

# Dynamic Evolution of Globular Clusters



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# Outline

- **Globular Clusters Conditions:**
  - **multiple stellar populations, a shift of paradigm**
- **Thermodynamics to the rescue:**
  - **Evolution on the two-body relaxation timescale**
- **Primordial Binaries**
- **Mass Segregation**

# Globular Clusters

The picture before  $\approx 2007$

— Compact stellar systems

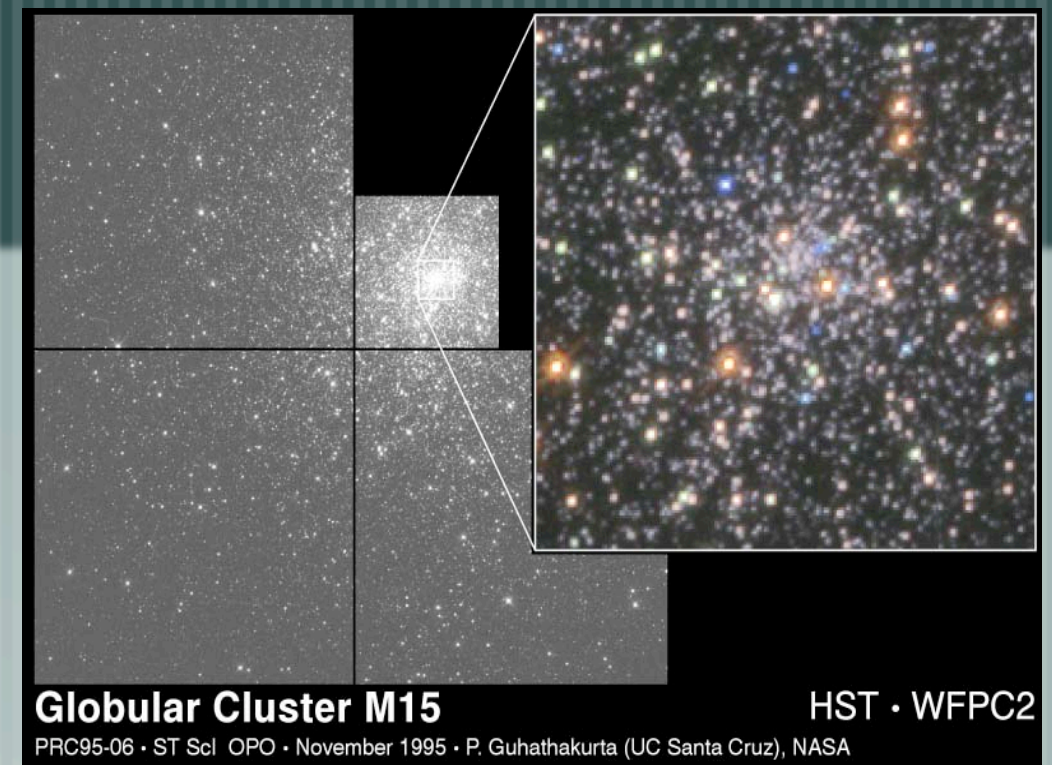
—  $\approx 10^5$ - $10^6$  old stars

— high concentration: typical dimension of a few pc

— Live in and around galaxies

— Simple stellar population

— Uniform age & chemical composition





# Globular Clusters

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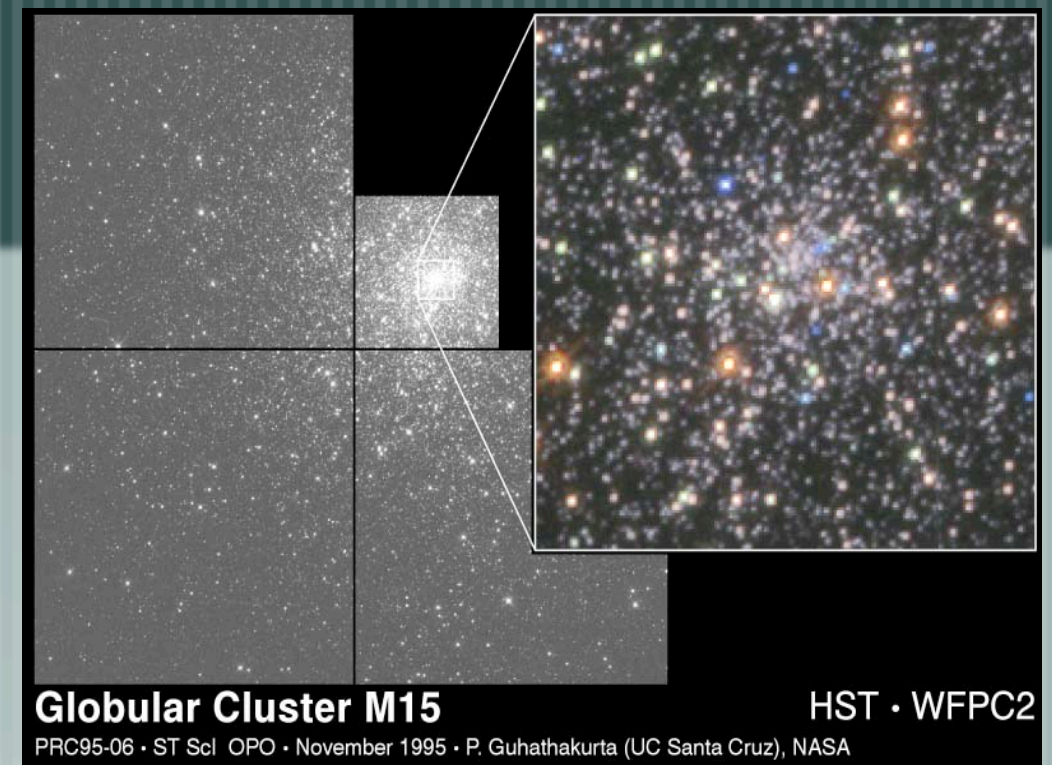
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# Globular Clusters

*The picture today*

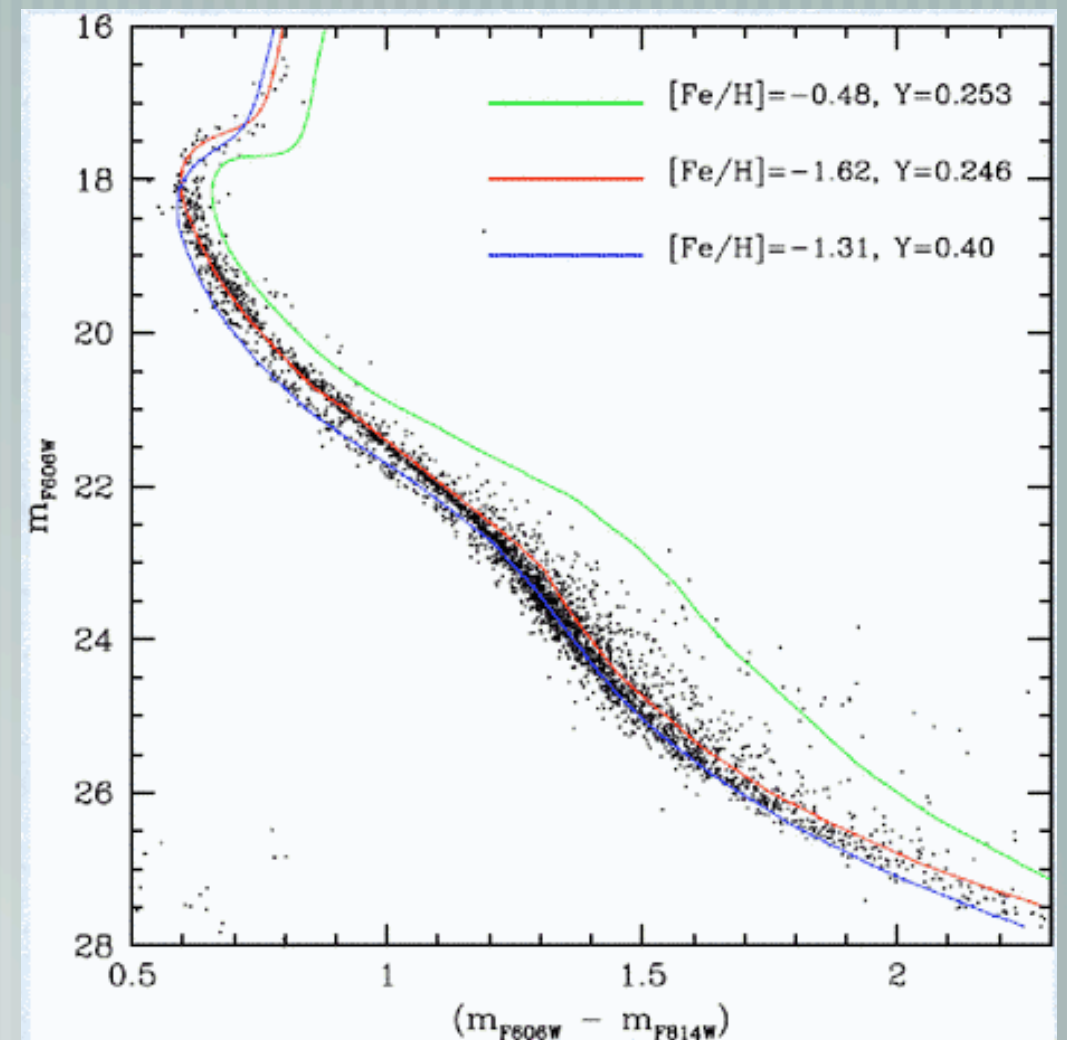
GCs have Multiple Stellar Populations

They imply different helium abundance

Can be explained with a complex dynamic formation history

Very significant mass loss in the first generation (Vesperini et al. 2008)

## Omega Cen



Piotto 2009 KITP conference

# Globular Clusters: long term evolution

- Evolution on the two-body relaxation timescale ( $\sim 10^9$  yr for globulars)

- Details of initial conditions are erased

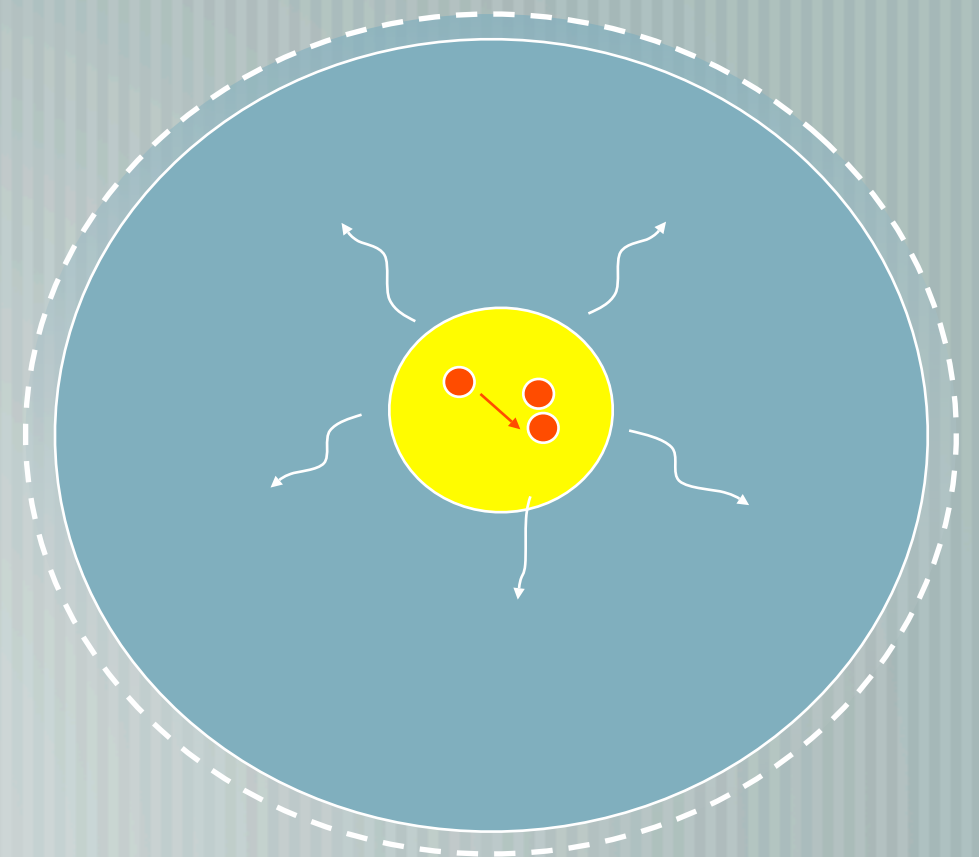
- Energy flux generated in the core through gravitational encounters

- Equilibrium established:

- core flux is equal to half mass radius flux

- this fuels global expansion

*Thermodynamics to the rescue*



# Our Modeling

- Direct N-body simulations with Aarseth's NBODY6:
  - NO softening
  - Exact treatment of all strong interactions (KS+chain regularization)
  - Up to  $N=32768$  for the results here; 64K&128K currently running on Lincoln
- Large Grid of Initial Conditions/Runs (embarrassingly parallel)
  - “Late Time” Mass function, Primordial Binary Fraction, Tidal Field, Concentration, central IMBH
- Runs carried out until tidal dissolution (typically  $>15 t_{rh}$ )

# The classical core collapse

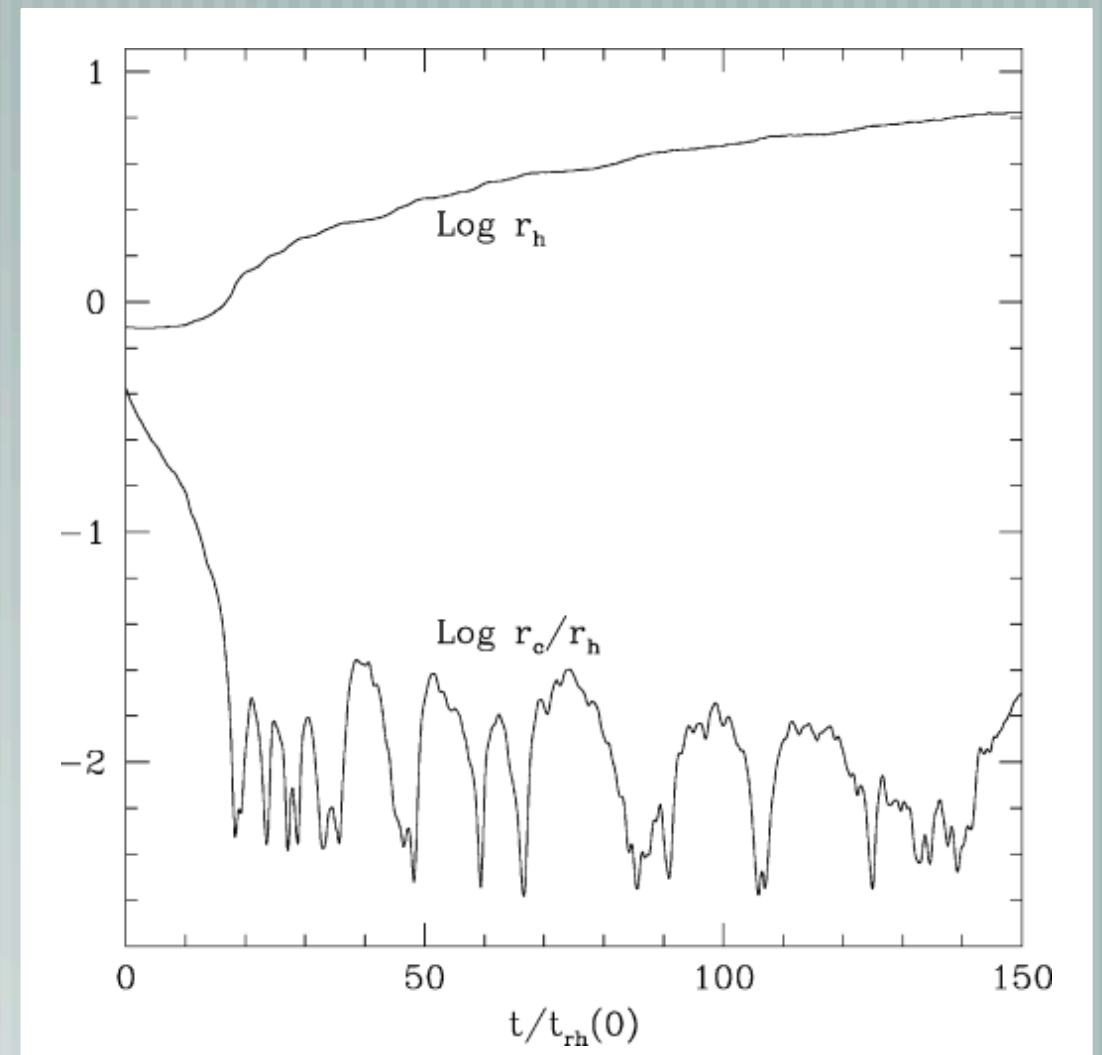
- Direct N-body simulations

- single stars only, equal mass

- core collapse (negative specific heat)

- 3-body binaries formed

- gravothermal oscillations + cluster expansion



Heggie, Trenti & Hut (2006)



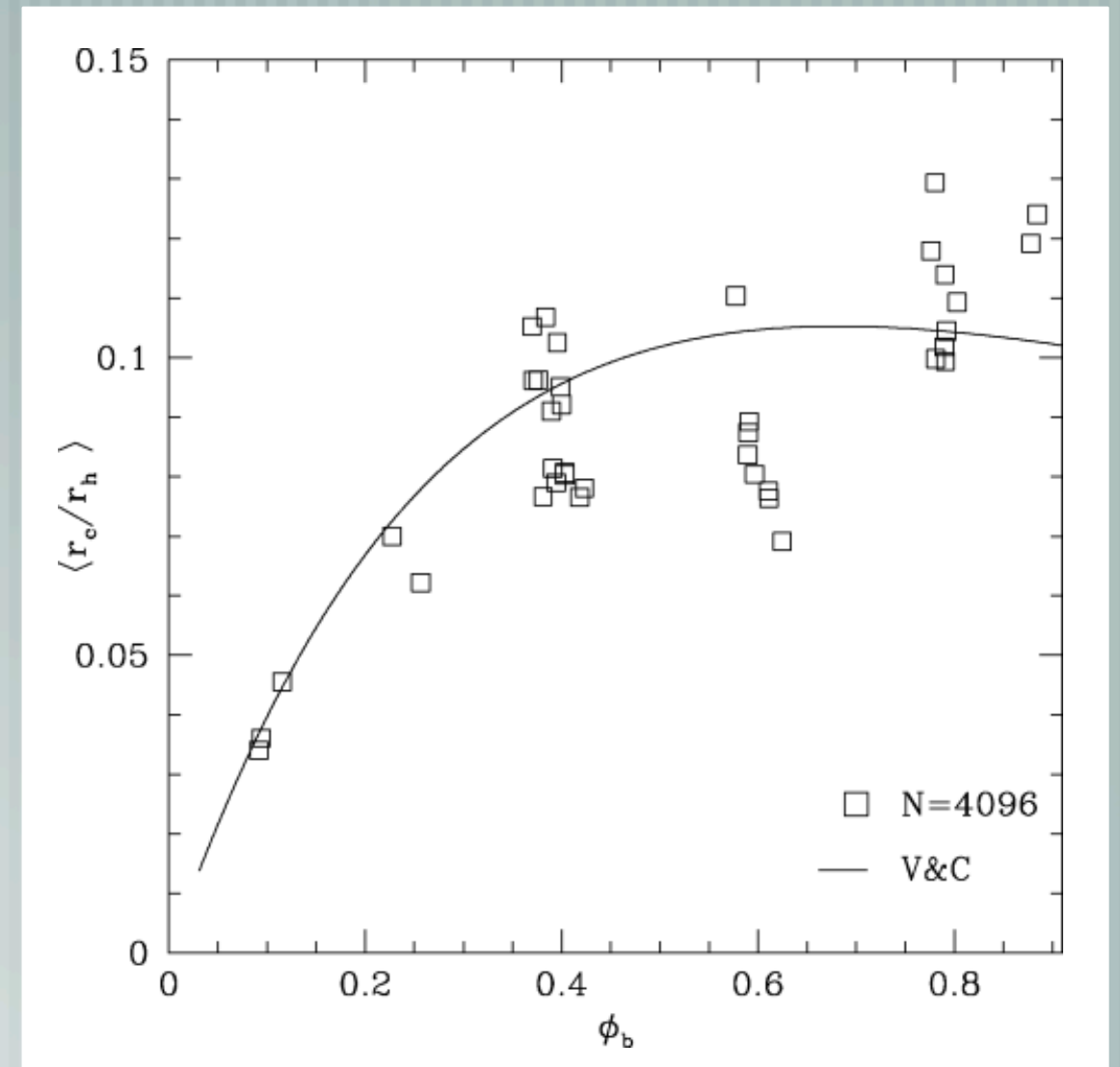
# Core size & Thermodynamics

— Vesperini & Chernoff (1994) model:  
core size with central energy source  
(binaries)

— Initial core size does not affect  
the model

— Excellent match to idealized  
simulations (equal mass,  
isolated, Plummer ICs)

— Saturation of binaries  
efficiency



Heggie, Trenti & Hut (2006)

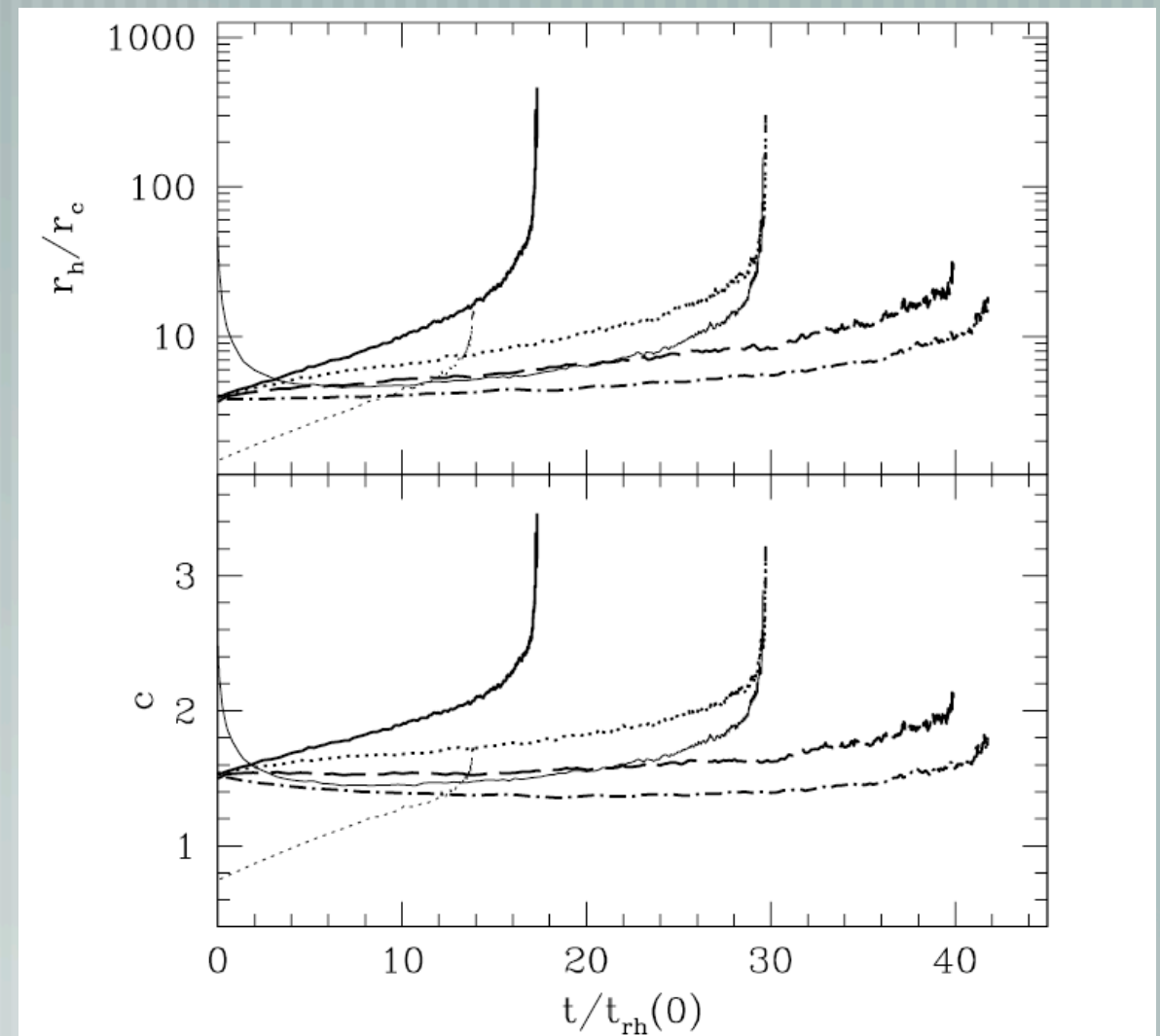
# Core size & Thermodynamics

Fregeau et al. (2003):

Initial conditions appear important!

Different binary fractions and tidal fields lead to a different evolutionary history

(Monte Carlo code based)



Fregeau et al. (2003)

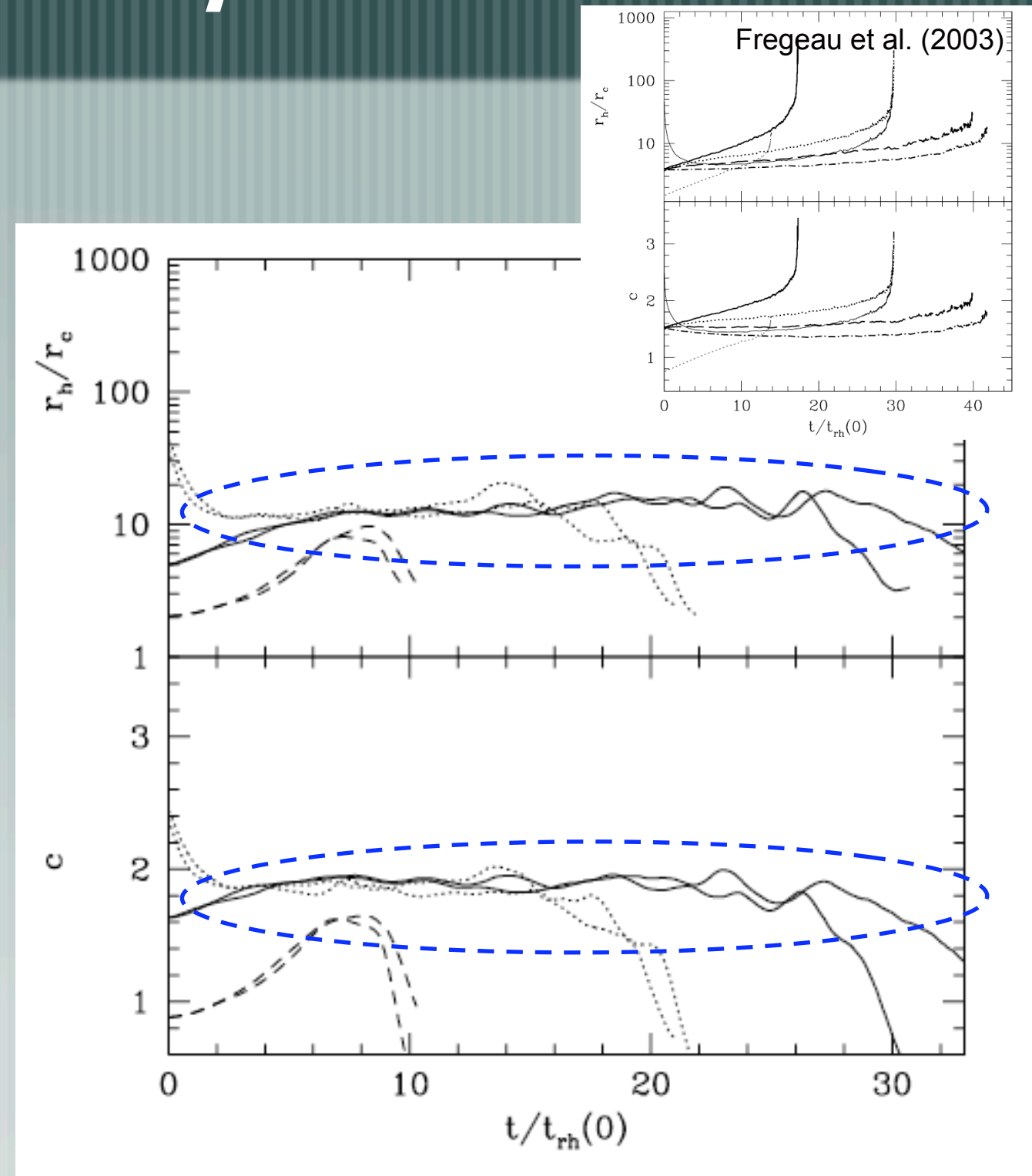
# Core size & Thermodynamics

The direct N-body point of view:

Different ICs evolve toward universal  $r_c/r_h$  and concentration until shortly before tidal dissolution

Fully consistent with theoretical expectation from thermodynamic

(MC code by Fregeau & Rasio (2007) has improved agreement with direct integration)



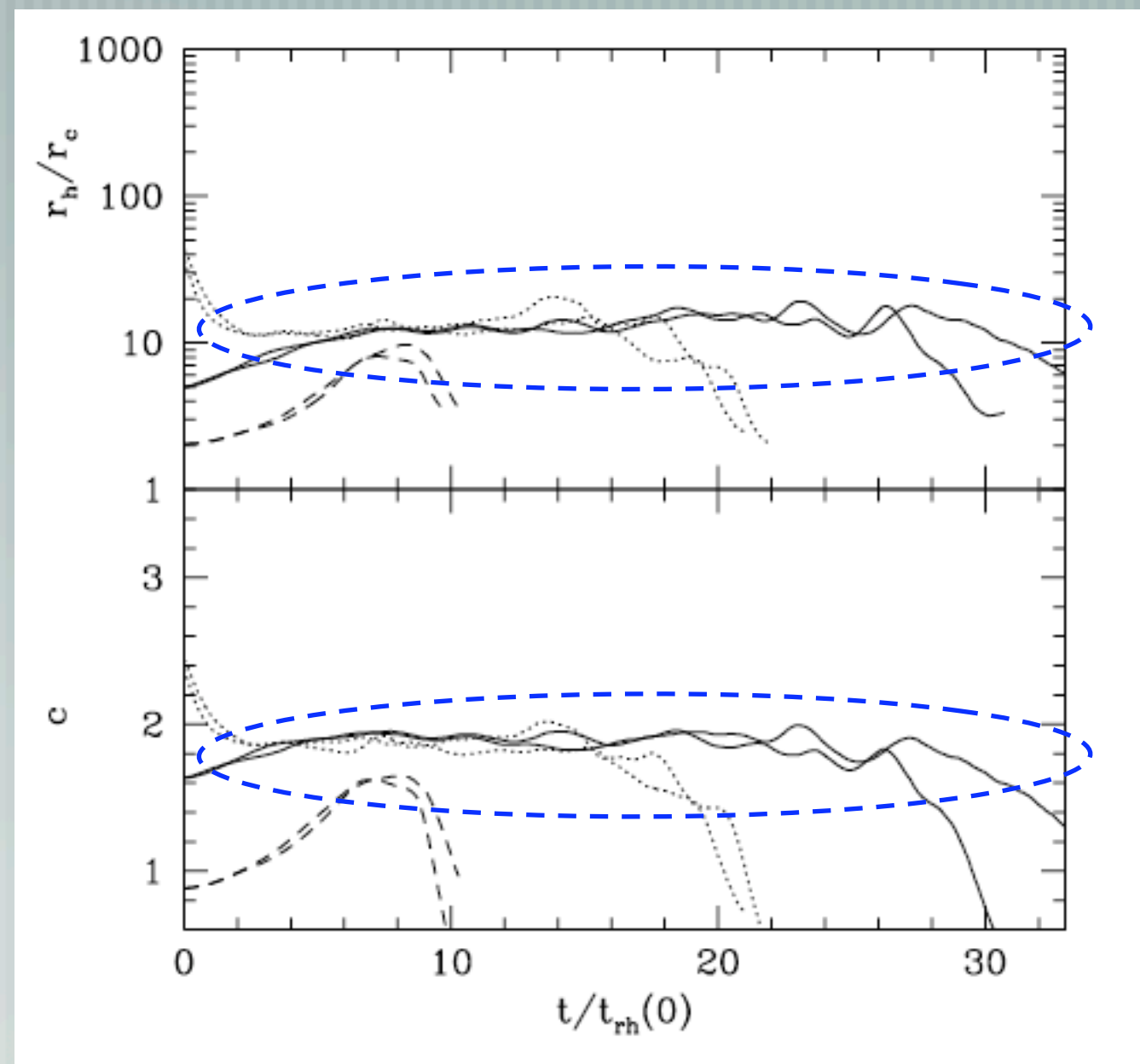
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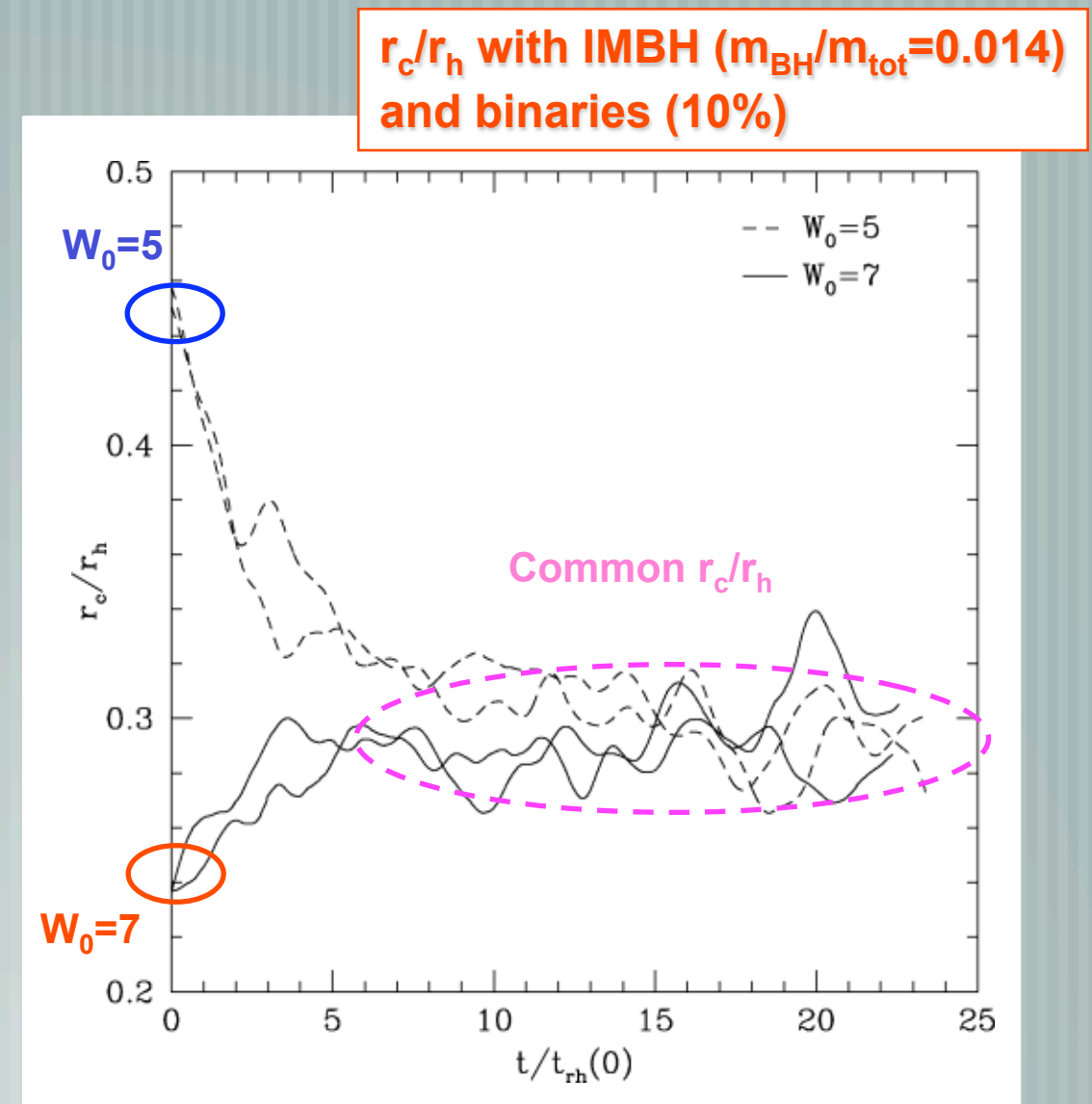
# More universal evolution: IMBH runs

Efficient IMBH heating leads to

Universal large  $r_c/r_h$  after a few relaxation times

There are other efficient heating sources besides binaries & IMBHs

Stellar evolution (Hurley 07),  
WD kicks (Fregeau et al. 09),  
Stellar collisions (Chatterjee et al. 09),  
Stellar BHs (Mackey et al. 08)



Trenti et al. (2007)

# Formation of triples

— Dynamical interactions lead to triple formation

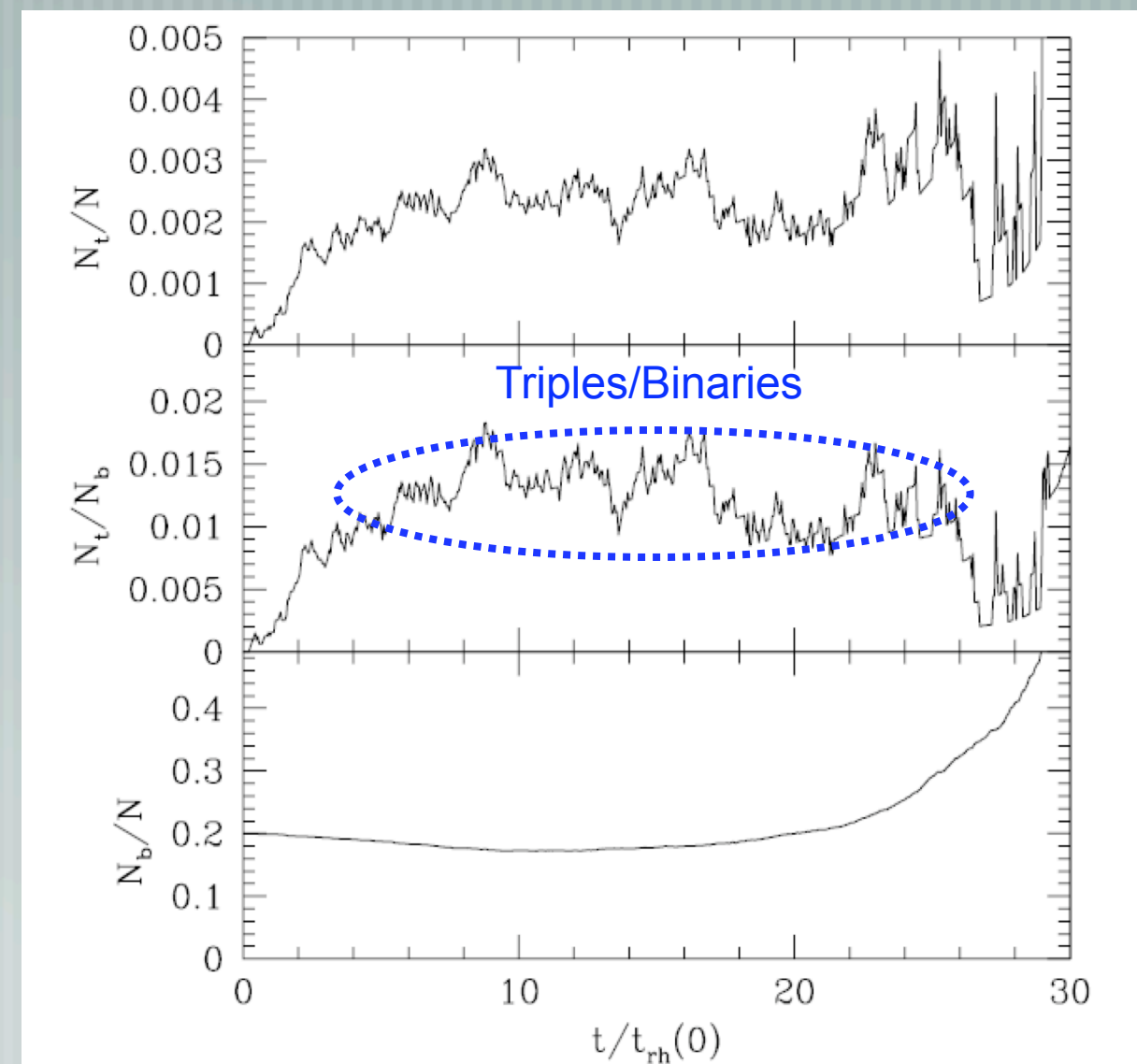
— binary-binary at lowest order

— Within a few relaxation times a steady state is attained

— Triple fraction proportional to binary fraction

— About 1%

**Binaries and triples fraction**



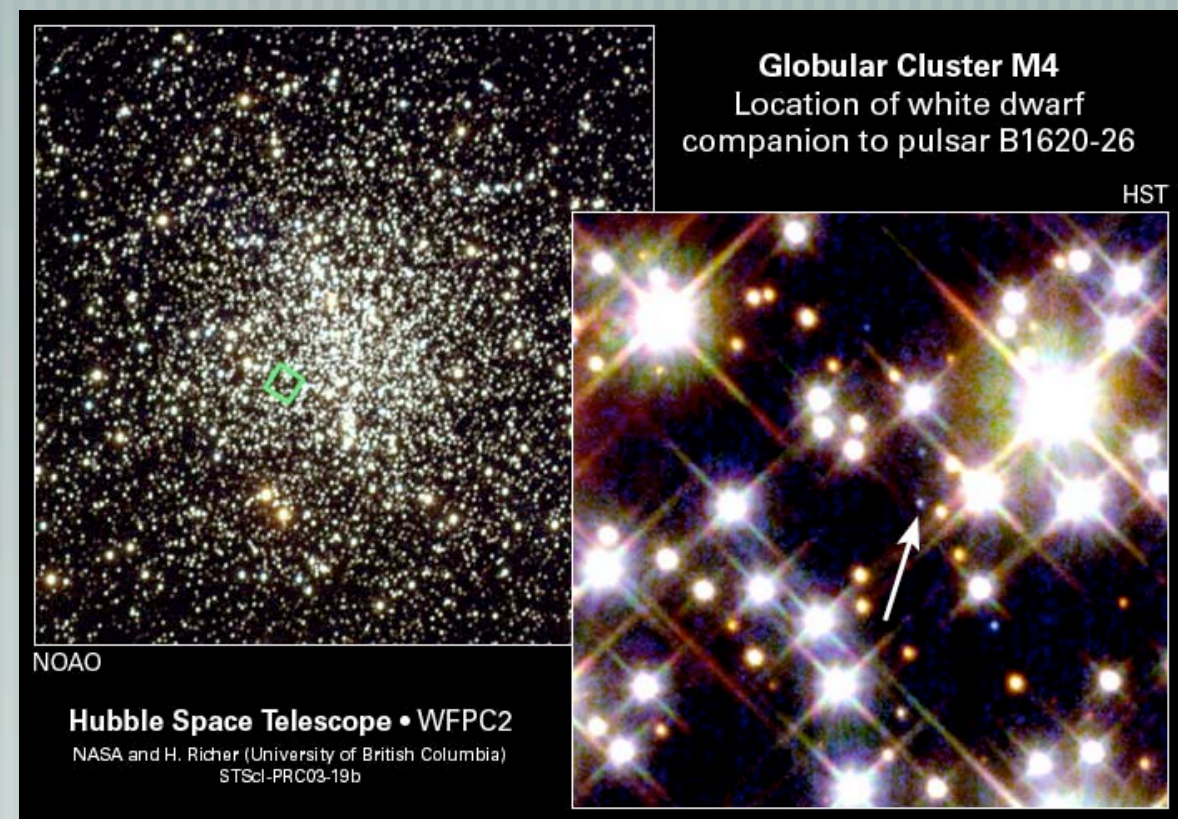
# Speculations on triples and planets

— We know about 100 pulsar binaries in GCs

—  $O(1)$  pulsar triple expected from our simulations

— B1620-26 is a pulsar triple with a  $2.5 M_{\text{Jupiter}}$  planet at  $\sim 20$  AU

— \*If\* the planet was dynamically captured, then planets in clusters are as common as stars!



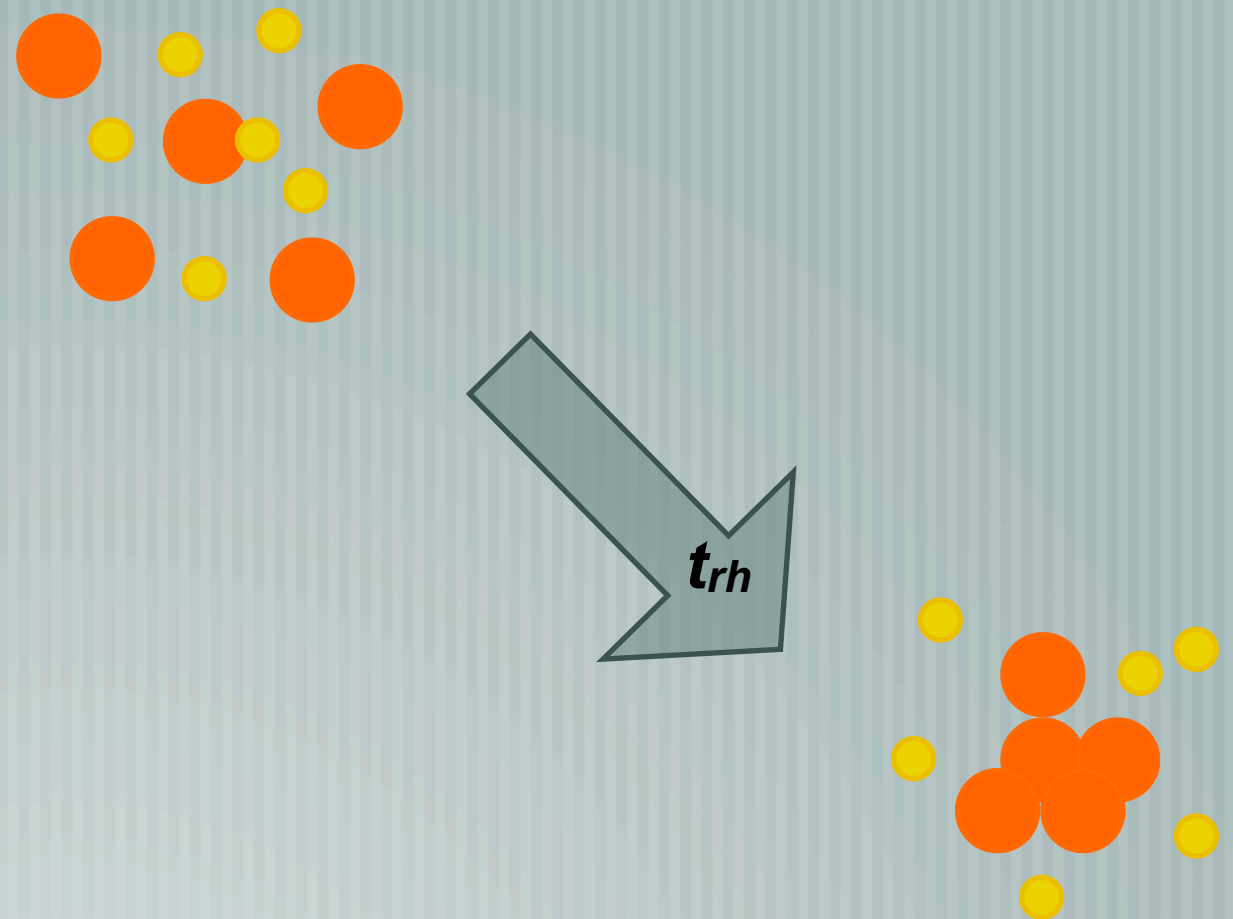
# Thermodynamics & Mass segregation

— In a GC the most massive stars segregate toward the center of the system (energy equipartition)

— Can we predict it?

— Does it depend on the initial conditions?

— How can we measure mass segregation?





# Measuring Mass Segregation

$$\Delta\langle m \rangle = \langle m(r = 0) \rangle - \langle m(r = r_h) \rangle$$

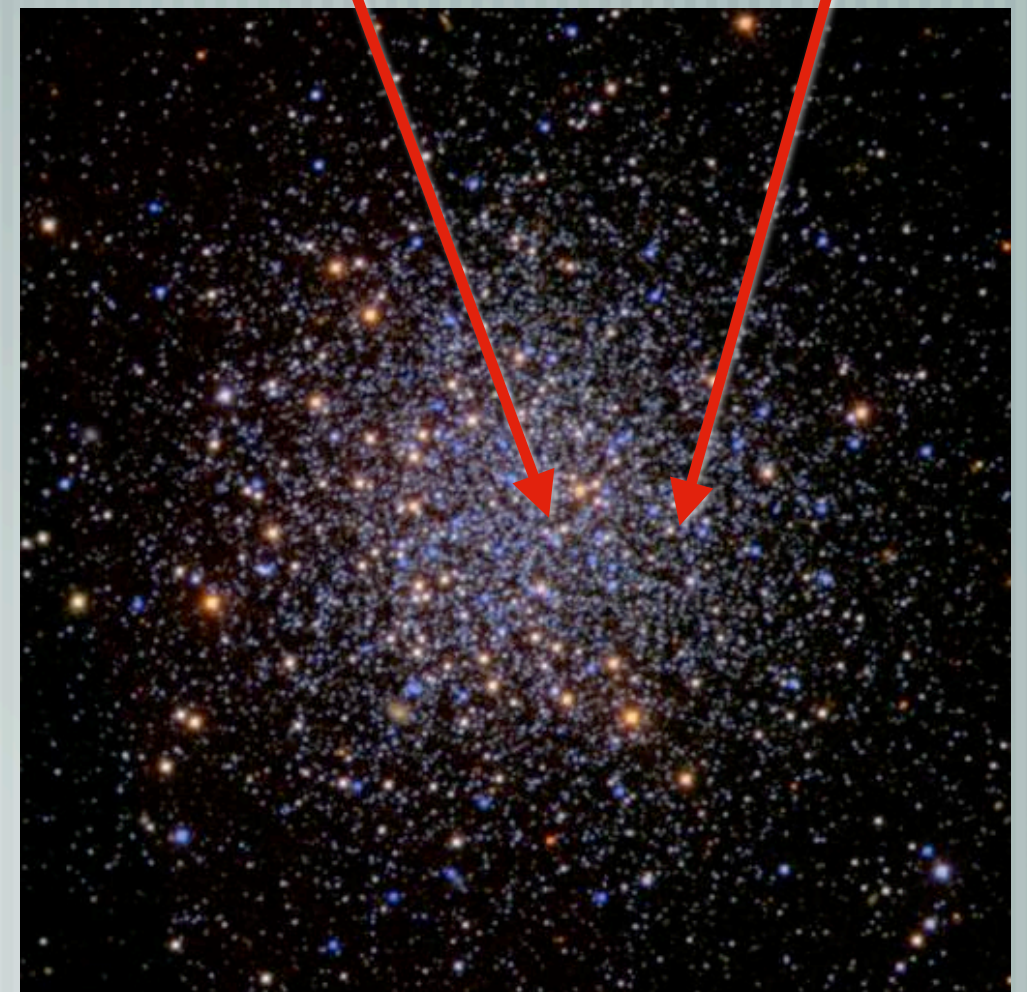
— Mass Segregation  $\Delta\langle m \rangle$  is measured as the difference in average main sequence mass between the center and the half mass radius

— Differential measure:

— erases dependence on the IMF

— Mass not light based:

— less sensitive to fluctuations due to small number of giant stars



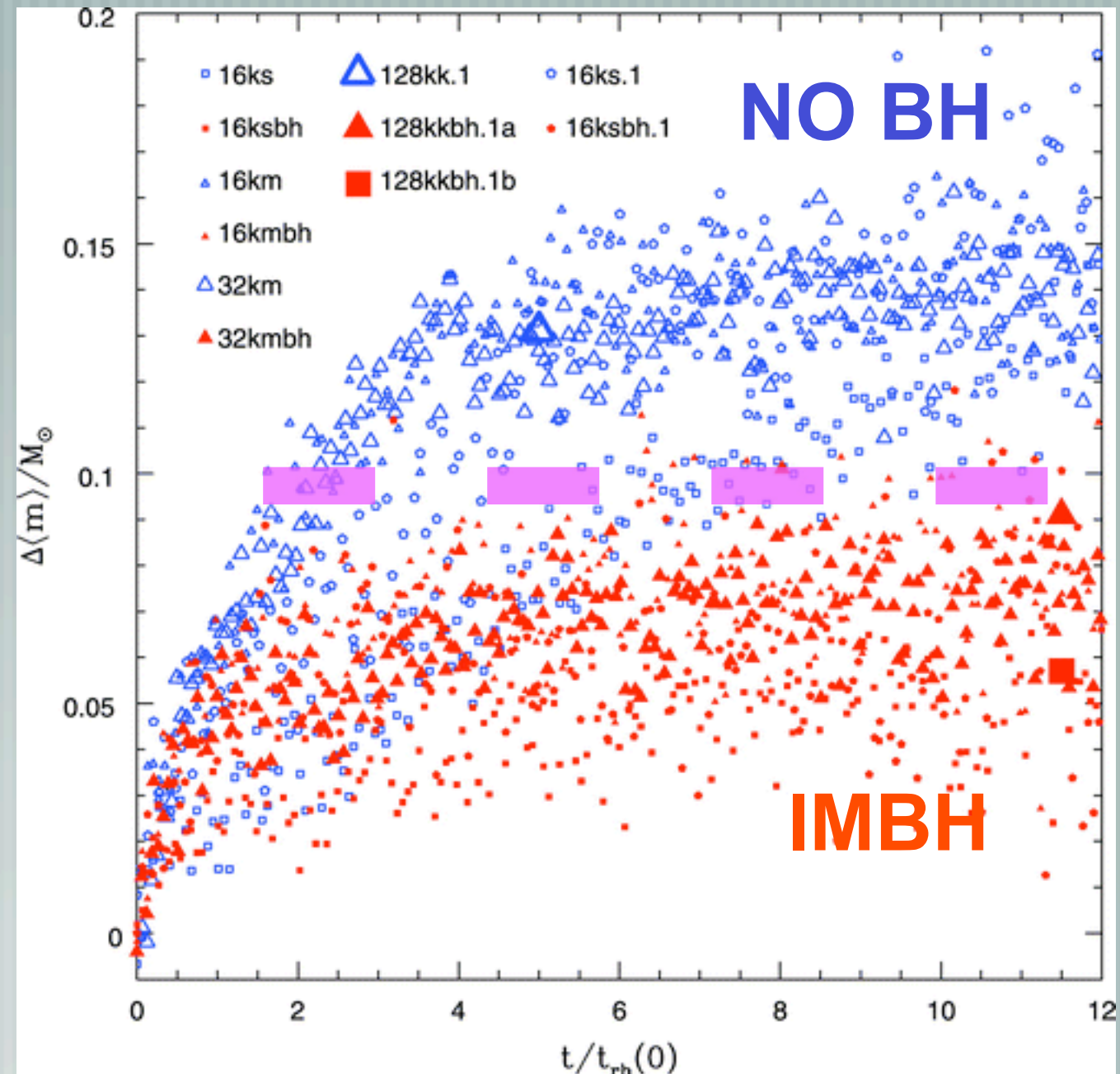
# Mass Segregation Results: Simulations

Simulations start with no mass segregation

After about 5 relaxation times **equilibrium** value of mass segregation is reached

Quasi-universal amount of mass segregation

(Good separation of runs with and without an IMBH)





# Comparison with NGC2298

## Cluster properties

$$t_{\text{rh}} = 10^{8.41} \text{ yr}$$

$$r_h = 49''$$

$$M_{\text{tot}} = 3 \times 10^4 \text{ Msun}$$

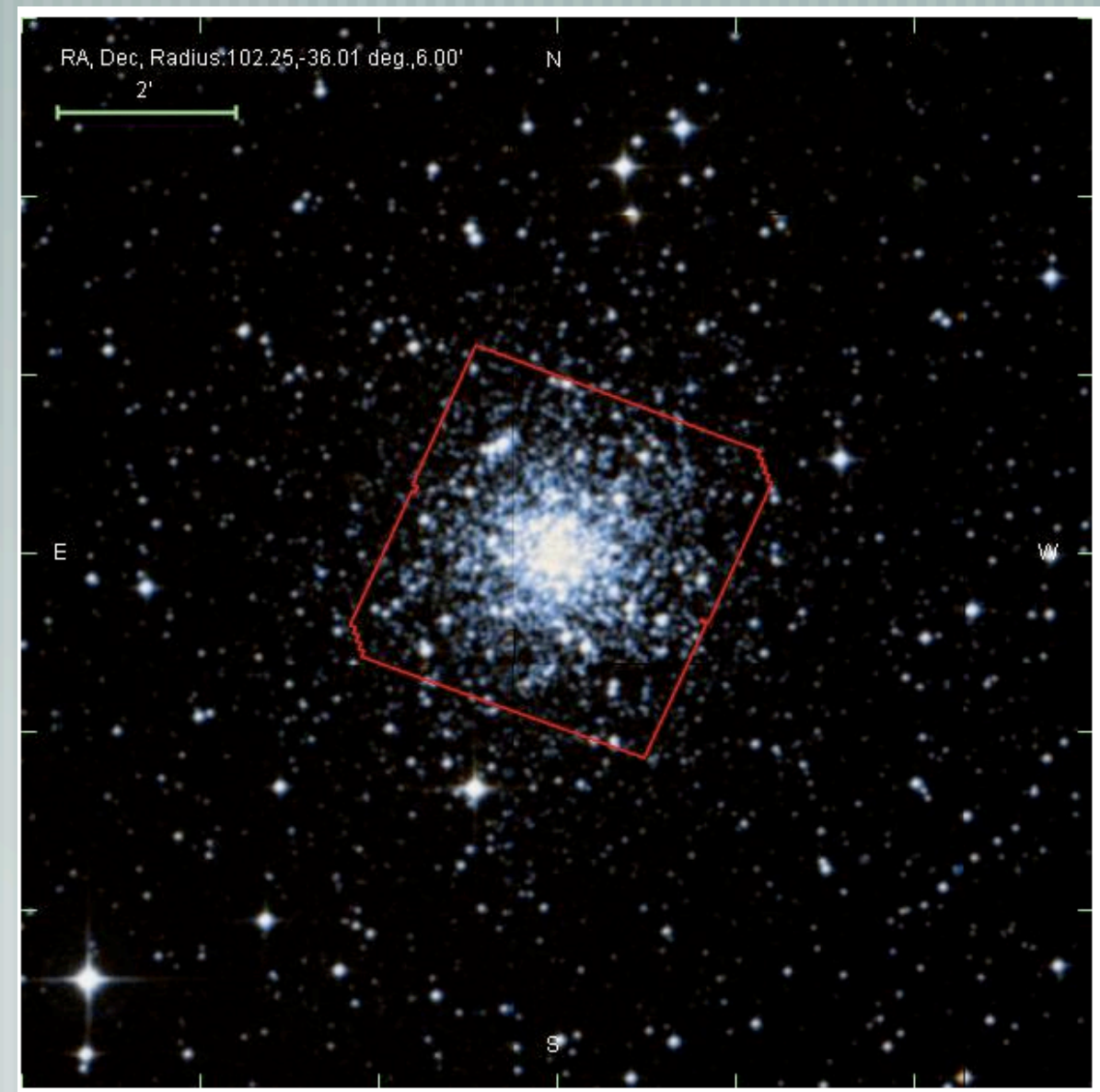
Data Reduction: DeMarchi & Pulone (2007)

HST-ACS WFC F606W & F814W

$10\sigma$  limit @  $m_{606}=26.5$ ,  $m_{814}=25.0$

$>50\%$  completeness @  $0.2 \text{ Msun}$

## NGC 2298



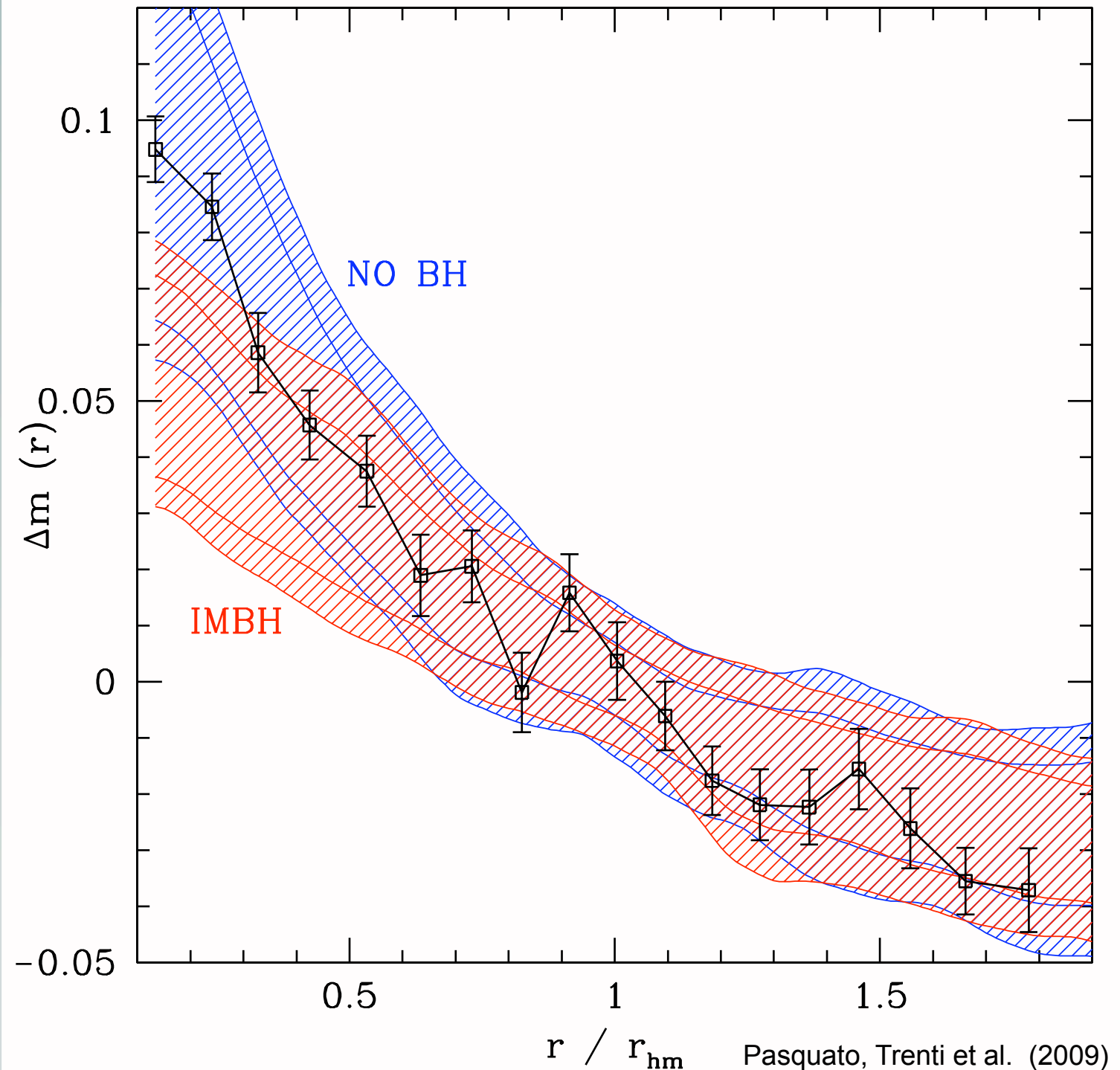
# NGC2298: comparison with simulations

Predicted quasi universal profile of mass segregation

Observed mass segregation profile is matched very well by simulations

Cluster is too segregated to be likely to host an IMBH

(Formal limit from the inner two points:  $>300M_{\text{sun}}$  BH excluded at  $3\sigma$  CL)





# Mass Segregation: testing the predictions

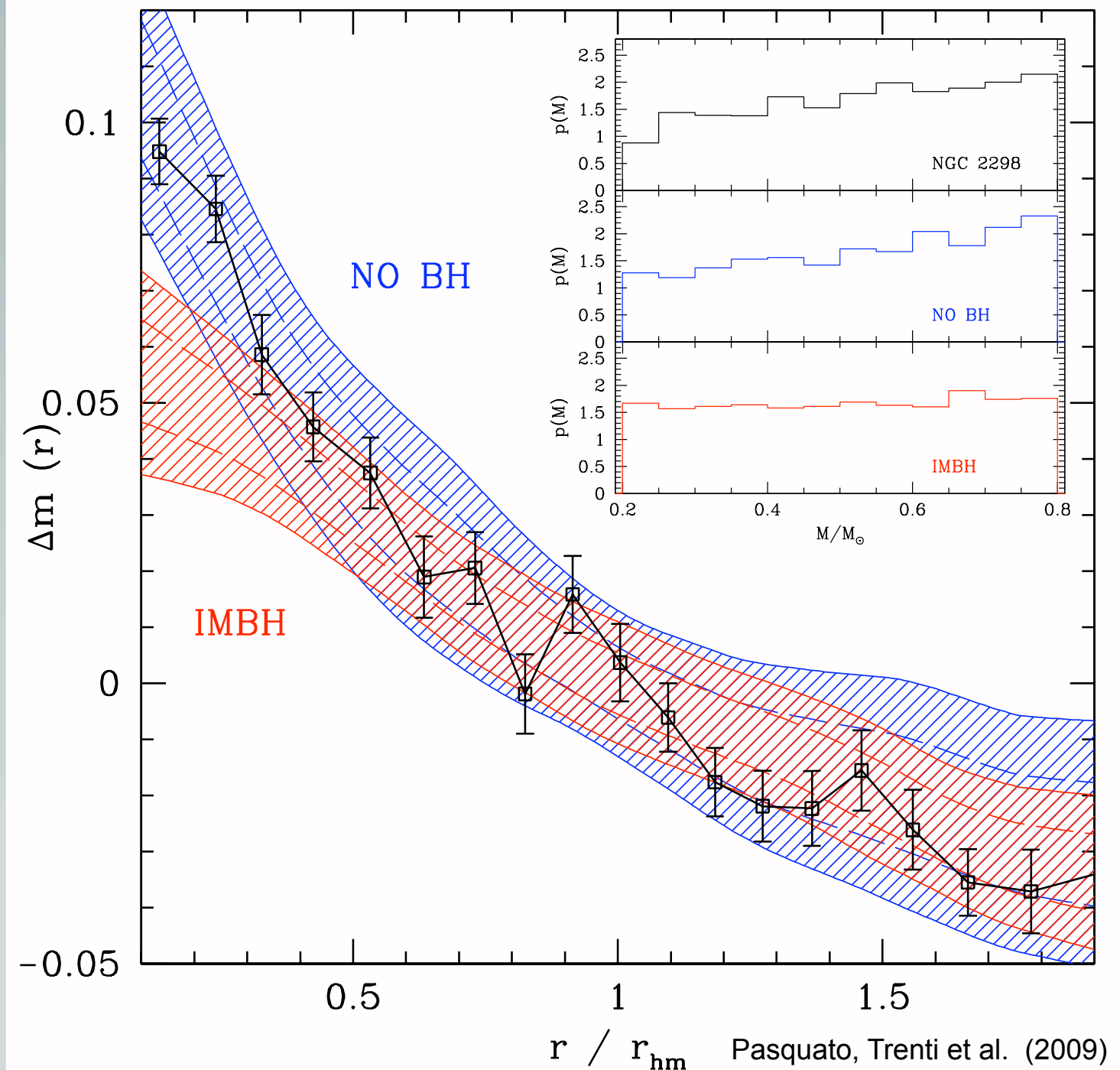
NGC2298 has a peculiar mass function (very deficient in low mass stars)

We match the *\*global\** observed mass function & mass segregation profile if we:

start with a Miller&Scalo IMF

wait until 75% of mass is lost

Excellent data-model match!



# Summary

- GCs had a complicated infancy
  - multiple stellar populations, primordial mass segregation, mass loss
- But the late time collisional evolution of GCs is insensitive to the details of ICs
  - Expected universal behavior of global properties of the system
- Successful data-model comparison:
  - NGC 2298 star counts follow the predicted universal mass segregation profile

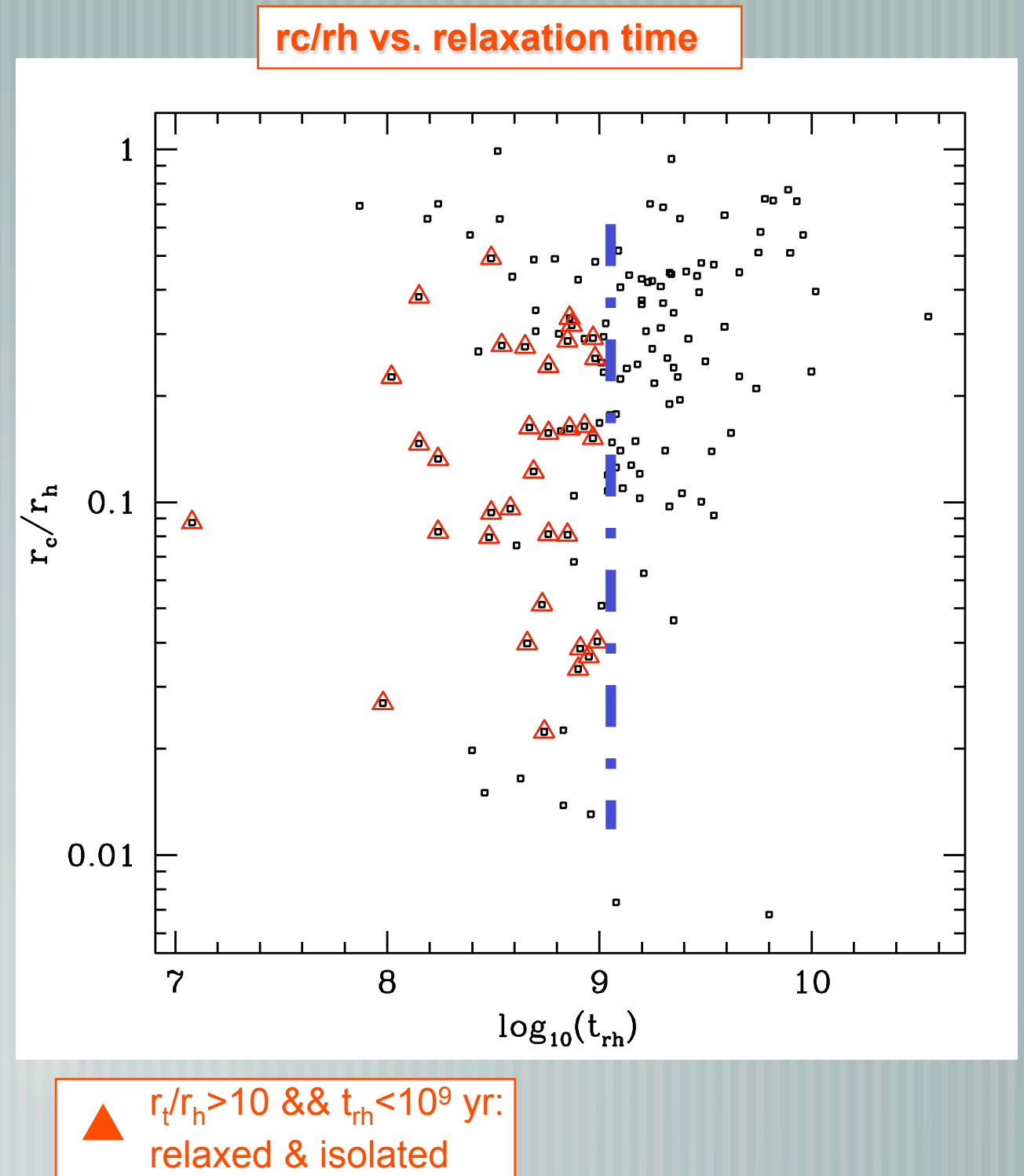
# Observed $r_c/r_h$ : any information?

Observed  $r_c/r_h$  should carry information on the core energy production for relaxed GCs

Harris catalog is based on integrated light profiles, possibly very uncertain

We should define structural parameters on star counts

And construct light-based predictions for simulations



# The future

- Larger sample of simulations:  
toward Heggie's Challenge

- NBODY-6 OpenMP/GPU code  
on NCSA Lincoln cluster

- Improved statistics, wider  
sampling of initial conditions,  
larger N (64K & 128K)

- HST data for star counts  
comparison are available in the  
archive for about 15 relaxed  
clusters





# NGC2298: Error budget

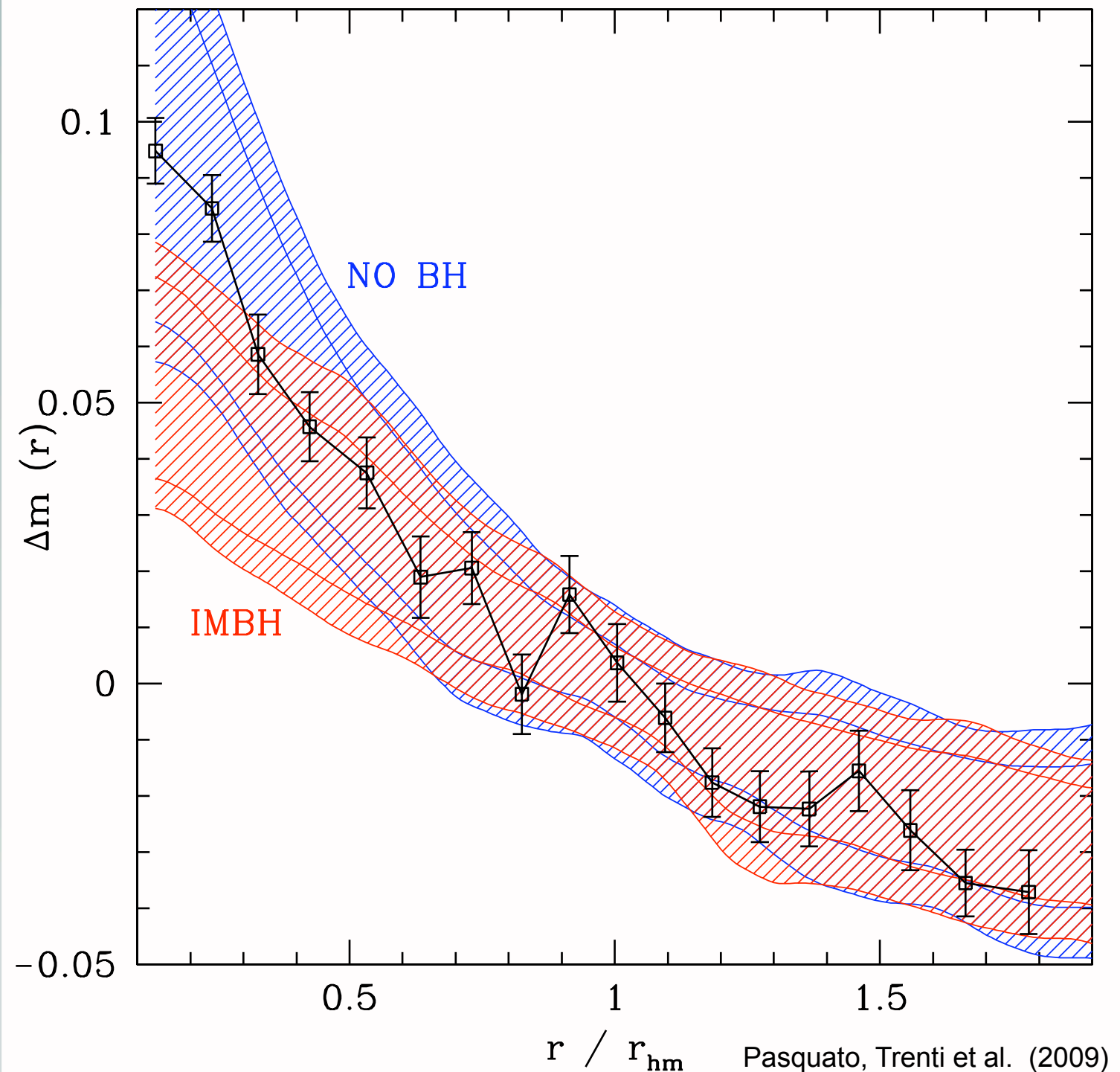
Poisson errors have been estimated by bootstrap (100 synthetic catalogs)

Possible systematic errors from determination of

Half mass radius. Even a  $\pm 4''$  mis-determination only shifts by less than  $1\sigma$  Poisson error

Center. We use mass, not light based measure, more stable:  $[0.4''$  uncertainty at  $1\sigma]$

Miscentering only increases BH rejection confidence level



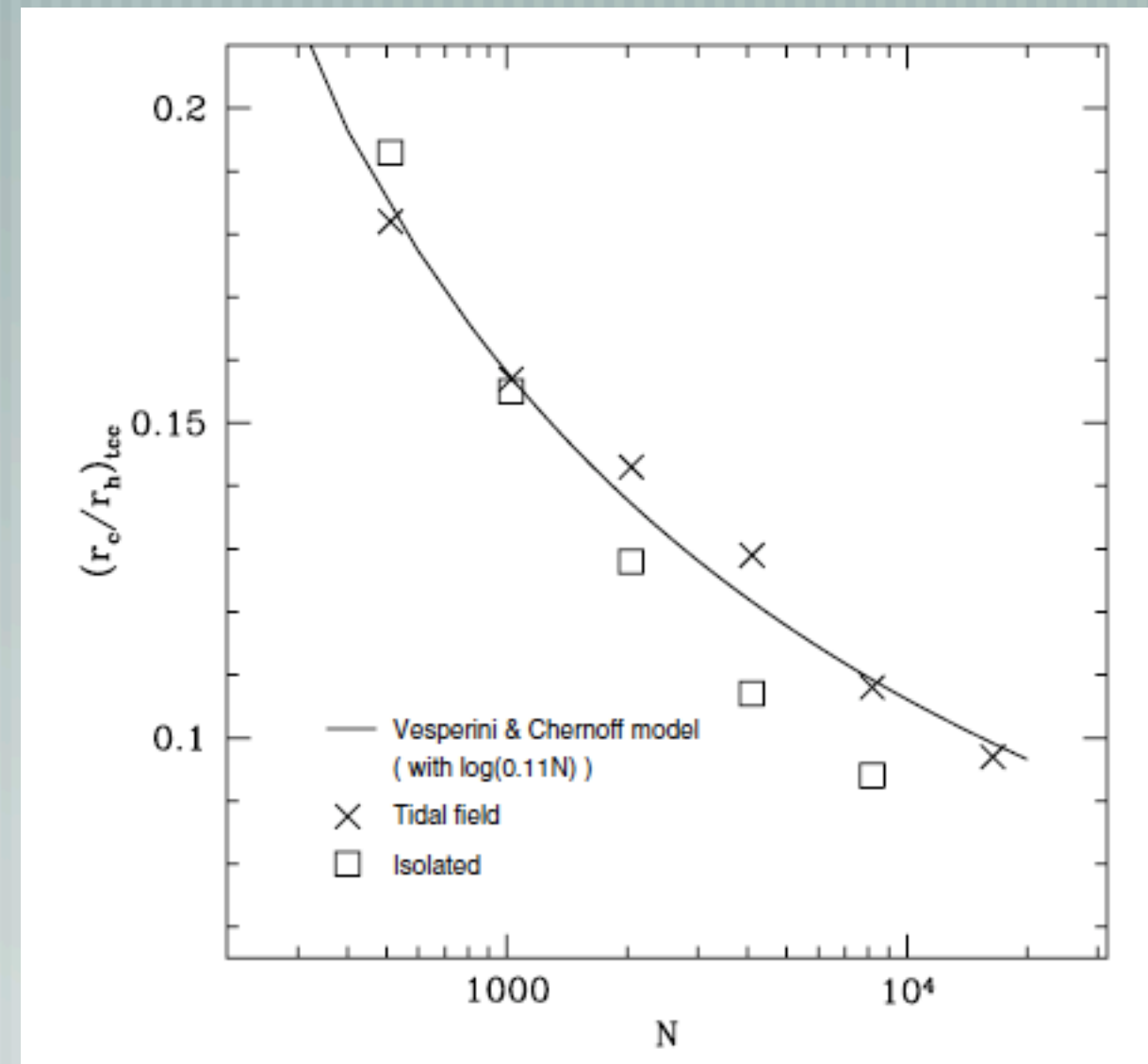
# Core size & Thermodynamics

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model: core size with central  
energy source (binaries)

— Initial core size does not  
affect the model

— Core size depends on  $N$

— Excellent match to  
simulations results



Trenti, Heggie & Hut (2007)

# Quenching of mass segregation

A Cartoon Picture

— IMBH quickly gains at least one tightly bound massive star:

— A super-scatter machine is born!

— Three body encounters with the BH scatter out incoming stars independently of their mass

— no strong dependence on BH mass  
expected or seen in simulations when  
 $m_{\text{BH}} \gg m_{\text{star}}$

— random walk of the IMBH within the core:  
loss cone is constantly replenished, high  
rate of interactions over time

