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# Dynamical Models of the Globular Clusters M4 and NGC 6397

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# Outline

## Introduction:

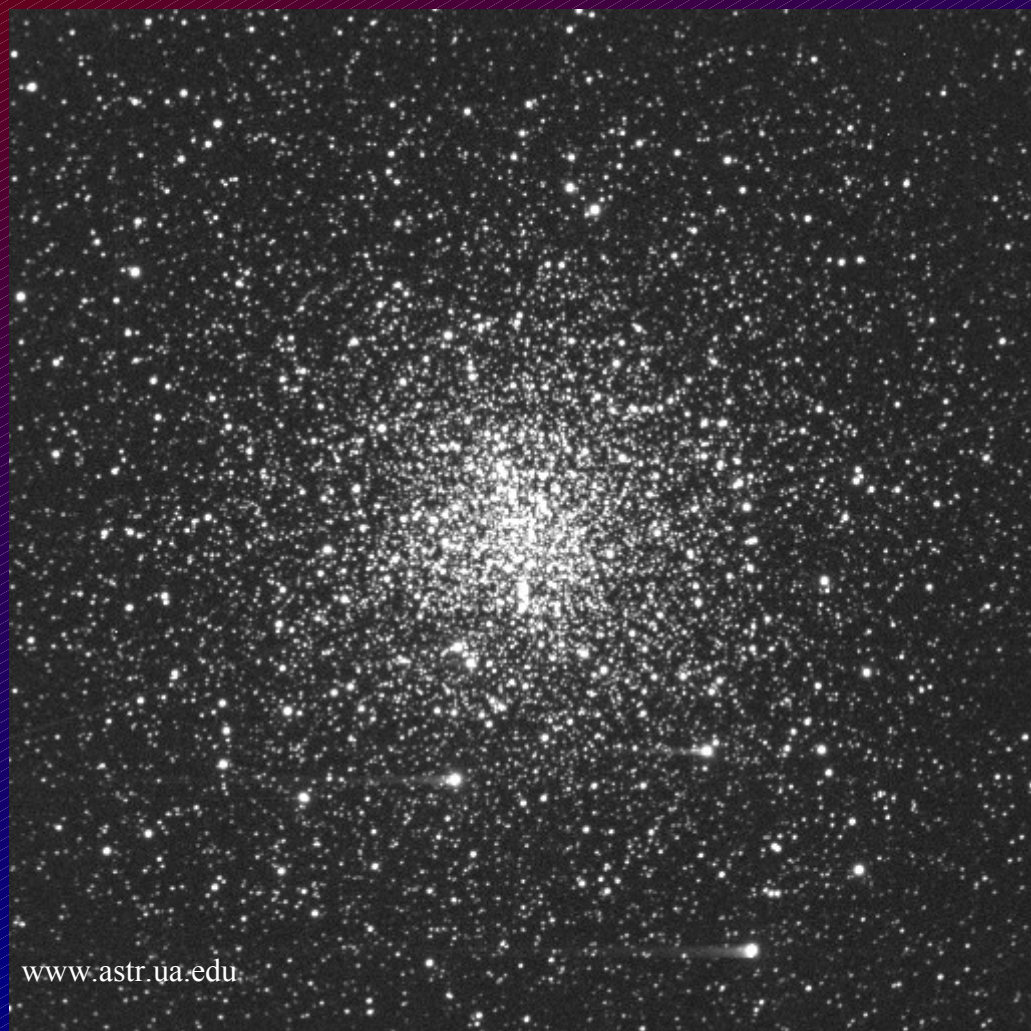
- M4 and NGC 6397
- modelling globular clusters
- surface brightness profiles

## What shapes the surface brightness profile?

- core collapse
- binaries
- intermediate-mass black holes
- stellar-mass black holes
- accidents

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# Two nearby galactic globular clusters



M4



NGC 6397

# Modelling globular clusters

## 1. Static (non-evolving) models

- Example: King's model

*[something like a generalized isothermal model of a star]*

## 2. Dynamic (evolutionary) models

- Example A:  $N$ -body models

*but globular clusters are/were too big*

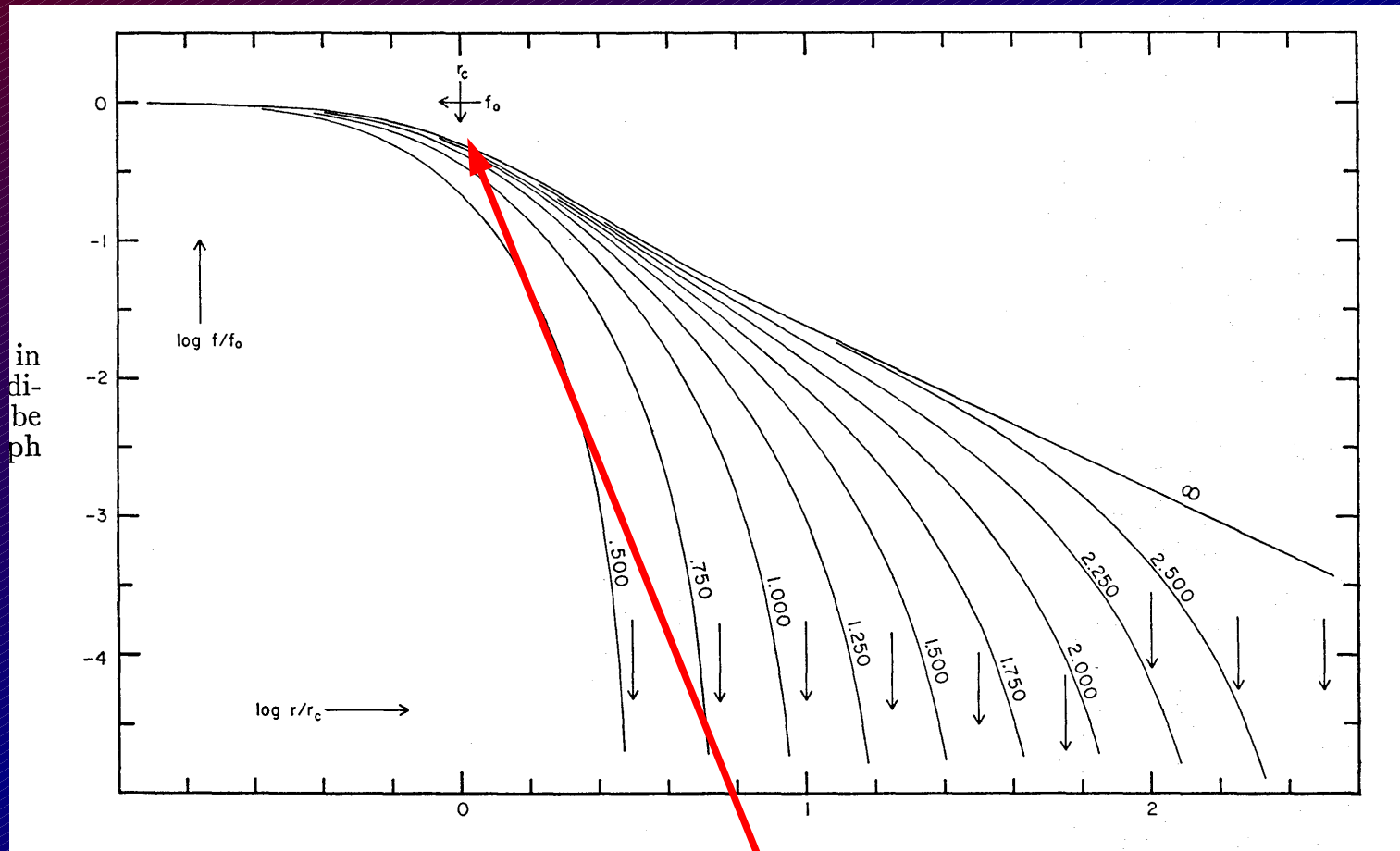
- Example B: Monte Carlo models (**this talk**)

(i) *Similar level of detail as  $N$ -body models*

(ii) *More assumptions than  $N$ -body models, e.g. spherical symmetry.*

# King models

Surface brightness



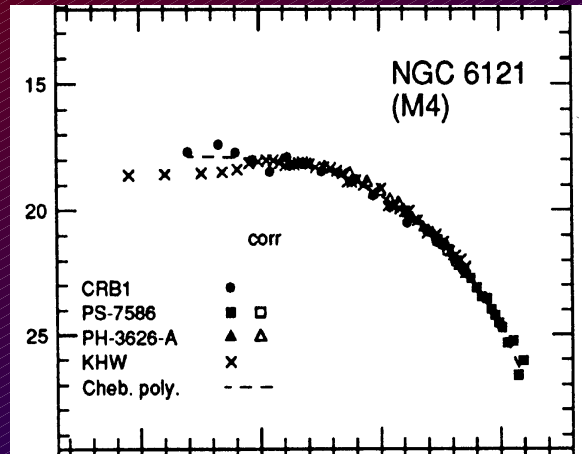
Projected radius  
 1-parameter sequence of shapes  
 + 2 scale parameters (core radius;  
 total luminosity)

Ivan King



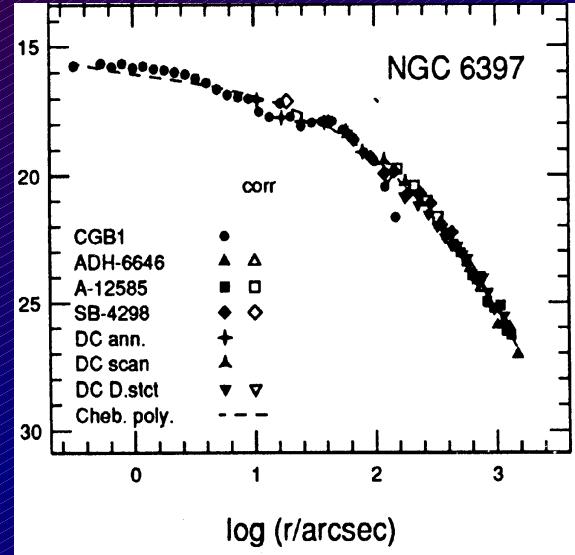
# The Surface Brightness Profiles

## M4



King profile  
 Resolvable core radius  
 Dimmer central SB

## NGC 6397



Non-King profile  
 Unresolvable core  
 Brighter central SB

# Modelling of M4 and NGC 6397

M4: H & Giersz, 2008, MNRAS, 389, 1858

NGC 6397: G&H, 2009, arXiv:0901.1085v1

Constructed models which approximately fit

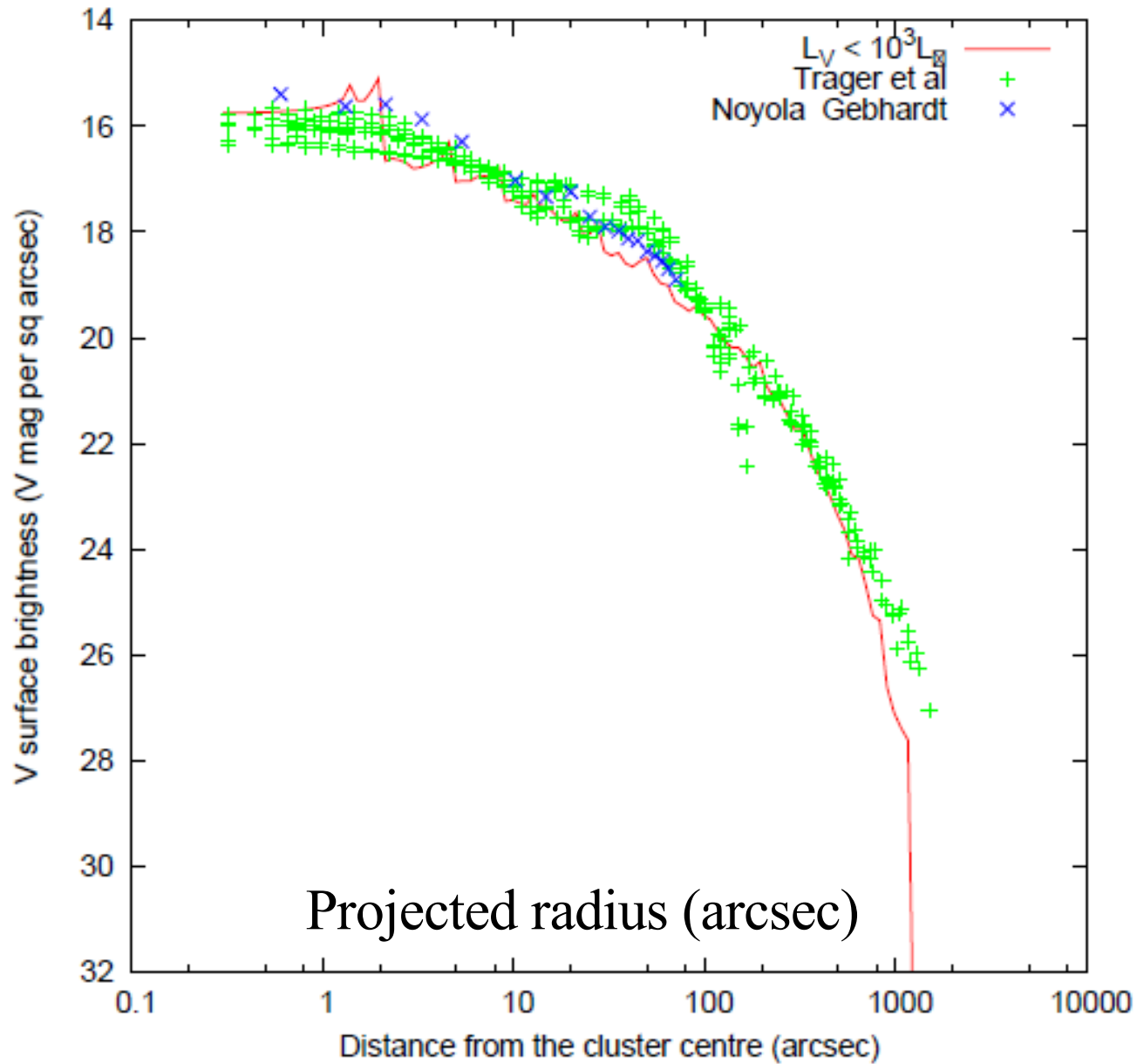
- surface brightness profile (*example shortly*)
- velocity dispersion profile
- luminosity function at two radii
- observed binary fraction

Technique:

- Monte Carlo dynamics
- Synthetic stellar and binary evolution

# Example: surface brightness profile of NGC 6397 and our model

Surface brightness ( $V$  mag/arcsec<sup>2</sup>)





## Comparison of M4 and NGC 6397

	M4	N6397
Distance from sun (kpc)	1.72	2.6
Distance to Galactic Centre (kpc)	5.9	6.0
Log Mass ( $M_{\odot}$ )	4.8	5.0
Half-light radius (pc)	2.2	2.2
Tidal radius (pc)	16	12
Central binary fraction	0.02 <sup>a</sup>	0.05 <sup>a</sup>
Metallicity [Fe/H]	-1.20	-1.95

These two clusters are very similar, *except* for the surface brightness profile

# What determines the surface brightness profile?

1. Core collapse
2. Tidal effects
3. Primordial binaries
4. Stellar-mass black holes
5. Intermediate-mass black holes

# Hypothesis I: Core Collapse (*standard explanation*)

Time scale  $\propto$  relaxation time.

But relaxation times are

0.22Myr (M4)

0.29Myr (NGC 6397)

*M4 is evolving faster, but has the “pre-collapse” profile*

Conclusion: core collapse is not the explanation

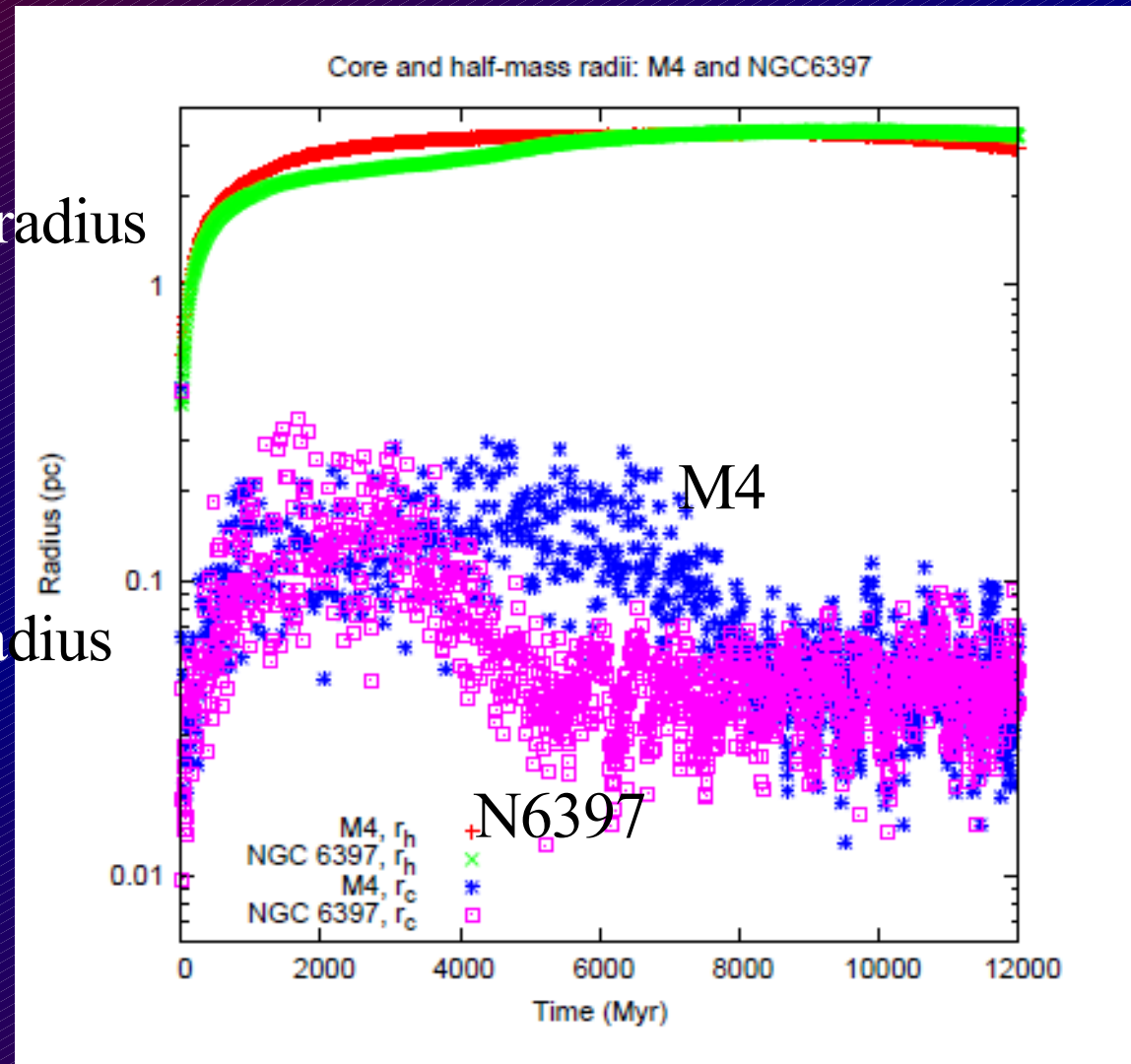
This conclusion is confirmed by the core evolution of our Monte Carlo models:

# Core evolution of the MC models

Half-mass radius

Core radius

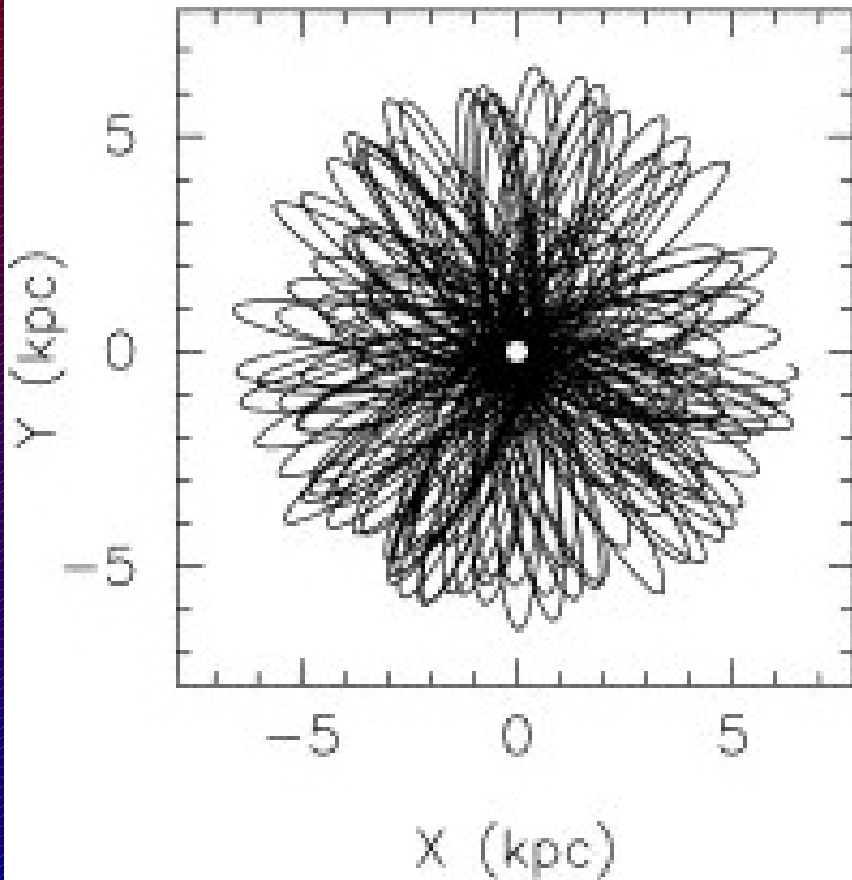
According to our models, both M4 and N6397 are post-core-collapse clusters, with King- and non-King profiles, respectively.



Time

# Hypothesis II: Tidal Effects

NGC 6121



## A galactic orbit for M4

*From Dinescu et al 1999*

Cluster	Apo	Peri
M4 (N6121)	5.9	0.6
NGC6397	6.3(7.0 <sup>a</sup> )	3.1(2.6 <sup>a</sup> )

<sup>a</sup>*Kalirai et al 2007*

M4 has the stronger tidal effects and should evolve faster to core collapse (other things being equal), but it has the “uncollapsed” profile.

# Hypothesis III: Primordial Binaries

More binaries would expand the core.  
Does this explain the difference between  
M4 and N6397?

No: M4 appears to have the smaller binary fraction  
(Richer et al 2004, Davis et al 2008)

	M4	NGC6397
Centre	~2%	5.1%
Off-centre	~1%	1.2%

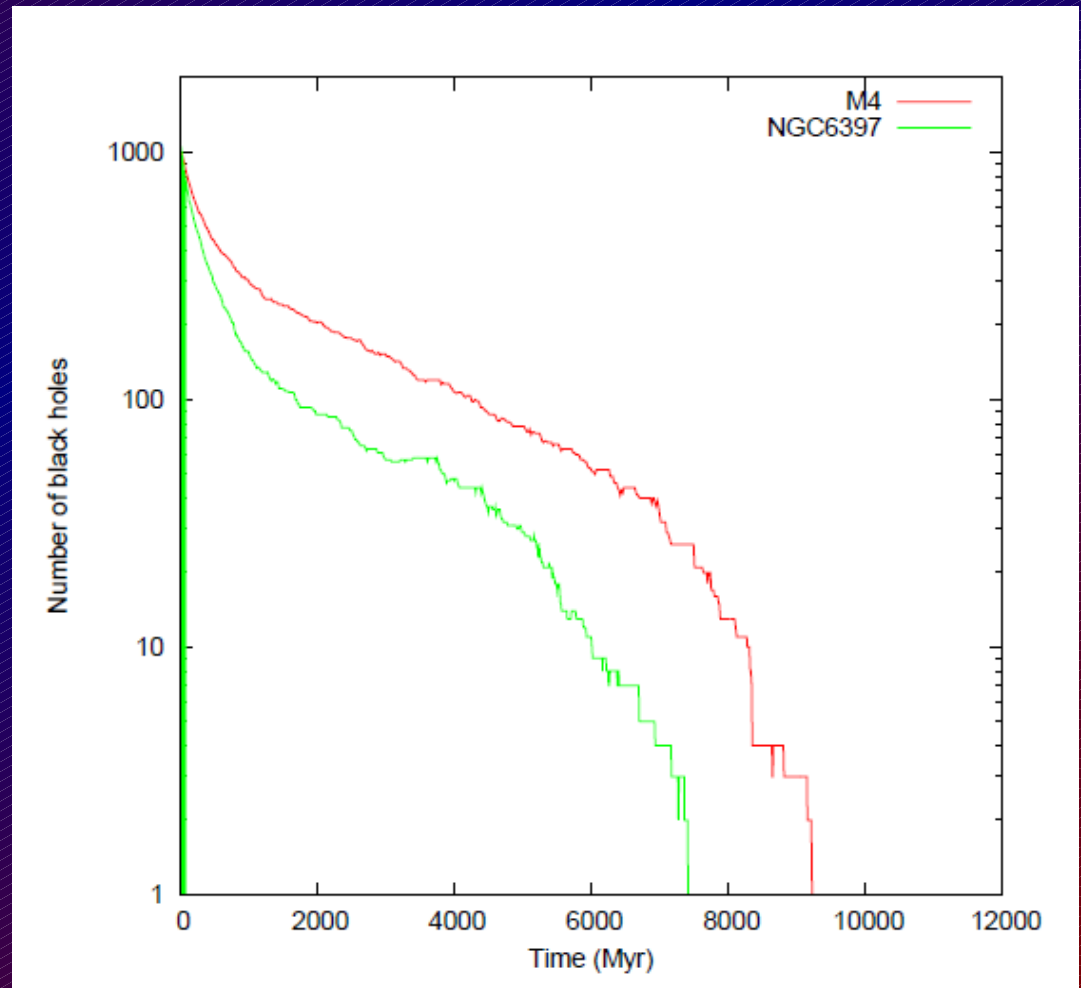
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# Hypothesis IV: stellar-mass black holes

Can cause core expansion: Merritt et al 2004, Mackey et al 2007

Inoperative in M4 and NGC6397  
for last few Gyr

Number of BH



Time (Myr)

# KITP Hypothesis V: Intermediate-Mass Black Holes

IMBH form a cusp, and may expand the core

NGC6397       $M / M_{\odot} < [390, 1290]$  (De Rijcke et al 2006)

M4              No literature

Remark: our models account completely for the velocity dispersion of M4 and NGC6397

*So why do M4 and NGC6397 have different surface brightness profiles?*



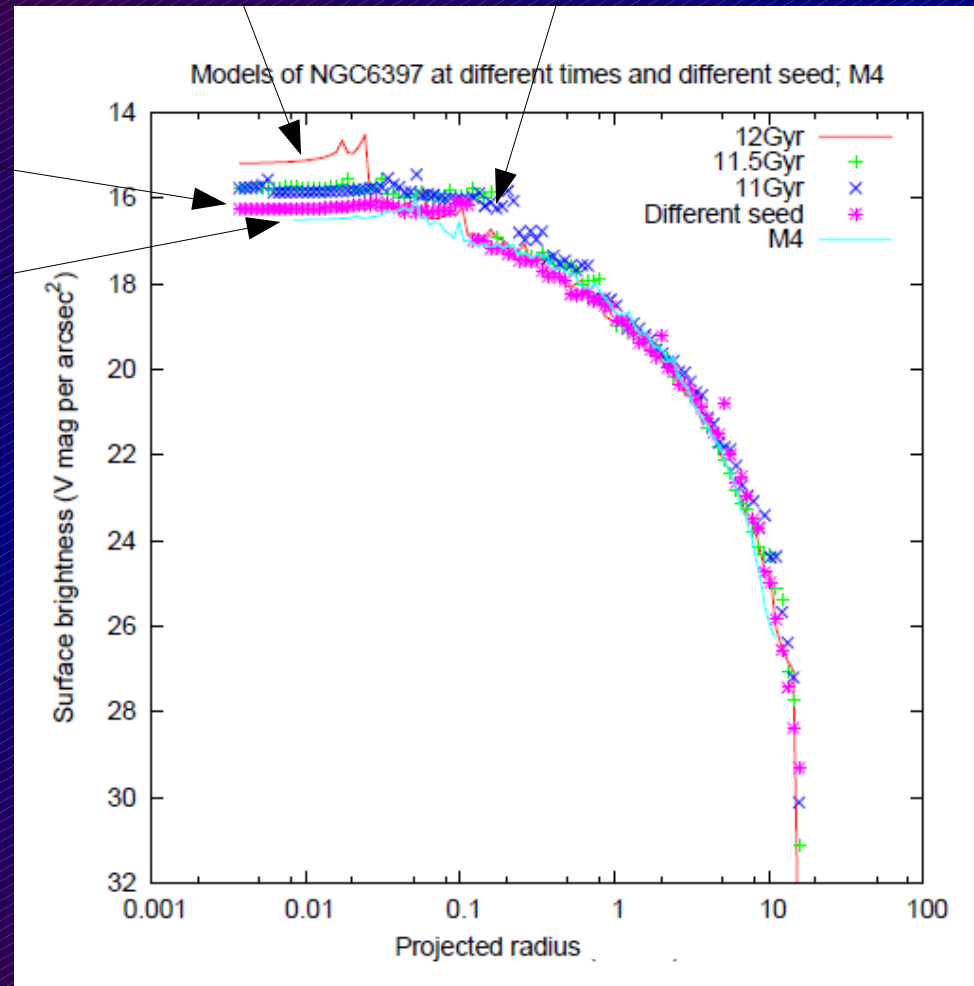
# Hypothesis VI: Fluctuations

Basic model    Earlier times (11, 11.5Gyr)

Different seed

M4 model

- our model of NGC6397 at 11, 11.5, 12 Gyr;
- a model of NGC6397 with different seed;
- our model of M4



Conclusion: sometimes NGC6397 has a non-King profile, sometimes it resembles M4

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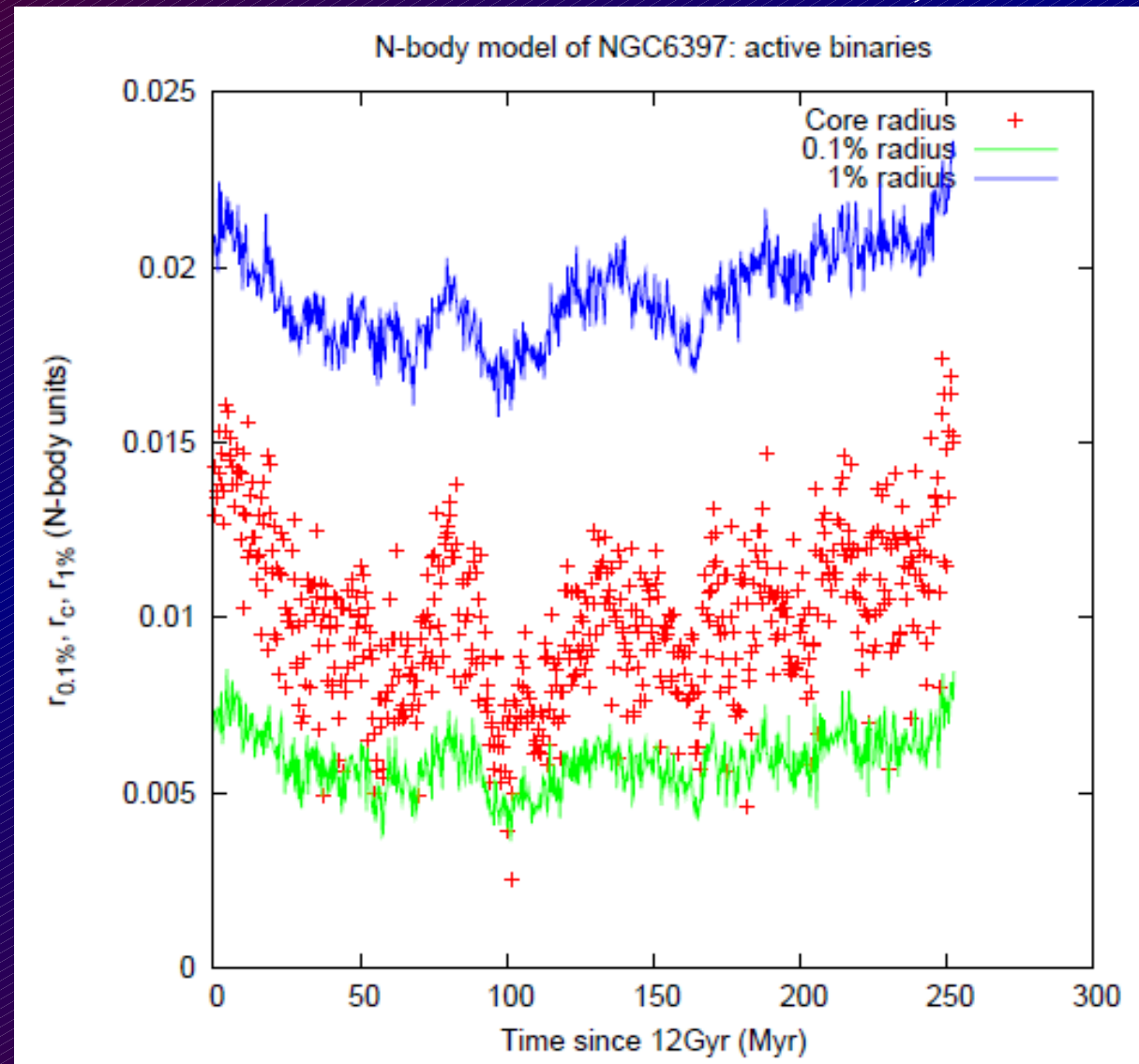
# Fluctuations in the core

We constructed an N-body model from our Monte Carlo model at 12Gyr, with active binaries, but no further stellar evolution.  $N = 112169$ , NBODY6/GPU

1% Lagrangian radius

(Dynamical) core radius

0.1% Lagrangian radius



Myr since 12Gyr

# Conclusion

The difference between the surface brightness profiles of M4 and NGC6397 is a fluctuation

## Remarks

1. These fluctuations are collective, akin to gravothermal oscillations
2. Studying the dynamical evolution of globular clusters is not deterministic