



Attila Csikász-Nagy

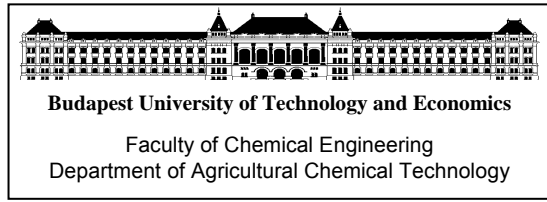
Models of the fission yeast cell cycle  
(Switches in time and space)

at

*Kavli Institute for Theoretical Physics*

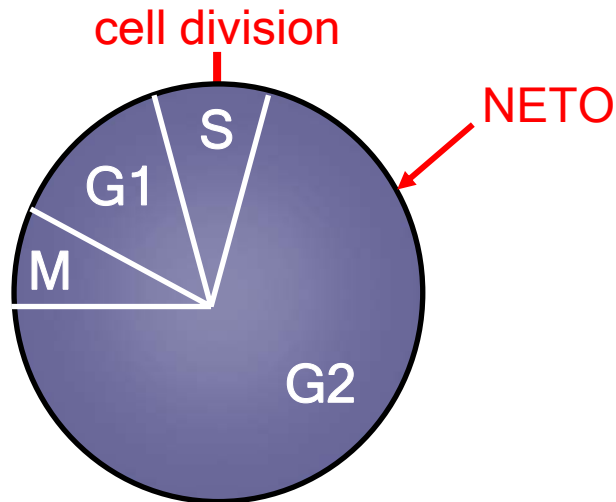
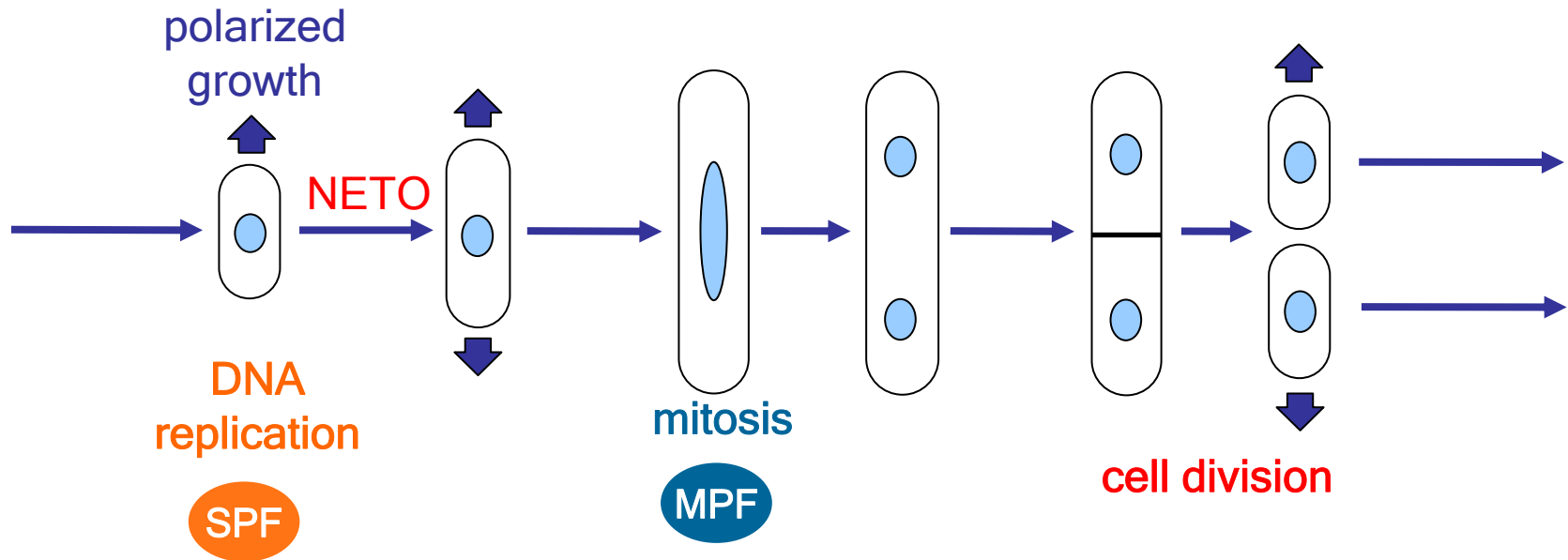


John J. Tyson



Béla Novák

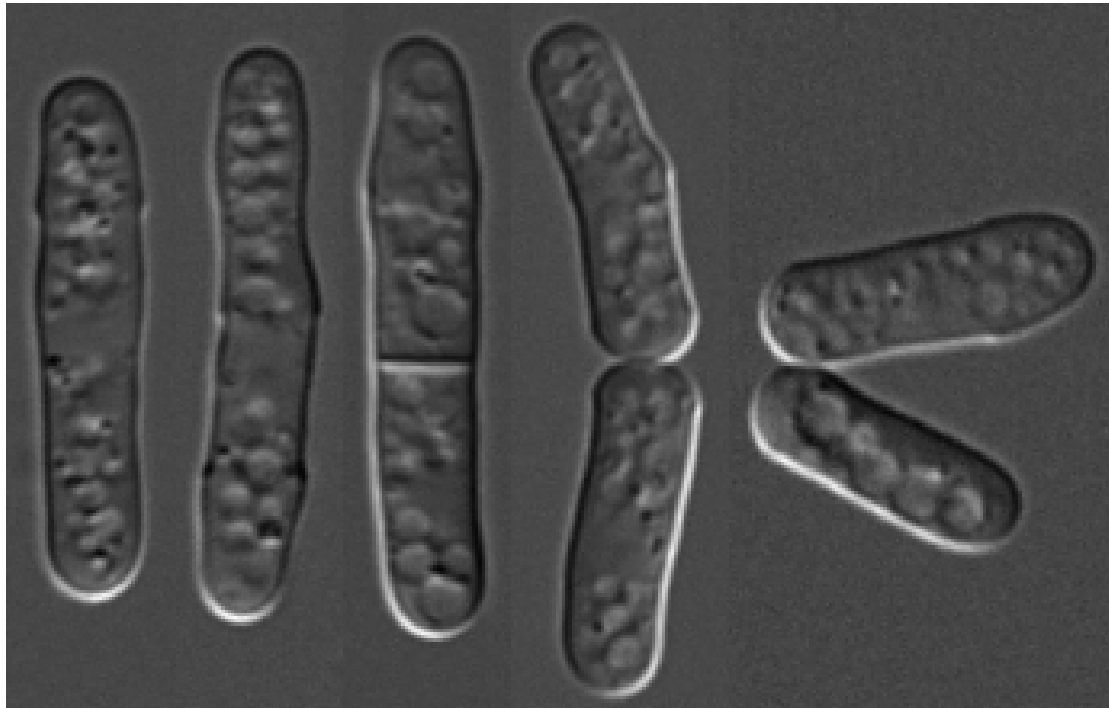
# Fission yeast - *Schizosaccharomyces pombe*



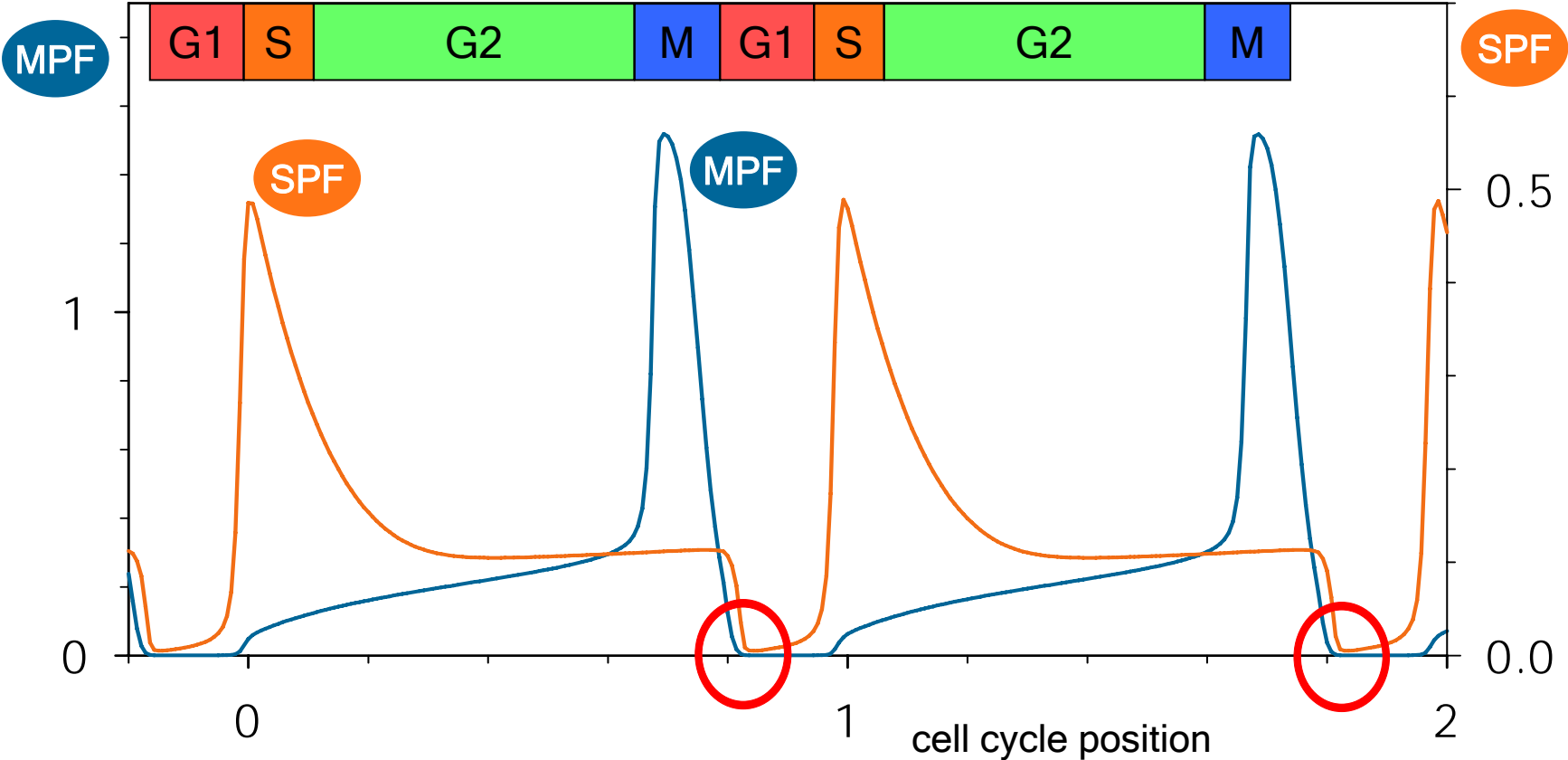
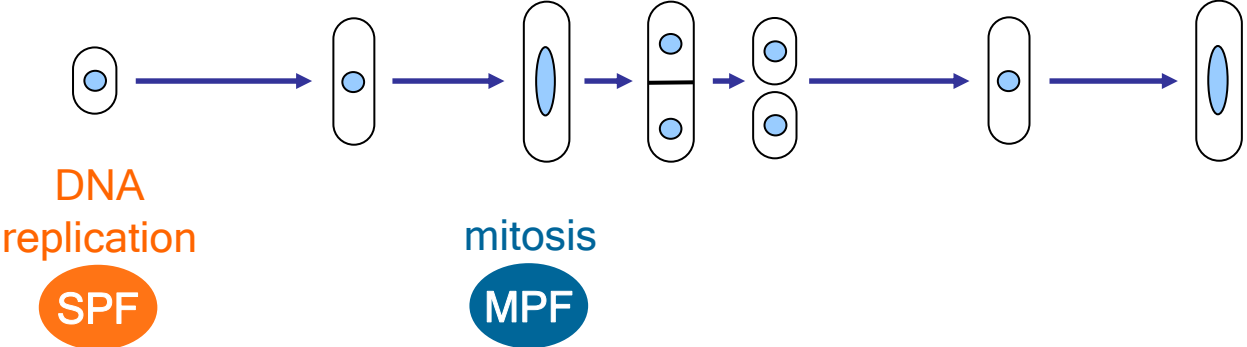
Switches to be described in this talk:

- ◆ Initiation of cell division
- ◆ Initiation of DNA replication
- ◆ NETO

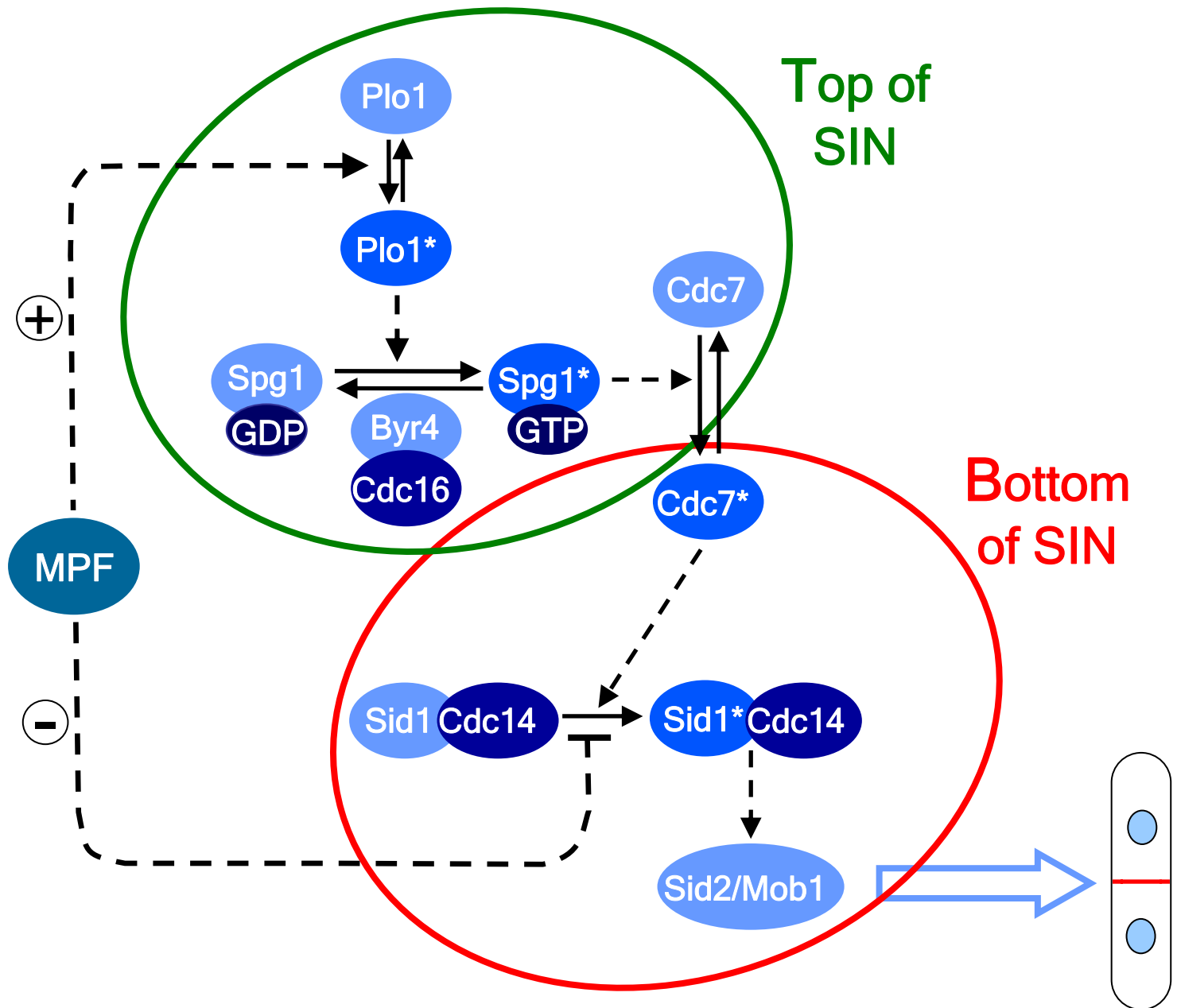
cell division = fission = septation



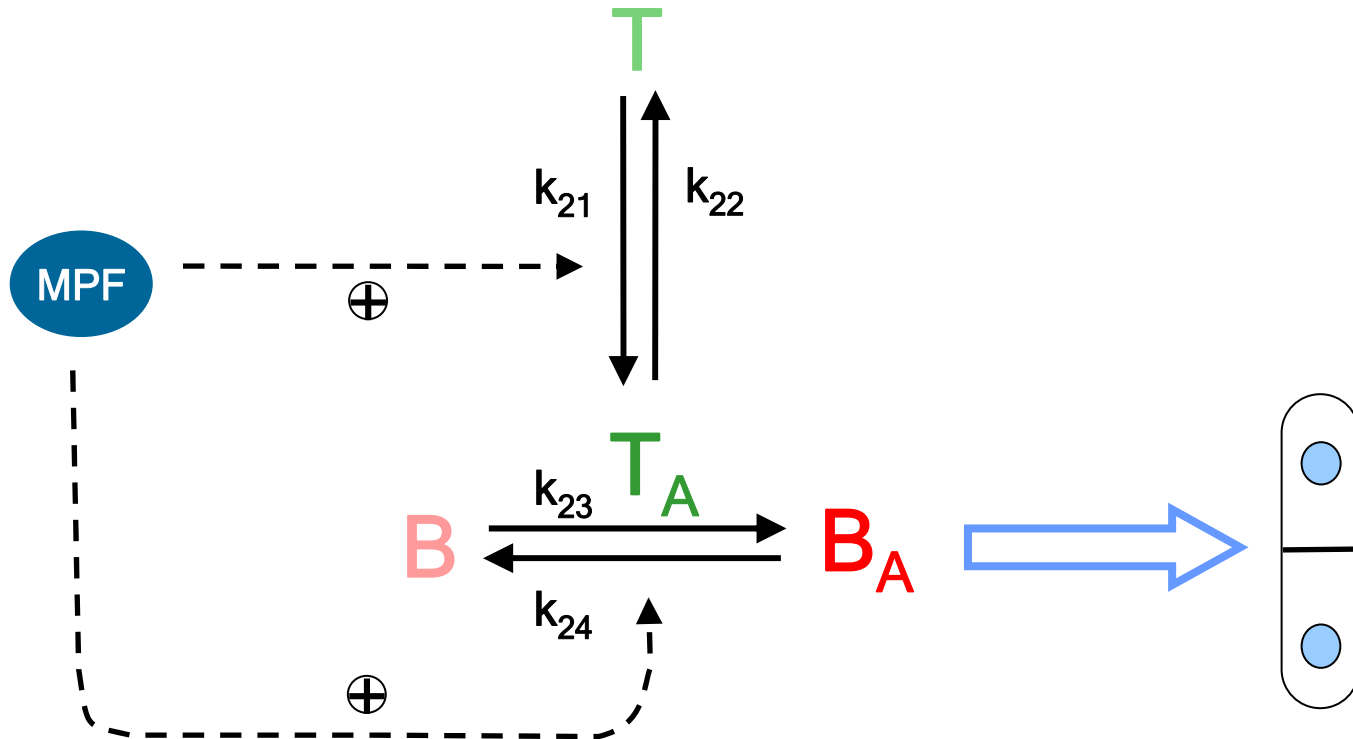
# The oscillation of SPF and MPF activity during the cell cycle



# SIN = Septation Initiation Network



# The simple kinetic model of SIN

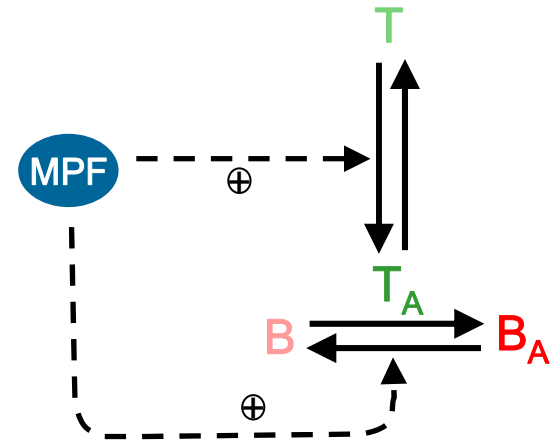


$$\frac{dT_A}{dt} = k_{21} * MPF * \frac{1 - T_A}{J_{21} + 1 - T_A} - k_{22} * \frac{T_A}{J_{21} + T_A}$$

$$\frac{dB_A}{dt} = k_{23} * T_A * \frac{1 - B_A}{J_{23} + 1 - B_A} - (k_{24}' + k_{24} * MPF) * \frac{B_A}{J_{23} + B_A}$$

## Parameter values = ?

SIN can be activated only transiently only after mitosis and only once per cell cycle:



1. SIN should not reside in a stable active state for any values of MPF



Inhibition by MPF has to be stronger than activation

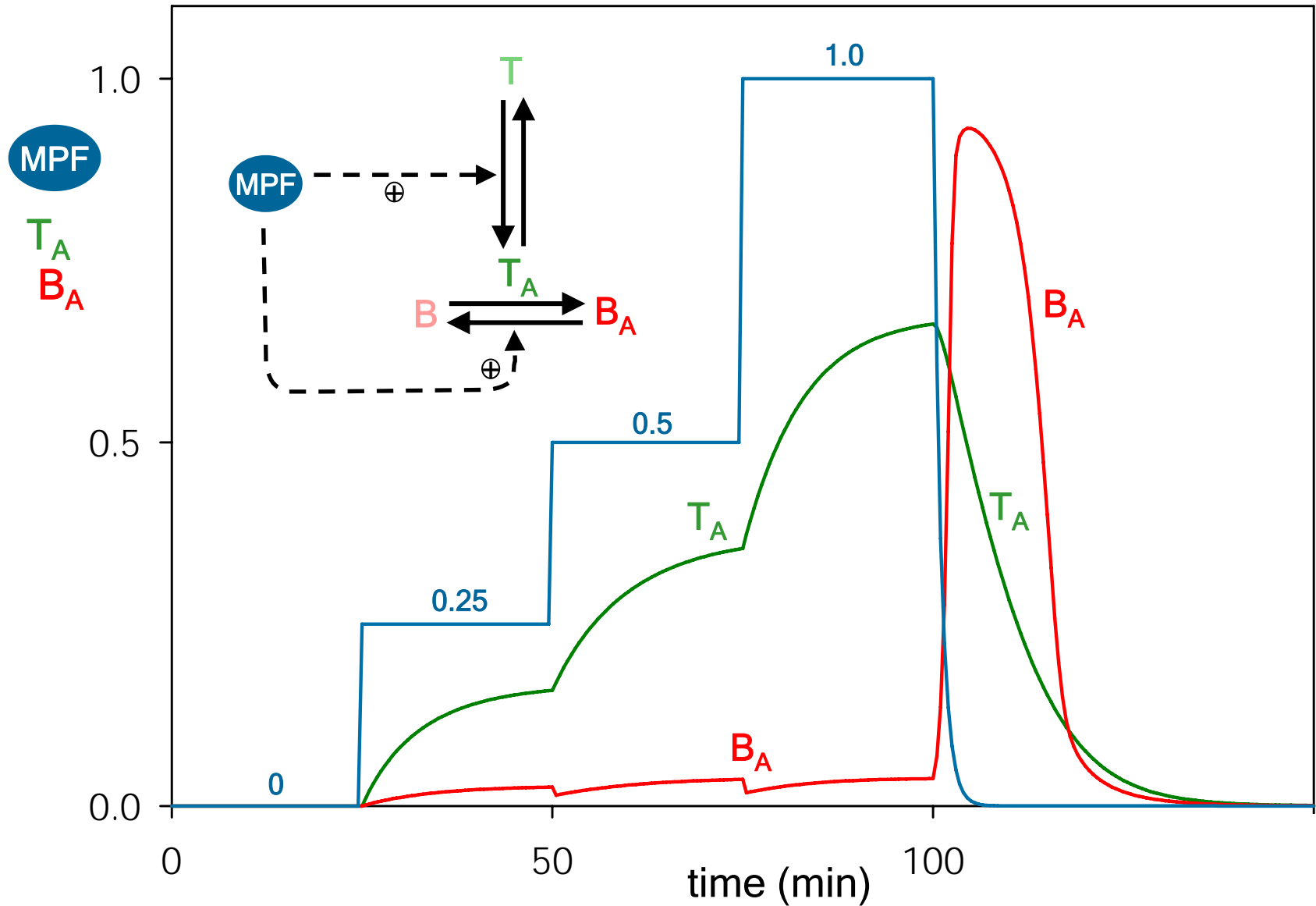
2. SIN should be activated transiently when the MPF activity drops after mitosis

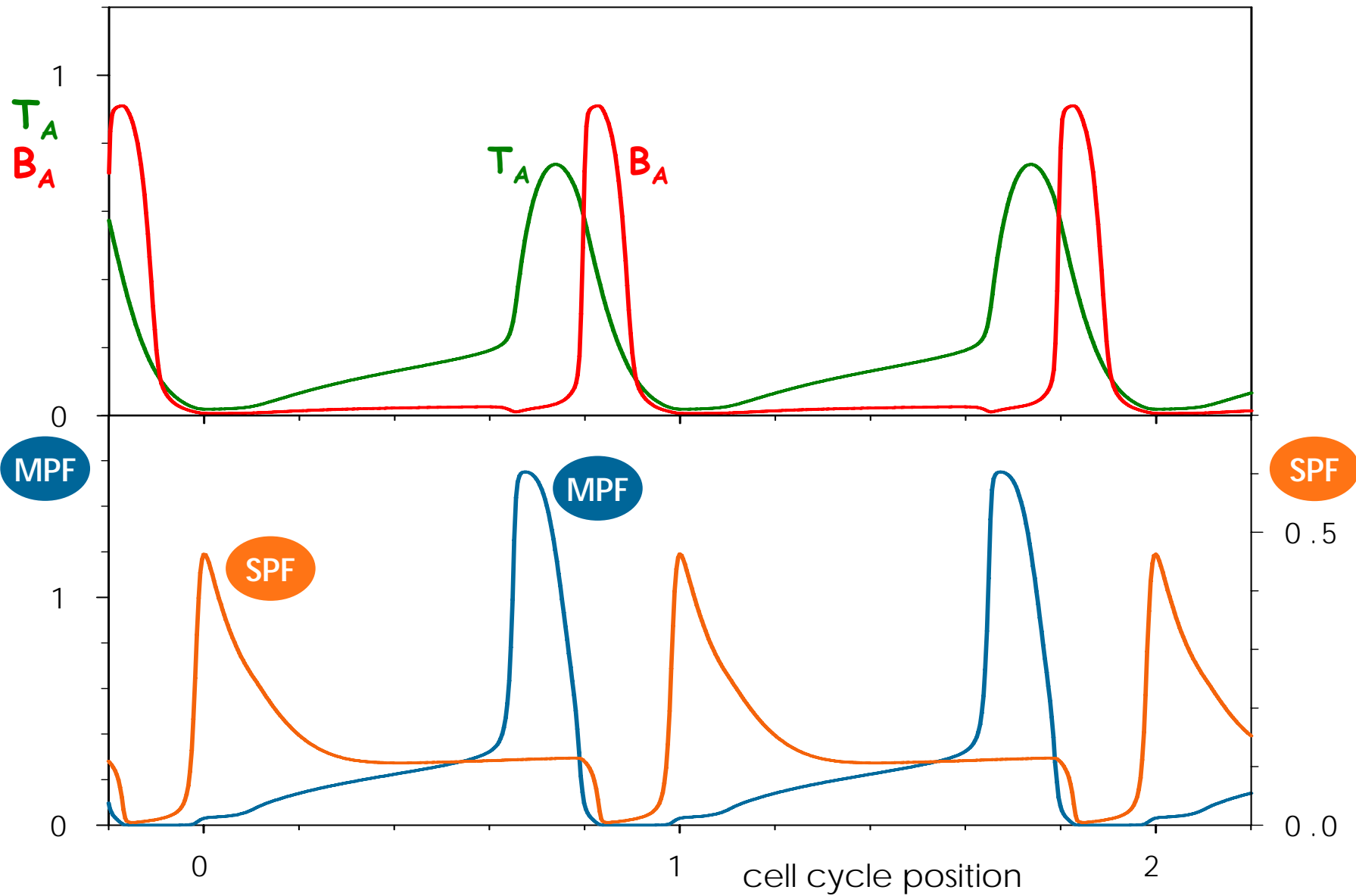
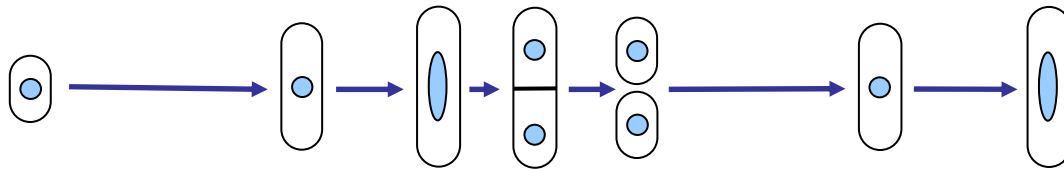


Top of SIN changes slower than Bottom of SIN

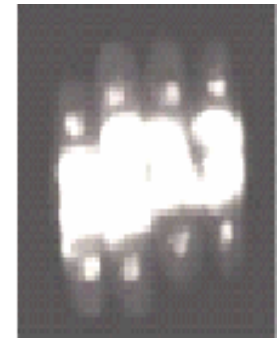


# Transient activation of the SIN by MPF

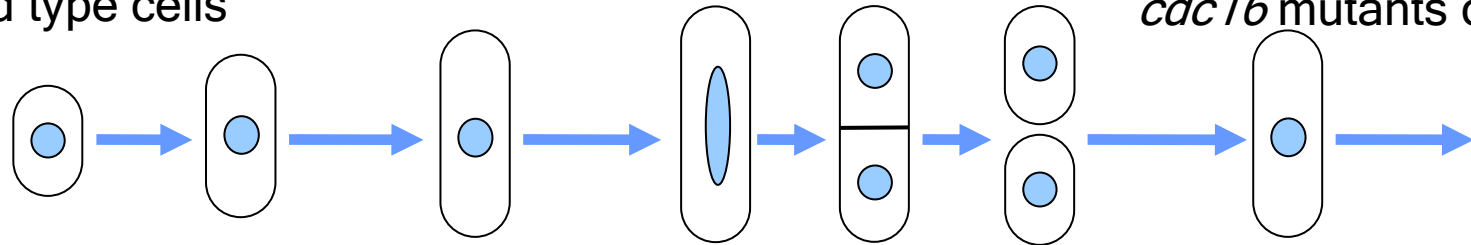




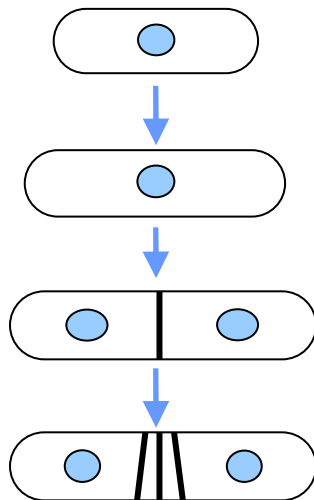
A *cdc16<sup>ts</sup>* mutants can not stop septating



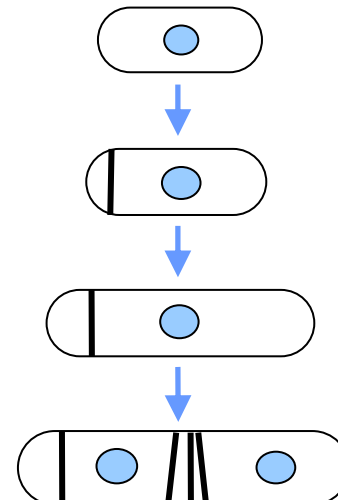
wild type cells



*cdc16* mutants cells



type I

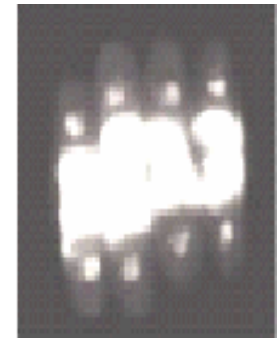


type II

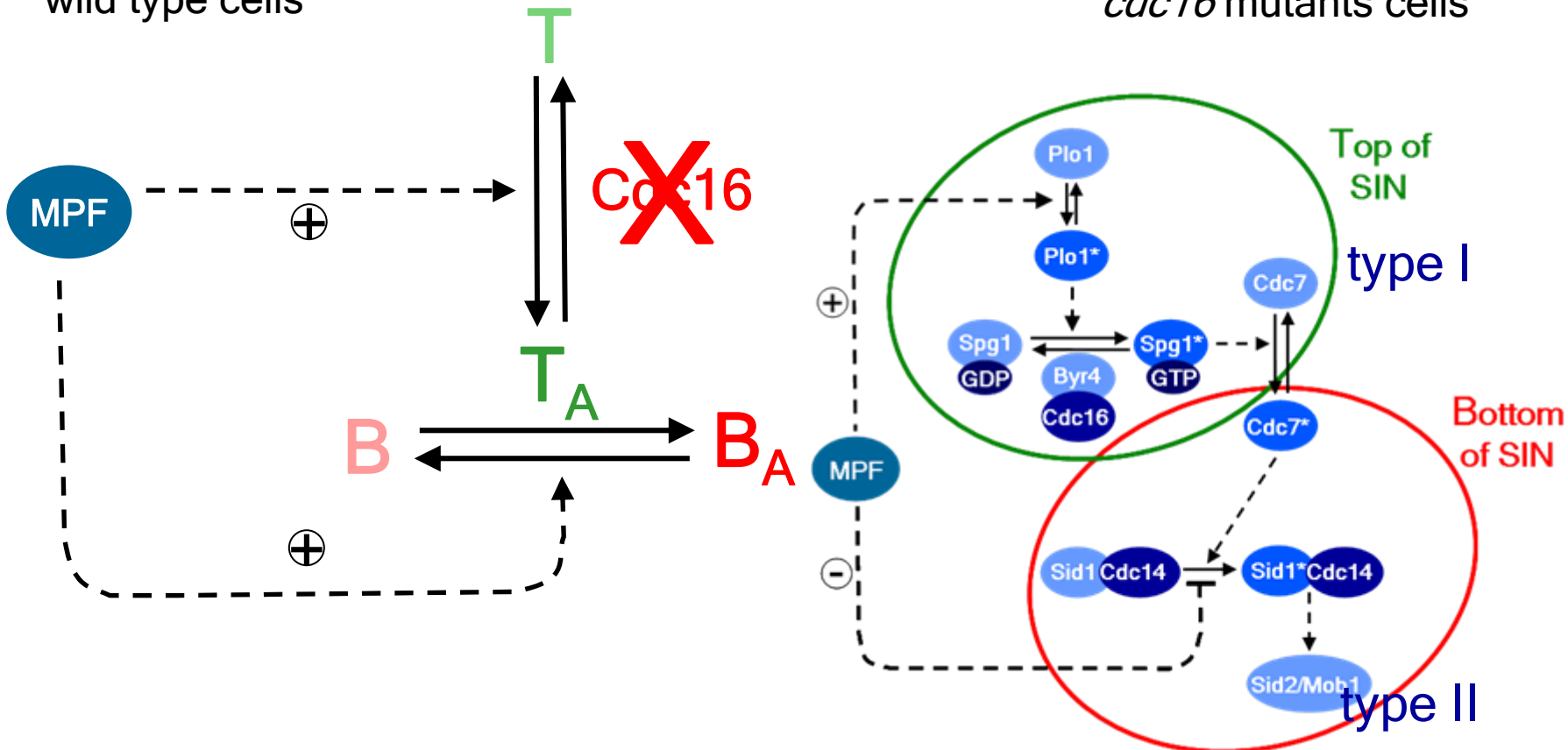
A *cdc16<sup>ts</sup>* mutants can not stop septating



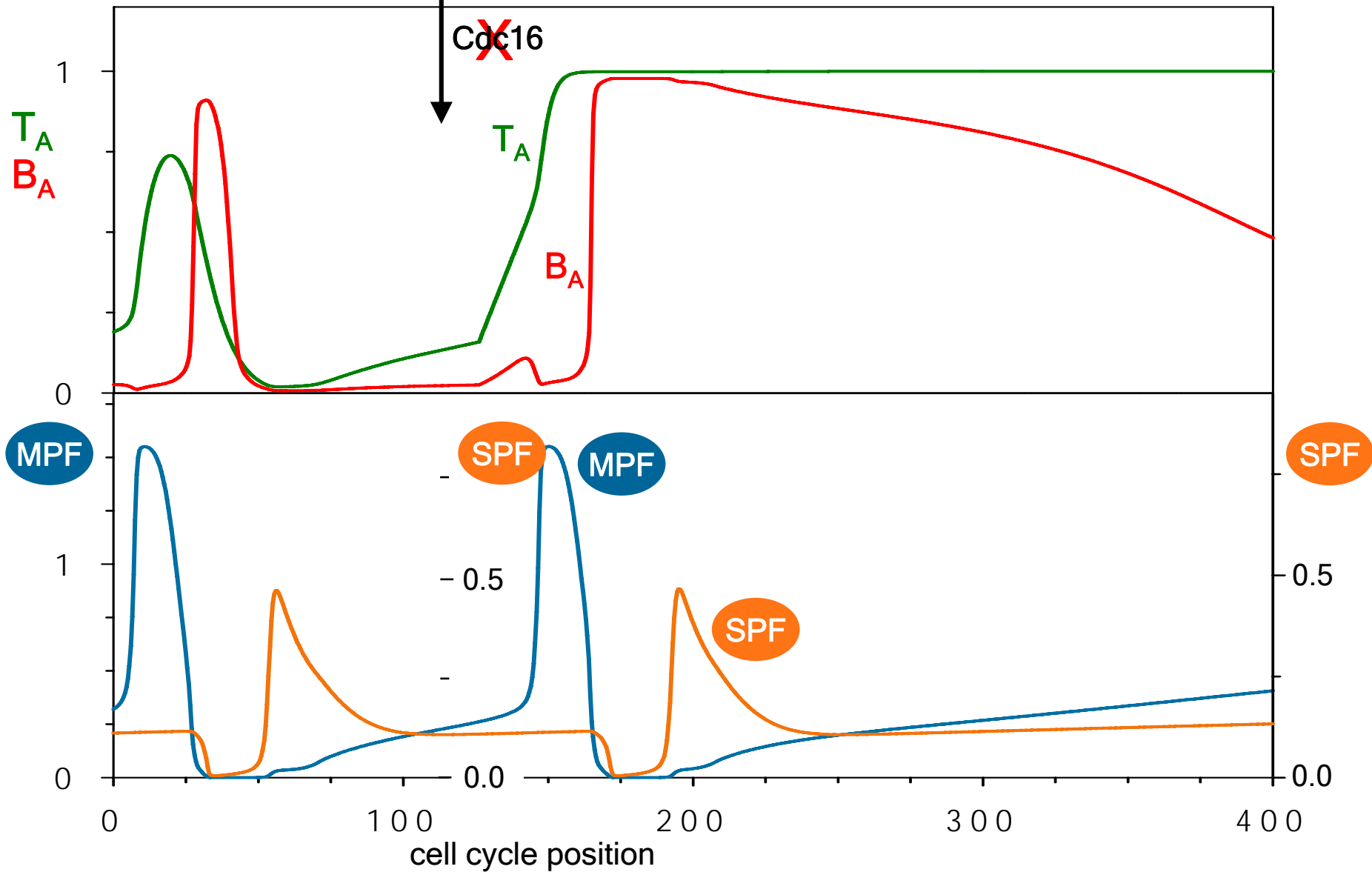
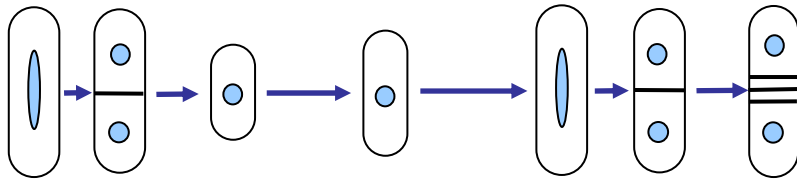
wild type cells



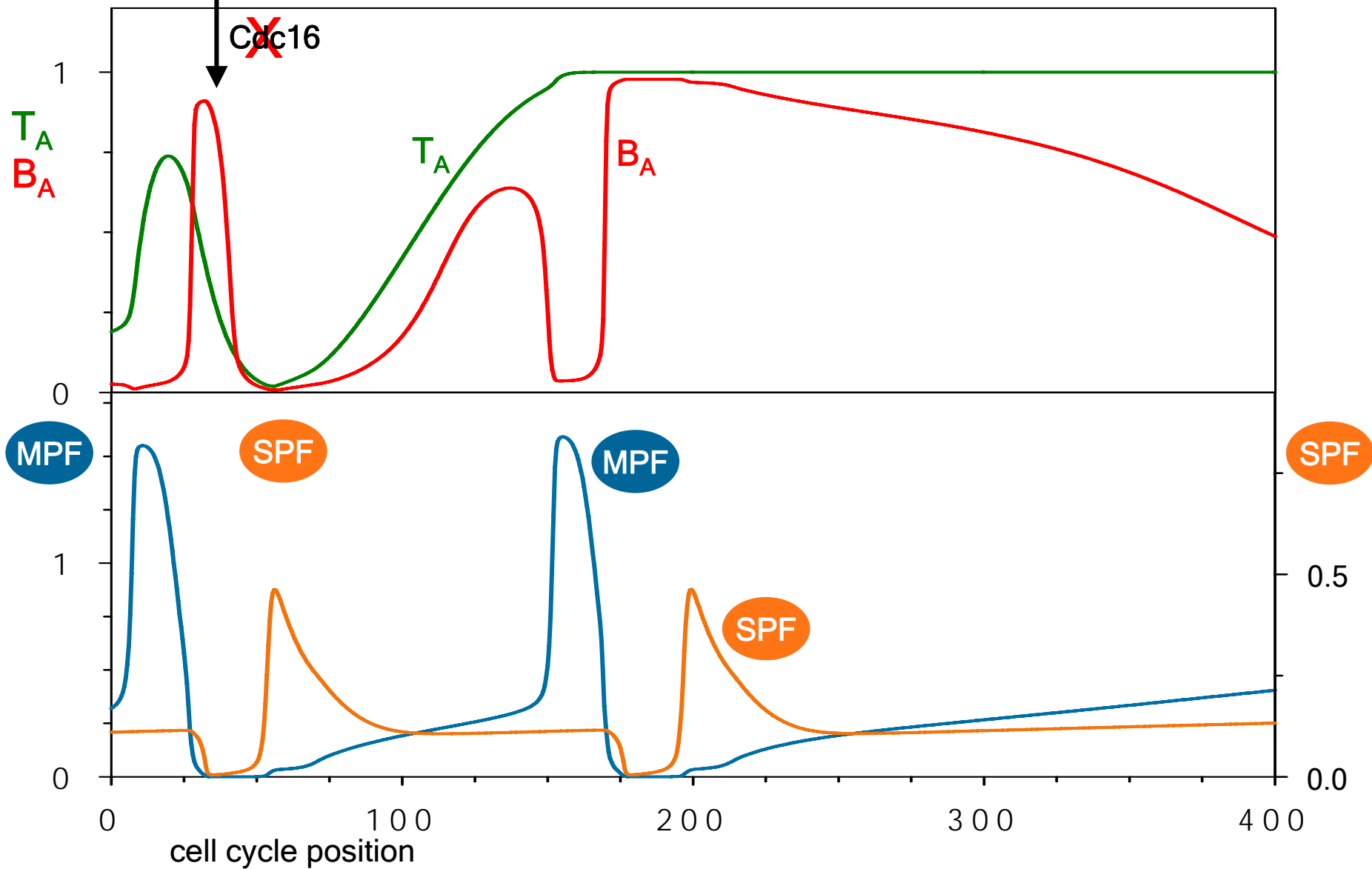
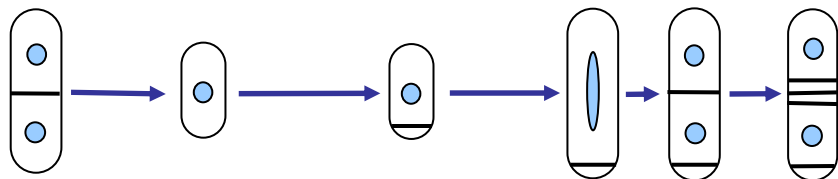
*cdc16* mutants cells



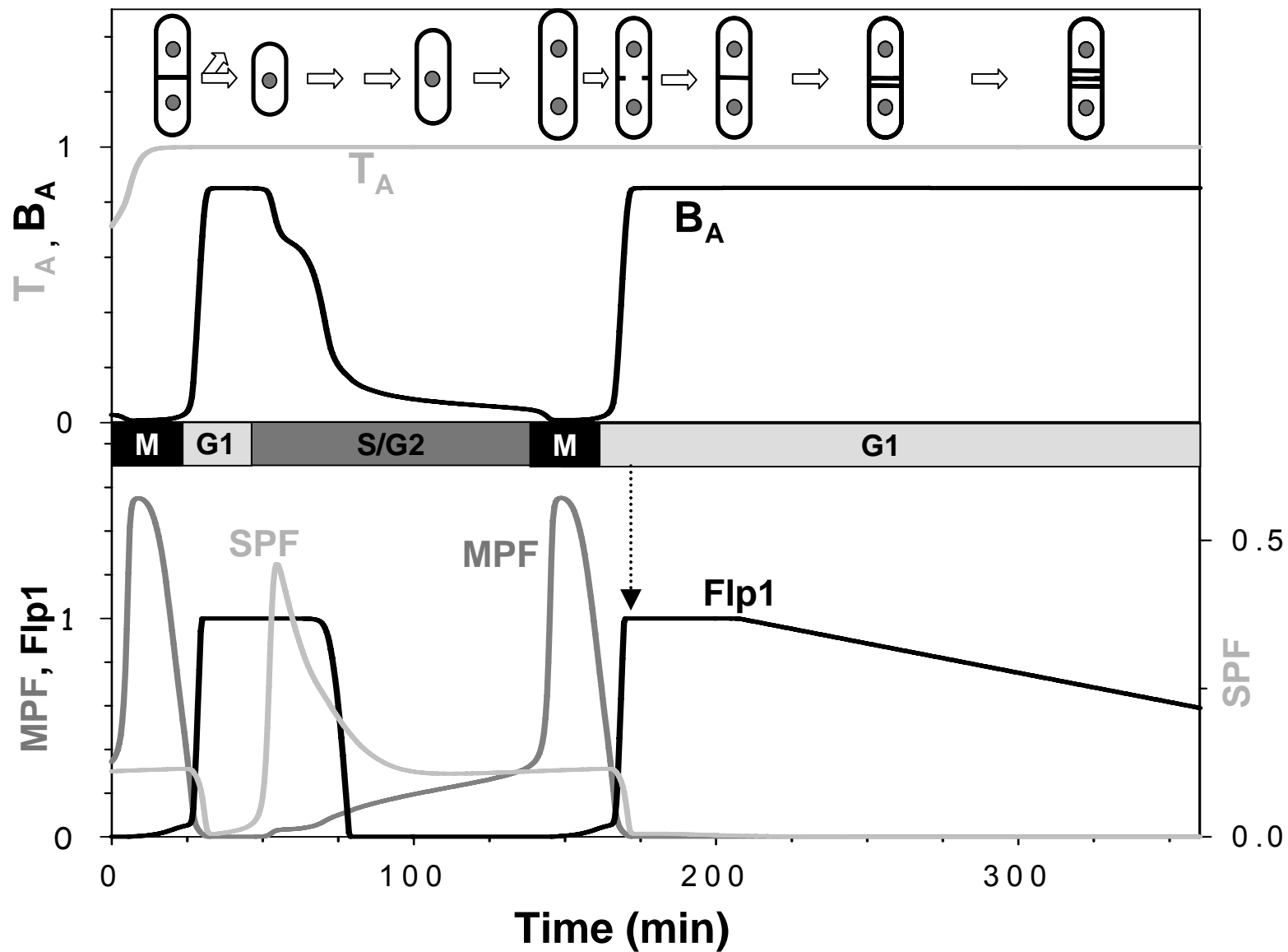
type I



type II

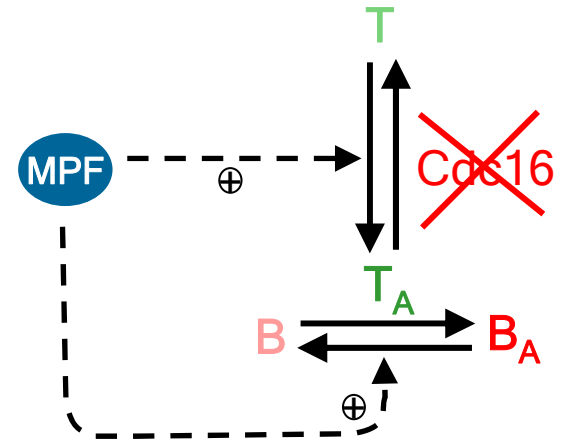


*cdc16<sup>ts</sup> sir* mutant



# *cdc16<sup>ts</sup> sir* mutant

Only MPF inhibits septation in this mutant  
In G1 phase MPF is inactive so SIN stays active



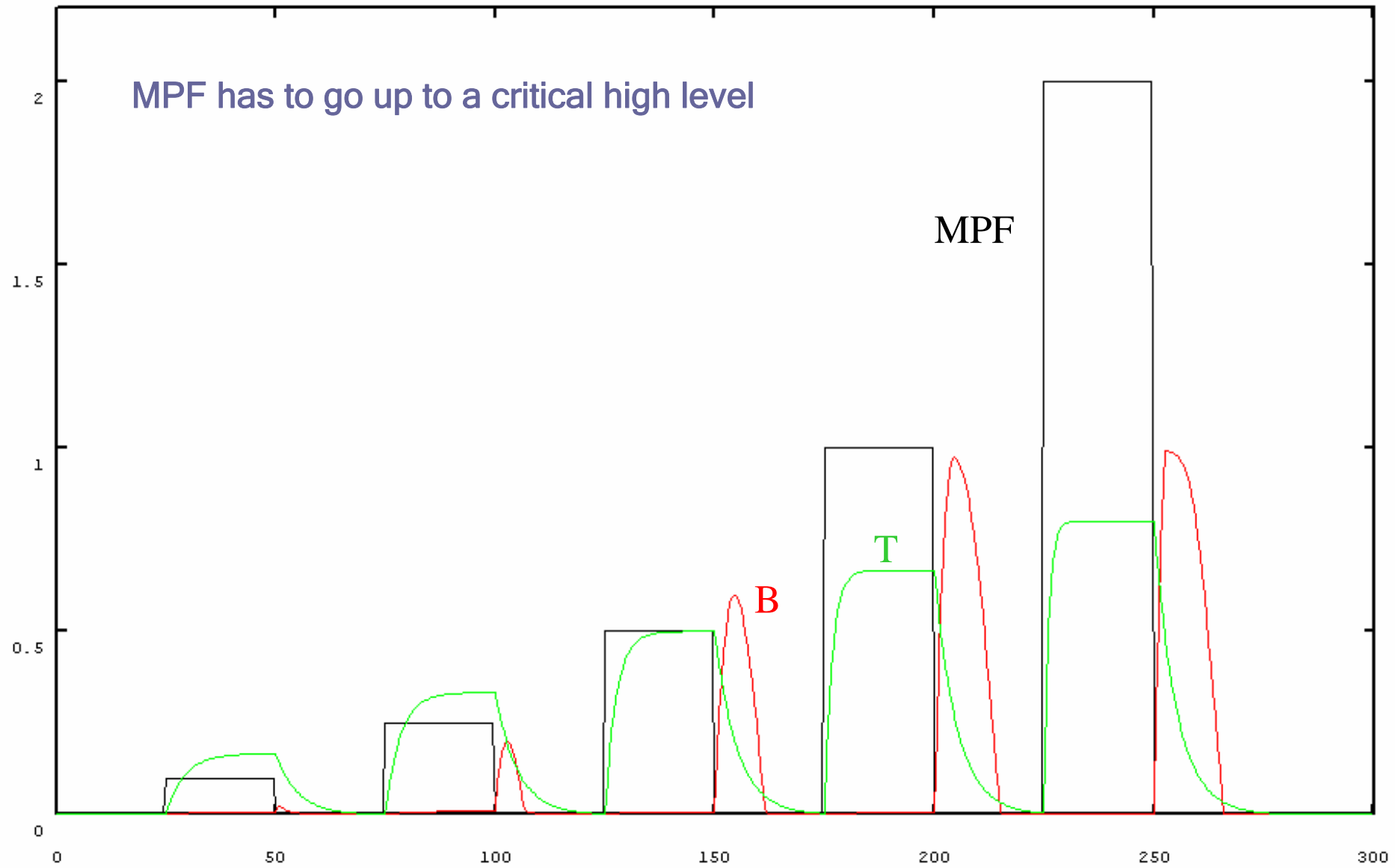


# Conclusions on this part

- ◆ We have created a simple mathematical model of septation initiation network (SIN) in fission yeast. SIN is regulated by MPF activity.
- ◆ SIN should be activated only transiently when MPF activity drops after mitosis, but it should be inactive during the rest of the cell cycle.
- ◆ This basic model can explain various mutant phenotypes and predict the behavior of new mutants

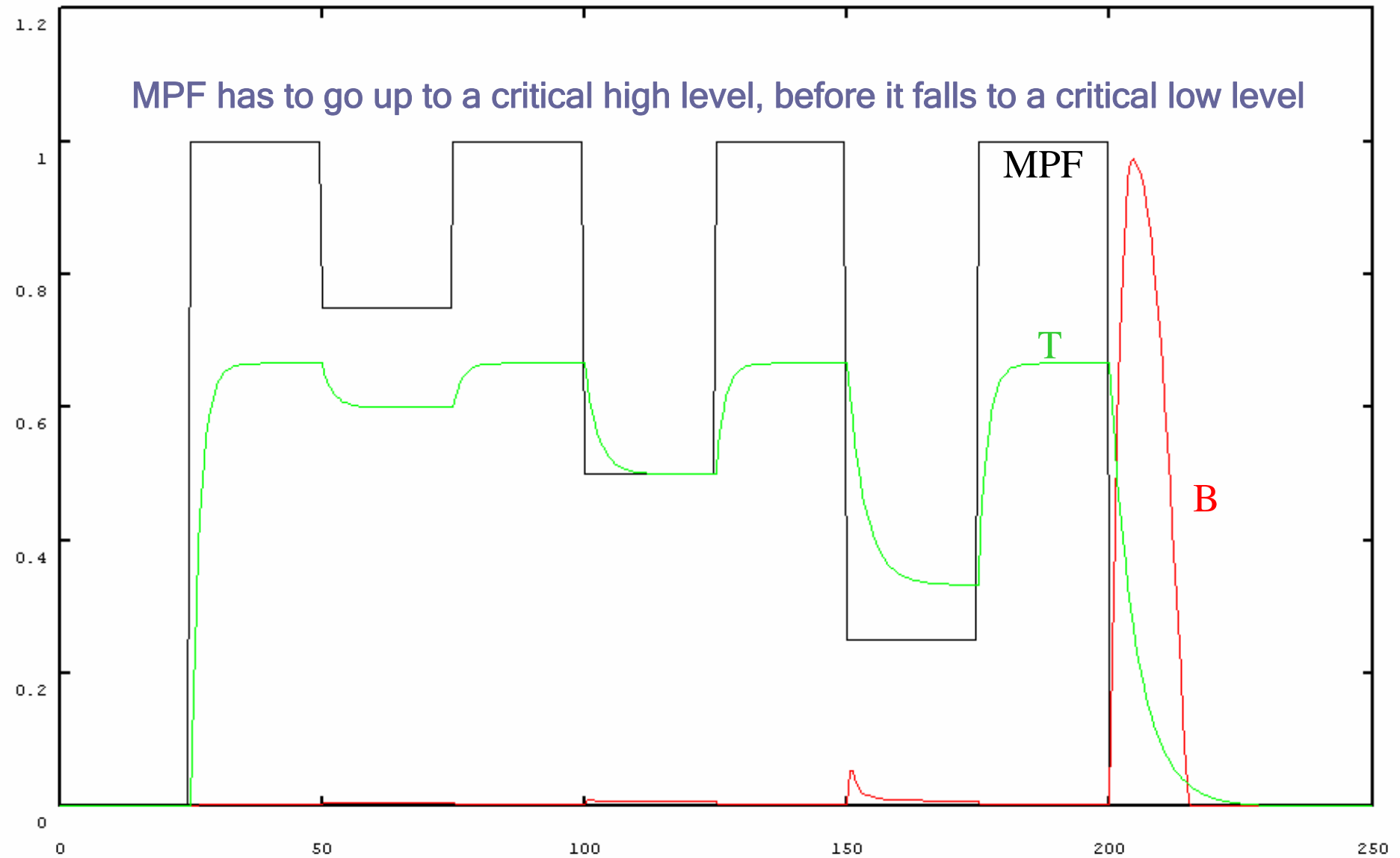
Csikász-Nagy, A., Kapuy, O., Gyórfy, B., Tyson, J.J., Novák B. Modeling the septation initiation network (SIN) in fission yeast cells. *Current Genetics* 51(4):245-55 (2007)

# Septation

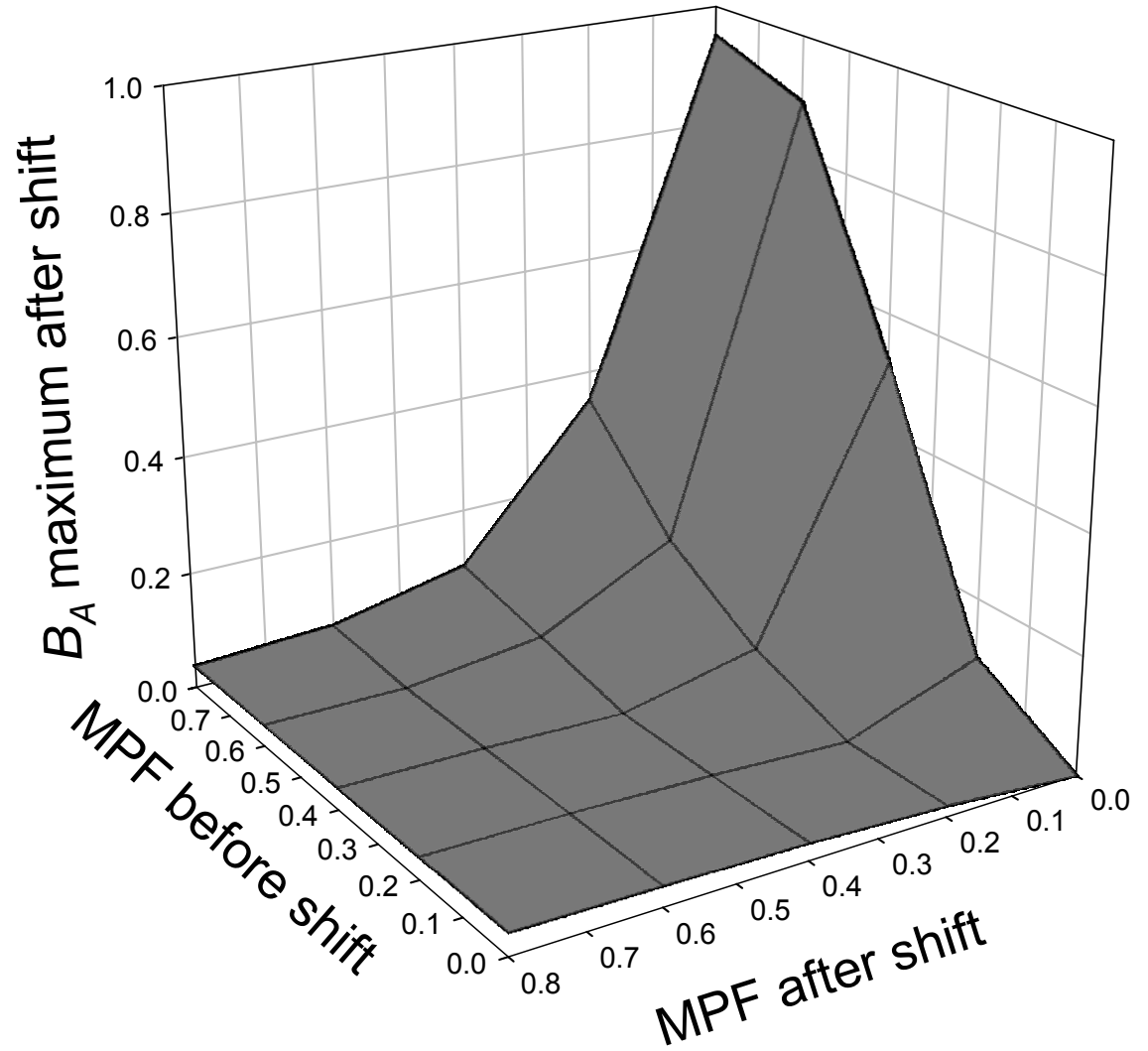


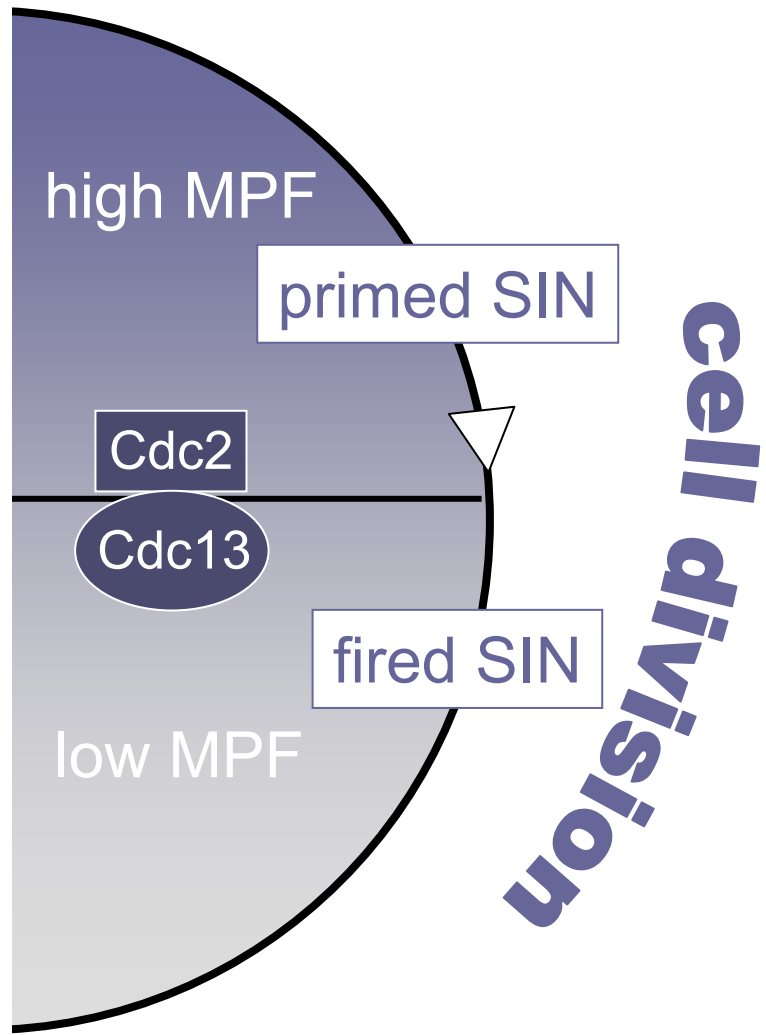
# Septation

MPF has to go up to a critical high level, before it falls to a critical low level

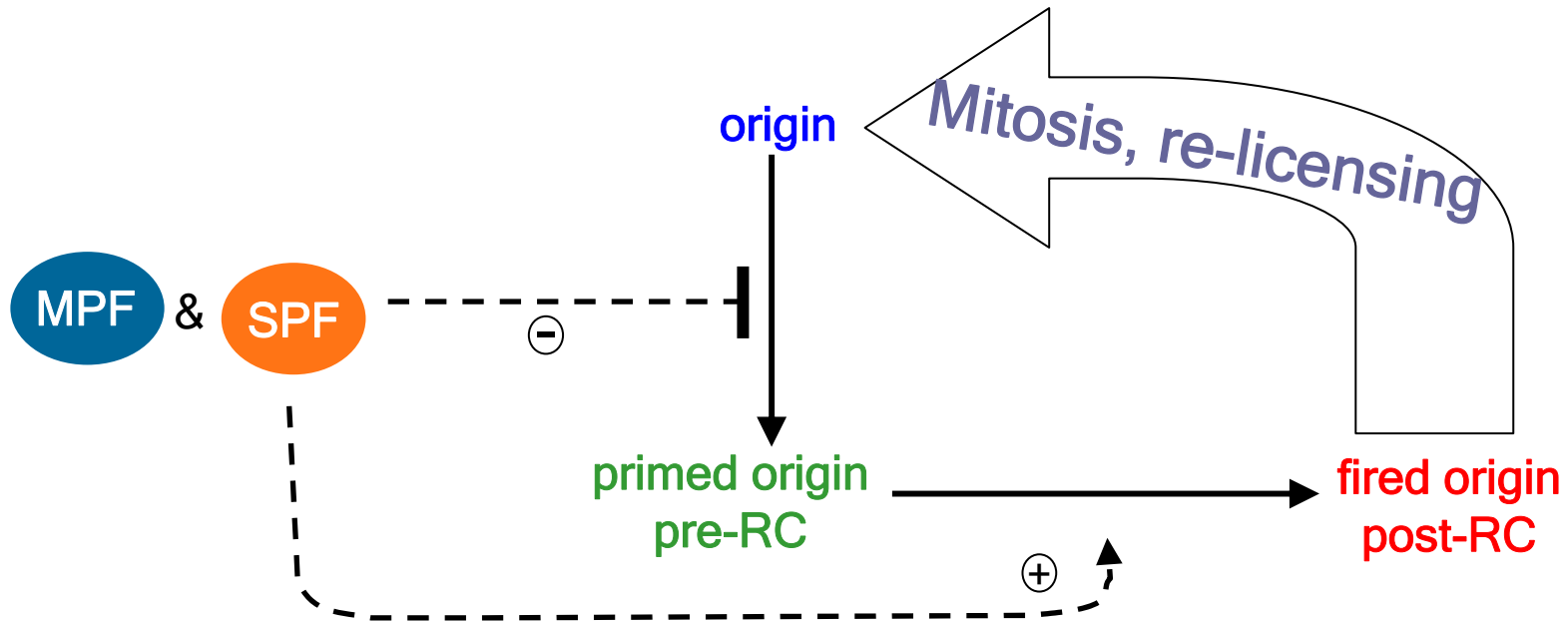


# Dependence of SIN activity on MPF



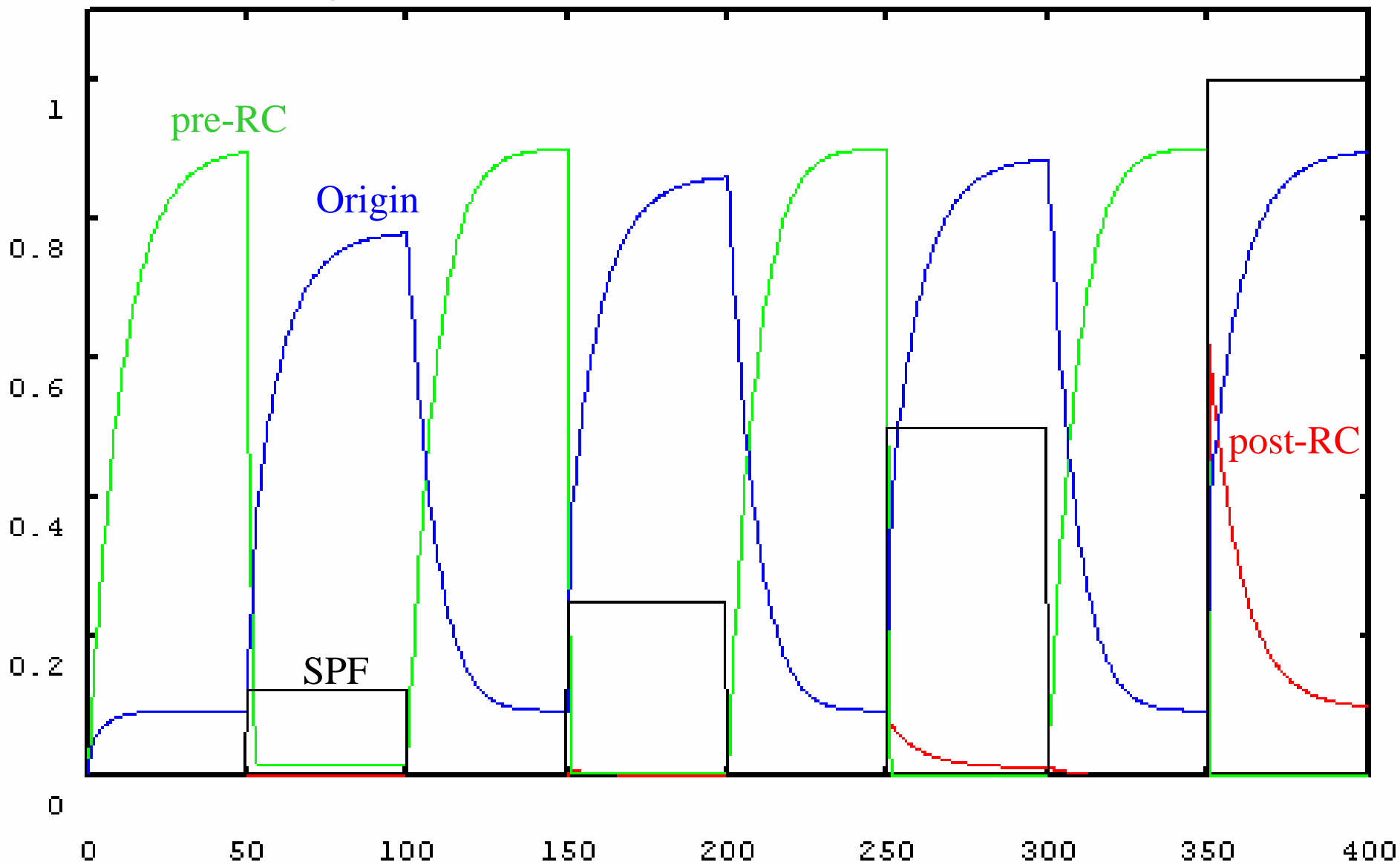


# DNA replication



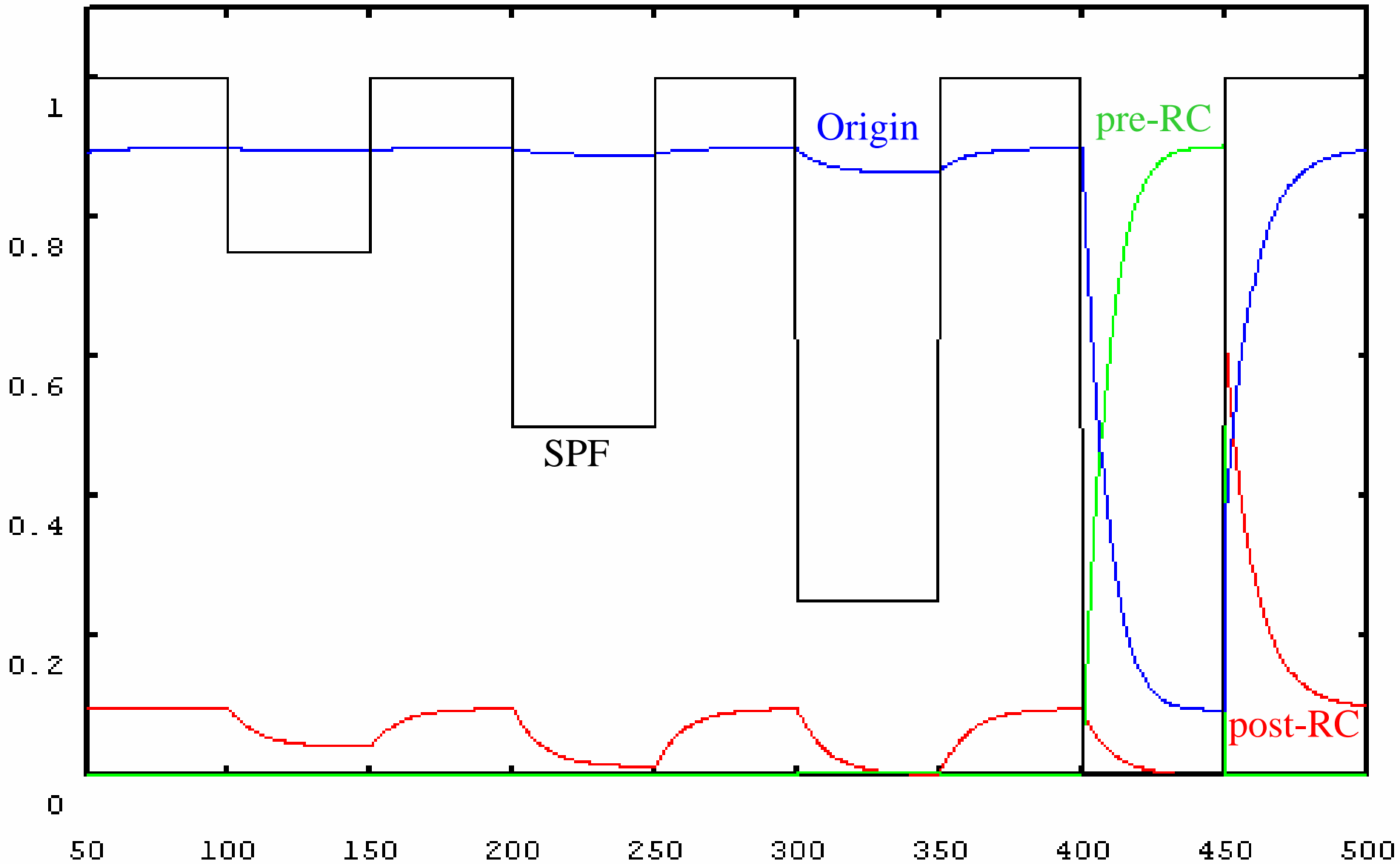
# DNA replication

SPF has to go up to a critical level



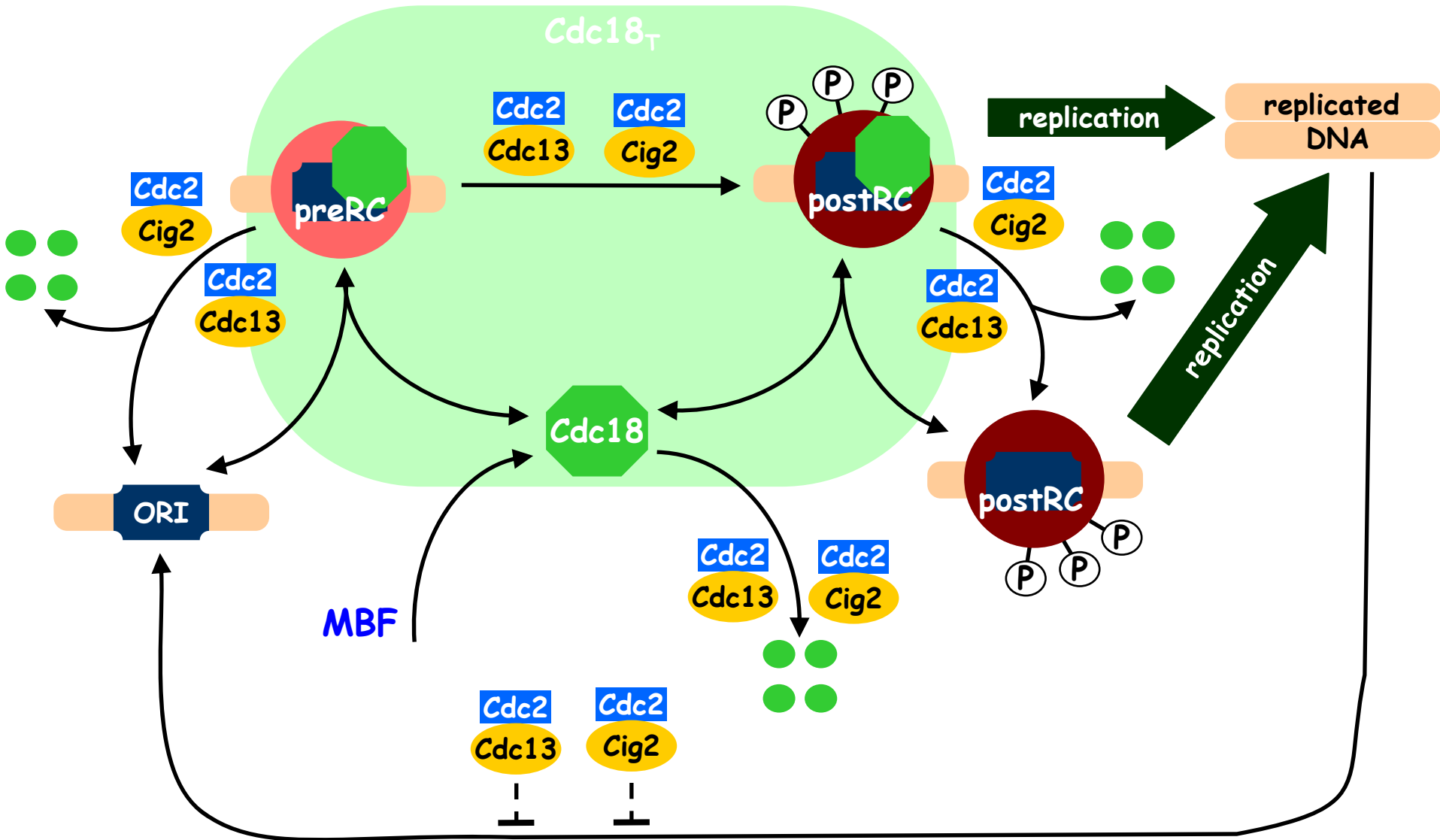
# DNA replication

SPF has to go up to a critical level, after it felt to a critical low level

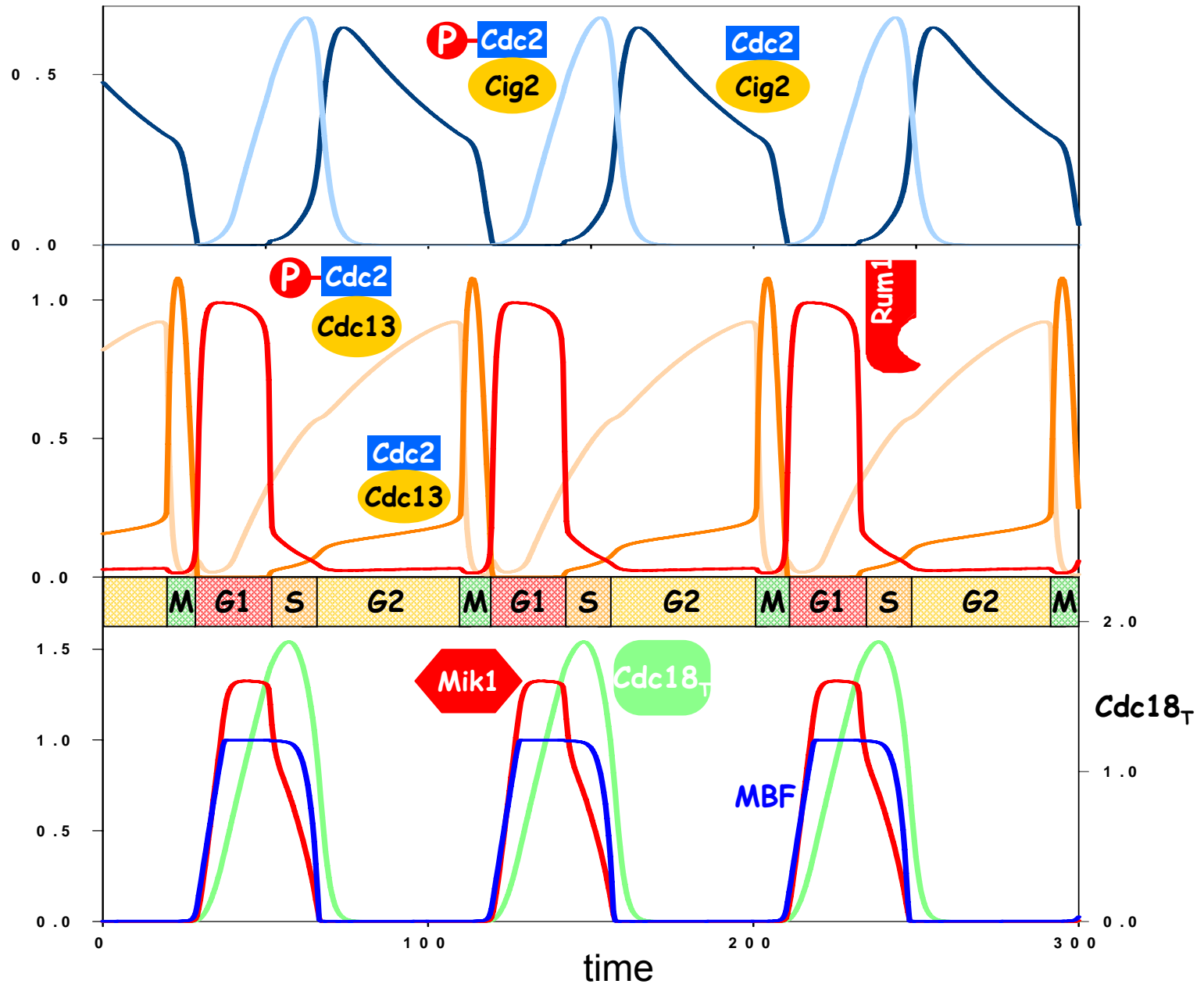




# Detailed model of fission yeast DNA replication



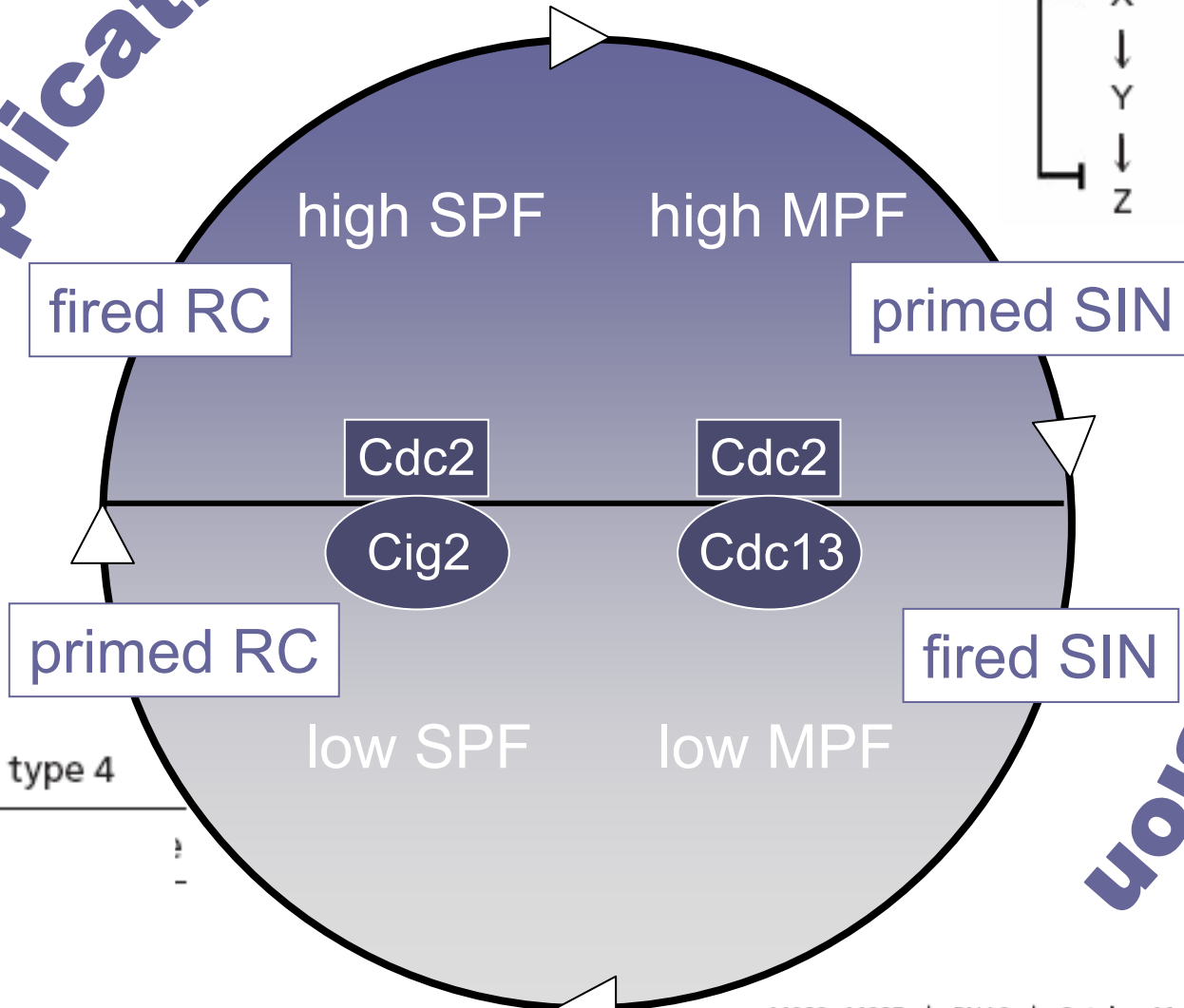
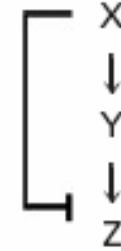
# Detailed model of fission yeast DNA replication



**DNA replication**

Incoherent type 3

Structure



**cell division**

Incoherent type 4

Structure

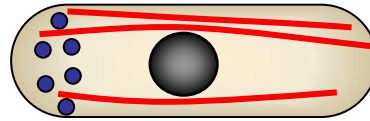


# Modelling fission yeast morphogenesis

# Growth patterns in fission yeasts

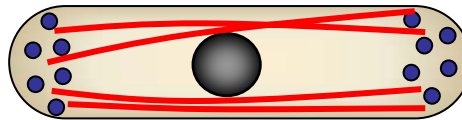
actin = growth    microtubules = direction

polarized growth



G1 phase

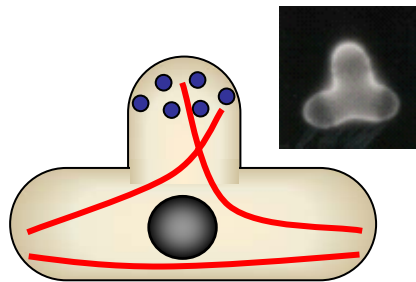
polarized growth



G2 phase

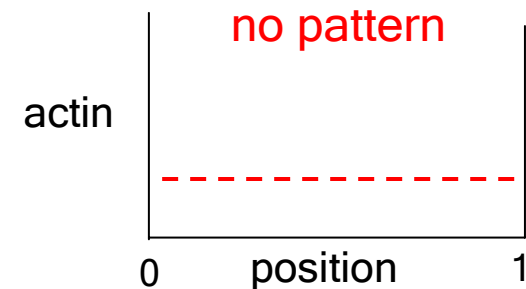
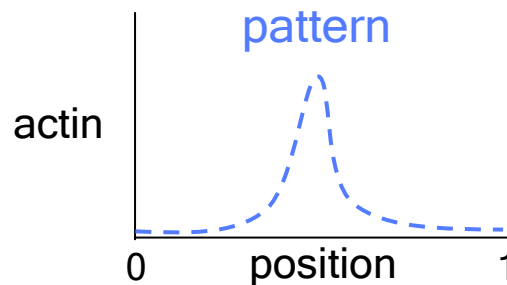
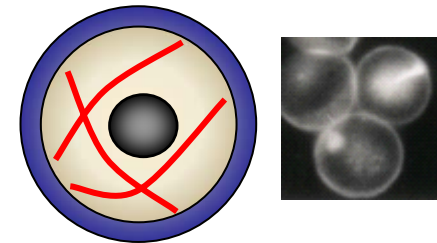
Tea mutants

polarized growth



Orb mutants

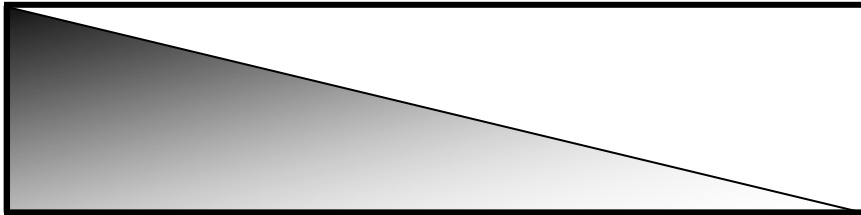
isotropic growth



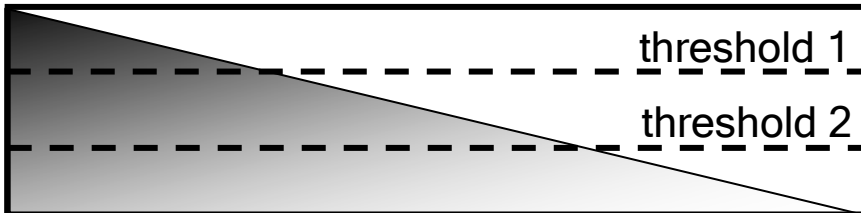
# Two different pattern formation mechanisms

## positional information

primary gradient



interpretation of gradient

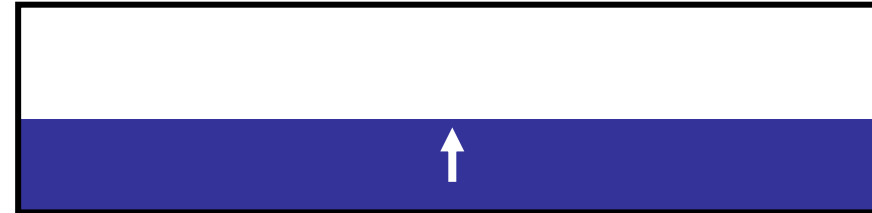


establishment of a new gradient

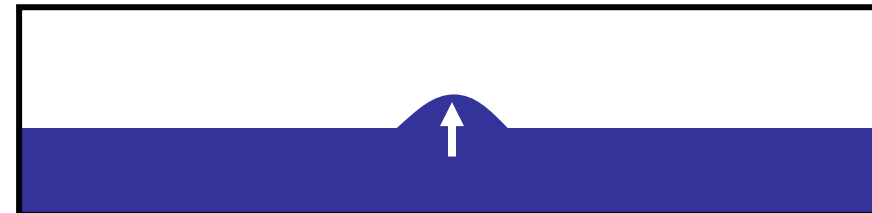


L. Wolpert (1969)

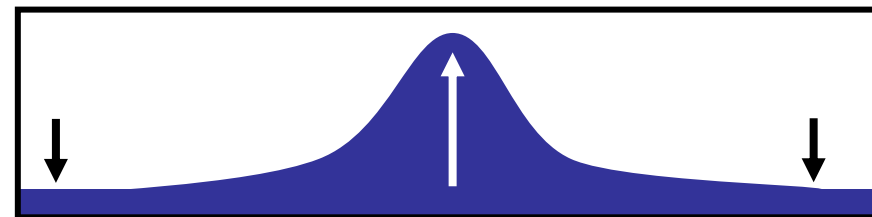
## self-organized gradient



local self-enhancement

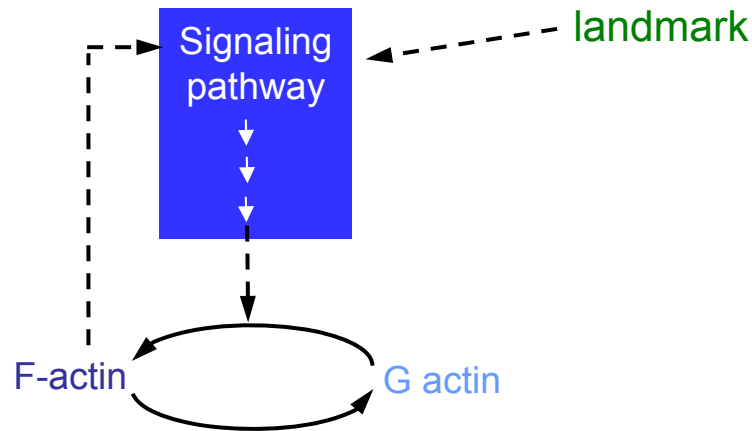
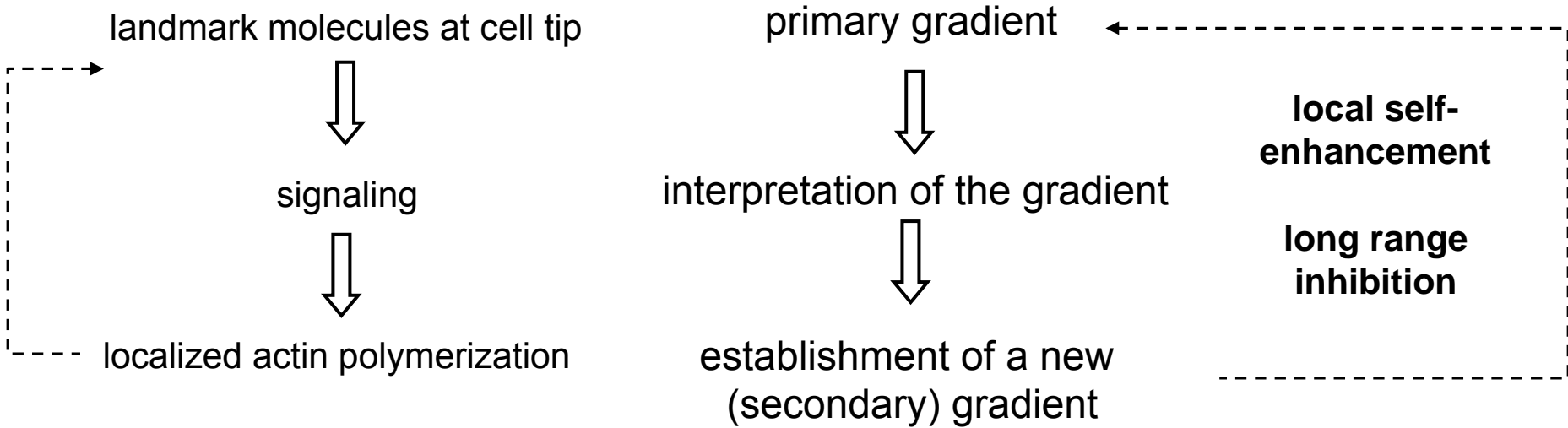


long range inhibition



A.M. Turing (1952); A. Gierer & H. Meinhardt (1972)

# The two mechanisms are not mutually exclusive



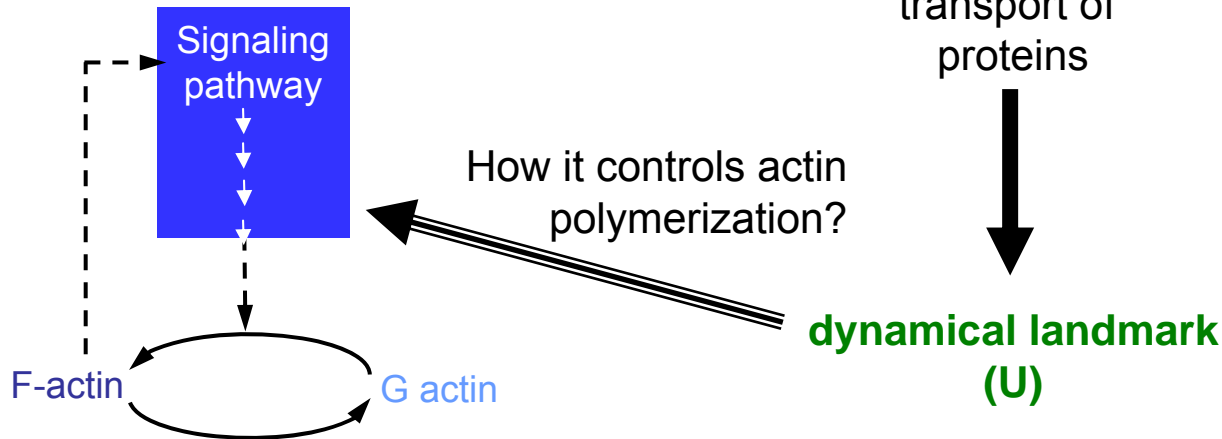
## Partial differential equations:

$$\frac{\partial y}{\partial t} = \underbrace{F(y)}_{\text{reaction}} + \underbrace{D_y \frac{\partial^2 y}{\partial x^2}}_{\text{diffusion}} + \underbrace{v_y \cdot \partial_x (y)}_{\text{convection}} - \underbrace{\frac{y}{h} \cdot \frac{\partial h}{\partial t}}_{\text{dilution}}$$

actin polymerization

MT related  
transport of  
proteins

cell growth

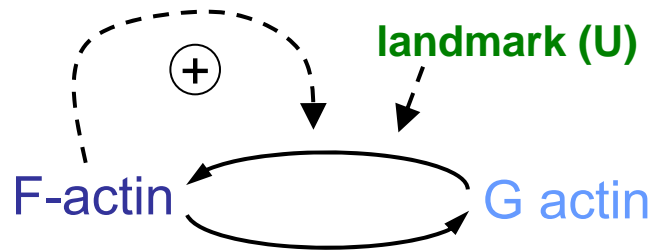


**Three equations :**

- G-actin
- F-actin
- landmark (U)

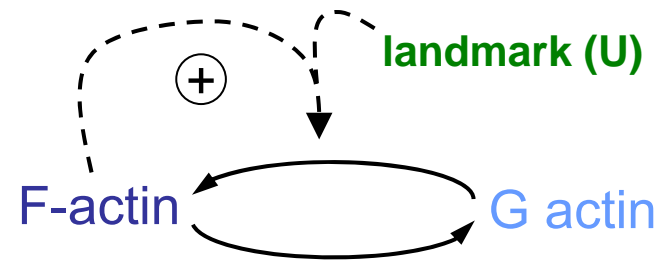


## de novo initiation

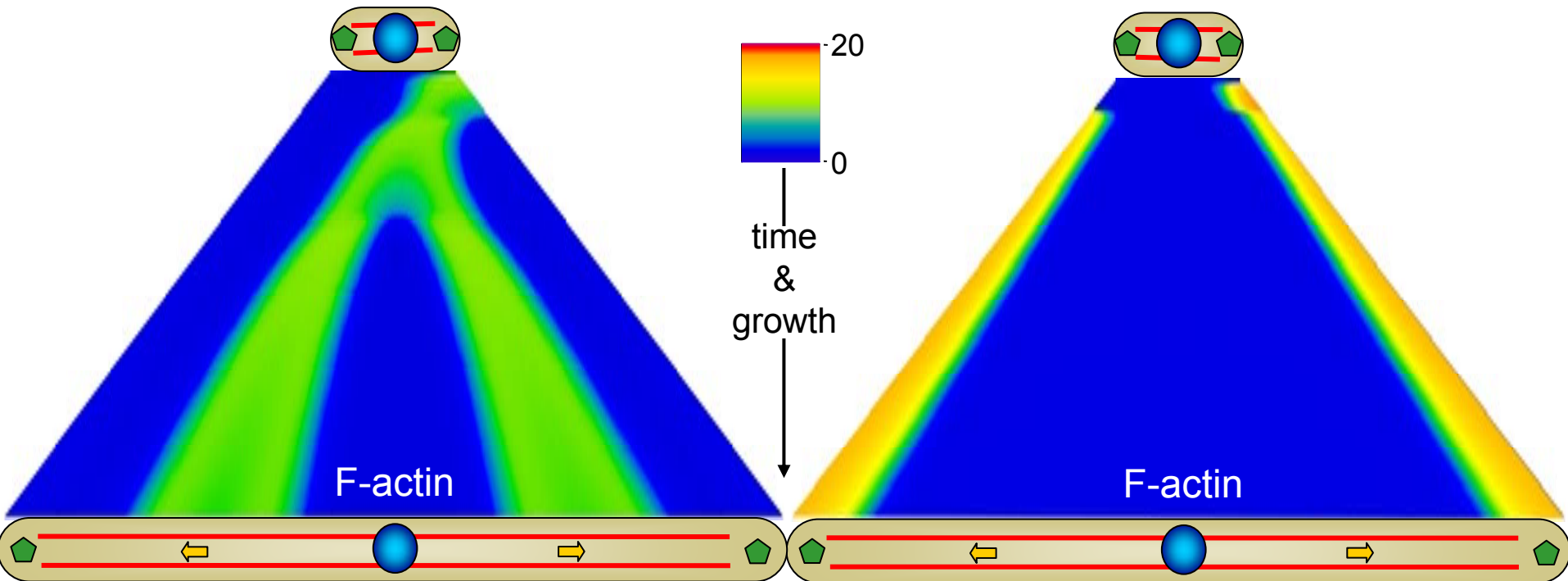


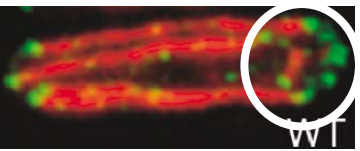
$$\text{F-actin production rate} = (k_3' \cdot \mathbf{U} + k_3'' \cdot f^2) \cdot g$$

## amplification



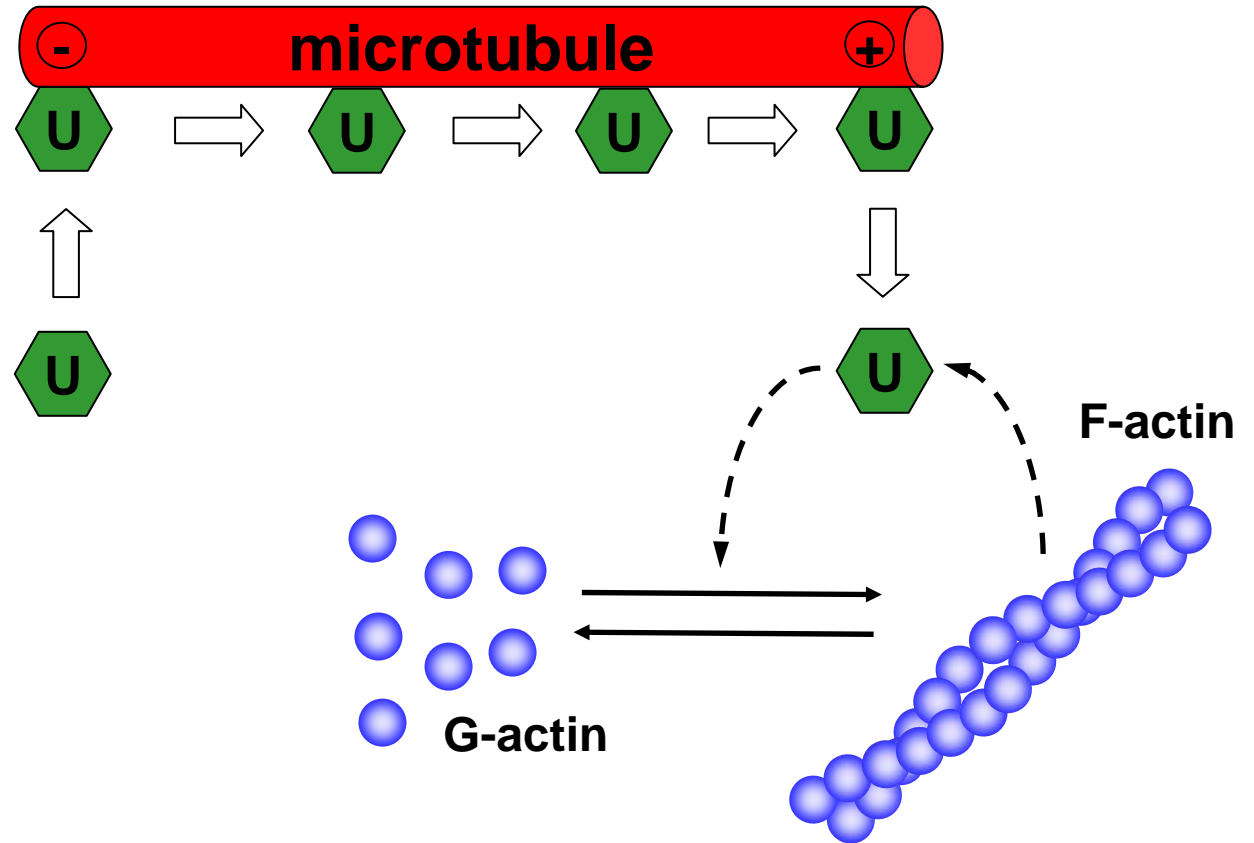
$$\text{F-actin production rate} = (k_3' + k_3'' \cdot \mathbf{U} \cdot f^2) \cdot g$$



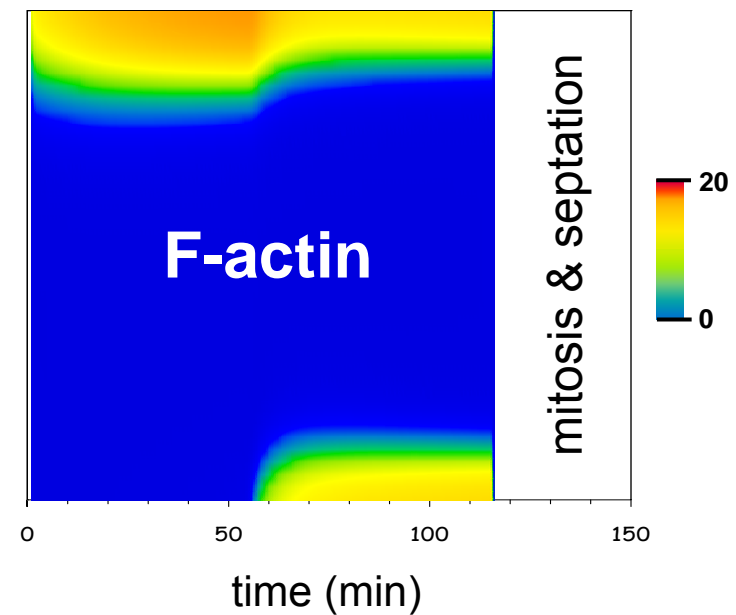
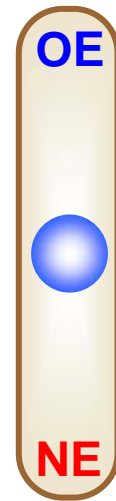
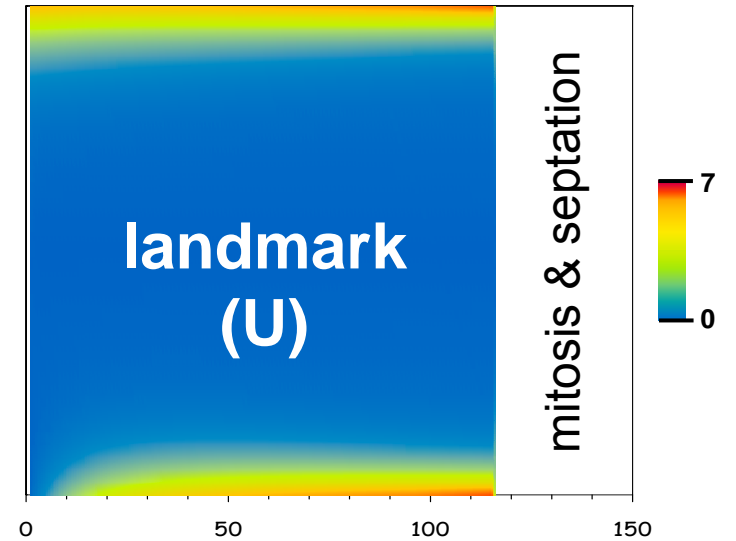
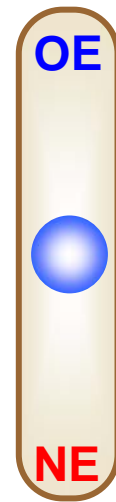
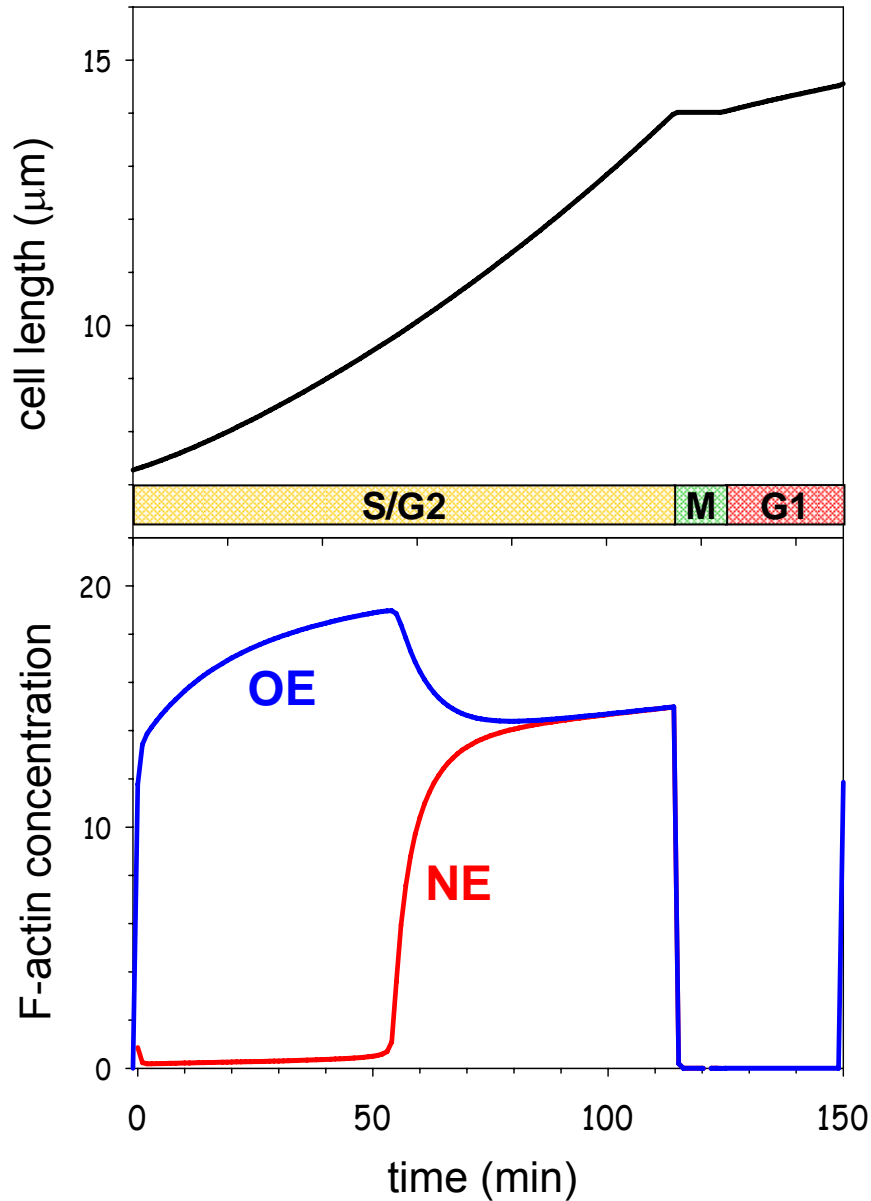


microtubules

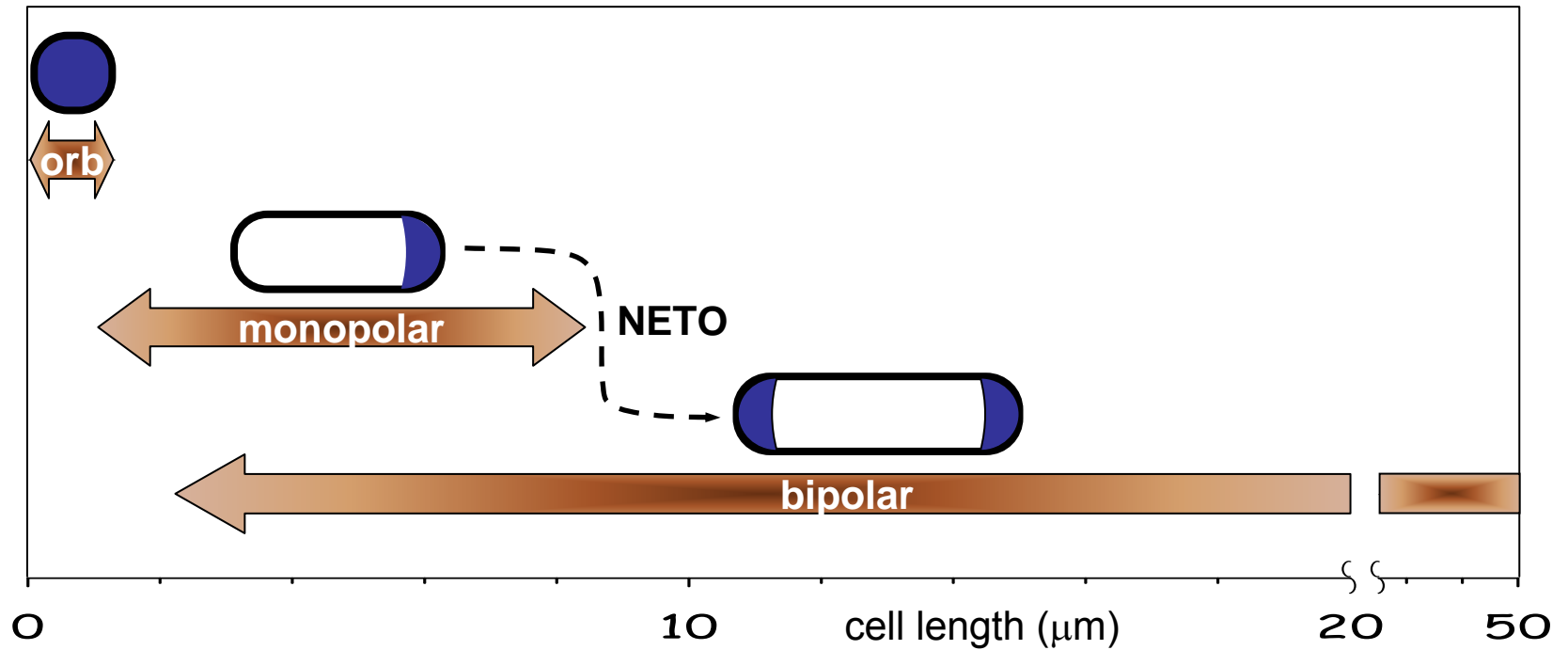
one of the landmarks



# Simulation of wild type cells



# Predicted possible growth patterns of wild type cells

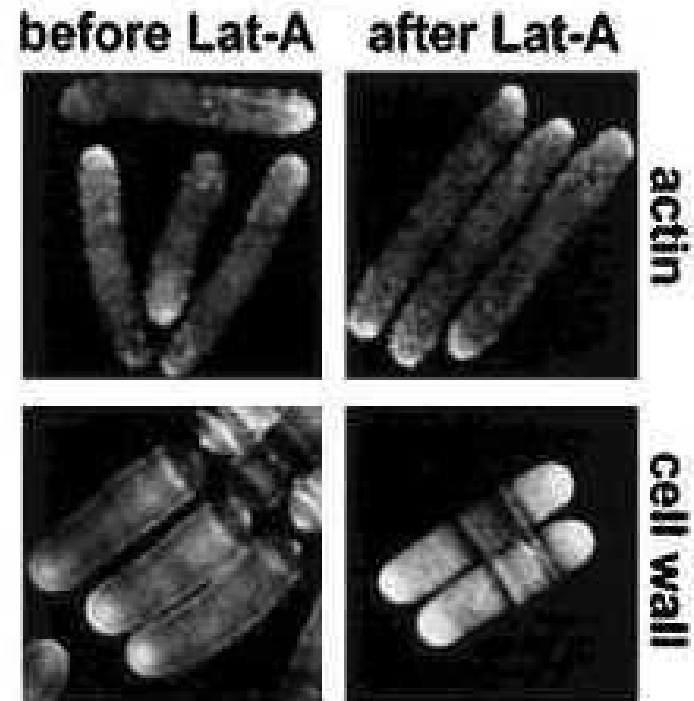
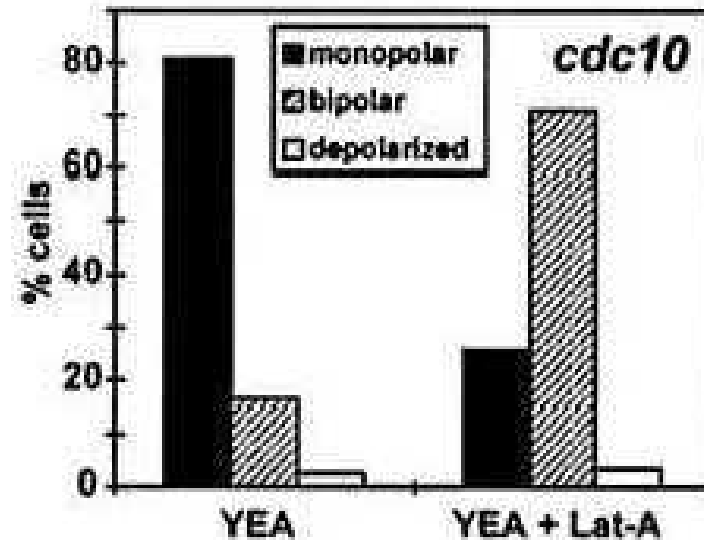


# Disruption of the actin system by Latrunculin-A

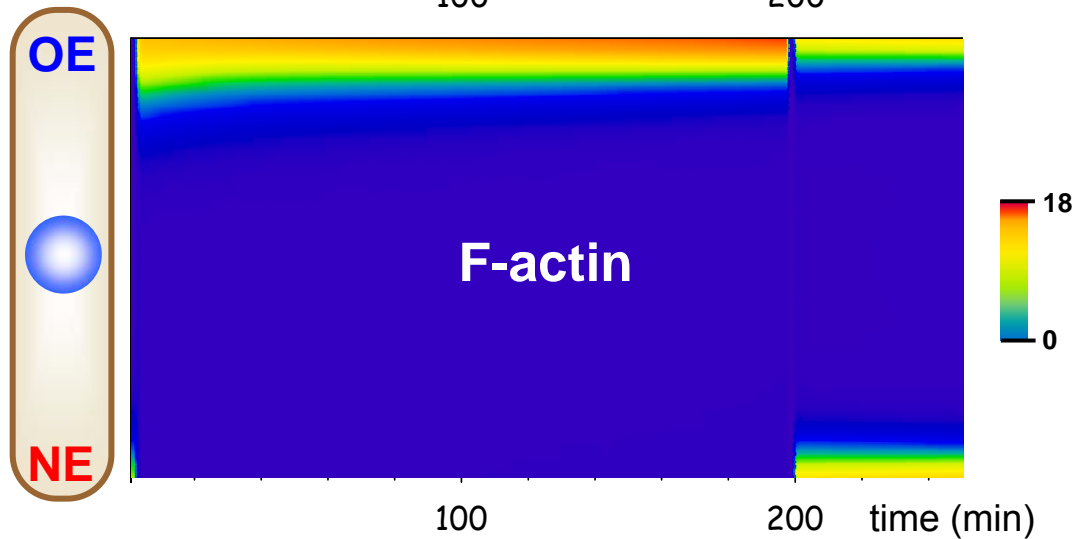
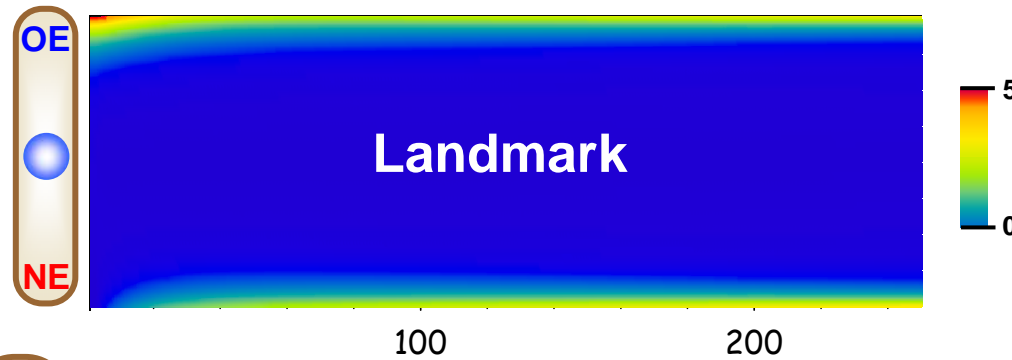
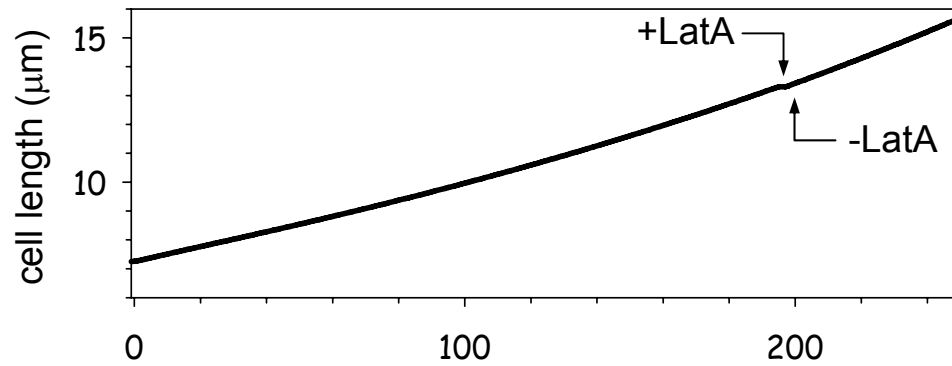
Molecular Biology of the Cell  
Vol. 10, 1495-1510, May 1999

## Ssp1 Promotes Actin Depolymerization and Is Involved in Stress Response and New End Take-Off Control in Fission Yeast

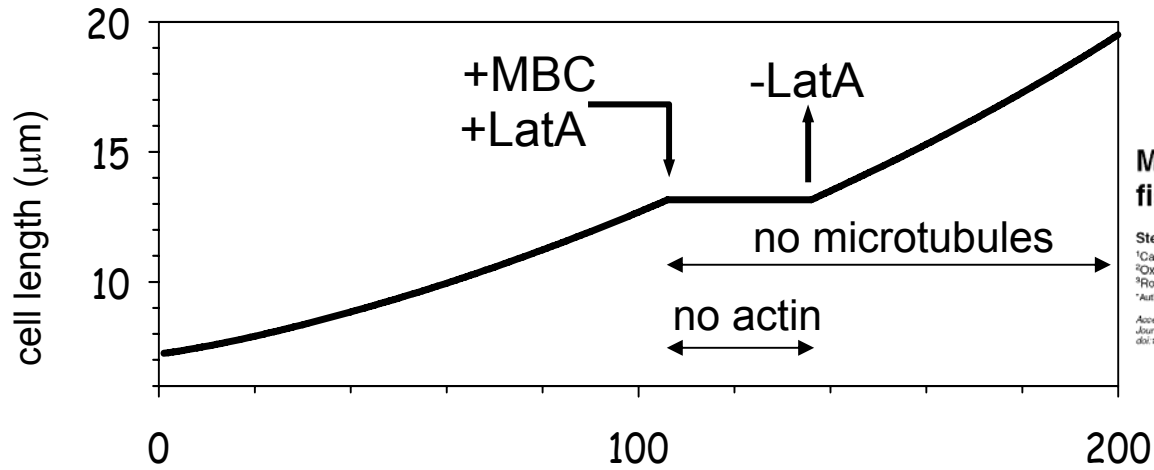
Ivan Rupeš, Zhengping Jia,\* and Paul G. Young†



# Simulation of the Rupes' experiment



# Verification of the underlying pattern forming reaction



## Microtubules offset growth site from the cell centre in fission yeast

Stefania Castagnetti<sup>1,\*</sup>, Béla Novák<sup>1,2</sup> and Paul Nurse<sup>1,3</sup>

<sup>1</sup>Cancer Research UK, Cell Cycle Lab, 44 Lincoln's Inn Fields, London, WC2A 3PX, UK

<sup>2</sup>Oxford Centre for Integrative Systems Biology, University of Oxford, South Parks Road, Oxford, OX1 3QU, UK

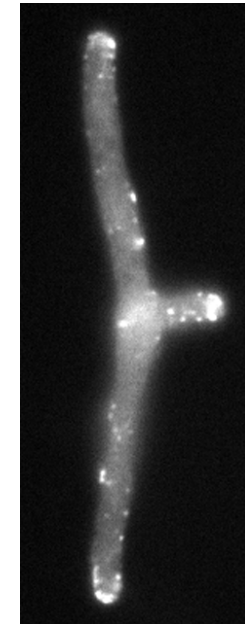
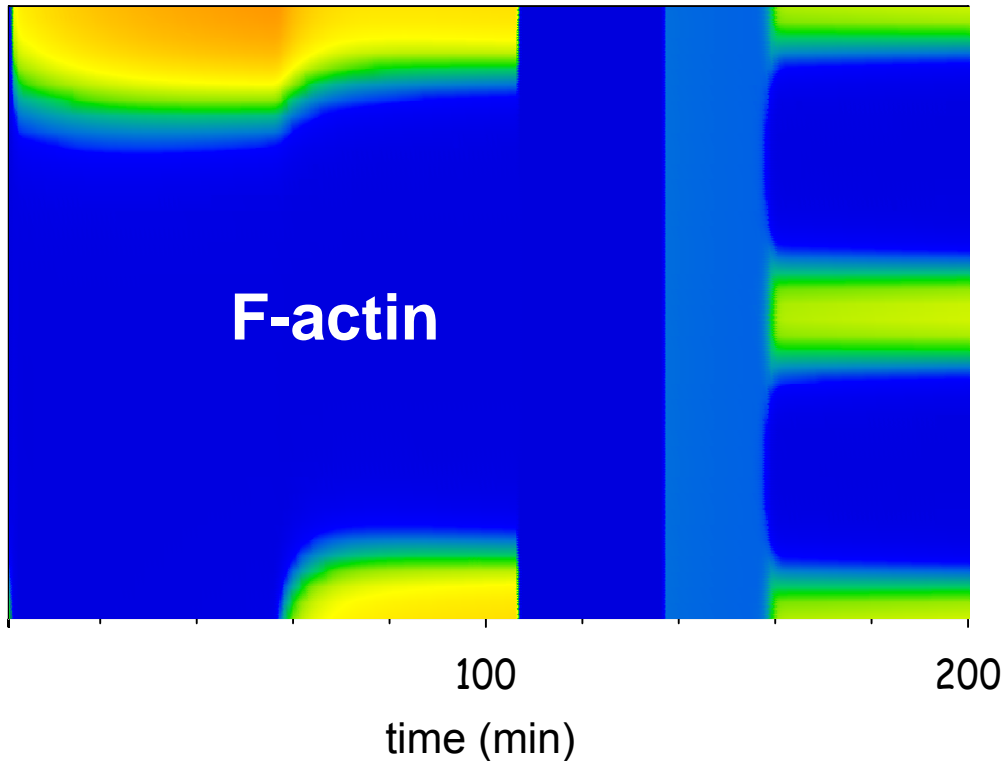
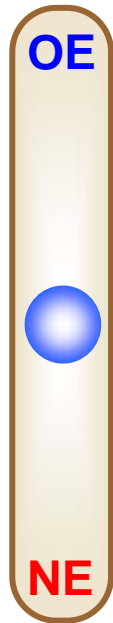
<sup>3</sup>Rockefeller University, 1230 York Avenue, New York, NY 10021, USA

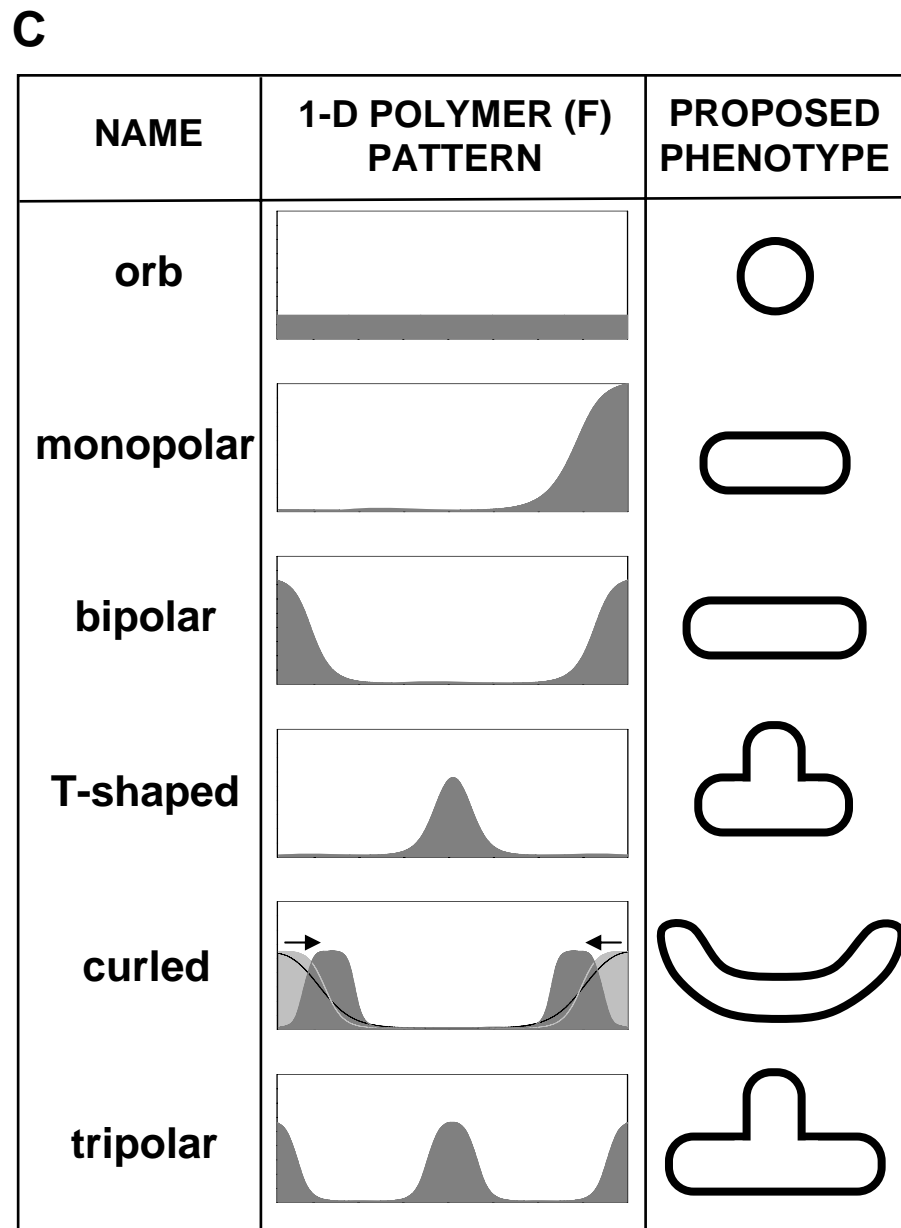
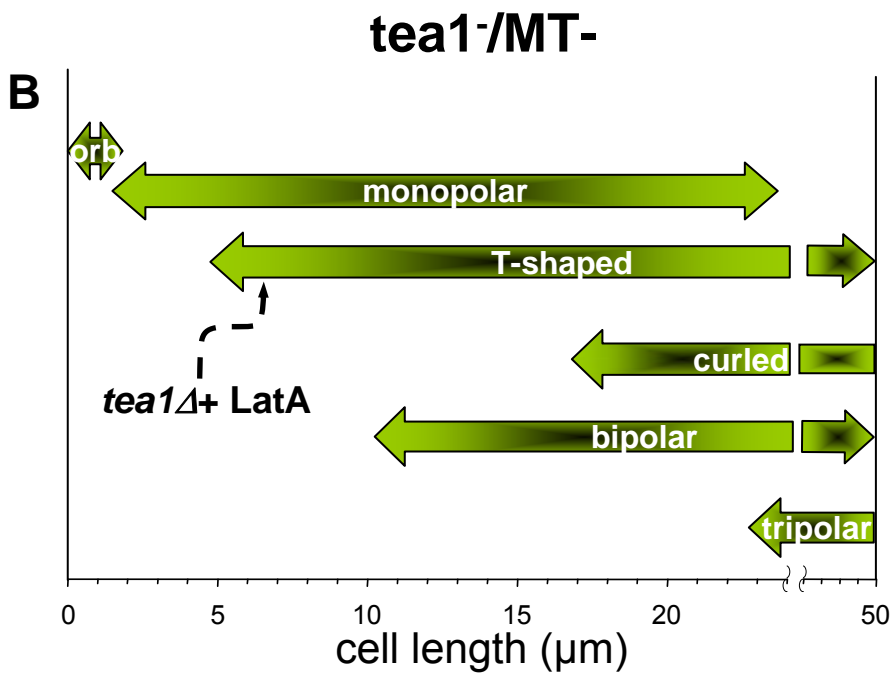
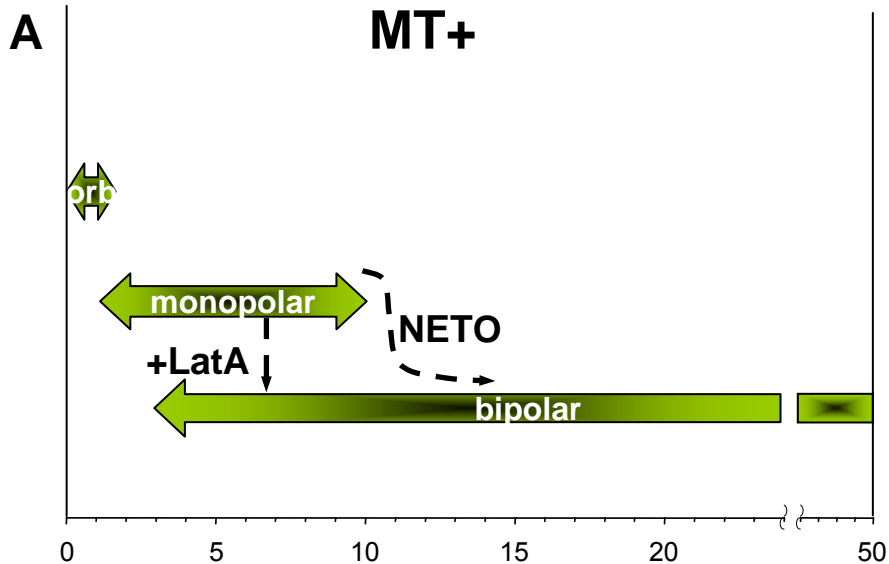
\*Author for correspondence (e-mail: S.Castagnetti@cancer.org.uk)

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Journal of Cell Science 120, 2205–2213 Published by The Company of Biologists 2007

doi:10.1242/jcs.03464

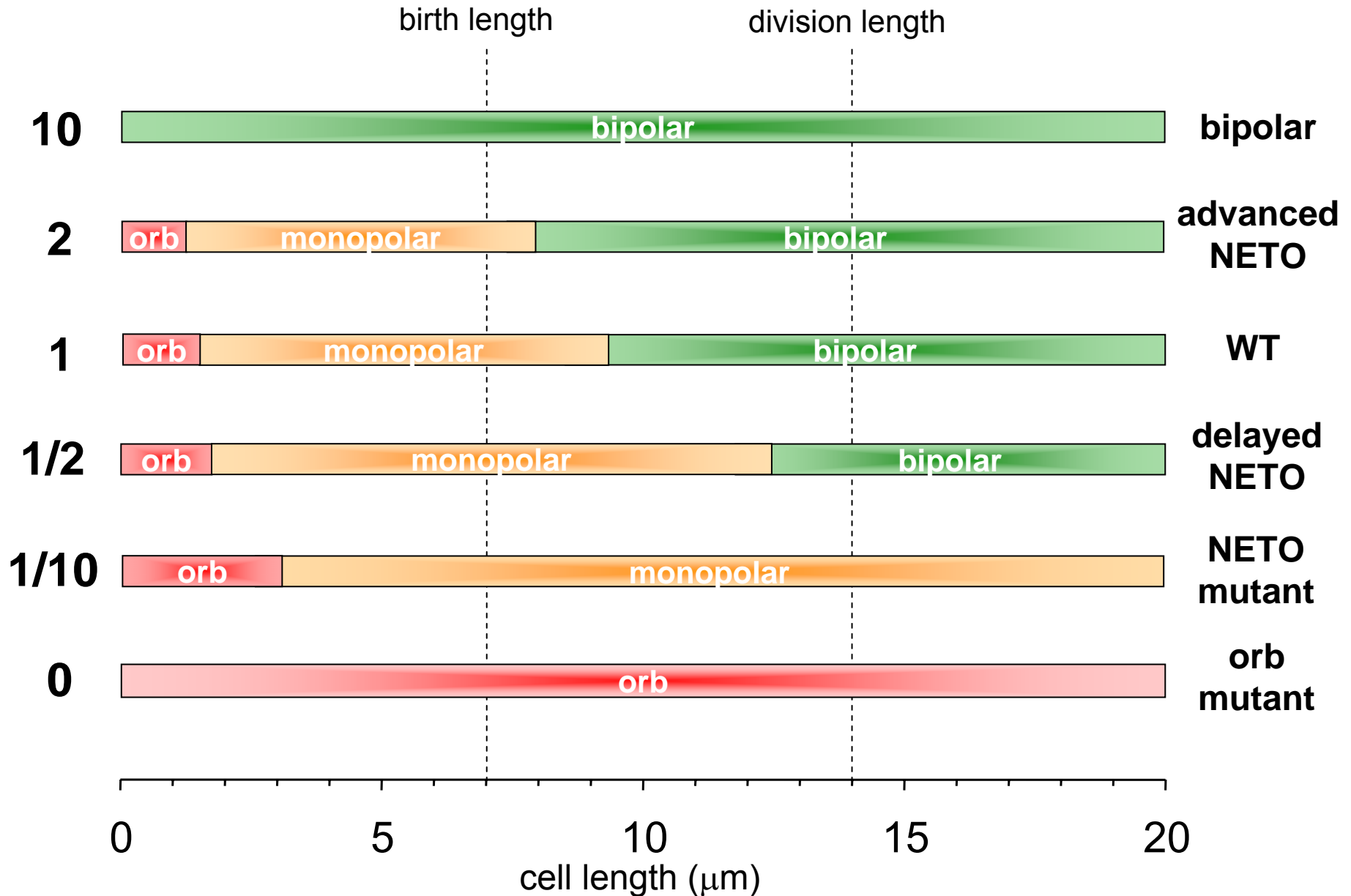






# Morphogenetic mutants & robustness

(positive feedback efficiency)



## Conclusions 2:

- ◆ Very simple model (3 variables)
- ◆ Can produce wild-type and mutant growth patterns → suggests protein function
- ◆ Possible biological role for Turing pattern (only in microtubule disrupted case)
- ◆ Predicts the role of microtubules in polarized growth regulation



S. Castagnetti



John J. Tyson    Béla Novák



Wolfgang Alt



Orsolya Kapuy



Béla Györfy



Ákos Sveiczler

