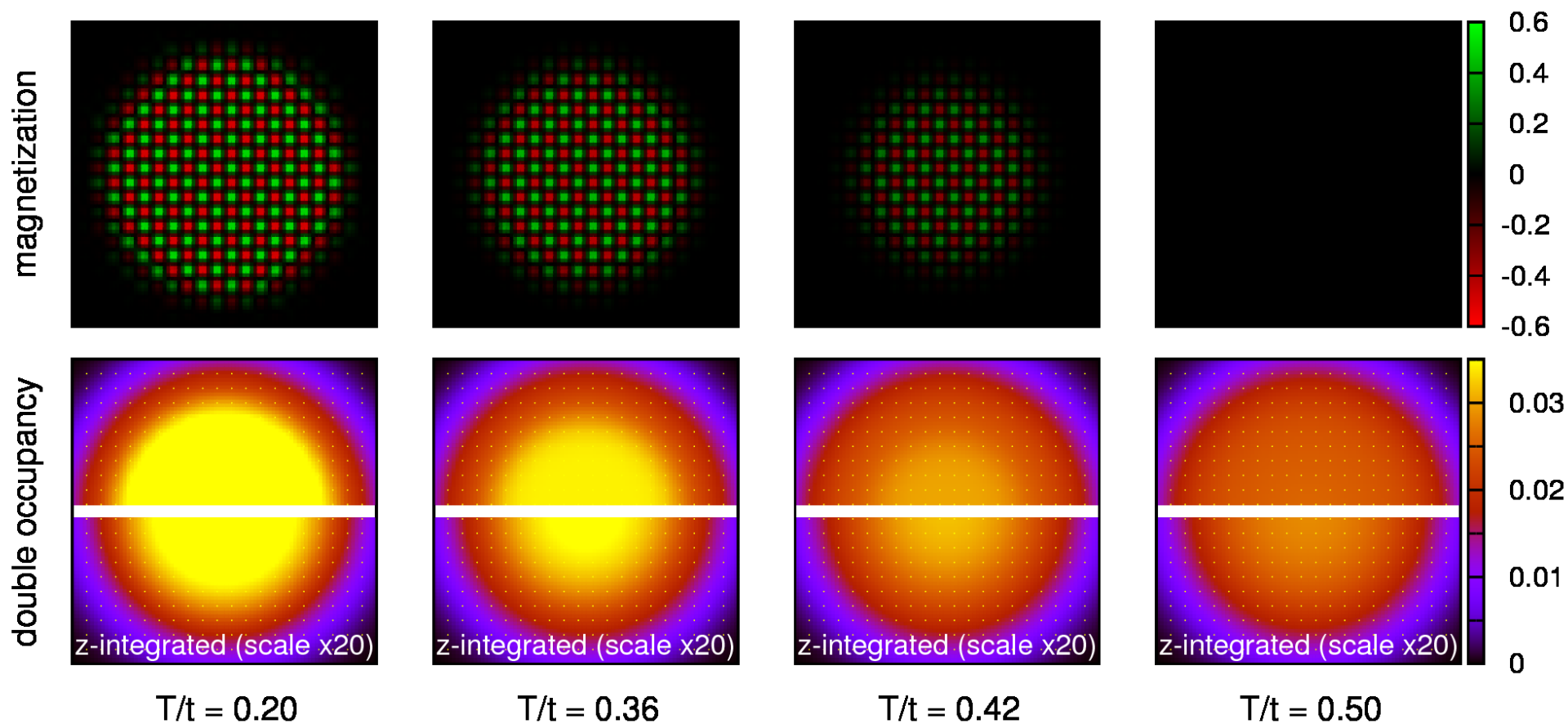


# Néel Transition of Lattice Fermions in a Harmonic Trap: a Real-Space Dynamic Mean-Field Study

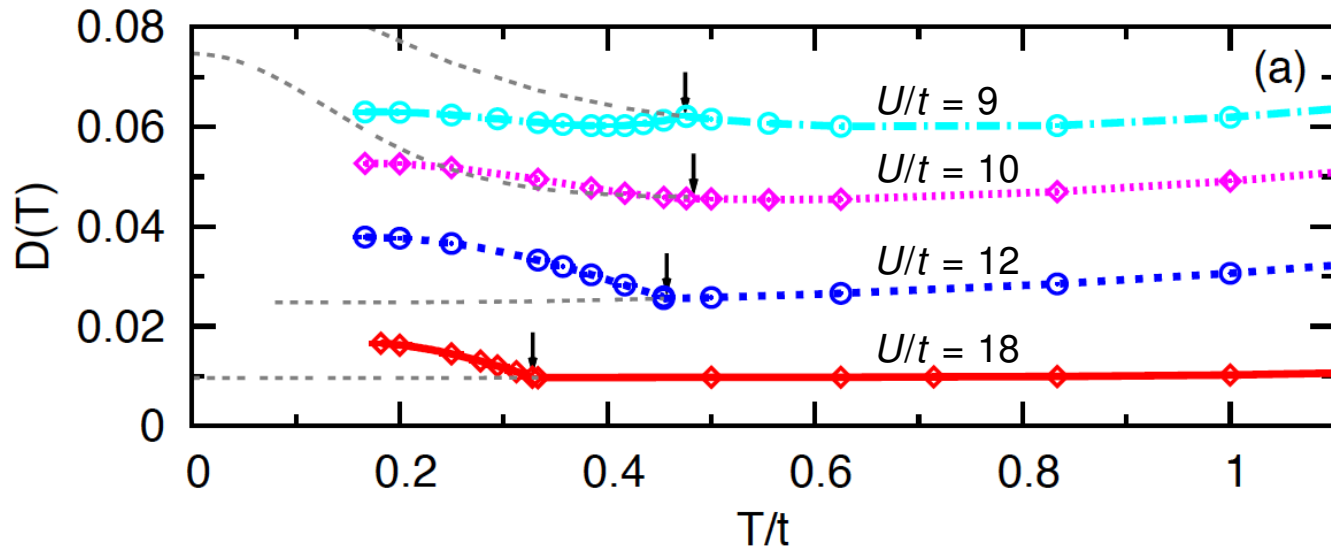
Elena Gorelik, Irakli Titvinidze, Walter Hofstetter, Michiel Snoek, and Nils Blümer

Nils Blümer, Univ. Mainz, Germany



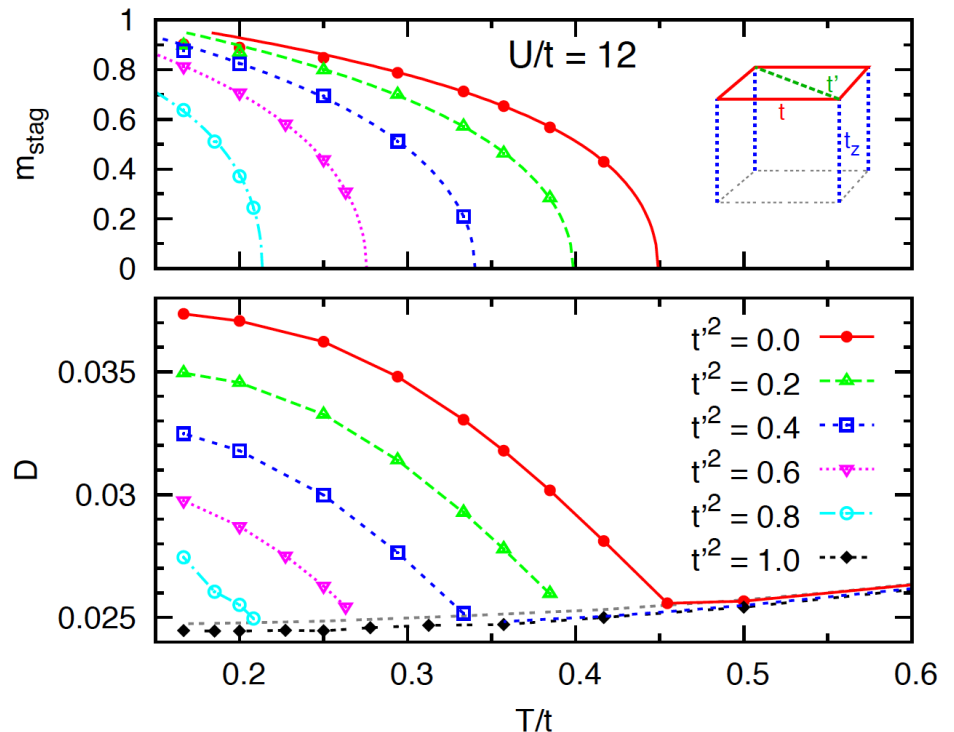
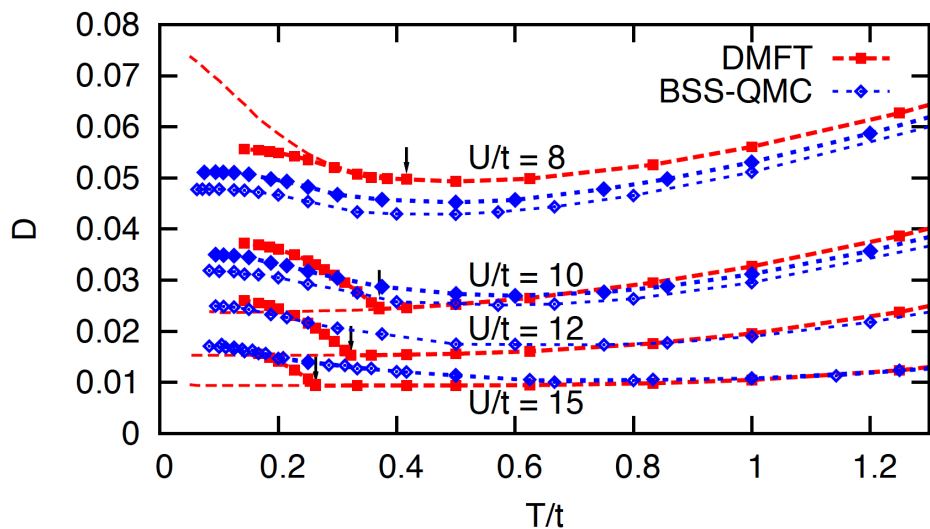
AF correlations signaled by **enhanced double occupancy** (cubic lattice,  $U/t = 12$ )

Enhancement of  $D$ : genuine **strong-coupling** effect (cubic lattice,  $n = 1$ )



DMFT scenario confirmed for  $\square$  lattice

Effect suppressed by **frustration** ( $\rightsquigarrow \Delta$ )



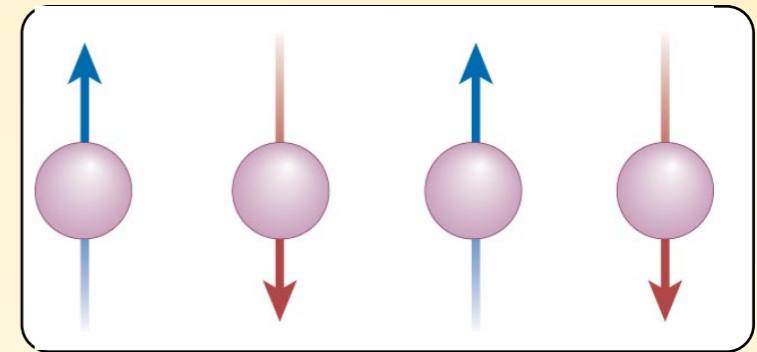
# Cavity-aided MRI of ultracold atoms

Nathan Brahms, T. Purdy, D.W.C. Brooks, T. Botter, D.M. Stamper-Kurn

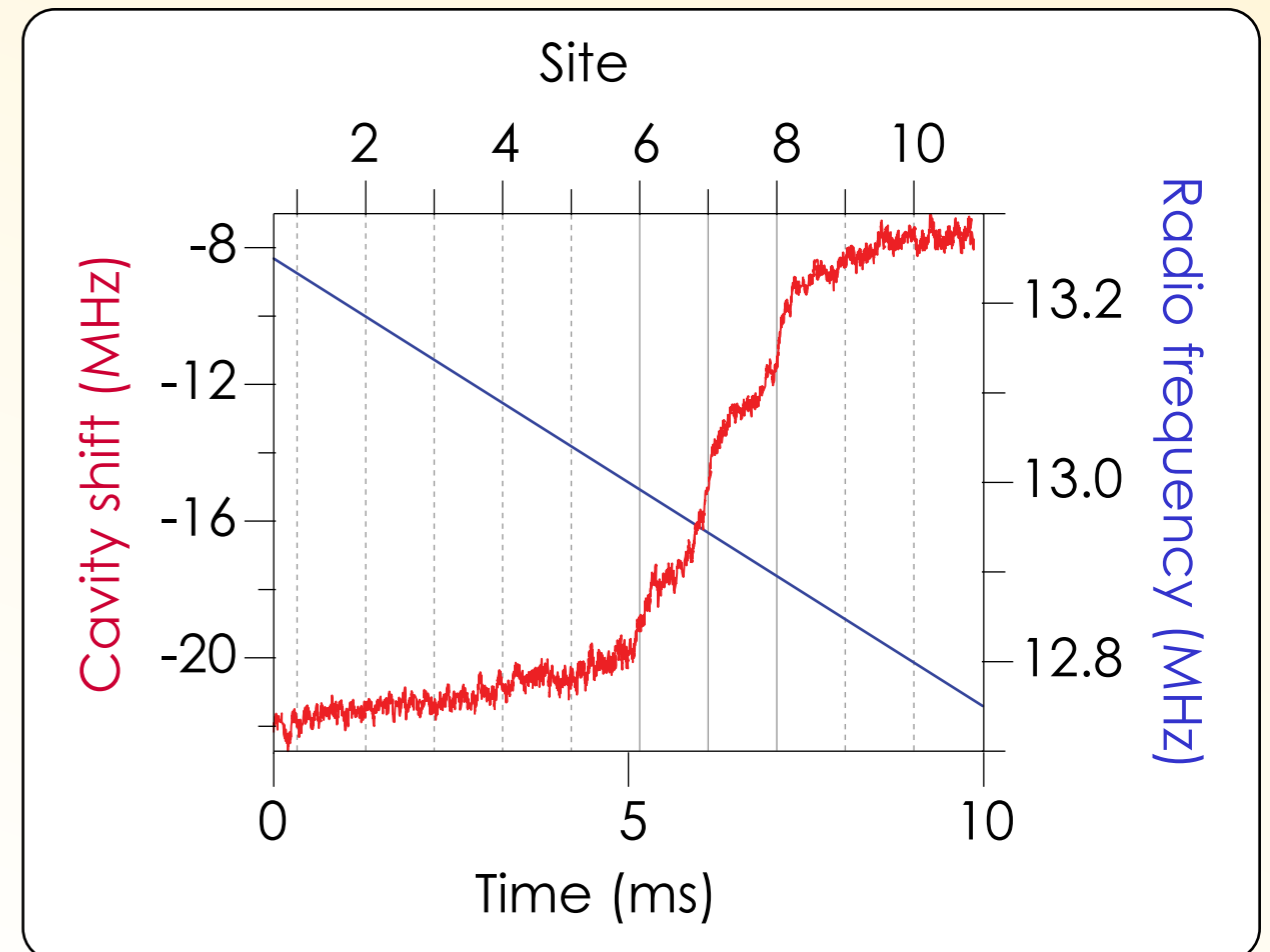
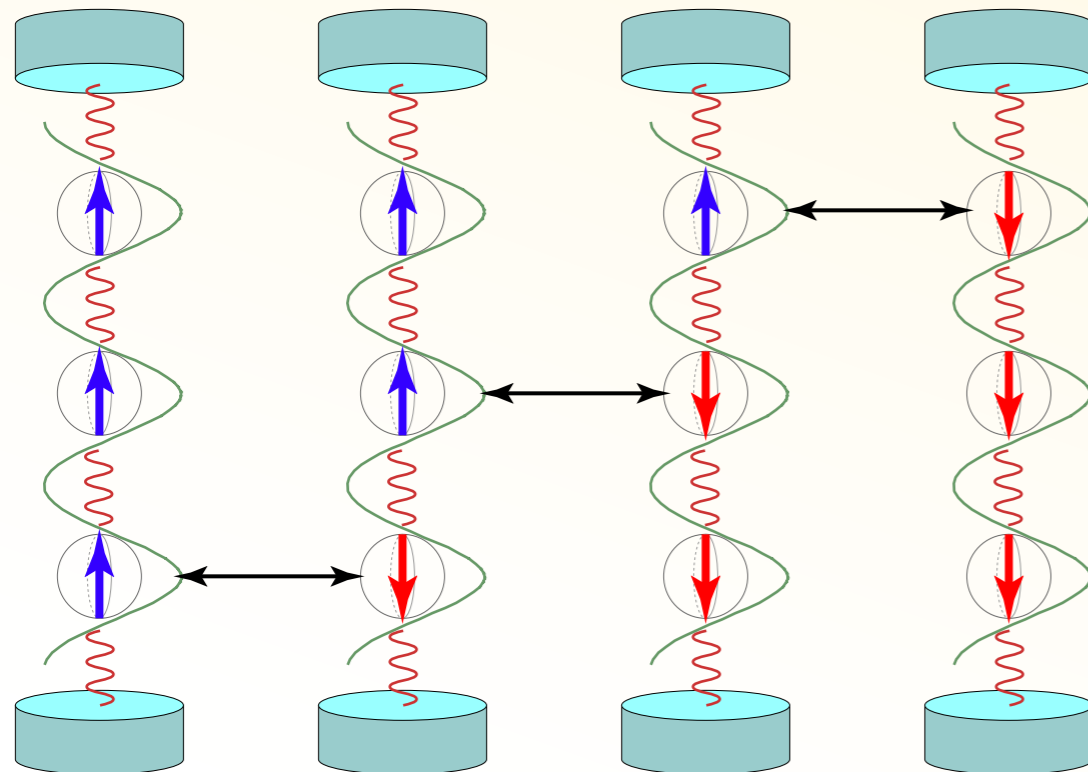
*University of California, Berkeley*

Microscopic imaging techniques for quantum magnetism, QIP, spatially varying properties

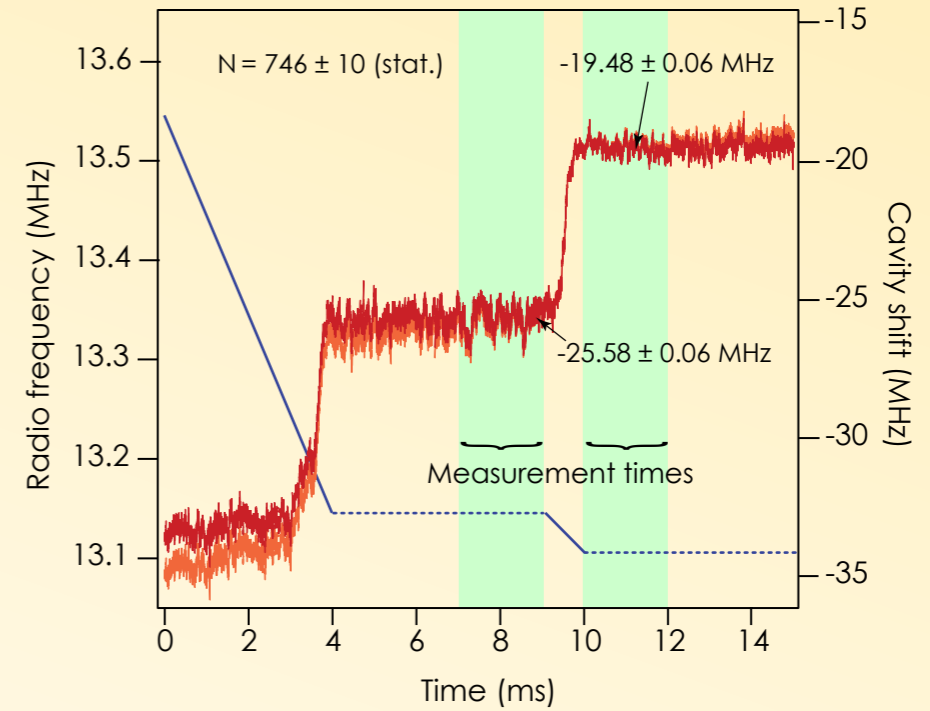
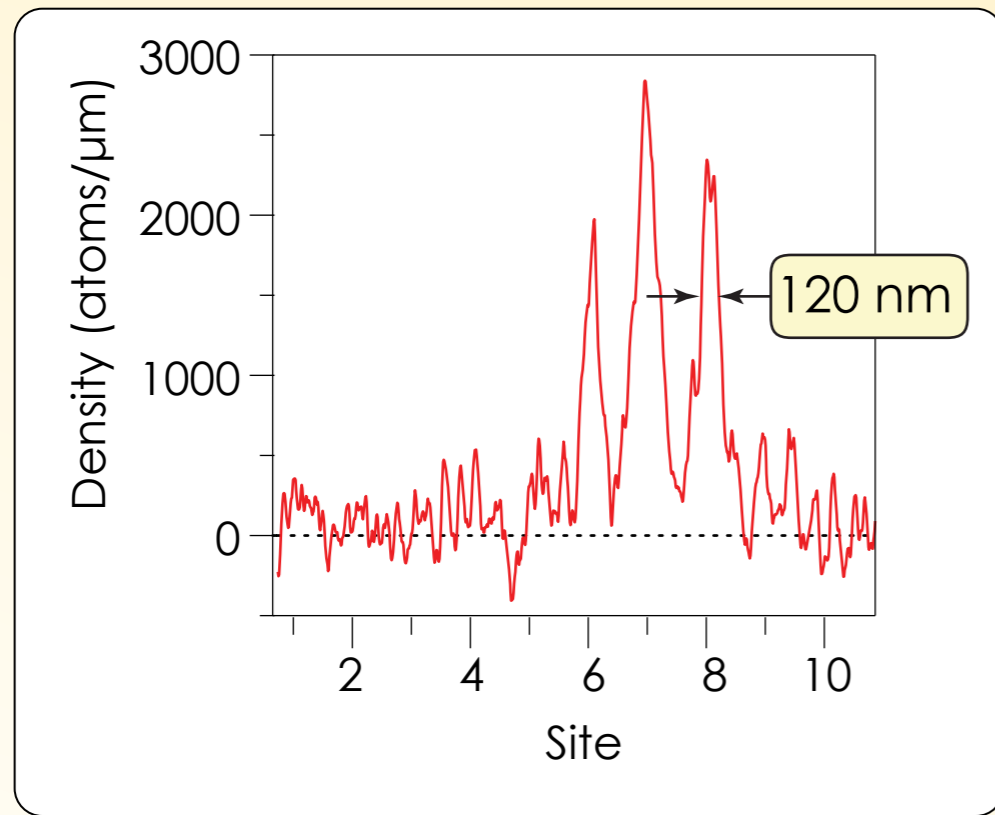
Use dispersive cavity QED + MRI for  
state-sensitive, minimally destructive,  
high-resolution, high-precision imaging



Coleman and Schofield, *Nature* **433**, 226 (2005)



# Sub-wavelength spatial resolution

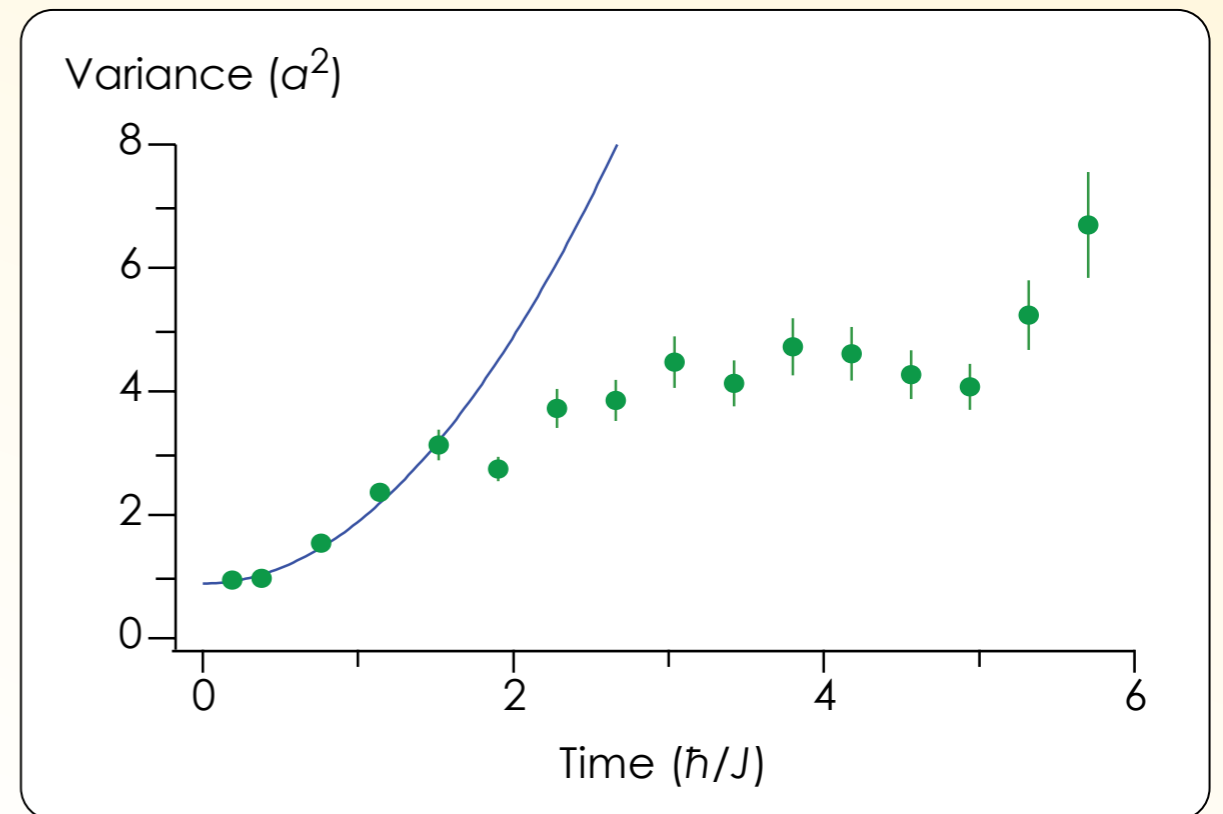
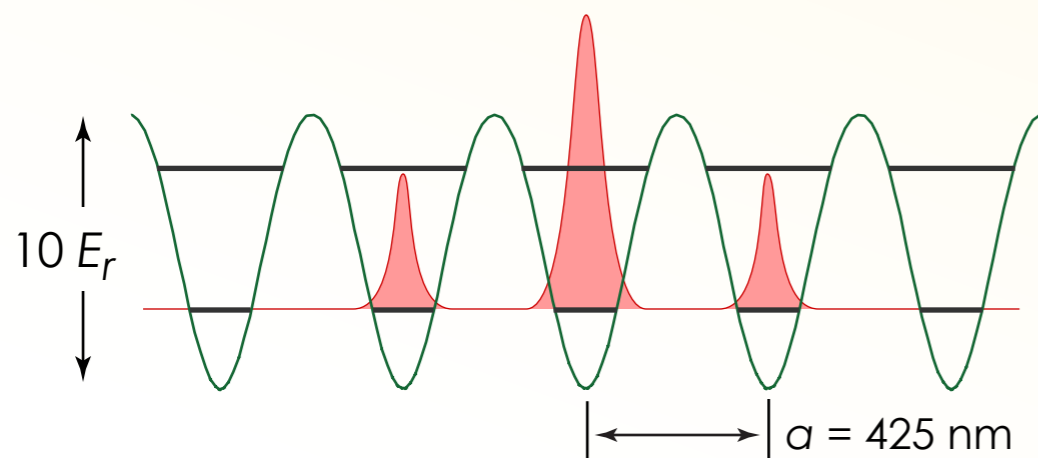


# Sub-Poissonian measurement precision

$$\delta S_z \sim 5 \hbar$$

$$\delta N \sim 2.4$$

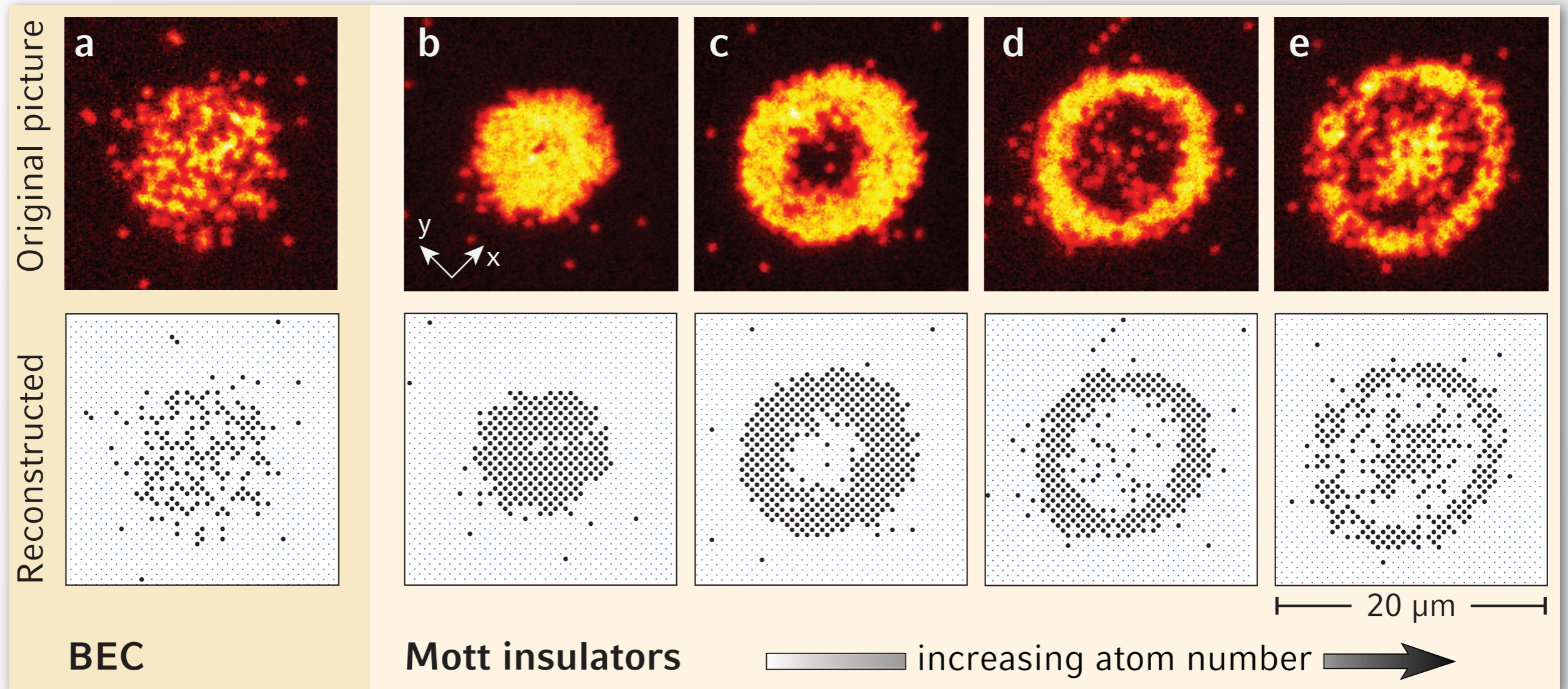
Physical application:  
Quantum transport in an optical lattice



# Single-site and single-atom resolved addressing of correlated quantum states in optical lattices

Talk by Stefan Kuhr this morning

## Observation of Mott insulators



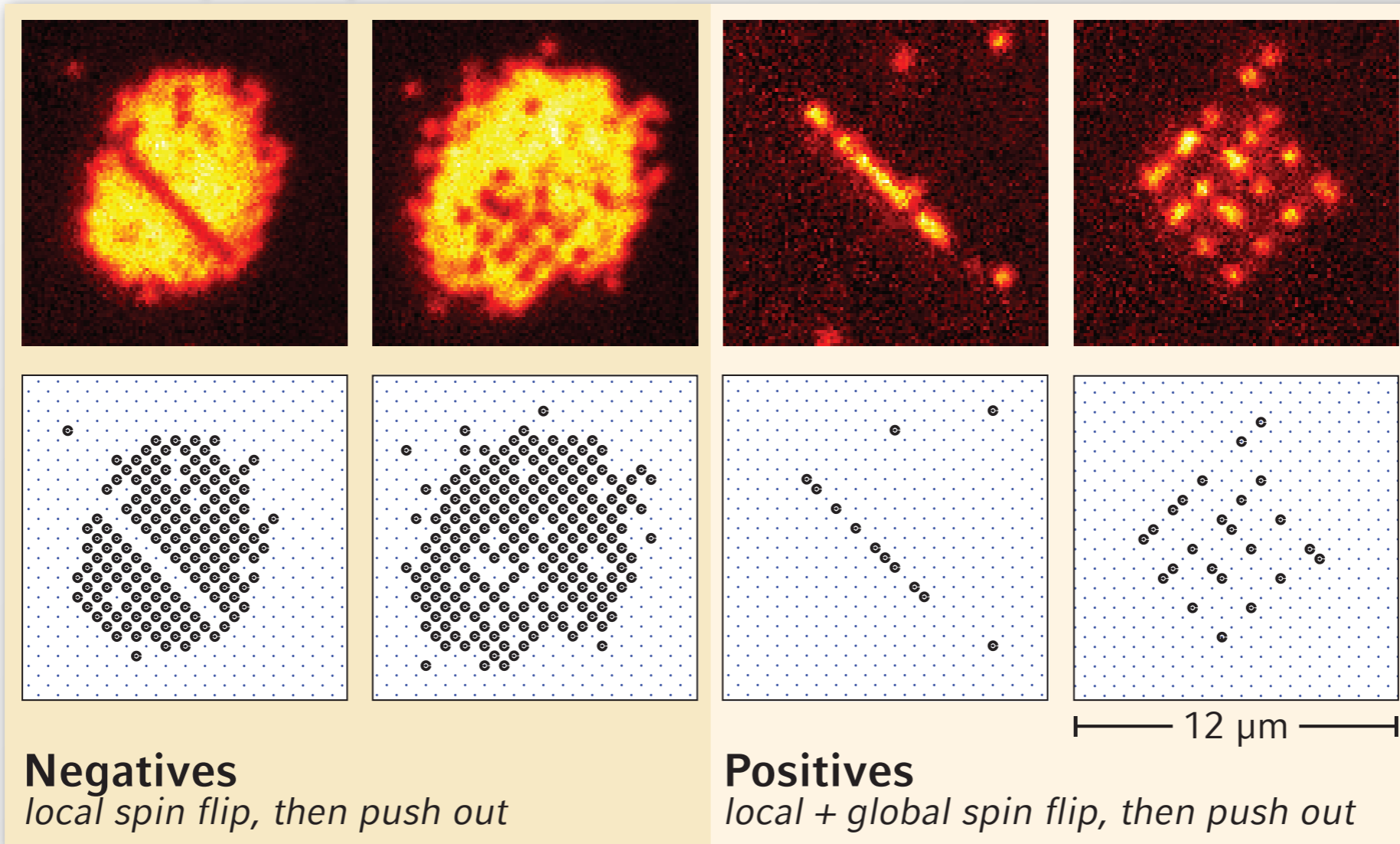
Marc CHENEAU

Max-Planck-Institut für Quantenoptik – Garching, Germany



# Single-site and single-atom resolved addressing of correlated quantum states in optical lattices

## Local spin flips



Marc CHENEAU

Max-Planck-Institut für Quantenoptik – Garching, Germany



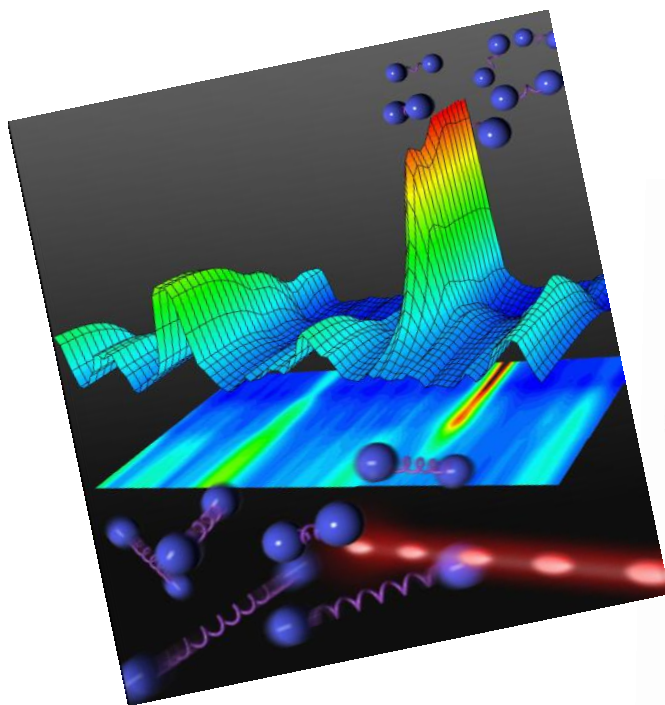
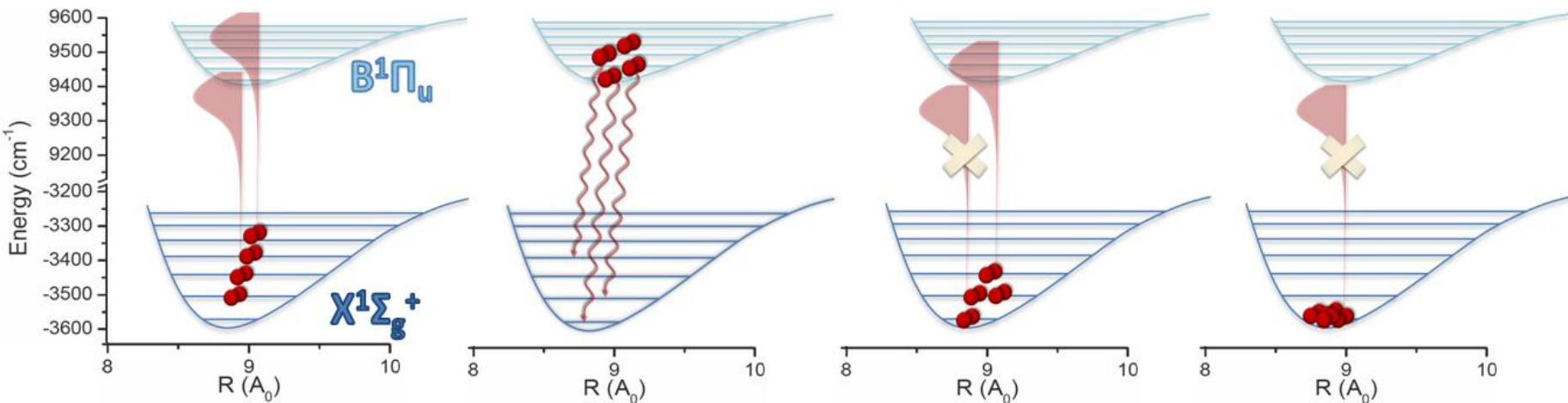
# Molecular (vibrational cooling) Optical Pumping with shaped light

D. Comparat, Laboratoire Aimé Cotton, CNRS, Orsay, France

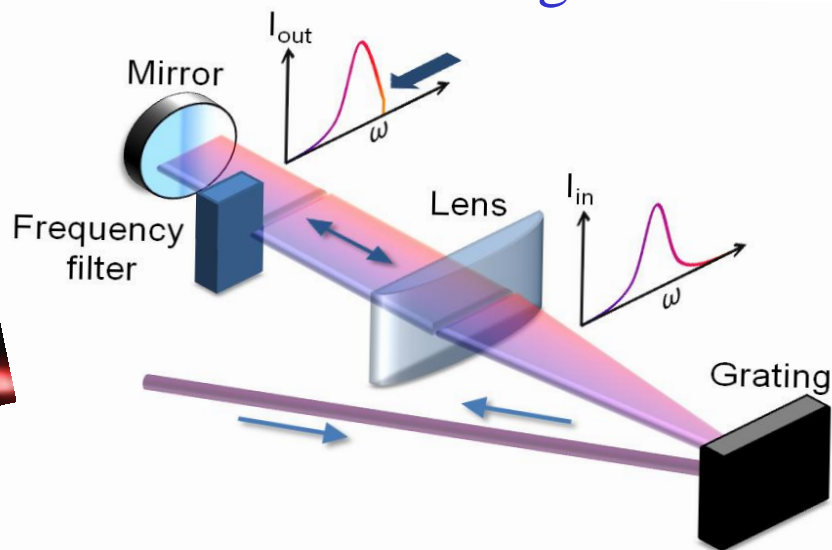
Coherent (pump-probe) control: femtosecond laser : A. Zewail Nobel 1999

1969	Optical pumping (sub-Zeeman)	Drullinger Zare
1972	Electric beam deflection (bi-alkali)	Dagdigian Wharton
1979	Light pressure force: beam deflection Na <sub>2</sub>	Herrmann, Leutwyler, Wöste, Schumacher
1981	Laser cooling (anti-stokes) of CO <sub>2</sub> by laser. (proposed in 1950 Kastler)	Djeu, Whitney
1997	Dipole Force	Corkum
1998-2008	Beam slowing, cryogenic cooling, molecular ions, ...	Meijer, Doyle, Drewsen, ...
2008	Internal state (Vibrational) cooling with incoherent shaped laser	Comparat, Pillet
2010	Laser cooling (momentum transfer) of SrF	DeMille

# Molecular (vibrational cooling) Optical Pumping with shaped light



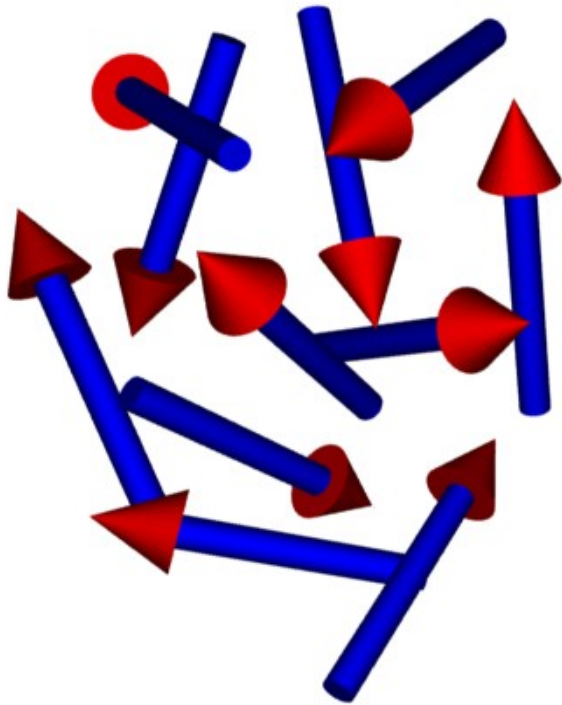
Triplet-singlet conversion  
Rotational cooling  
Toward general laser cooling



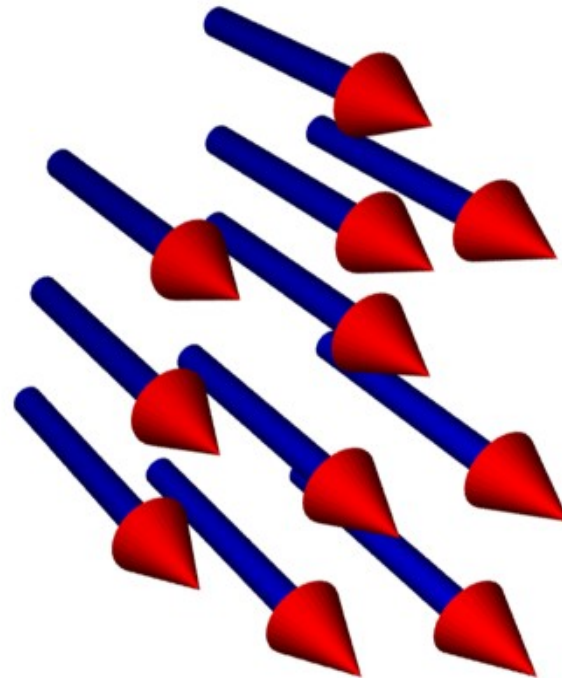


# Perspectives on itinerant ferromagnetism in an atomic Fermi gas

Weak interactions



Strong interactions



**Gareth Conduit**<sup>1,2</sup>, **Ben Simons**<sup>3</sup> & **Ehud Altman**<sup>1</sup>

1. Weizmann Institute of Science, 2. Ben Gurion University, 3. University of Cambridge



# T-matrix approach for few-body physics in ultracold atoms

Xiaoling Cui

Institute for Advanced Study, Tsinghua University, Beijing

$$T = U + UG_0(E)T$$

$$\text{Det}[1 - UG_0(E_b)] = 0$$

***Well-known method but bran-new application in  
cold atoms!***

**X.L. Cui, Y.P. Wang and F. Zhou, Phys. Rev. Lett. 104, 153201(2010)**

**X.L. Cui, to appear on arxiv**

## Main results:

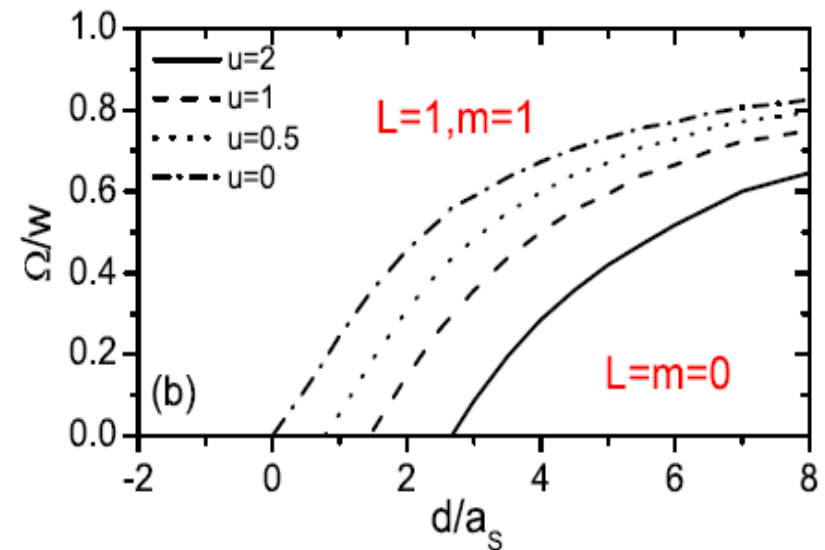
In most general cases, the problem is reduced to a matrix equation expanded by various orthogonal molecular states describing **external center-of-mass motions** of a pair of interacting particles; while each matrix element is guaranteed to be finite by properly renormalizing the short-range contributions for **internal relative motions**.

## Advantage:

I. **systematic**, bridge from two-body to many-body problem

II. **Physically insightful**, by employing concept of renormalization

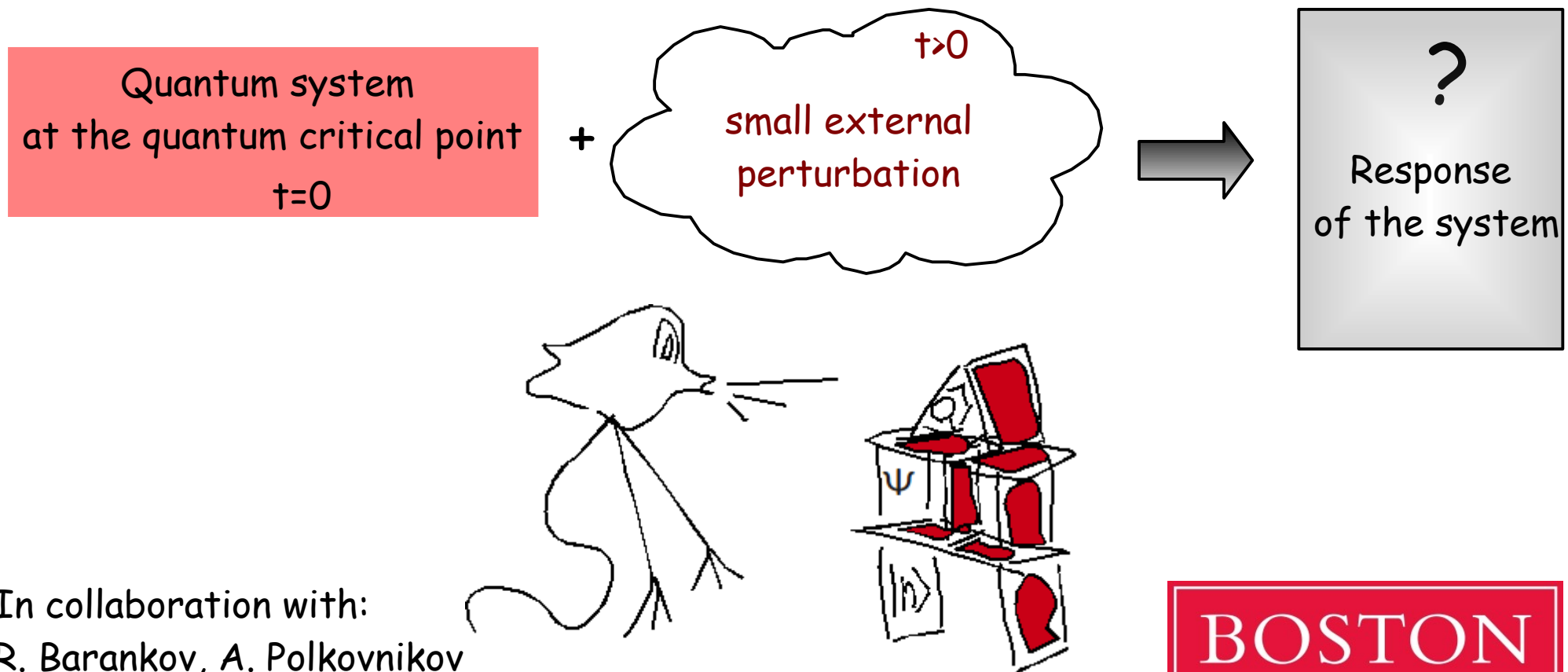
III. **Transparent** to analyze scattering properties and energy spectrum



**Application:** quantum Hall transitions of atom-dimer fermionic system in a rotating harmonic trap

# Probing quantum systems through adiabatic dynamics

Claudia De Grandi

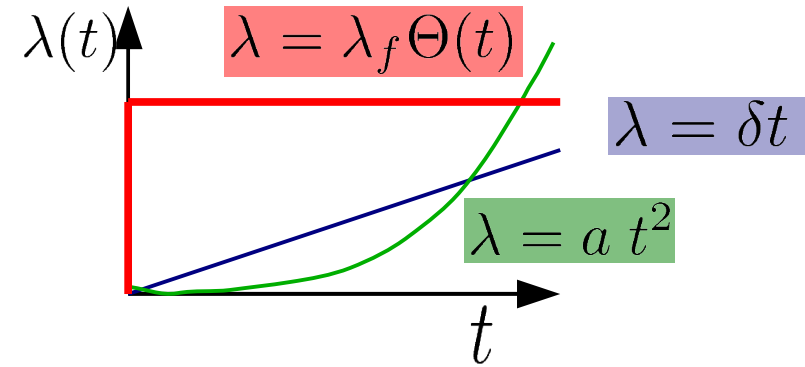
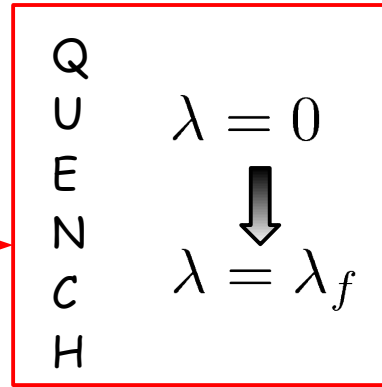


In collaboration with:  
R. Barankov, A. Polkovnikov  
V. Gritsev (U. of Fribourg)

BOSTON  
UNIVERSITY

$$H(\lambda) = H_0 + \lambda V$$

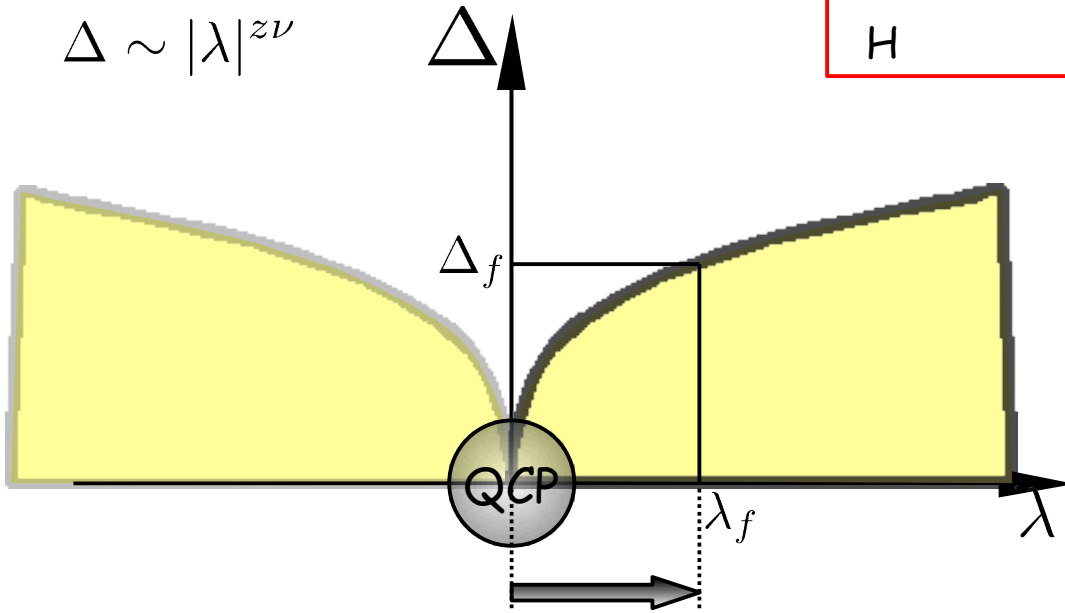
external parameter



Compare different power laws dependence in time

$$\lambda(t) = v \frac{t^r}{r!} \Theta(t)$$

$$\Delta \sim |\lambda|^{z\nu}$$



Applications to 1D Bose gases are discussed (sine-Gordon model)

Scaling of the number of excitations due to the quench:

RESULTS

quadratic scaling

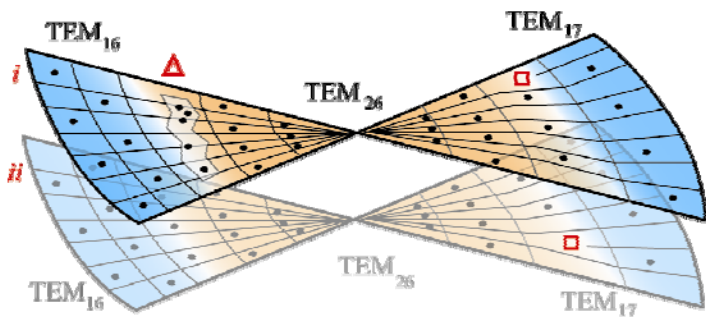
system size

dimension

$r = \text{power of the quench}$

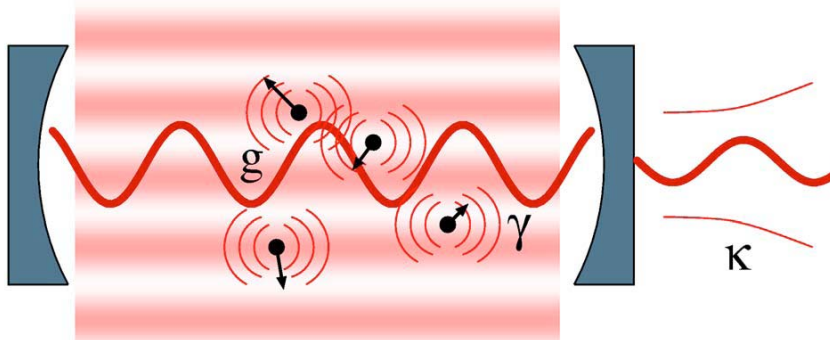
$$n_{\text{ex}} \sim \begin{cases} v^2 L^{2/\nu - d + 2zr} & \xi(\nu) \gg L \\ |v| d\nu / (z\nu r + 1) & \xi(\nu) \ll L \end{cases}$$

Kibble-Zurek scaling



# Solidity and frustration in multimode optical cavities

Sarang Gopalakrishnan  
 (with Benjamin Lev, Paul Goldbart)  
 University of Illinois at Urbana-Champaign



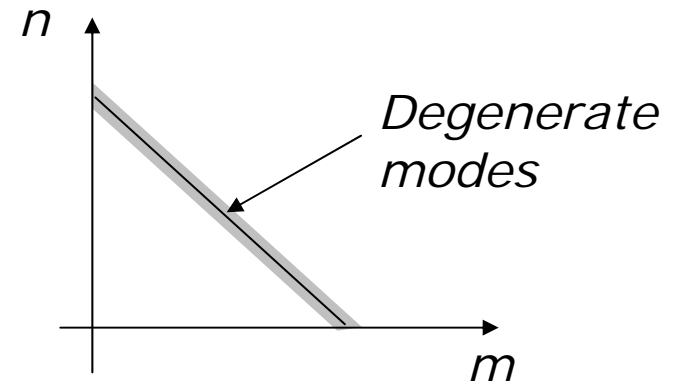
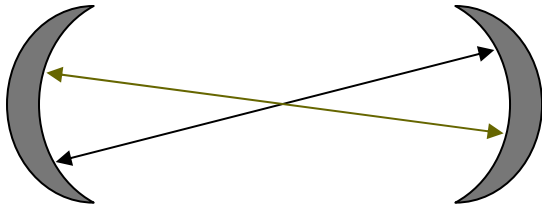
Domokos, Ritsch (PRL, 2002)  
 Asbóth et al (PRA, 2005)

## Crystallization in cavities

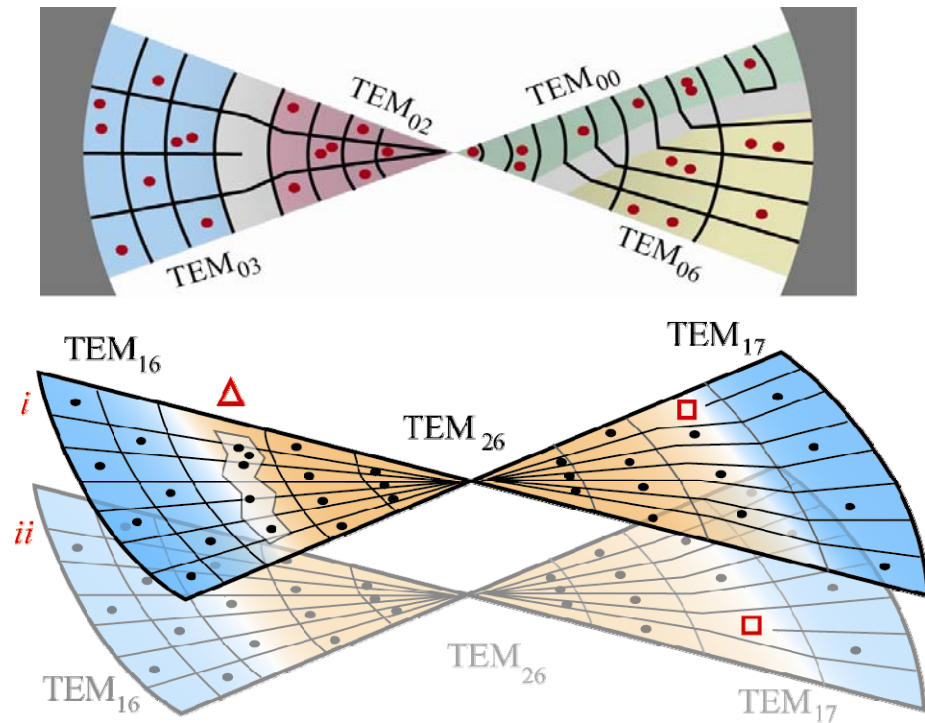
- Red-detuned lasers **transverse** to cavity, high-field-seeking atoms
- Atoms scatter light coherently between pump and cavity
- Atoms one wavelength apart emit in phase
- Photons trap atoms at even/odd antinodes
- Spontaneous even/odd symmetry breaking

## Multimode cavities

(ring, confocal, **concentric**)



- Many more possibilities for ordering
- 2D case realizes Brazovskii's transition
- Ordered state expected to have defects, dislocations
- In 3D, frustration
  - Center and edge must order differently
  - Forces dislocations, etc.
- Supersolidity? Glassiness?



arxiv:0903.2254

## Chain of trapped ions



Quantum simulator

## Spin model

$$H = J_z \sum_{i < j} \frac{1}{|i-j|} S_i^z S_j^z \\ + J_{xy} \sum_{i < j} \frac{1}{|i-j|} (S_i^x S_j^x + S_i^y S_j^y) \\ - \mu \sum_i S_i^z$$

with dipolar interaction  
and tunneling

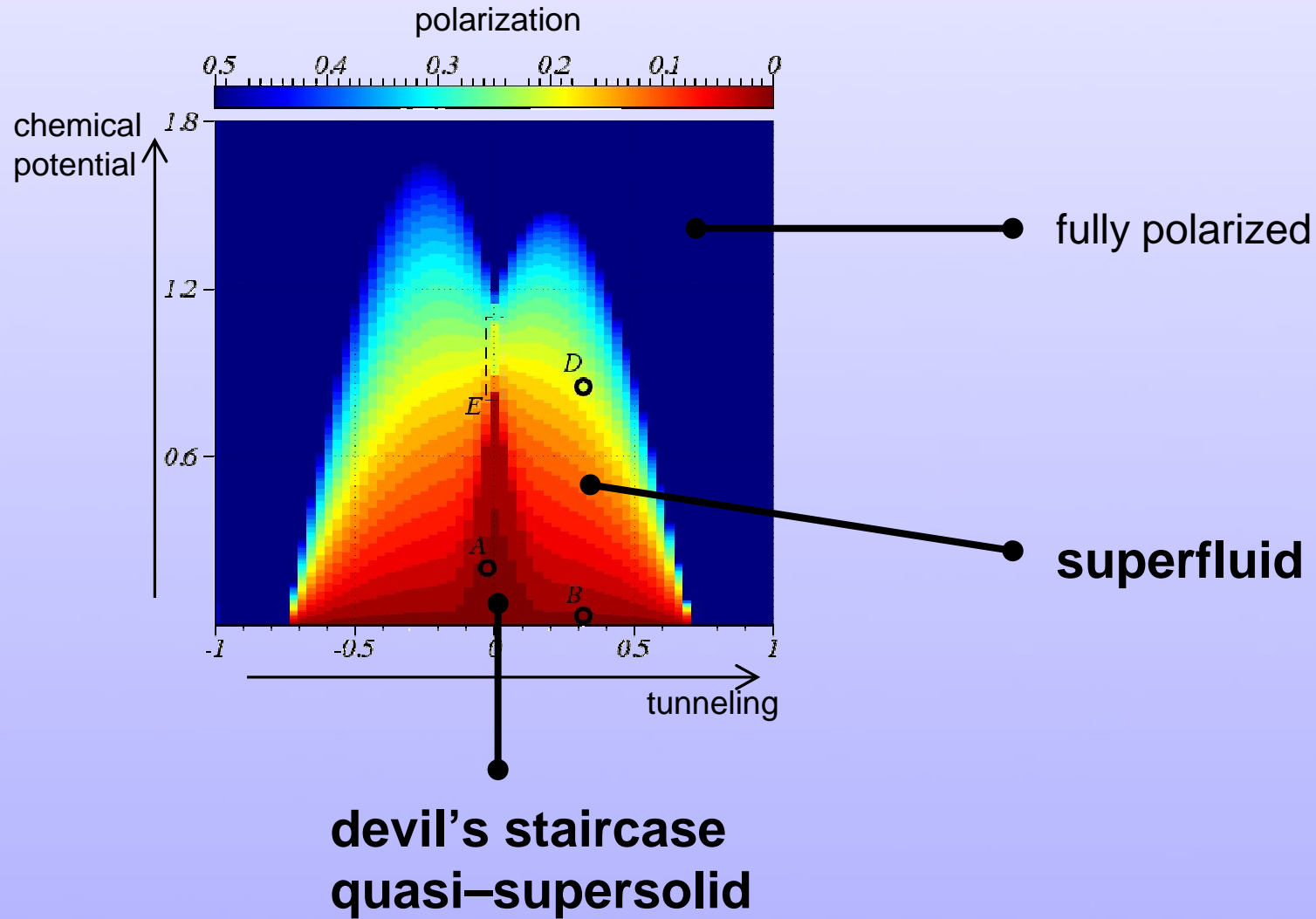
Philipp Hauke, F. M. Cucchietti, M. Lewenstein (ICFO)

A. Müller-Hermes, M.-C. Bañuls, J. I. Cirac (MPQ)

*arXiv:1008.2945*, 2010



# A quasi-supersolid phase emerges



# Density ripples in expanding low-dimensional gases as a probe of correlations

**Adilet Imambekov, Rice University**

Theory: PRA 80, 033604 (2009), A. Imambekov et. al.

1D Experiment: PRA 81, 031610(R) (2010), S. Manz et. al.

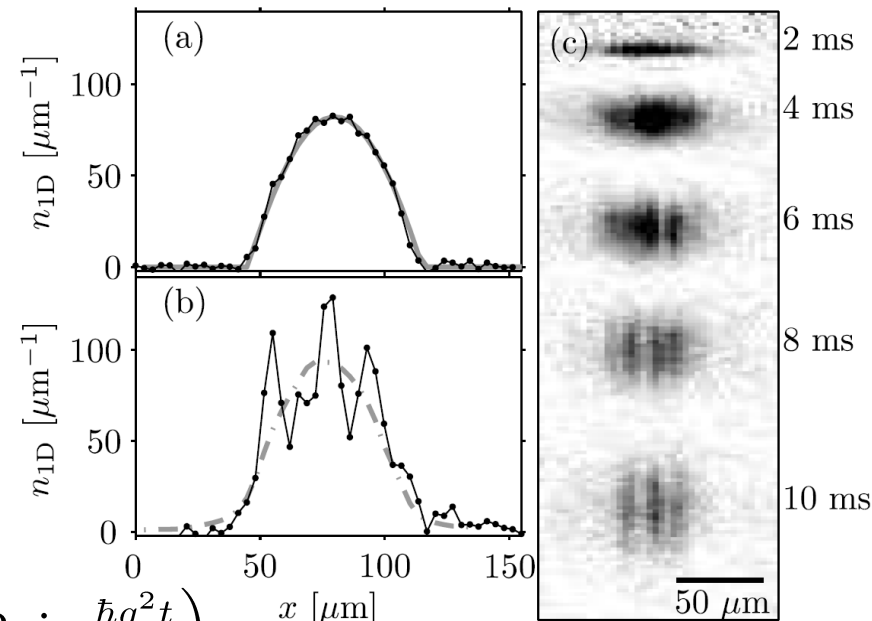
TOF in “Infinite size” limit:  $t \ll \frac{mL^2}{\hbar} \sim 10s$

velocity fluctuations +  
expansion



density ripples

$$\frac{\langle |\rho(q)|^2 \rangle}{n_{1D}^2 \xi_h} \approx \frac{\lambda_T q - e^{\frac{-2\hbar q t}{m \lambda_T}} \left( \lambda_T q \cos \frac{\hbar q^2 t}{m} + 2 \sin \frac{\hbar q^2 t}{m} \right)}{q \xi_h (1 + \lambda_T^2 q^2)}$$

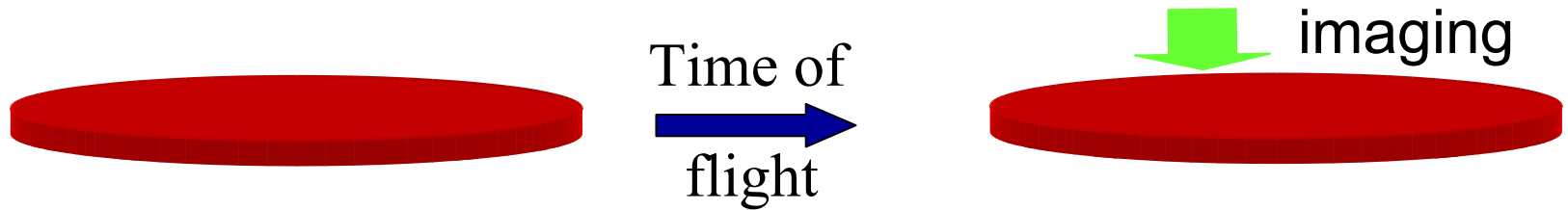


# 2D: Probe of BKT transition

$$\langle \hat{\psi}^\dagger(\mathbf{r}, 0) \hat{\psi}(0, 0) \rangle \approx n_{2D} \left( \frac{\lambda_{2D}}{r} \right)^\eta \text{ for } r \gg \lambda_{2D}$$

$\eta < 1/4$  , algebraic decay of correlations

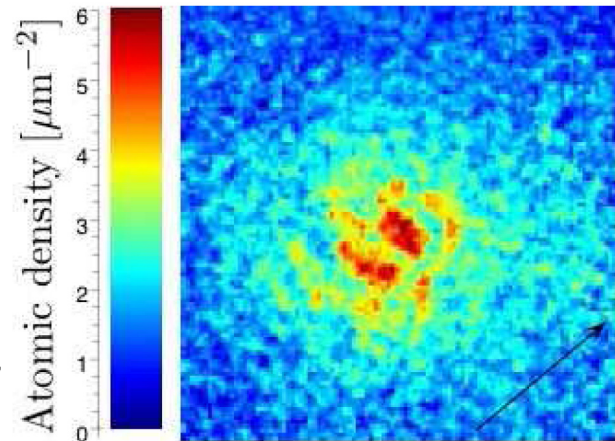
$\eta = 1/4$  , vortex unbinding, exponential decay above that T



**Theory:**  $y = \frac{\hbar q^2 t}{m}$

$$\langle |\rho(q)|^2 \rangle \approx n_{2D}^2 \lambda_{2D}^2 \left( \frac{\hbar t}{m \lambda_{2D}^2} \right)^{1-\eta} F(\eta, y)$$

**Scaling:**  $\int_0^{\sqrt{\frac{2\pi m}{\hbar t}}} dq \langle |\rho(q)|^2 \rangle \propto t^{1/2-\eta}$



# Thermodynamics in an Unitary Fermi Gas

Kaijun Jiang

*Wuhan Institute of Physics and Mathematics, Chinese Academy of Sciences, Wuhan, China; Laboratoire Kastler Brossel, Ecole normale supérieure, Paris, France*

**Exploring the thermodynamics of ultracold atoms**

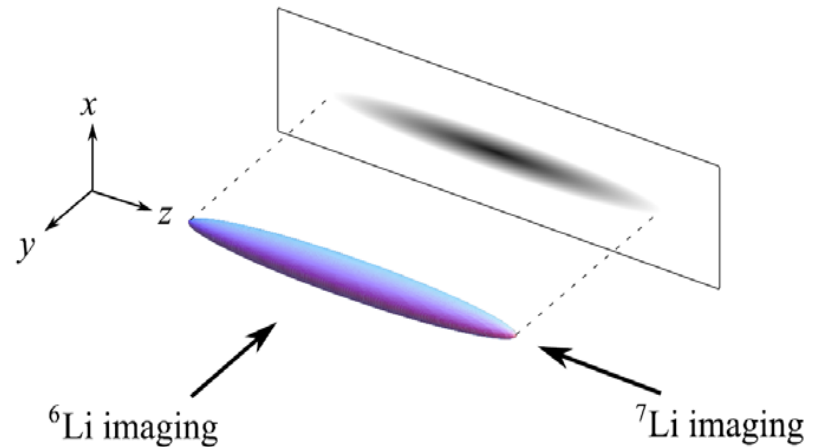
$$P(\mu_1, \mu_2, T) = P(\mu_1, T) h\left(\eta = \frac{\mu_2}{\mu_1}, \zeta = \exp\left(\frac{-\mu_1}{k_B T}\right)\right)$$

## Method and technique

**LDA**  $\mu_{iz} = \mu_i^0 - V(z) = \mu_i^0 - \frac{m\omega_z^2 z^2}{2}$

**Local pressure**  $P(\mu_1, \mu_2, T) = \frac{m\omega_r^2}{2\pi} (n_{1z} + n_{2z})$

**Temperature: Bosonic Li<sup>7</sup> colliding with Li<sup>6</sup> to equilibrium**



# 1, Balanced Fermi Gas with Finite Temperature

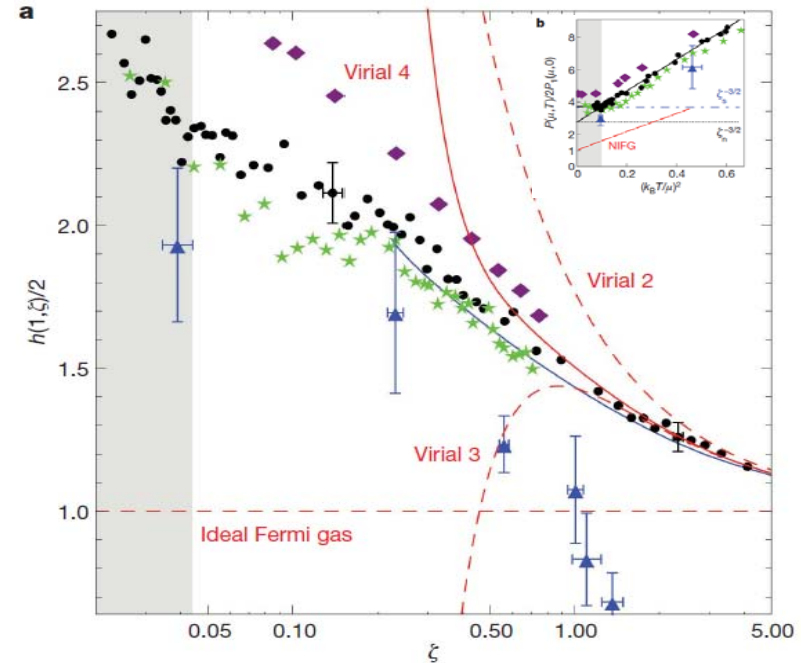
High temperature: Virial expansion

$$\frac{h(1, \zeta)}{2} = \frac{\sum_{k=1}^{\infty} ((-1)^{k+1} k^{-5/2} + b_k) \zeta^{-k}}{\sum_{k=1}^{\infty} (-1)^{k+1} k^{-5/2} \zeta^{-k}}$$

Low temperature: Phase transition

$T > T_c$ , Fermi liquid

$$P(\mu, T) = P(\mu, 0) \left( \xi_n^{-3/2} + \frac{5\pi^2}{8} \xi_n^{-1/2} \frac{m^*}{m} \left( \frac{k_B T}{\mu} \right)^2 \right)$$



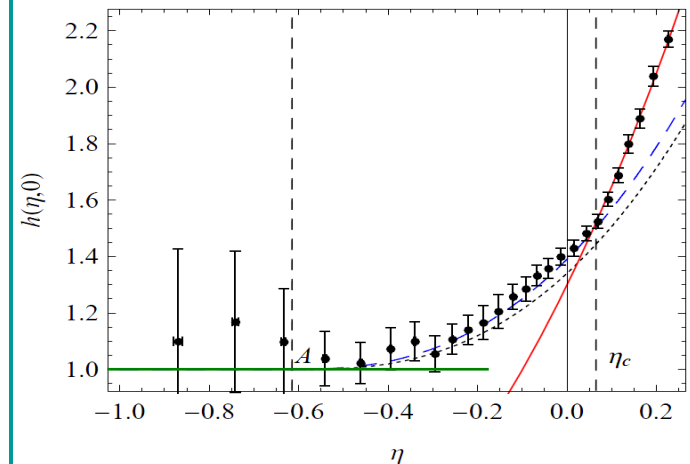
# 2, Imbalanced Fermi Gas with Zero Temperature

Superfluid:  $\eta > \eta_c$   $h_s(\eta, 0) = \frac{1}{(2\xi_s)^{3/2}} (1 + \eta)^{5/2}$

Normal mixture  $A > \eta > \eta_c$

$$h_n(\eta, 0) = 1 + \left( \frac{m_p^*}{m} \right)^{3/2} (\eta - A)^{5/2}$$

Full polarized ideal gas:  $\eta < A$   $h_i(\eta) = 1$





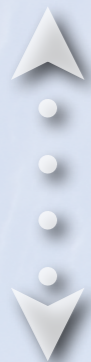
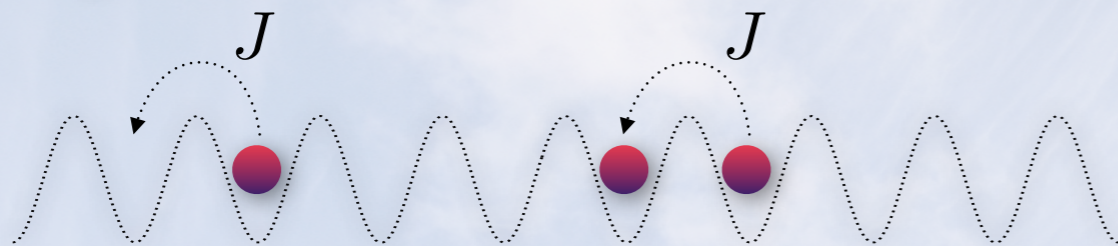
# Statistically induced Phase Transitions

arXiv:1009.2036v1

Tassilo Keilmann<sup>1,2</sup>, Simon Lanzmich<sup>2</sup>, Ian McCulloch<sup>3</sup> & Marco Roncaglia<sup>2,4</sup>

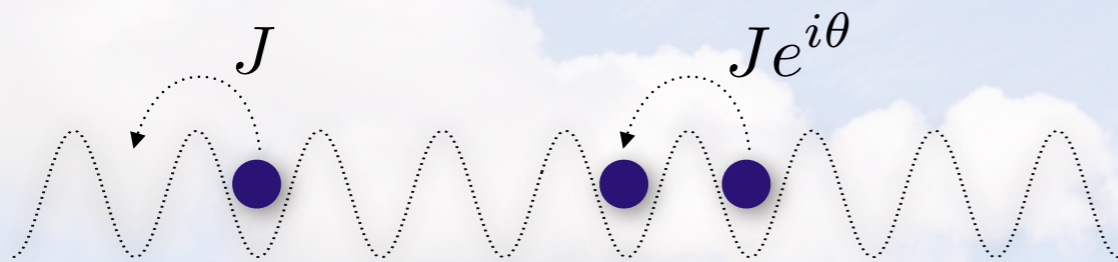
1: LMU Munich | 2: MPQ Garching | 3: Queensland University | 4: ISI Foundation Torino

## Anyons in 1D

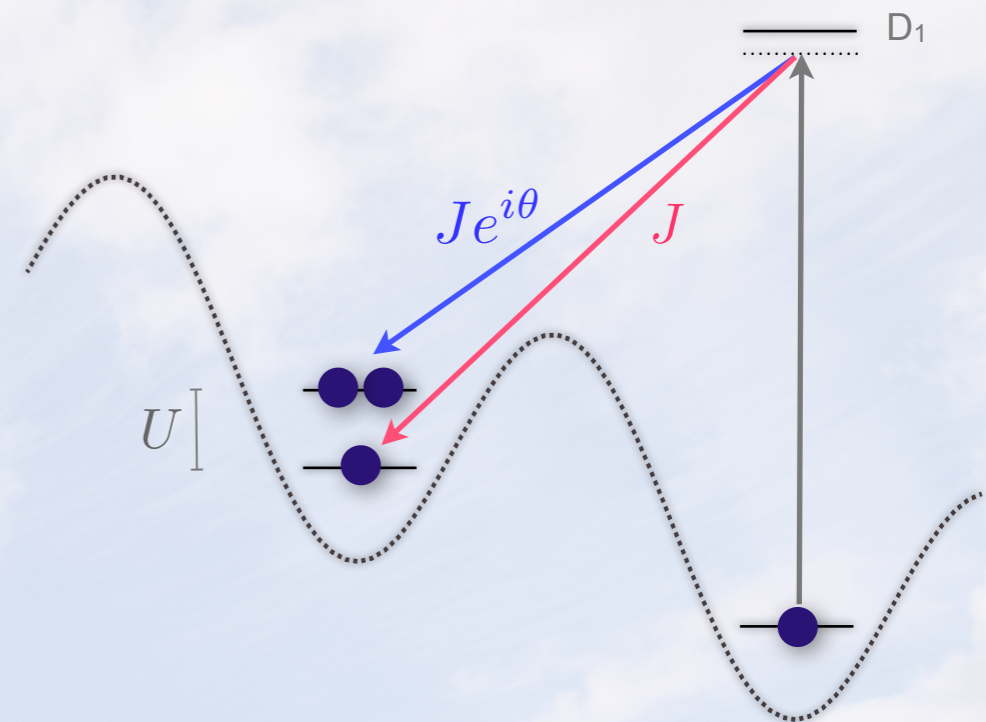


1:1 mapping

## Bosons in 1D



## Experimental proposal



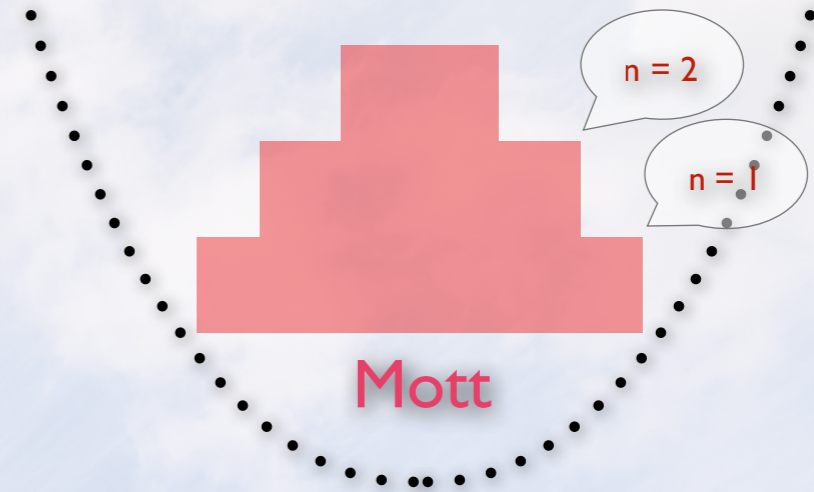
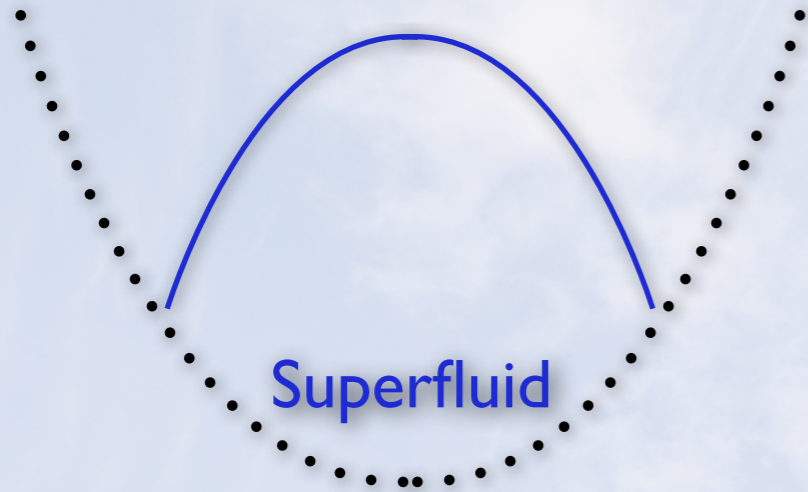


# Statistically induced Phase Transitions

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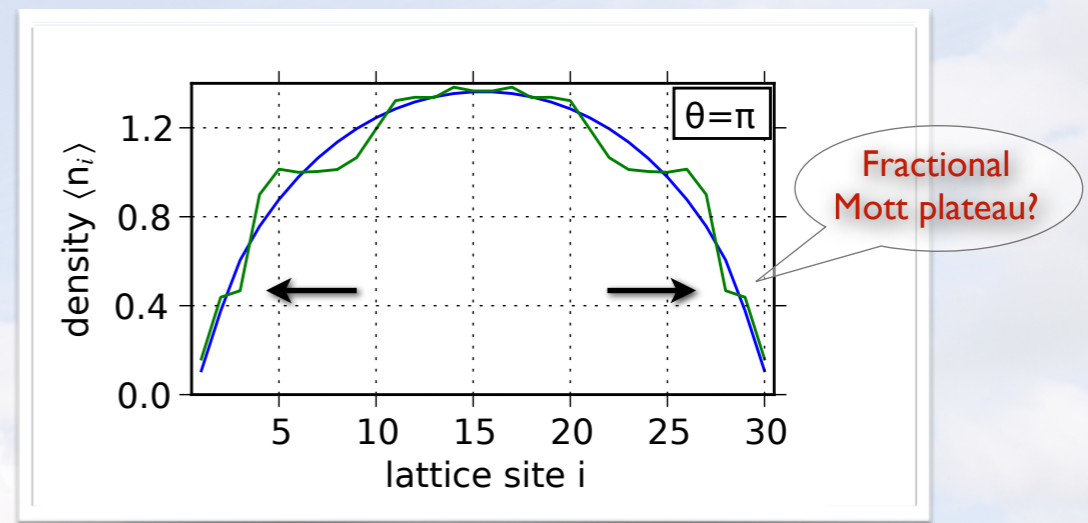
1: LMU Munich | 2: MPQ Garching | 3: Queensland University | 4: ISI Foundation Torino



bosons

a n y o n s

pseudo-fermions



# Dynamical Gauge Fields on Optical Lattices : A Lattice Gauge Theorist Point of View

Yannick Meurice, University of Iowa

- Dynamical gauge fields are essential to recover the main features of strong interactions (confinement, mass gap, chiral symmetry breaking, asymptotic freedom) in lattice gauge theory simulations.
- “Pure gauge” (no fermions or scalars) MC simulations are fast and easy but simulations involving fermions are very demanding (calculations of determinants and propagators). Simulations at real time or with a chemical potential have a sign problem. I propose two strategies to use optical lattices to mimic lattice gauge theory simulations.
- Strategy I: Engineer *quantum* link variables with plaquette interactions. They would play the role of (dynamical) hopping parameters for the atoms located at the sites of the optical lattice. An underlying local gauge invariance is highly desirable.

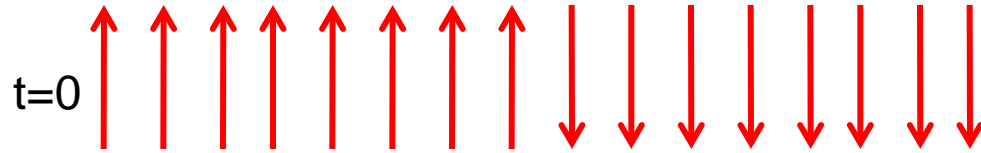


- Strategy II: Use numerical link variables as obtained in a MC simulation and replace the classical calculations of the fermion determinants and propagators in a fixed gauge background by measurements of fermion correlations on the optical lattice. This possibility requires the ability to manipulate locally the hopping parameters.

## Challenges

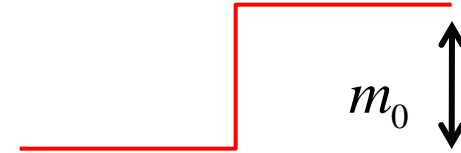
- Relativistic fermions with global color (from hyperfine levels).
- Dynamical link variables as condensates:  $U_{\mathbf{x},\mathbf{e}_i}^{ab} = \phi_{\mathbf{x}}^{*a} \phi_{\mathbf{x}+\mathbf{e}_i}^b$  .
- Local manipulation of hopping parameters.
- Local symmetry and plaquette interactions.

# TIME EVOLUTION OF AN INITIAL DOMAIN WALL PROFILE IN THE XX MODEL



Initial Energy density

$$\frac{E}{L} = \frac{1}{\pi} \cos(\pi m_0)$$

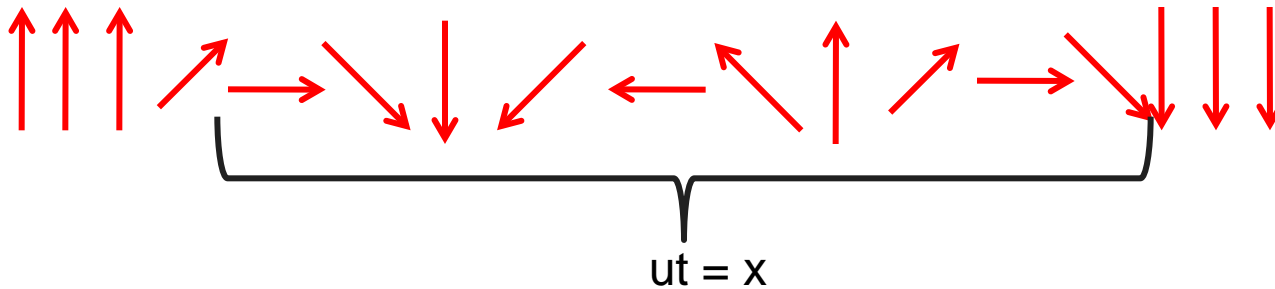
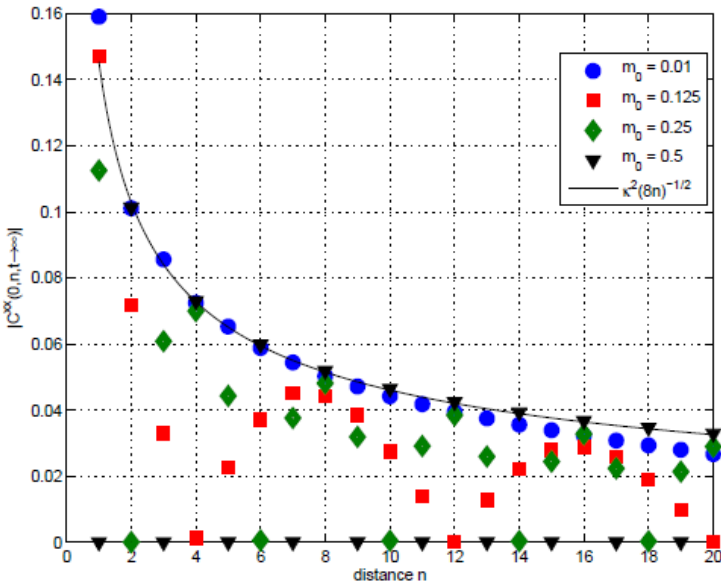


Wavelength of the inhomogeneity depends on the initial domain wall height

$$C^{xx}(j, j+n, t) \xrightarrow{t \rightarrow \infty} C_{eq}^{xx}(n) \cos\left(\frac{2\pi n}{\lambda}\right)$$

$$\lambda = \frac{2}{m_0} \quad C_{eq}^{xx}(n) \approx \frac{1}{\sqrt{8n}} \kappa^2$$

Energy density of the XX model =  $2C^{xx}(n=1) = \frac{1}{\pi} \cos(\pi m_0)$

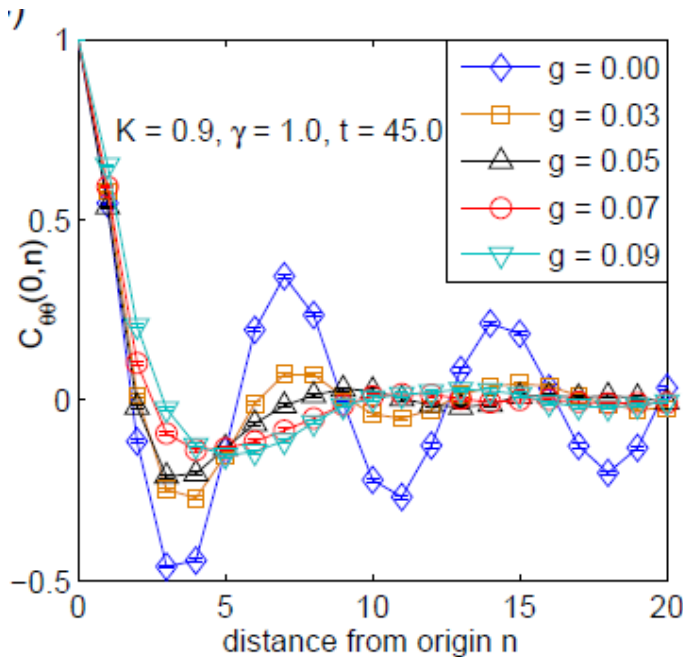
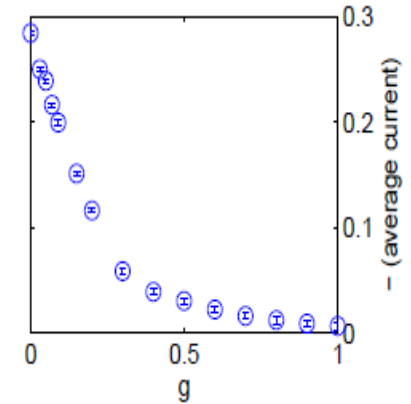
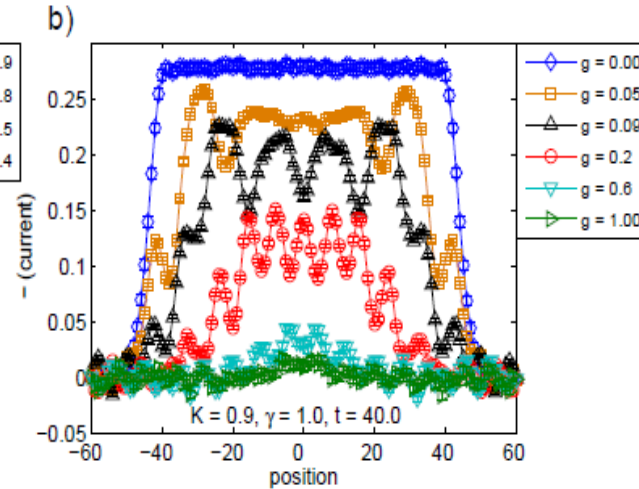
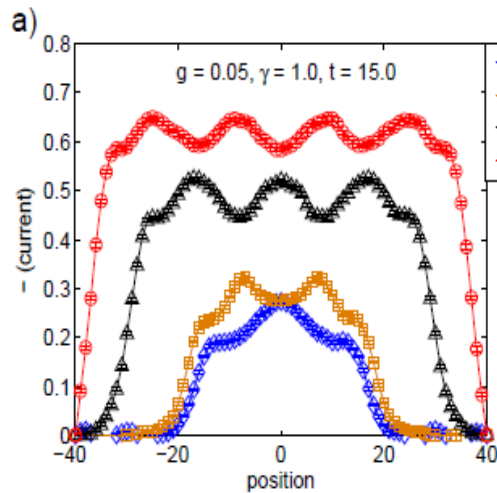


$$\frac{dS^z}{dt} = -\frac{dj}{dx}$$

$$j_l = iJ [S_l^+ S_{l+1}^- - S_l^- S_{l+1}^+]$$

Net spin current  $\frac{J}{\pi} \sin[\pi m_0]$

# TIME EVOLUTION OF AN INITIAL DOMAIN WALL PROFILE IN THE QUANTUM SINE-GORDON MODEL USING TRUNCTATED WIGNER APPROXIMATION



Current persists even in the presence of a back-scattering interaction. Consistent with quench at the Luther-Emery point

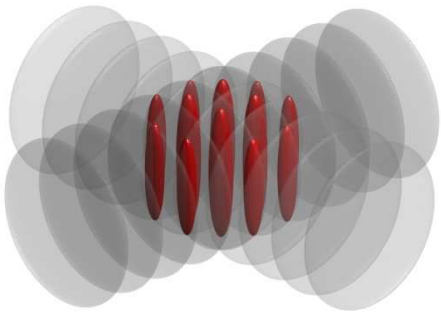
$$H'_f = H'_i(\mu=0) + m \int dx \left[ \psi_R^\dagger(x) \psi_L(x) + \psi_L^\dagger(x) \psi_R(x) \right]$$

$$j = u \left[ \psi_R^\dagger \psi_R - \psi_L^\dagger \psi_L \right]$$

$$j_0 = \mu / \pi$$

$$j = j_0 - (m/\pi) \tan^{-1} (j_0 \pi / m)$$

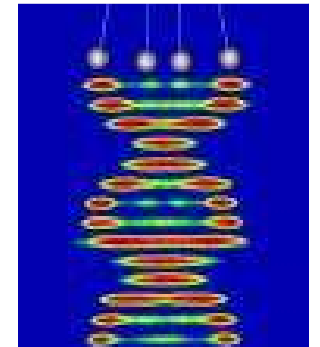
# Dynamics of repulsively and attractively interacting bosons in 1D after an interaction quench



**Dominik Muth, Michael Fleischhauer**

New J. Phys. 12, 083065 (2010)

Phys. Rev. Lett. 105, 150403 (2010)

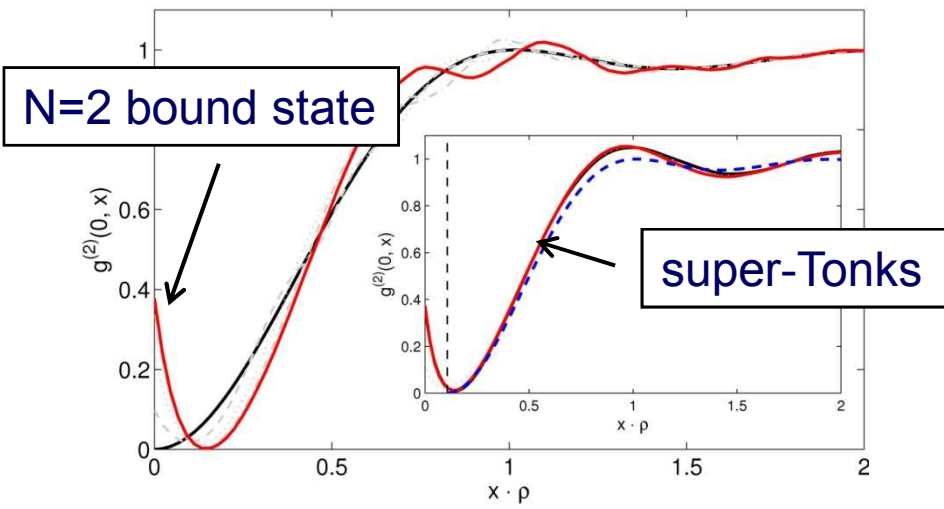
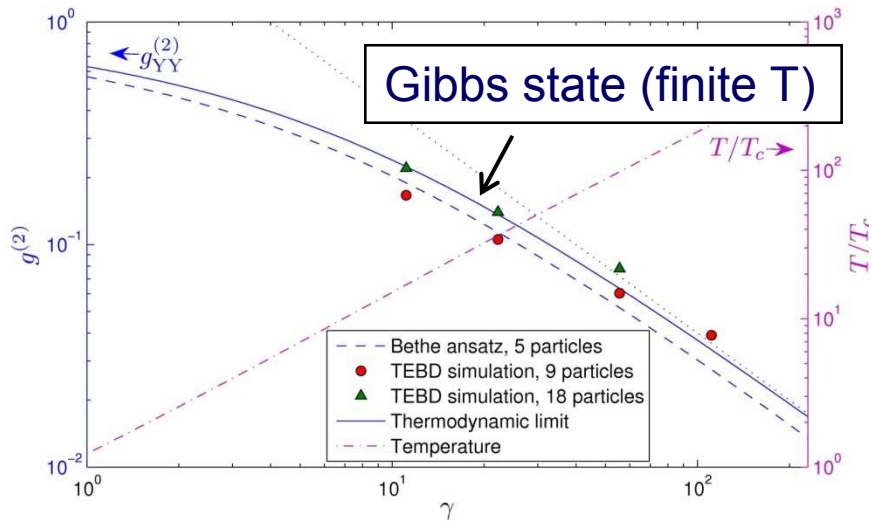
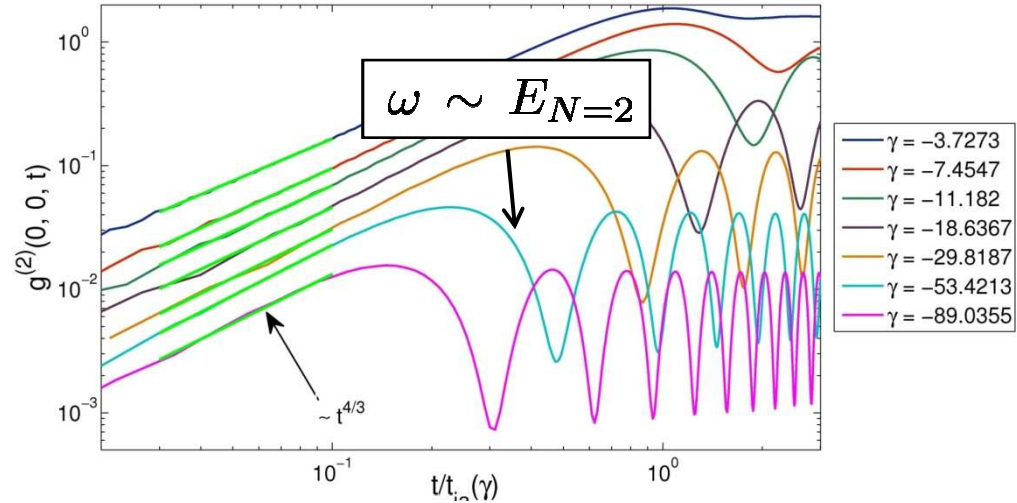
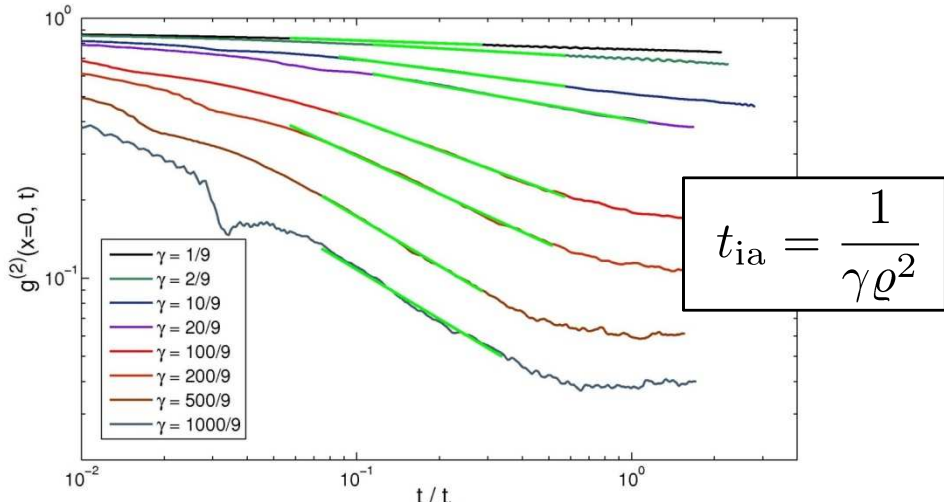


- quench dynamics of strongly interacting systems
- thermalisation of local quantities?

method: TEBD (strong interactions) adapted to continuous systems, lattice approximation with  $L > 1000$

$$\gamma = 0 \rightarrow \gamma \gg 1$$

$$\gamma = +\infty \rightarrow \gamma \ll -1$$



fast thermalization of local quantities

superposition sTG + bound pairs

# Universal Fermi gases in *mixed* dimensions

Dimensionality of space can be controlled  
in cold atom experiments by strong optical lattices

✓ 3D → 2D → 1D and more ?

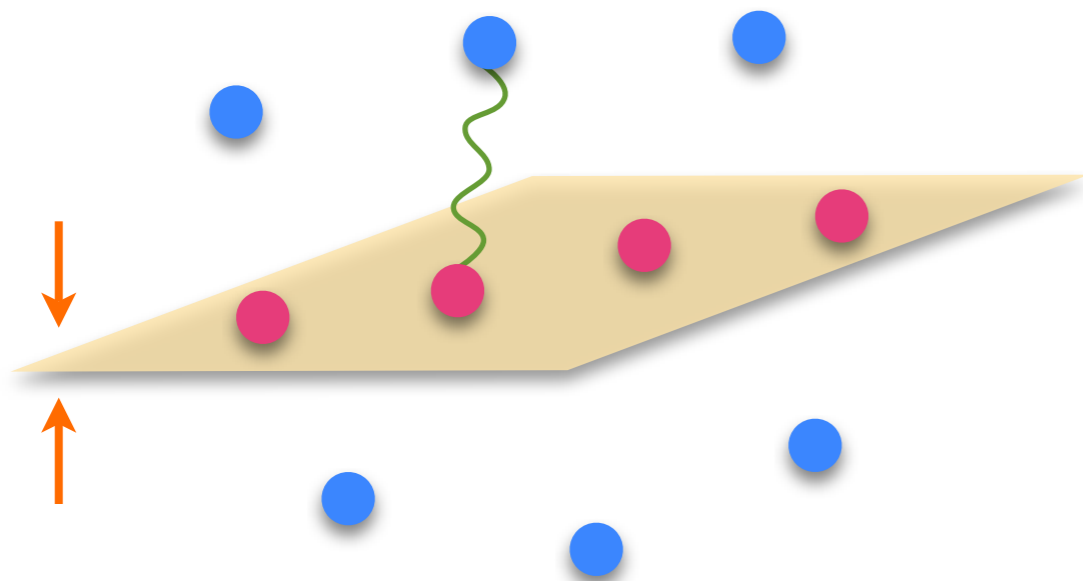
# Universal Fermi gases in *mixed* dimensions

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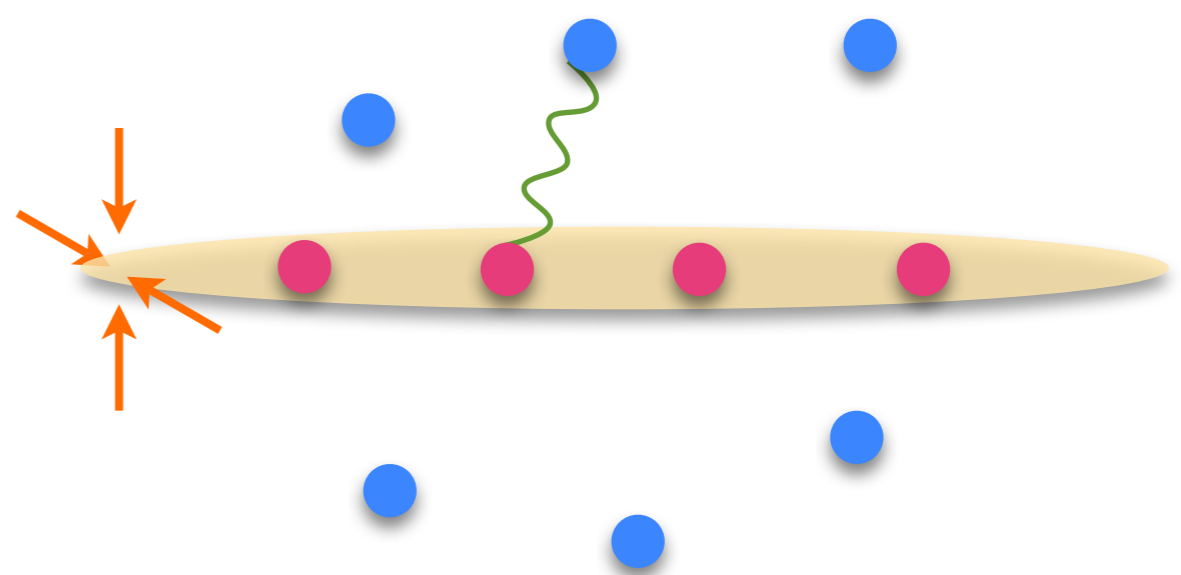
✓ 3D → 2D → 1D and more ?

✓ mixed dimensions

2D-3D mixture



1D-3D mixture



# Universal Fermi gases in *mixed* dimensions

✓ 2-body physics

✓ 3-body physics

✓ many-body physics



# Universal Fermi gases in *mixed* dimensions

## ✓ 2-body physics

S-wave Feshbach resonance in a free space

➡ s-wave, p-wave, d-wave, ... resonances in mixed D

➡ long-lived BEC of p-wave molecules

## ✓ 3-body physics

## ✓ many-body physics

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Efimov effect for fermions occurs for  $m_A/m_B > 13.6$  in a free space

➡  $m_A/m_B > 6.35$  in 2D-3D &  $m_A/m_B > 2.06$  in 1D-3D

➡ realization of the Efimov effect for fermionic  $^{40}\text{K}$ - $^{40}\text{K}$ - $^6\text{Li}$

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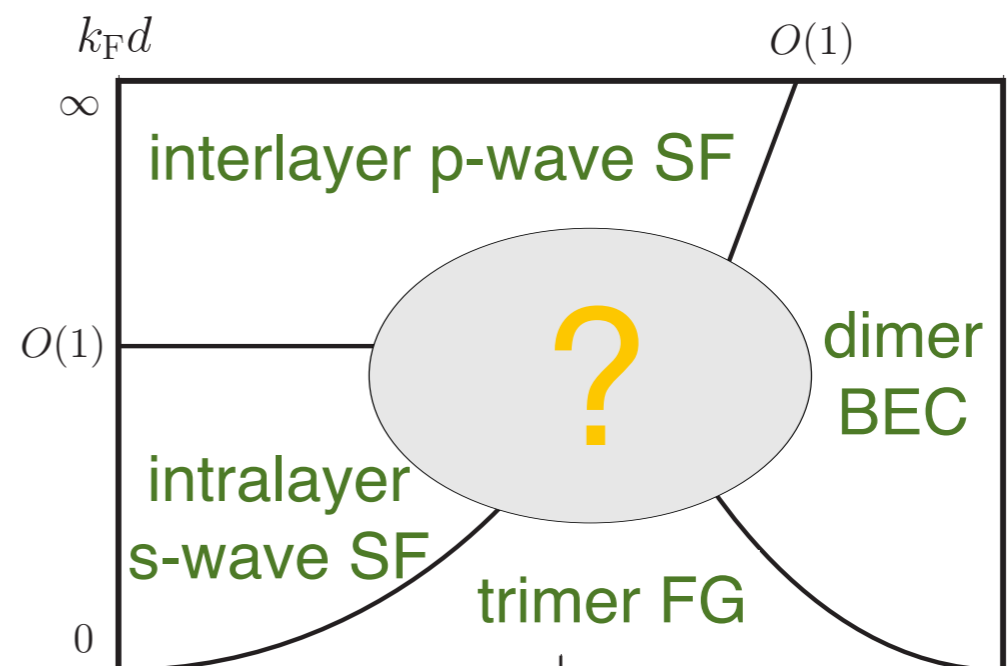
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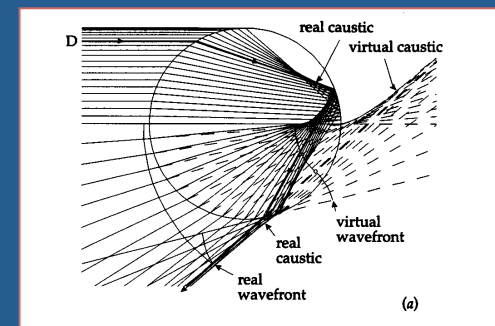
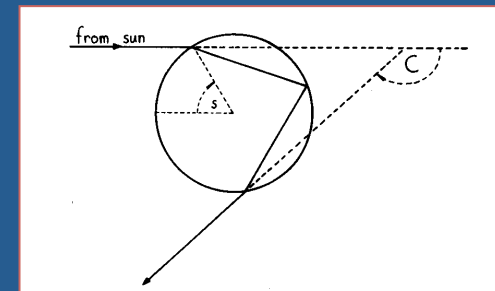
## ✓ many-body physics

Bilayer Fermi-Fermi mixture  
shows very rich phase diagram



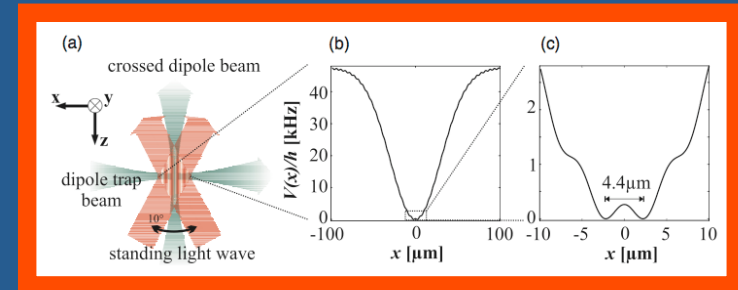
# Rainbows in the atomic Josephson Junction

Duncan O'Dell  
McMaster University

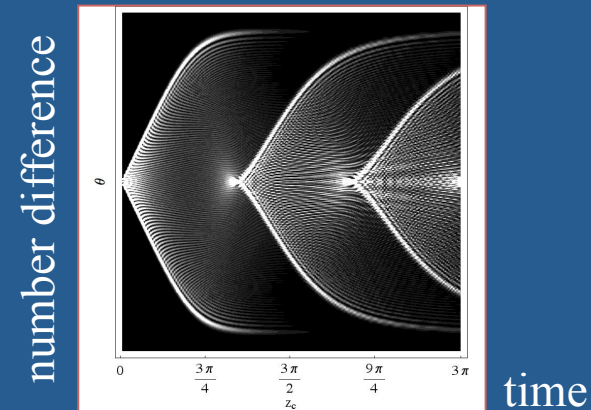


# Rainbows in the atomic Josephson Junction

Atomic Josephson junction setup of Oberthaler group, Heidelberg. For review see R. Gati and M.K. Oberthaler, J. Phys. B **40**, R61 (2007).

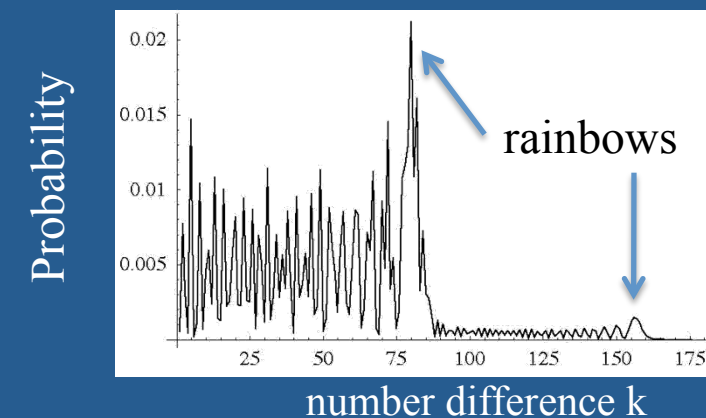


Time dynamics of number difference between two wells when two BECs are suddenly brought into contact.



Classical field theory (GPE) diverges at particular values of number difference (the rainbow). Divergence is cured by 2<sup>nd</sup> quantizing.

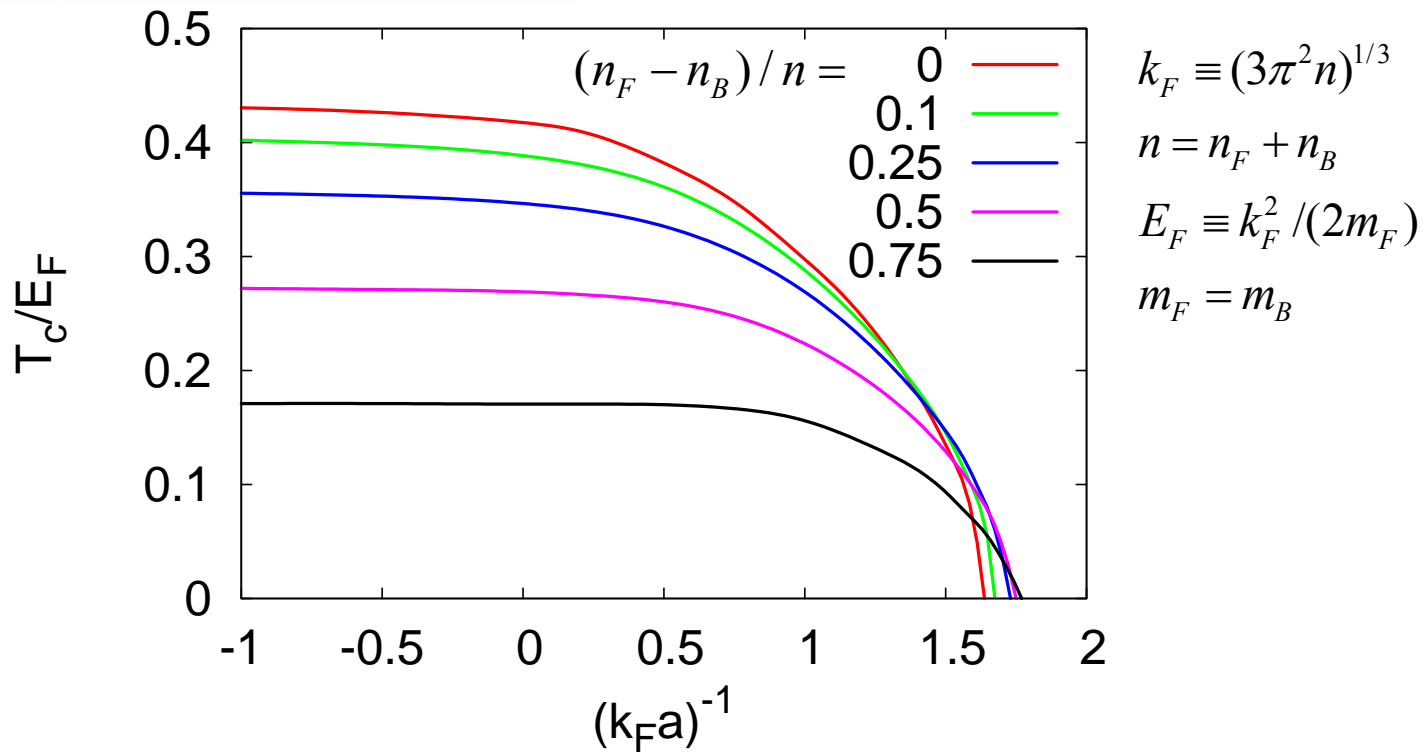
$$\Psi(k_{\text{rainbow}}) \sim \mathcal{O}(1/\hbar^{1/3})$$



# Pairing and condensation in a resonant Bose-Fermi mixture



Elisa Fratini and Pierbiagio Pieri  
University of Camerino, Italy



Boson condensation critical temperature vs Bose-Fermi coupling



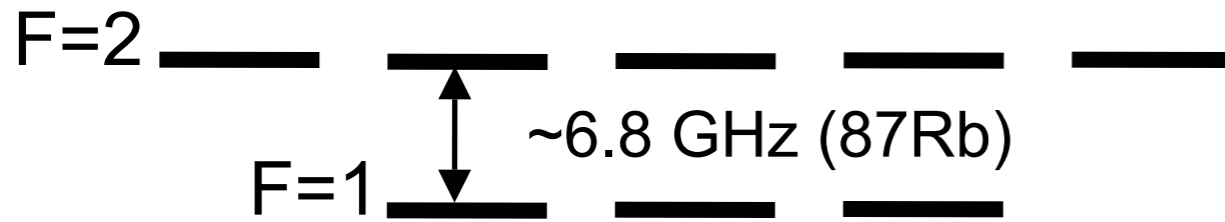
# Quantum Simulations with Optical Superlattices



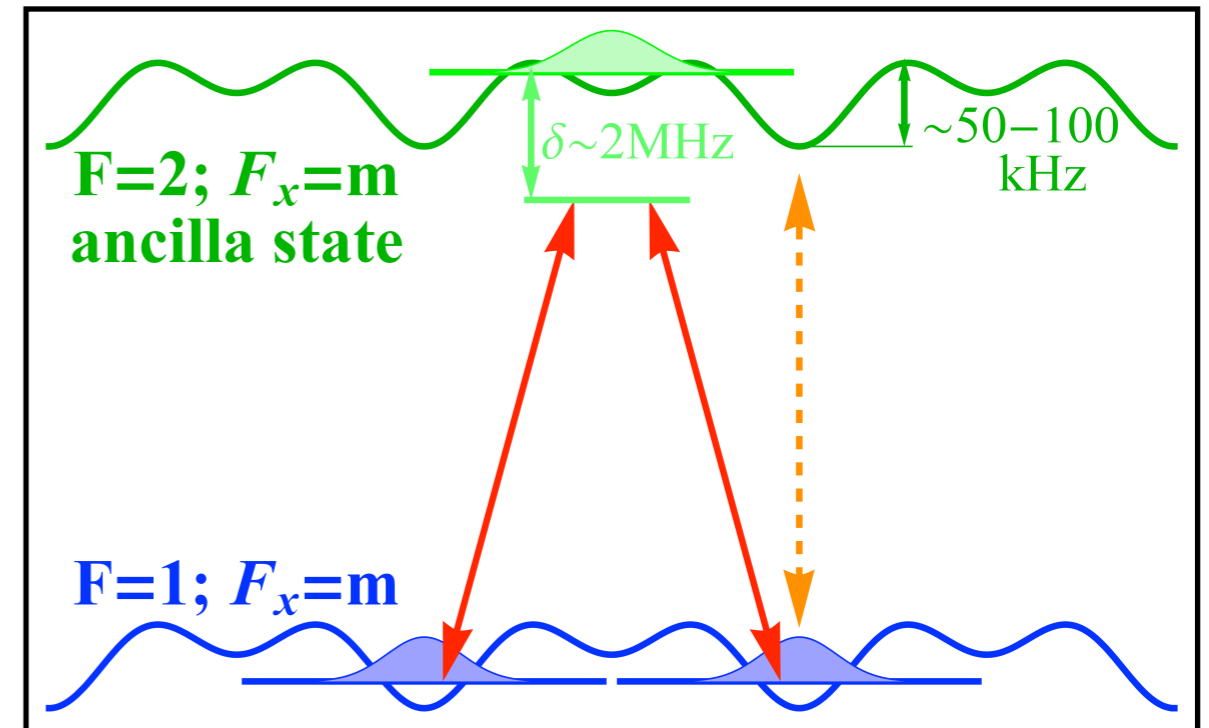
L.Mazza, M.Rizzi, M.Lewenstein, J.I.Cirac



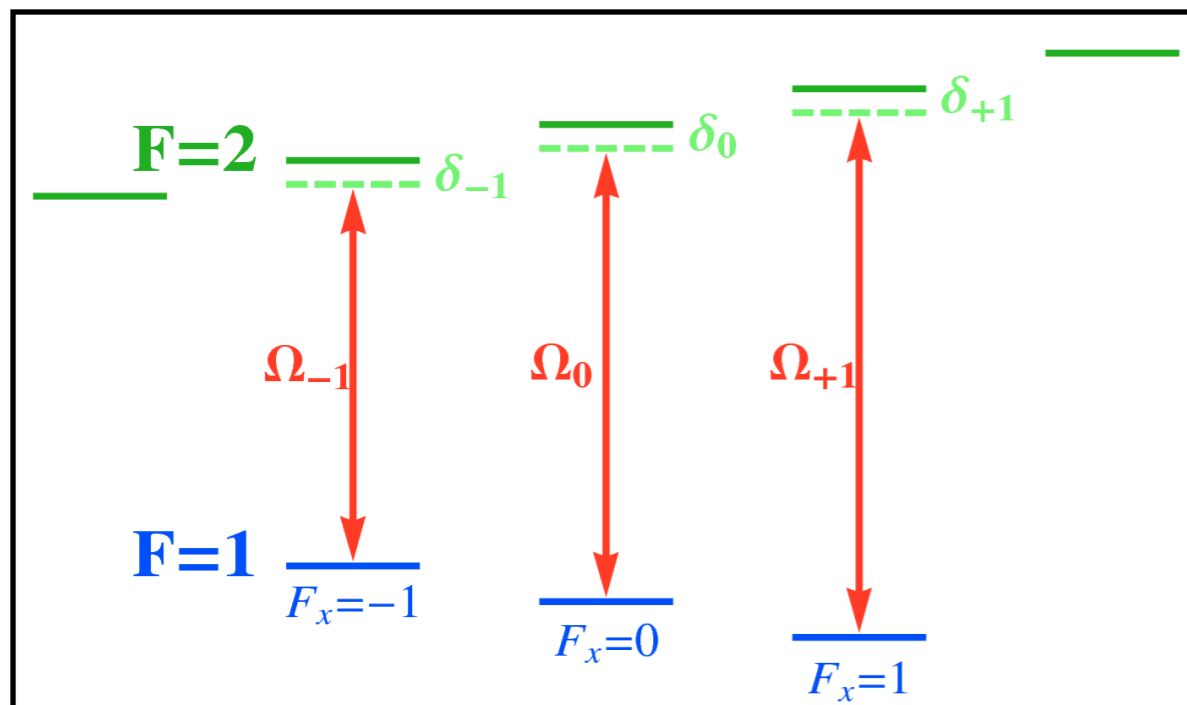
## spin-independent optical superlattices



## Raman realisation of non-trivial hopping operators



## Zeeman effect allows for spin-dep. control



It works in principle in 1D, 2D, 3D!

Extendable to all the alkalis!

Fermions and Bosons!

Original idea conceived with Ulrich Schneider

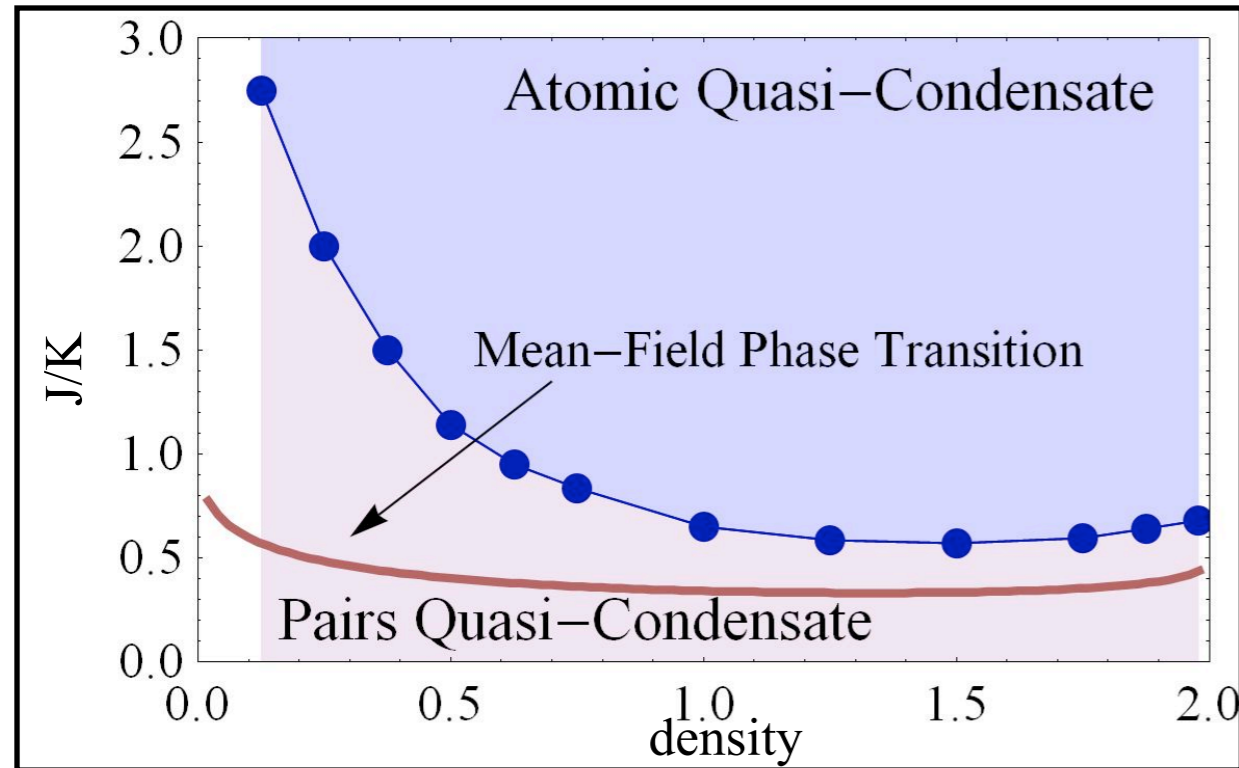
# 1D 3-hardcore bosons $(a_i^+)^3 = 0$

$$H = -J \sum_i a_i^+ a_{i+1} - K \sum_i (a_i^+)^2 a_{i+1}^2 + H.c.$$

density  $\leftrightarrow$  magnetization of the spin condensate

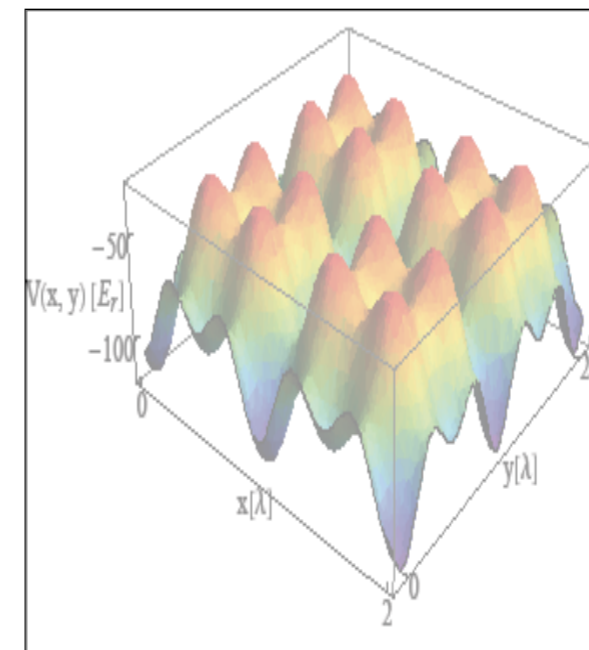
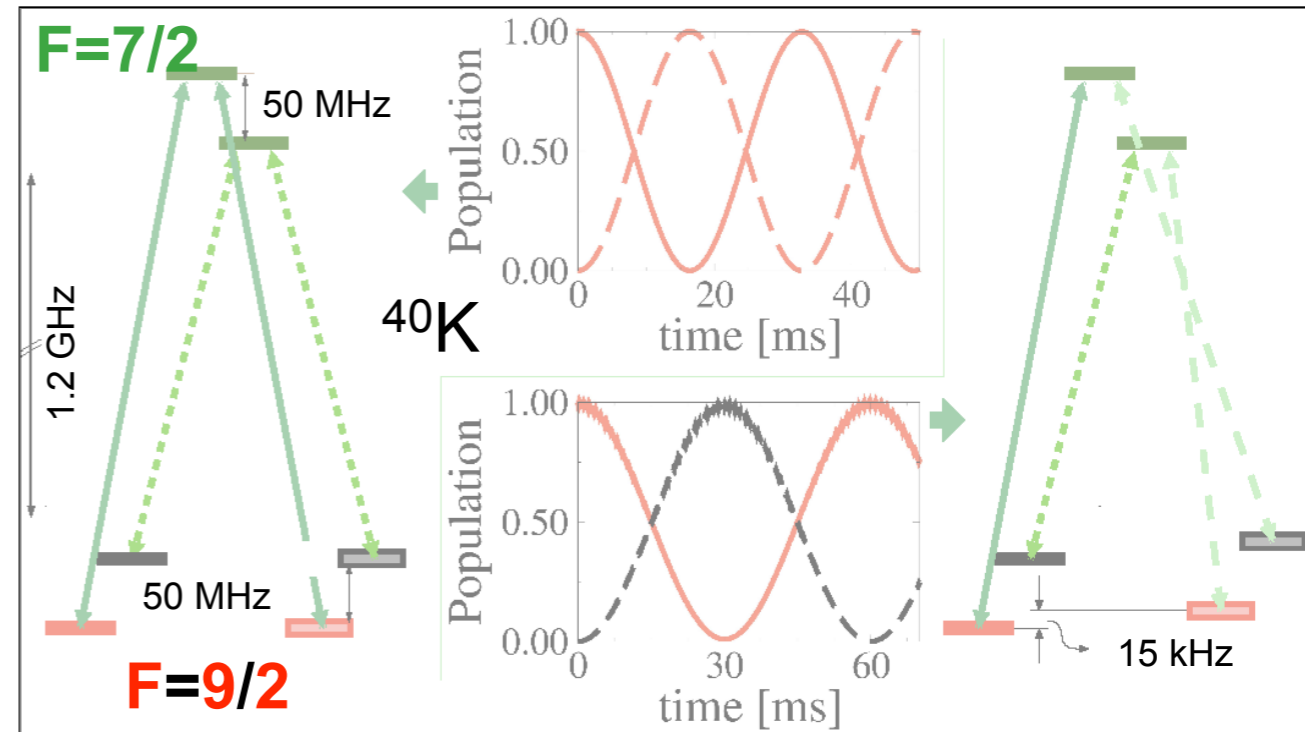
$J/K$  tuned modifying the hopping of  $m_z=0$  species

	$\langle a_i^+ a_{i+\delta} \rangle$	$\langle (a_i^+)^2 a_{i+\delta}^2 \rangle$
AQC	algebraic in $\delta$	
PQC	exponential in $\delta$	algebraic in $\delta$



Mazza, Rizzi, Lewenstein, Cirac  
arXiv:1007.2344 (PRA)

# Fermionic Models & Non-diagonal Hopping



## Goals

- 3D Dirac fermions
- Massive Fermions
- Wilson Fermions
- Axion Electrodynamics

Bermudez, Mazza, Rizzi, Goldman,  
Lewenstein, Martin-Delgado  
arXiv:1004.5101 (PRL)



# Localized and Extended States in Disordered Traps

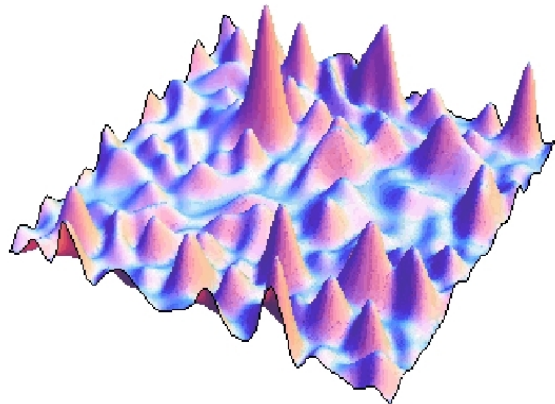
Luca Pezzè and Laurent Sanchez-Palencia

Institut d'Optique and CNRS  
(Palaiseau, France)

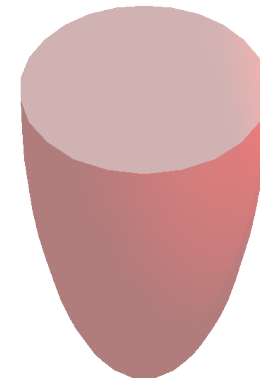
arXiv:1006:4049

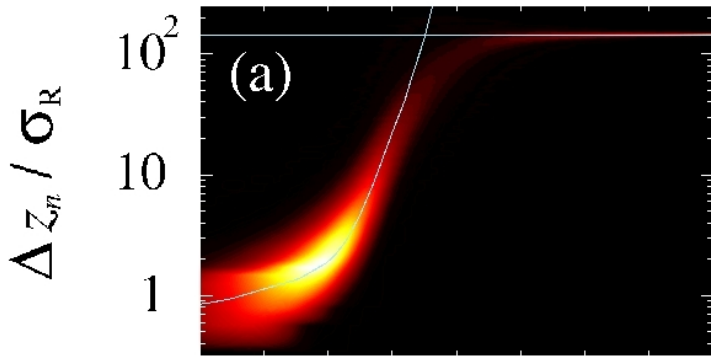
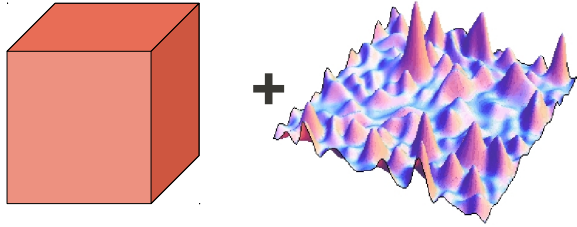
$$\hat{H} = -\hbar^2 \nabla^2 / 2m + \underbrace{V(\mathbf{r})}_{\text{Disordered potential}} + \underbrace{V_T(\mathbf{r})}_{\text{inhomog. trap}}$$

**Disordered potential**  
(eg. speckle field)

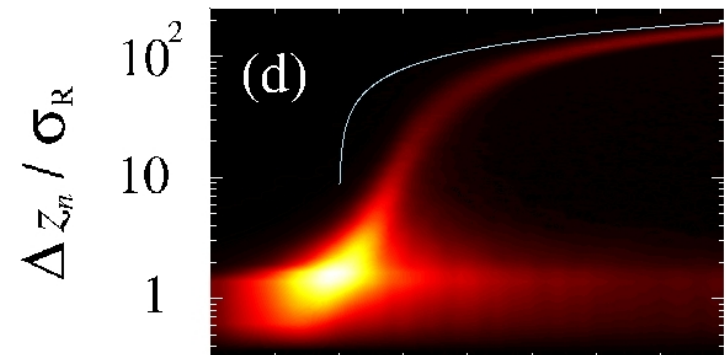
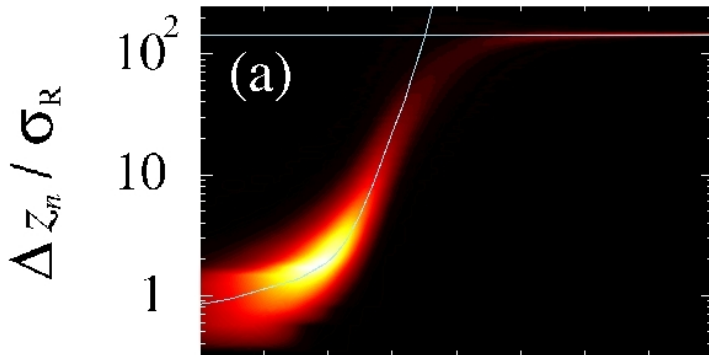
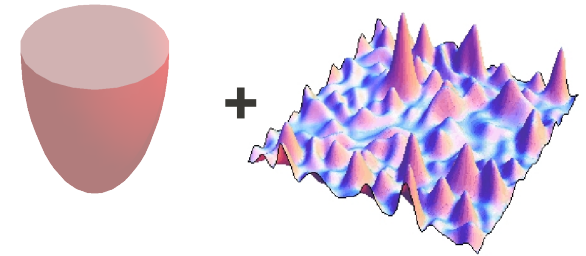
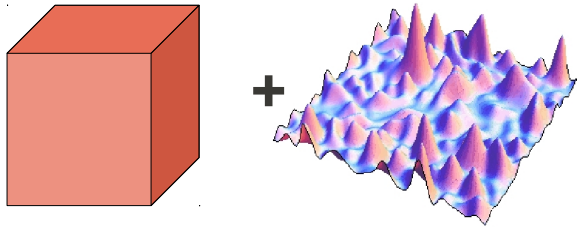


inhomog. trap





- ▶  $L_{\text{loc}} \nearrow$  with  $V_R$
- ▶ No coexistence of localized & extended states
- ▶ Mott's argument



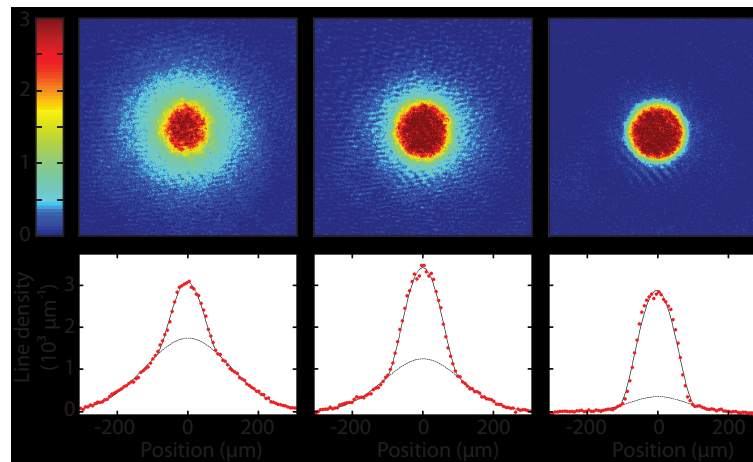
- ▶  $L_{\text{loc}} \nearrow$  with  $V_R$
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- ▶ Mott's argument

- ▶ Coexistence of localized & extended states
- ▶ Beyond finite-size effect

# Degenerate Bose Gases With Tuneable Interactions

R. Smith, R. Campbell, N. Tammuz, S  
Beattie, S. Moulder and Z. Hadzibabic

- Recently  $^{39}\text{K}$  has proved a promising candidate for a Bose gas with tuneable interactions
- Unfortunately  $^{39}\text{K}$  is difficult to cool to degeneracy; this had only been achieved in one group [1]
- We describe the second experimental apparatus to produce a  $^{39}\text{K}$  BEC and the optimisation which allowed us to increase the condensate number to over  $4 \times 10^5$ .

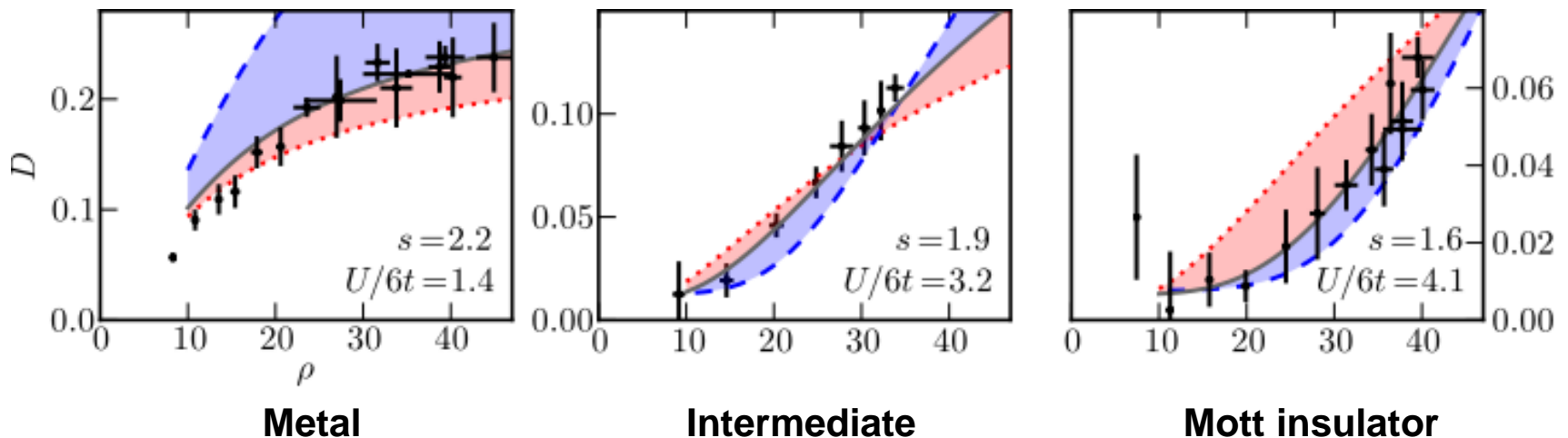


# Quantitative study of the metal-Mott insulator transition with ultracold fermions in an optical lattice

Leticia Tarruell, ETH Zürich

Probe: occupation of lattice sites

*Mott insulator: reduced number fluctuations  $\rightarrow$  reduced double occupancy*



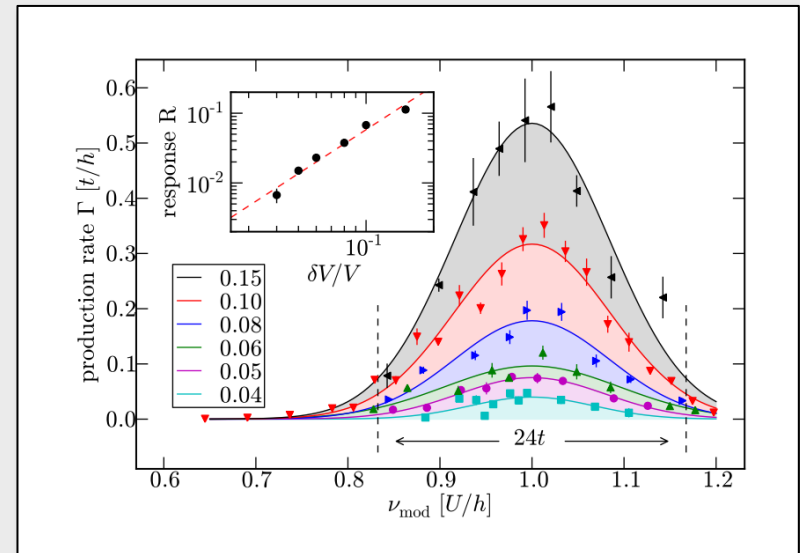
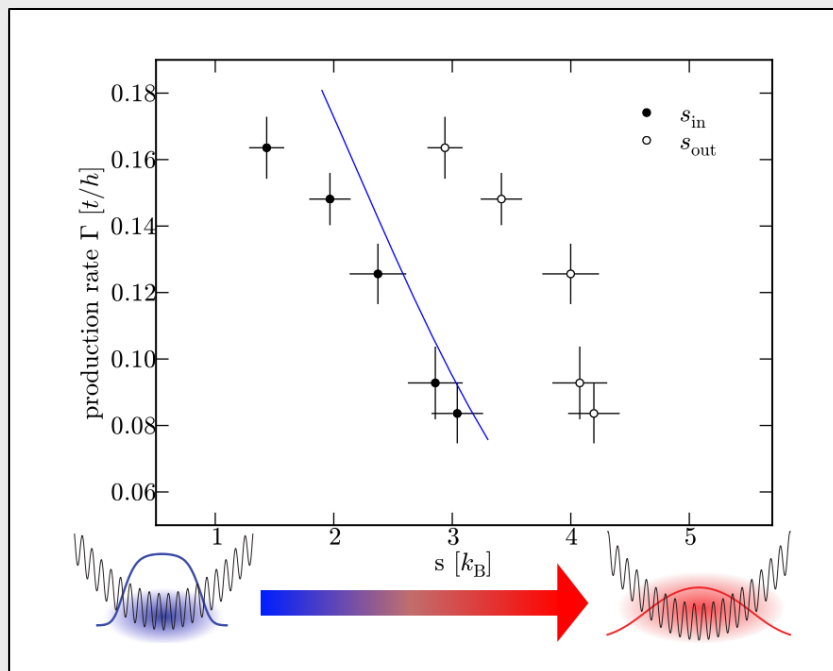
Quantitative agreement with DMFT and high temperature series expansions  
Determine entropy in the lattice

# Probing nearest-neighbor correlations

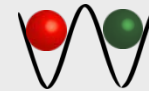
Modulation of the lattice depth  
in the ***perturbative regime***

2<sup>nd</sup> order perturbation theory

Response: doublon production rate



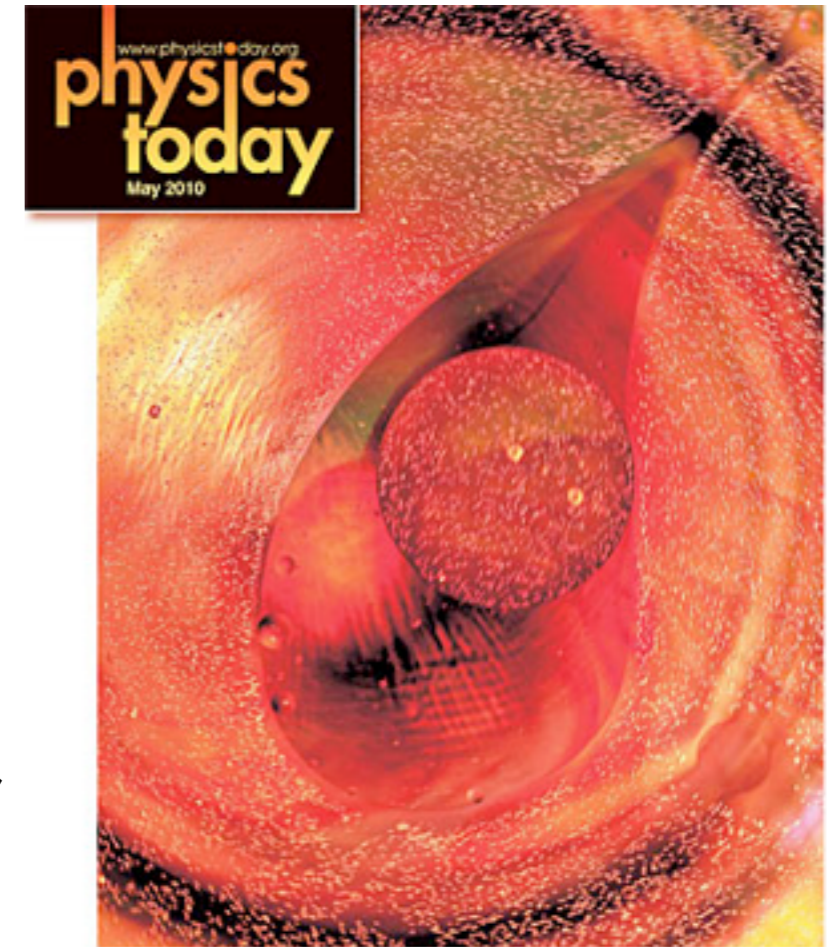
Determine nearest-neighbor  
density and spin correlation function



Useful for thermometry

# Viscosity sum rules and spectral functions

Edward Taylor  
The Ohio State University



In search of perfect fluids

A publication of the American Institute of Physics

- We derive sum rules for the frequency dependent shear  $\eta$  and bulk  $\zeta$  viscosities in a dilute Fermi gas:

$$\frac{1}{\pi} \int_0^{\infty} d\omega \left[ \eta(\omega) - \frac{C}{10\pi\sqrt{m\omega}} \right] = \frac{\varepsilon}{3} - \frac{C}{10\pi ma}$$

$$\frac{1}{\pi} \int_0^{\infty} d\omega \zeta(\omega) = \frac{1}{72\pi ma^2} \left( \frac{\partial C}{\partial a^{-1}} \right)_s$$

- $C$  = contact (prob. of finding two fermions close together);  $a$  = s-wave scattering length;  $\varepsilon$  = energy density.



ET & Mohit Randeria, PRA **81**, 053610 (2010)





# Bulk viscosity

$$\frac{1}{\pi} \int_0^{\frac{1}{mr_0^2}} d\omega \zeta(\omega) = \frac{1}{72\pi ma^2} \left( \frac{\partial C}{\partial a^{-1}} \right)_s$$

- Bulk viscosity is zero at unitarity at all frequencies (scale invariance of w.f.):

$$\zeta(\omega) = 0 \quad \forall \omega \quad (|a| = \infty)$$

- Contact is a monotonically increasing through the crossover:

$$\partial C / \partial a^{-1} \geq 0 \quad \forall a$$

- At unitarity, shear viscosity can be measured by e.g., Bragg scattering:

$$\eta(\omega) = \lim_{q \rightarrow 0} \frac{3\omega}{4q^4} \text{Im} \chi_{\rho\rho}(q, \omega)$$

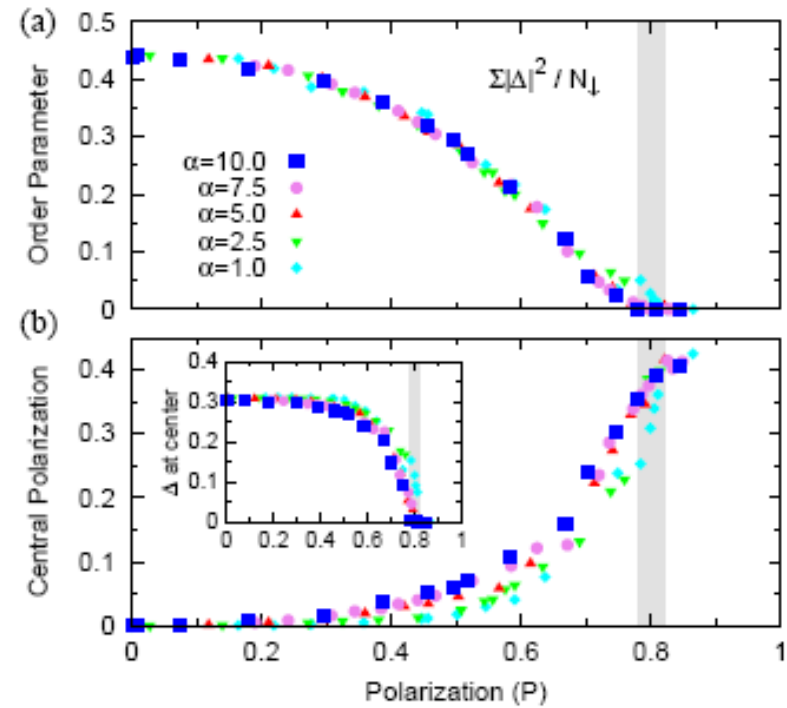
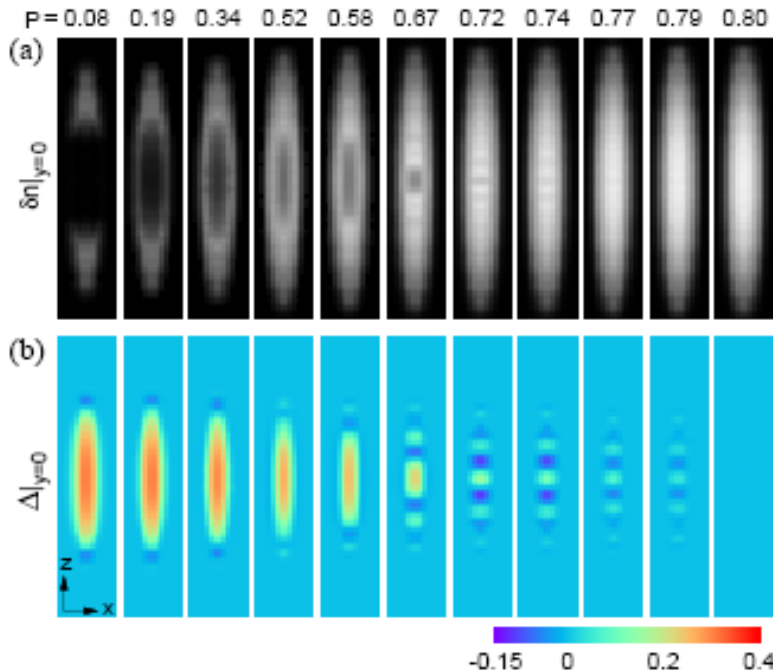
# Shear viscosity

$$\frac{1}{\pi} \int_0^{\frac{1}{mr_0^2}} d\omega \left[ \eta(\omega) - \frac{C}{10\pi\sqrt{m\omega}} \right] = \frac{\varepsilon}{3} - \frac{C}{10\pi ma}$$

- We prove that  $\rho_n=0 \Rightarrow \eta(0)=0$ .
- High-frequency  $C/\sqrt{\omega}$  tail:
  - ▶ Generic feature of high- $\omega$  response (RF, Bragg, neutron,...): At large energies, momentum conservation  $\Rightarrow$  virtual **pair** excitations. **Contact** **(C)** physics.
- At unitarity: area under “Drude peak” = energy. Also for  $N=4$  SSYM, where  $\eta(0) = s/4\pi$ .

**POSTER 1:**

**1. DMFT for imbalanced Fermi gas in elongated traps (arXiv:1009.5676)**



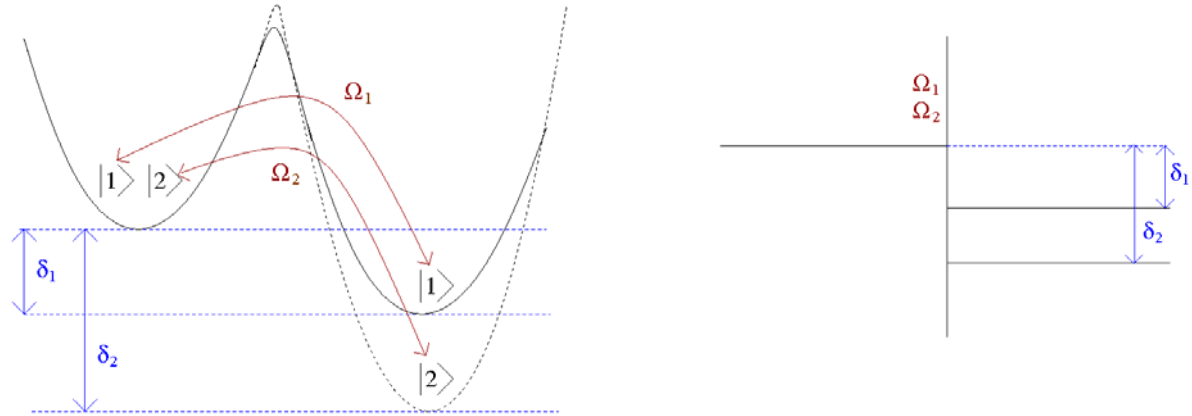
**2. Signatures of FFLO by hopping modulation (TEBD) (PRL 2010)**



Aalto University  
School of Science  
and Technology

## POSTER 2:

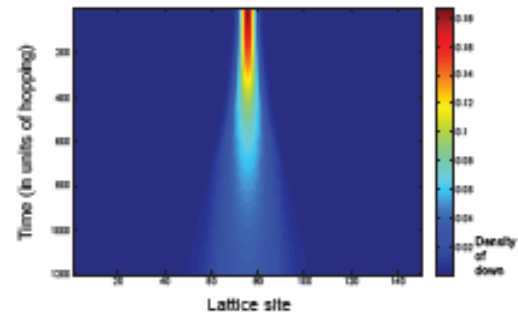
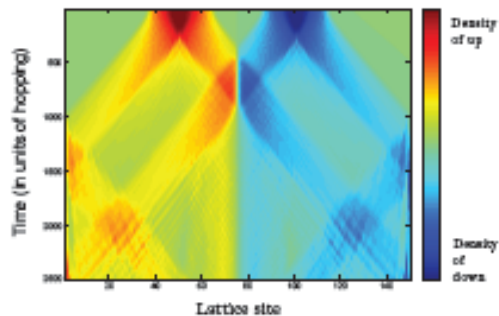
### 1. Spin-asymmetric Josephson effect (arXiv:0911.4678)



### 2. Speed of sound in a FFLO state (in preparation)

## POSTER 3:

### Dynamics (TEBD) of 1D Fermi gases (in preparation)



# Bose-Fermi solid and its quantum melting in a one-dimensional optical lattice

Bin Wang<sup>1</sup>, Daw-Wei Wang<sup>2</sup>, and Sankar Das Sarma<sup>1</sup>

*1 CMTC, Department of Physics, University of Maryland,  
College Park, Maryland 20742, USA*

*2 Physics Department and NCTS, National Tsing-Hua  
University, Hsinchu 30013, Taiwan*



# Ground state phase diagram

