

# Double-well geometries and species-selective environments

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4T5, MA'46



# Outline

- Species selective optical lattices
- Bose-fermi mixtures on a chip
- RF-dressed double well traps
- Direct observation of number squeezing?
- Other topics for discussion



# Research Group

## Postdocs

**Dr. Jason McKeever**

(PhD Caltech w/Kimble)

Formerly:

**Dr. Seth Aubin**

→ Prof @William&Mary

**Dr. Thorsten Schumm**

→ Prof @Vienna

## Graduate Students

**Marcus Extavour**

**Lindsay LeBlanc**

Alma Bardon

Dylan Jarvis

Amir Mazouchi

## Visitors

Gael Veroquaux

## Technical staff

Alan Stummer

(Research Technologist)

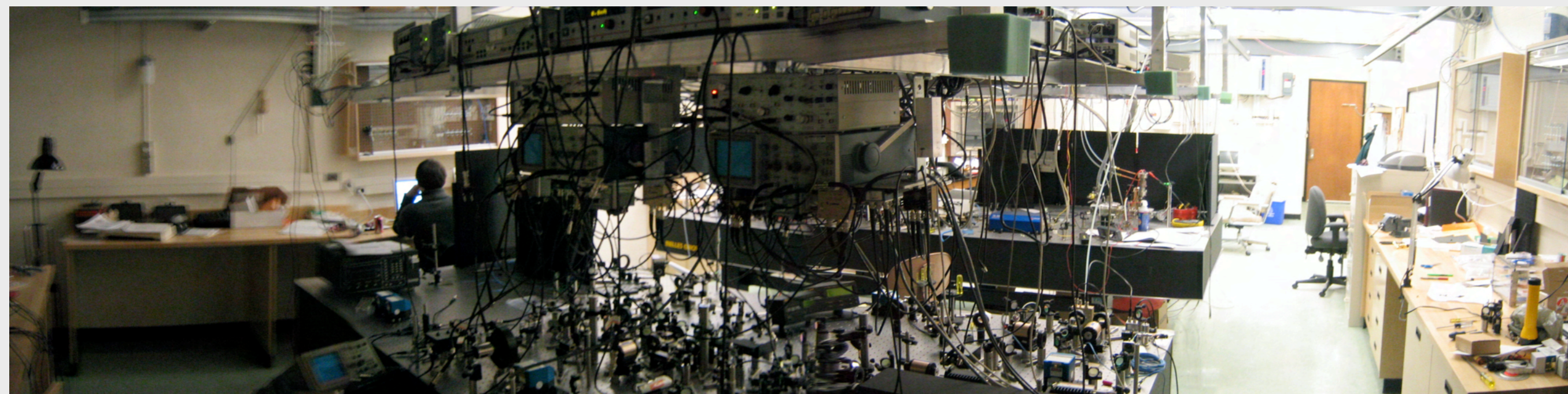
“Next gen:”

Brian Shuve → Harvard

Ian Leroux → MIT (Vuletic)

Dave McKay → DeMarco gp.

Dave Shirokoff → MIT



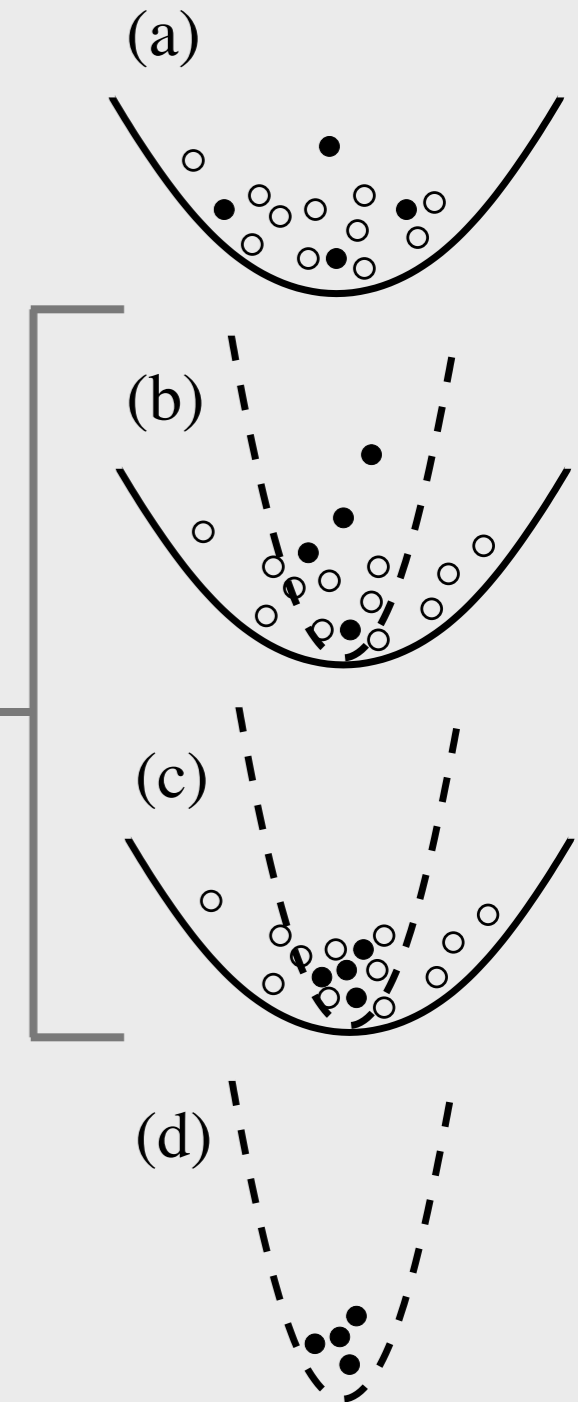
# Species-selective optical lattices

L. J. LeBlanc and J. H. Thywissen  
**Species-specific optical lattices**  
c-m/0702034 and *Physical Review A* (2007)

# Wouldn't it be nice if...

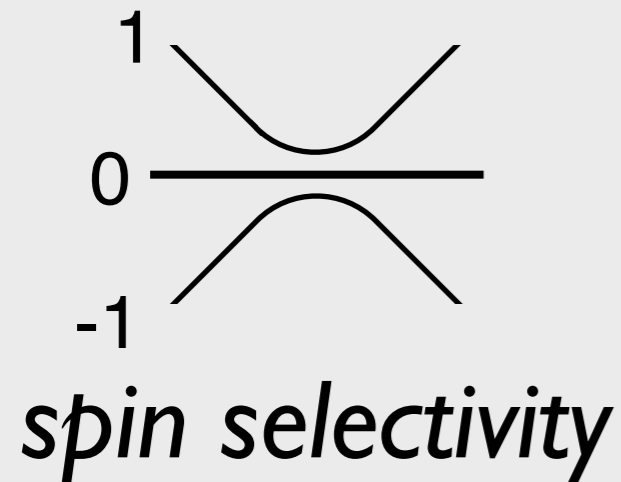
...we could choose trapping potential *independently* for different species?

- selective lattices
- isothermal compression
- single-species tweezers  
[Fei Zhou: dressing vortices]
- overlap engineering  
[equal TF radii for unequal  $\mu$ ]
- ...

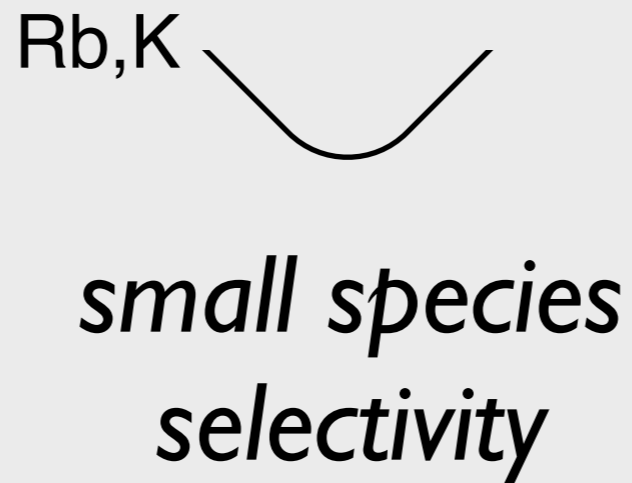


# approaches

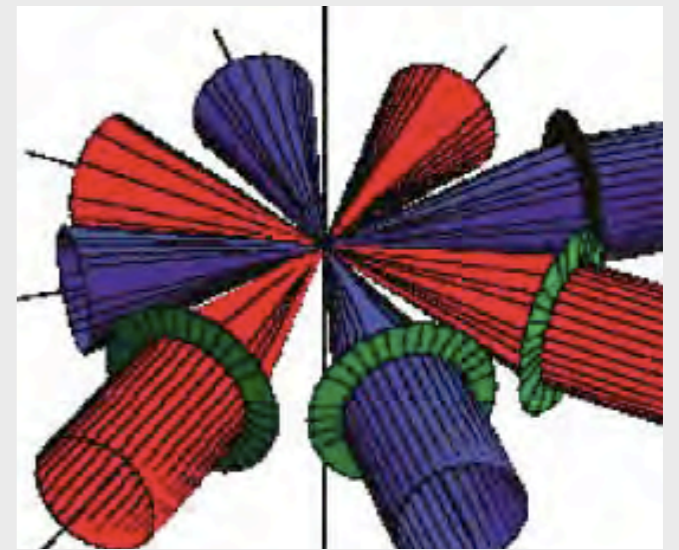
magnetic trap



FORT



2-color trap

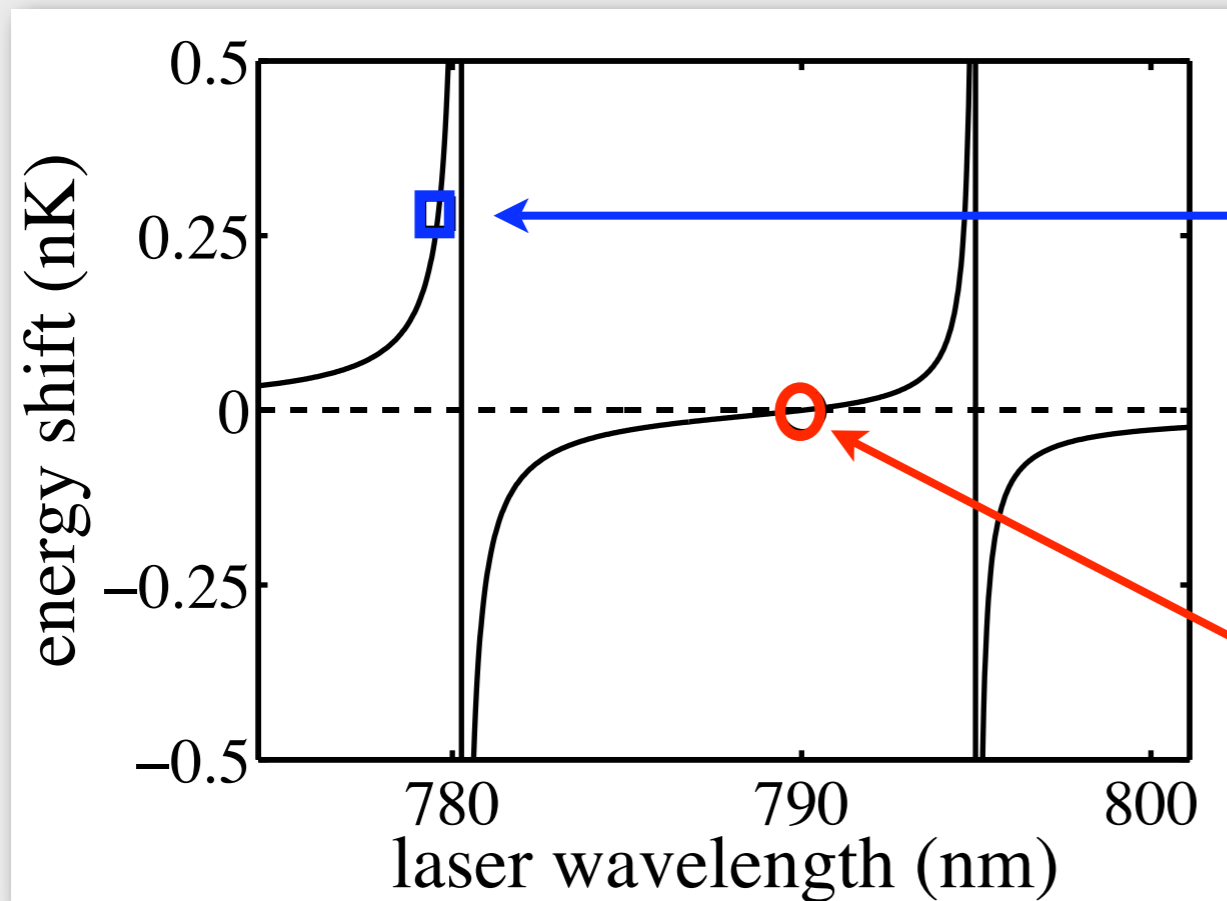


Onofrio et al. (2001,2002)

- None of these can create species-selective optical lattices
- We analyze two alternative optical approaches, that are *not* far-detuned

# two selective detunings

Rb87



**“Tune in”**

Near resonance, much stronger shift on Rb than, eg, K

At crossover, no shift on Rb: so only K affected.

**“Tune out”**

$$U_g = \frac{1}{2\epsilon_0 c} \sum_e \left[ \frac{|\langle e | \mathbf{d} \cdot \hat{\mathbf{e}} | g \rangle|^2}{\hbar(\omega_L - \omega_{eg})} - \frac{|\langle e | \mathbf{d} \cdot \hat{\mathbf{e}} | g \rangle|^2}{\hbar(\omega_L + \omega_{eg})} \right] I$$

$$\gamma_g = \sum_e \frac{\Gamma_e |\langle e | \mathbf{d} \cdot \hat{\mathbf{e}} | g \rangle|^2}{\Delta_{eg}^2} I \quad \leftarrow \text{problem: heating (light scattering).}$$

# Optimization

target



spectator



- Criterion 1:  
Selective

$$\rho = \left| \frac{U_t}{U_s} \right| \quad \text{“selectivity”}$$

U=shift  
H=heating

- Criterion 2:  
Low heating rate

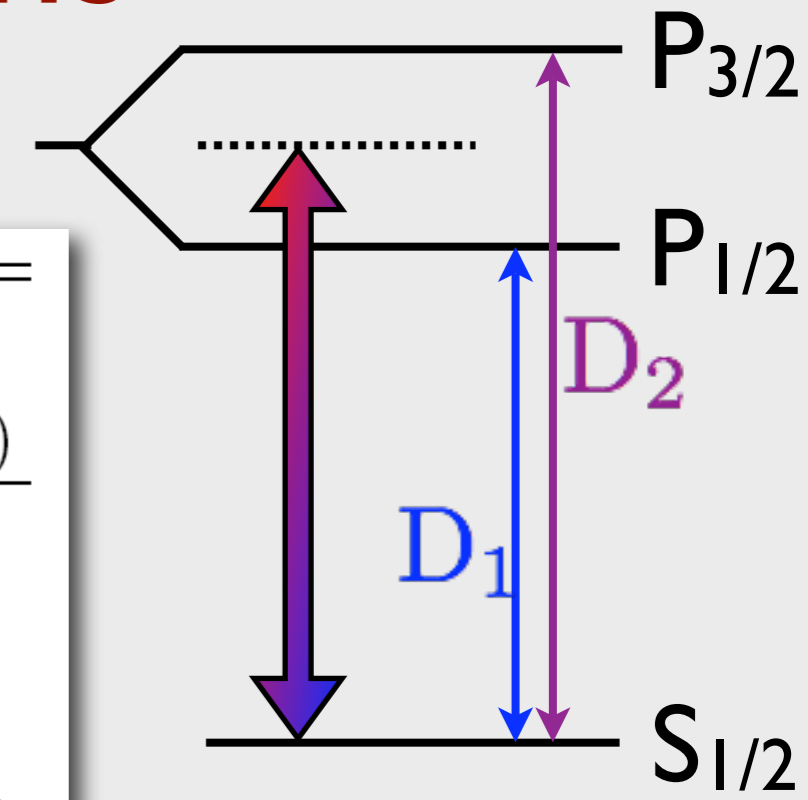
$$s = \frac{U_t}{H_t + H_s} \quad \text{“sustainability”}$$

Question: what scheme maximizes both  $\rho$  and  $s$  ?



# Tune out wavelengths

Element	$ F, m_F\rangle$	$\lambda_{\text{TIO}}$ (nm)		$\gamma_{\text{sc}}/I$ ( $\text{cm}^2/\text{mJ}$ )
		Eq. 1	Eq. 2	
${}^6\text{Li}$	$ \frac{3}{2}, \frac{3}{2}\rangle$	670.99	670.99	2.8
${}^7\text{Li}$	$ 2, 2\rangle$	670.97	670.97	2.4
${}^{23}\text{Na}$	$ 2, 2\rangle$	589.56	589.56	$2.0 \times 10^{-3}$
${}^{39}\text{K}$	$ 2, 2\rangle$	768.95	768.95	$1.4 \times 10^{-4}$
${}^{40}\text{K}$	$ \frac{9}{2}, \frac{9}{2}\rangle$	768.80	768.80	$1.7 \times 10^{-4}$
${}^{87}\text{Rb}$	$ 2, 2\rangle$	790.04	790.01	$9.1 \times 10^{-6}$
${}^{133}\text{Cs}$	$ 4, 4\rangle$	880.29	880.06	$1.5 \times 10^{-6}$



- Heating rates low for elements with large fine splittings (Cs,Rb)
- Selectivity is infinite

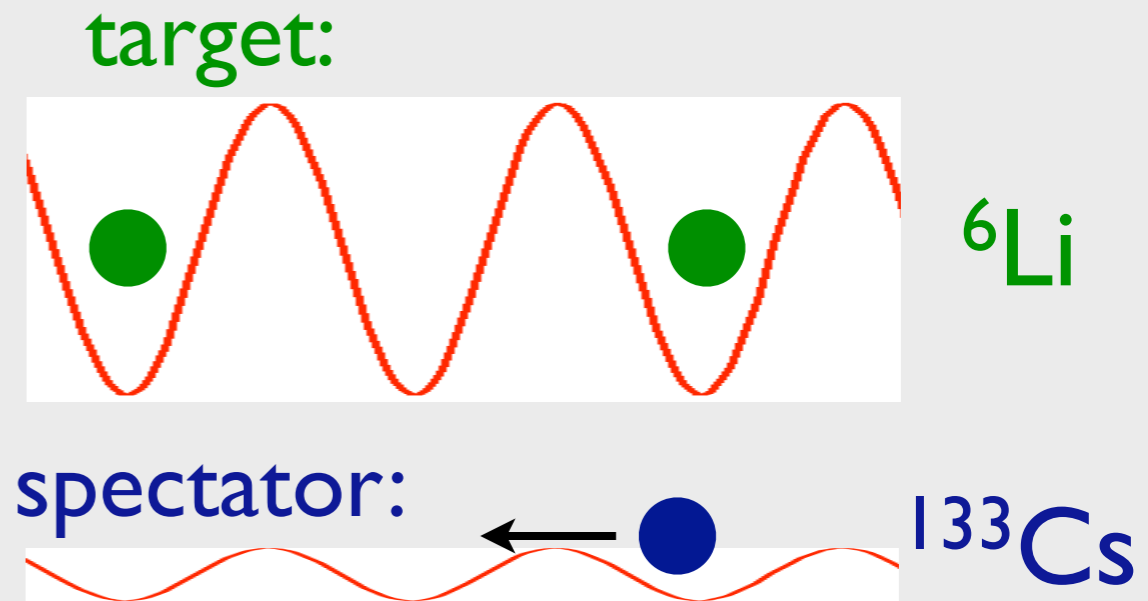
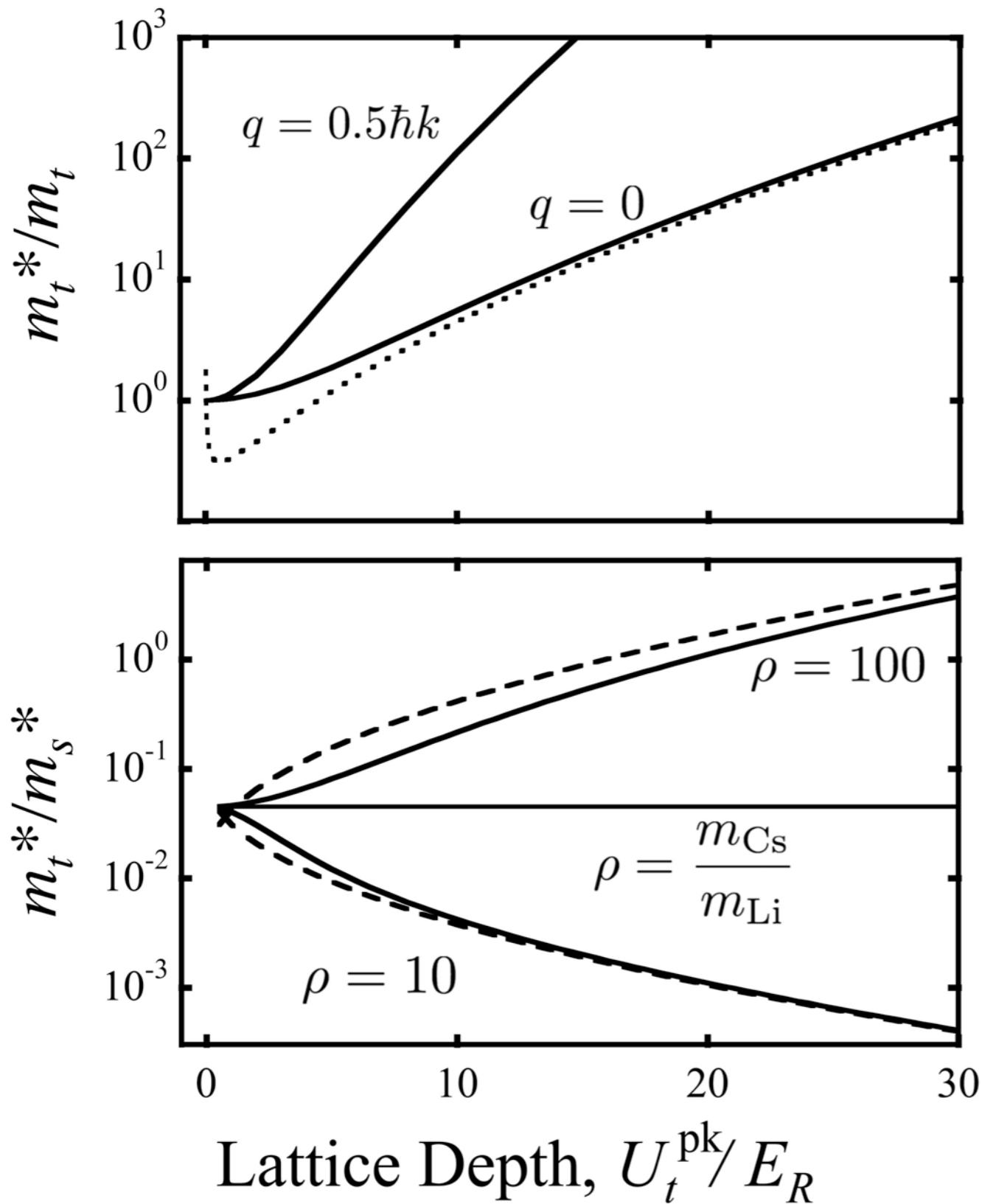
# Sustainability of B-F mixtures for TO vs. TI

Target	$\rho$	Spectator				
		${}^7\text{Li}$	${}^{23}\text{Na}$	${}^{39}\text{K}$	${}^{87}\text{Rb}$	${}^{133}\text{Cs}$
${}^6\text{Li}$	$\infty$	0.00134	$7.77 \times 10^{-4}$	-0.0381	-1.20	-8.45
	100	$2.66 \times 10^{-5}$	0.281	0.220	0.239	0.347
	10	$3.92 \times 10^{-6}$	2.54	2.30	2.49	3.57
${}^{40}\text{K}$	$\infty$	$4.28 \times 10^{-7}$	$5.77 \times 10^{-4}$	0.188	-9.03	-25.8
	100	3.05	5.78	$3.64 \times 10^{-5}$	0.251	1.39
	10	29.2	53.0	$4.65 \times 10^{-4}$	3.27	18.8

units: seconds

- ☑ Optimal approach depends on mixture
- ☑ Several combinations have sustainability greater than 10s

# application: Effective mass tuning

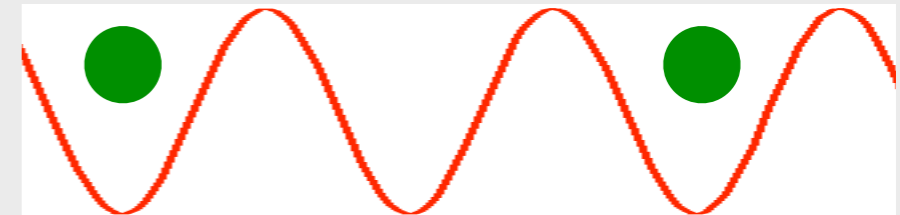


$$\frac{m_t^*}{m_s^*} \approx \frac{\exp \left\{ 2\sqrt{\eta_t} \left( 1 - \sqrt{m_s/\rho m_t} \right) \right\}}{\rho^{3/4}} \left( \frac{m_t}{m_s} \right)^{1/4}$$

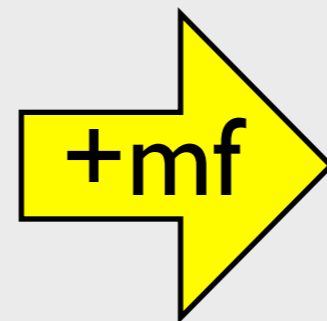
# application: non-optical lattice

- Mean field of trapped target atoms create a lattice potential for spectator atoms

target:



spectator:



- Limits selectivity: 
$$\rho_{\max} = \frac{\hbar \mu_{\text{st}} \eta^{1/4}}{32\pi |a_{\text{st}}| m_t^{3/2} E_R^{1/2}}$$
- Also creates non-optical lattice: non-sinusoidal, and possibly dynamic.

# Prospects

- mediated interactions between fermions
- effective mass engineering
- new kinds of lattices
- isothermal increase of phase space density

# Issues

- Heating rates low enough?
- Selectivity limited by interactions
- Thermalization may be slow

# Bose-Fermi mixtures on a chip

S. Aubin, S. Myrskog, M.H.T. Extavour, L. J. LeBlanc, D.  
McKay, A. Stummer, J. H. Thywissen

**Rapid sympathetic cooling to Fermi degeneracy on a chip**

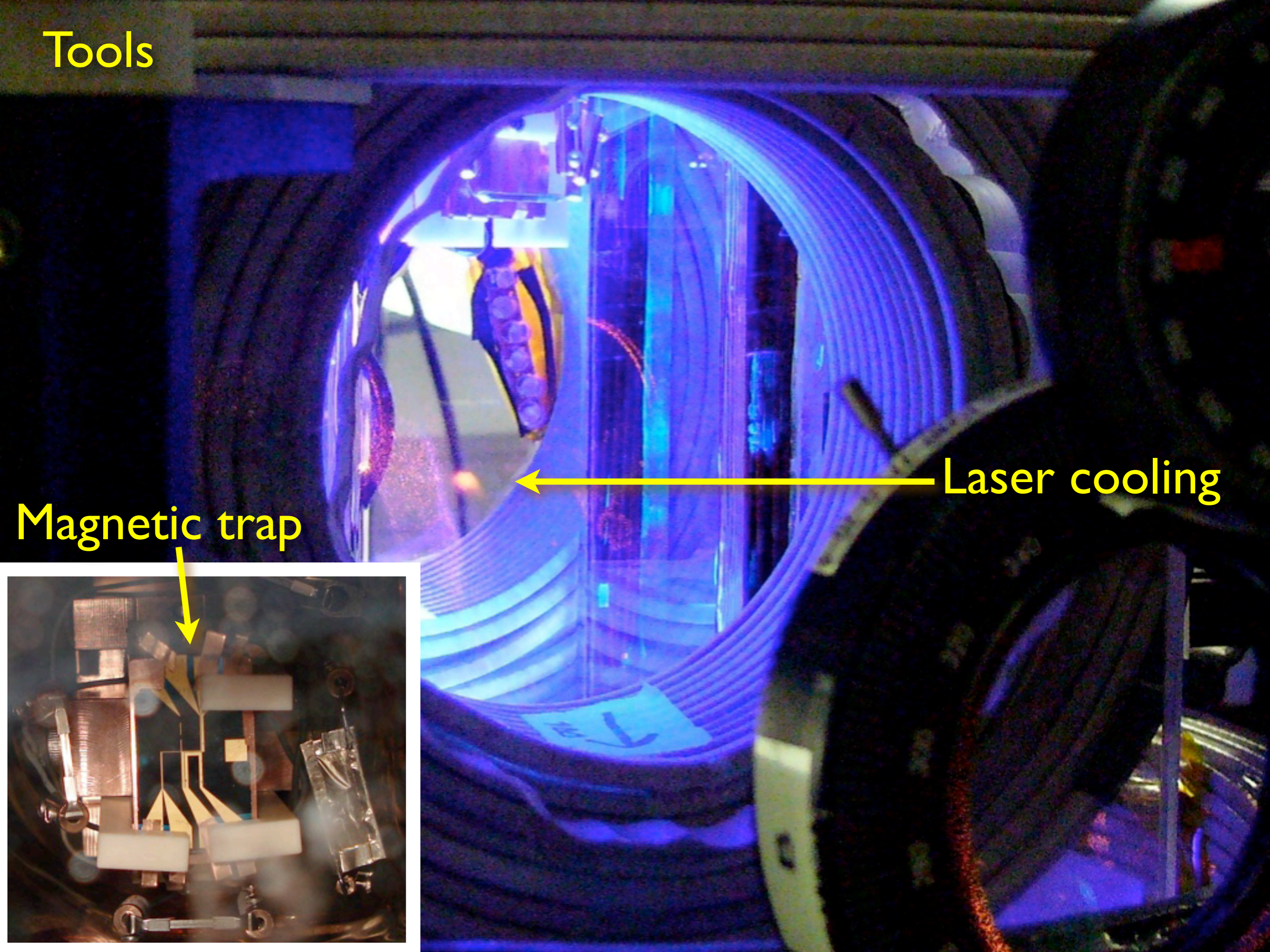
*Nature Physics* **2**, 384-387 (2006)



Approach:

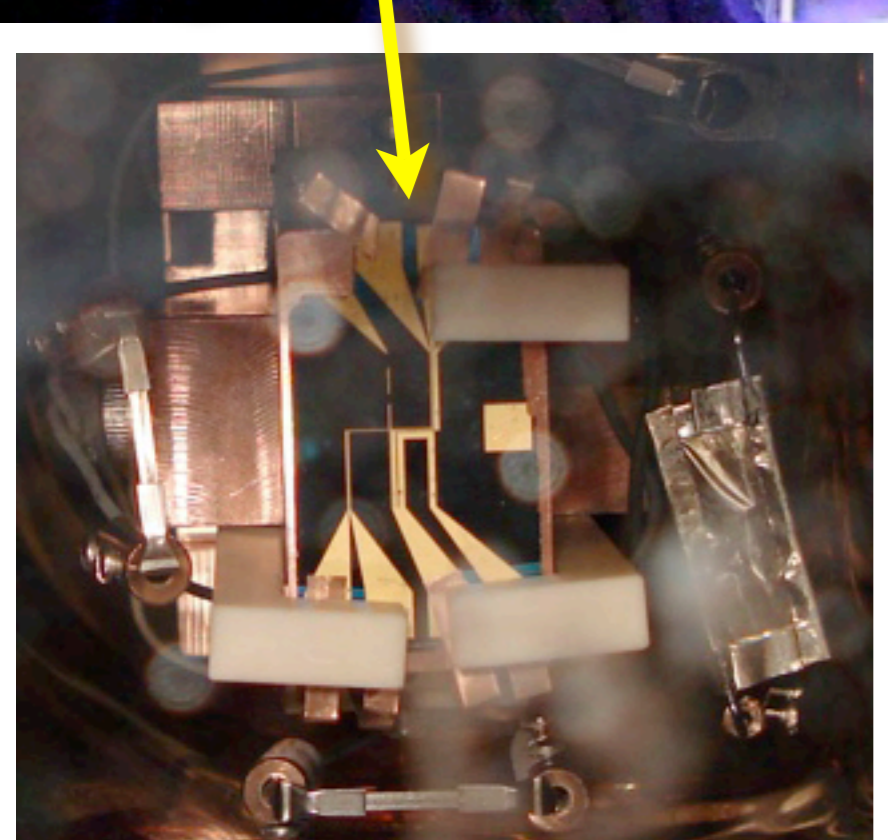
- $^{87}\text{Rb}$  &  $^{40}\text{K}$
- single chamber
- 6-beam MOT
- magnetic transport
- chip trap

Tools



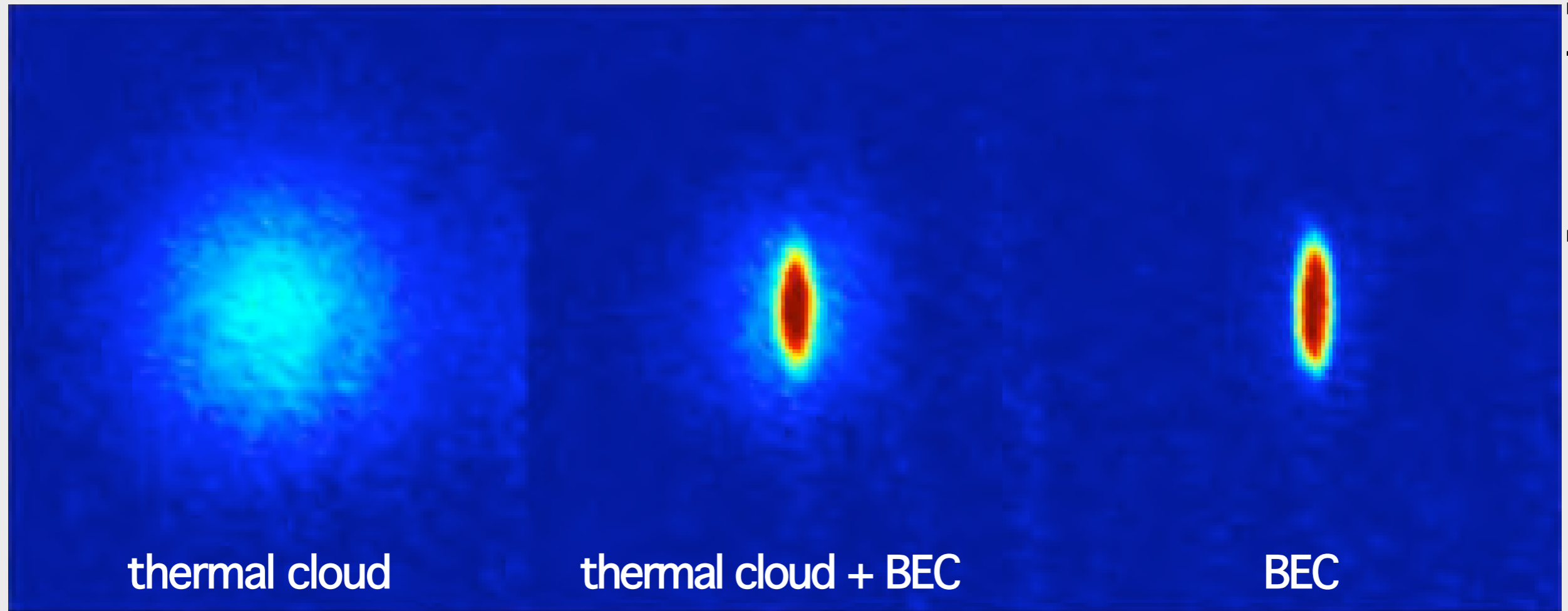
Laser cooling

Magnetic trap



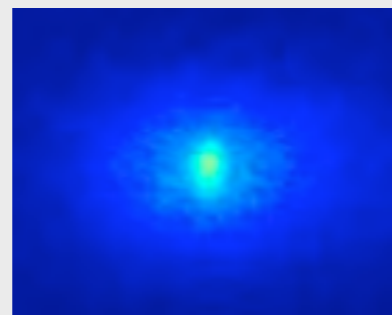


# Efficient evaporation



[April 2005]

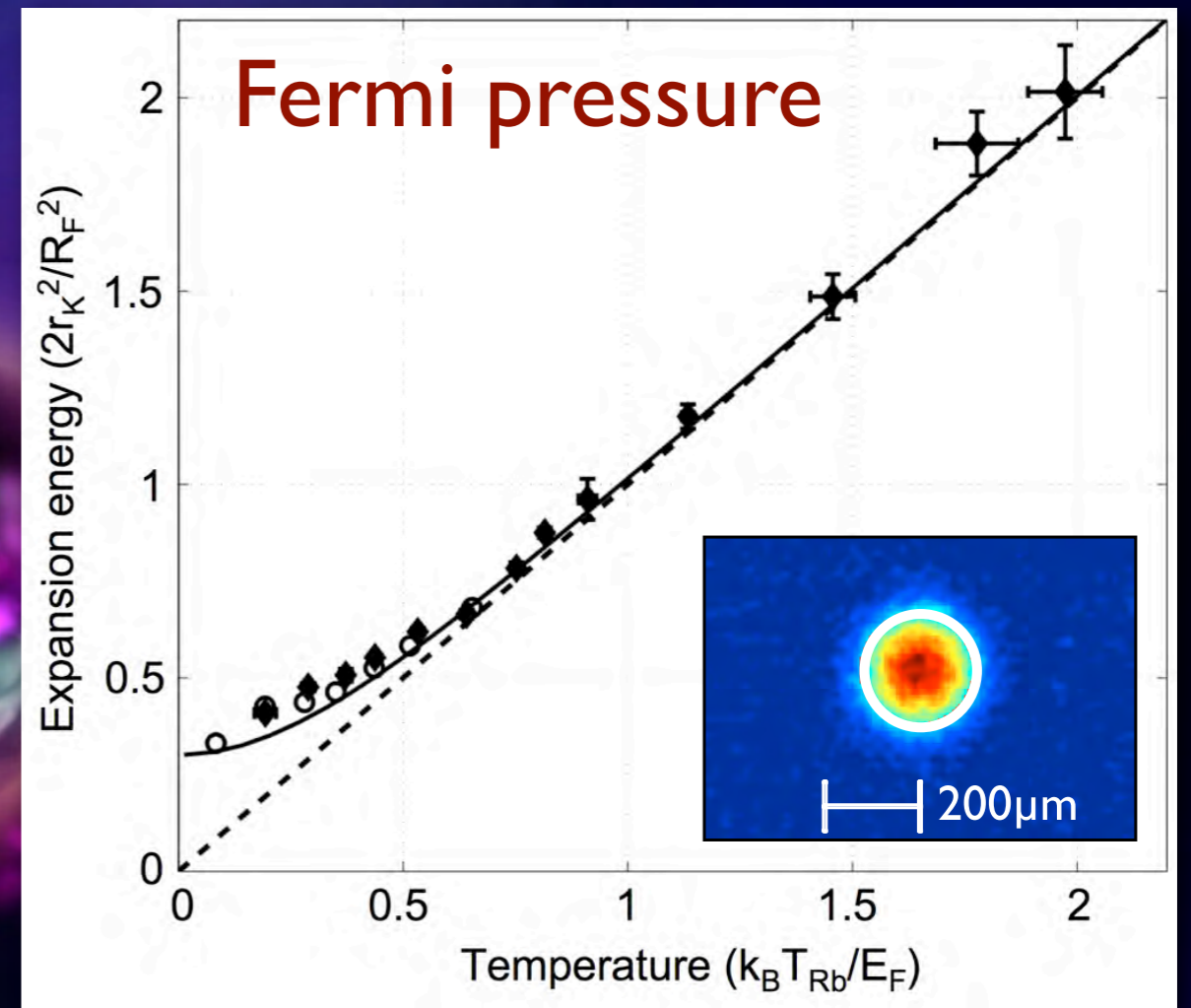
@1.725 MHz:  
 $N = 6.4 \times 10^5$ ,  $T \sim T_C$



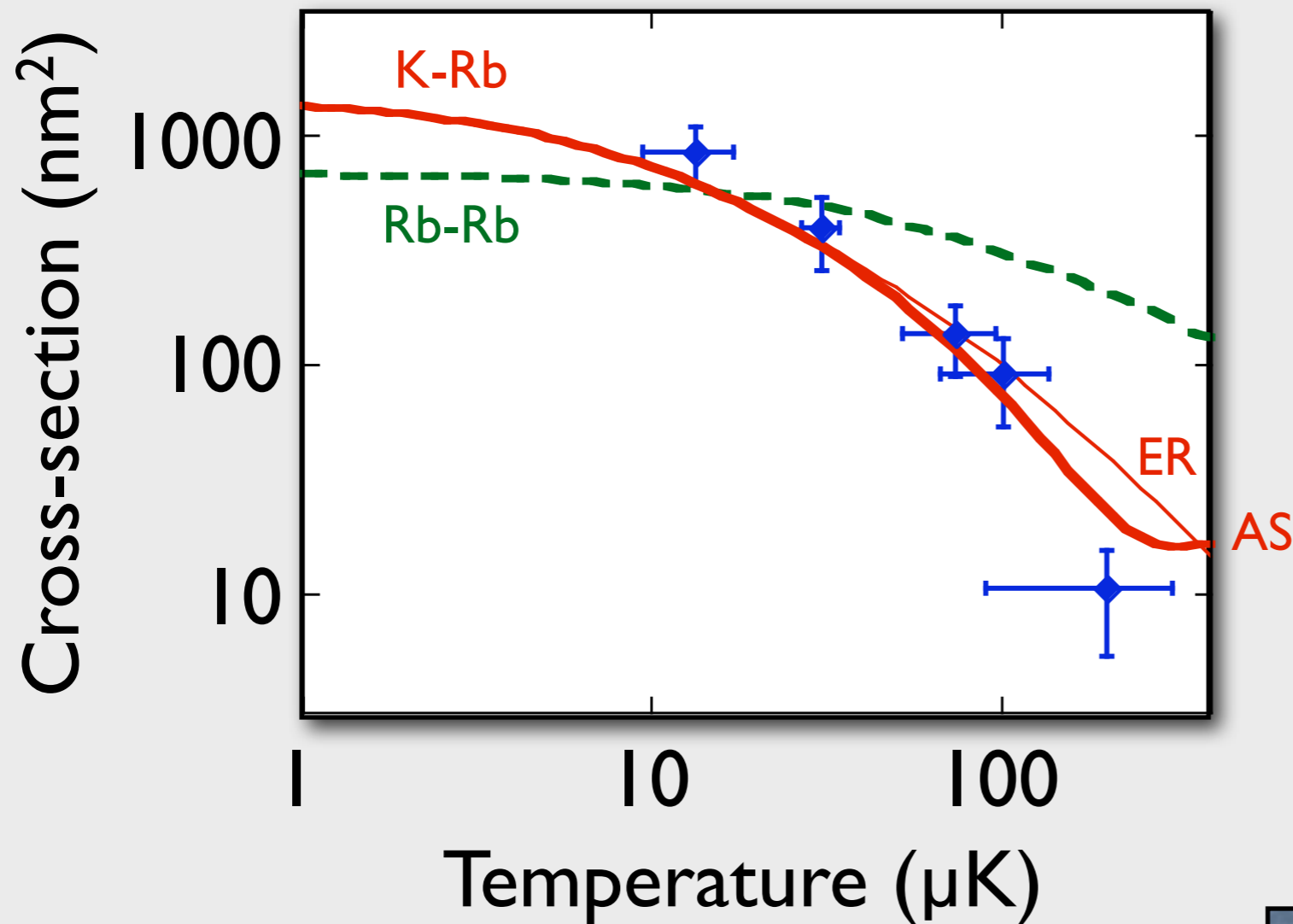
Surprise! Reach BEC with only a 30x loss in atom number.

Compare to trap loaded with  $2 \times 10^7$  atoms

# sympathetic cooling on a chip



# Ramsauer-Townsend Effect



Both data & theory  
put K-Rb below Rb-  
Rb at  $T > 20 \mu\text{K}$ .

# Advantages of $\mu$ fab traps

- Simple and robust approach: single cell
- High data rate:  
Sympathetic cooling in only 6s !
- New tools available:
  - single atom detection [eg, Reichel, Vuletic]
  - Strong rf manipulation
  - device integration

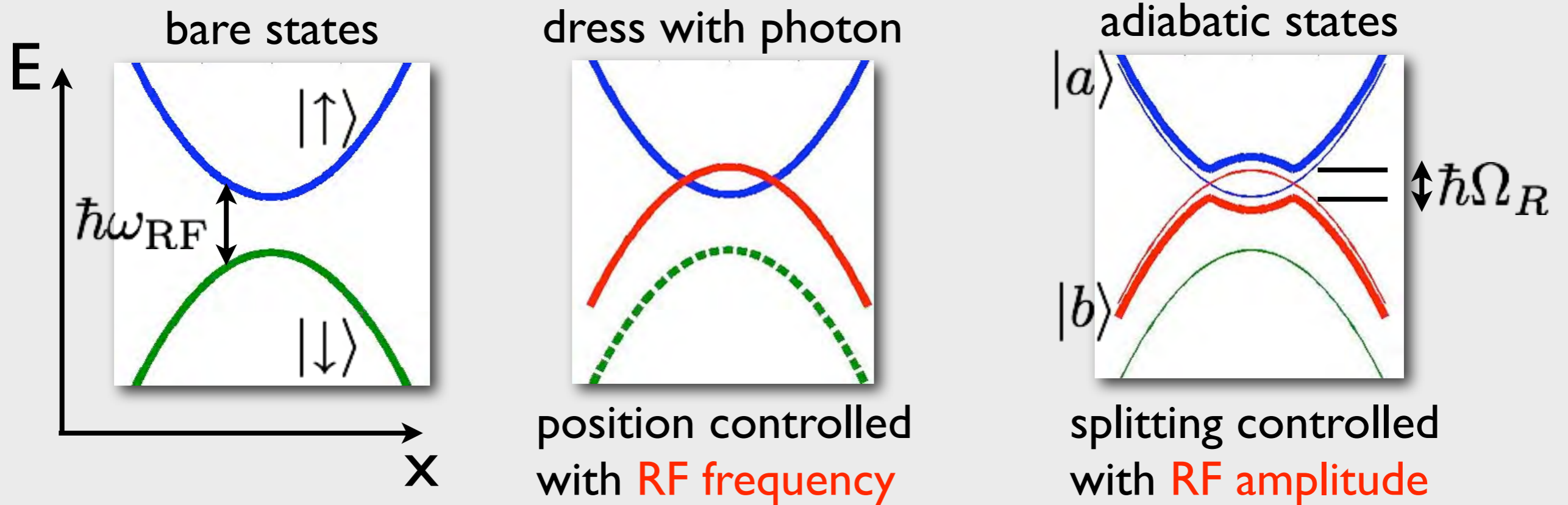
# Double-well geometries for $^{87}\text{Rb}$ and $^{40}\text{K}$

M. H. T. Extavour, L. J. LeBlanc, T. Schumm, B. Cieslak, S. Myrskog,  
A. Stummer, S. Aubin, and J. H. Thywissen  
**Dual-species quantum degeneracy of  $^{40}\text{K}$  and  $^{87}\text{Rb}$  on an atom chip**  
*Atomic Physics* **20**, 241-249 (2006)

# Double well formation

- Idea: combine static magnetic fields with (dressing) RF fields. This couples magnetic states:

[1D picture:]



Refs:

Zobay&Garraway PRL (2001)

Colombe...Perrin, Europhys. Lett. (2004)

Schumm...Schmiedmayer, Nature Physics (2005)

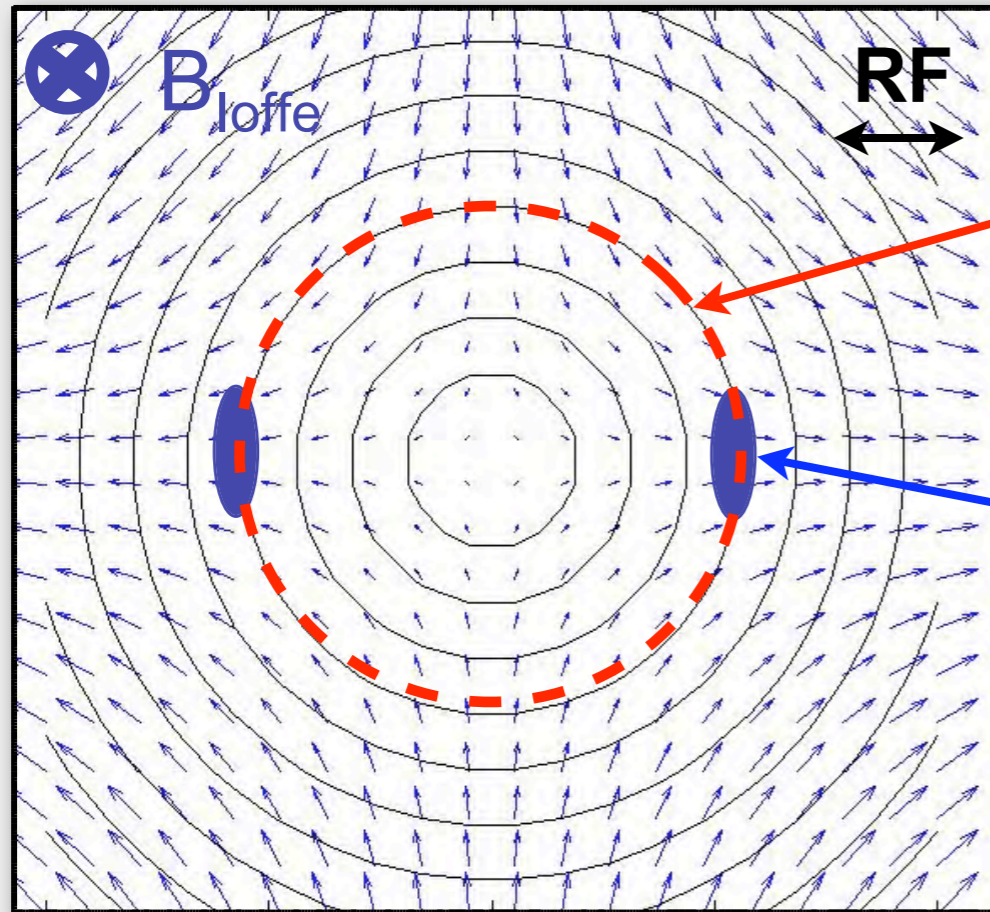
DeMarco, PRA (2006)

[credit for this and next two slides:  
adapted from Schumm & Hoeffelberth]

# Adiabatic RF dressed potentials

- In 3D, the polarization of the RF field breaks rotational symmetry:

$$V = g_F m'_F \sqrt{\underbrace{[\mu_B B_{dc} - h\nu_{rf}/g_F]^2}_{\text{red underline}} + \underbrace{[\mu_B B_{rf,\perp}/2]^2}_{\text{blue underline}}}$$

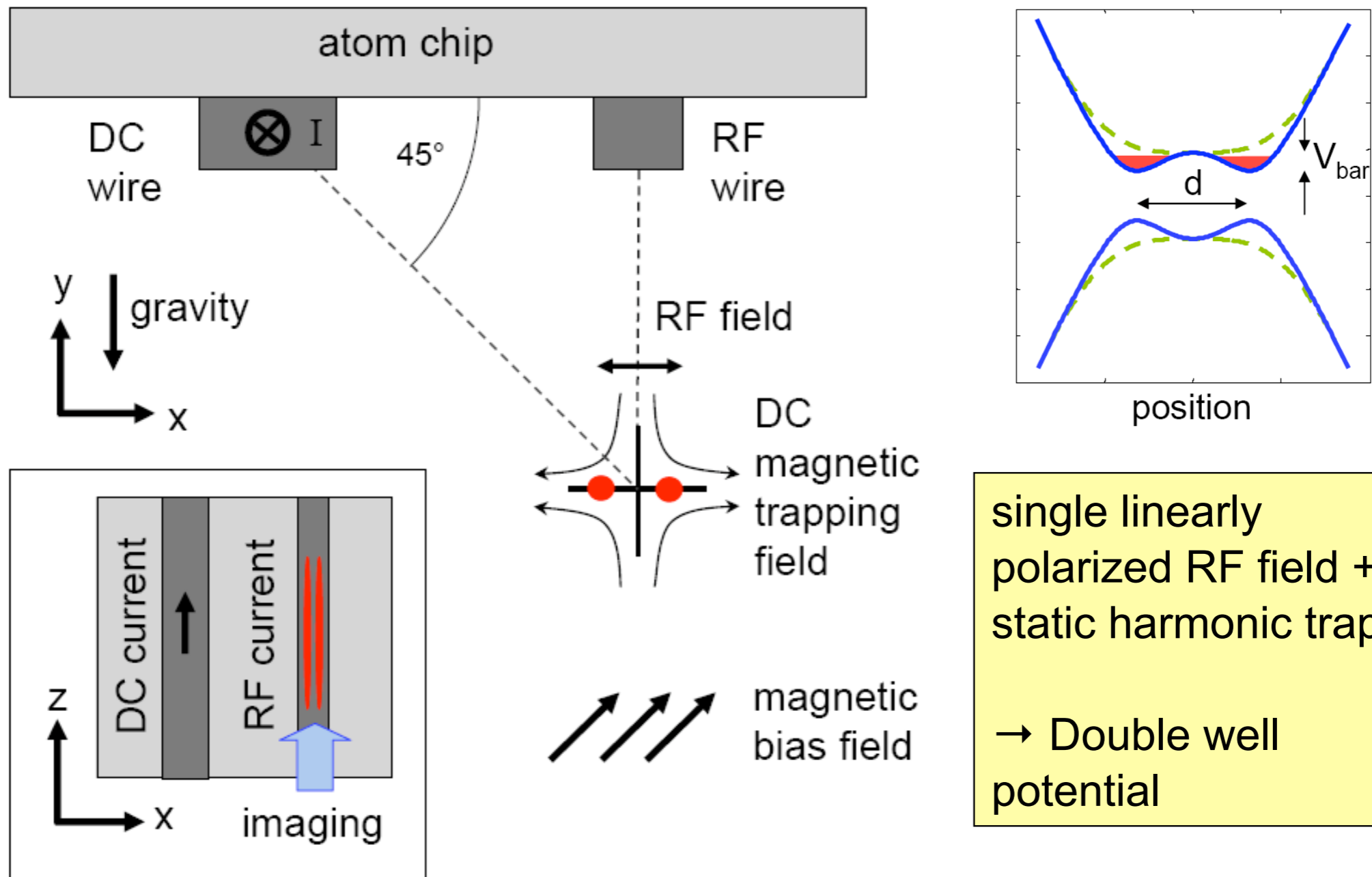


resonance condition forces the trap minimum on a circle

vector-dependent coupling term creates double well

# Heidelberg experiment

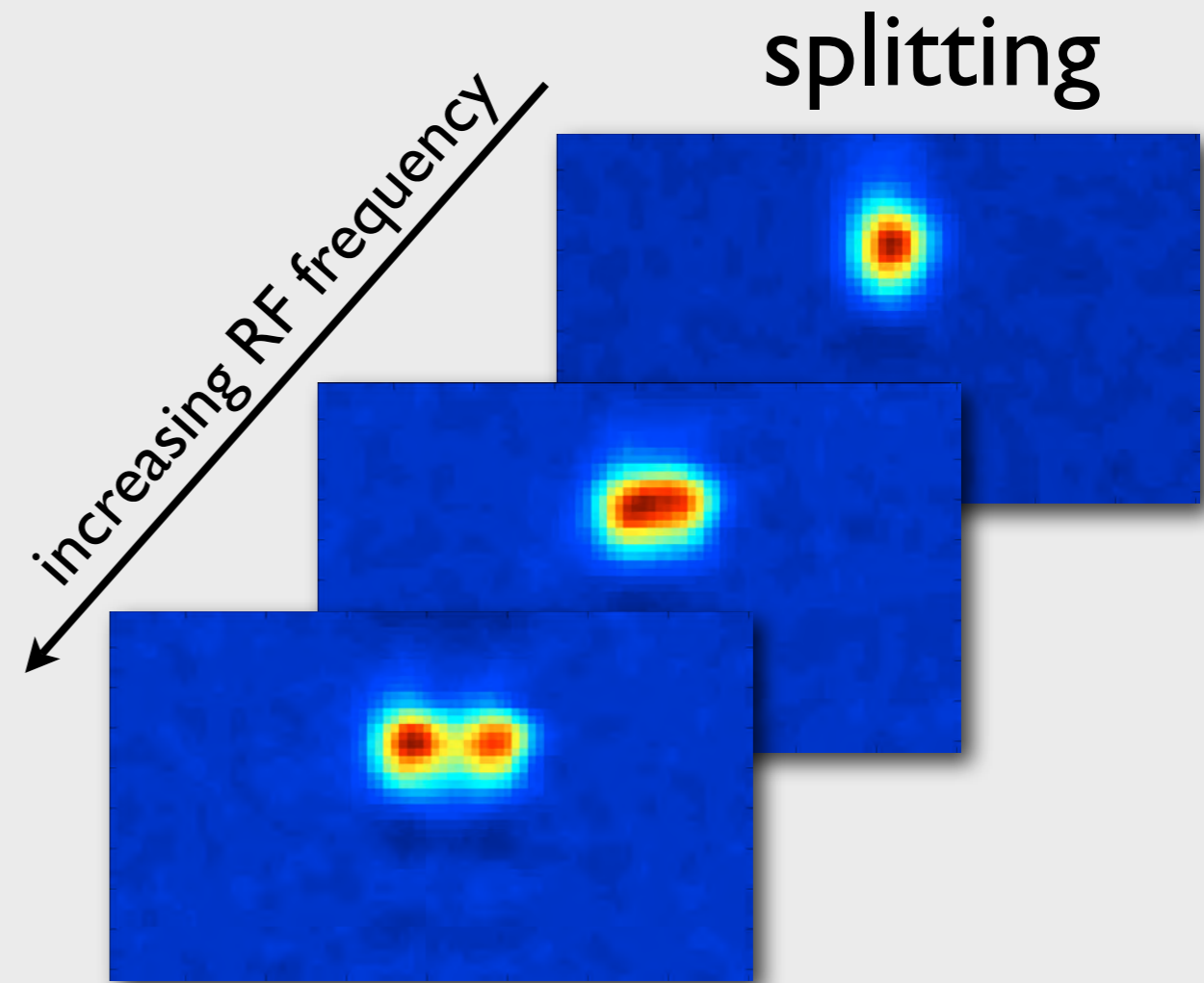
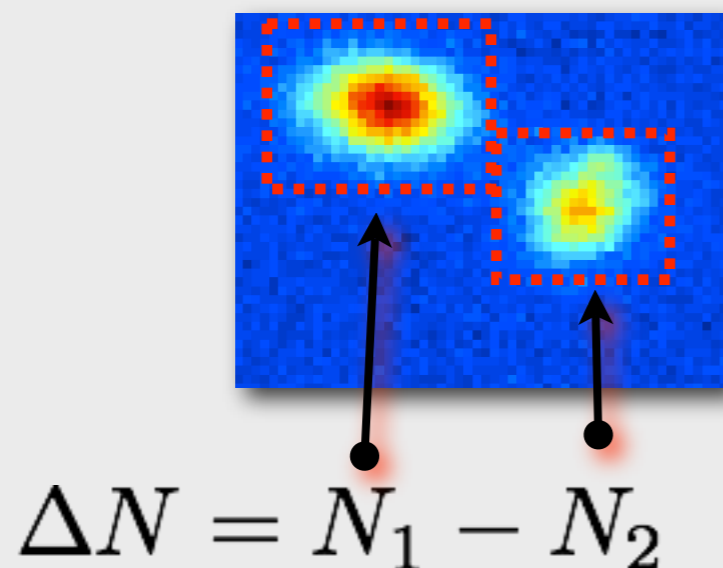
## RF beamsplitter: setup





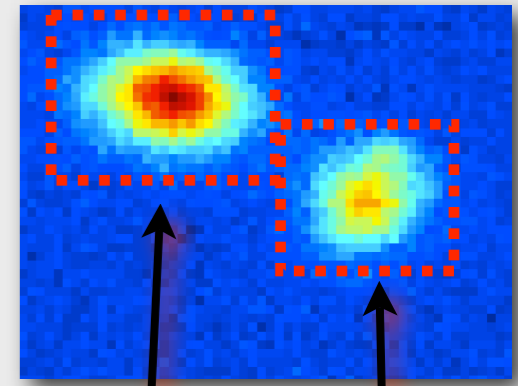
# Two types of measurement

- **NUMBER:**  
large initial separation & short TOF  
(clouds distinct)  
image to count  $N$



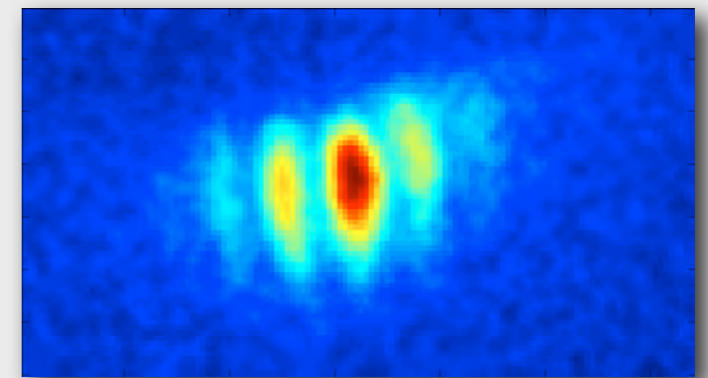
# Two types of measurement

- NUMBER:  
large initial separation & short TOF  
(clouds distinct)  
image to count  $N$



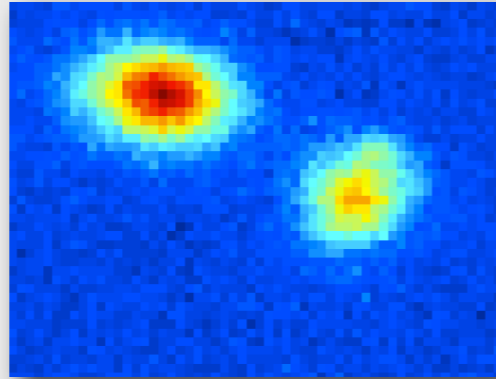
$$\Delta N = N_1 - N_2$$

- PHASE:  
small initial separation & long TOF  
(clouds interfere)  
image to measure phase

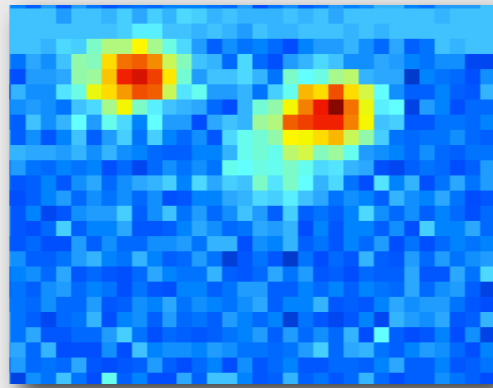


$$n(x) \sim 1 + a \cos(kx + \phi)$$

# Bosons or Fermions

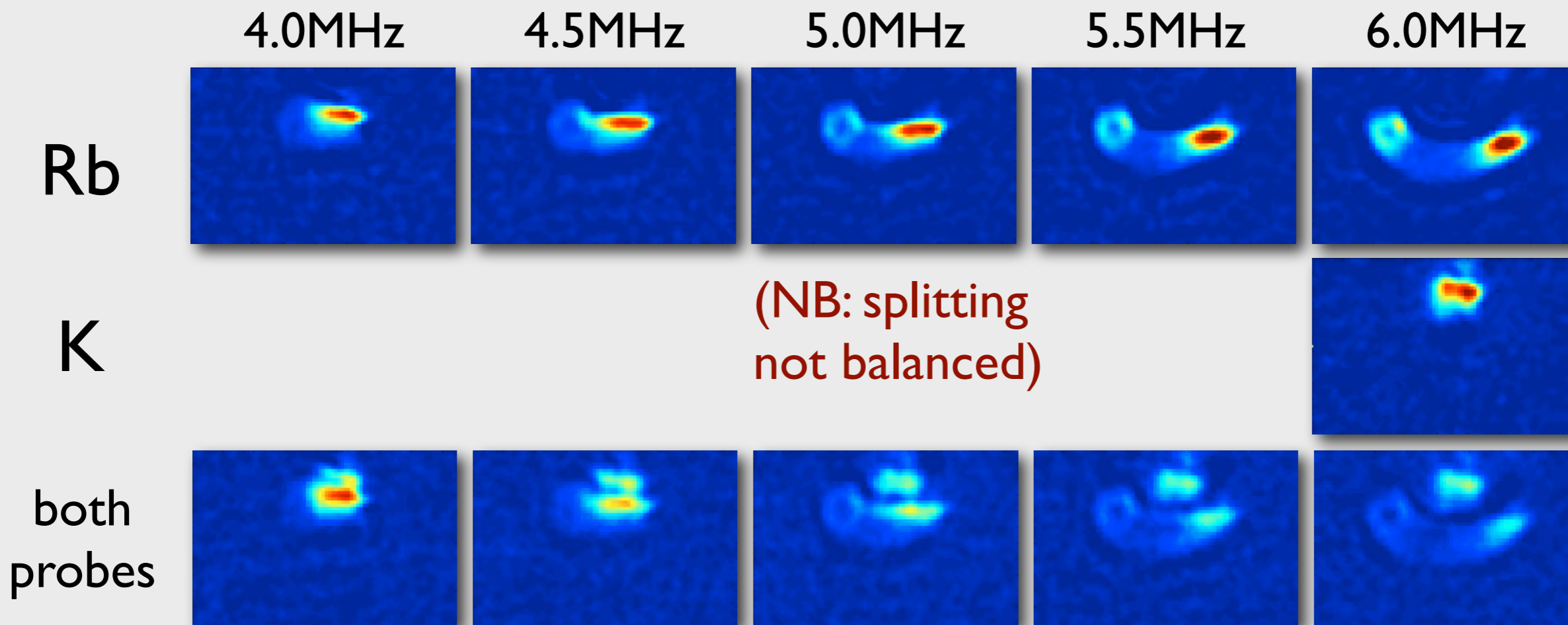


bosonic  
 $^{87}\text{Rb}$



fermionic  
 $^{40}\text{K}$

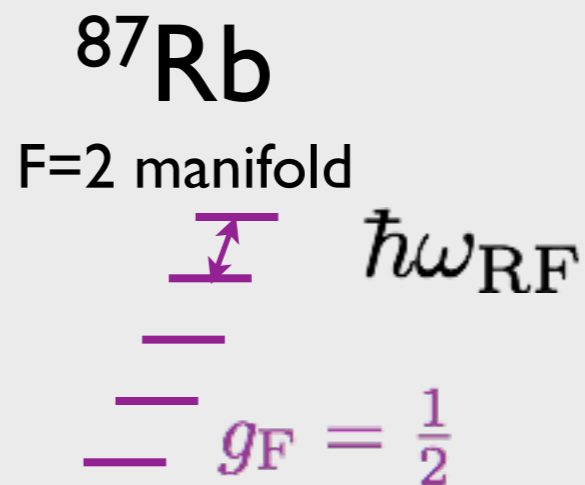
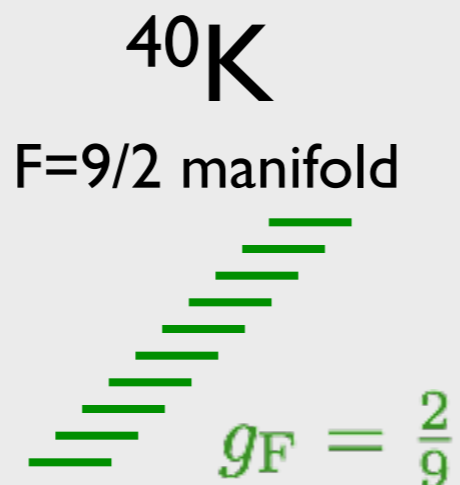
# Species-specific!



M. H. T. Extavour, *Atomic Physics* **20**, 241 (2006)

## Why?

Zeeman shifts:  
(& selection rules)



# Towards a direct observation of number squeezing



# Josephson effect: history

“external” effect:

- superconductors (Josephson 1962)
- $^4\text{He}$  or  $^3\text{He}$  through a narrow channel (Anderson 1966, Avenel&Varoquaux 1988)
- Kasevich (1998); Oberthaler (2005)

“internal” effect:

- NMR in superfluid  $^3\text{He}$  (Leggett 1975)
- Cornell/Wieman (1998)

# Model for double well

$$H = \frac{U}{2}M^2 + \frac{J}{2}\phi^2$$

where

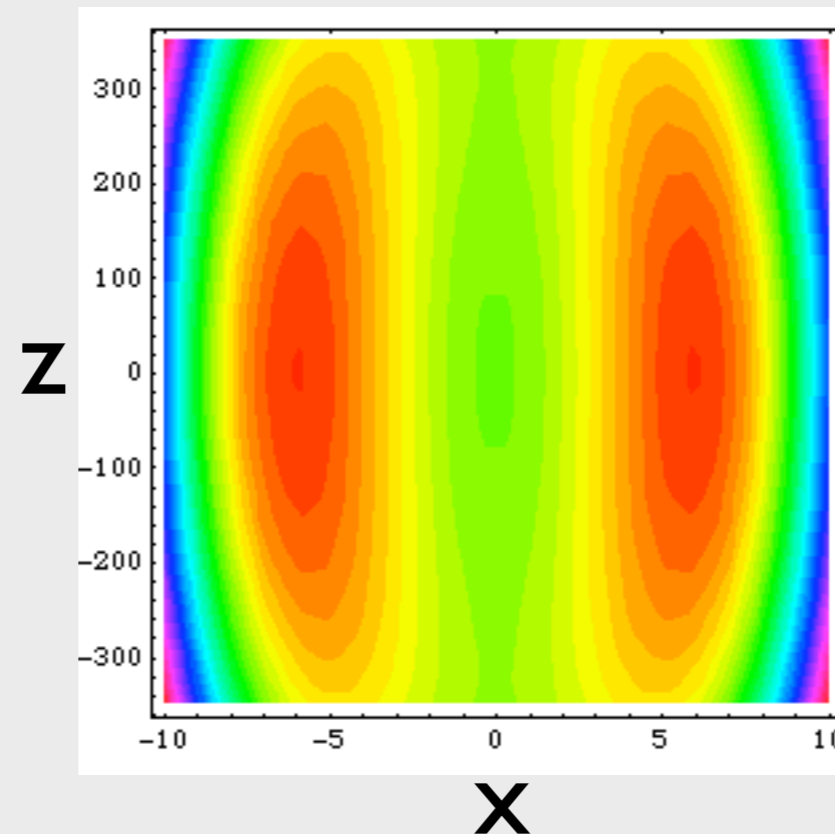
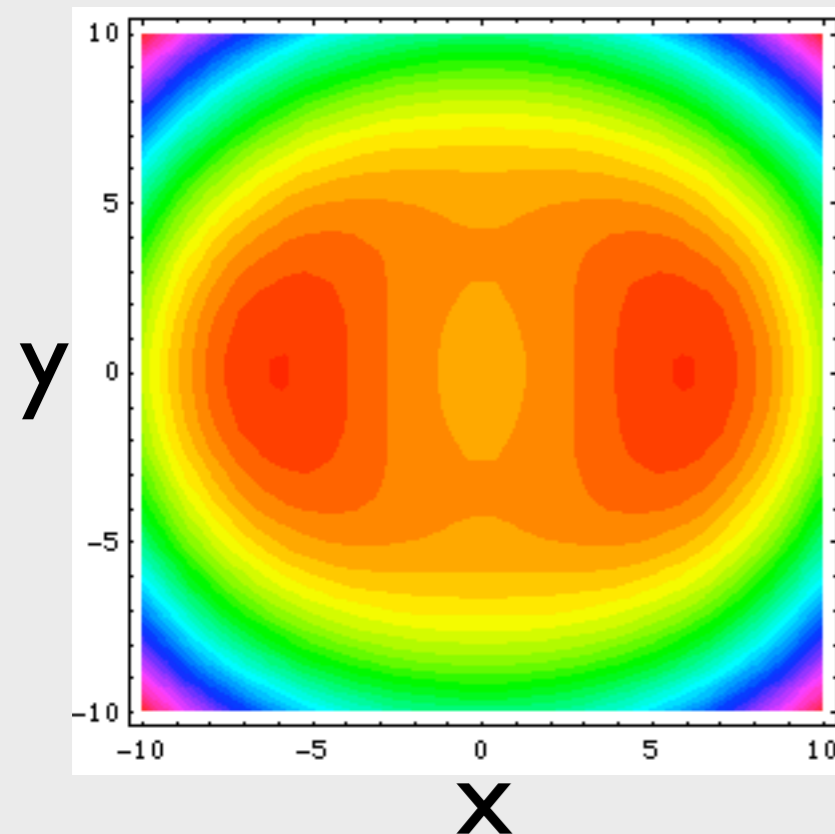
$U$  = charging energy

$J$  = tunneling strength

$M$  = number diff / 2

$\phi$  = relative phase

potential:

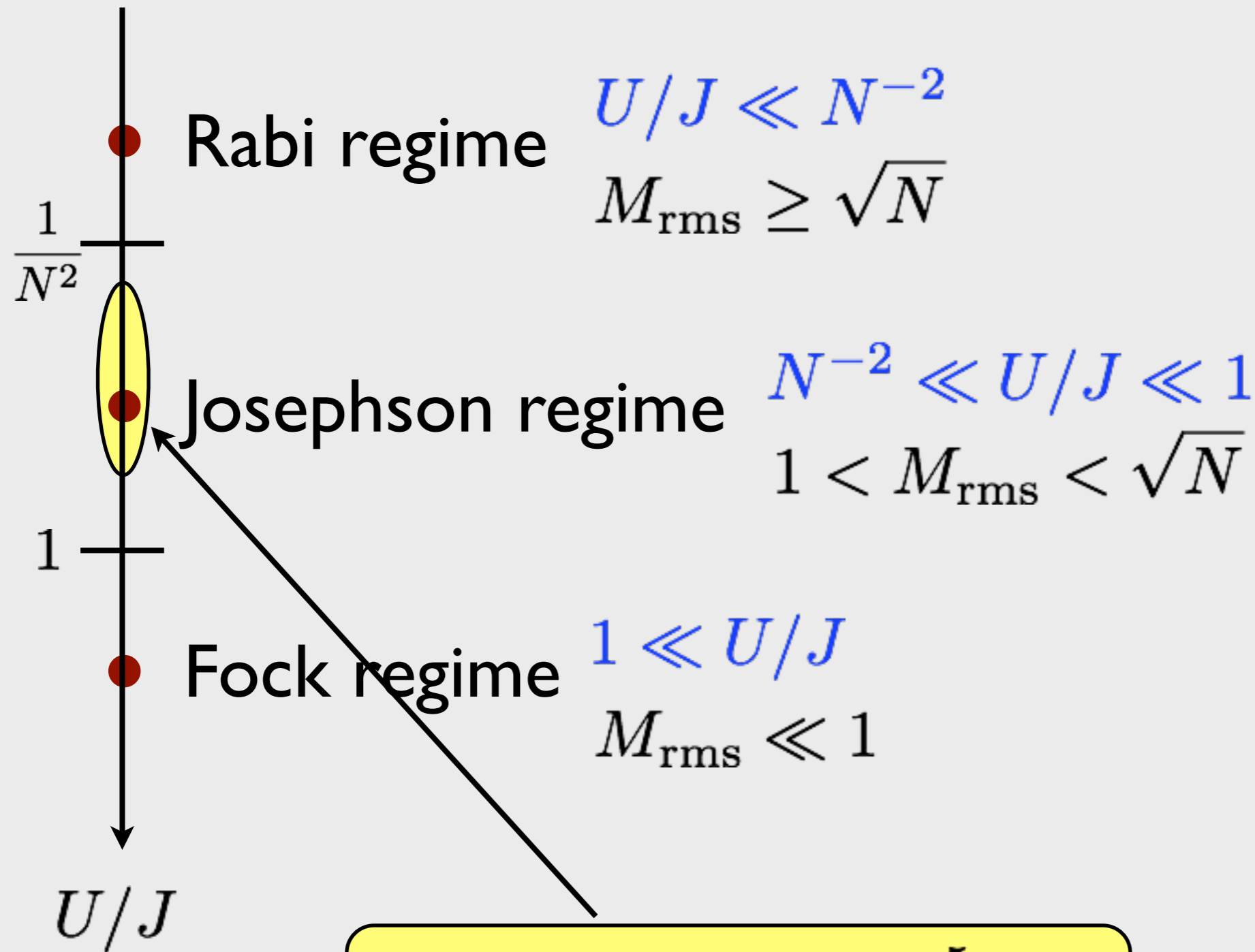


well separation:  
0 to 200 $\mu\text{m}$  (here 10 $\mu\text{m}$ )

junction area:  
5 $\mu\text{m}$  x 100 $\mu\text{m}$

atom number:  
10<sup>3</sup> to 10<sup>4</sup>

# regimes of $U/J$



reminiscent of:

SF

Mott

(when  $N \sim 1$ )

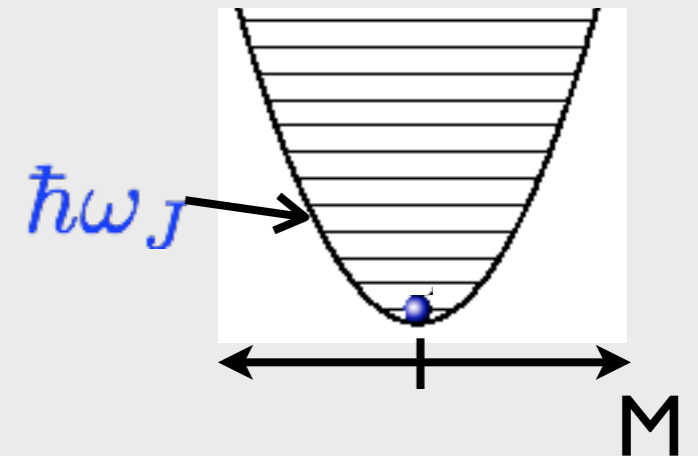


# Josephson physics

Classical oscillation frequency

$$\hbar\omega_J = \sqrt{UJ}$$

also the level spacing near ground state:



Ground state  $\langle M \rangle = 0$  has width

$$M_{\text{rms}} = (J/U)^{1/4}$$

Basic idea:

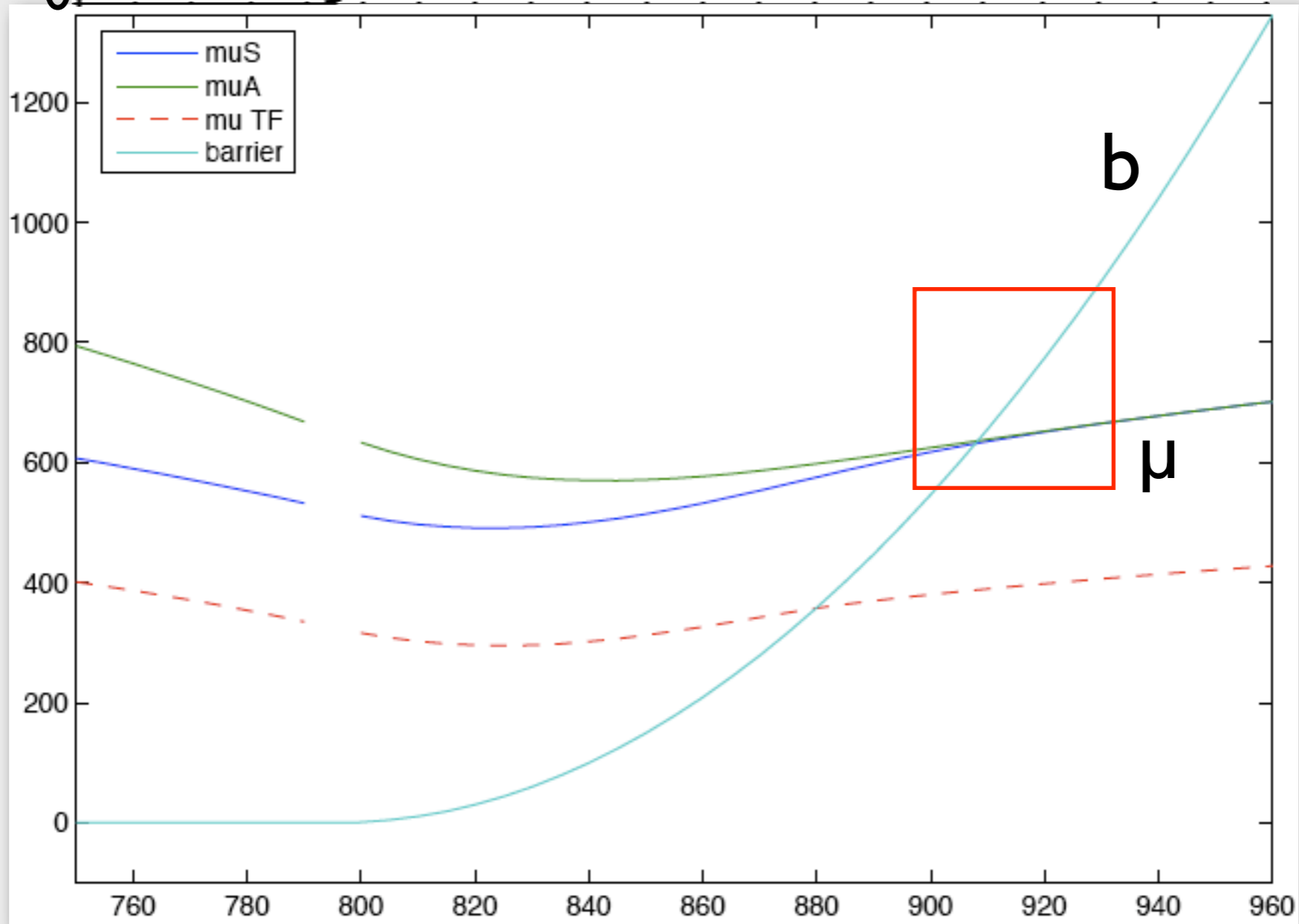
Tune **J** by increasing double-well separation. Look for reduced quantum fluctuation of ground state.

# Tuning

splitting ( $\mu\text{m}$ )

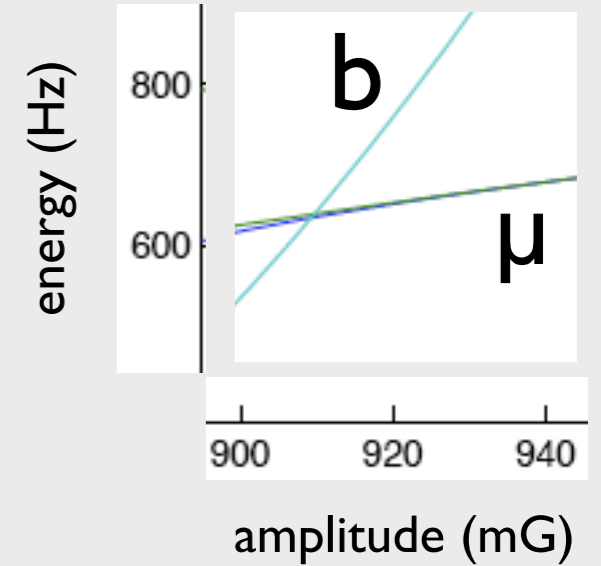
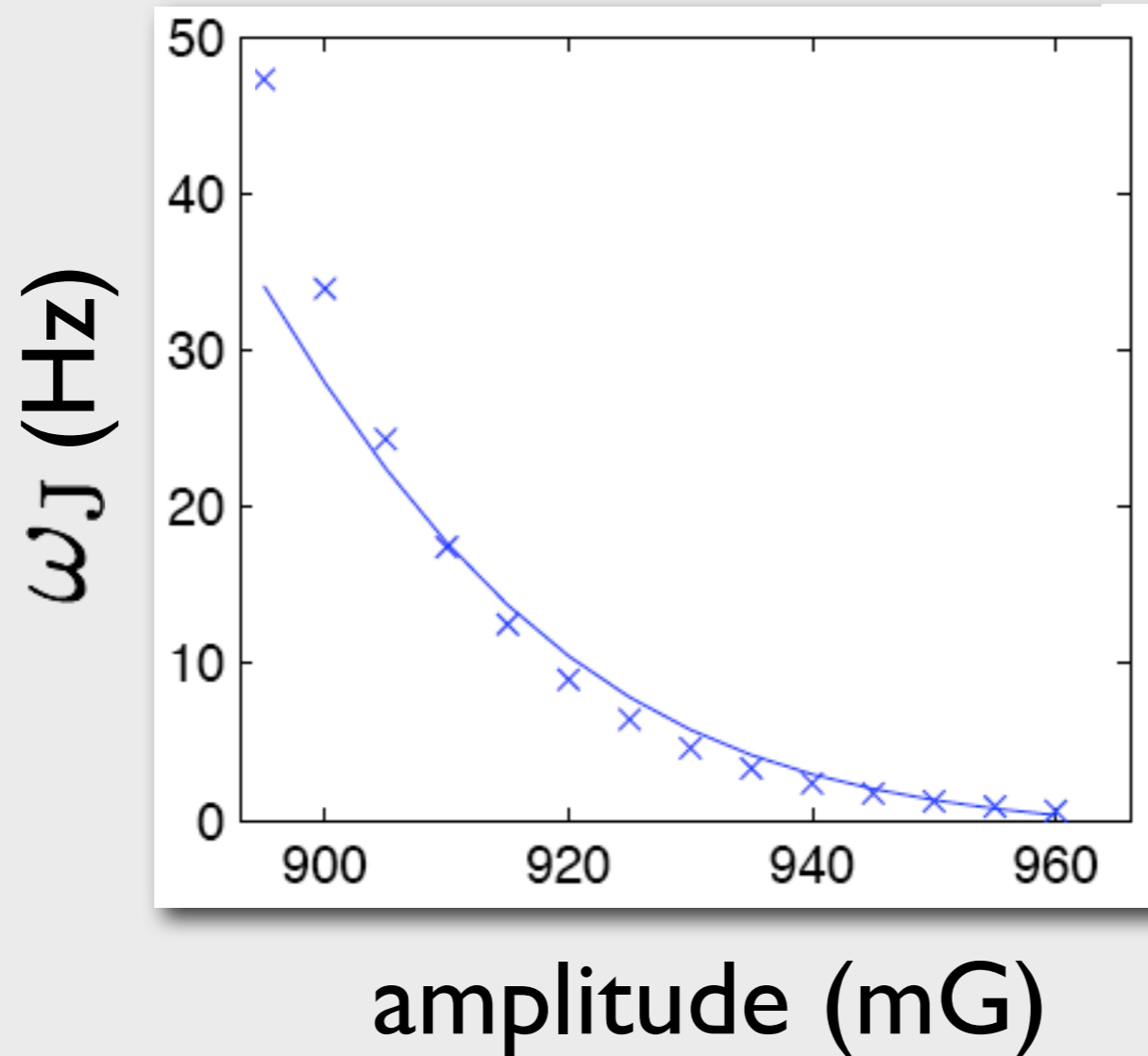
4  
2  
0

energy (Hz)



amplitude (mG)

# Splitting



$U \sim 0.1$  Hz  
 $J \sim 5$  kHz

**x** = simple exponential fit:  
decreases  $1/e$  in 15 mG

# Adiabatic-to-nonadiabatic evolution

- Ground state variance decreases so long as evolution adiabatic:

$$\dot{\omega}_J \ll \omega_J^2 \quad \text{adiabatic}$$

- Assume that  $M_{\text{rms}}$  “freezes” when  $\dot{\omega}_J \sim \omega_J^2$
- If  $\omega_J = \omega_J^0 e^{-t/\tau}$  then this transition occurs when  $\omega_J = 1/\tau$  or:

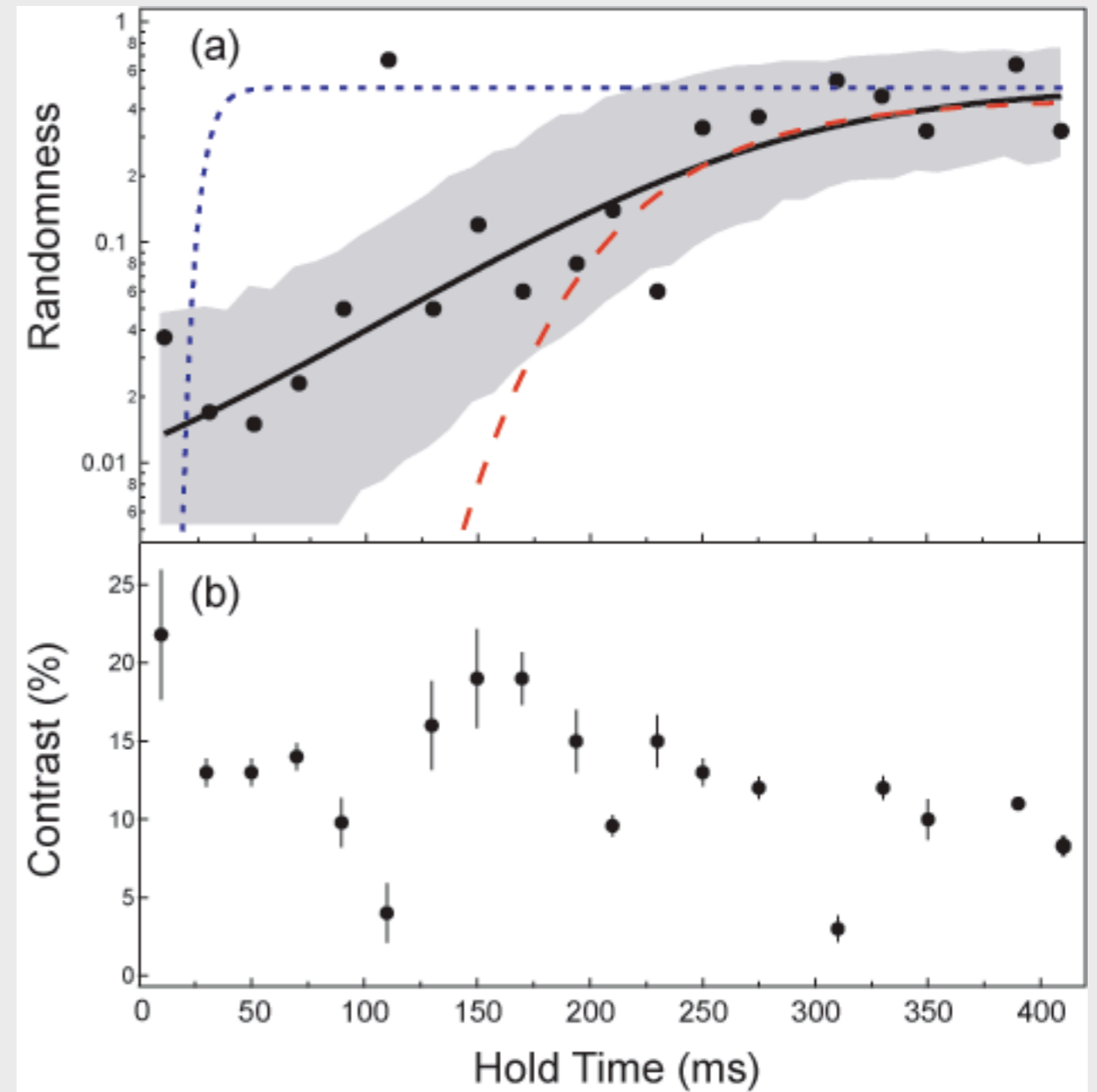
$$M_{\text{rms}} = \sqrt{\frac{\hbar}{U\tau}}$$

& thus

$$\frac{M_{\text{rms}}}{\sqrt{N}} \sim \sqrt{\frac{\hbar}{\mu\tau}}$$

# Evidence of JJ number squeezing

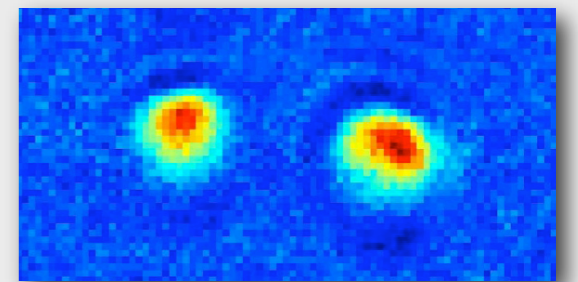
- measure width of phase distribution at various hold times
- Compare to expectation for coherent state
- Initial M spread leads to phase spread at long t
- Factor of 10 squeezing agrees with adiabatic est.



G. B. Jo ...W.Ketterle PRL **98**, 030207 (2007)  
(see also: Kasevich, 2007)

# Towards a direct measurement

- To date, measurements on coupled/split BEC systems have been exclusively on the phase
- We are developing sub-shot-noise *number* measurements
- Motivation:
  - direct, unambiguous signature
  - independent of dephasing physics
  - study role of adiabaticity
  - applicable to Fermions



status:

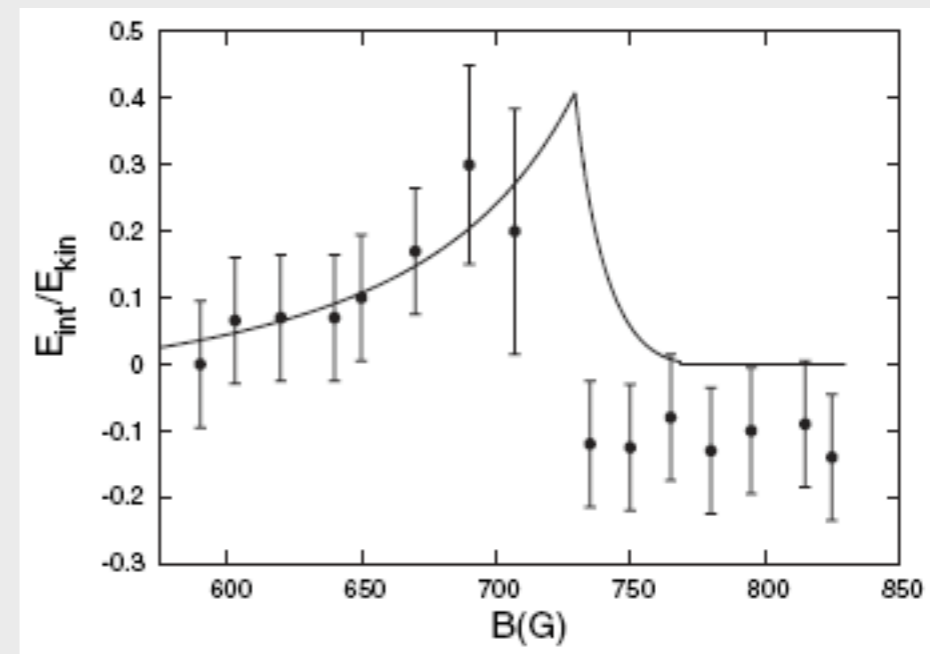
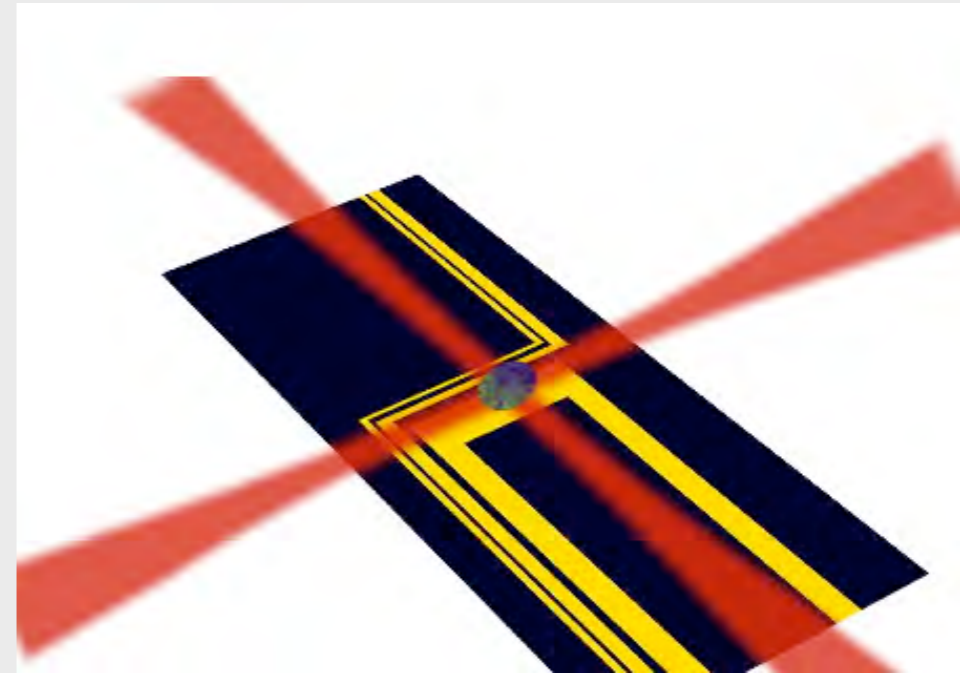


And just in case that wasn't  
enough to chat about...

# Strongly interacting fermions

- Transfer 40K to crossed dipole trap
- go to Feshbach resonance (200G).
- Measure spin coherence time:  
“Itinerant magnetism?”

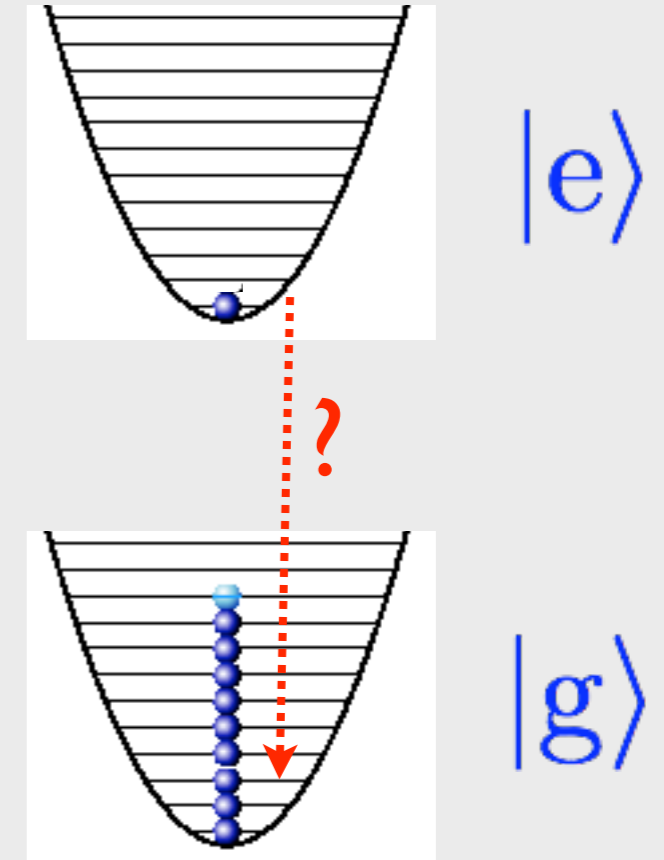
RA Duine, AH MacDonald, →  
PRL **95**, 230403 (2005)





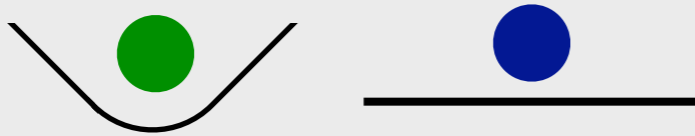
# Light scattering off Fermions

- New analytics: can now do calculation for full 3D problem without symmetries
- In the lab:
  - optical trapping holds all mF states
  - internal state tagging
  - high ER/EF possible

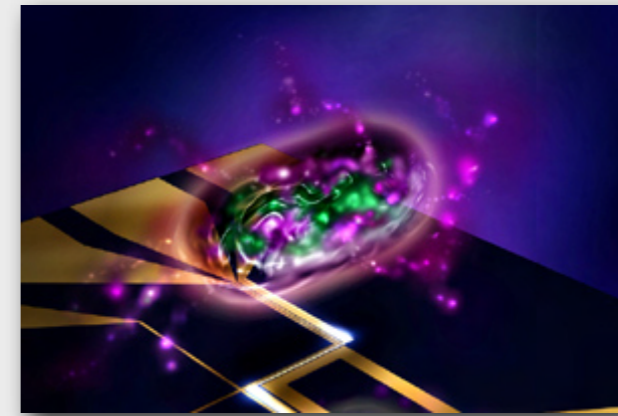


# Summary

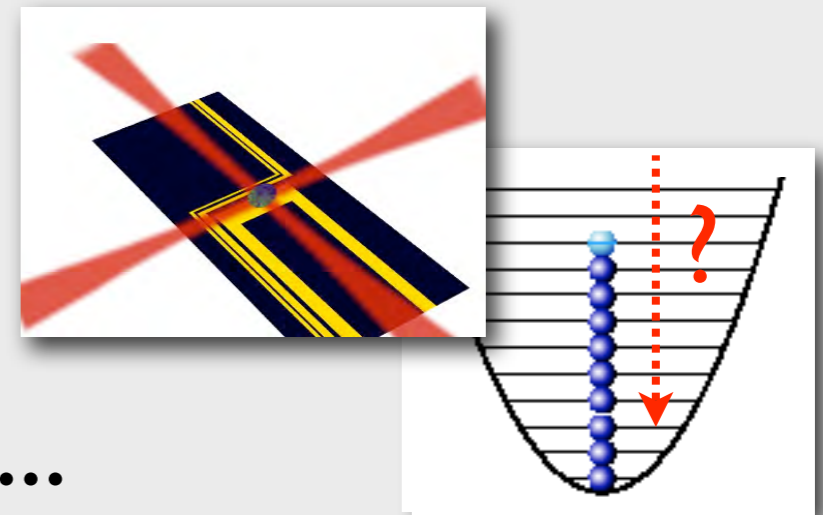
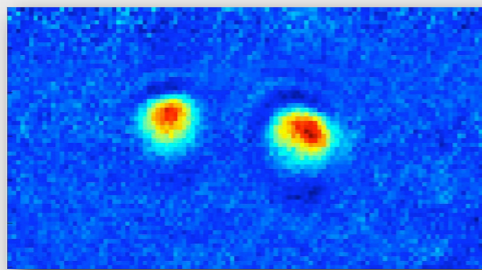
Species selective environments



DFG with  $\mu$ fab trap



Double well potentials & fluctuation statistics



etc...



Thank you!

