

# Chromosome Positioning from Activity-based Segregation



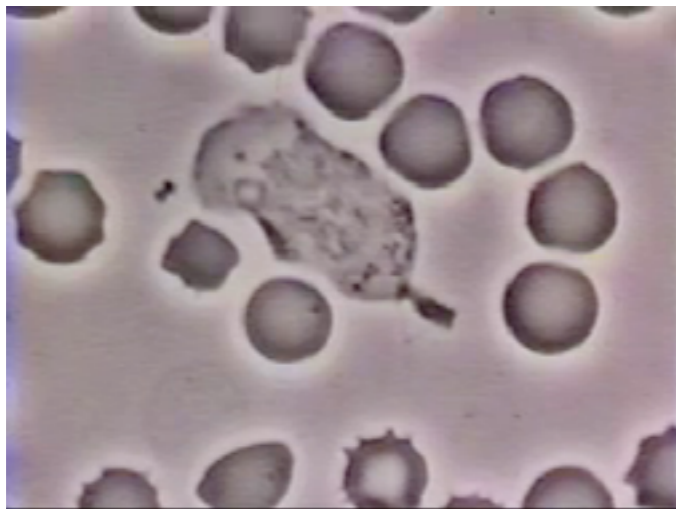
Gautam I. Menon

The Institute of Mathematical Sciences,  
Chennai, India

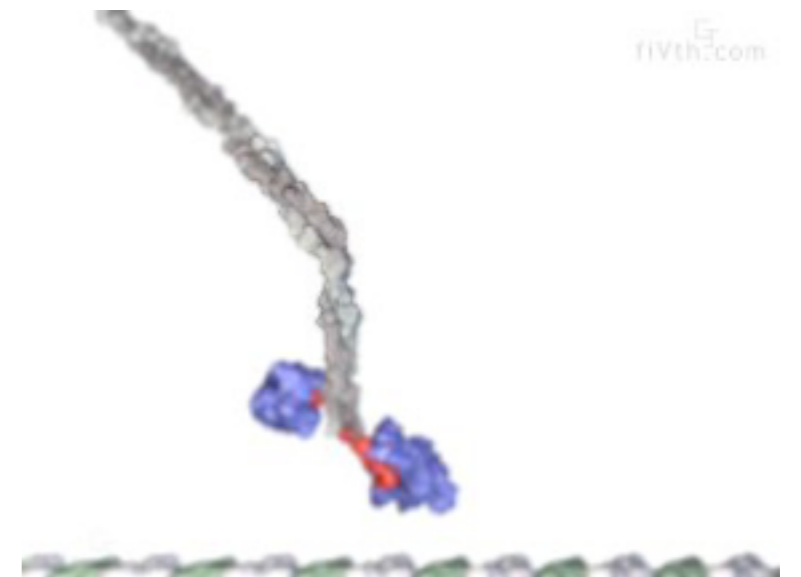
With: Nirmalendu Ganai (Vidyasagar College, India) and Surajit Sengupta (TIFR-H, IACS, India)

# Active Matter paradigm for biological systems

Physical description: Matter **out of thermal equilibrium**, driven internally by ATP consuming processes, non-equilibrium biochemical reactions



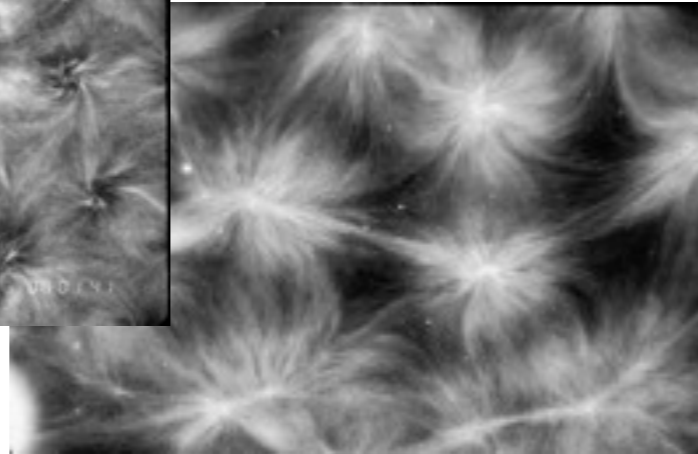
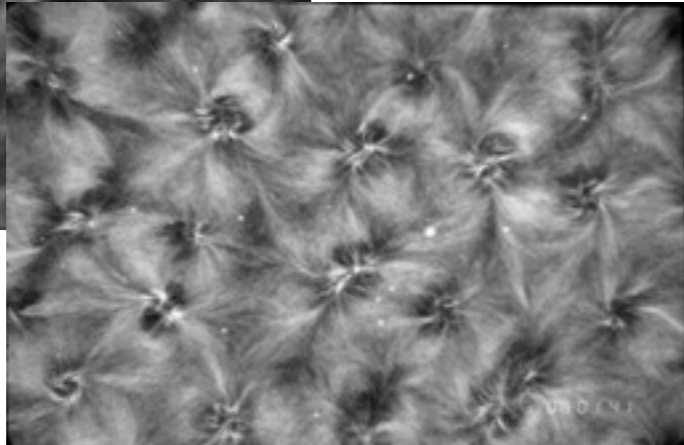
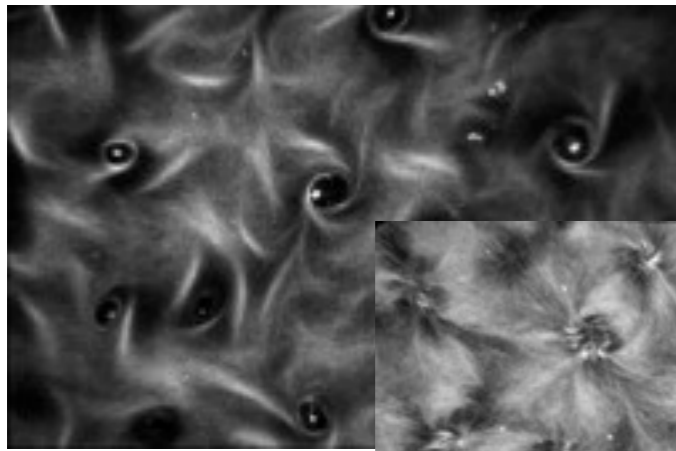
<http://www.biochemweb.org/neutrophil.shtml>



<http://valelab.ucsf.edu/moviepages/movies.html>

Specific consequences: **Large fluctuations**, **increased sensitivity**, **collective behaviour**, **coupling across very different length and time scales**, **spatial structuring**

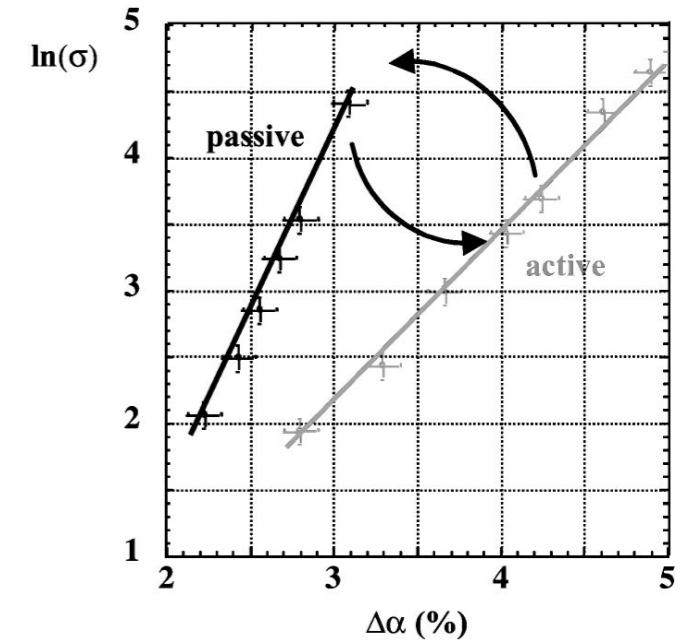
# In vitro models



Motor-microtubule pattern formation

Nedelec, Surrey, Maggs and Leibler Nature 1997.

## Active membranes



Prost, Bruinsma, Bassereau, Manneville, Ramaswamy ..  
EPL '96, PRL '99, PRE '01

# Self-propelled objects *a la* Vicsek



Andrea Cavagna  
homepage

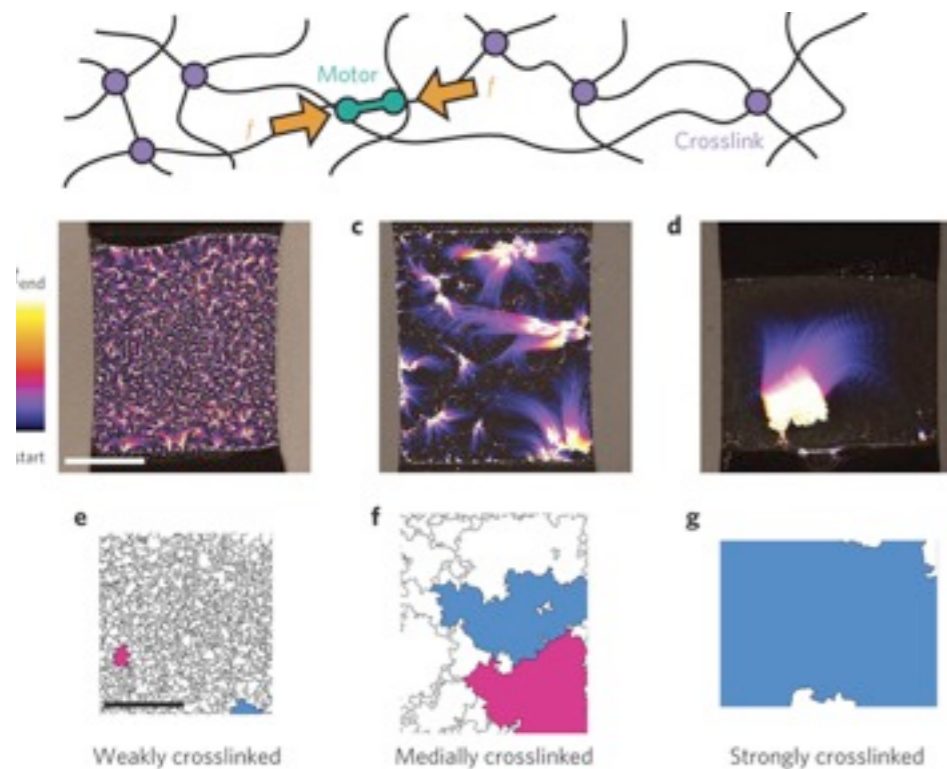


<http://cognition.ups-tlse.fr/dynactom/>

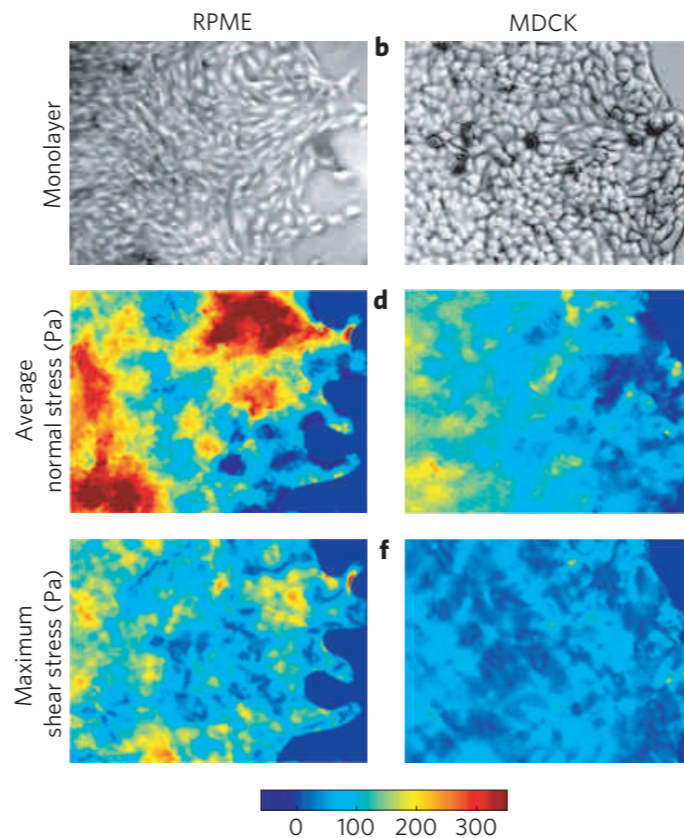


# Active self-organization

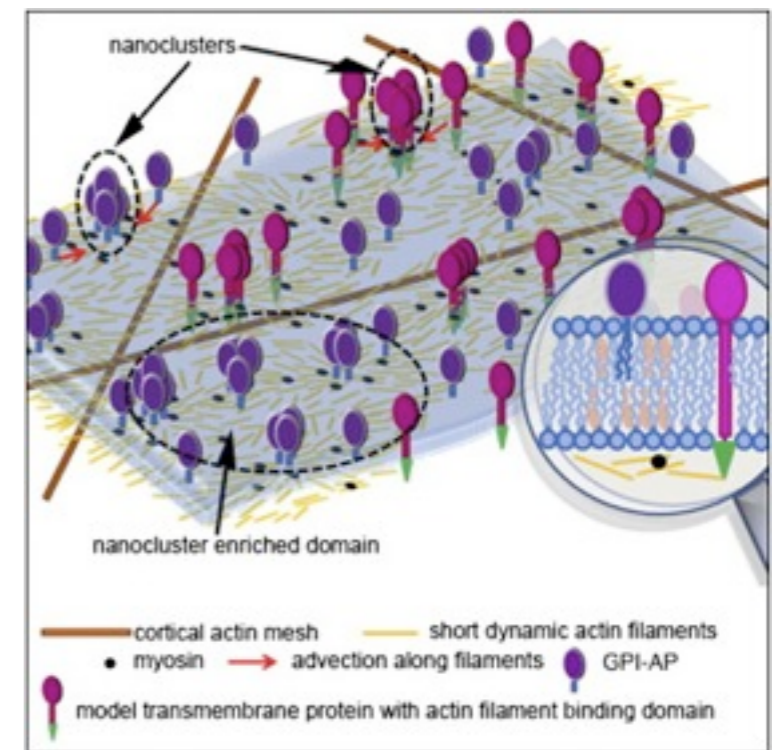
+ acto-myosin gels, cell-substrate interactions, nanoclustered domains on membranes, tissues ..



**Alvarado et al**, Nat Phys 2013



**Tambe et al**, Nat Mat 2011

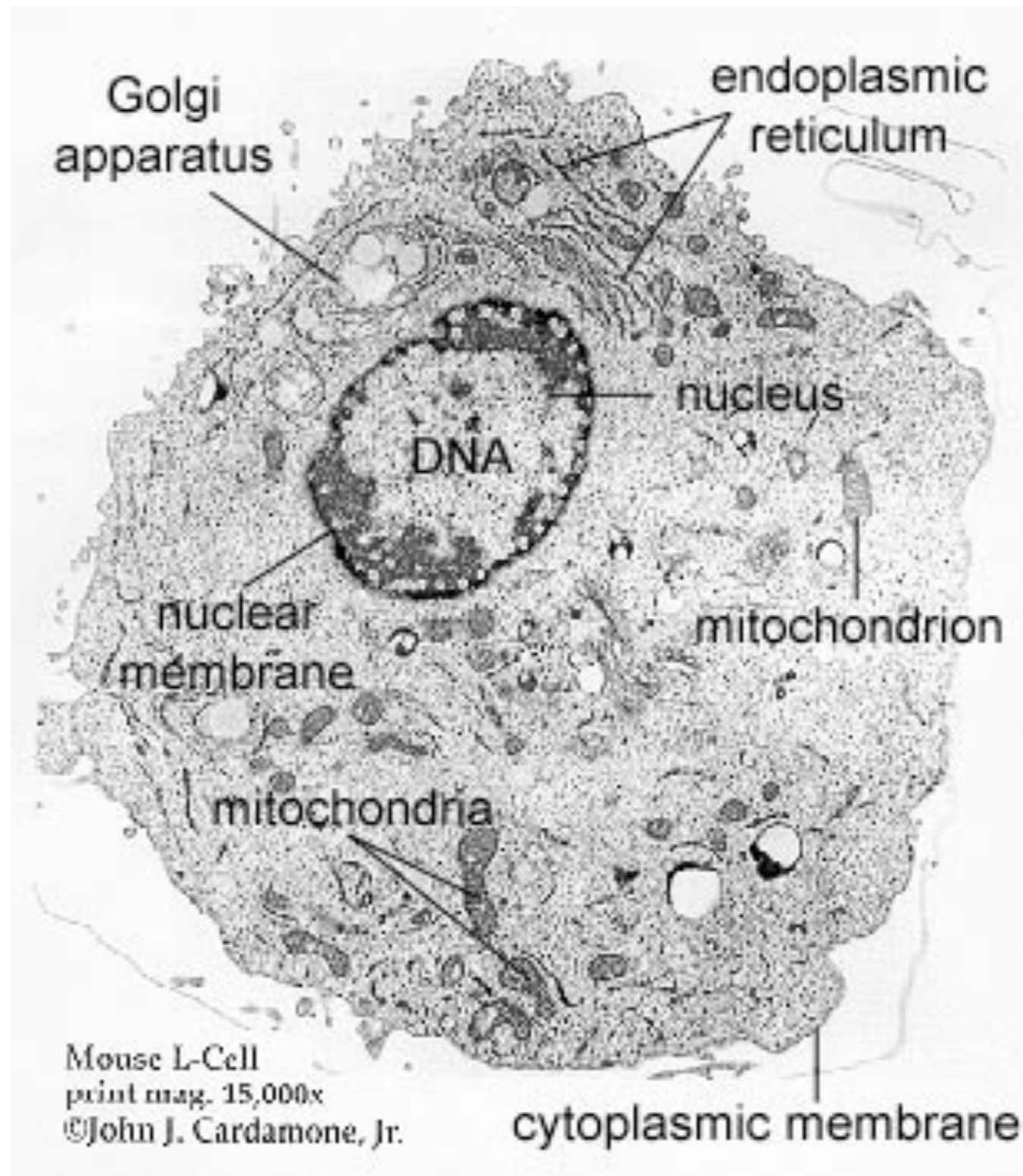


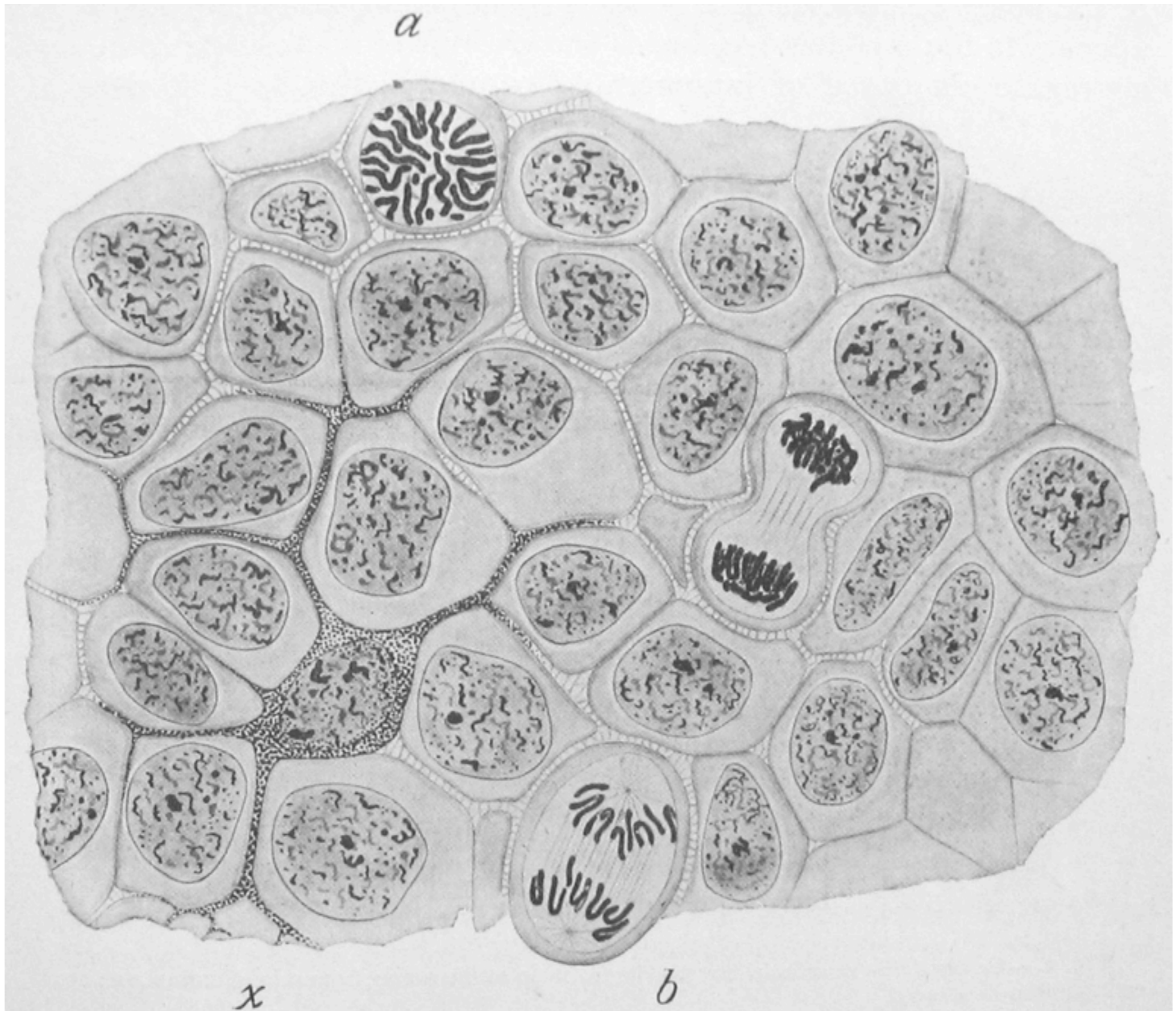
**Gowrishankar et al**, Cell 2012

Other “tractable” *in vivo* active matter systems?

Chromatin in the interphase cell nucleus

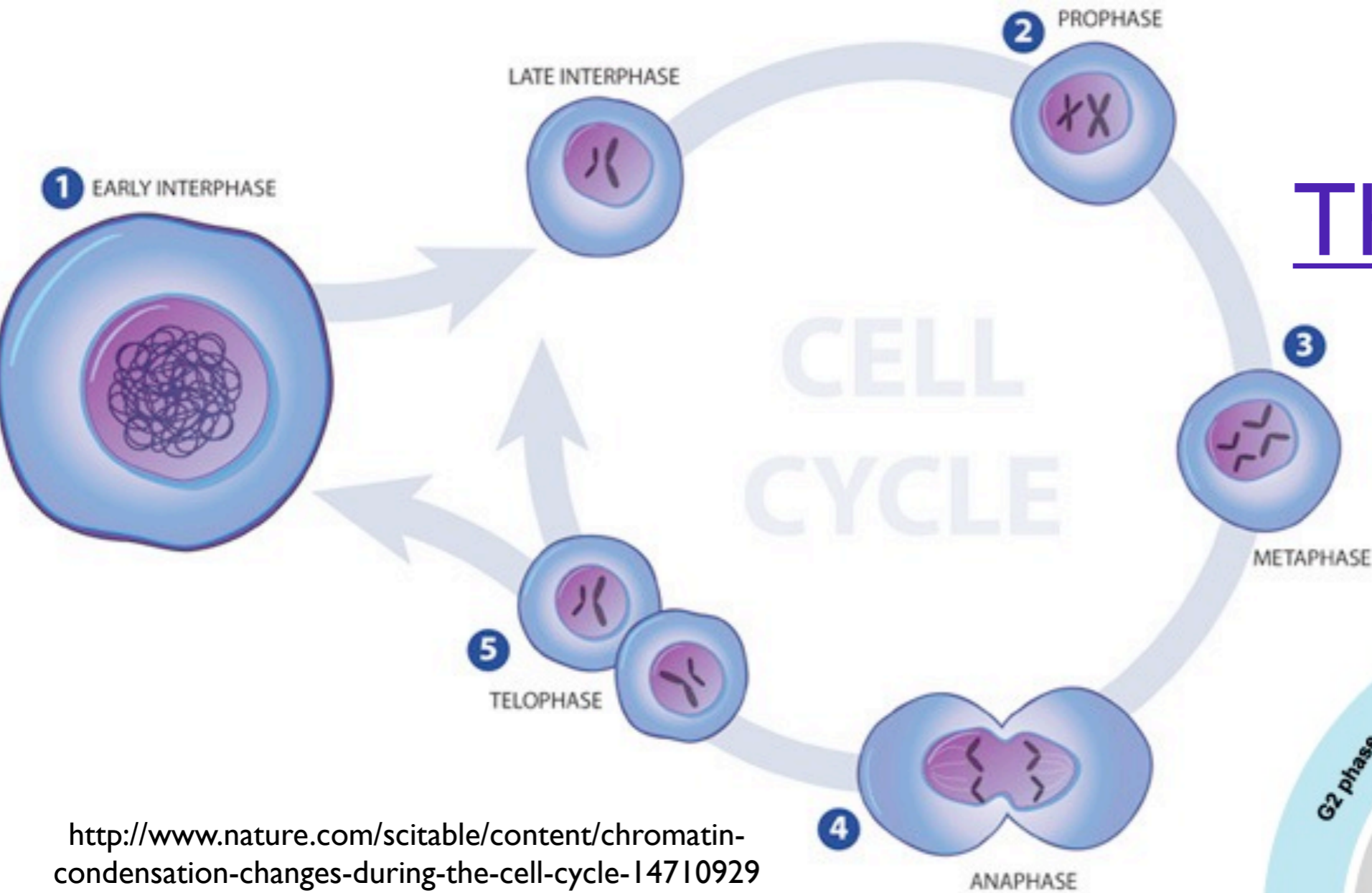
# Nucleus in eukaryotic cells



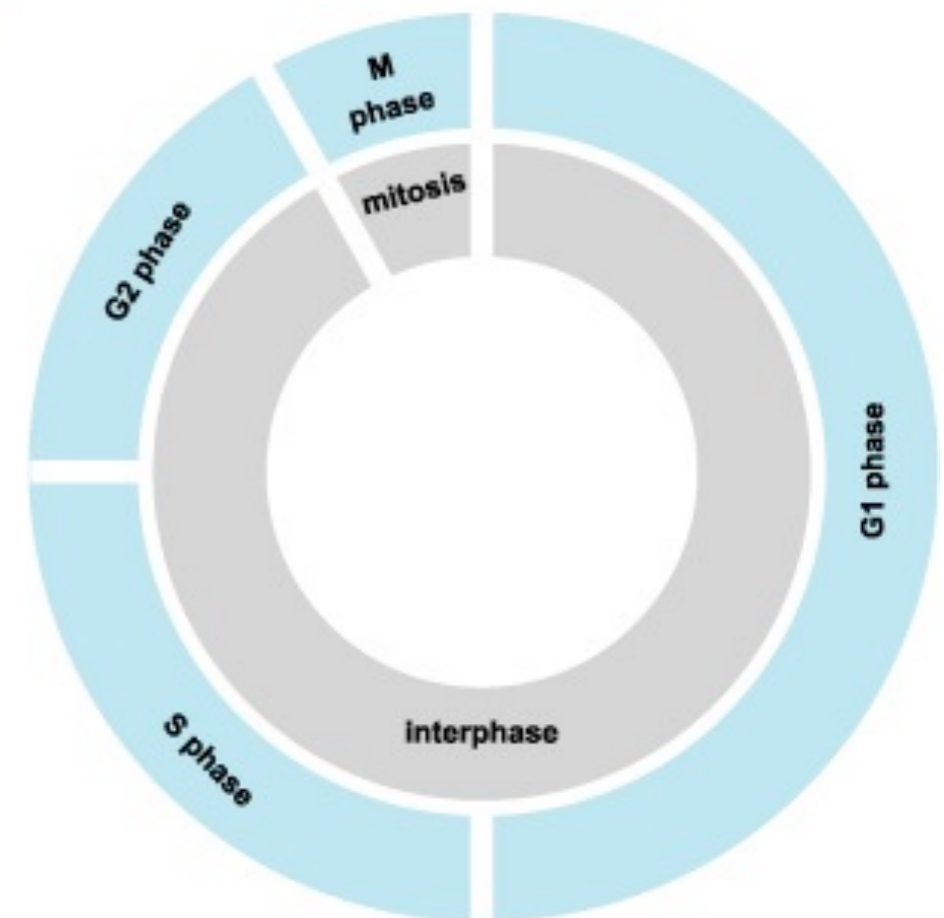


Wilson, Edmund B. (1900) The cell in Development and Inheritance (second edition). Wikimedia Commons

# The Cell Cycle

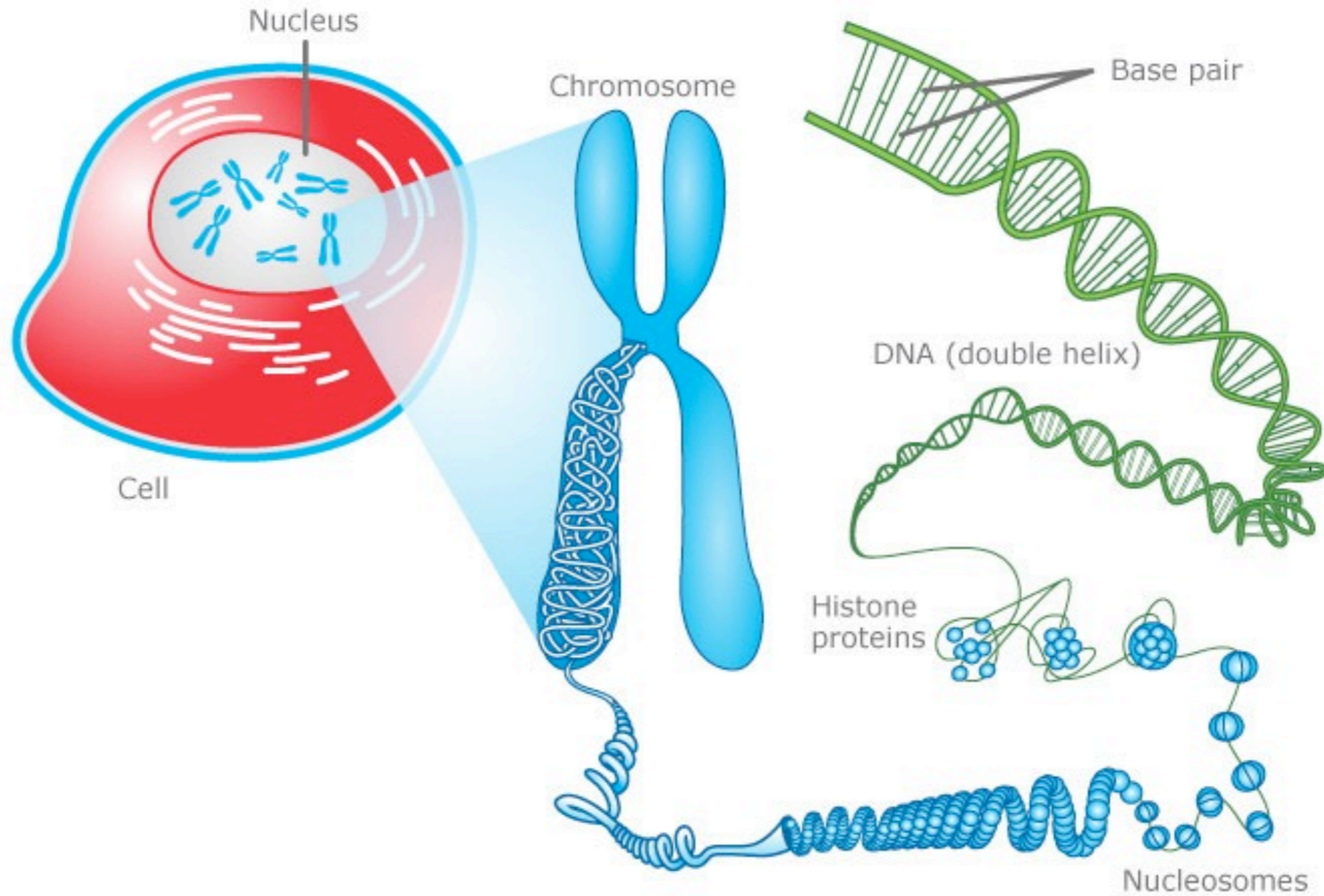


<http://www.nature.com/scitable/content/chromatin-condensation-changes-during-the-cell-cycle-14710929>



**Chromosomes in interphase nuclei**

<http://www.answers.com/topic/cell-cycle>



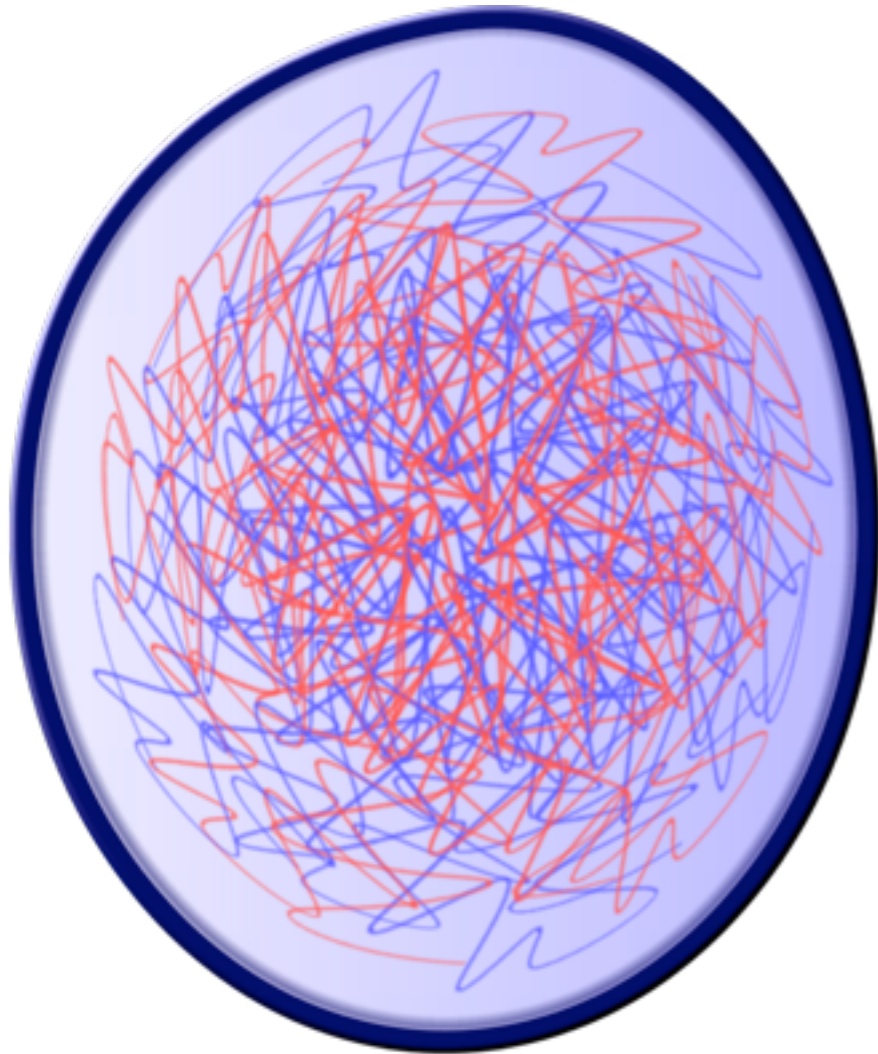
DNA packaged by **histones**.

Formed protein/DNA complex is **chromatin**  
(heterochromatin/euchromatin)

Structural entity of chromatin is the **nucleosome**



# Eukaryotic interphase chromatin was thought for many years to have no obvious pattern of organization



*During the 1970s and 1980s, most researchers seemed content with the assumption that the nucleus is filled with intermingling chromatin fibers and loops like a dish of spaghetti, an assumption widely reflected by textbooks of cell biology .....*

T. Cremer and M. Cremer, Cold Spring Harb Perspect Biol (2010)

Ability to fluorescently label each chromosome (FISH), showed that chromosomes

- are **territorial**
- have **nonrandom arrangements**

Rabl 1885, Boveri 1908, Stack 1977, Cremer, Bickmore, Misteli, ..

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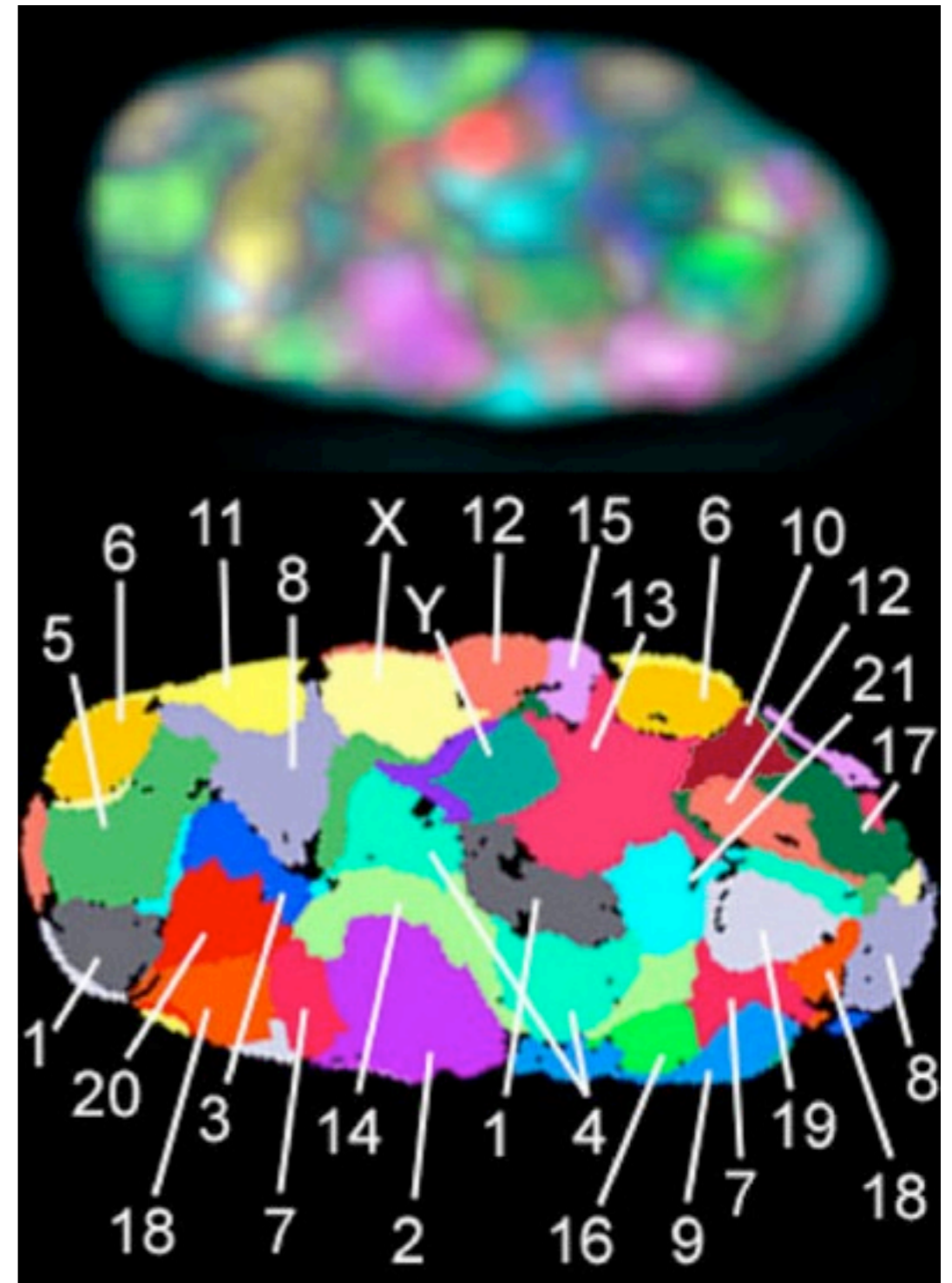
What governs the large-scale architecture of chromosome territories?

FISH =  
Fluorescence  
In-situ  
Hybridization

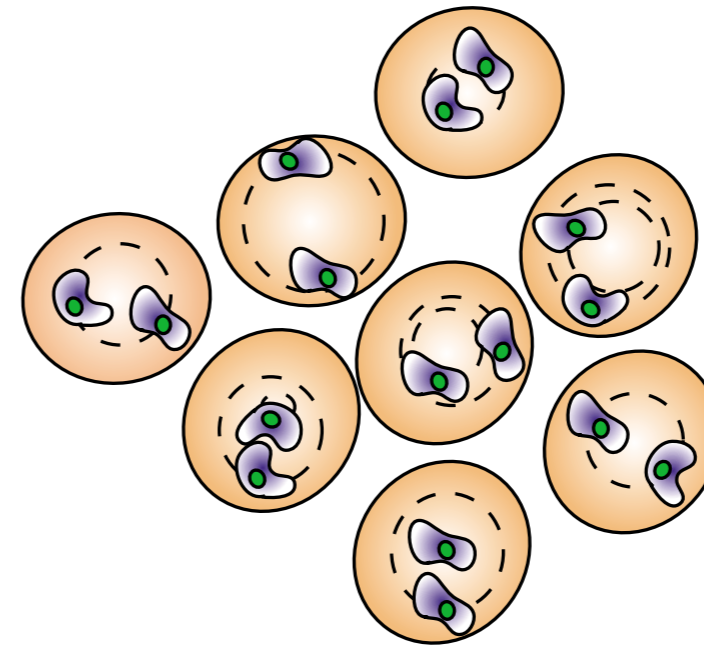
Three-Dimensional Maps of All Chromosomes in Human Male Fibroblast Nuclei and Prometaphase Rosettes

Andreas Bolzer<sup>1\*</sup>, Gregor Kreth<sup>2</sup>, Irina Solovei<sup>1</sup>, Daniela Koehler<sup>1</sup>, Kaan Saracoglu<sup>3</sup>, Christine Fauth<sup>4,5</sup>, Stefan Müller<sup>1</sup>, Roland Eils<sup>3</sup>, Christoph Cremer<sup>2</sup>, Michael R. Speicher<sup>4,5</sup>, Thomas Cremer<sup>1\*</sup>

Bolzer et al, PloS Biology (2005)

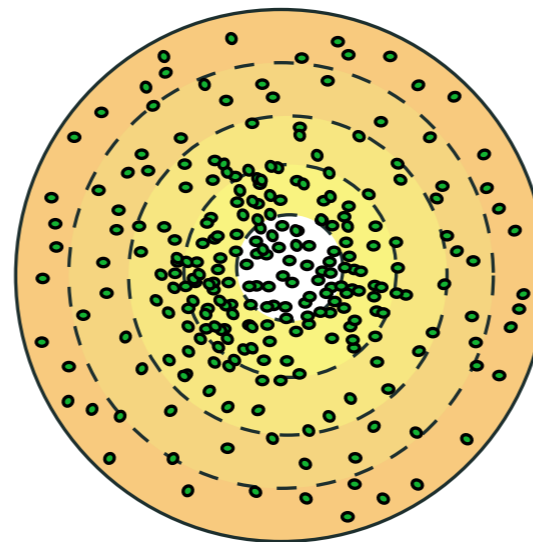


Given that  
chromosomes  
occupy non-random  
locations, what are  
the ‘**positioning rules**’  
that govern them?

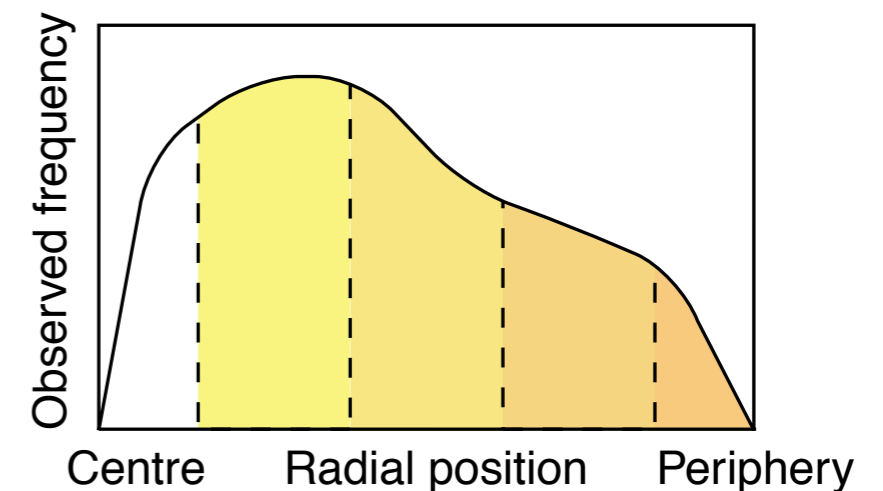


Experimental  
observation

Graphical  
representation



Statistical  
representation



## Differences in the Localization and Morphology of Chromosomes in the Human Nucleus

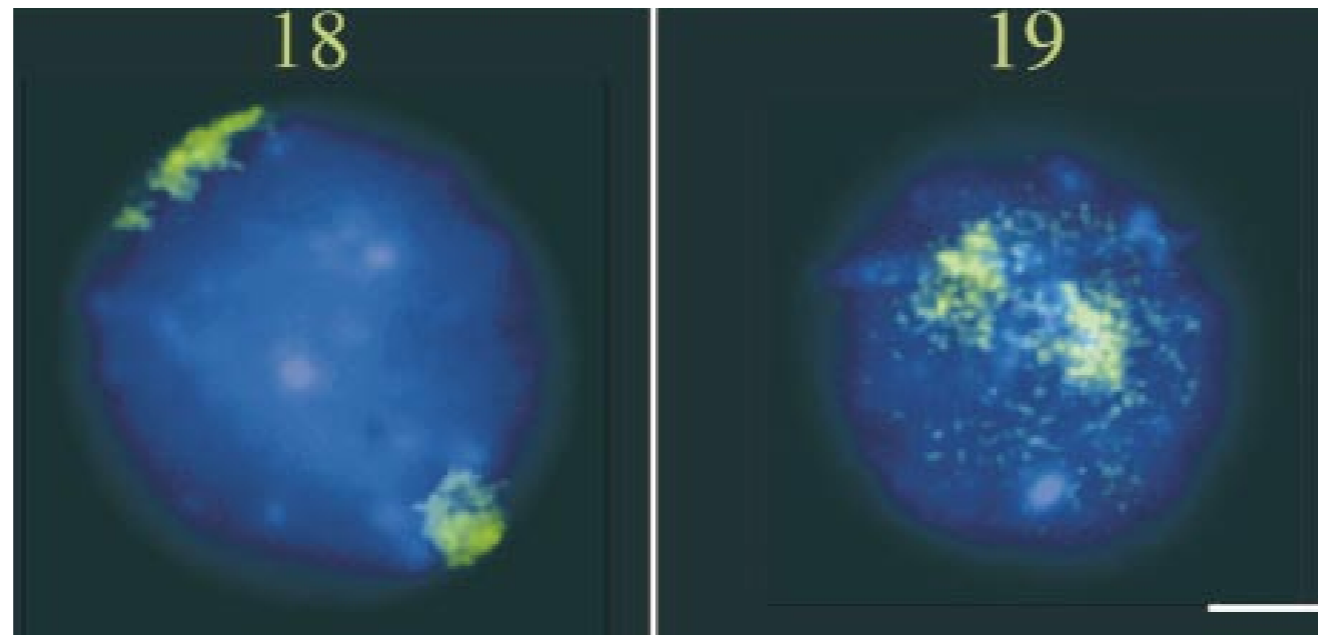
Jenny A. Croft, Joanna M. Bridger, Shelagh Boyle, Paul Perry, Peter Teague, and Wendy A. Bickmore

The Journal of Cell Biology, Volume 145, Number 6, June 14, 1999 1119–1131

*Abstract.* Using fluorescence in situ hybridization we show striking differences in nuclear position, chromosome morphology, and interactions with nuclear substructure for human chromosomes 18 and 19. Human chromosome 19 is shown to adopt a more internal position in the nucleus than chromosome 18 and to be more extensively associated with the nuclear matrix.

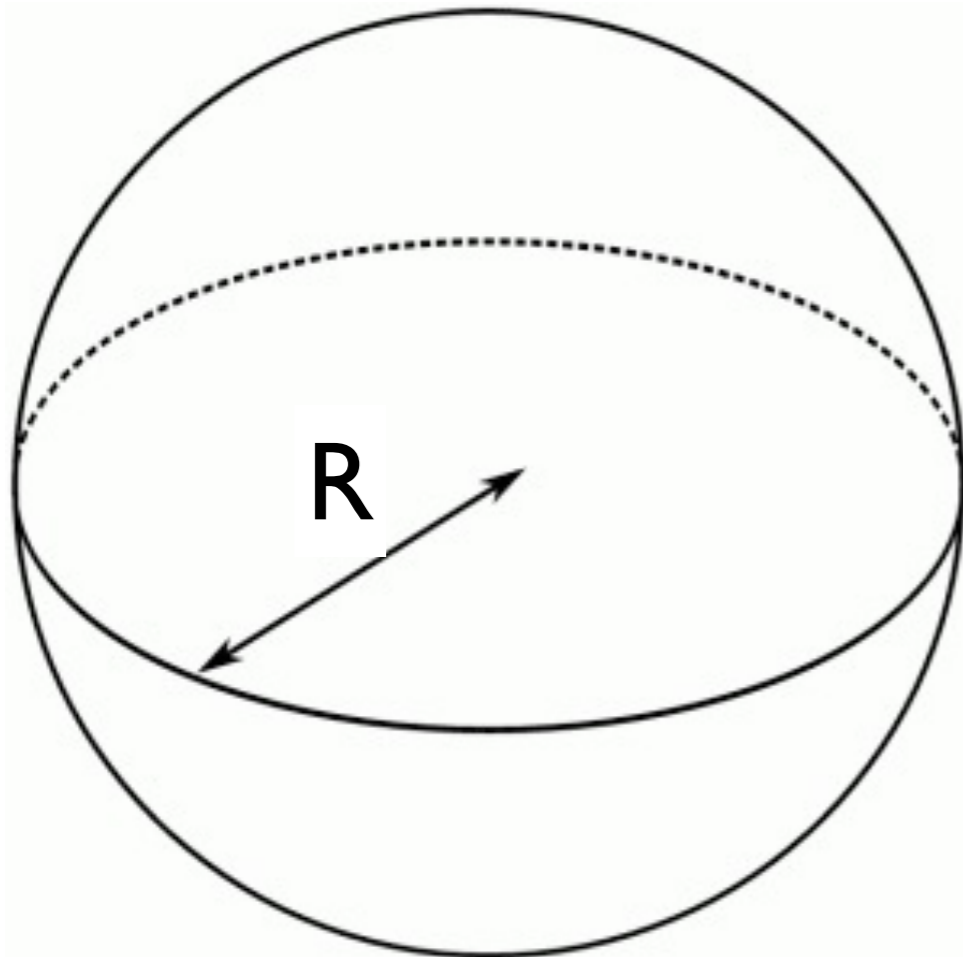
Chromosome 19:  
62.03 genes/Mb and  
60 Mb size

Chromosome 18:  
18.64 genes/Mb and  
78 Mb size

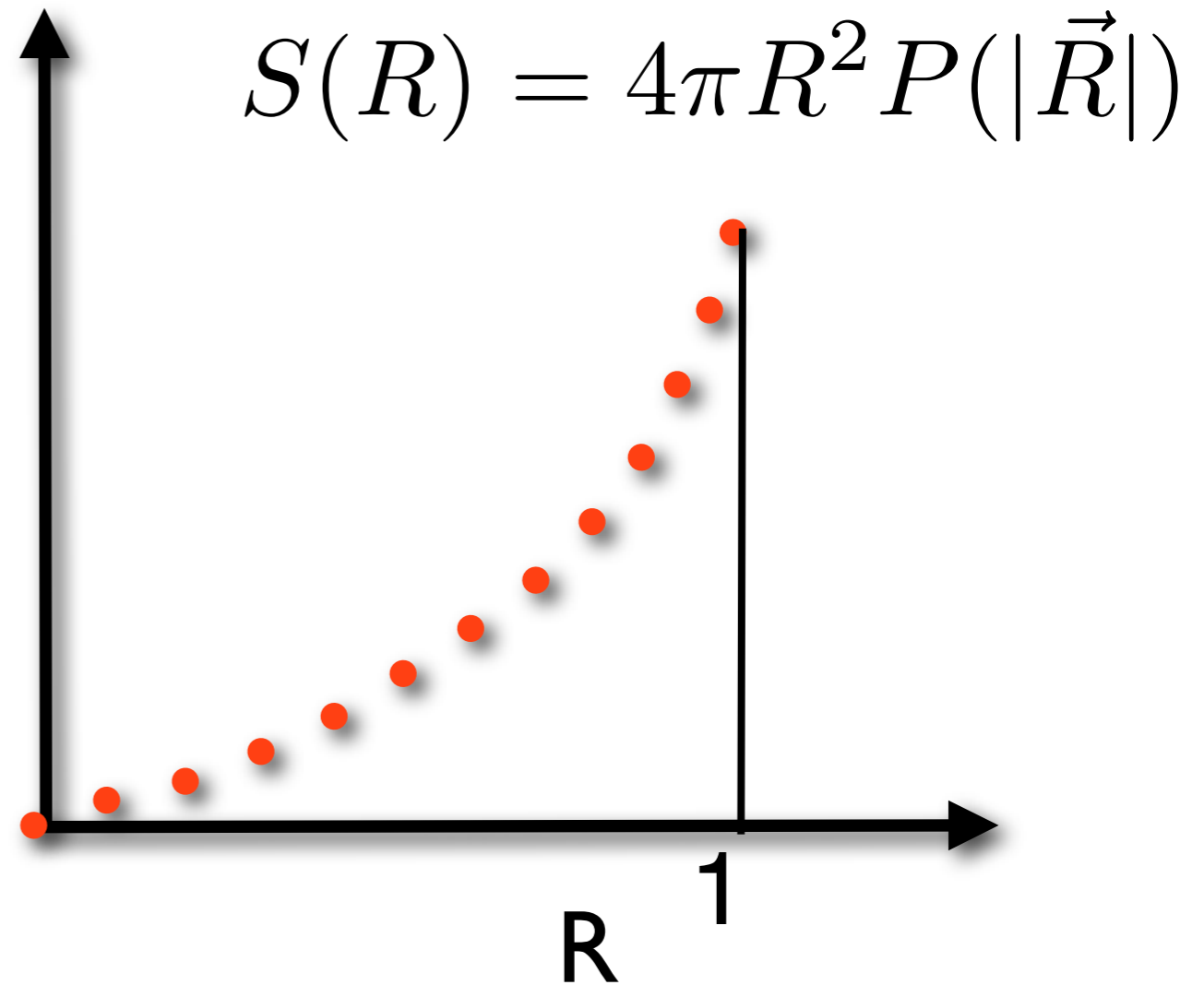


Radial chromosome positioning dependent on  
gene density?

## Radial symmetry



$S(R)$



If each chromosome is distributed uniformly throughout the nucleus, then  $S(R)$  quadratic, maximum at nuclear envelope

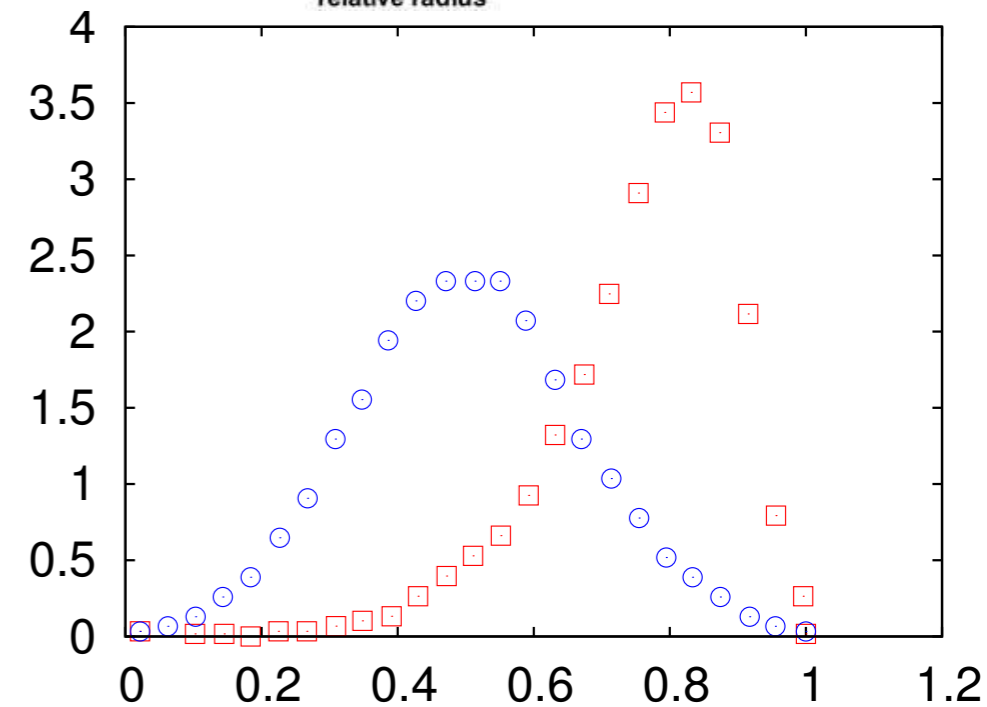
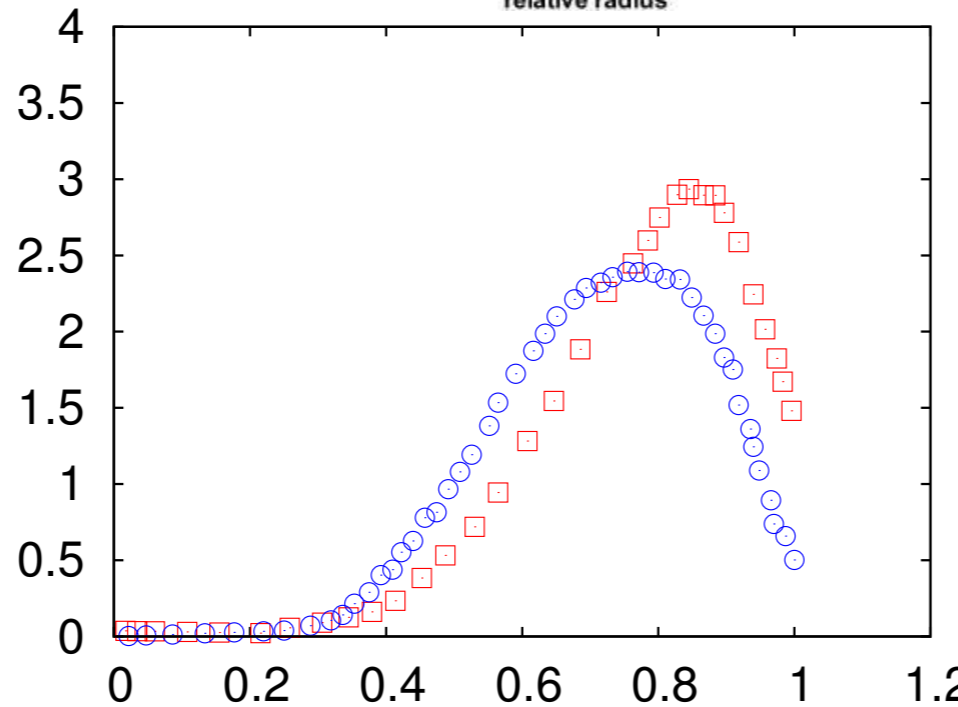
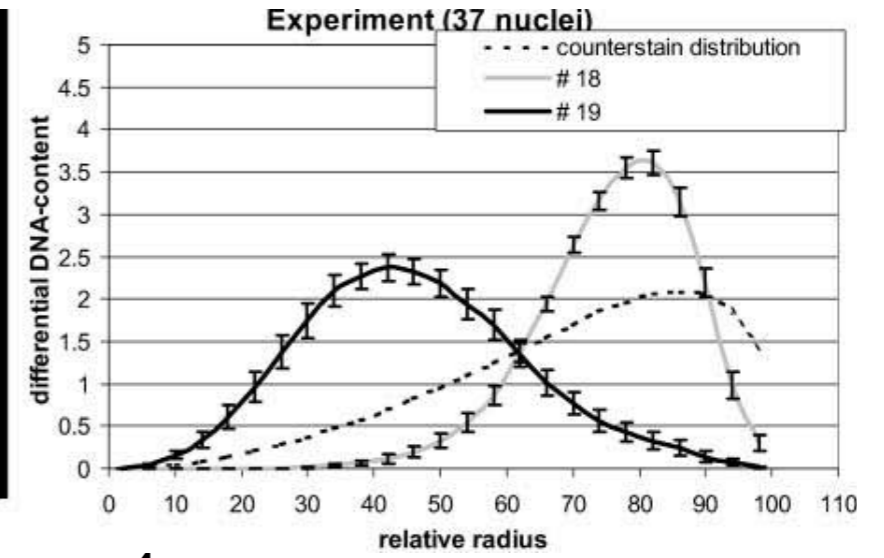
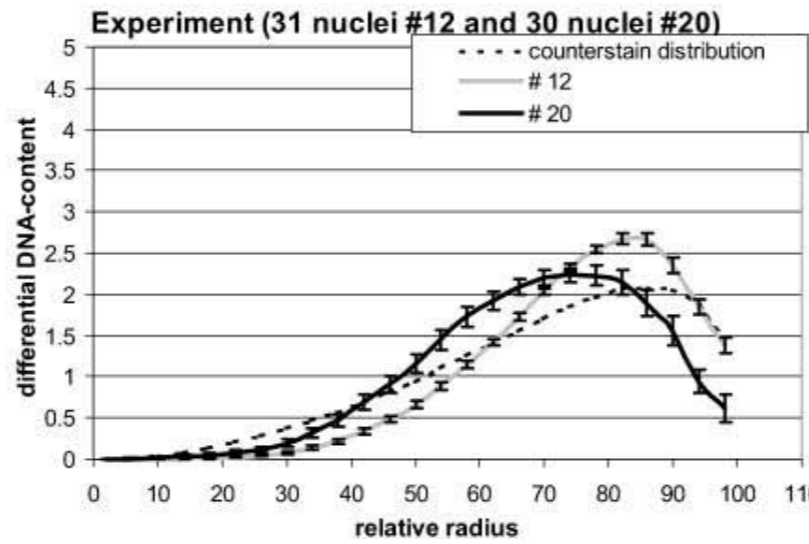
Good diagnostic for non-random placement

Chromosome 12:  
30.92 genes/Mb  
and 134 Mb size,

Chromosome 20:  
29.71 genes/Mb  
and 63 Mb size)

Chromosome 19:  
62.03 genes/Mb  
and 60 Mb size

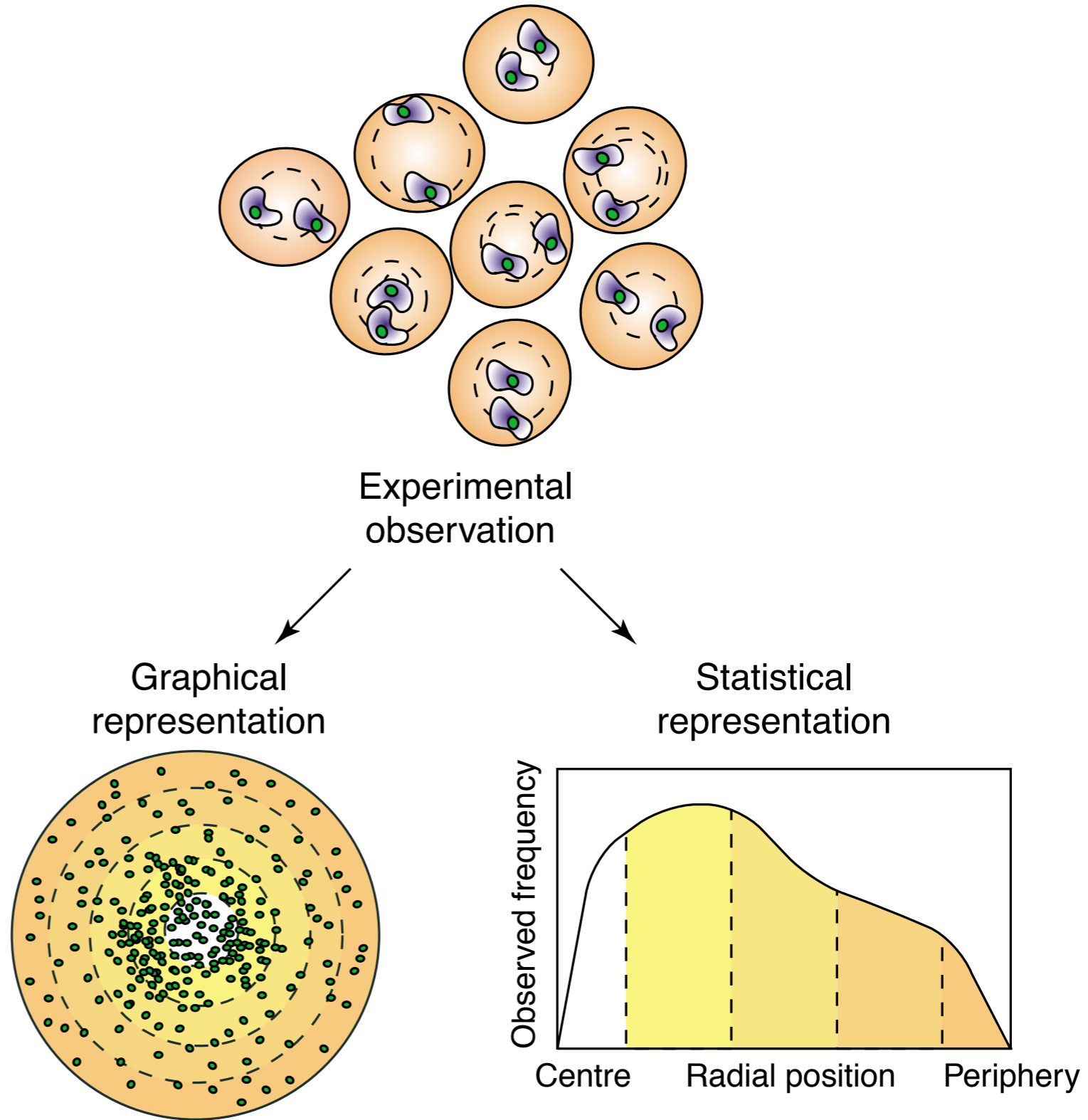
Chromosome 18:  
(red) 18.64 genes/  
Mb and 78 Mb size



Chromosomes 12 and 20 have different sizes  
but the same gene density

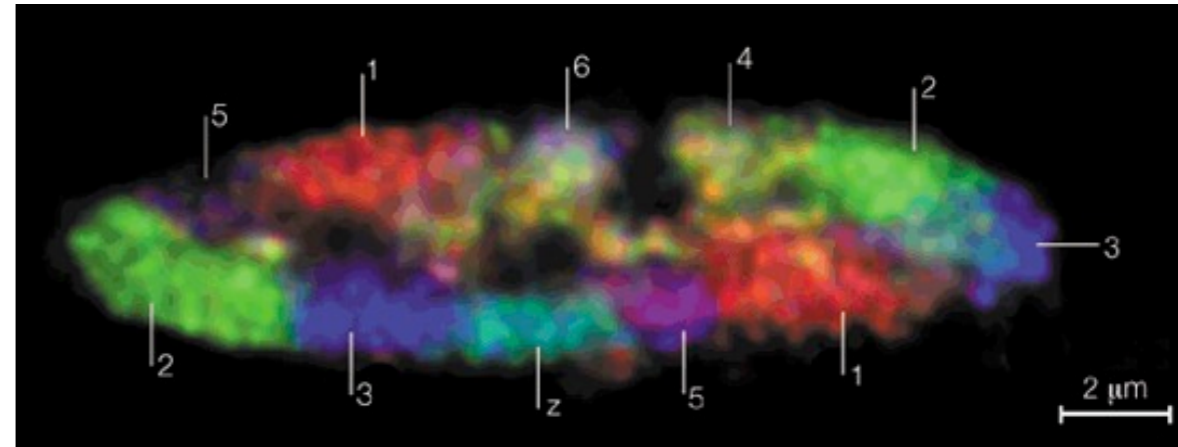
Chromosomes 18 and 19 have roughly the  
same size but different gene densities

Given that chromosomes are (in many but not all cases) radially ordered by gene density, how do we understand this specific ‘positioning rule’?



# Hypothesize:

Non-equilibrium mechanical activity (transcription and chromatin remodeling machinery), inhomogeneous across gene-rich and gene-poor regions gives gene-density-based radial segregation



T.Cremer and C. Cremer, Nature Reviews Genetics vol. 2, no. 4, pp. 292-301 (April, 2001)

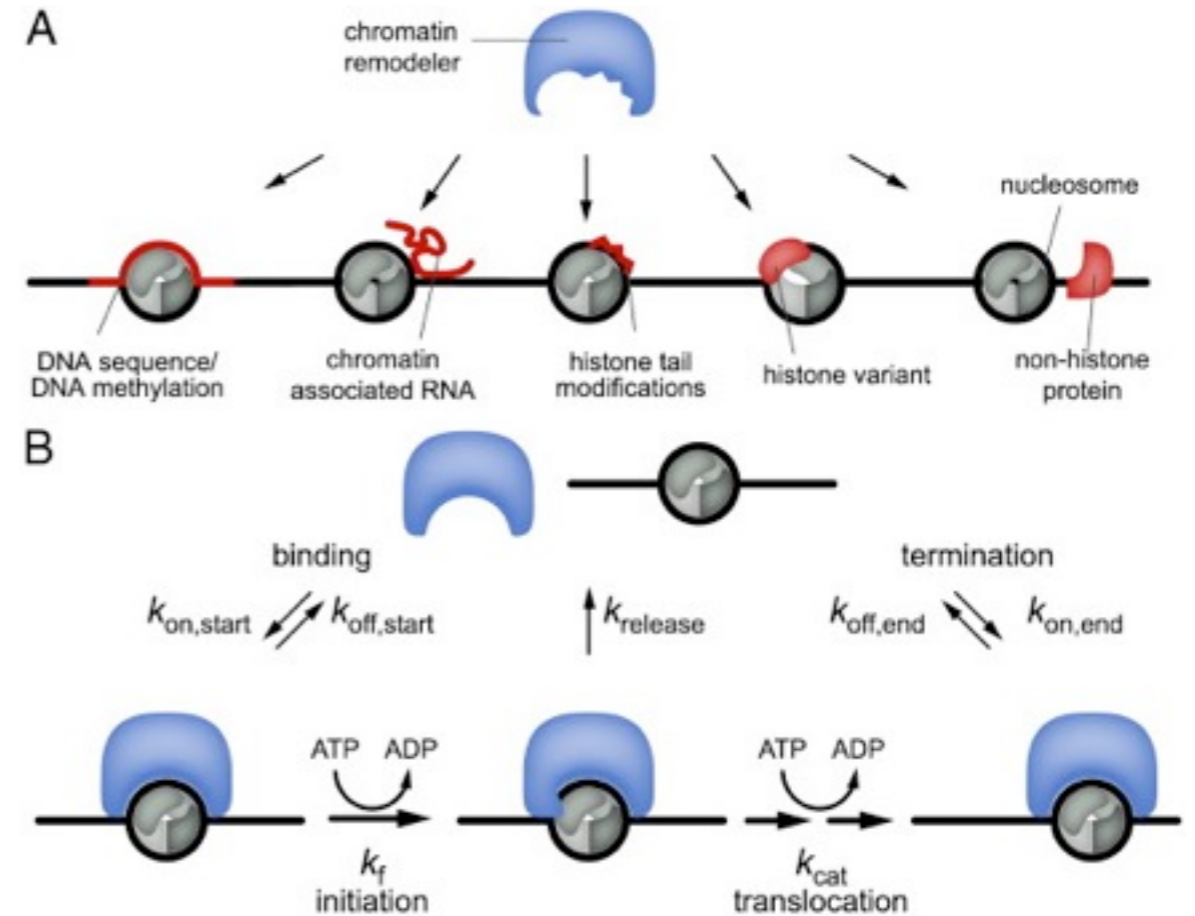
No self-propulsion - unlike in all active matter models studied so far - but inhomogeneous activity, confinement and polymer character all important

Chromosome territories a natural consequence of compact chromosome configurations and activity



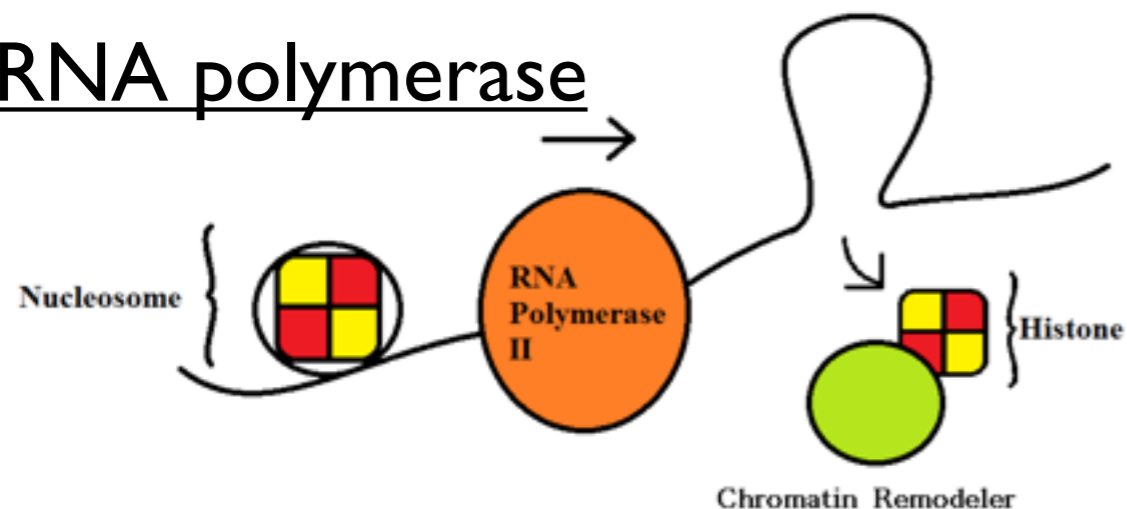
ATP-driven molecular machines change chromatin structure, translocate nucleosomes, evict nucleosomes, change nucleosomal histone composition, involved in transcription. Work in concert through remodeler-specific interactions. Highly dynamic. Present at large density

# Chromatin Remodelers



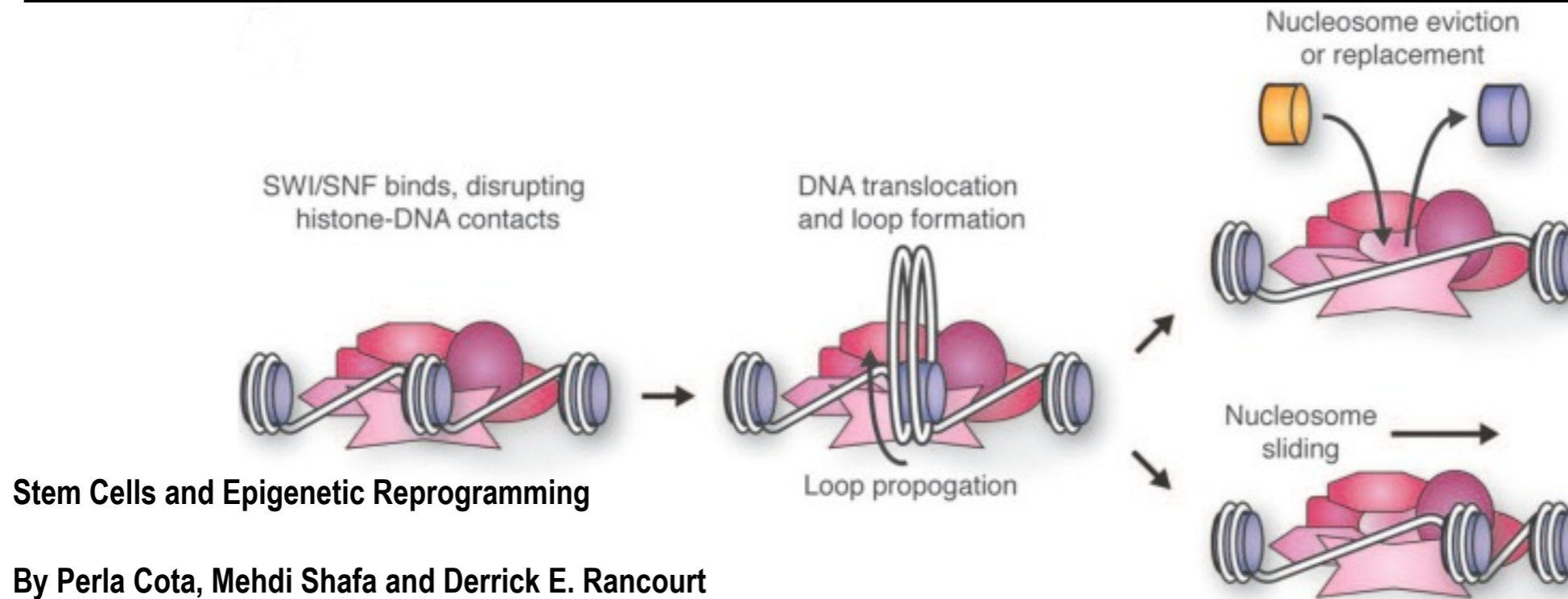
Erdel et al, BBA (2011)

## RNA polymerase



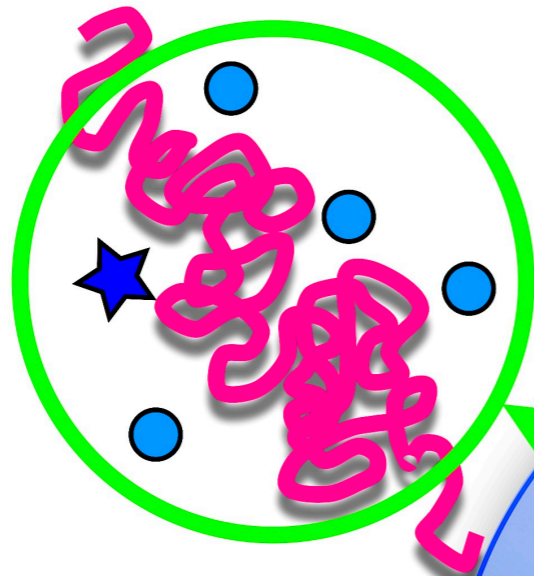
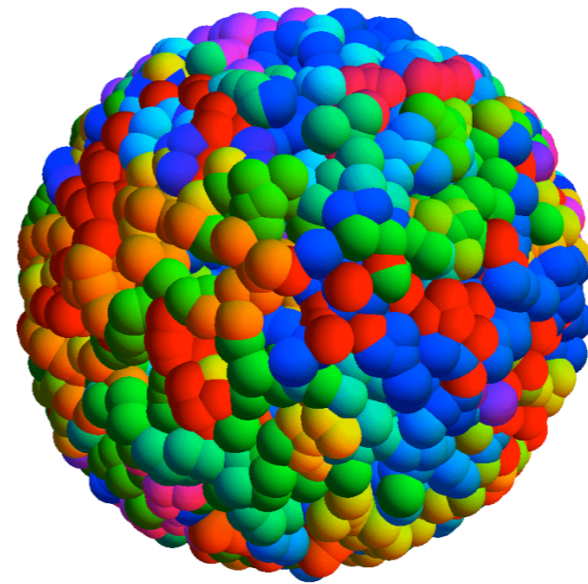
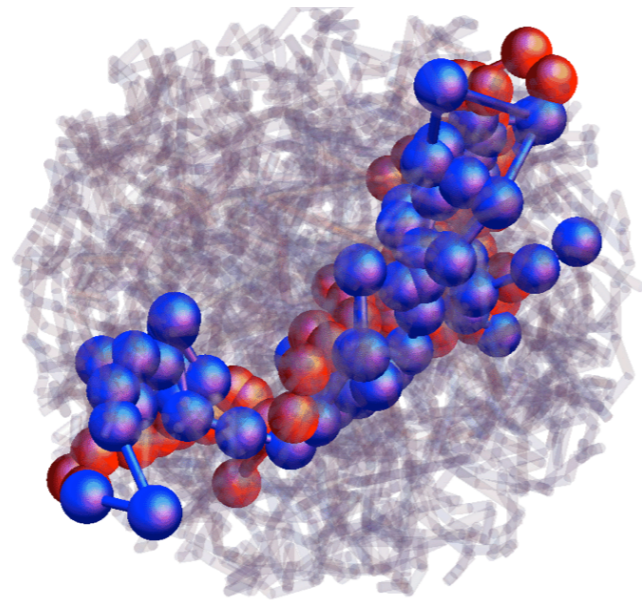
Barriers to nucleosome motion: 20-40 kT

# 'Mechanical' effects of active chromatin remodelers?

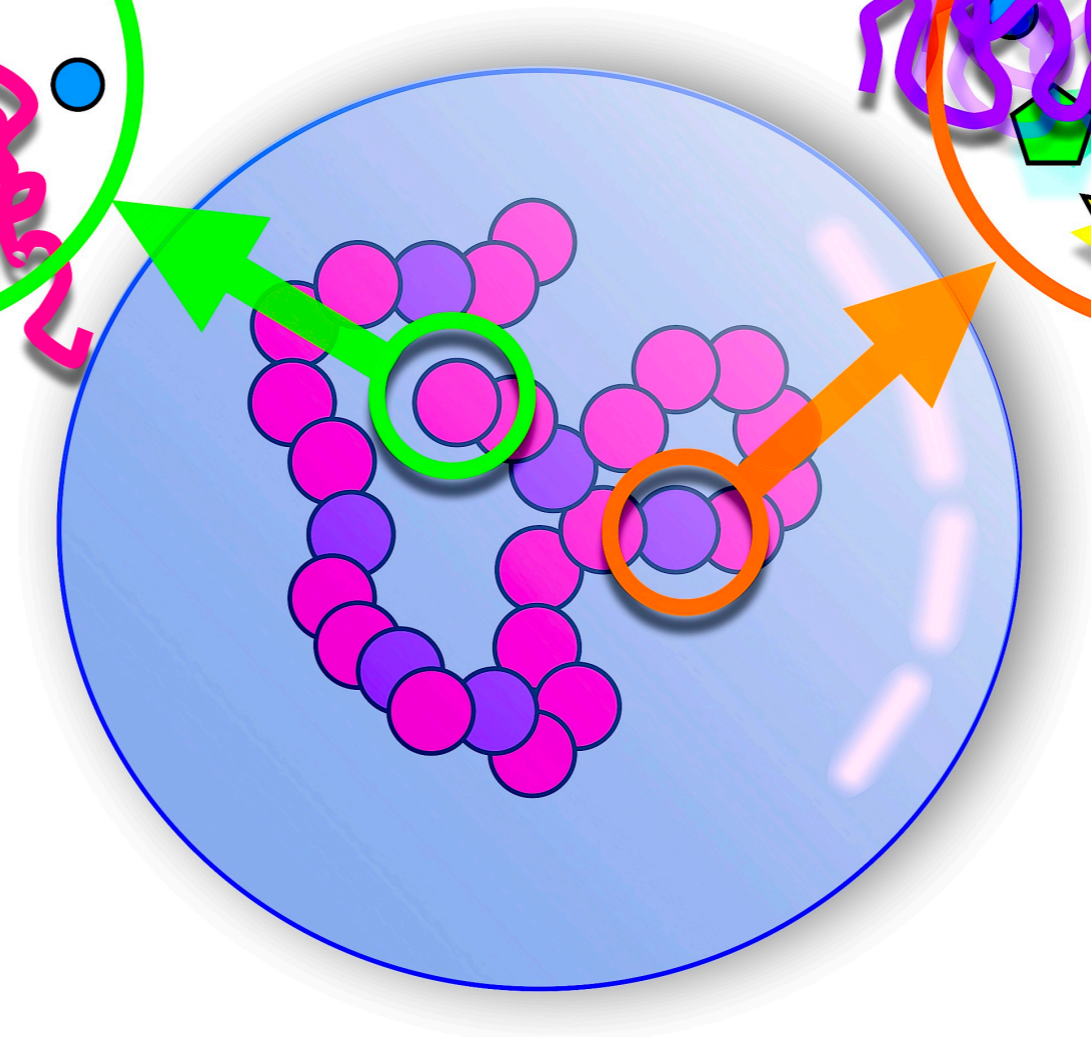


in "Pluripotent Stem Cells", ed. Deepa Bhartiya and Nibedita Lenka, Intech (2013)

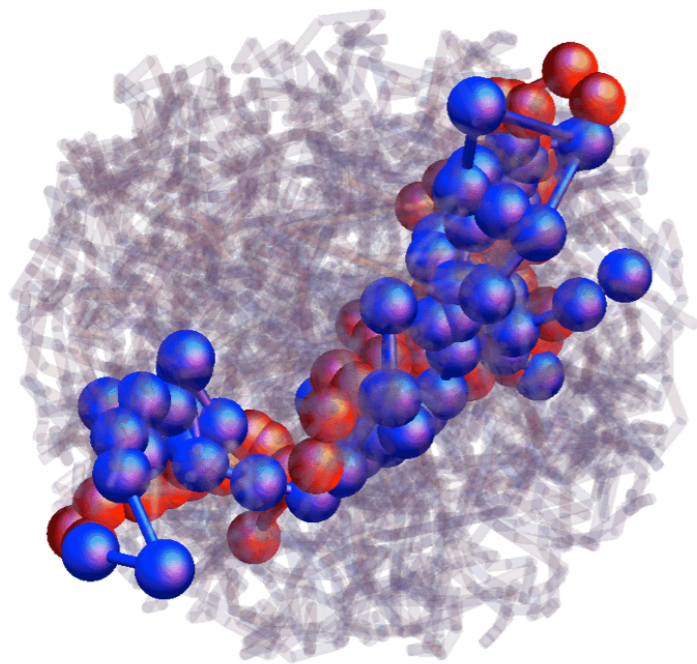
1. Effective local 'active temperature'  $T_{act}$ , associated with gene density. More transcription implies more ATP-consuming activity from remodeling/transcription-coupled enzymes
2. Coarse-grain to athermal noise acting on, **1Mb scale** monomers (Known to be appropriate to functional units of chromosome territories)
3. Estimate scales of active temperature (barriers to nucleosome motion, etc):  $T_{act} = 20T_{therm}$



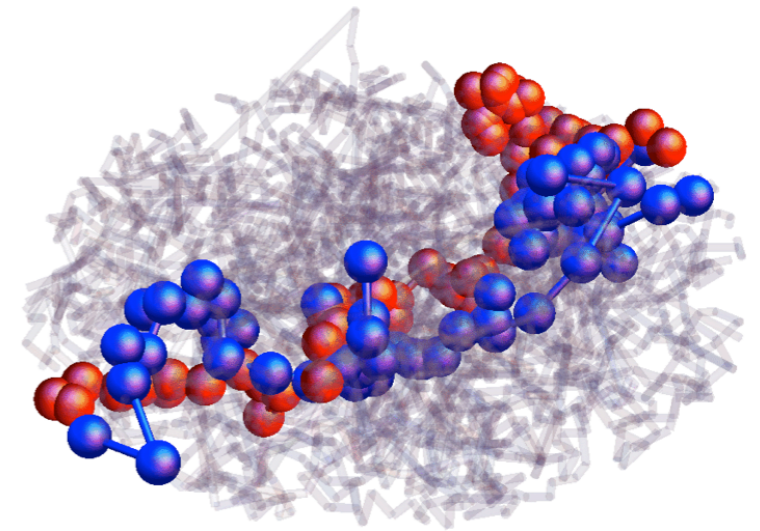
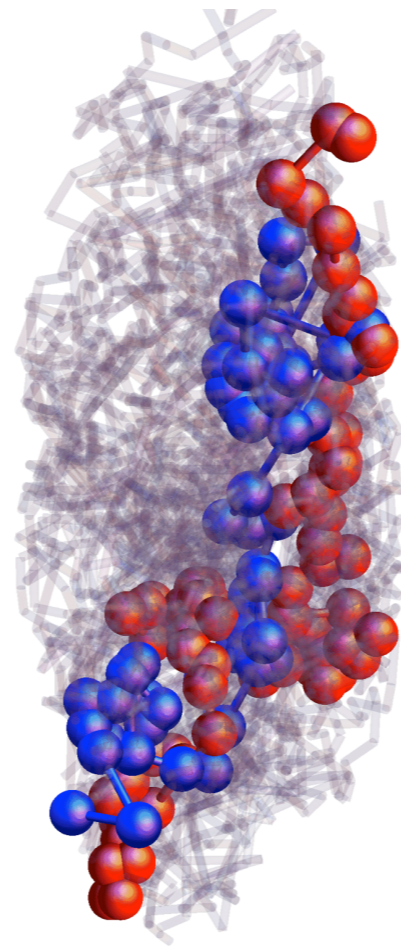
*inactive*



*active*



Simulations using the  
SCD model (spherical  
chromatin domain)



$$\zeta \frac{d\mathbf{r}_i}{dt} = \mathbf{F}_i + \eta_i$$

$$\langle \eta_i^\alpha(t) \eta_j^\alpha(t') \rangle = 2k_B T_i \zeta \delta_{ij} \delta(t - t').$$

Brownian dynamics, 3-d: 6098 monomers

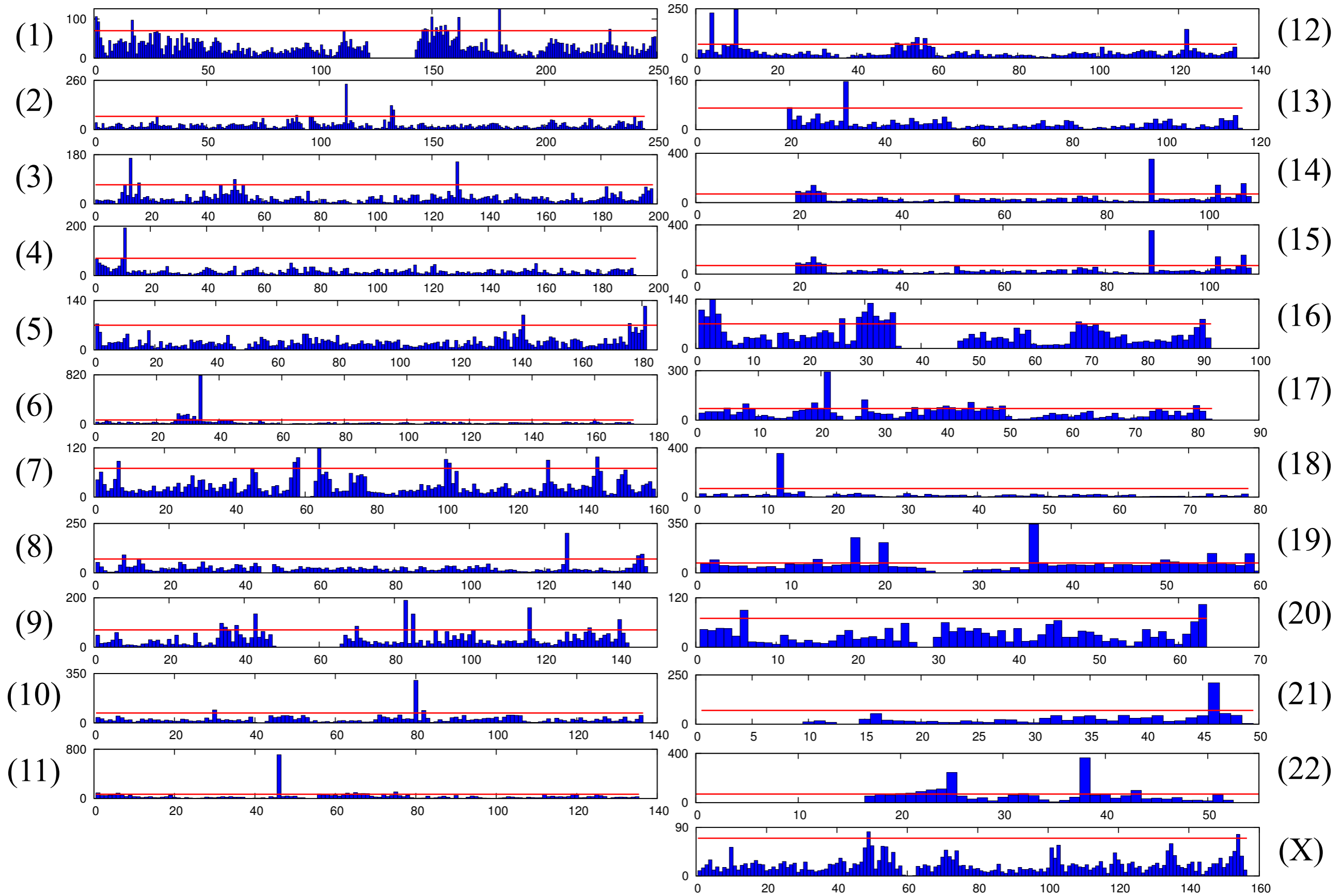
Different effective temperature for each monomer

Assign this depending on gene density (very nonlinearly)

Varied nuclear shape: spherical, ellipsoidal

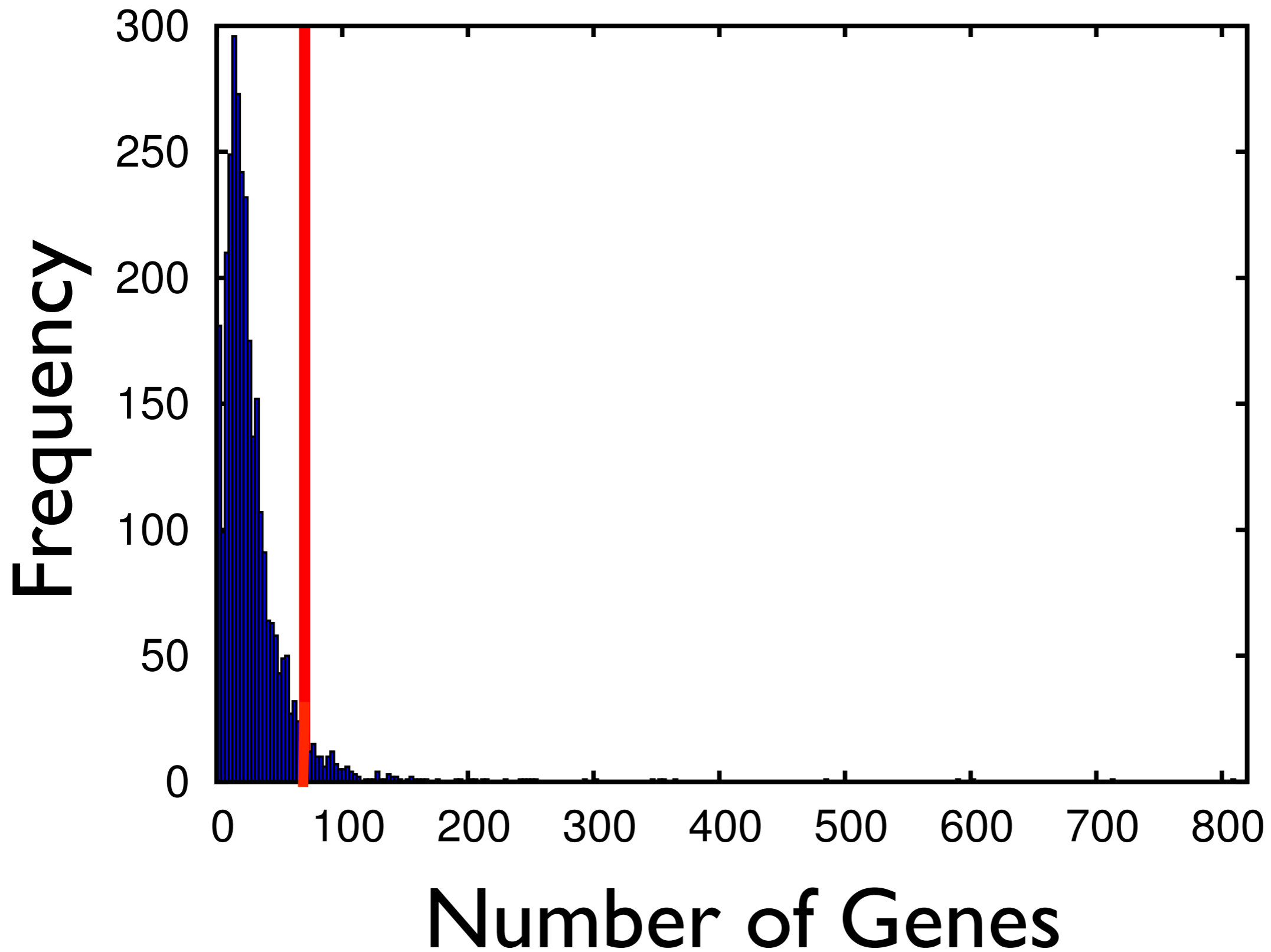
Passive and active confinement

Number of Genes



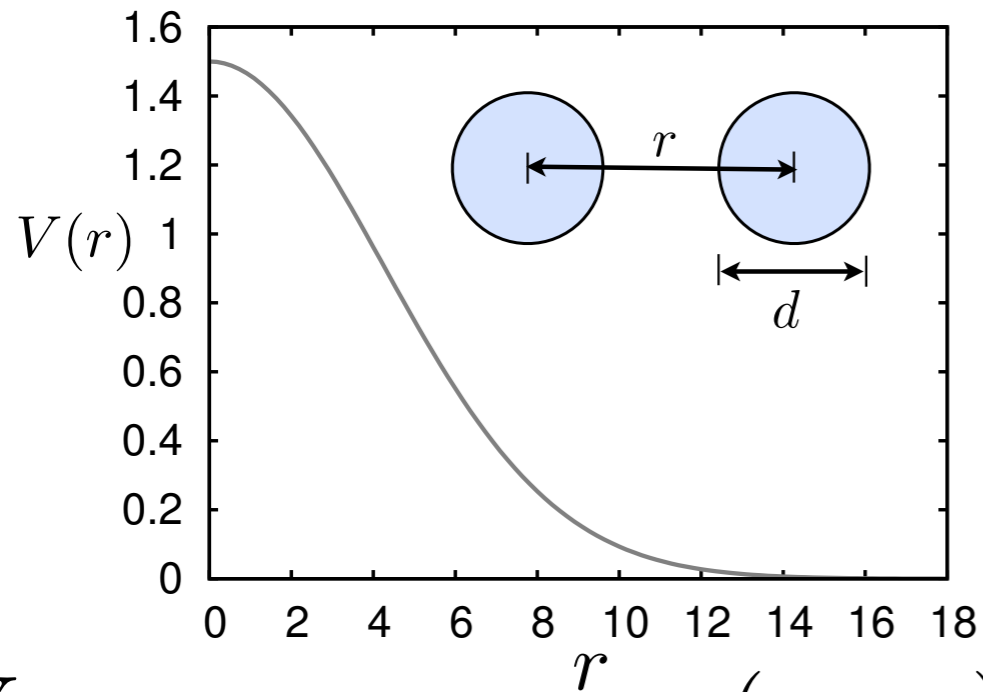
Location (Mbp)

# Assigning activity to each monomer, from gene densities



$$V_{neighbour\ monomers}(\mathbf{r}_i, \mathbf{r}_{i+1}) = \frac{1}{2}k(|\mathbf{r}_i - \mathbf{r}_{i+1}|)^2$$

## Monomer-Monomer Interactions



$$d \simeq 500nm,$$

$$R_0 \simeq 6.7\mu m$$

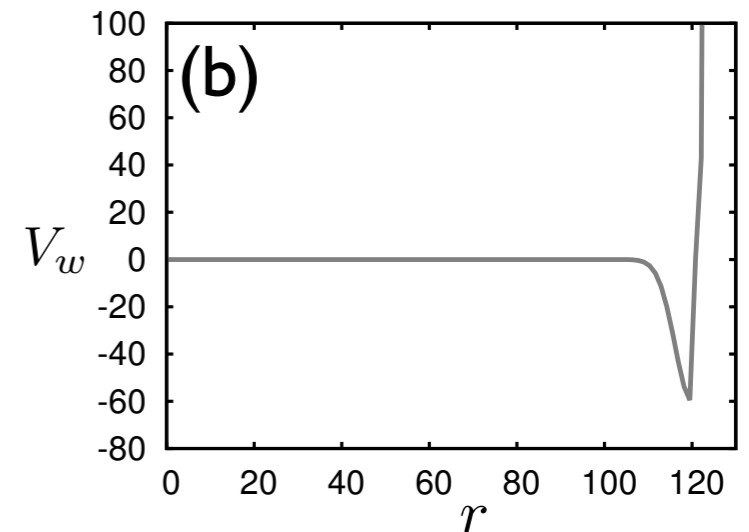
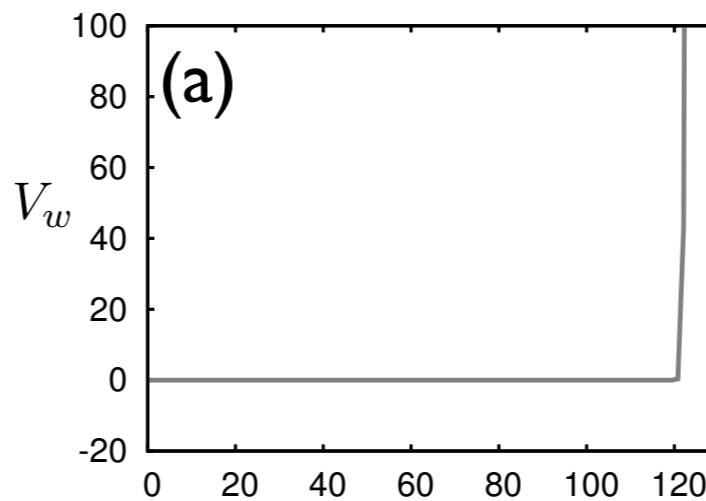
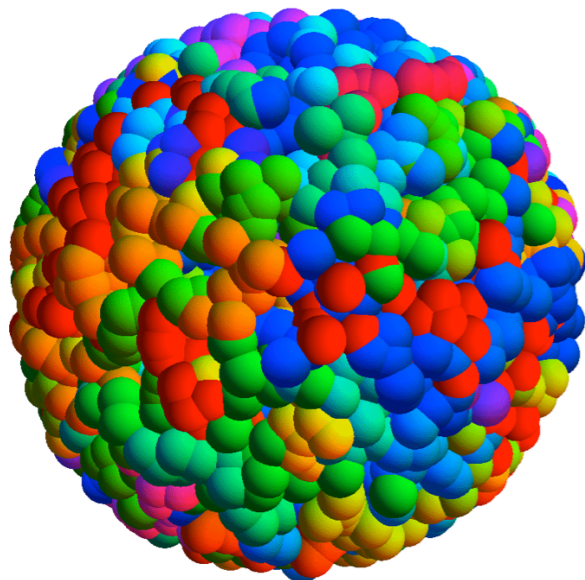
$$\ell_0 \simeq 600nm$$

$$V_0 \simeq 1.5k_B T_{eq}$$

**Self-repelling but not self-avoiding**

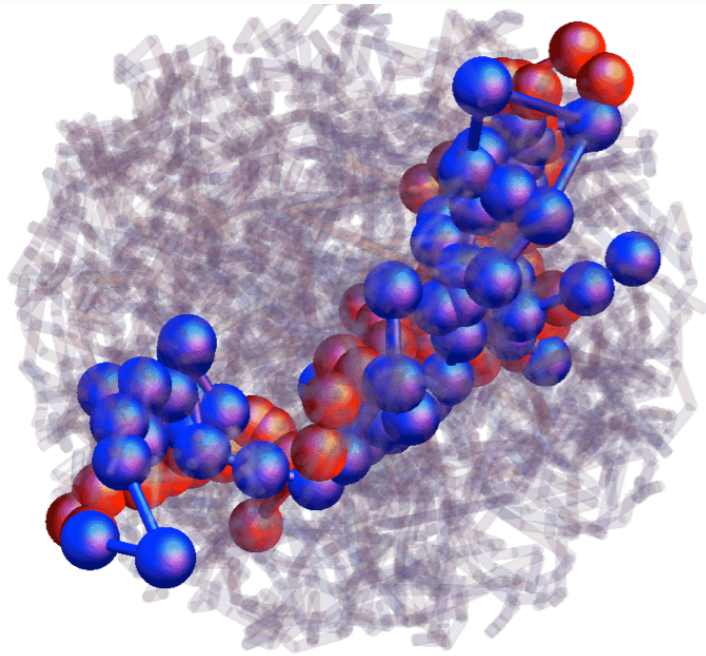
$$V_{monomer-monomer}(\mathbf{r}_i, \mathbf{r}_j) = V_0 \exp(-|\mathbf{r}_i - \mathbf{r}_j|^2 / \sigma^2)$$

## Monomer-Wall Interactions

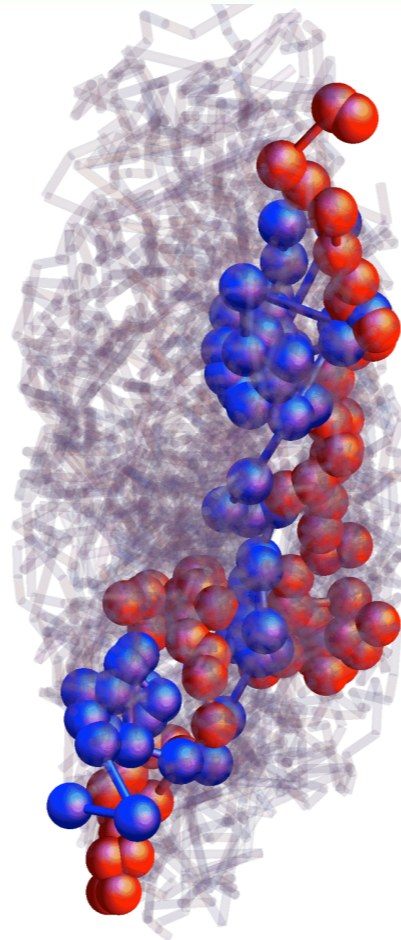


$$V_{wall}(\mathbf{r}_i) = \frac{V_{conf}}{a^5} (|\mathbf{r}_i| - R_0)^5, \quad |\mathbf{r}_i| > R_0$$

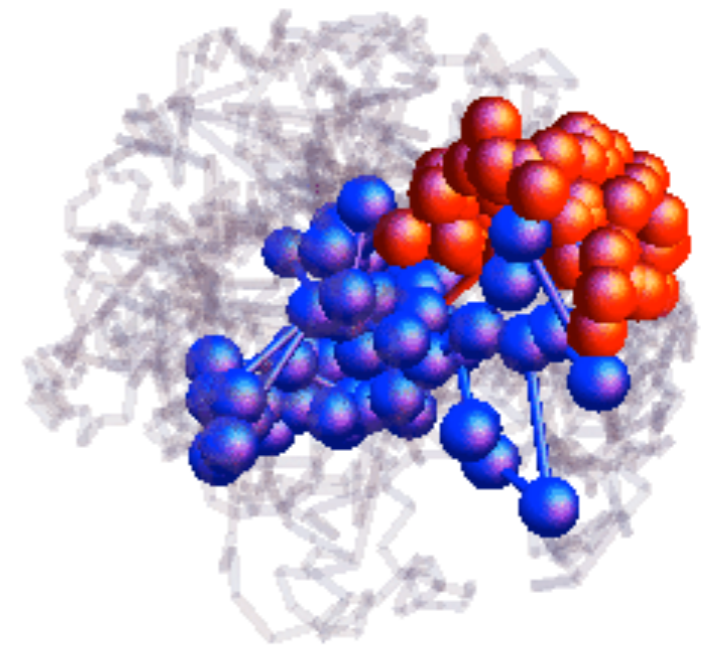
# Simulation Configurations



Spherical Confinement,  
Equilibrium



Ellipsoidal Confinement,  
Equilibrium



Spherical  
Confinement, non-  
Equilibrium



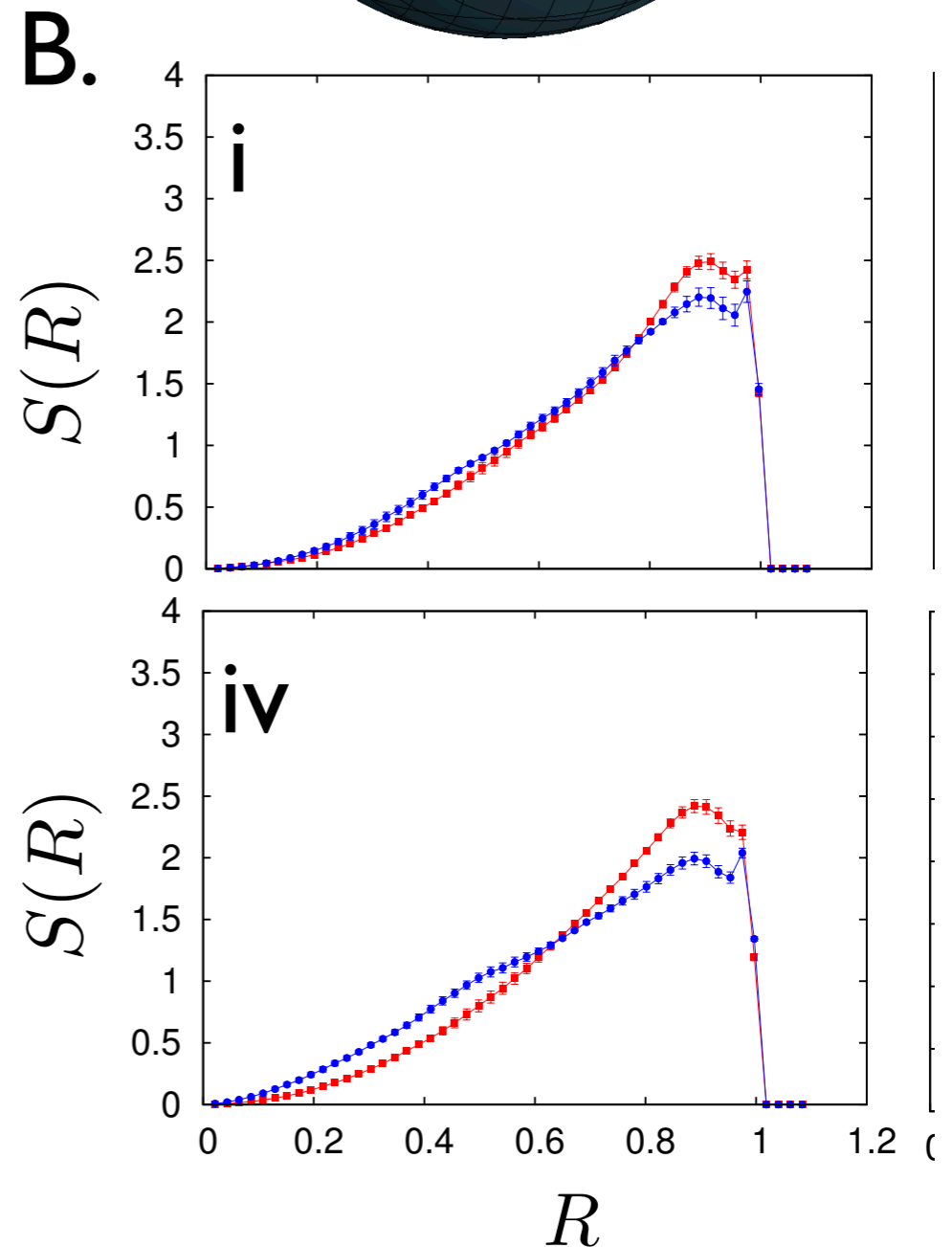
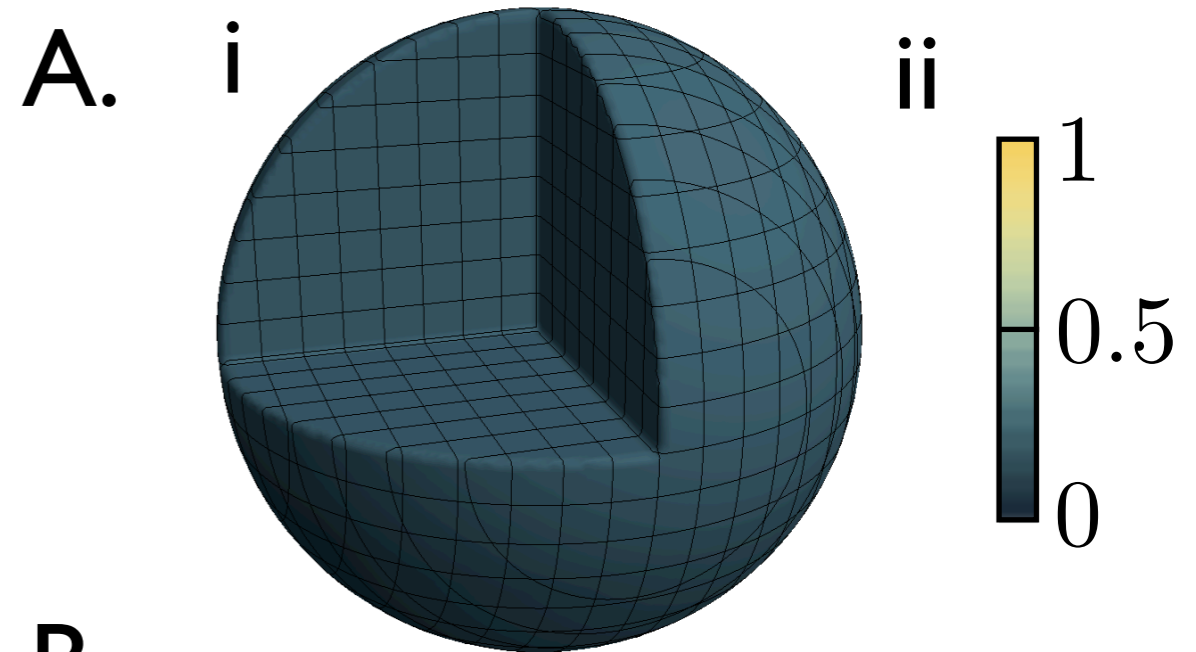
Cut-away sphere  
representation of local activity

Thermal equilibrium

Chromosome 18/19

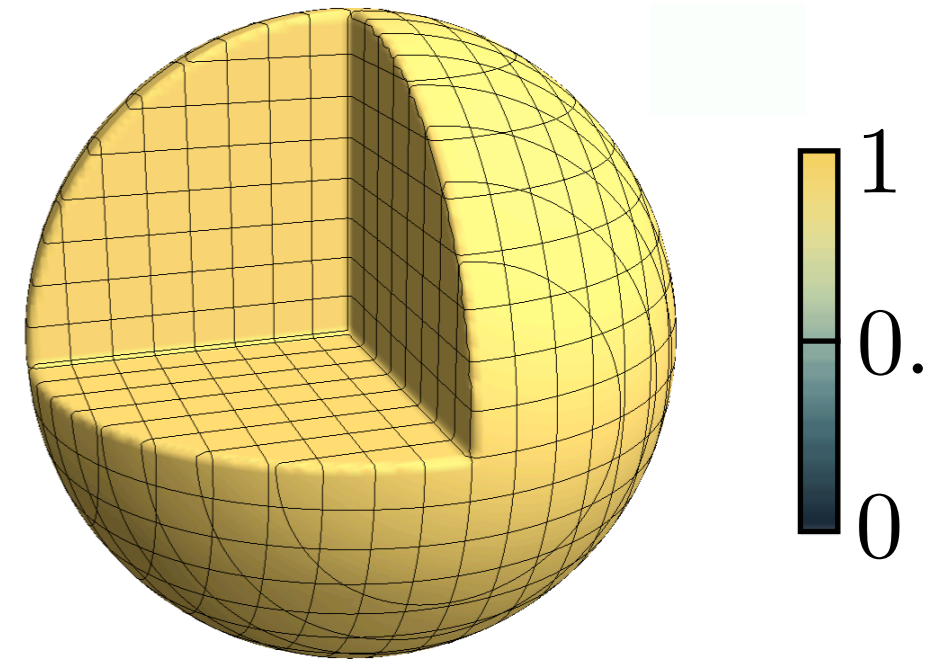
$T = T_{\text{therm}}$

Chromosome 12/20



# Cut-away sphere representation of local activity

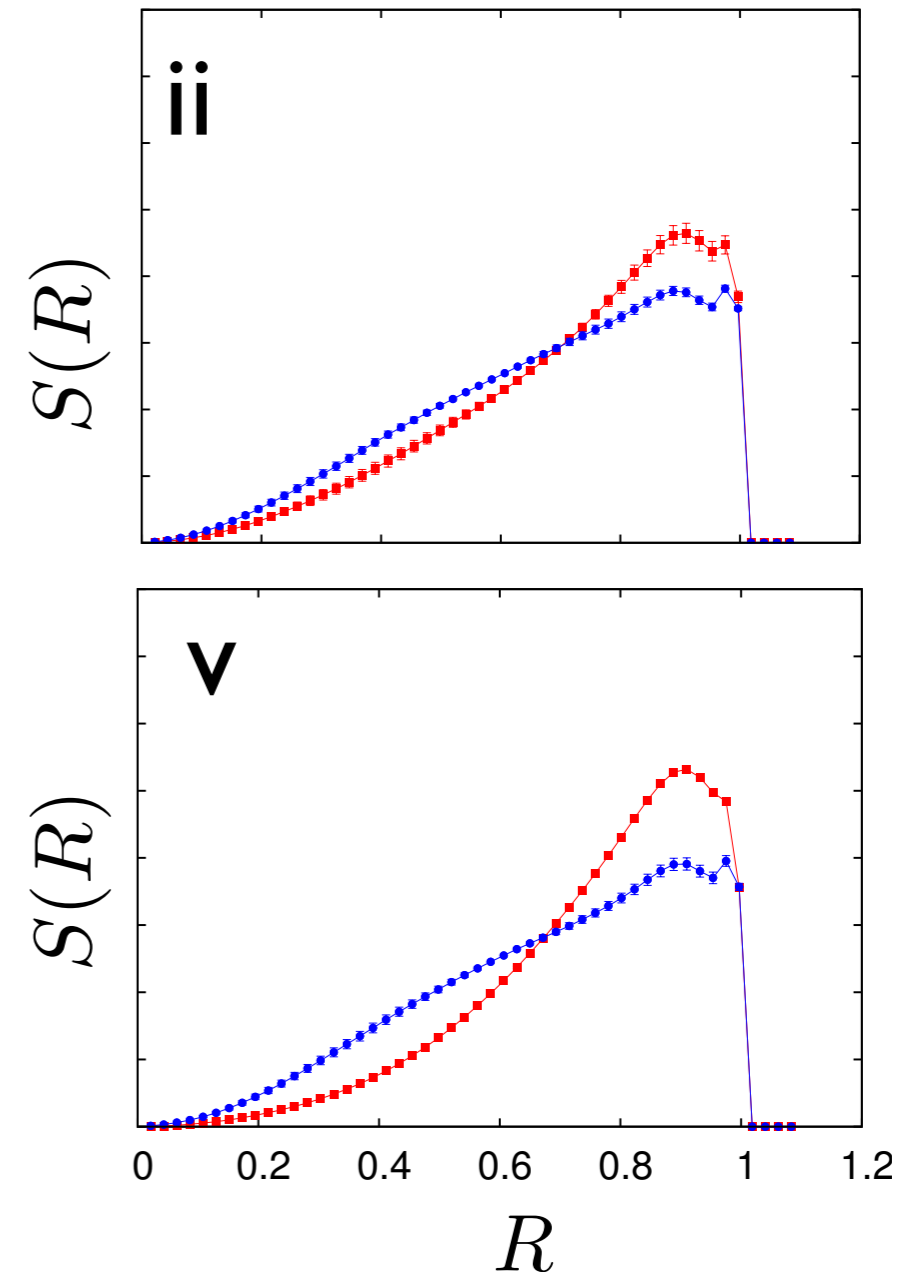
All monomers at uniform high active temperature



Chromosome 18/19

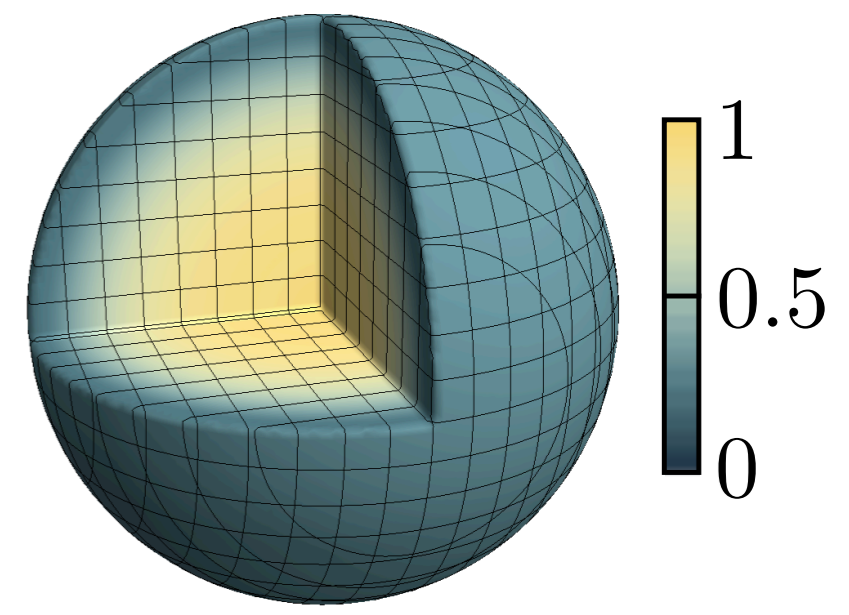
$T = 20 T_{\text{therm}}$

Chromosome 12/20

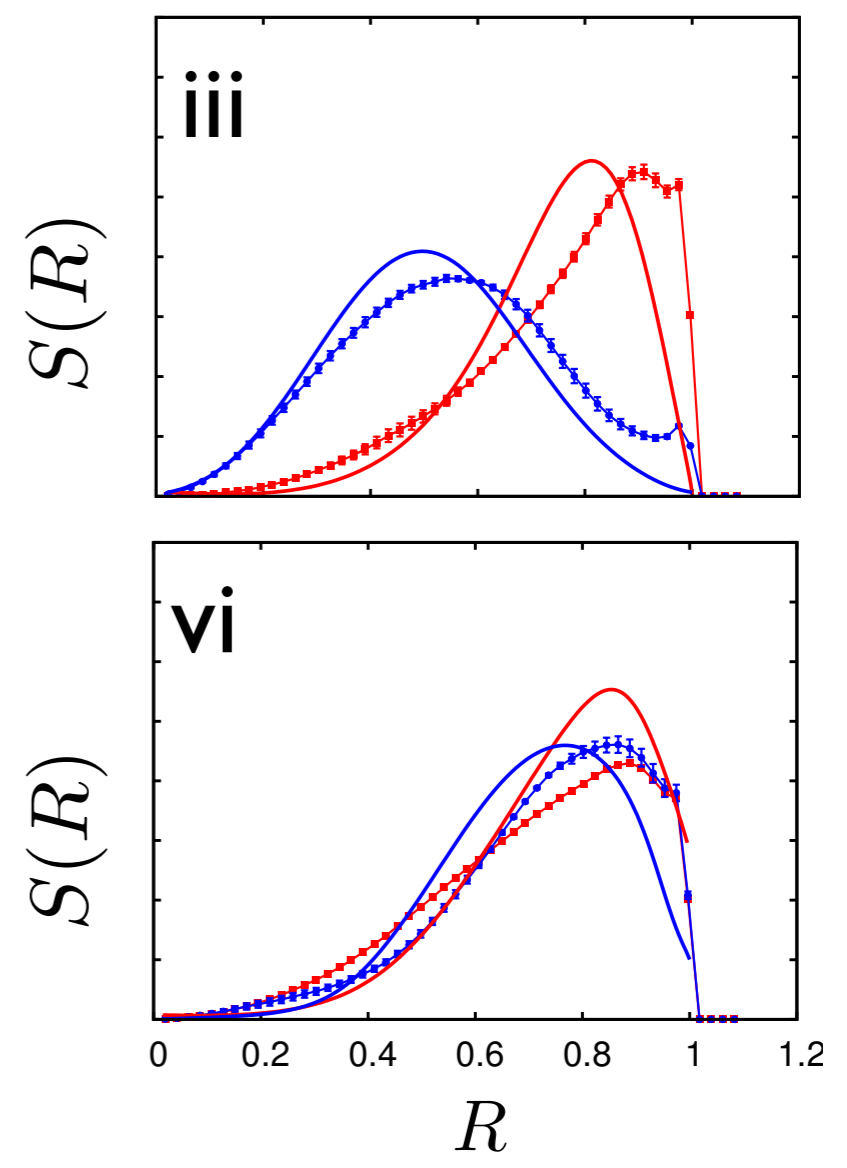


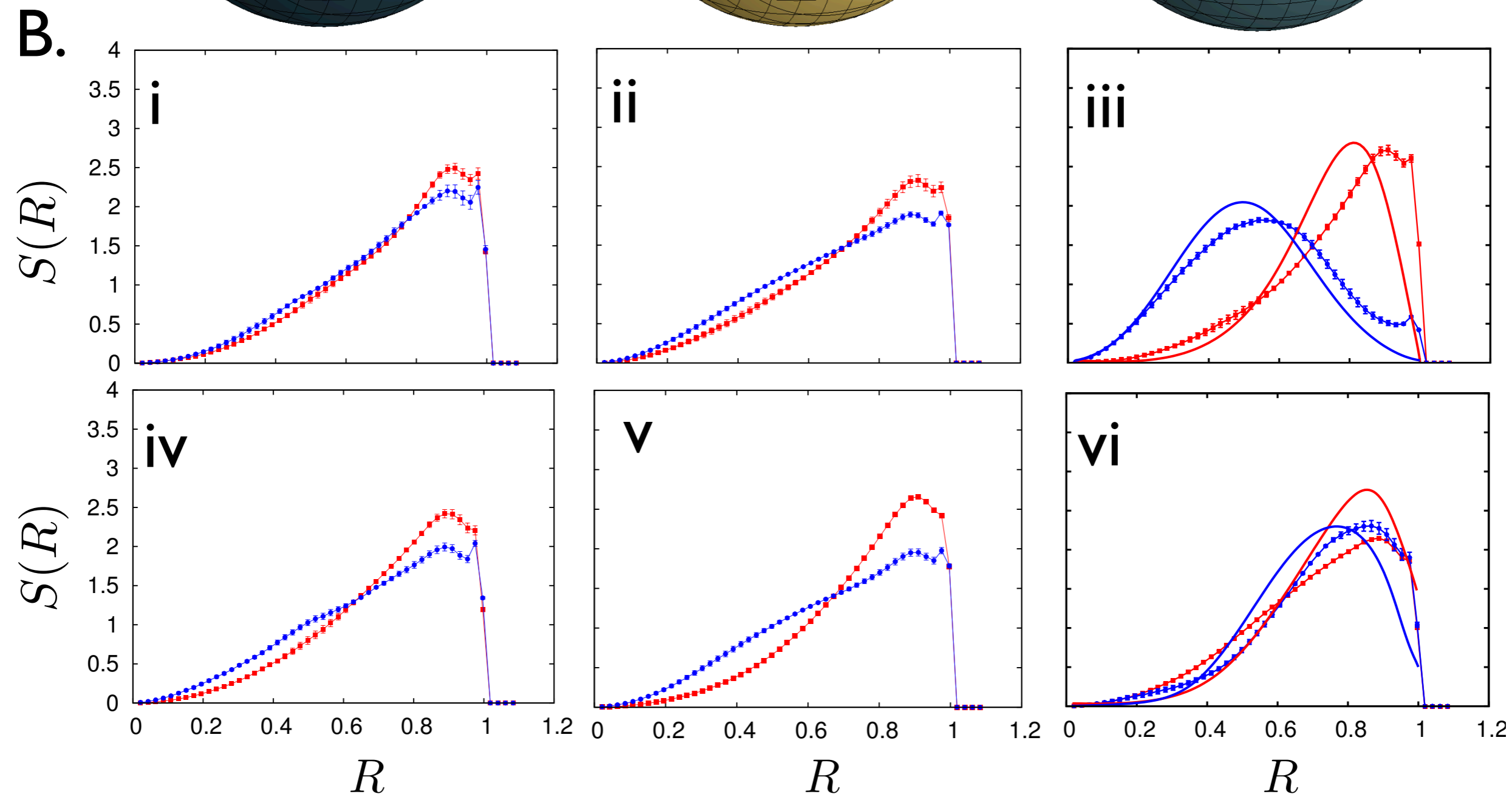
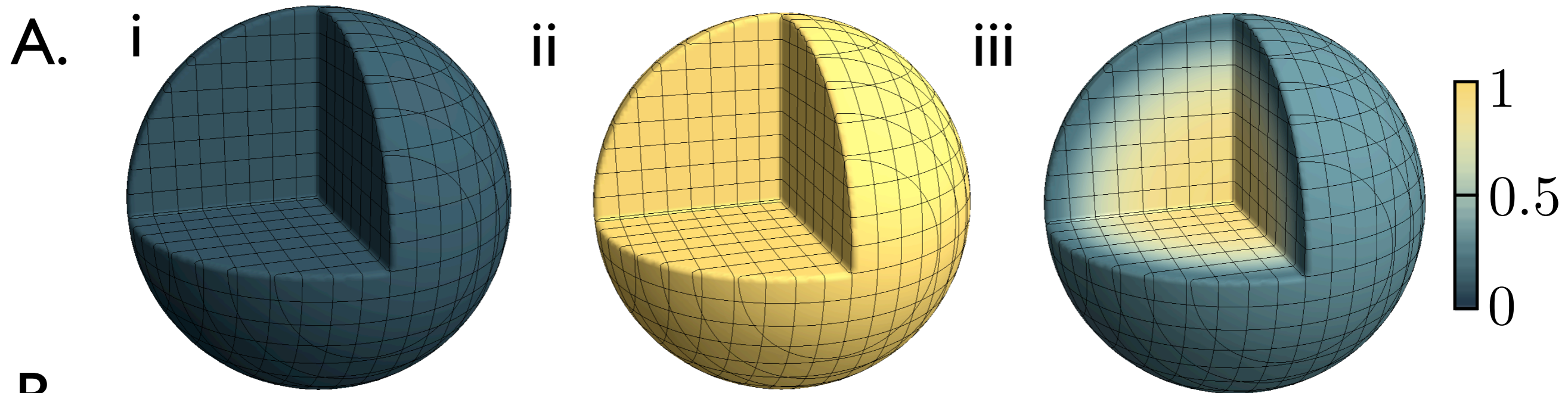
Cut-away sphere  
representation of local activity

Mixture of monomers at different  
active temperatures



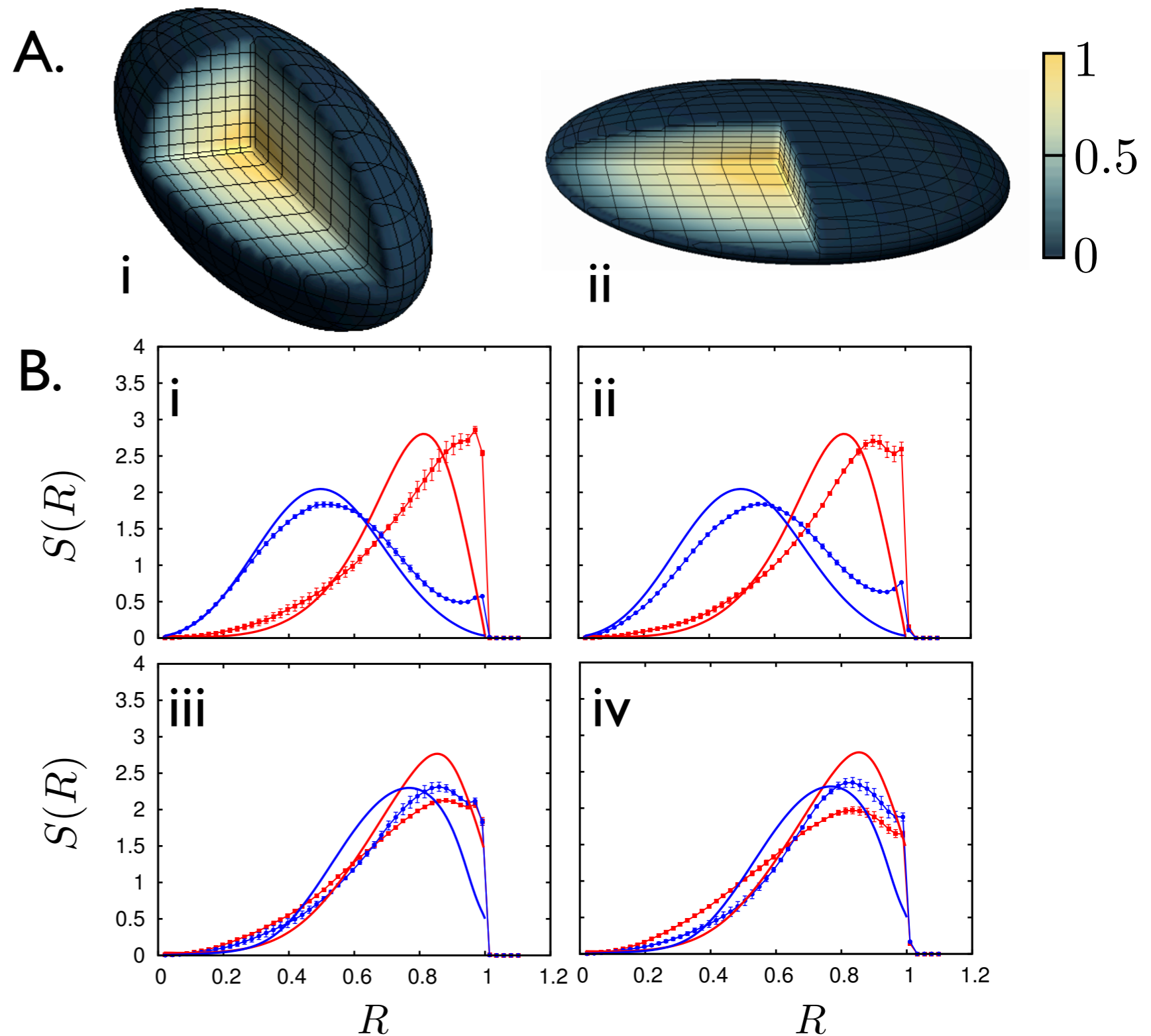
Chromosome 18/19  
95% at  $T = T_{\text{therm}}$   
5% at  $T = 20 T_{\text{therm}}$   
Chromosome 12/20





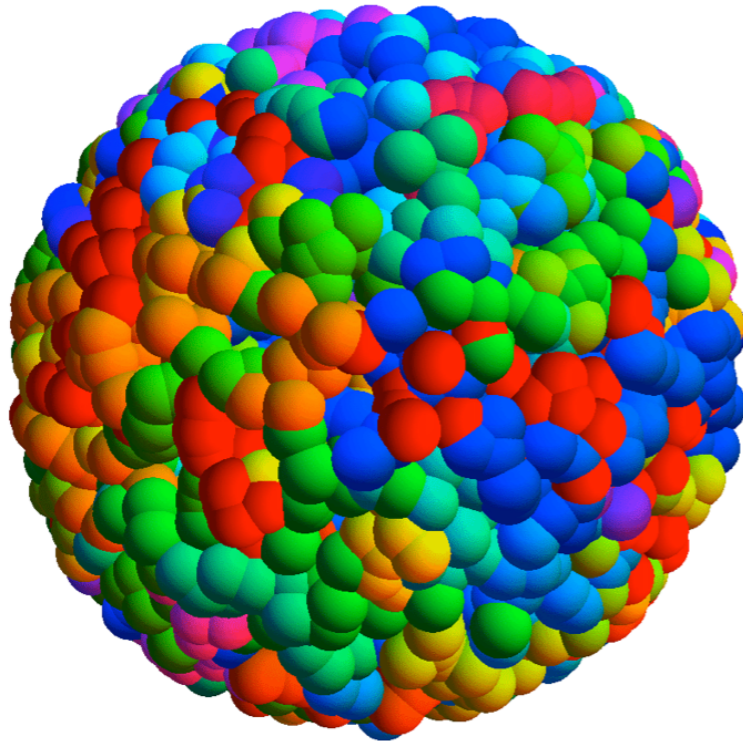
Can simulate  
prolate and  
oblate  
ellipsoidal  
nuclei

Only a  
marginal  
influence of  
nuclear  
shape



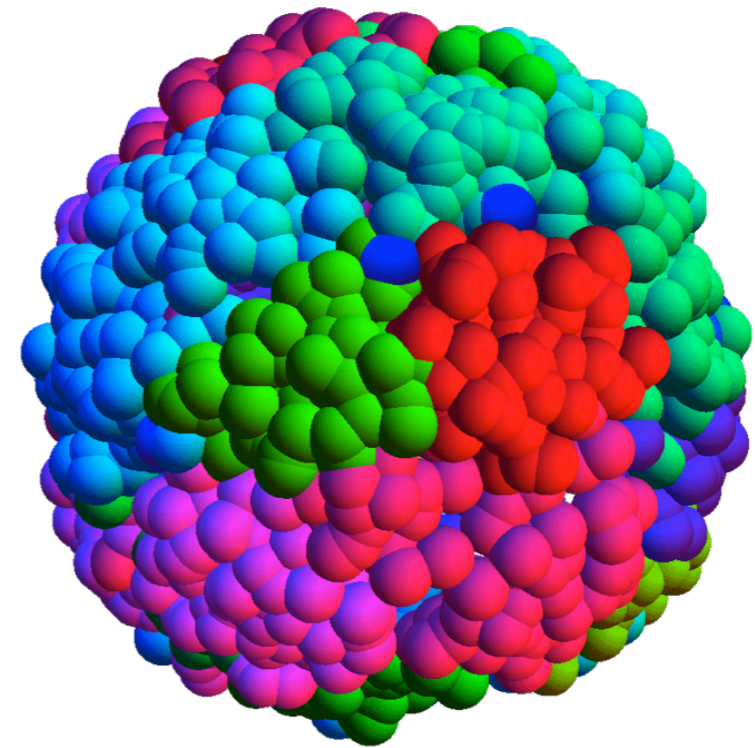
But, no chromosome territories ...

We get



Why?

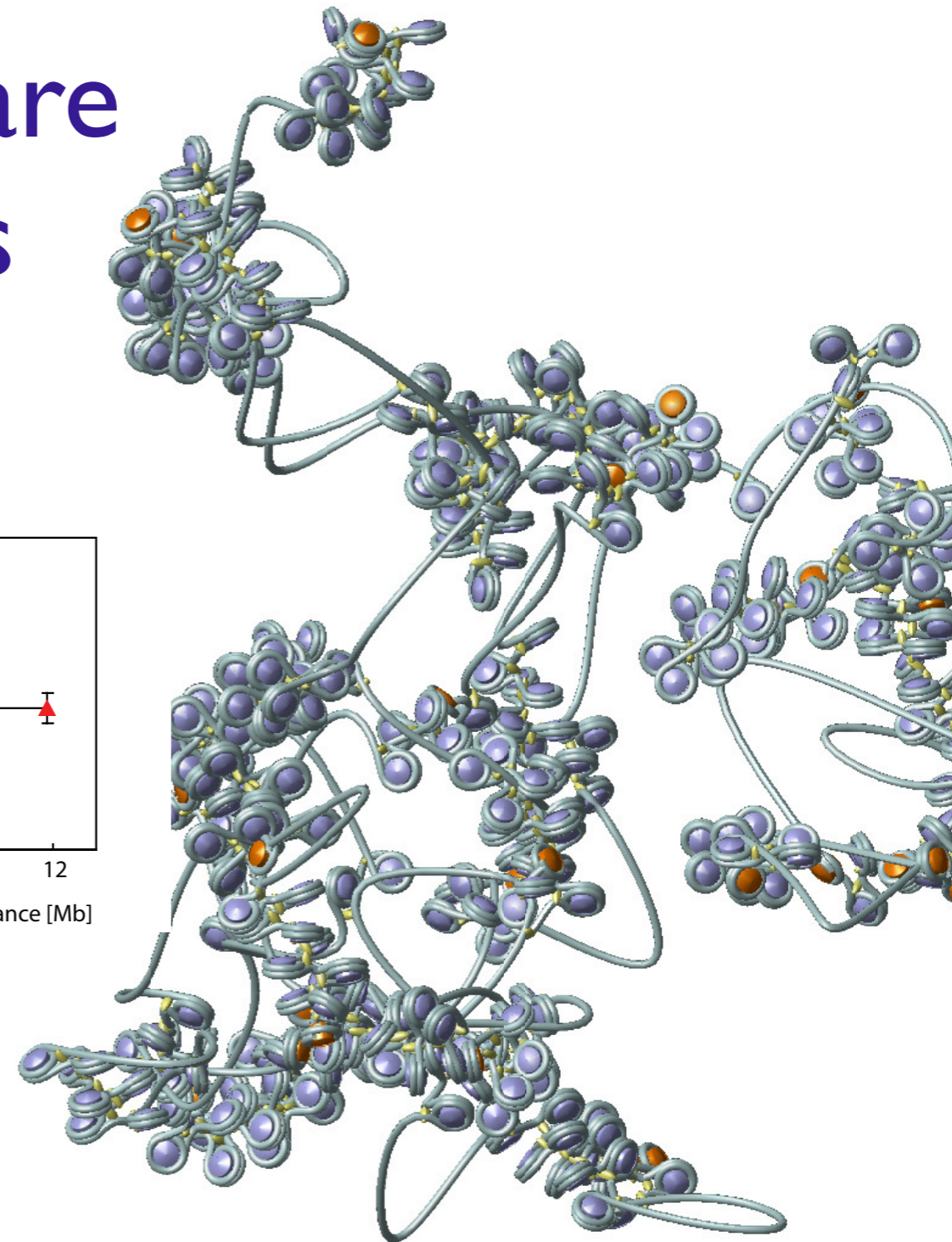
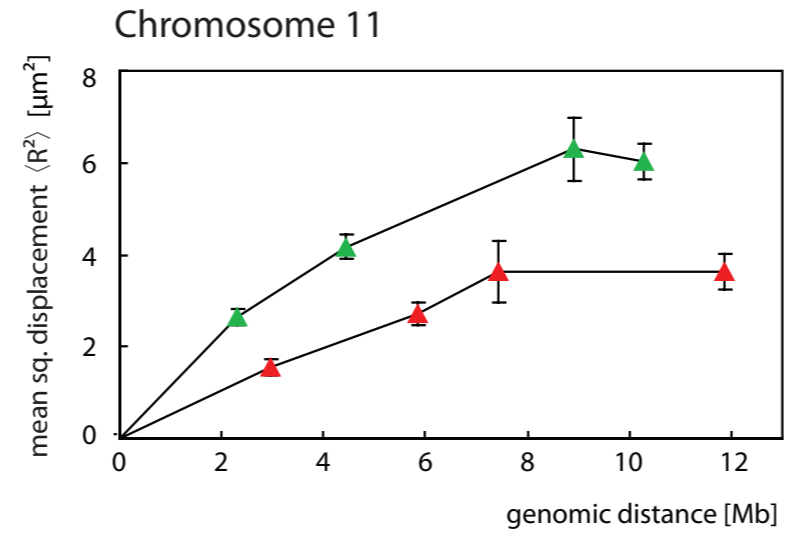
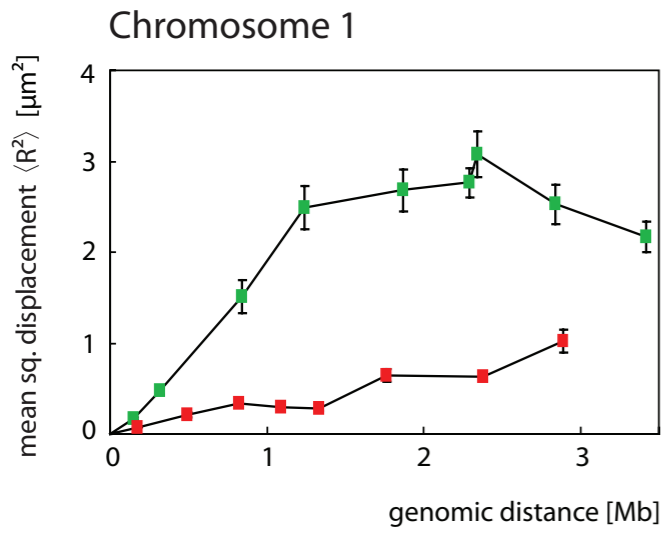
Whereas we should have got



Our model for individual chromosomes assumes no structuring

# Individual chromosomes are compact on large scales

B Mateos-Langerak et al, PNAS 2009



## Models for large-scale chromosome structure

Rosette model

Helical fold model

Network model

Random loop model

Fractal globule model + ....

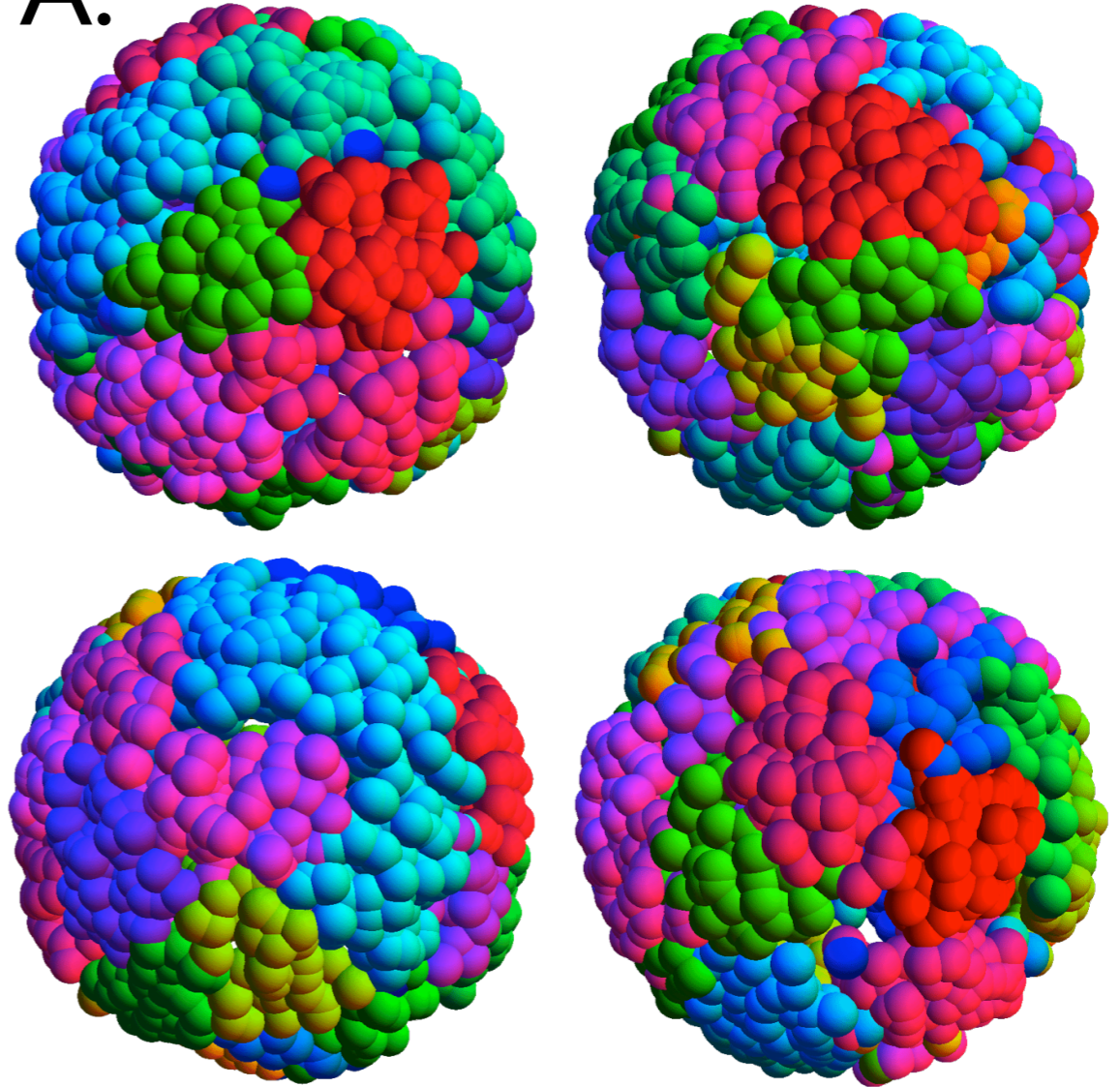
P.M. Diesinger and D.W. Heermann, Biophys. J. (2009)

# We implement the random loop model

Our model  
chromosomes are  
now compact on large  
scales

Can compactness and  
inhomogenous activity  
generate “chromosome  
territories”?

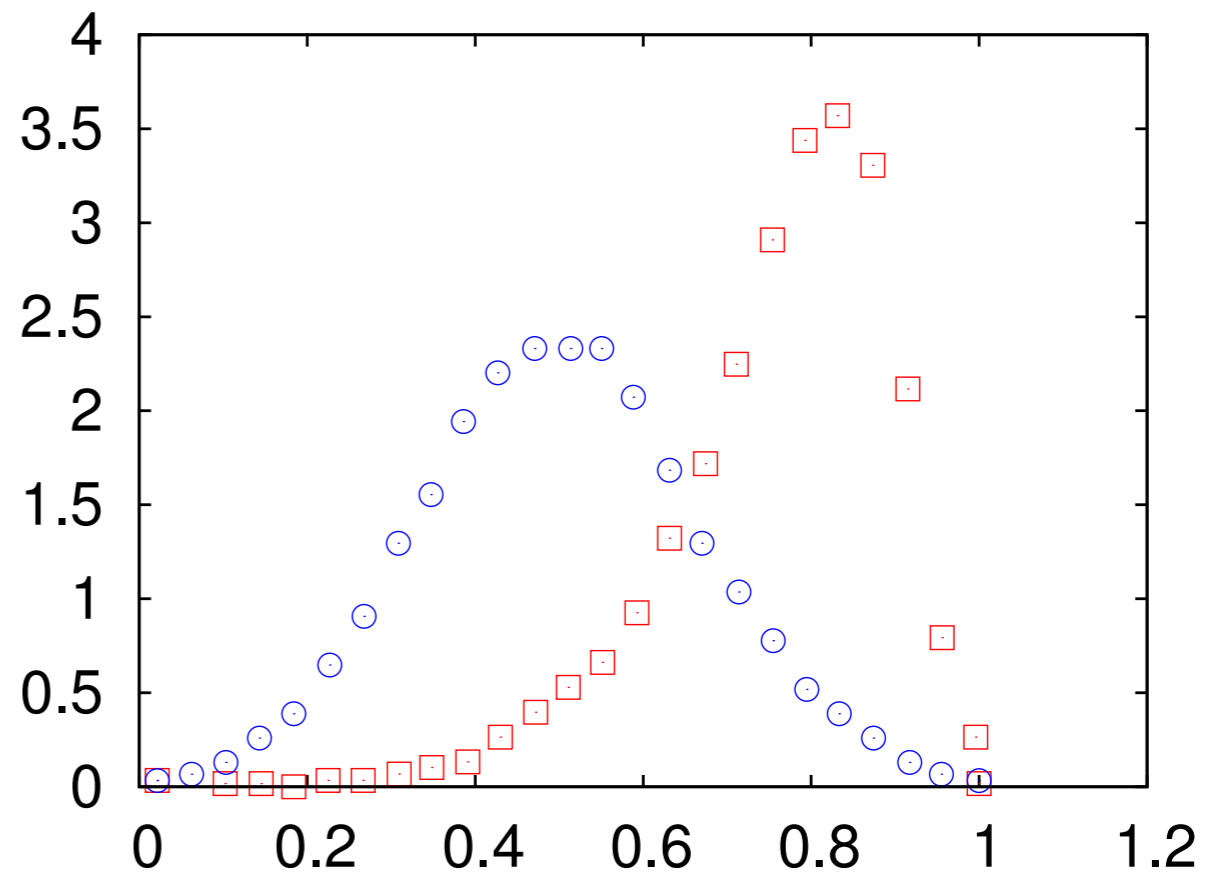
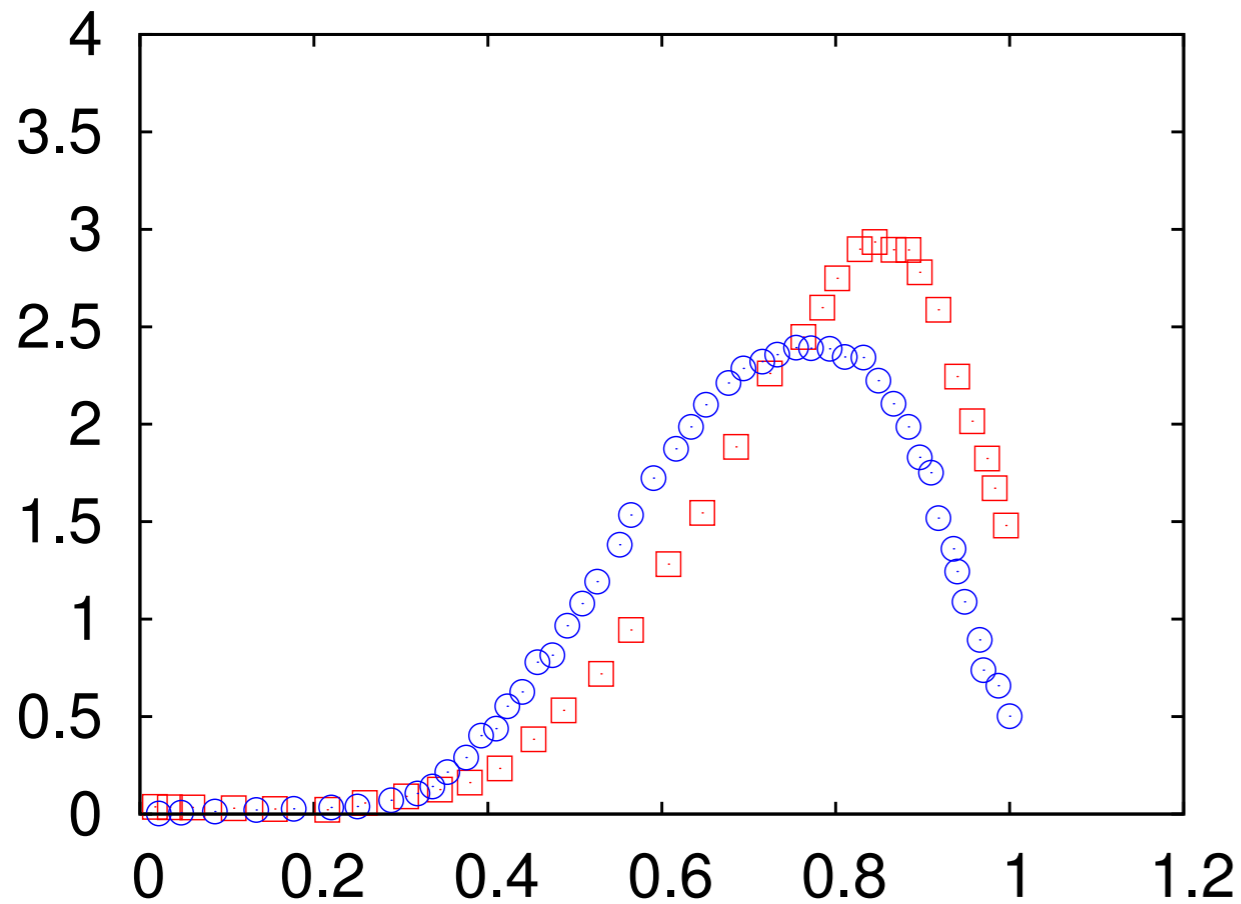
A.



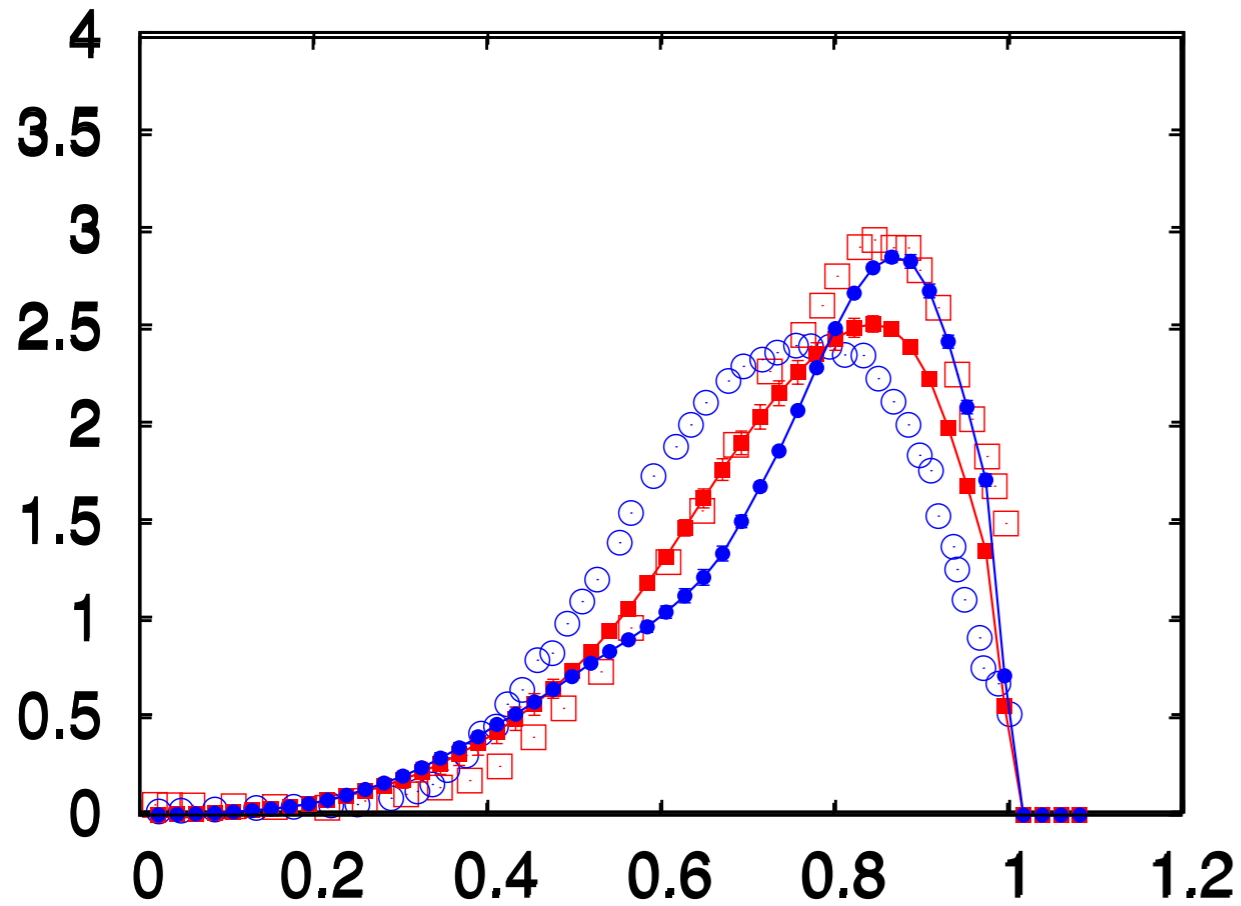
Yes



With inhomogeneous activity and compactness at large scales, how does our model compare to data?



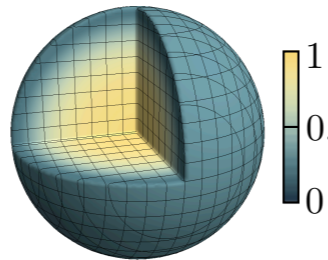
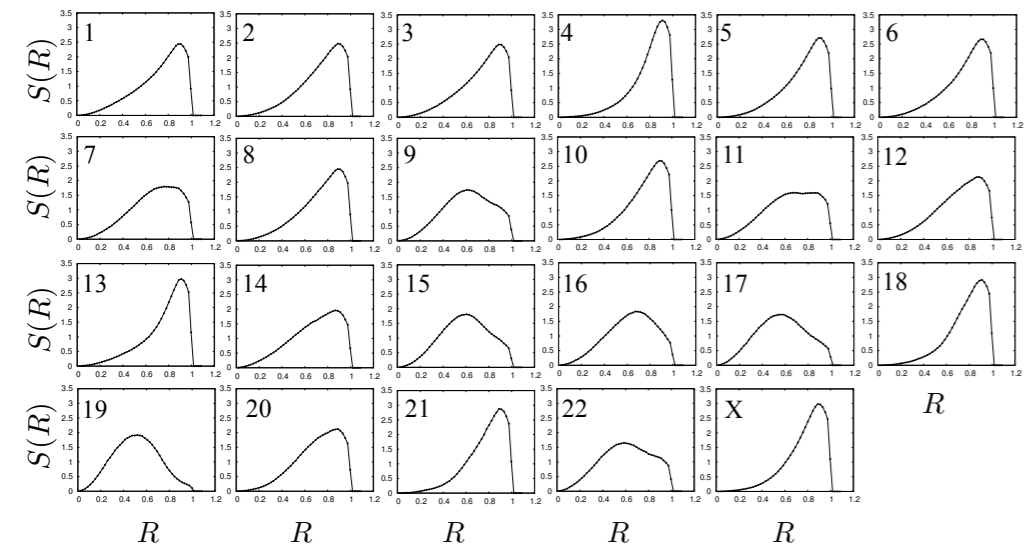
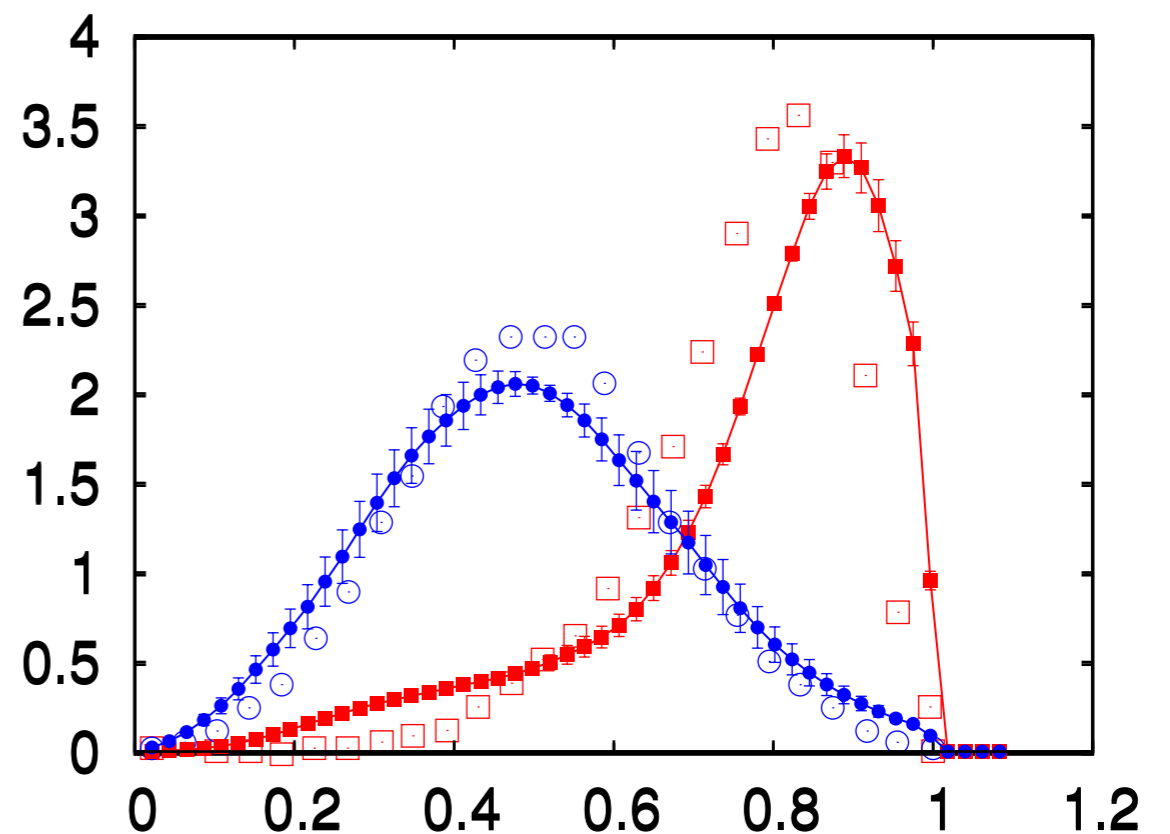
With inhomogeneous activity and compactness at large scales, how does our model compare to data?



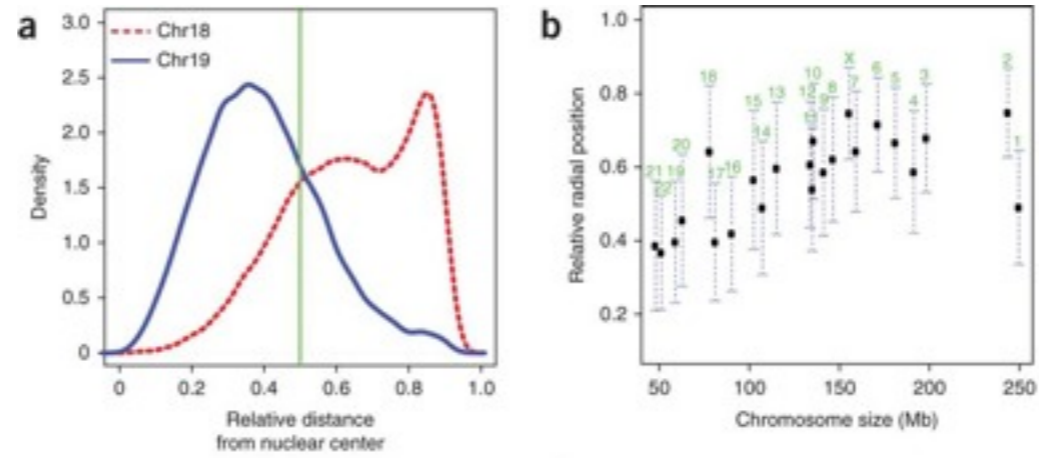
Chromosome 12/20

Reasonably well, despite the utter simplicity of the model

Chromosome 18/19



Positioning  
correlates to  
chromosome size?  
Nuclear shape?

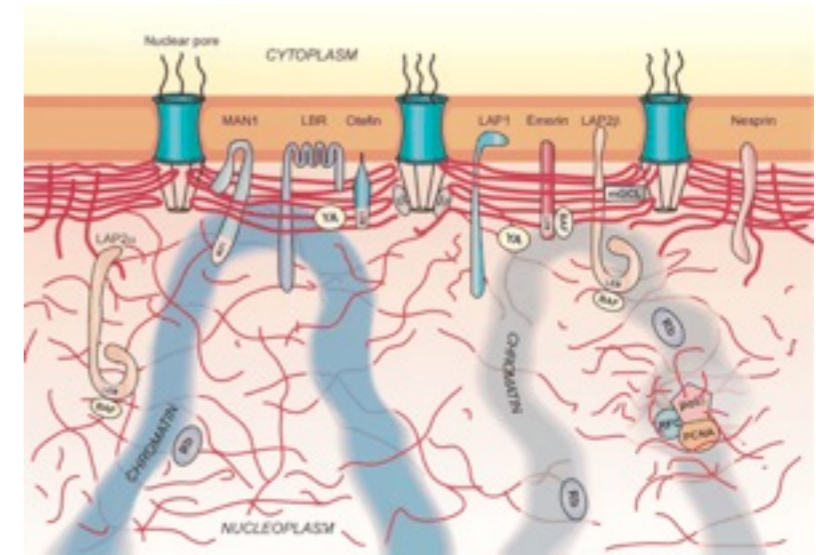


Kalhor et al, Nat Biotech (2012)



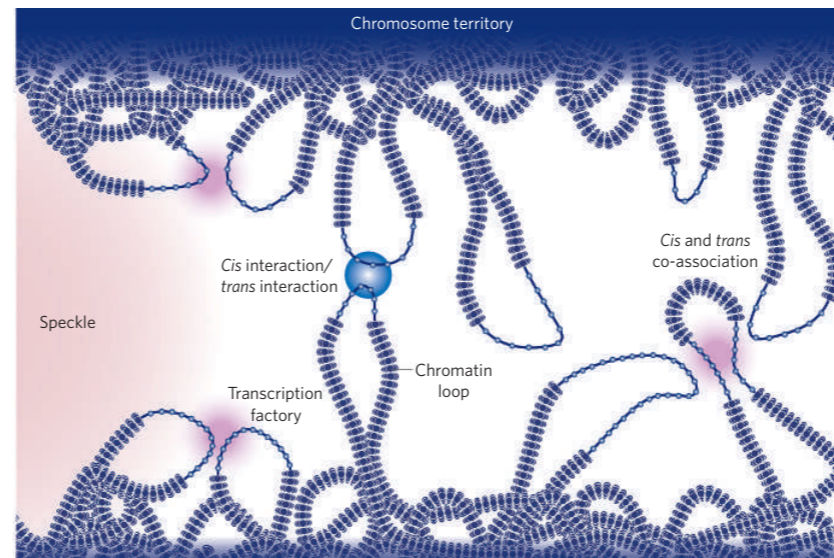
Caution:  
Not so  
fast ...

Lamins and nuclear  
architecture/  
chromatin  
structuring?



Goldman et al, Genes Dev (2002)

Importance of relative  
positioning,  
transcription  
factories, looping ... ?



Fraser and Bickmore, Nature (2007)

Very far  
from  
these ..

# A hierarchy of positioning drivers ... ?

Increasing  
complexity

?

Nuclear actin/myosin?

Higher-order interactions

TF's, Inter-chromatin domains

Nuclear shape/envelope/lamins/

Activity-based radial segregation



Activity- based radial segregation might provide a generic initial template for local physical and biochemical events acting to further stabilize and optimize positioning

# Conclusions

1. Chromatin as a model system for active matter

2. Suggest: Segregation by gene density and the formation of chromosome territories have a common origin in “activity-based segregation”

3. Inhomogeneous activity, confinement and polymeric nature of chromosomes are central

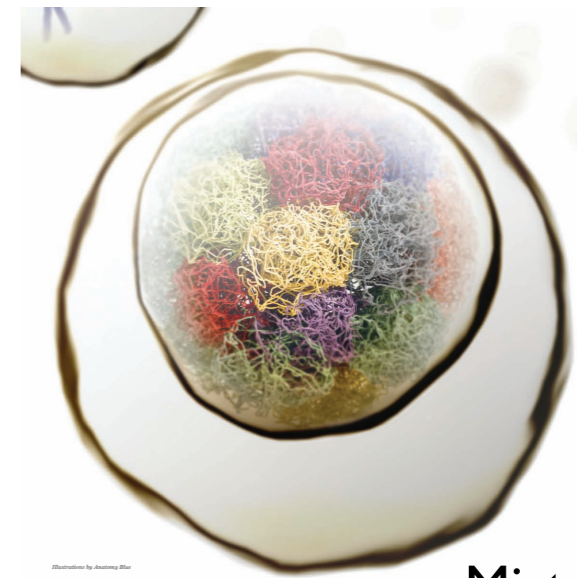
Nucleic Acids Research Advance Access published January 22, 2014

*Nucleic Acids Research*, 2014, 1–15  
doi:10.1093/nar/gkt1417

## **Chromosome positioning from activity-based segregation**

Nirmalendu Ganai<sup>1</sup>, Surajit Sengupta<sup>2,3</sup> and Gautam I. Menon<sup>4,5,6,\*</sup>

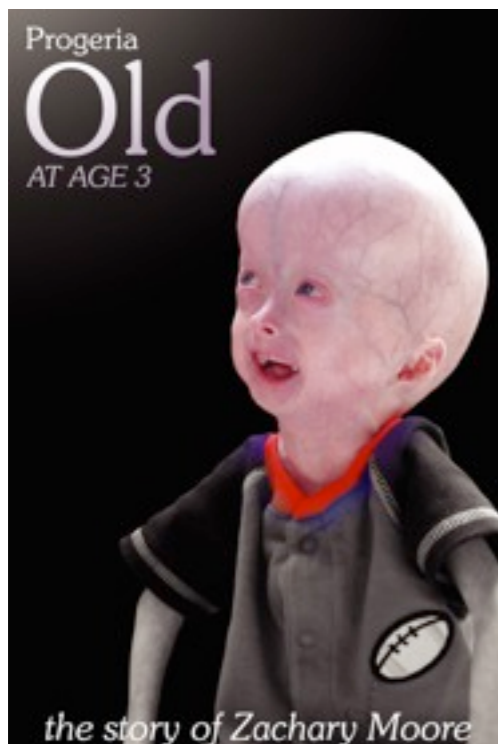
The discovery of distinct radial positions of chromosomes and genes has changed the way we think about genome organization. It has highlighted the non-randomness of higher-order genome organization and it has inspired the pursuit of how spatial genome organization contributes to function.



Misteli, Scientific American (2011)

**Further  
Work**

“Meaning of gene positioning”, Takizawa, Meaburn & Misteli, Cell (2008)



Hutchinson–Gilford progeria syndrome

Other directions (biological): positioning in specific cell types, effects of nuclear envelope, repositioning on DNA damage, stem cell chromatin ... ?

Other directions (statistical-mechanical): What determines activity-based segregation, confined active matter