



**YbRb**  
**A Candidate for an Ultracold  
Paramagnetic Molecule**

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# Outline

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- 1. Introduction: The Yb-Rb system**
- 2. Yb + Rb: Interactions in a conservative trap**
- 3. YbRb\* : Photoassociation spectroscopy**
- 4. Towards YbRb in the ground state:  
Feshbach resonances and/or  
Photoassociation**

# 1. Introduction: The Yb-Rb system

# Why Ytterbium and Rubidium?

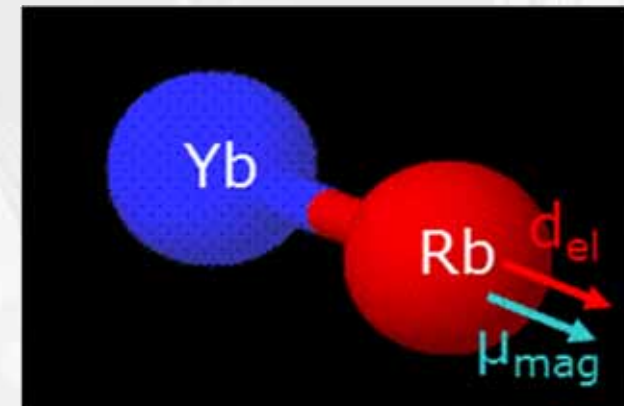
## Yb + Rb as a mixture



paramagnetic diamagnetic

- unexplored interactions
- independent manipulation
- optical and (possibly) magnetic Feshbach resonances
- 5 stable bosonic and 2 stable fermionic Yb isotopes

## YbRb as a molecule



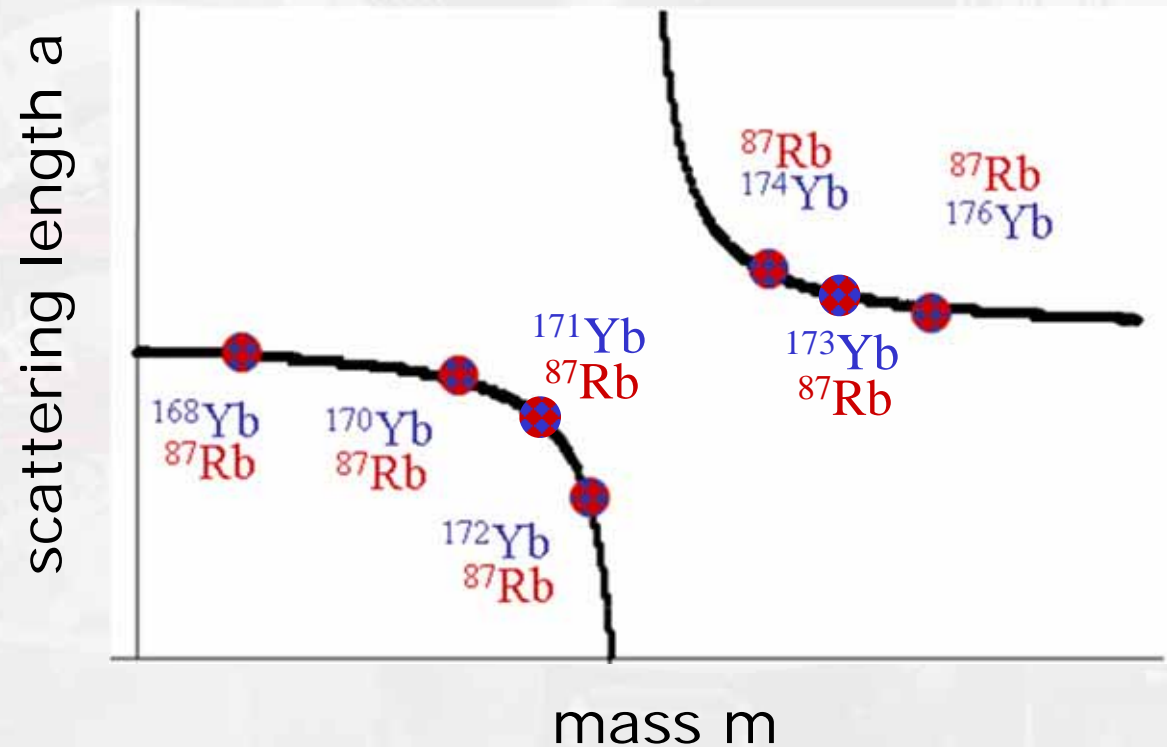
- heteronuclear
- $^2\Sigma_{1/2}$  ground state
- electric and magnetic dipole
- „toolbox“ for spin lattice models<sup>1</sup>

1) Micheli et al., Nature Physics 2, 341 (2006)

# Properties of Yb-Rb mixtures

## Heteronuclear scattering length (fictitious values)

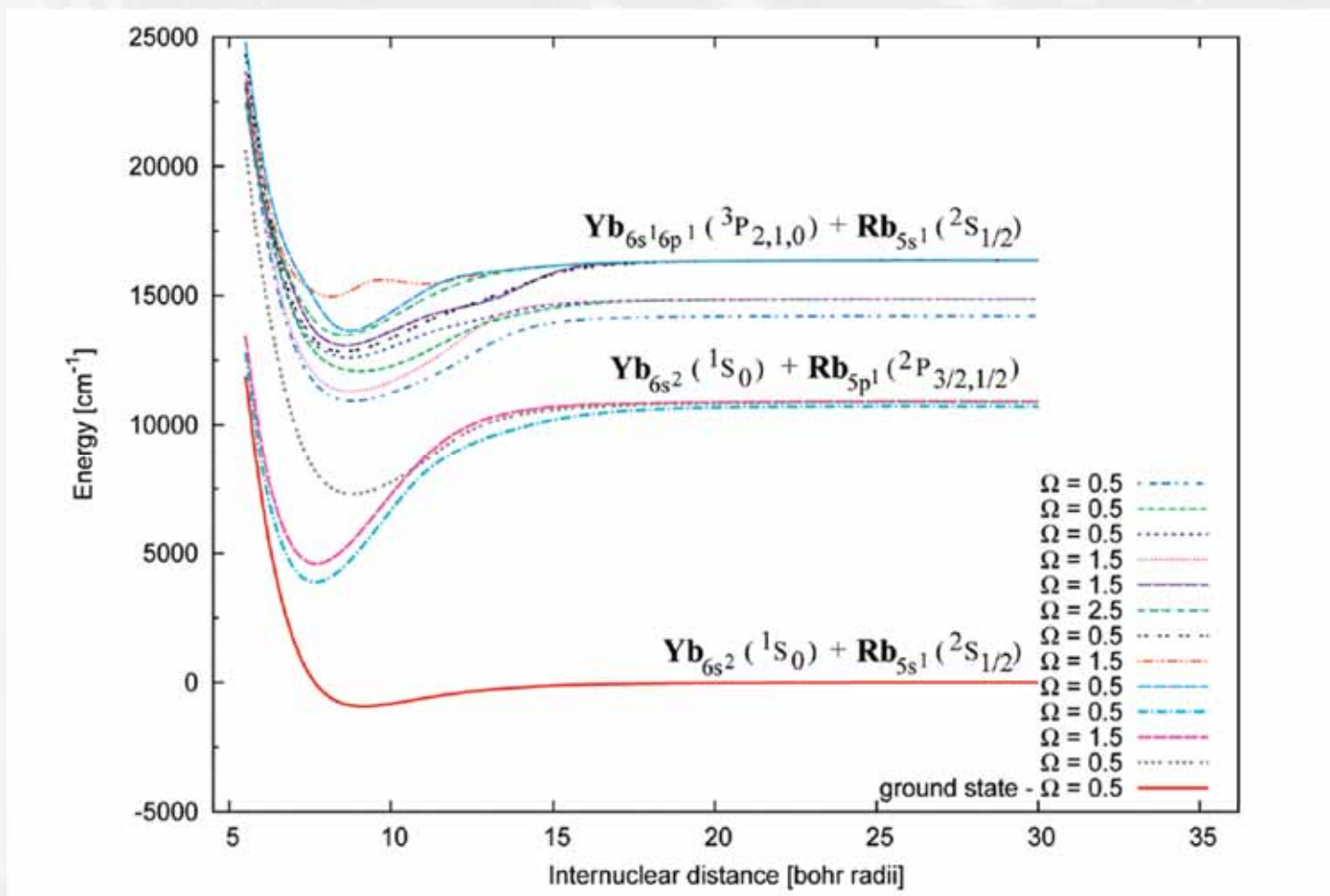
$^{87}\text{Rb}$   
+  
Bosons:  $^{168}\text{Yb}$ ,  $^{170}\text{Yb}$ ,  
 $^{172}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  
 $^{176}\text{Yb}$   
Fermions:  $^{171}\text{Yb}$ ,  $^{173}\text{Yb}$



⇒ **Wide range of interaction properties expected**

# YbRb-Molecules

## Ab-initio potentials:

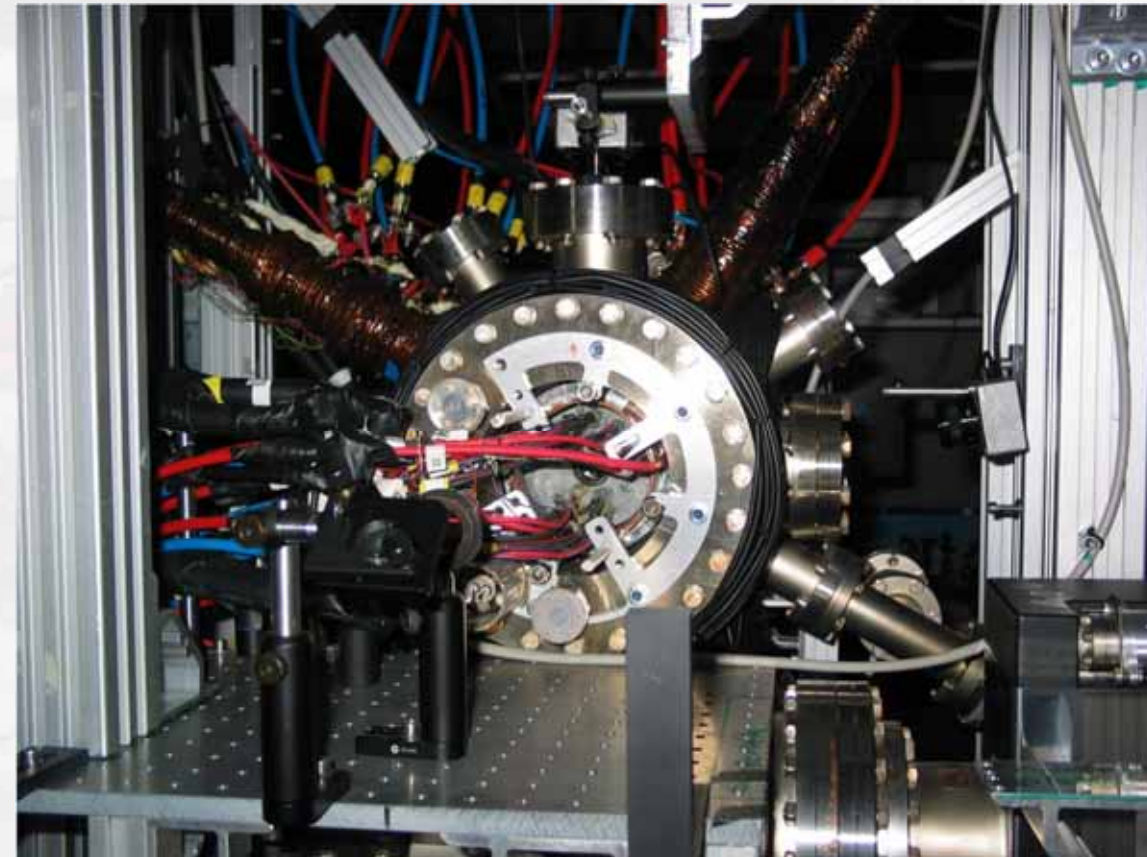
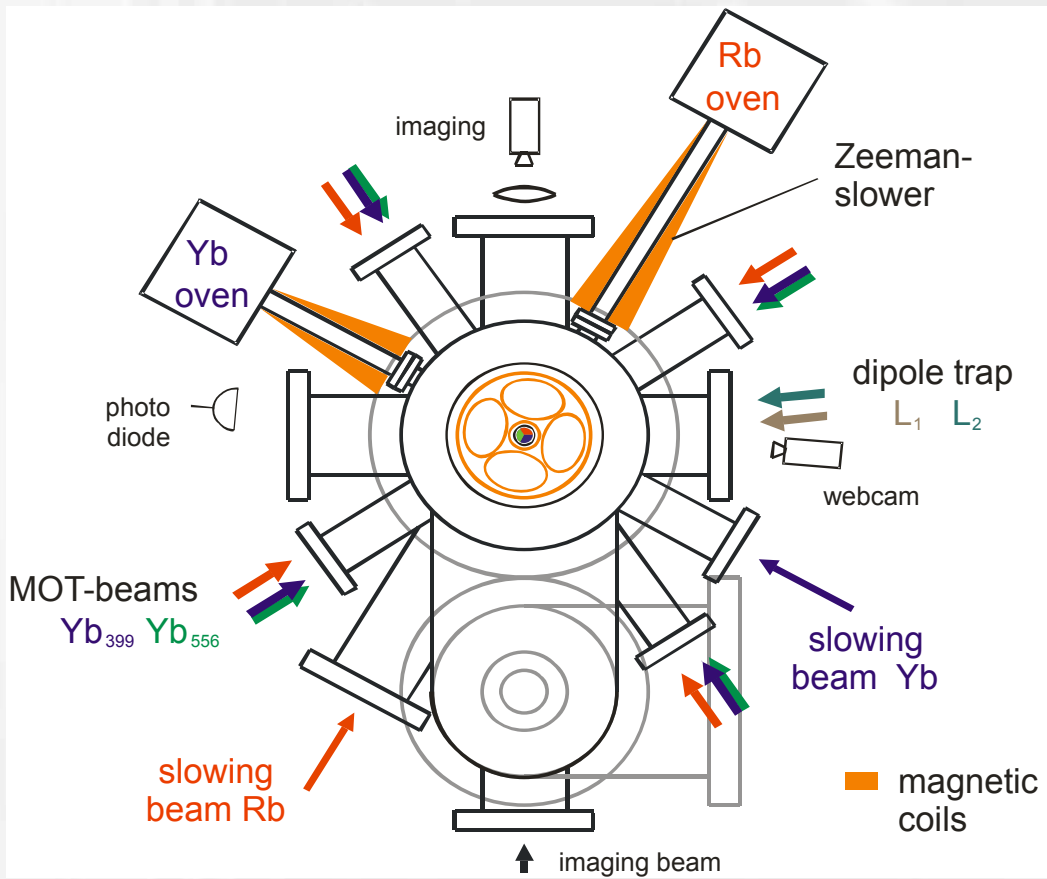


$$D_e \sim 865 \text{ cm}^{-1}$$

$$R_e \sim 8.85 a_0$$

**electric dipole  
moment:  
~ 1 Debye**

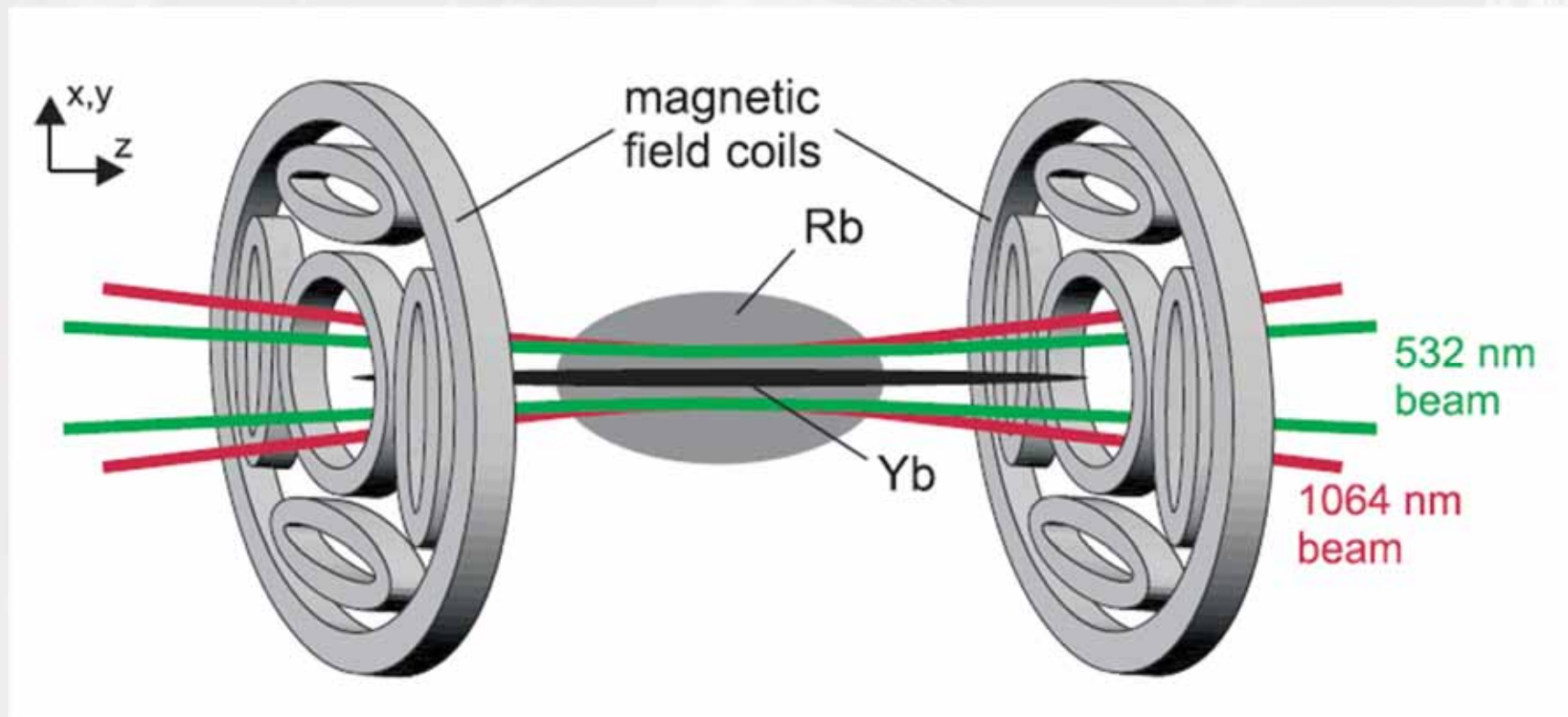
# The Machine



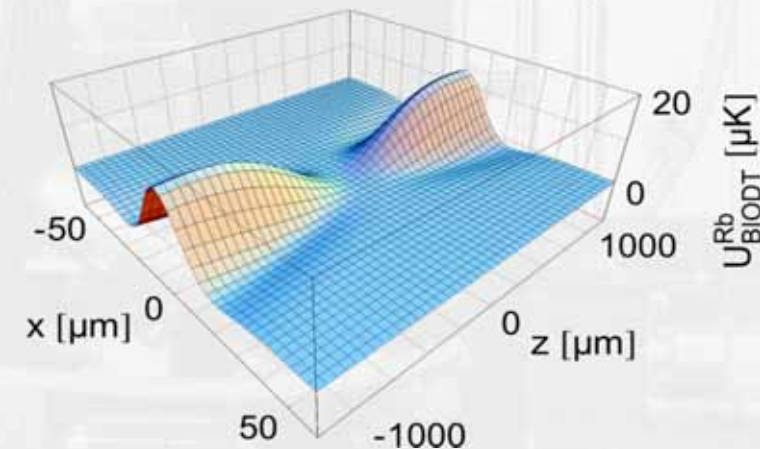
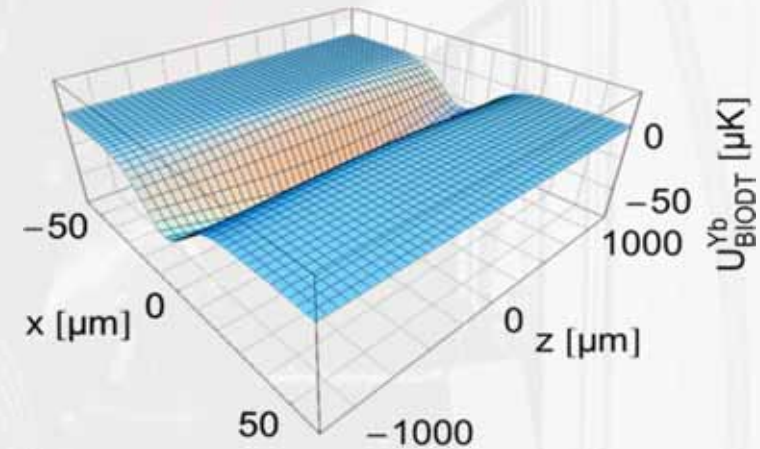
# 2. Yb + Rb: Interactions in a conservative trap



# The hybrid trap



# Bichromatic optical dipole trap

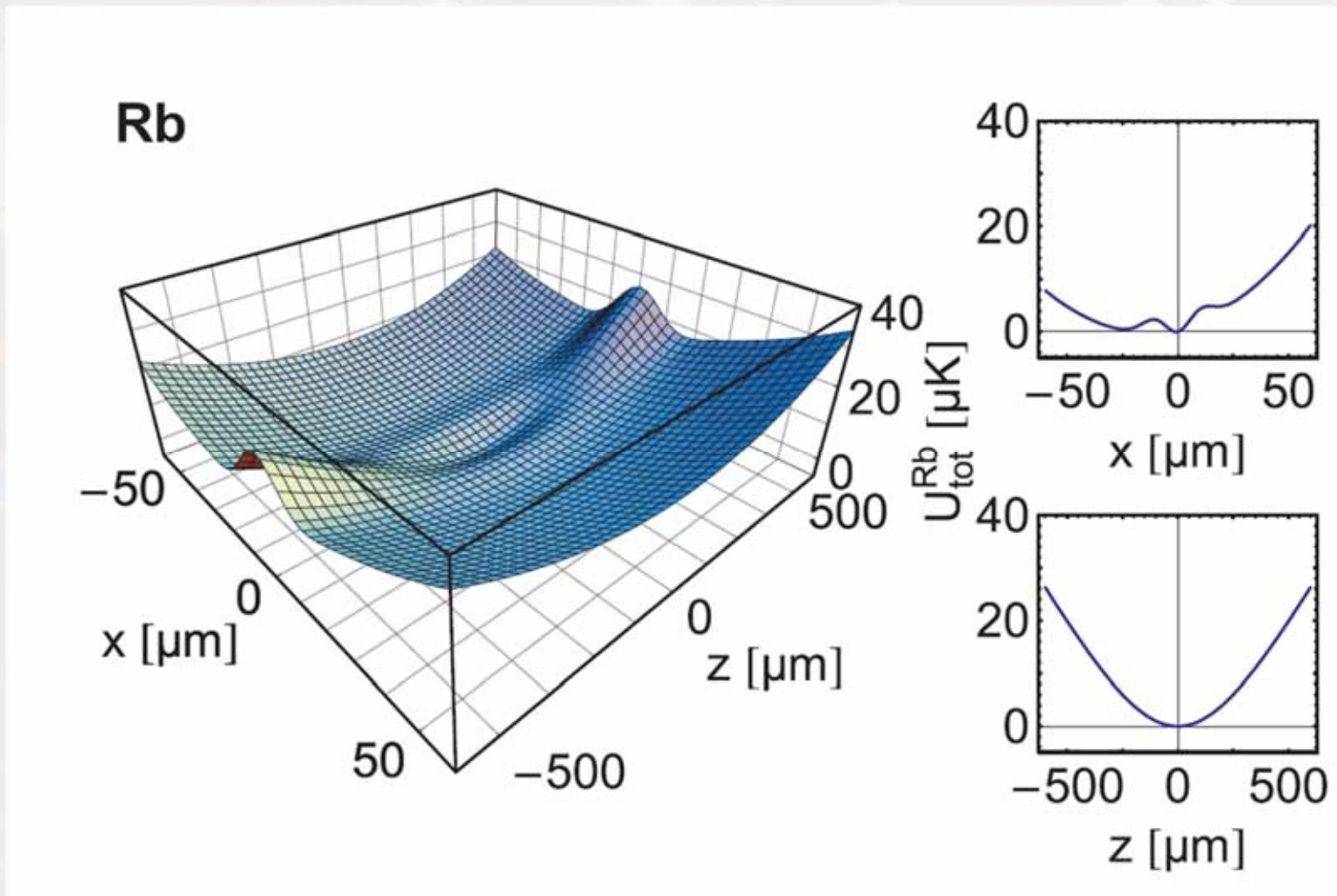


$$\begin{aligned}
 \lambda_{\omega_{\text{Yb}}} &< \lambda_{\text{ODT}1} &< \lambda_{\text{Rb}} &< \lambda_{\text{ODT}2} \\
 399 \text{ nm} &< 532 \text{ nm} &< \begin{matrix} 780 \text{ nm} \\ 795 \text{ nm} \end{matrix} &< 1064 \text{ nm}
 \end{aligned}$$

$$U_{532}(r=0) = U_{1064}(r=0)$$

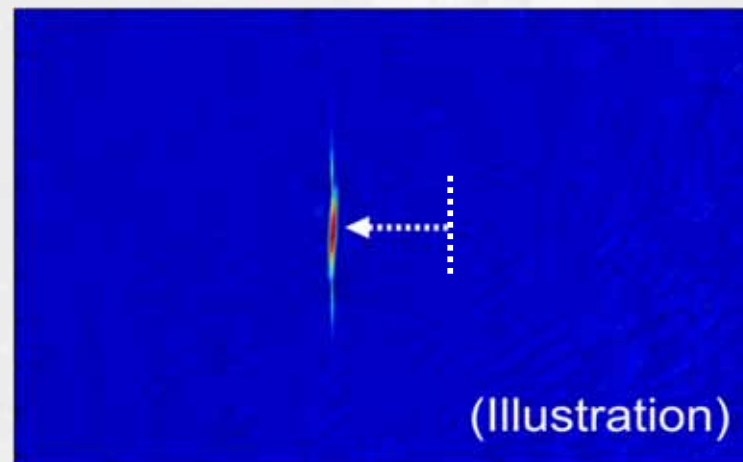
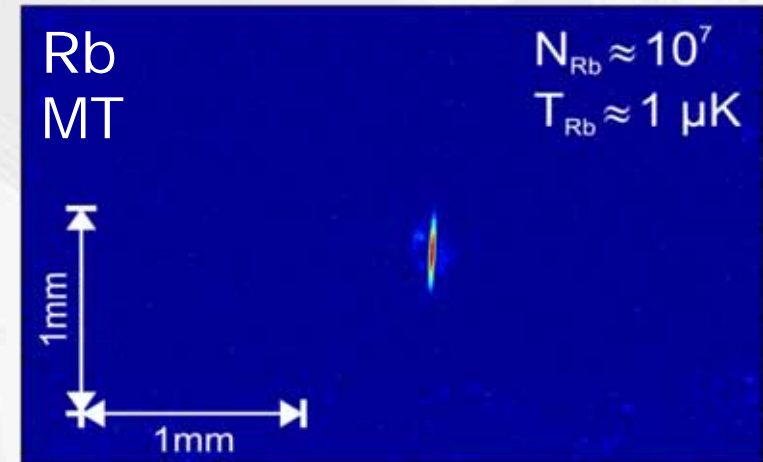
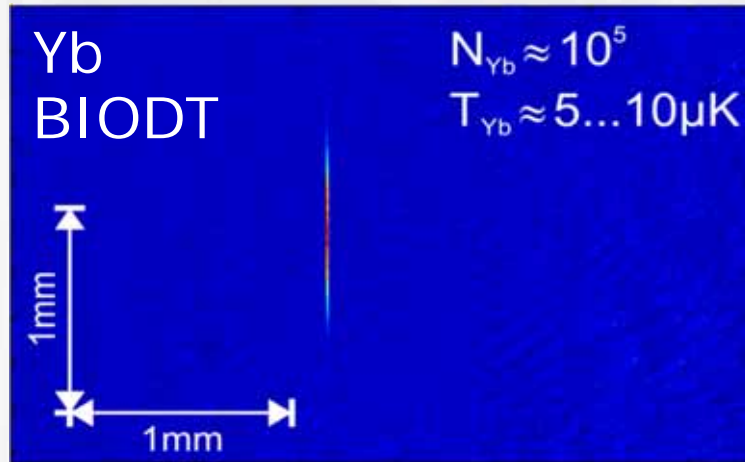
# Bichromatic optical dipole trap

„Real“ potential:



# Collisions at $\mu\text{K}$ -temperatures

Pure s-wave collisions (p-wave threshold  $\sim 60 \mu\text{K}$ )



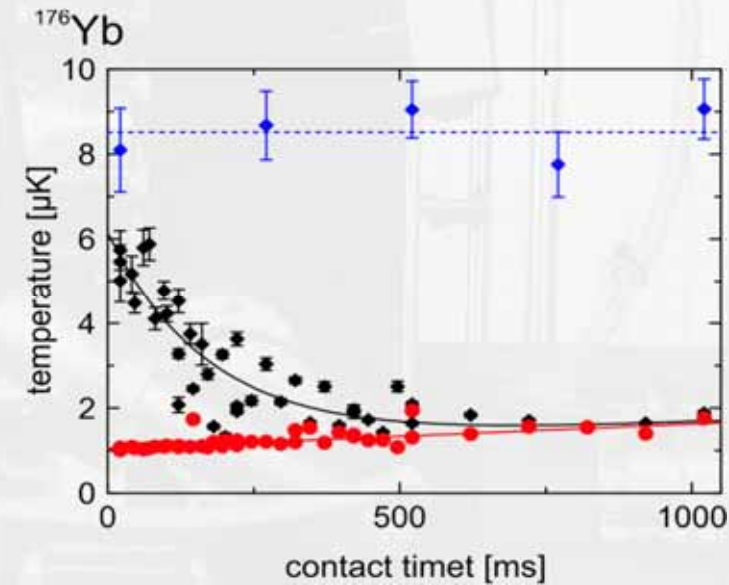
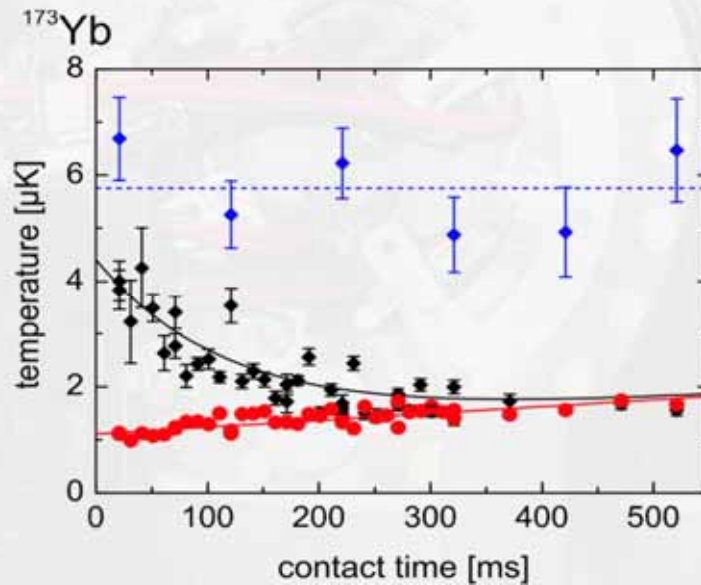
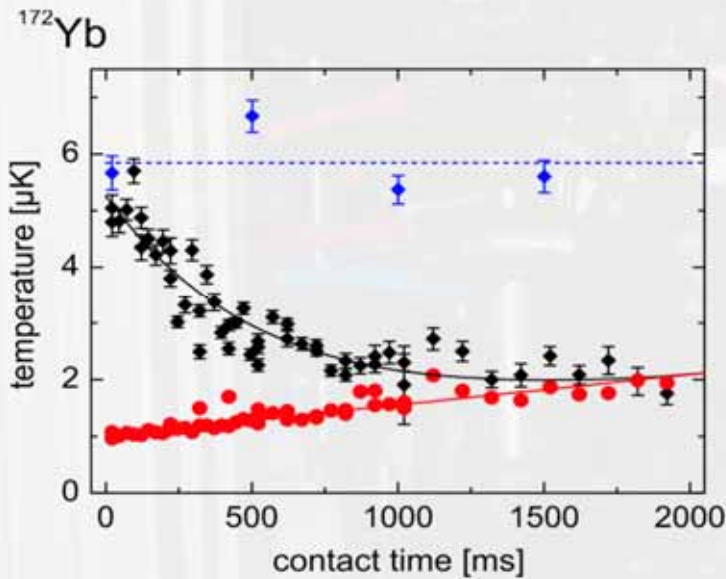
defined spatial overlap  
between Yb and Rb cloud

# Thermalization

... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$   
 $\Rightarrow$  strong isotope dependence

normal behavior

◆ Yb without Rb   ◆ Yb with Rb   ● Rb



# Thermalization

... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

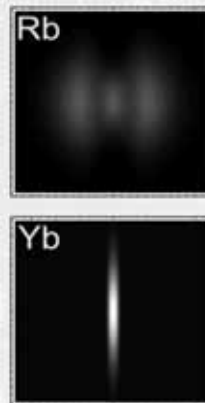
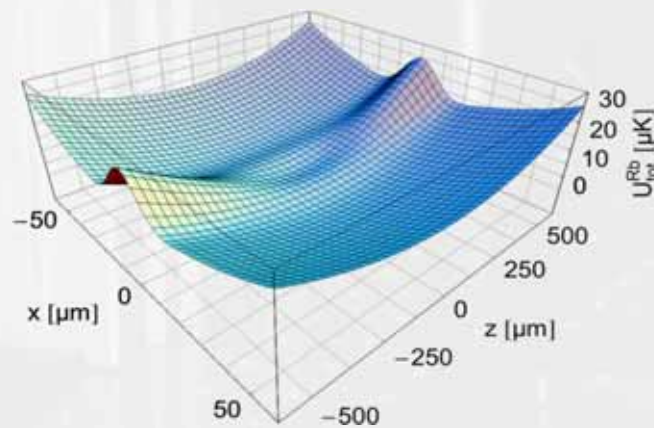
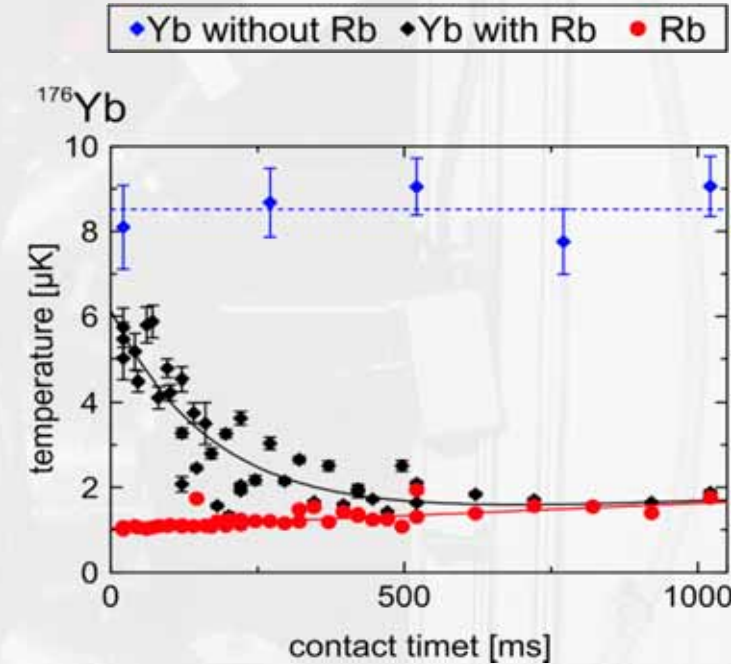
## quantitative analysis:

thermalization rate

Yb-Rb scattering cross section

overlap integral

$$\gamma_{\text{Th}} \propto n_{\text{YbRb}} \cdot \sigma_{\text{YbRb}}$$



**in this trap geometry:**

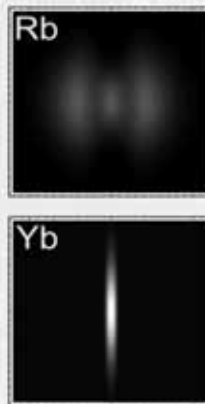
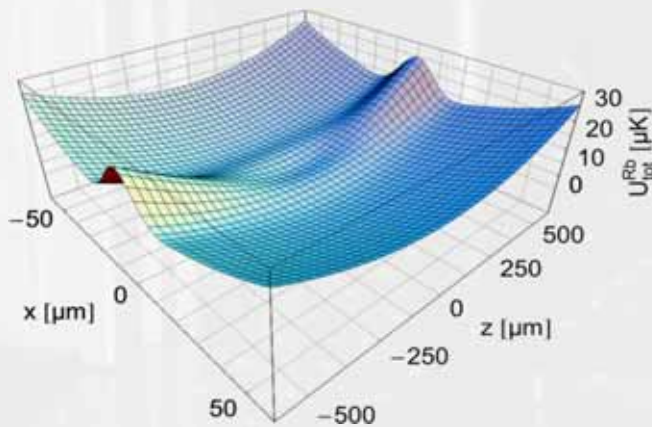
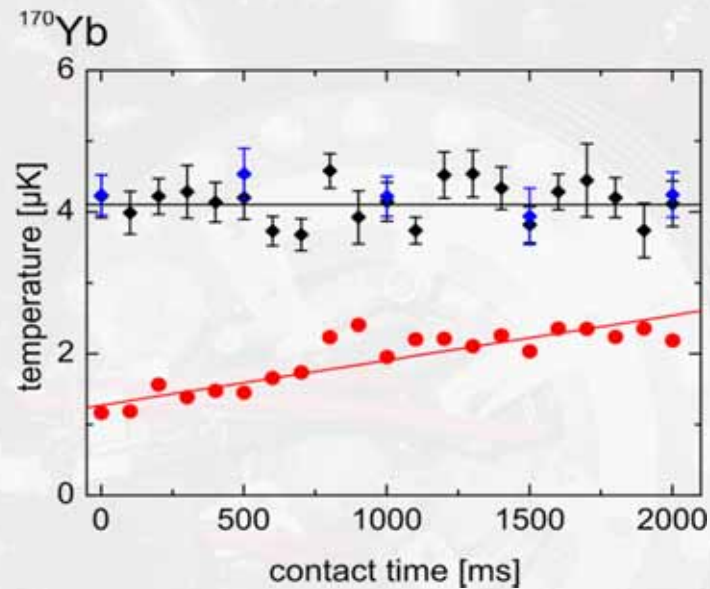
$n_{\text{YbRb}}$  hard to control

$\Rightarrow$  only relative values for  $\sigma_{\text{YbRb}}$  can be reliably deduced

# Thermalization

... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

extraordinary behavior

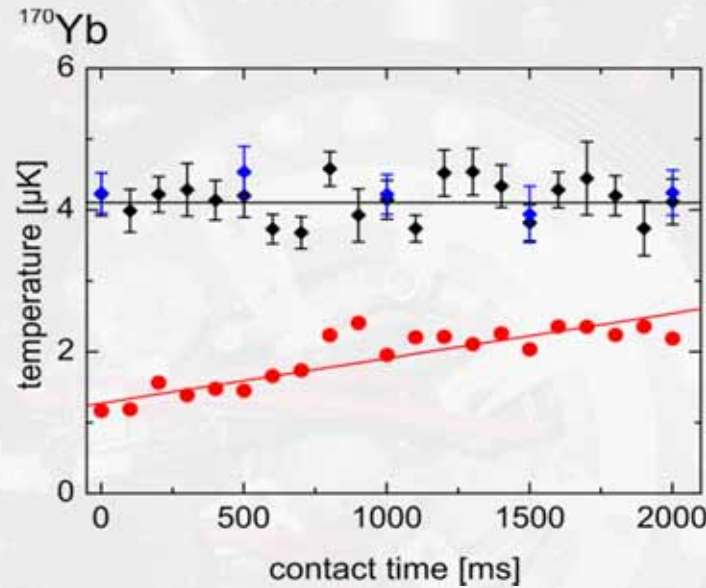


$^{170}\text{Yb}$  does not thermalize at all  
 $\Rightarrow$  (extremely) small elastic scattering cross section for this isotope

# Thermalization

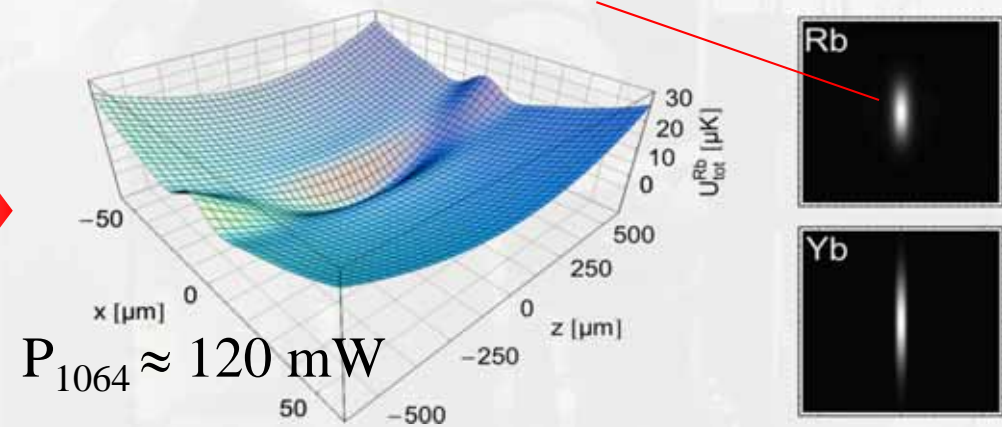
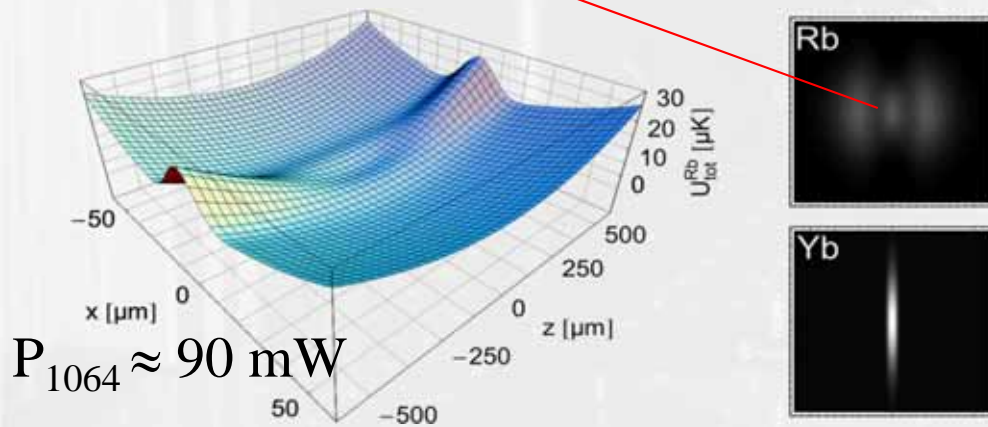
... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

extraordinary behavior



$n_{\text{Rb}} \approx 10^{10} \dots 10^{11} \text{ cm}^{-3}$

$n_{\text{Rb}} \approx 10^{13} \dots 10^{14} \text{ cm}^{-3}$

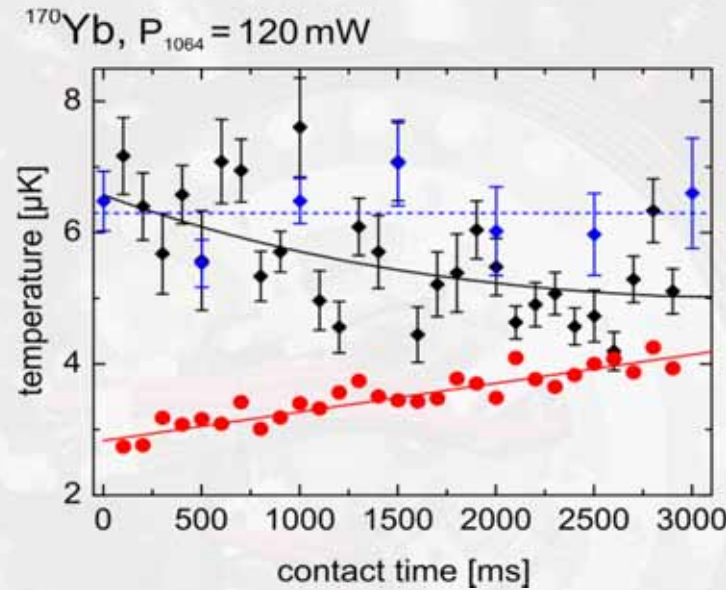




# Thermalization

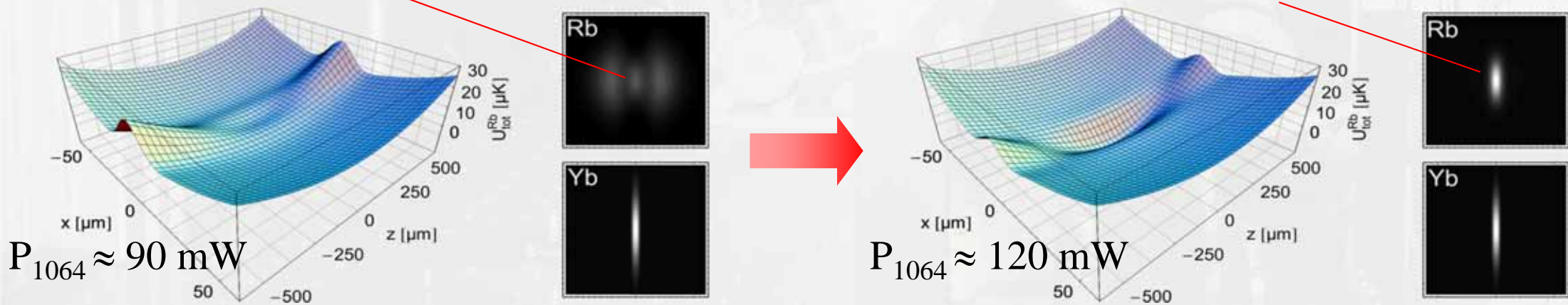
... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

extraordinary behavior



$n_{\text{Rb}} \approx 10^{10} \dots 10^{11} \text{ cm}^{-3}$

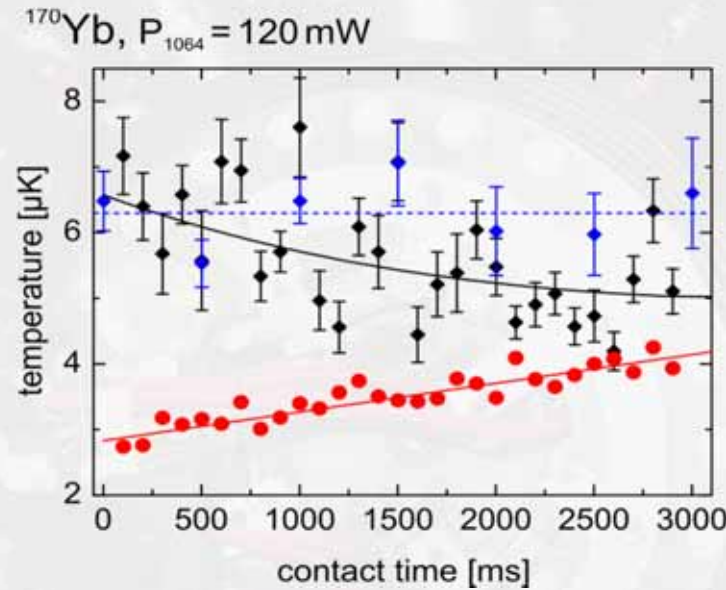
$n_{\text{Rb}} \approx 10^{13} \dots 10^{14} \text{ cm}^{-3}$



# Thermalization

... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

extraordinary behavior



better control of  $n_{\text{YbRb}}$

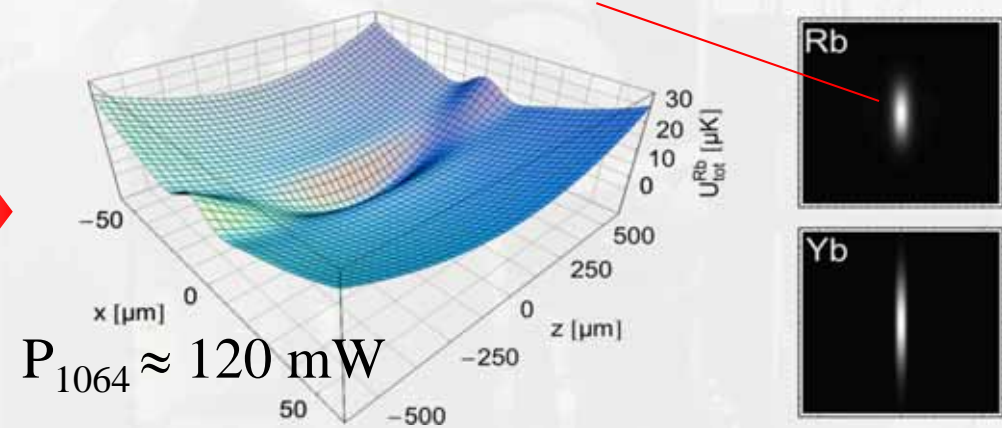
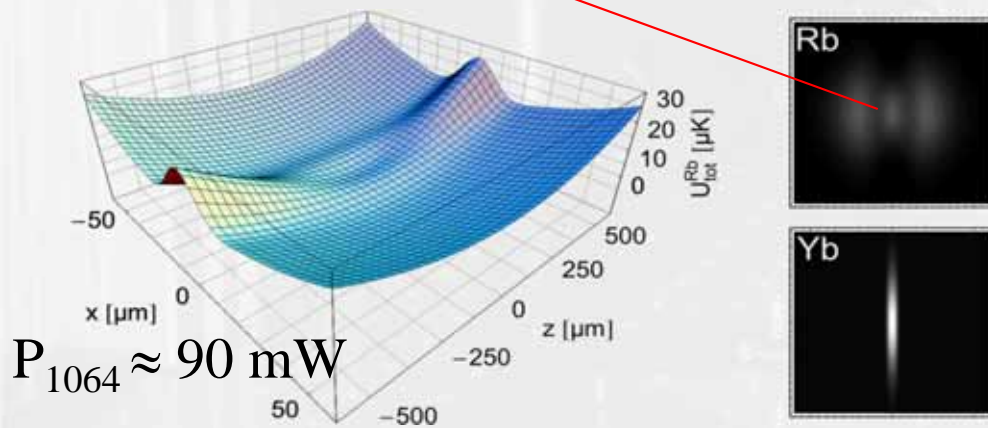
$$\Rightarrow \sigma_{\text{YbRb}} = 4 \pi a^2$$

$\Rightarrow$  scattering length:

$$|a_{170-87}| \sim 10 a_0$$

$$n_{\text{Rb}} \approx 10^{10} \dots 10^{11} \text{ cm}^{-3}$$

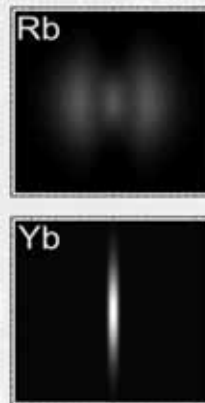
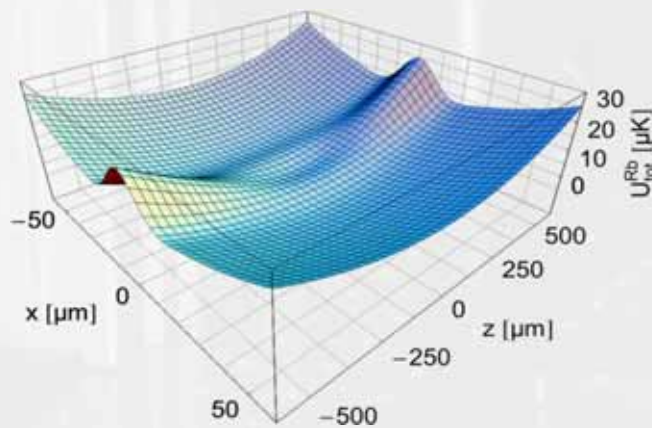
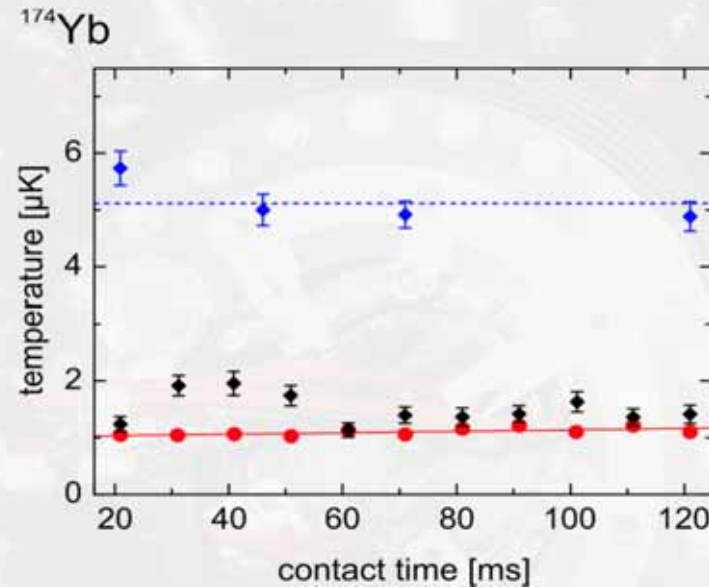
$$n_{\text{Rb}} \approx 10^{13} \dots 10^{14} \text{ cm}^{-3}$$



# Thermalization

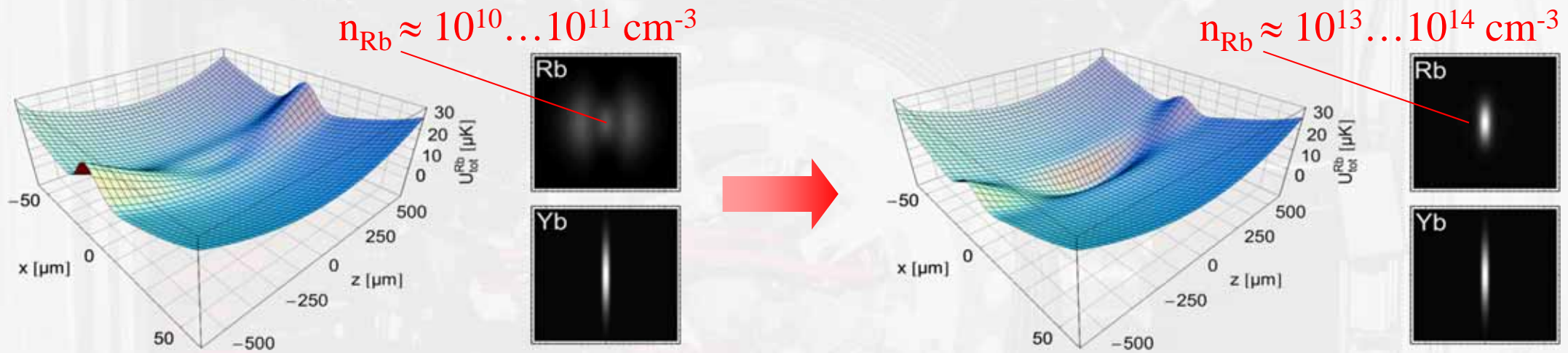
... between  $^{170}\text{Yb}$ ,  $^{172}\text{Yb}$ ,  $^{173}\text{Yb}$ ,  $^{174}\text{Yb}$ ,  $^{176}\text{Yb}$  and  $^{87}\text{Rb}$

extraordinary behavior



$^{174}\text{Yb}$  thermalizes instantaneously  
 $\Rightarrow$  (extremely) large elastic scattering cross section for this isotope

# $^{174}\text{Yb}$ – $^{87}\text{Rb}$ mixture at large $n_{\text{Rb}}$



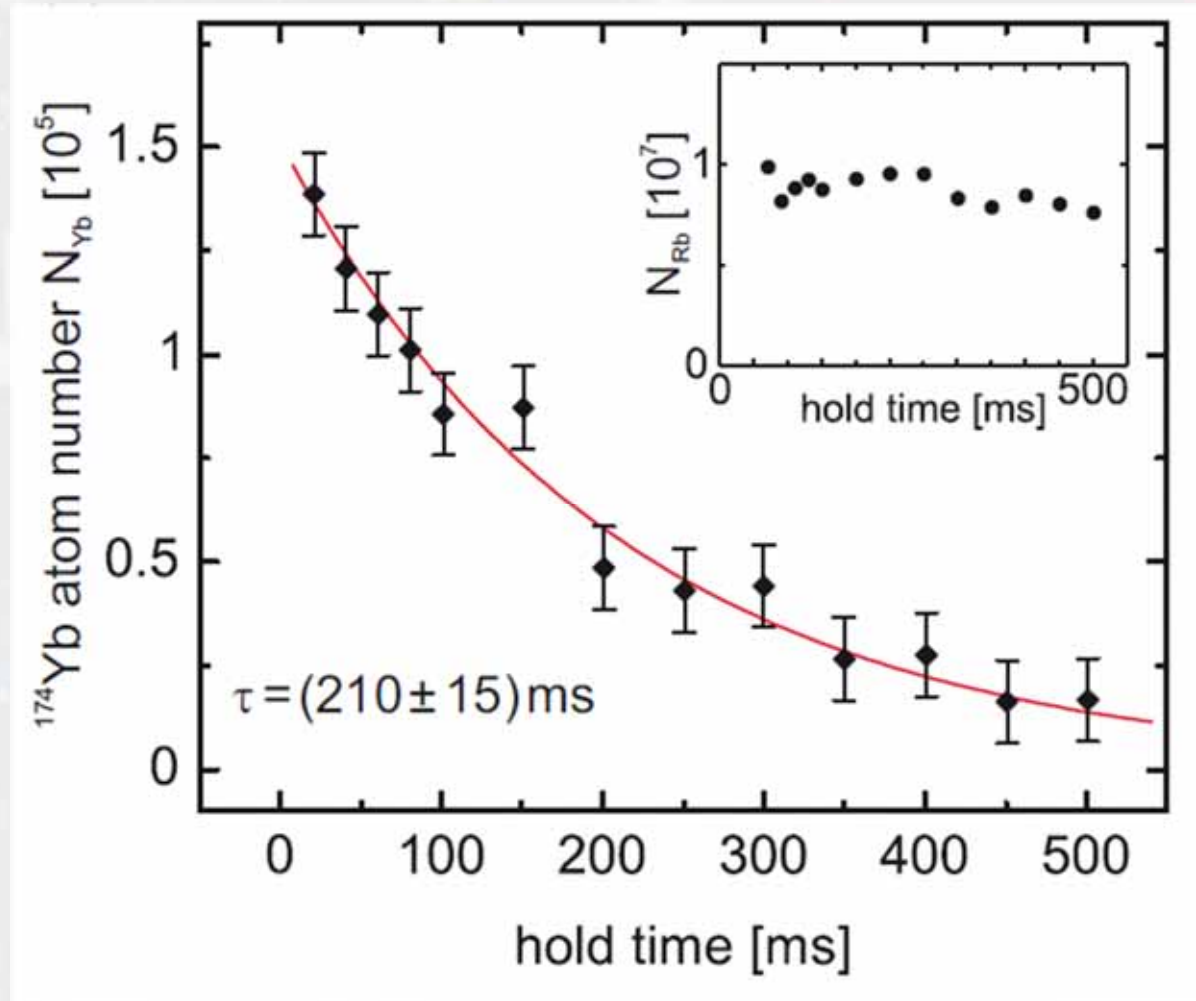
$^{174}\text{Yb}$  thermalized with  $^{87}\text{Rb}$

**trap frequencies:**

$\omega_r \sim 1 \text{ kHz}$ ,  $\omega_z \sim 10 \text{ Hz}$

?

# $^{174}\text{Yb}$ – $^{87}\text{Rb}$ mixture at large $n_{\text{Rb}}$



⇒ fast loss of  $^{174}\text{Yb}$  attributed to large 3-body loss

# Spatial separation of $^{174}\text{Yb}$ and $^{87}\text{Rb}$

$$T \approx 3 \mu\text{K}$$

$$N_{\text{Yb}} \approx 10^5$$

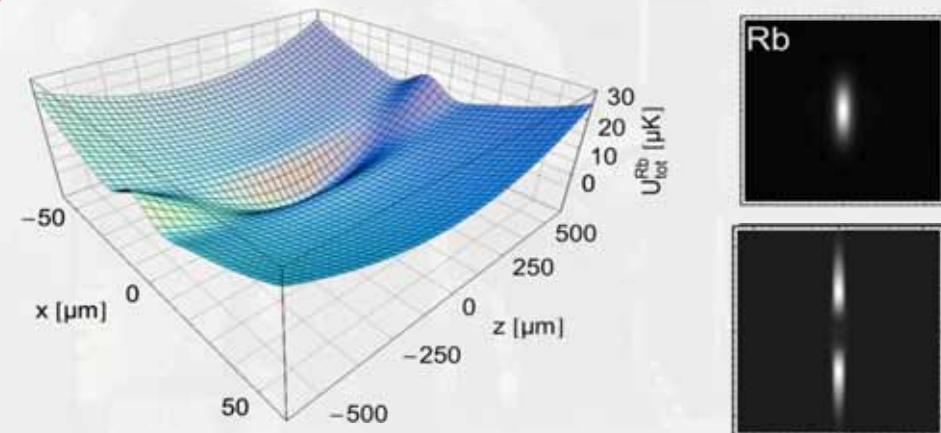
$$N_{\text{Rb}} \approx$$

$$(a) 7 \times 10^5$$

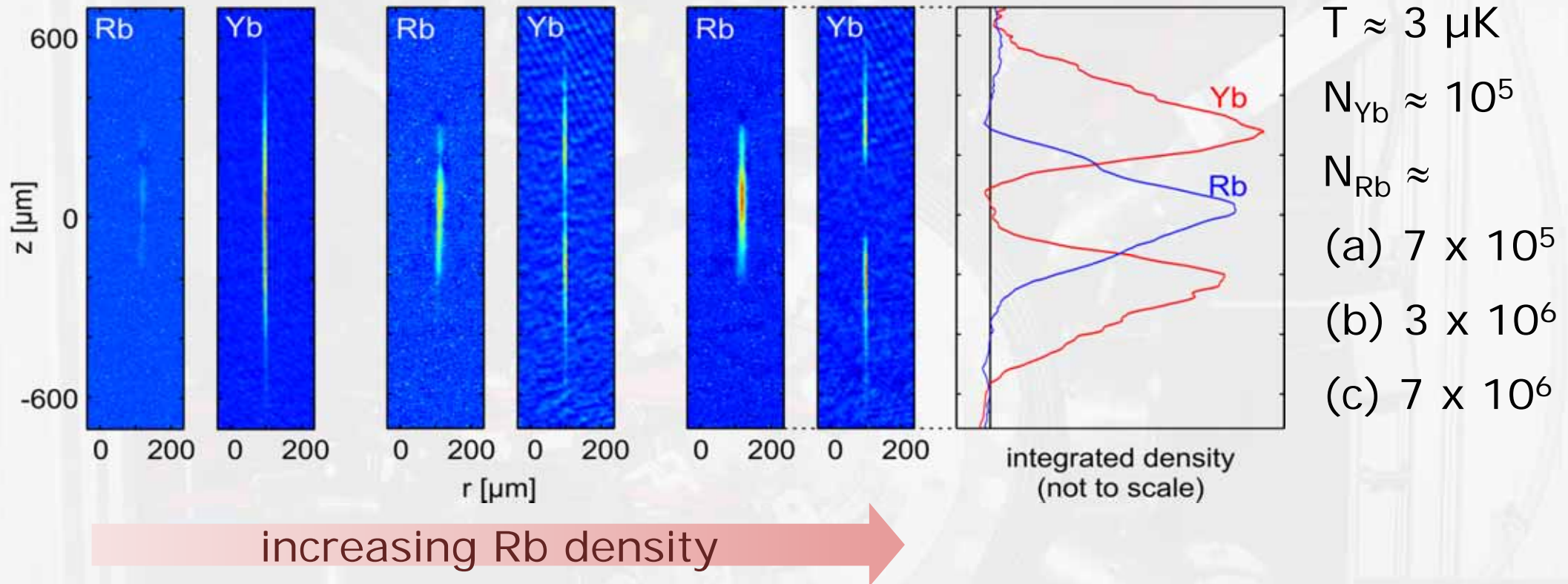
$$(b) 3 \times 10^6$$

$$(c) 7 \times 10^6$$

increasing Rb density 



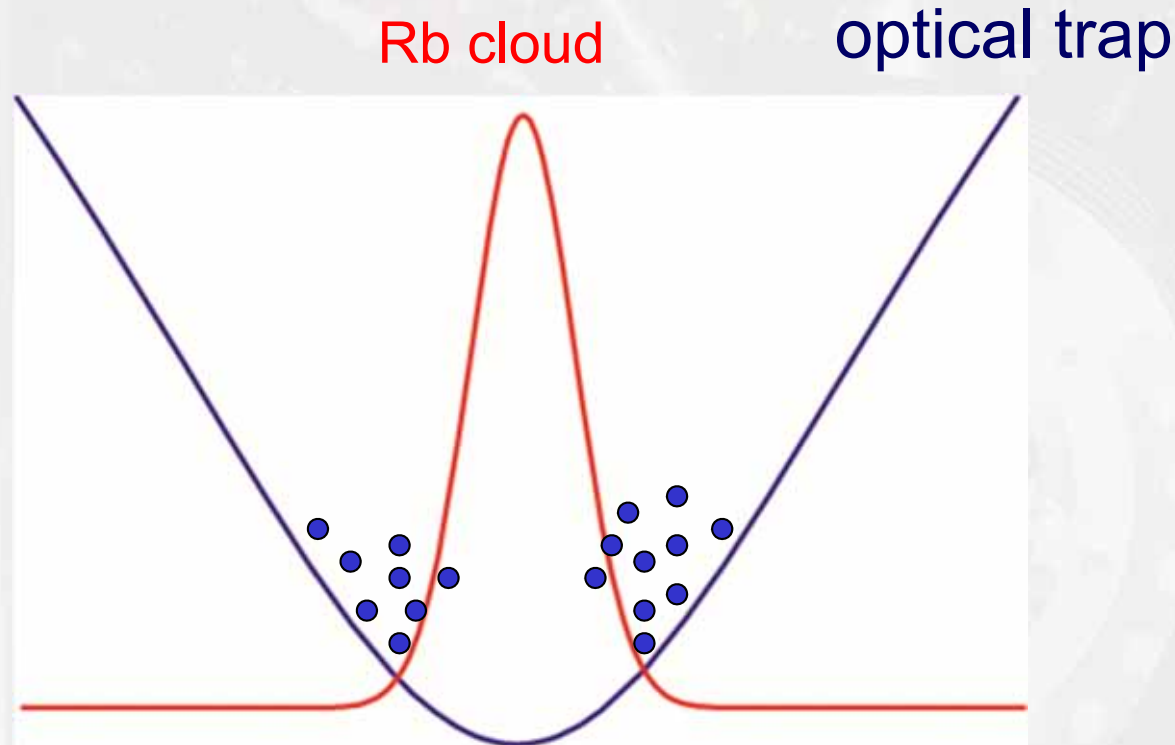
# Spatial separation of $^{174}\text{Yb}$ and $^{87}\text{Rb}$



- separation of the  $^{174}\text{Yb}$ -cloud and the (smaller)  $^{87}\text{Rb}$ -cloud located in the trap center observed at temperatures  $1.5 \dots 7 \mu\text{K}$
- due to  $N_{\text{Yb}} \ll N_{\text{Rb}}$ , no detectable effect on  $^{87}\text{Rb}$

$\Rightarrow$  **unusually strong interactions between  $^{87}\text{Rb}$  and  $^{174}\text{Yb}$**

# Diffusion model

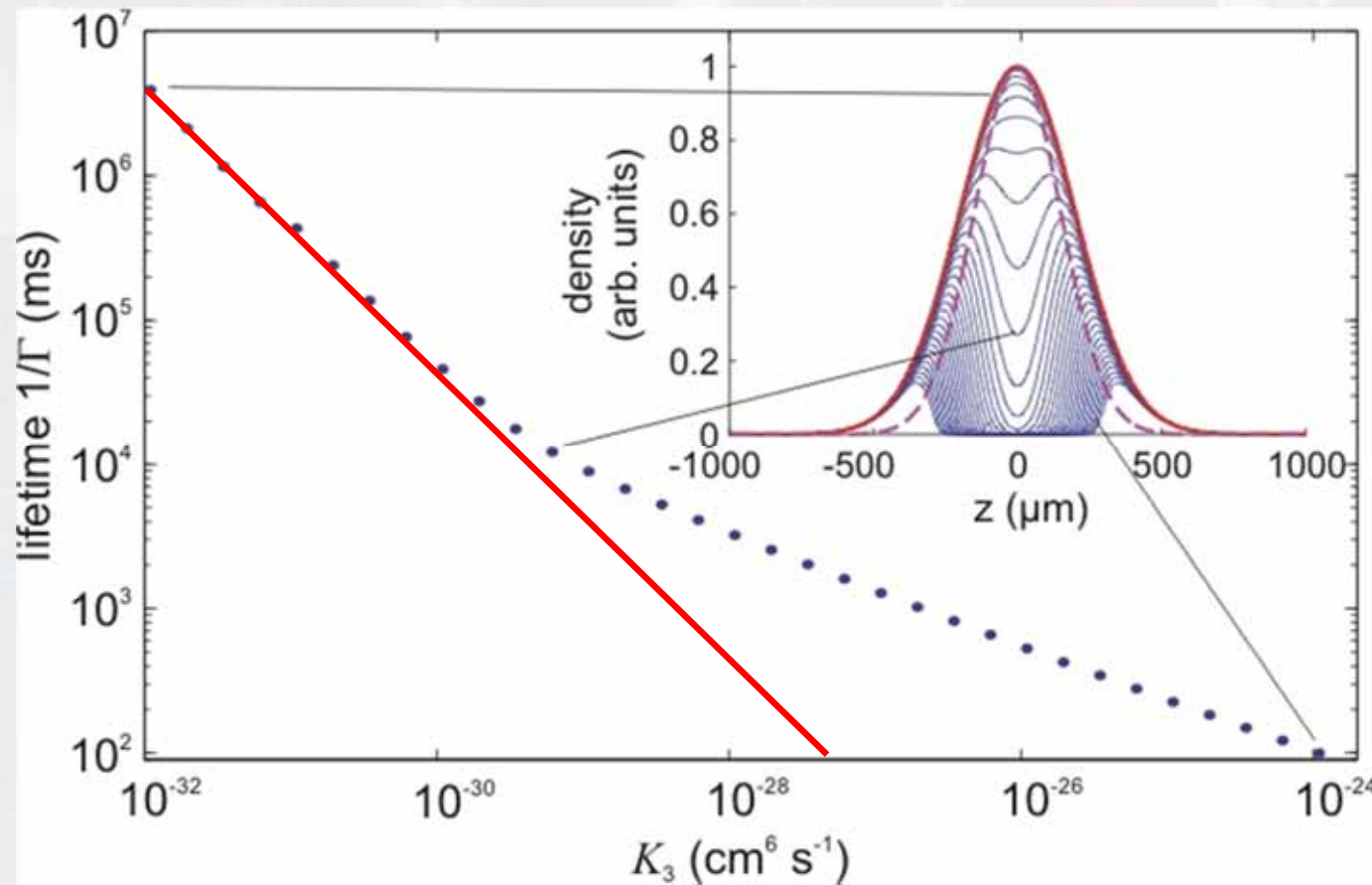


- large  $\sigma_{\text{YbRb}}$   
 $\Rightarrow$  motion of Yb is slowed
- large  $K_3$   
 $\Rightarrow$  loss of Yb due to Rb+Rb+Yb collisions primarily in trap center
- Slowed, spatially dependent Yb loss  
 $\Rightarrow$  „hole“ in Yb distribution



# Diffusion model

## Calculated axial density distribution for 1D diffusion model

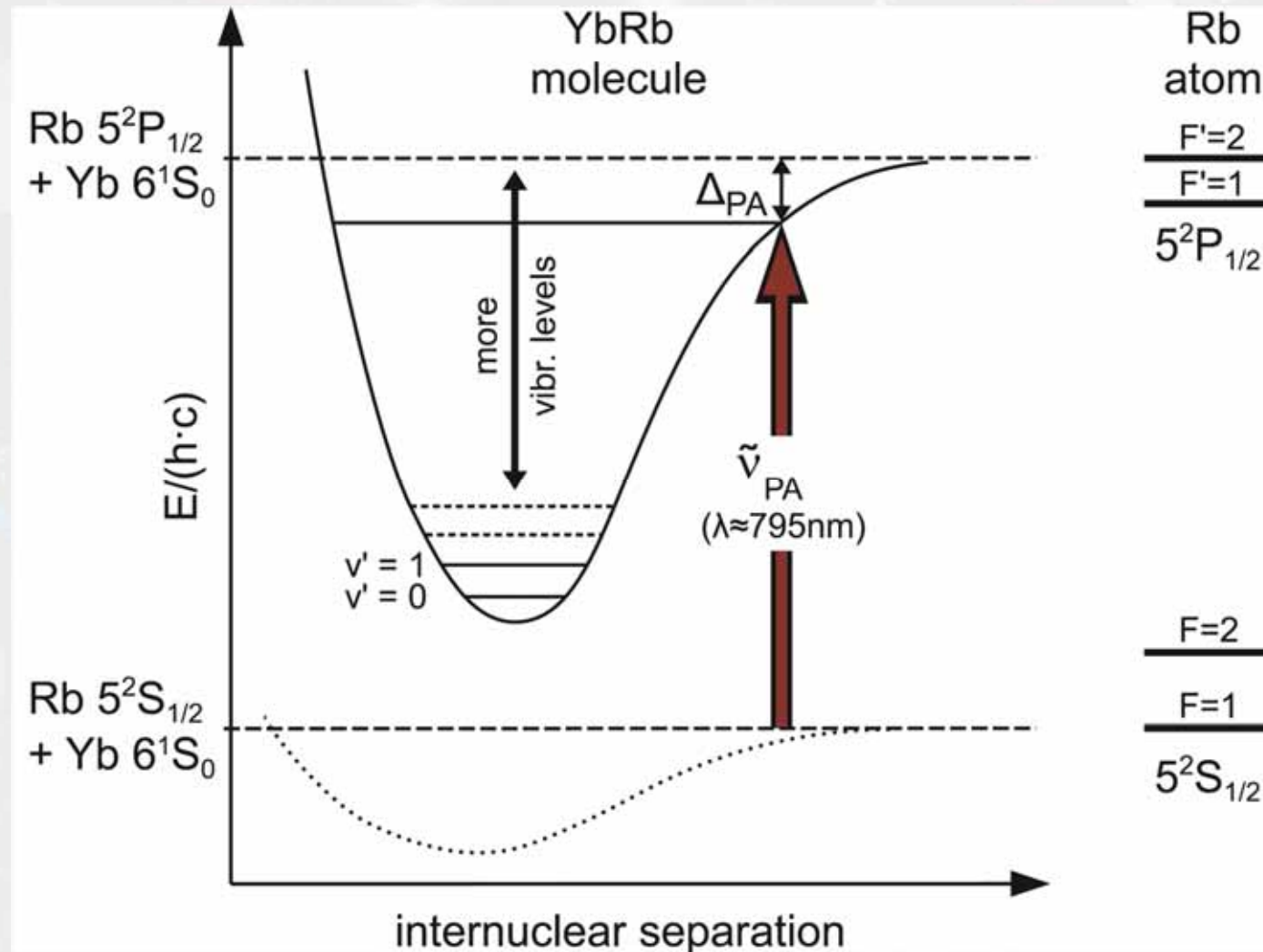


Assumption: unitarity-limited  $\sigma_{\text{YbRb}}$ ,  $n_{\text{Rb}} = 3 \times 10^{14} \text{ cm}^{-3}$

# 3. YbRb: Photoassociation Spectroscopy

# Photoassociative production of $\text{YbRb}^*$

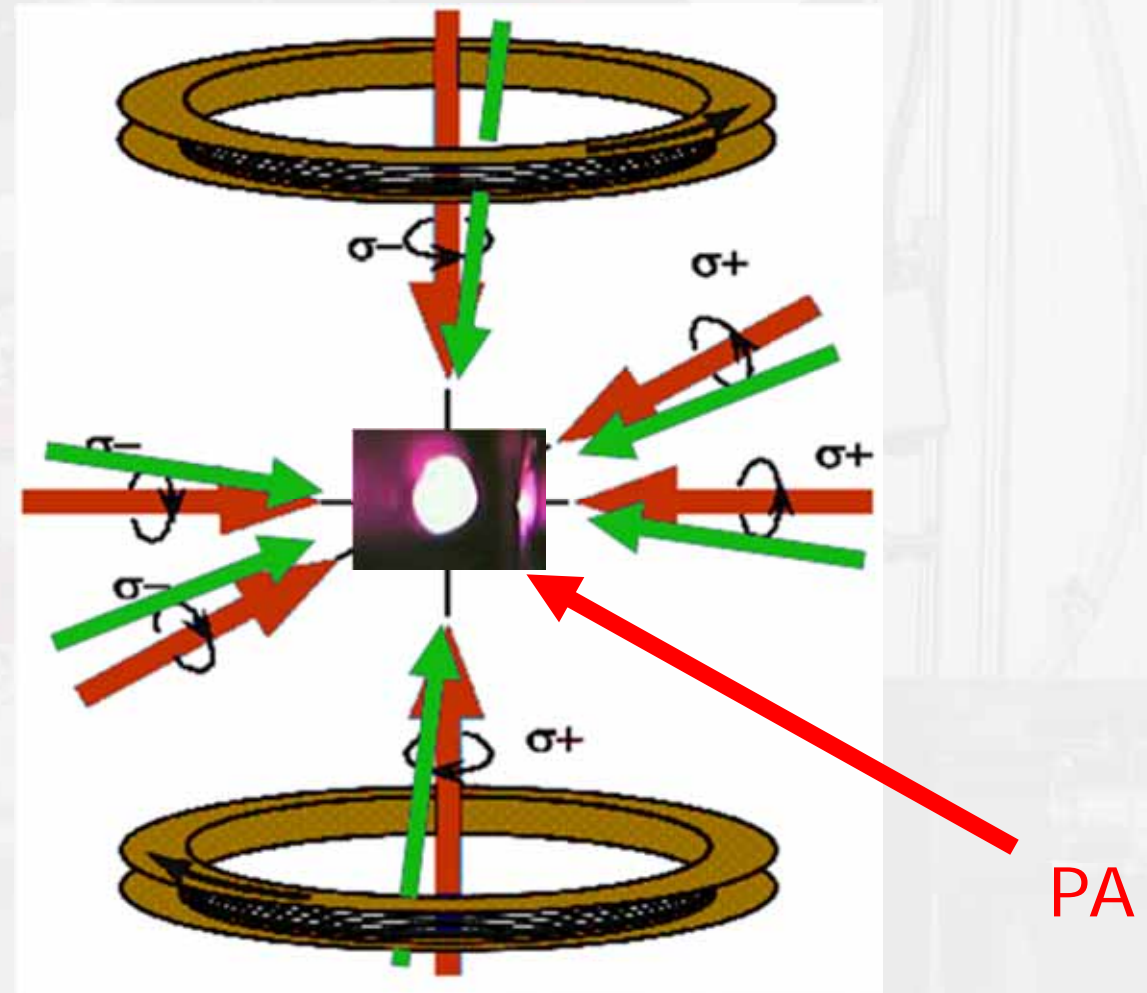
## 1-Photon photoassociation



# Experimental scheme

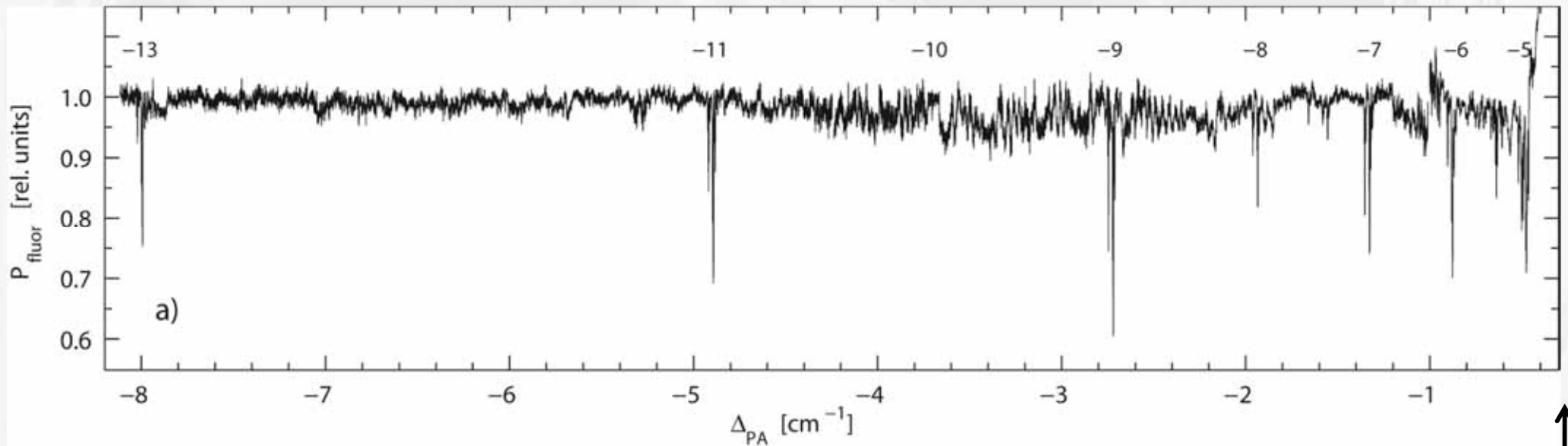
## Continuously loaded simultaneous MOTs:

- **Yb** – „green“ MOT:  
~  $10^6$  atoms (loaded directly from slower)
- **Rb** - Dark Spot MOT:  
~  $10^9$  atoms;  $n \sim 10^{10}$ - $10^{11}$  cm<sup>-3</sup>
- **PA-laser** induces loss
- **Rb**-loss  $\Rightarrow$  **Rb<sub>2</sub>** formation
- **Yb**-loss  $\Rightarrow$  **YbRb\*** formation



# Photoassociative production of $\text{YbRb}^*$

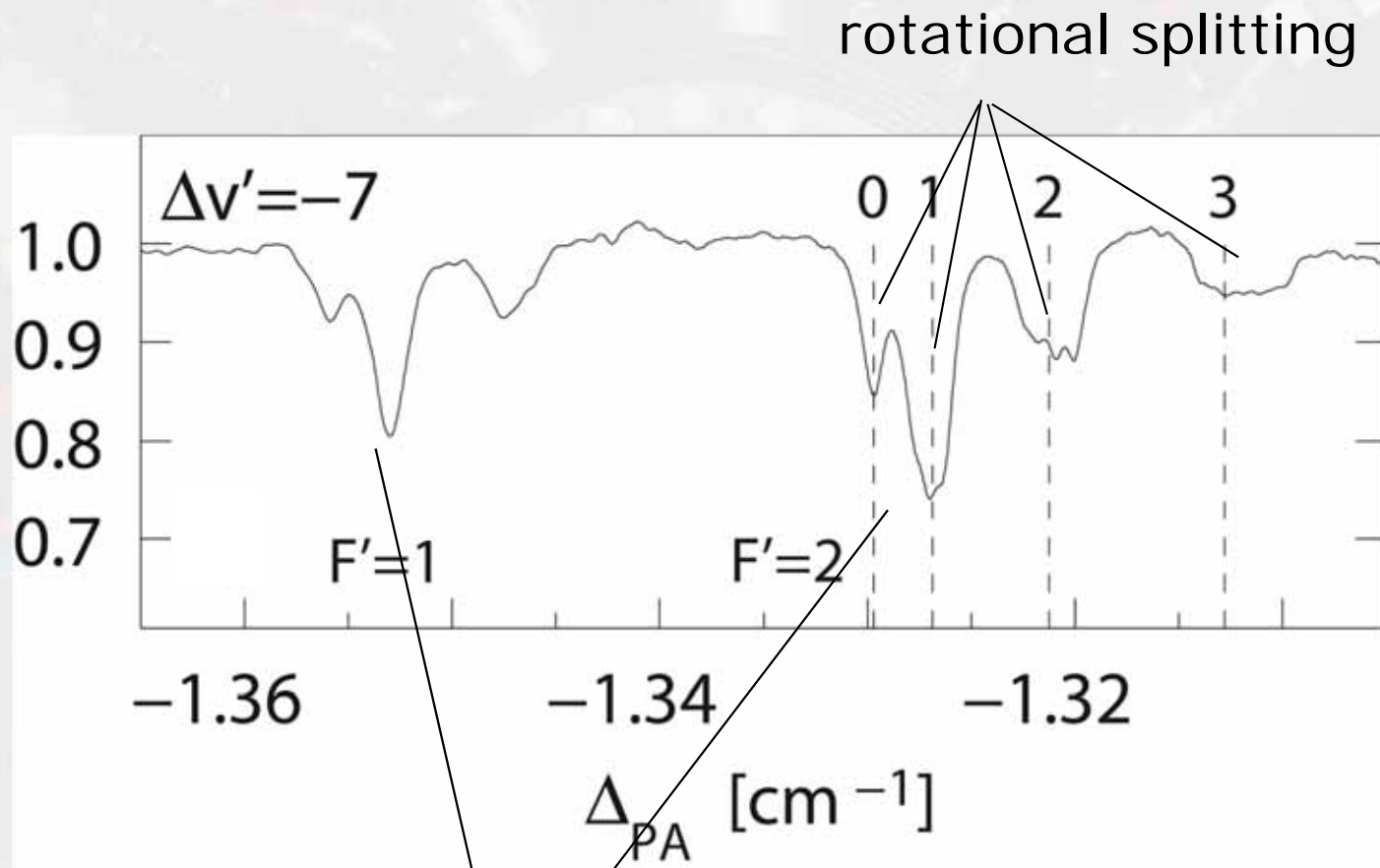
$^{176}\text{Yb}^{87}\text{Rb}$



↑  
Rb D1-line  
@ 795 nm

# YbRb\* photoassociation

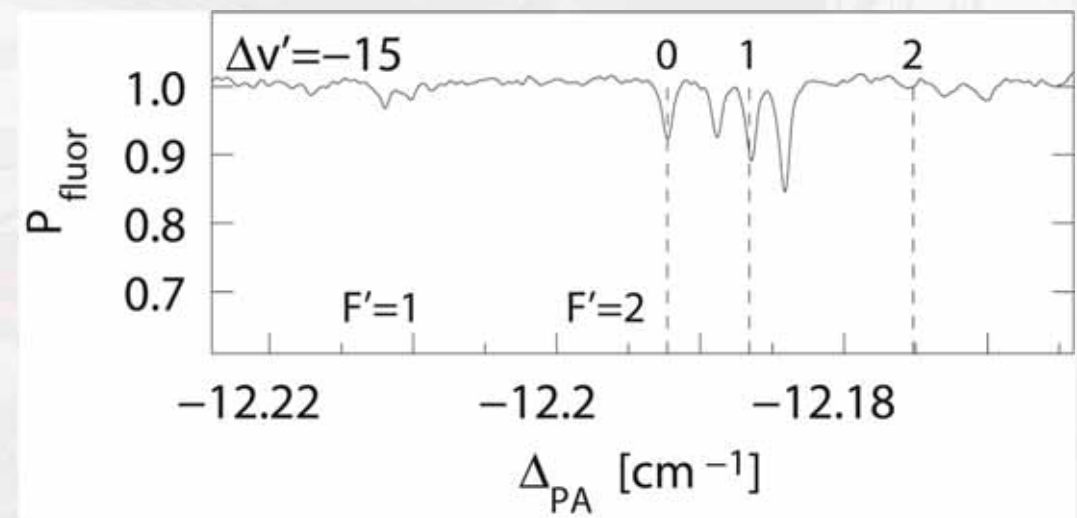
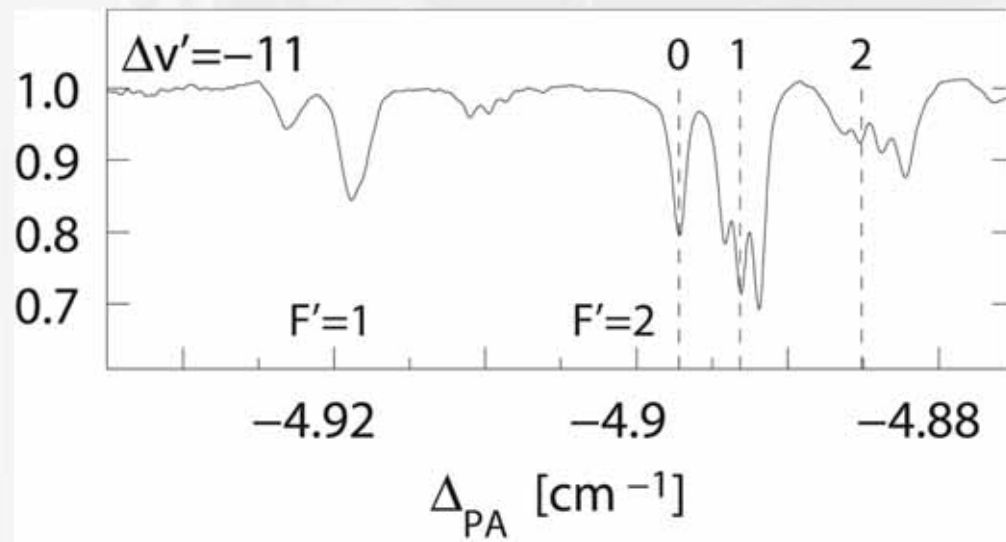
## Resolved structure of vibrational level:



hyperfine splitting

# YbRb\* photoassociation

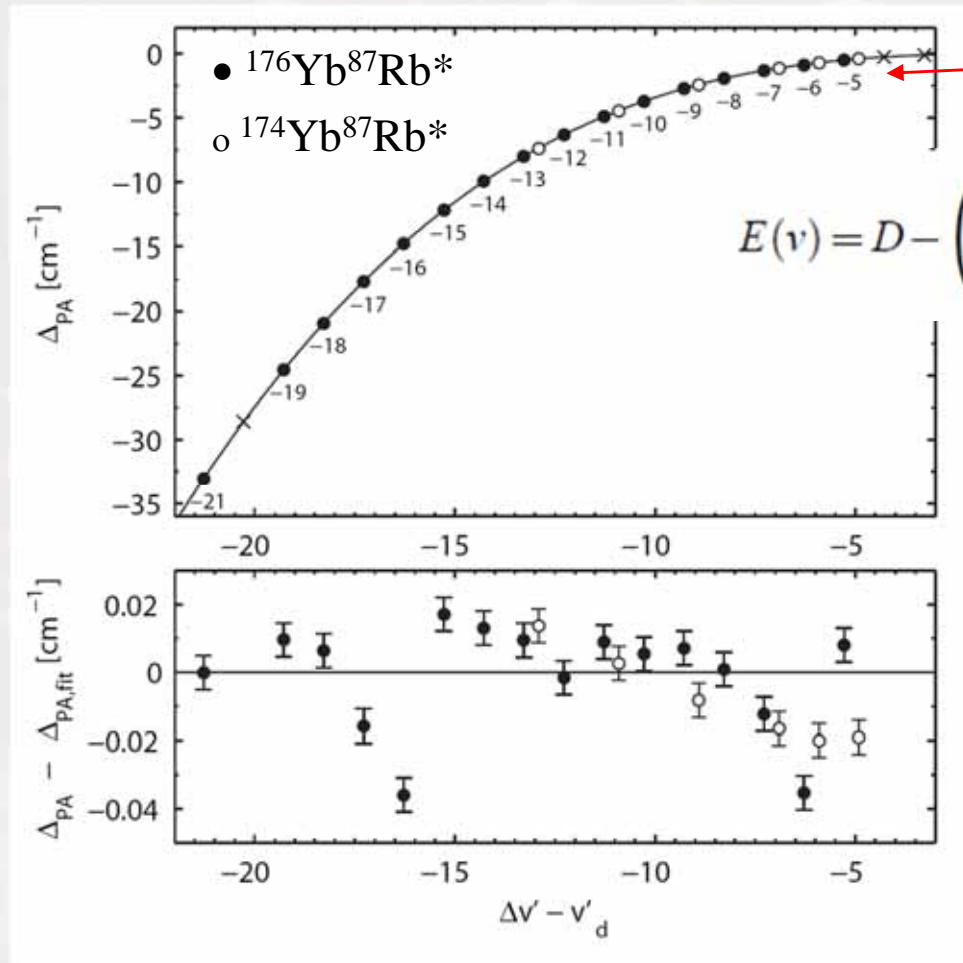
## Splitting of rotational levels:



**explanation:** coupling of  $F'$  to  $R'$  (Hund's case (e))

Rb total angular momentum  $\nearrow$   
nuclear rotation  $\nearrow$

# Interpretation of results: Leroy-Bernstein Fit



Fit to Leroy-Bernstein formula<sup>1</sup>

$$E(v) = D - \left( \hbar \left( \frac{2\pi}{\mu} \right)^{1/2} \frac{\Gamma(1+1/n)}{\Gamma(\frac{1}{2}+1/n)} \frac{n}{C_n^{1/n}} (v_D - v) \frac{n-2}{2n} \right)^{\frac{2n}{n-2}}$$

assuming potential:

$$V(r) = -C_6/R^6$$

⇒  $C_6$ -coefficient for  
 $\text{YbRb}^*$ :

$$C_6 = 5684 \text{ a.u.}$$

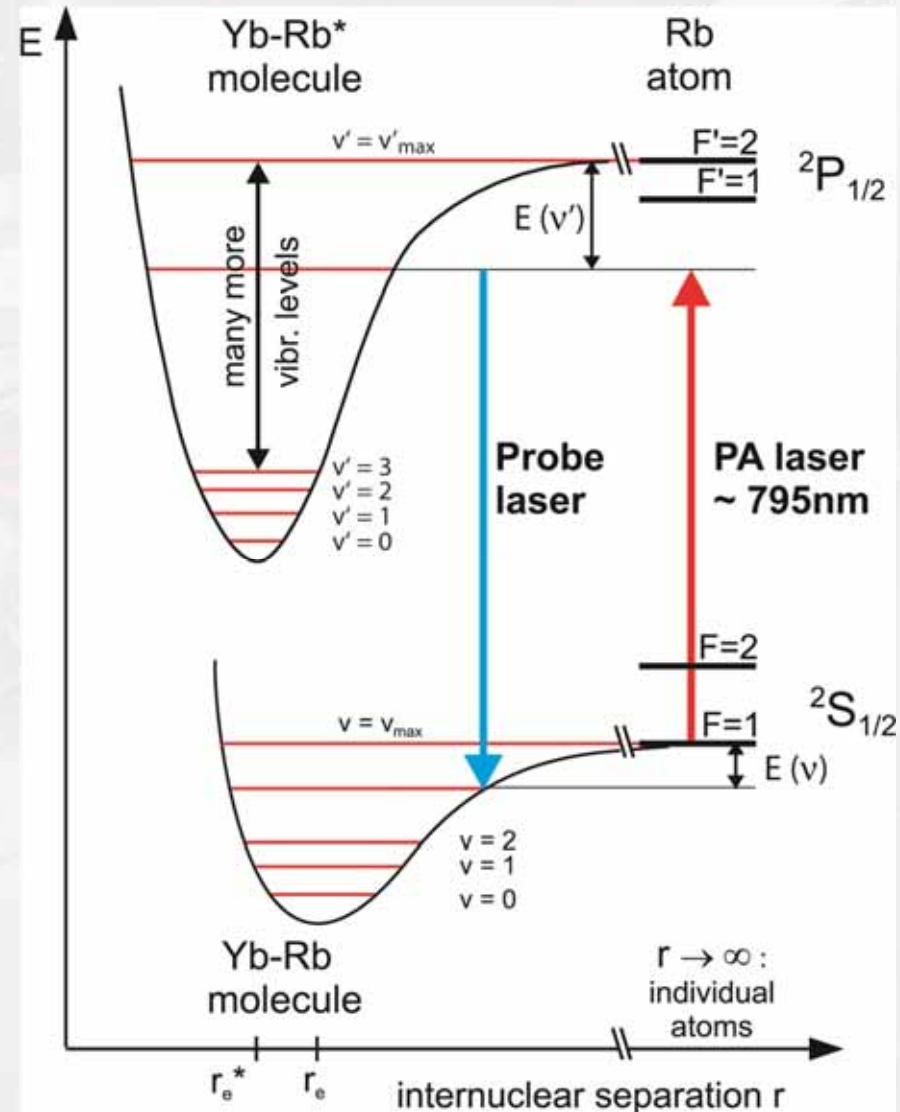


# 2-Photon PA-spectroscopy

binding energy  
of ground state level

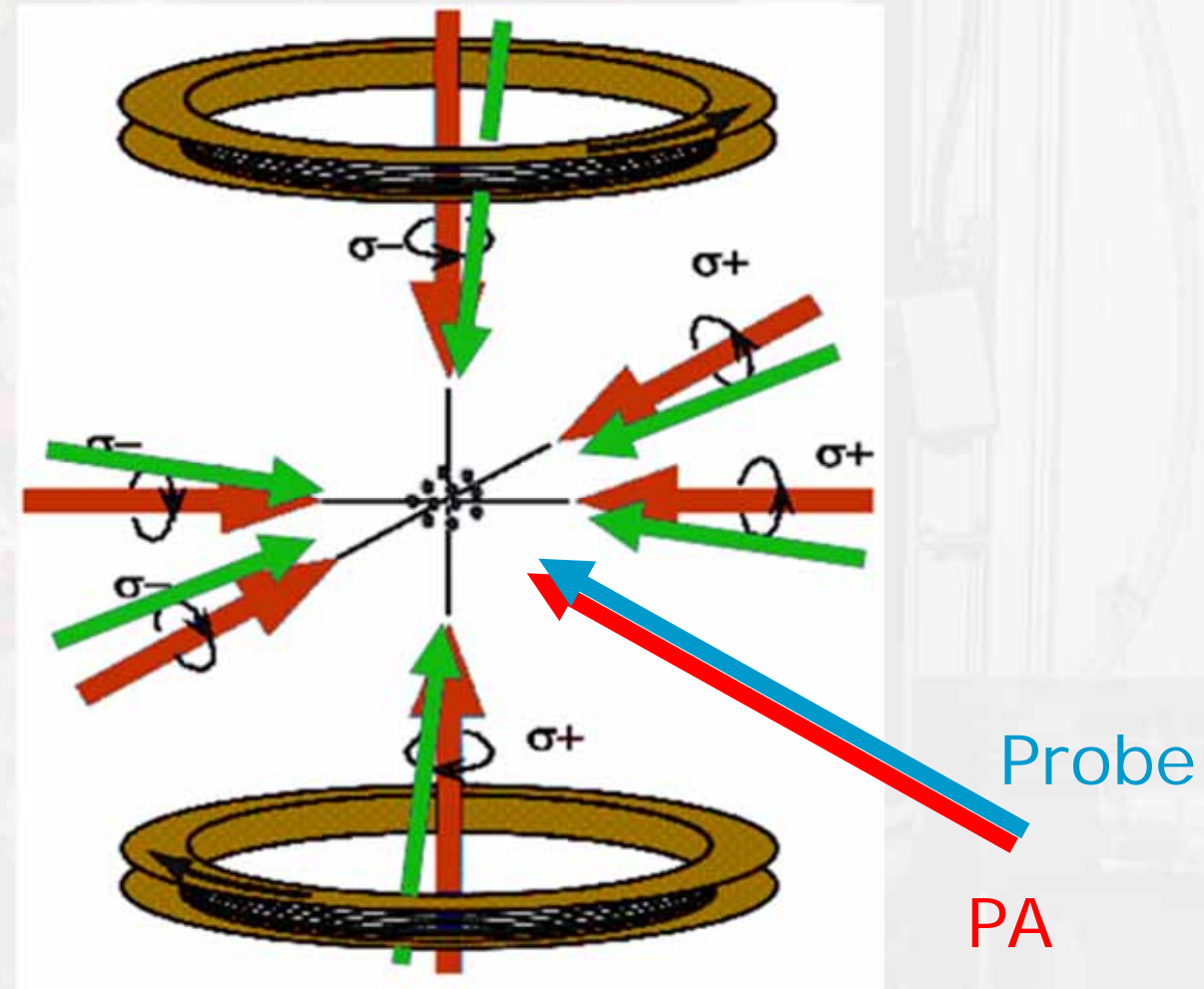
$$\nu_{\text{PA}} - \nu_{\text{Probe}} = E(\nu)/h \quad (+ \nu_{\text{Hyperfine}})$$

Probe laser only couples to transitions with  $\Delta R = R - R' = 0$



# Experimental scheme

- PA laser frequency set to single photon resonance  
 $[\nu_{PA} = \nu_{D1} - E(v')/h]$   
 $\Rightarrow$  continuous trap loss
- if  $\nu_{probe} = \nu_{PA} - E(v)/h$   
 $\Rightarrow$  reduced trap loss due to light shift of probe beam on molecular transition  $v \rightarrow v'$

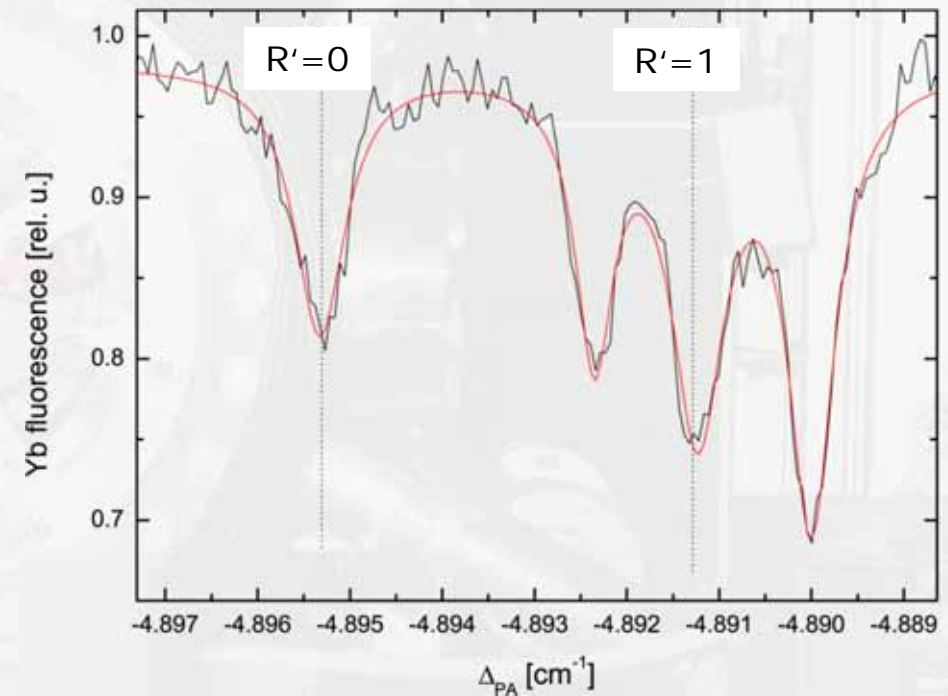
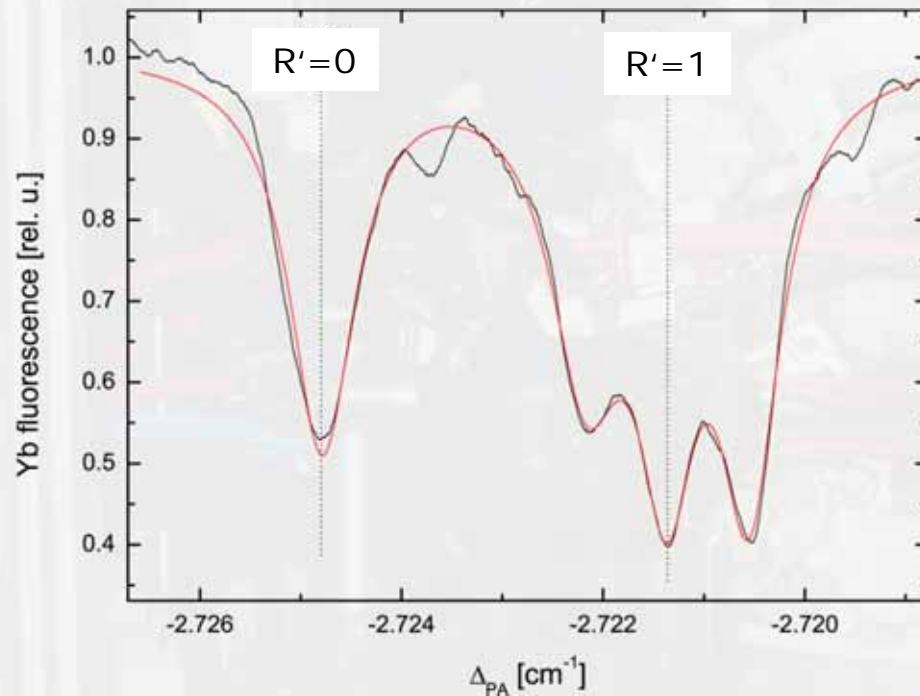


# 2-Photon PA-spectroscopy

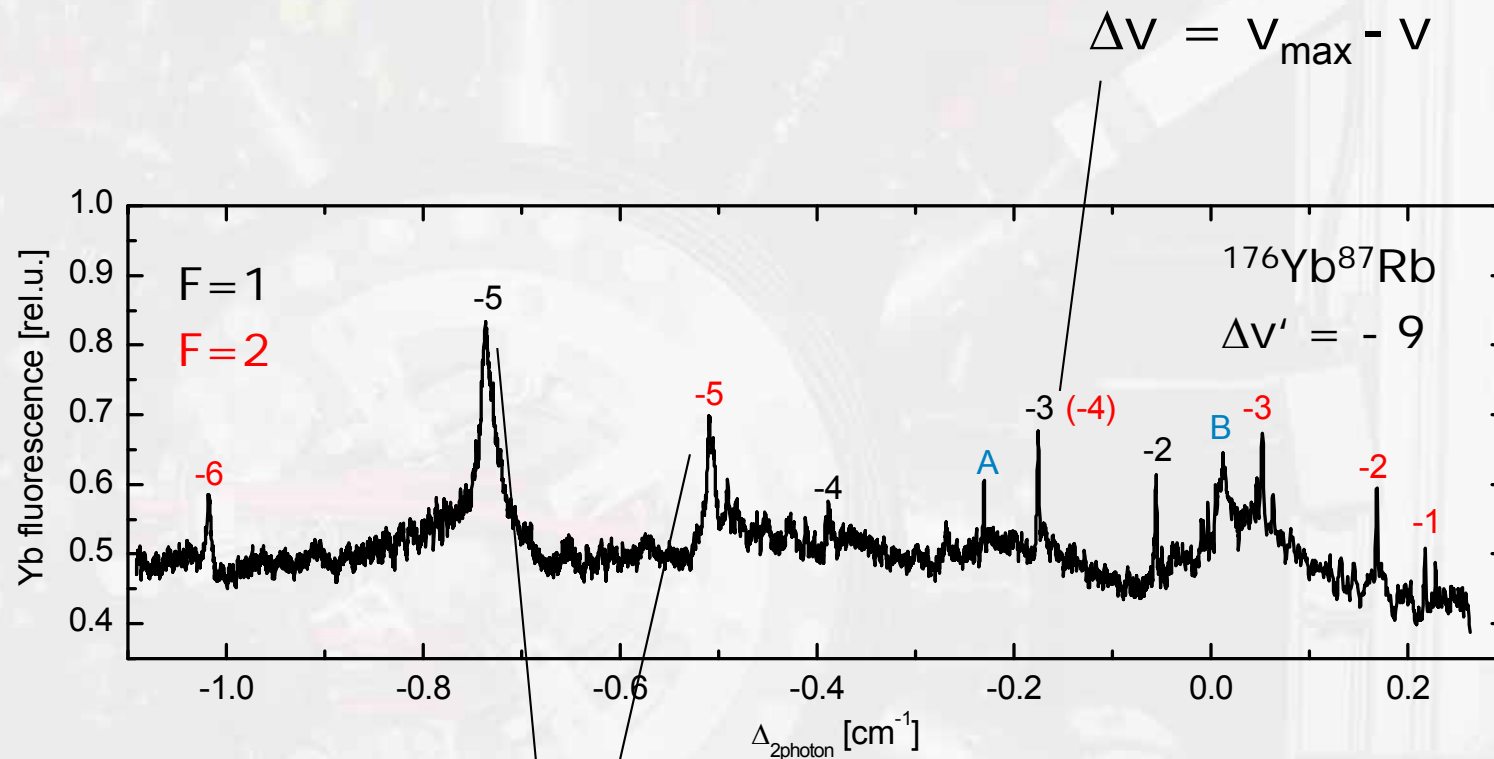
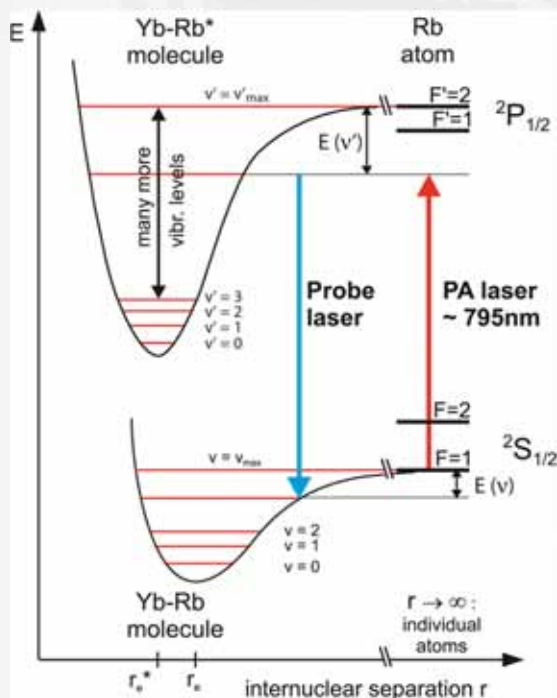
Single-photon PA resonances used:

$$\Delta v' = -9$$

$$\Delta v' = -11$$



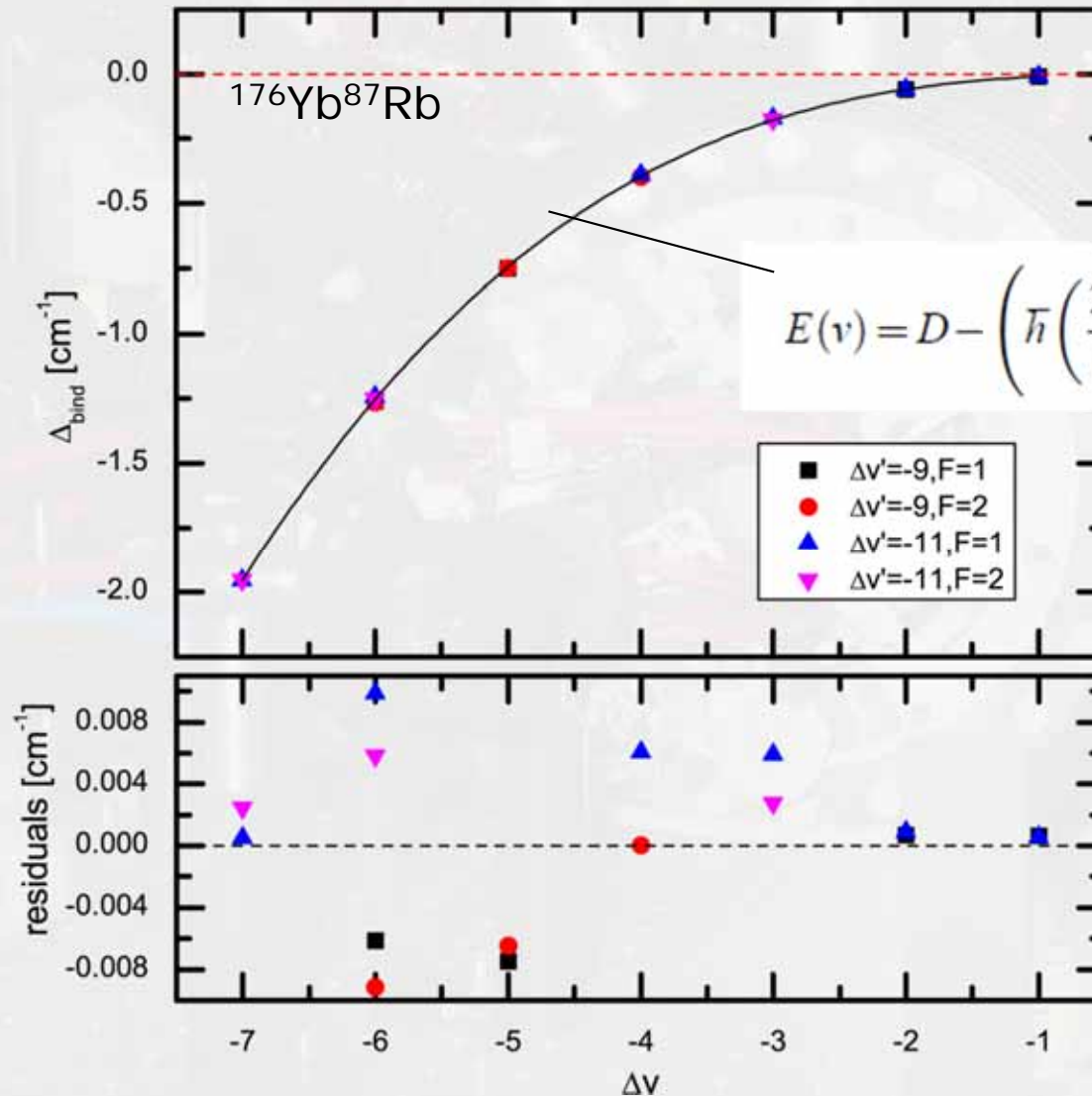
# 2-Photon PA-spectroscopy



- PA laser is fixed
- probe laser is scanned

(ground state)  
hyperfine splitting

# Binding energies: LeRoy-Bernstein Fit

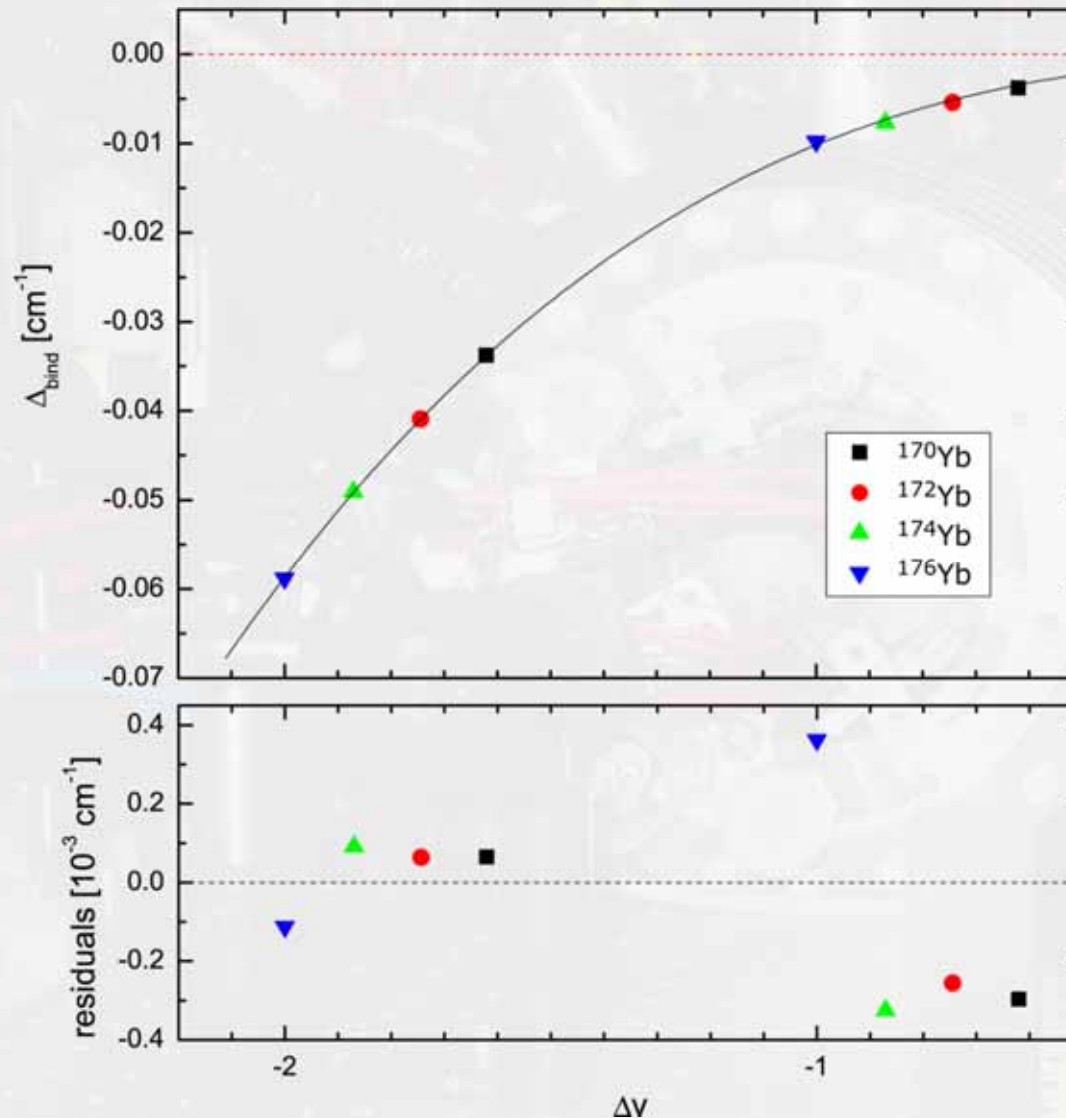


Assuming  
Long-range potential:  
 $V(R) = -C_6/R^6$

$$E(v) = D - \left( \hbar \left( \frac{2\pi}{\mu} \right)^{1/2} \frac{\Gamma(1+1/n)}{\Gamma(\frac{1}{2}+1/n)} \frac{n}{C_n^{1/n}} (v_D - v) \frac{n-2}{2n} \right)^{\frac{2n}{n-2}}$$

$\Rightarrow C_6 \sim 2600 \text{ a.u.}$

# Binding energies of $^x\text{Yb}^{87}\text{Rb}$



- binding energy of high-lying levels detected with  $\pm 10$  MHz inaccuracy
- $\nu_D$  adjusted for each Yb isotope (corresponding to mass scaling)

# Scattering lengths

Theoretical modelling by M. Borkowski, P. Zuchowski,  
R. Ciurylo, P. Julienne\*

Binding energies are fit by:

scaling parameter

switching function

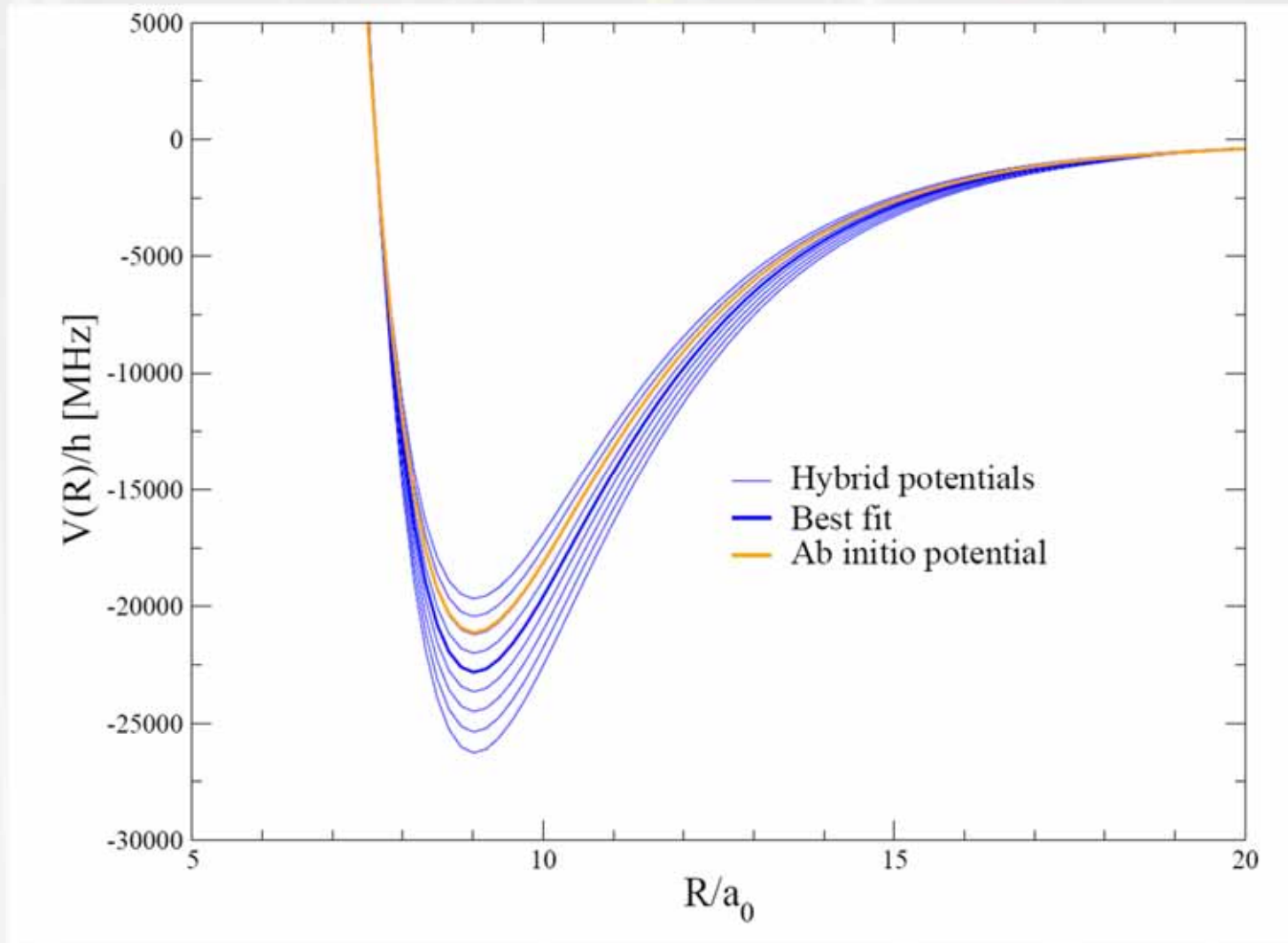
$$V(r) = dV_{\text{sh}}(r) (1 - f(r)) - f(r) (C_6 R^{-6} + C_8 R^{-8})$$

ab-initio potential

Fit parameters:  $C_6$ ,  $C_8$ ,  $d$  (corresponding to  $D_e$ )

\*M. Borkowski et al., (in preparation)

# Scattering lengths



Best fit:

$$C_6 = 2813 \text{ a.u.}$$

$$C_8 = 4.37 \times 10^5 \text{ a.u.}$$

$$D_e = 761 \text{ cm}^{-1}$$

\*M. Borkowski et al., (in preparation)



# Scattering lengths

⇒ scattering length given by\*

$$a = \bar{a} \left[ 1 - \tan \left( \Phi - \frac{\pi}{8} \right) \right]$$

with background scattering length:

$$\bar{a} = 2^{-\frac{3}{2}} \frac{\Gamma(3/4)}{\Gamma(5/4)} (2\mu C_6 / \hbar^2)^{\frac{1}{4}}$$

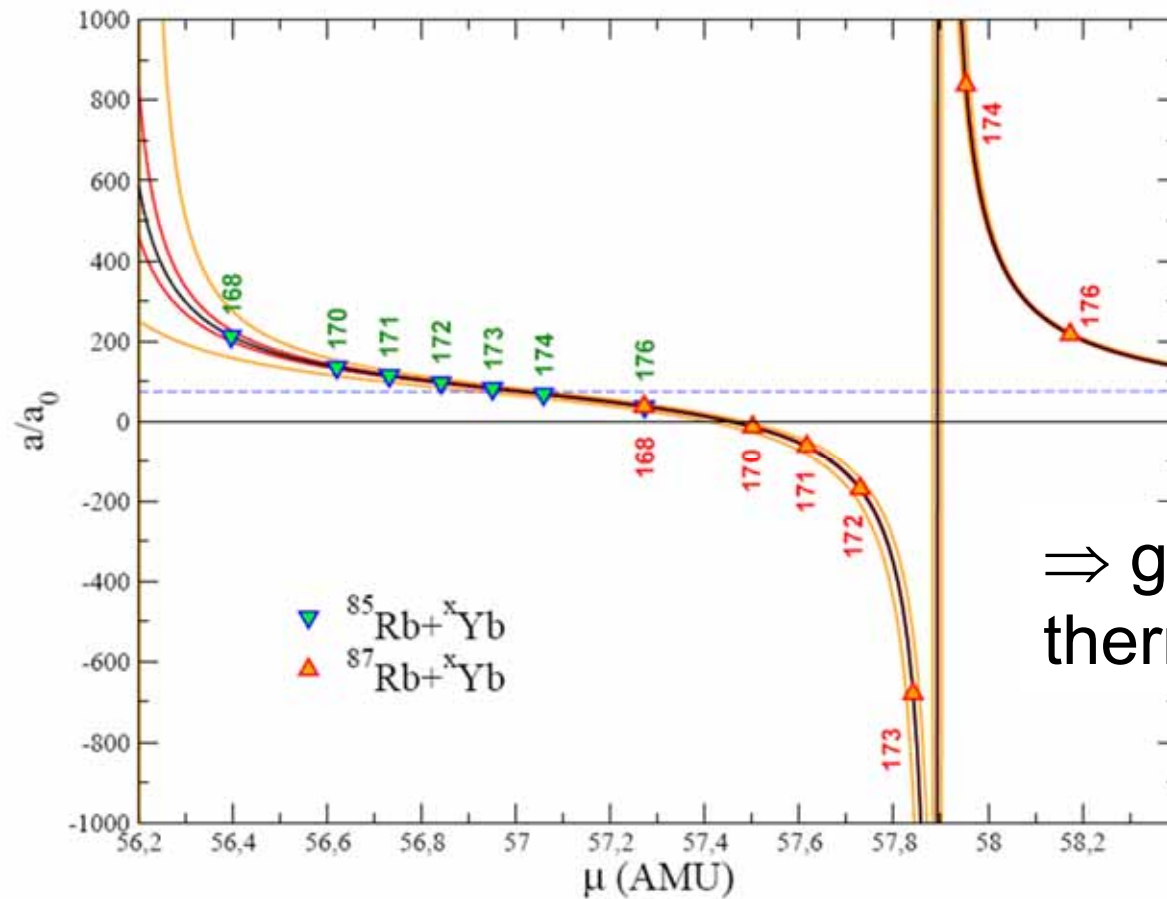
and phase:

$$\Phi = \frac{\sqrt{2\mu}}{\hbar} \int_{R_{\text{in}}}^{\infty} \sqrt{-V(r)} dr.$$

\*G. F. Gribakin and V. V. Flambaum, PRA 48, 546 (1993).

# Scattering lengths

From best fit:

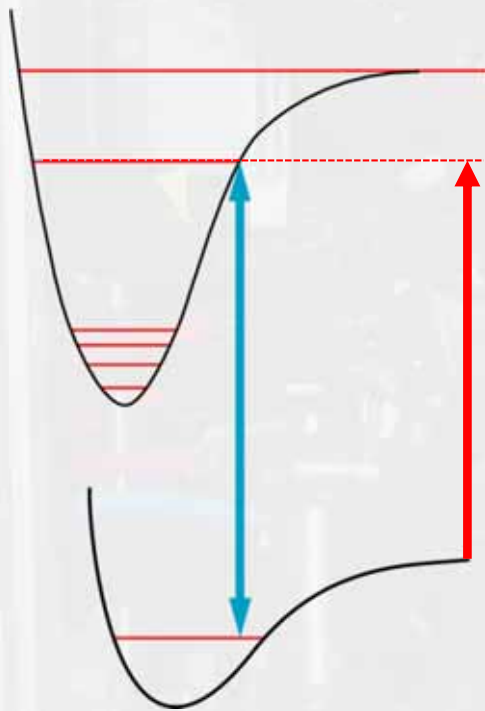


$$\Rightarrow a_{87,170} \sim -14.5 a_0$$
$$a_{87,174} \sim 840 a_0$$

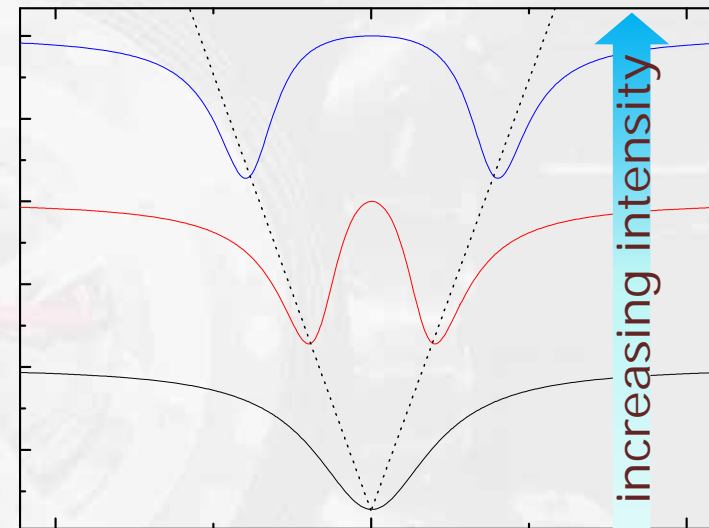
$\Rightarrow$  good agreement with thermalization measurements

# Autler-Townes Spectroscopy

transition dressed by  
coupling laser



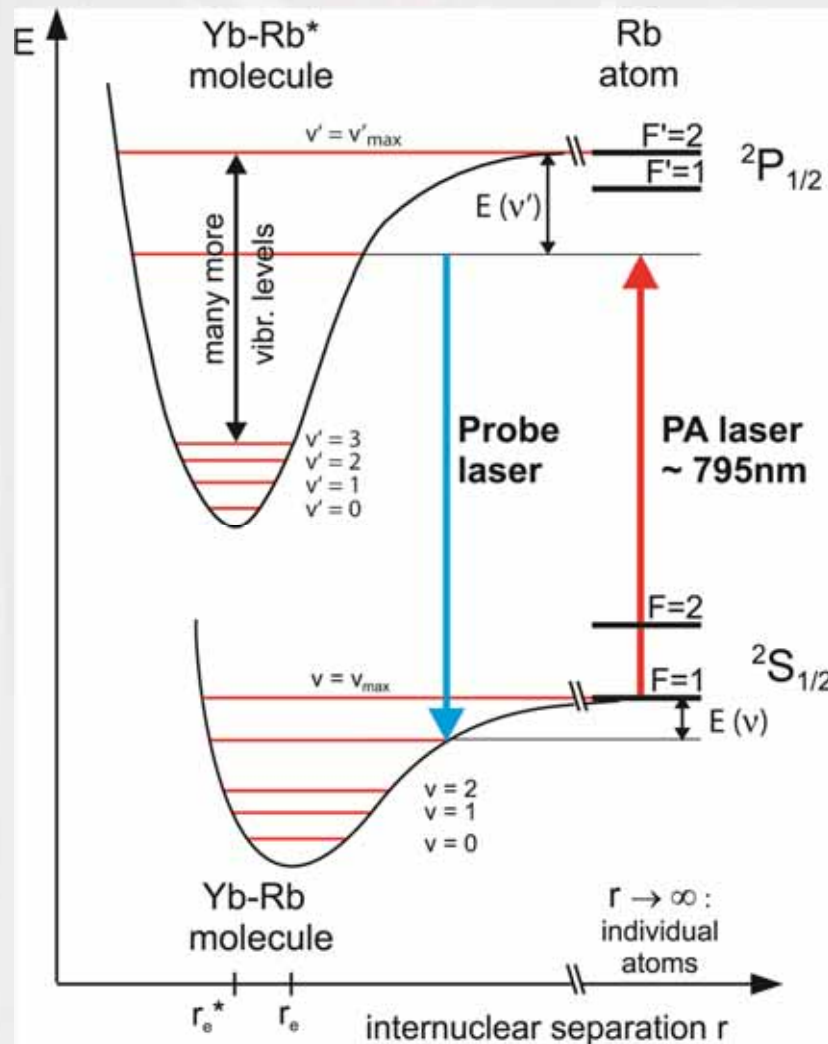
splitting of **line**



Splitting

$$\Delta = \sqrt{\delta^2 + \Omega_0^2}$$

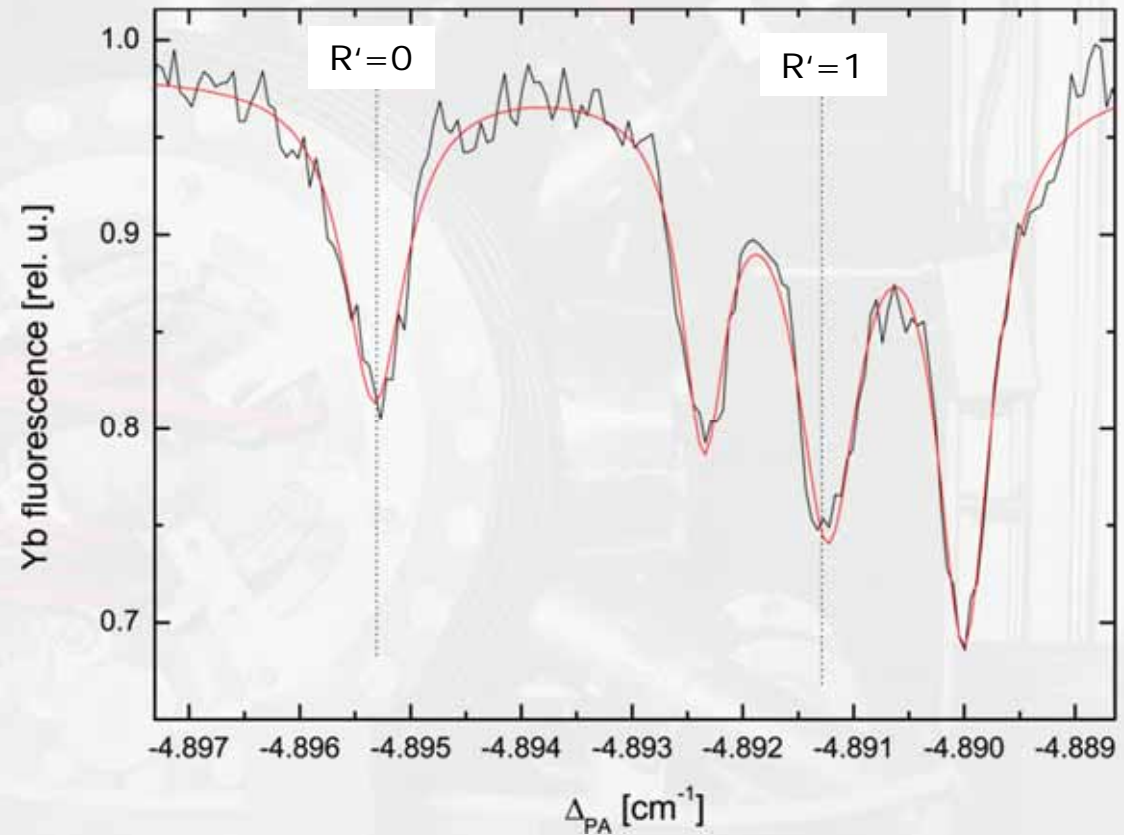
# Autler-Townes Spectroscopy



- probe laser couples to a bound-bound transition
- PA laser scanned over 1-Photon-PA resonance (free – bound)  
 $\Rightarrow$  observation of splitting  
 $\Rightarrow$  determination of Rabi frequency

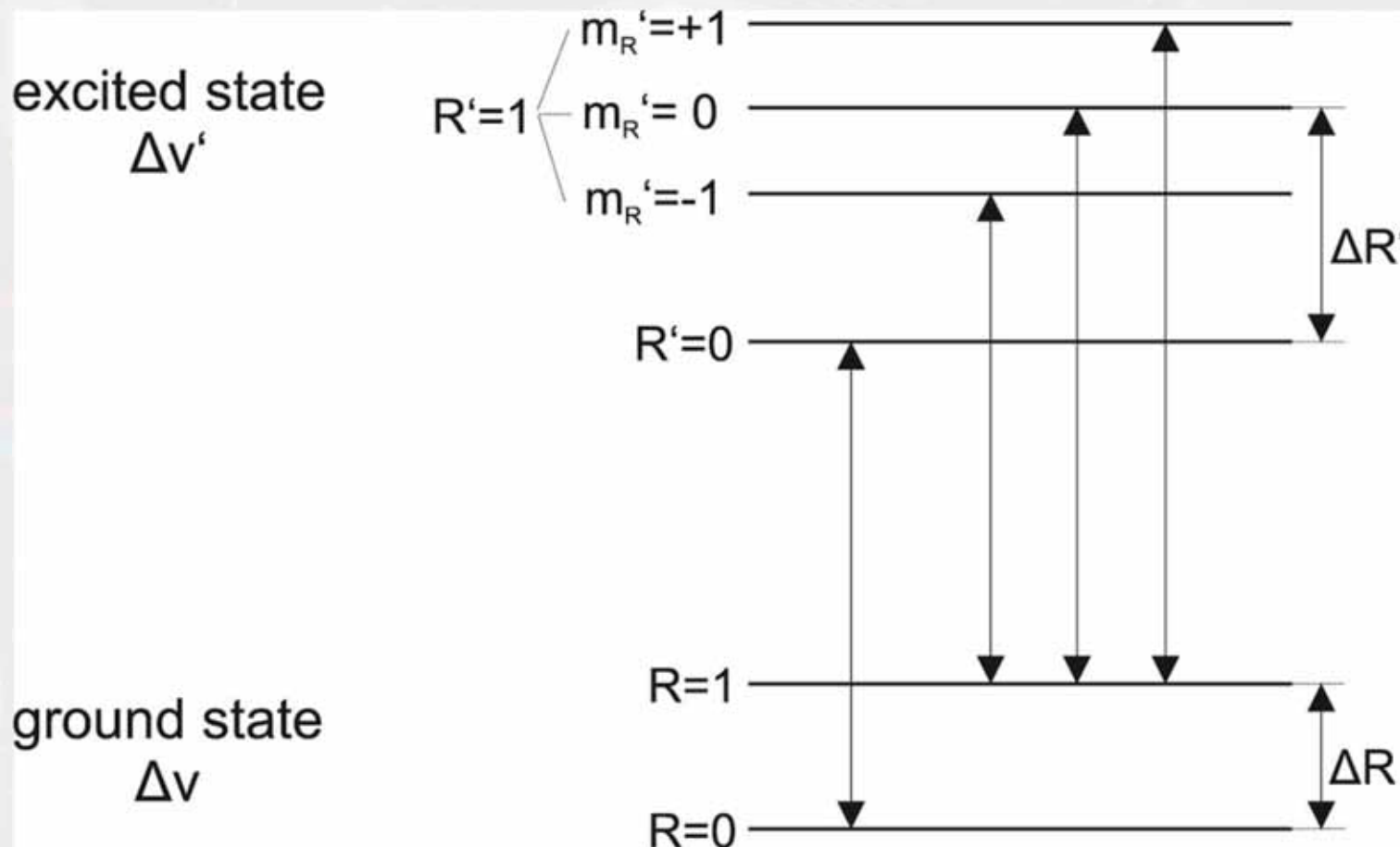
# Autler-Townes Spectroscopy

1-photon PA spectrum  
without coupling laser  
( $\Delta v = -6 \rightarrow \Delta v' = -11$ )



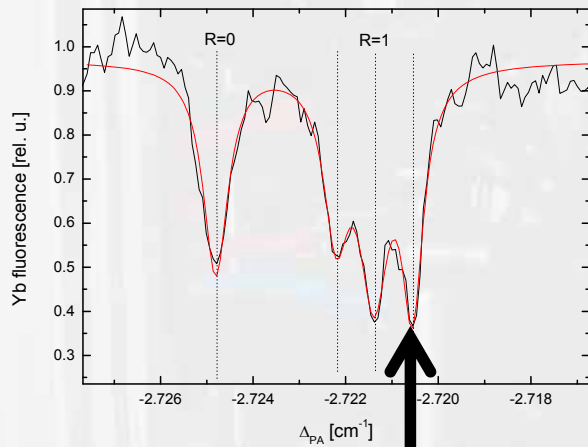
# Autler-Townes Spectroscopy

relevant levels for coupling laser

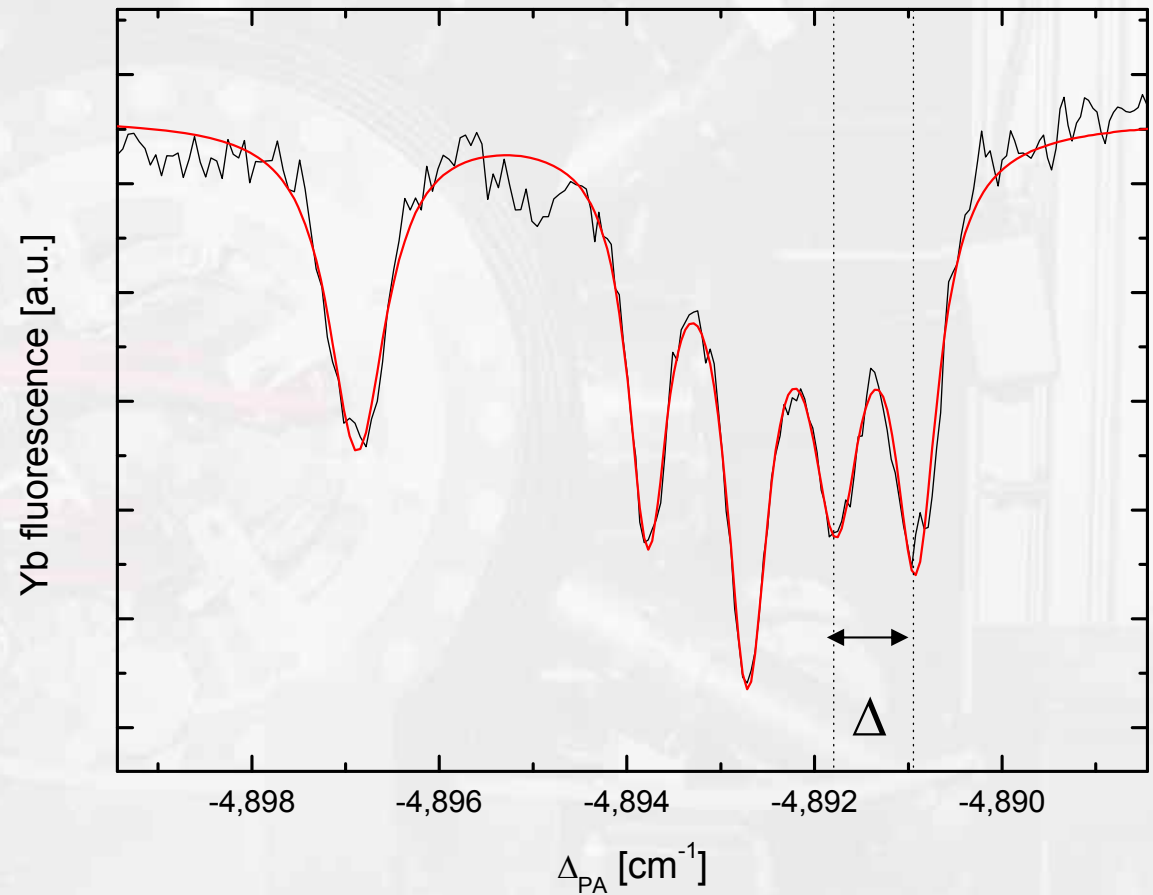


# Autler-Townes Spectroscopy

1-photon PA spectrum  
with coupling laser

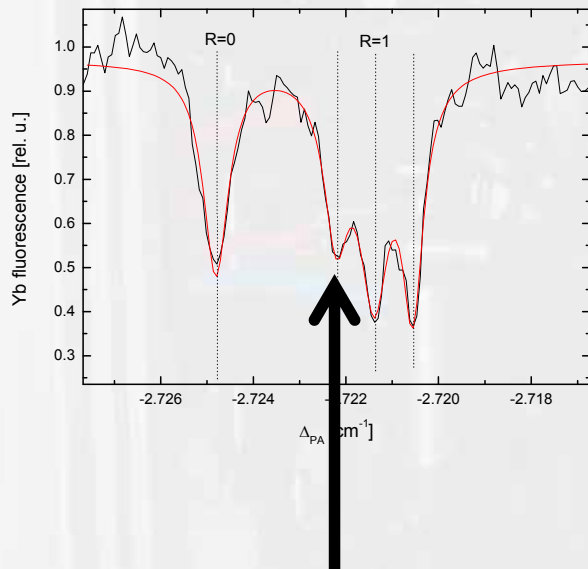


coupling laser  
( $\Delta v = -6 \rightarrow \Delta v' = -11$ )

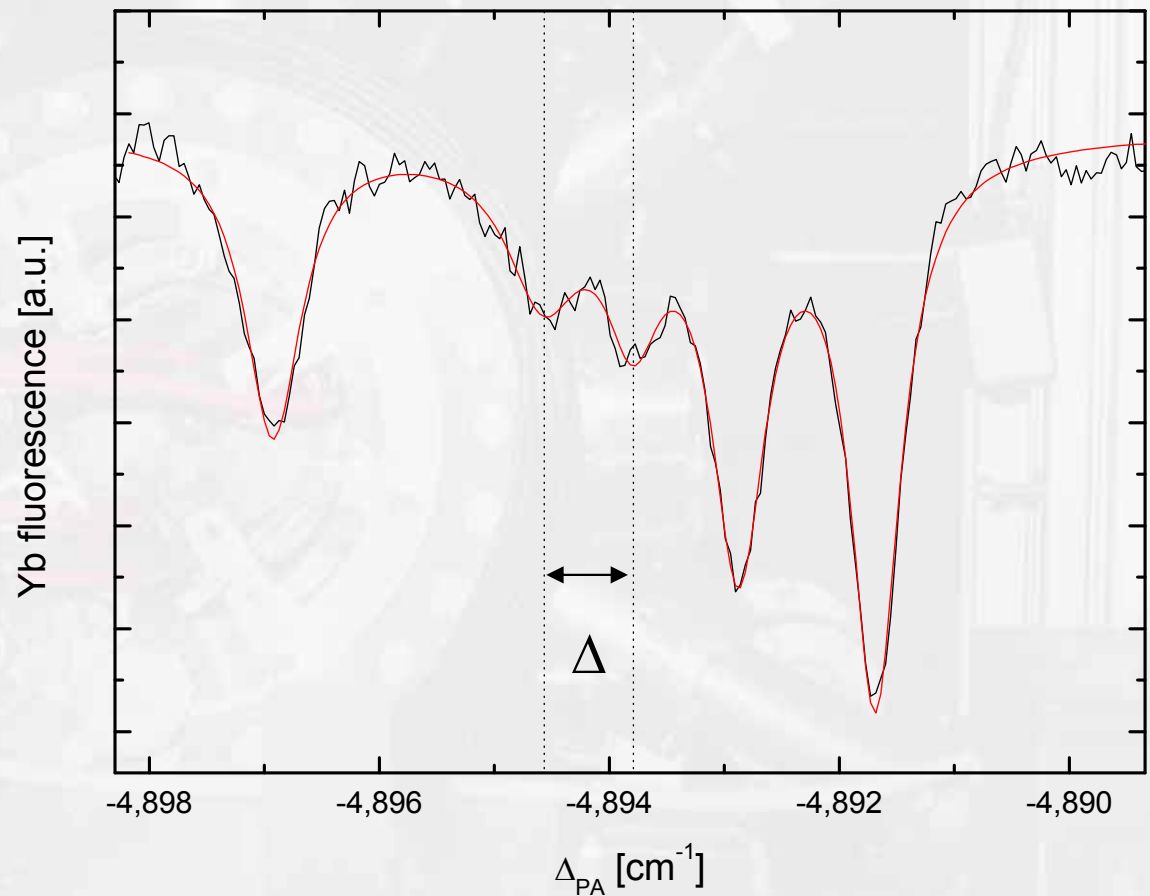


# Autler-Townes Spectroscopy

1-photon PA spectrum  
with coupling laser



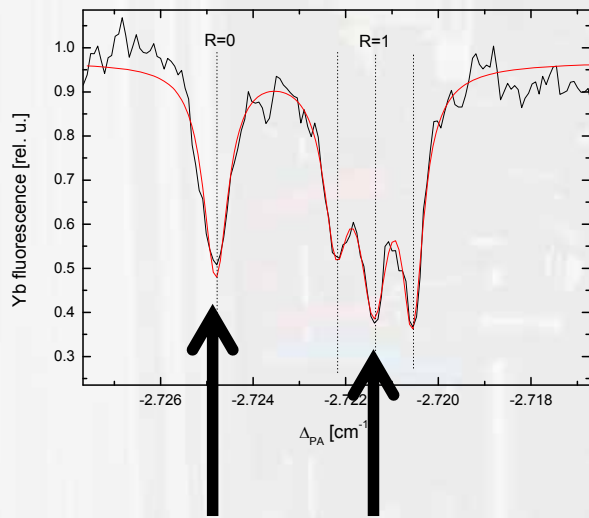
coupling laser  
( $\Delta v = -6 \rightarrow \Delta v' = -11$ )



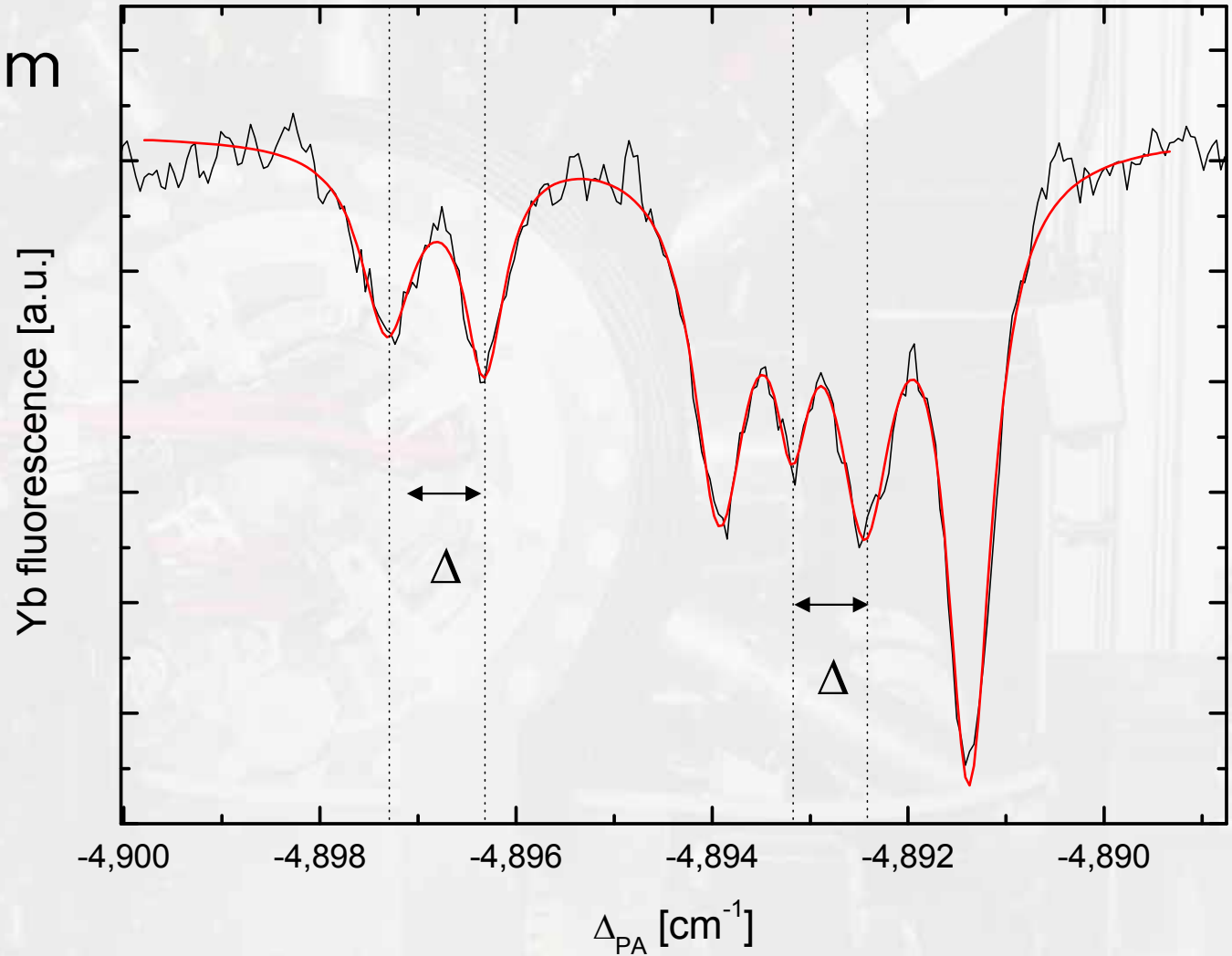


# Autler-Townes Spectroscopy

1-photon PA spectrum  
with coupling laser

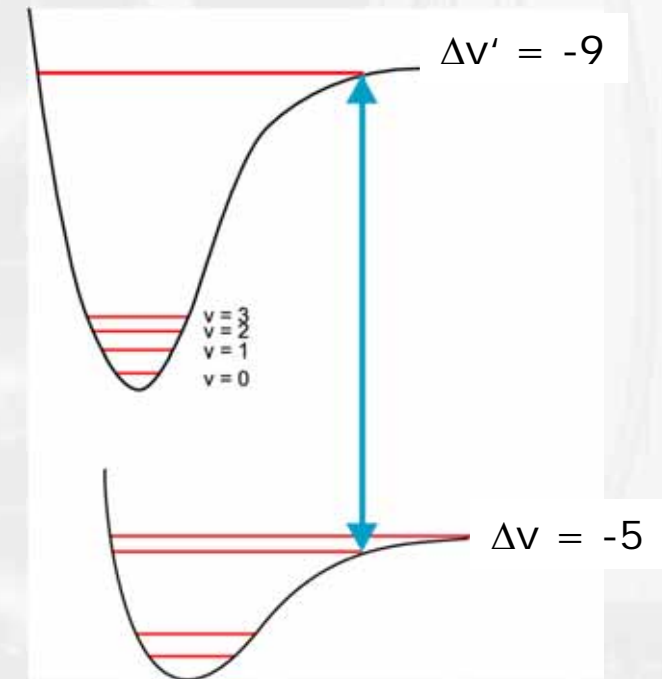
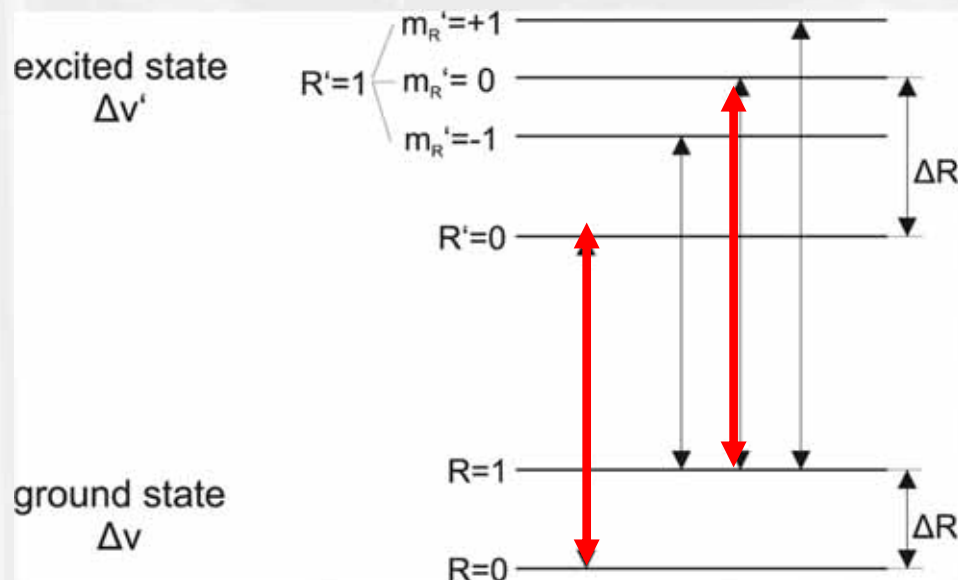


coupling laser  
( $\Delta v = -6 \rightarrow \Delta v' = -11$ )



# Autler-Townes Spectroscopy

⇒ coupling laser couples  $R=1$  and  $R=0$  transitions

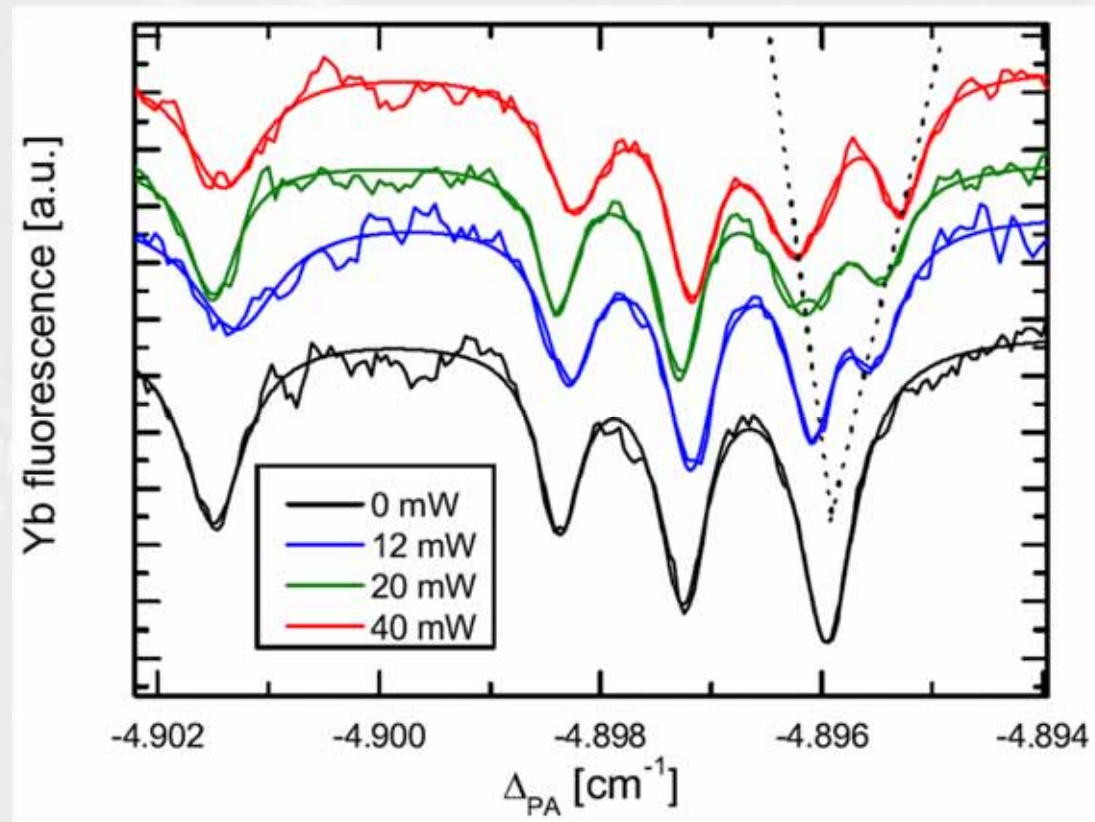


⇒  $\Delta R \sim \Delta R'$

⇒ similar classical outer turning points for ground and excited state

# Autler-Townes Spectroscopy

## Intensity-dependent splitting

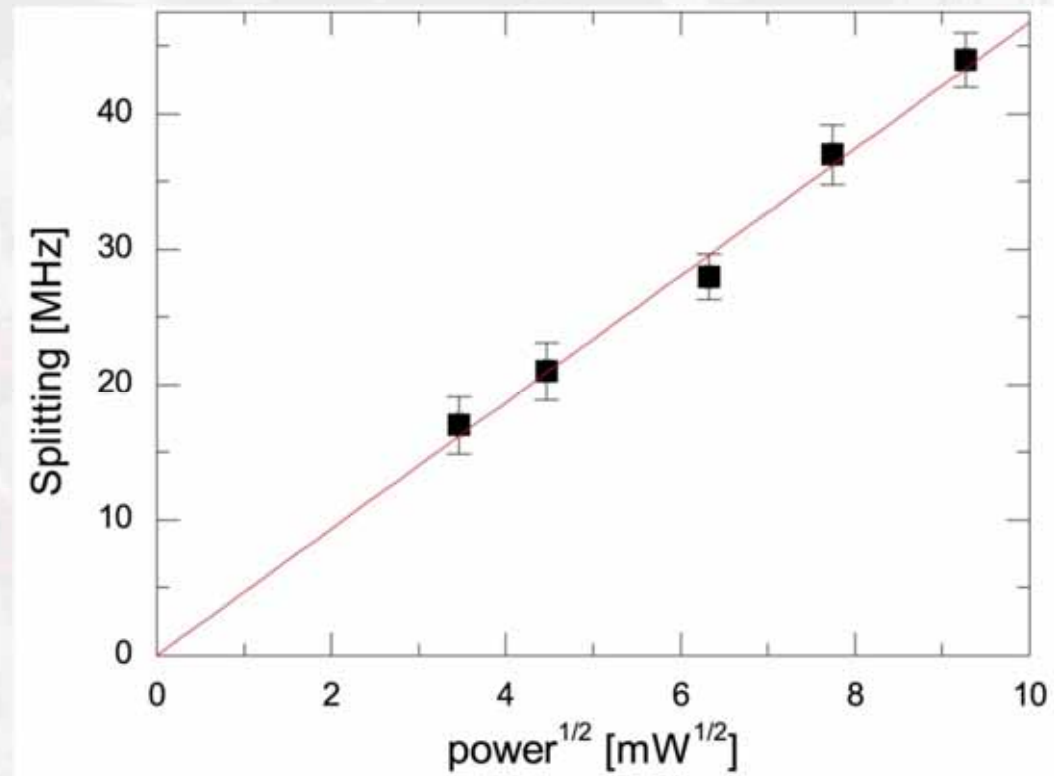


coupling laser  
( $\Delta v = -7 \rightarrow \Delta v' = -11$ )

# Autler-Townes Spectroscopy

Rabi frequency:

$$\Omega_{12} = \alpha |\langle b_1 | b_2 \rangle| \gamma_1 \sqrt{\frac{I}{4I_{\text{sat}}}}$$



coupling laser  
( $\Delta v = -7 \rightarrow \Delta v' = -11$ )

# Autler-Townes Spectroscopy

Franck-Condon factor

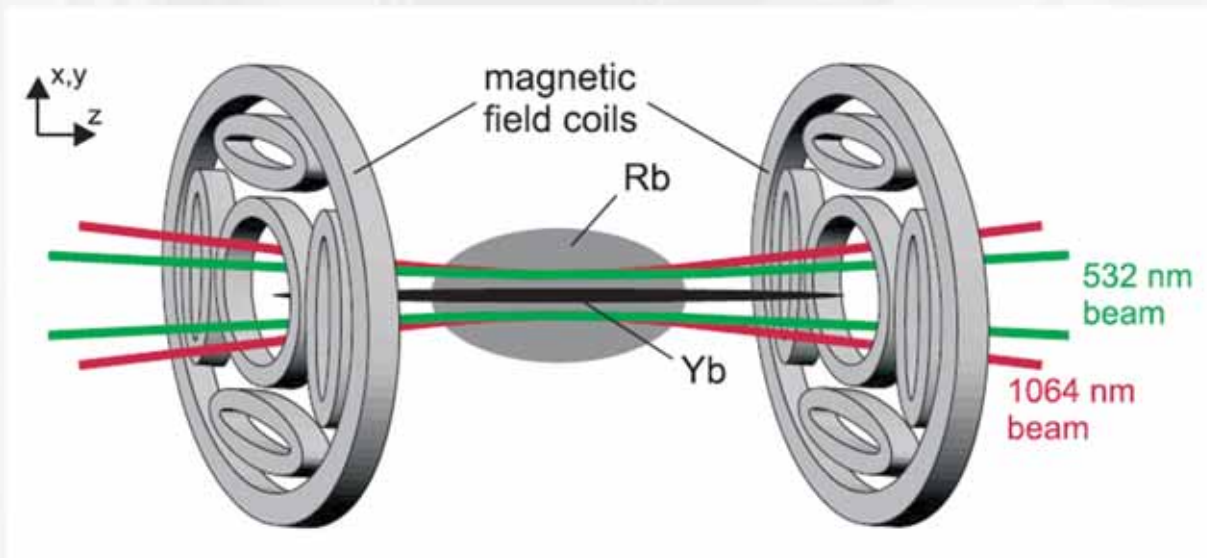
$$f_{FC} = |\langle b_1 | b_2 \rangle|^2 = \frac{\Omega_{12}^2}{\alpha^2 \gamma_1^2} \frac{4I_{\text{sat}}}{I}$$

$\Delta v'$	$\Delta v$	$\Delta_{\text{bind}} \text{ (cm}^{-1}\text{)}$	$f_{FC} \text{ (rel. units)}$
-11	-4 (F=1)	-0.390	$0.036 \pm 0.008$
	-6 (F=1)	-1.248	$0.35 \pm 0.10$
	-6 (F=2)	-1.248	$0.17 \pm 0.03$
	-7 (F=1)	-1.954	$0.030 \pm 0.002$
-9	-5 (F=1)	-0.751	$0.37 \pm 0.04$
	-5 (F=2)	-0.751	$0.41 \pm 0.02$

# 4. YbRb in the ground state: Feshbach resonances and/or Photoassociation

# Back to the conservative trap

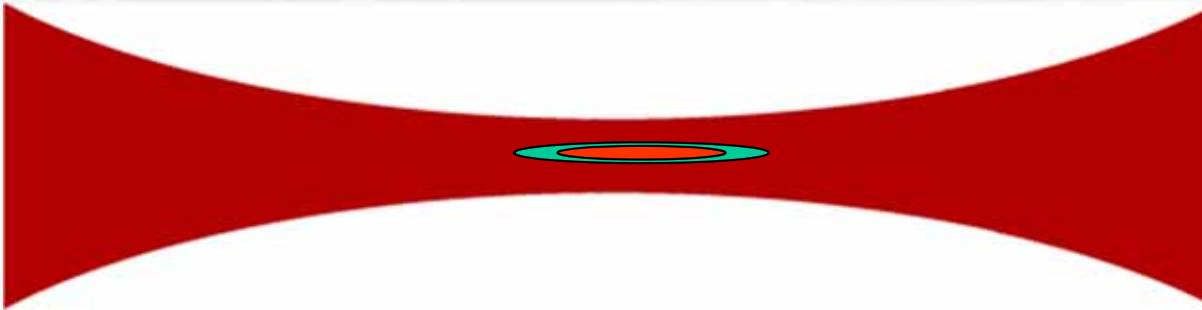
## Hybrid trap



- + independent manipulation
- + similar trap depths for Yb and Rb
- imperfect overlap
- hard to control experimentally

# Back to the conservative trap

## or simple optical trap?

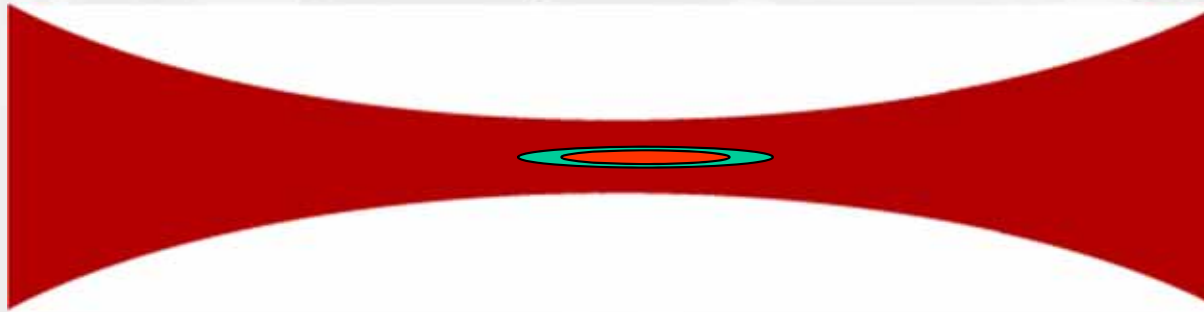


- + experimentally simple
- + automatic overlap of atomic clouds (for tight confinement)
- 5 x deeper trap for Rb
- no independent manipulation



# Back to the conservative trap

## 1st try: simple optical trap

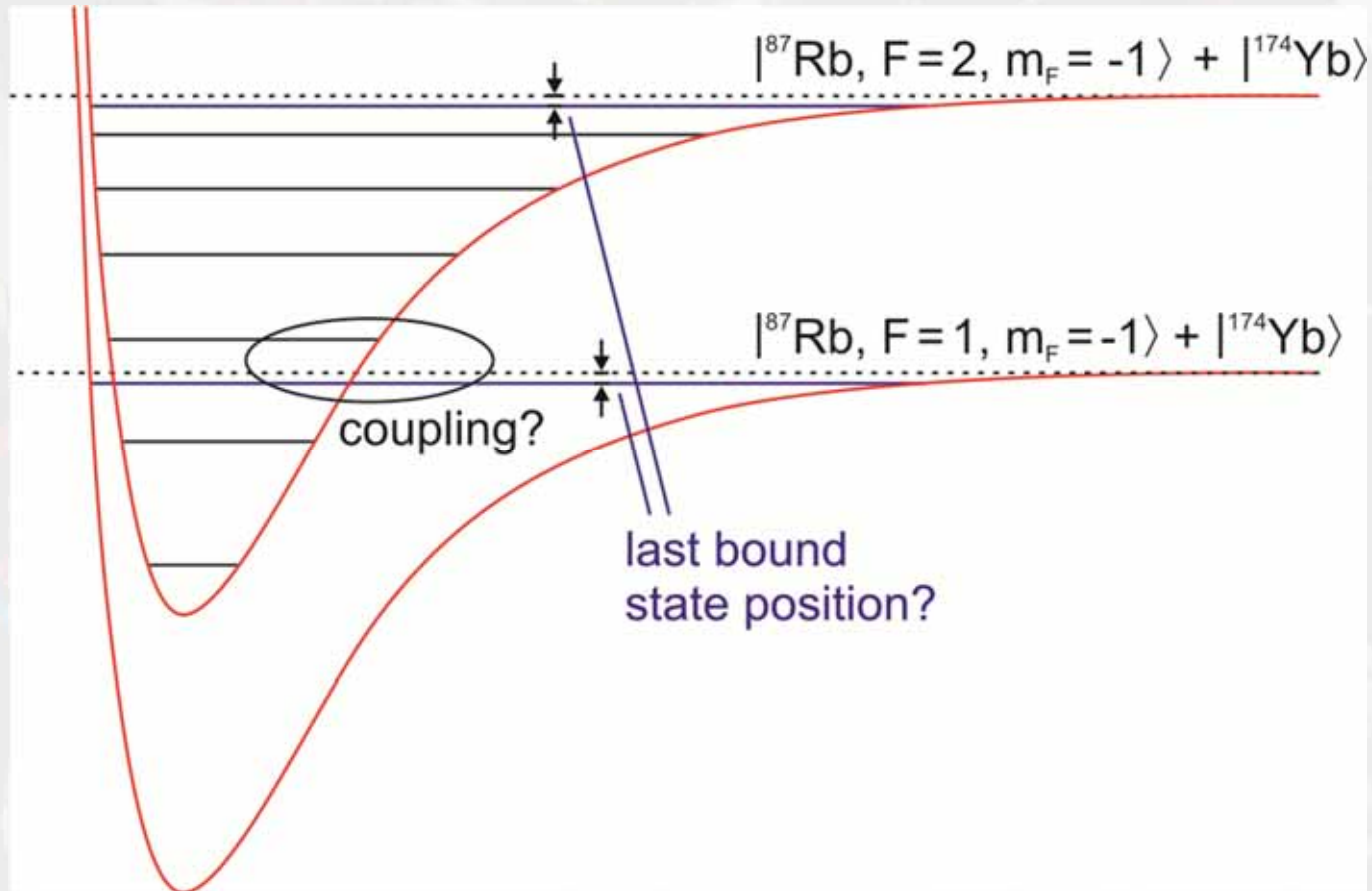


1st goal: Find Route to create vibrationally excited molecules

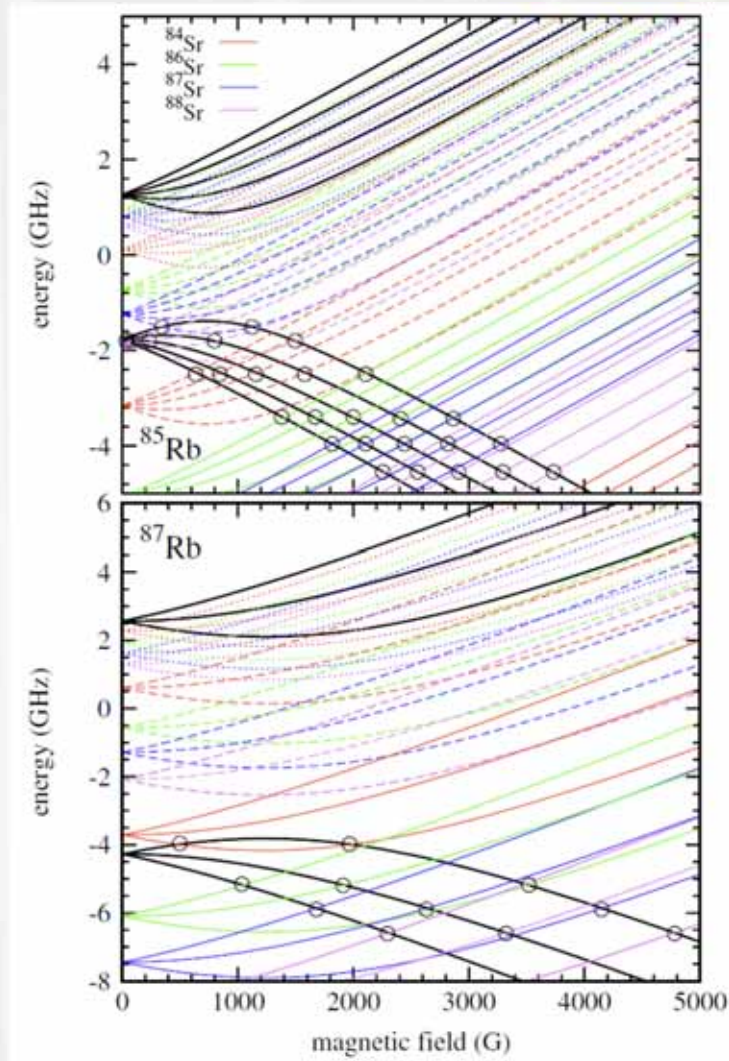
Feshbach

Photoassociation

# Feshbach resonances in YbRb



# Predictions for SrRb



	B (G)	$a_{bg}$	$\Delta B$ (mG)	
$^{87}\text{Rb}^{84}\text{Sr}$	477	1715.0	7.41	
	1959	1700.3	- 122	
	$^{87}\text{Rb}^{86}\text{Sr}$	1036	55.0	- 0.209
		1896	55.0	- 1.08
3472		55.0	- 2.29	
$^{87}\text{Rb}^{87}\text{Sr}$	1660	31.5	- 0.636	
	2608	31.5	- 2.27	
	4096	31.5	- 3.79	
$^{87}\text{Rb}^{88}\text{Sr}$	2281	1.6	- 33.6	
	3280	1.6	- 101	
	4716	1.5	- 153	

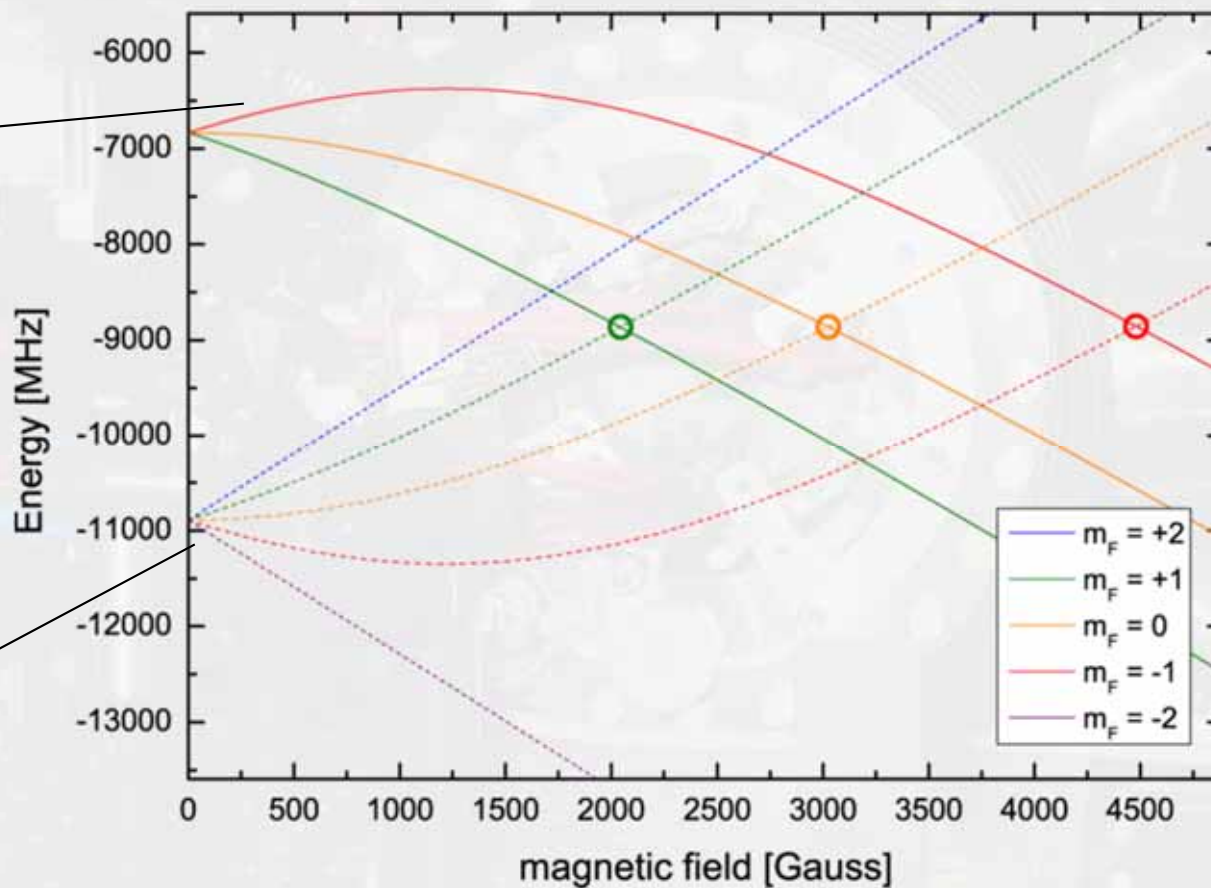
P. Zuchowski et al., PRL 105, 153201 (2010)  
for YbLi see D. Brue et al., PRL 108, 043201 (2012).

# Feshbach resonances in $^X\text{Yb}^{87}\text{Rb}$

$^{174}\text{Yb}^{87}\text{Rb}$

open  
channel

closed  
channel  
( $\Delta v = -4$ )



bosonic Yb:

$$\Rightarrow I_{\text{Yb}} = 0$$

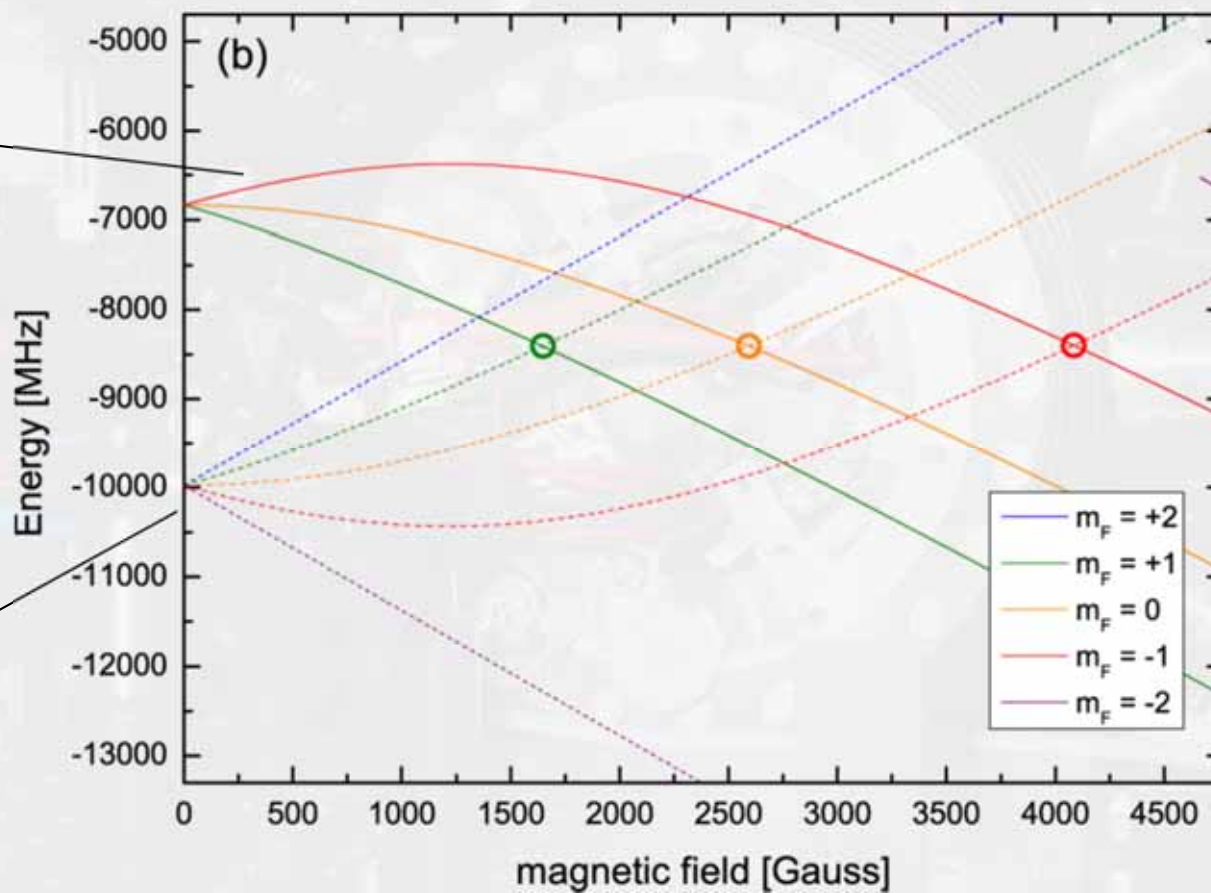
$\Rightarrow$  only  $\Delta m_F = 0$   
resonances

# Feshbach resonances in $^X\text{Yb}^{87}\text{Rb}$

$^{172}\text{Yb}^{87}\text{Rb}$

open channel

closed channel  
( $\Delta v = -4$ )



\*lowest resonances with  $^{87}\text{Rb}$ :

$^{168}\text{Yb}$	~ 850 G
$^{170}\text{Yb}$	~ 1250 G
$^{172}\text{Yb}$	~ 1650 G
$^{174}\text{Yb}$	~ 2000 G
$^{176}\text{Yb}$	~ 2500 G
$^{171}\text{Yb}$	~ 1150 G
$^{173}\text{Yb}$	~ 1550 G

\* values derived from simplified model

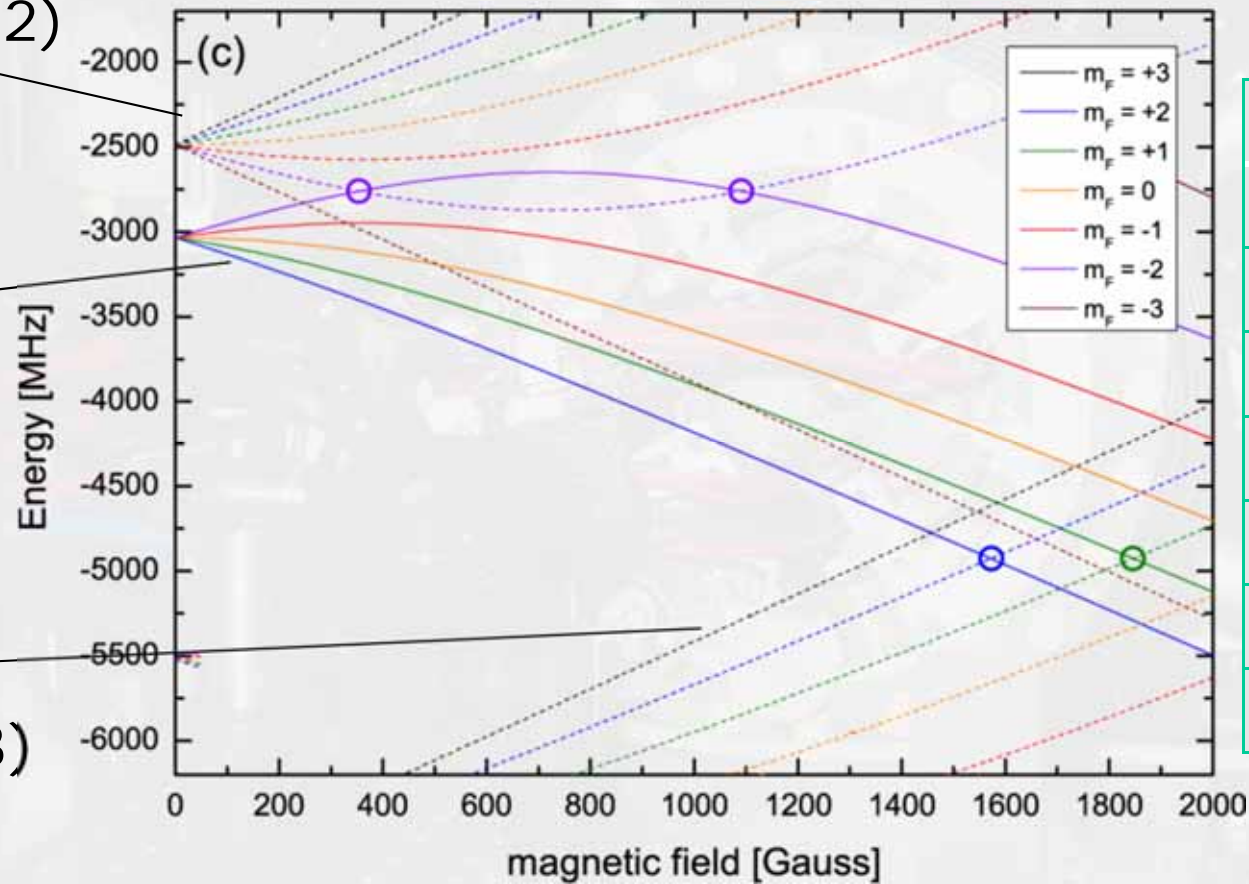
# Feshbach resonances in $^X\text{Yb}^{85}\text{Rb}$

closed channel  
( $\Delta v = -2$ )

$^{172}\text{Yb}^{85}\text{Rb}$

◊ lowest resonances with  $^{85}\text{Rb}$ :

open channel



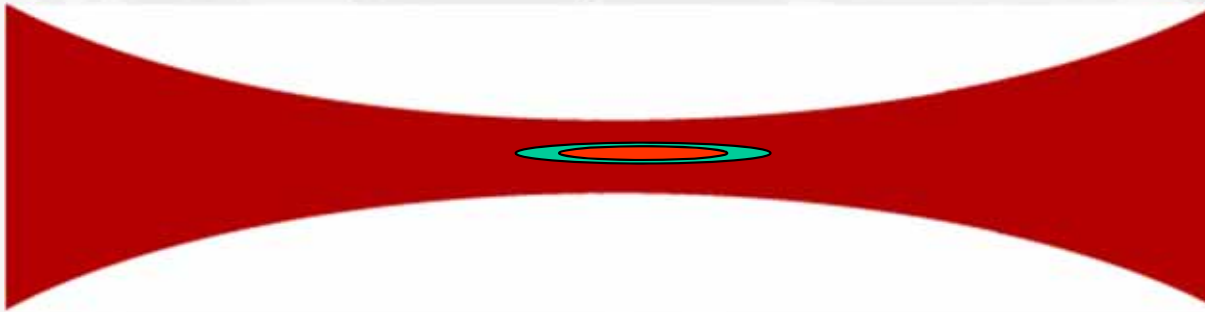
closed channel  
( $\Delta v = -3$ )

Isotope	B (G)	F, $m_F$
$^{168}\text{Yb}$	1078	2, 2 (a)
$^{170}\text{Yb}$	1323	2, 2 (a)
$^{172}\text{Yb}$	348	2, -2 (e)
$^{174}\text{Yb}$	98	2, -2 (e)
$^{176}\text{Yb}$	111	2, 2 (a)
$^{171}\text{Yb}$	539	2, -2 (e)
$^{173}\text{Yb}$	215	2, -2 (e)

◊ from model potential

# Searching Feshbach resonances

$^{174}\text{Yb}$  and  $^{85}\text{Rb}$  in single-beam optical trap

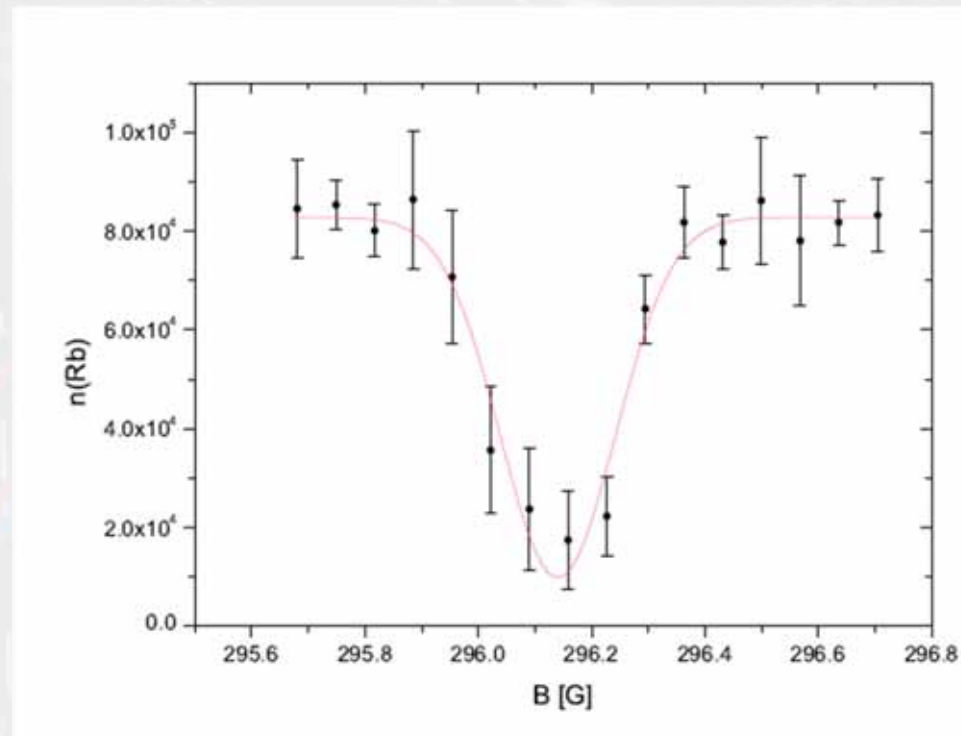


+ tunable magnetic field

⇒ Feshbach loss spectroscopy

# Searching Feshbach resonances

$^{85}\text{Rb} + ^{85}\text{Rb}$  Feshbach resonance



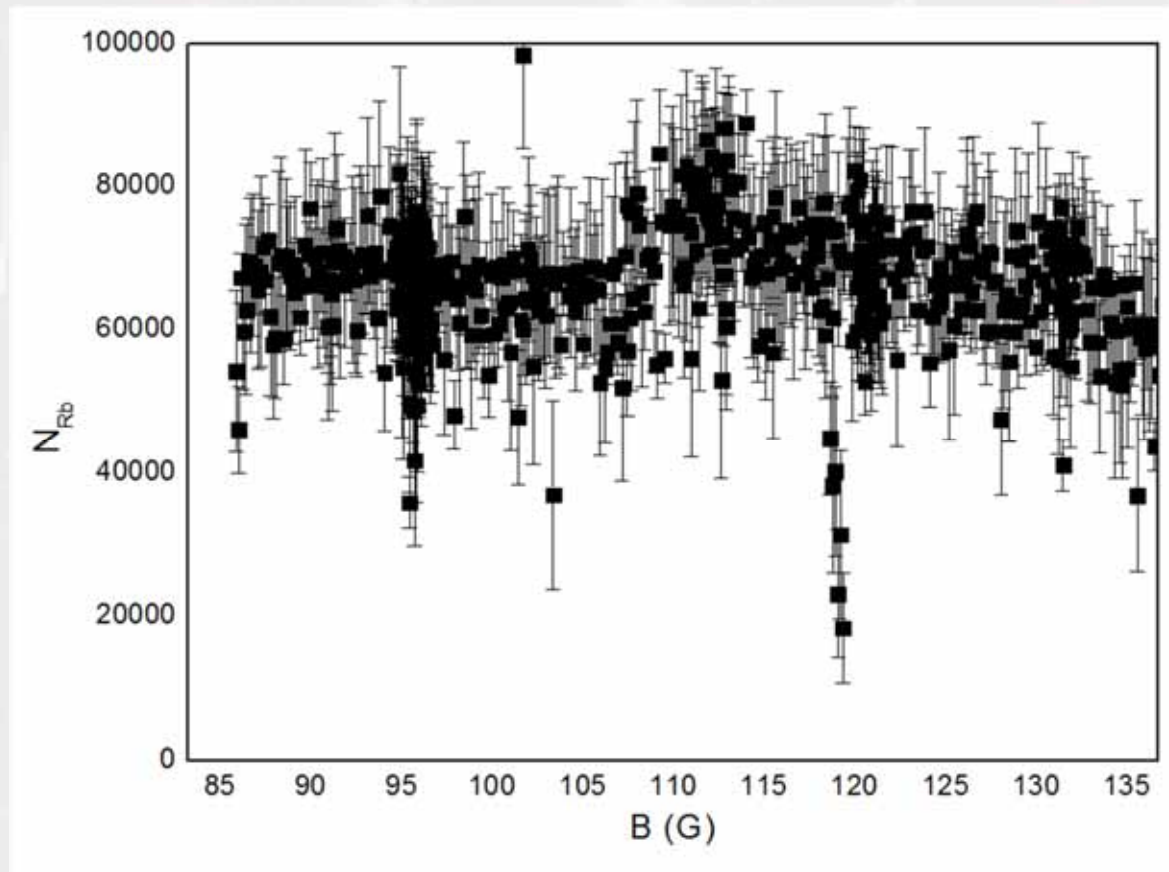
theoretical width<sup>1</sup>:  
 $\Delta \sim 1.8 \text{ mG}$

<sup>1</sup> C.Blackley et al. , arXiv:1212.5446



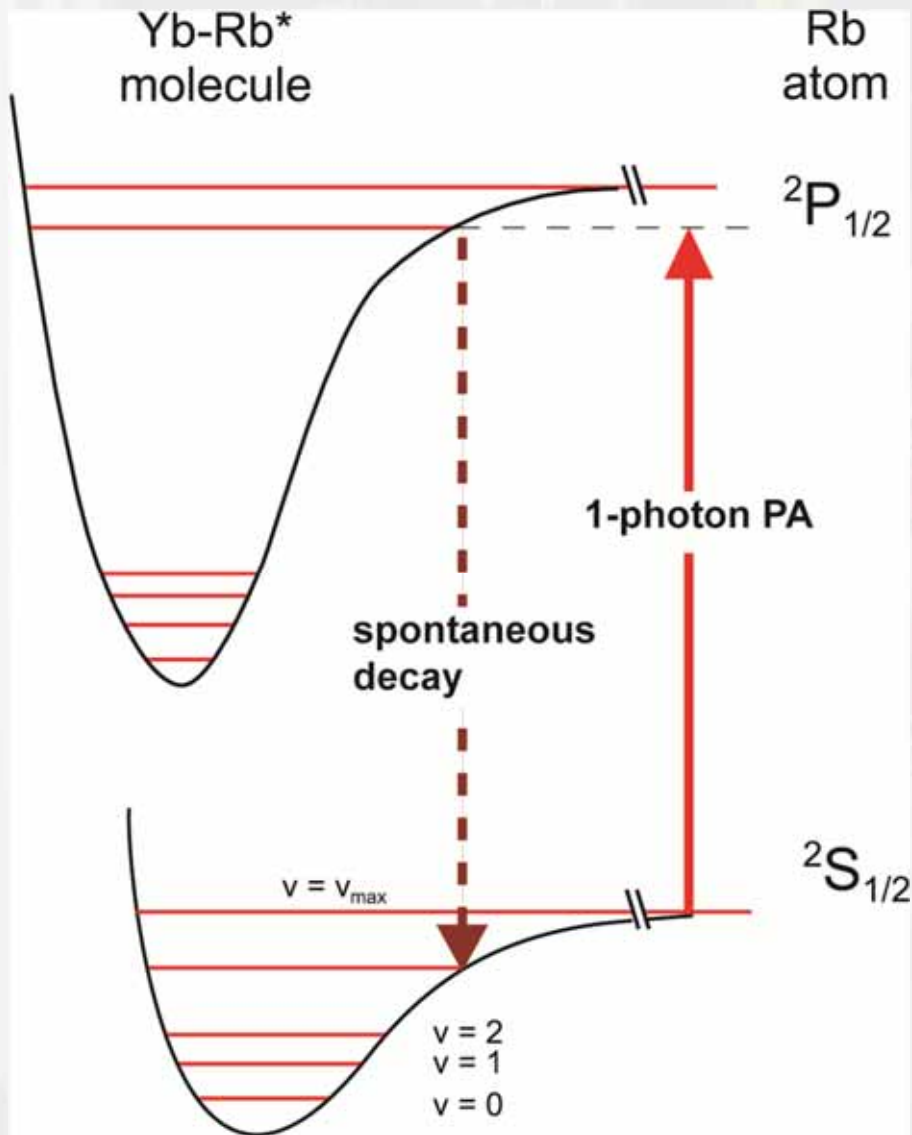
# Searching Feshbach resonances

Search for  $^{85}\text{Rb} + ^{174}\text{Yb}$  Feshbach resonance



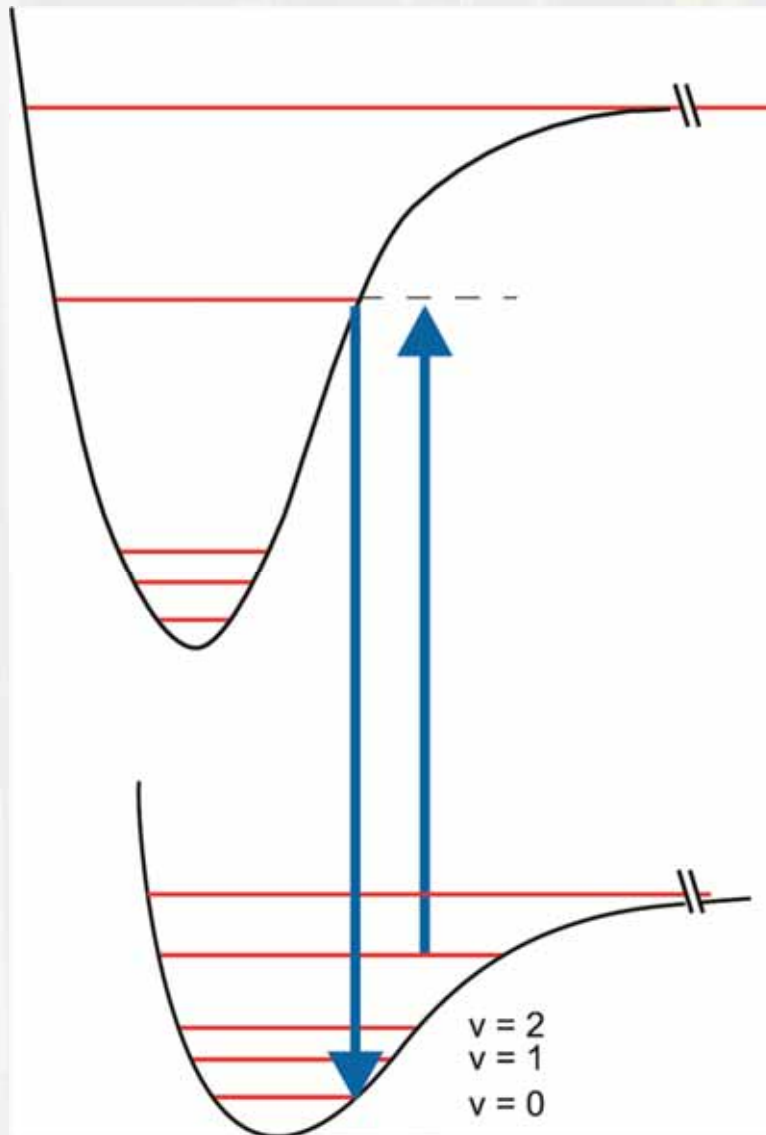
⇒ No Yb-Rb resonances observed so far

# Alternative Route: 1-Photon PA + spontaneous decay



- Excitation of YbRb\* (or Yb\*Rb) by single-photon PA
- Make use of large FC-Factors to populate only few vibrational levels of the ground state

# Final Step: STIRAP to lowest vibrational level



- STIRAP to  $v=0$  by choice of appropriate intermediate level
- YbRb is not chemically stable
- Possible environment: optical lattice @  $2 \mu\text{m}$

# The Team

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Cristian Bruni  
(PhD-student)

Ali Al-Massoudi  
(former MSc-student)

Fabian Wolf  
(MSc-student, not in  
picture)

## **Former members:**

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Nils Nemitz (PhD)

S.Tassy (PhD)

M. Madalinski (MSc)

