

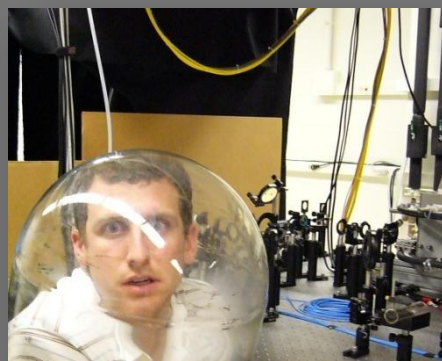
# Disordered Insulator in an Optical Lattice

Brian DeMarco

University of Illinois at Urbana-Champaign



Josh Zirbel



Matt Pasienski



David McKay



Stan Kondov



David Chen



Carrie Meldgin



Will McGehee



Paul Koehring

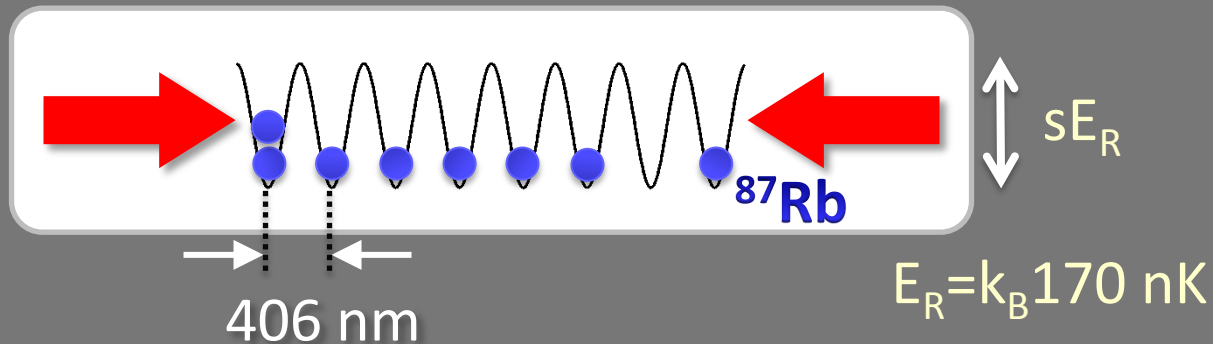
# Outline

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- Disordered Bose-Hubbard model
- Creating a disordered lattice
- Transport measurements: SF–IN transition
- Updates:  
compressibility, spin-dependent lattices

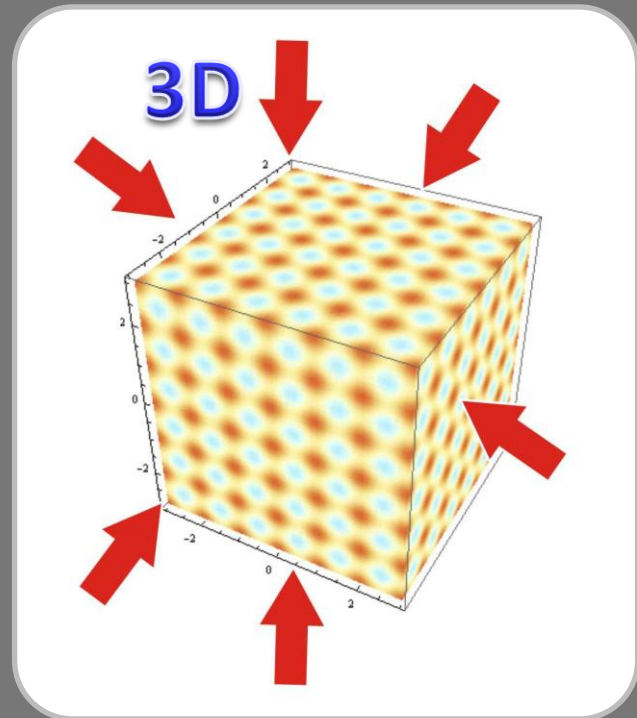
**1 atom / site in the center of the lattice**

# Optical lattices: clean BH model

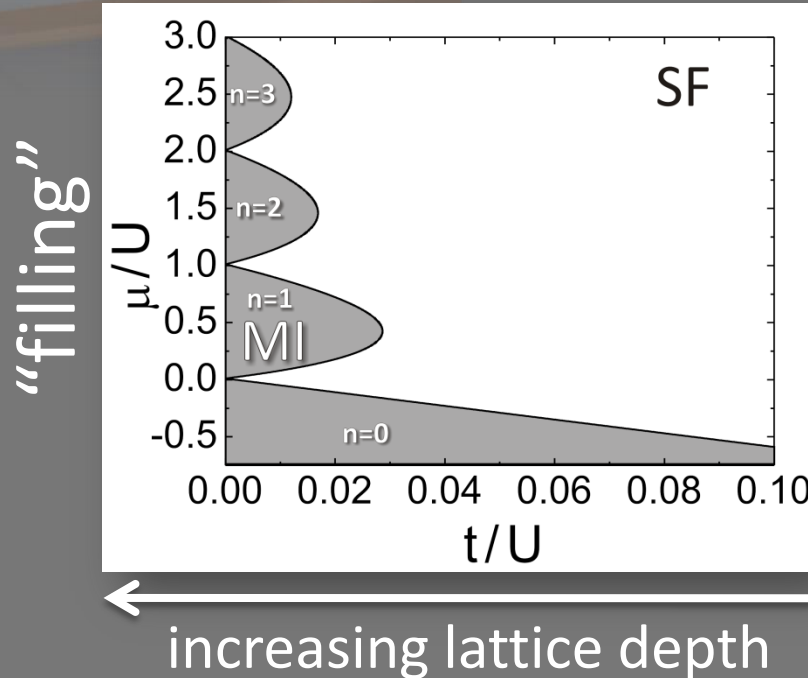
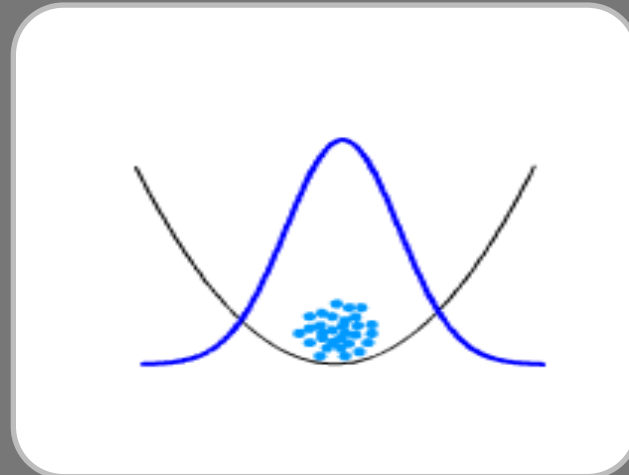
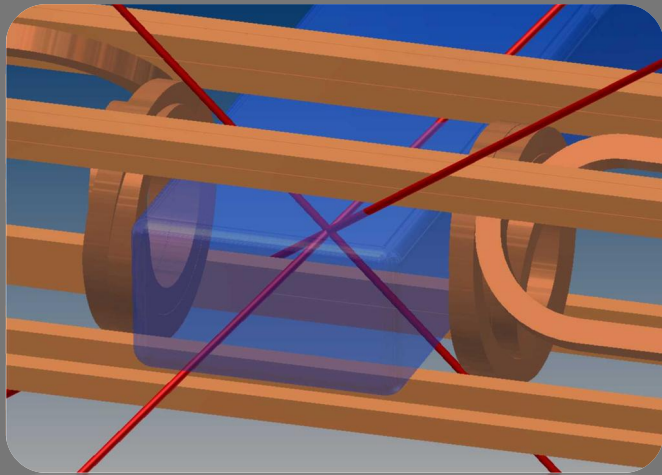


$$H = -t \sum_{\langle ij \rangle} (b_i^\dagger b_j + b_j^\dagger b_i) + \frac{U}{2} \sum_i n_i (n_i - 1)$$

$t/U$  controlled by lattice depth



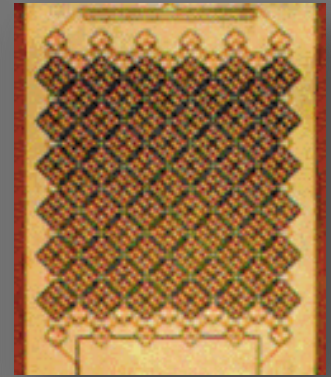
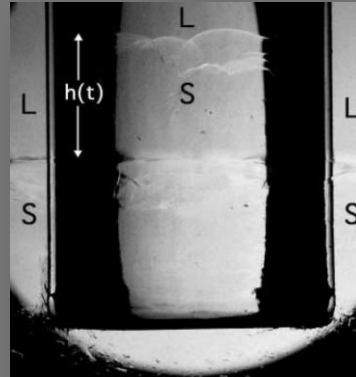
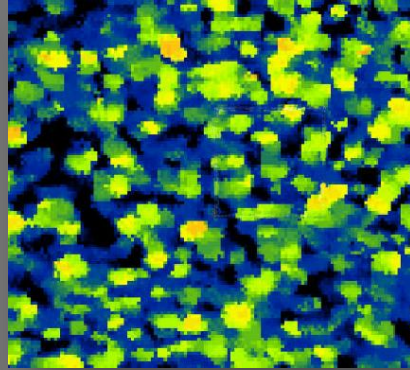
# Clean BH model



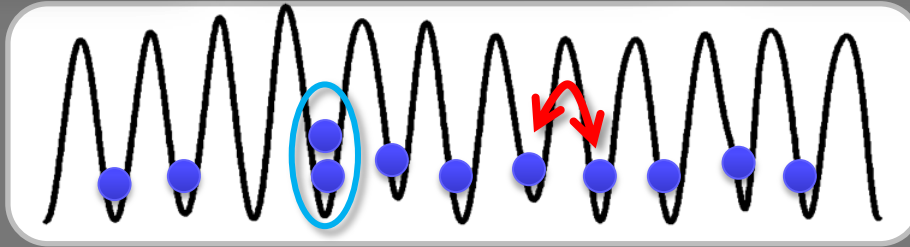
- Weak lattice:
- Superfluid (SF)
- Strong lattice:
- Mott-insulator (MI)

# The Disordered BH model

## Disordered bosonic materials



disordered  
lattice



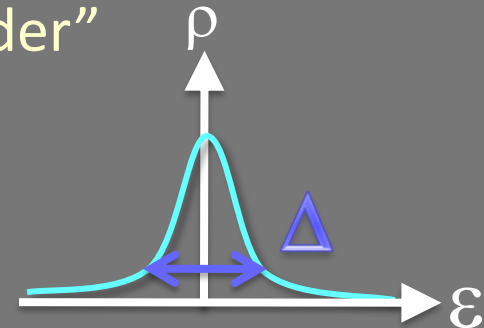
$\varepsilon_i$ : site energies  
“diagonal disorder”

$U_i$ : interaction energy

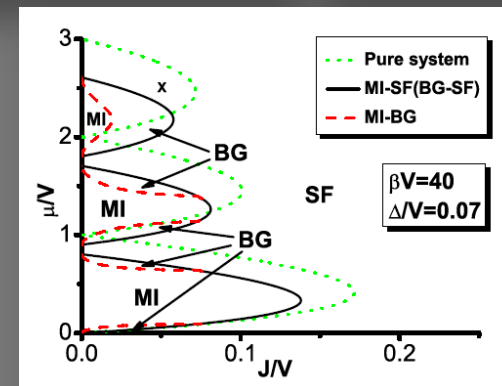
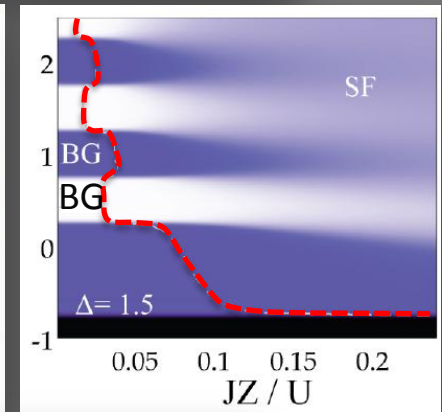
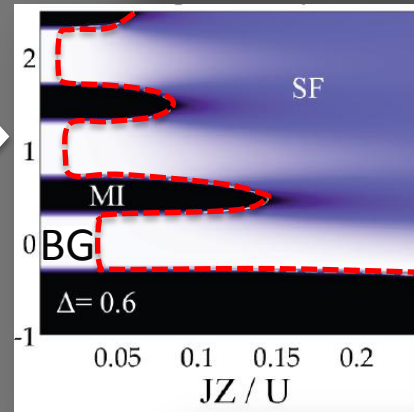
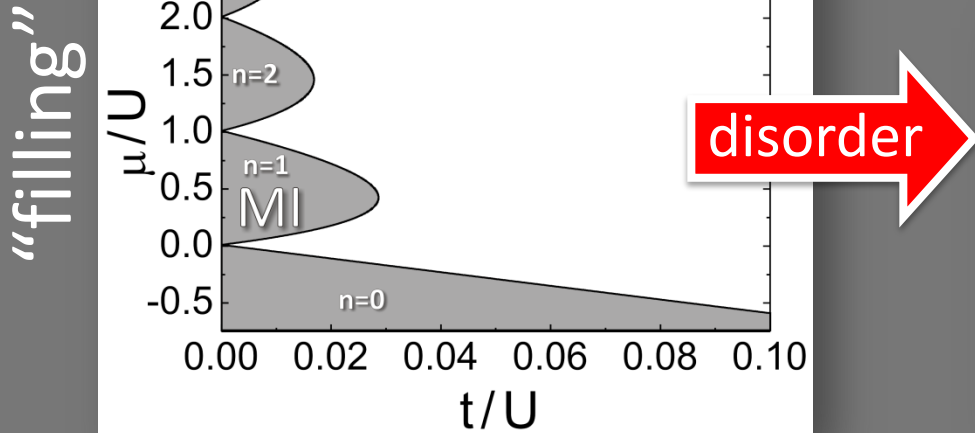
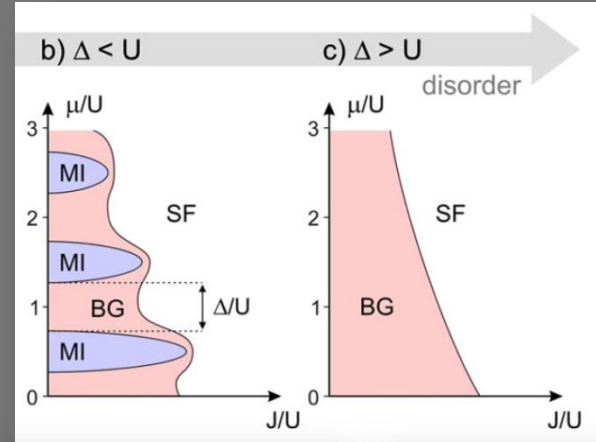
$t_{ij}$ : tunneling energy

“off-diagonal disorder”

$$H = \sum_i n_i \varepsilon_i - \sum_{\langle ij \rangle} t_{ij} (b_i^\dagger b_j + b_j^\dagger b_i) + \frac{1}{2} \sum_i U_i n_i (n_i - 1)$$



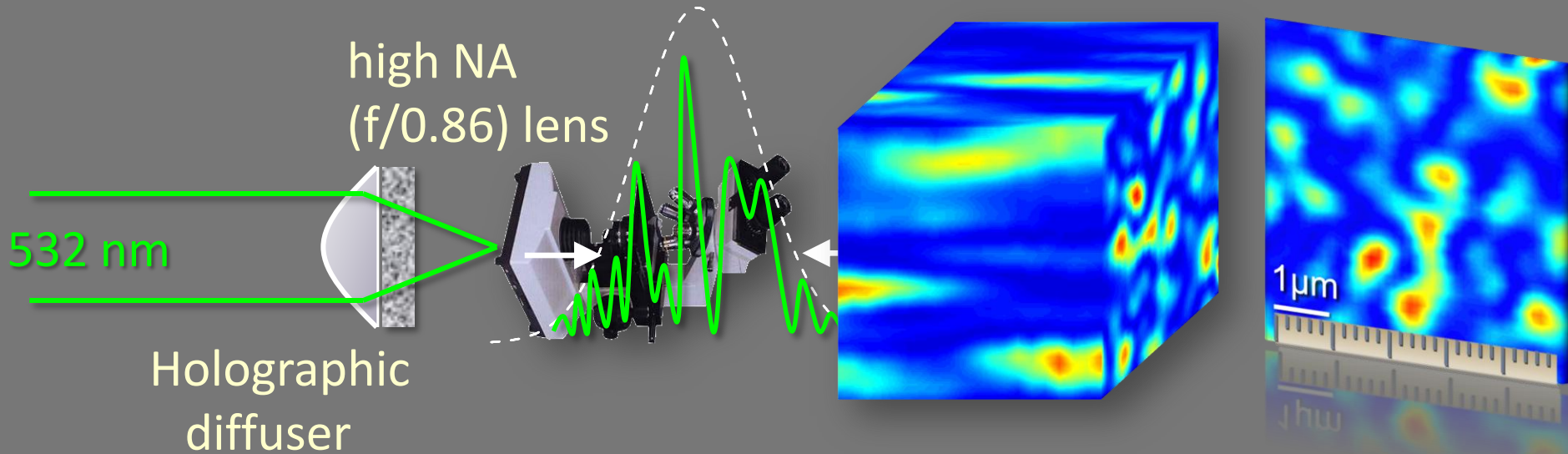
# Disordered BH model: theory



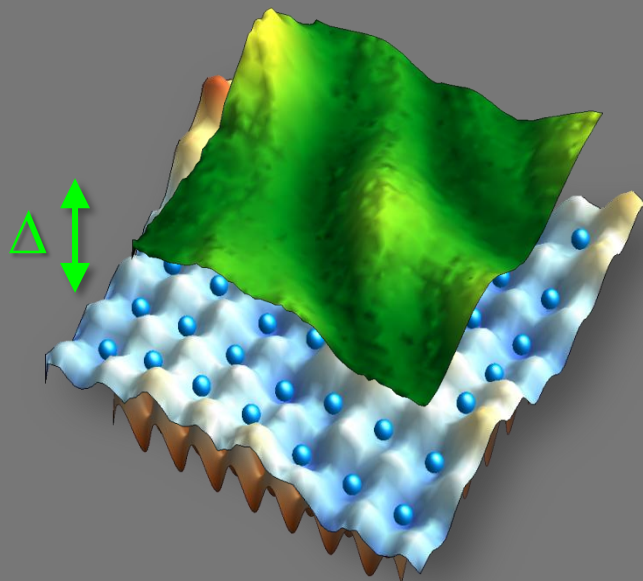
← increasing lattice depth

SF: superfluid MI: Mott-insulator  
 BG: Bose-glass (gapless, compressible IN)  
 MG: Mott-glass (gapless, incompressible IN)

# Controllable disorder: speckle



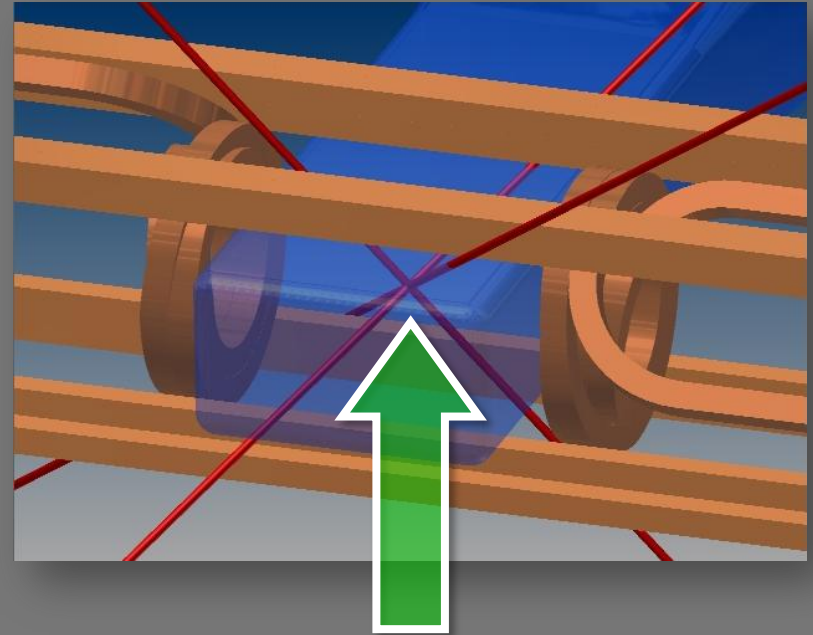
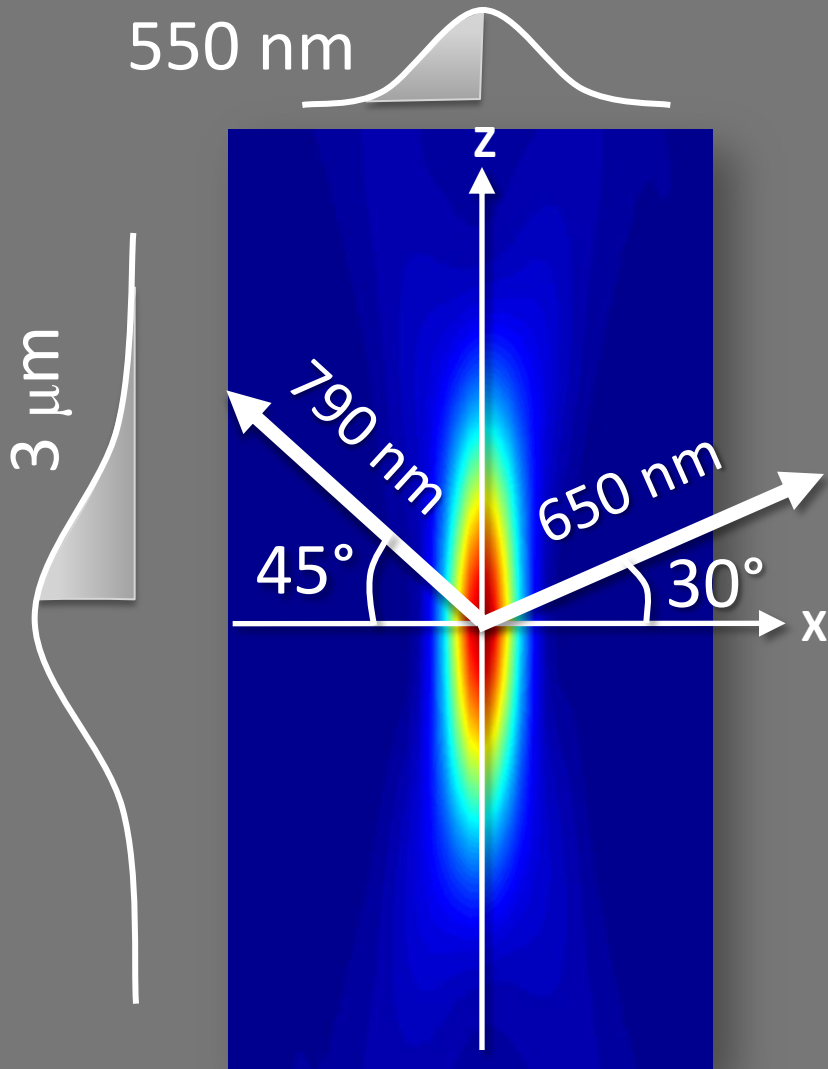
**Known disorder!**



Potentials add to  
produce disordered lattice

*Aspect, Ertmer, Engels\*, Hulet, Inguscio...*

# Fine-grain 3D disorder



Fine grained disorder:

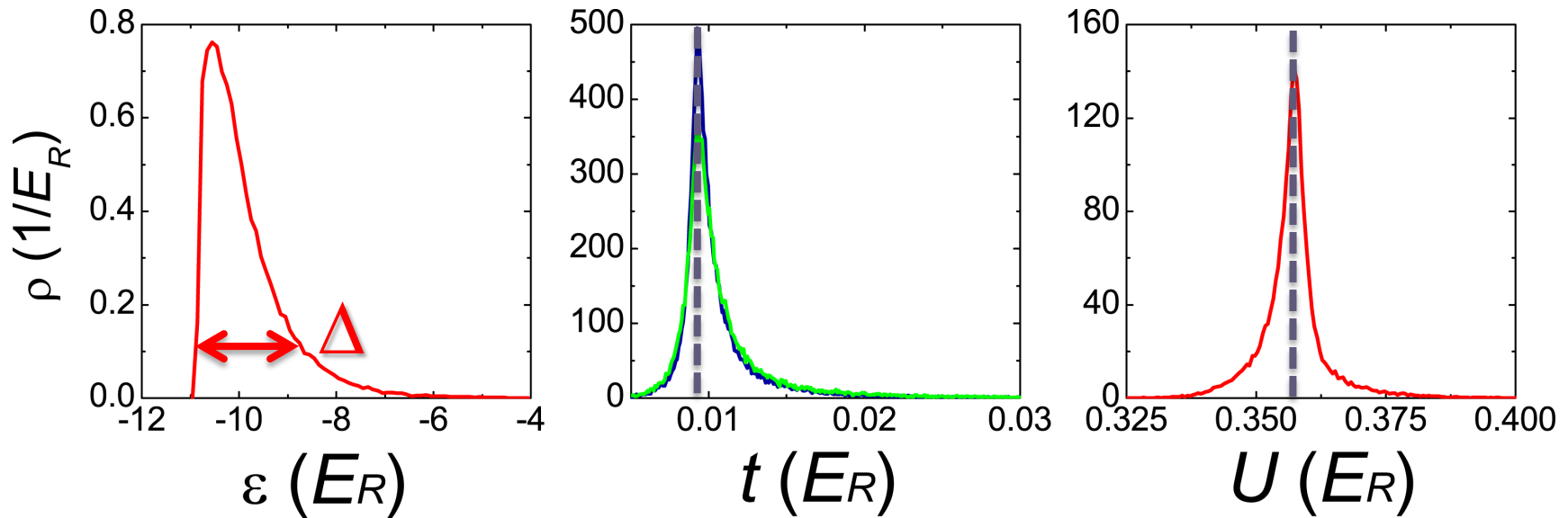
- Assumed in theory
- Required to realize disorder in  $t$  and  $U$

$$\langle I(\vec{x}) I(\vec{x} + \vec{r}) \rangle$$



# BH parameters

Calculation by Ceperley's group using known potential



Disordered "material" in which microscopic disorder completely determined

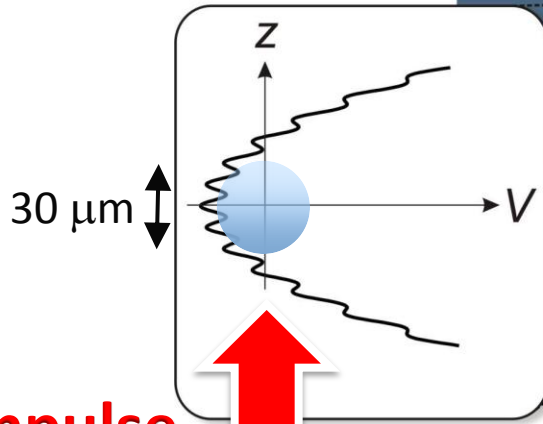
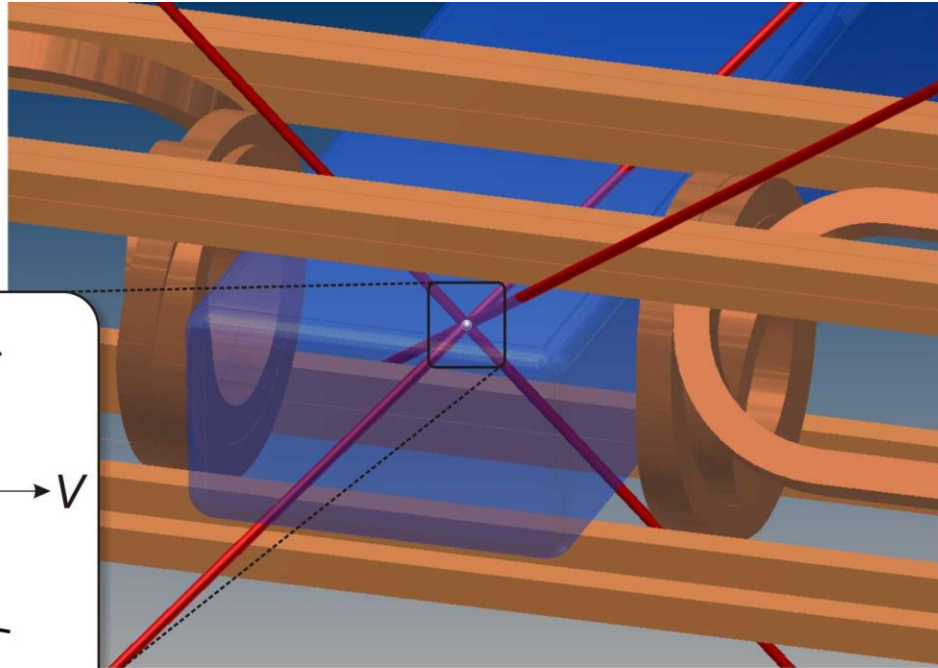
# Transport Measurements

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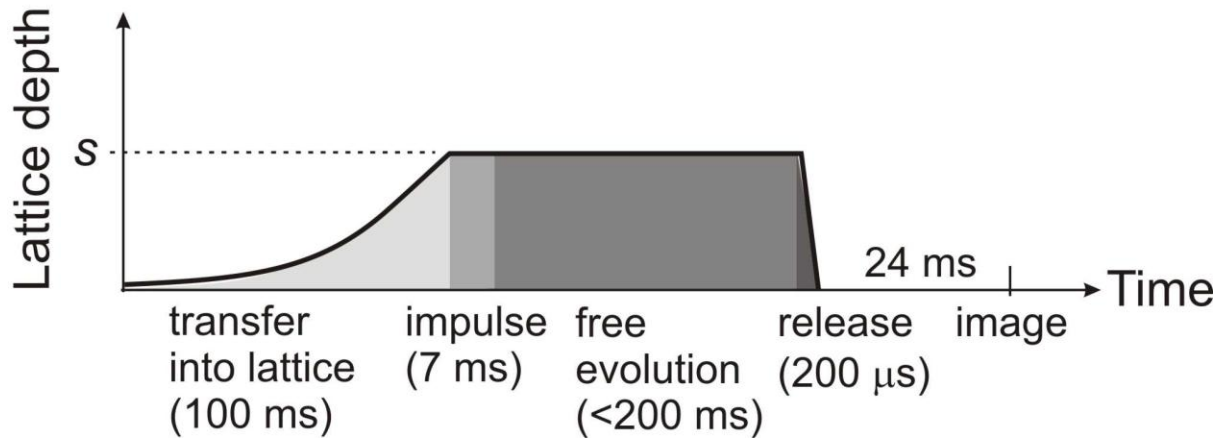


resistivity  $\rho \propto \frac{V}{I}$

# Transport



**Impulse**

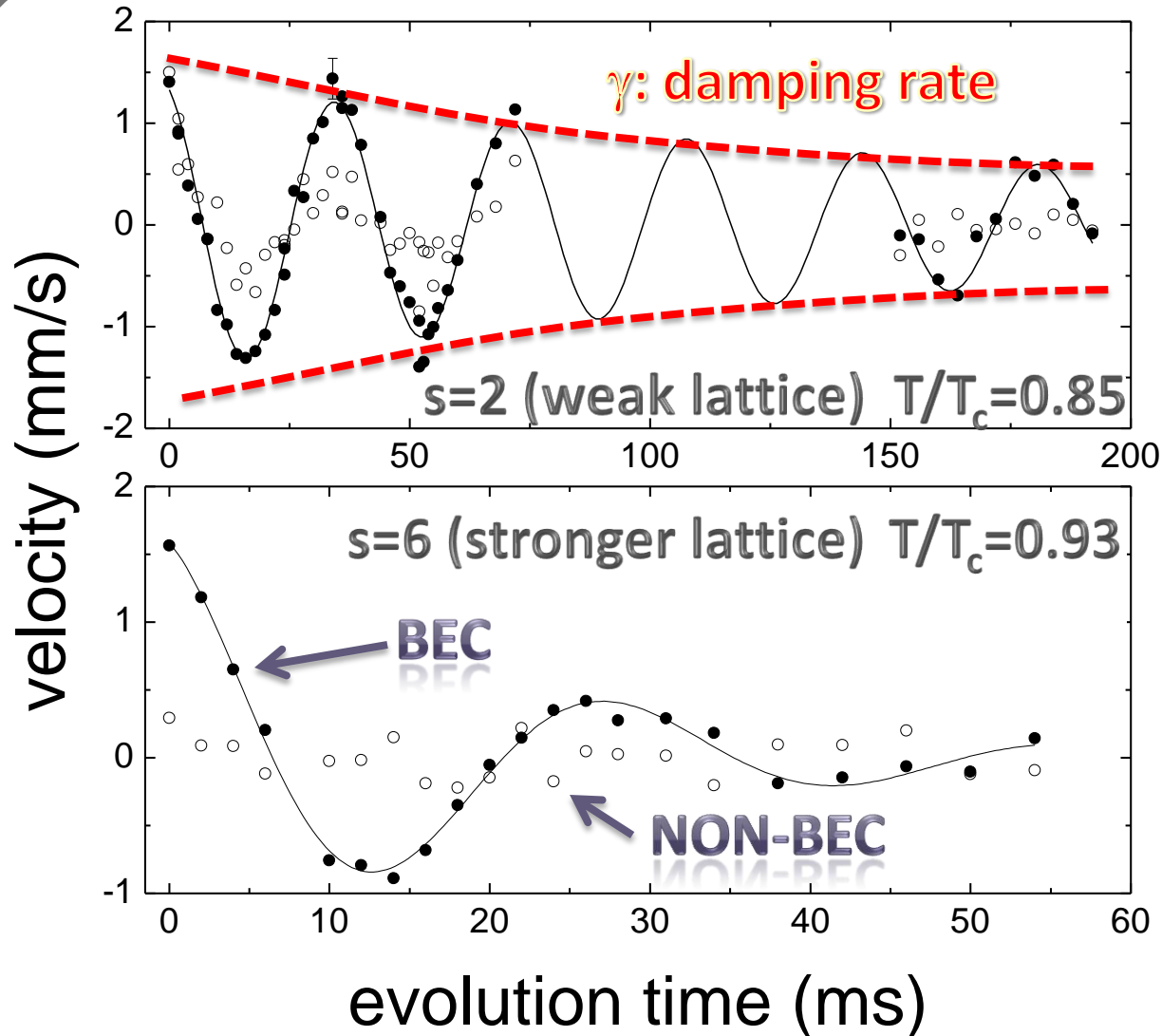


# Motion

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# Observable: center-of-mass velocity



We measure:

- Damping rate (resistance)

We change:

- Lattice depth ( $t/U$ )
- Temperature
- Disorder strength

# Clean system: phase slips

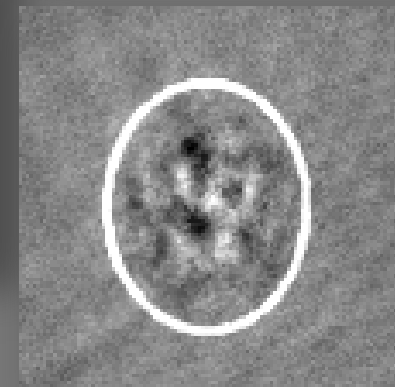
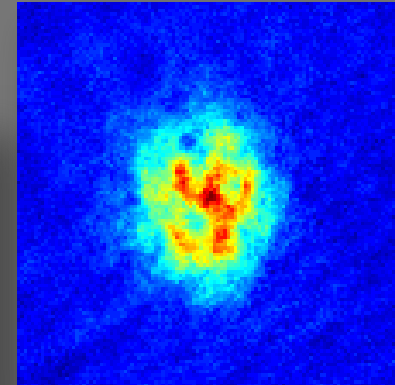
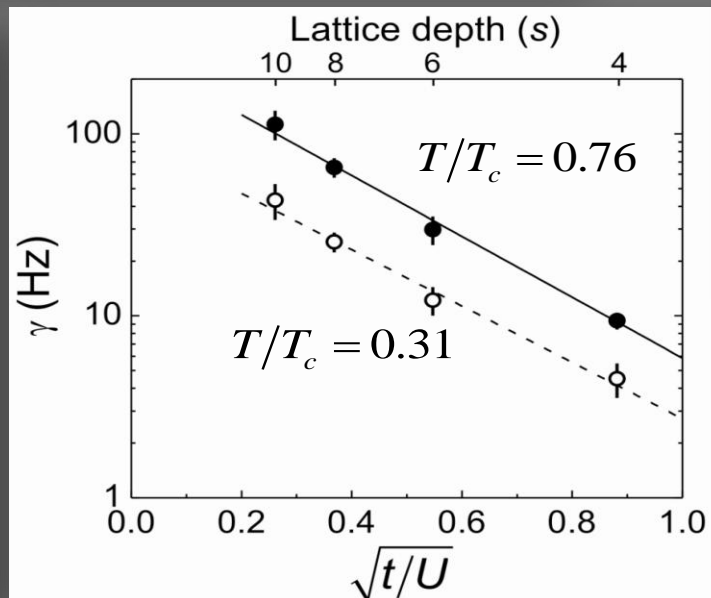
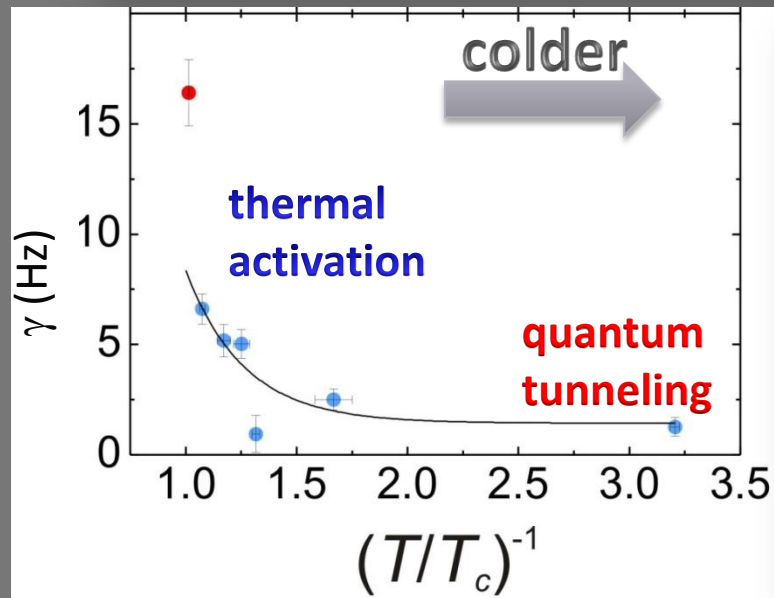
nature

Vol 453 | 1 May 2008 | doi:10.1038/nature06920

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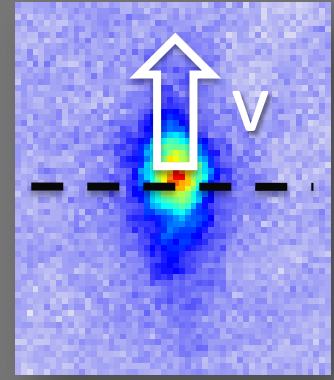
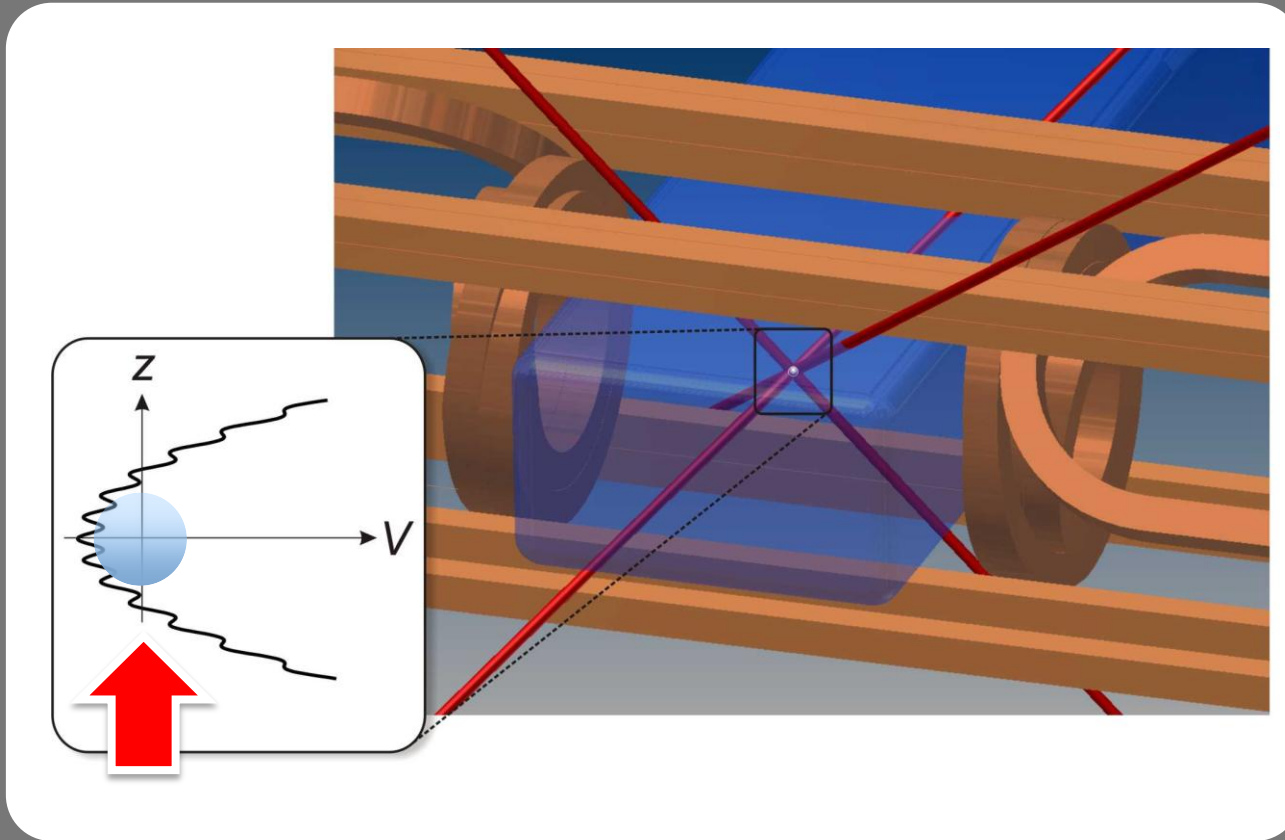
## Phase-slip-induced dissipation in an atomic Bose-Hubbard system

D. McKay<sup>1</sup>, M. White<sup>1</sup>, M. Pasienski<sup>1</sup> & B. DeMarco<sup>1</sup>



# Resolving an insulator

Apply impulse, measure total center-of-mass velocity

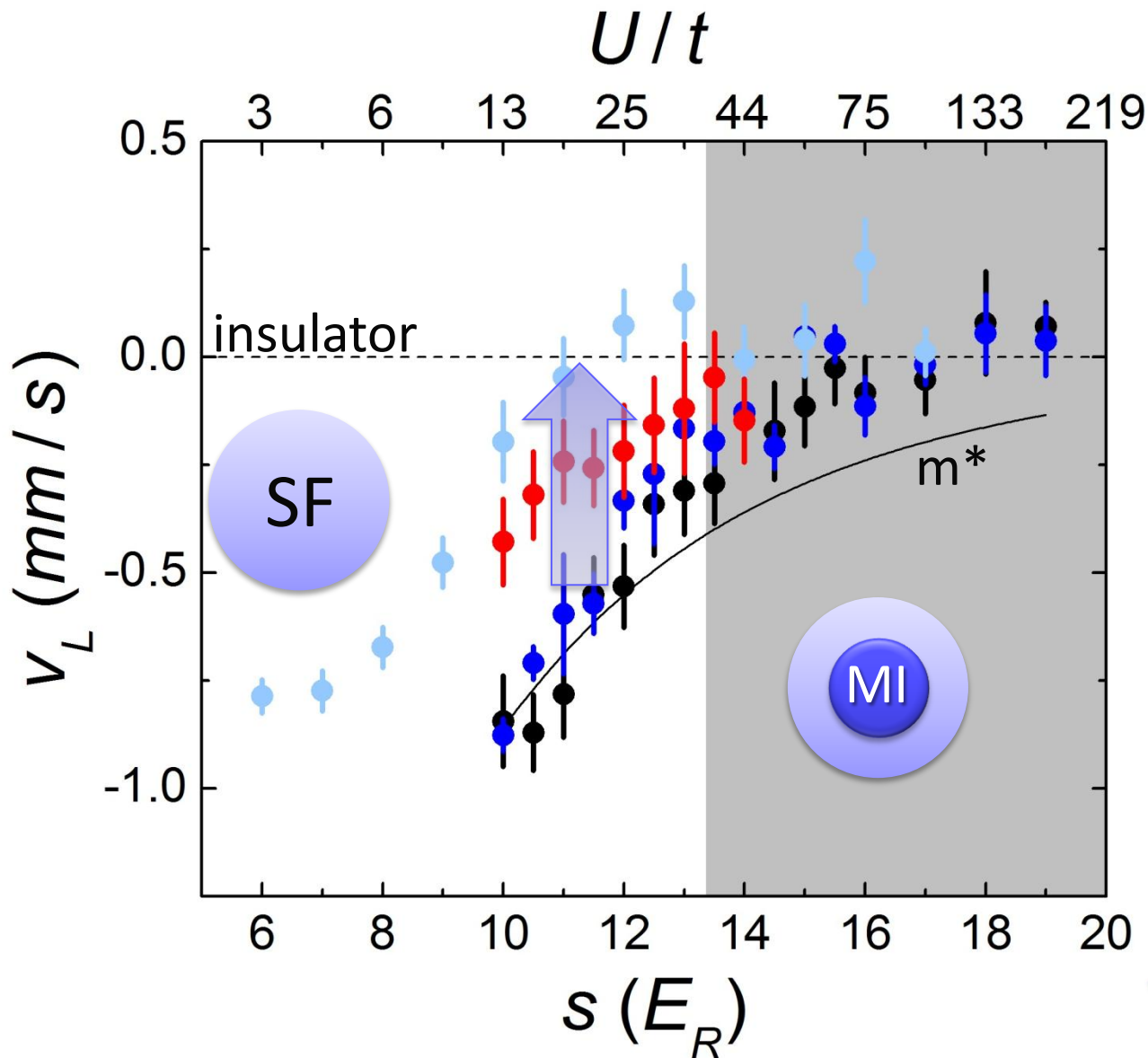


$$v_0 = \frac{N_C v_C + N_{NC} v_{NC}}{N}$$

For a damped,  
SHO in the limit  $\gamma \gg 1/t \gg \omega$ :

$$v_0 = \frac{Ft}{m^*} e^{-\gamma t}$$

# Disorder-induced SF-IN transition

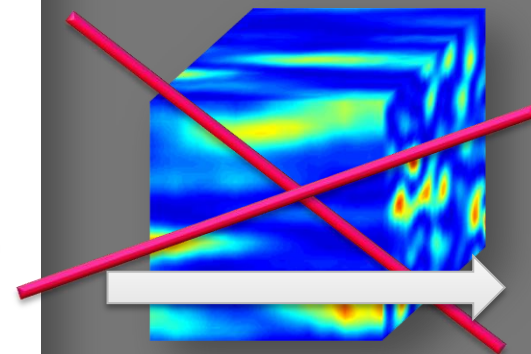


$$\Delta = 3 E_R$$

$$\Delta = 0.75 E_R$$

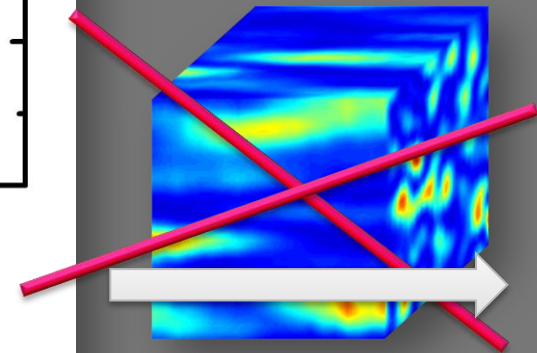
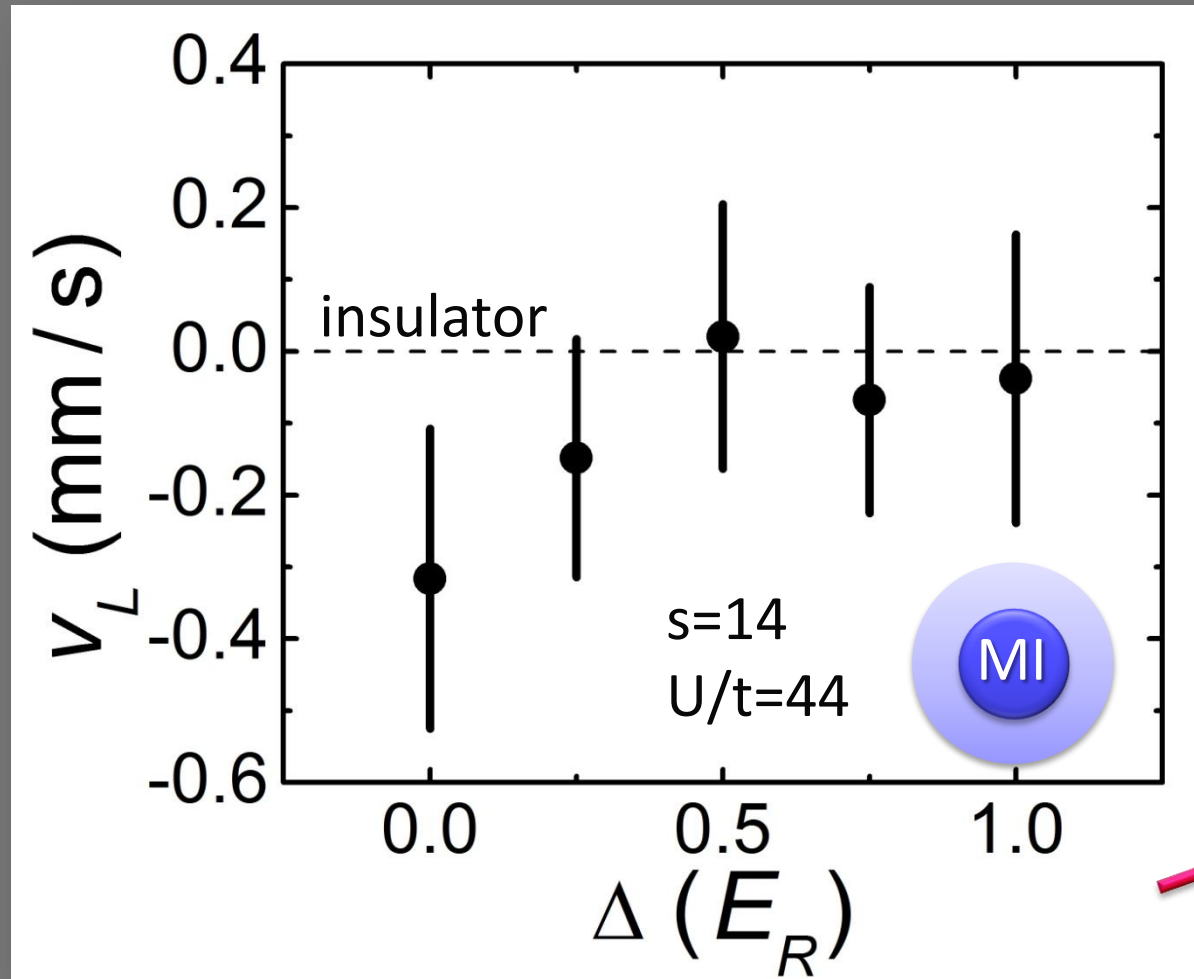
$$\Delta = 0 E_R$$

$$\Delta = 0 E_R \text{ hot}$$





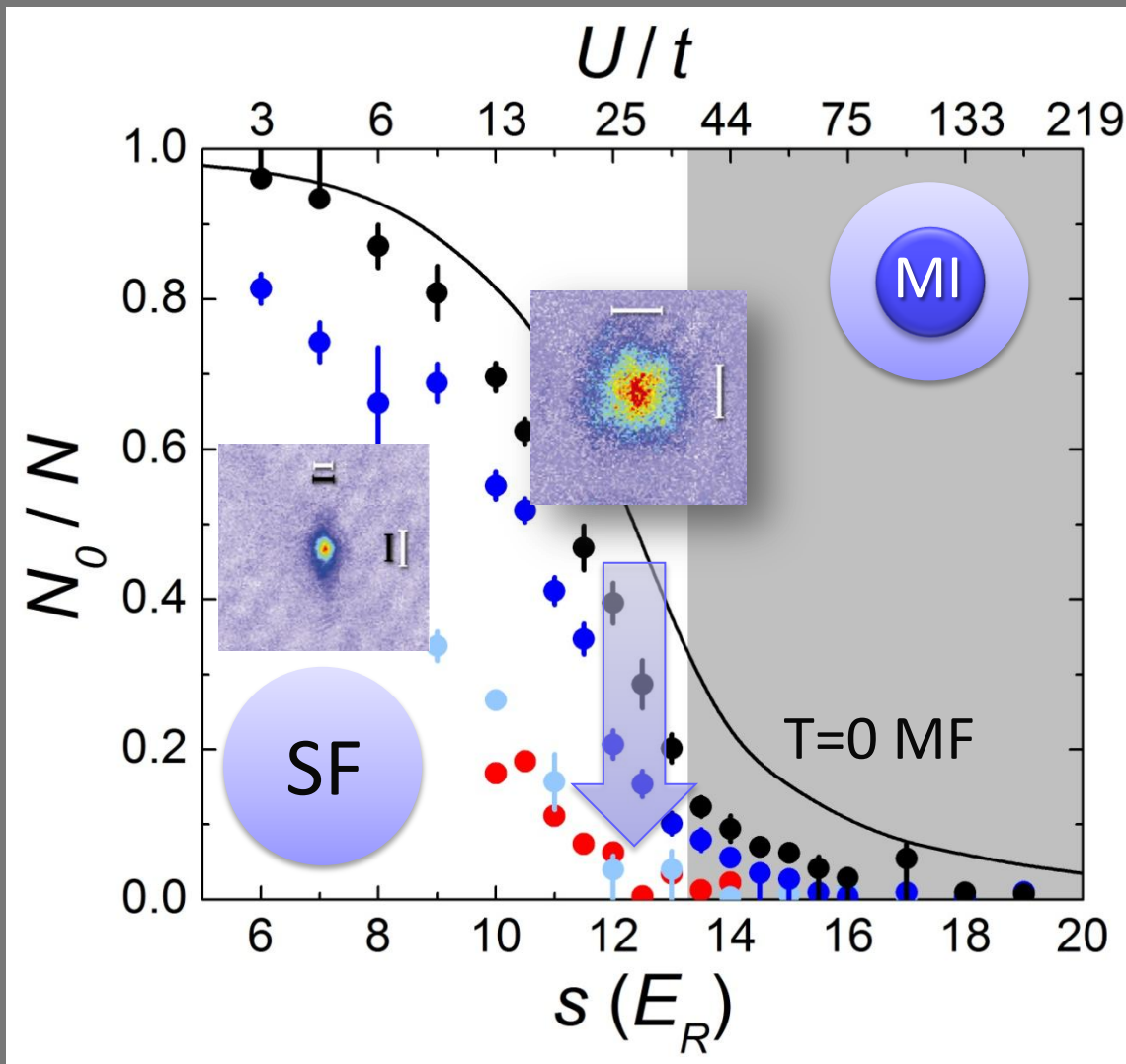
# Disorder mediated IN-to-SF?



More disorder always leads to more dissipation

# Disorder-induced SF-*IN* transition

Destruction of condensate  $\rightarrow$  insulator

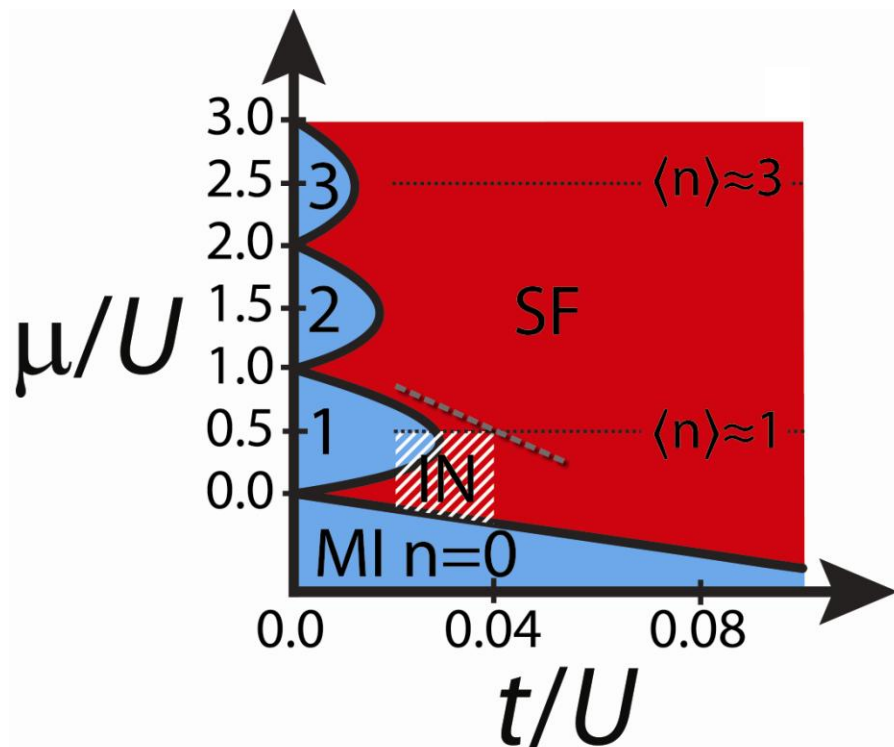


$\Delta=0 E_R$   
 $\Delta=0.75 E_R$   
 $\Delta=3 E_R$   
 $\Delta=0 E_R$  hot

# Conclusions

- Disorder-induced insulator for “strong” disorder
- No evidence for disorder-induced MI  $\Rightarrow$  SF transition

Nature Physics doi:10.1038/nphys1726 (2010)



- Temperature low enough?
- LDA?
- Finite system?
- Equilibrium?

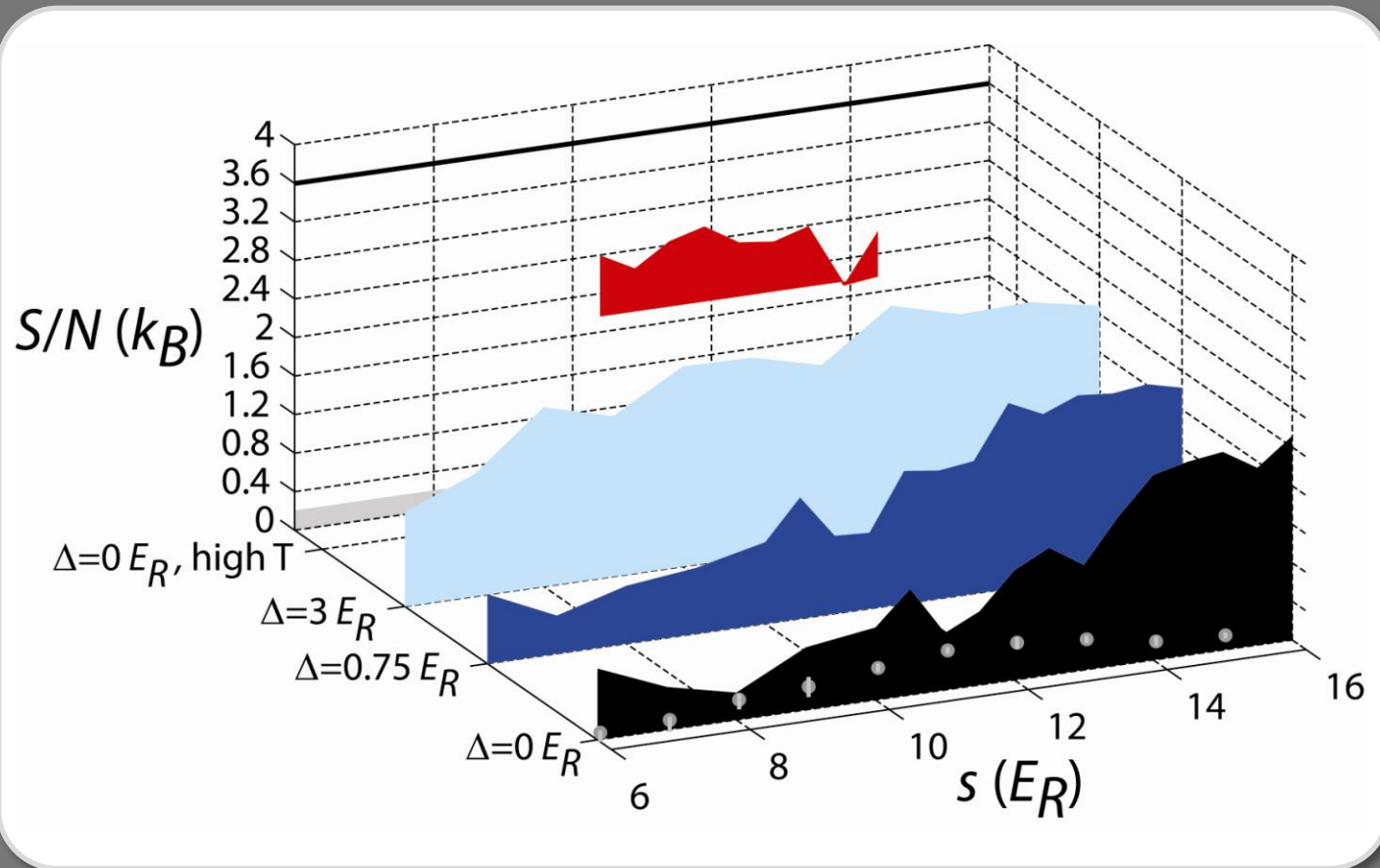
# Bounds on entropy

**Upper bound:** entropy after slow (15 ms) turn off

\*separate measurements indicate this is not truly adiabatic!

**Lower bound:** entropy before turning on lattice

Clean lattice:  
Estimate from  
 $N_0/N$  using finite  
temperature  
LDA+site-  
decoupled MFT



# Conclusions

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## On the horizon:

- Measuring compressibility / center of lattice
- Implement isotropic disorder

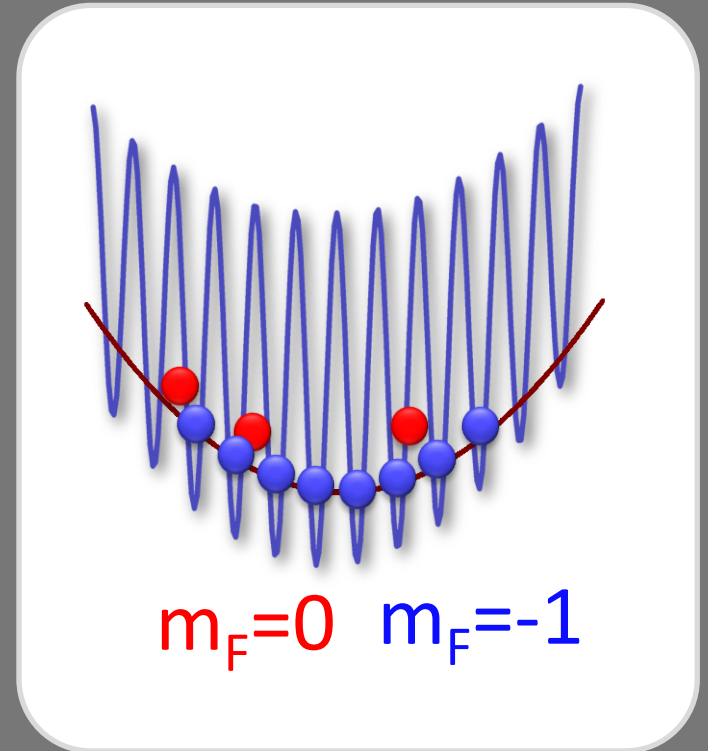
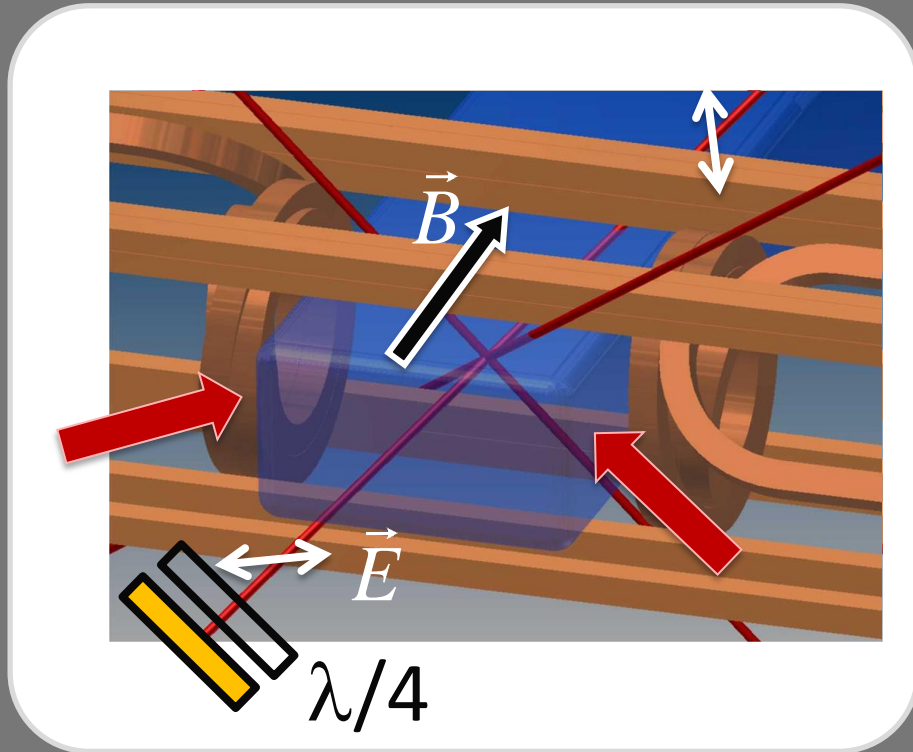
## Other projects:

- Measuring temperature in a lattice (PRA 79, 063605 (2009))
- Spin-dependent lattices (NJP 12, 055013 (2010))
- Non-equilibrium dynamics in 2D and 3D lattices
- Simulating thermopower in Mott-Hubbard materials

## There is a lot we still don't understand! Help!

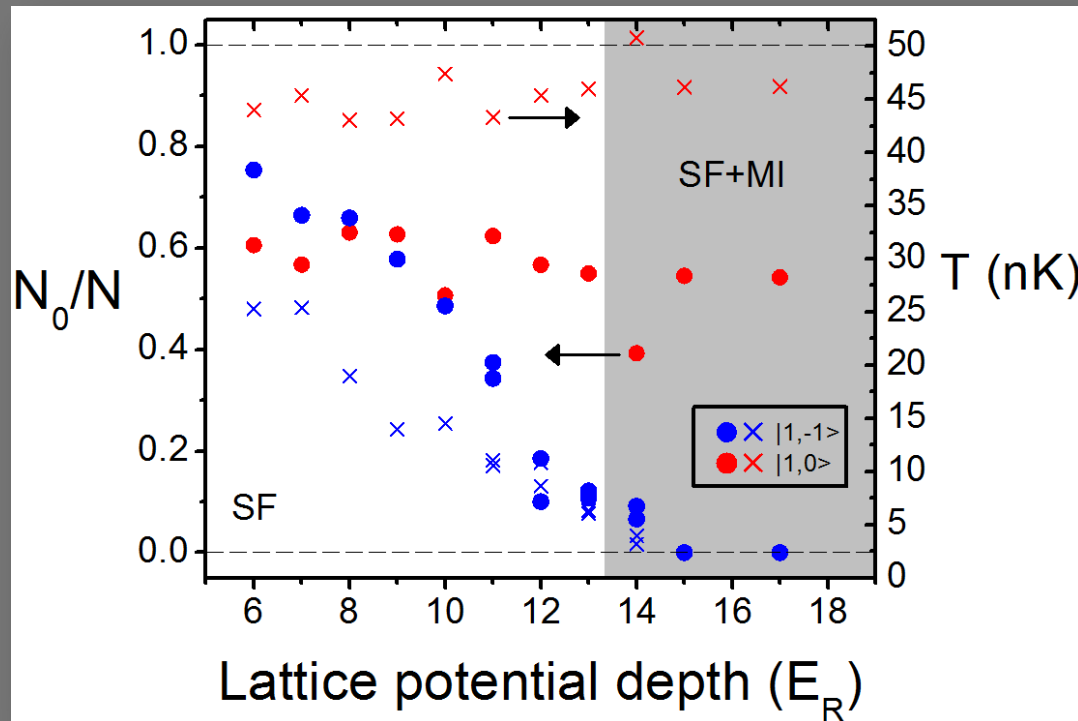
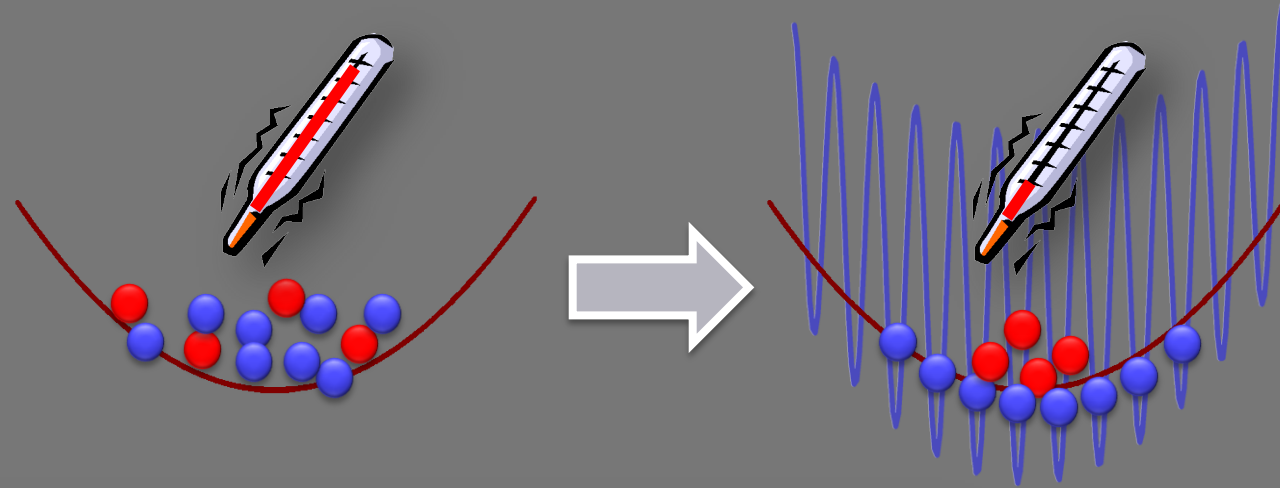
- Detailed dirty transport measurements
- Phase slips in finite 3D systems
- ...

# Spin-Dependent Lattices



Use  $m=0$  atoms for thermometry, cooling, phonon bath...

# Loss of thermal contact



- Not macro-/micro-scopic phase separation
- Detailed thermalization measurements using selective heating

# Advertisement

“Cooling in strongly correlated optical lattices: prospects and challenges”

arXiv:1010.0198v1

To appear in *Reports on Progress in Physics*

