

# Implementing machine learned parameterizations in climate models

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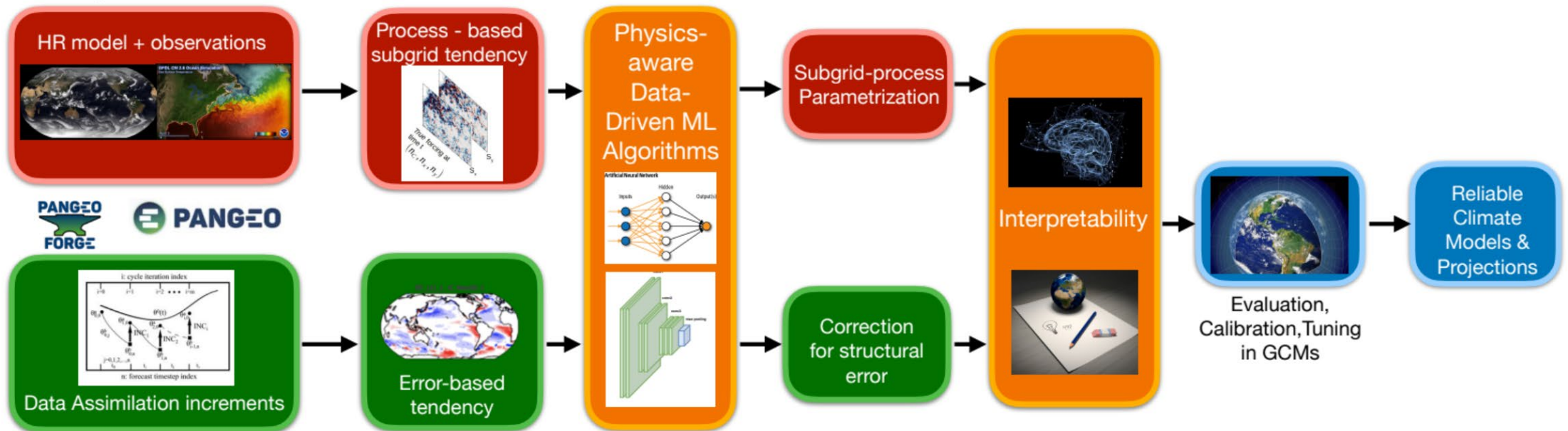


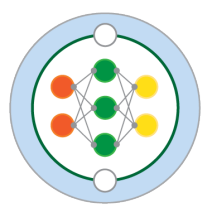


# M<sup>2</sup>LInES: Multiscale Machine Learning In Coupled Earth System Modeling

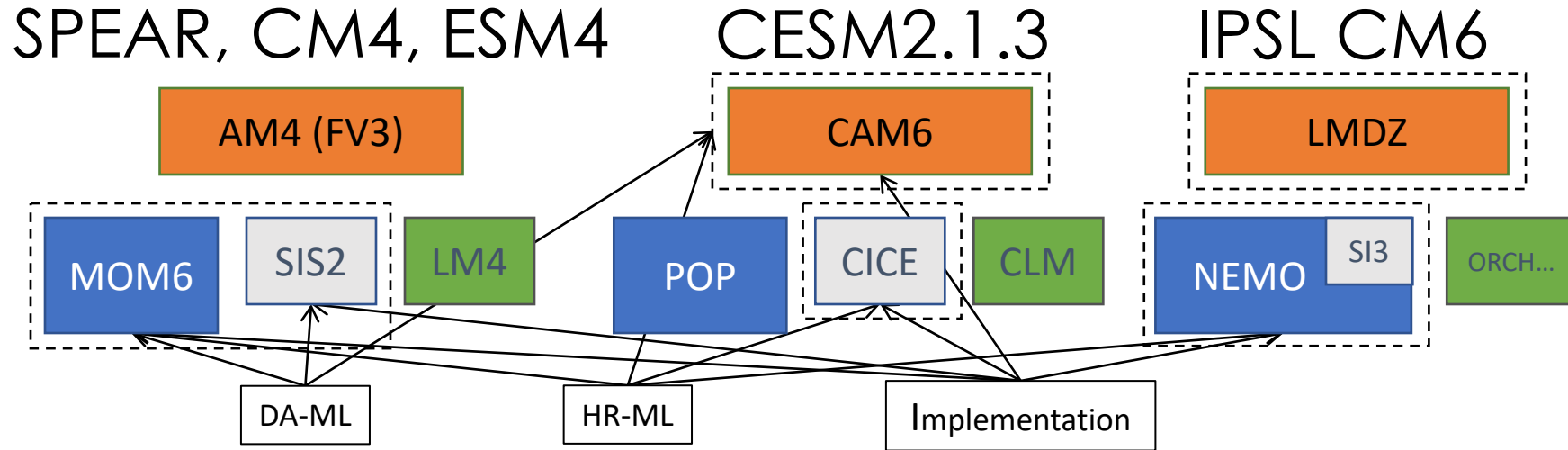
**Goal:** Improve the skill in modelled surface ocean, ice, atmospheric fields on timescales of hours to centuries in global climate models

- **Development of new data-driven, physics-aware parameterizations** of subgrid ocean, ice & atmosphere processes
- **Reduction of structural model biases** (numerics, missing physics & poor subgrid parameterizations) **in existing climate models** at NCAR, GFDL & IPSL





# M<sup>2</sup>LInES: The climate models



- 11 institutions, US + Europe, climate modeling centers
- These are AR6 climate models, with well established component models
- Learning from data-assimilation (DA-ML)
- Learning from High-resolution simulations (HR-ML)

- Implementation across component models
- The diversity of components models, resolutions, and climates, requires ML parameterizations to be:
  - Transferable
  - Scale-aware
  - Generalizable



# M<sup>2</sup>LinES Team



Laure Zanna



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Julien Le Sommer



Arthur Guillaumin



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Lorenzo Zampieri



Ziwei Li



Tarun Verma



Aakash Sane



Cem Gultekin



Dhruv Balwada



Alex Connolly



Cheng Zhang



Pavel Perezhgin



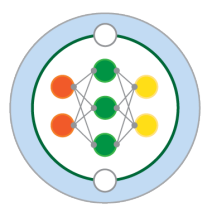
Anastasia Gorbunova



Will Chapman

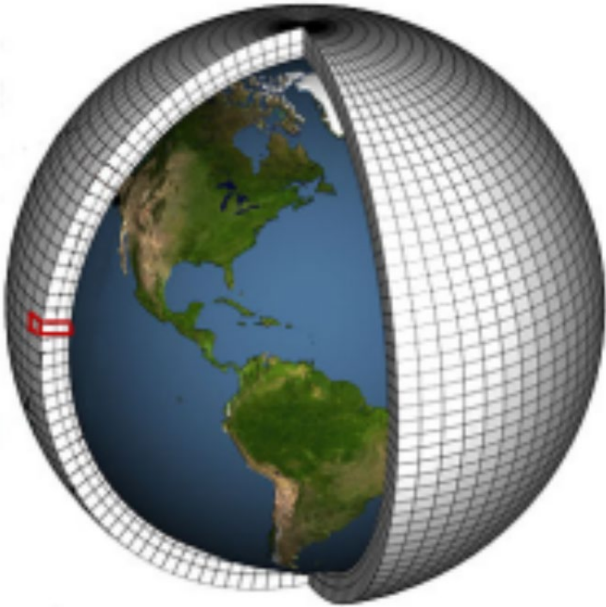


Will Gregory



# Challenge: to use ML in Climate Models

## Climate models

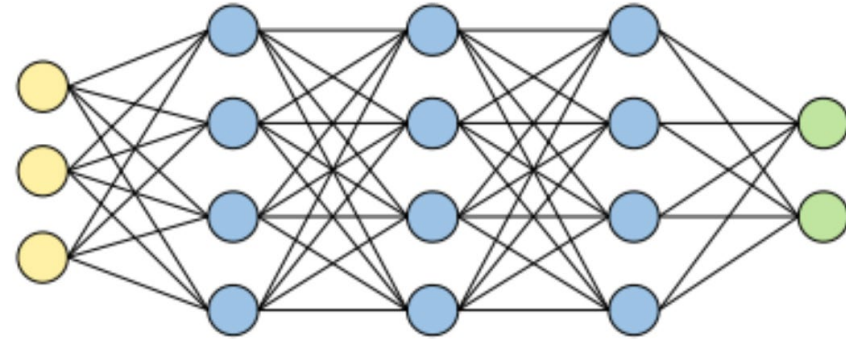


NOAA's Gaea (ORNL)



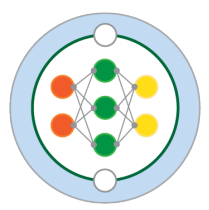
- 1,000,000+ lines of Fortran/c
  - Decades of experience
  - Almost exclusively use CPUs

## Machine learned models



- 50+ lines of python/Julia
  - Leveraging widely adopted packages under the hood
  - Utilizing GPUs

**There is an apparent (computer) language barrier**



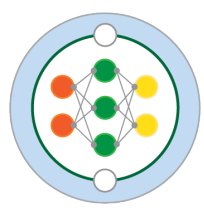
# Using a trained ML model from climate code

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Options to tackle inter-language barrier:

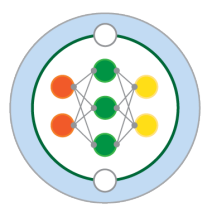
- Code final ML model in Fortran
  - e.g. Fortran-Keras bridge (Ott, Pritchard, et al., 2020)
- Build/use a Fortran-python interface using C-API
  - e.g. python-embedding (Python manual), `call_py_fort` (Noah Brenowitz)
- Use turn-key package (CPU-GPU)
  - HPE's SmartSim (Partee et al., 2021, subm.)

**There are solutions – but there are more subtle challenges with code**



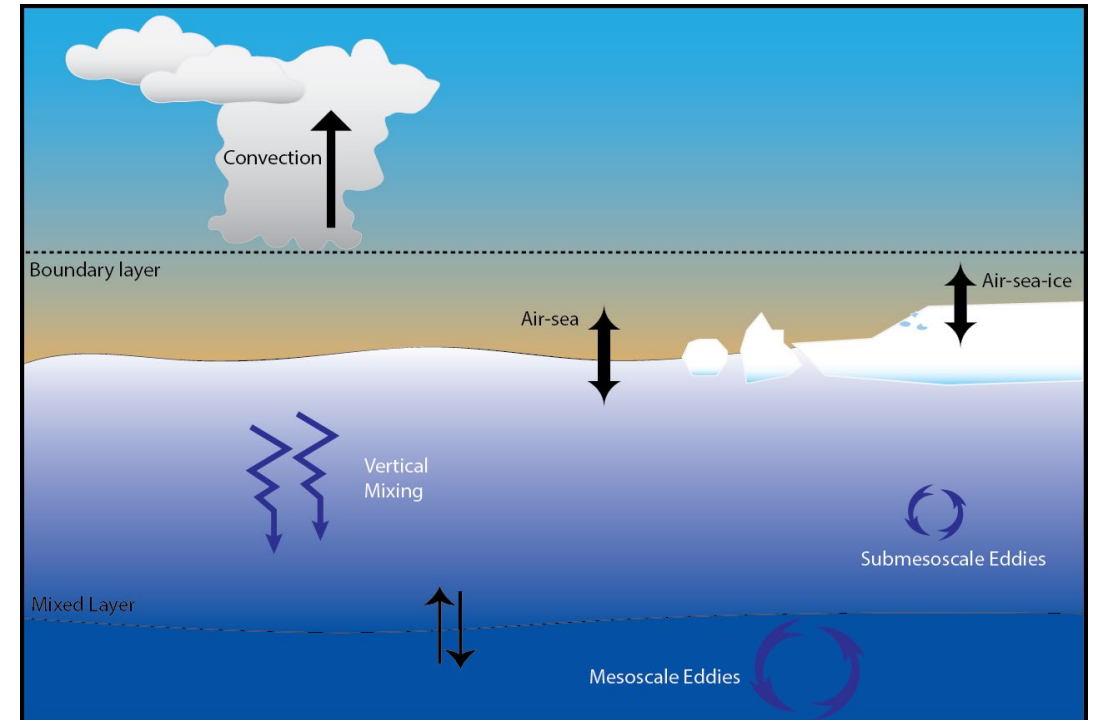
# Other challenges with climate codes

- Climate model data structures unique to each model/component/process
  - Definitions, approximations, and units of variables vary between models, e.g.
    - Ocean: practical salinity vs absolute salinity
    - Atmosphere: CLUBB uses (anelastic) liquid water potential, rather than enthalpy, CAM expects enthalpy+KE conservation
    - Vertical coordinates differ i) between models, ii) between analysis and models, iii) between columns, iv) between dynamics and physics s/r
  - Parallelism: decomposed data might not support wide stencils (for CNN)
  - Data availability: parameterizations might only have access to single column data but ML model need multiple columns

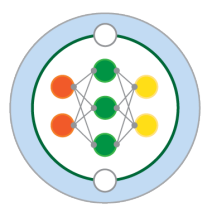


# Interactions between processes

- Information interaction
  - Use of intermediate/secondary variables, e.g. sub-grid parameters (cloud fraction, mixing length scale, ...)
- Physical interaction
  - e.g. mesoscale+sub-mesoscale eddy re-stratification balancing mechanical/buoyant mixing of ocean boundary layer
- Compensating errors
  - ML models will improve representation of model physics ... but can make model look worse due to prior tuning

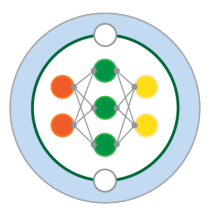






# Online stability

- Offline training not always stable when used in a forward model
- Depends on effective eigenvalues
  - Lyapunov exponents
- Calculating/modelling increments vs tendencies vs fluxes makes a difference
- Conservation properties, and generalization, should be beneficial
  - **Recent successes, e.g. Yuval et al. 2021**
- Can ML model tendencies,  $N^n$ , simply be added to model tendencies  $M^n$  ?
- GCMs each use different algorithms
  - e.g. (with  $a = \frac{3}{2} + \epsilon$ )
$$u^{n+1} = u^n + \Delta t(aM^n - (1 - a)M^{n-1})$$
- Damping modes
  - e.g. Euler forward
$$u^{n+1} = u^n + \Delta t(M^n + N(u^n))$$
- Oscillatory modes
  - Multi-level, multi-stage, e.g.
$$u^* = u^n + \frac{1}{2}\Delta t(M^n + N(u^n))$$
$$u^{n+1} = u^n + \Delta t(M^n + N(u^*))$$
- Fast modes
  - Implicit, e.g.
$$u^{n+1} = u^n + \Delta t(M^n + N(u^{n+1}))$$
- Implications for training?



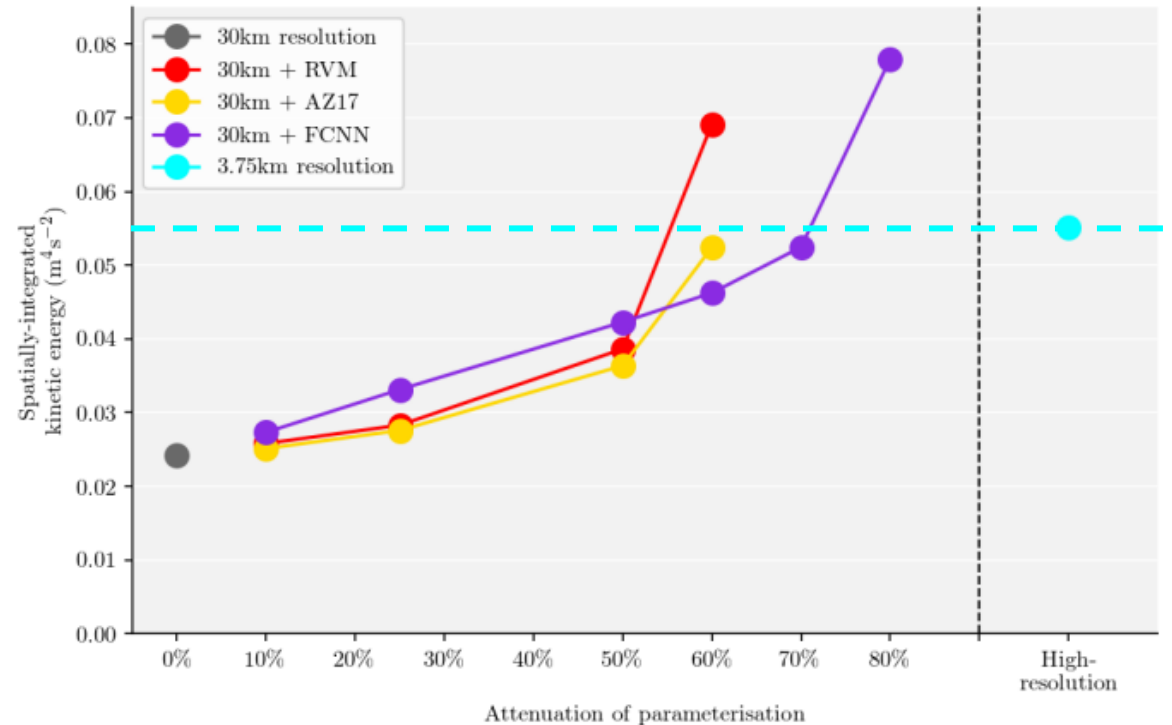
# Stability and efficacy

- Effect of online parameterization often needs scaling
  - Feedback between basic state and parameterization missing when training offline
  - Resolved gradients imperfect
- e.g. ZB20 parameterization energizes flow
  - FCNN needed the least attenuation, but none could be used at full effect
- Parameterizations are always tuned

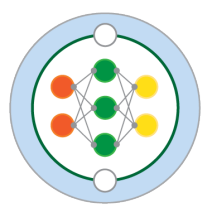
Coarse-resolution model with sub-grid forcing

$$\frac{\partial}{\partial t} \bar{u} + (\bar{u} \cdot \bar{\nabla}) \bar{u} = \bar{F} + \bar{D} + \bar{S}$$

Mean-kinetic energy of final 5 years of spin-up while varying parameterisation attenuation

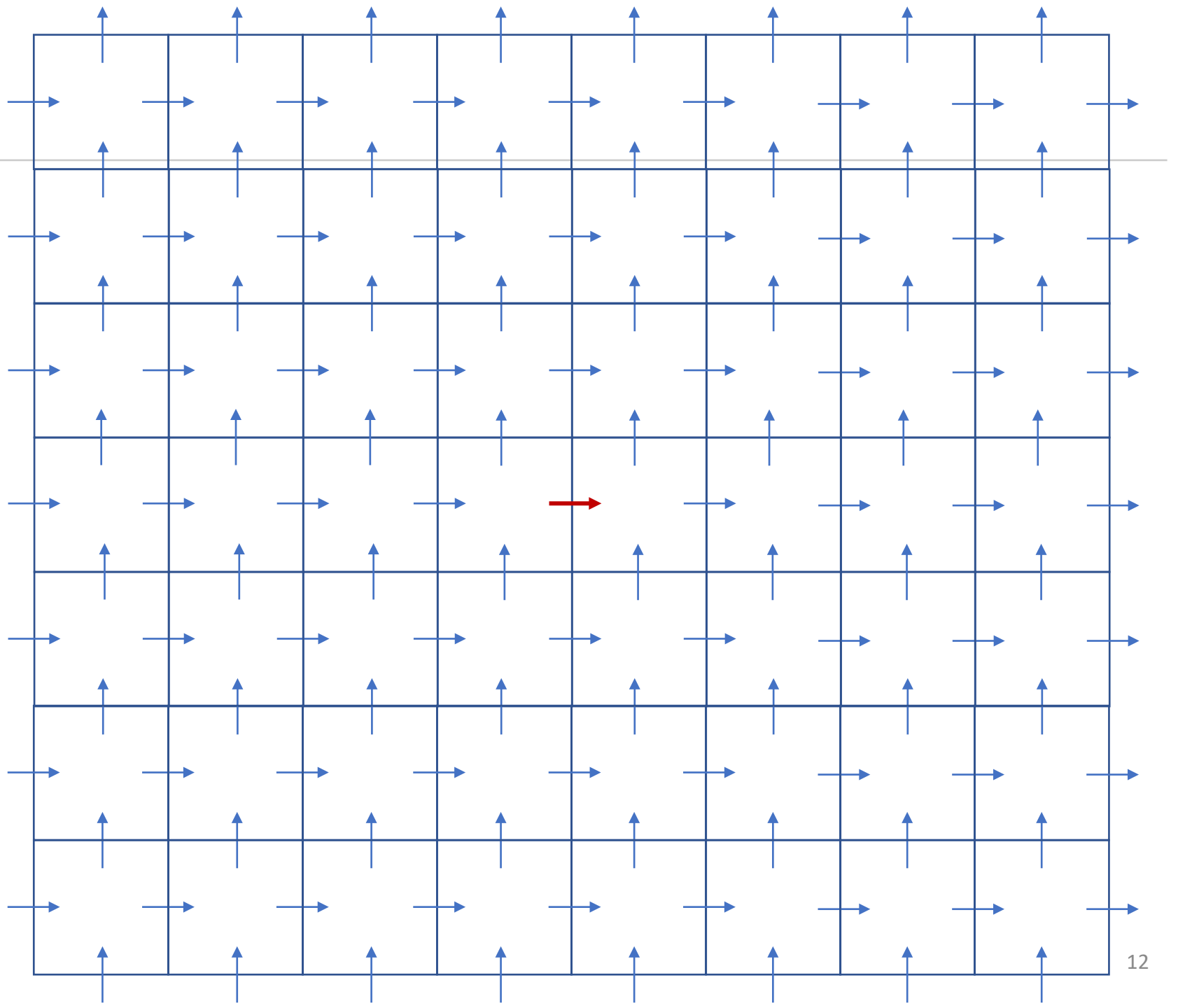


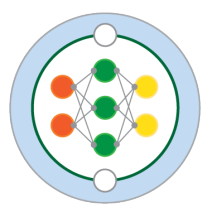
Zanna & Bolton, 2020  
(Fig. S9)



# Stencils

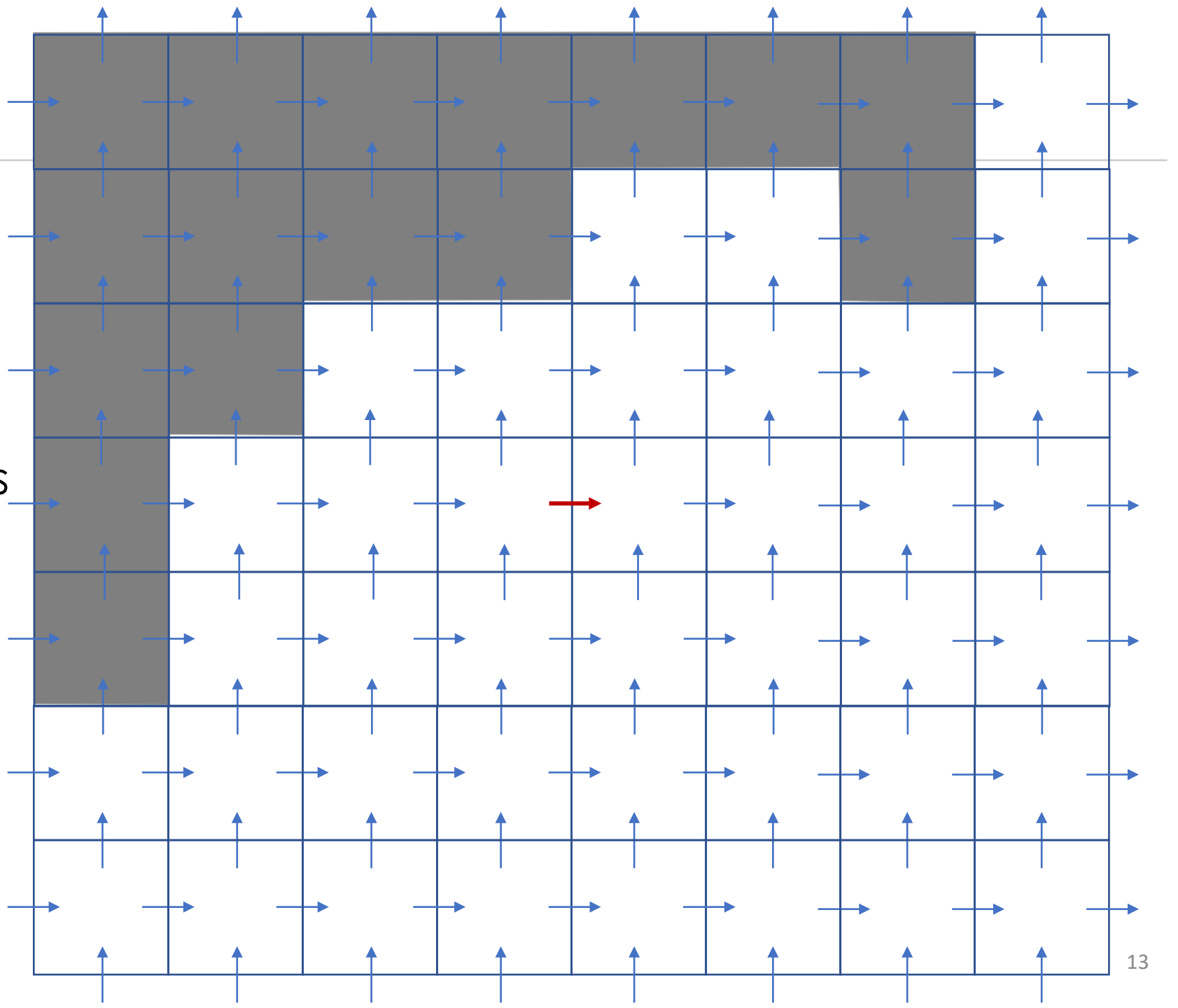
- ZB20 FCNN
  - 4 layers x 3x3
  - No padding
- For contrast, GZ21 CNN
  - 2 layers x 5x5
  - 5 layers x 3x3

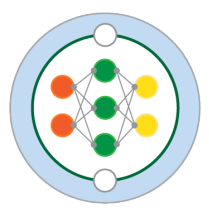




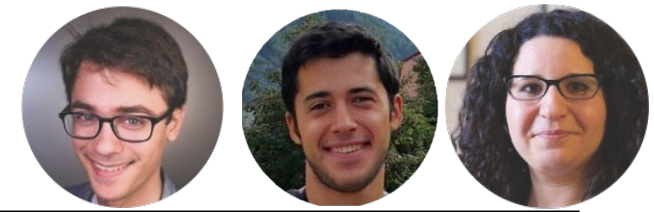
# Stencils

- Irregular coasts absent from training
- ZB20 FCNN
  - Disabled 4 points from boundary



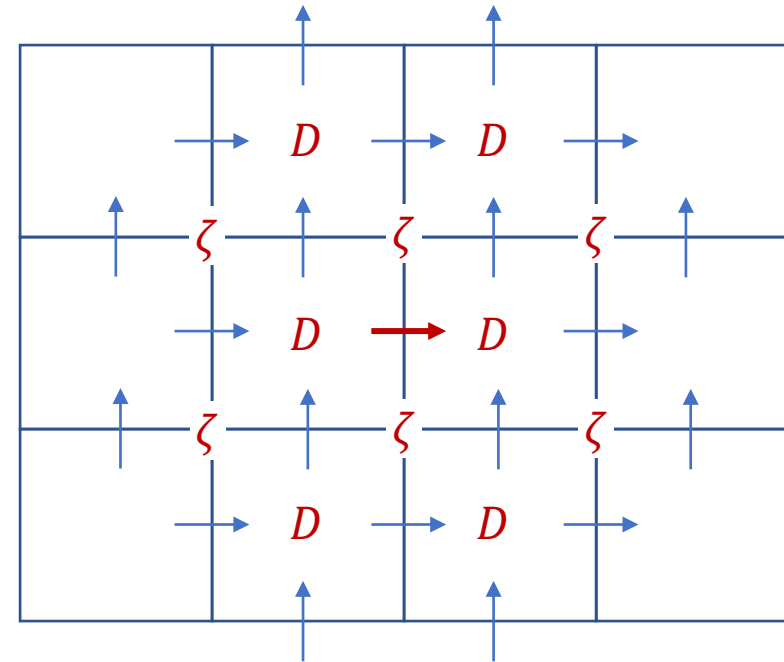


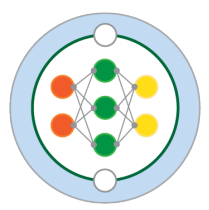
# Stencils



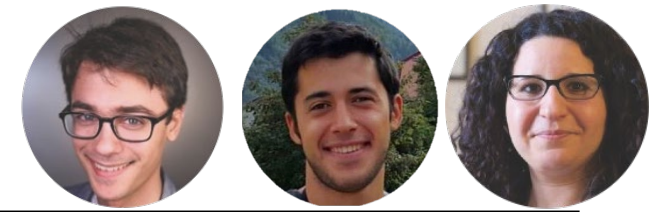
- Discovered equations in ZB20 (and AZ17) have small stencil (for 2<sup>nd</sup> order FV/FD)
- Expressions are using physical quantities likely already available in models
- ZB20 9-term does not extend stencil

$$\kappa \bar{\nabla} \cdot \begin{pmatrix} \zeta^2 - \zeta D & \zeta D \\ \zeta D & \zeta^2 + \zeta D \end{pmatrix}$$



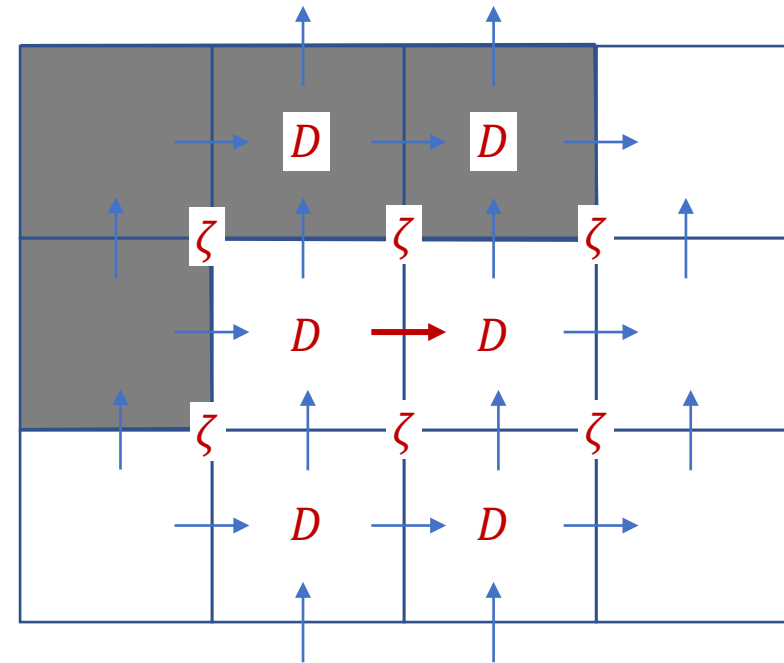


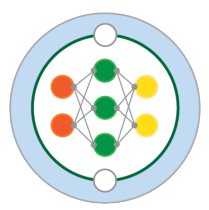
# Stencils



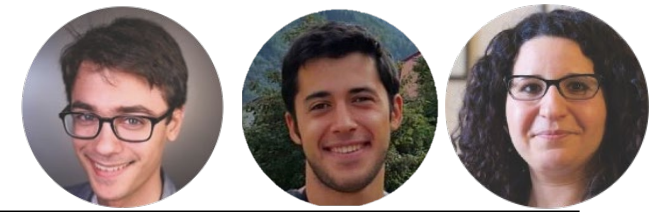
- We know how to implement physical boundary conditions when calculating the quantities
- Caveat: may not be the right boundary condition for the way the ML parameterization “apparently” used the quantities
  - If in testing we find near-boundary artifacts, we should train with boundaries

$$\kappa \bar{\nabla} \cdot \begin{pmatrix} \zeta^2 - \zeta D & \zeta D \\ \zeta D & \zeta^2 + \zeta D \end{pmatrix}$$

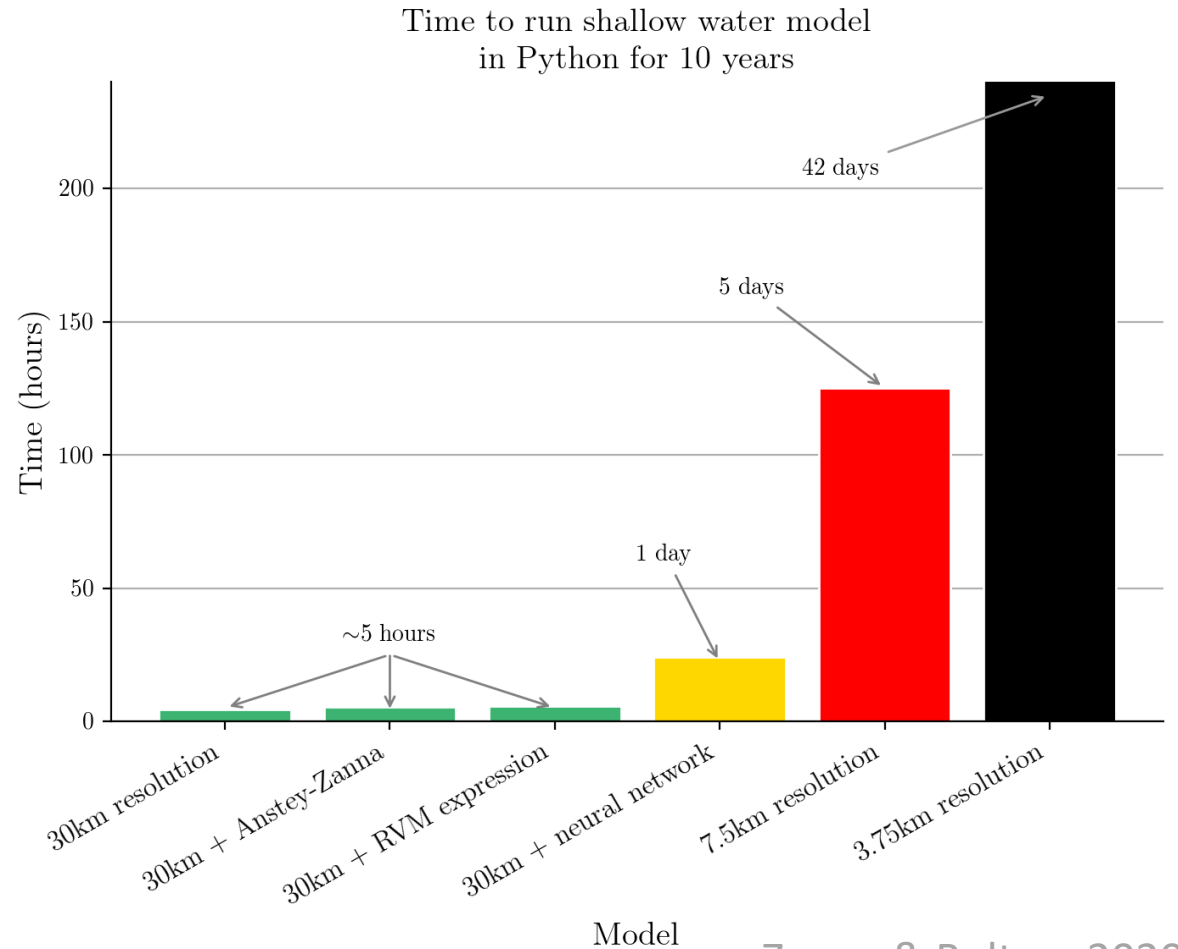




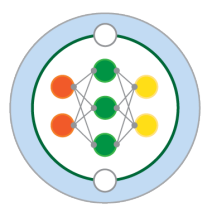
# Performance



- Deep Learning is ideal on GPUs
  - High arithmetic intensity
- ML has been proposed as a mean to accelerate models
  - Balance between volume of inputs and cost of transferring inputs to GPU
- **Equation discovery**
  - More efficient (less arithmetic) implementation than NN
  - Scientific interpretation and understanding



Zanna & Bolton, 2020  
(Fig. S12)



# Active implementations

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- Ocean horizontal momentum closure

- Guillaumin & Zanna, 2021
- Zanna & Bolton, 2021



- Atmospheric convection

- Yuval & O’Gorman, 2020, Yuval et al., 2021, Yuval & O’Gorman, in prep.

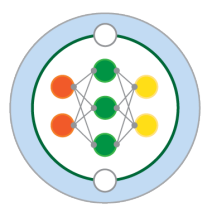


- Ocean surface boundary layer parameter profiles

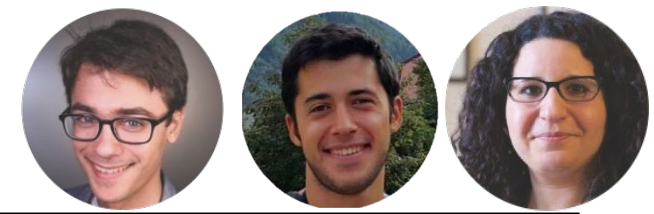
- Ongoing work of Sane et al.







# Momentum closures



- Fine-resolution model evolves as

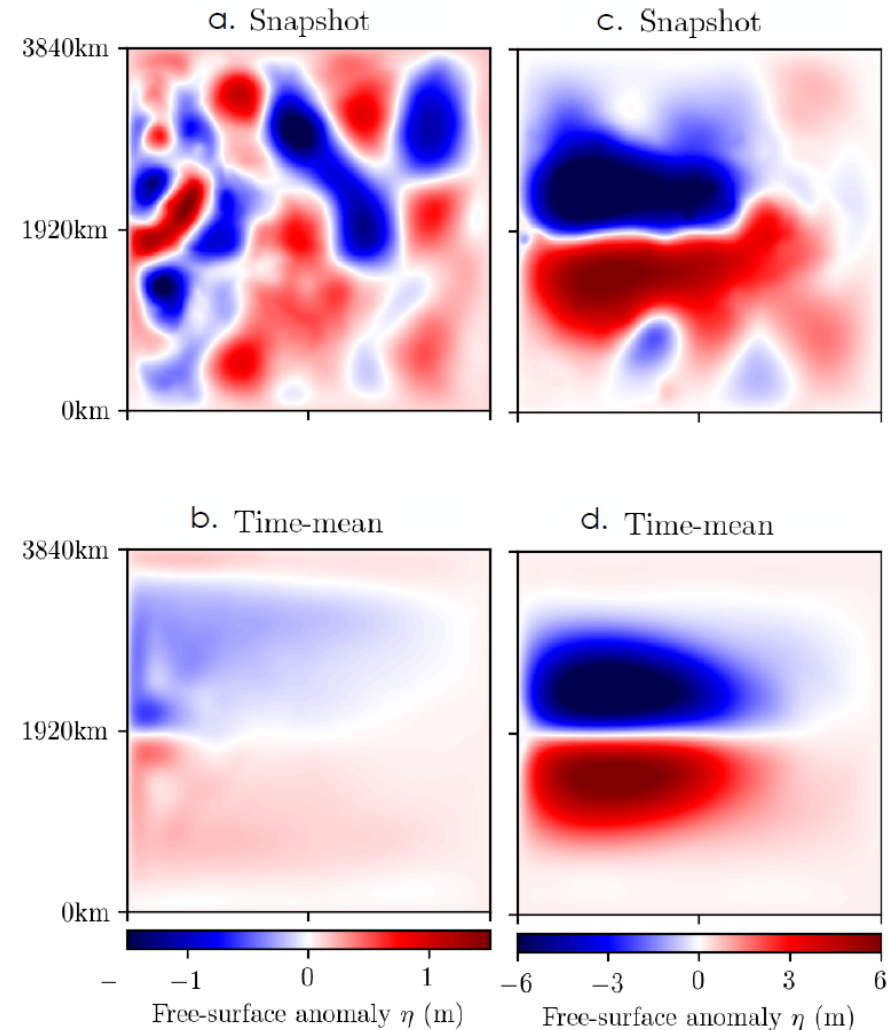
$$\partial_t u + (u \cdot \nabla)u = F + D + S$$

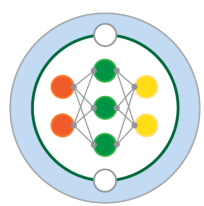
- Sub-grid scale momentum transfer diagnosed by filtering and coarsening ( $\bar{\quad}$ )

$$S = \begin{pmatrix} S_x \\ S_y \end{pmatrix} = (\bar{u} \cdot \bar{\nabla})\bar{u} - \overline{(u \cdot \nabla)u}$$

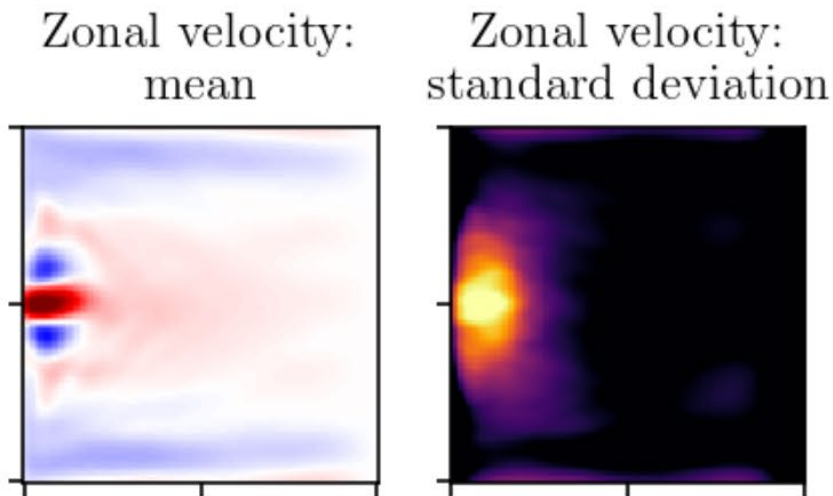
- So that coarse model evolves according to

$$\partial_t \bar{u} + (\bar{u} \cdot \bar{\nabla})\bar{u} = \bar{F} + \bar{D} + S$$

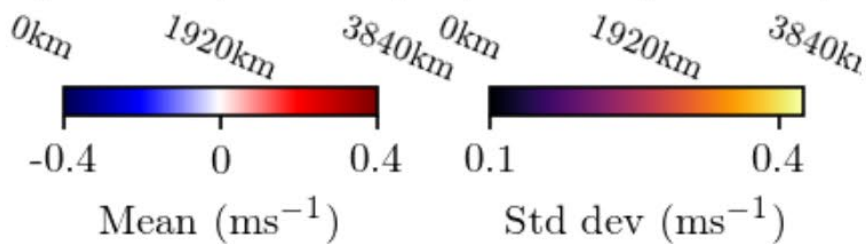
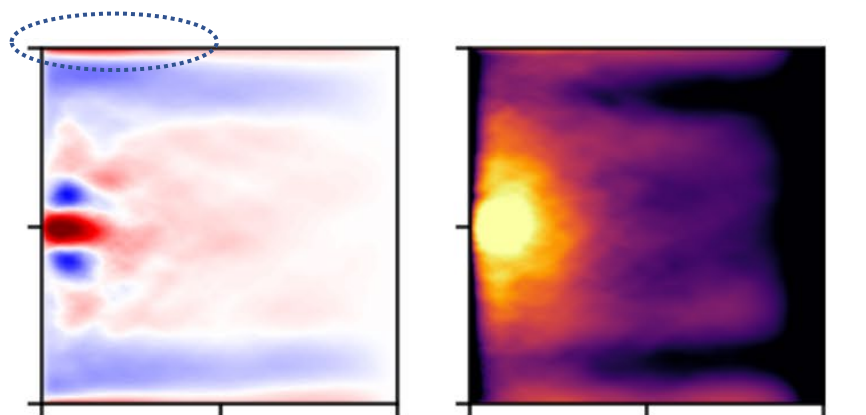




Coarse resolution  
30km

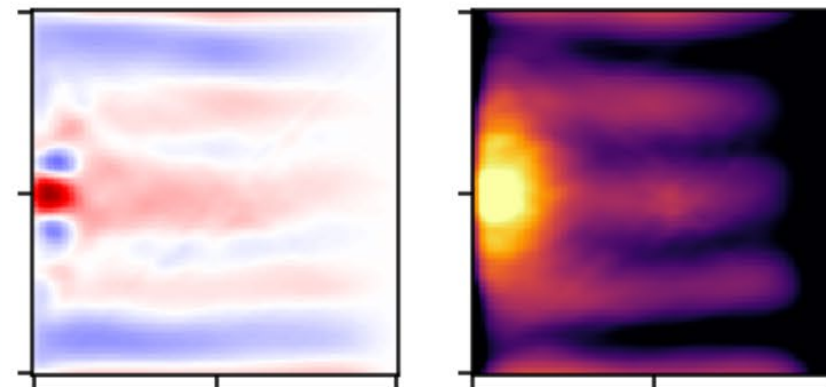


Fine resolution  
3.75km

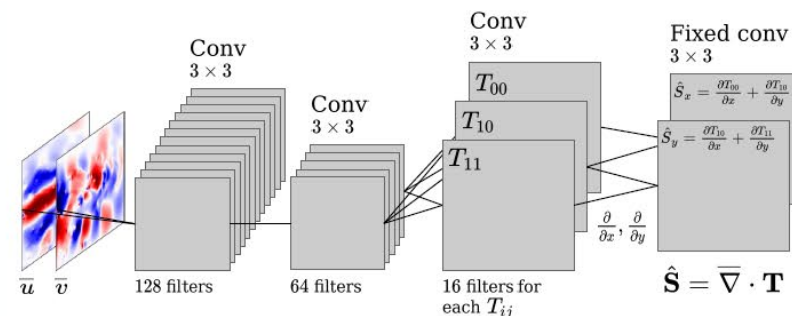
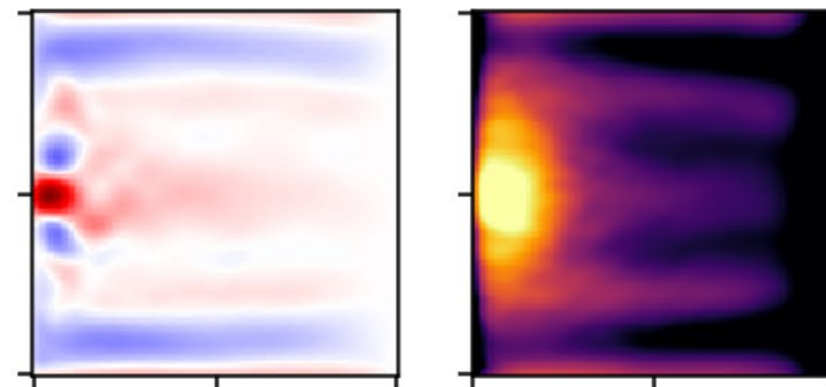


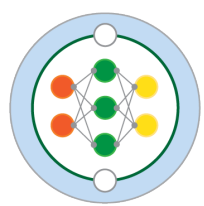
Zanna & Bolton, 2020 (Fig. S10)

Coarse resolution + eqn discovery



Coarse resolution + NN + conservation





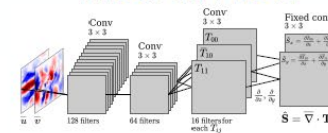
High-resolution

Physics-driven

Equation-  
discovery

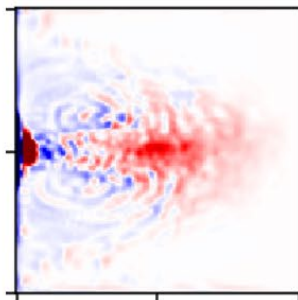
Neural Nets

$$\bar{\nabla} \cdot \begin{pmatrix} -\zeta D & \zeta D \\ \zeta D & \zeta D \end{pmatrix} \quad \kappa \bar{\nabla} \cdot \begin{pmatrix} \zeta^2 - \zeta D & \zeta D \\ \zeta D & \zeta^2 + \zeta D \end{pmatrix}$$

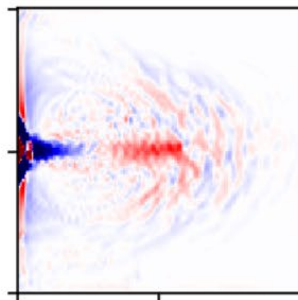


Mean

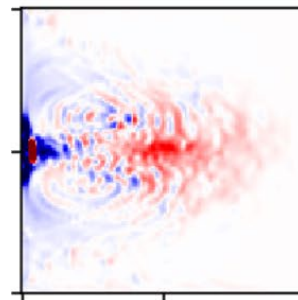
a. True  $S_x$   
mean



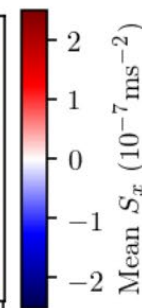
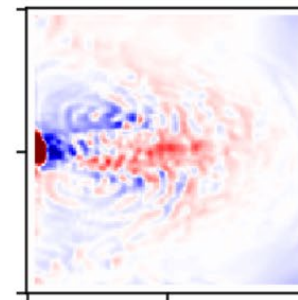
b. AZ17  $\hat{S}_x$   
mean



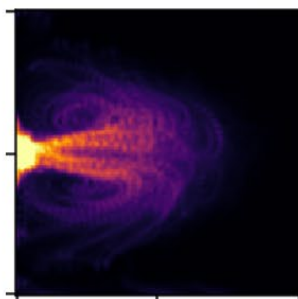
c. RVM  $\hat{S}_x$   
mean



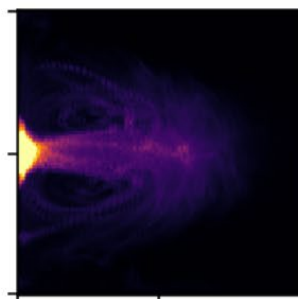
d. FCNN  $\hat{S}_x$   
mean



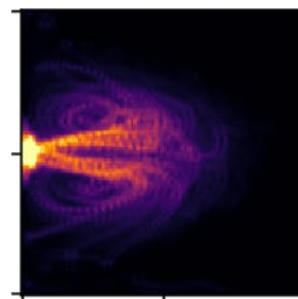
True  $S_x$   
std dev



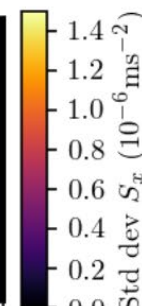
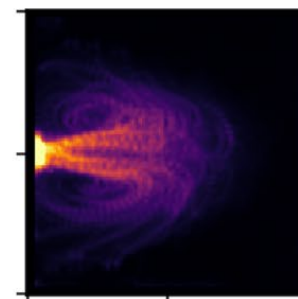
AZ17  $\hat{S}_x$   
std dev



RVM  $\hat{S}_x$   
std dev

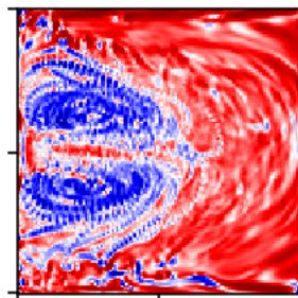


FCNN  $\hat{S}_x$   
std dev

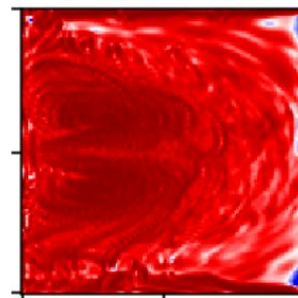


Standard  
Deviation

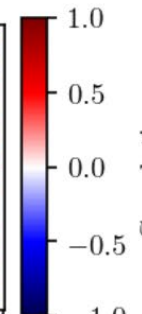
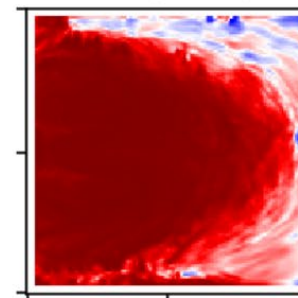
AZ17  
Corr( $S_x, \hat{S}_x$ )



RVM  
Corr( $S_x, \hat{S}_x$ )

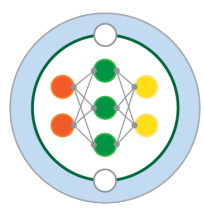


FCNN  
Corr( $S_x, \hat{S}_x$ )

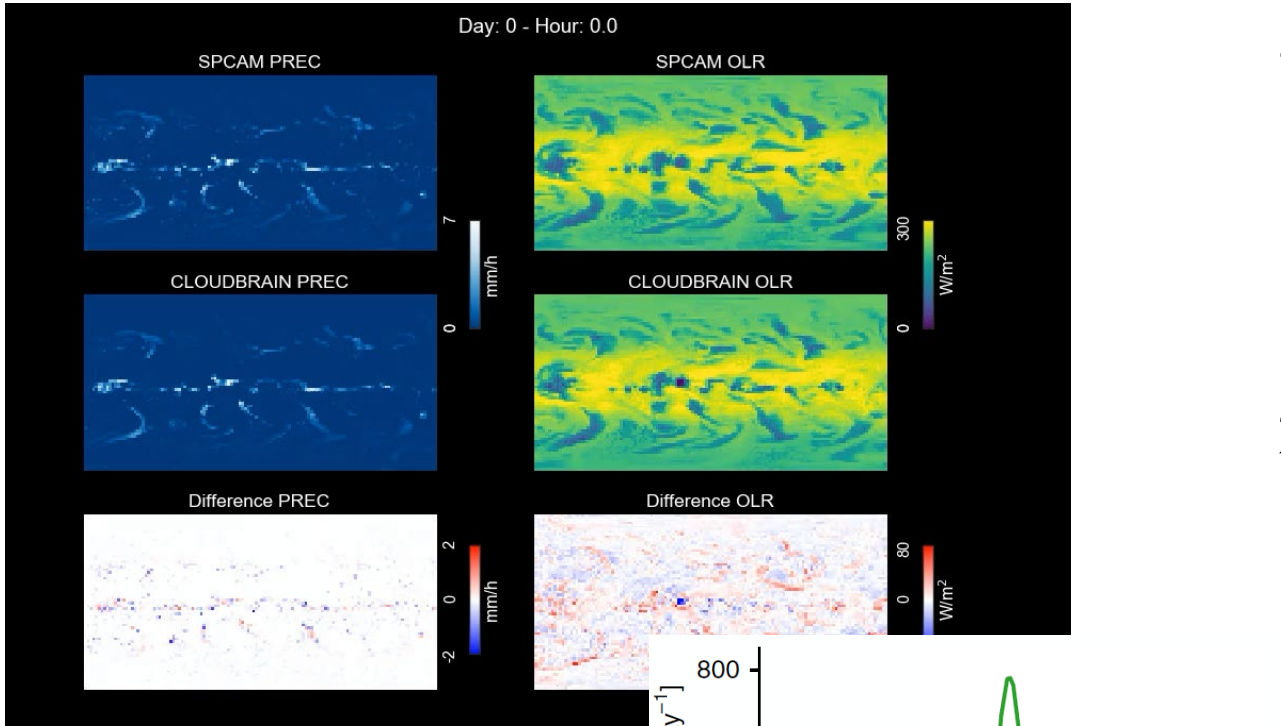


Correlation

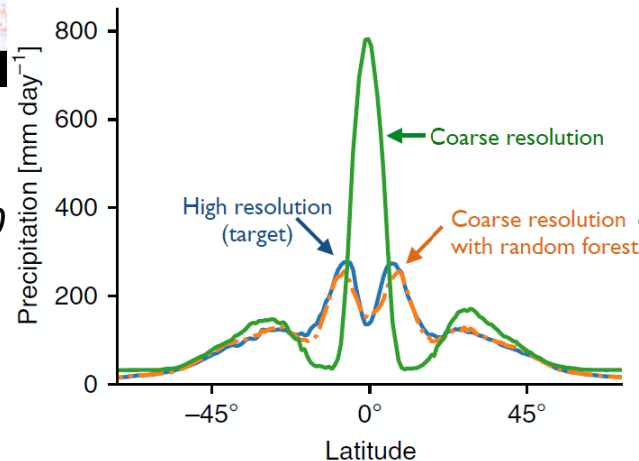
Zanna & Bolton, 2020  
(Fig. S2)



# Atmospheric Convection

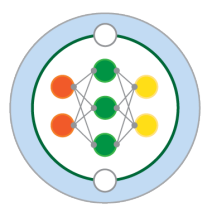


- Train a parameterization by coarse-graining a high-resolution simulation, or learning from SPCAM
  1. Accuracy: calculate the subgrid terms exactly by coarse-graining the equations process by process
  2. Ensure conservation of energy and water:
    - a) Neural network: predict fluxes and sources/sinks (rather than net tendencies) or enforce in architecture/training
    - b) Random forest: predictions are averages over training samples

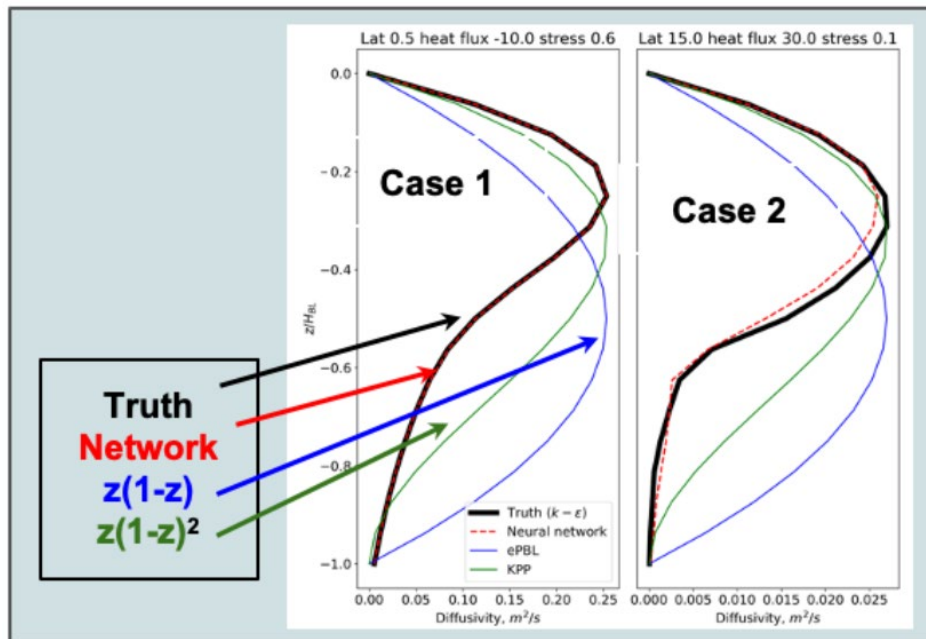
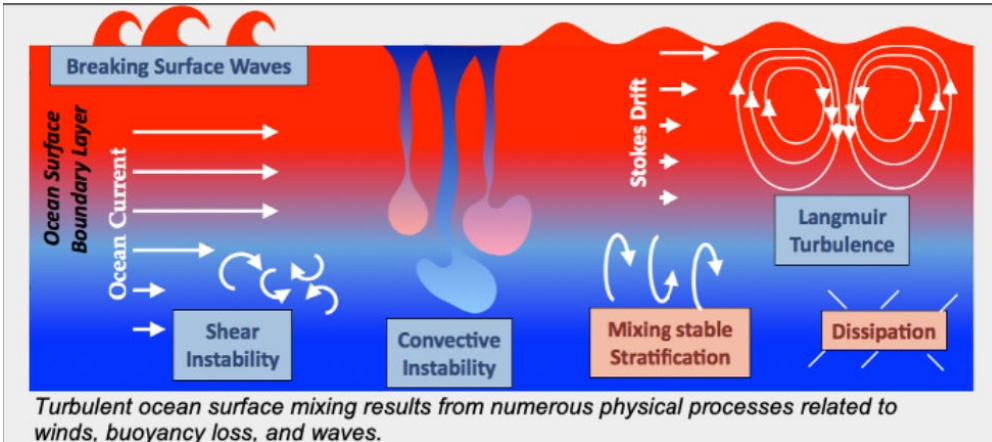


- Stable and accurate simulations using random forests *and* neural nets

Yuval and O'Gorman, *Nat. Comm.* '20  
 Yuval, O'Gorman, Hill, *GRL*, 2021  
 Gentine et al. *GRL* 2018  
 Rasp et al. *PNAS* 2018  
 Beucler et al. *Phys Rev* 2021

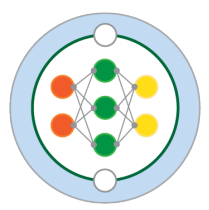


# Ocean surface boundary layer



- ePBL uses an energetically constrained approach for turbulent fluxes in the surface boundary layer
- The energetic constraint provides numerical and physical stability benefits for climate simulation
- Neural networks to parameterize variation in the turbulent mixing profile that **maintains previously established energetic constraints**
- Embedding the network in the existing approach improves the turbulent flux profiles while maintaining the stability benefits
  - Improves on traditional profiles

Reichl & Hallberg, 2018 Reichl & Li, 2019



# Summary

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- M<sup>2</sup>LInES
- To date: implementation of ML parameterizations mostly evaluated in idealized models ... we're working on getting them into GCMs
- Quite a few issues arise, some mundane, other's tricky
  - Stability not guaranteed
  - Online model data stencil needed for ML parameterizations can be wider than we are used to
  - Boundary conditions require more work
- Equation discovery
  - Addresses many of the above problems
  - And aids in interpretation