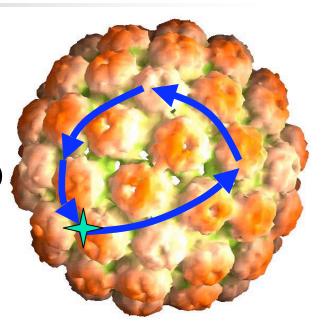


Prof. David Wu
Colorado School of Mines
KITP - 27 June 2006



Travelogue

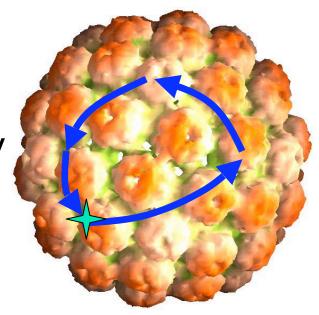
- Origins & trip plans
- Wading into the swamp
- According to Mapquest
- Places to visit next



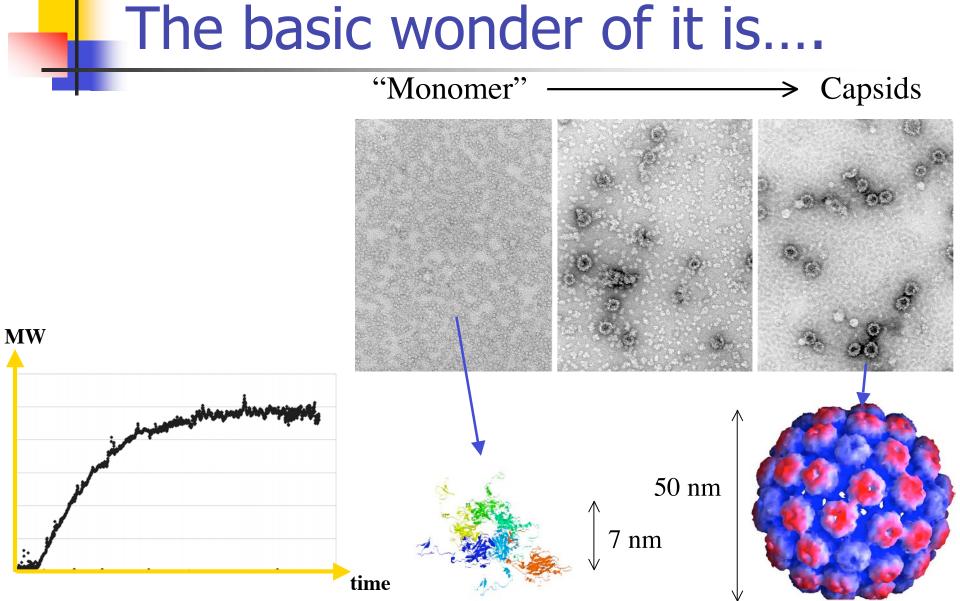


Origins & trip plans

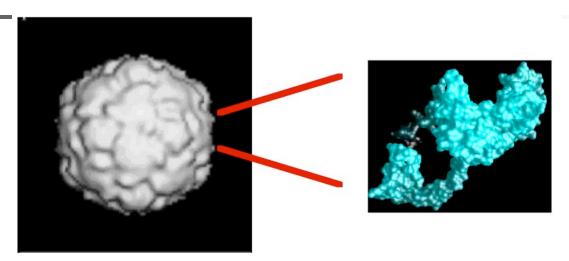
- Where my interest started
- Introduce relevant virology

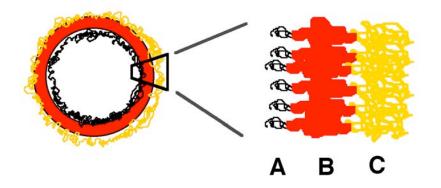






A Parallel....?







Essential questions

- Questions about the part
 - How much information?
 - Consequences of shape/specific interactions/mechanical properties, etc.
- Questions about the process
 - Mechanisms
 - Cooperativity
 - Thermodynamics & Kinetics
 - Fluctuations



Mechanism

- Is there an identifiable "mechanism" or pathway? (cf. Aggregation)
 - Sequential addition? Subtraction?
- Are there important intermediates?
- Does assembly proceed by "nucleation & growth"?



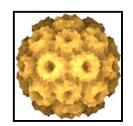
Thermodynamics & kinetics

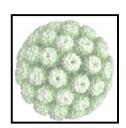
- Do different structures correspond to thermodynamic or energetic optima?
- Or is structure under kinetic control?
- Competing pathways/products
 - Off-size capsids, off-symmetry capsids, ribbons, winding shells...
- Timescale/rate of assembly
 - Responsive to biological signals

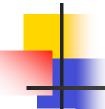


Fluctuations

- Virology has been strong on structure, comparatively weak on dynamics:
 - Is microscopic reversibility relevant?
 - Error correction--does it happen?
 - Functional role for fluctuations?
 - e.g. mechanical/transport
 - Role in protein-protein binding?



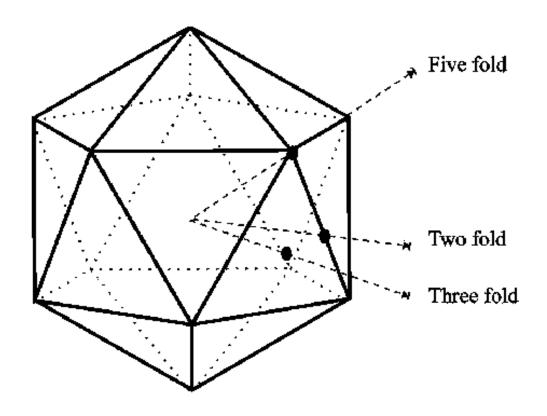




Icosahedral capsids

Icosahedral

- 20 identical triangles
- Characterized by a pattern of 5-fold, 3fold and 2-fold rotational symmetry
- Large volume/surface area

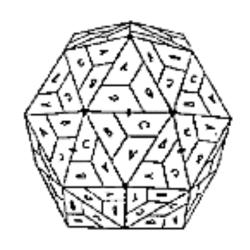


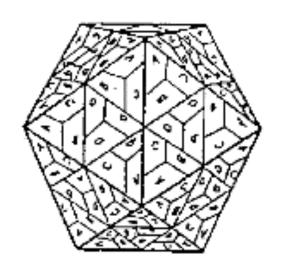


Quasiequivalence

(Caspar & Klug, 1962)





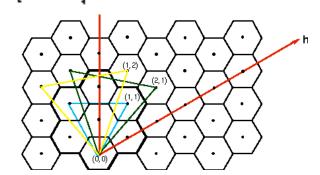


$$T = 1$$

$$T = 3$$

$$T = 4$$

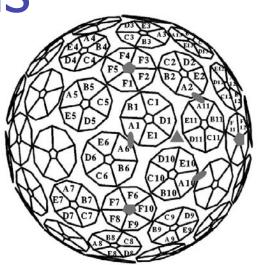
- 60*T copies, with T=1,3,4,7,9,12...
- 12 5-fold and T(10-1) locally 6-fold sites
- Chiral (like fullerenes)

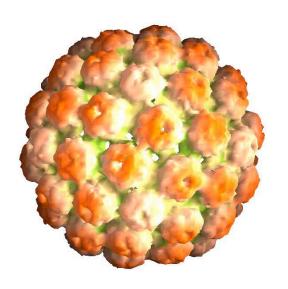




Inequivalent positions

- How do proteins find their correct positions?
- Errors and correction?
- Papilloma, Polyoma, SV40 are exceptions: not quasiequivalent
 - T=7d surface lattice
 - Prebonded pentamers
 - "5 around 1" intermediates?





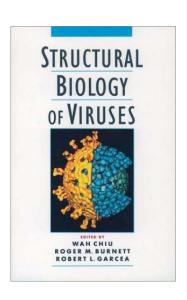


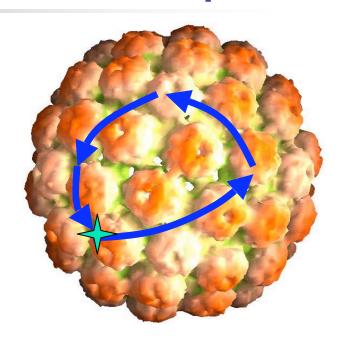
Wandering into the swamp

- MALS light-scattering experiments on capsid assembly
- Track kinetics by average molecular weight



Bob Garcea UCHSC

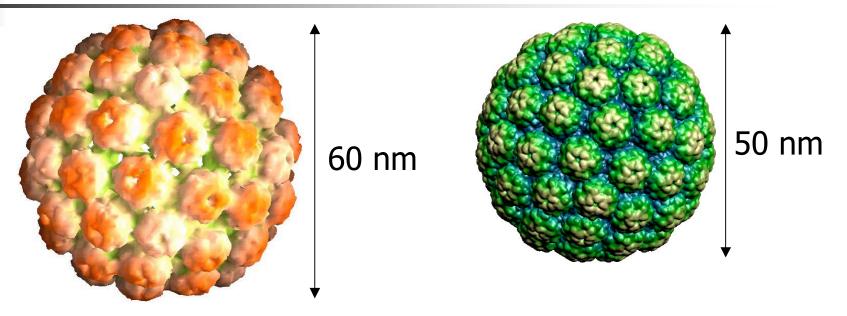




Casini et al., Virology, 2004

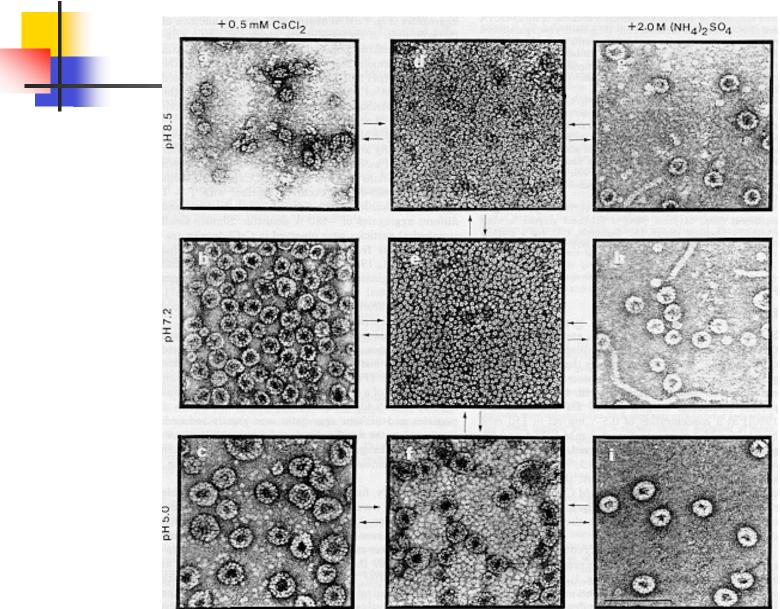


Papilloma & Polyoma



- Two subfamilies of Papovaviridae
- Structural similarity at tertiary and quaternary (T=7) level, but not secondary

Reversible normal & monster assembly

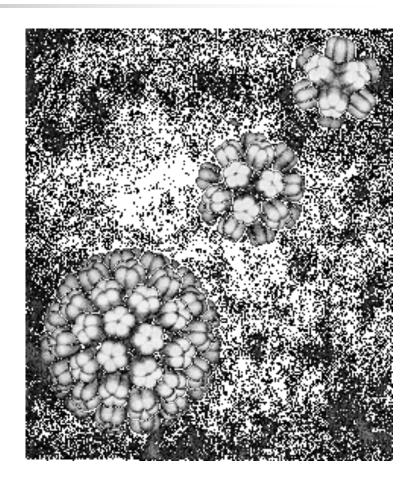


Polyoma VP1 Garcea et al. Nature '87



Various symmetries possible

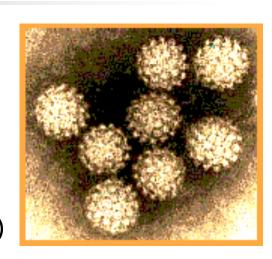
- Three different complete shell assemblies can form:
 - 12-icosa
 - 24-octa
 - 72-icosa
- (12 & 24 are mutant)

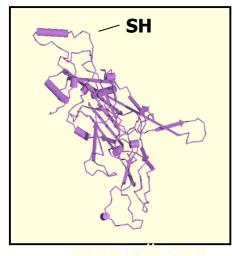




Human papillomavirus (HPV)

- >90 strains
- Closed circular 8kb dsDNA in minichromosome
- Two structural proteins
 - Major capsid protein L1 (500 residues)
 - Minor capsid protein L2 (3%)
- Assembly occurs in nucleus of cell, not reducing cytoplasm
- Host chaperones mediate assembly and disassembly







HPV and Cervical Cancer

- Cervical Cancer kills 300,000 women/yr worldwide (mostly in developing countries)
 - 2nd after breast cancer, 1st in some developing countries
 - Nearly all cervical cancers show HPV infections
 - 75% of sexually active women have been infected
 - 2 x 10⁷ currently infected worldwide
 - 6 x 10⁶ new HPV infections/yr in US

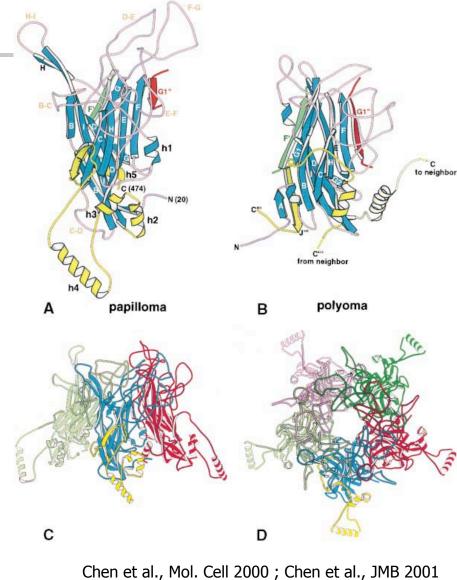


Capsids for Cancer Vaccine

- HPV Virus-Like Particles (capsids) as vaccine
- Gardasil (Merck) approved June 2006
 - 2nd cancer vaccine
 - ~100% effective in Phase III on 12,000 women in 13 countries
 - Targets HPV 6, 11, 16, 18 VLPs
 - 70% of Cervical cancer cases & 90% genital warts
 - \$360/person , expect \$2B/yr sales
 - To be administered pre-puberty (two decades from infection to cancer)
 - Gates Foundation \$30M grant to study & distribute to poorer countries

Protein and pentamer structure

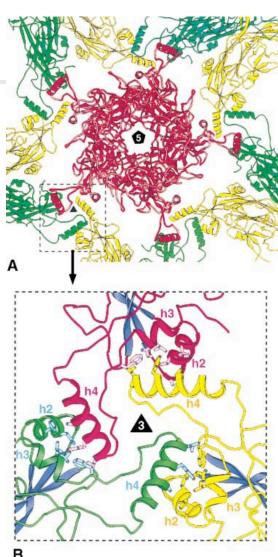
- Classical jelly roll beta sandwich
- HPV
 - Helical subdomain near Cterminus needed for interpentamer contacts for assembly
 - N-terminus controls size (T=7 -> T=1)
 - C-terminus + charged, disordered, inside
- Polyoma
 - N-terminus + charged
 - C-terminus disordered, orders upon invasion of neighboring pentamer, w/ Ca²⁺ contacts



T=1 HPV VLP Crystal



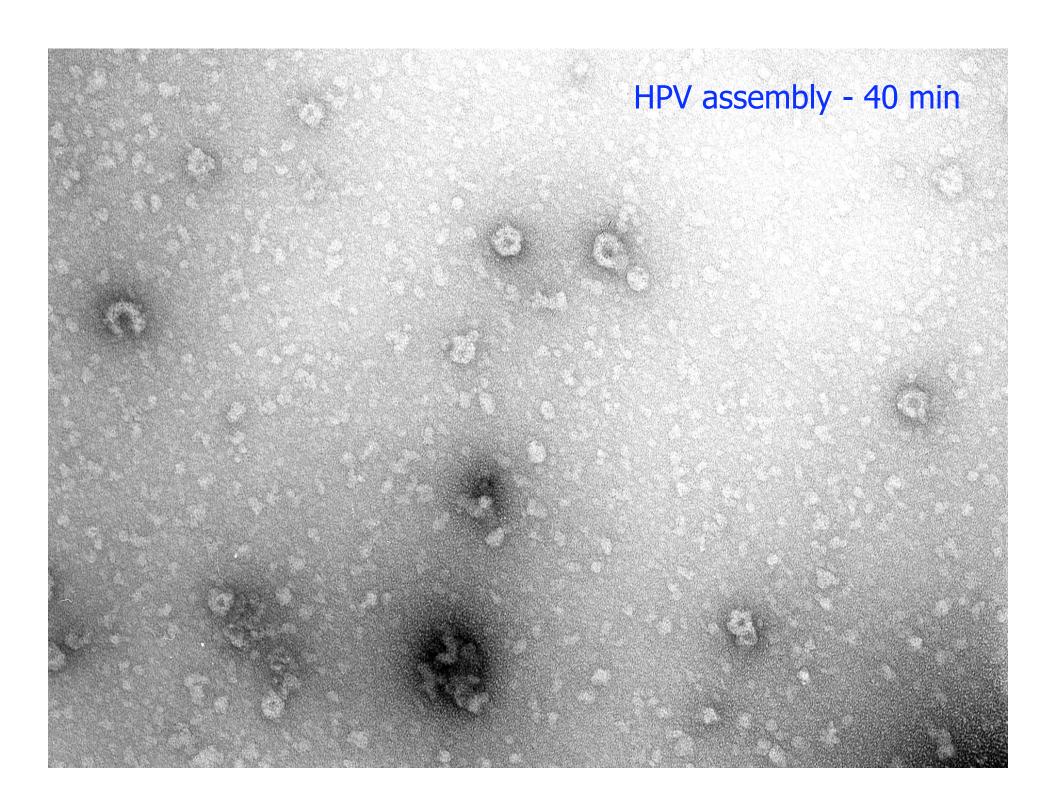
- Helical subdomain mediates 3-fold interpentameric hydrophobic contact
- Two conserved cysteines presumed to form interpentameric disulfide bonds during HVP capsid formation
 - Disulfide bonds in Polyoma are intrapentameric

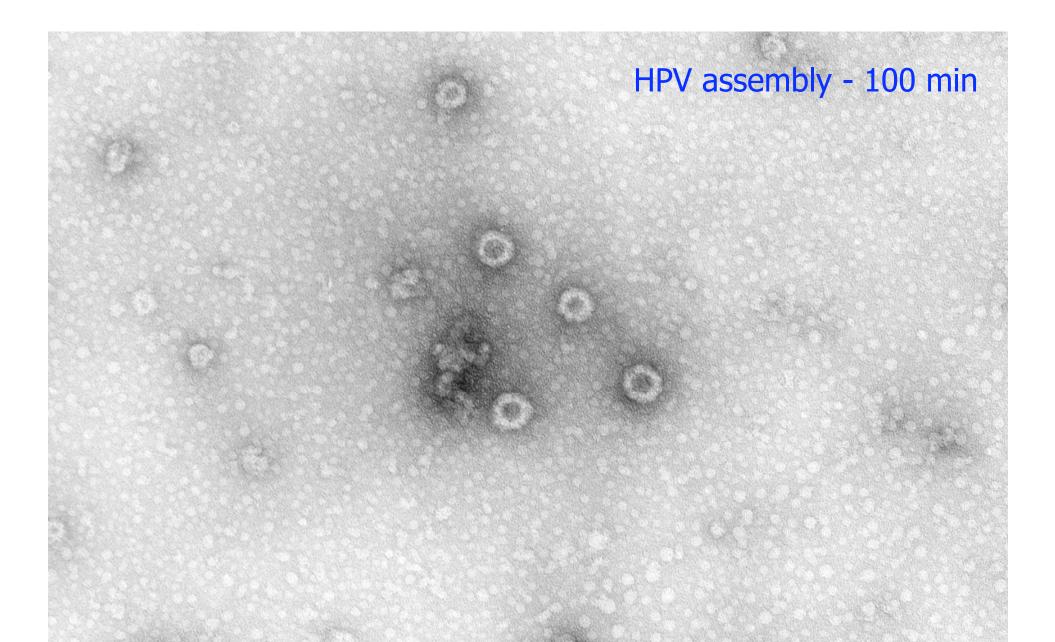


HPV Virus Like Particles Structure

- Human Papillomavirus
 - Major Capsid Protein L1 Type 11
 - Molecular Weight 55 kD
 - Capsomeres are L1 pentamers 275 kD
 - 60 Hexavalent Capsomeres
 - 12 Pentavalent Capsomeres
 - Arranged in a T=7 surface lattice
 - Virion Capsid 20 MD
 - 72 capsomeres = 360 protein units
 - Diameter 52nm

HPV assembly - 10 min

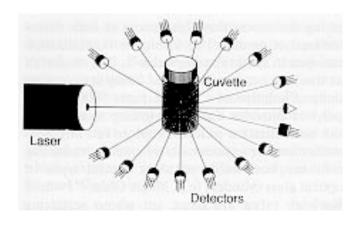






Experimental procedure

- Multi-Angle Light Scattering (MALS)
 - Procedure
 - Absolute MW and R_g
- Data collected
 - Various concentrations
- Analysis
 - Relative rates of assembly
 - Initial growth rate
 - Lag time



Procedure

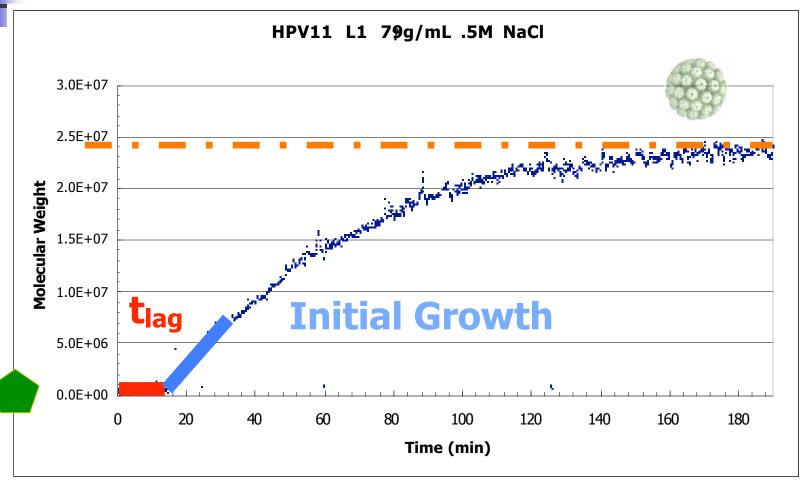
- Sample L1 protein is stored in a Tris buffer @ pH 8.0, 0.1M NaCl and a T=-70°C
- Protein introduced to acetate buffer @ pH 5.2 and 0.5M NaCl
- Assembly begins
- Afterwards, the concentration is determined by UV Spectrometry
 - Typical concentration: 20-200μg/mL
- Extrapolation to find molecular weight

$$\frac{R(\Theta)}{K^*c} = M_w \cdot [1 - \frac{16\pi^2 n_o^2 r_g^2}{3\lambda_o^2} \sin^2(\Theta/2)]$$

Wyatt, P., Analytica Chimica Acta, 272(1993)1-40

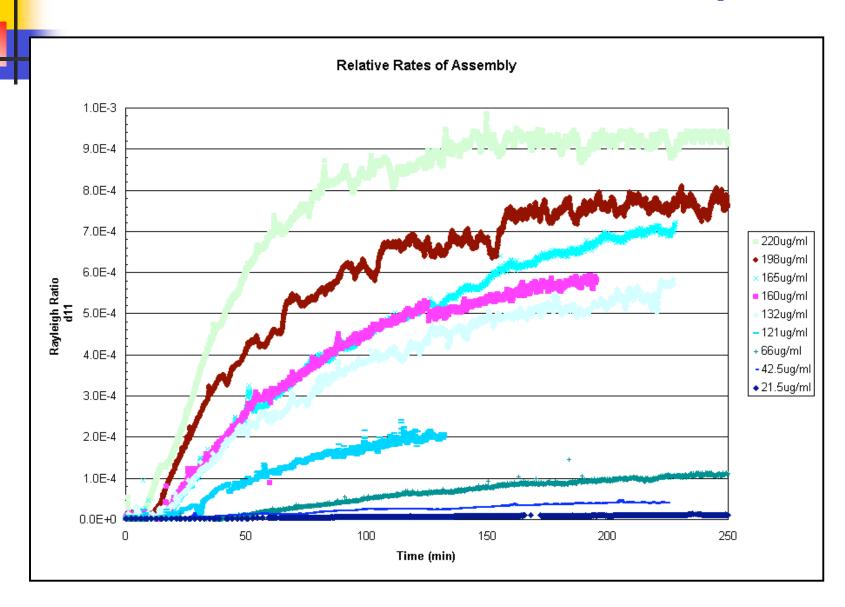


Avg MW growth during assembly



Assembly begun @ t=0

Relative rates of assembly





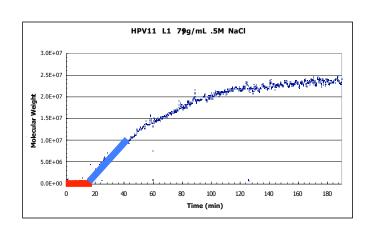
Interpretation of key kinetic features

I. Initial Growth

- What occurs during this period?
- What does the growth relate to?

II. Lag Time

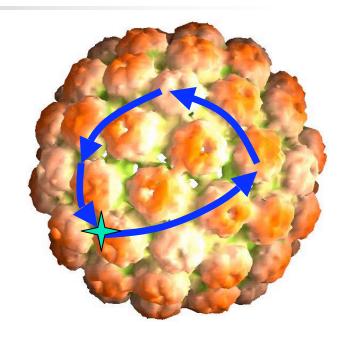
- What is it dependent on?
- Not as sharp in other studies

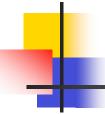




According to Mapquest...

 Comparison of experiment against sequential growth model (Zlotnick)





Modeling capsid assembly kinetics

- Tracking large number of reactions and intermediates difficult
- Simulation approaches
 - Kinetic Rate Laws
 - Dominant & Multiple Path Assembly
 - Molecular Simulation

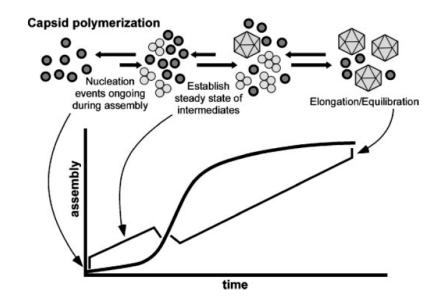


Kinetic rate law simulations

Simple kinetic simulations have been performed¹

subunits ⇔ nuclei + subunits ⇔ capsids

- Information obtained
 - Nucleation size
 - Nucleation rate
 - Contact ∆G
 - Elongation rate

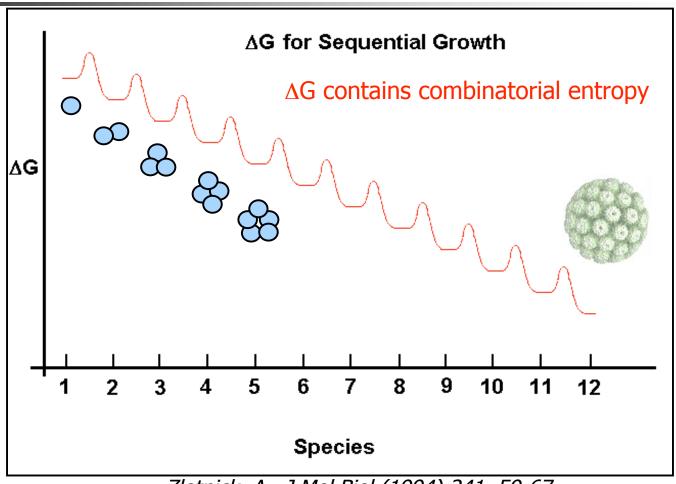


1 Zlotnick, J. of Mol. Recognit. 18, 479-490 2005

2 Zhang, T. et al, Biophys. J. 90 57-64 2006

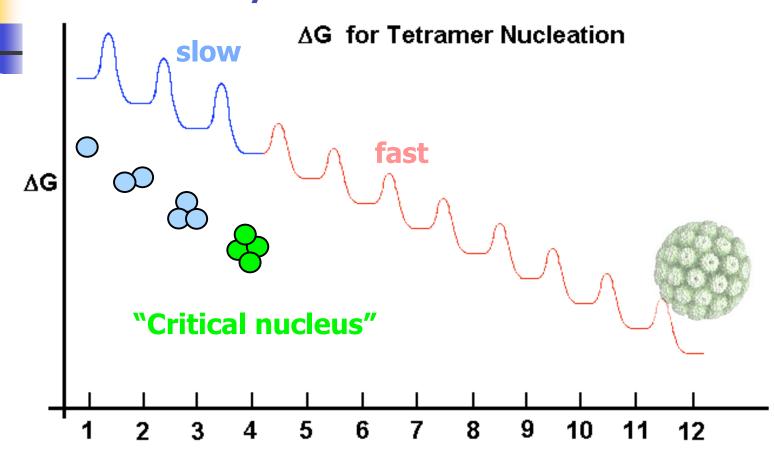
3 Schwartz R. et al, Biophys. J. **75** 2626-2636 1998

Dominant path "equilibrium" assembly



Zlotnick, A., J.Mol.Biol (1994) 241, 59-67 Flory, Paul, Principles of Polymer Chemistry, 1953

Kinetically limited "nucleation"



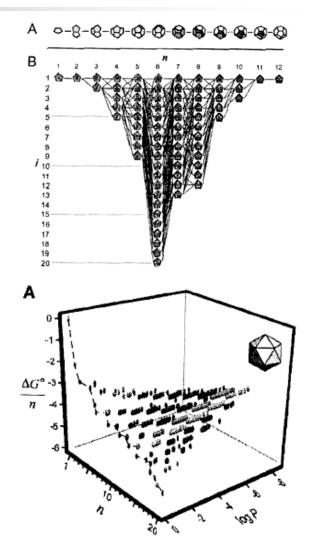
Species

Zlotnick, A. et al., Biochemistry (1999) 28, 14644. Endres and Zlotnick, Biophys. J. (2002) 1217.



Kinetic rate law simulation: multiple path assembly

- Reaction landscape enumeration^{1,2} for 12-mer
 - Access intermediates
 - Limited to simple systems
- Concluded dominant path was sufficiently accurate
- But 12-mer has no quasiequivalence
- Errors neglected



Sequential growth

Monomer Additions

$$C_{1} + C_{1} \stackrel{k_{1}, k_{-1}}{\longleftrightarrow} C_{2}$$

$$C_{2} + C_{1} \stackrel{k_{2}, k_{-2}}{\longleftrightarrow} C_{3}$$

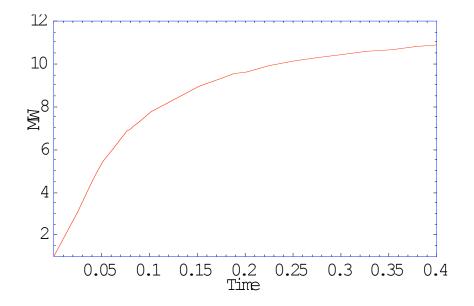
$$C_{3} + C_{1} \stackrel{k_{3}, k_{-3}}{\longleftrightarrow} C_{4} \dots$$

$$C_{11} + C_{1} \stackrel{k_{11}, k_{-11}}{\longleftrightarrow} C_{12}$$

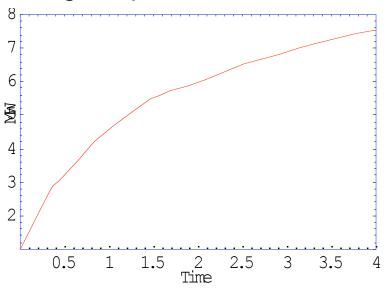
Zlotnick, A., J. Mol. Biol. (1994)241,59-67

Dominant pathway assembly

- Equilibrium
- $k_{forward} = 10^8$



- Kinetic Limiting Trimer
- $k_1 = k_2 = 10^6$
- $k_3 = k_4... = 10^8$



Lag times tend to be rounded, especially in MW curves

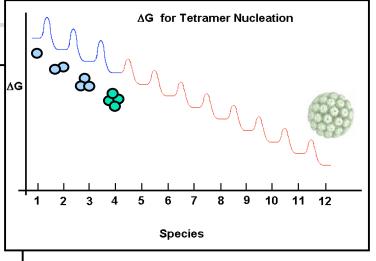
What controls the initial slope?

$$\frac{d[nucleus]}{dt} = k_n[subunit]^N$$

$$[nucleus] \propto [capsid] \propto MW_w$$

$$(slope of MW_w) = k_n \cdot [C_o]^N$$

$$\log(rate of LS) = \log(k_n) + N \log[C_o]$$

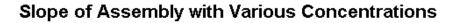


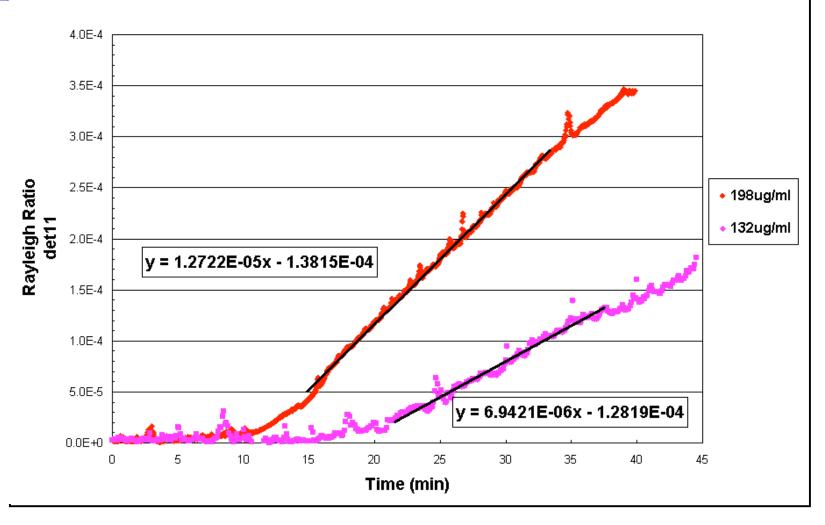
Note: Zlotnick proposed more accurate estimators of the nucleus size based on number of capsids at a given time.

Our curves are quite linear, and so the two give similar results.

Zlotnick,A., J. Mol. Biol. (1994) 241,59-67, Prevelige,P.,Biophysical Journal, (1993) 64, 824-835

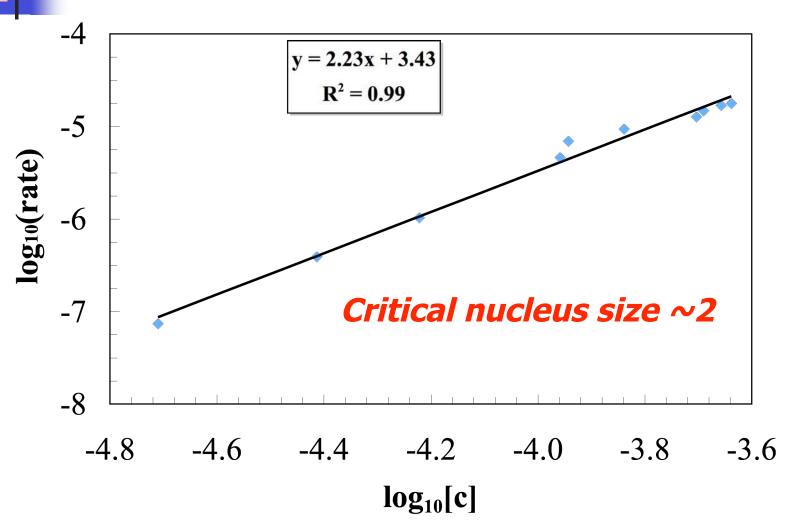
Slope of assembly rate





4

Critical nucleus is a dimer

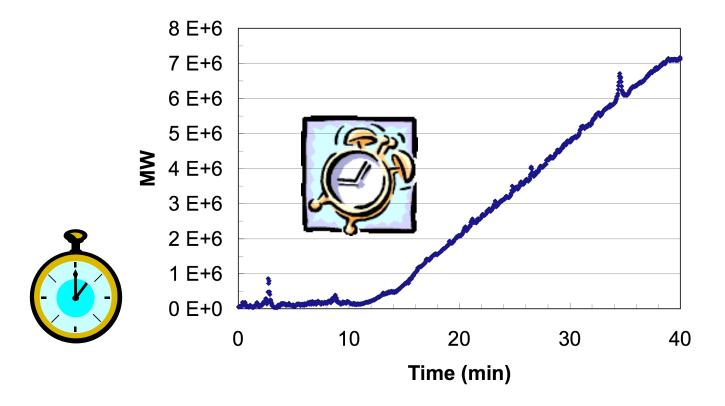




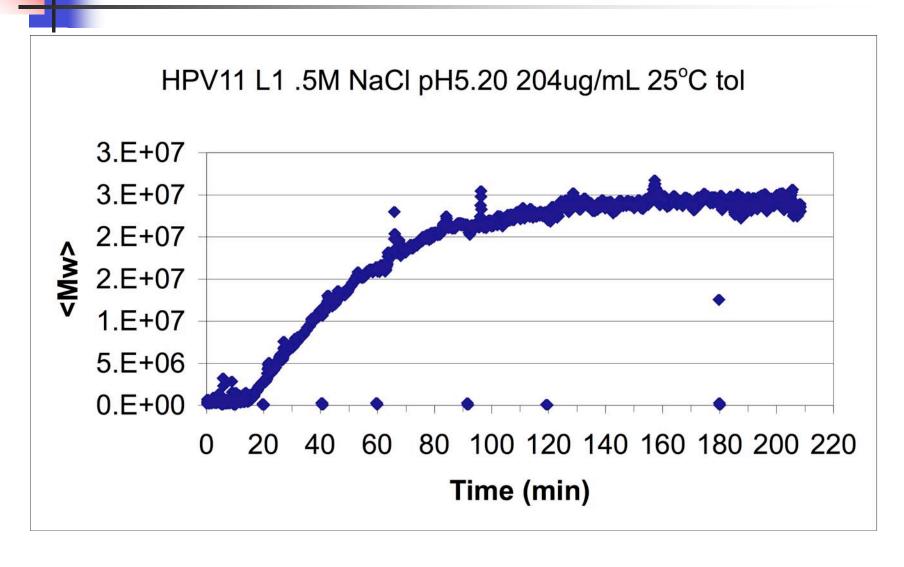
- Perhaps transient nucleation is sharp
- Other kinetic mechanistic explanations?

Question...

What type of mechanism shows a rapid increase after a reproducible lag?

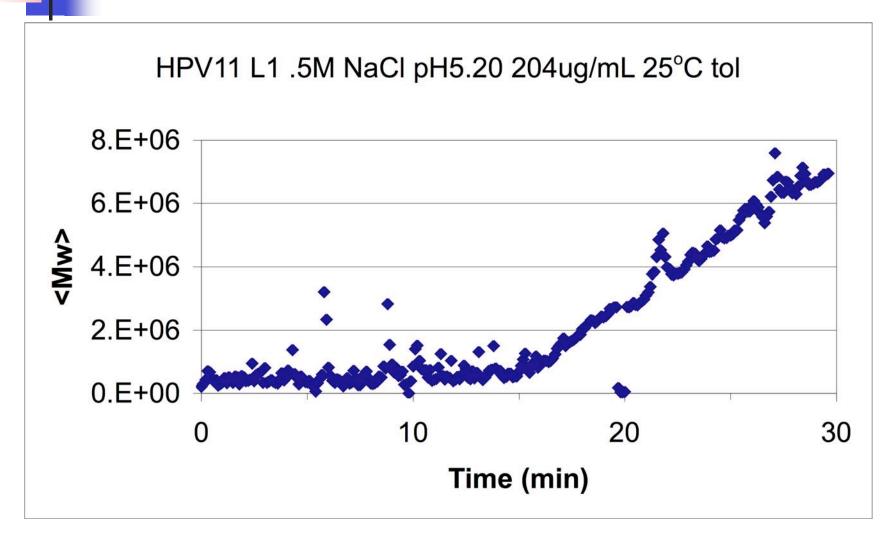








Lag time close up

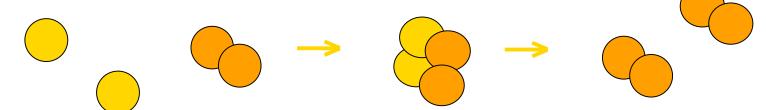


Autocatalysis

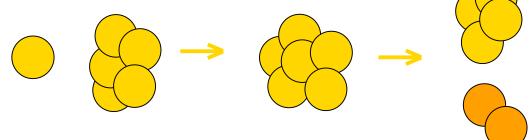
- Explains the sudden growth
- Supported by monomer binding

Variations on autocatalysis

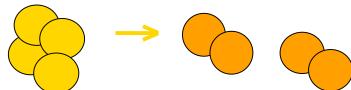
Dimer as an enzyme



Splintering



Fragmentation



Could help explain error correction

Possible mechanism

Nucleation – low rate constant

$$C_1 + C_1 \stackrel{k_1, k_{-1}}{\longleftrightarrow} C_2$$

Autocatalysis – medium rate constant

$$2C_1 + C_2 \stackrel{k_a, k_{-a}}{\longleftrightarrow} 2C_2$$

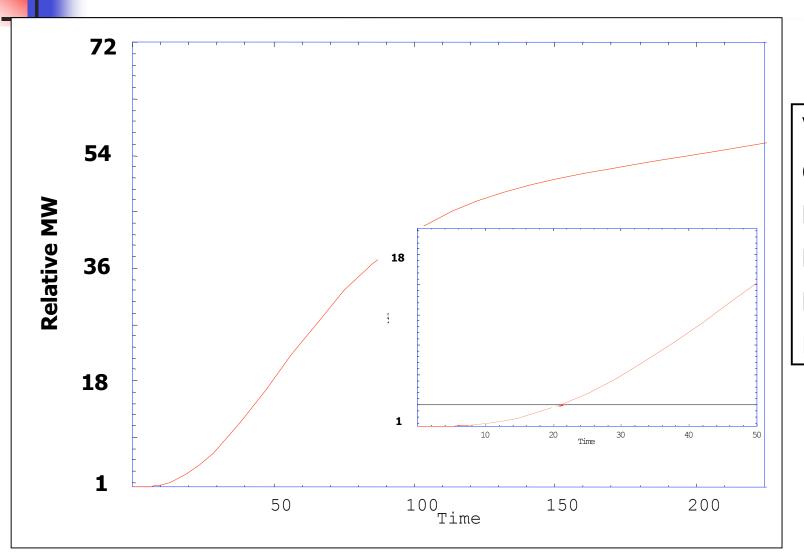
■ Growth – high rate constant

$$C_{2} + C_{1} \stackrel{k_{f}, k_{r}}{\longleftrightarrow} C_{3}$$

$$C_{3} + C_{1} \stackrel{k_{f}, k_{r}}{\longleftrightarrow} C_{4} \dots$$

$$C_{71} + C_{1} \stackrel{k_{f}, k_{r}}{\longleftrightarrow} C_{72}$$

Model prediction of MW



Values:

 $C_0 = .0002$

 $k_1=1$

 $k_a = 10^3$

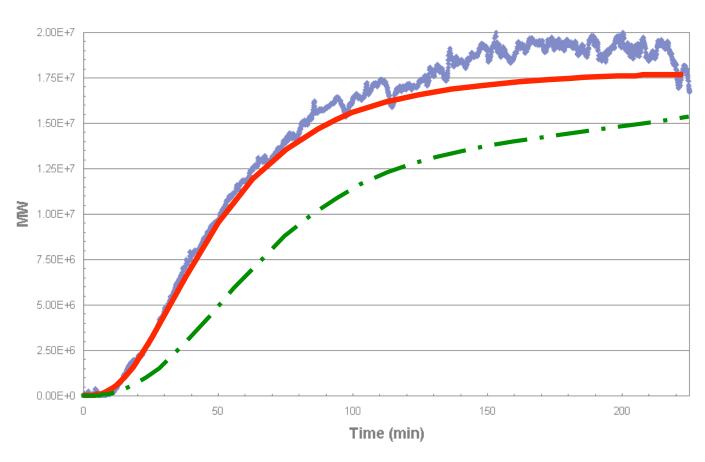
 $k_f = 10^4$

 $K_{eq} = 10^5$



Fit to experiment





Values:

$$k_1=1$$

$$k_a = 10^8$$

$$k_f = 10^4$$

$$K_{eq} = 10^5$$

Values:

$$k_1=1$$

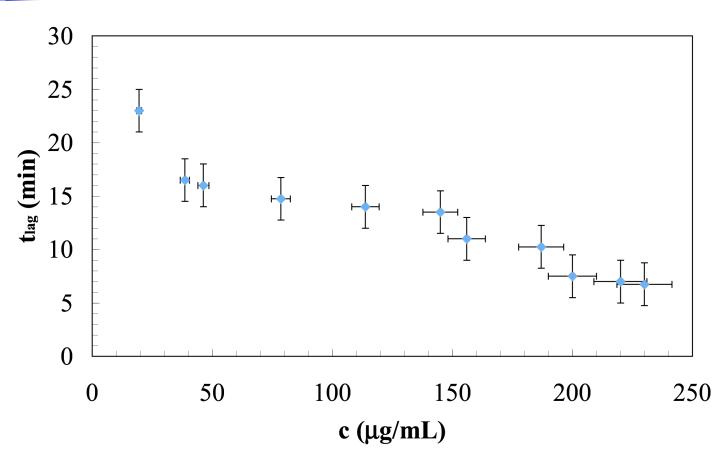
$$k_a = 10^3$$

$$k_f = 10^4$$

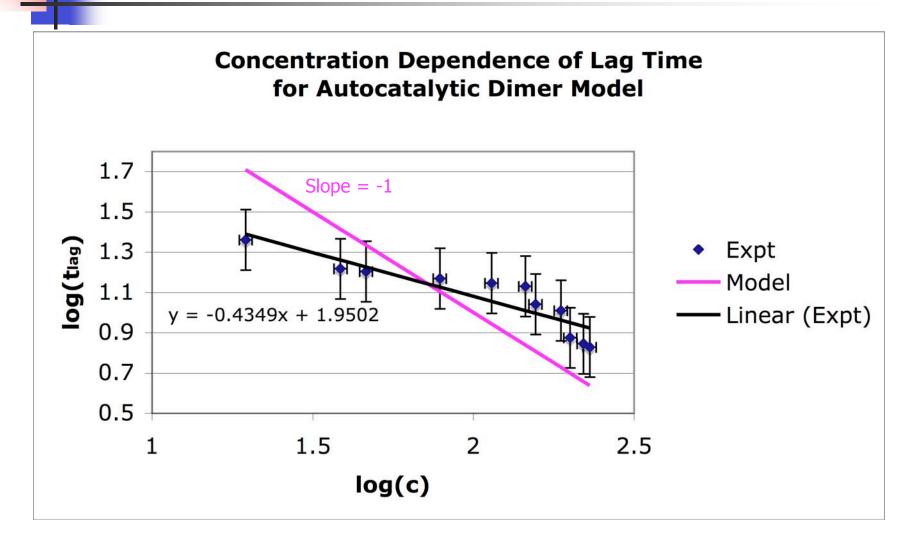
$$K_{eq} = 10^5$$



Concentration dependence



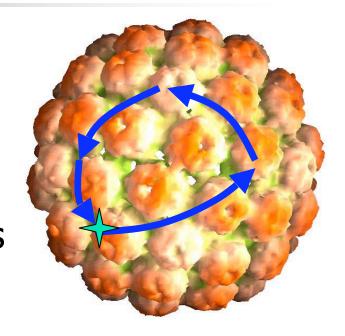






Places to visit next....

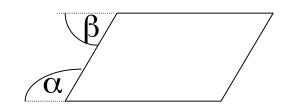
- This map may need more dimensions
- Error correction for quasiequivalent structures





Toy model for error correction

- 2D polygonal "capsid"
 - Different local binding conformations



- Check for closing contact
- Approximate check for overlap: exterior angles sum to < 360°
- Does the existence of "errors" qualitatively change assembly kinetics?
- If so, how are errors controlled?

Kinetic rate law model

<u>Chemical Reactions</u> \Longrightarrow <u>Reaction Formulas</u> \Longrightarrow <u>Reaction Rates</u>

Step #1

$$+$$
 k_f or or

step #1
$$H + H \xrightarrow{k} \alpha$$
or
$$H + H \xrightarrow{k} \beta$$

$$\frac{d}{dt}[H] = -\left(4kH[t]^2 + k[\alpha][H] + k[\beta][H]\right)$$

$$\frac{d}{dt}[\alpha] = k[H]^2 - 2k[\alpha][H]$$

$$\frac{d}{dt}[\beta] = k[H]^2 - 2k[\beta][H]$$

$$\angle$$
 + \angle k_r or k_r

step #2 a
$$\alpha + \Pi \xrightarrow{k} \alpha \alpha$$
or
$$\alpha + \Pi \xrightarrow{k} \alpha \beta$$

$$\frac{d}{dt} [\alpha \alpha] = -k[\alpha][H]$$

$$\frac{d}{dt} [\alpha \beta] = -k[\alpha][H]$$

$$\frac{d}{dt} [\beta \alpha] = -k[\beta \alpha][H]$$

$$\frac{d}{dt} [\beta \beta] = -k[\beta \beta][H]$$

Step #2b

$$+$$
 k_r

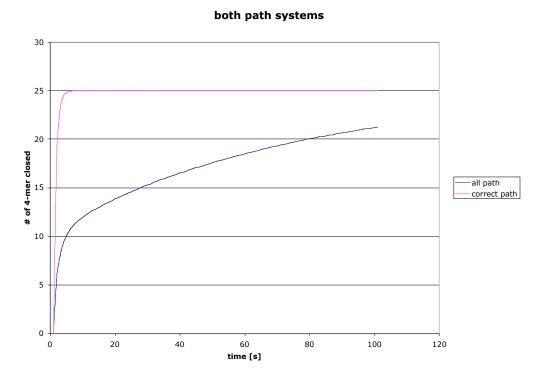
step #2 b
$$\beta + \Pi \xrightarrow{k} \beta \alpha$$
or
$$\beta + \Pi \xrightarrow{k} \beta \beta$$

Evaluate multitude of reactions by stochastic MC



Possibility of errors produces 2 stage assembly

- Initial rapid assembly
- Slow conversion of incorrect structures
- Slow in comparison with Dominant Path mechanism
 - Using same rate constants





Depth of error matters

Two rhombi compared:

•
$$\alpha = 11^{\circ}, \beta = 169^{\circ}$$

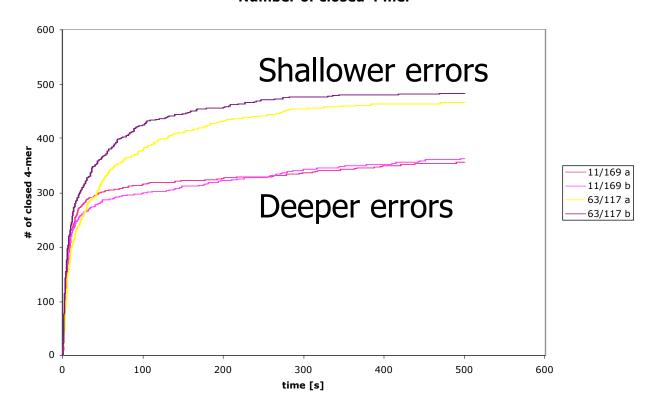
•
$$\alpha = 63^{\circ}$$
, $\beta = 117^{\circ}$

Two reverse rates compared:

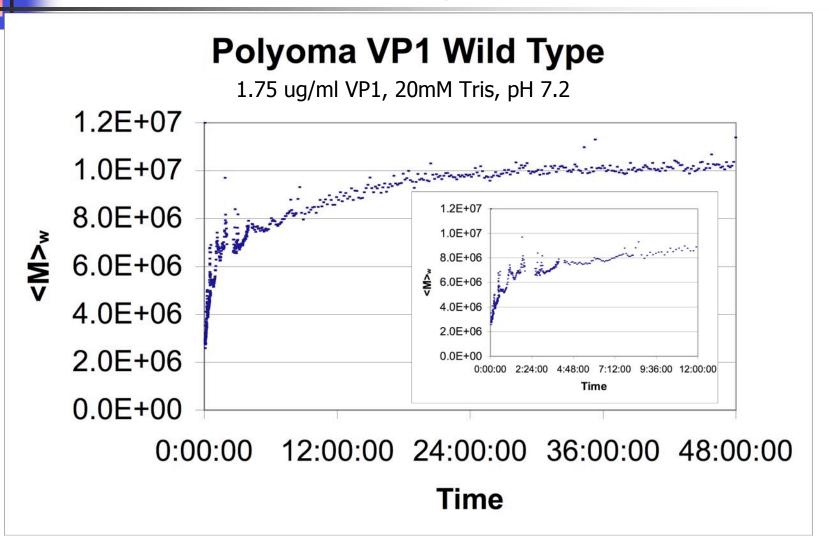
■
$$a \rightarrow k_r=1$$

■
$$b \rightarrow k_r = 2$$

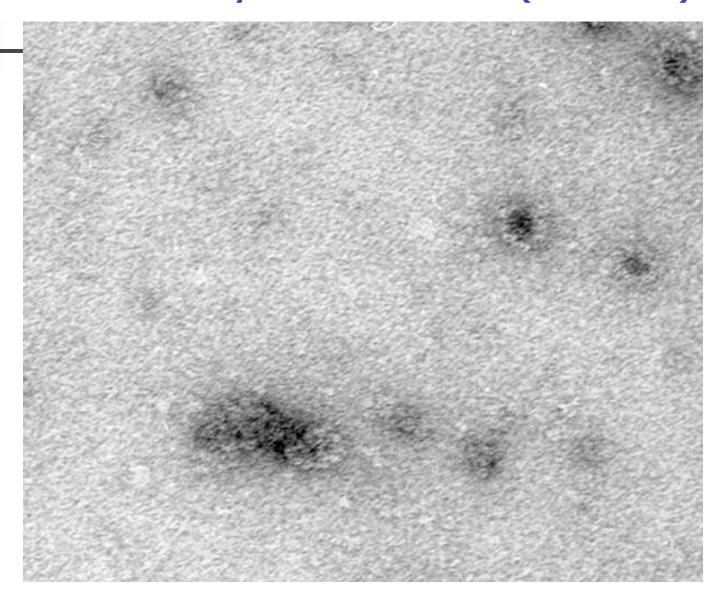
Number of closed 4 mer



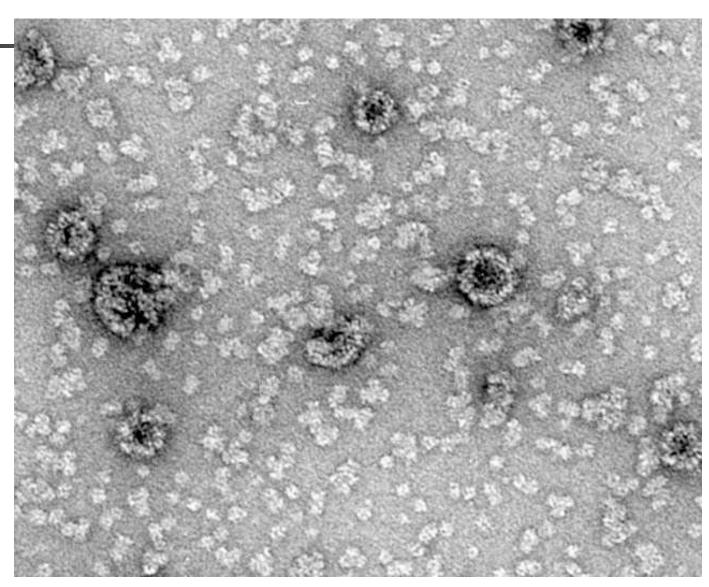
Polyoma assembly shows two-stage kinetics



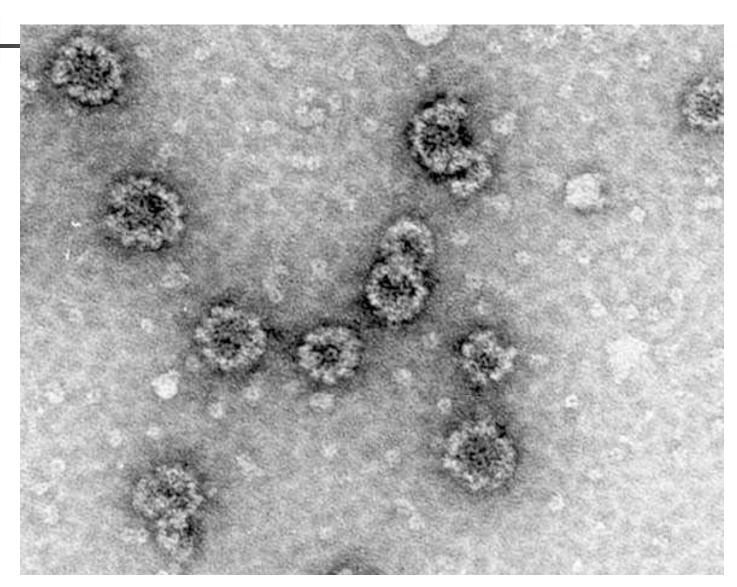
VP1 Assembly at 1M Salt (10 min)



VP1 Assembly at 1M Salt (1 hr)



VP1 Assembly at 1M Salt (1 day)





- Experiments support a critical nucleus of a dimer for HPV assembly within nucleated dominant path mechanism
- Autocatalysis is a possible mechanism to explain the experimental lag time
- Model suggests, that once dimers are made, assembly to capsids proceed via an autocatalytic mechanism of those dimers

Conclusions

- Concentration dependence of lag time in the model does not fit experiment
- However, this dependence is a function of the specific autocatalysis mechanism
- Off-pathway assembly may be important
- Error correction for quasiequivalence
 - 2D Toy model shows error depth matters
 - In 3D, cooperative (e.g. strain) may limit error depth



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- University of Colorado Health Sciences Center
 - Robert Garcea
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 - David Graham (PhD)
- Undergraduate Students
 - Travis Jones
 - Shaun Bevers