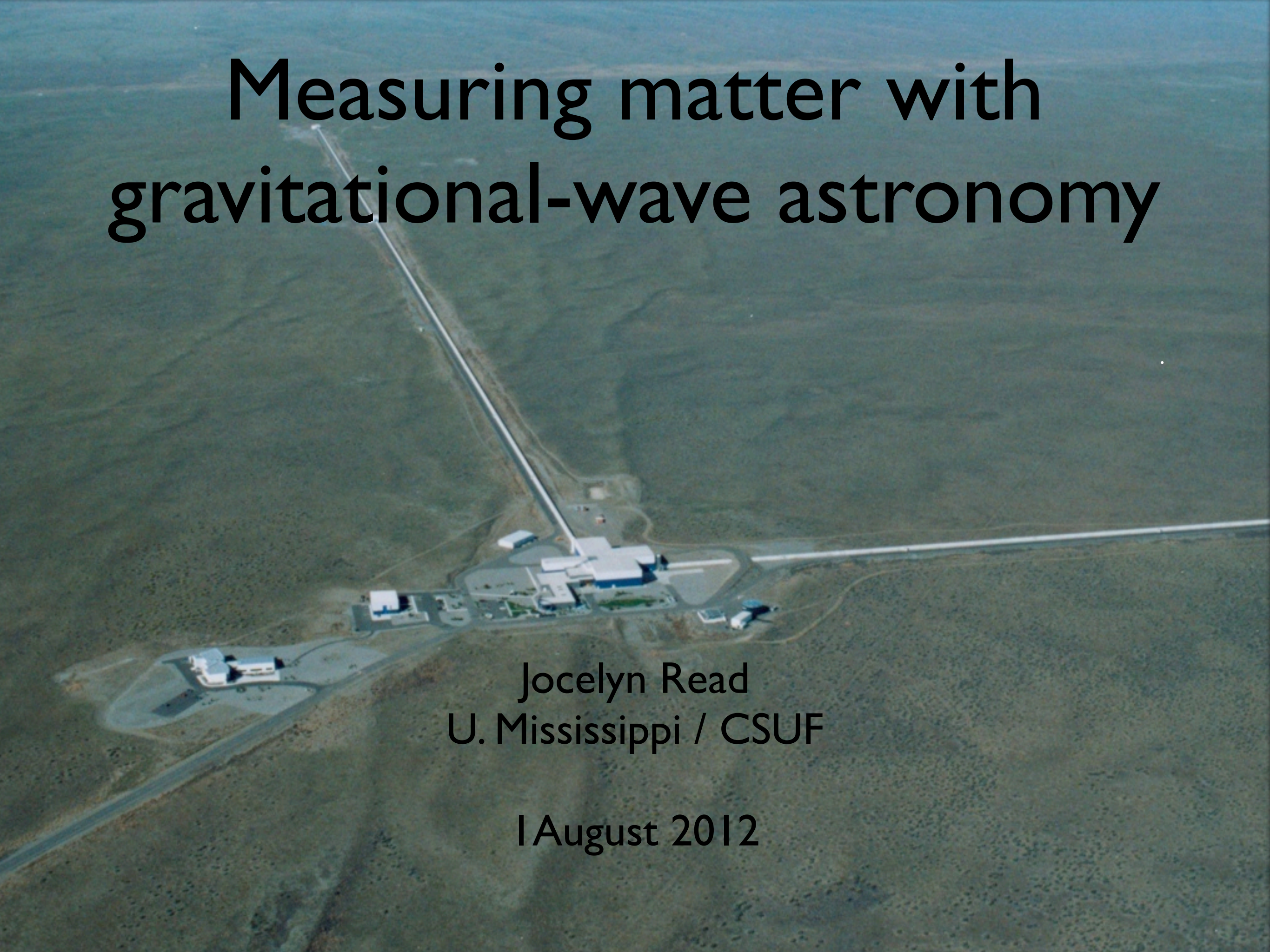


Measuring matter with gravitational-wave astronomy

An aerial photograph of the LIGO Livingston Observatory. The image shows two long, parallel vacuum tubes extending across a flat, open landscape. The tubes meet at a central hub containing several buildings, including the control room and support structures. The surrounding terrain is a mix of green and brown, suggesting a rural or semi-rural area.

Jocelyn Read
U. Mississippi / CSUF

1 August 2012

Tidal deformation in PN

NSNS: Tanja Hinderer (Maryland), Ben Lackey (Wisconsin–Milwaukee), and Ryan Lang (NASA Goddard)

BHNS: Francesco Panaralle (AEI), Frank Ohme (AEI), Luciano Rezzolla (AEI)

Numerical simulations and analysis

L. Baiotti (Osaka), J. Creighton (Wisconsin–Milwaukee), J. Friedman (Wisconsin–Milwaukee), B. Giacomazzo (JILA), K. Kyutoku (YITP), C. Markakis (Wisconsin–Milwaukee), L. Rezzolla (AEI), M. Shibata (YITP), and K. Taniguchi (Tokyo),

QCD phase diagram

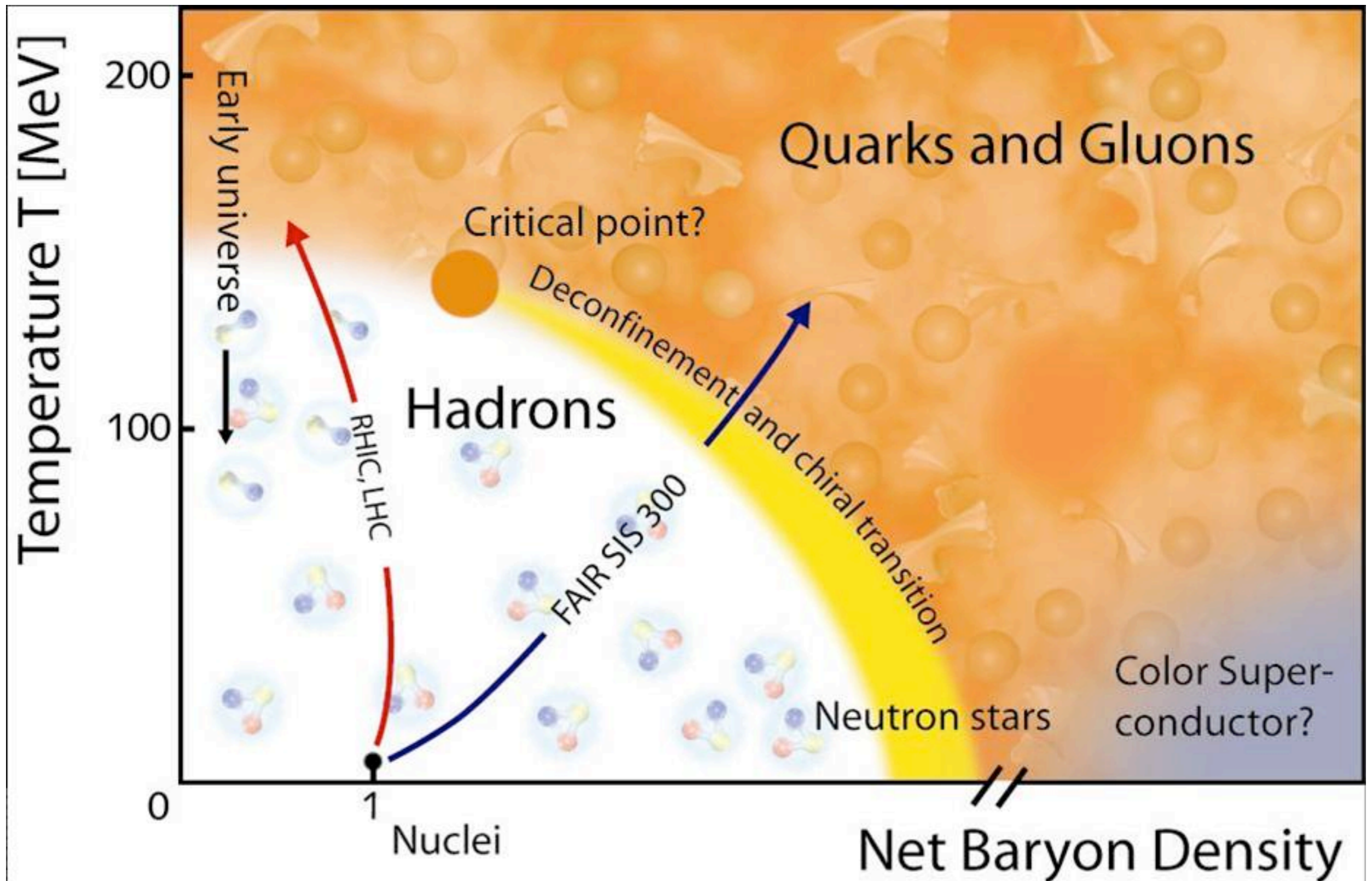


figure from FAIR CBM experiment

QCD phase diagram

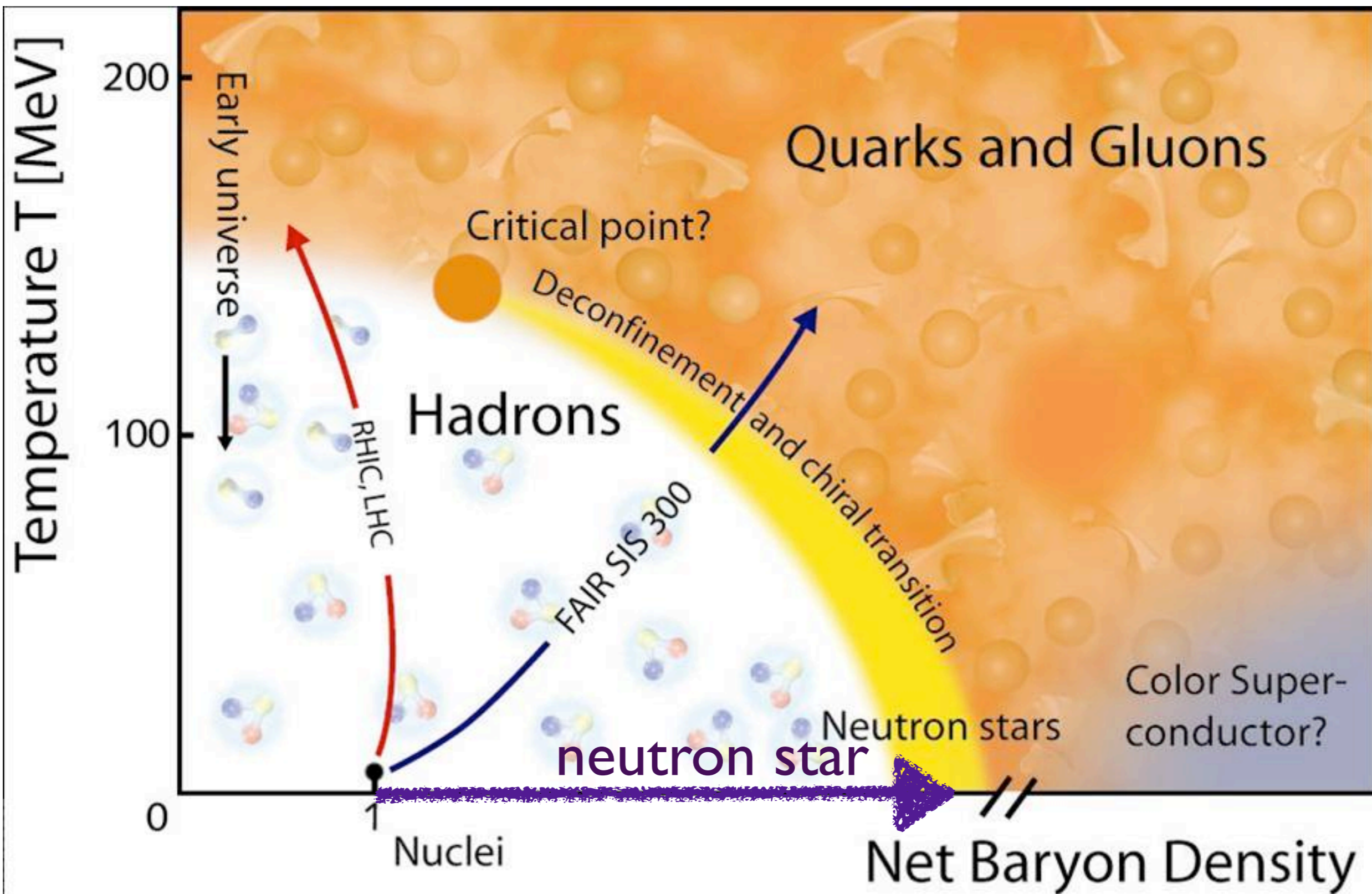


figure from FAIR CBM experiment

QCD phase diagram

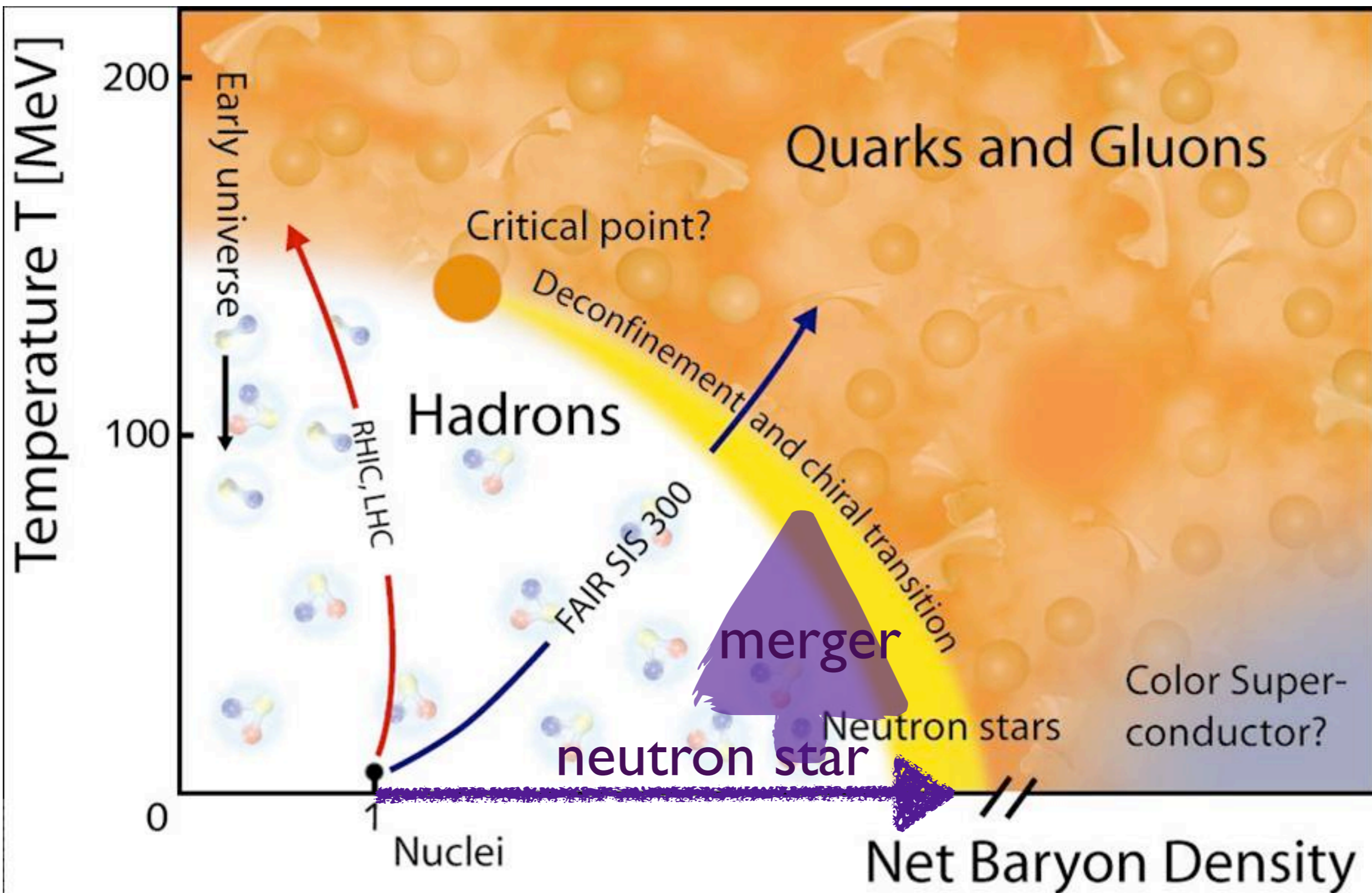
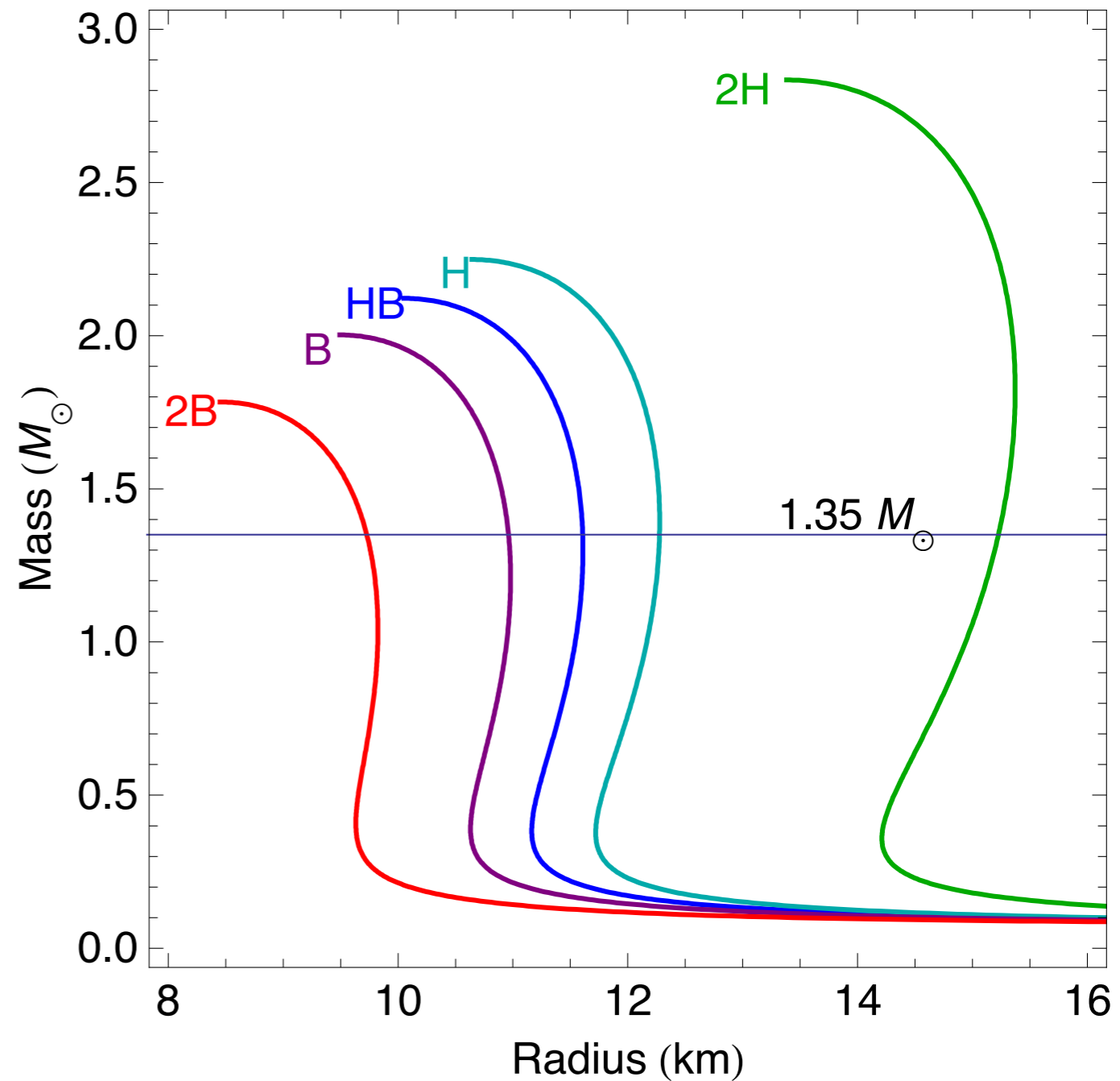
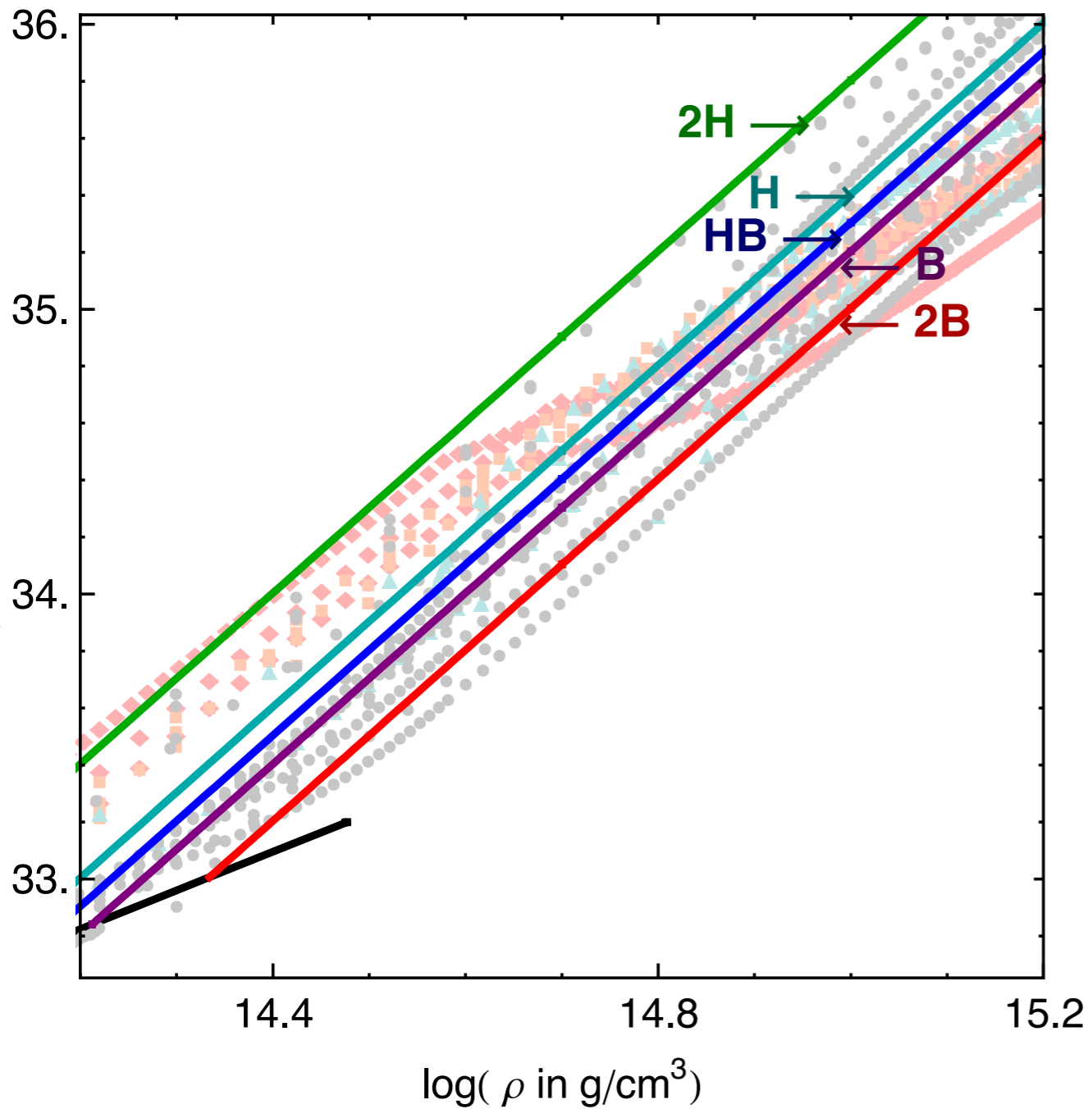


figure from FAIR CBM experiment

Equation of state above nuclear density determines NS structure



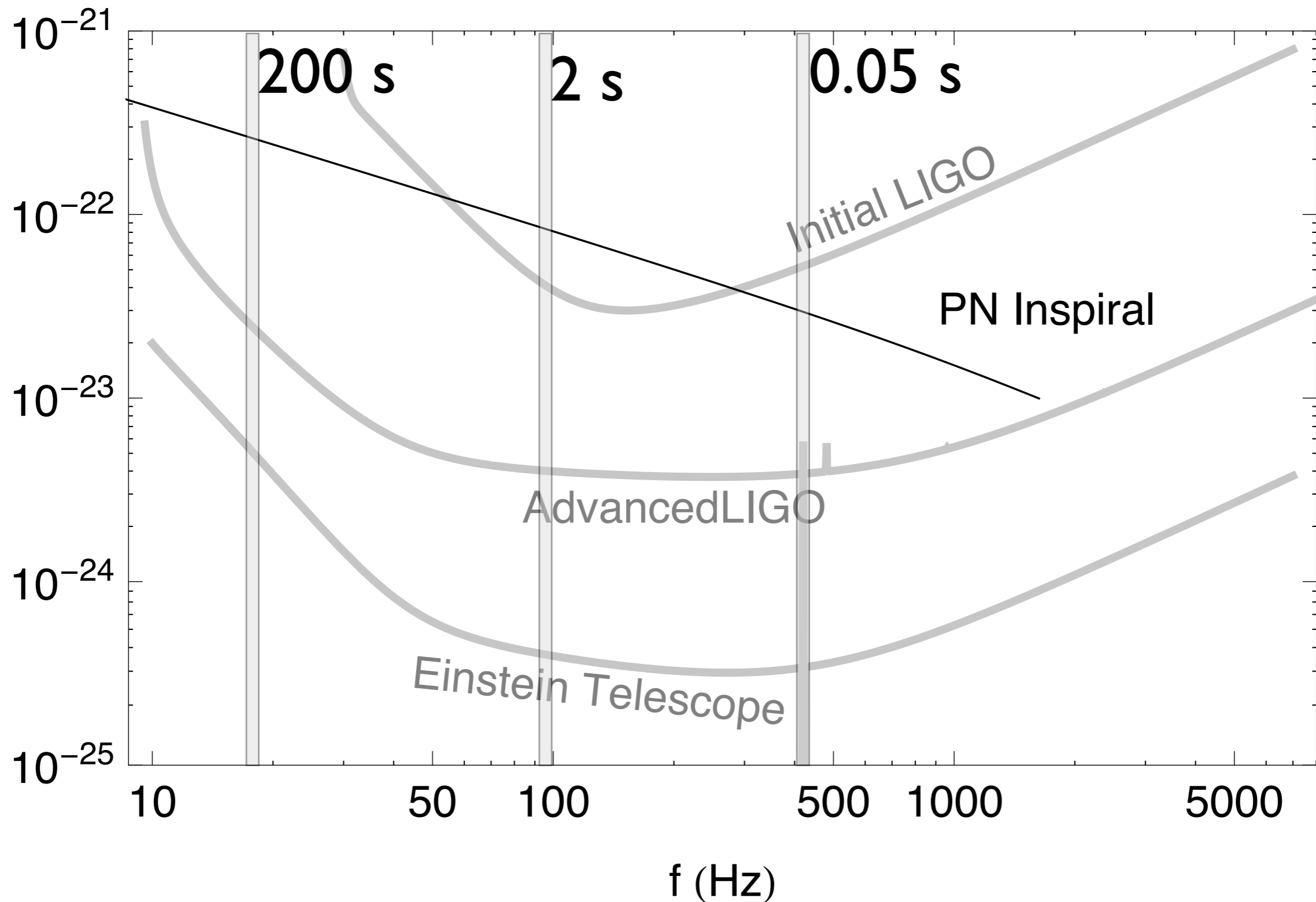
Constraint on EOS from neutron-star observations

Observed masses, spin frequencies, and oscillation frequencies must be **possible** with given EOS.

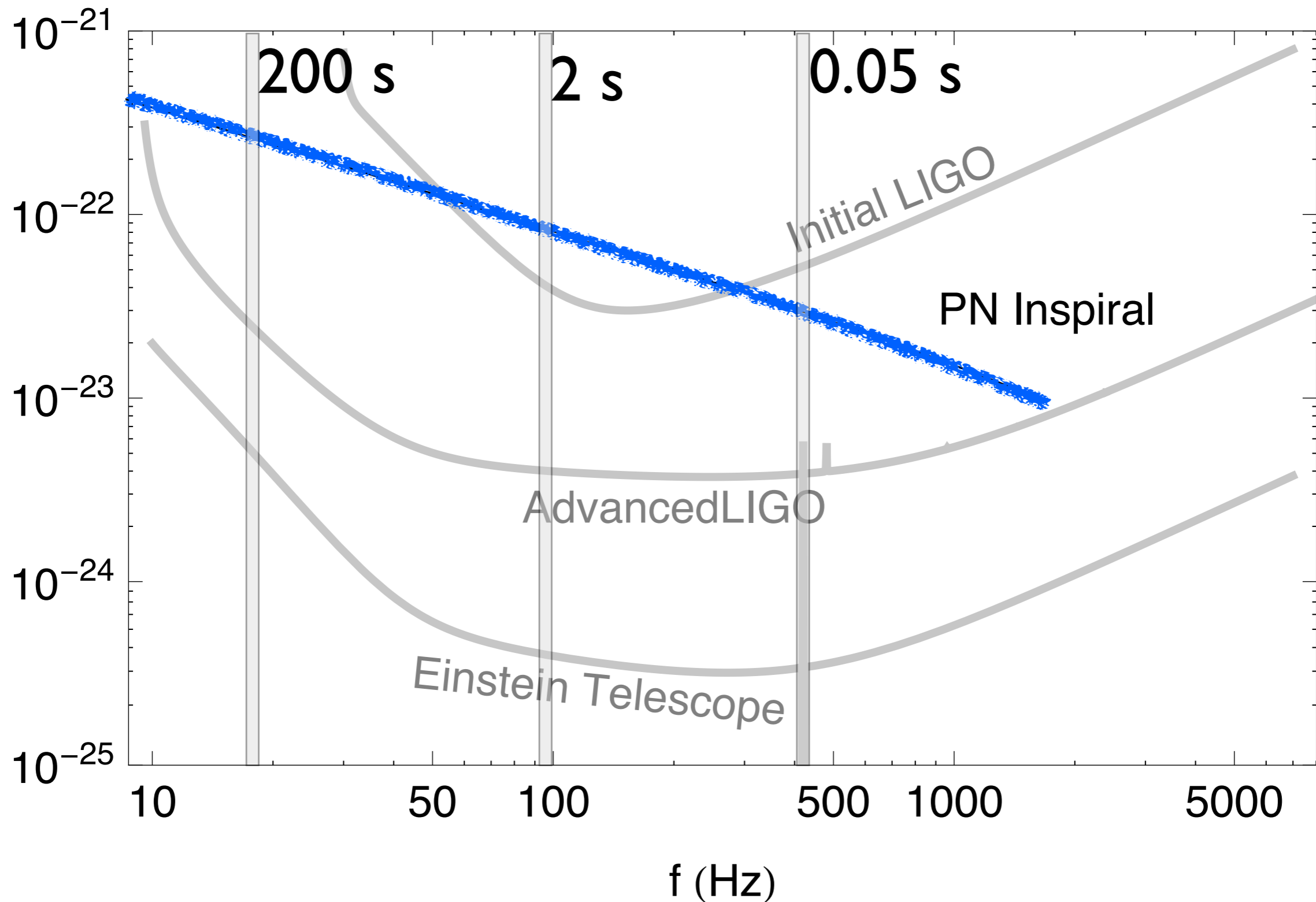
If one can measure multiple properties:
observationally implied radius, moment of inertia, or tidal deformability must be **predicted** by given EOS at **observed mass**.

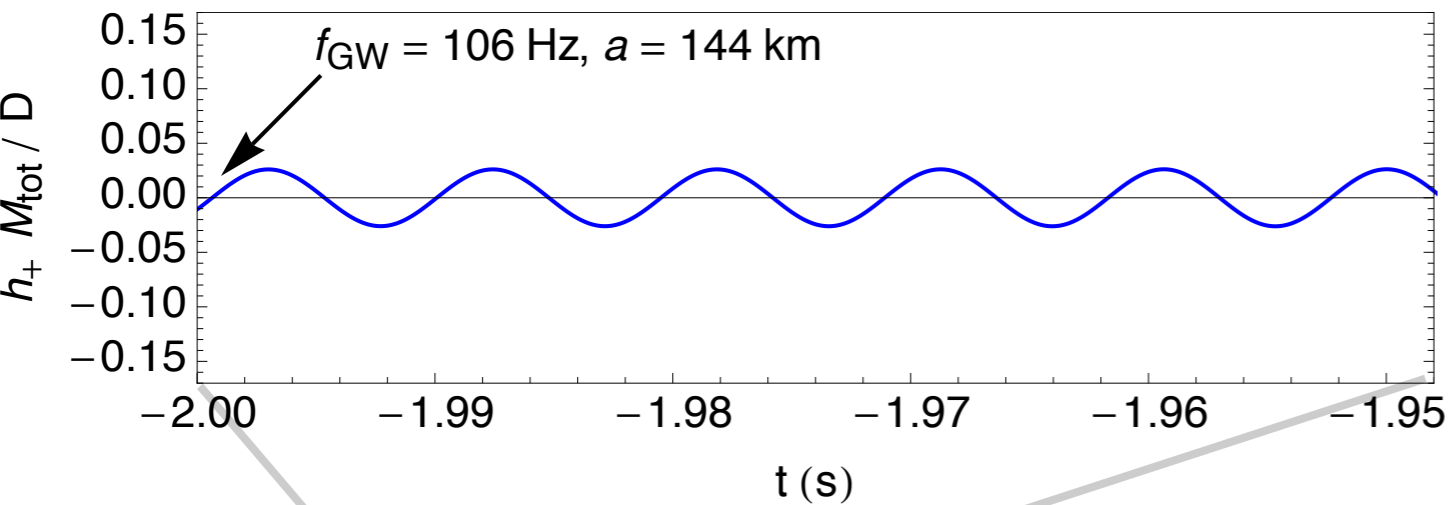
Gravitational dynamics

The path of an inspiraling double neutron star

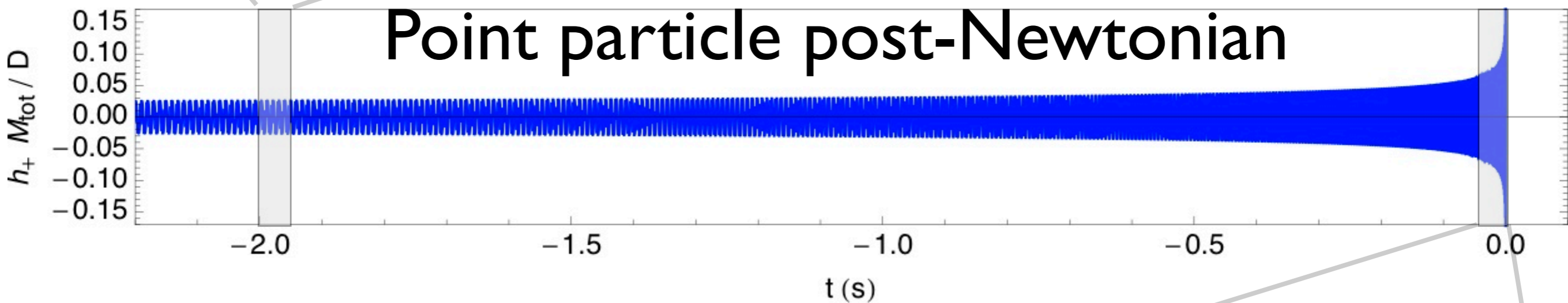


The path of an inspiraling double neutron star

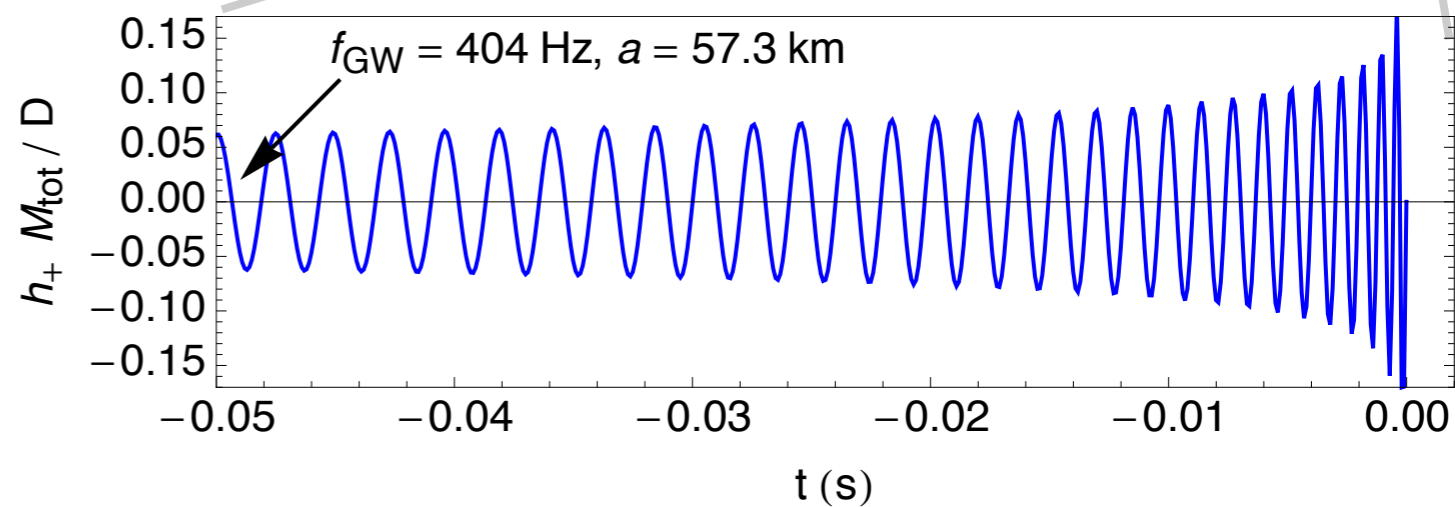




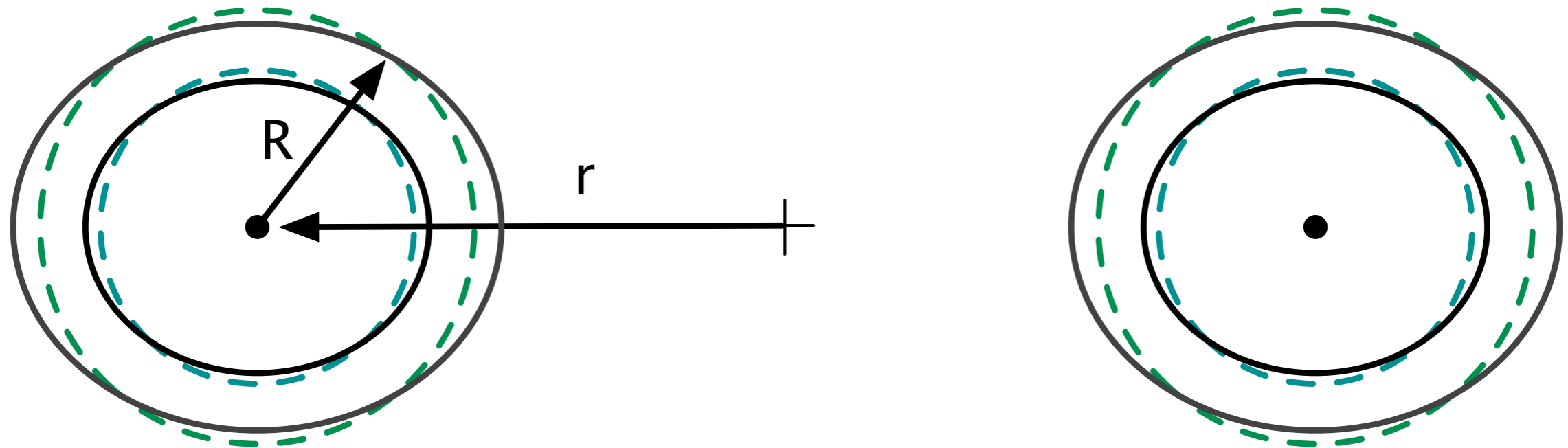
Two seconds before merger



Last 0.05 s



What changes the waveform?



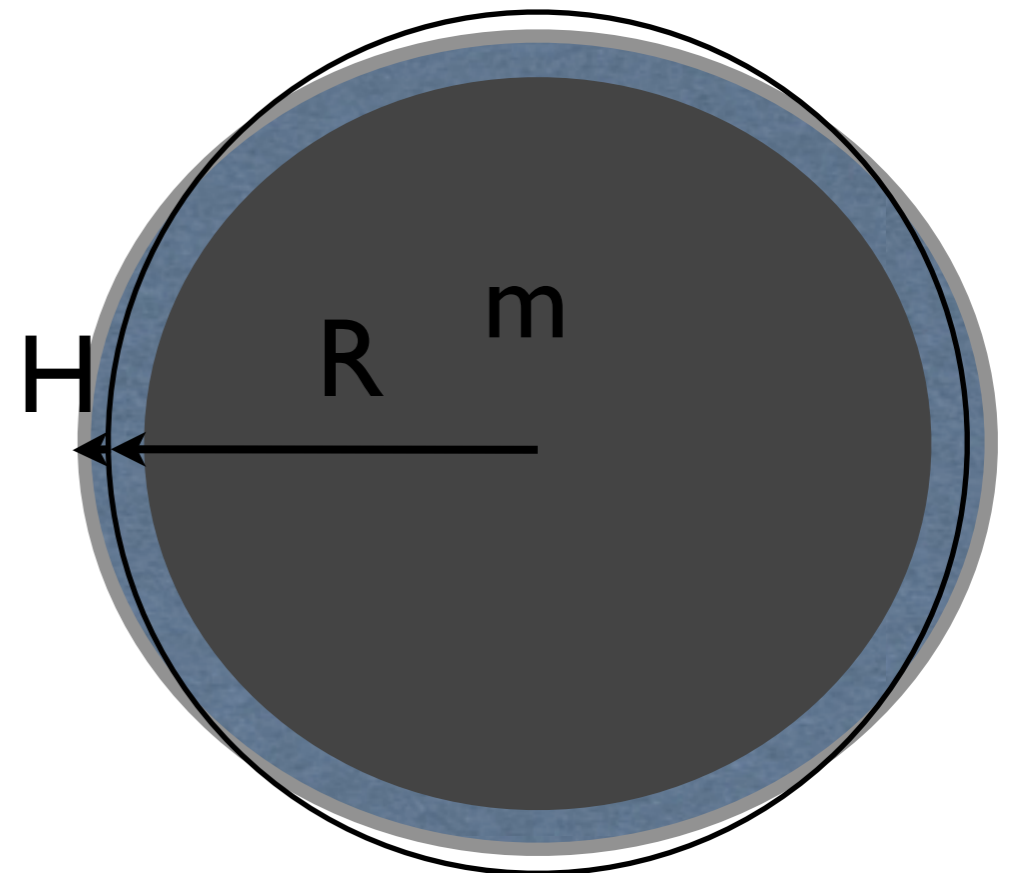
For an object following its orbit, the leading residual effect of gravity is felt in tides.

Surface deformation Love number h:

Love number h determines deformation of surface.
larger h deforms more easily (e.g. ocean vs. rock)

$$H = h \left(\frac{M}{m} \right) \left(\frac{R}{a} \right)^3 R \frac{(3 \cos^2 \theta - 1)}{2}$$

M mass of Jupiter
 m mass of Enceladus
 R radius of Enceladus
 a distance to Jupiter



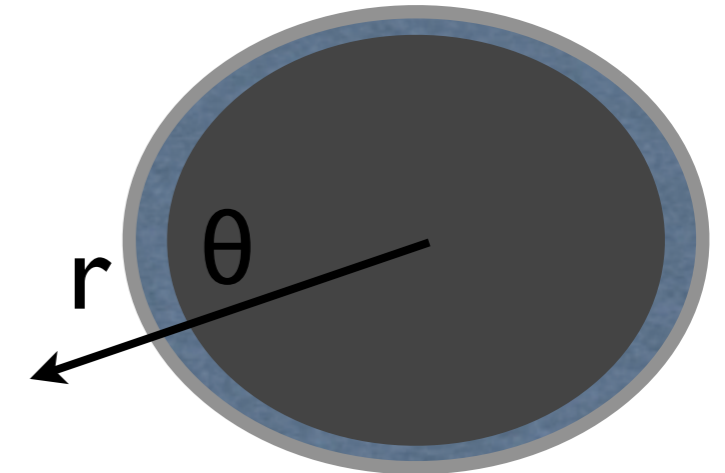
Gravitational potential Love number k

Love number k determines quadrupole moment Q of deformed body

$$Q = km \frac{R^5}{a^3}$$

Q determines the gravitational potential around the deformed body

$$U = -\frac{M}{r} - \frac{3}{2} \frac{Q(\cos^2 \theta - 1)}{r^3}$$



e.g.

M mass of moon

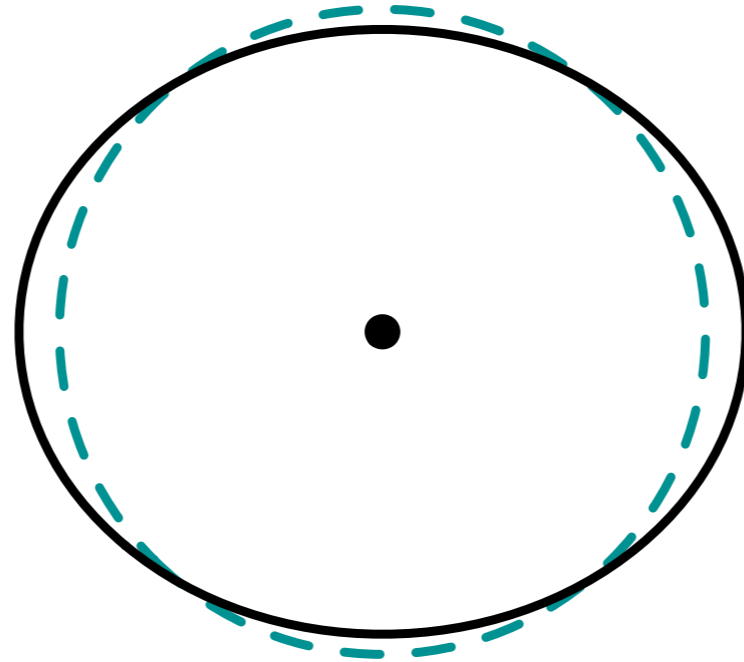
m mass of Earth

R radius of moon

a distance to Earth

This tells us about things like satellite movement around the body, tidal locking (“back-reaction” on bulges), and **orbital dynamics in binary systems**

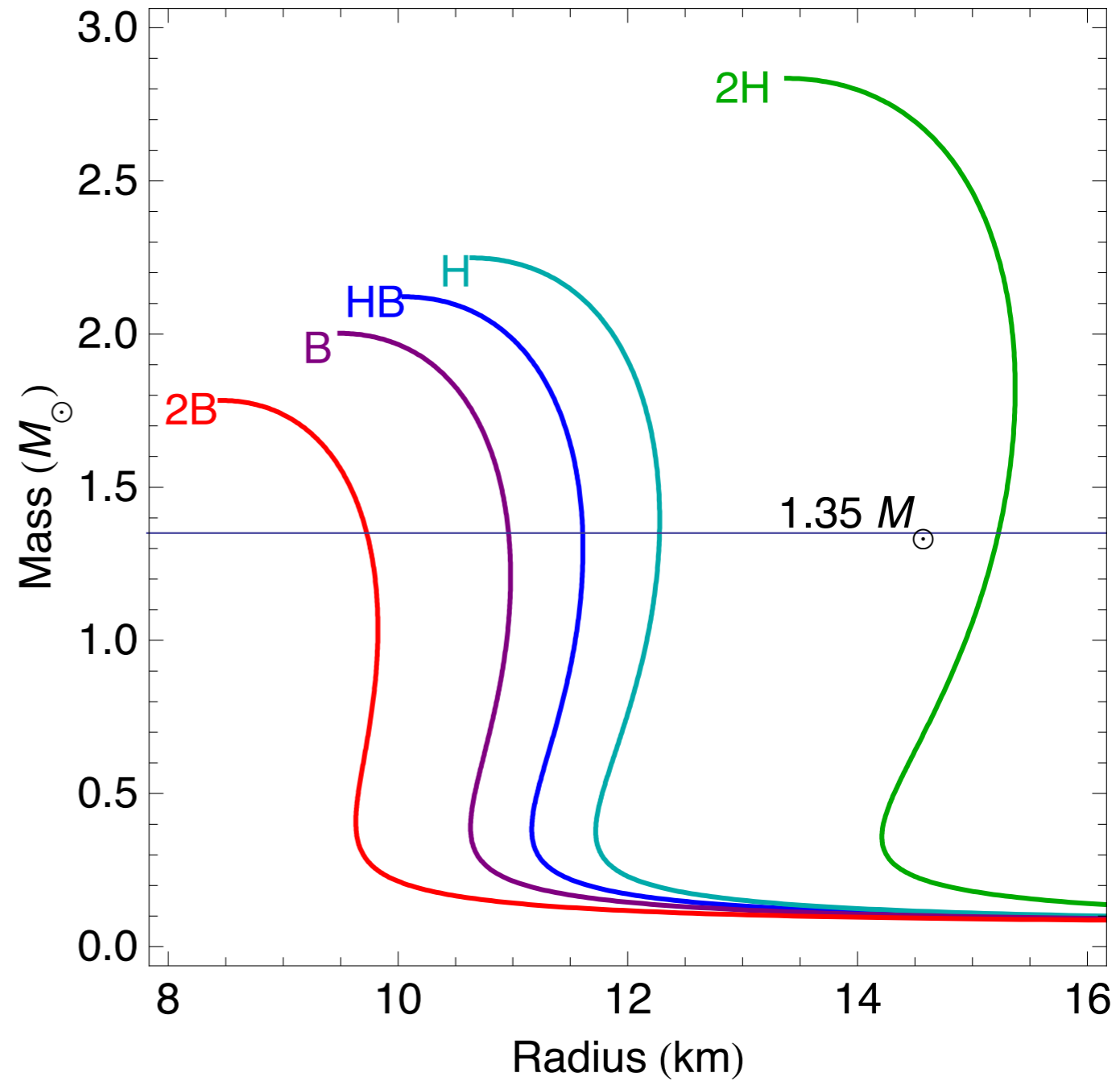
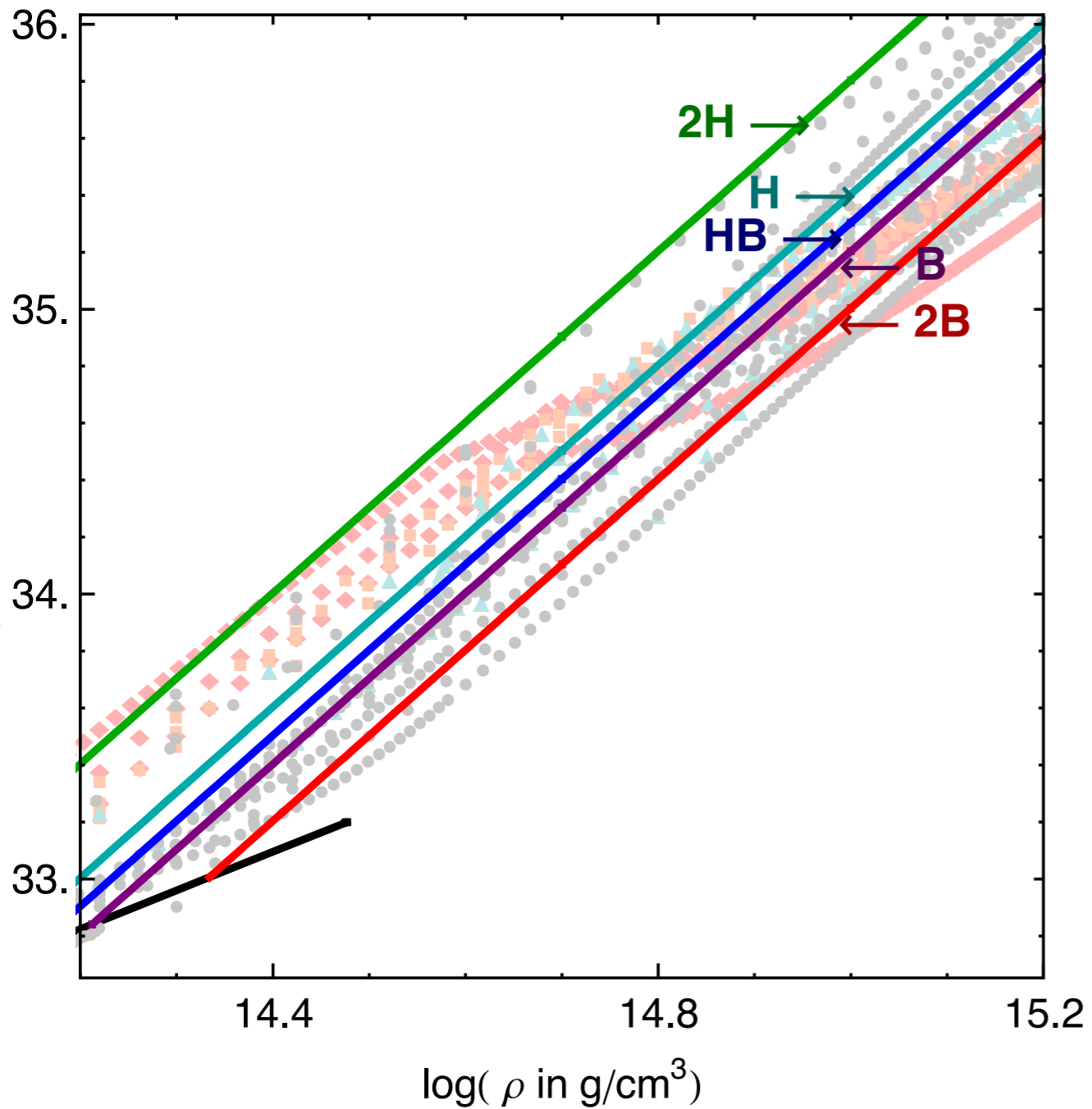
Calculate to leading order:



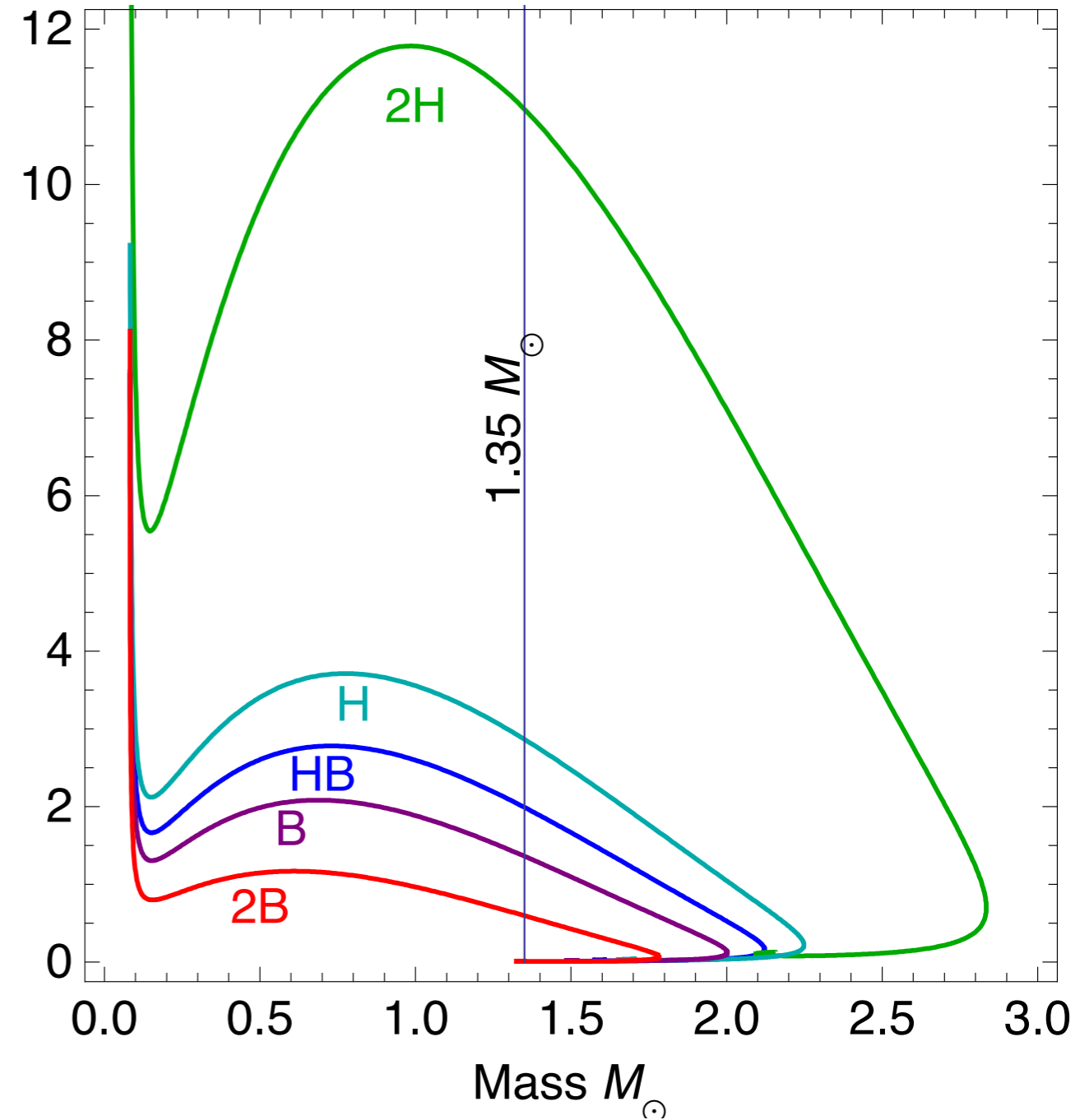
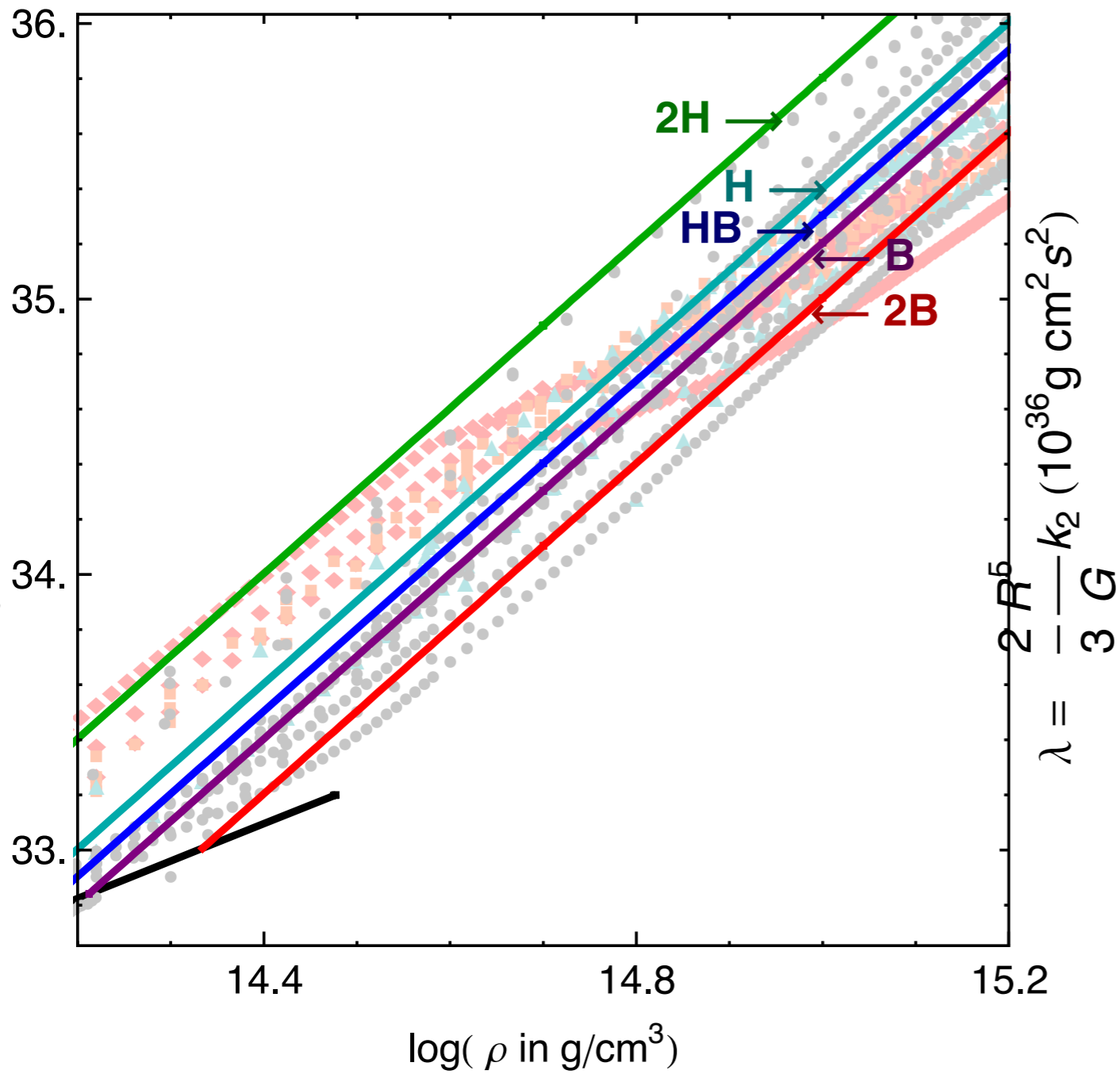
Perturb a spherically symmetric star with given EOS

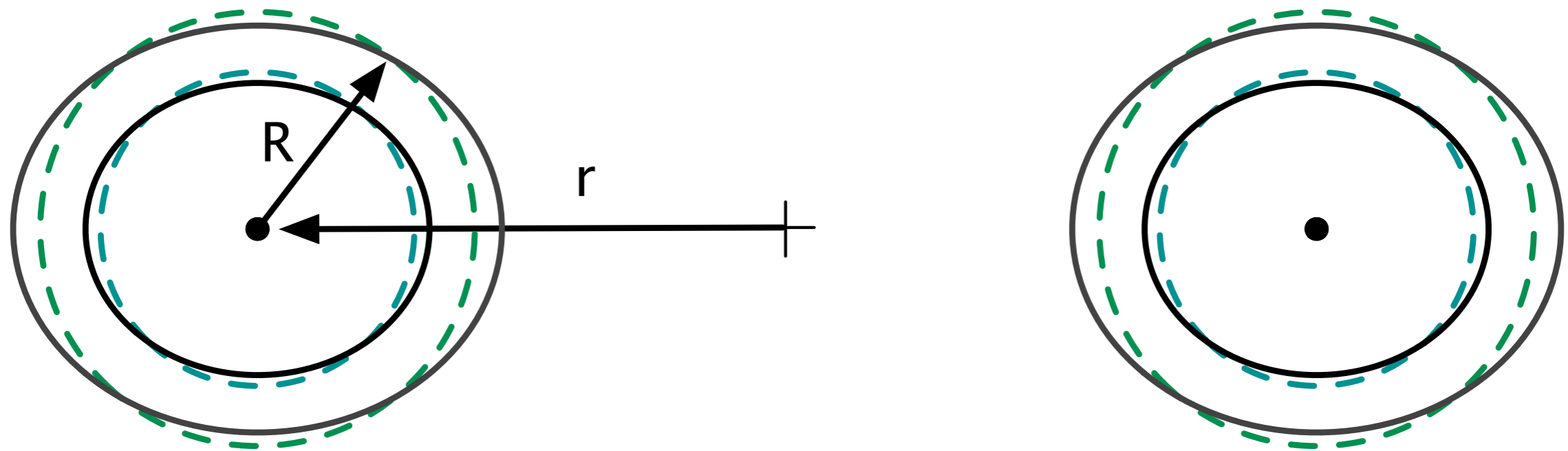
$$\lambda = \frac{Q}{\mathcal{E}} = \frac{\text{size of quadrupole deformation}}{\text{strength of external tidal field}}$$

Equation of state determines NS structure



Equation of state determines NS structure



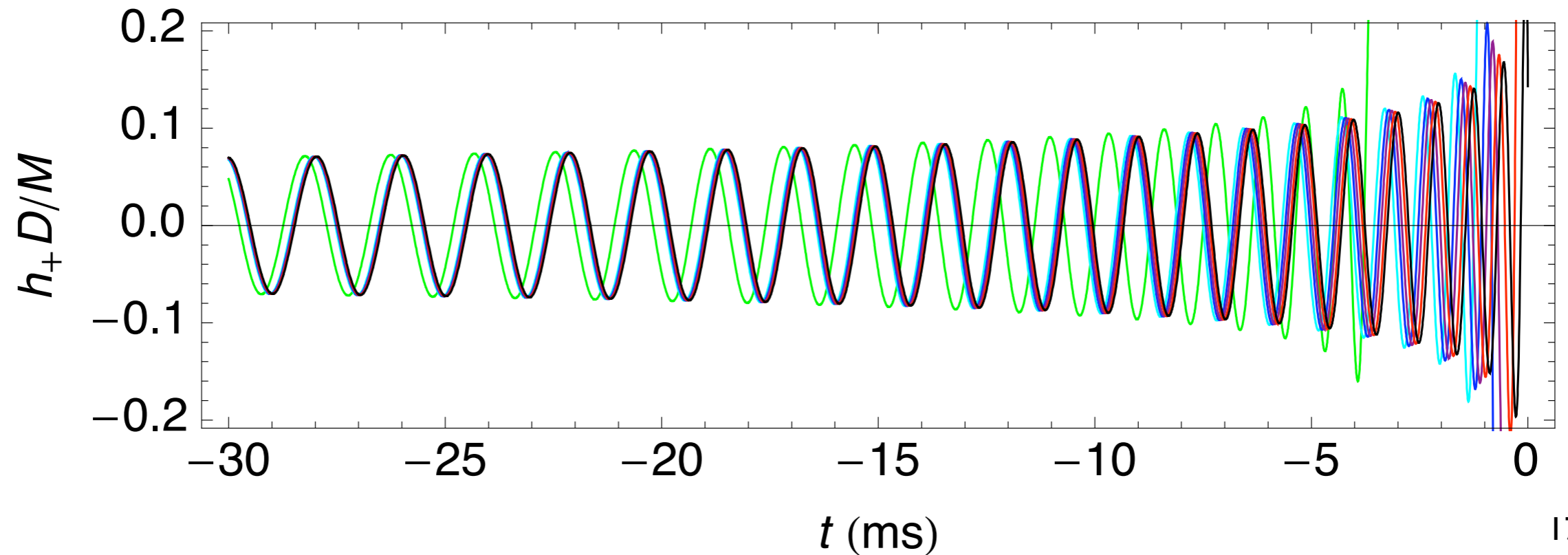
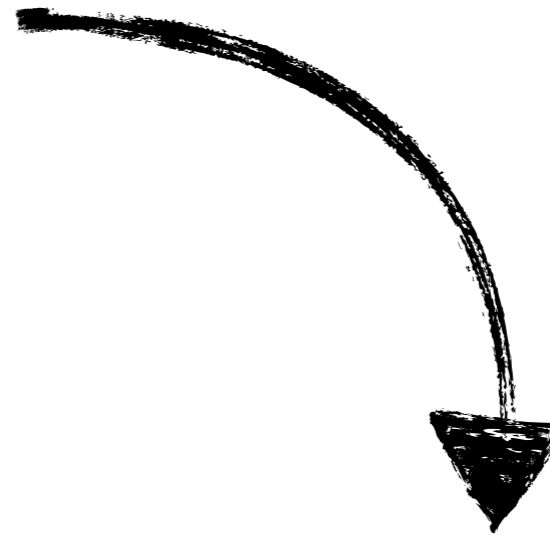
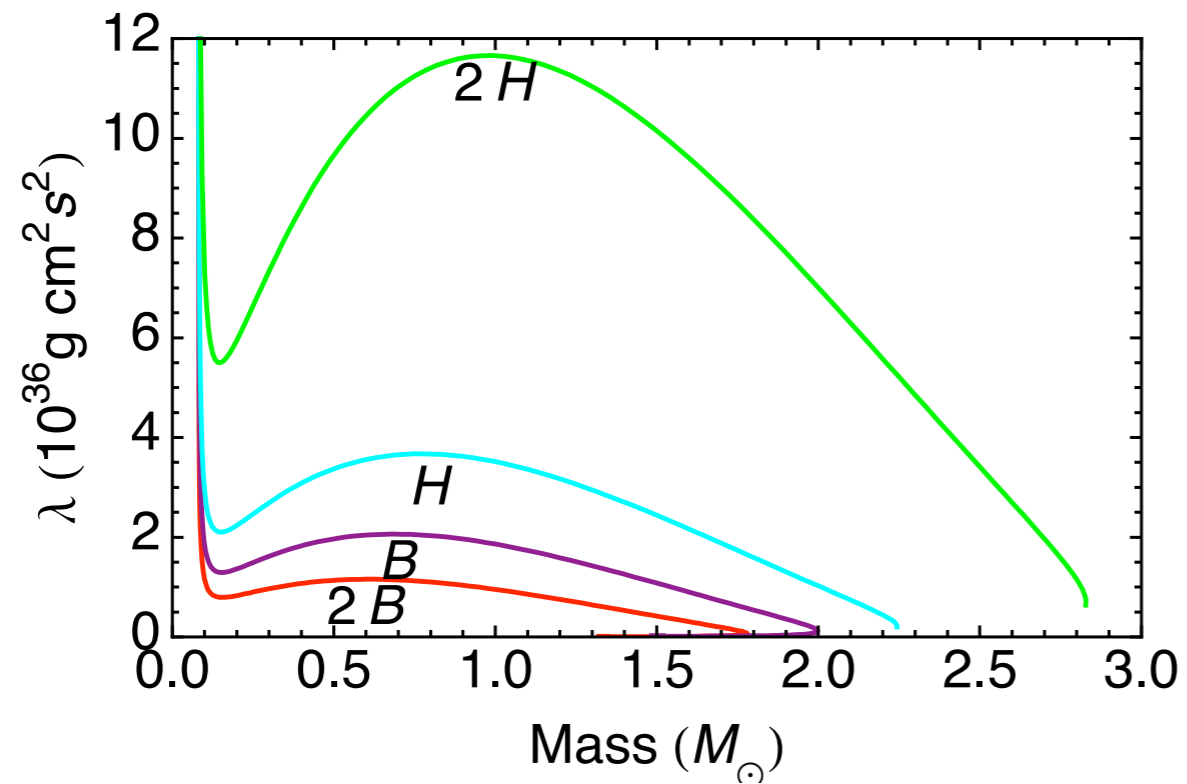


Early tidal interactions:

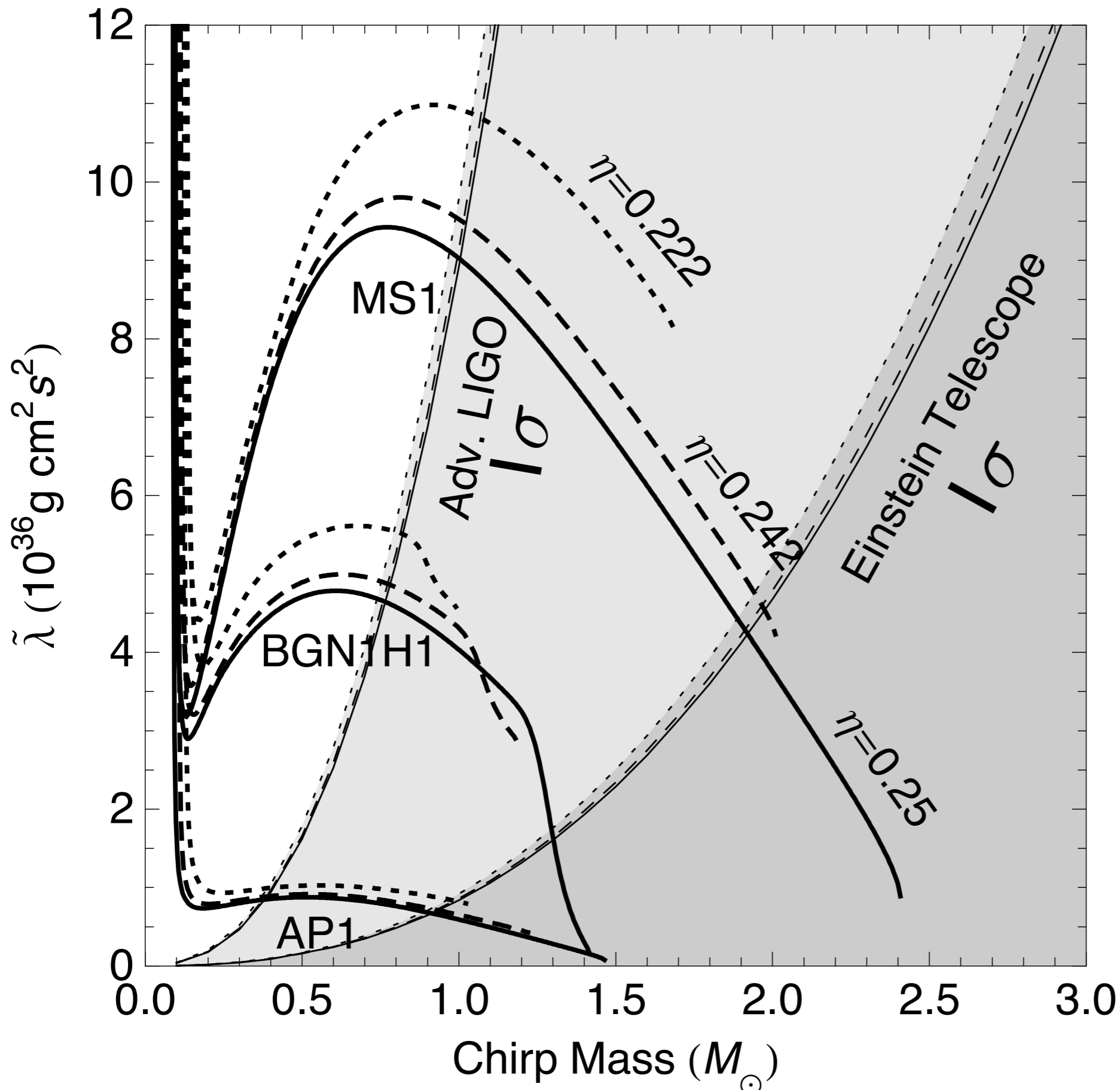
Some energy goes into deforming the stars

Moving tidal bulges add a bit to the gravitational radiation

Effect on waveforms from different EOS



Analytic estimates of measurability



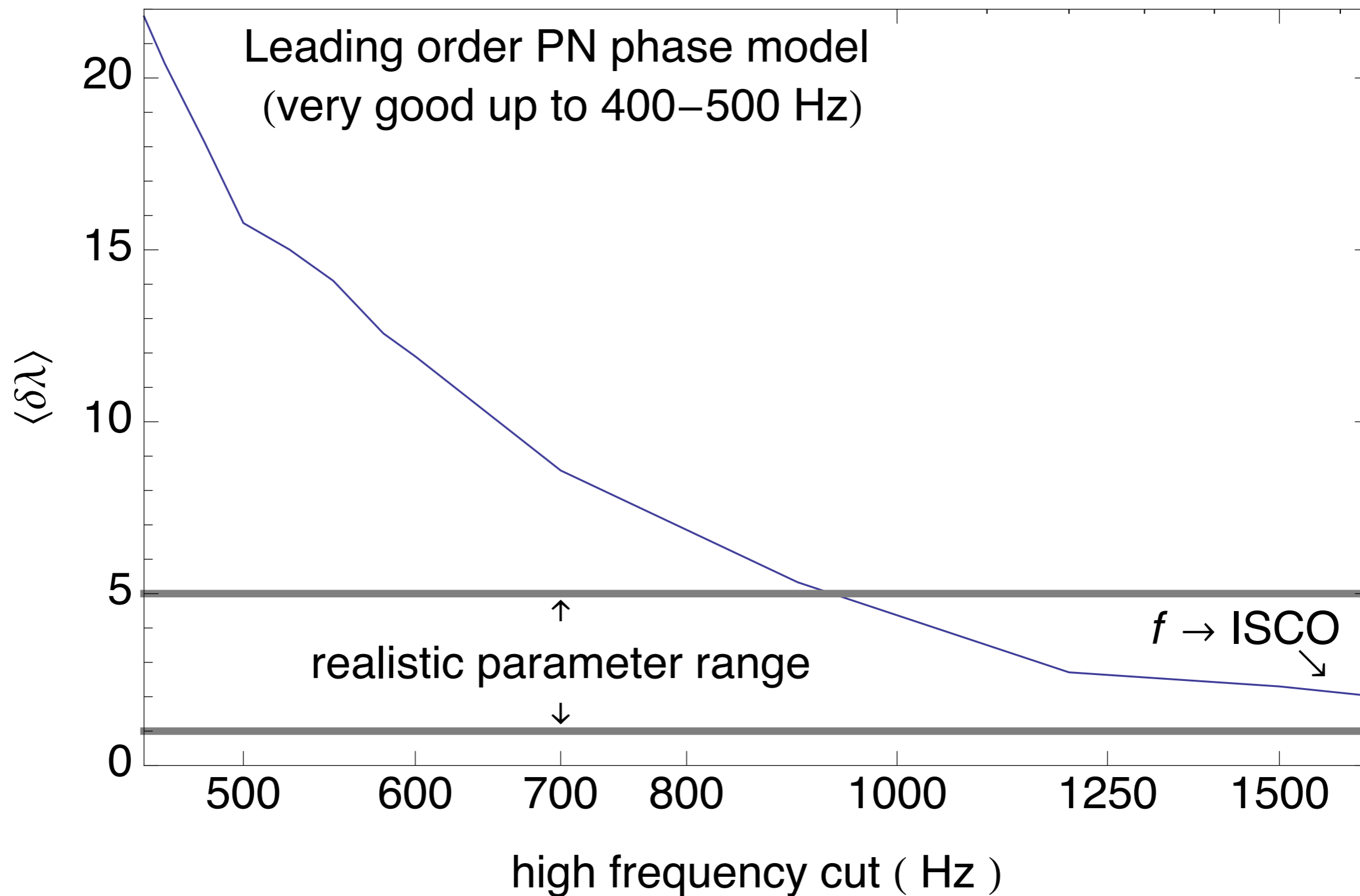
Limit to signal
before 450 Hz

Expect “clean”
signal

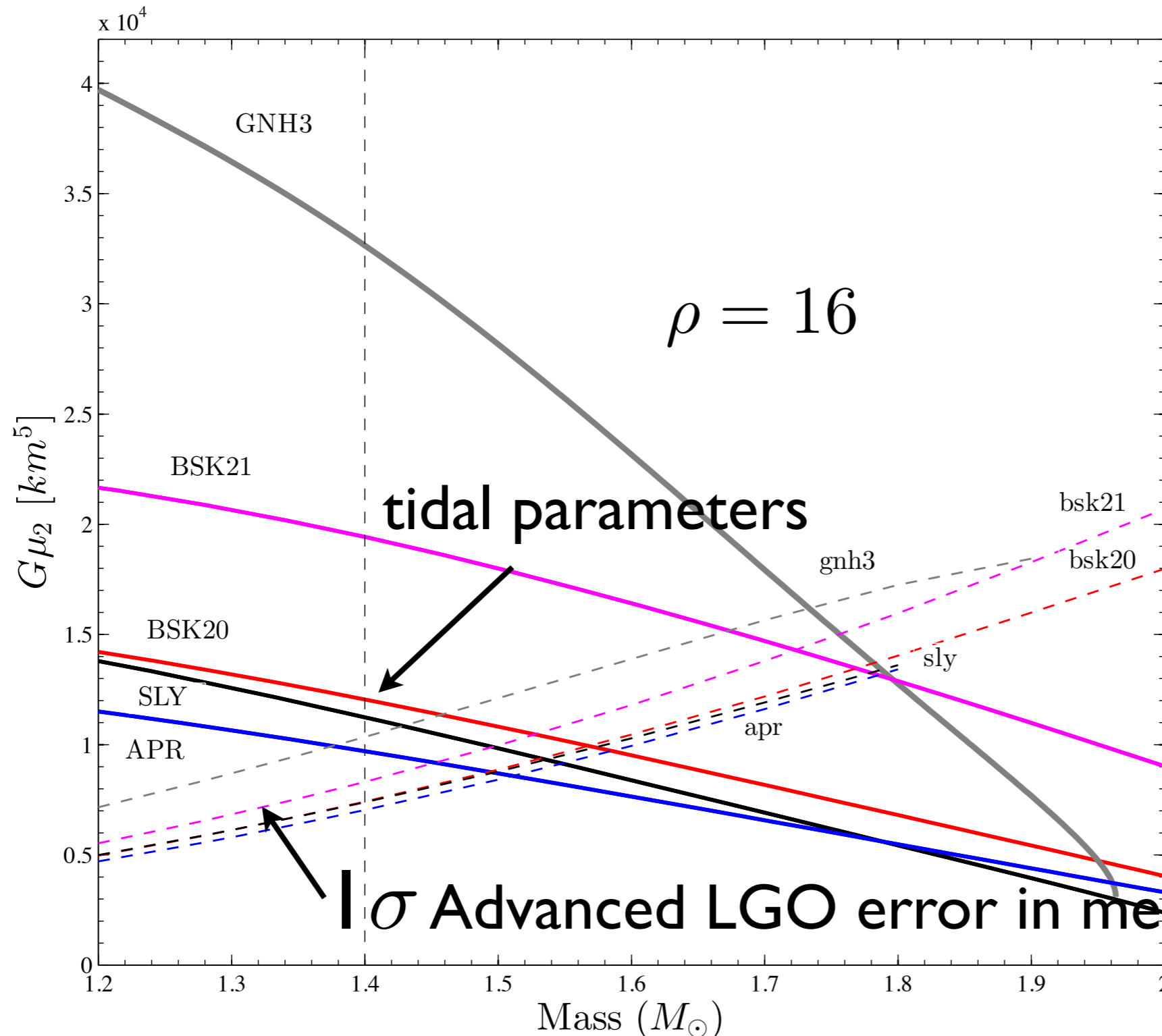
marginalize over
spin, mass ratio

CAVEAT: see
poster by M.
Favata; need to
understand
comparable order
point dynamics

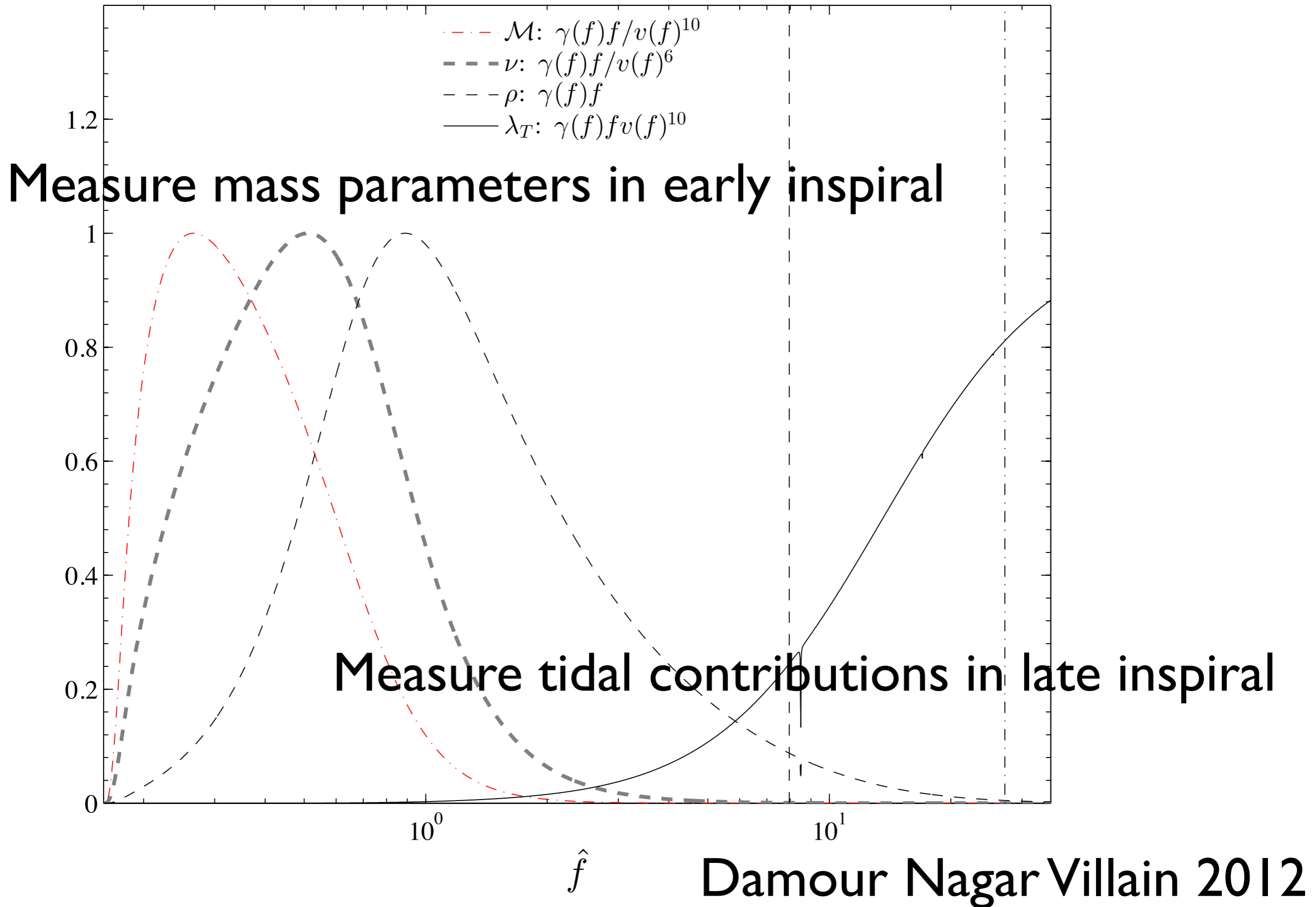
Fisher matrix estimate of measurability in AdLIGO high power configuration



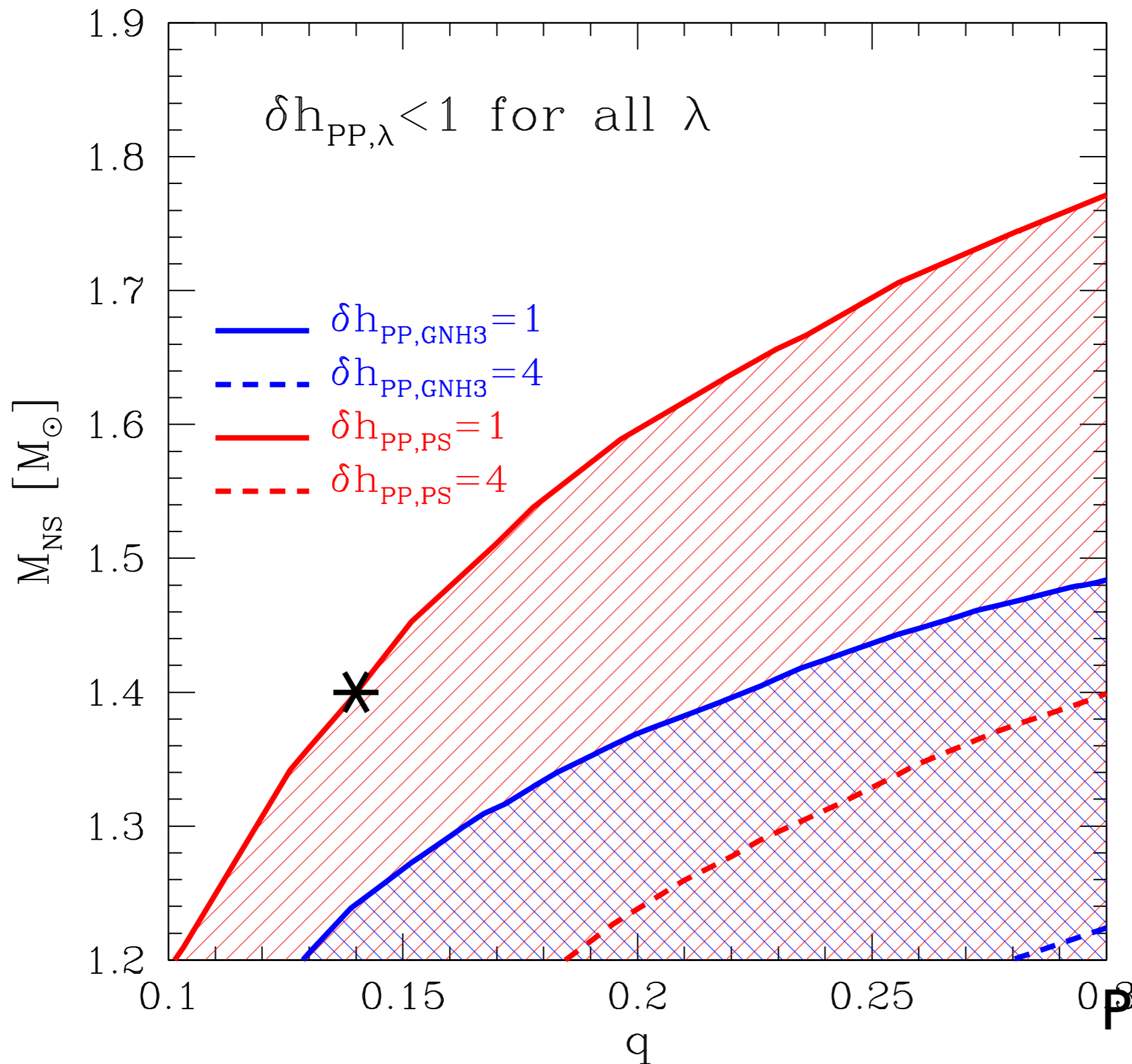
Damour, Nagar, Villain have a much stronger estimate of measurability



assume inspiral waveform known through to 1704 Hz (estimate of radius contact), neglect spin



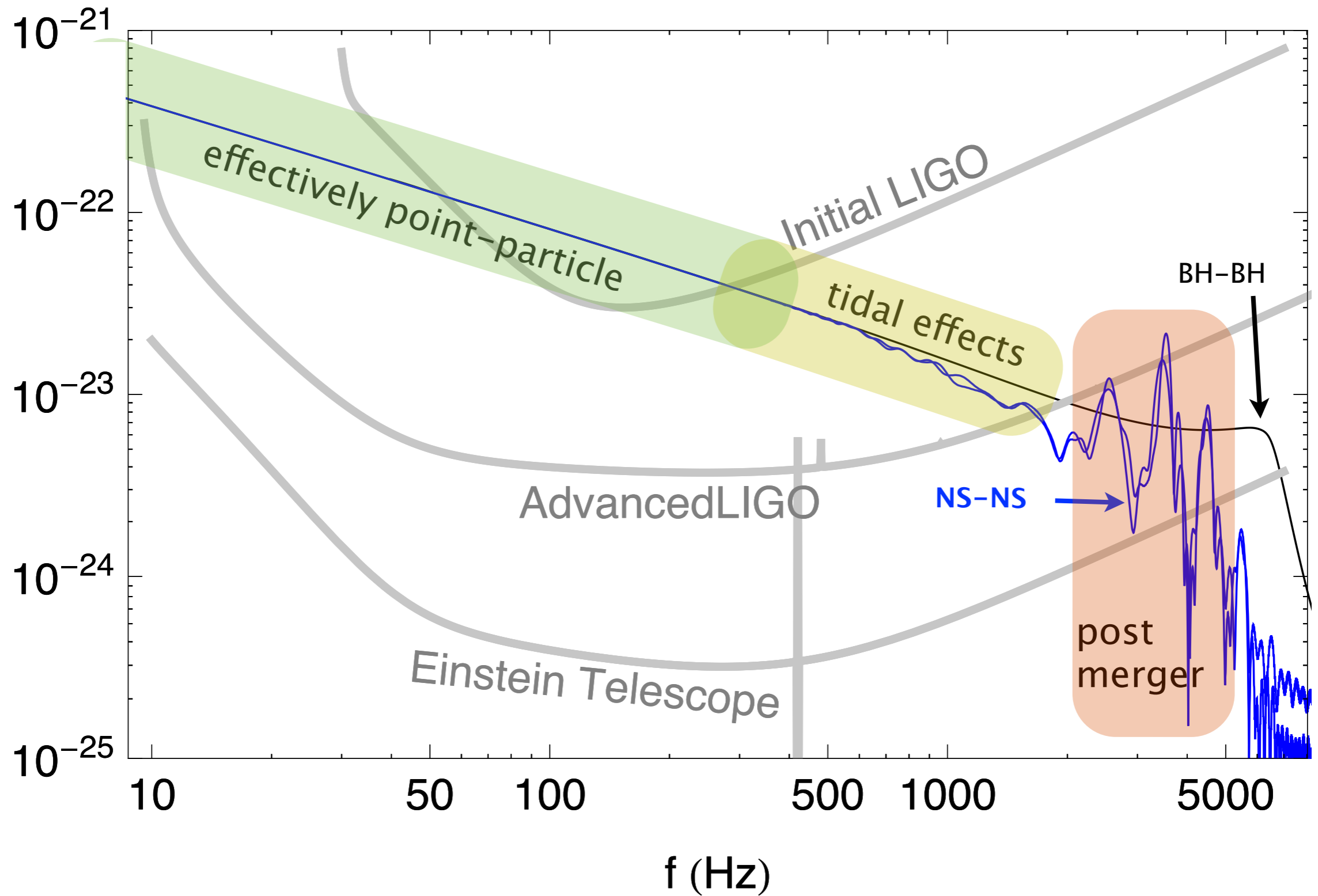
Similar extrapolation in BHNS is less promising

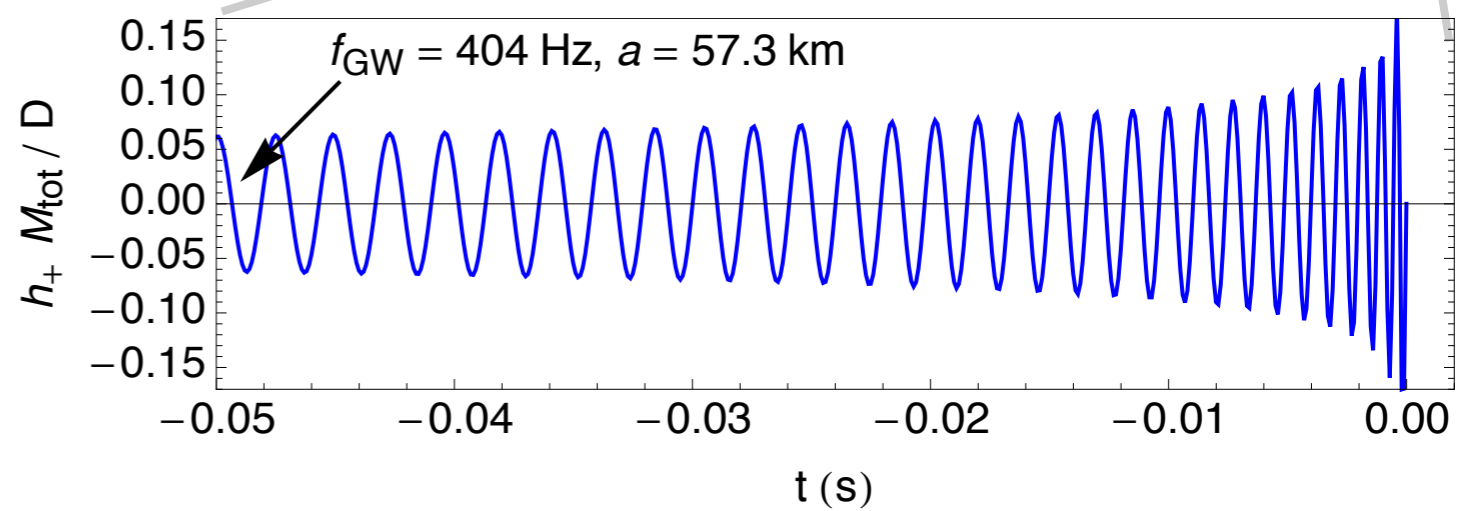
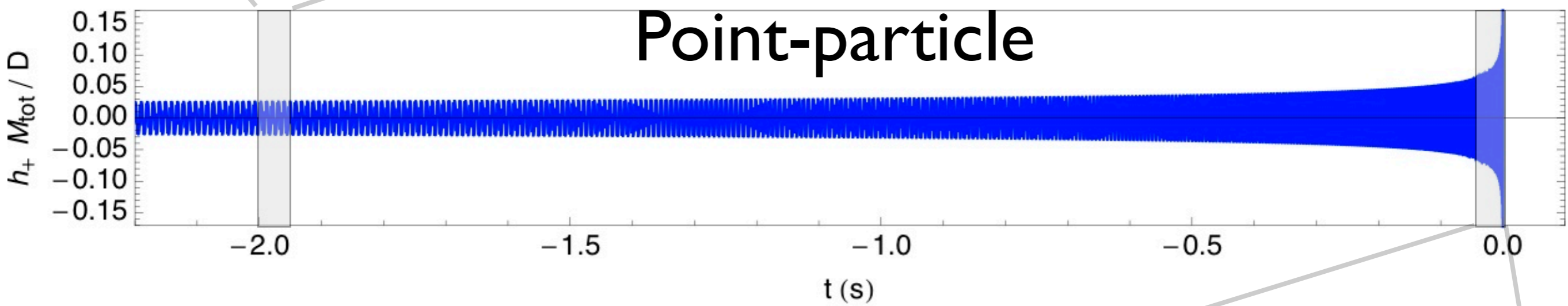
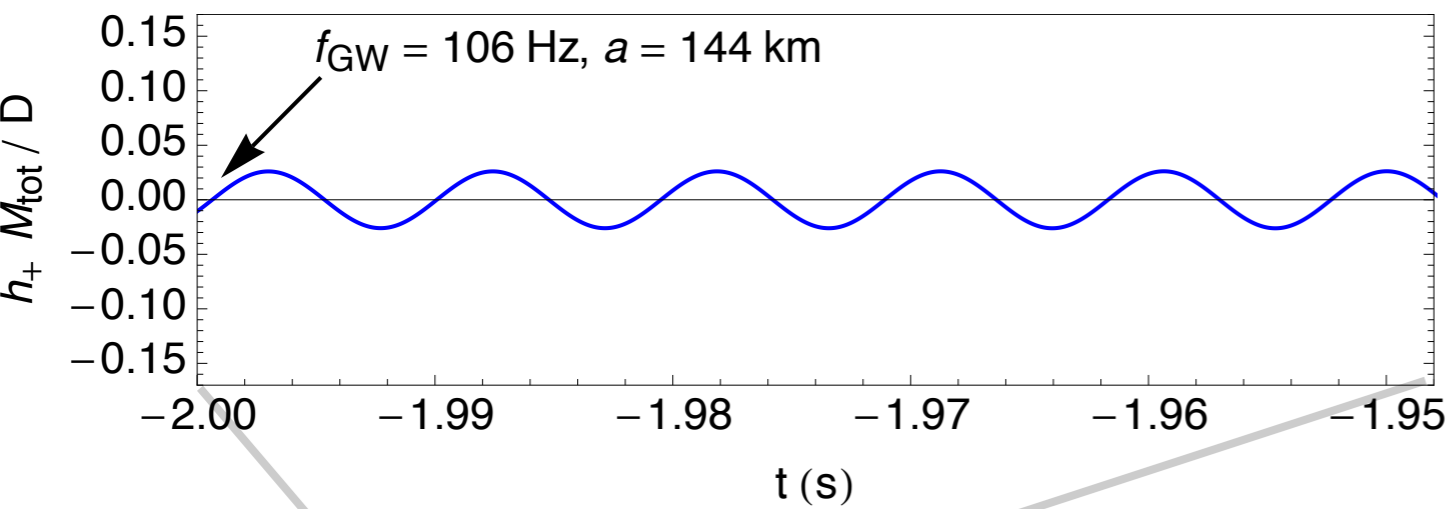


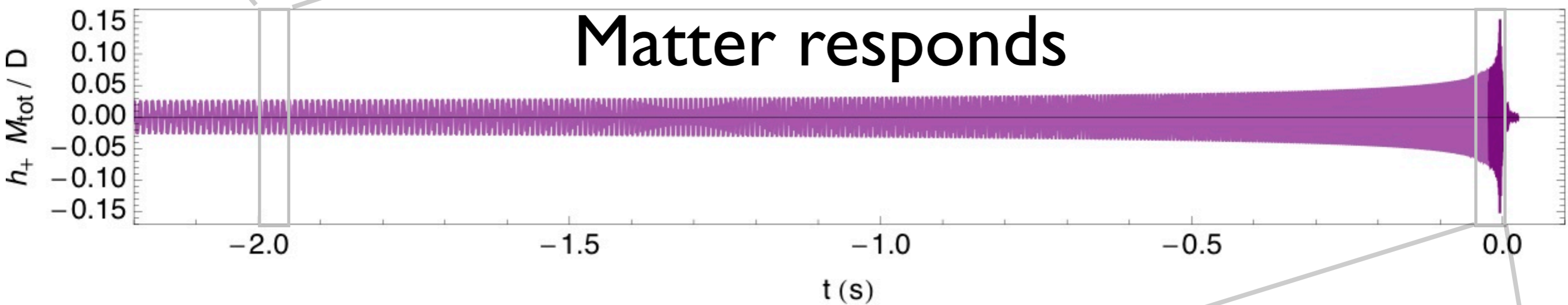
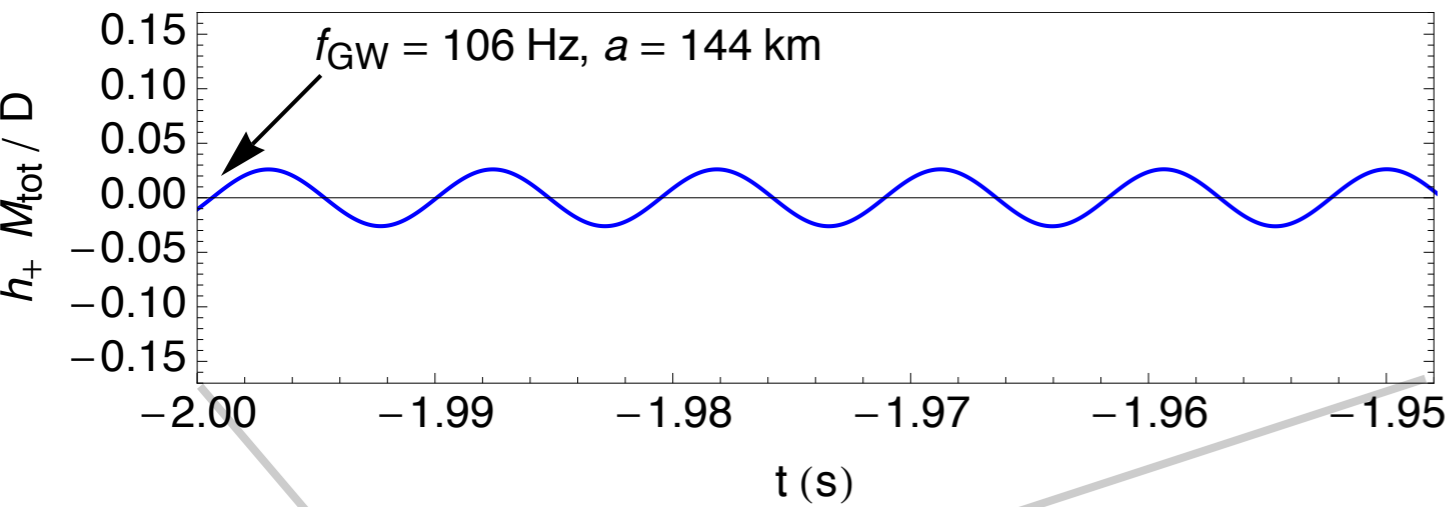
@100 Mpc
distinguishing
very stiff EOS
only in low
mass ratio
systems

Numerical only estimates

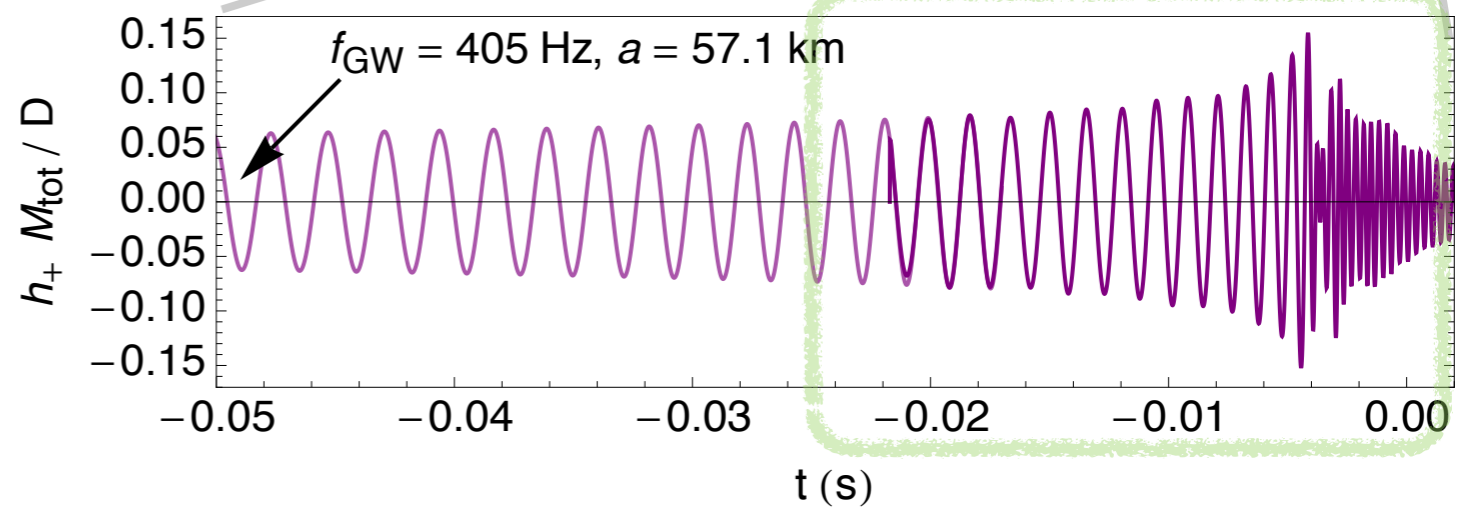
NS NS waveforms



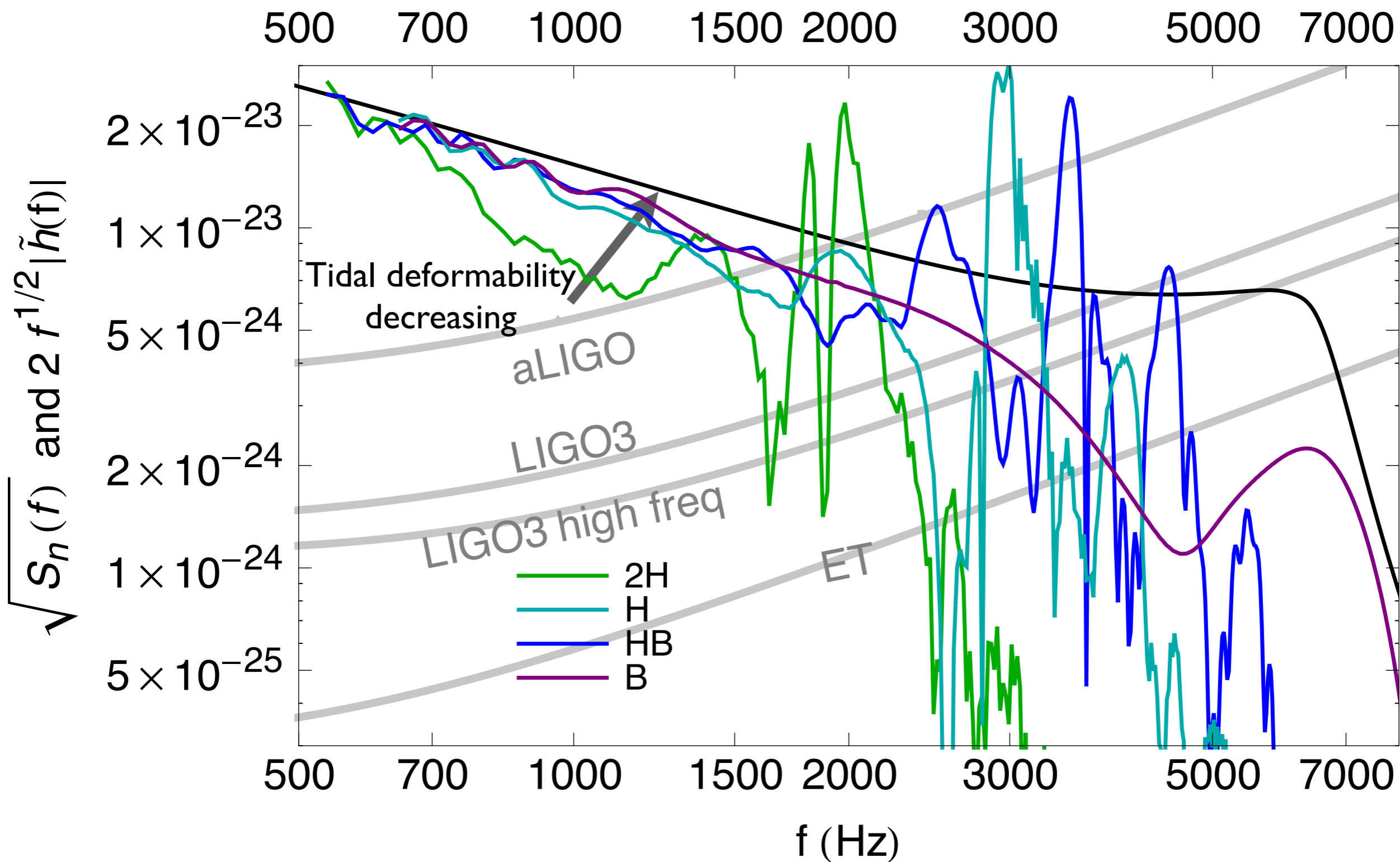




For the final coalescence,
numerical simulation
required



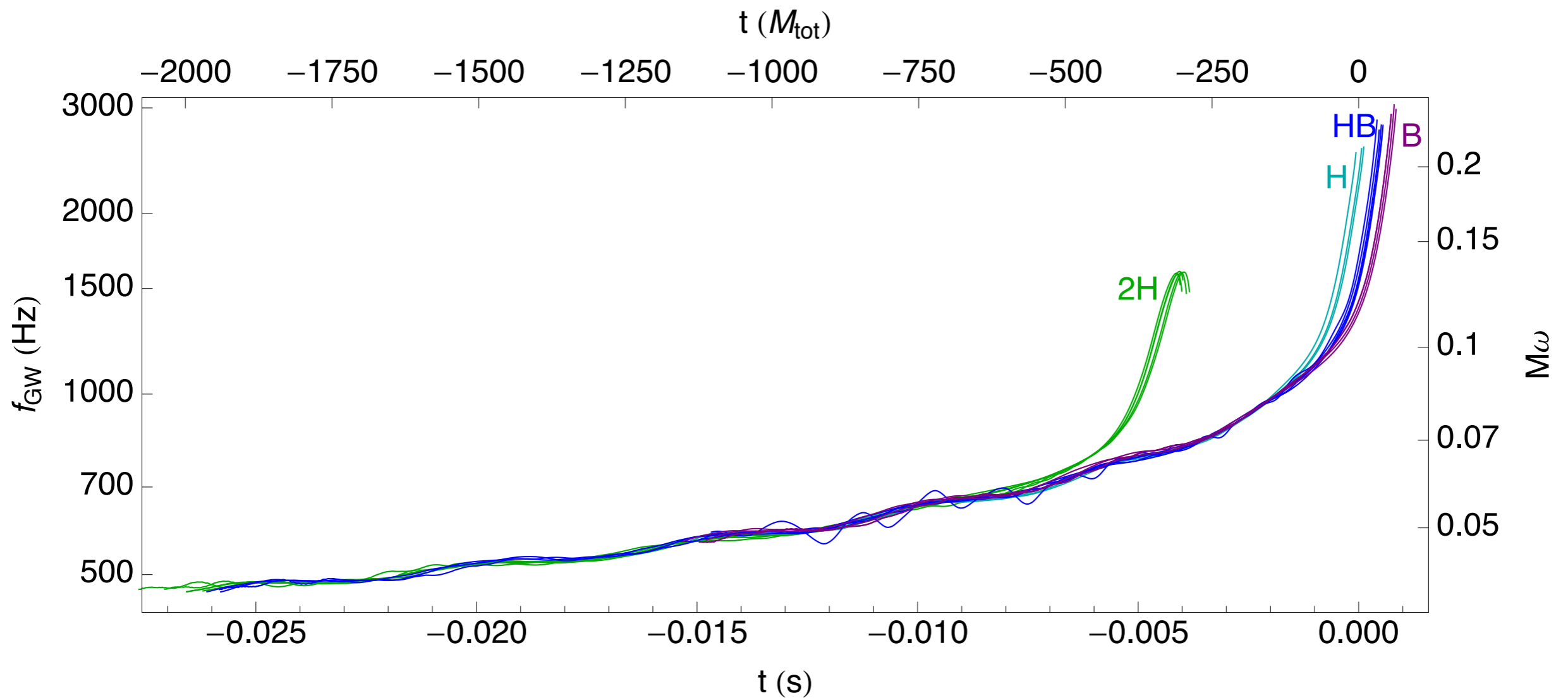
NS-NS: What can we extract?



Measurable?

Avoid high PN systematics; use numerical simulations only.

Minimized differences between noise weighted inspirals with different EOS



SNR of differences between waveforms

Advanced LIGO high-power detuned

EOS	H	HB	B
2H	2.162 ± 0.030	2.210 ± 0.036	2.234 ± 0.035
H	-	0.896 ± 0.099	1.0452 ± 0.087
HB	-	-	0.580 ± 0.168

Einstein Telescope configuration D

EOS	H	HB	B
2H	20.352 ± 0.314	20.739 ± 0.369	20.890 ± 0.360
H	-	7.740 ± 0.914	9.130 ± 0.866
HB	-	-	5.095 ± 1.490

$$\langle \delta R \rangle \Big|_{R_{avg}} \simeq \frac{R_1 - R_2}{\langle h(R_1) - h(R_2) | h(R_1) - h(R_2) \rangle^{1/2}}$$

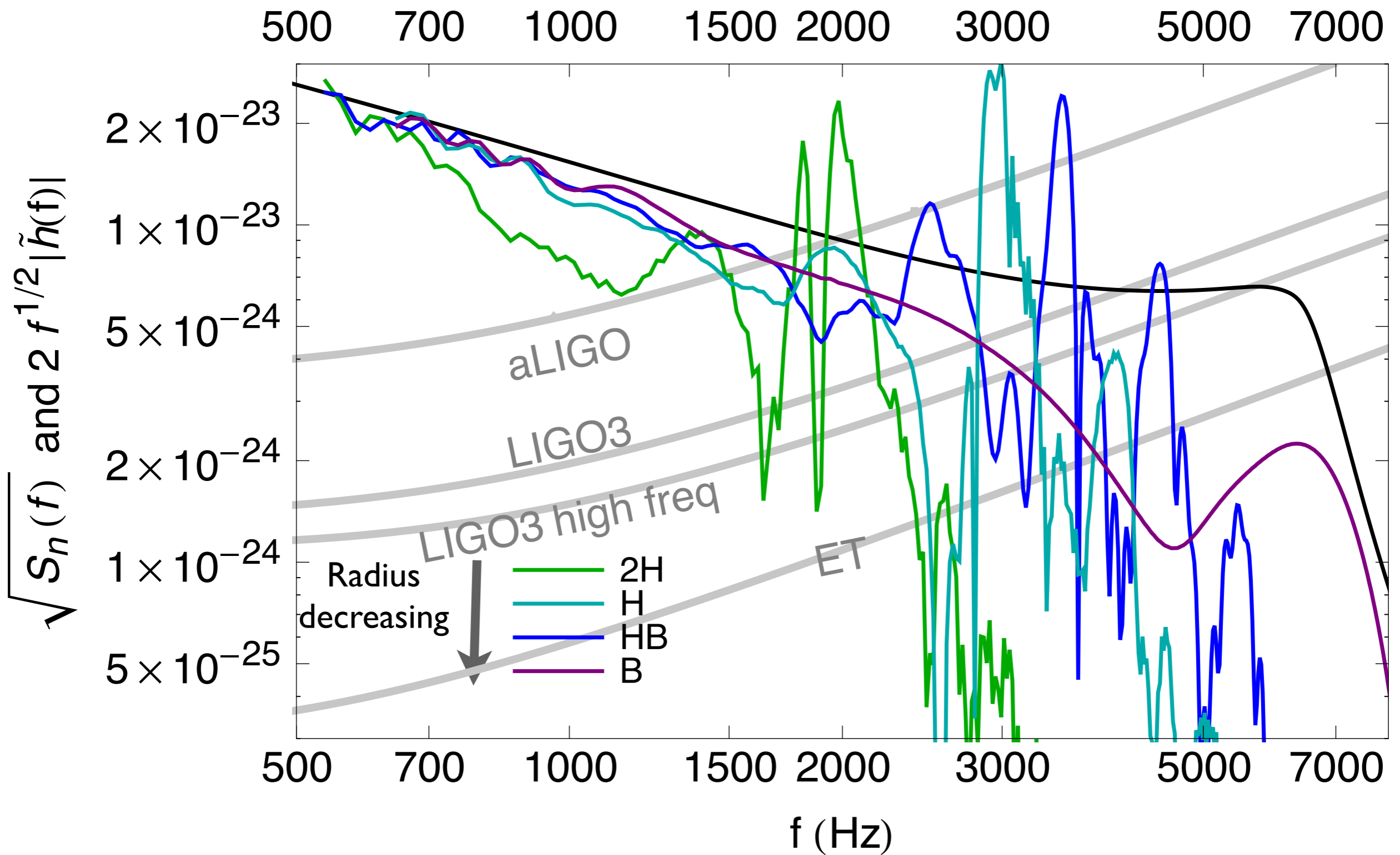
$\langle \delta R \rangle$, R is radius of isolated neutron star

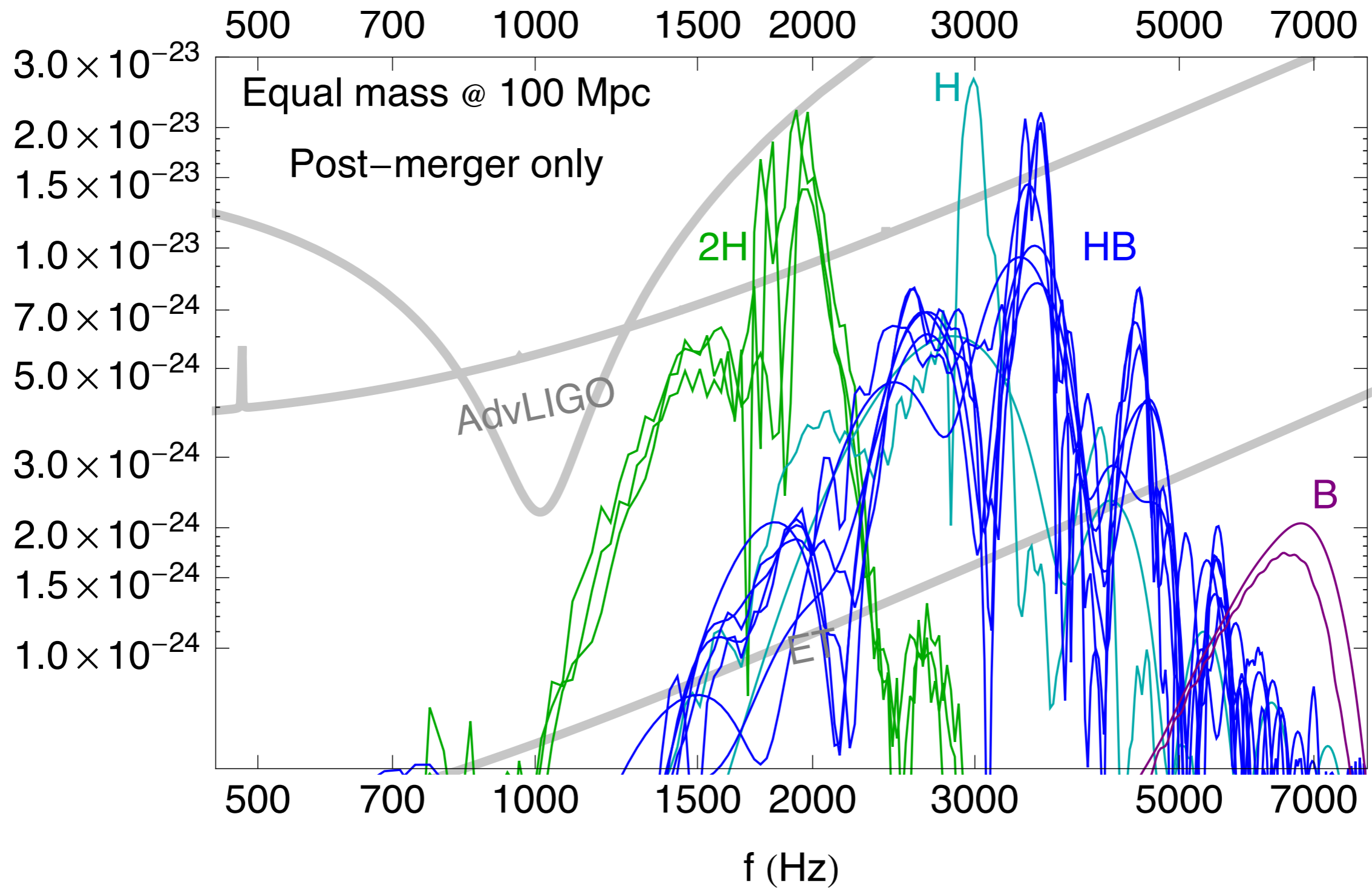
	Broadband AdLIGO	ET-D
$R = 10.8$	± 0.9 km	± 0.09 km
$R = 11.9$	± 0.8 km	± 0.10 km

Radius can be constrained with a strong Advanced LIGO signal
(in high-power detuned configuration)
based on numerical waveform alone.

Systematics from different numerical simulations with same EOS ~ 0.1 km
Other sources: parameterization choice, discrete parameter sampling

Effect of matter post-merger





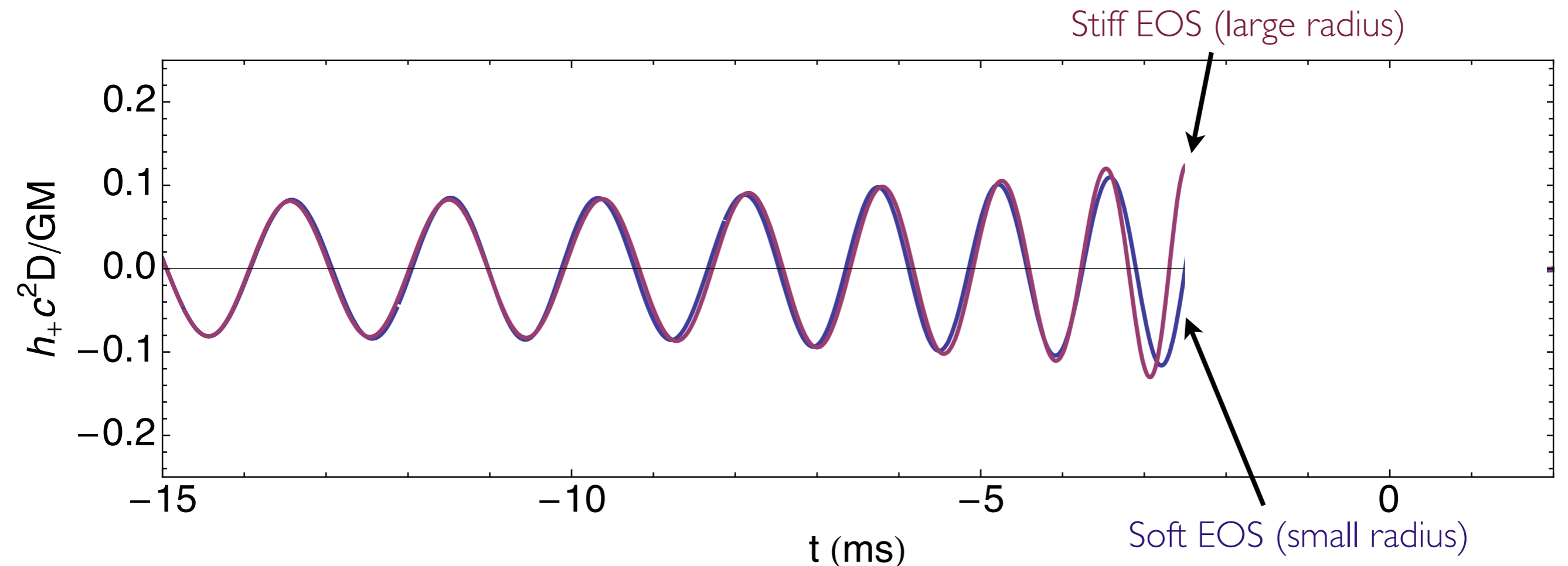
It is harder to measure the post-merger than the (extrapolated) inspiral

EOS	SNR $\times (100 \text{ Mpc}/D_{\text{eff}})$		f_p (kHz)
	aLIGO Broadband	ET-D	
2H	0.83	6.1+	2
H	0.54	5.6+	3
HB	0.47	3.3+	3.5
B	0.07	0.7	6.5–7
B _s	0.07	0.7	6.5–7
B _{ss}	0.03	0.3	6.5–7
HB _s	0.06	0.4	6.5–7
HB _{ss}	0.05	0.7	6.5–7

Hybrid estimates

NSBH: What can we extract?

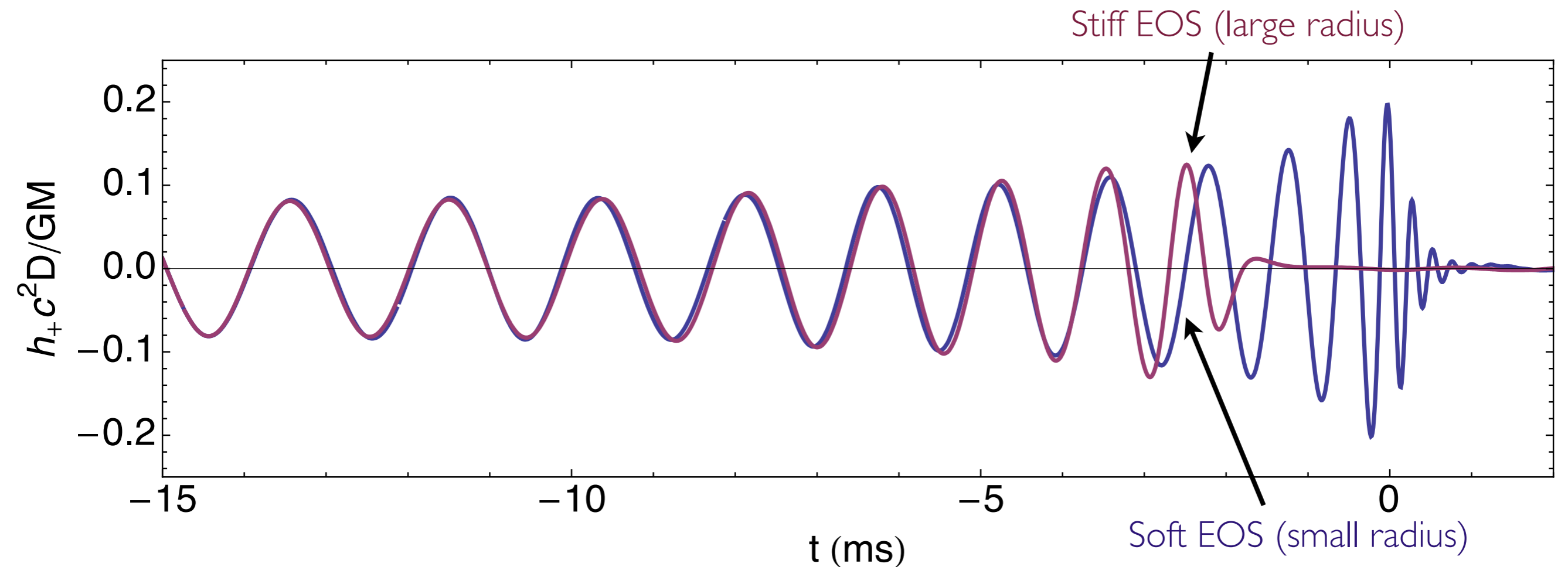
- Phase shift $\delta\Phi$ during inspiral
 - Much smaller than for BNS systems because
$$\delta\Phi \propto \frac{\lambda}{(1+q)^5 M_{\text{NS}}^5} = \frac{\Lambda}{(1+q)^5}$$
 - Only marginally observable with Advanced LIGO (Pannarale et al. arXiv:1103.3526)



Slide from Ben Lackey

NSBH: What can we extract?

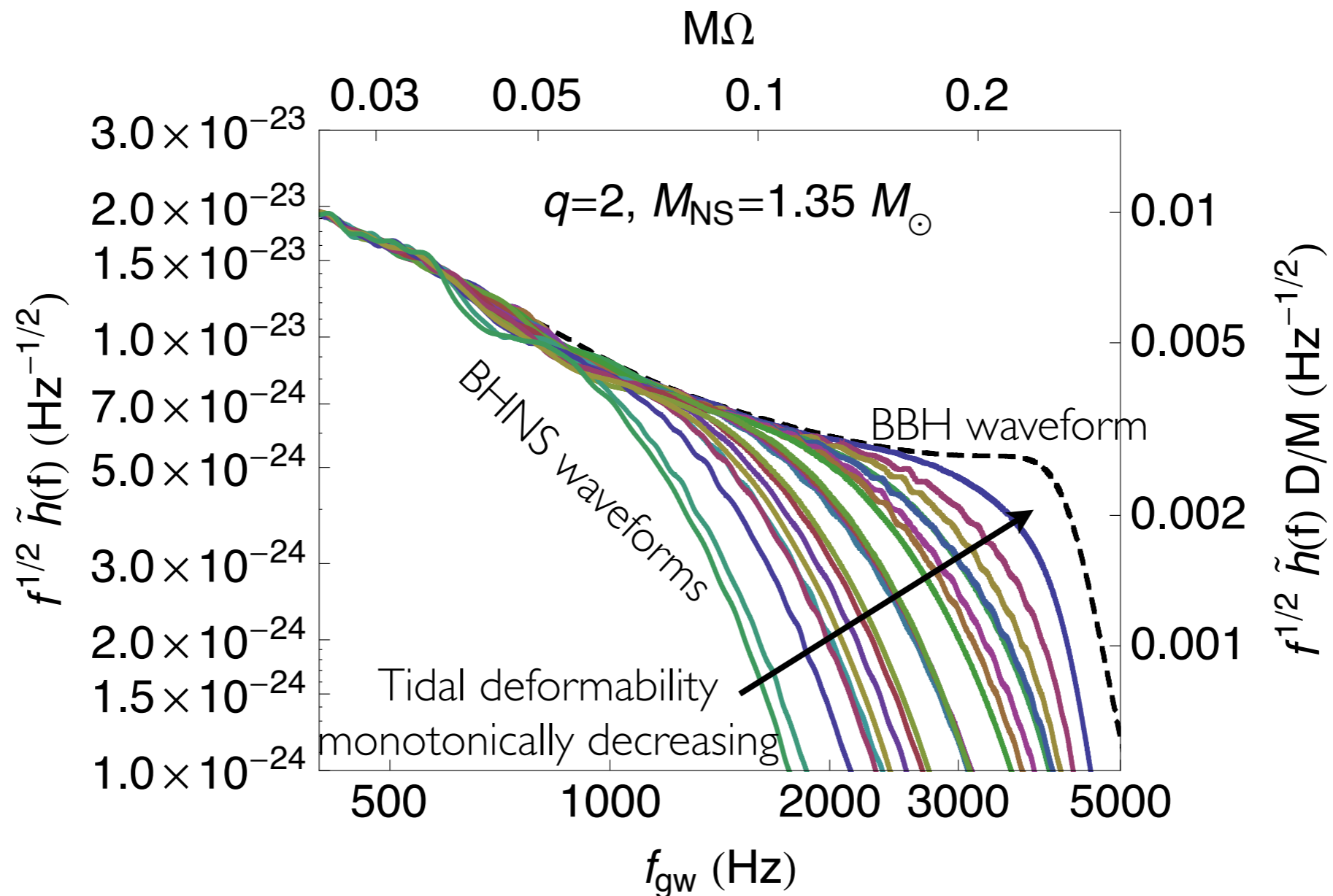
- Cutoff in amplitude from tidal disruption
 - Occurs earlier (lower frequency) for larger stars
 - Much larger effect than phase shift



Slide from Ben Lackey

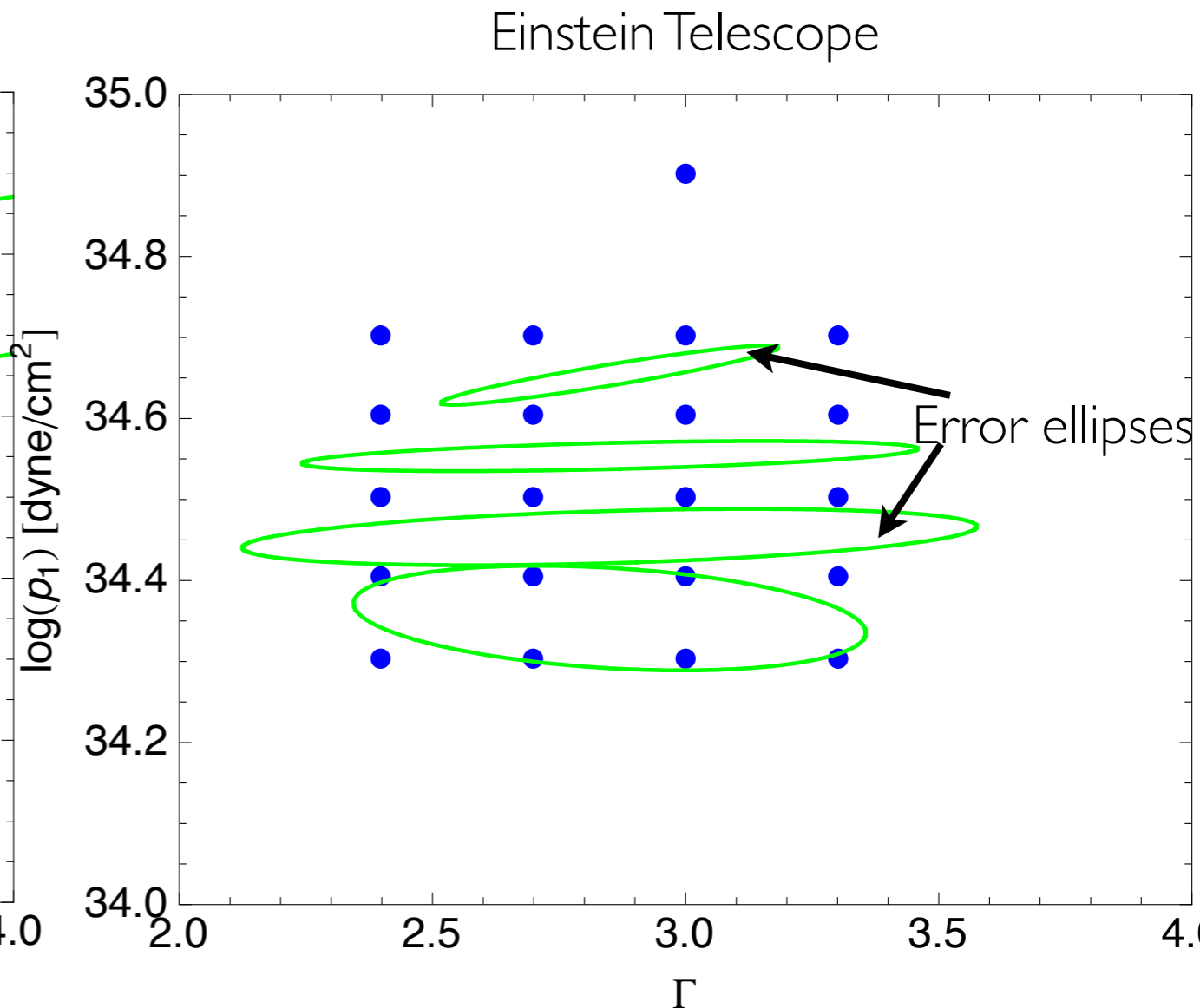
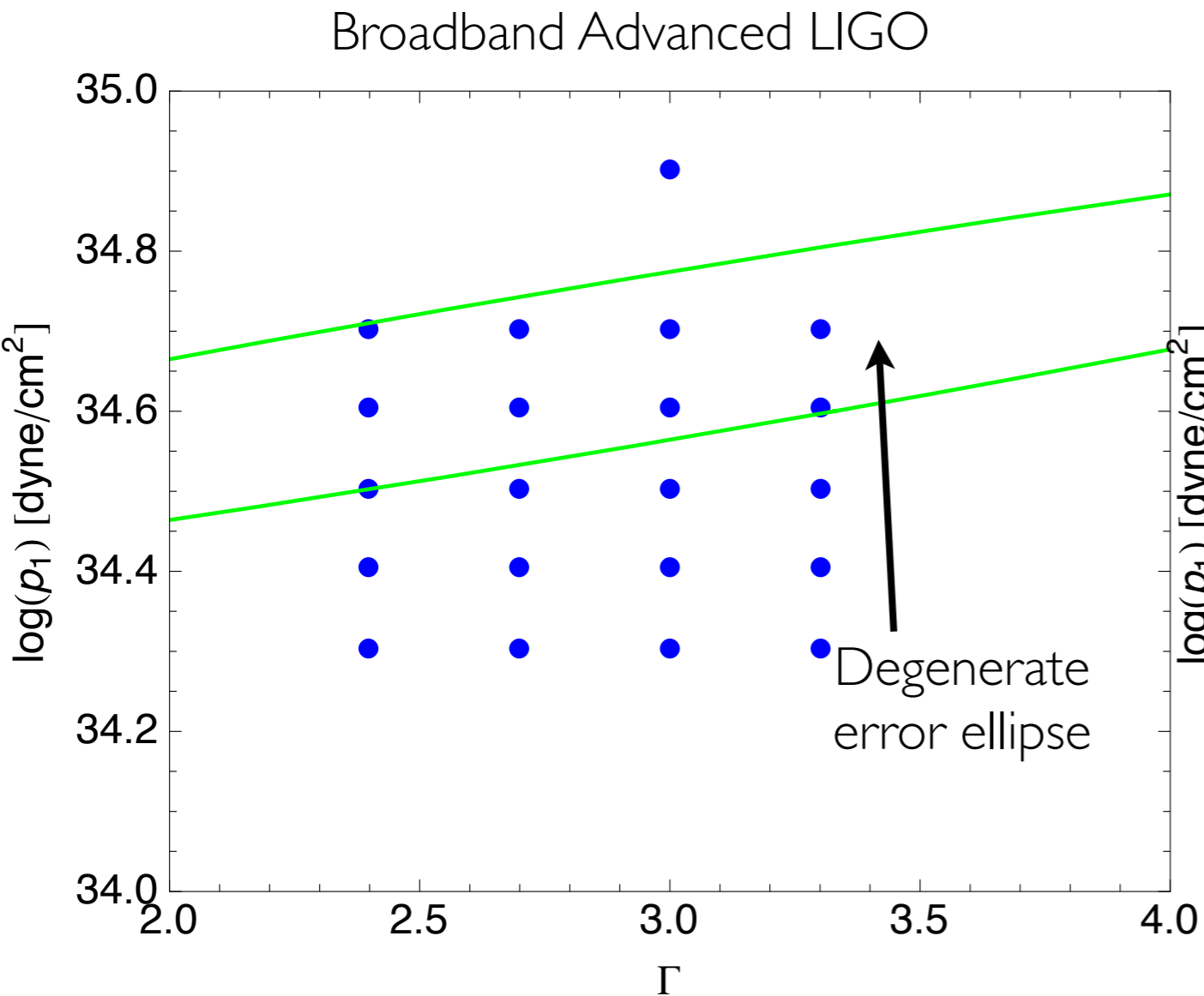
NSBH: What can we extract?

- Cutoff frequency depends on tidal deformability parameter Λ



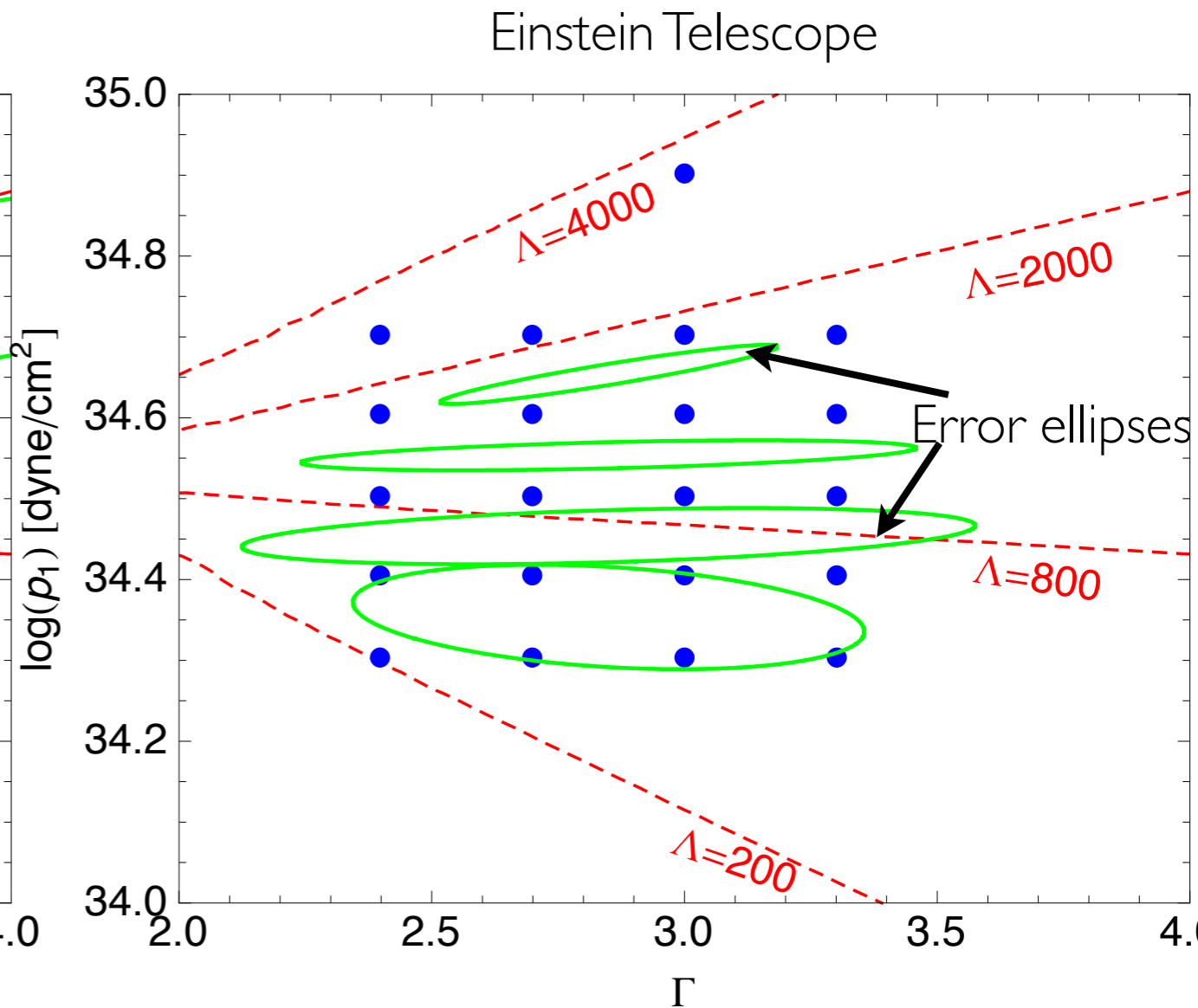
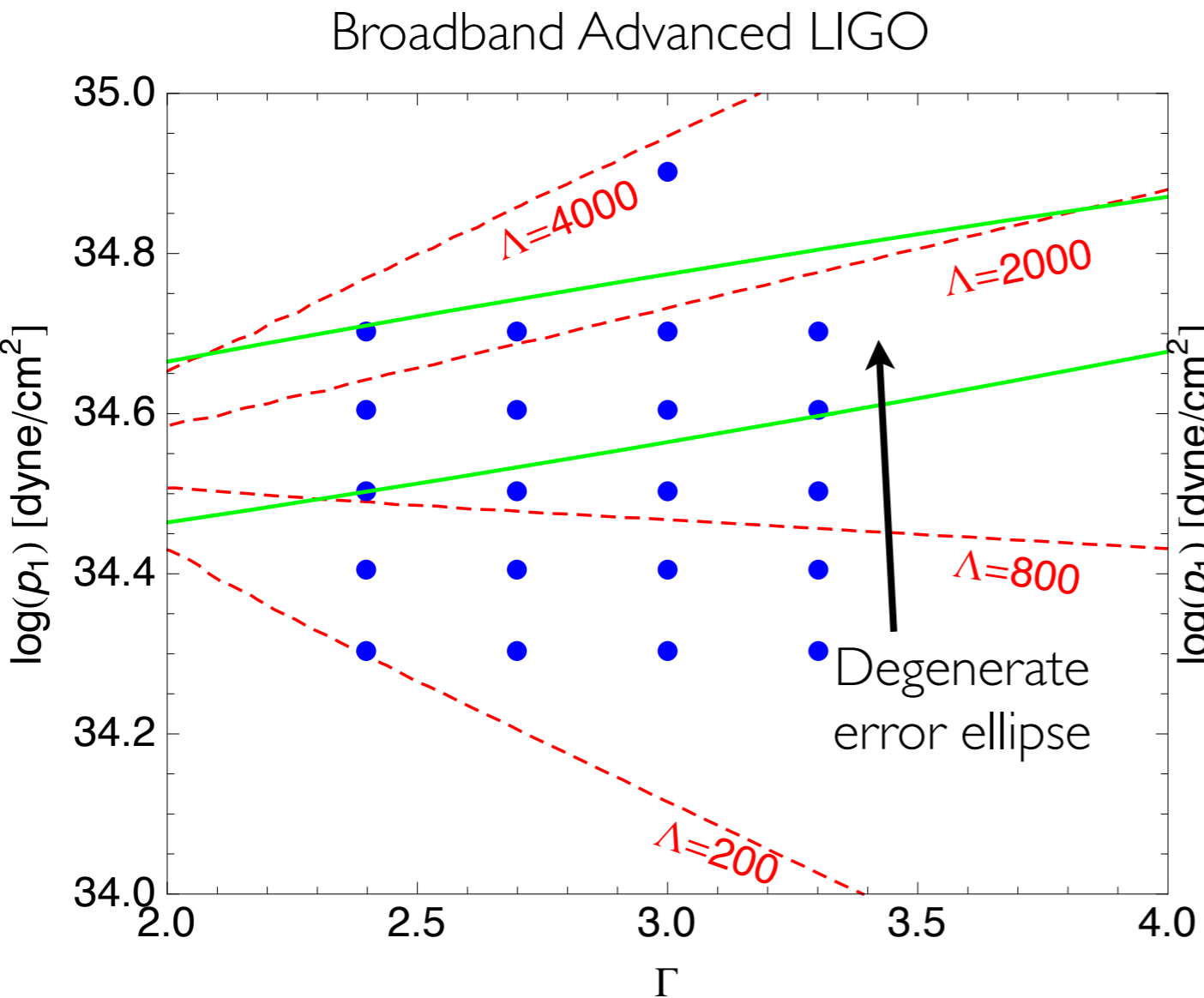
EOS parameter estimates

- 1-sigma errors shown for single binary optimally oriented at 100Mpc
- Errors for proposed Einstein Telescope 5-10 times smaller than for Advanced LIGO



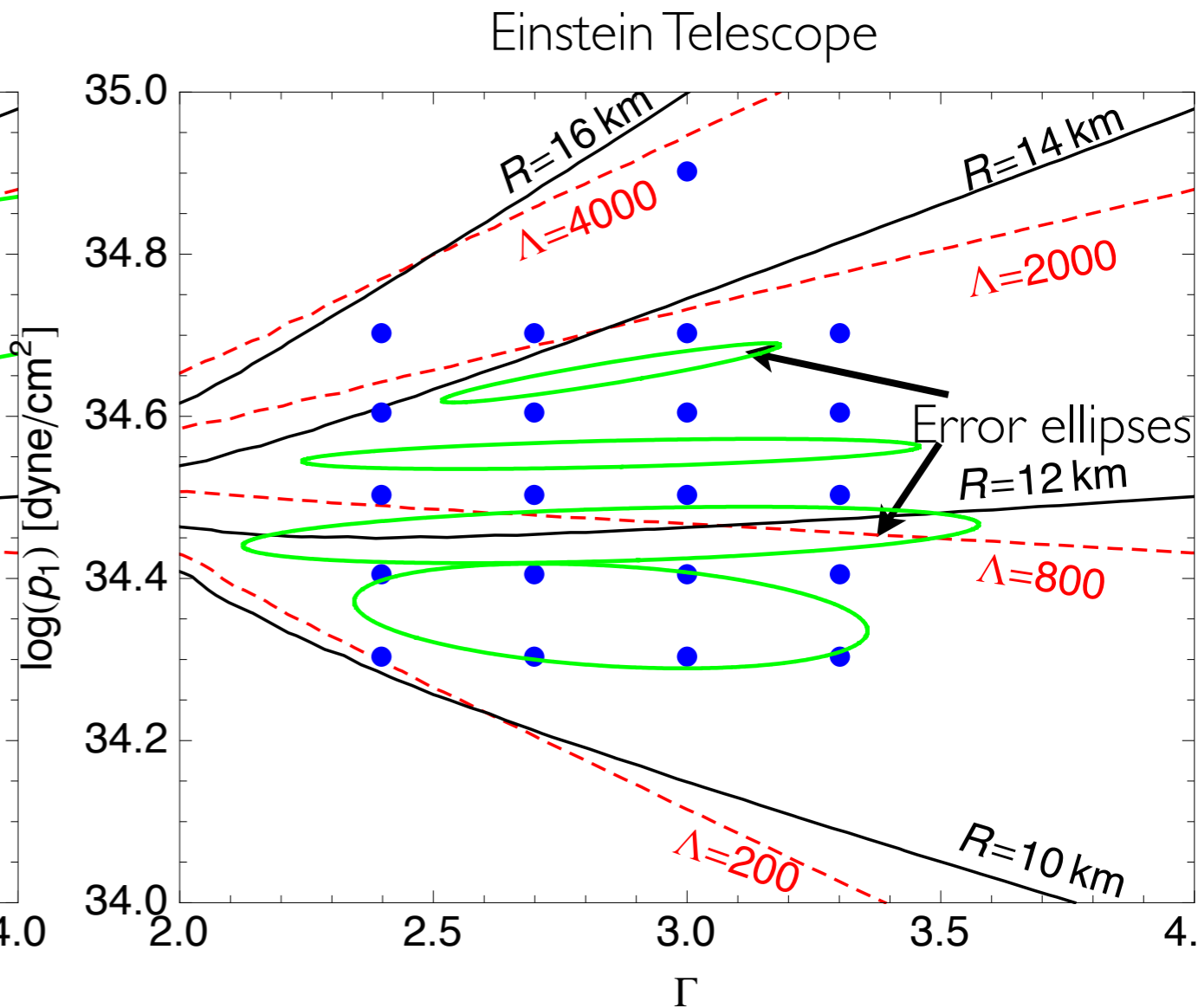
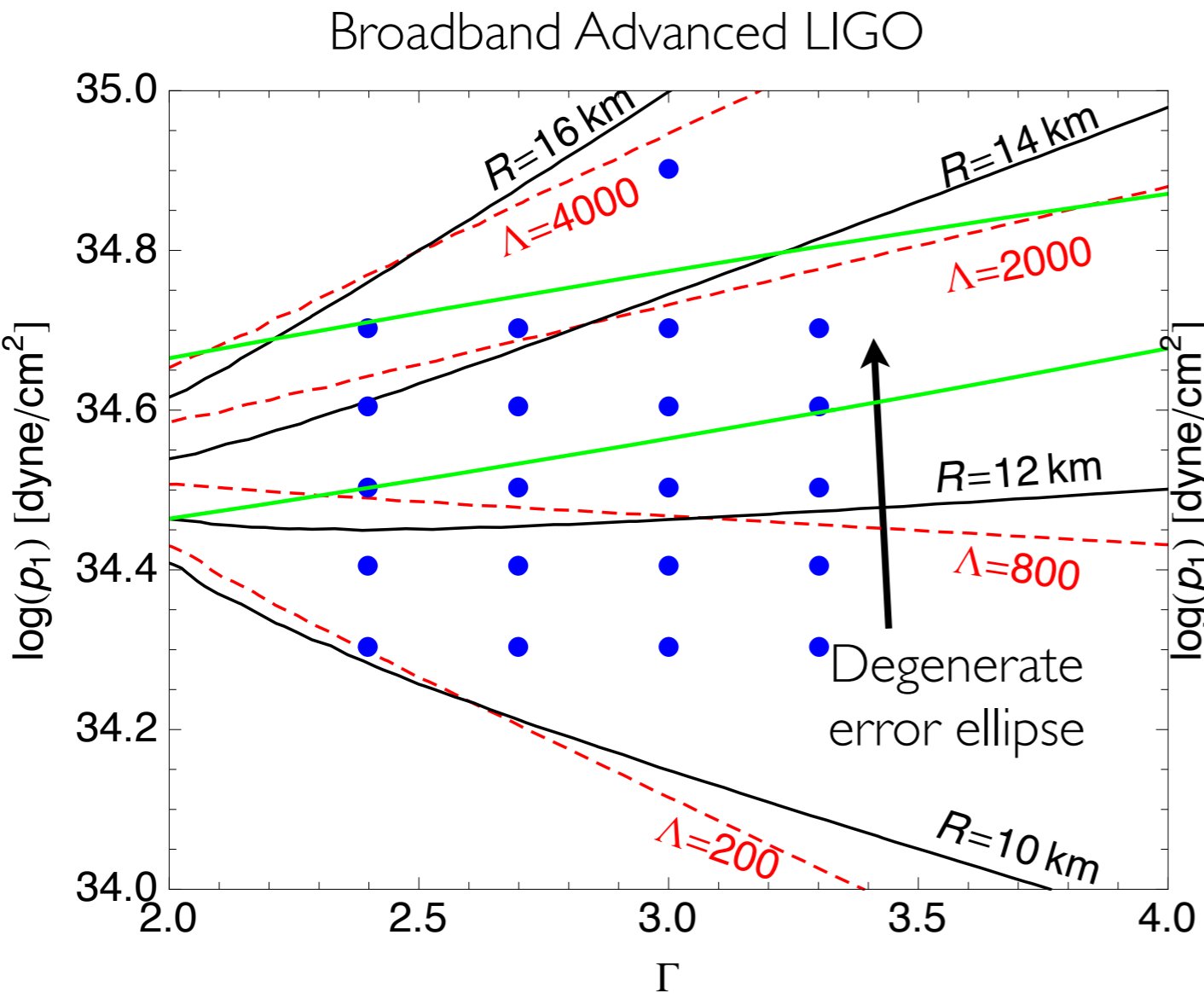
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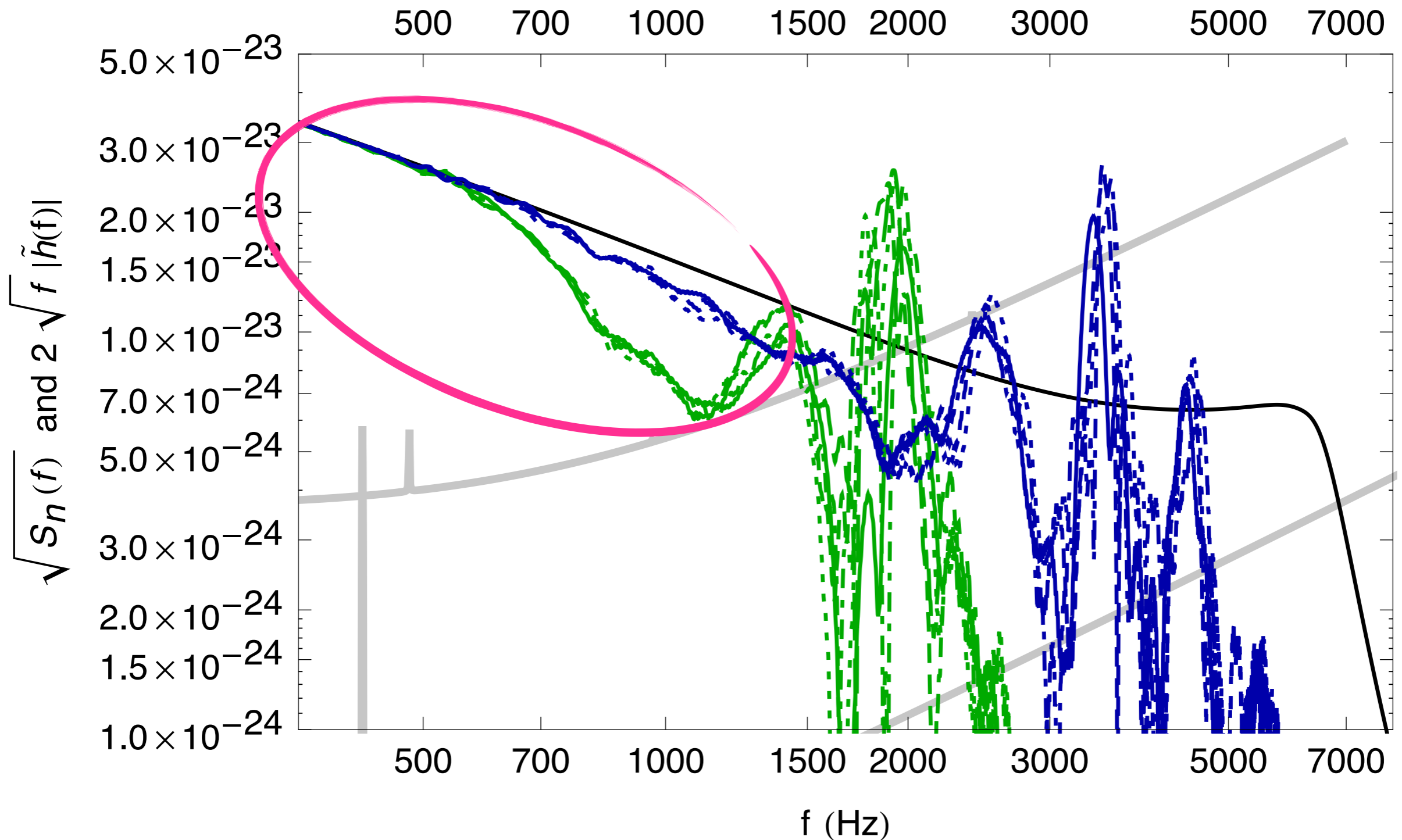
EOS parameter estimates

- 1-sigma errors shown for single binary optimally oriented at 100Mpc
- Errors for proposed Einstein Telescope 5-10 times smaller than for Advanced LIGO

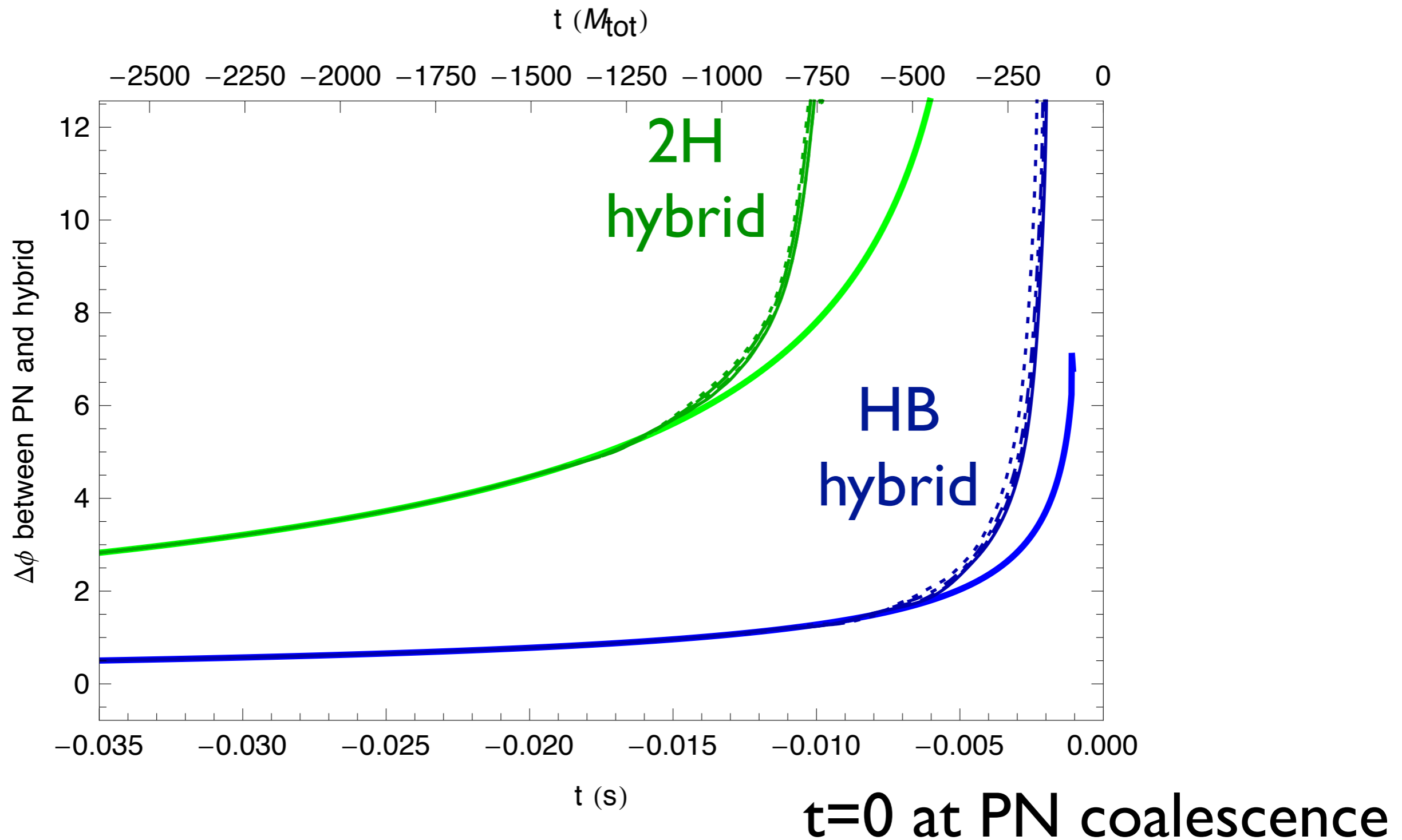


- The same EOS parameter that determines behavior during inspiral also accurately describes behavior during merger/ringdown

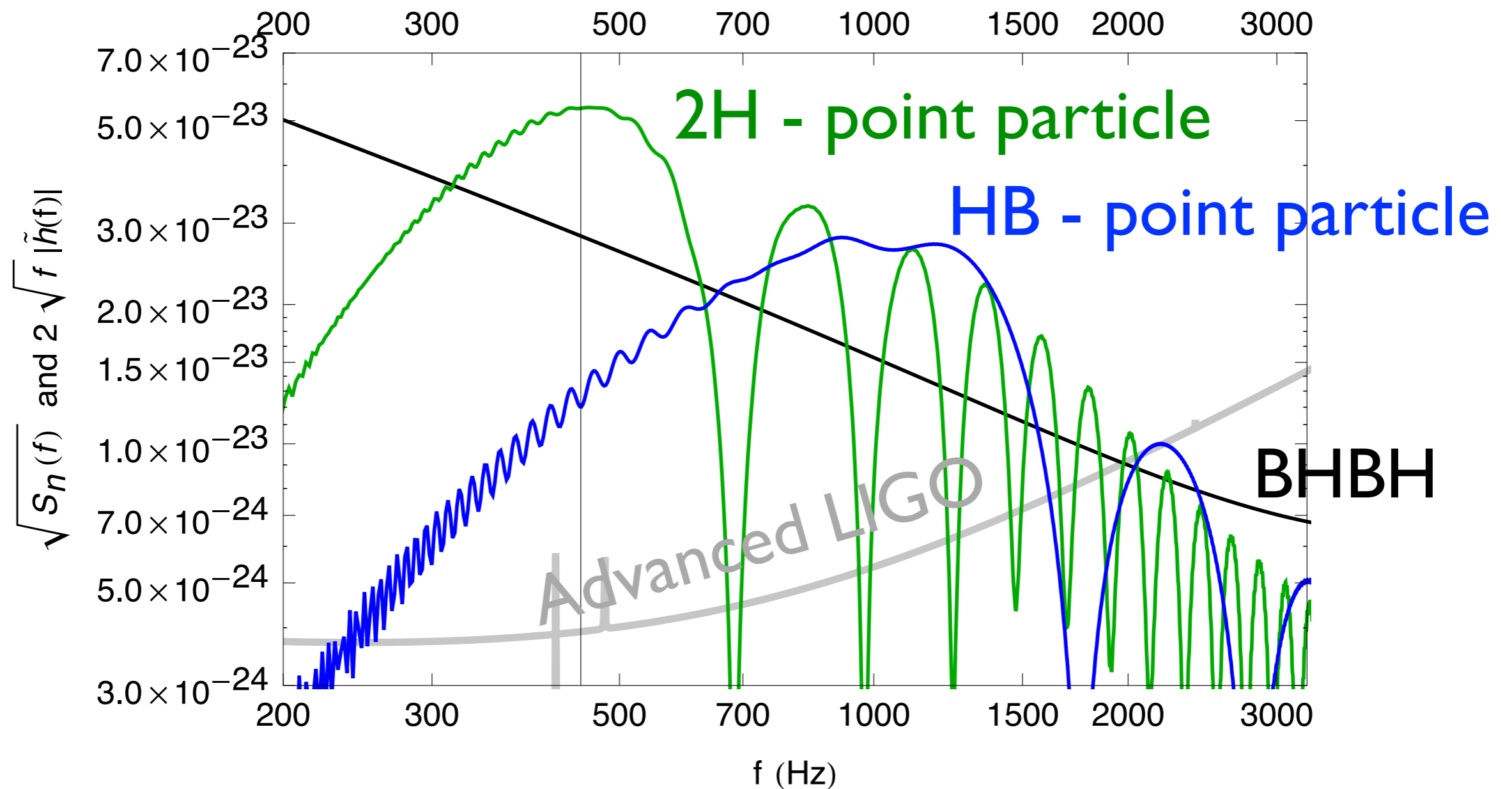
NSNS: Hybrid construction improves inspiral measurability



Transition hybrid to numerical merger in late inspiral,
resolution does not significantly modify phase evolution



Amplitude spectrum of difference between NSNS waveforms and waveforms with no matter
(This better encodes the accumulated phase differences)



	Broadband aLIGO	ET-D
EOS 2H to EOS HB		
$R = 13.42$	± 0.50 km	± 0.05 km
$(\Lambda)^{1/5} = 2.02$	± 0.07	± 0.01
EOS 2H to unmodified PN		
$(\Lambda)^{1/5} = 1.18$	± 0.20	± 0.02
EOS HB to unmodified PN		
$(\Lambda)^{1/5} = 0.84$	± 0.28	± 0.03

Some systematics: 3% from change in numerical simulation of same system, 5% variation in hybridization region, 1% neglecting higher order tidal terms