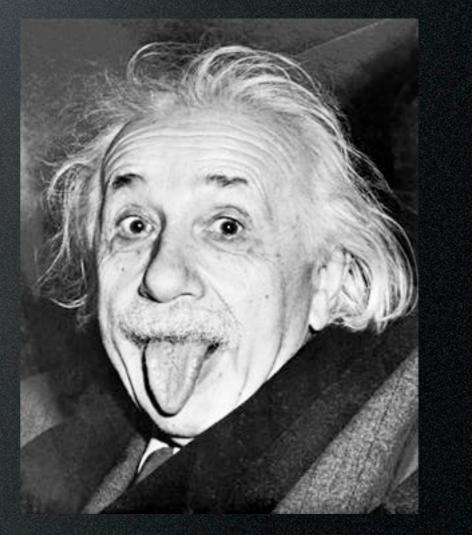
Testing General Relativity with Future GW Observations Scientific Workshop Montana State University, April 5th-April 7th, 2013 http://www.physics.montana.edu/gravity/workshop/workshop.htm

Part of Celebrating Einstein Mega-Outreach Event Montana State University, April 1st-April 6th, 2013



Testing General Relativity with Compact Binary Inspirals

> Nico Yunes Montana State University

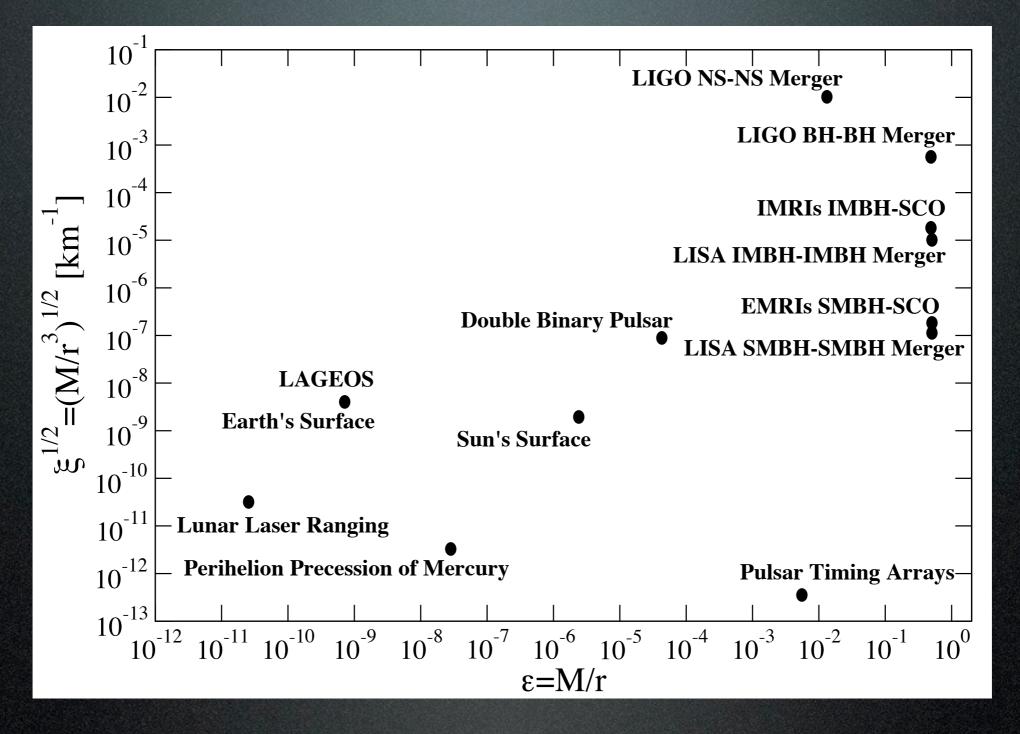
> > Aug. 3rd, 2012, KITP, UCSB

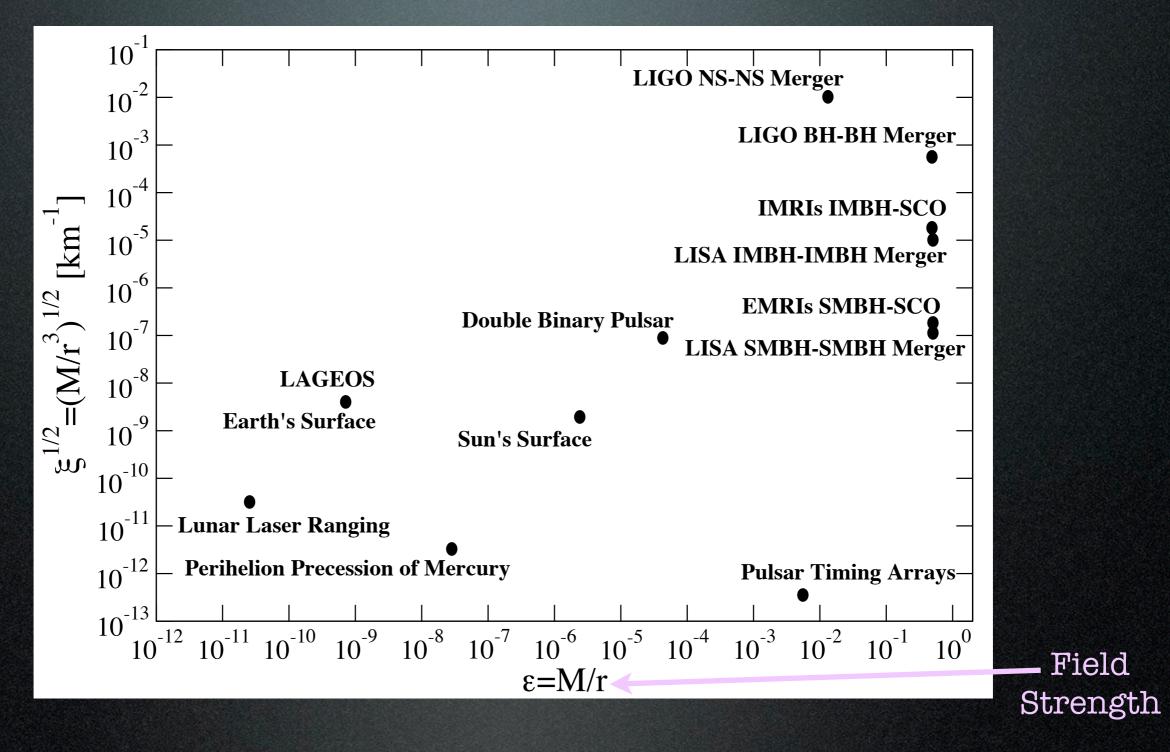
Standing on the shoulders of...

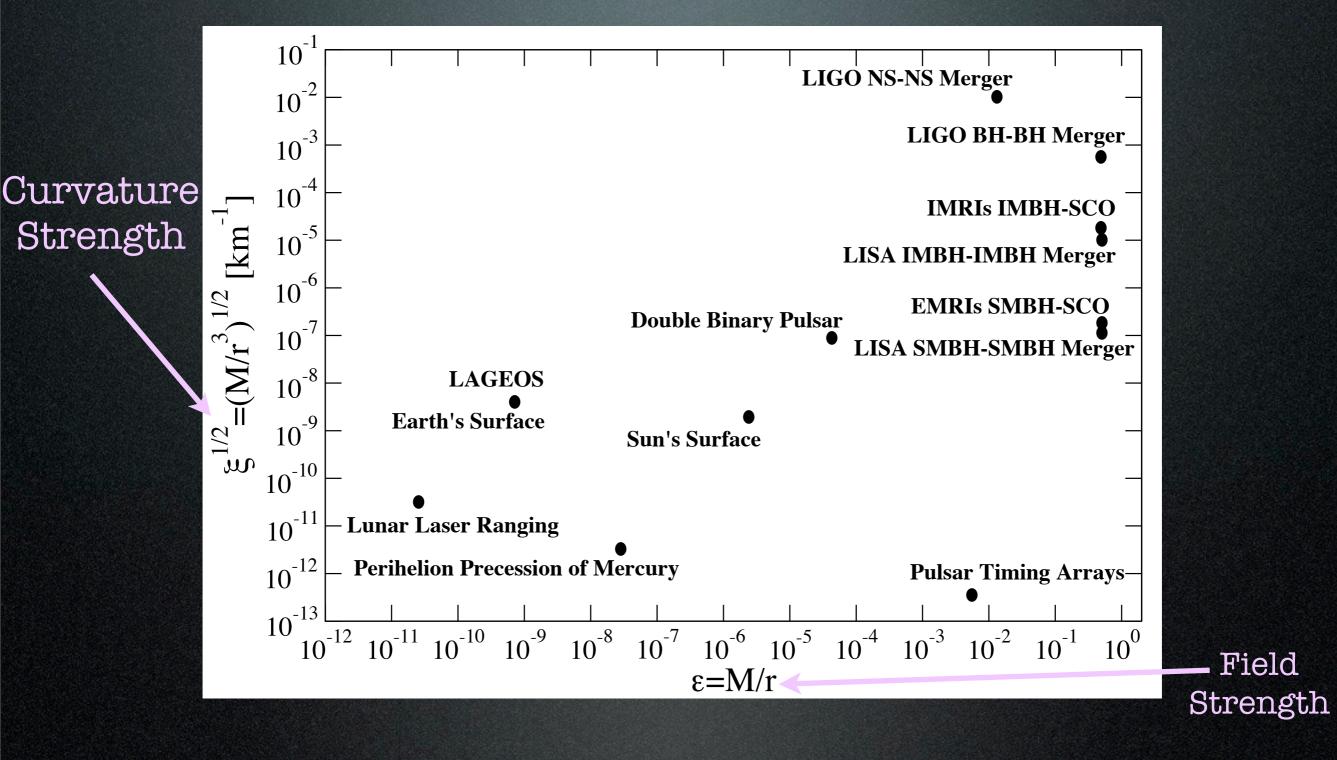
Clifford Will, Jim Gates, Stephon Alexander, Abhay Ashtekar, Sam Finn, Ben Owen, Pablo Laguna, Emanuele Berti, Uli Sperhake, Dimitrios Psaltis, Avi Loeb, Vitor Cardoso, Leonardo Gualtieri, Daniel Grumiller, David Spergel, **Frans Pretorius, Neil Cornish**, Scott Hughes, Carlos Sopuerta, Takahiro Tanaka, Jon Gair,

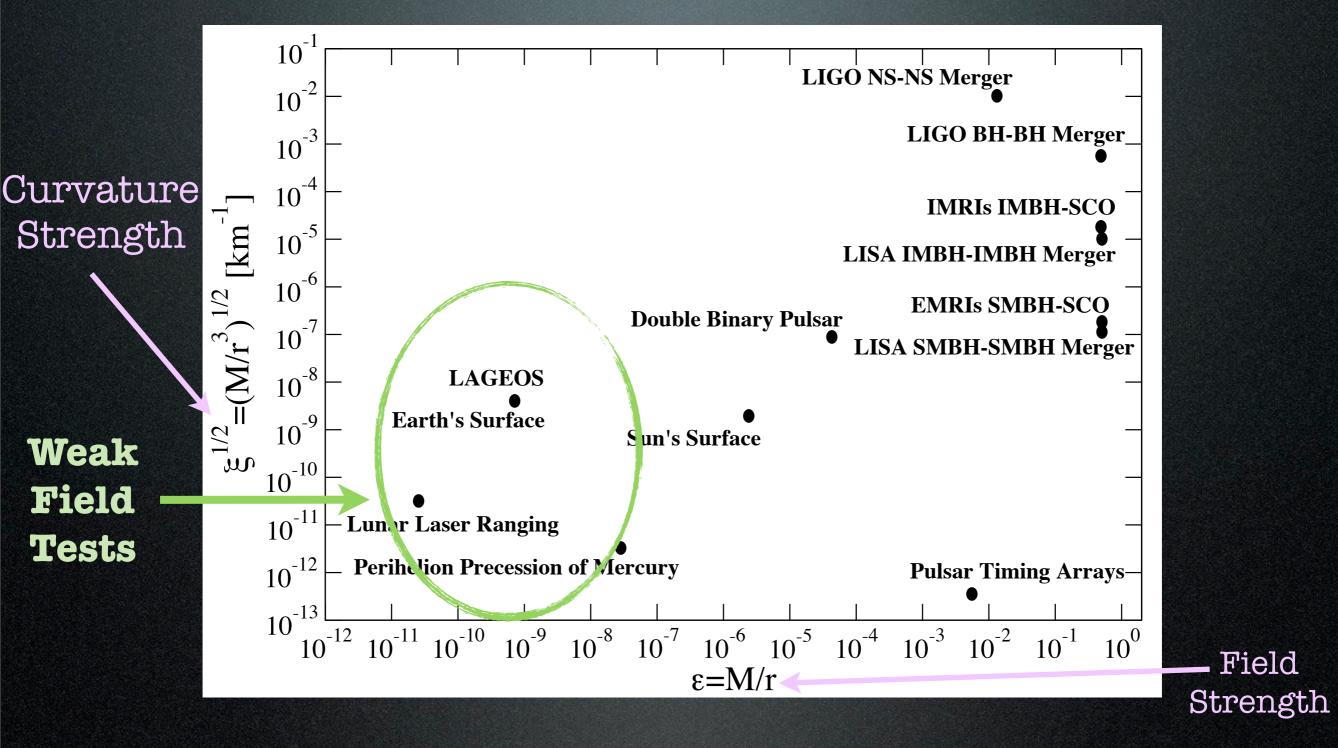
An incomplete summary of the Theory behind Inspiral GW tests of GR

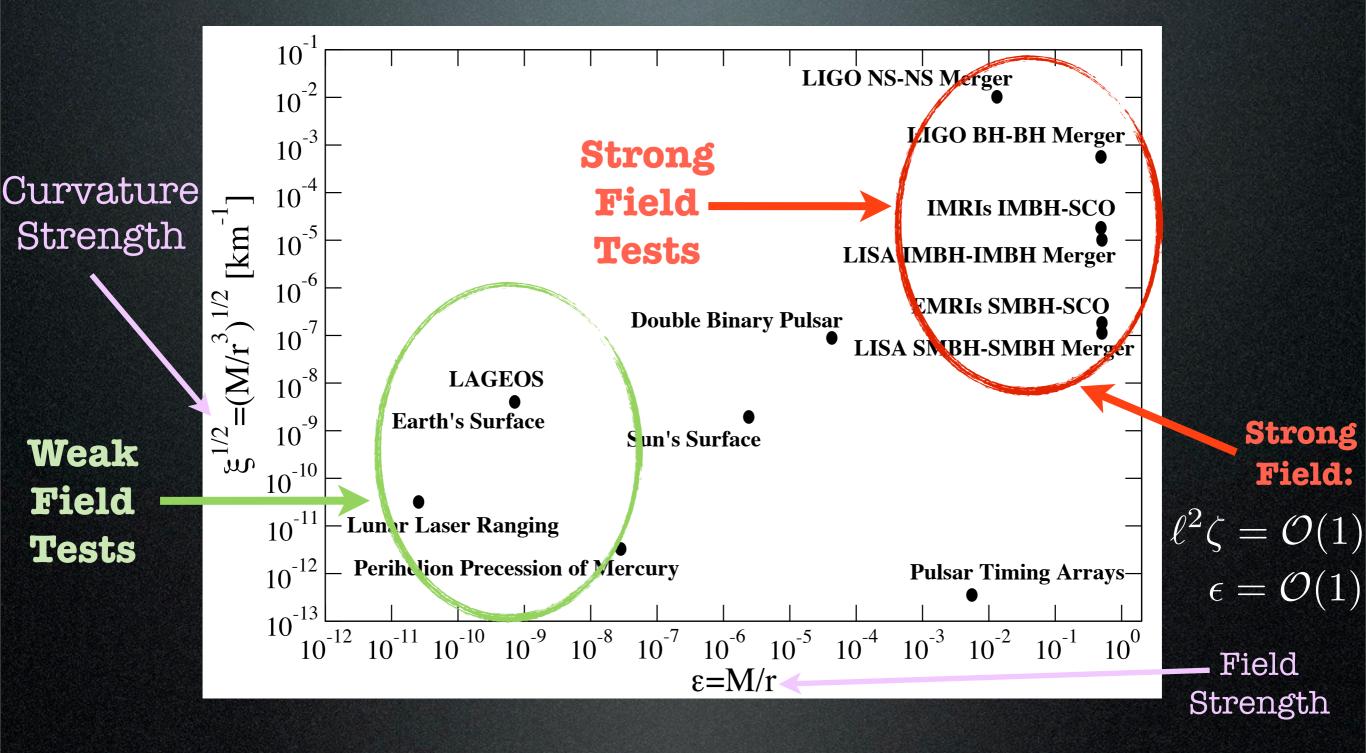
Paolo Pani, Antoine Klein, Kent Yagi, Laura Sampson, Leo Stein, Sarah Vigeland, Katerina Chatziioannou, Haris Apostolatos,
Philippe Jetzer, Leor Barack, Curt Cutler, Kostas Glampedakis,
Stanislav Babak, Ilya Mandel, Chao Li, Eliu Huerta, Chris Berry,
Alberto Sesana, Carl Rodriguez, Georgios Lukes-Gerakopoulos,
George Contopoulus, Chris van den Broeck, Walter del Pozzo, Jon
Veitch, Nathan Collins, Deirdre Shoemaker, Sathyaprakash, etc.

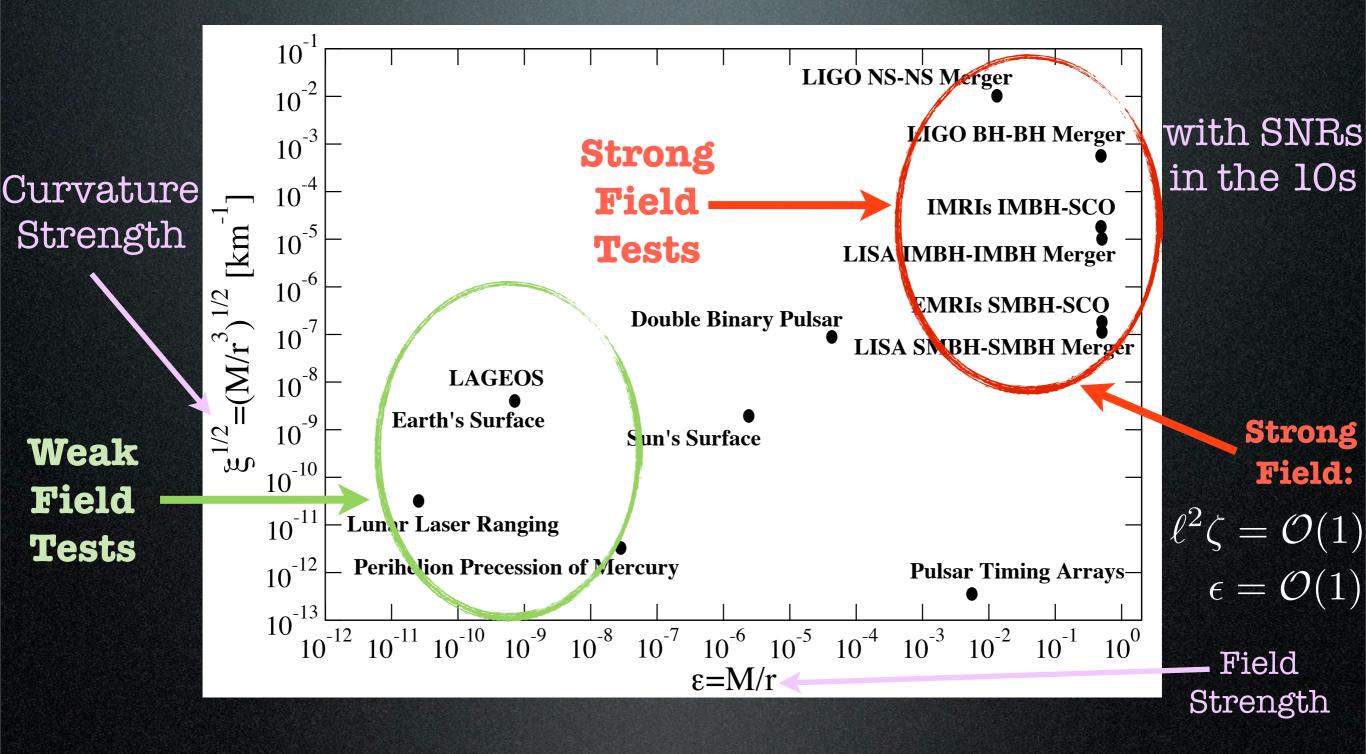


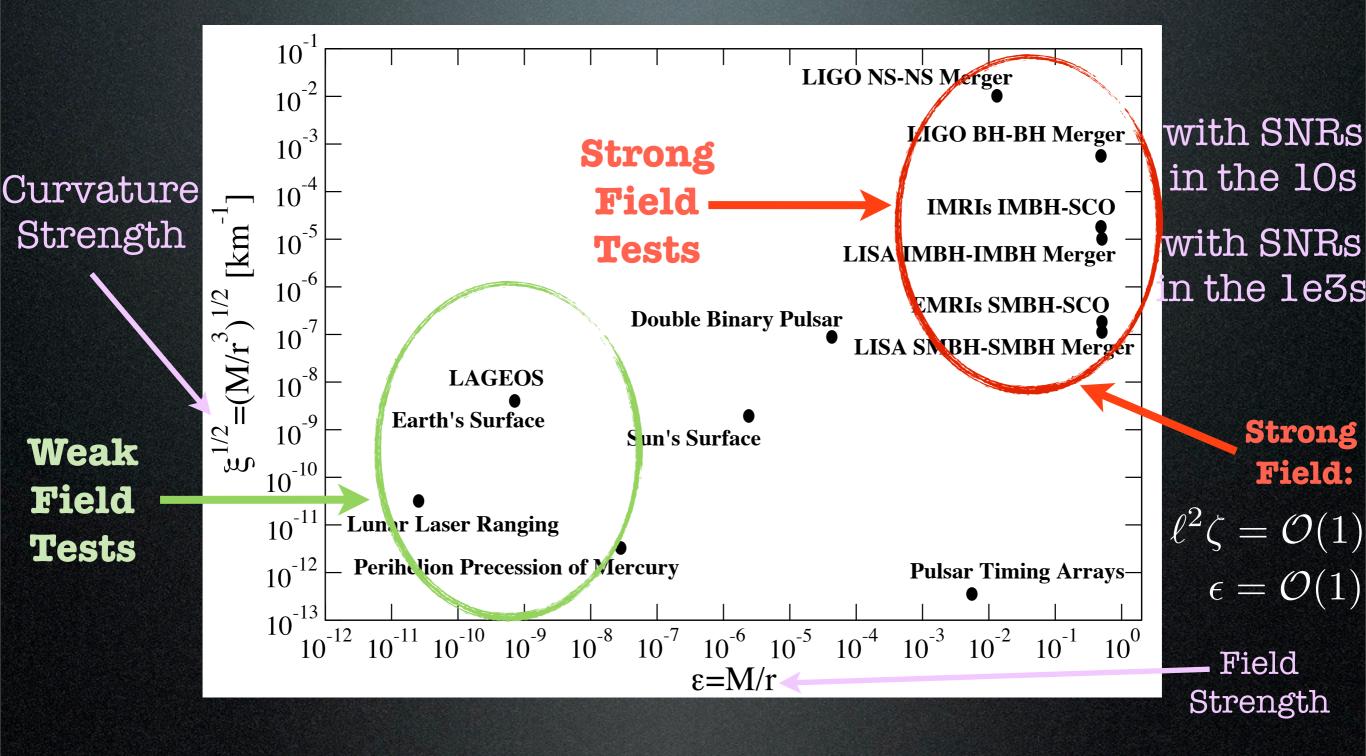


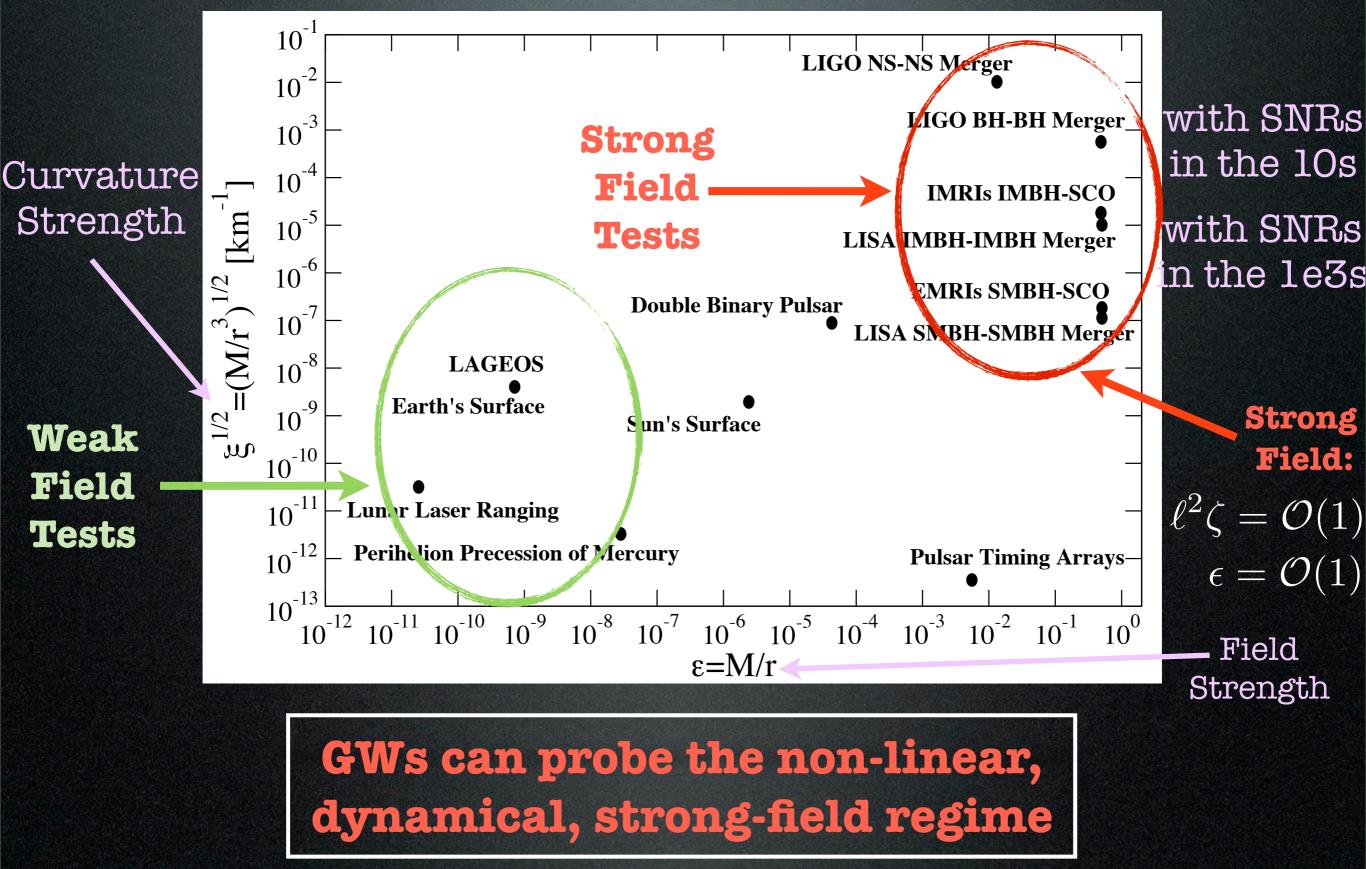










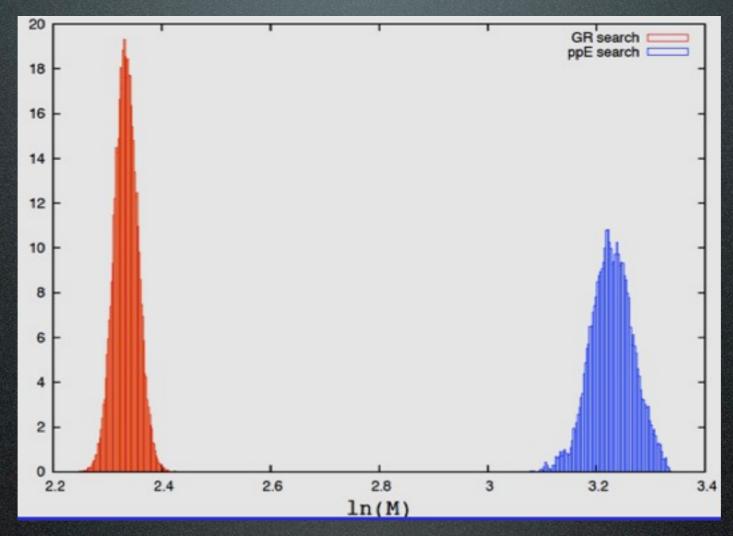


Verify and only then Trust

Unconstrained GR modifications can alter astrophysical inferences (fundamental bias).

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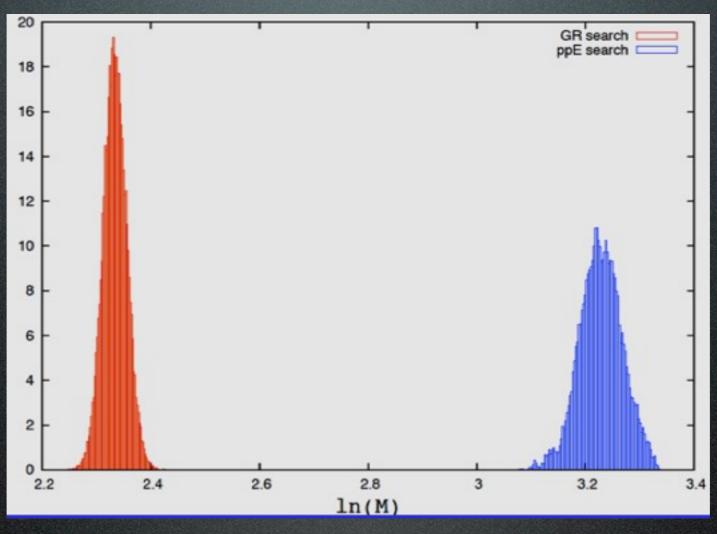
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Cornish, Sampson, Yunes & Pretorius, 2011

Verify and only then Trust

Unconstrained GR modifications can alter astrophysical inferences (fundamental bias).



Cornish, Sampson, Yunes & Pretorius, 2011

Modified theories can:

i) Change GW amplitude -> error in GW DL and inc. angle.
ii) Change GW phase -> error in GW Mchirp, mass ratio, EOS.

iii) Change ISCO -> error in EM spin measurement.

Road Map

ppE Theory

ppE Implementation

What I will leave out

>Data analysis [Veitch].

>Detailed waveform modeling within GR [Pan]
>Non-Integrable orbits, Chaos, Poincare Islands
>Cosmology.

>Quasi-normal ringdown and merger tests.

ppE Theory

I.

Test Classification

Non-Generic Tests

• Pick a theory and test it. Eg. Brans-Dicke Theory.

• Problem: what theory do you pick? Do we have to consider all possibilities?

Will, PRD 50, 1994,
Will, PRD 57, 1998,
Scharre & Will, PRD 65, 2002,
Will & Yunes, CQG 21, 2004,
Berti, et al PRD 71, 2005,
Stavridis & Will, CQG 28, 2009,
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• Search for modelindependent GR deviations.

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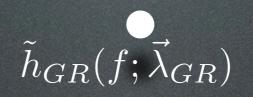
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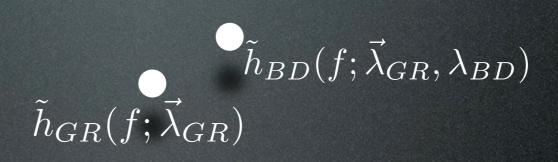
Generic Tests

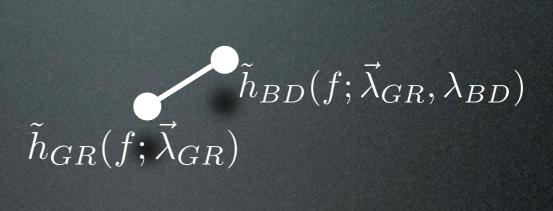
• Search for modelindependent GR deviations.

• Develop a "meta"-model (e.g. ppN) but for GWs: **pp**E

> Yunes & Pretorius, PRD 80, '09, Yunes & Hughes, PRD 82, '10, Yagi, Stein, Yunes and Tanaka '11, Cornish, Sampson, Yunes & Pretorius, '11, del Pozzo, et al, PRD 83, '11 Li, et al, '12, Arun, CQG '12 Chatziioannou, Yunes & Cornish, '12,









 $ilde{h}_{MG}(f;ec{\lambda}_{GR},\lambda_{MG})$ $\tilde{h}_{BD}(f; \vec{\lambda}_{GR}, \lambda_{BD})$ $\tilde{h}_{GR}(f;\vec{\lambda}_{GR})$

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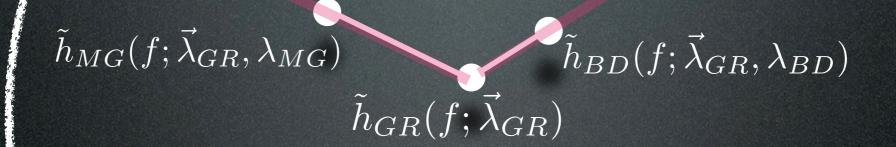
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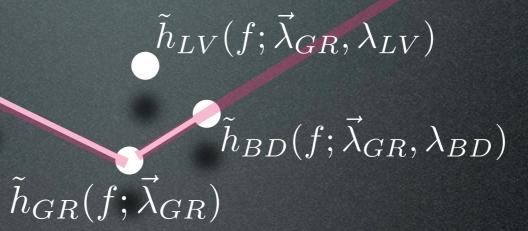
", ι^{0} ",



", ι^{0} ",



$\tilde{h}_{MG}(f; \vec{\lambda}_{GR}, \lambda_{MG})$



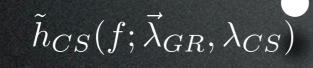
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$ilde{h}_{MG}(f;ec{\lambda}_{GR},\lambda_{MG})$

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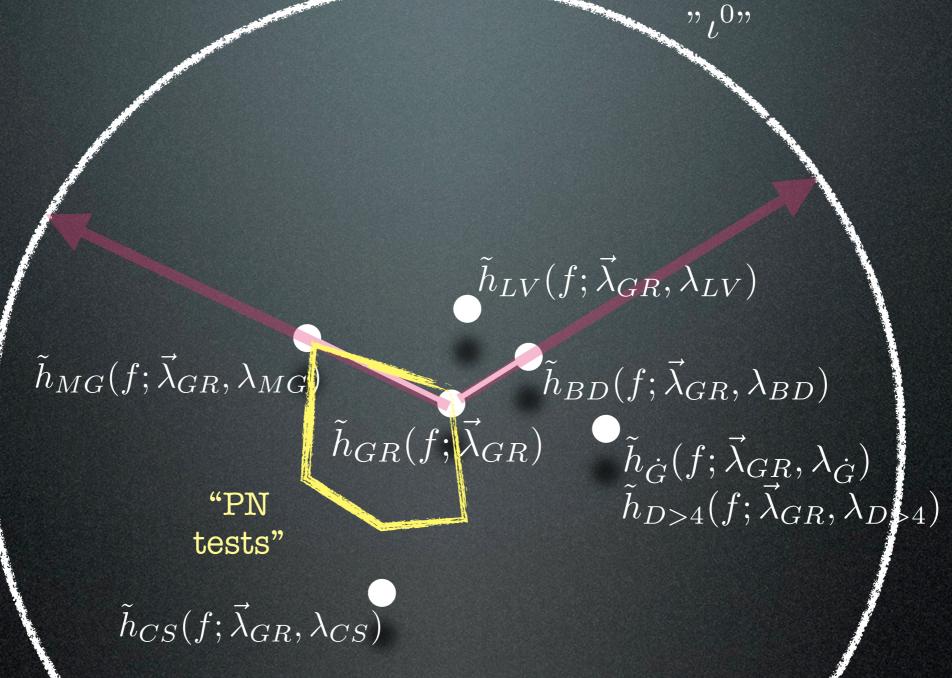
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 $ilde{h}_{LV}(f;ec{\lambda}_{GR},\lambda_{LV})$

»,⁰,

 $ilde{h}_{CS}(f;ec{\lambda}_{GR},\lambda_{CS})$





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"PN

tests"

 $\tilde{h}_{ppE}(f;\vec{\lambda}_{GR},\vec{\lambda}_{ppE})$

Theoretical ppE Construction

Yunes & Pretorius, PRD 2009 Mirshekari, Yunes & Will, PRD 2012 Chatziioannou, Yunes & Cornish, PRD 2012

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>I. Parametrically deform the Hamiltonian.

 $A = A_{\rm GR} + \delta A$ $\delta A_{H,RR} = \bar{\alpha}_{\rm H,RR} v^{\bar{a}_{\rm H,RR}}$

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$$h = F_+h_+ + F_\times h_\times + F_s h_s + \dots$$

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>I. Parametrically deform the Hamiltonian.

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 $A = A_{\rm GR} + \delta A$ $\delta A_{H,RR} = \bar{\alpha}_{\rm H,RR} v^{\bar{a}_{\rm H,RR}}$

$$E_a^2 = p_a^2 c^4 + \tilde{\alpha} p_a^{\tilde{a}}$$

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>I. Parametrically deform the Hamiltonian.

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>IV. Parametrically deform g propagation.

> Result: To leading PN order and leading GR deformation

$$\tilde{h} = \tilde{h}_{\rm GR} \left(1 + \alpha f^a \right) e^{i\beta f^b}$$

$$A = A_{\rm GR} + \delta A$$
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$$E_g^2 = p_g^2 c^4 + \tilde{\alpha} \ p_g^{\tilde{a}}$$

$$\Gamma + II + \Gamma \times II \times + \Gamma_s II_s +$$

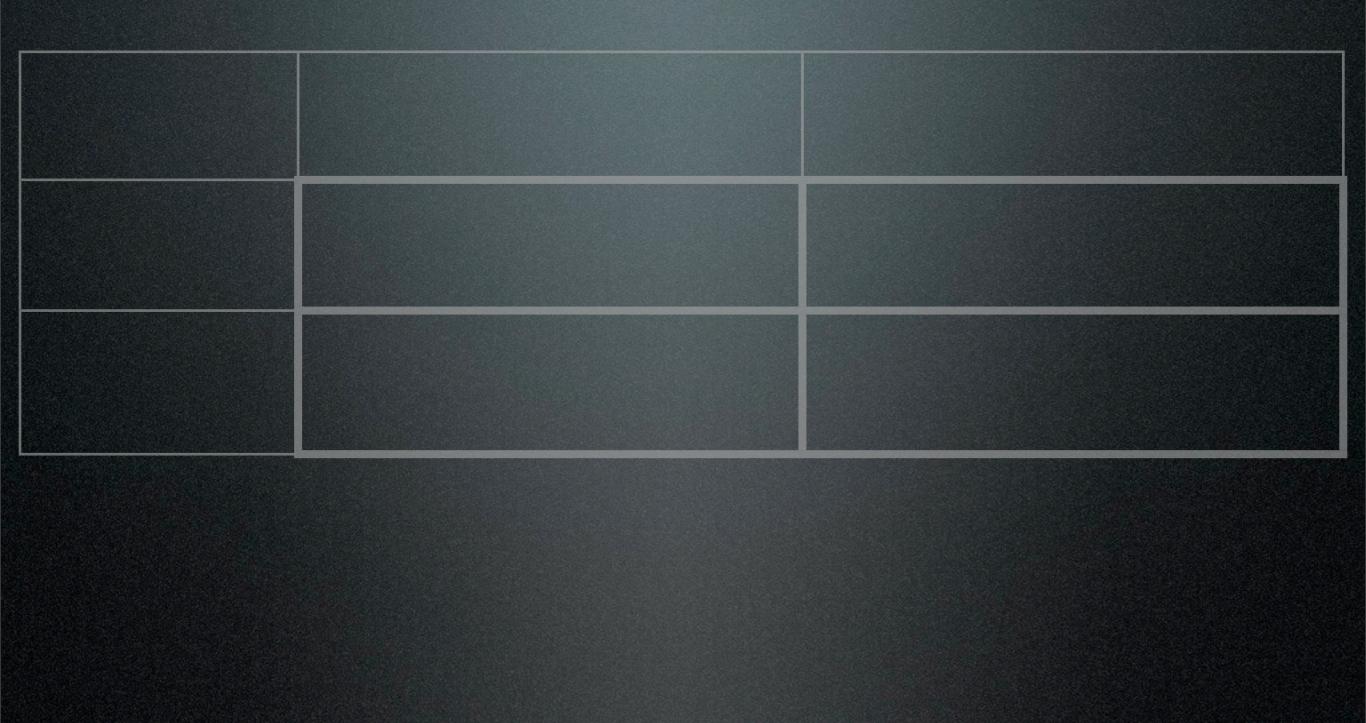
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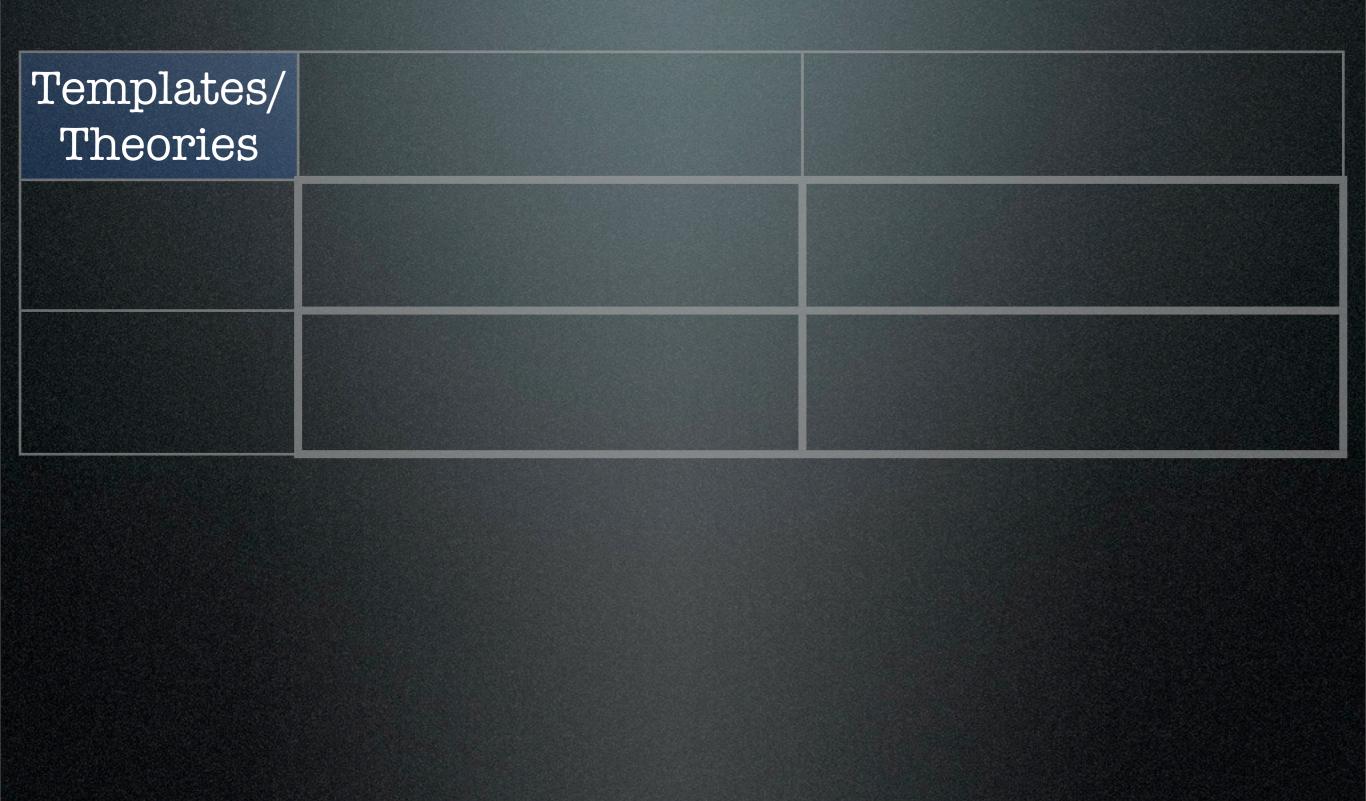
ppE Recovery of Theories $\tilde{h} = \tilde{h}_{\text{GR}} \left[1 + \alpha_{\text{ppE}} \left(\pi \mathcal{M} f \right)^{a_{\text{ppE}}/3} \right] e^{i\beta_{\text{ppE}} \left(\pi \mathcal{M} f \right)^{b_{\text{ppE}}/3}}$

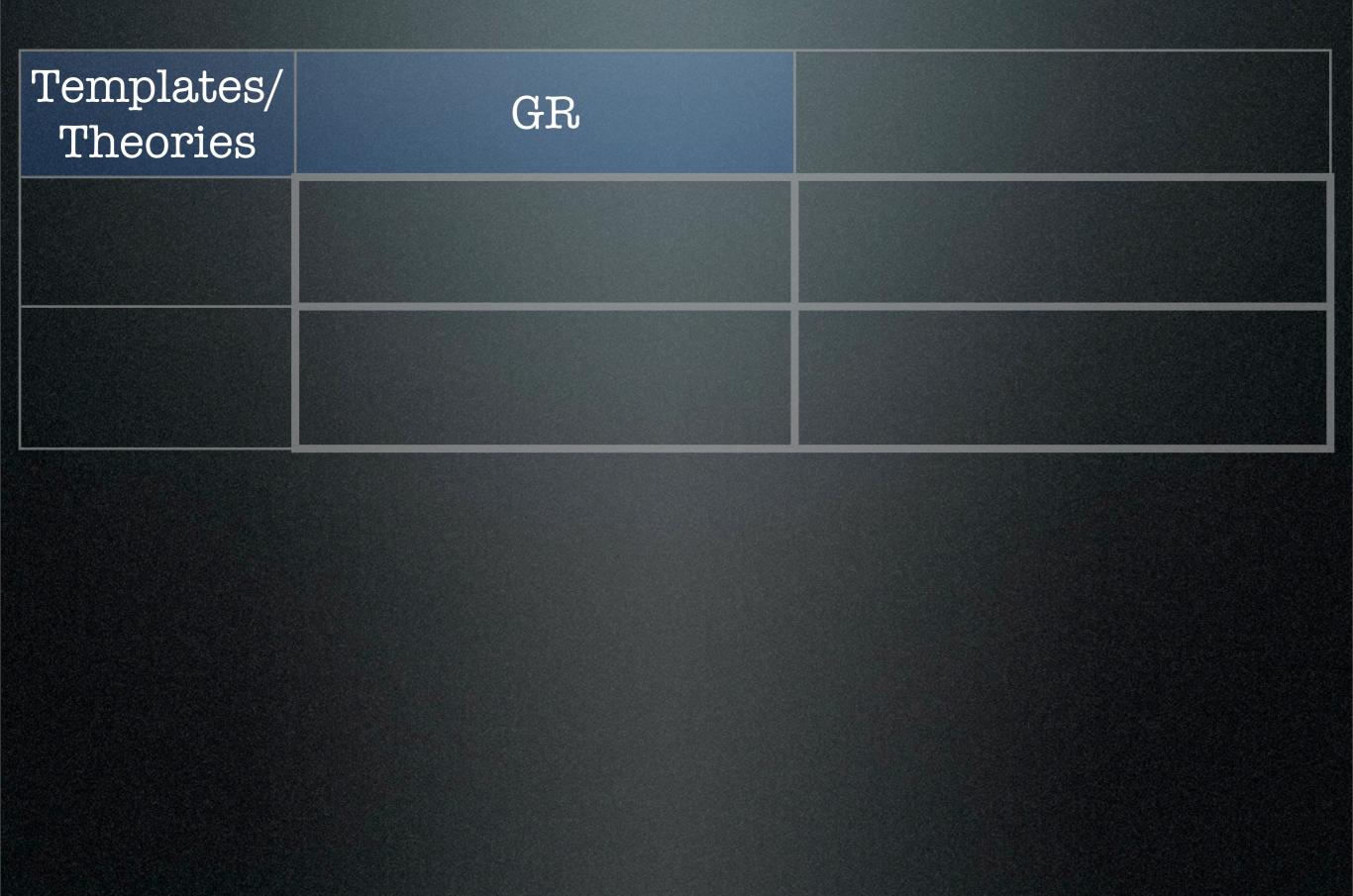
Theory	$lpha_{ m ppE}$	$a_{\rm ppE}$	$\beta_{\rm ppE}$	$b_{\rm ppE}$
Jordan-Brans- Dicke-Fierz	$-rac{5}{96}rac{S^2}{\omega_{ m BD}}\eta^{2/5}$	-2	$-rac{5}{3584}rac{S^2}{\omega_{ m BD}}\eta^{2/5}$	-7
Conservative Einstein-Dilaton- Gauss-Bonnet gravity	$\frac{5}{6}\eta^{-4/5}\zeta_3$	4	$\frac{25}{64}\eta^{-4/5}\zeta_{\text{EDGB}}$	-1
Dissipative Einstein-Dilaton- Gauss-Bonnet gravity	0	•	$-rac{5}{7168}\zeta_3\eta^{-18/5}rac{(m_1-m_2)^2}{m^2}$	-7
Massive Graviton	0	•	$-rac{\pi^2 D\mathcal{M}}{\lambda_g^2(1+z)}$	-3
Lorentz Violation	0	•	$-rac{\pi^{2-\gamma}}{(1-\gamma)}rac{D_{\gamma}}{\lambda_{ m LV}^{2-\gamma}}rac{{\mathcal M}^{1-\gamma}}{(1+z)^{1-\gamma}}$	$-3\alpha_{\rm LV}-3$
G(t) Theory	$-\frac{5}{512}\dot{G}\mathcal{M}$	-8	$-\frac{\frac{25}{65536}\dot{G}_{c}\mathcal{M}}{-\frac{75}{2554344}\frac{dM}{dt}\eta^{-4}(3-26\eta+24\eta^{2})}$	-13
Extra Dimensions		•	$-\frac{75}{2554344}\frac{dM}{dt}\eta^{-4}(3-26\eta+24\eta^2)$	-13
Non-Dynamical Chern-Simons Gravity	$lpha_{ m PV}$	3	$\beta_{\rm PV}$ Siemens & Yunes,	6 LRR '13

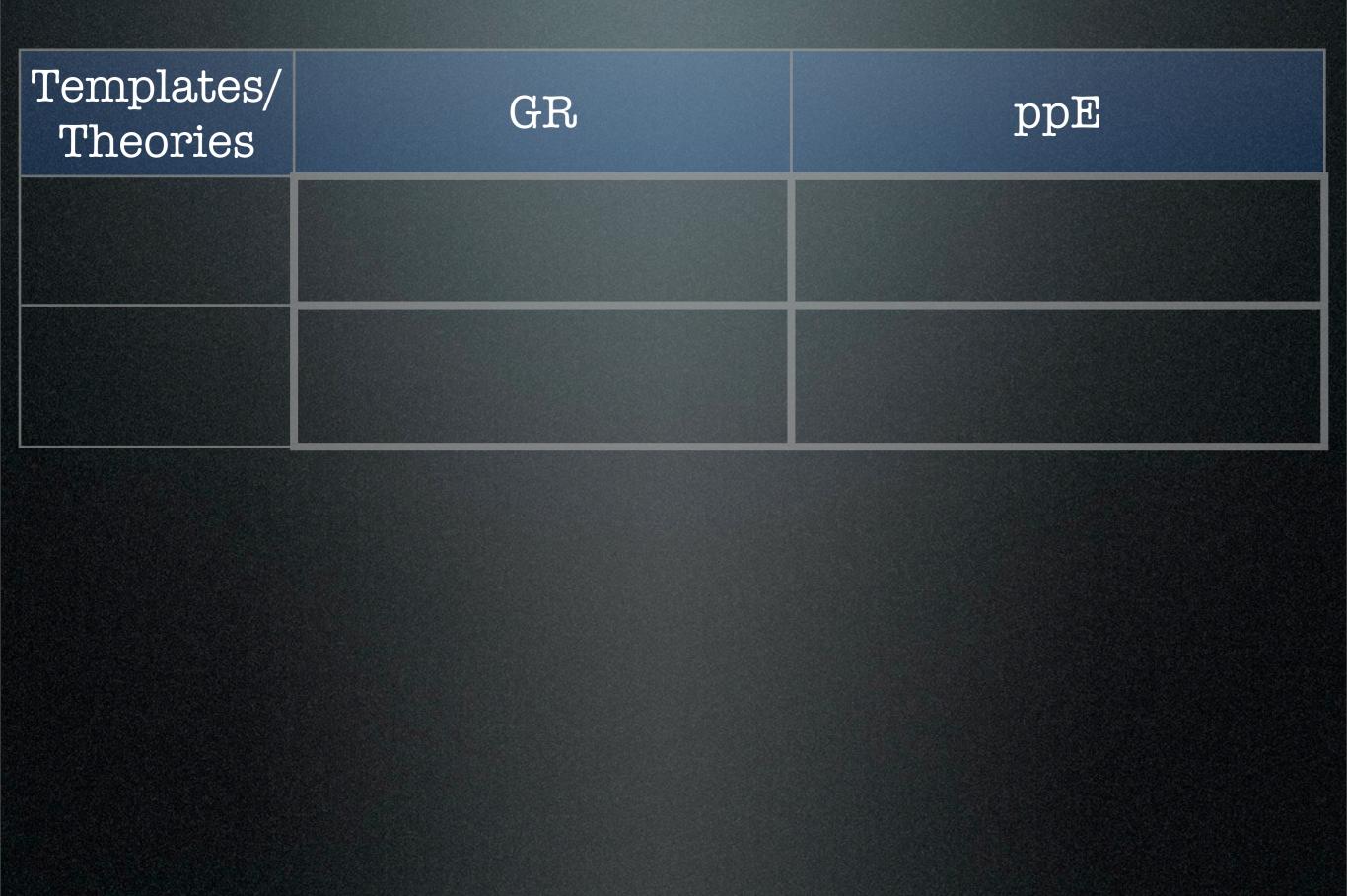
ppE Implementation

II.









Templates/ Theories	GR	ppE
GR		

Templates/ Theories	GR	ppE
GR	Business as usual	

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GR	Business as usual	Quantify the statistical significance that the detected event is within GR. Anomalies?

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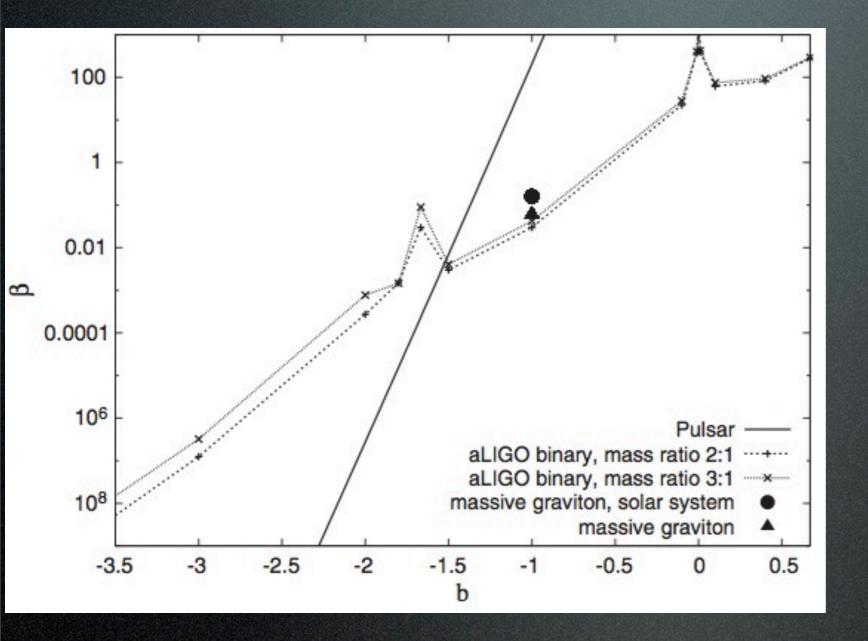
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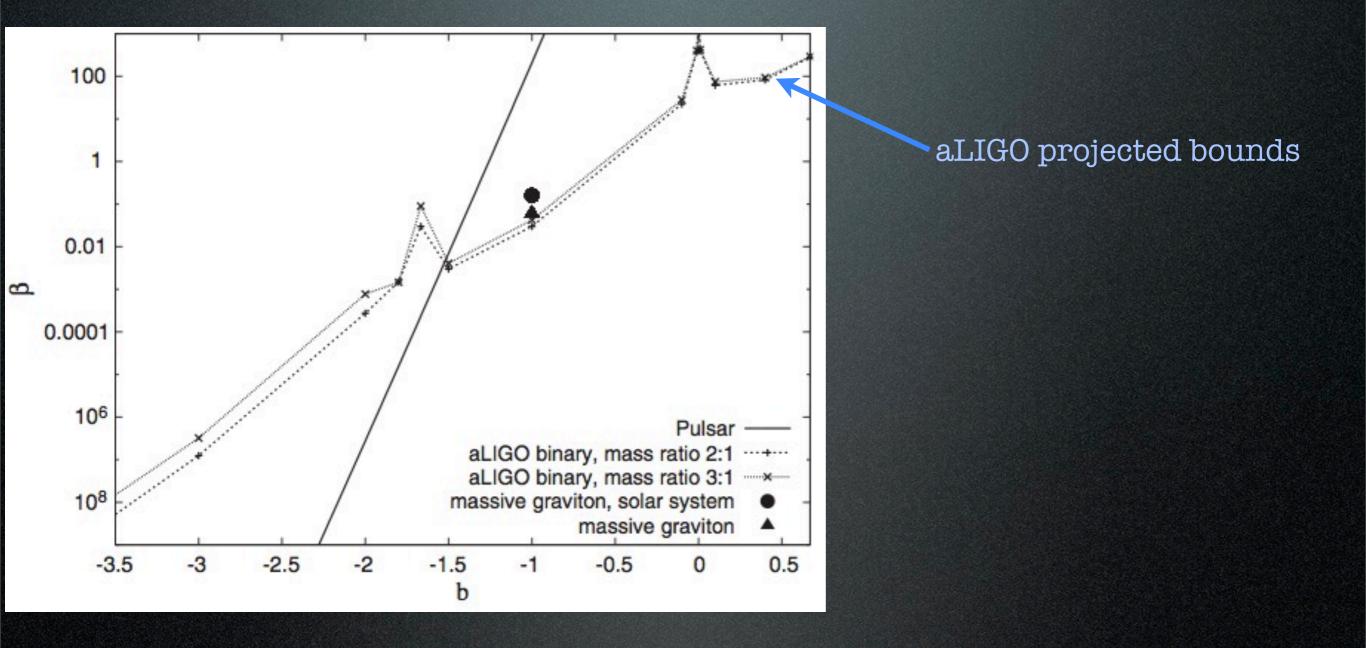
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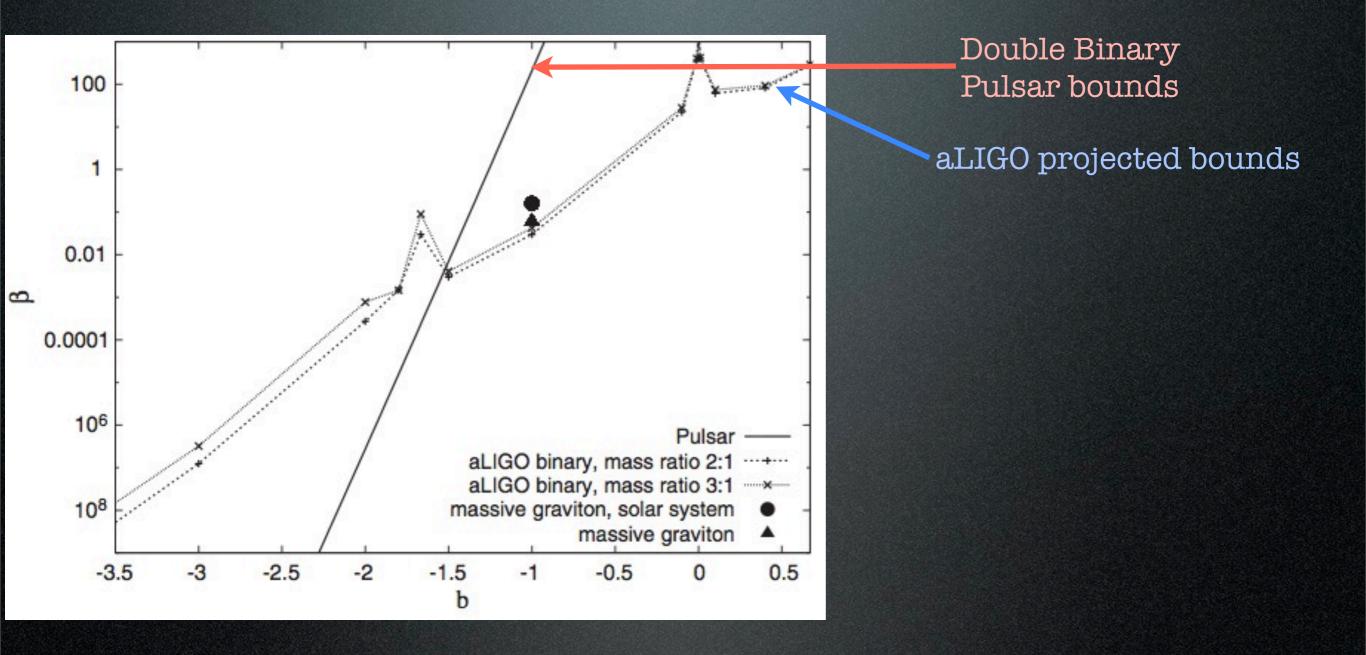
>Confusion III: Mismodeling -> Only a problem for sys with large M



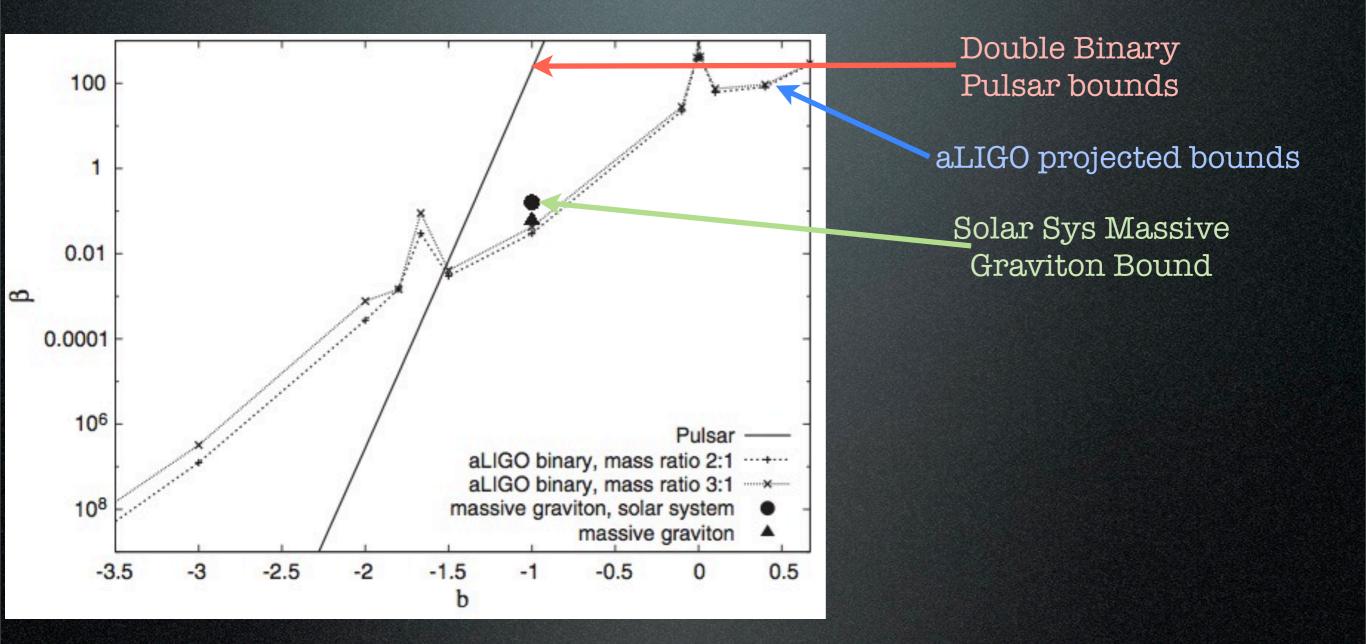
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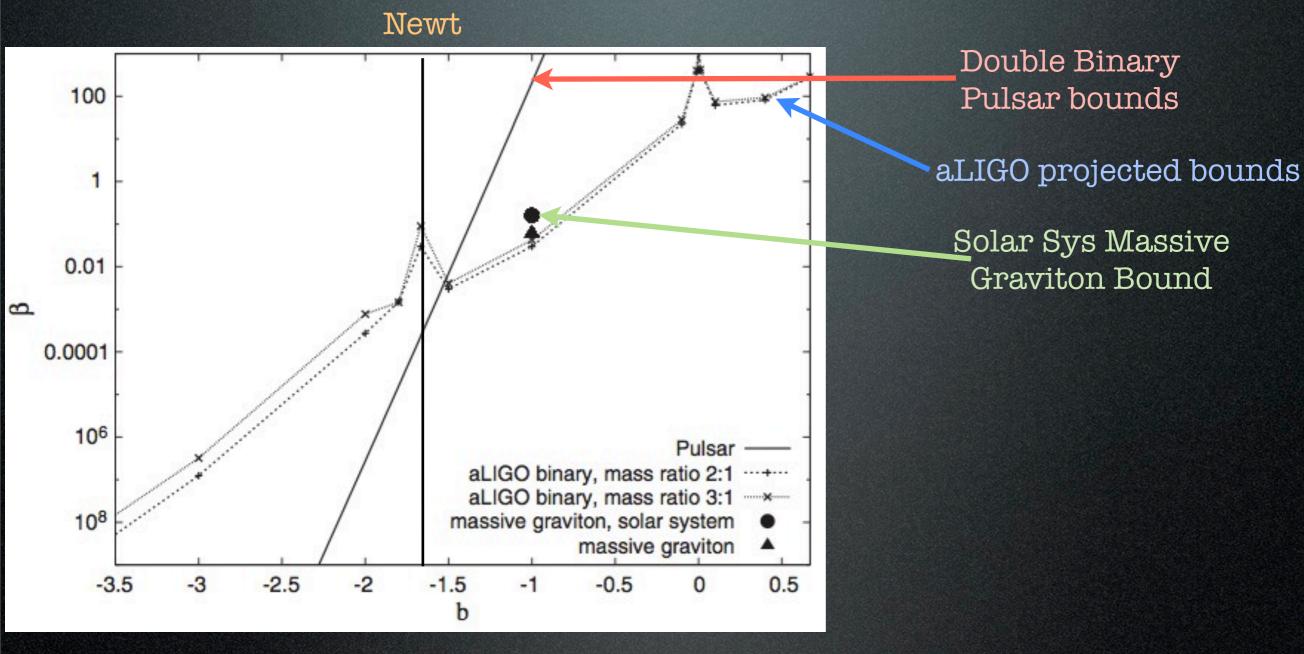


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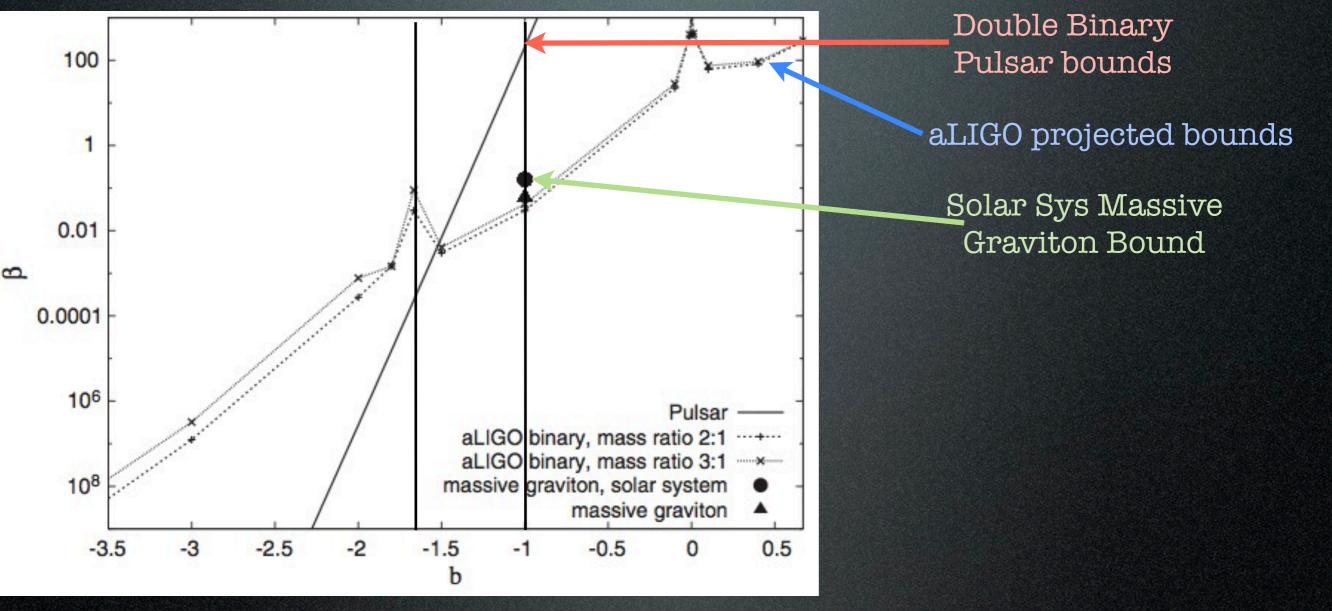
GR Signal/ppE Templates, 3-sigma constraints, SNR = 20



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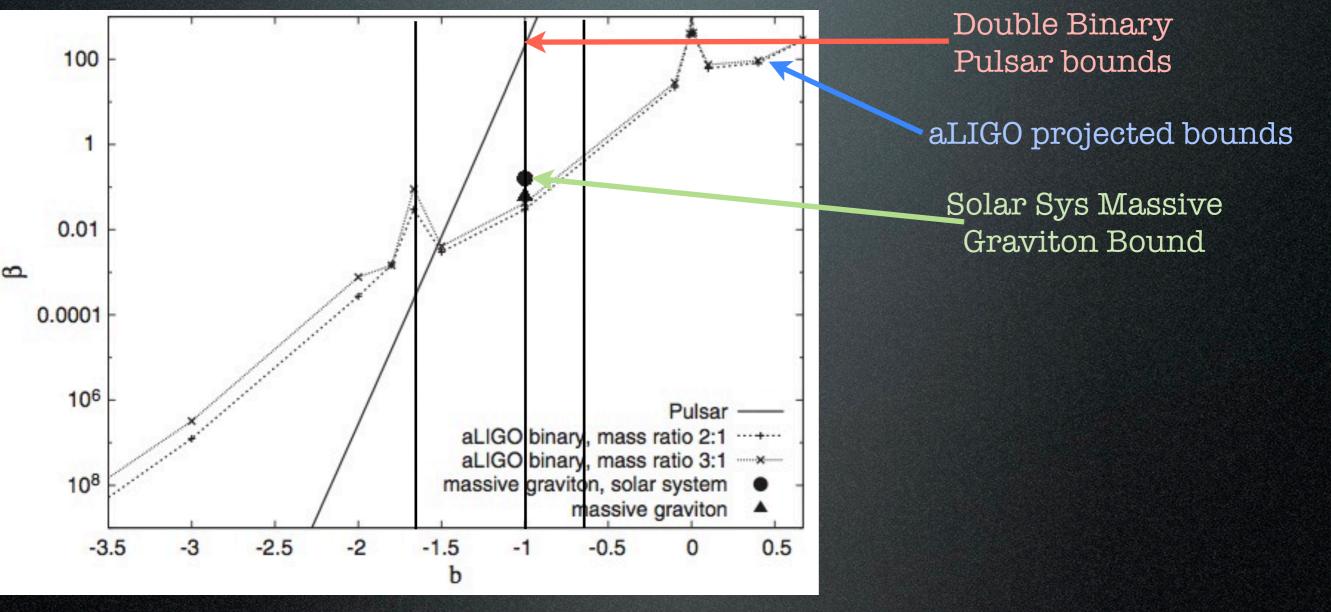
Newt 1PN



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GR Signal/ppE Templates, 3-sigma constraints, SNR = 20

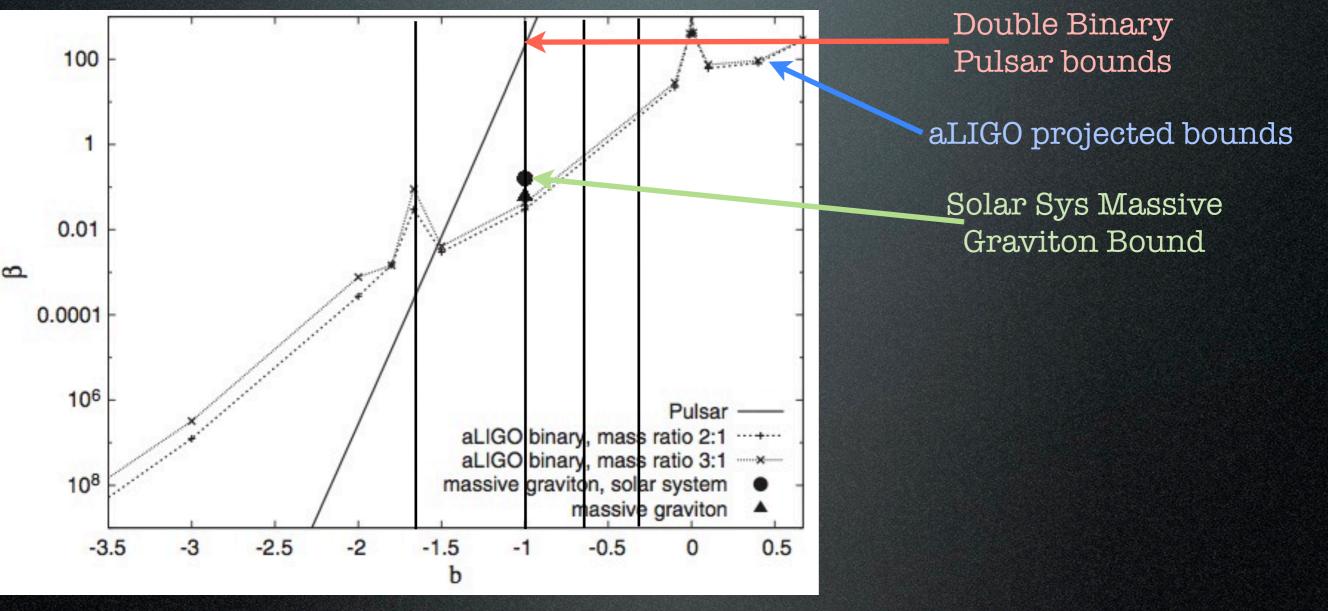
Newt 1PN 1.5



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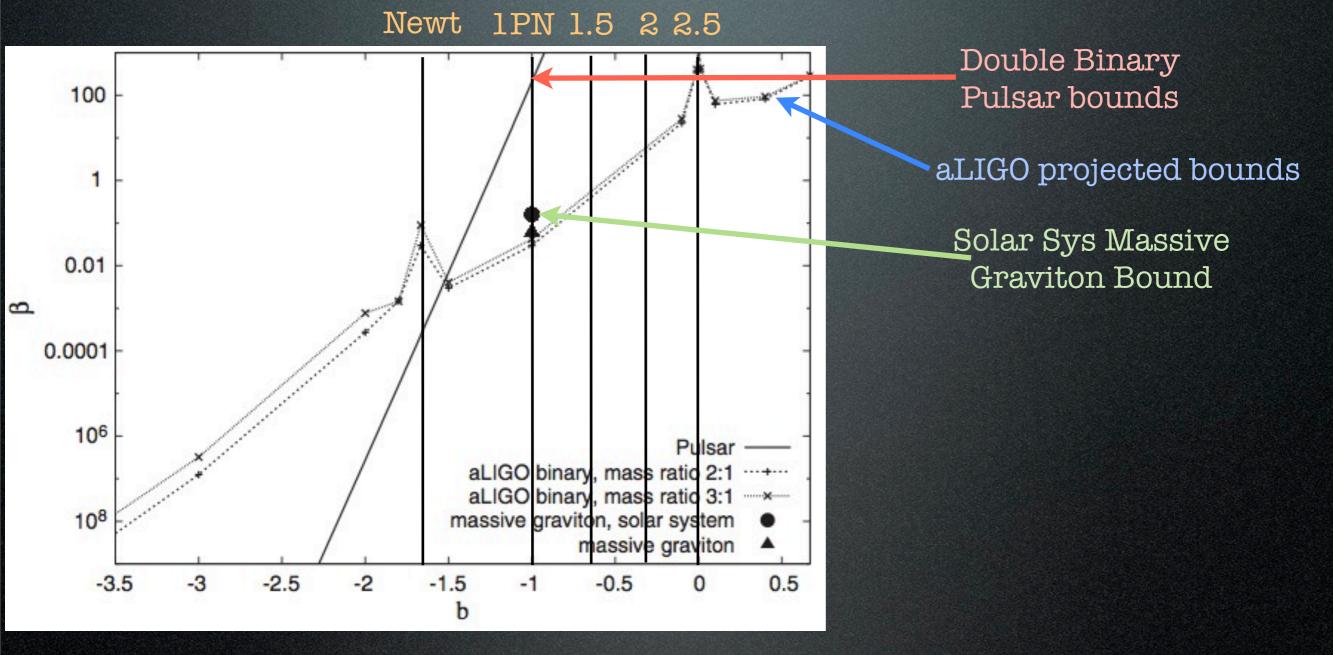
GR Signal/ppE Templates, 3-sigma constraints, SNR = 20

Newt 1PN 1.5 2



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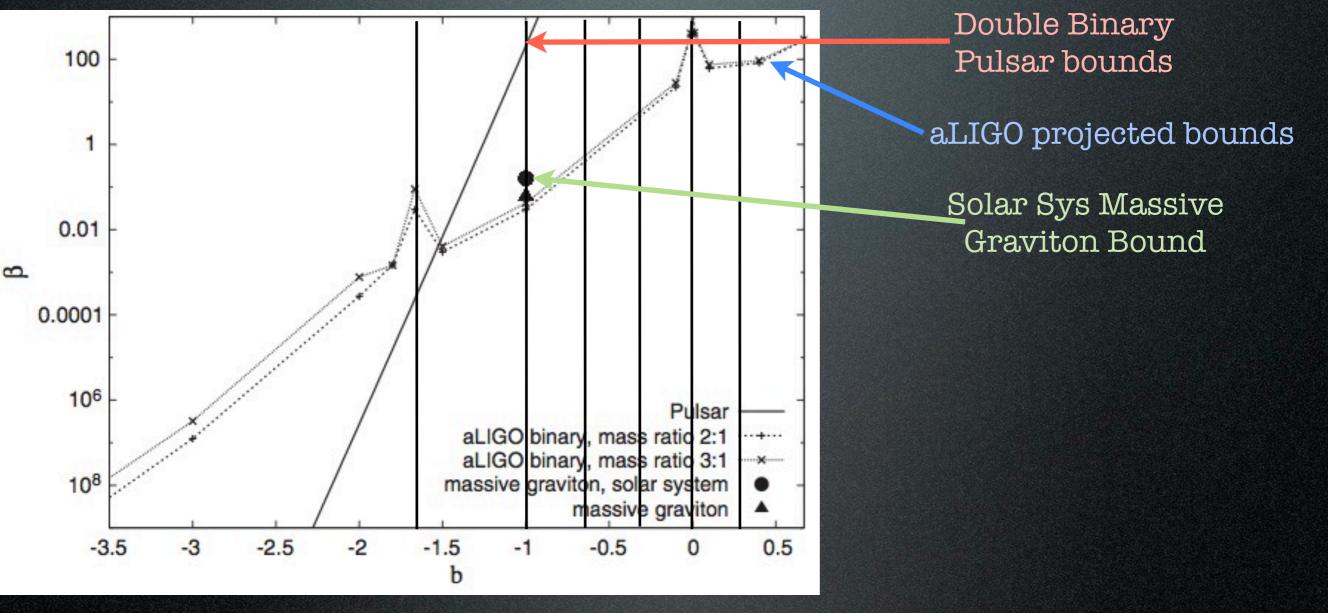
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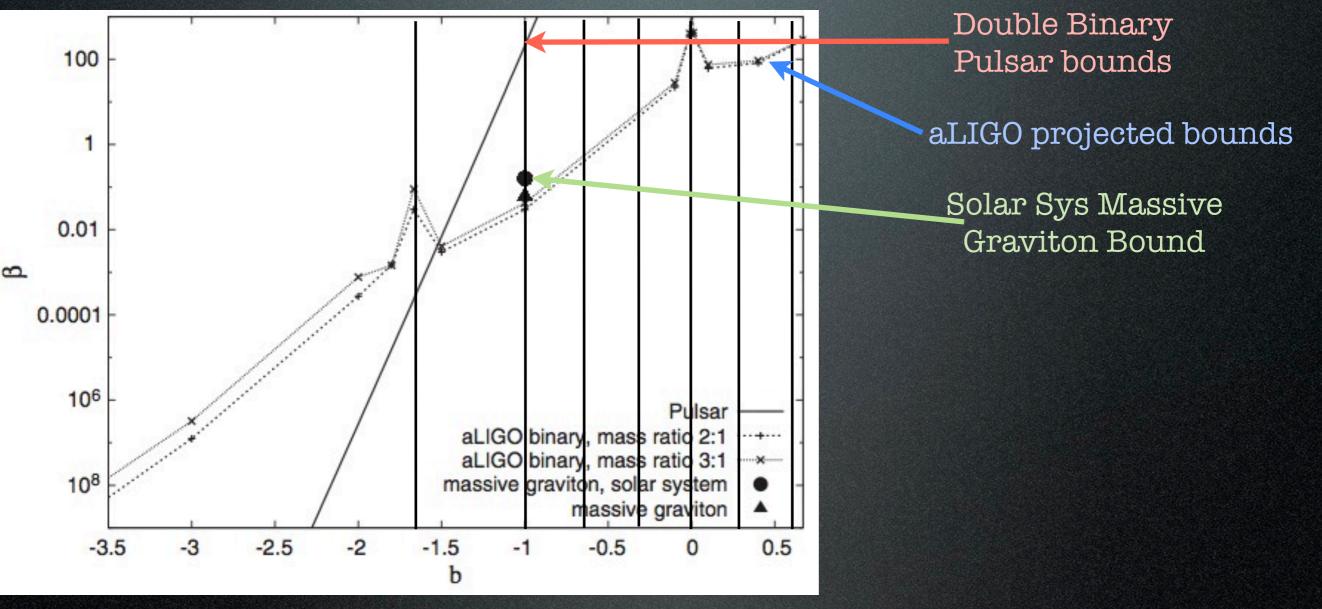
<u>Newt 1PN 1.5</u> 2 2.5 3



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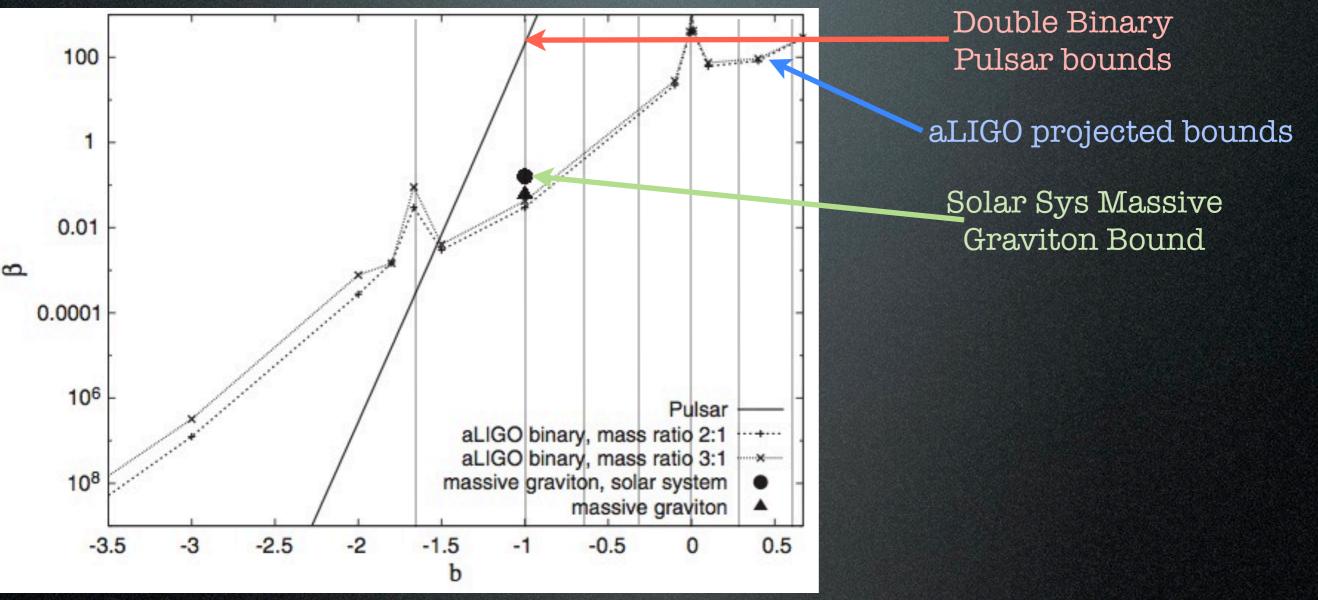
Newt 1PN 1.5 2 2.5 3 3.5



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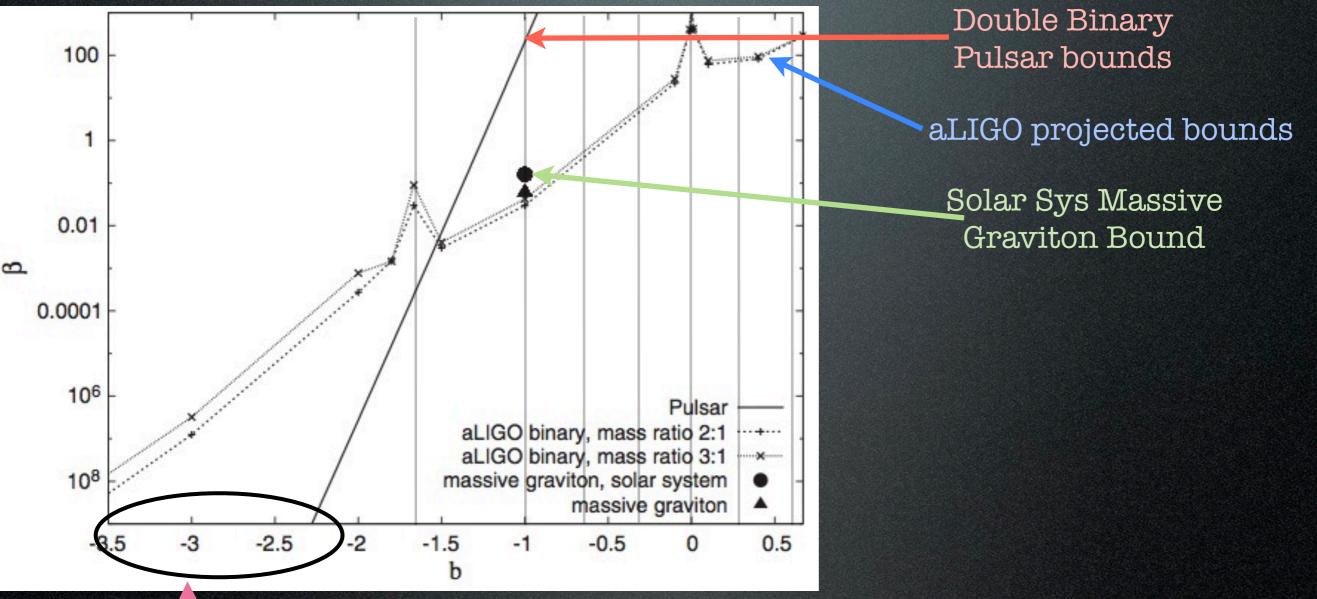
Newt 1PN 1.5 2 2.5 3 3.5



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Newt 1PN 1.5 2 2.5 3 3.5

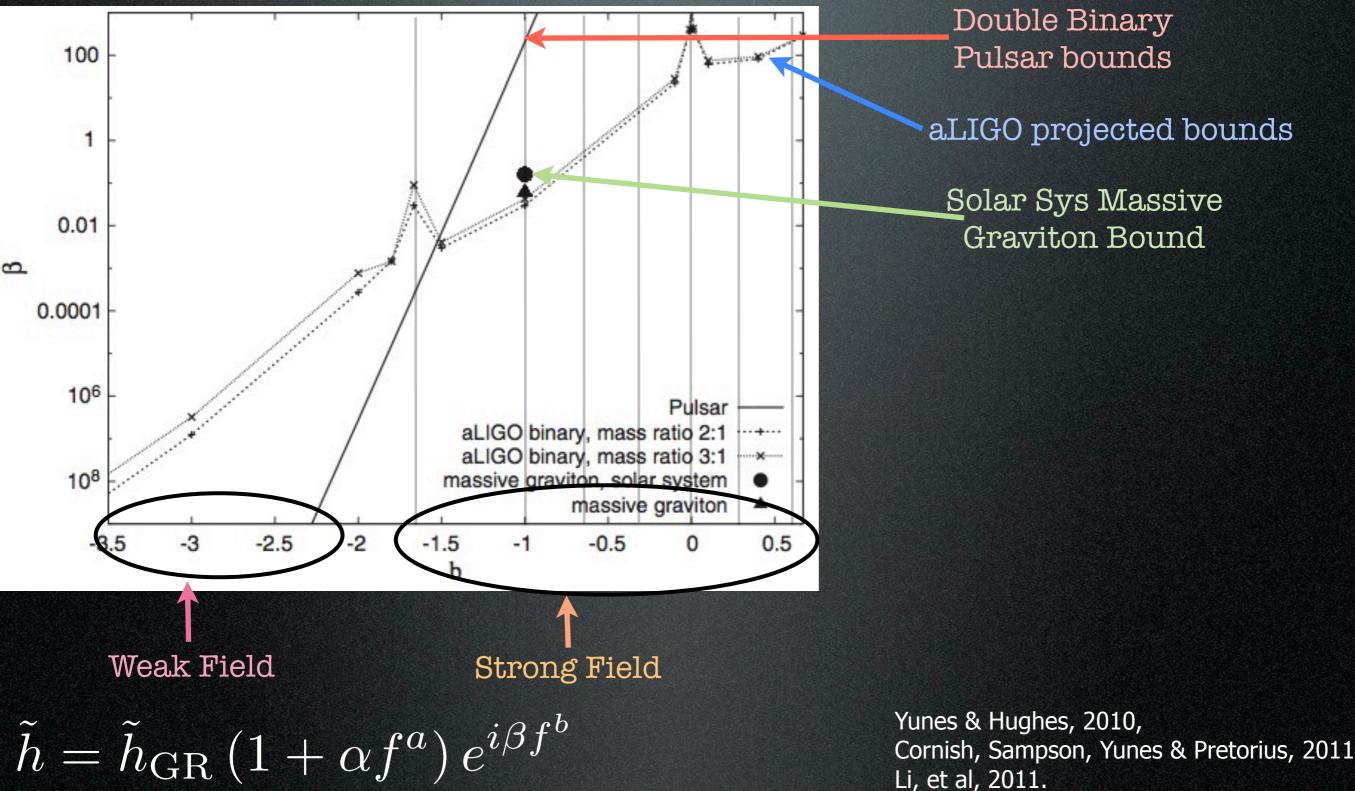


Weak Field

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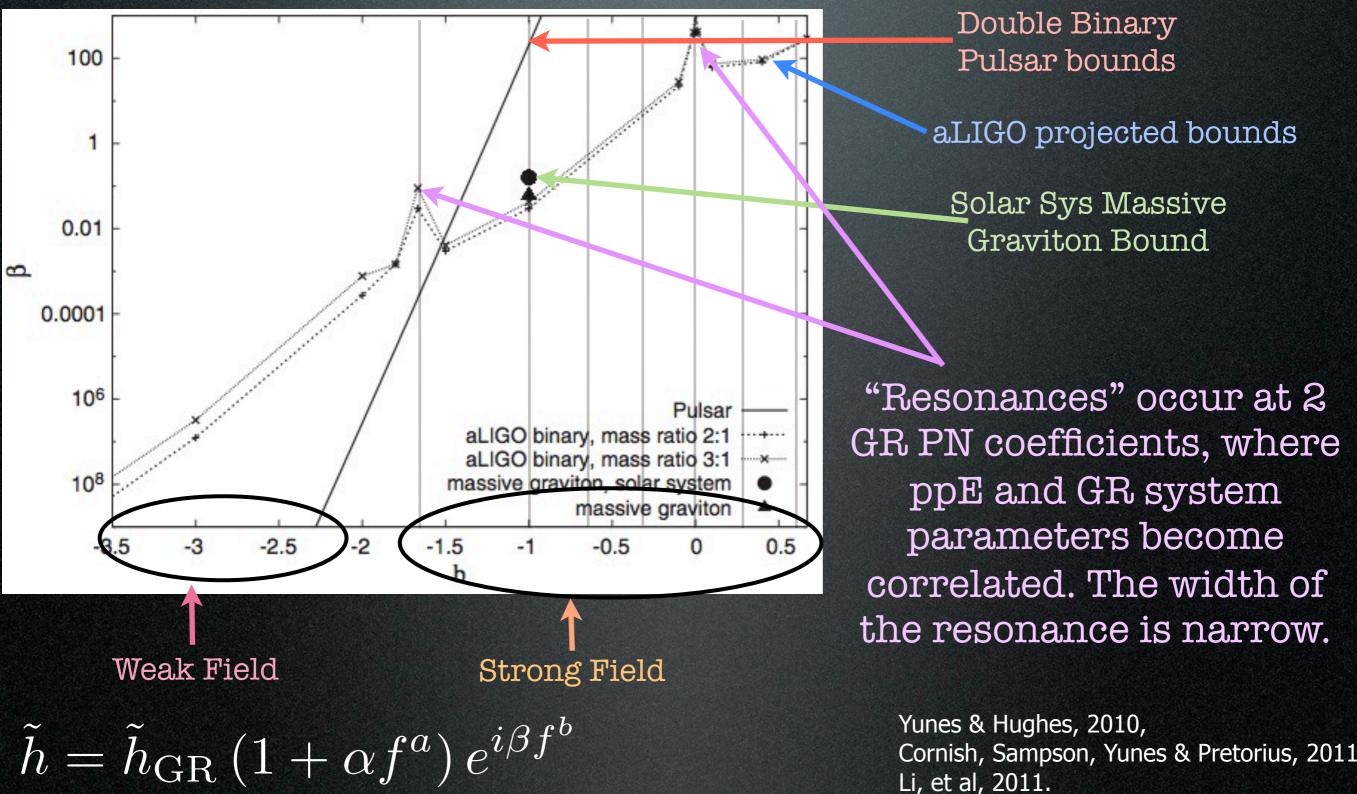
GR Signal/ppE Templates, 3-sigma constraints, SNR = 20

Newt 1PN 1.5 2 2.5 3 3.5



GR Signal/ppE Templates, 3-sigma constraints, SNR = 20

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Can we extend the ppE framework to constrain the existence of additional non-GR polarizations?

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If we observe a non-GR signal with all its PN corrections or with a nonanalytic deformation, like a Heavisde function, can a simple leadingorder ppE search signal a departure from GR? Sampson, Cornish, & Yunes, 2012.

Learning How to Breath before How to Crawl Can we extend the ppE framework to constrain the existence of additional non-GR polarizations? V Yes Arun 2012, Chatziioannou, Yunes & Cornish, 2012.

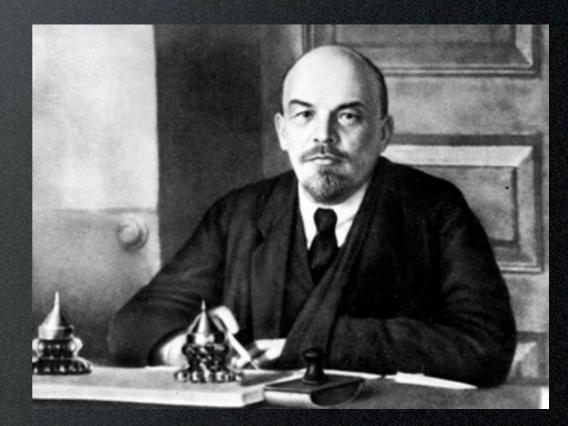
Given a non-GR ppE detection, can we identify what type of GR correction such a detection corresponds to?

Yunes, et al., 2010, 2011, 2012

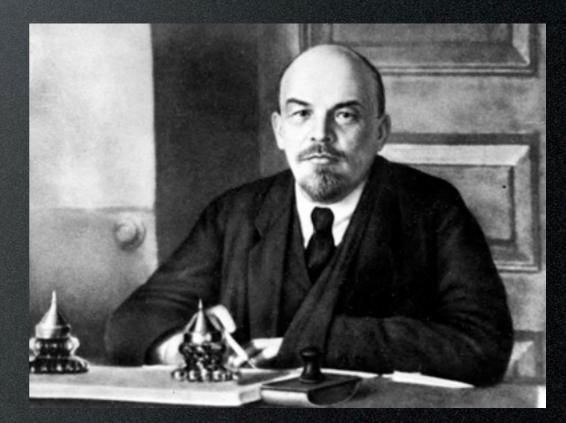
Given multiple detectors, how do we leverge the ppE Scheme? Sampson, Cornish, & Yunes, 2012.

If we observe a non-GR signal with all its PN corrections or with a nonanalytic deformation, like a Heavisde function, can a simple leadingorder ppE search signal a departure from GR? Sampson, Cornish, & Yunes, 2012.

> How do Systematics Affect the ppE Implementation? We'll see... Yagi, Yunes & Cornish, 2012.

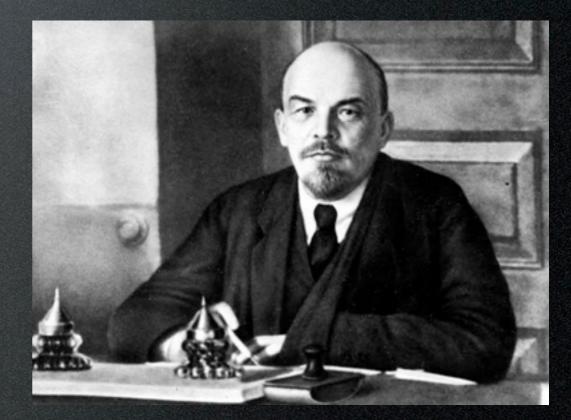


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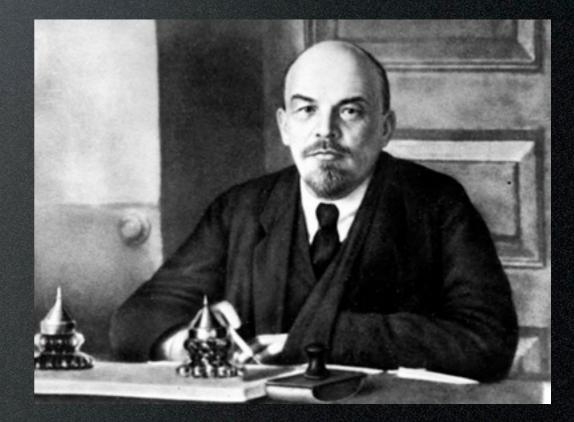
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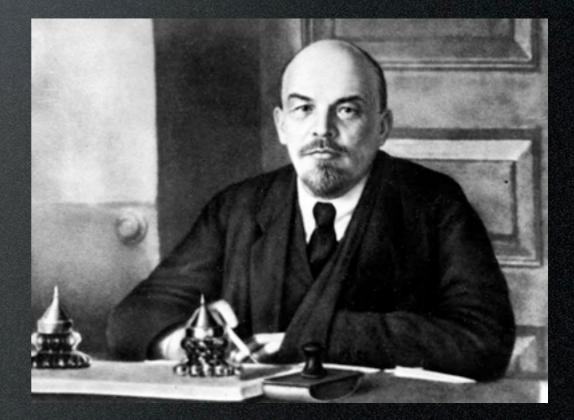


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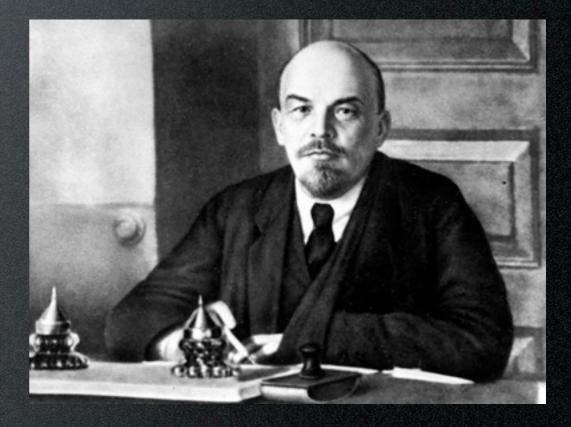
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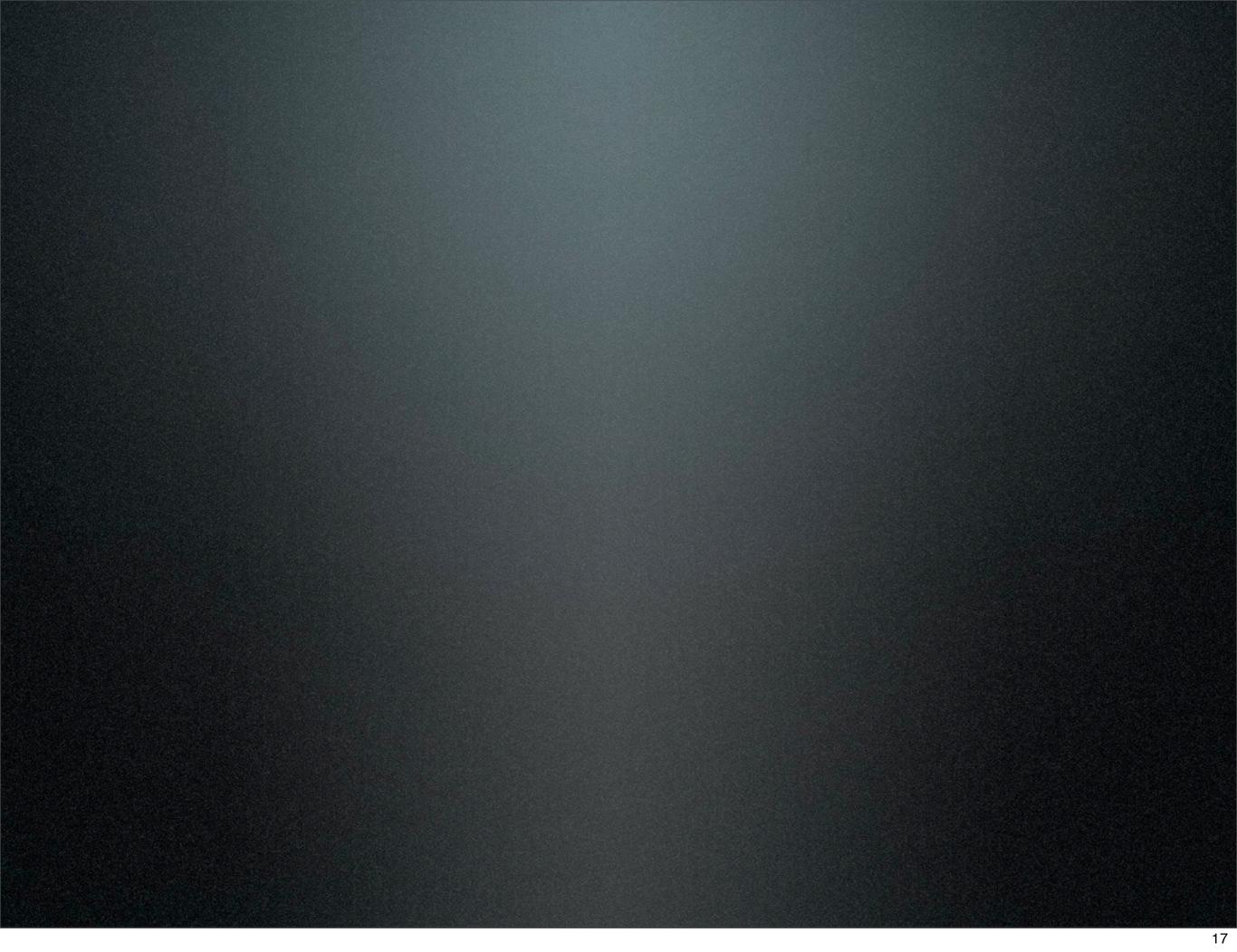
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And all of this will allow us to heavily constrain modified theories to unparalleled levels.

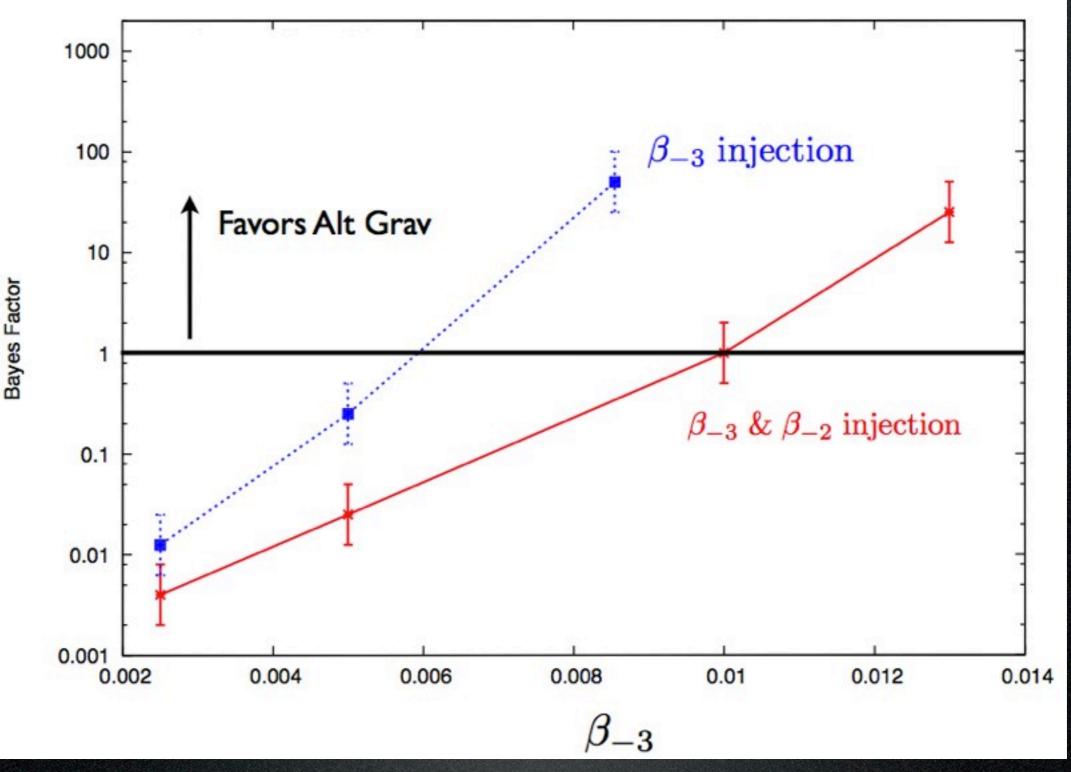




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Bayes Factors

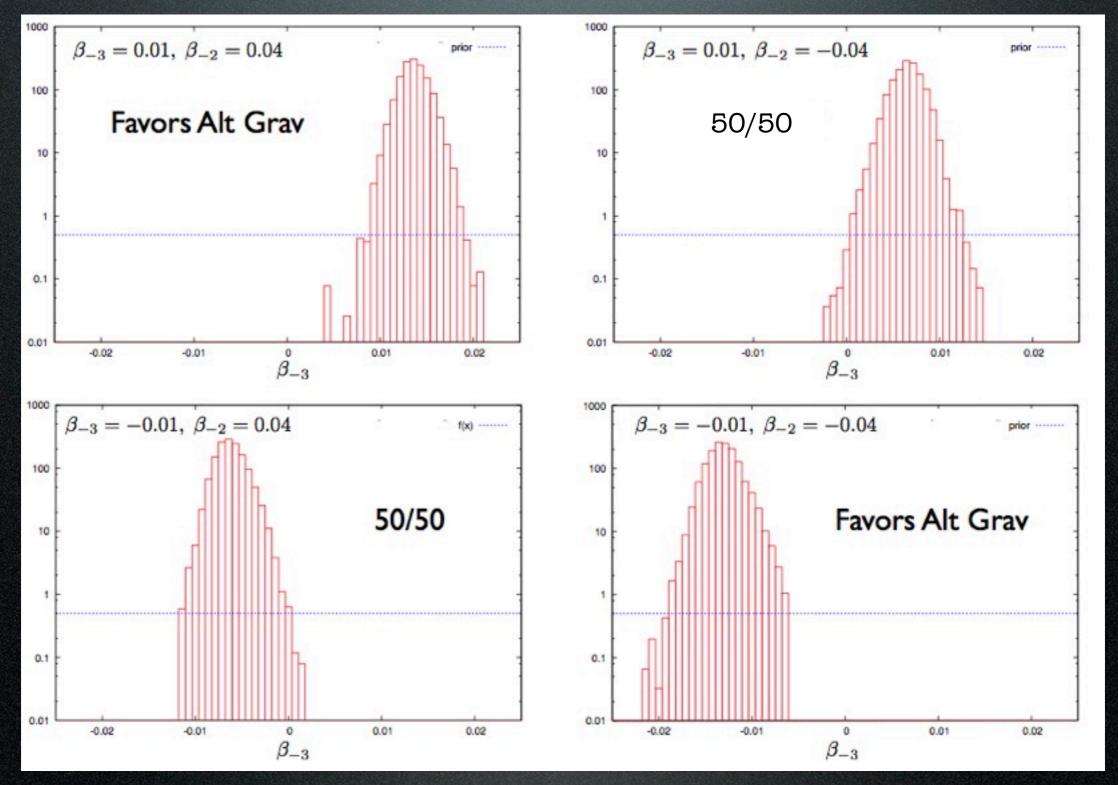
Single ppE template search β_{-3}



Sampson, Cornish & Yunes, 2012

High-Order PN Effects

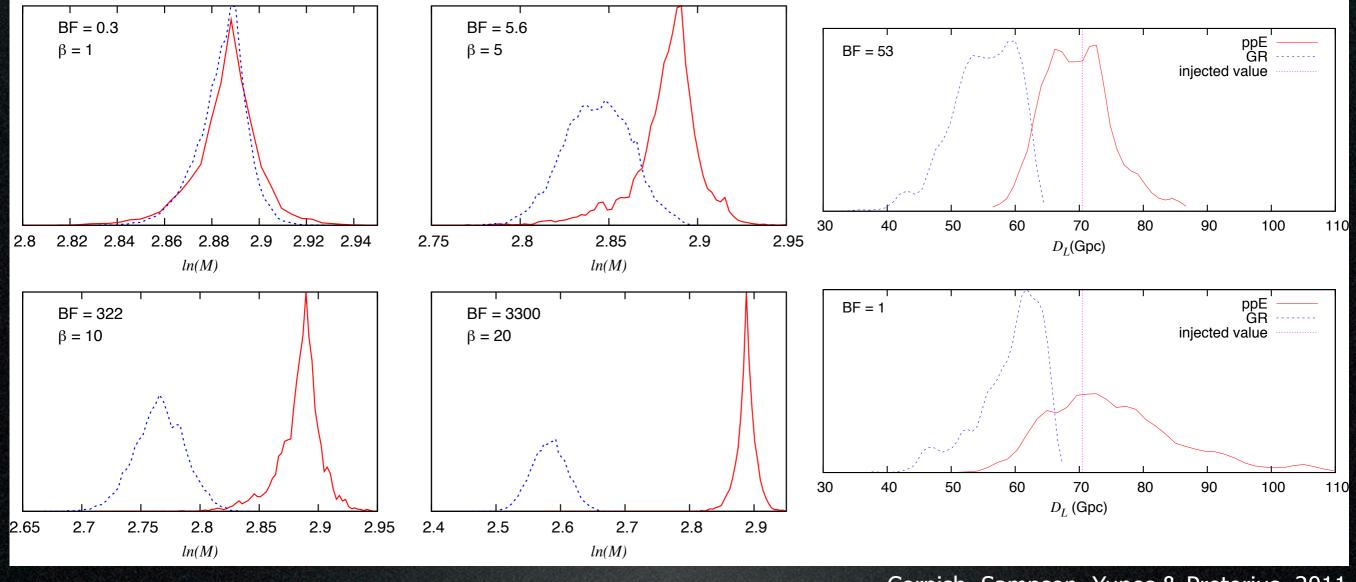
Alt Grav NS-NS injection with $\beta_{-3} \neq 0 \neq \beta_{-2}$ single ppE template search β_{-3}



Sampson, Cornish & Yunes, 2012

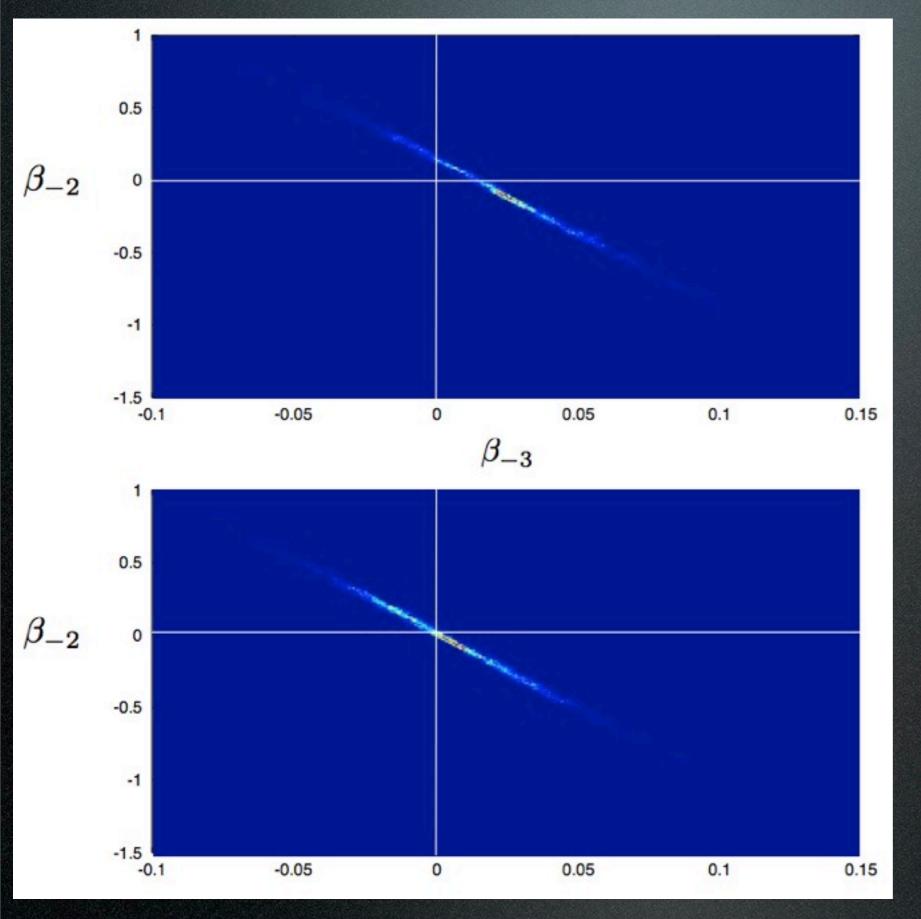
Fundamental Bias and Deviations Non-GR Signal/GR Templates, SNR = 20

Non GR injection, extracted with GR templates (blue) and ppE templates (red). GR template extraction is "wrong" by much more than the systematic (statistical) error. "Fundamental Bias"



Cornish, Sampson, Yunes & Pretorius, 2011

2-Parameter ppE Effectiveness

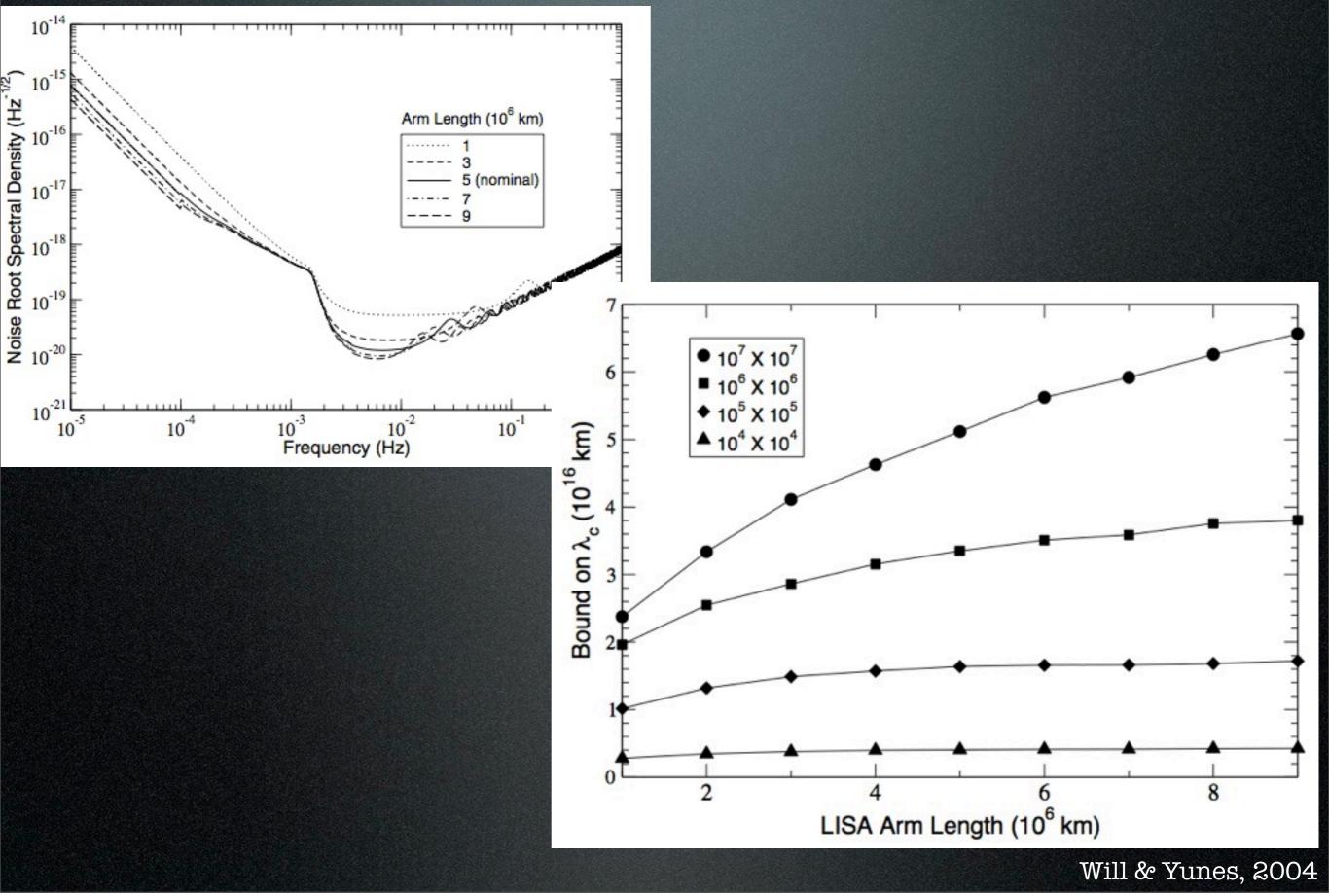


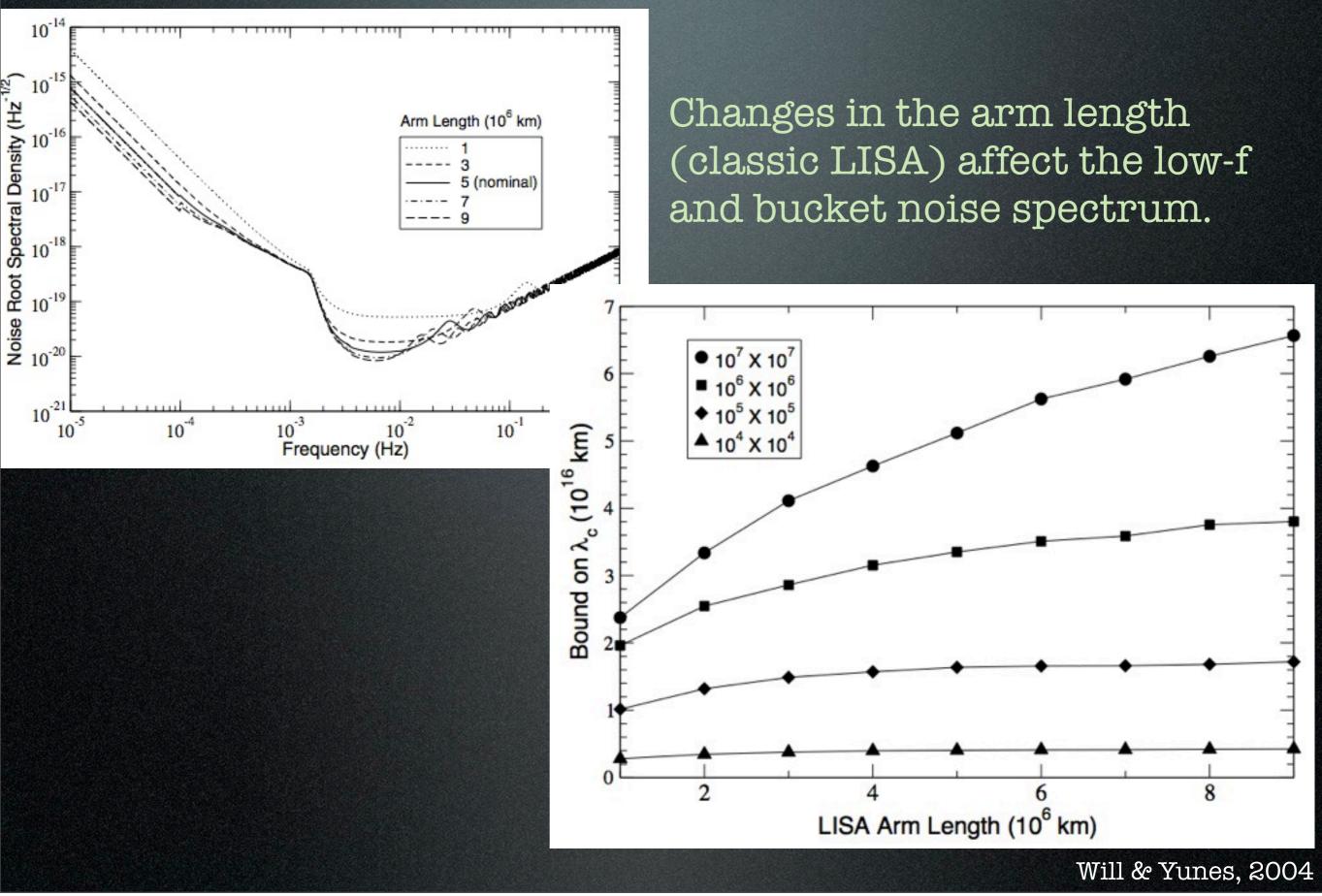
$$\beta_{-3} = 0.025, \beta_{-2} = -0.1$$

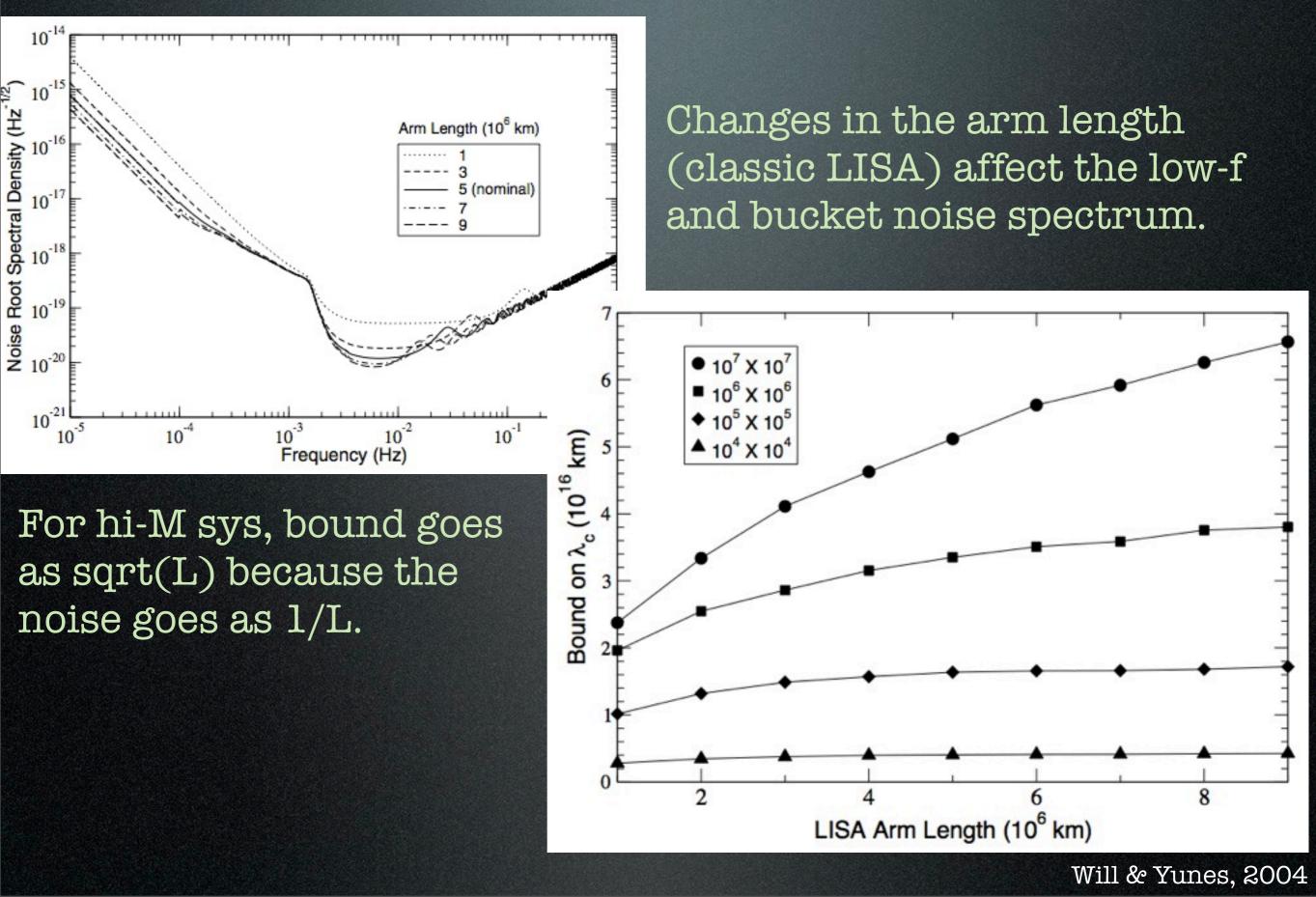
Detectable GR departure

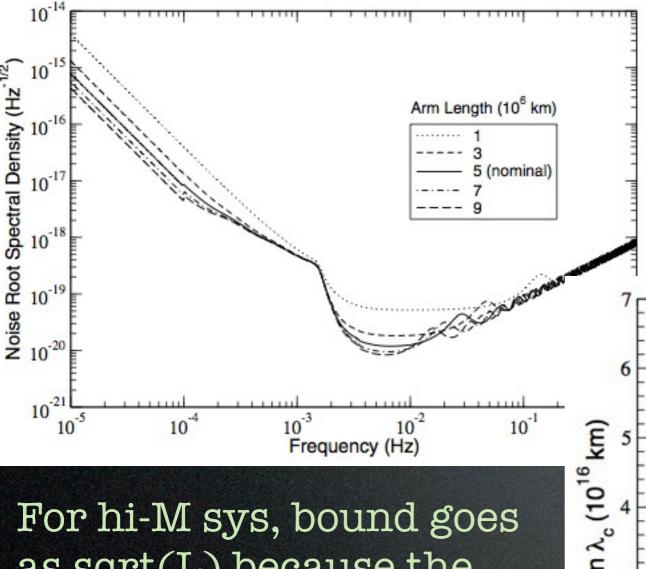
 $eta_{-3}=0.005, eta_{-2}=-0.02$ Consistent with GR

Sampson, Cornish & Yunes, 2012



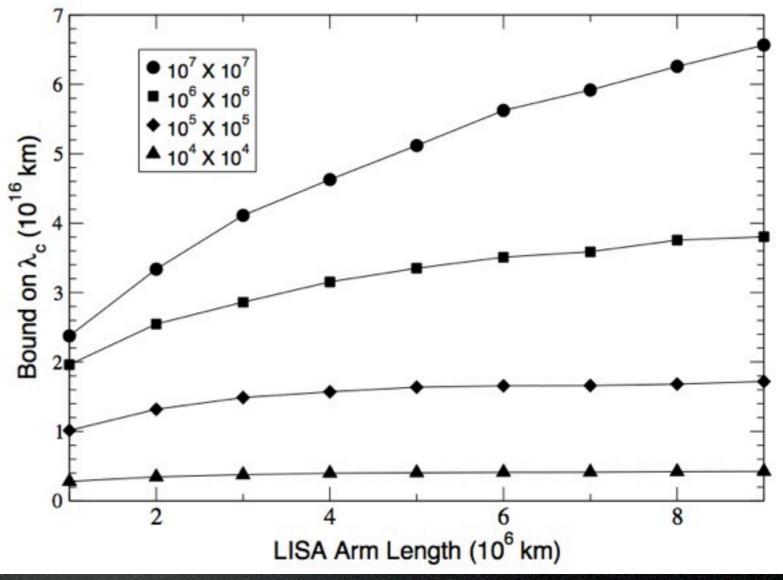






as sqrt(L) because the noise goes as 1/L.

For lo-M sys, low-f noise has little effect because signal dominated by WD confusion noise. Changes in the arm length (classic LISA) affect the low-f and bucket noise spectrum.



Will & Yunes, 2004