



Self-organization & Collective Behaviour of Active Colloids

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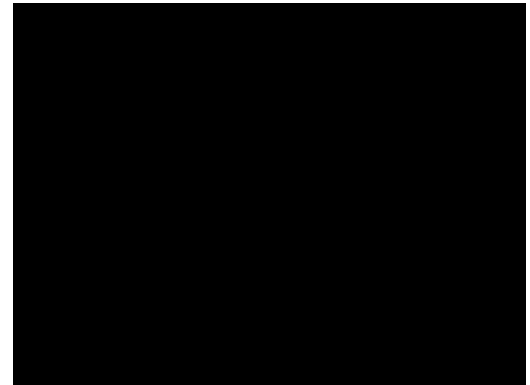
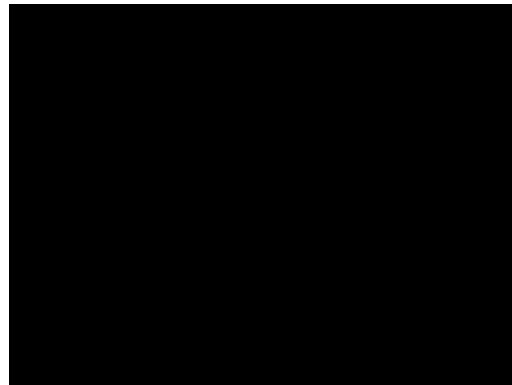
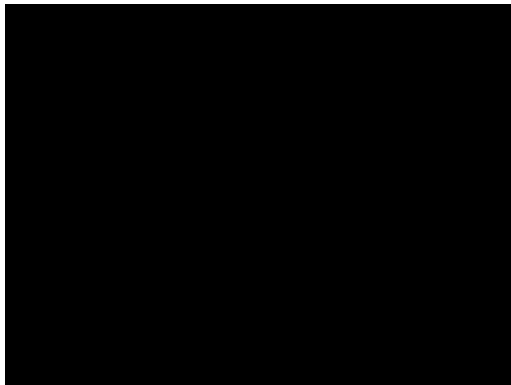
Rudolf Peierls Centre for Theoretical Physics

Active Matter: Cytoskeleton, Cells, Tissues and Flocks
KITP, UCSB
March 21, 2014

Active Colloids

Questions we would like to address:

- How can we make colloids active?
- How will their behaviour differ from passive colloids?
- What happens when we put them together and they interact?



Non-equilibrium Transport: Phoretic Motion

- **Electrophoresis**

Smoluchowski (1903)

- **Thermophoresis**

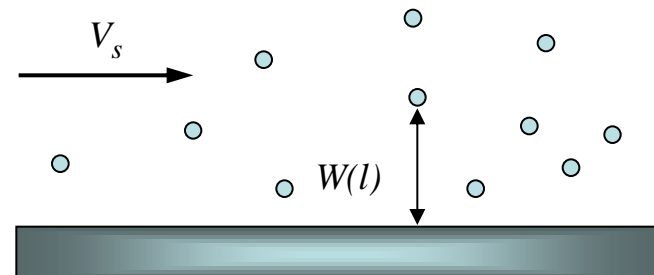
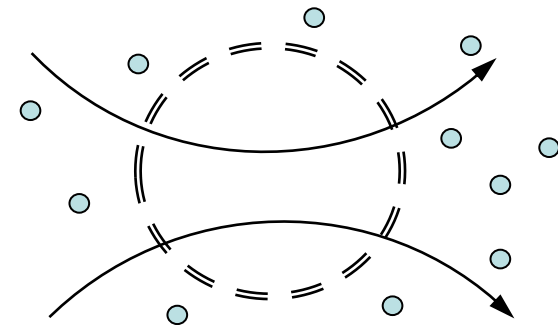
Ludwig (1856), Soret (1879)

- **Osmophoresis**

Sackmann *et al* (1999)

- **Diffusiophoresis**

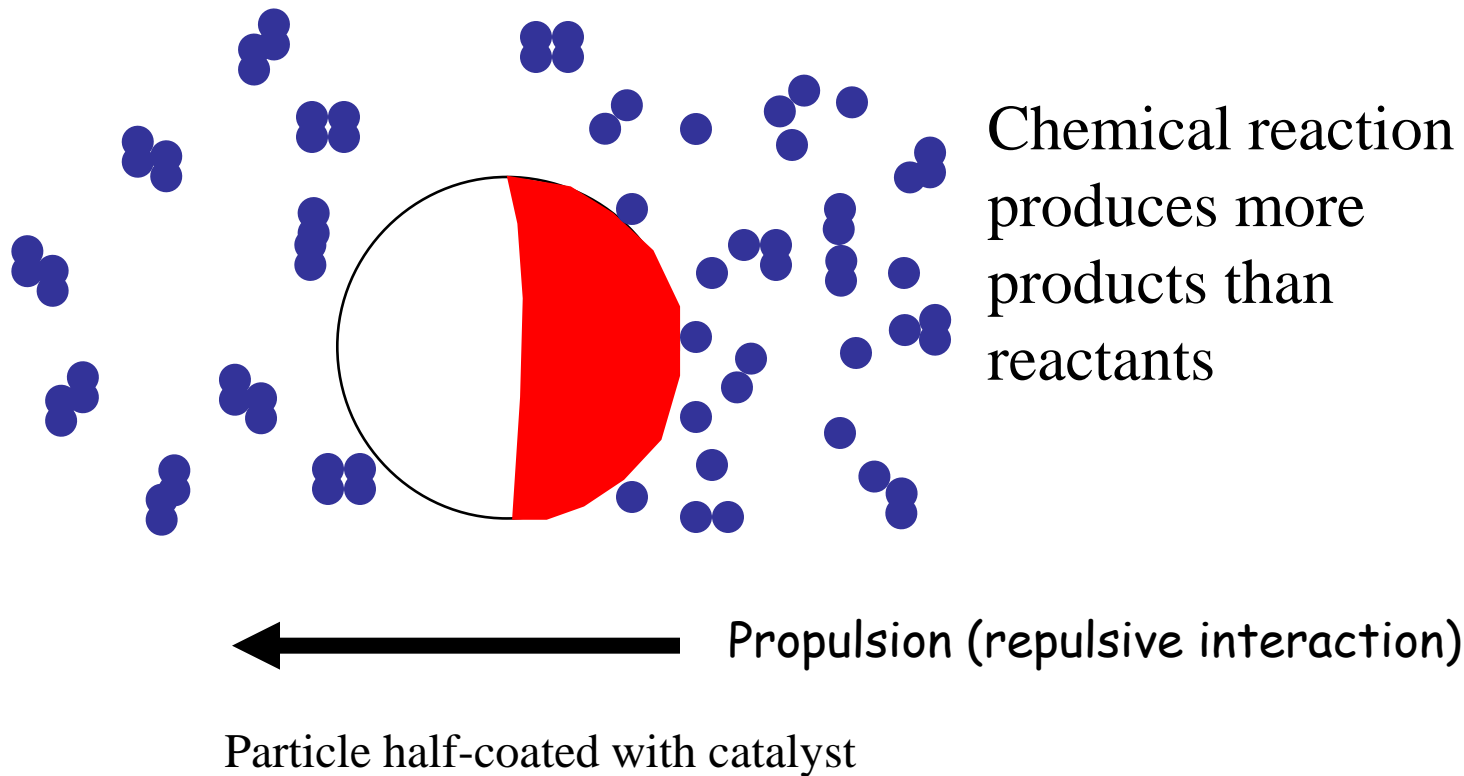
Derjaguin *et al* (1961),
Anderson & Prieve (1984)



Phoretic Transport is Force-Free

Propulsion via Self-Phoresis

e.g. self-diffusiophoresis



Analysis of the Motion

- Slip Velocity $\mu = k_B T \lambda^2 / \eta$

$$\lambda_D^2 = \int_0^\infty dl l [1 - e^{-W(l)/k_B T}]$$

$$\mathbf{v}_s(\mathbf{r}_s) = \mu(\mathbf{r}_s) (\mathbf{I} - \mathbf{nn}) \cdot \nabla c(\mathbf{r}_s)$$

- Source at the Surface

$$D \nabla^2 c = 0$$

$$- D \mathbf{n} \cdot \nabla c(\mathbf{r}_s) = \alpha(\mathbf{r}_s)$$

mobility

activity

Propulsion via Self-Phoresis

- Swimming Velocity

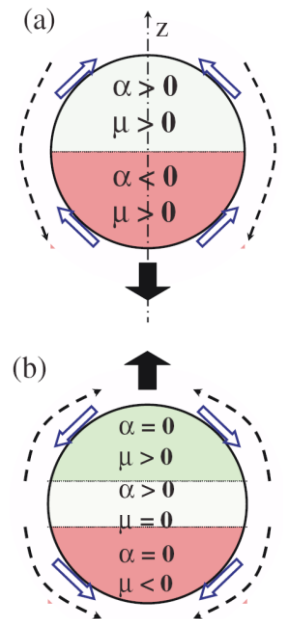
$$V \sim \alpha\mu/D$$

- Design-related Questions

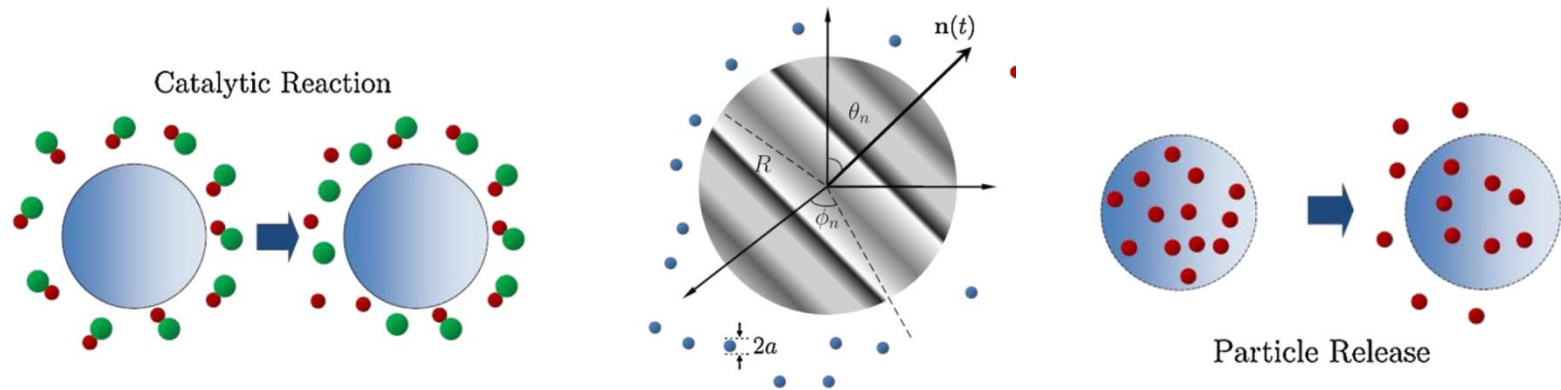
- Symmetry breaking
- Relative importance of activity/mobility
- Effect of Geometry

- Generic for Any Phoresis

-> Self-Thermophoresis

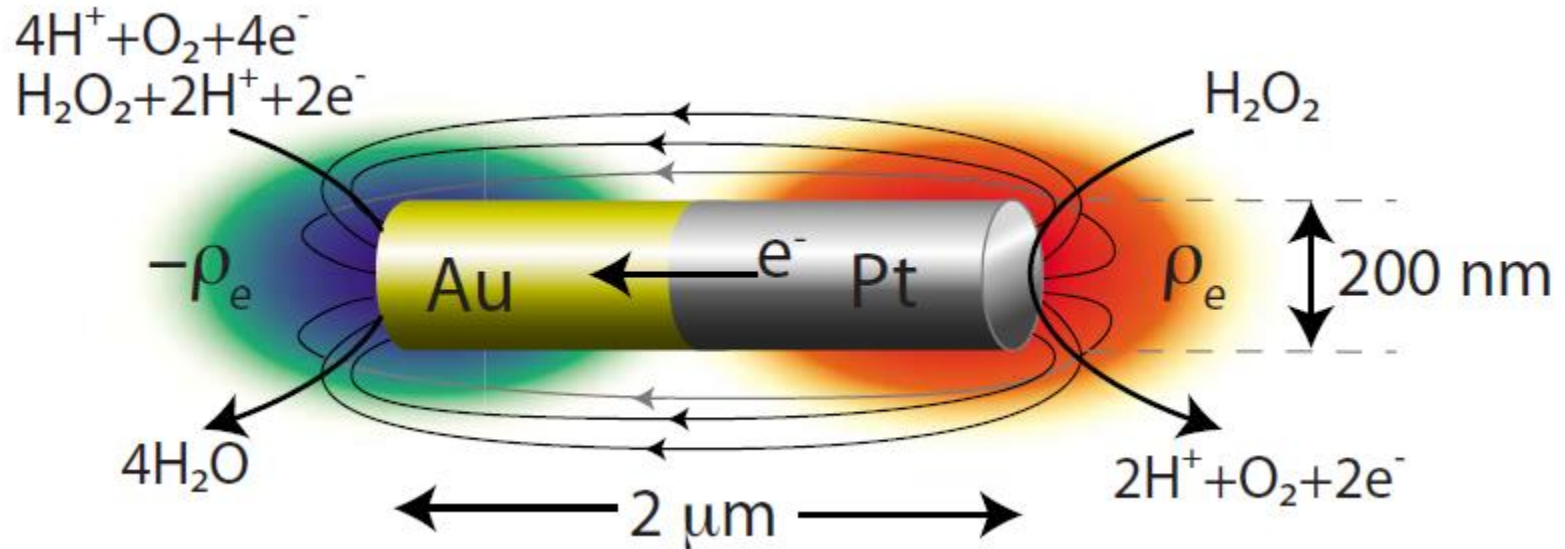


Stochastic Dynamics of Phoretic Swimmers



Asymmetric Contribution	$\sim t^2$ <i>inertial</i>	$\sim t^2$ <i>propulsive</i>	$\sim t^2 - \gamma t^{3/2}$ <i>propulsive + anomalous</i>	$\sim t$ <i>diffusive</i>
Symmetric Contribution	$\sim t^2$ <i>inertial</i>	$\sim t^{3/2}$ <i>anomalous</i>	$\sim t$ <i>diffusive</i>	
Hydrodynamic Contribution	$\sim t^2$ <i>inertial</i>	$\sim t - \beta t^{1/2}$ <i>diffusive + anomalous</i>		
		τ_h	τ_d	τ_r

Experiments on Self-Phoresis

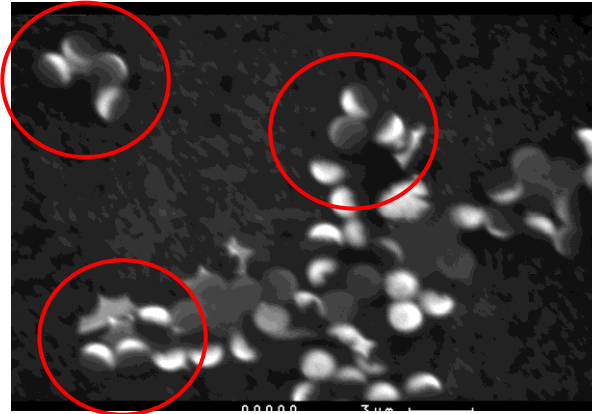


Paxton et al, JACS **126**, 13424 (2004) [Ayusman Sen Group]

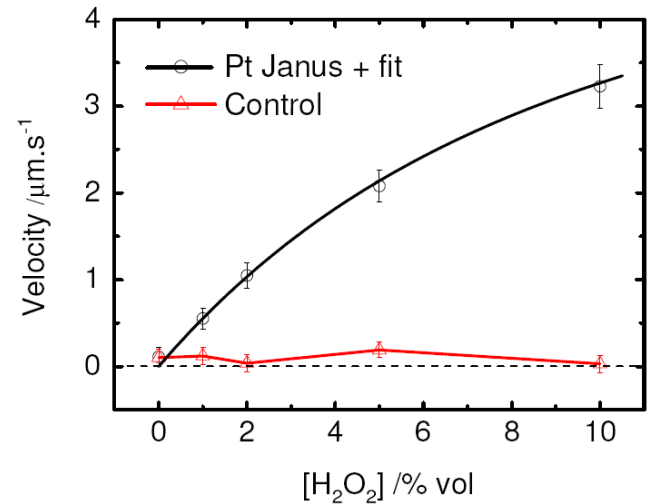
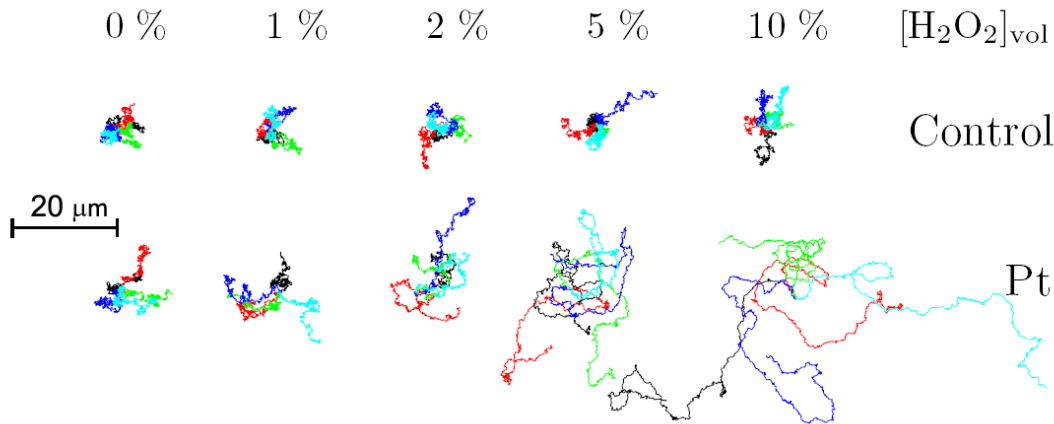
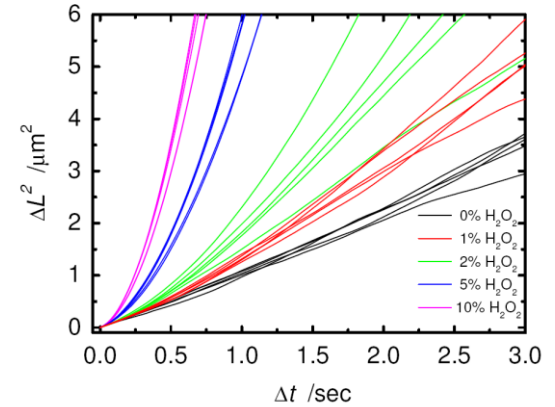
Redox Self-Electrophoresis: a short circuited battery!

Theoretical Analysis: Moran, Wheat & Posner, PRE **81**, 065302(R) (2010)

Experiments on Self-Phoresis

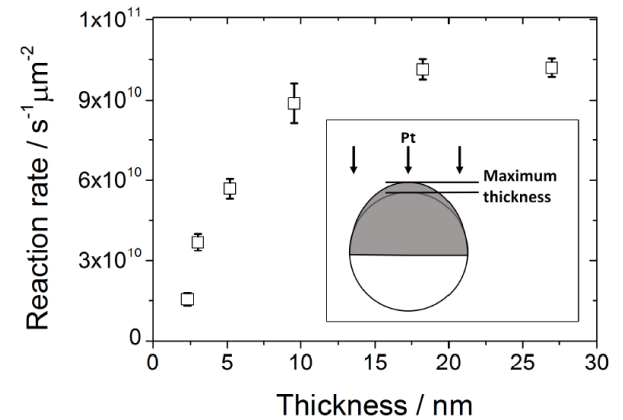
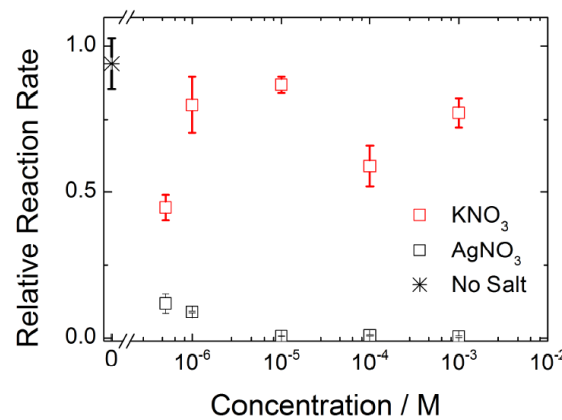
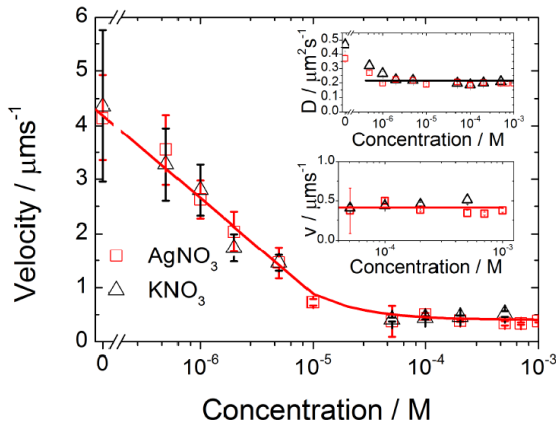


half-Pt coated spherical
PS beads in aqueous
hydrogen peroxide solution

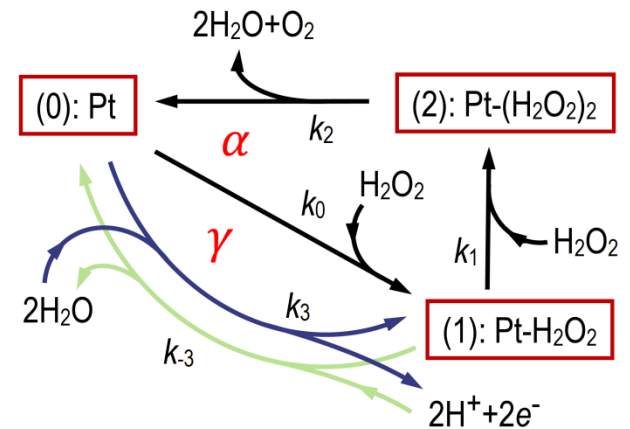
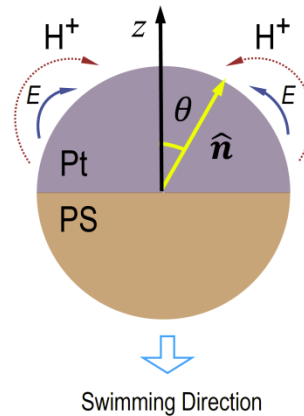


Experiments on Self-Phoresis

There are subtle electrokinetic effects for the Pt-PS beads ...



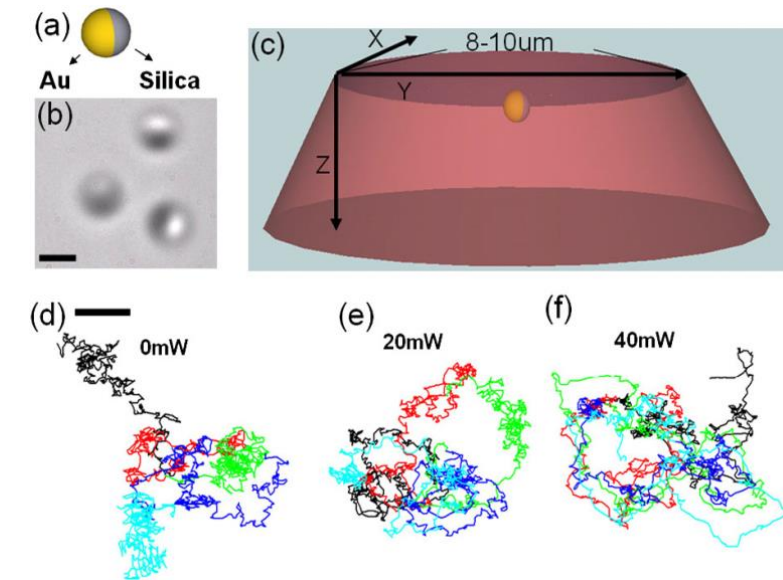
- nested loops
- charged intermediates



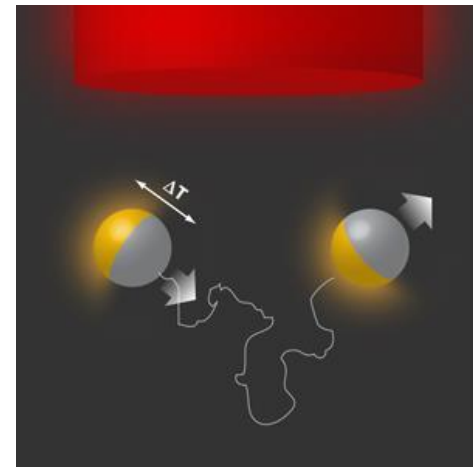
- S. Ebbens, D.A. Gregory, G. Dunderdale, J.R. Howse, Y. Ibrahim, T.B. Liverpool & R. Golestanian, arXiv:1312.6250
- A. Brown & W. Poon, arXiv:1312.4130

Experiments on Self-Phoresis

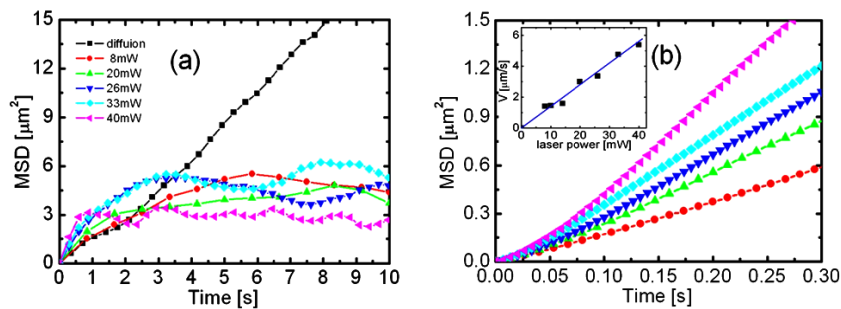
Self-Thermophoresis



The Mechanism



Golestanian, Liverpool & Ajdari (2007)



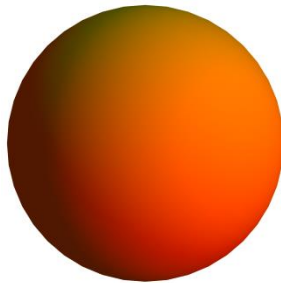
Jiang, Yoshinaga & Sano, PRL **105**, 268302 (2010)

Active Colloidal Molecules

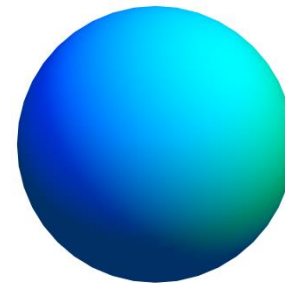
Source or Sink of Chemicals: $C(r) \sim \alpha R^2 / (Dr)$

Analogous to **Coulomb** or **Gravitational** potential

Two active colloids: it's complicated!
(as in relationships, complicated!!)



$$\vec{V}_1 \sim -\alpha_2 \mu_1 \frac{R^2 \vec{r}_{12}}{D |\vec{r}_{12}|^3}$$



$$\vec{V}_2 \sim \alpha_1 \mu_2 \frac{R^2 \vec{r}_{12}}{D |\vec{r}_{12}|^3}$$

Action \neq Reaction

Active Self-Assembly

Brownian dynamics simulation:

$$\frac{d\vec{r}_i}{dt} = \sum_{k \neq i} \frac{\alpha_k \mu_i R^2}{6\pi D} \frac{\vec{r}_{ik}}{|\vec{r}_{ik}|^3} + \vec{\xi}_i(t) = V_0 \sum_k \tilde{\alpha}_k \tilde{\mu}_i \frac{\sigma^2 \vec{r}_{ik}}{|\vec{r}_{ik}|^3} + \vec{\xi}_i(t)$$

+excluded volume effect.

Colloidal molecules spontaneously form via self-assembly, and exhibit different types of activity depending on **symmetry**

Two types of colloids for simplicity, with different valences:



$$\tilde{\alpha}_A \geq 1 \quad \tilde{\mu}_A \geq 0$$



$$\tilde{\alpha}_B = \tilde{\mu}_B = -1$$

$AB, AB_2, AB_3, \dots, AB_n$

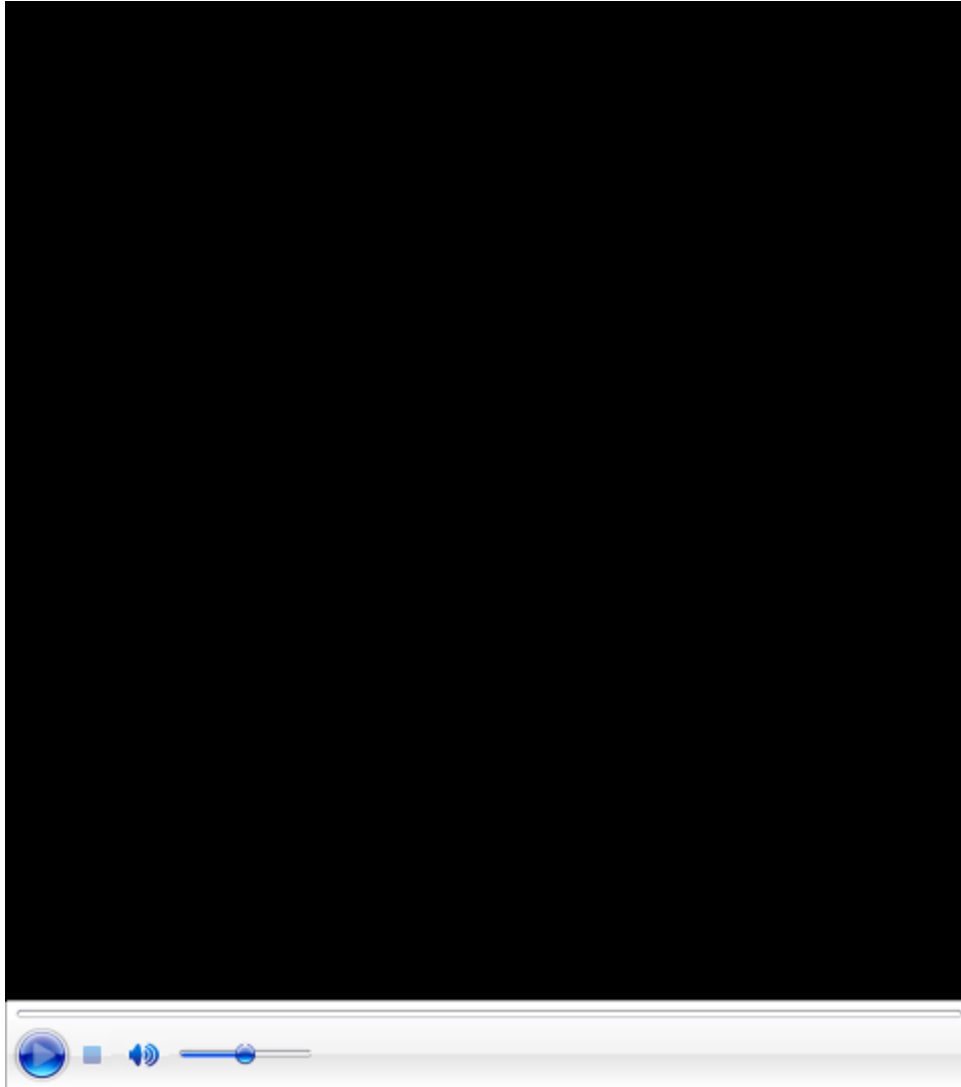
A 

$$\tilde{\alpha}_A = 3$$

$$\tilde{\mu}_A = 0$$

B 

$$\tilde{\alpha}_B = \tilde{\mu}_B = -1$$

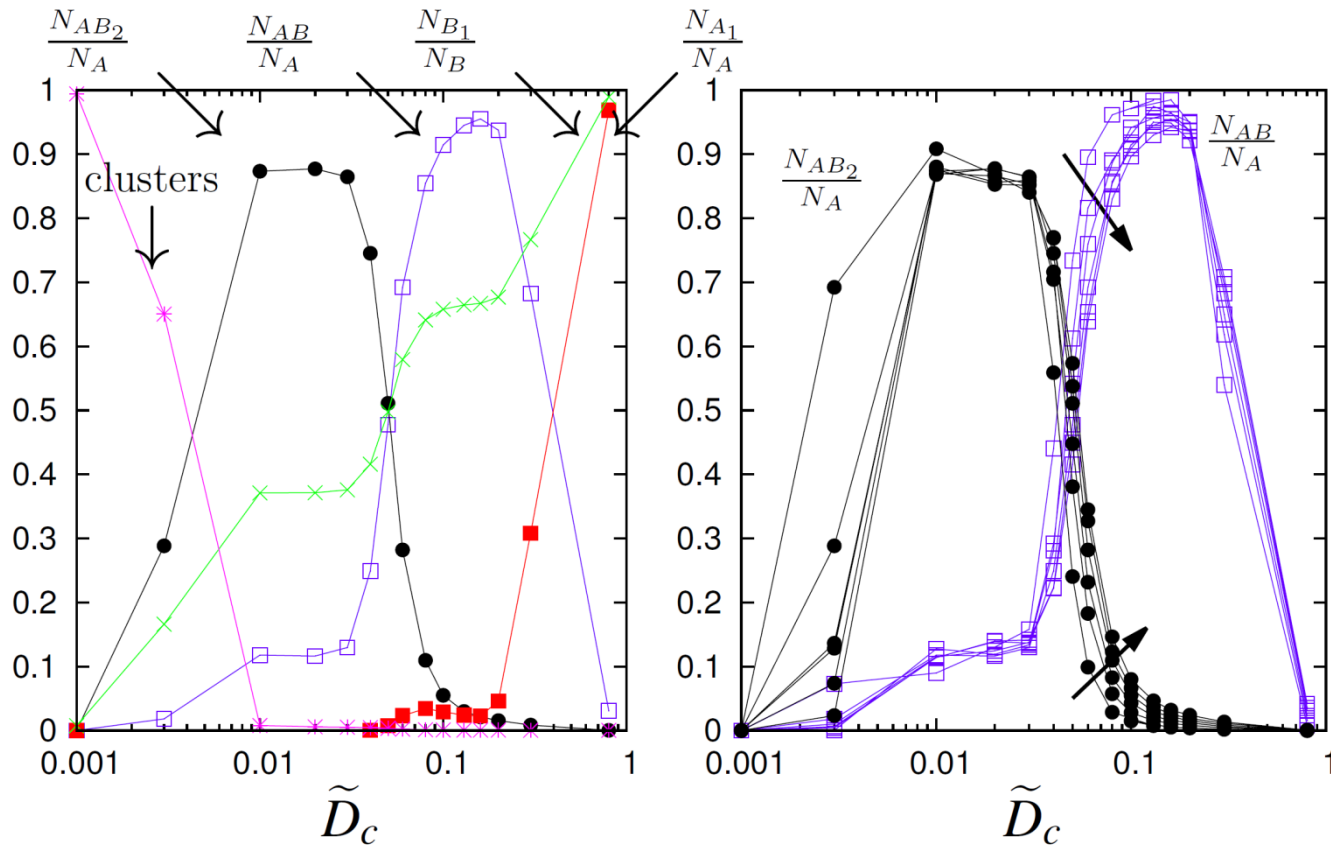


Molecular Populations vs Temperature

A ● $\tilde{\alpha}_A = 3$ $\tilde{\mu}_A = 0$

B ● $\tilde{\alpha}_B = \tilde{\mu}_B = -1$

Stable molecules are not necessarily "charge neutral"

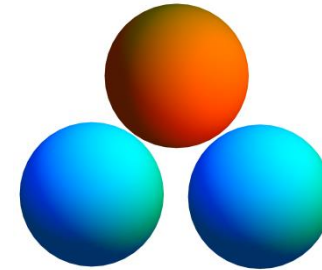


AB_2 Isomers



linear
Inert

preferred angle 180 deg



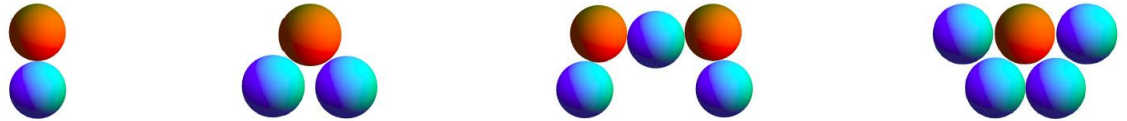
planar
Self-propelled

preferred angle 60 deg

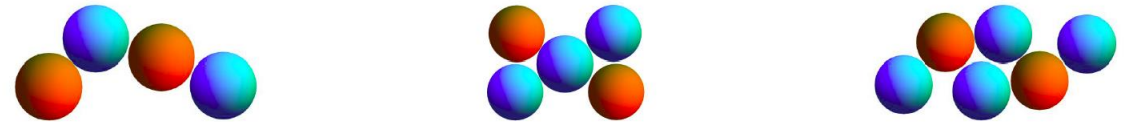
We observe isomerization and bi-stability

Tabulating Active Molecules

Translational propulsion



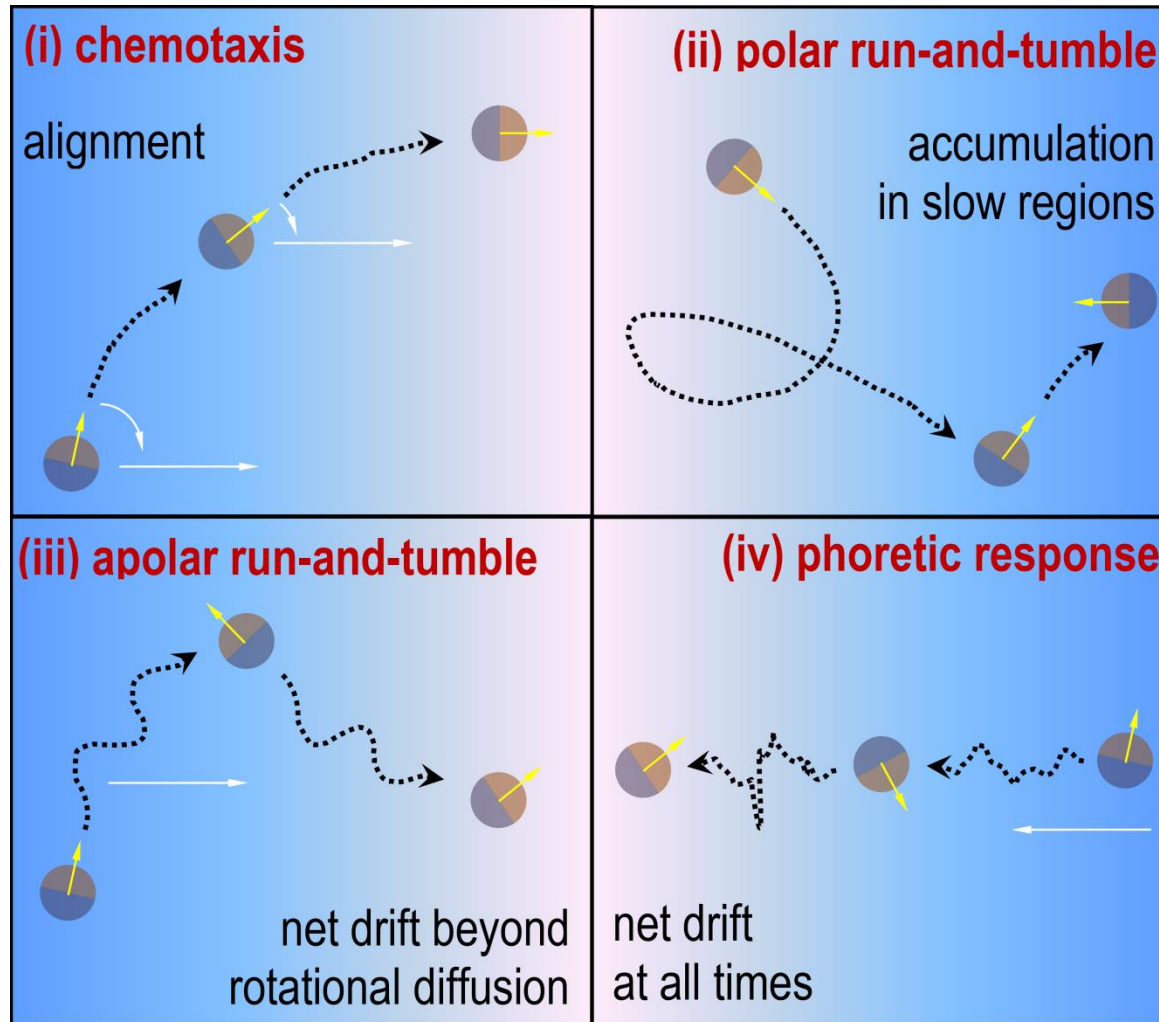
Rotational propulsion



Inert molecules



Response to Nonuniform Chemical Profile



Many-Colloid Chemotaxis: Screened Case

Michaelis-Menten rule
leads to screening

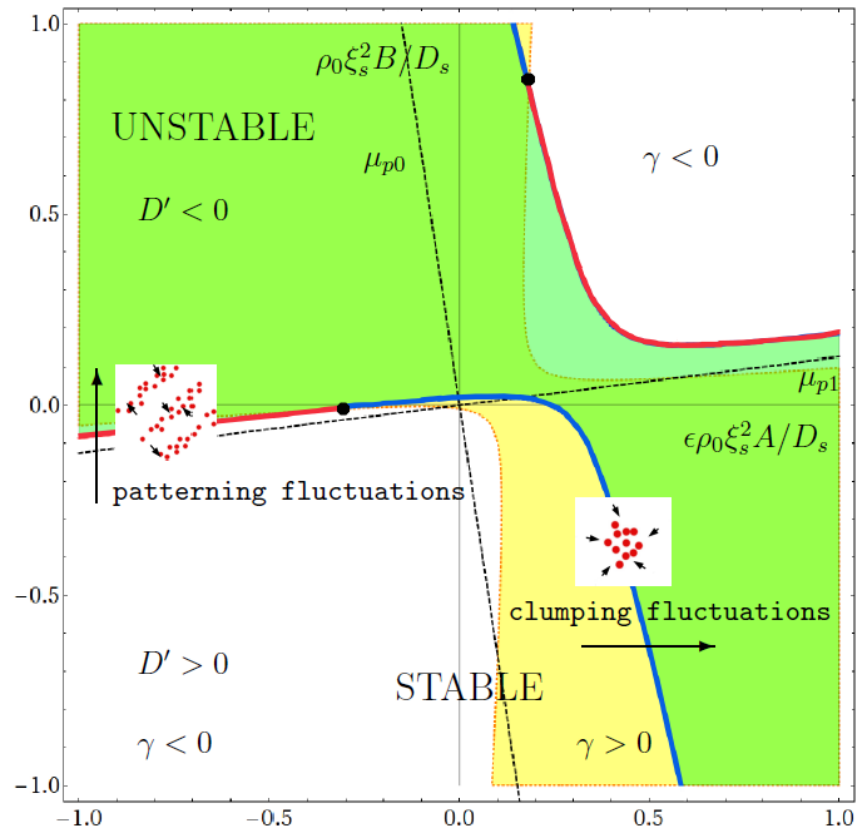
Screening length:

$$\xi_s = [N\rho_0\kappa'(s_0)/D_s]^{-1/2}$$

Signature in density field:
Instabilities and Fluctuations

No flocking.

$$\kappa(s) \equiv \kappa_2\kappa_1s/(\kappa_2 + \kappa_1s)$$

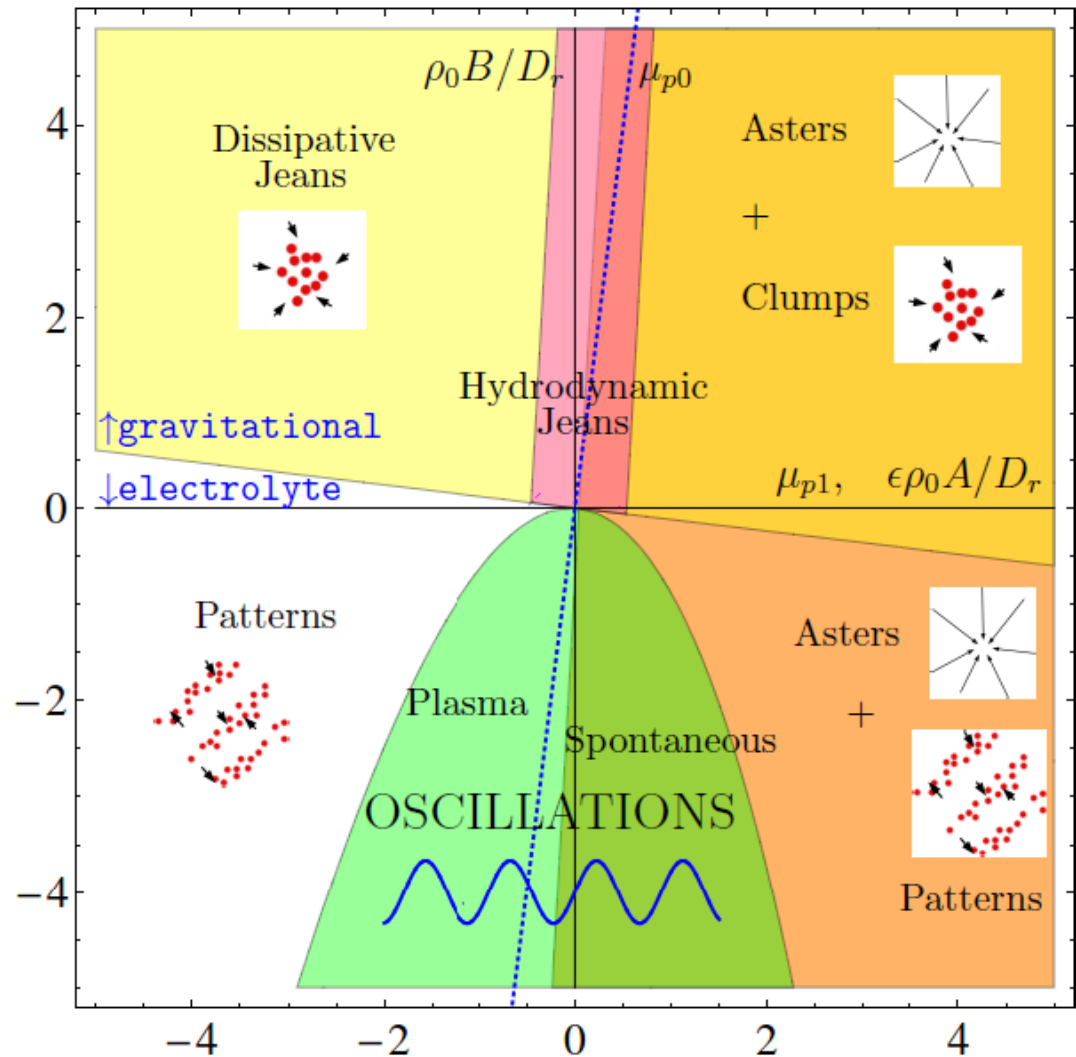


Collective Behaviour: Unscreened Case

Interplay between **self-propulsion**, **spin**, **drift**, **alignment**, driven by and mediated via chemicals

-> Variety of Behaviours:

- Clustering
- Aster condensation
- Pattern formation
- Plasma Oscillations
- Ringing



Collective Thermotaxis

- Intra-colloid Activity

- Mobile heat source
- Self-propelled, if asymmetric

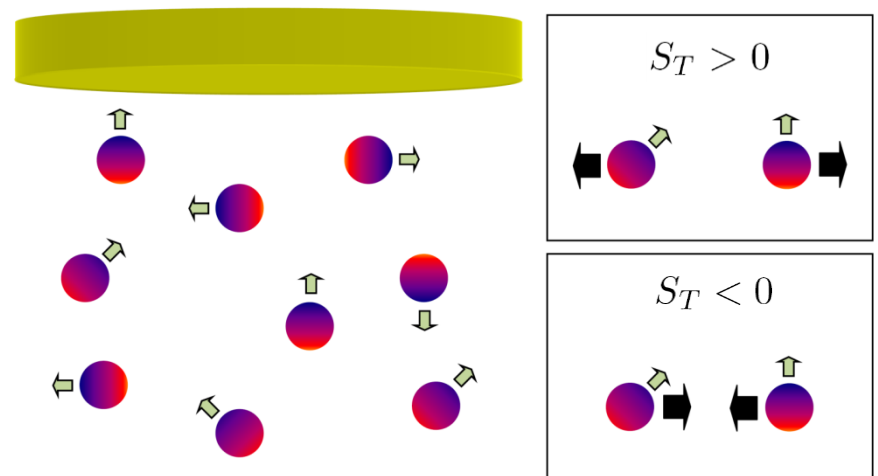
$$v_0 = \frac{\epsilon I D_T}{6\kappa}$$

- Inter-colloid Interaction

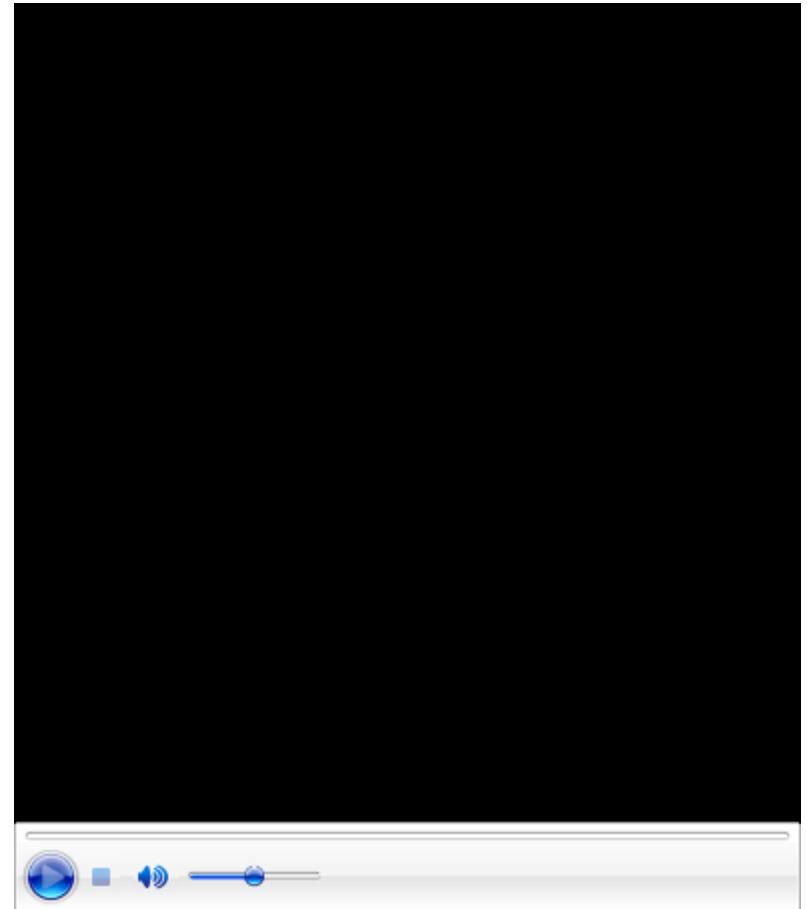
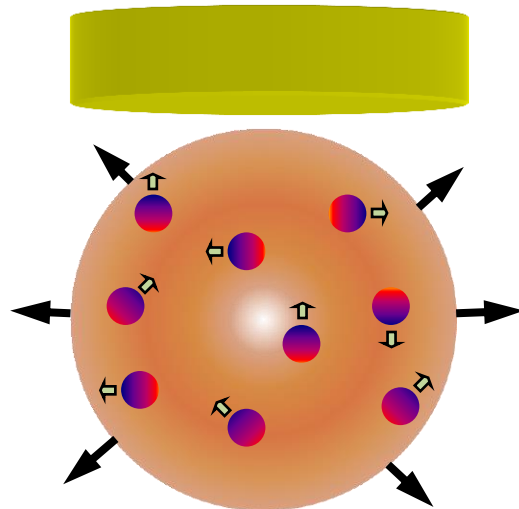
$$\mathbf{v} = -D_T \nabla T$$

- Thermo-repulsive
- Thermo-attractive

$$S_T = \frac{D_T}{D}$$



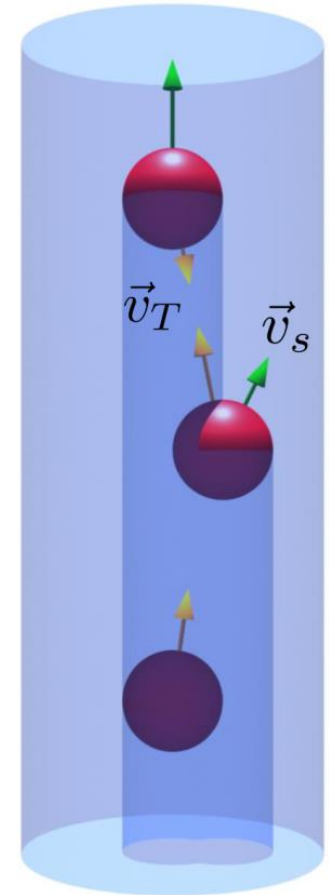
Thermo-Attractive (“Gravitational”) Case



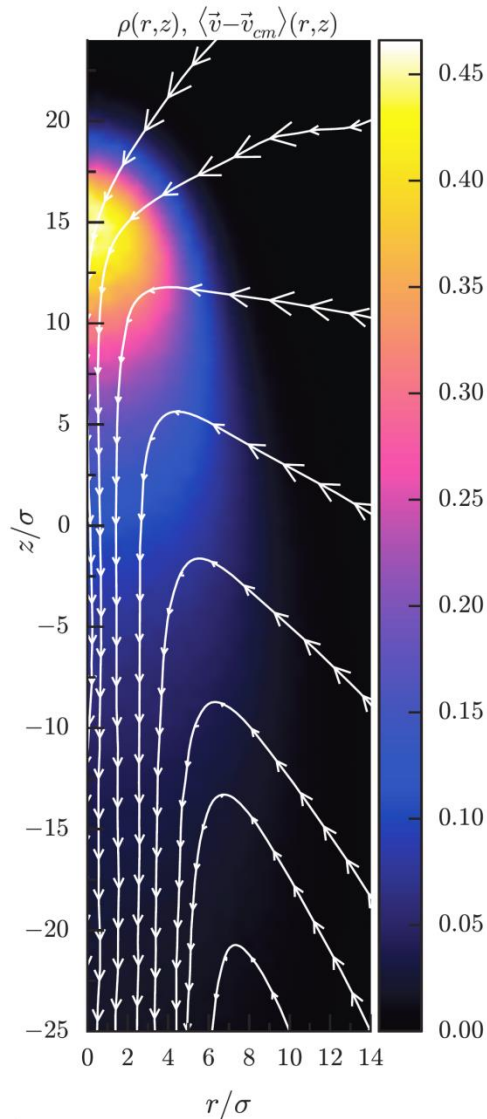
- Heat flux at the boundary cannot balance the heat generated inside
-> uncontrolled build-up of heat
- In molecular systems:
exothermic combustion reactions -> thermal explosion!

A More Realistic Description

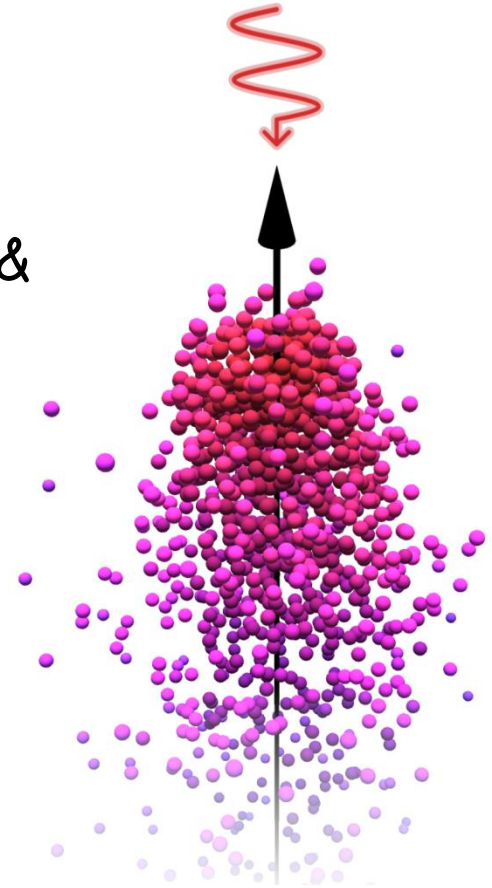
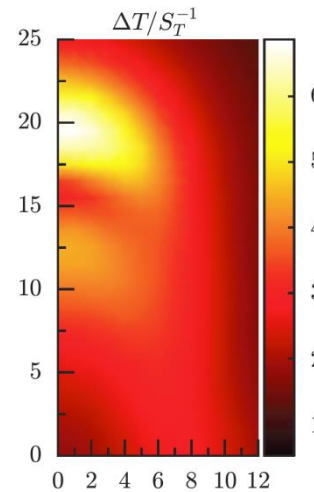
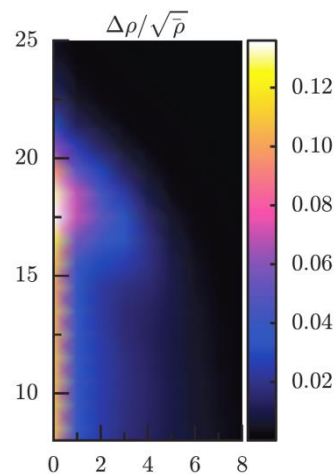
- Photo-taxis
 - Attraction
 - Excluded volume
 - Shadowing
- uniform illumination from the top
 - propulsion due to self-generated $\text{grad}T$
 - mutual attraction due to $\text{grad}T$ caused by mobile heat sources



Comet-like Swarming



- uniform average motion
- hot-and-dense head
- circulation
- large density fluctuations & temperature fluctuations

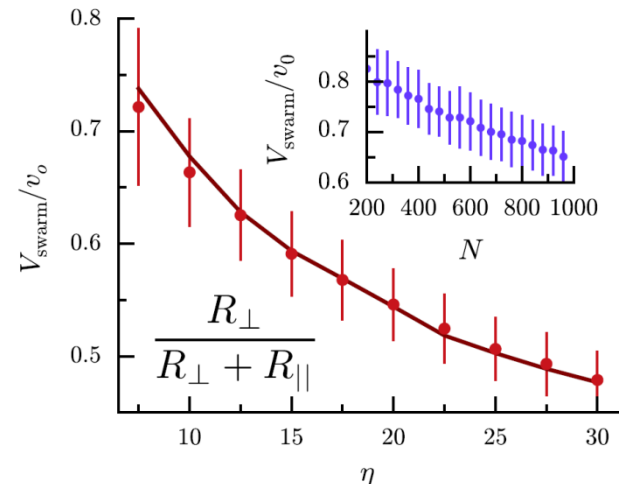
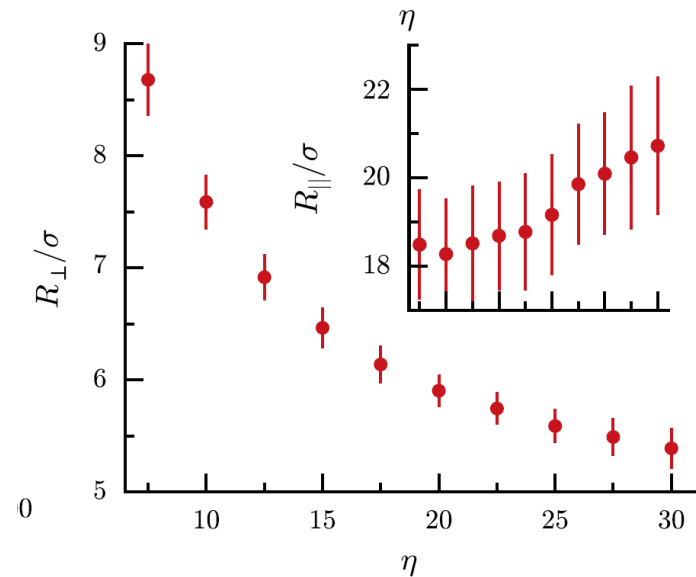


Changing the Coupling Strength

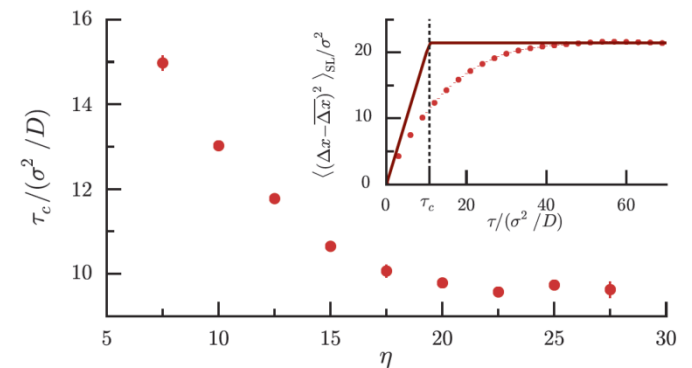
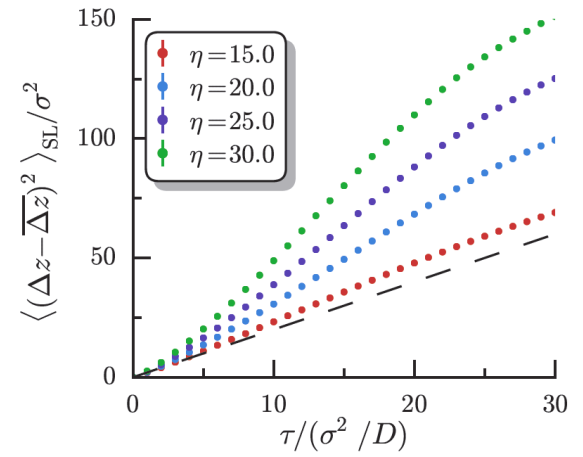
$$\eta = \sigma \epsilon I |S_T| / \kappa$$

As the coupling strength increases, the Swarm:

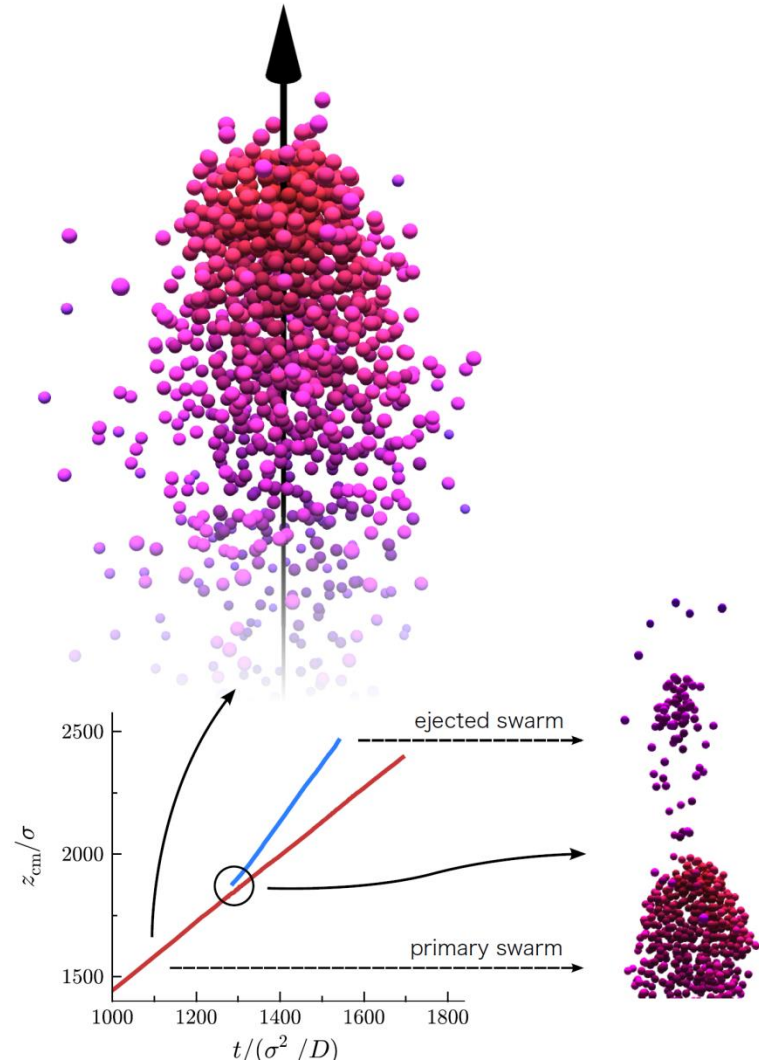
- elongates
- narrows down
- slows down
- becomes more dynamic



Particle Tracking: Confinement

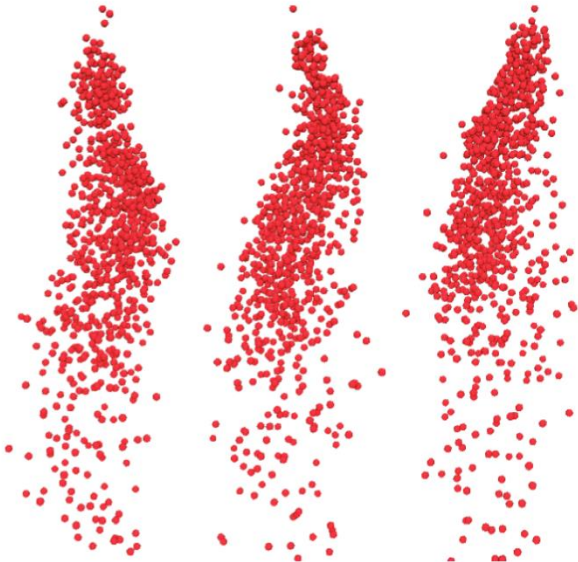


Increased Coupling Behaviour: Fission

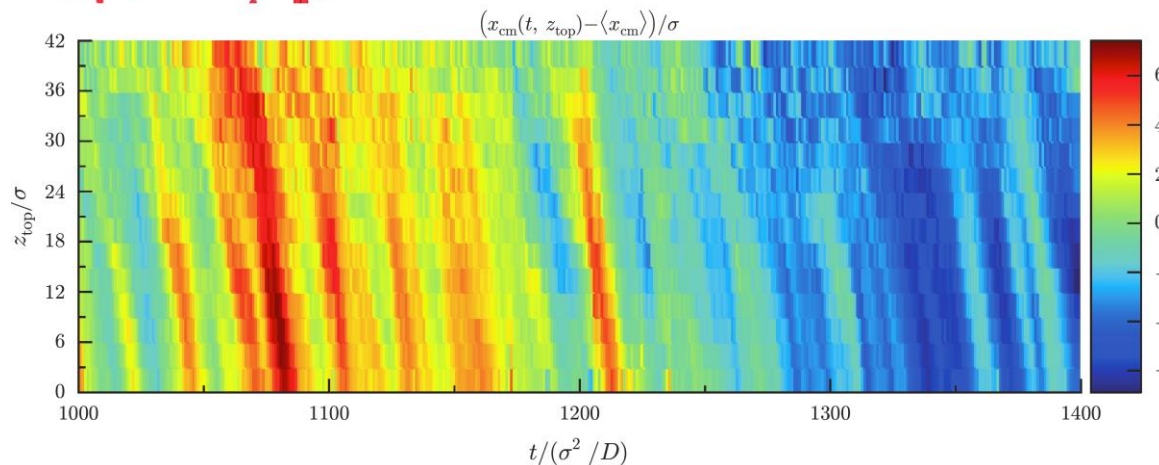


Increased Coupling Behaviour: Waves

$t = 1203 \sigma^2 / D$ $t = 1208 \sigma^2 / D$ $t = 1213 \sigma^2 / D$



- waves can start randomly
- they propagate from tail to head
- constant propagation velocity
- no dispersion or damping



Conclusion

- Colloids can be made **active**, i.e. driven out of equilibrium, in a variety of ways...
- Active colloids will have self-propulsion, if they are "sufficiently asymmetric"
- Both self-propelled and symmetric active colloids perform anomalous stochastic motion depending on the time scale
- Collective behaviour of active colloids could be very rich due to the long-range nature of their interactions