

# Unresolved processes in climate models: lessons from the laboratory

Paul Williams

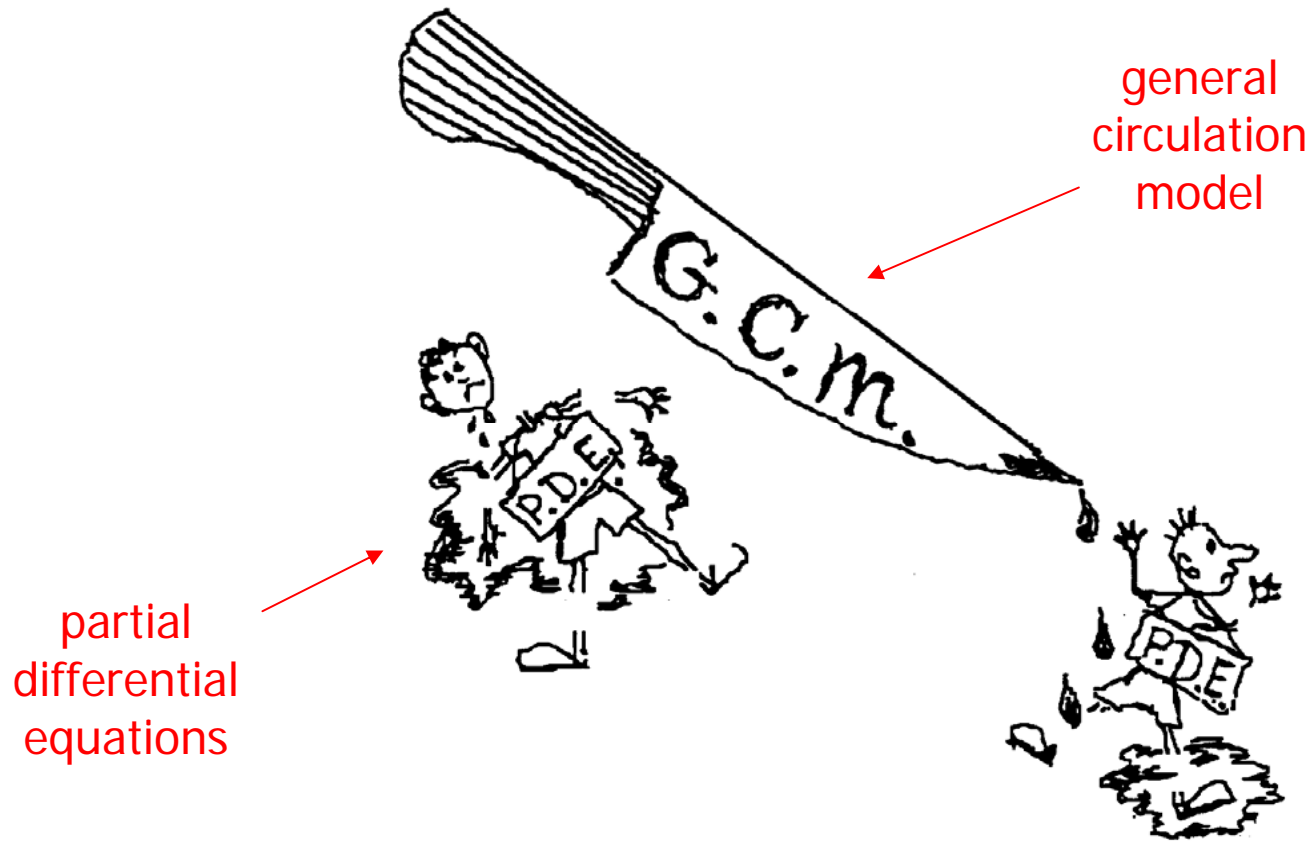
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# Outline

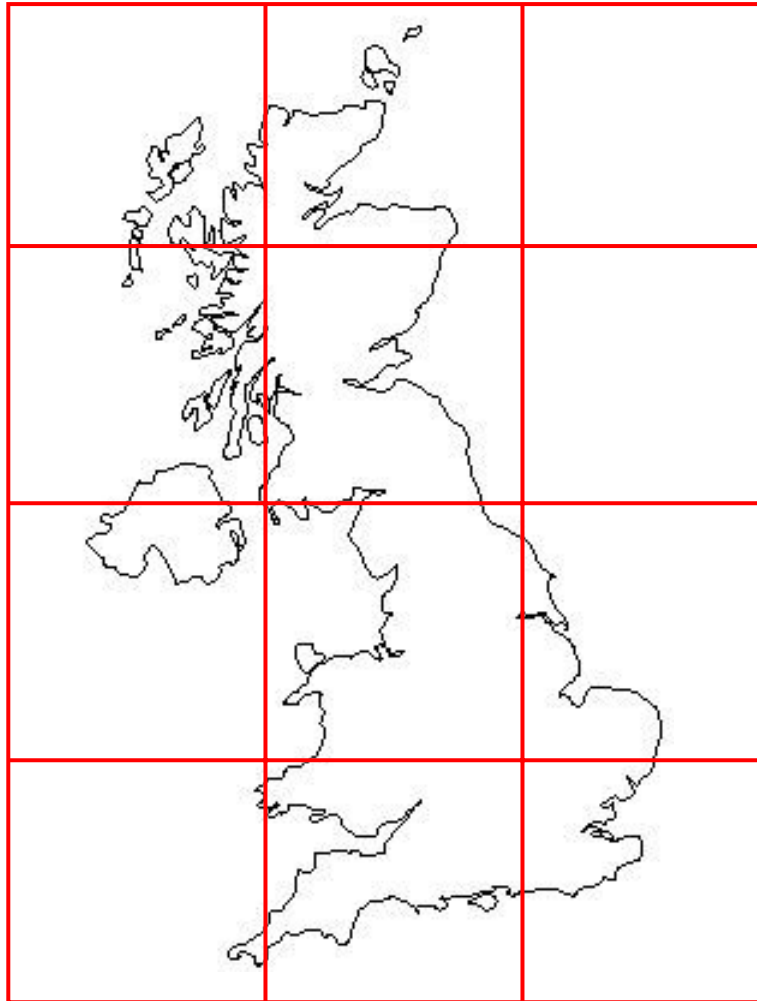
- Introduction
- Oceanic case study:  
the thermohaline circulation
- Atmospheric case study:  
sudden stratospheric warmings
- Conclusions

# Why climate simulation is hard:



(Schertzer & Lovejoy 1993)

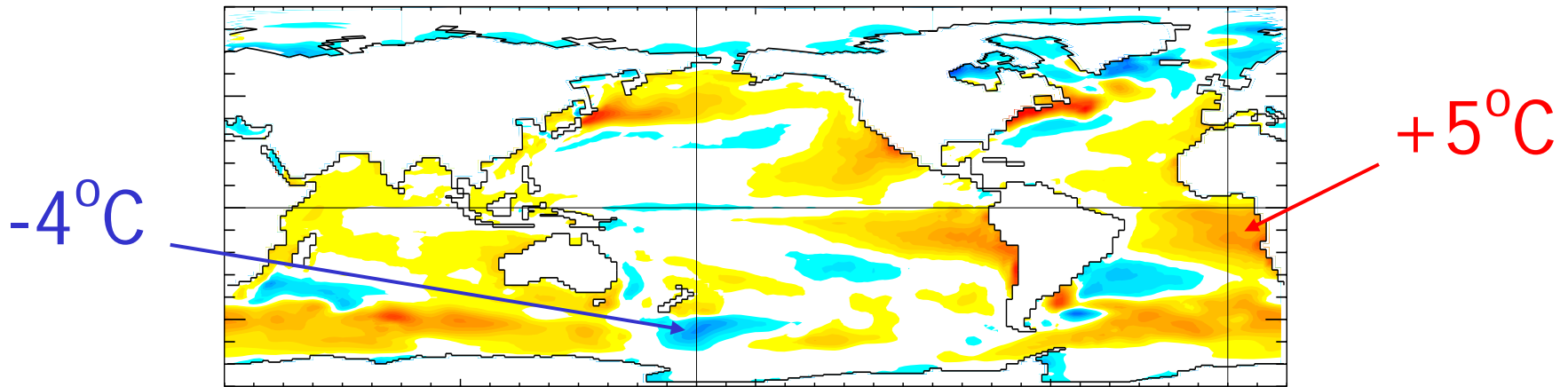
# Typical grid for climate simulation:



← grid boxes

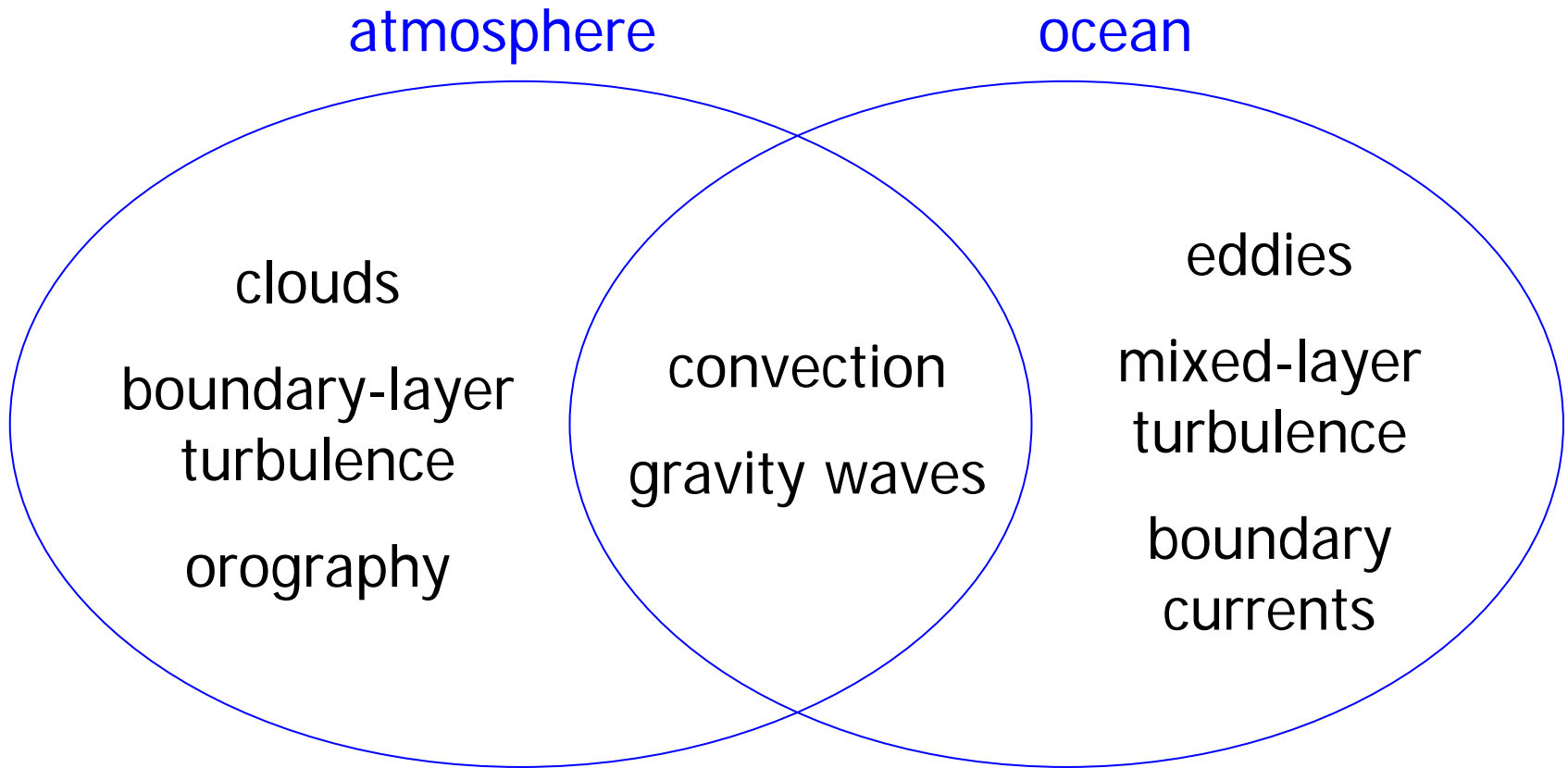
- GCMs **cannot resolve** many of the **most important processes** in the climate system

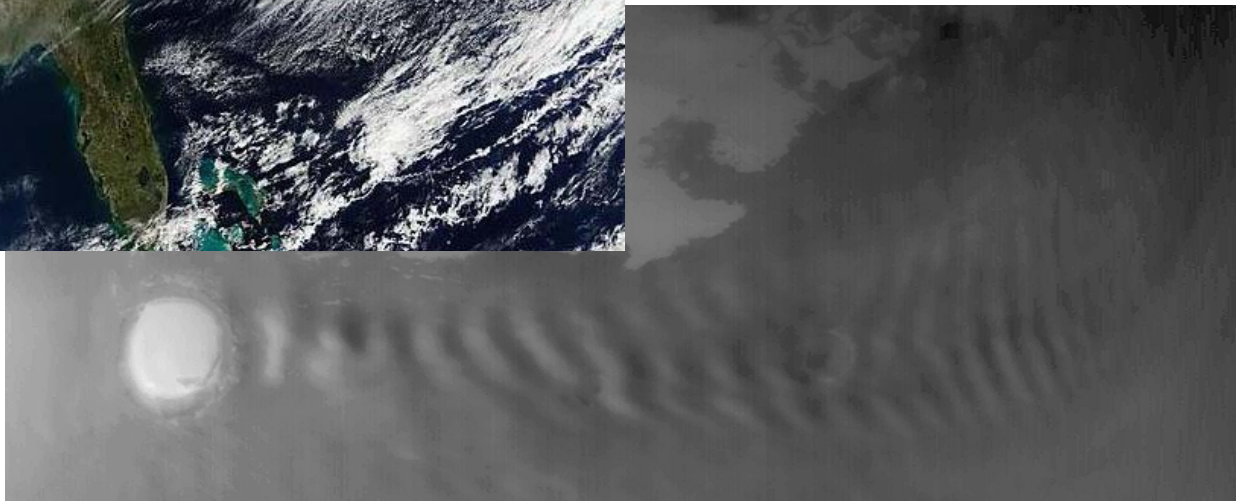
# Systematic climate biases result:



*“to understand and characterise the important unresolved processes... in the climate system” is a “high priority area for action” (IPCC, 2001)*

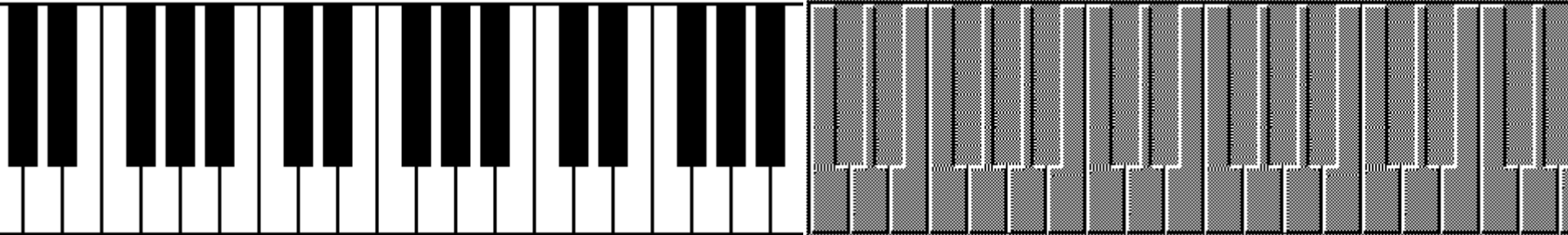
# Unresolved processes in GCMs







# GCMs = broken pianos!



Rossby waves

gravity waves

“We might say that the atmosphere is a musical instrument on which one can play many tunes... and nature is a musician more of the Beethoven than of the Chopin type.”

Letter from Jule Charney to Phillip Thompson, 12 February 1947

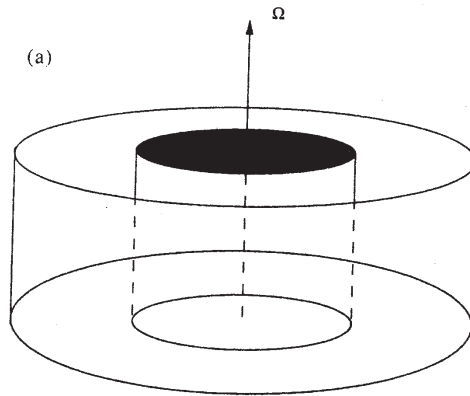


# Pertinent questions:

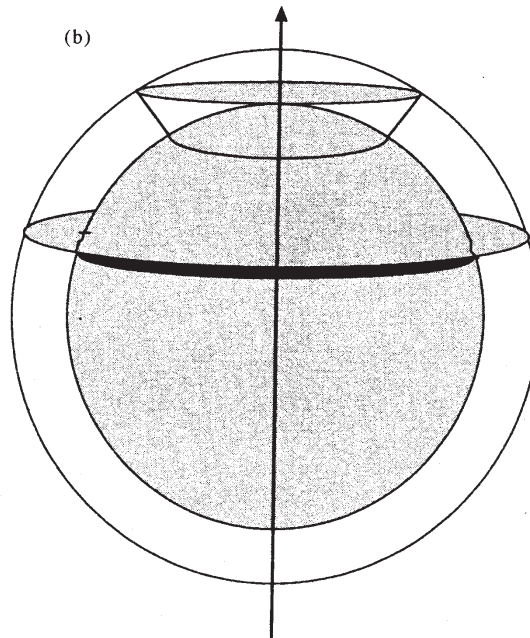
- Does it matter that gravity waves are not resolved in weather/climate models?
- Phrased differently, do gravity waves interact with the resolved flow?
- If so, can the interaction be parameterized?
- How do we even try to find answers to these questions?!

# Dynamical similarity

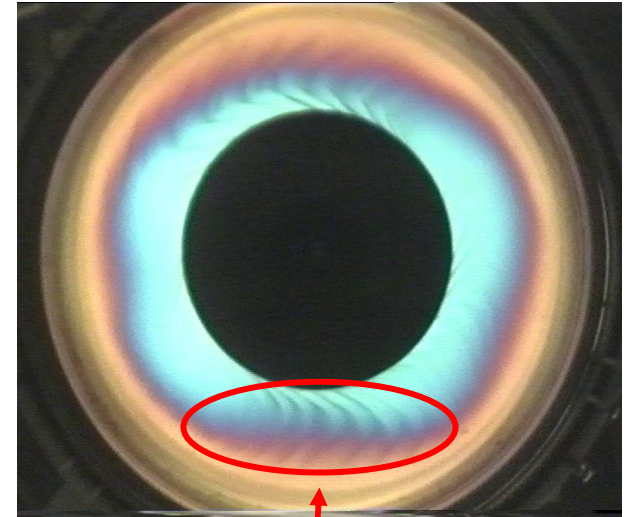
rotating  
annulus:



rotating  
planet:



(Read et al., 1998)



(Williams et al. 2003)



(Dalin et al. 2004)

# Oceanic case study: the thermohaline circulation

Acknowledgements: Tom Haine & Peter Read

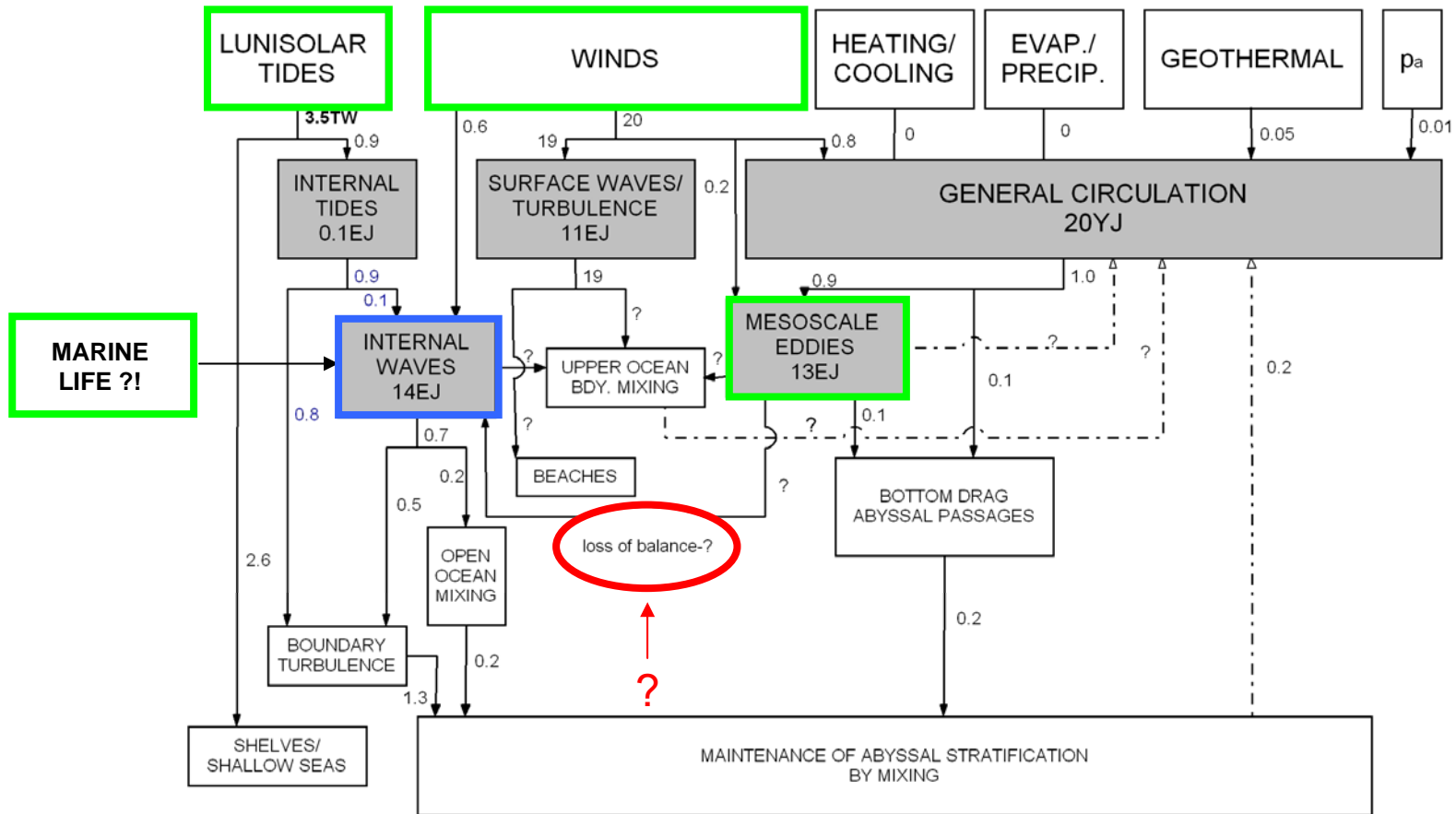
# The thermohaline circulation



# Ocean energetics

- **deep-water formation** acts to reduce the ocean's potential energy
- so does the **baroclinic generation of eddies**
- but the ocean is in a **steady state**  $\Rightarrow$  need to re-supply this lost potential energy
- this is achieved via **vertical mixing** due to **internal gravity waves** (without which the deep ocean fills with uniformly cold, motionless water; Sandström, 1908)
- **how are internal waves (and hence deep ocean mixing) powered?**

# Energy budget for global ocean circulation



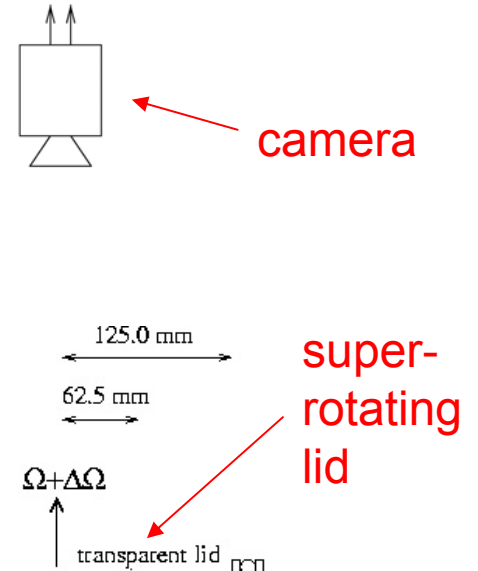
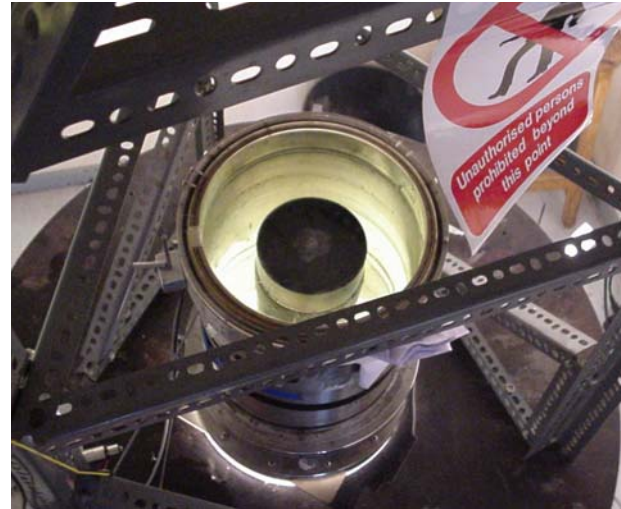
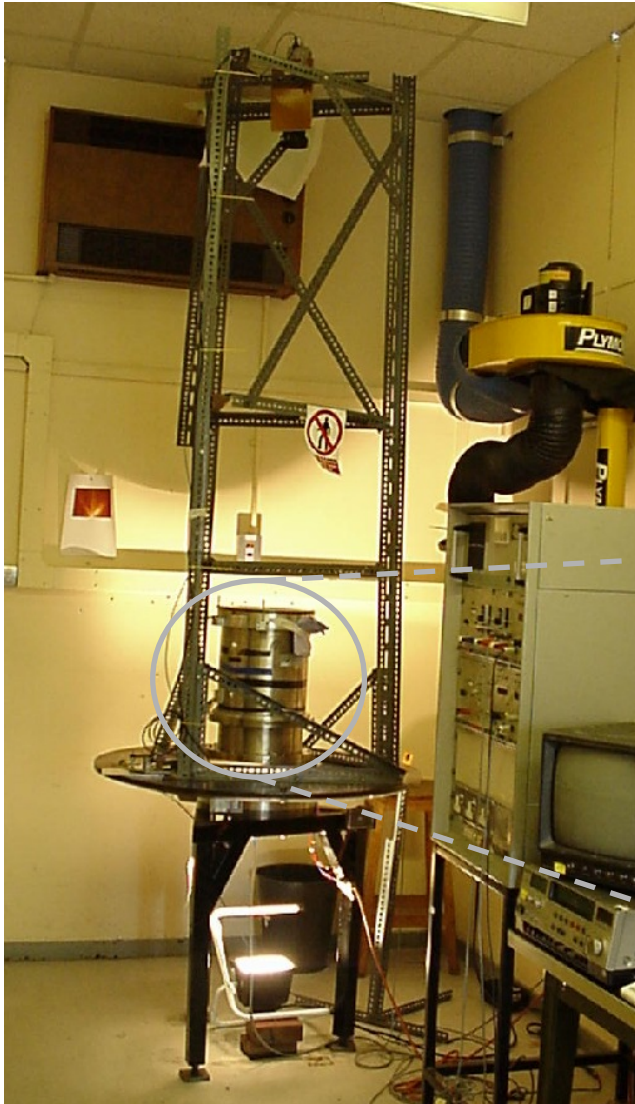
(Wunsch & Ferrari, 2004)

# How can we quantify the “loss of balance” energy pathway?

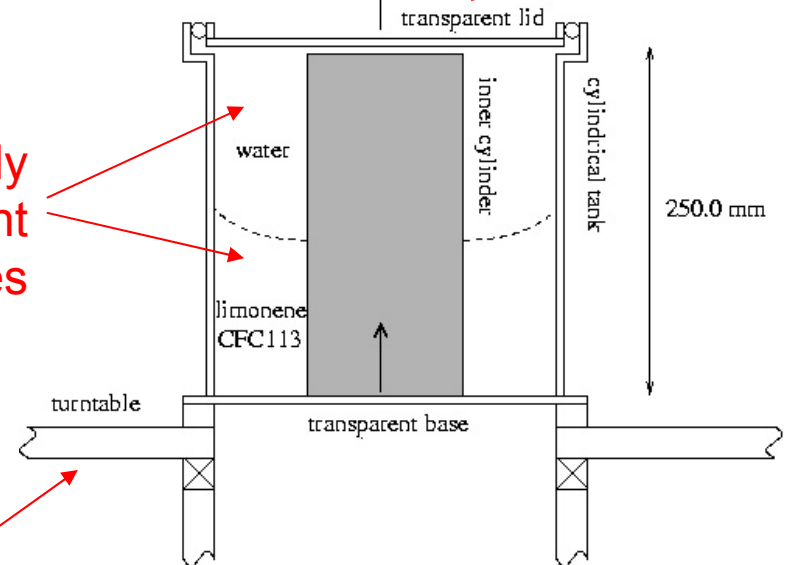
- **slow manifold theories?** But they contain many *ad hoc* approximations in order to make them analytically tractable
- **numerical models?** But global General Circulation Model grids are usually too coarse to resolve eddies and internal waves
- **laboratory experiments?** Let's see!



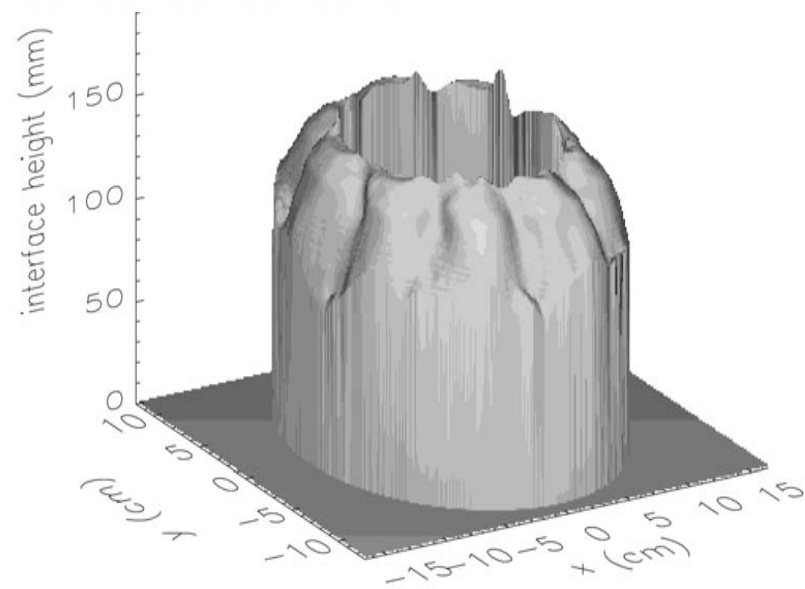
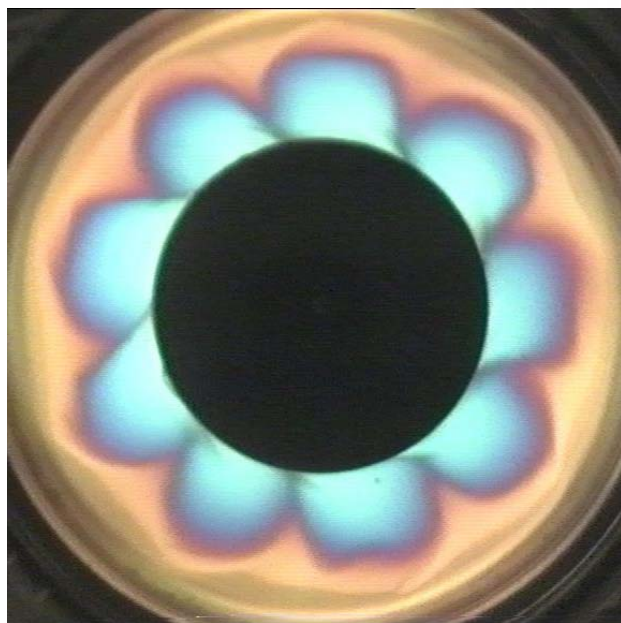
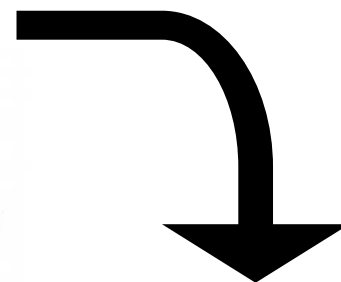
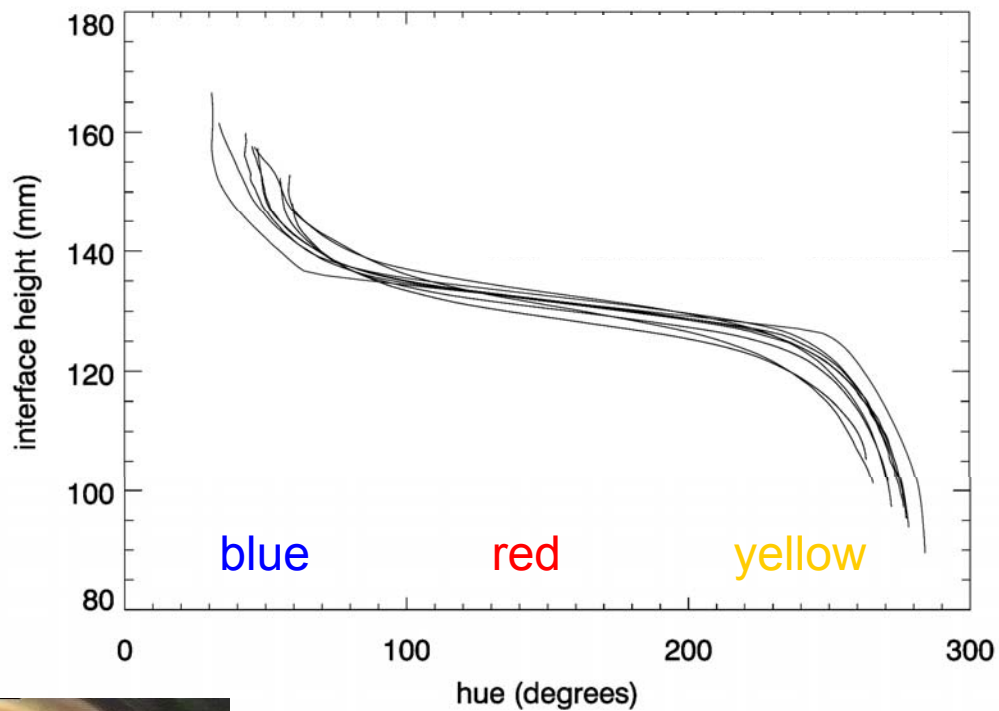
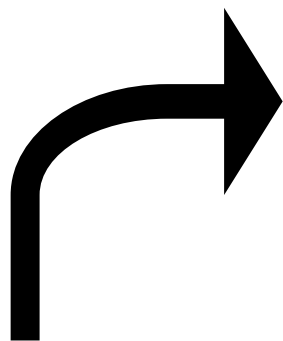
# Rotating two-layer annulus experiment



slightly different densities

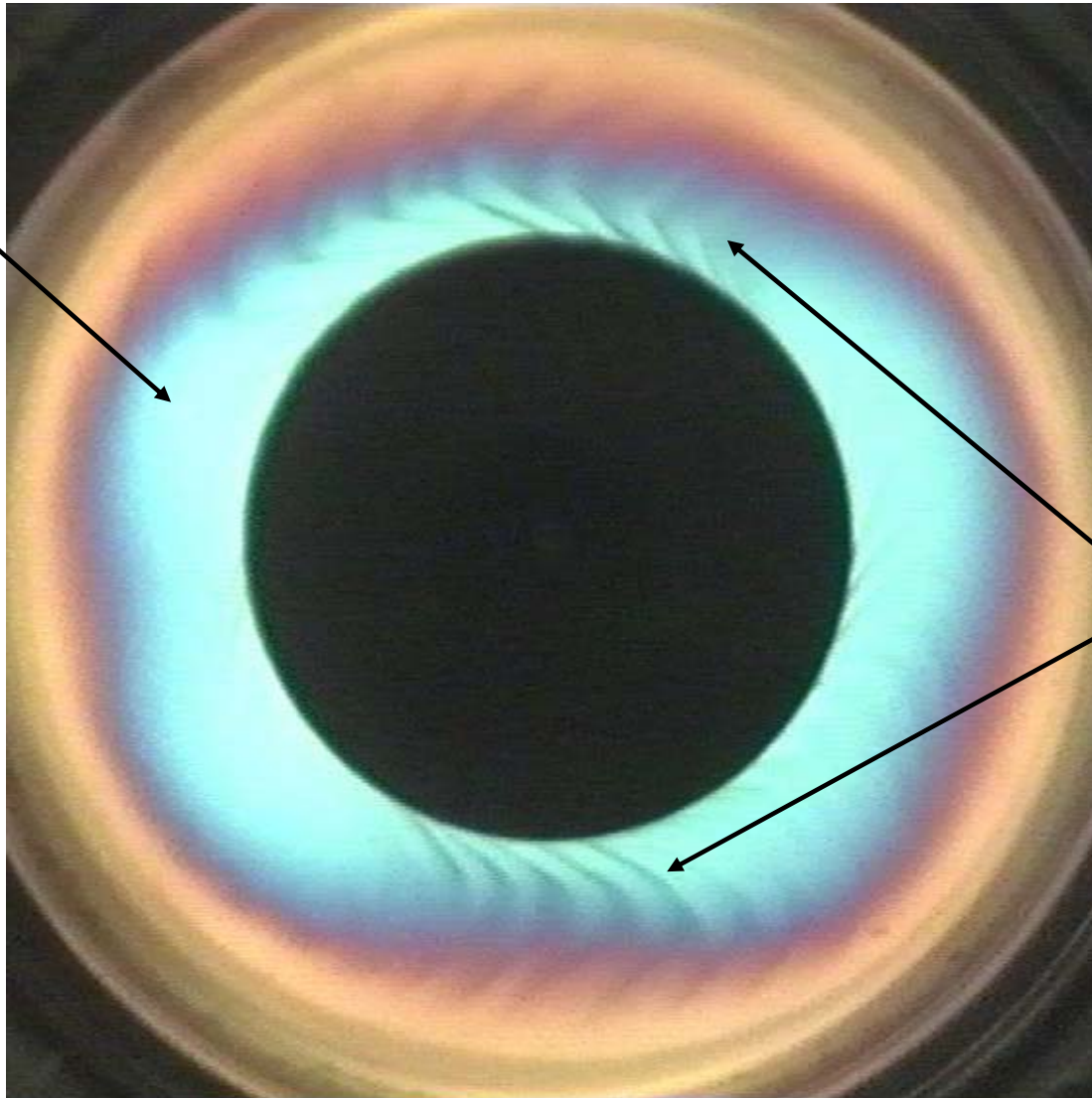


rotating turntable



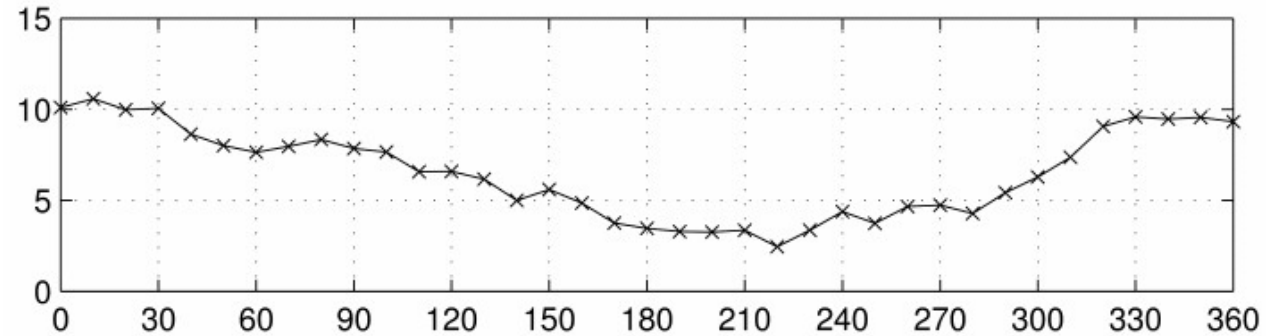
# Typical interface height field seen by camera

balanced  
flow

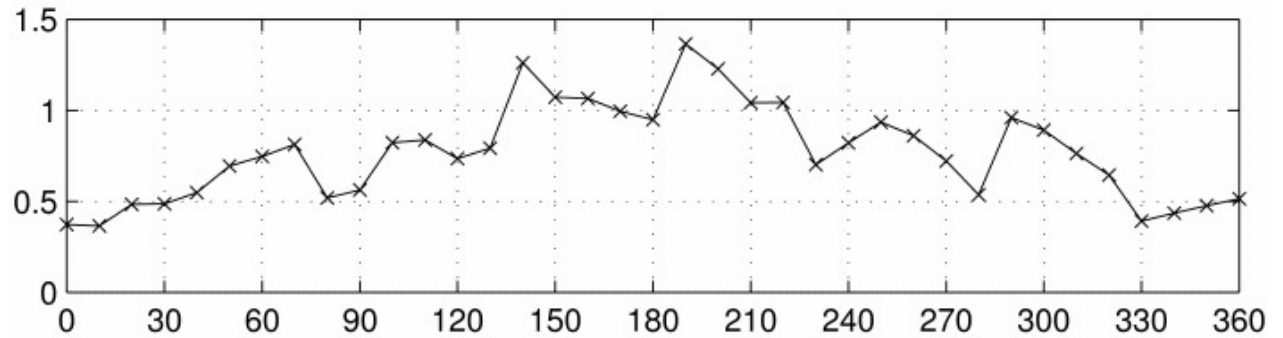


internal  
inertia-  
gravity  
waves  
(IGWs)  
generated  
by loss of  
balance

balanced flow  
amplitude



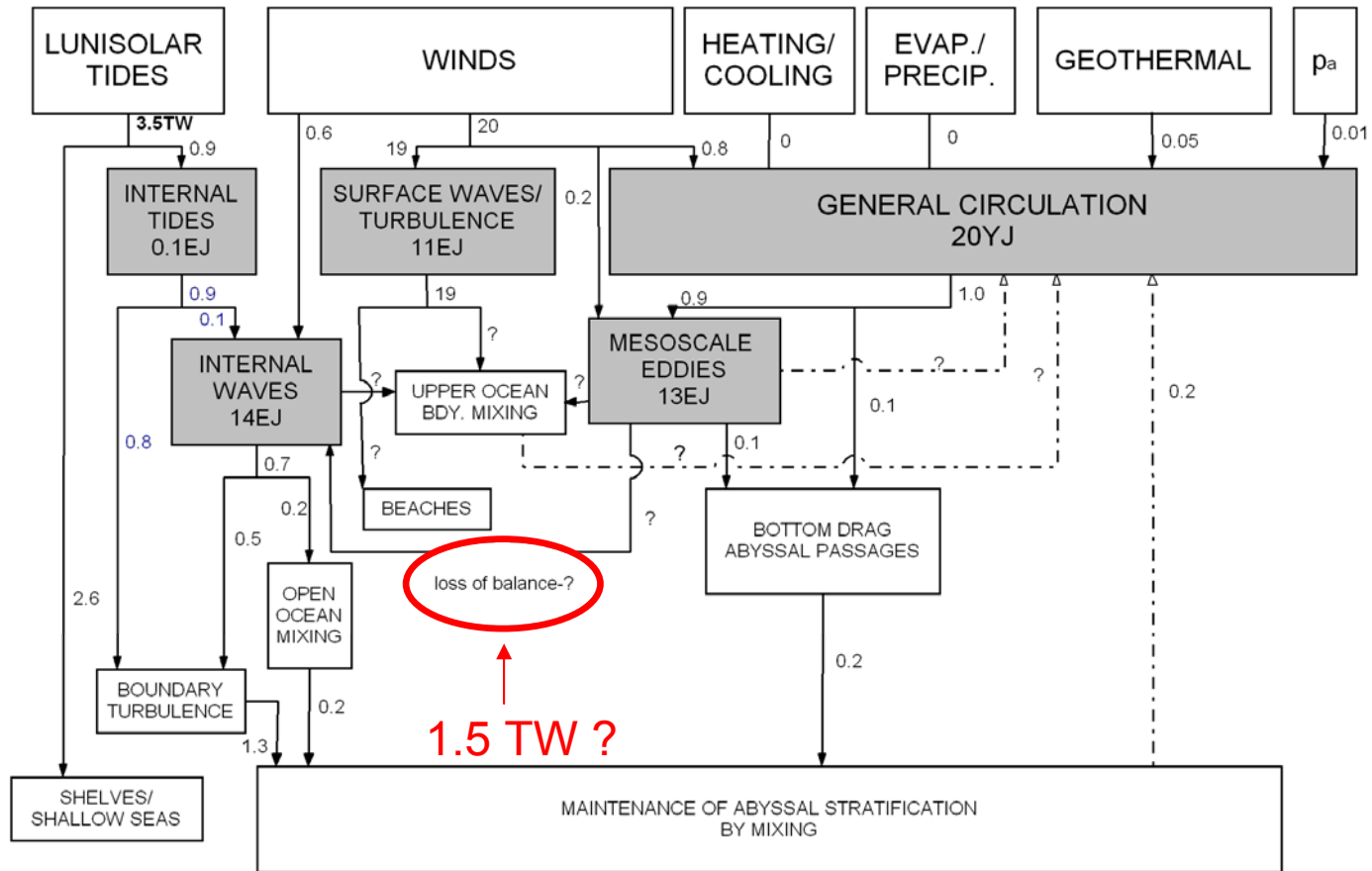
IGW  
amplitude



time

→ rate of energy growth in IGWs, as a fraction of the balanced flow energy, is  
**~1% per rotation period**

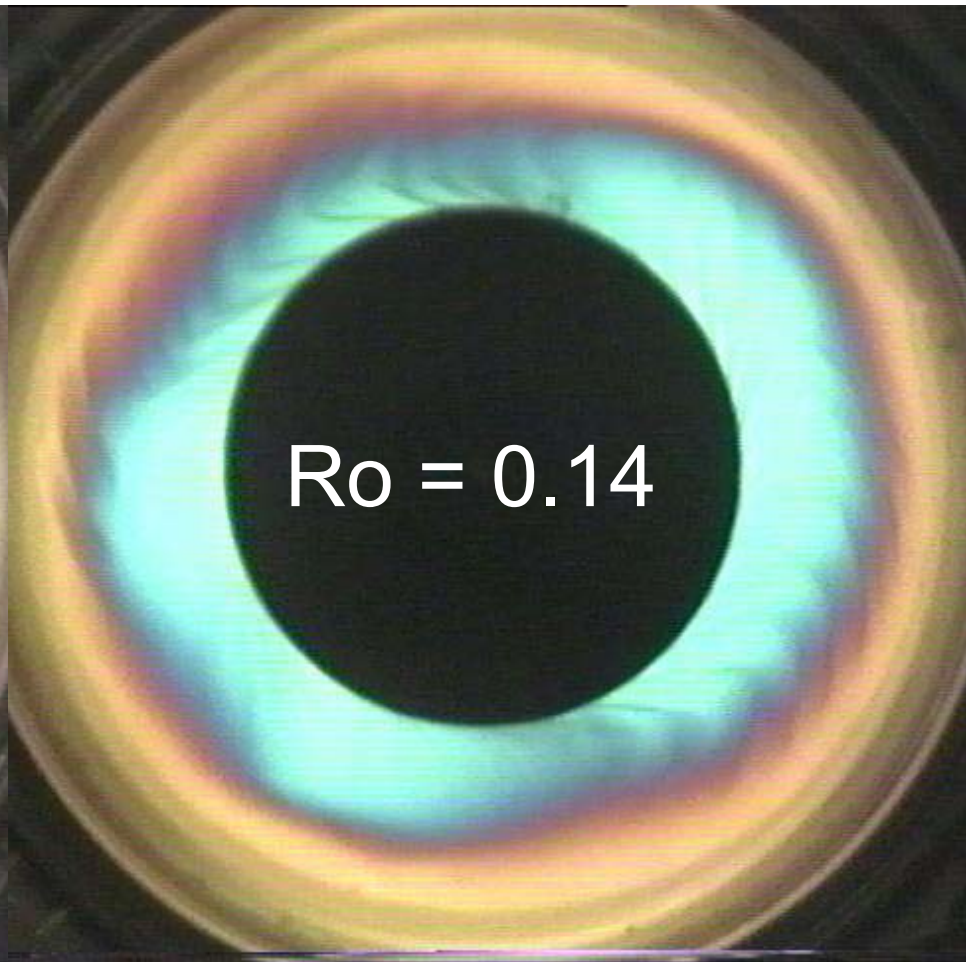
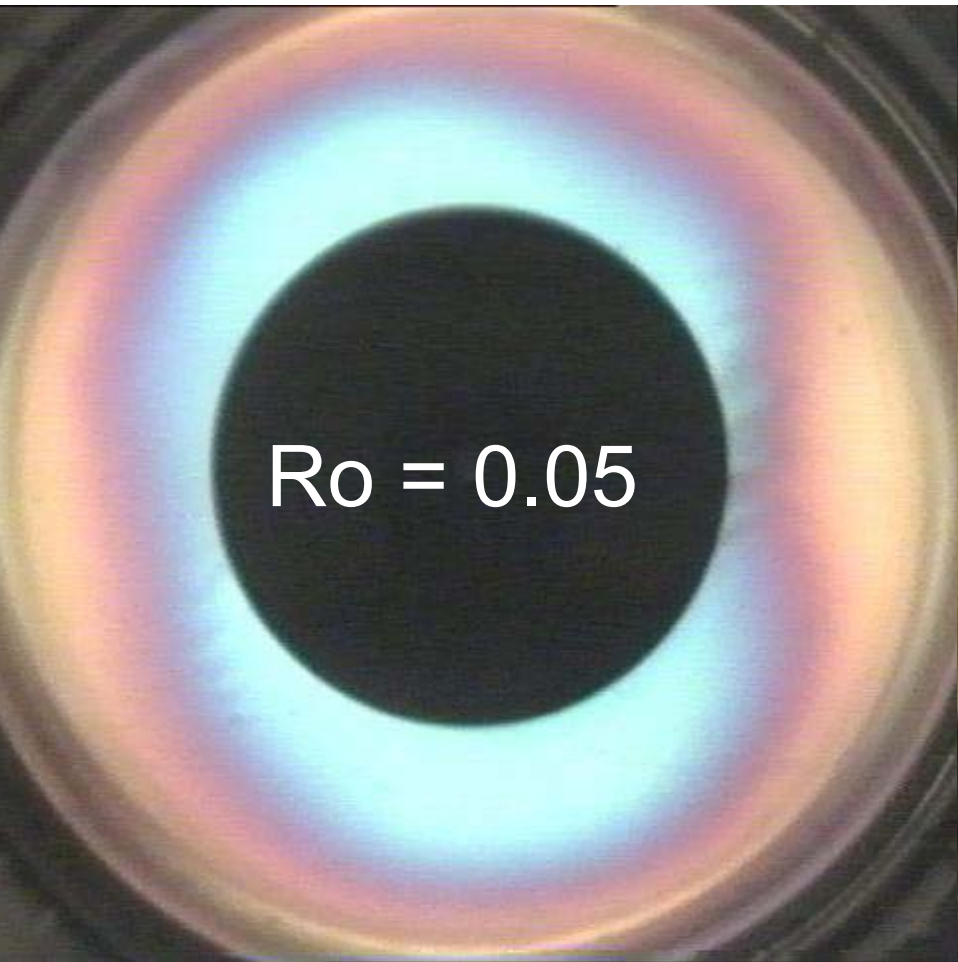
# Energy budget for global ocean circulation:



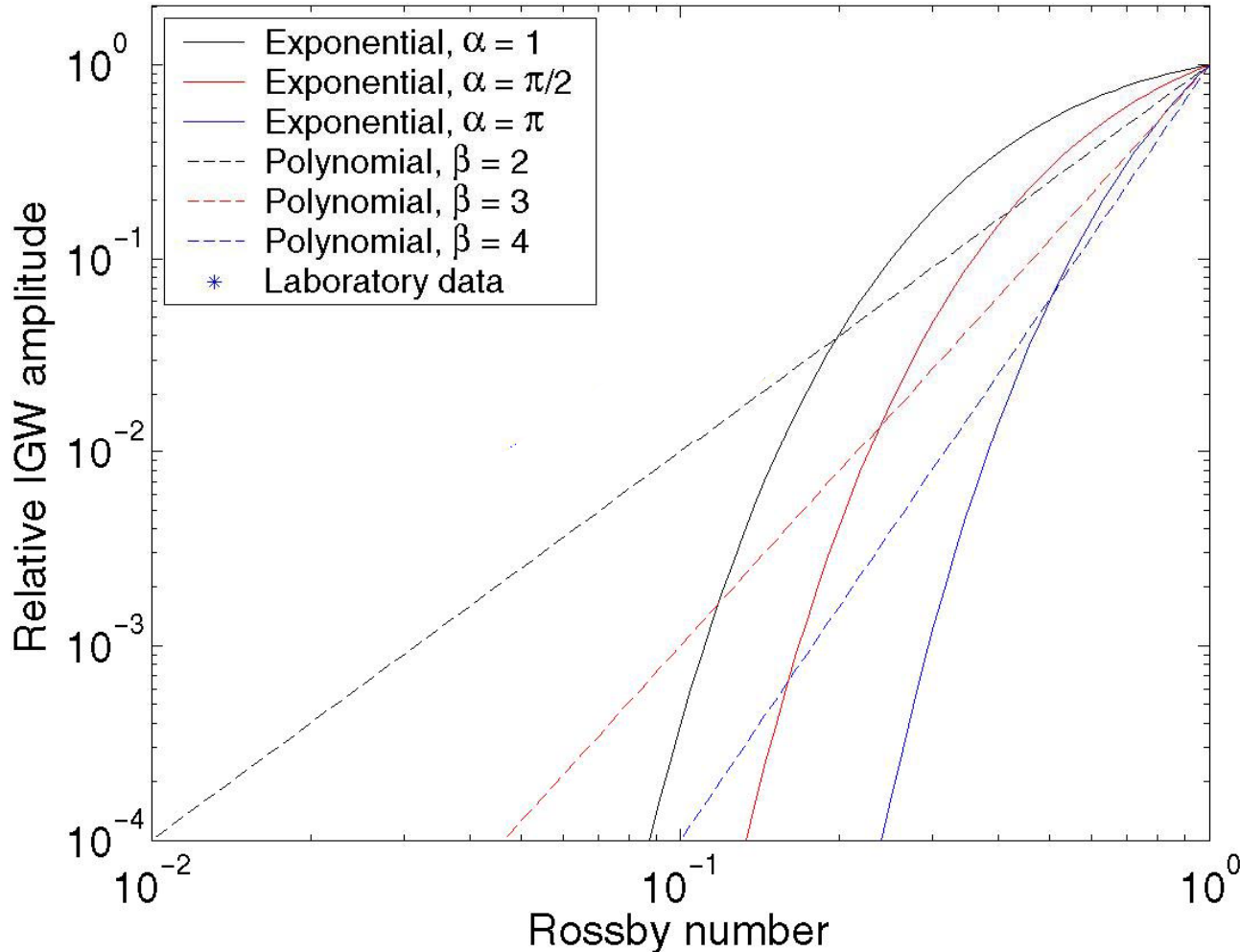
(Wunsch & Ferrari, 2004)



How do IGWs vary with Rossby number?



# How do IGWs vary with Rossby number?



- non-asymptotic theories suggest  $\sim Ro^{-1/2} \exp(-\alpha/Ro)$  (e.g. Vanneste & Yavneh 2004; Plougonven et al. 2005 find that  $\alpha \geq \pi/2$ )

- standard asymptotic analysis suggests  $\sim Ro^\beta$ ,  $\beta \geq 2$

- but the laboratory data suggest  $\sim Ro^{1.2}$



# THC case study: conclusions

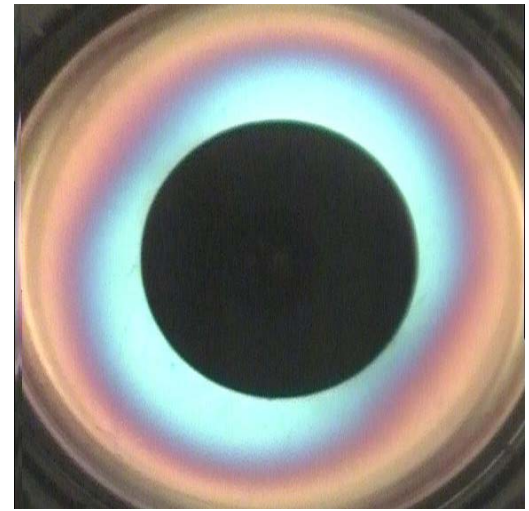
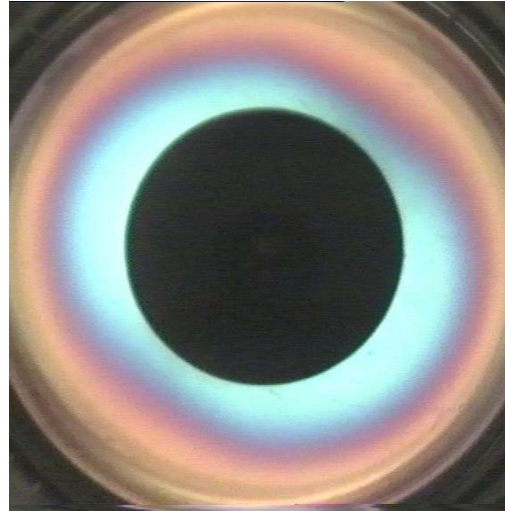
- vertical mixing due to (unresolved) breaking internal waves plays a **critical role** in maintaining the global ocean circulation
- **about 1%** of the large-scale flow energy is lost to internal waves each 'day' in the lab
- crude extrapolation to the ocean  $\Rightarrow$  **1.5 TW**
- but at least the vertical mixing due to unresolved internal waves is amenable to parameterisation in GCMs...

# Atmospheric case study: sudden stratospheric warmings

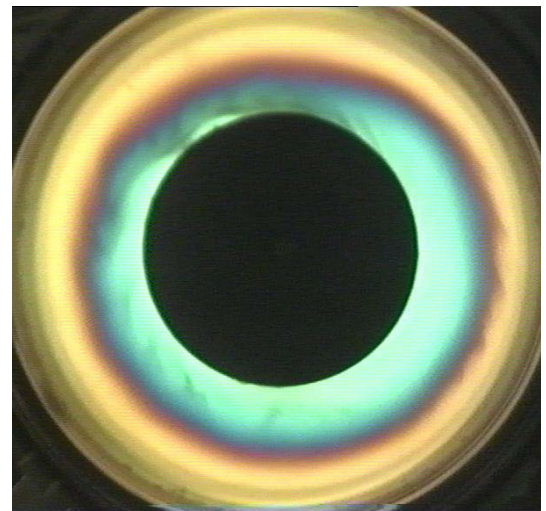
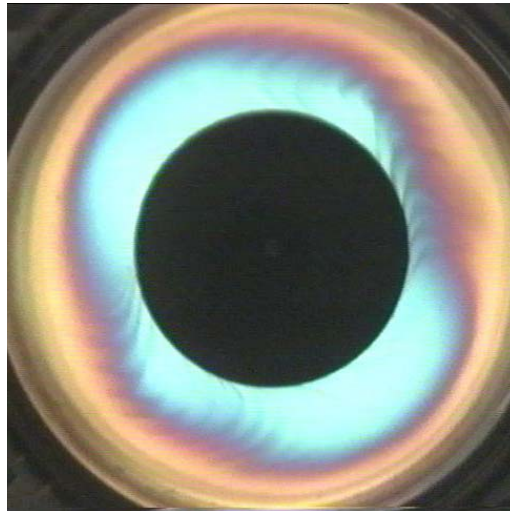
Acknowledgements: Thomas Birner

# 'Noise'-induced transitions in the lab

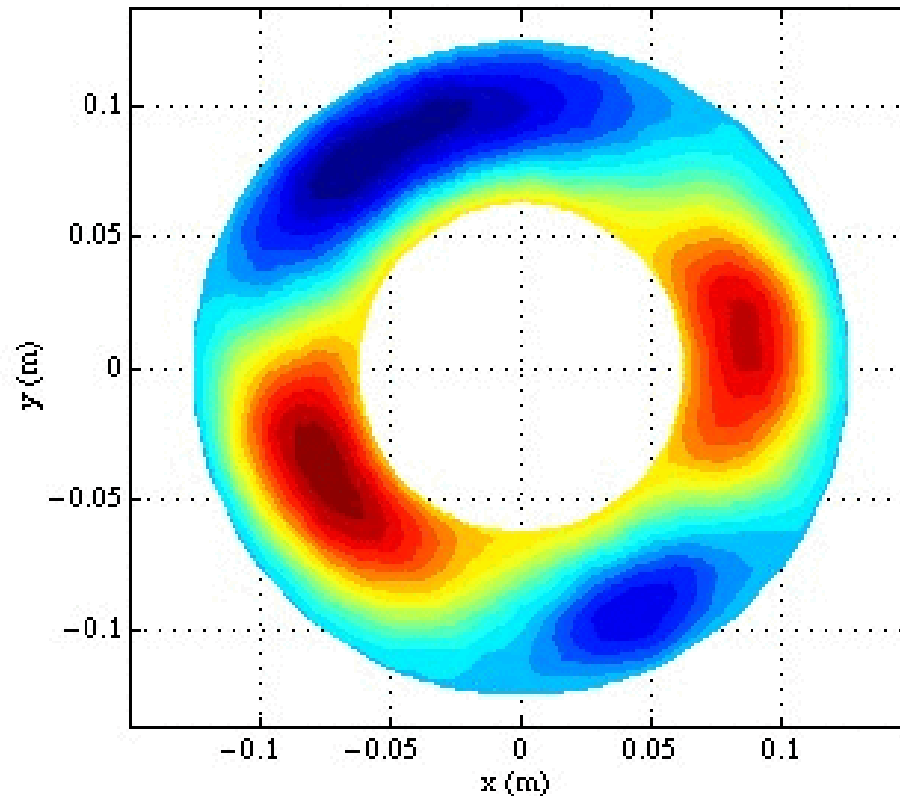
without  
gravity  
waves:



with  
gravity  
waves:



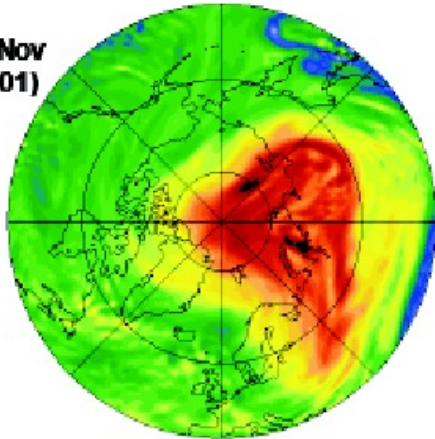
# Noise-induced transition in a QG model with a stochastic GW parameterisation



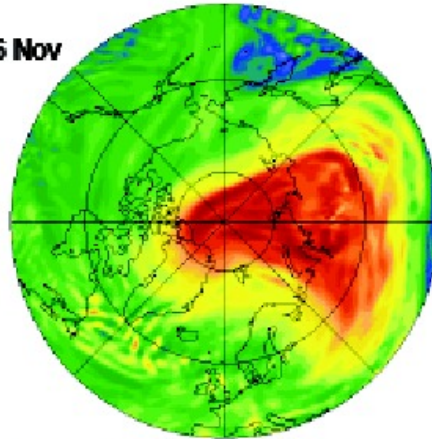
Williams et al. (2003)

# Arctic polar vortex split

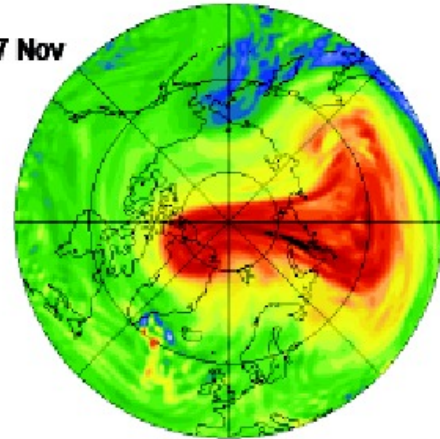
25 Nov  
(2001)



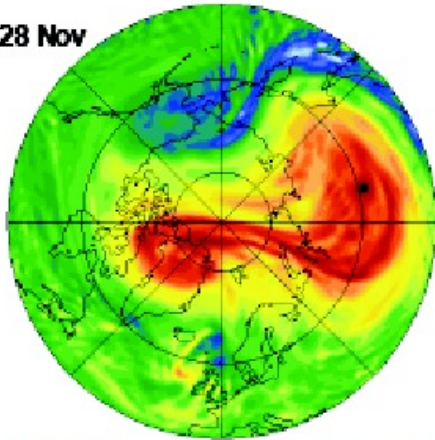
26 Nov



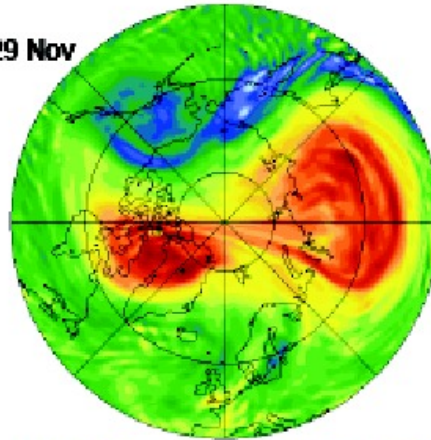
27 Nov



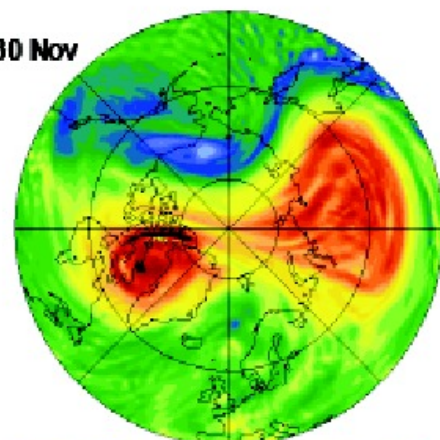
28 Nov



29 Nov



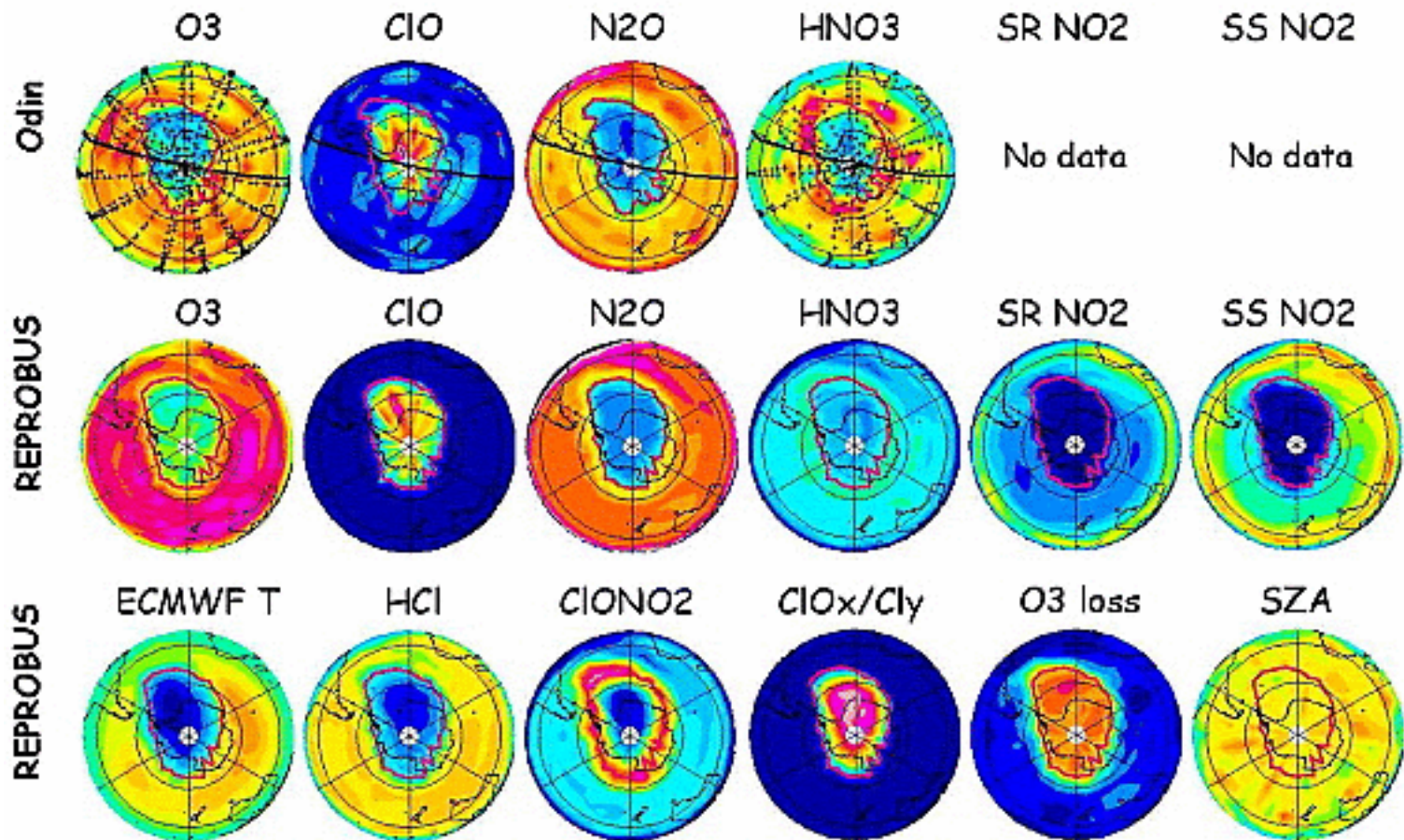
30 Nov





# Antarctic polar vortex split

19-20 September 2002



Ricaud et al. (2005)

# Holton and Mass (1976) model


Quasi-geostrophic  $\beta$ -plane channel, 30-90°N, from tropopause to mesopause:

'linearised' QGPV equation: 
$$(\partial_t + \bar{u}\partial_x)q' + \beta'\partial_x\psi' + \frac{f_0^2}{\rho}\partial_z\left(\frac{\alpha\rho}{N^2}\partial_z\psi'\right) = 0$$

equation for zonal-mean flow: 
$$\partial_t\left[\partial_{yy}\bar{u} + \frac{f_0^2}{N^2\rho}\partial_z(\rho\partial_z\bar{u})\right] = -\frac{f_0^2}{N^2\rho}\partial_z[\alpha\rho\partial_z(\bar{u} - U_R)] + \frac{f_0^2}{N^2}\partial_{yy}\left[\rho^{-1}\partial_z(\overline{\rho\partial_x\psi'\partial_z\psi'})\right]$$

where  $q' = \nabla^2\psi' + \frac{f_0^2}{\rho}\partial_z\left(\frac{\rho}{N^2}\partial_z\psi'\right)$  and  $\beta' = \beta - \partial_{yy}\bar{u} - \frac{f_0^2}{\rho}\partial_z\left(\frac{\rho}{N^2}\partial_z\bar{u}\right)$

$$\begin{aligned} \bar{u}(y, z, t) &= U(z, t) \sin ly \\ \psi'(x, y, z, t) &= \text{Re}\{\Psi(z, t)e^{ikx}\}e^{z/2H} \sin ly \end{aligned}$$

 **coupled equations for  $U(z, t)$  and  $\Psi(z, t)$**



# Ruzmaikin et al. (2003) model

⇒ coarsely discretize HM76 in  $z$  (using 3 levels) and substitute  $\Psi = X + iY$  to obtain 3 coupled equations for  $X(t)$ ,  $Y(t)$ ,  $U(t)$  at mid-height:

$$\dot{X} = -\alpha_1 X - rY + sUY - \xi h$$

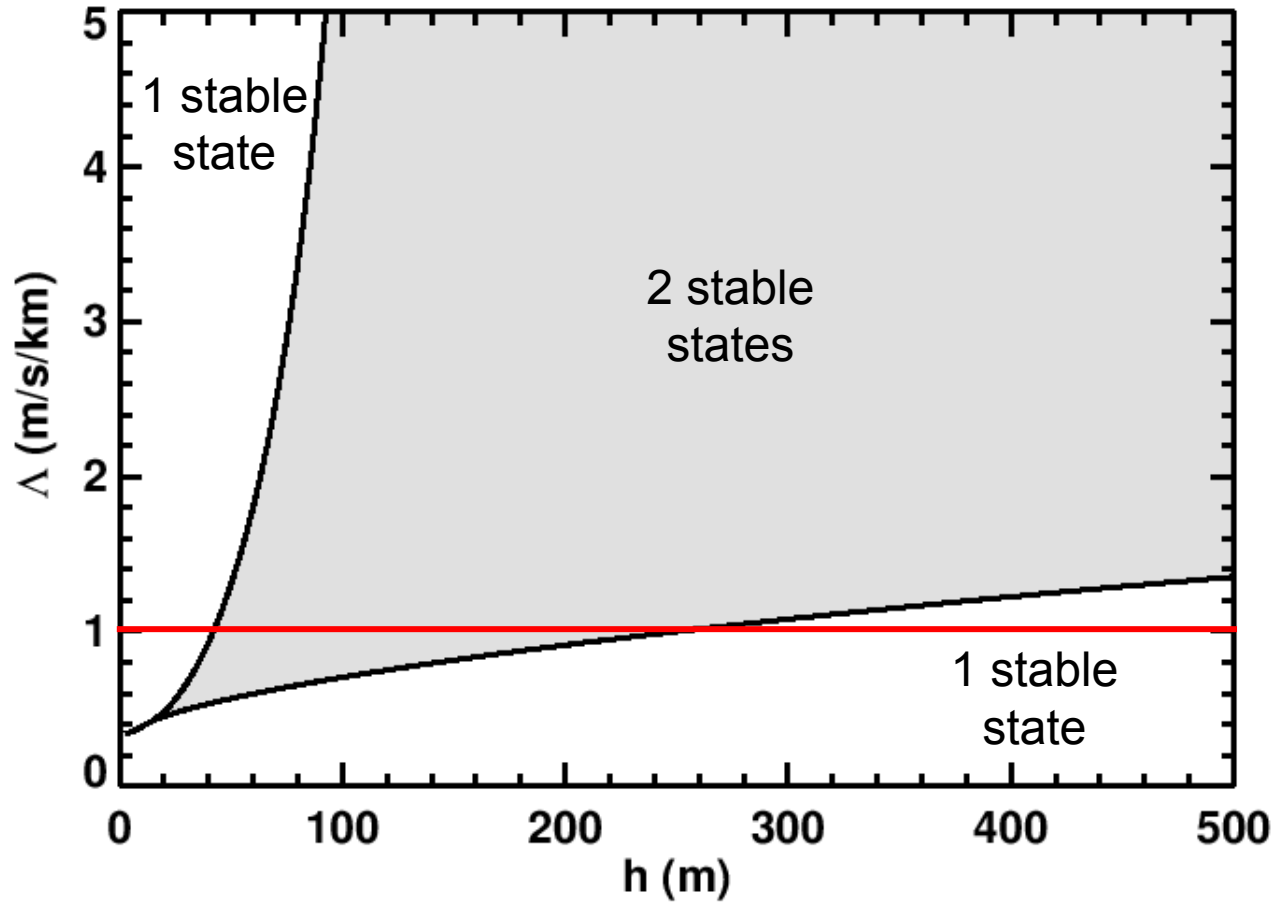
$$\dot{Y} = -\alpha_1 Y + rX - sUX + \zeta hU$$

$$\dot{U} = -\alpha_2(U - U_R) - \eta hY$$

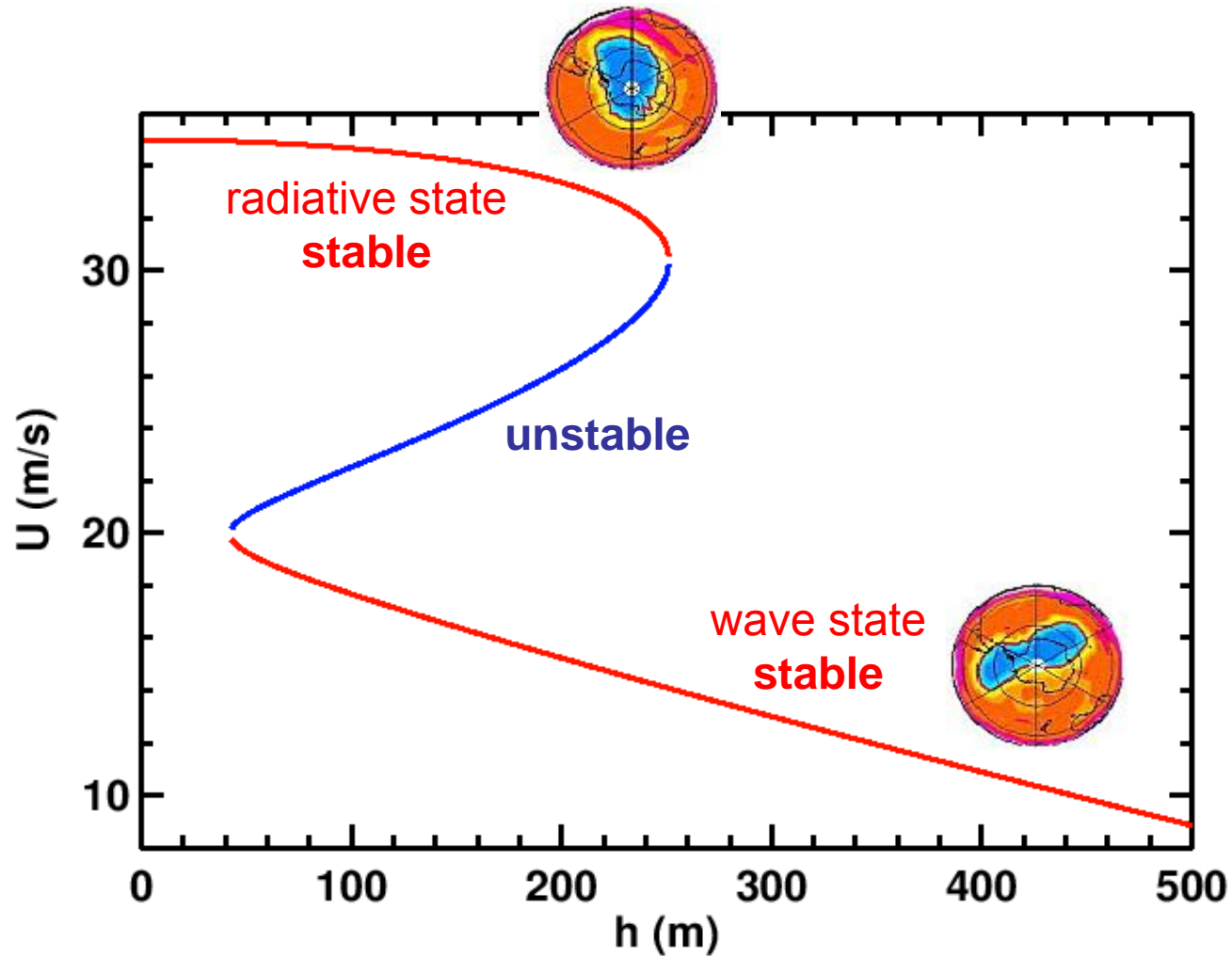
where  $h$  = planetary wave forcing (geopotential height perturbation at tropopause)

$\Lambda$  = vertical shear of radiative equilibrium flow =  $U_R / \Delta z$

# Regime diagram



# Equilibrium solutions for $\Lambda = 1 \text{ m/s/km}$



# Unresolved processes

- The atmosphere exhibits small-scale variability, e.g. induced by gravity wave momentum fluxes that are neither captured in our simple model nor in GCMs (in the latter they are of course parameterized to some extent).
- Since the gravity wave field is highly variable, conventional deterministic parameterizations are likely to be inadequate, suggesting the need for a stochastic approach.
- A natural way to represent gravity wave drag is to introduce an additive noise term to the right-hand side of the evolution equation for  $U$ ...

# Ruzmaikin et al. (2003) + noise

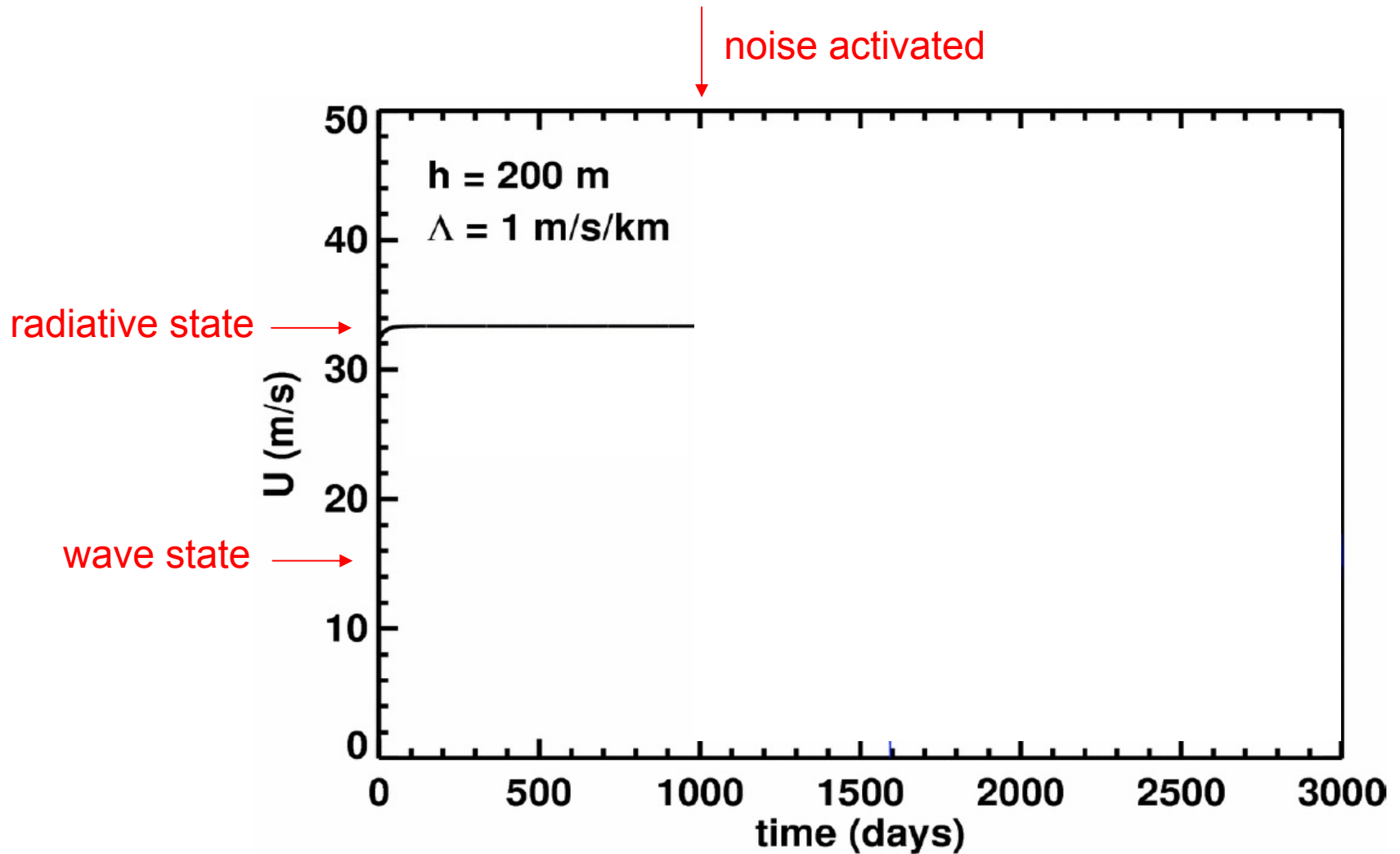
$$\dot{X} = -\alpha_1 X - rY + sUY - \xi h$$

$$\dot{Y} = -\alpha_1 Y + rX - sUX + \zeta hU$$

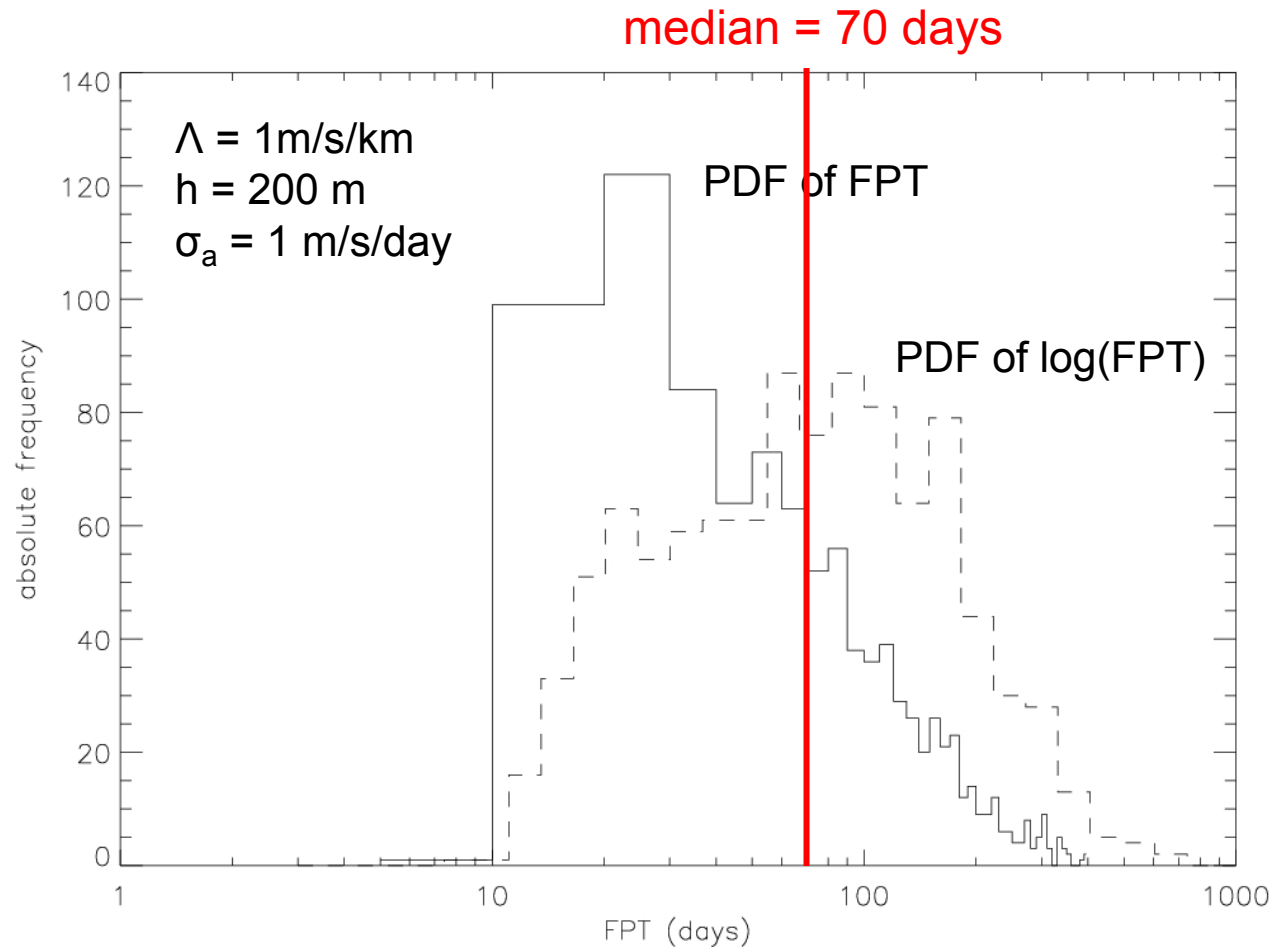
$$\dot{U} = -\alpha_2(U - U_R) - \eta hY + \chi_a$$

Gaussian white noise:  $\overline{\chi_a(t)\chi_a(t')} = \sigma_a^2 \delta(t - t')$

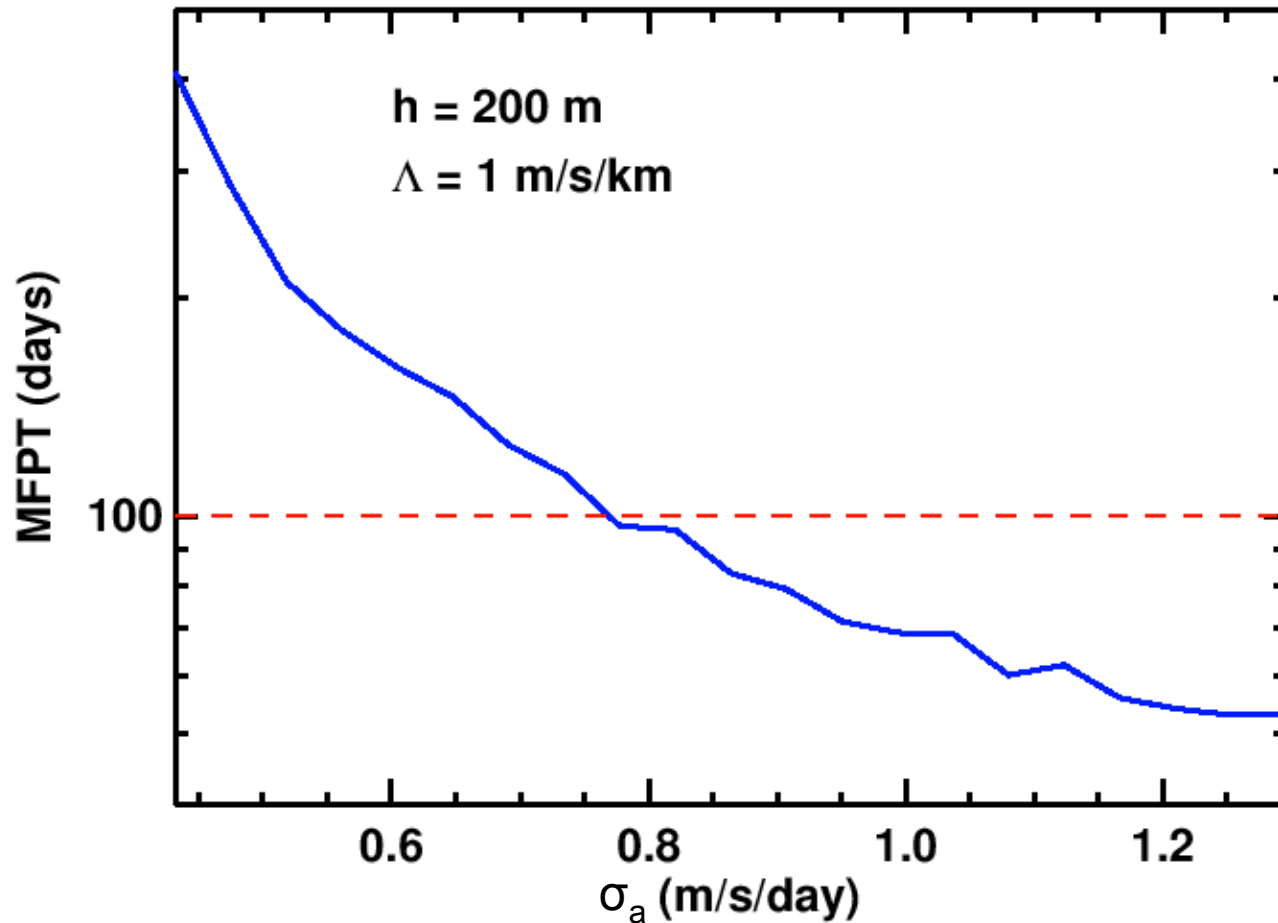
# Typical solution for $U(t)$



# Distribution of First Passage Times



# Median First Passage Time (MFPT)





# Fokker-Planck equation

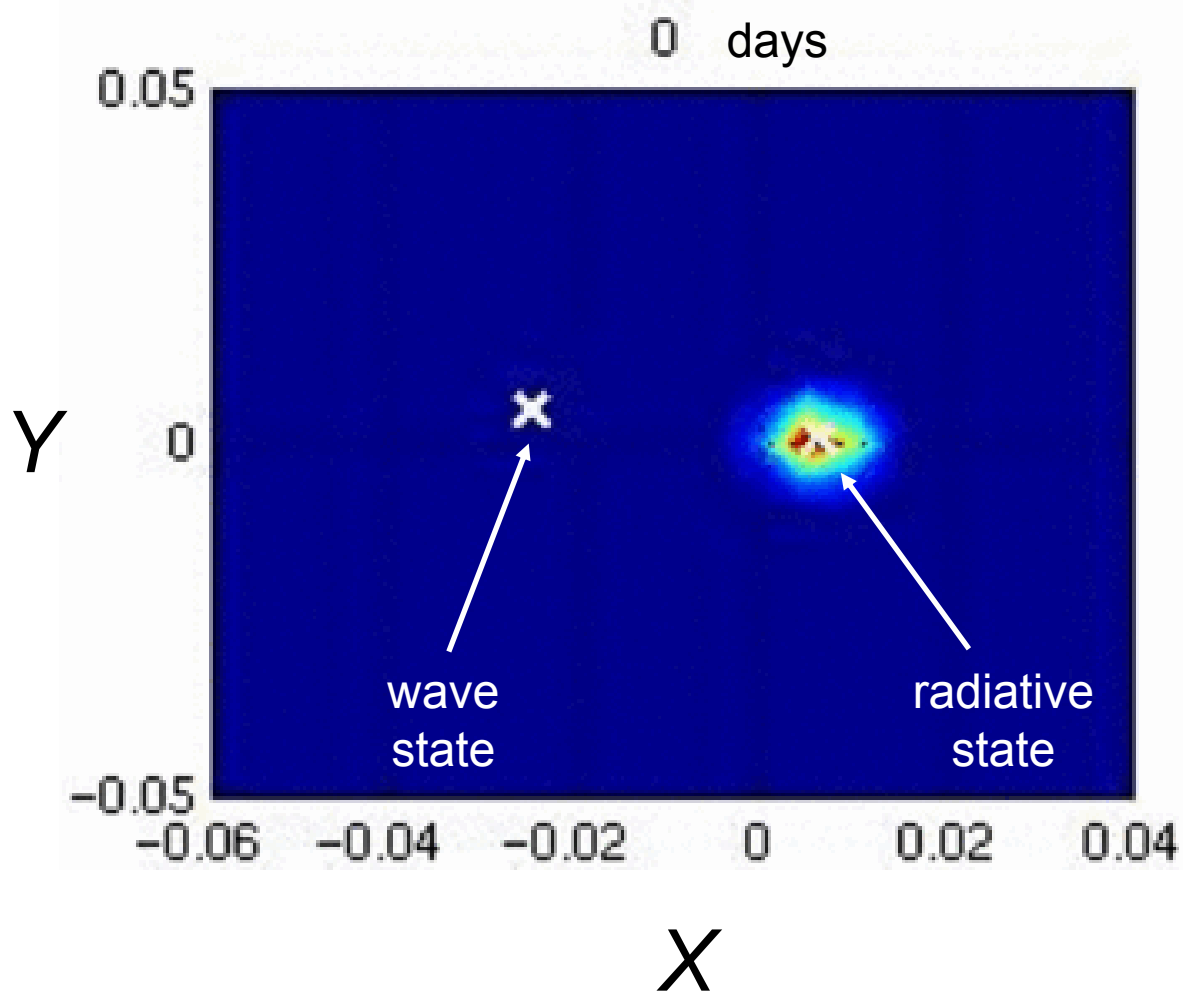
For a system governed by  $\frac{d\mathbf{x}}{dt} = \mathbf{A}(\mathbf{x}) + \mathbf{B}(\mathbf{x})\boldsymbol{\eta}^M + \boldsymbol{\eta}^A$

the F-P equation is

$$\begin{aligned} & \frac{\partial p(\mathbf{x}, t)}{\partial t} \\ &= -\sum_i \frac{\partial}{\partial x_i} \left[ A_i + \alpha \sum_{j,k} (\sigma_j^M)^2 \left( \frac{\partial}{\partial x_j} B_{ik} \right) B_{jk} \right] p(\mathbf{x}, t) \\ &+ \frac{1}{2} \sum_{i,j} (\sigma_j^M)^2 \frac{\partial^2}{\partial x_i \partial x_j} (\mathbf{B}\mathbf{B}^T)_{ij} p(\mathbf{x}, t) \\ &+ \frac{1}{2} \sum_i (\sigma_i^A)^2 \frac{\partial^2}{\partial x_i^2} p(\mathbf{x}, t), \end{aligned}$$

(e.g. Sura, 2002; Sura et al., 2005)

Evolution of  $\overline{p(\mathbf{x}, t)}^U$  when  $\sigma_a = 3$  m/s/day



# SSW case study: conclusions

- gravity wave **'noise'-induced regime transitions** occur in laboratory fluid flows
- **polar vortex splits** may also have a possible interpretation as gravity wave **'noise'-induced transitions**
- such transitions are **unlikely to be captured** by deterministic gravity wave drag parameterisations in GCMs
- motivates **stochastic parameterisation**

**PHILOSOPHICAL  
TRANSACTIONS**  
— OF —  
THE ROYAL  
SOCIETY **A**



*Stochastic Physics and Climate Modelling*

Tim Palmer and Paul Williams (eds.)

coming summer 2008