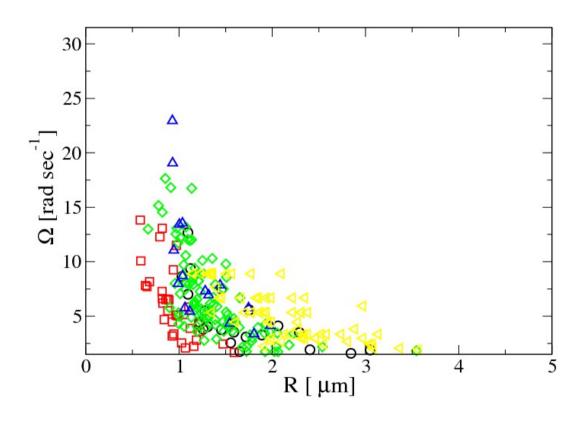
experiments

simulations

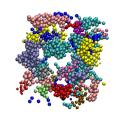
persistent clusters rotate unidirectionally







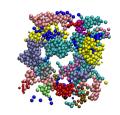
angular velocity of a cluster decreases with its size



#### Conclusions

- ✓ Activity suppresses phase separation
- ✓ At lower polymer concentrations, formation of self-propelled and unidirectionally rotating clusters
- ✓ Activity & propulsion are the ingredients to self-assemble functional clusters

Research highlight in Nature Materials/Nature Physics (2012)



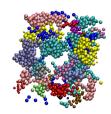
#### However...

✓ in the bacteria & polymer mixture, we changed the attraction strength (polymer concentration) between active colloids

✓ but we did not modify their speed...

✓ therefore clusters were just transient and would aggregate at long times

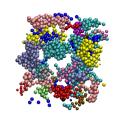
#### Outline



✓ Active colloids

- ✓ Self-assembly of active colloids
- ✓ What happens in a bacteria & polymer mixture?
- ✓ Can we make living clusters of active colloids in low concentrated suspensions

### Living clusters





Daan Frenkel

#### The team:

**Cambridge University** 



Stefano Angioletti Uberti

**Columbia University** 



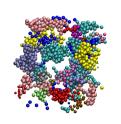
Bortolo Mognetti



Angelo Cacciuto

Andela Sairc

# Phase separation/clusters in 2 dim self-propelled systems



2 dim rod-shaped (at low/high concentrations) steric/ideal

Peruani, Deutsch, Bar (2006)

Yan, Marceau, Gompper (2010)

Ginelli, Peruani, Bar, Chate(2006)

or 2dim spherical shaped interacting via a repulsive potential

(at high concentration)

Stenhammar, Tirabocchi, Allen,

Redner, Hagan, Baskaran (2013)

Marenduzzo, Cates (2011)

Tailleur, Cates (2013)

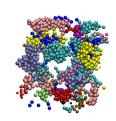
Henke, Fily, Marchetti (2011)

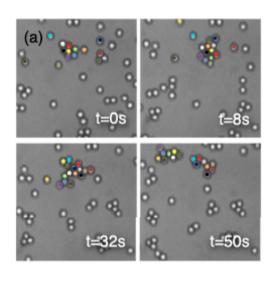
or 2dim spherical shaped interacting via an attractive potential (at high concentration)

Redner, Baskaran, Hagan (2013)

What happens for attractive self-propelled spheres at low concentrations?

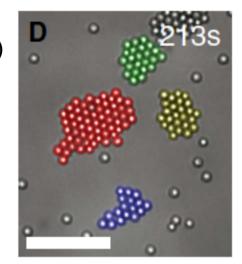
# Experimental evidences for living clusters in 2 dim





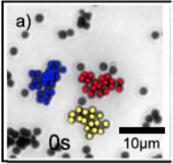
Theurkauff, Cottin-Bizonne, Palacci, Ybert, Bocquet (2012)

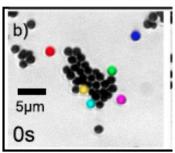
cluster phase at intermediate densities



Buttinoni, Bialke, Kummel, Lowen, Bechinger, Speck (2013)

dynamic clusters at low densities in a 2dim suspension of SP purely repulsive colloids



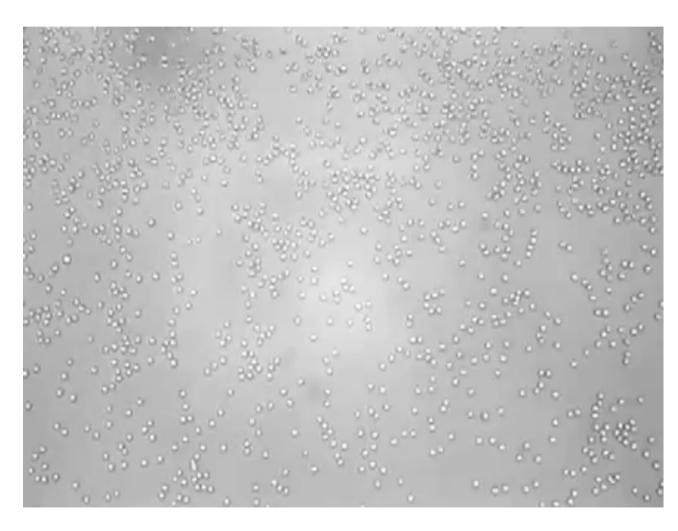


Palacci, Sacanna, Steinberg, Pine, Chaikin (2013)

living clusters and crystals

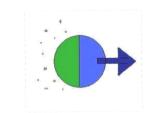
# Experimental evidences for living clusters in 2 dim





# Which low concentrated suspensions of active colloids?

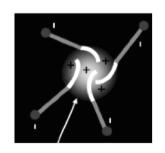
√ Self-propelled colloids (SP)



to mimic reactive colloids

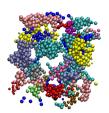
√ Self-displaced colloids (SD)

to mimic synthetic centrosomes (colloids & microtubules)



(Spoerke Langmuir (2008)

### Self-propelled colloids



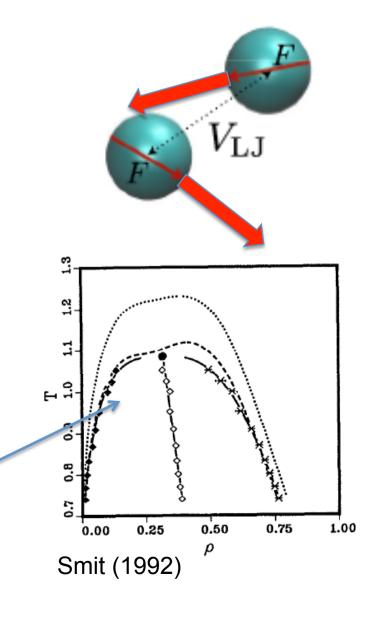
$$m\ddot{r}_i = -\sum_{j\neq i} \frac{\partial V(r_{ij})}{\partial r_i} - \zeta \dot{r}_i + F_i + F_{R,i}$$

$$V(r_{ij}) = 4\epsilon \left[ \left( \frac{\sigma_p}{r_{ij}} \right)^{12} - \left( \frac{\sigma_p}{r_{ij}} \right)^6 \right]$$

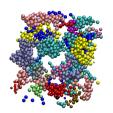
truncated and shifted Lennard-Jones interaction

at low concentrations ( $\phi$ =0.01-0.1)

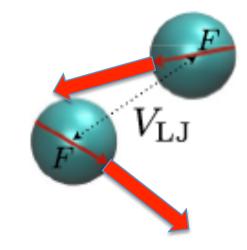
**LAMMPS** 



### Self-propelled colloids



$$m\ddot{r}_{i} = -\sum_{j\neq i} \frac{\partial V(r_{ij})}{\partial r_{i}} - \zeta \dot{r}_{i} + F_{i} + F_{R,i}$$



equilibrium: Lennard-Jones attraction

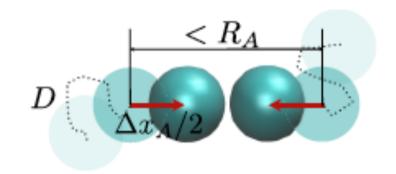
non-equilibrium: self-propulsion

Active versus equilibrium force

# Self-displaced colloids



In the presence of ATP two centrosomes are cross-linked by molecular motors and displaced towards each others

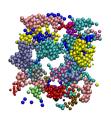


Monte Carlo

at low concentrations ( $\phi$ =0.01-0.1)

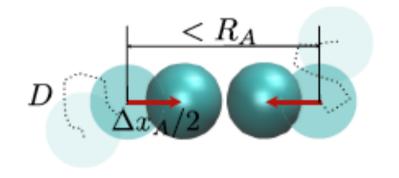


### Self-displaced colloids



equilibrium: Brownian motion of hard-spheres with

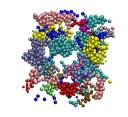
diffusion D

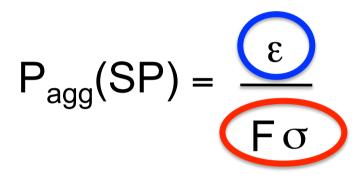


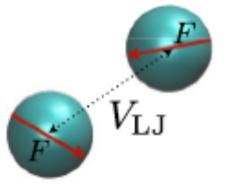
non-equilibrium: two colloids are displaced toward each other by molecular motors with a pulling rate v

Active versus equilibrium force

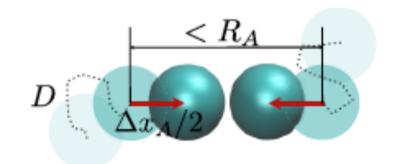
# Is there a propensity for aggregation?



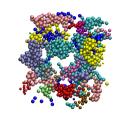


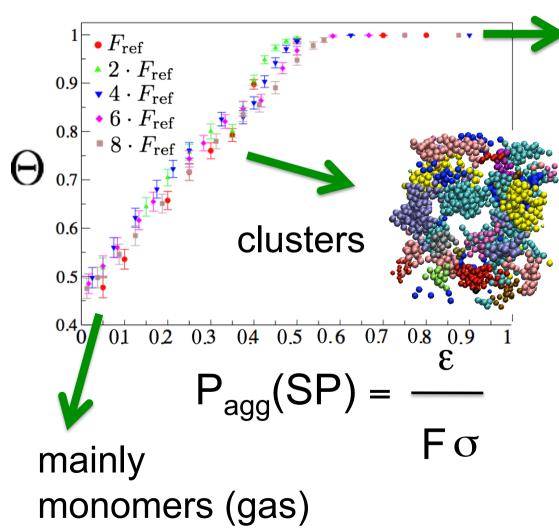


$$P_{agg}(SD) = \frac{v}{D/(R_A - \sigma)^2}$$





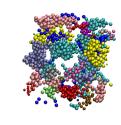


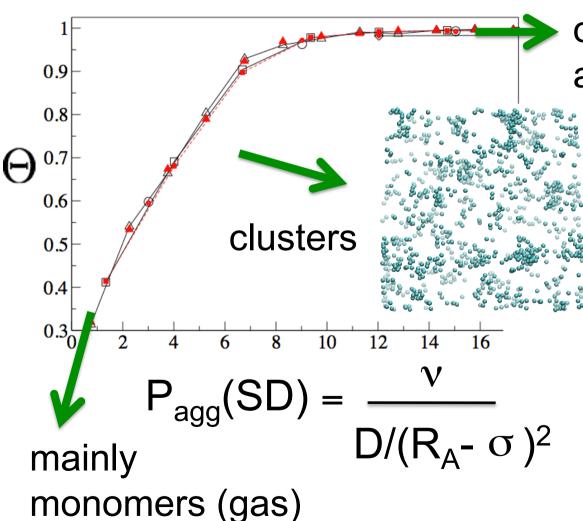


one large aggregate (liquid&gas)

Self-propelled colloids





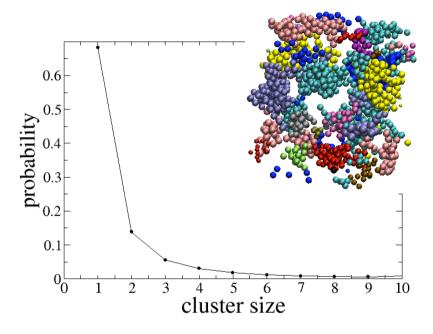


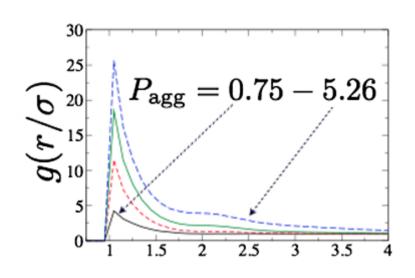
one large aggregate (liquid&gas)

Self-displaced colloids







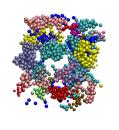


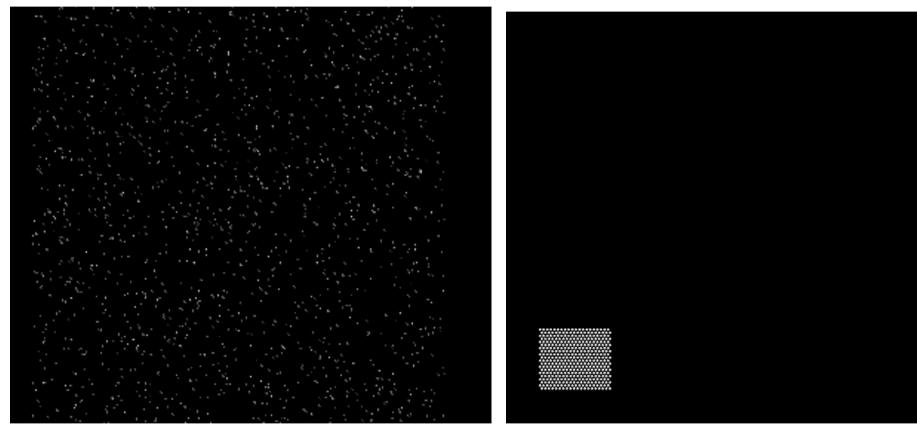
cluster-size distribution seems power-law

clusters are amorphous

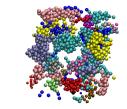
clusters grow and shrink dynamically





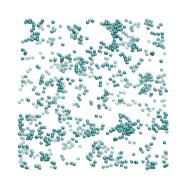


initial configuration: gas initial configuration: crystal we observe them for different initial conditions



#### Therefore

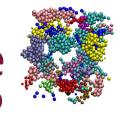
the formation of living clusters at low concentrations is independent on the active suspension under study

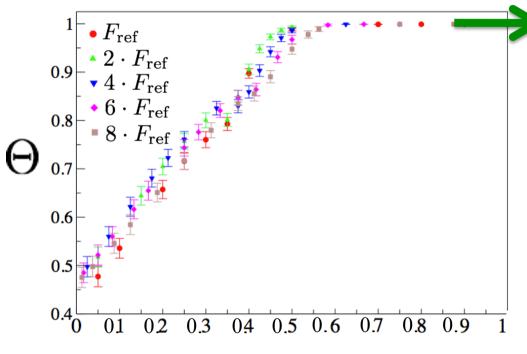


whether self-displaced or self-propelled

as long as there is a competition between equilibrium and active force

# Is there anything special in the structure formed at large $P_{agg}$ ?



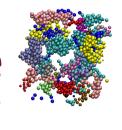


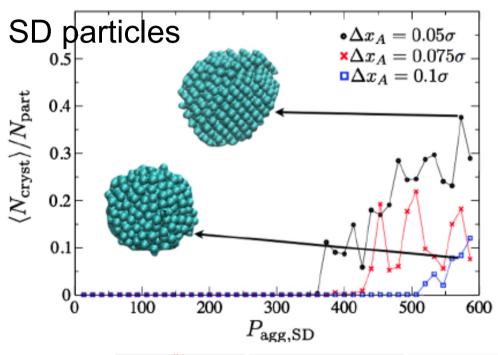
the system forms one large amorphous aggregate that crystallizes thanks to the activity

P<sub>agg</sub>(SP)<sub>activity</sub> helps annealing defects!

irreversible crystallization, not living crystals

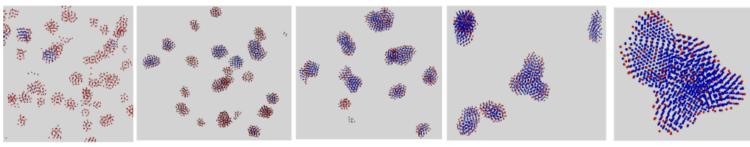
# Is there anything special in the structure formed at large $P_{agg}$ ?

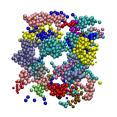




the system forms one large amorphous aggregate that crystallizes thanks to the activity

SP particles



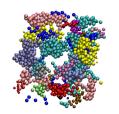


#### Conclusions

- ✓ In a diluted suspension of active colloids where an active force competes with an equilibrium one, the system can aggregate into living clusters
- ✓ When attraction dominates, the clusters can irreversibly crystallize

Physical Review Letter, 111 245702 (2013)

Focus article: Physics, 6 134 (2013)



### Take-home message

- ✓ Activity suppresses phase separation
- ✓ Activity & propulsion are the ingredients to self-assemble functional clusters
- ✓ In a diluted suspension of active colloids where an active force competes with an equilibrium one, the system can aggregate into living clusters

Physical Review Letter, 111 245702 (2013) Focus article: Physics, 6 134 (2013)

PNAS 106 4052 (2012)

Research highlight in Nature Materials/Nature Physics (2012)





- ✓ Can we better characterize the clusters?
- ✓ What is the effect of hydrodynamic interactions?
- ✓ What is the effect of particles' shape in the process of self-assembly?
- ✓ What if we make the attraction anisotropic?
- ✓ What happens if we consider active and passive colloids?









## Muchas gracias!

Physical Review Letter, 111 245702 (2013)

Focus article: Physics, 6 134 (2013)

PNAS 106 4052 (2012)

Research highlight in Nature Materials/Nature Physics (2012)

Living clusters

Bacteria & Polymers