

# Defect dynamics of active nematics and rheology of isotropic gels



Stephen DeCamp



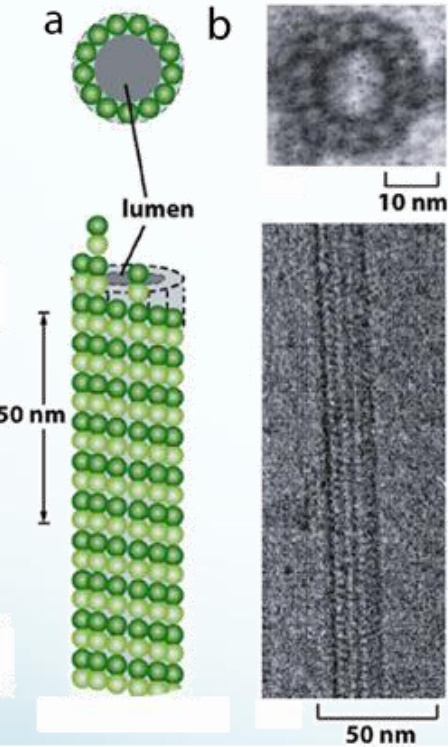
Gabriel Redner



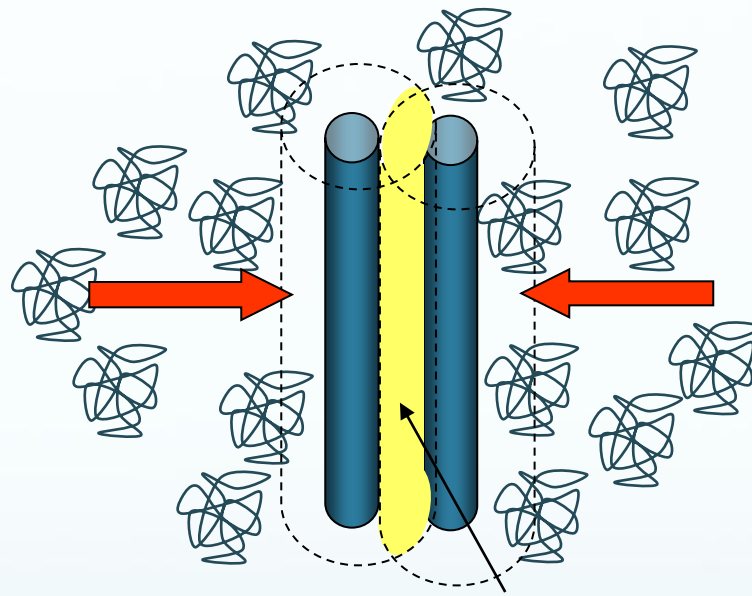
Mike Hagan

# Basic building blocks of active nematics

## microtubules

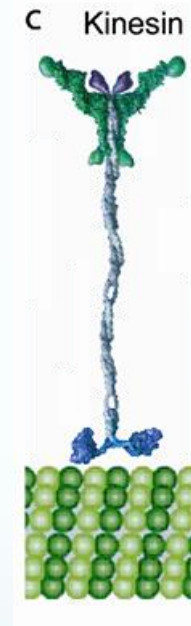


## depletion induced MT bundling



- non-adsorbing polymer (PEG) induced effective attractive interactions which lead to MT bundling

## molecular motor kinesin



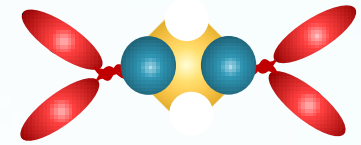
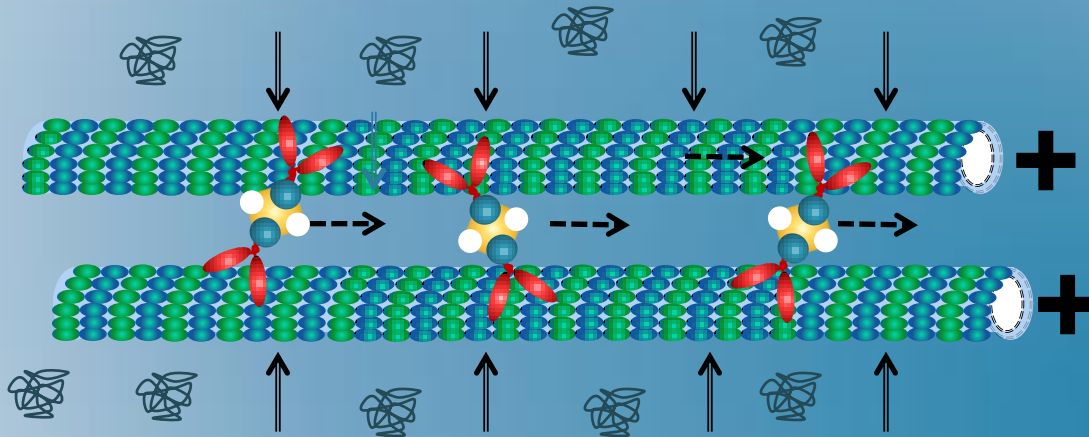
- motors convert energy from ATP hydrolysis into movement along MT backbone

- long rigid filaments
- stabilized with GMPCPP

# Basic building blocks – extensile MT bundles

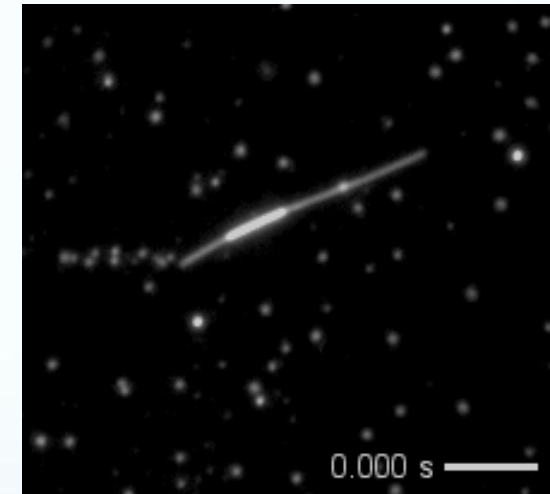
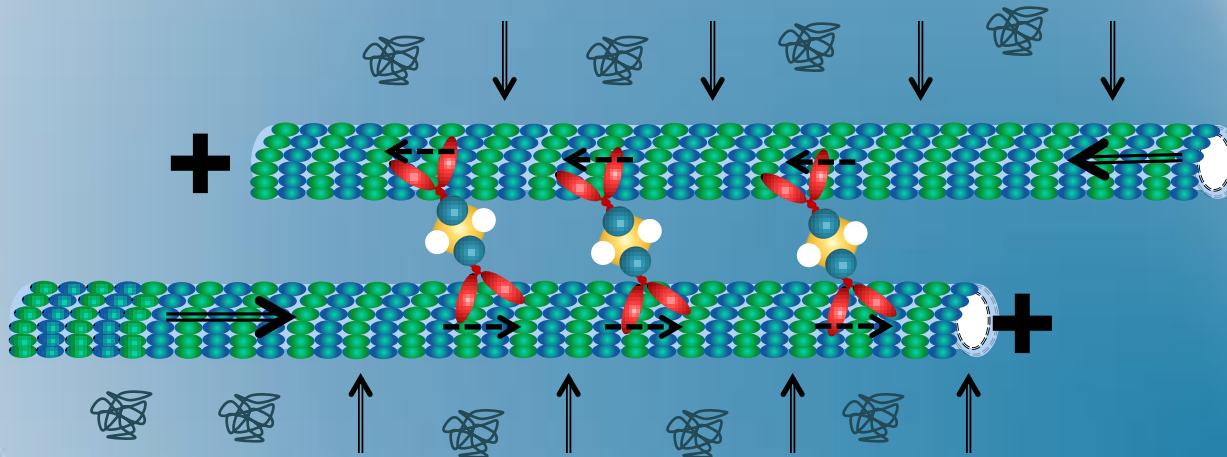
polar MT bundle

no interfilament sliding



biotin labeled kinesin are Bound into clusters via Tetrameric streptavidin.

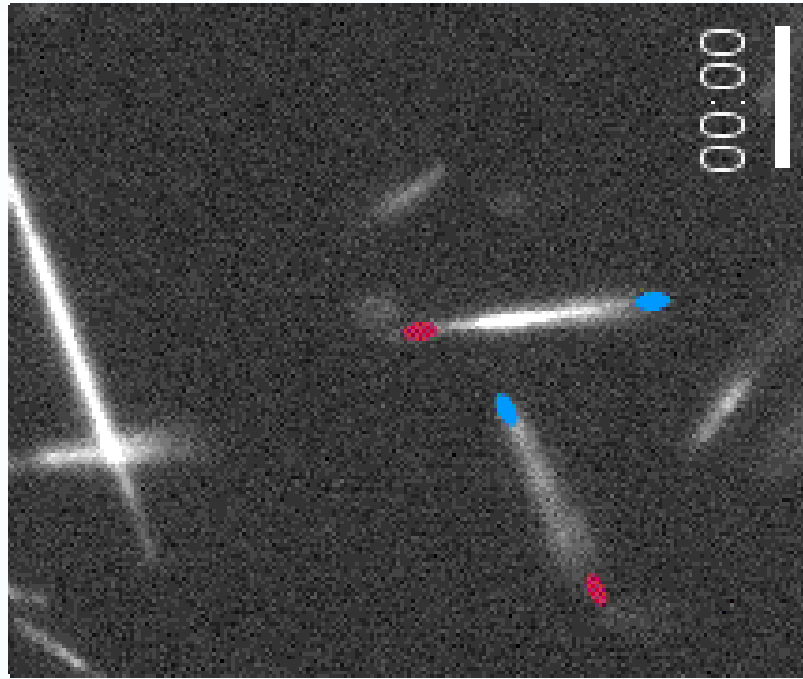
anti-polar MT bundle – motor driven filaments sliding



passive MT bundles – diffusive interfilament sliding

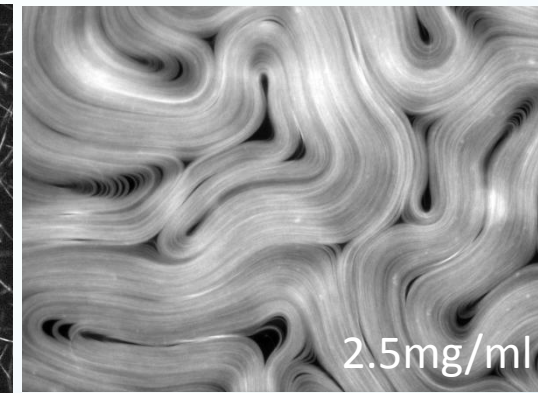
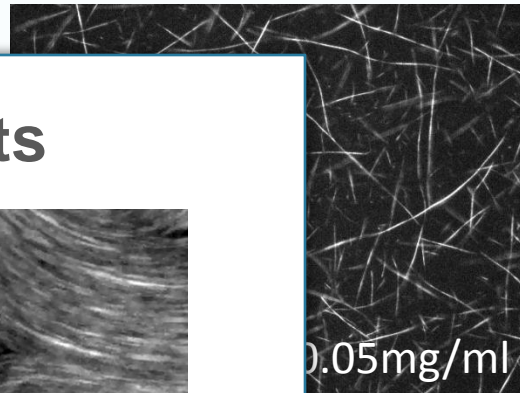
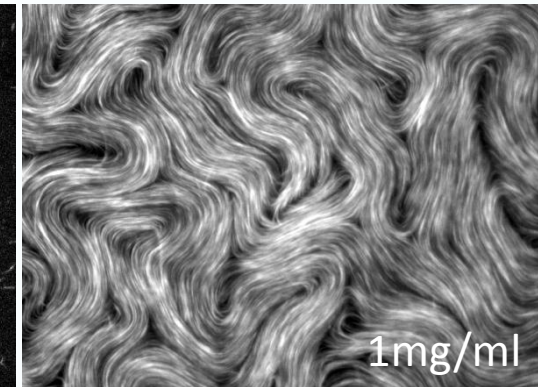
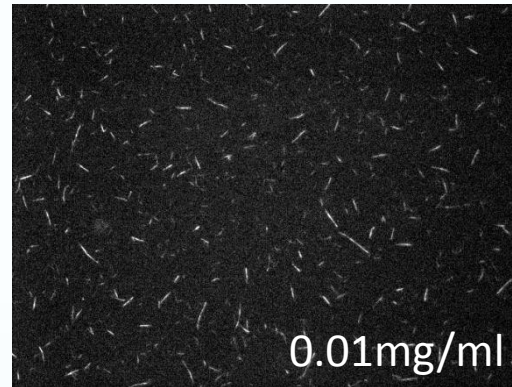
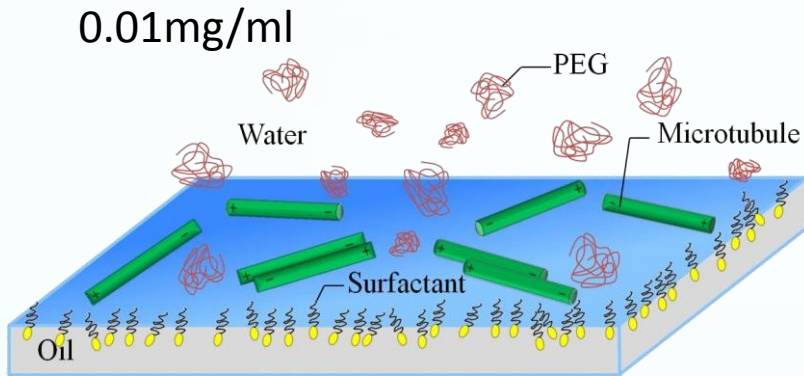
- bundle geometry greatly increases filament sliding efficiency
- MT sliding depends on relative filament polarity !!!

# dynamics of isolated extensile MT bundles

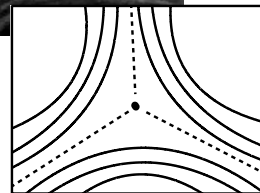
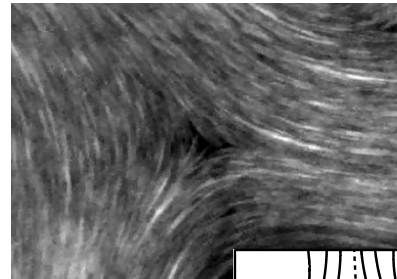
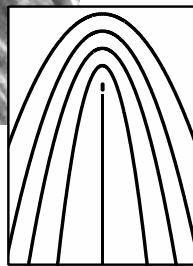
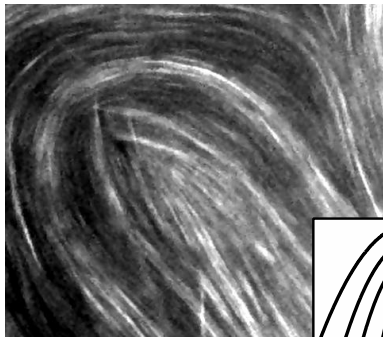


- isolated MT bundles are static indicating polarity sorting
- bundle recombination reinitializes local polarity sorting

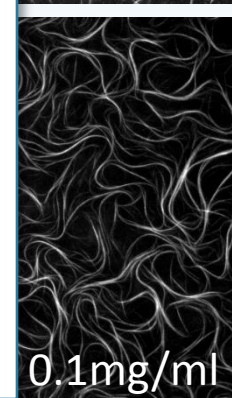
# Active Nematic liquid crystals



## topological defects



$1/2$  and  $-1/2$  disclinations indicate nematic order



# disclination defects in equilibrium nematics

topological charge  $Q = +1$

traversing the defect core  
requires  $360^\circ$  rotation



topological charge  $Q = 1/2$

traversing the defect core  
requires  $180^\circ$  rotation

$Q = +1/2$

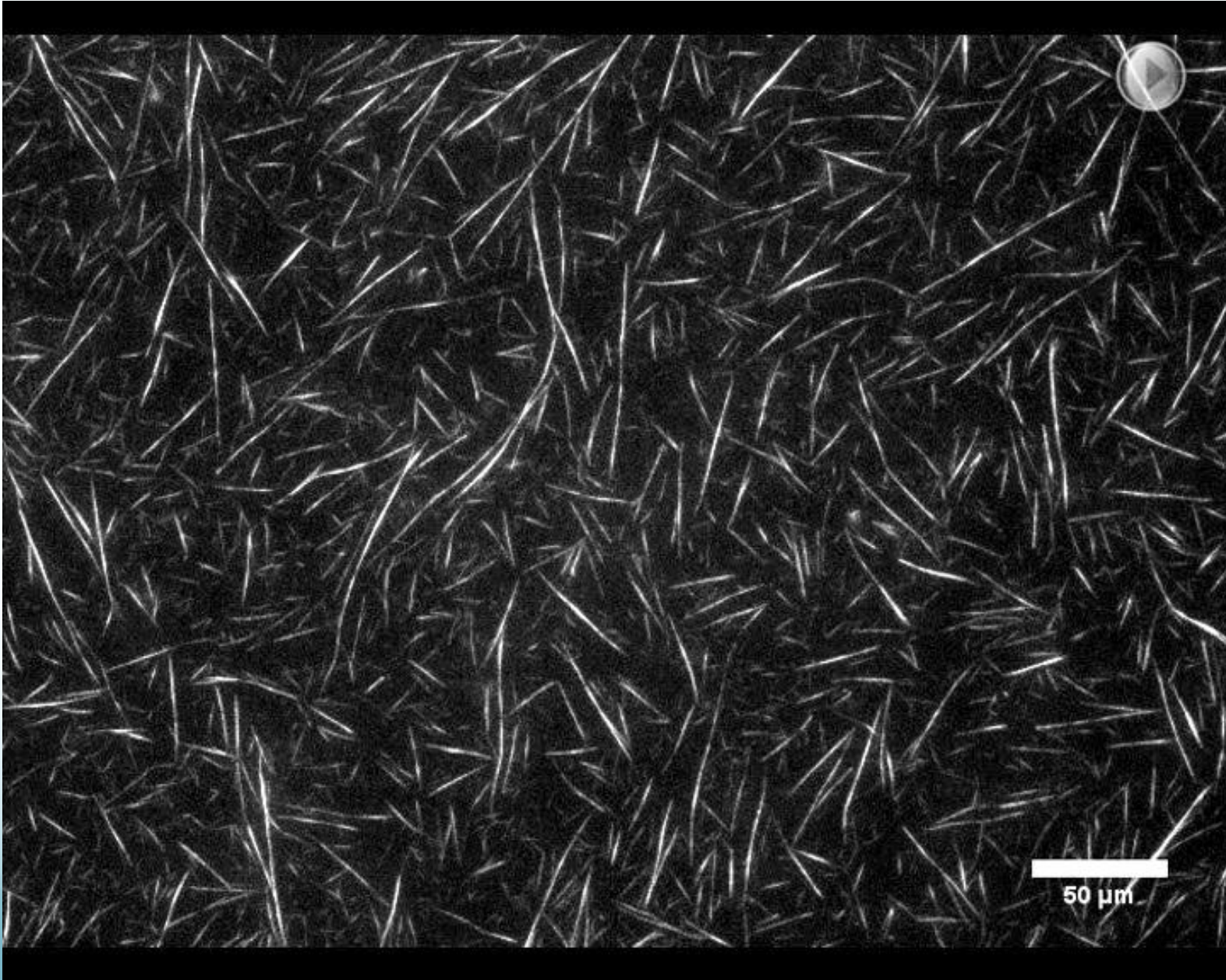


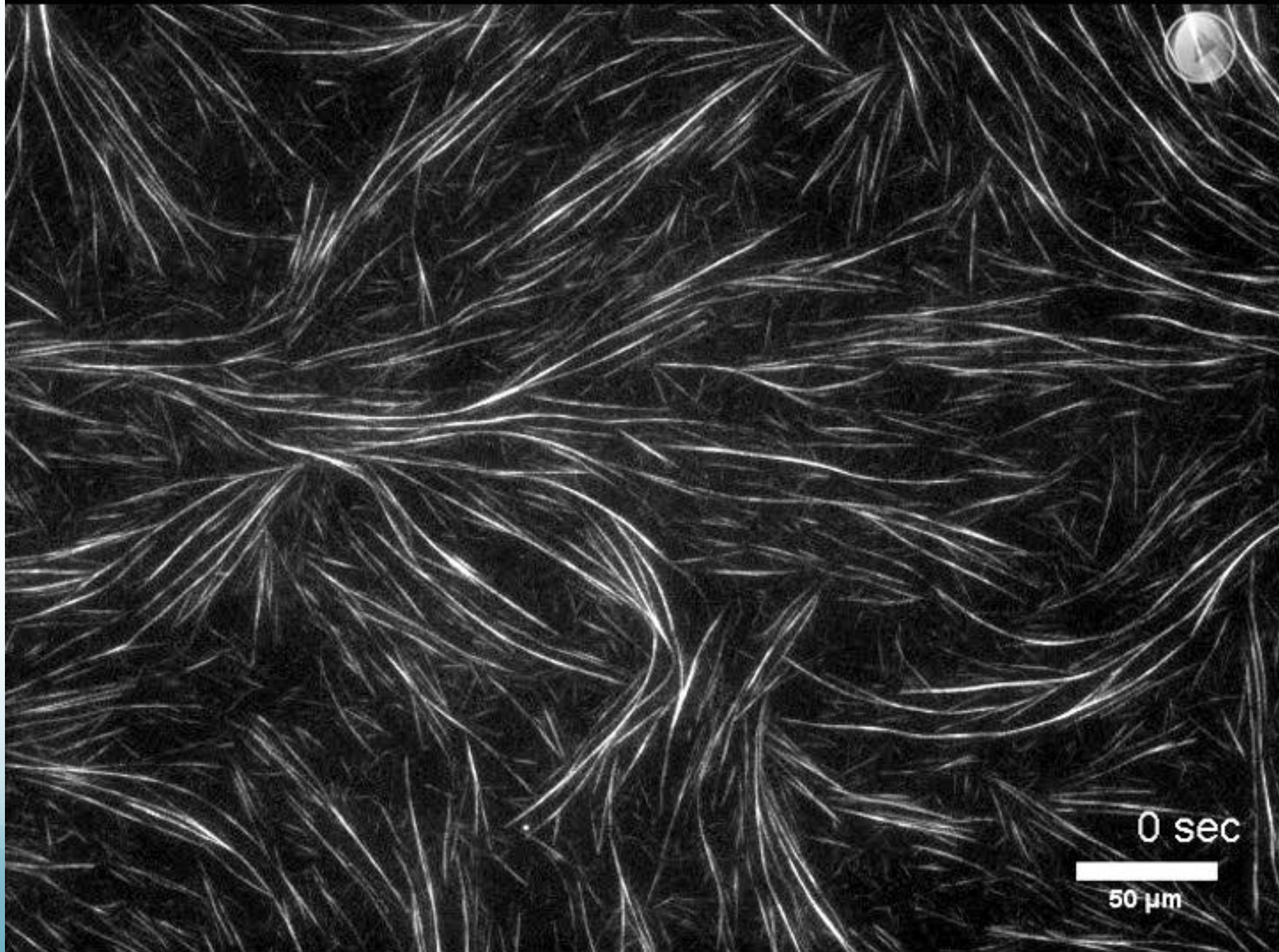
$Q = -1/2$



- $+1/2$  and  $-1/2$  defects can annihilate to create defect free nematic
- thermal fluctuations are not strong enough to drive spontaneous unbinding of defect pair
- $1/2$  defect only form in a system with nematic symmetry (arrowless bar)

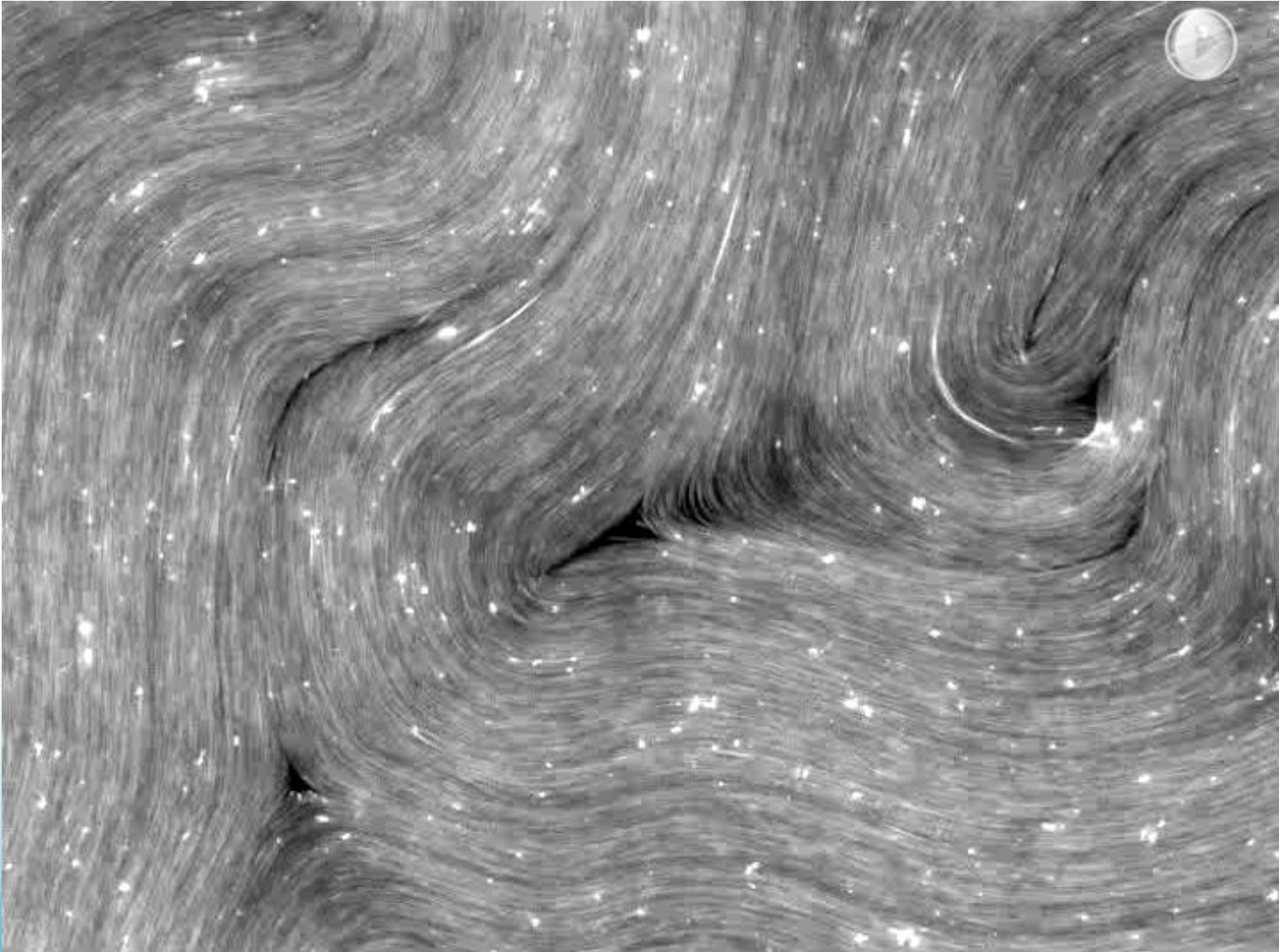




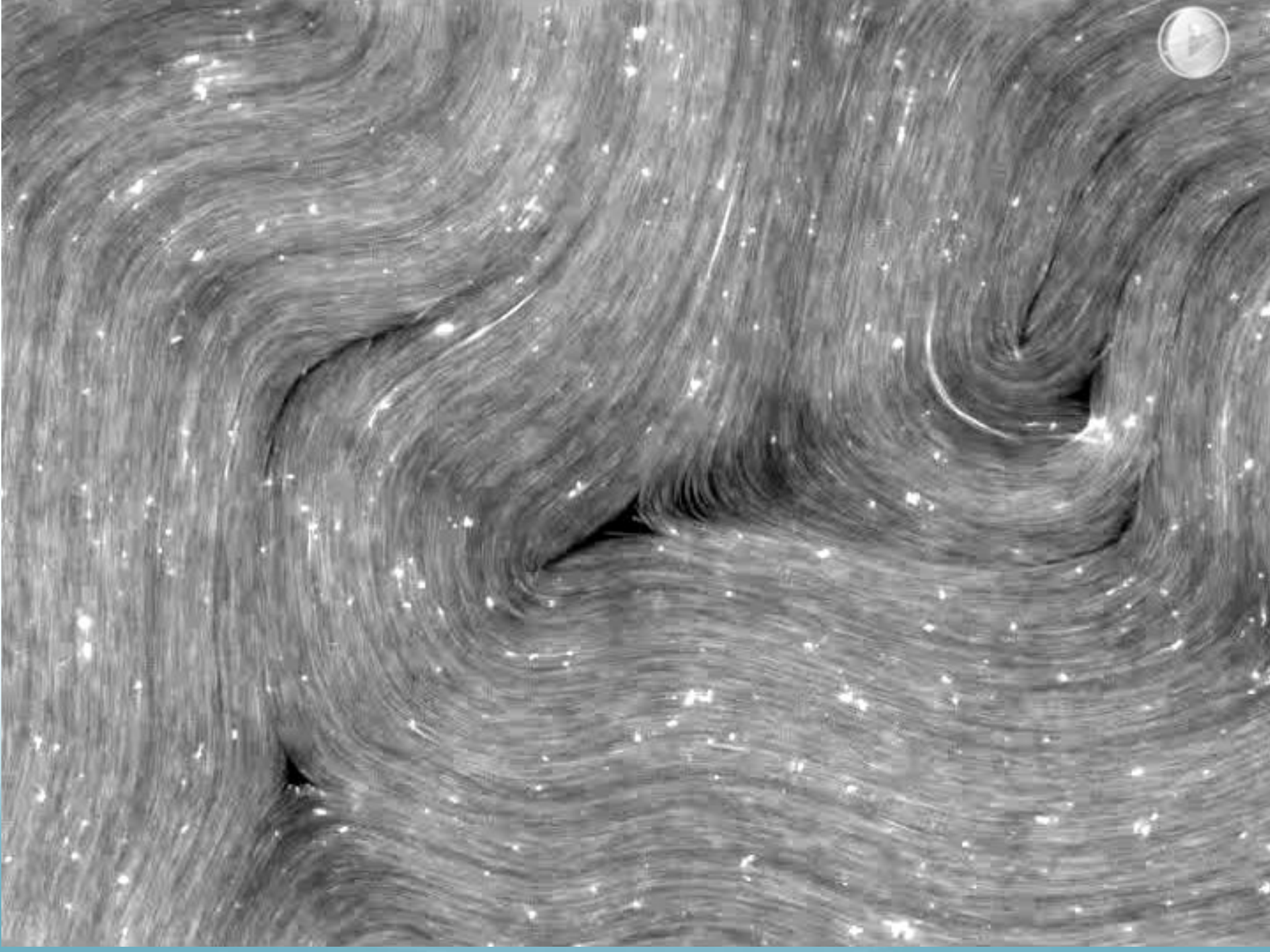


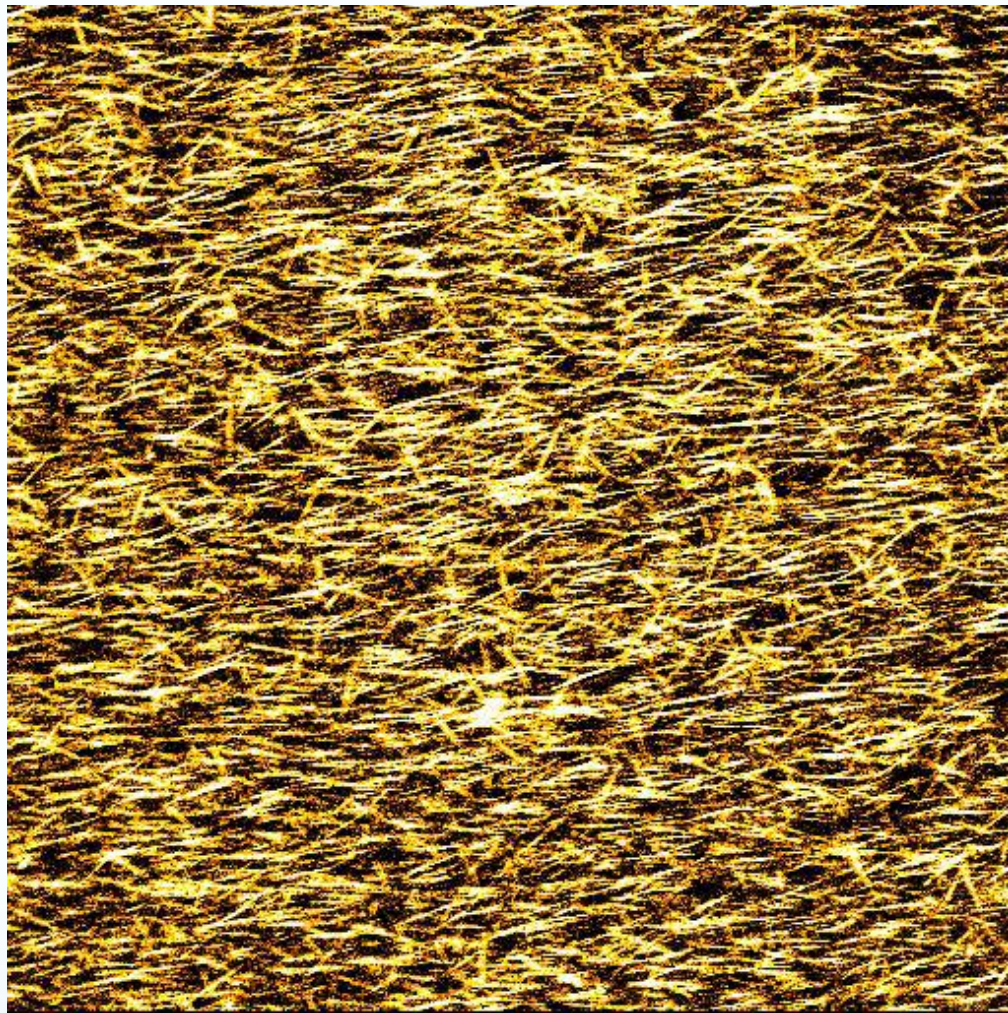


- equilibrium liquid crystals – static defects
- active liquid crystals – spontaneous motility

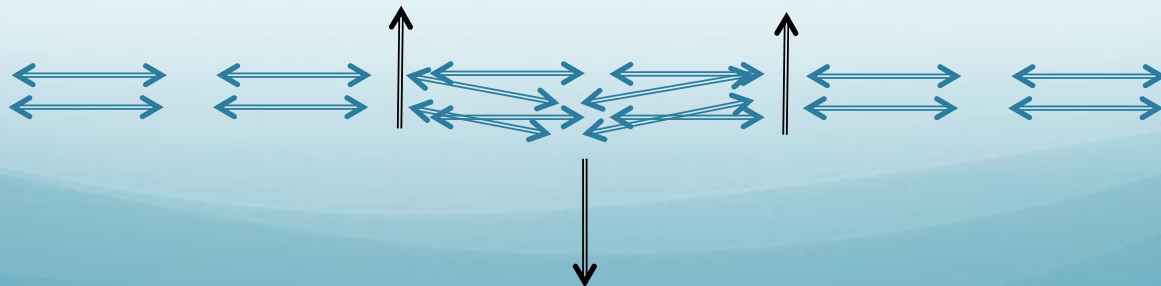


Active liquid crystals exhibit streaming flows !

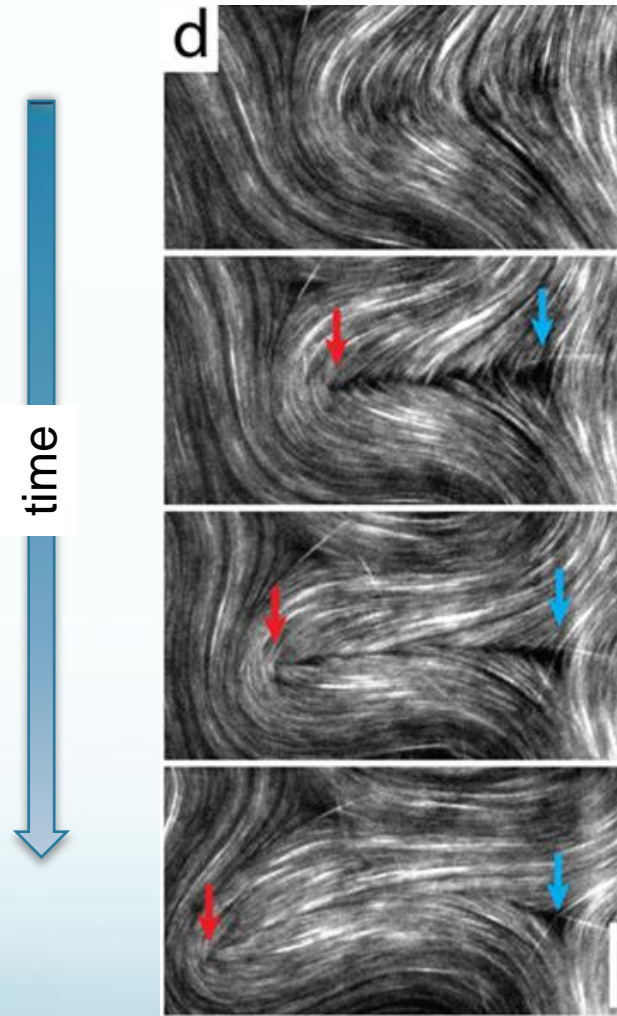




**aligned extensile filaments are unstable against bend fluctuations**



# MT active nematics: bucking instability leads to defect creation and annihilation



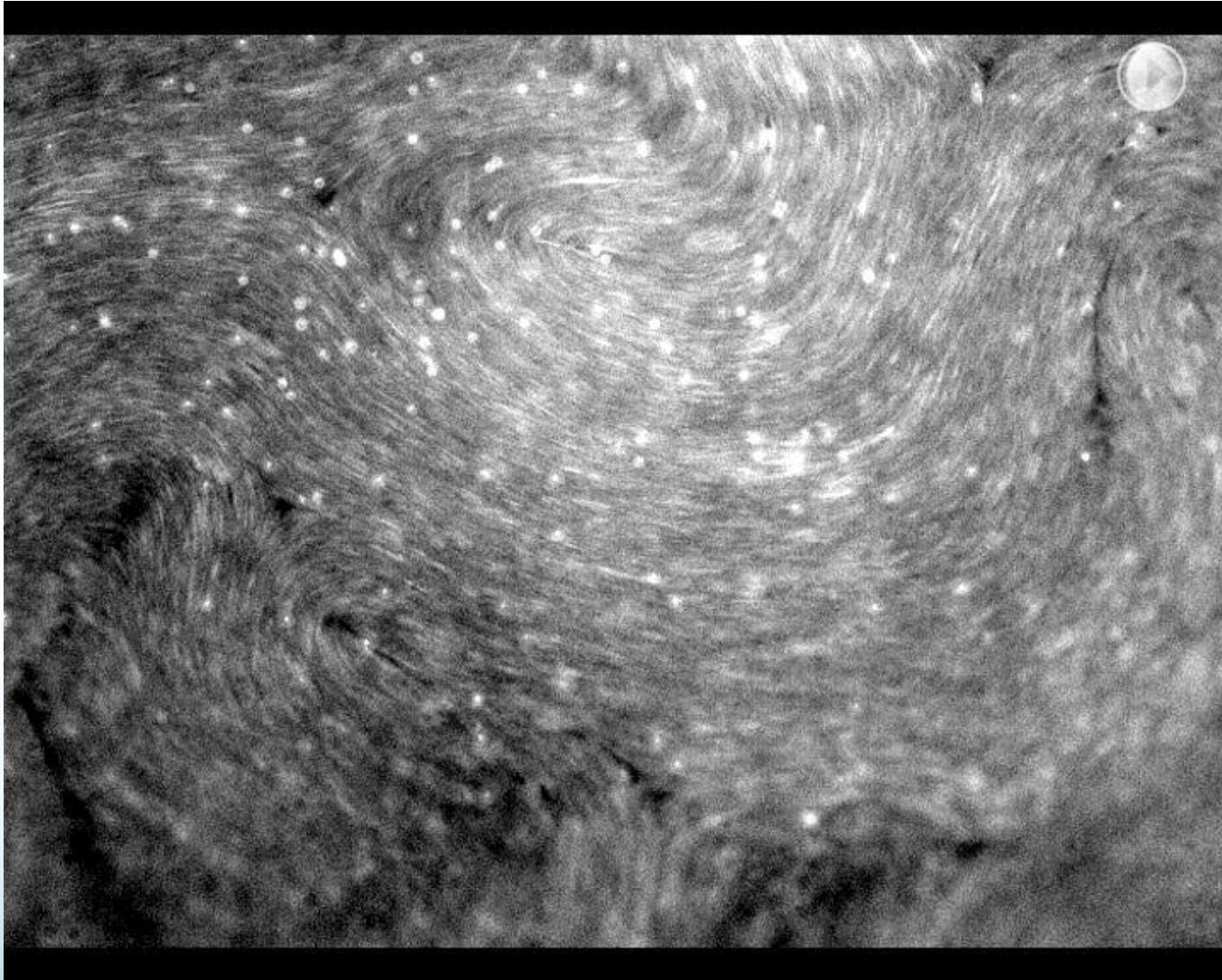
bend instability  
leads to buckling

fracture of the director field  
leads to unbinding of a  
defect pair

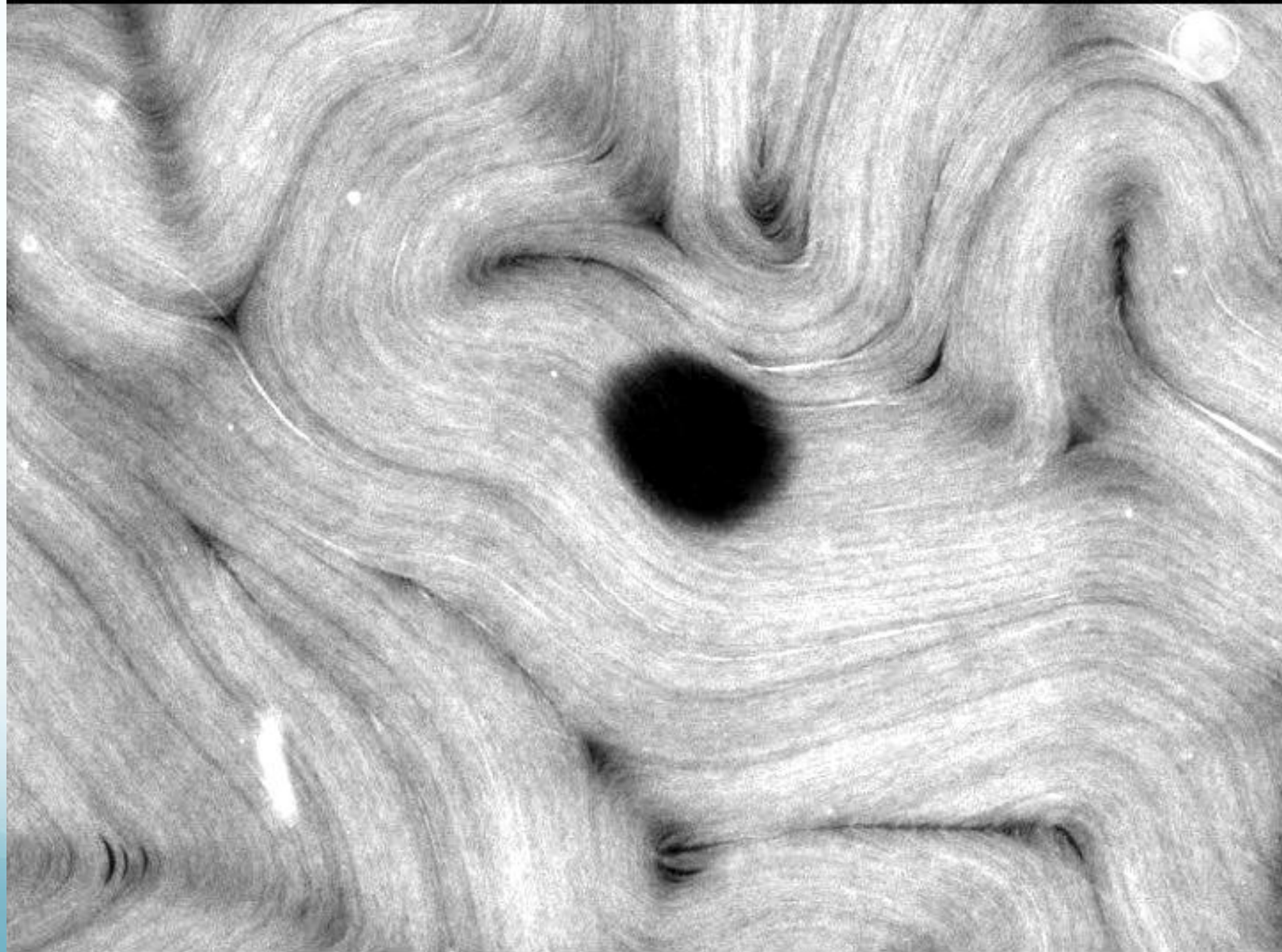
asymmetric  $+1/2$  defect  
is motile

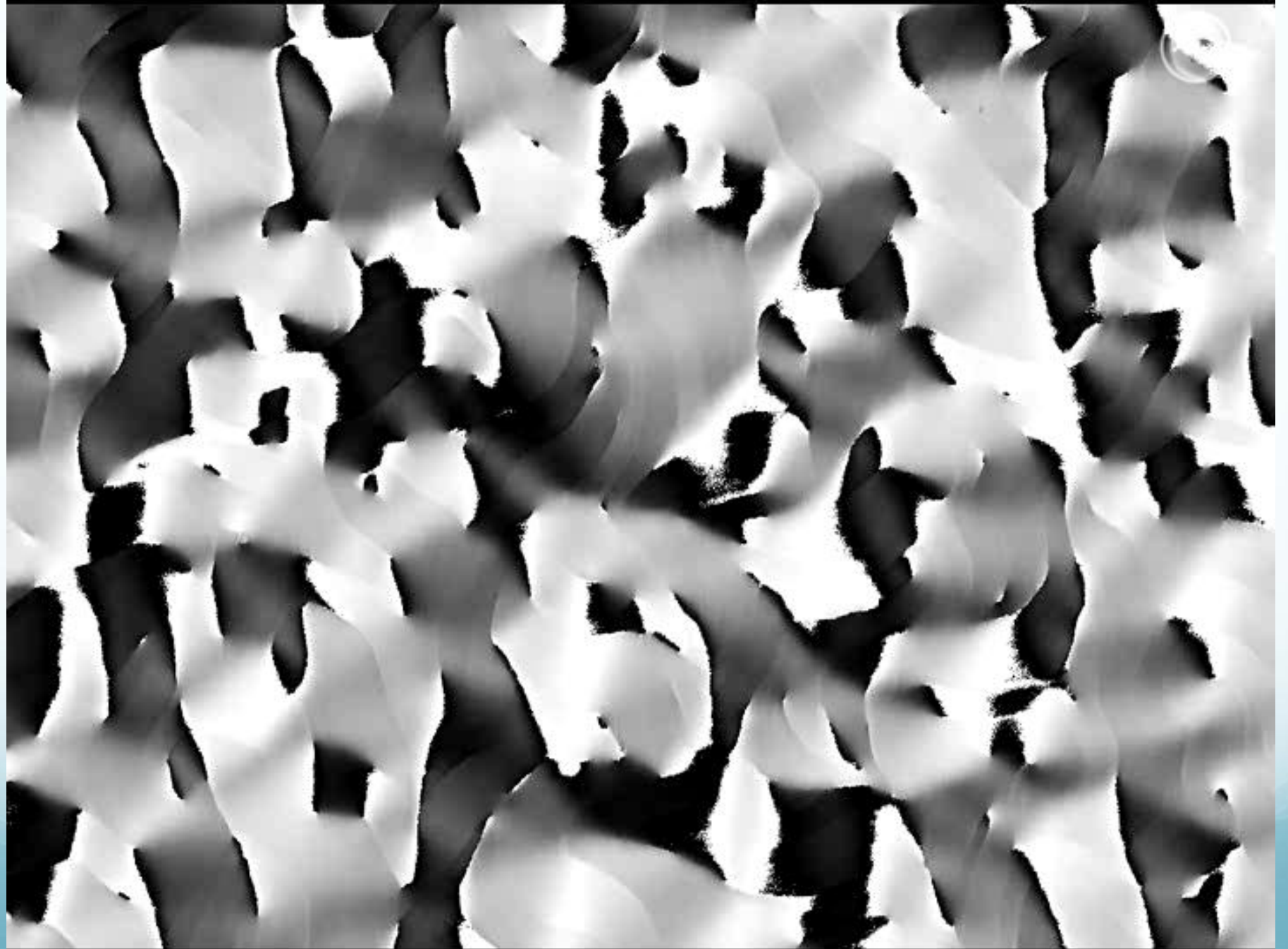
fracture line  
self-healing

# Annihilation of Defect Pairs

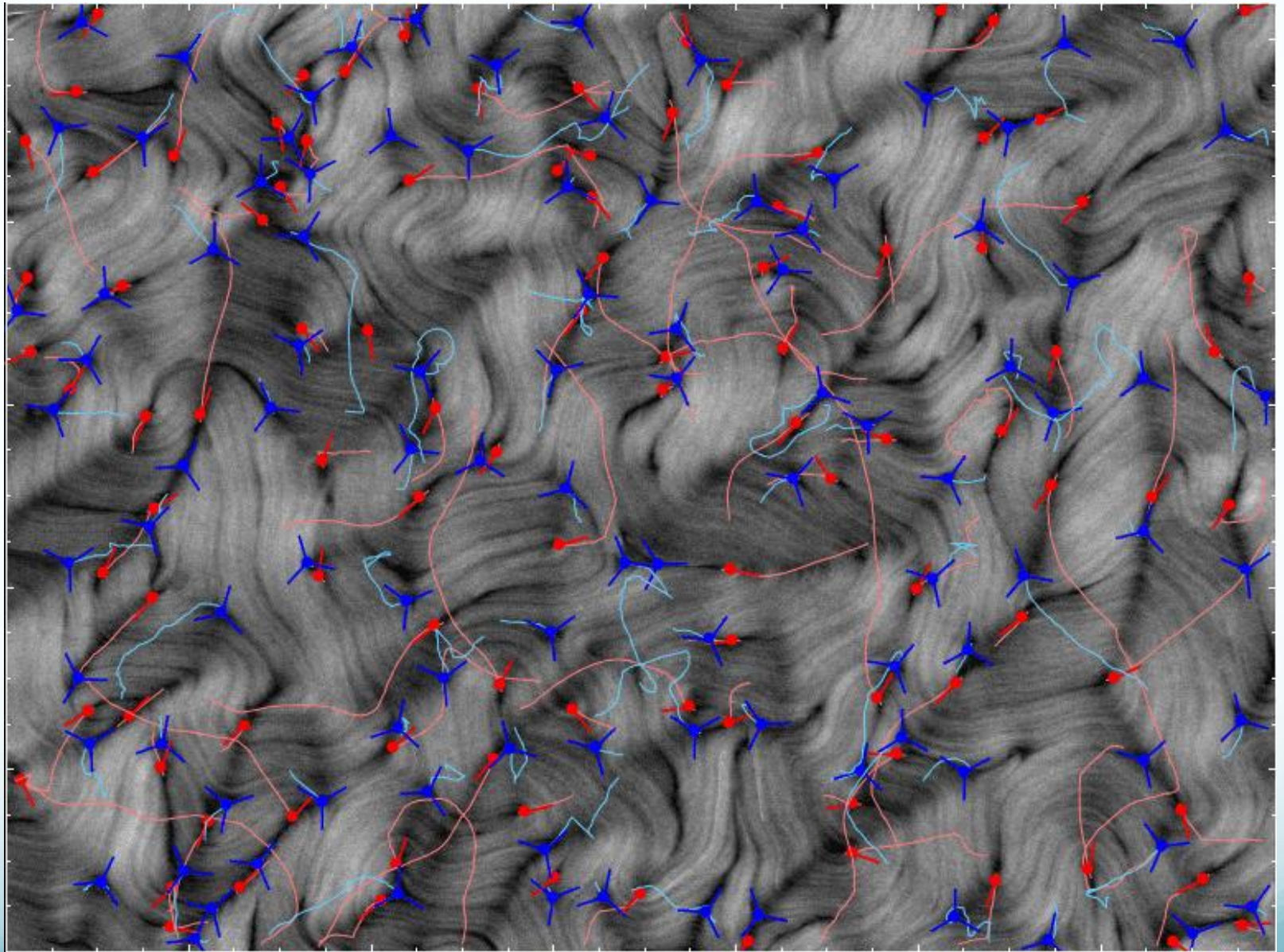


Steady state – rate of defect creation is equal to rate of defect annihilation



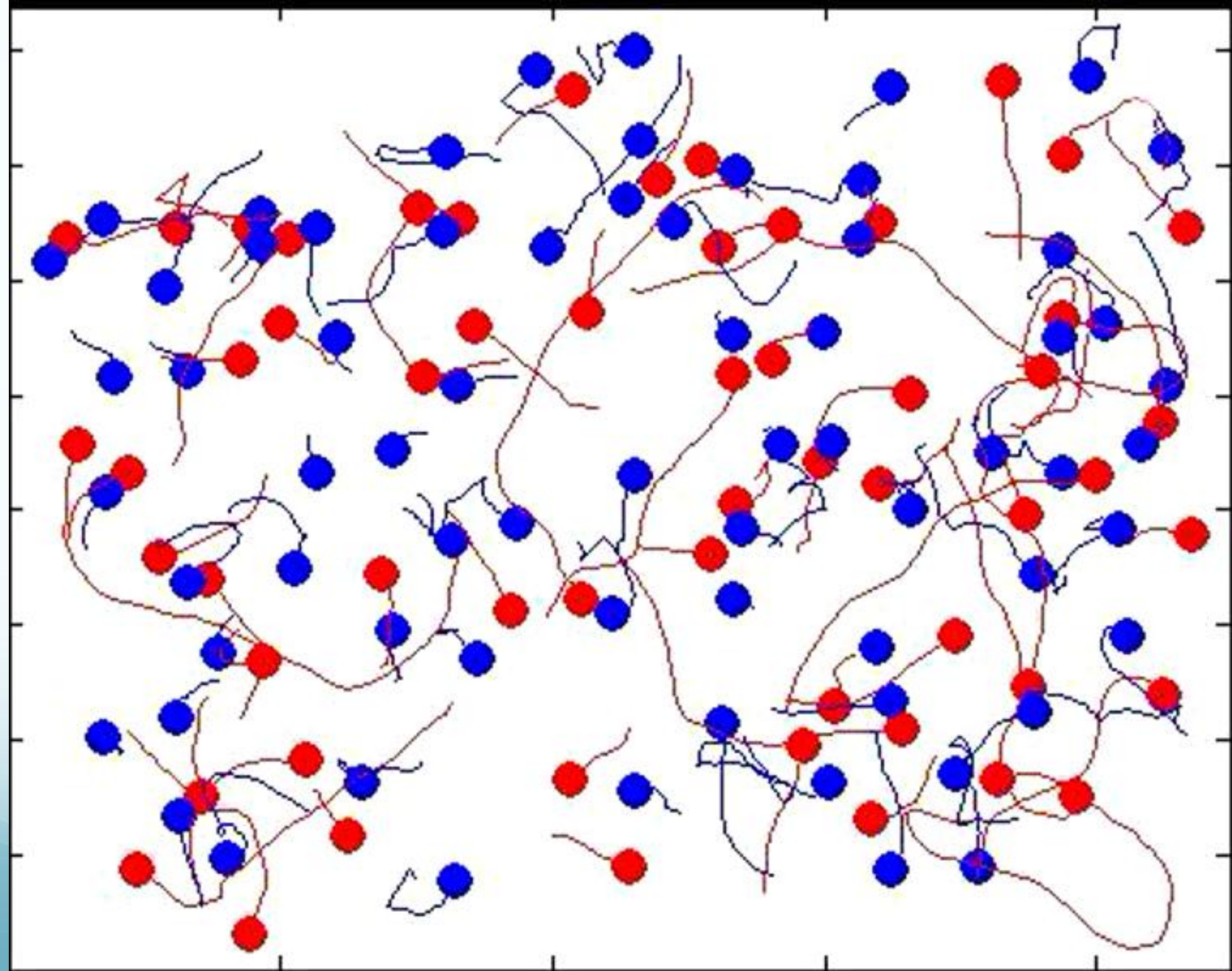


2.5 mm

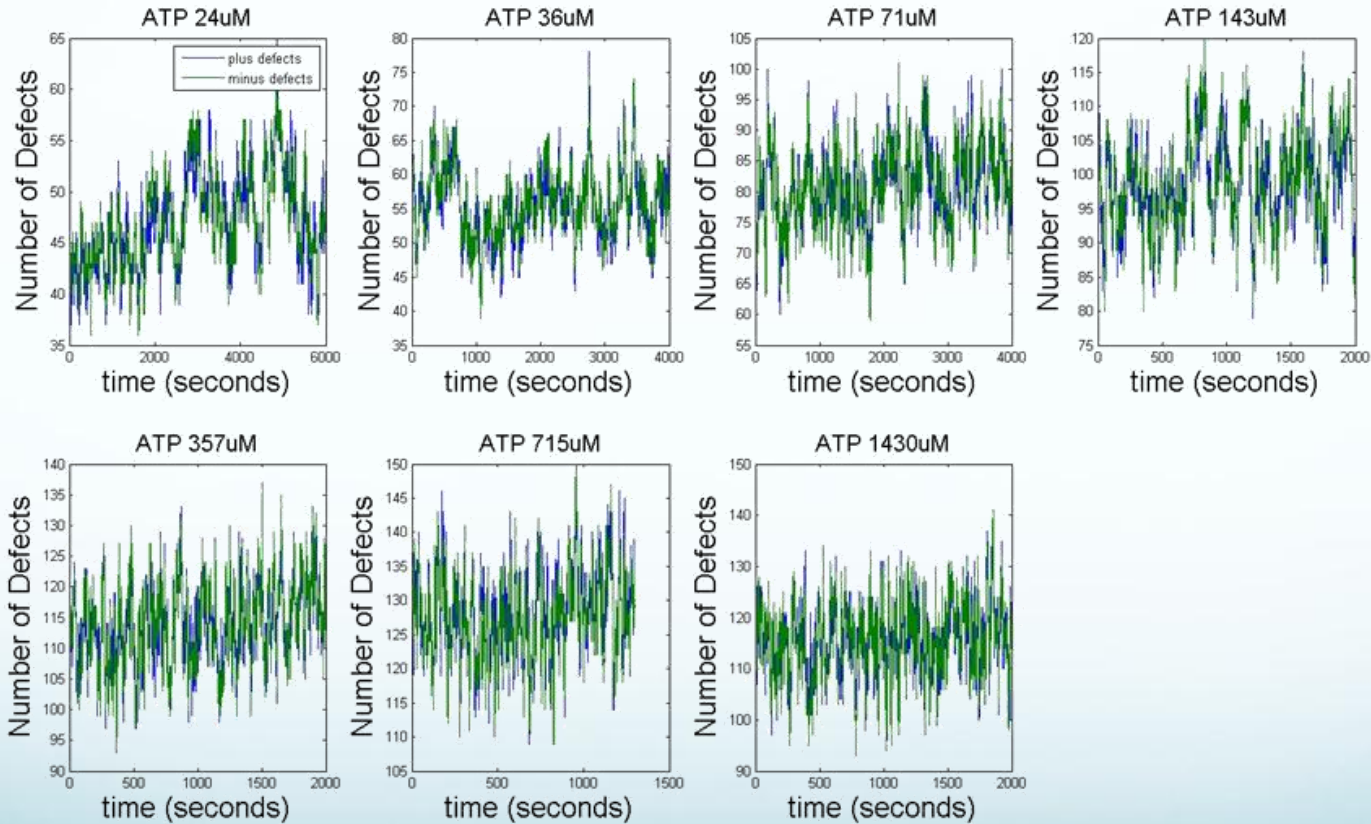


steady-state rate of defect creation and annihilation

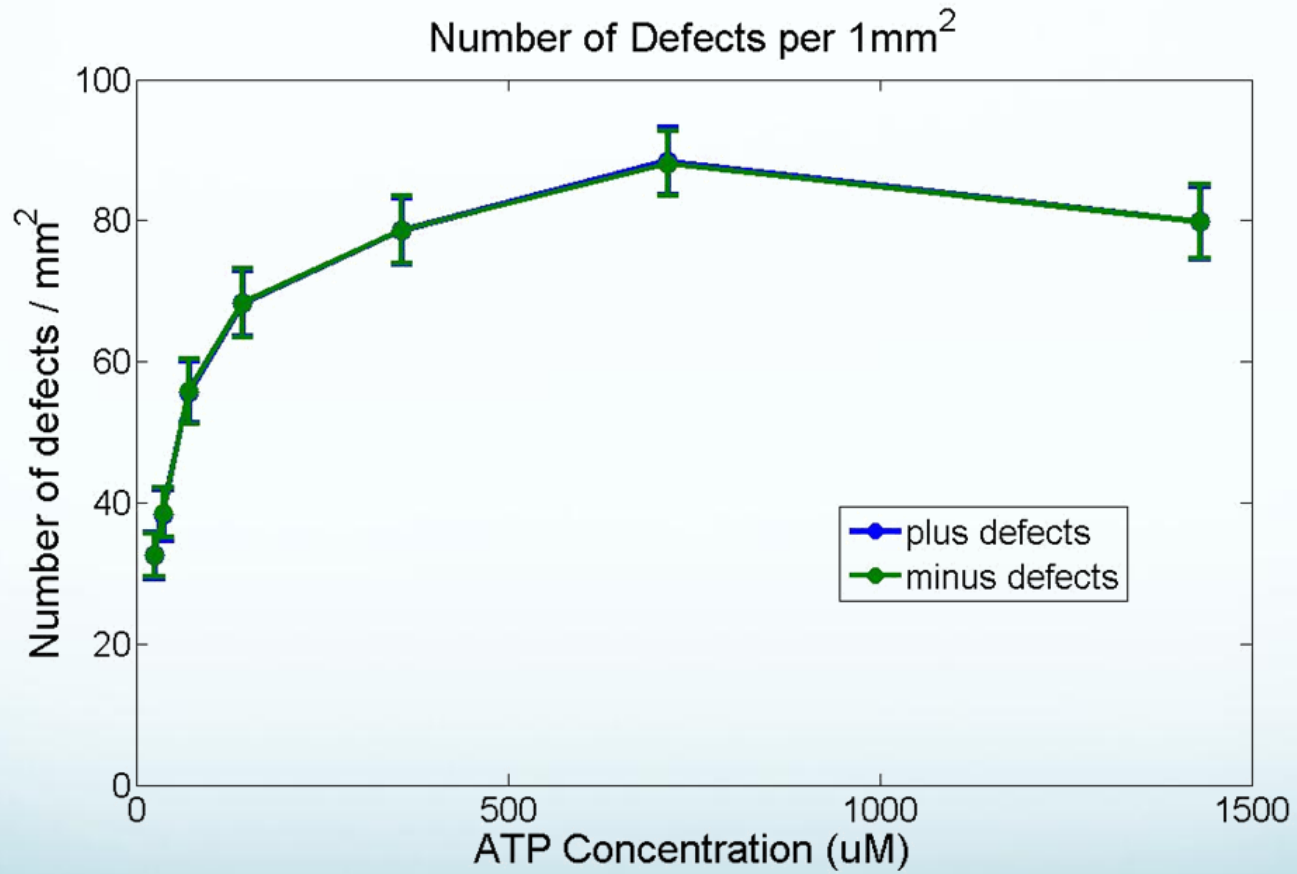




# Number of Defects vs Time

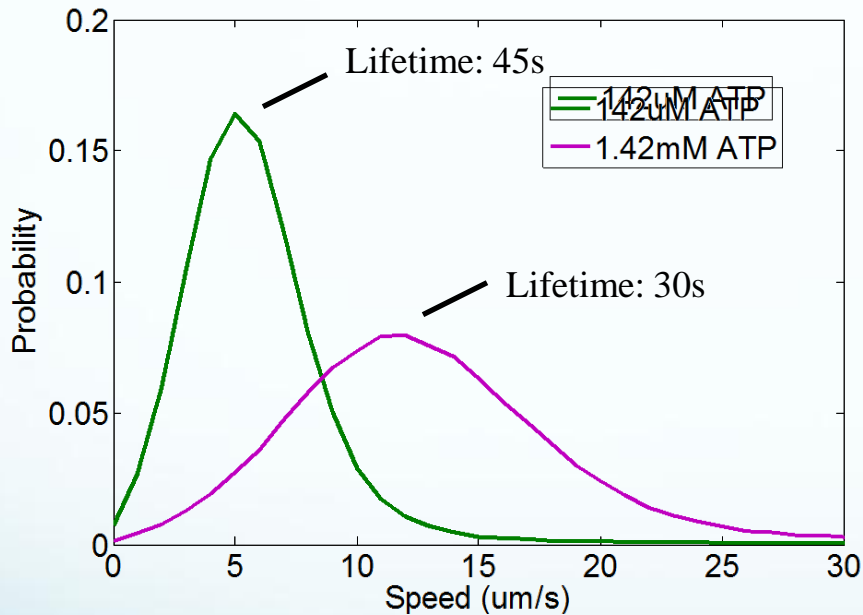


# Defect Density

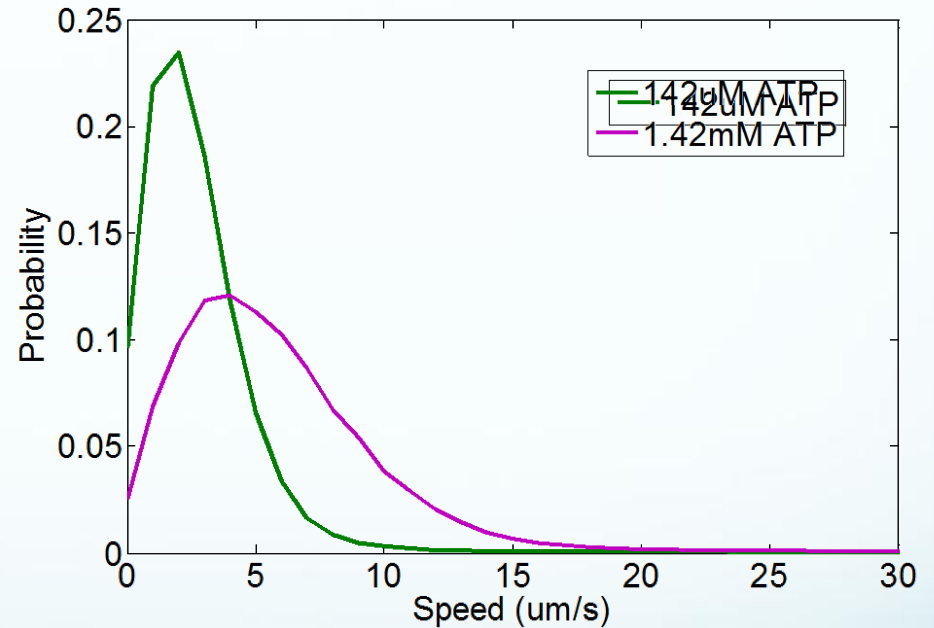


# Tunable Defect Speeds

Speed of +1/2 Defects



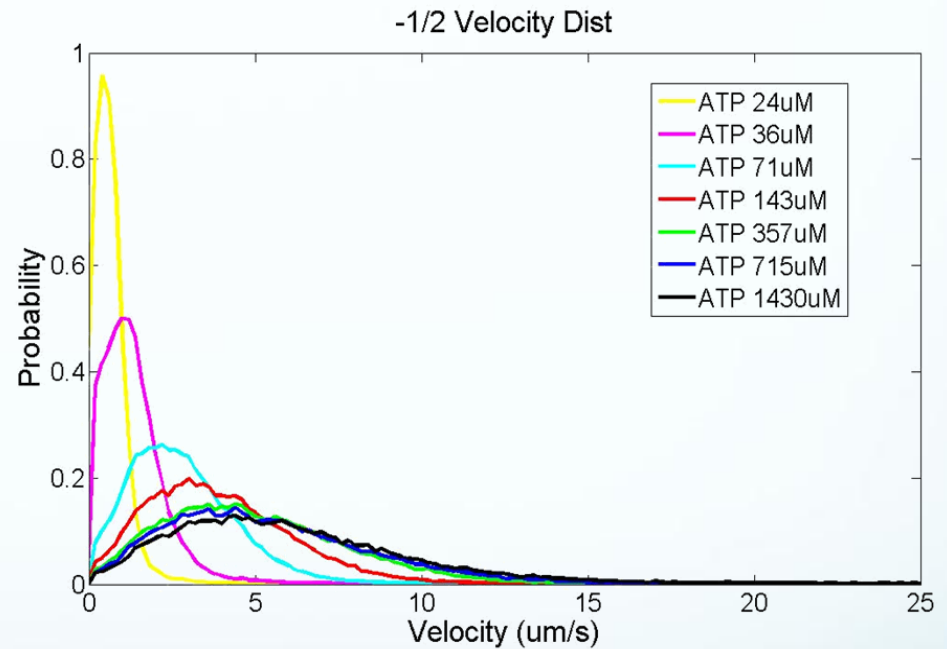
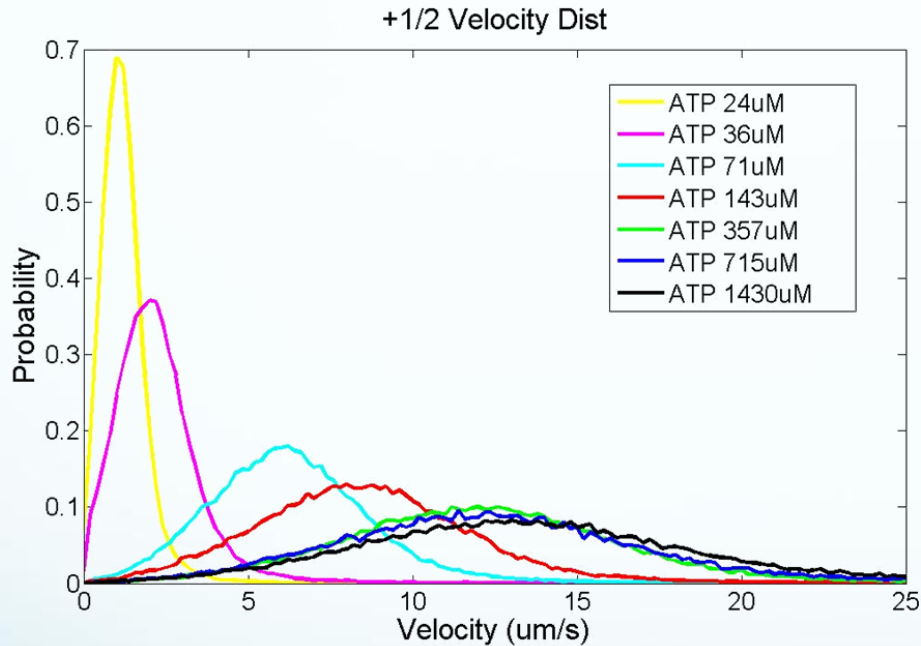
Speed of -1/2 Defects



+1/2 Defects stream faster than -1/2 defects.  
System is tunable – [ATP] tunes activity

Speeds from inter-frame displacements.

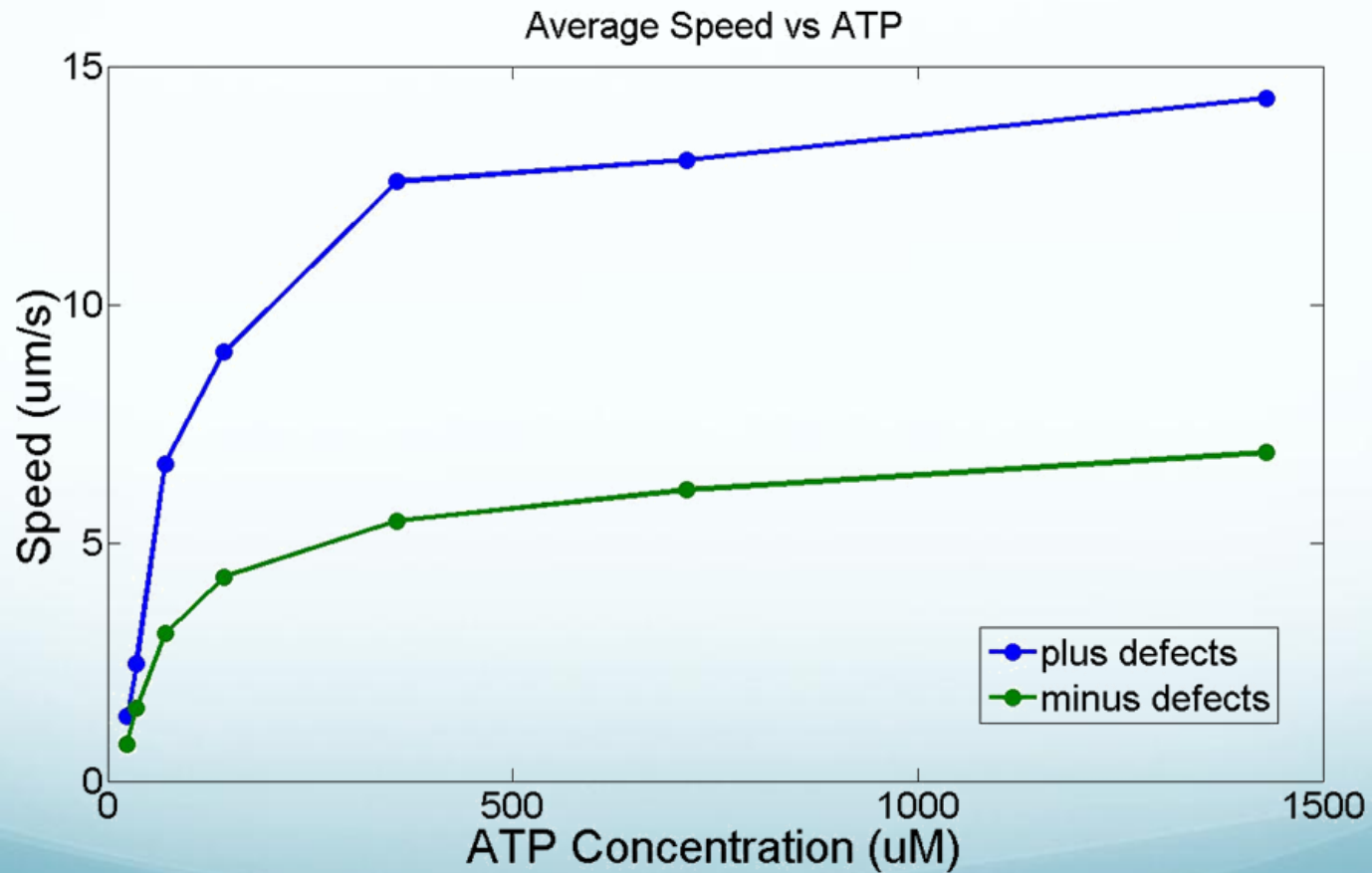
# Tunable Defect Speeds



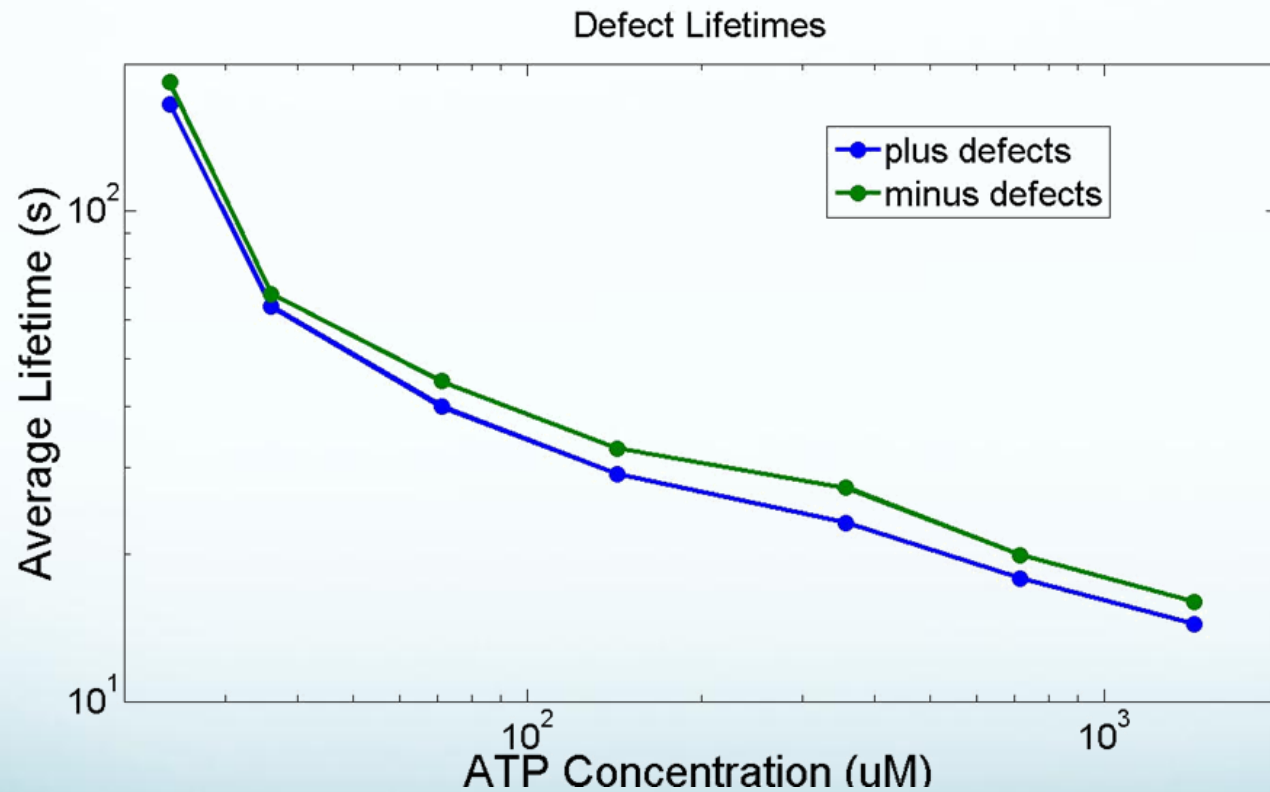
+1/2 Defects stream faster than -1/2 defects.  
System is tunable – [ATP] tunes activity

Speeds from inter-frame displacements.

# Average Speed vs ATP

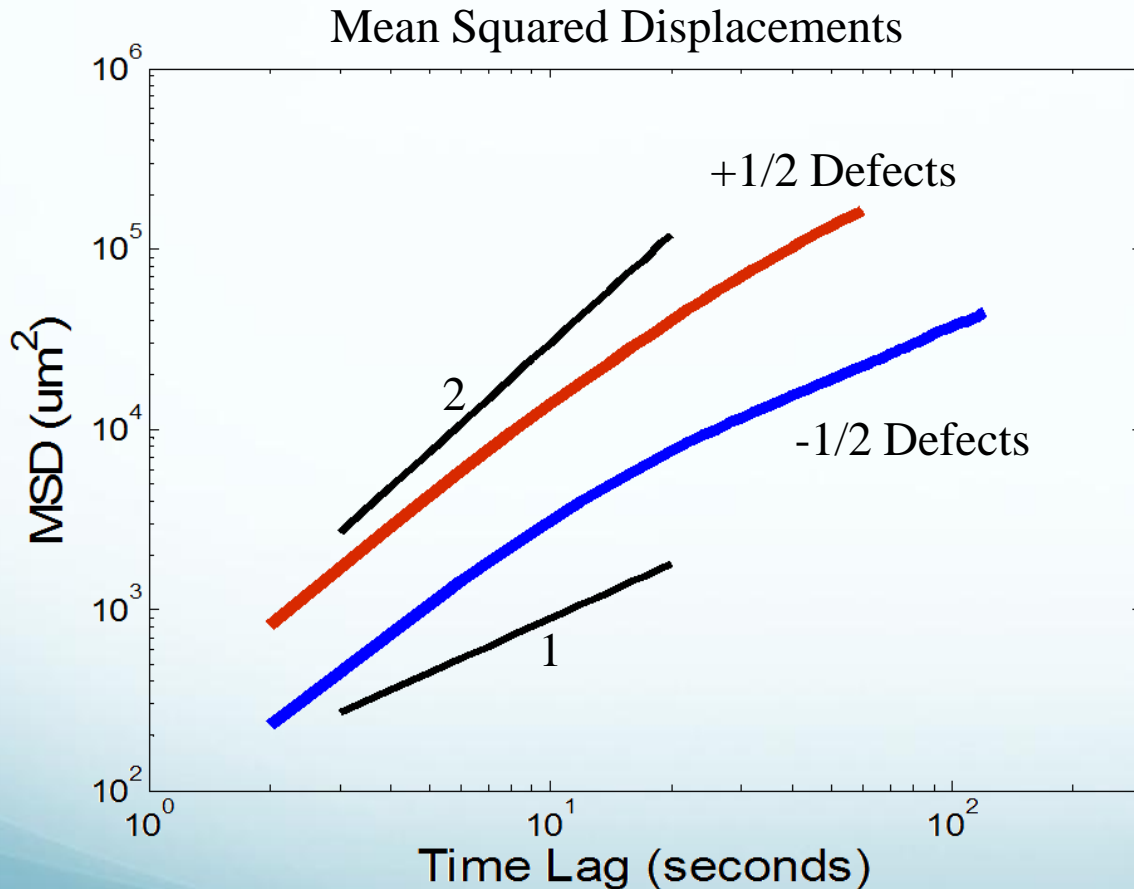


# Defect Lifetimes



The average lifetime of a defect vs ATP concentration.

# Defect MSDs



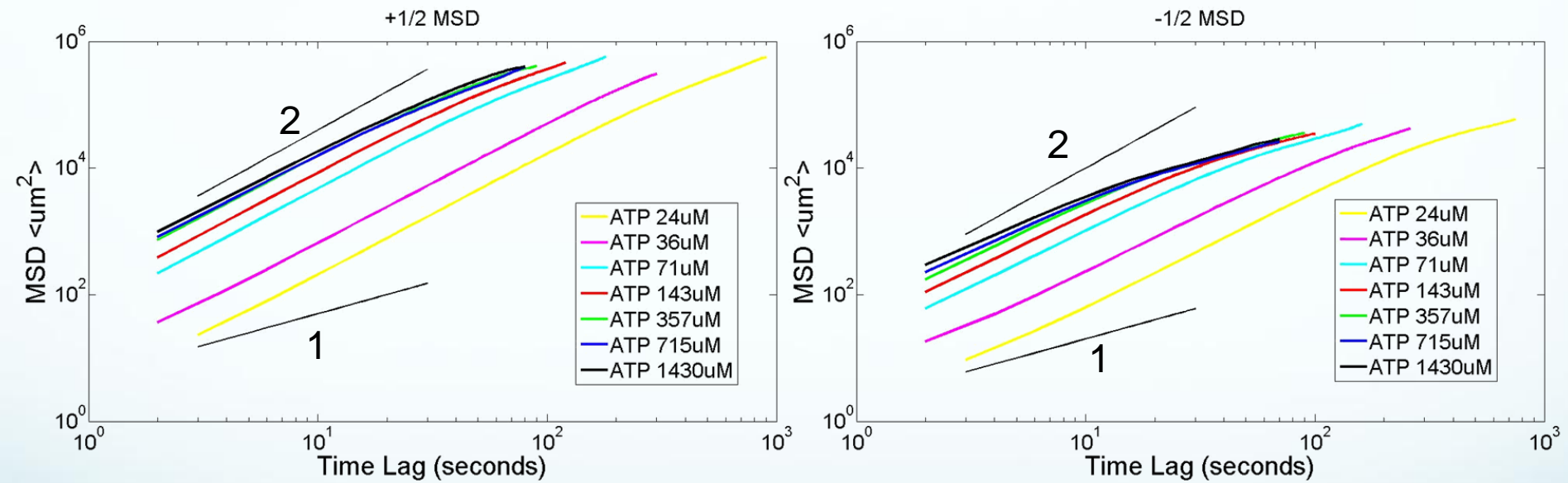
Asymmetric +1/2 defects drive motion of -1/2 defects.

-1/2 defects exhibit Brownian-like dynamics due to random kicks by +1/2 defects.

Data for 1.42mM ATP

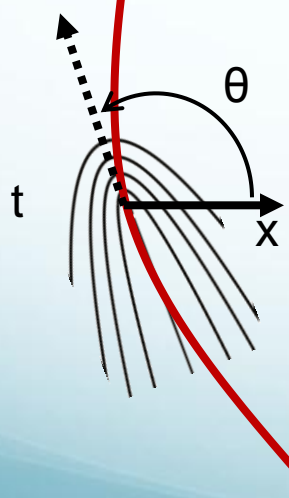
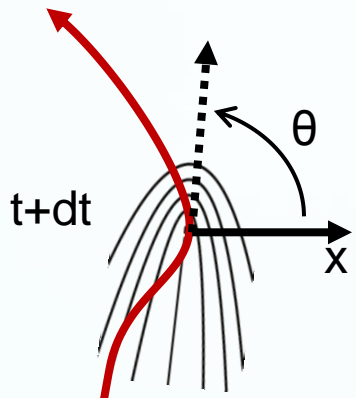


# Defect MSDs vs ATP



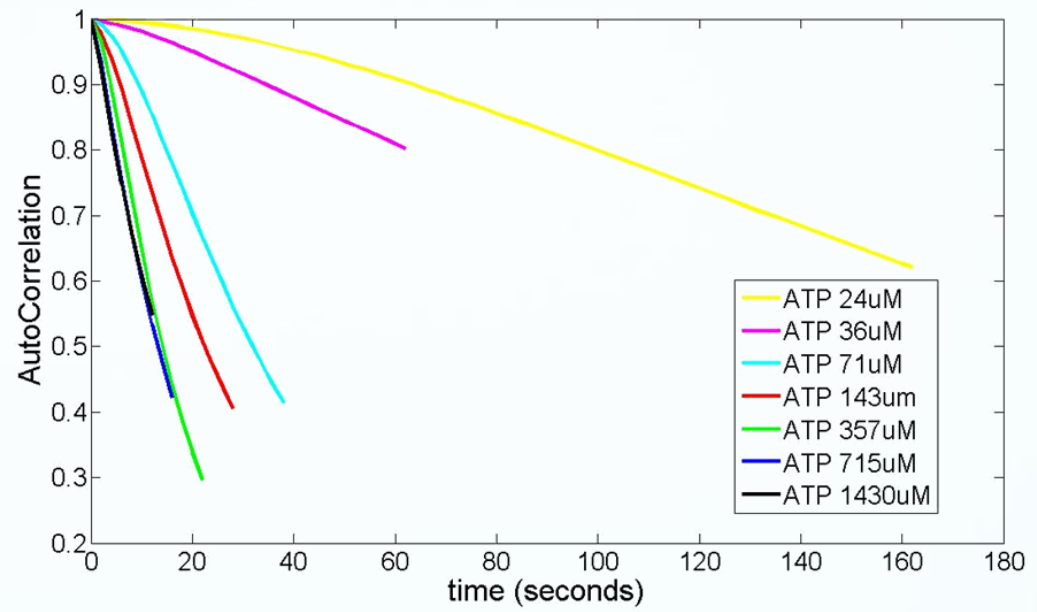
# Persistence of Orientation

$$\langle \theta(t) * \theta(t+dt) \rangle$$

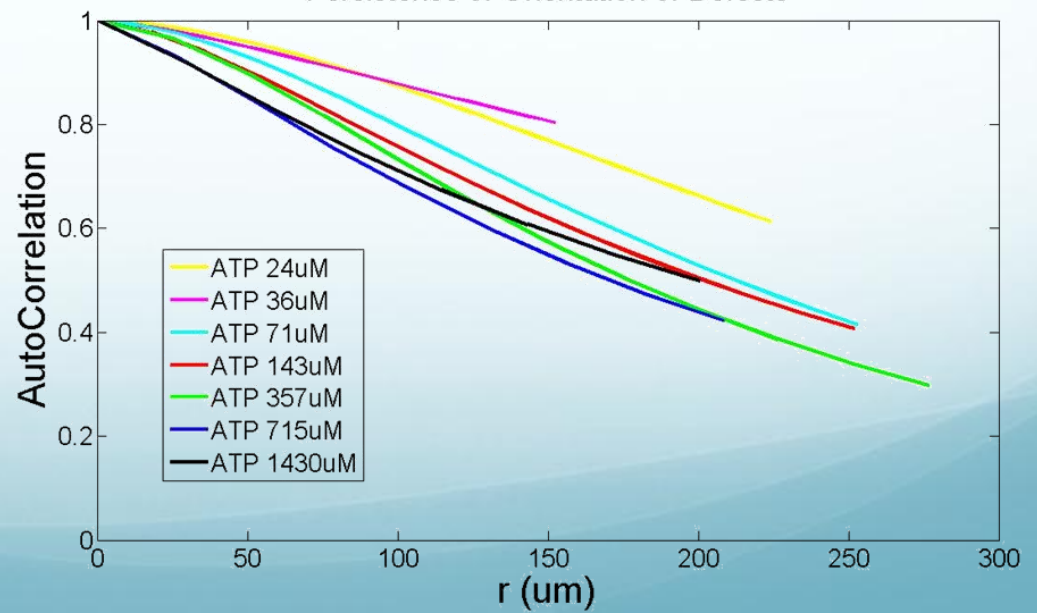


+1/2 Defect Trajectory

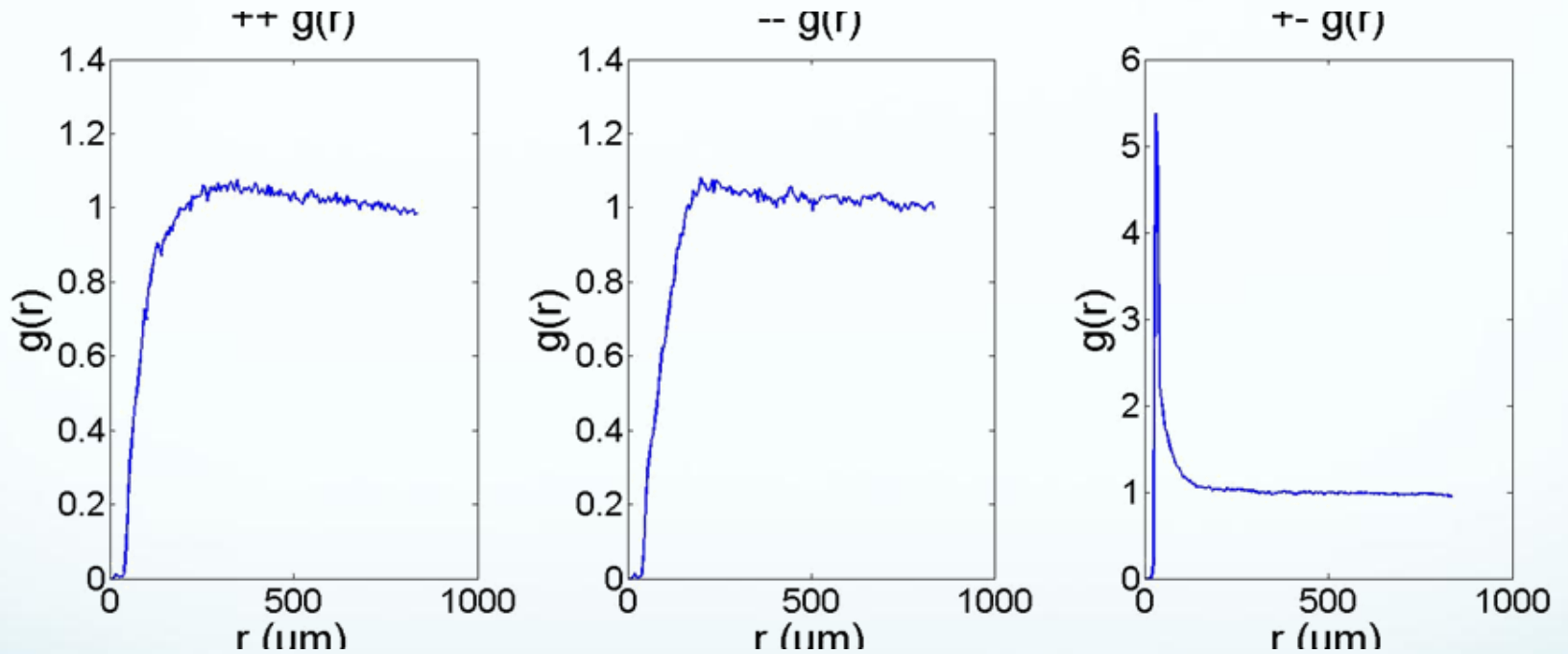
Persistence of Orientation of Defects



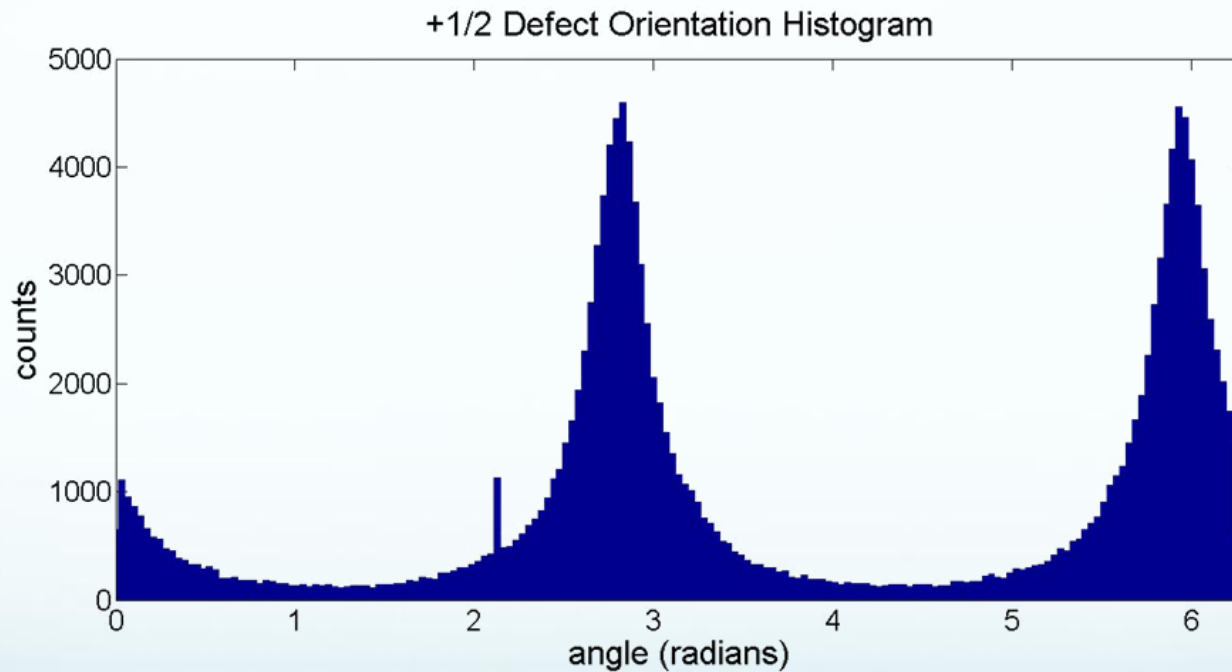
Persistence of Orientation of Defects



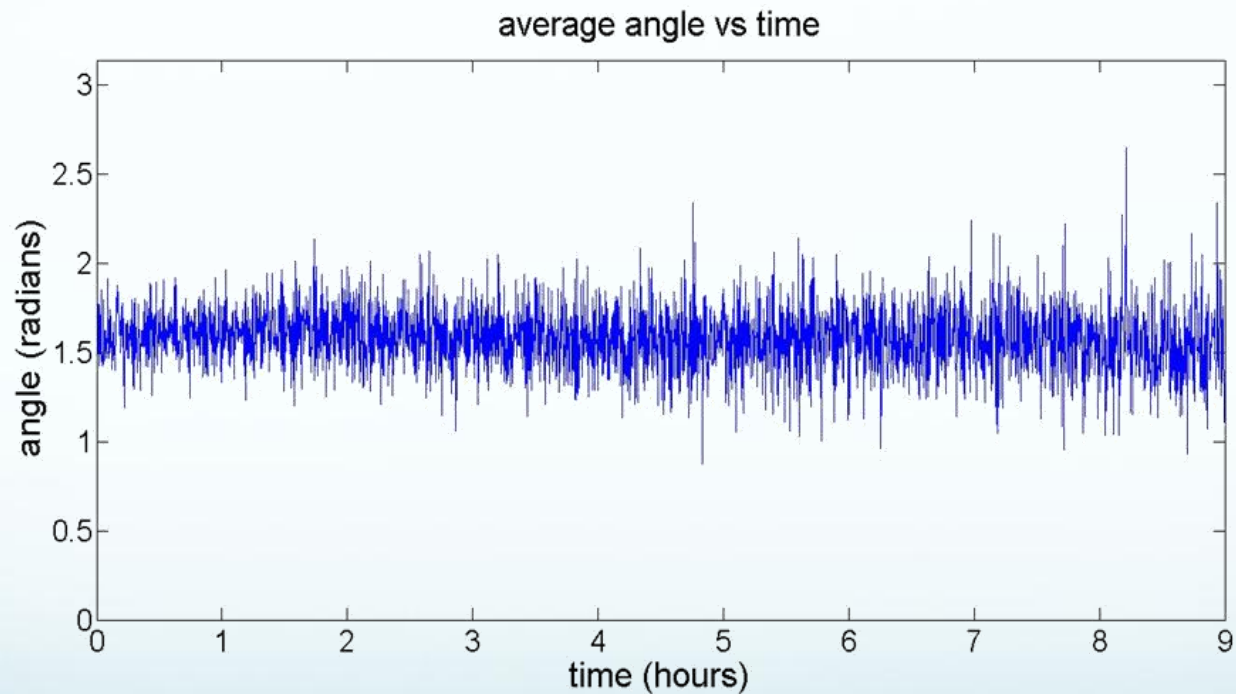
# Spatial structure of active nematic defects



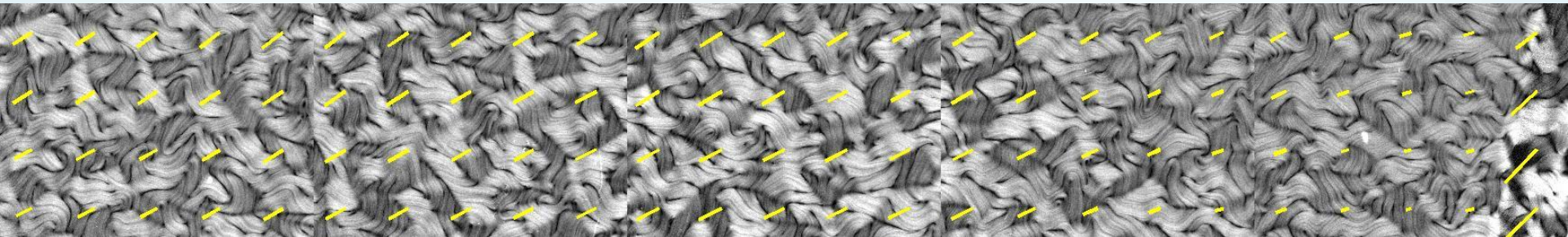
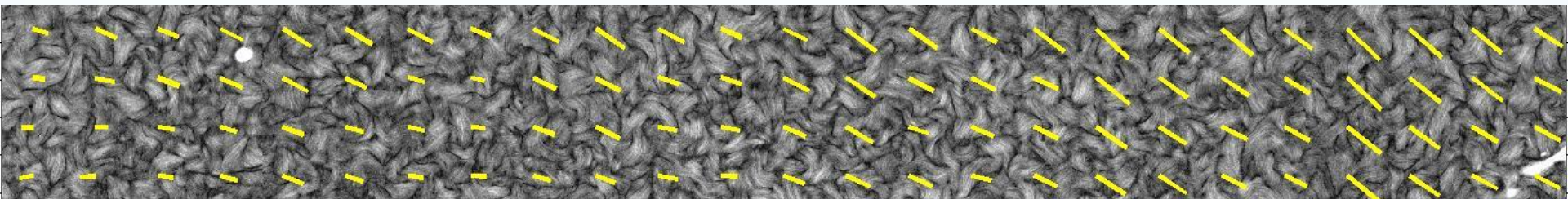
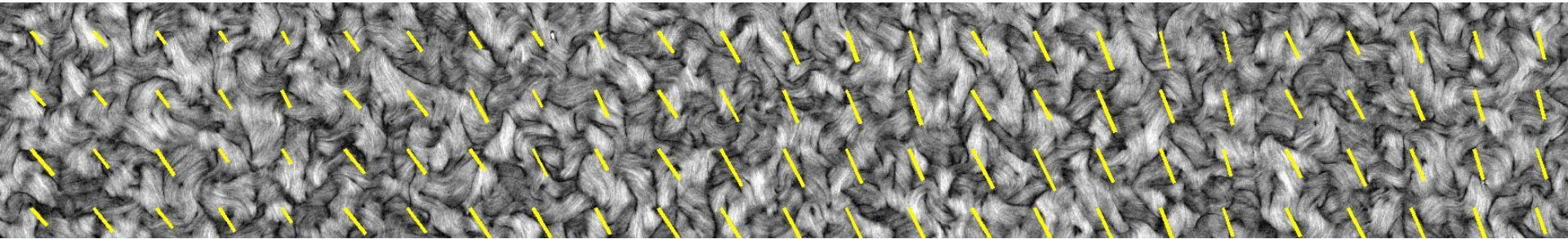
# +1/2 defect from a nematic phase



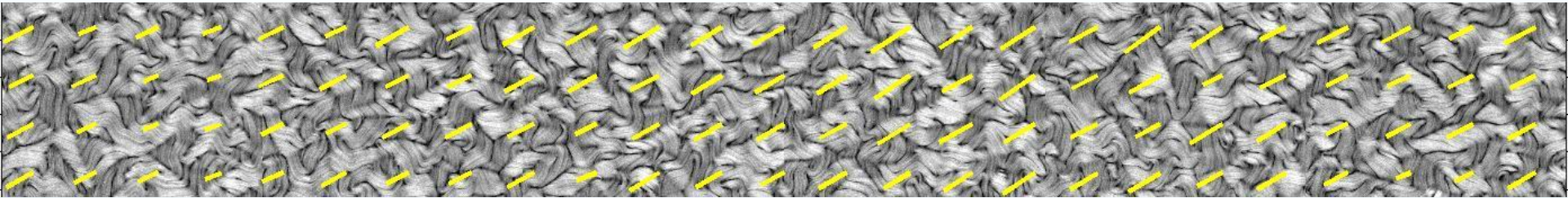
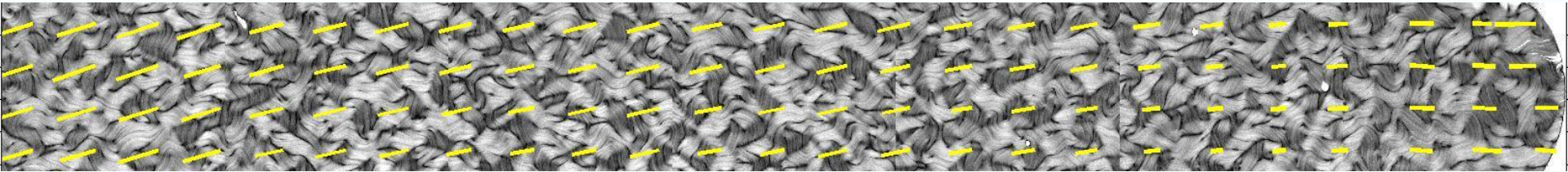
# Time evolution of nematic director



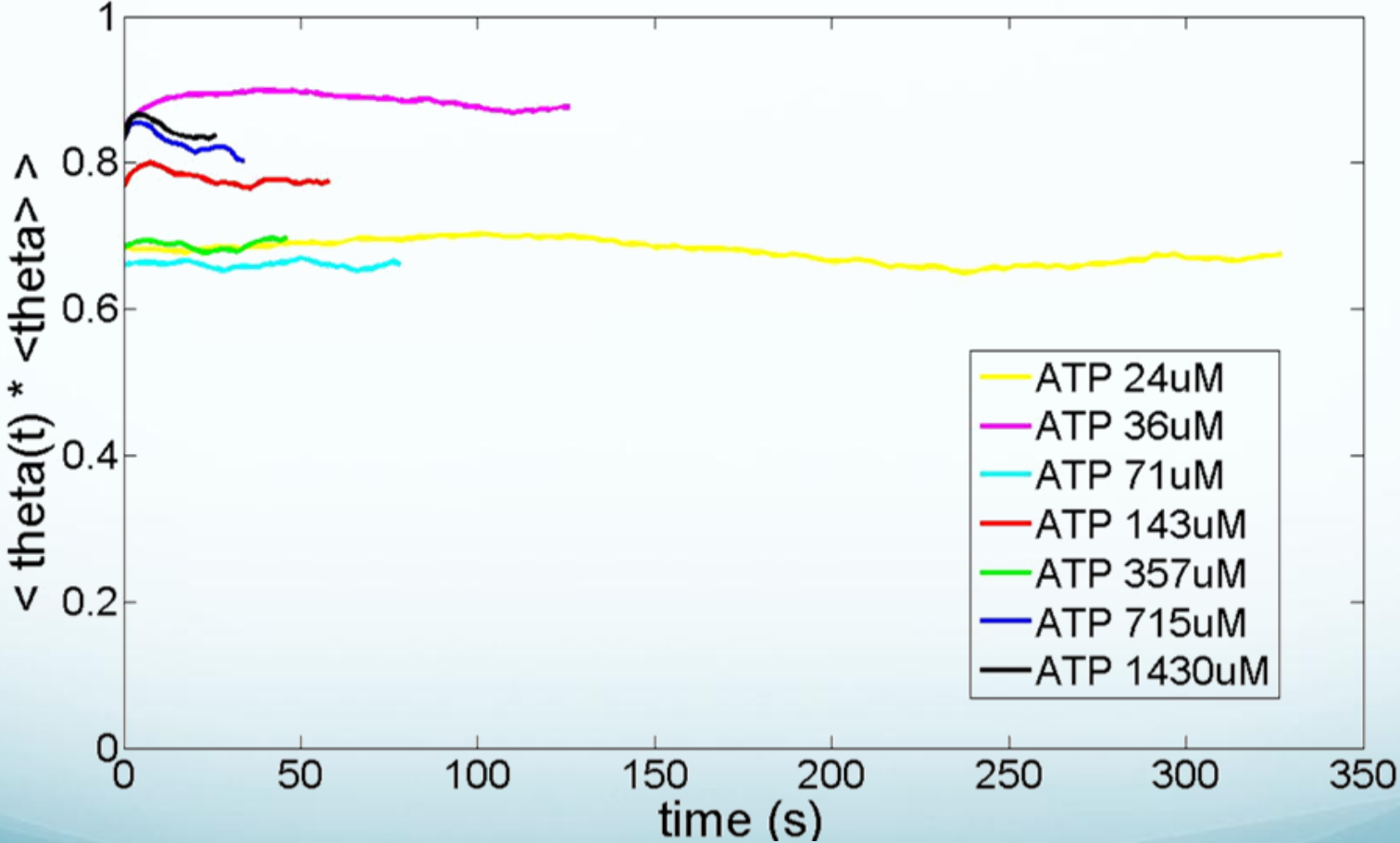
# Large Spatial Coherence



# Large Spatial Coherence

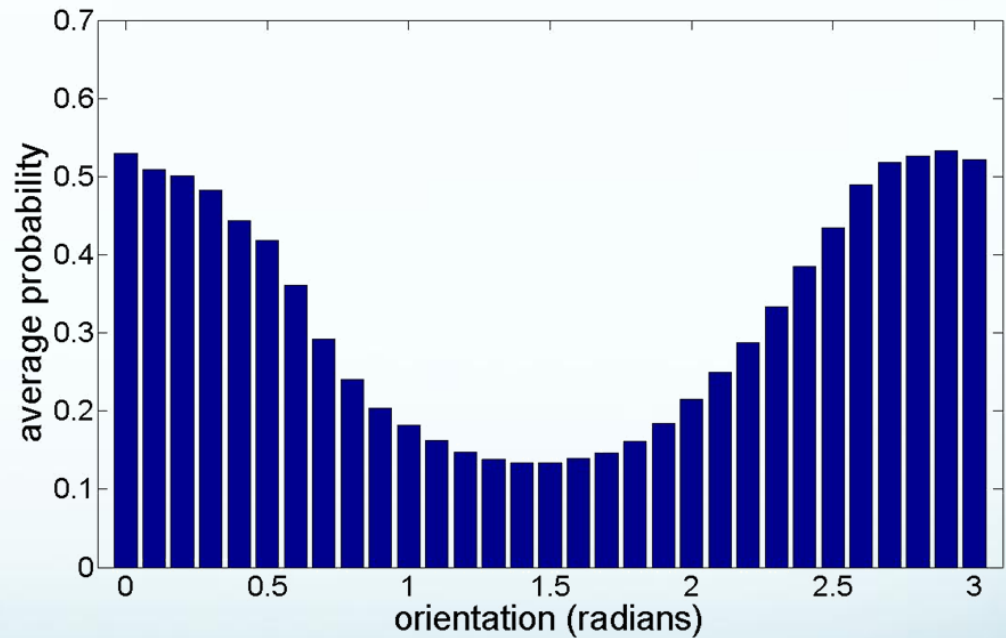
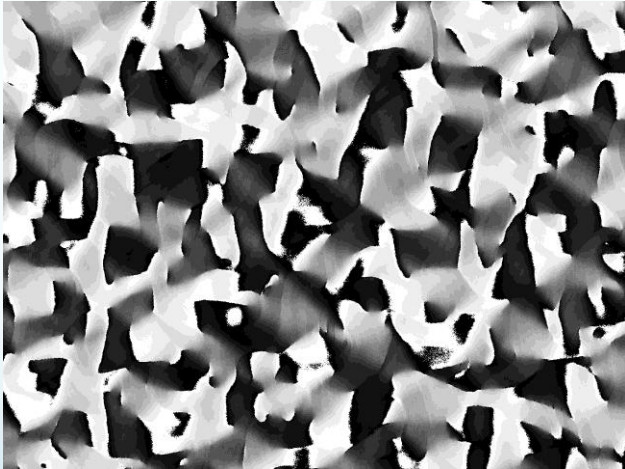


# Defect orientation does not depend of the defect age





# Average Nematic Director Orientation



## 2D active nematics

- bend deformation is unstable – gives rise to defect generation
- steady state – balanced rate of defect generation and annihilation.
- at larger scales defect organize into a nematic recovering long range order
- defect velocity is determined by activity coefficient (ATP conc)

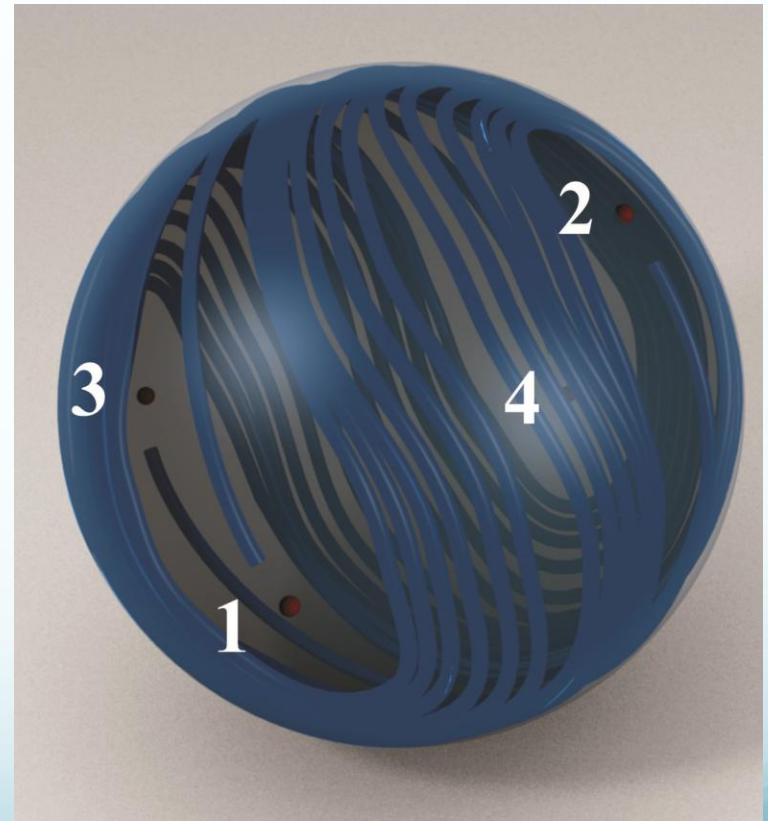
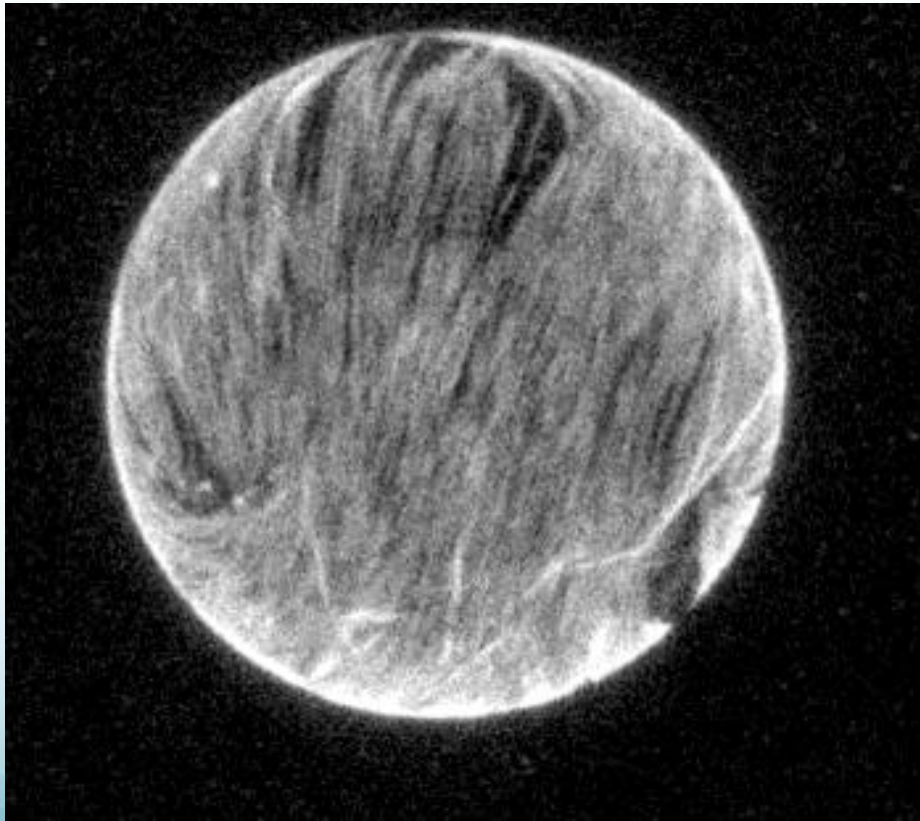
correlate flow velocity and director dynamics



# Motile defects on a spherical surface

Constraint on defect dynamics

- minimize elastic interaction energy
- move with preferred direction
- move with speed determined by activity coefficient (ATP concentration)

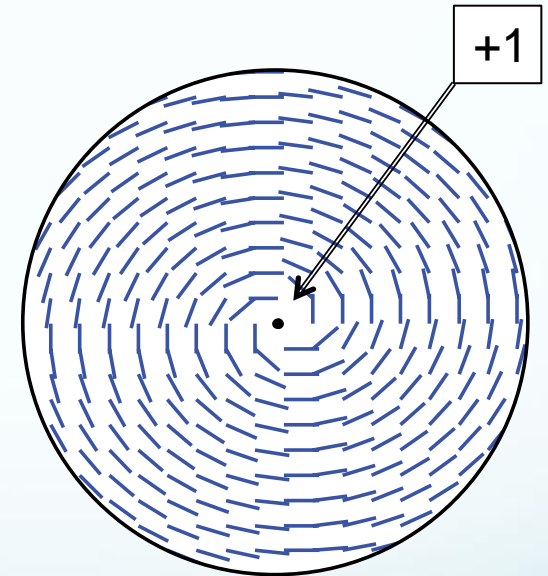
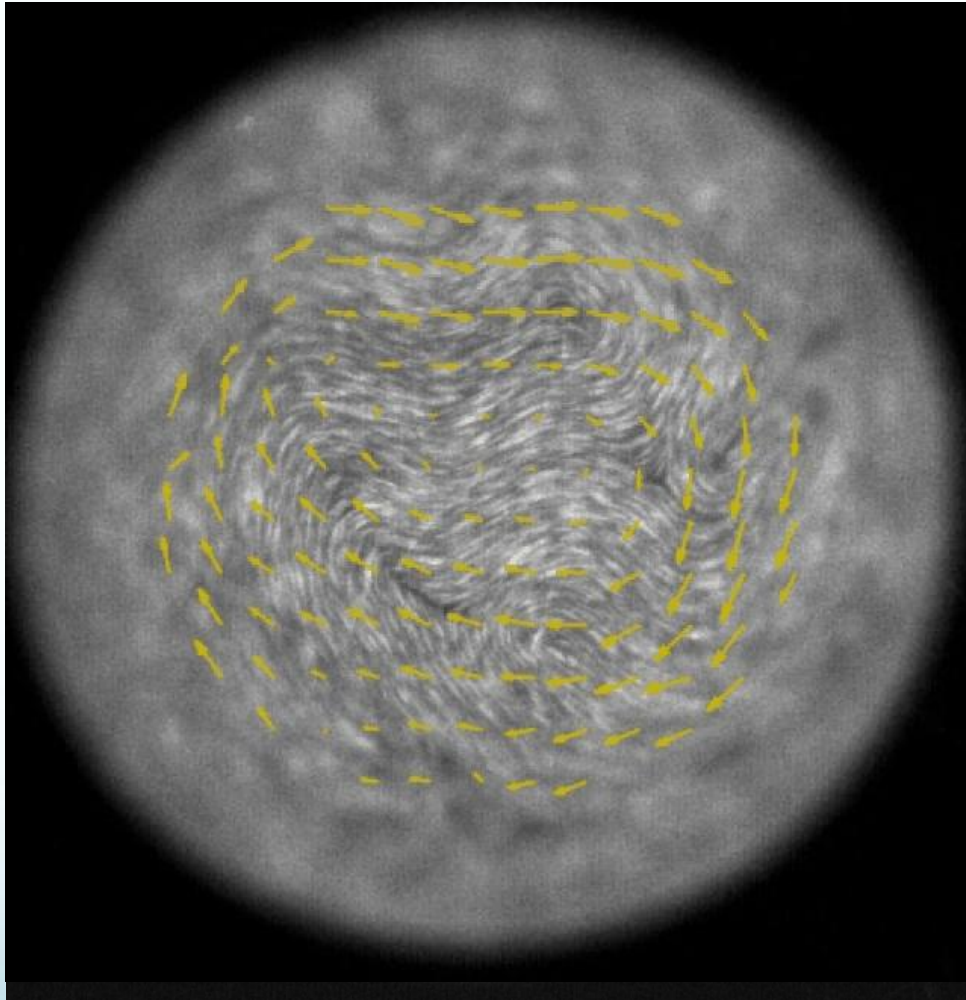


What is the defect dynamics on spherical surface?

Are trajectories chaotic or periodic?

# Active MT liquid crystals on a 2D circular membrane

- persistent unidirectional circular flows (> 24 hrs)



$$\text{Total charge} = \frac{1}{2} + \frac{1}{2} + \frac{1}{2} - \frac{1}{2} = +1$$

Can two clocks synchronize through hydrodynamic interactions?

What is dynamics of active nematics on a annulus?

# Isotropic active gels: solid or liquid?



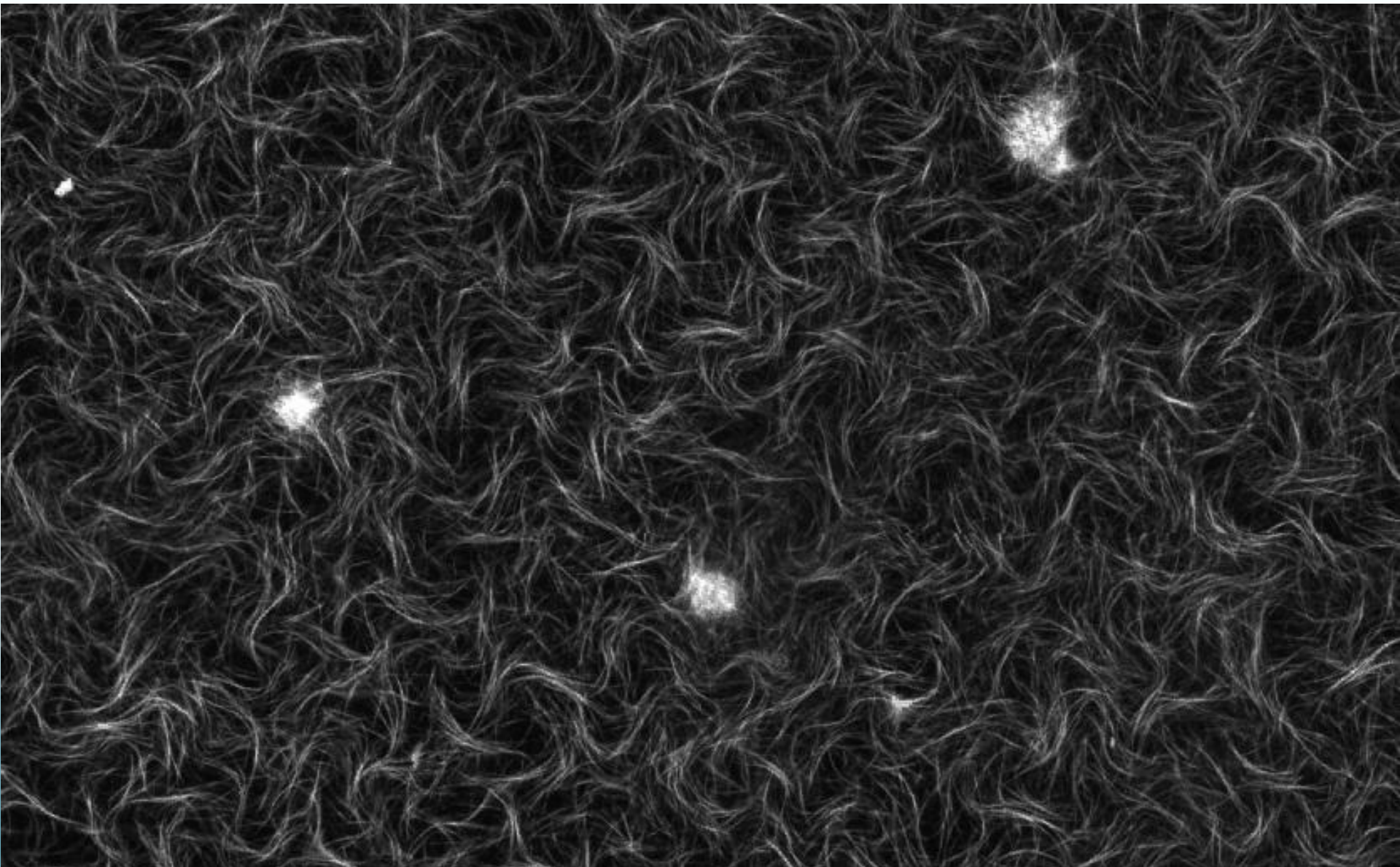
Daniel Chen



Daniel Blair

# Active Isotropic Gels in 3D

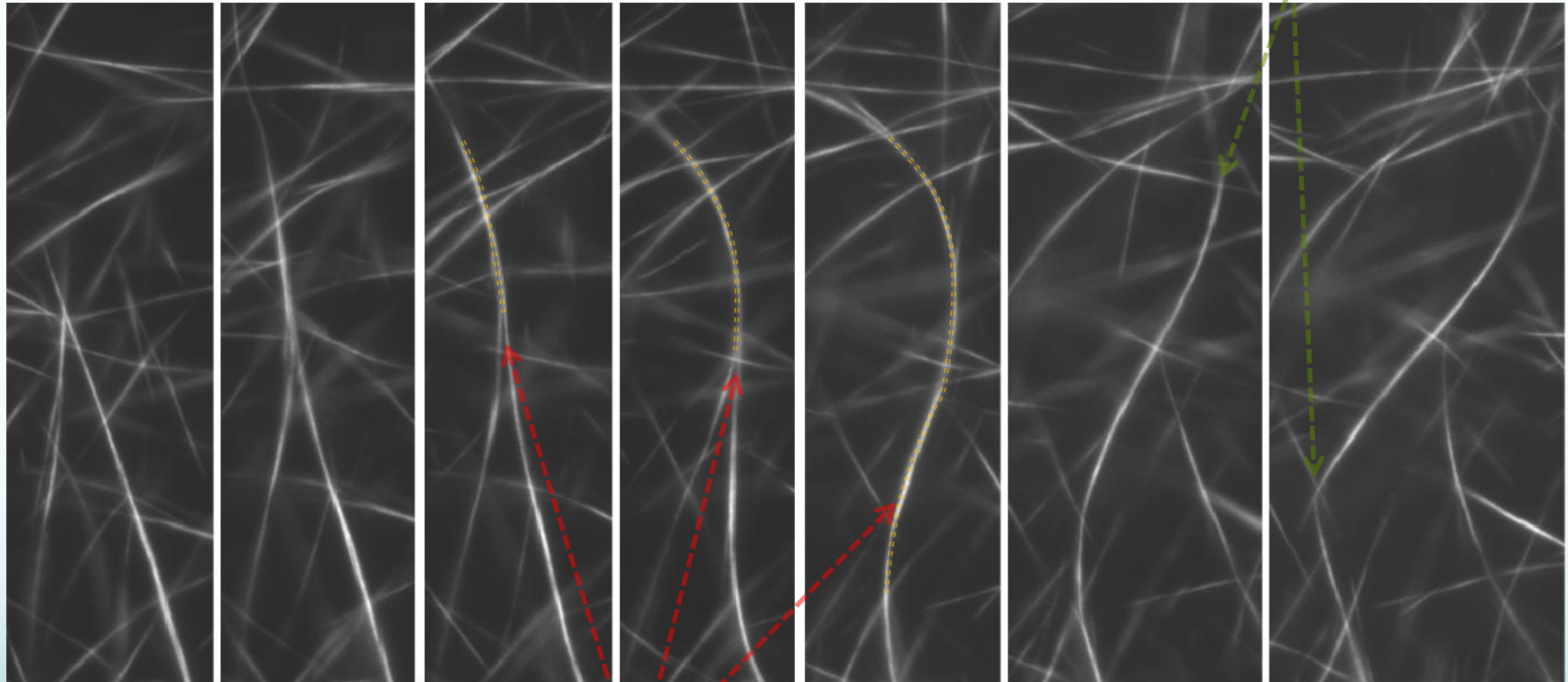
1500  $\mu\text{m}$



# MT dynamics in active gels

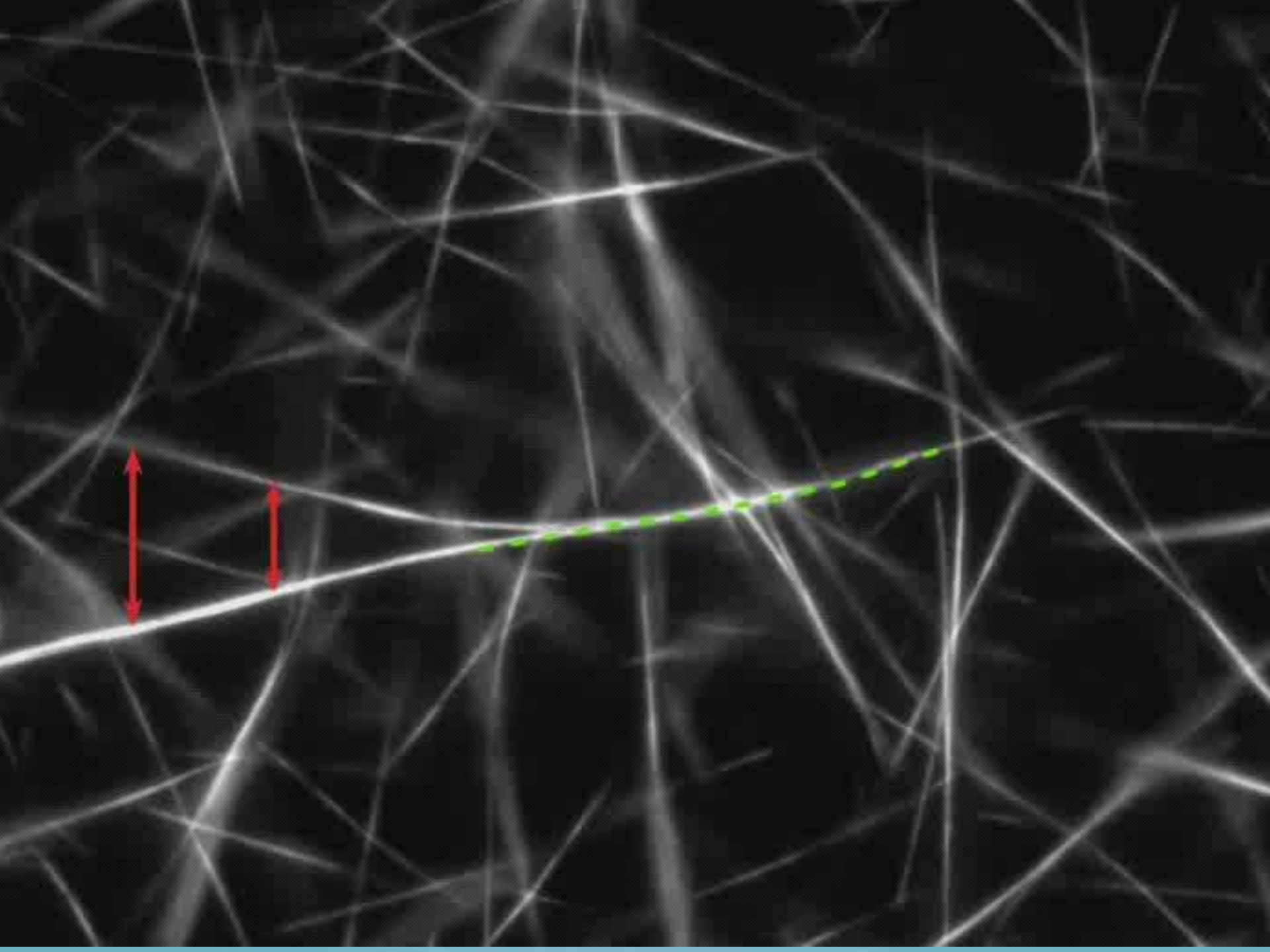
extension, polarity sorting  
and buckling

bundle fracture

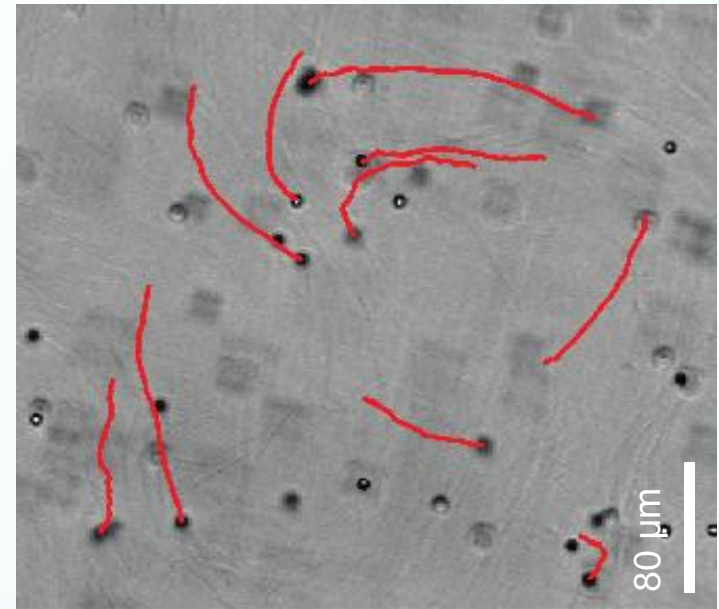
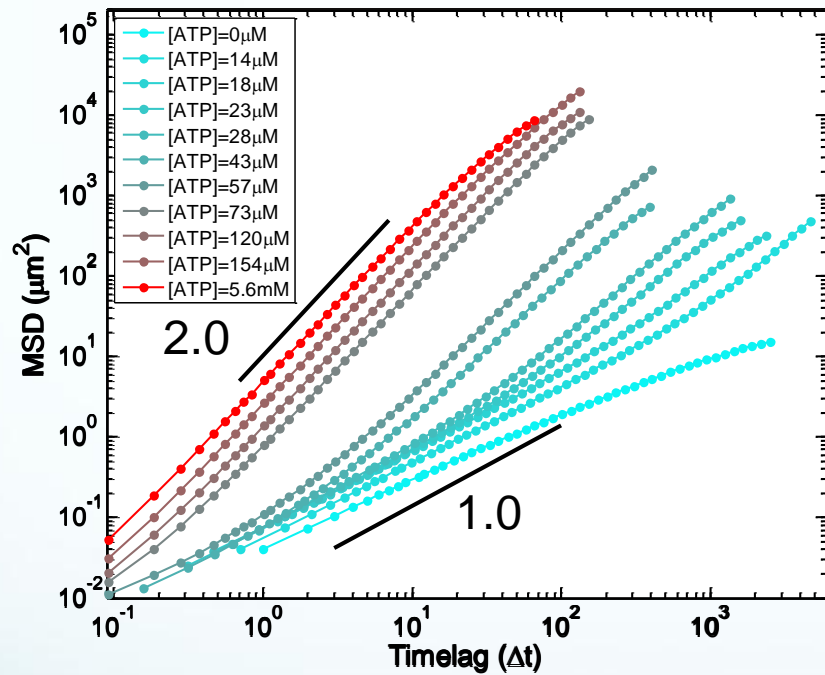


bundle merging





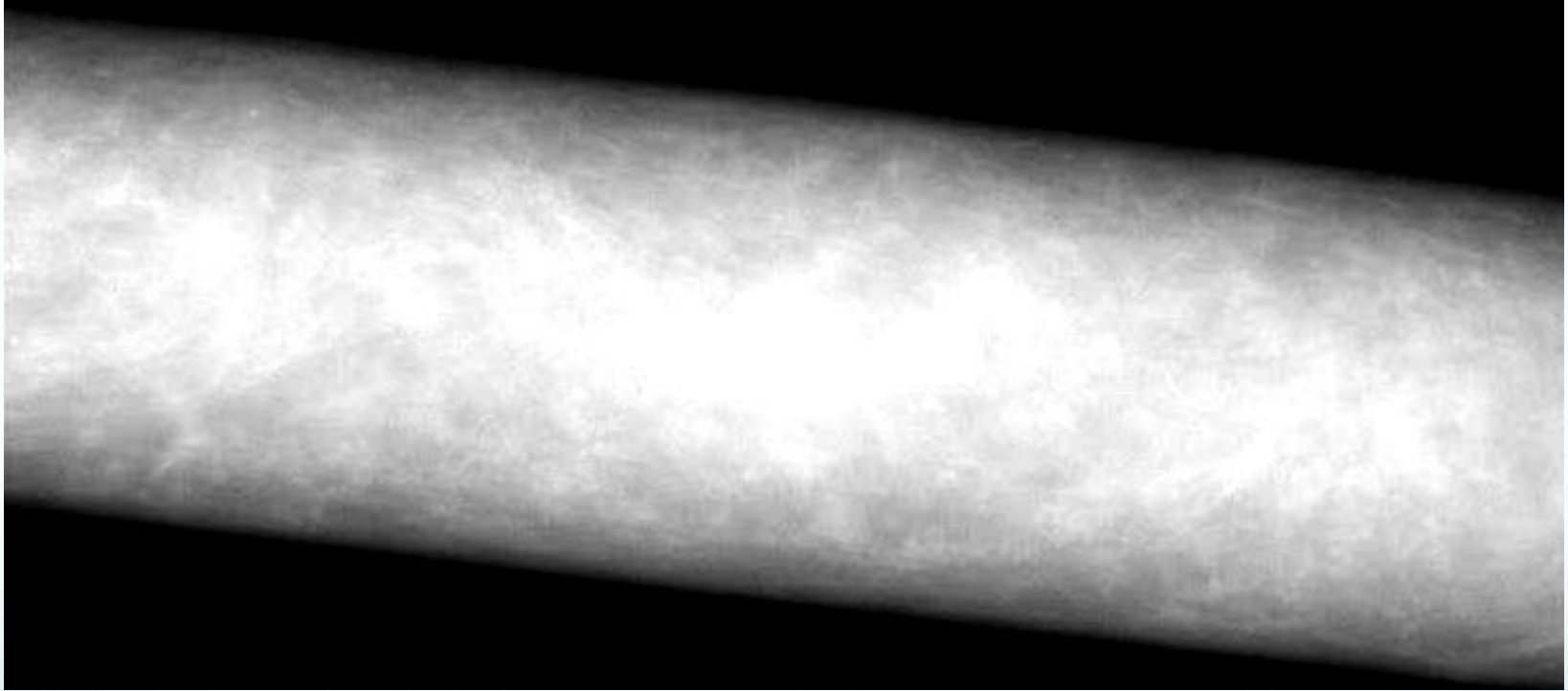
# Fluid Flow ATP-dependence: Particle MSD



Totally tunable from subdiffusive to ballistic (equilibrium to non-equilibrium)

# Recap, so far...

- assembly of isolated extensile MT bundles
- high bundle concentration – tunable active isotropic gels characterized by spontaneous internal flows, enhanced transport and mixing

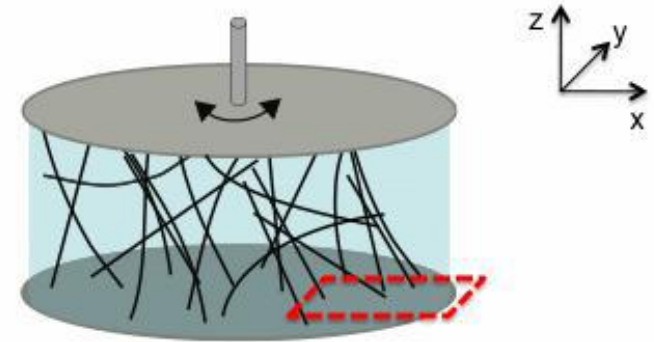
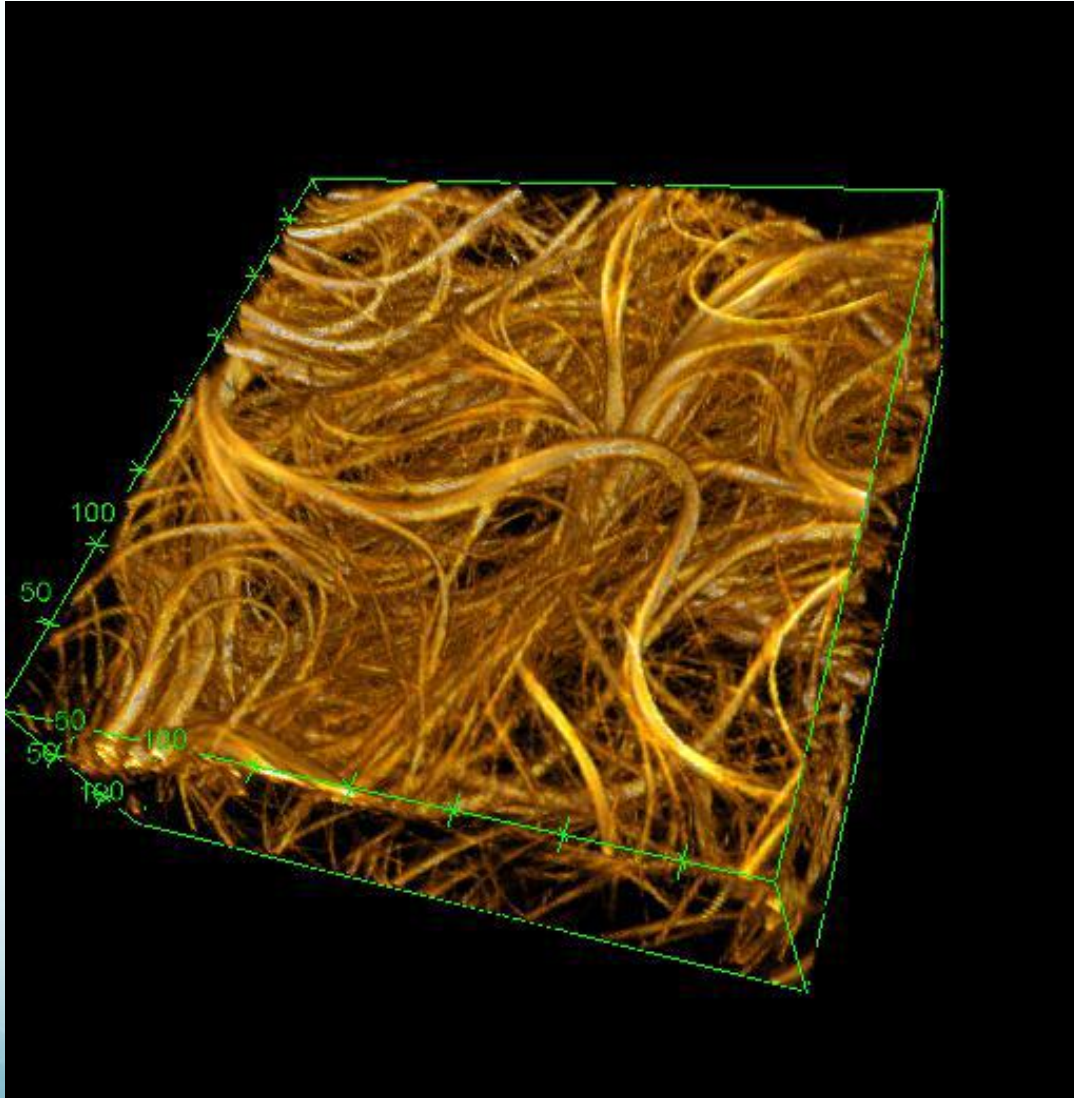


Active gels in confined geometries – emergence of spontaneous macroscopic flows

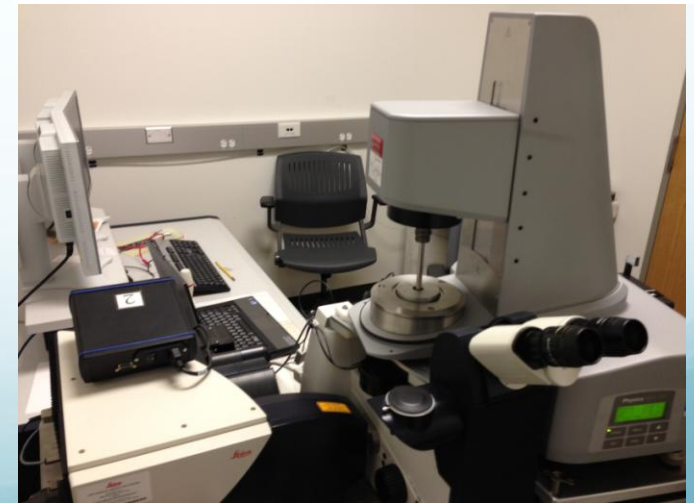
Soft materials that exerts force on their boundaries to produce macroscopic force

**How does the observed behavior depend on filament concentration?**

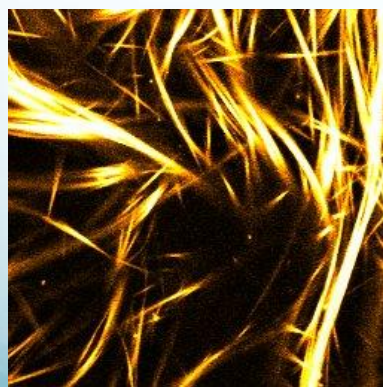
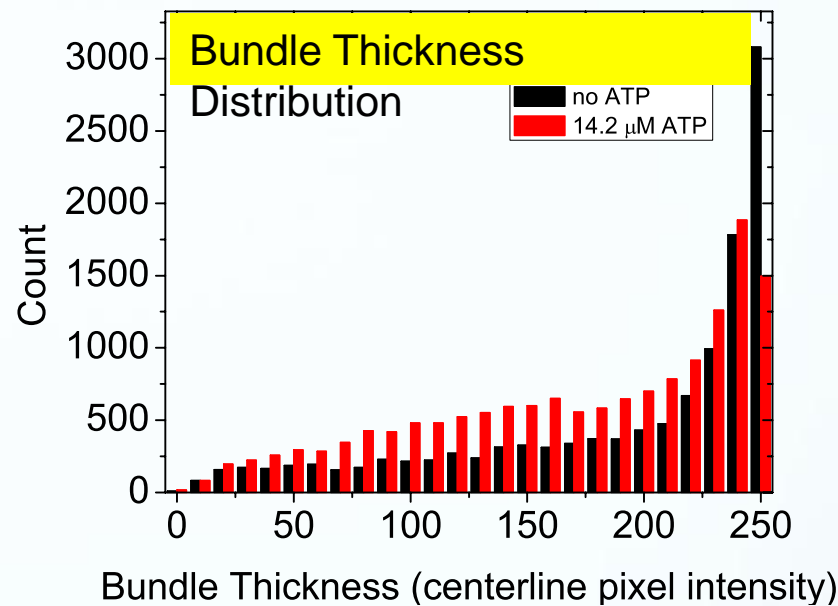
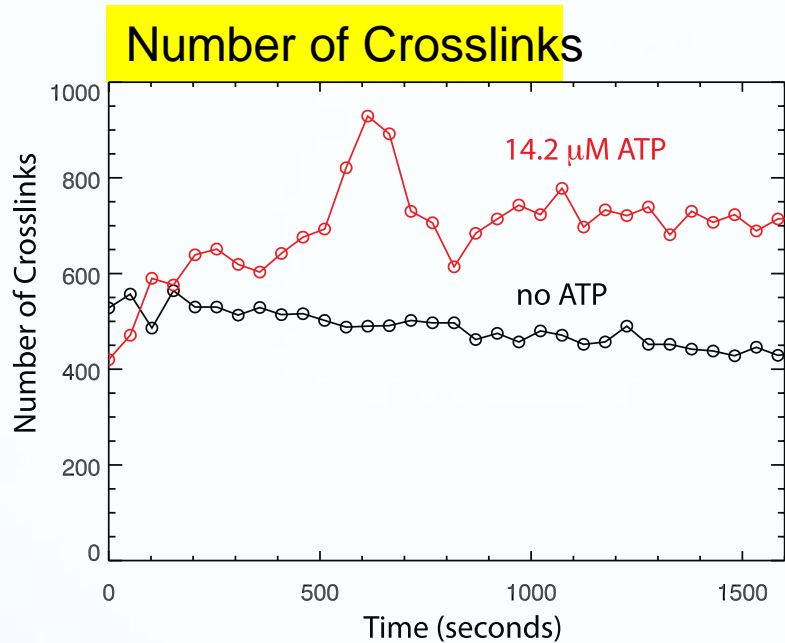
# Confocal Rheology of Active Networks



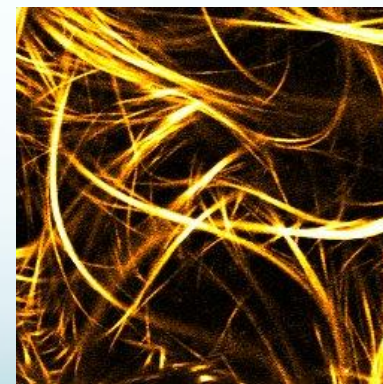
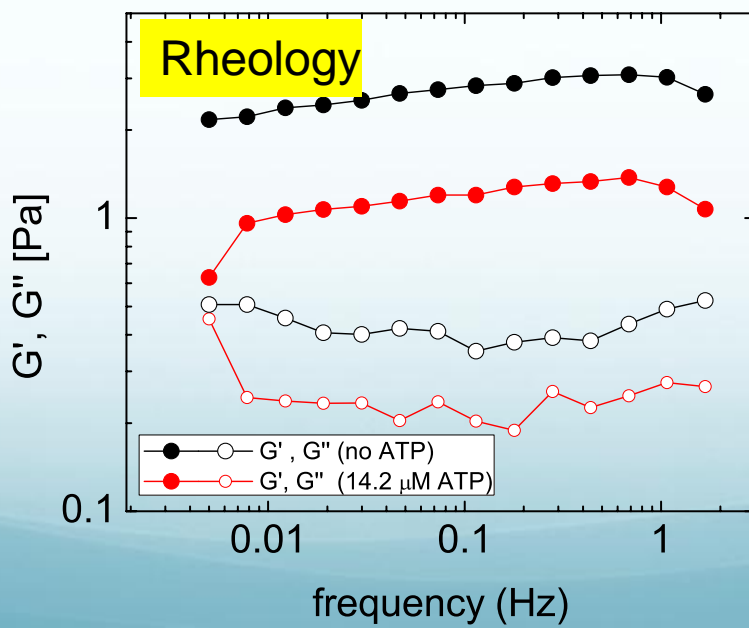
Confocal Microscope



# Network Morphology $\leftrightarrow$ Rheology

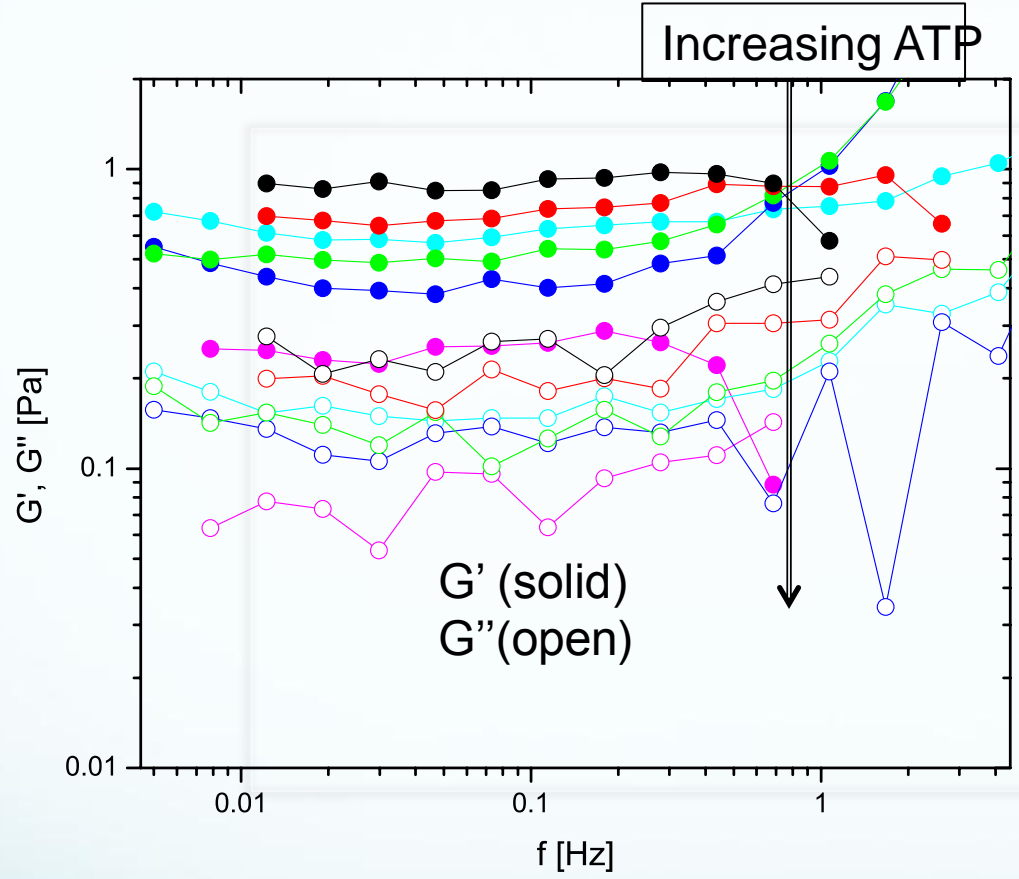


No ATP

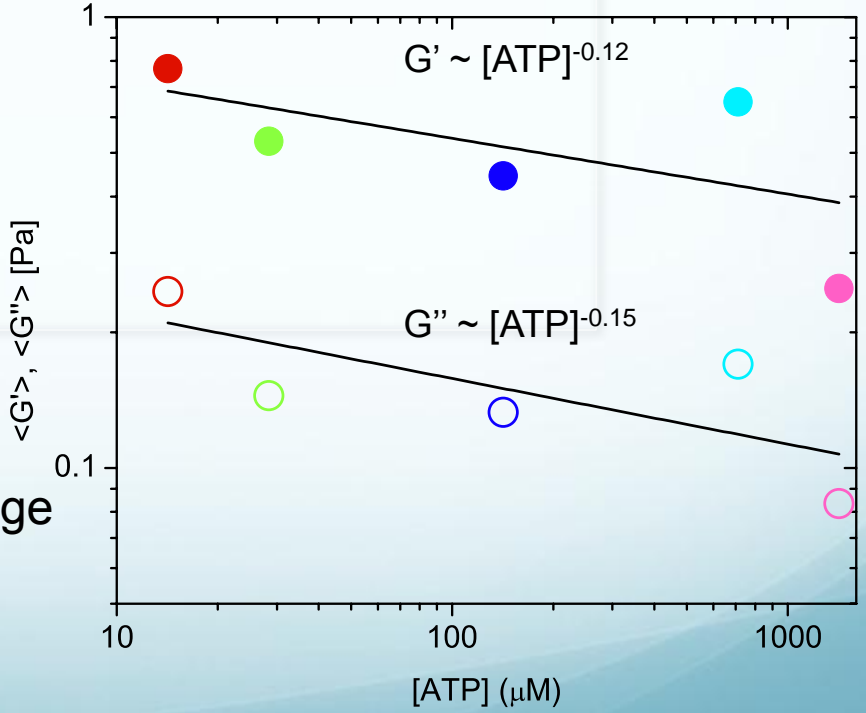


14.2 μM ATP

# Linear Viscoelastic Moduli of Active Network



- [ATP]
- 0  $\mu\text{M}$
  - 14.2  $\mu\text{M}$
  - 28.4  $\mu\text{M}$
  - 142  $\mu\text{M}$
  - 710  $\mu\text{M}$
  - 1.42 mM



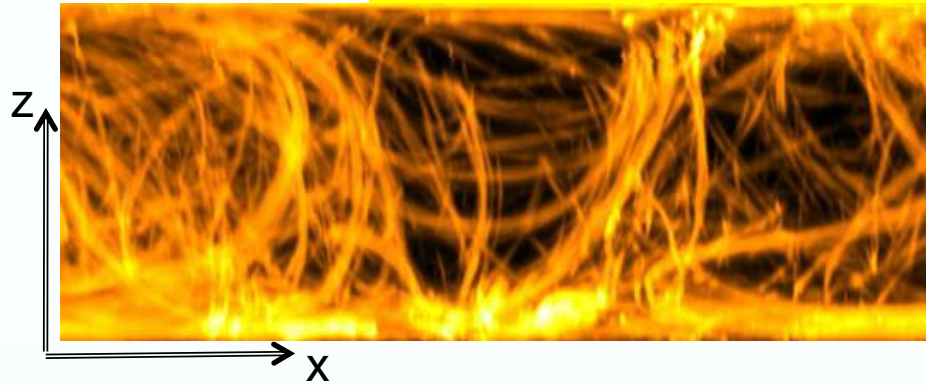
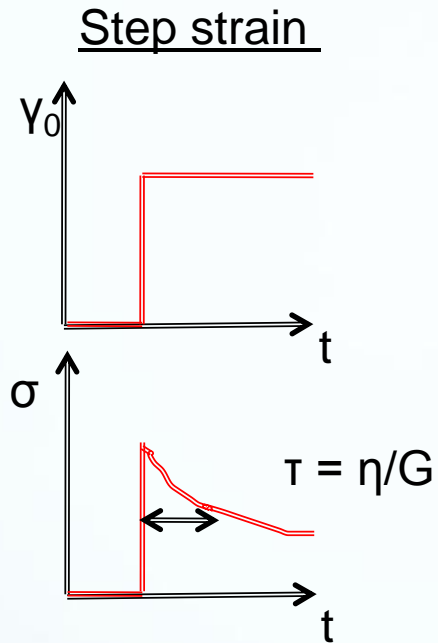
Network is a gel ( $G' > G''$ ) over entire [ATP] range

$G''/G' \sim 0.3$ , damping independent of [ATP]

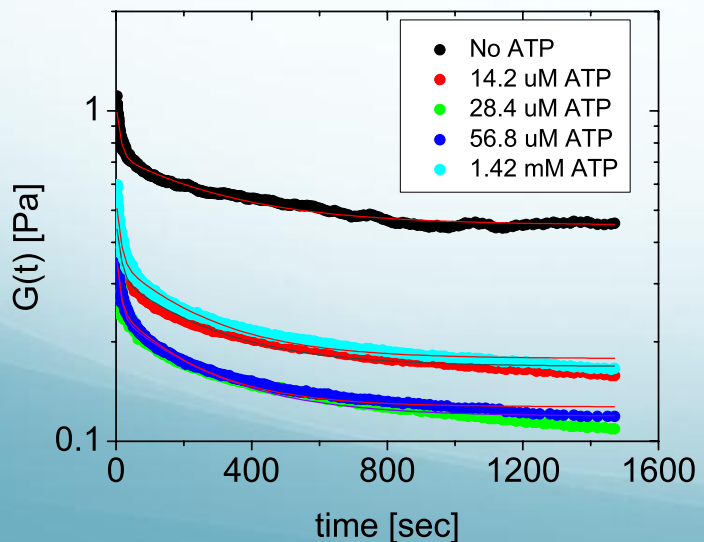
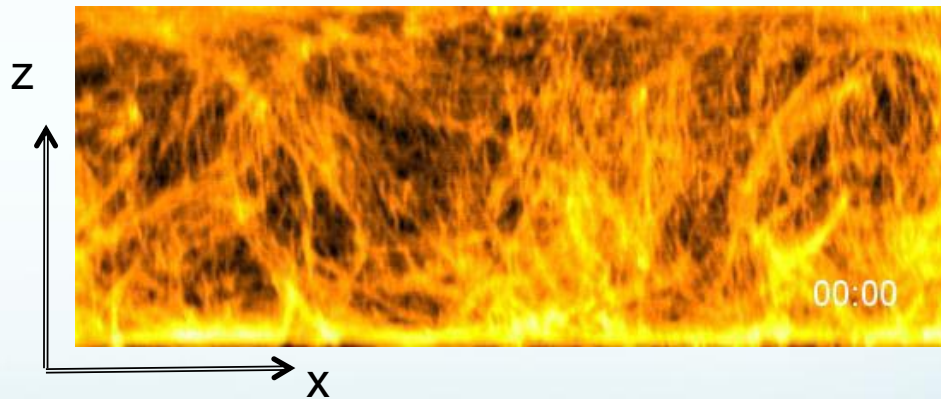
No relaxation at low frequencies.

# Step Strain $\Leftrightarrow$ Anomalous Stress Memory

No ATP, Step strain  $\gamma_0 =$

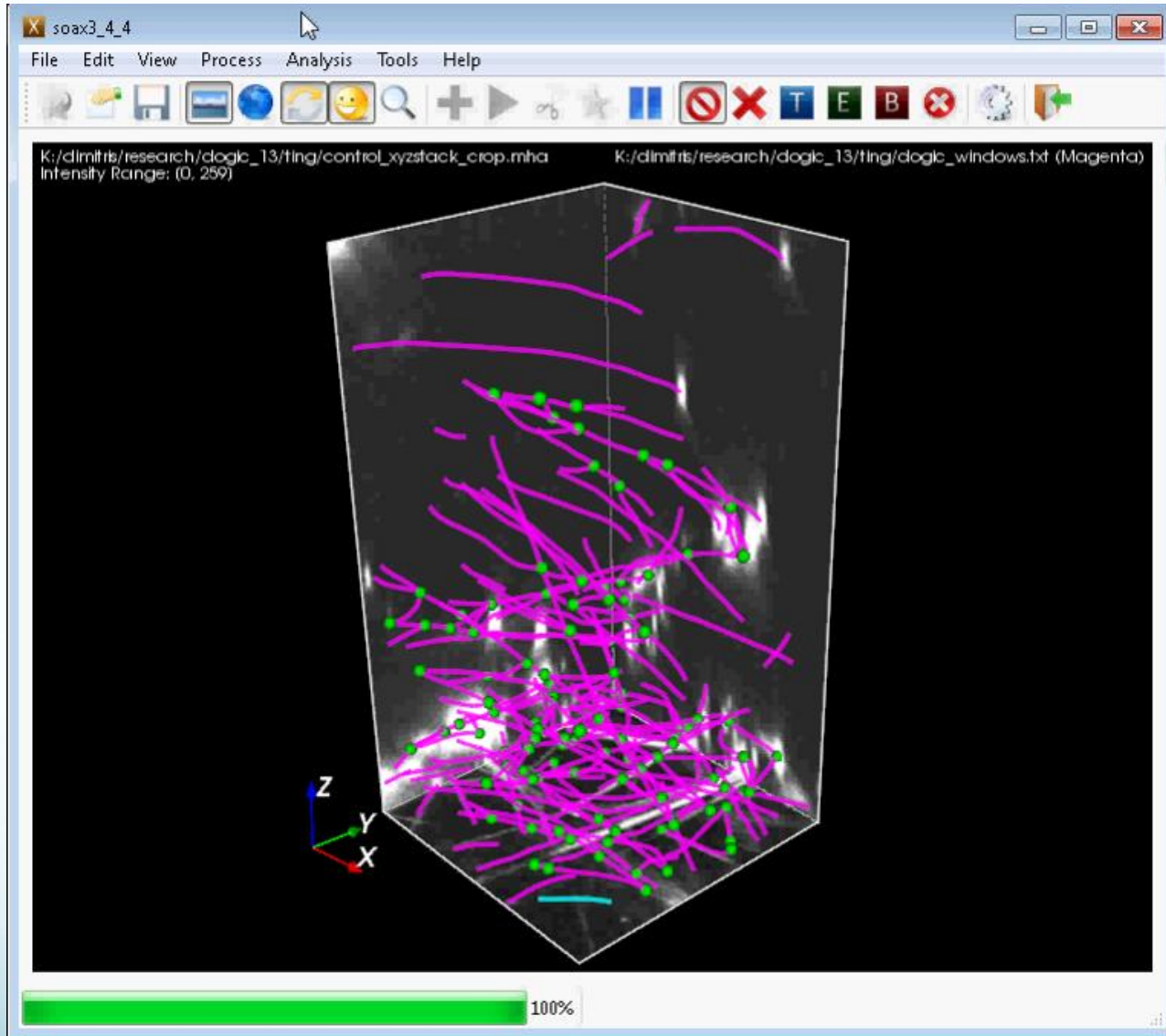


28.4  $\mu\text{M}$  ATP, Step strain  $\gamma_0 = 100\%$



Recoil despite total turnover of network

# Direct visualization and analysis of network dynamics



Active Snake Analysis: Ting Xu, Demetrios Vavylonis, Xiaolei Huang (Lehigh University)



# Active Networks perform work

