coherent control of photoassociation at ultracold temperatures: opportunities and fundamental limits

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U N I K A S S E L V E R S I T A T

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work done in collaboration with



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Ronnie Kosloff @ HUJI

wave properties of matter (superposition principle)

variation of phase between different, but indistinguishable quantum pathways:

constructive *interference* in desired channel destructive *interference* in all other channels

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how to solve the inversion problem? 'intuitive' approaches optimal control theory

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how to solve the inversion problem?



optimal control theory e STIRAP



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how to solve the inversion problem? 'intuitive' approaches optimal control theory

- bichromatic control
- pump-dump/probe
- STIRAP
 → DFS & other
 symmetry-adapted control

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how to solve the inversion problem?

'intuitive' approaches

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 → DFS & other
 symmetry-adapted control

optimal control theory

• theory: iterative solution of control equations



photoassociation = optical production of molecules



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• photoassociation possible

requires only optical transition

• photoassociation difficult

phase space compression

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coherent time evolution does not change 'quantumness' of the sample

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 $\hat{\boldsymbol{\rho}}_{T}=rac{1}{Z}e^{-\hat{\mathbf{H}}/k_{B}T}$

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example: photoassociation

assembling molecules from atoms using laser light

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- assembling molecules from atoms using laser light
- *short-pulse* photoassociation: after bond formation we can play the usual games of coherent control
 - pump-probe & pump-dump-probe schemes
 - engineering (coherent) wave packet dynamics
 - optical interference in multi-photon absorption

Koch & Shapiro, Chem Rev 212, 4928 (2012)

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• prototype of a light-induced binary reaction

controlling binary reactions

quantum system + light + interaction = pathway



- a femtosecond pulse induces a manifold of such state-to-state transitions
- the interferences are manipulated by shaping the exciting pulse and controlling the time delay between pulses

laser light = {frequency, amplitude, phase, polarization}

controlling a binary reaction



controlling a binary reaction



coherent control

• experimentally : extremely successful in unimolecular,

destructive processes (*dissociation*, *ionization*, . . .)

• open challenge: coherent control of

bond formation / binary reactions photoassociation = very simple binary reaction

photoassociation



= how to enhance reaction rate?

control versus entropy:

$$\operatorname{Tr}\{\hat{\boldsymbol{\rho}}_{T}^{2}\}$$
 $\hat{\boldsymbol{\rho}}_{T}=\frac{1}{Z}e^{-\hat{\mathbf{H}}/k_{B}T}$

two steps: photo-association & photo-stabilization

Improve the second s

- coherent control of tunneling resonances
- multi-photon femtosecond photoassociation
- 2 more efficient transitions to $X^1\Sigma_g^+(v=0)$:
 - strong spin-orbit interaction in heavy atoms

SrYb: Tomza, Pawłowksi, Jeziorska, Koch, Moszynski, Phys Chem Chem Phys 13, 18893 (2011) Sr₂: Skomorowski, Moszynski, Koch, Phys Rev A 85, 043414 (2012)

engineered wavepacket dynamics

Koch & Moszynski, Phys Rev A 78, 043417 (2008)

coherent photoassociation



Koch, Luc-Koenig, Masnou-Seeuws, Phys Rev A 73, 033408 (2006)

initial state: cold collisions

photoassociation is difficult

initial state

$$\hat{\boldsymbol{\rho}}_{T} = \frac{1}{Z_{eq}} e^{-\frac{\hat{\boldsymbol{h}}_{g}}{k_{B}T}}$$
$$= \frac{1}{Z_{eq}} \sum_{n,J} (2J+1)$$
$$e^{-\frac{E_{n,J}}{k_{B}T}} |E_{n,J}\rangle \langle E_{n,J}|$$

=thermal ensemble

Koch, Kosloff, Luc-Koenig, Masnou-Seeuws, Crubellier, J Phys B 39, S1017 (2006)

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hot vs cold photoassociation



- only few lowest partial waves
 → high initial purity Tr[p²_T]
- photoassociation at large R
- huge influence of resonances

hot vs cold photoassociation





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- many partial waves \rightarrow almost zero initial purity $\text{Tr}[\hat{\rho}_T^2]$
- photoassociation at short *R*
- some influence of resonances

hot photoassociation: FC filtering at short R

Rybak, Amaran, Levin, Tomza, Moszynski, Kosloff, Koch, Amitay, Phys Rev Lett 107, 273001 (2011) Rybak, Amitay, Amaran, Kosloff, Tomza, Moszynski, Koch, Faraday Discuss. 153, 383 (2011)



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photoassociated molecules = sub-ensemble of higher purity

hot vs cold photoassociation





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Naidon & Masnou-Seeuws, Phys Rev A 68, 033612 (2003)

reduced pair wave function



 $\Phi_{00}(x,y) = \frac{1}{\sqrt{2}} \Psi_0(x) \Psi_0(y) \varphi(x,y)$

Naidon & Masnou-Seeuws, Phys Rev A 68, 033612 (2003)

reduced pair wave function

if

- extent of $\varphi(x, y; t) \ll$ condensate length scale
- igher than 2nd order terms do not affect φ(x, y; t)

then

$$i\hbar\frac{\partial\varphi}{\partial t} = \left(-\frac{\hbar^2}{2m}\Delta_x + \Delta_y + V_2(x-y)\right)\varphi(x-y)$$



$$\Phi_{00}(x,y) = \frac{1}{\sqrt{2}} \Psi_0(x) \Psi_0(y) \varphi(x,y)$$

(x, y; t)

equivalent result obtained for 1st order cumulant expansion Köhler & Burnett, Phys Rev A 65, 033601 (2002)



first experiment

demonstrating femtosecond photoassociation of ultracold atoms

Salzmann et al., PRL 100, 233003 (2008) [Weidemüller & Wöste groups]



narrow transitions & broad-band light



certain phase functions annihilate the two-photon absorption

Meshulach & Silberberg, Nature 396, 239 (1998)
two-photon photoassociation

$$\mathbf{\hat{H}}(t) = \begin{pmatrix} \mathbf{\hat{T}} + V_g(\mathbf{\hat{R}}) + \omega_g^S(t) & \chi(t)e^{-i\varphi(t)} \\ \chi(t)e^{i\varphi(t)} & \mathbf{\hat{T}} + V_e(\mathbf{\hat{R}}) + \Delta_{2P} + \omega_e^S(t) \end{pmatrix}$$

generalization of model for two-photon absorption of Trallero-Herrero et al., Phys Rev A 71, 013423 (2005)

we seek broadband excitation which is dark for the atoms but excites molecules

Koch, Ndong, Kosloff, Faraday Discuss. 142, 389 (2009)

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generalization of model for two-photon absorption of Trallero-Herrero et al., Phys Rev A 71, 013423 (2005)

two-photon couplings:

$$\chi(t) = -\frac{1}{4}E_0^2|S(t)|^2\sum_m \frac{\mu_{em}\mu_{mg}}{\omega_{mg}-\omega_L}$$

dynamic Stark shifts:

$$\omega_i^S(t) = -\frac{1}{2} E_0^2 |S(t)|^2 \sum_m |\mu_{mi}|^2 \frac{\omega_{mi}}{\omega_{mi}^2 - \omega_L^2}, \quad i = g, e$$

we seek broadband excitation which is dark for the atoms but excites molecules

Koch, Ndong, Kosloff, Faraday Discuss. 142, 389 (2009)

atoms: two-photon dark states

analytical solutions

weak field

strong field

• two-photon absorption $\sim \int d\omega E(\omega) E(\omega_L - \omega)$



• phase function: destructive IF

atoms: two-photon dark states analytical solutions

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g

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strong field

- chirped pulse
- phase locking: laser phase compensates for matter phase due to dynamical Stark shift
- Rabi cycling: two-photon 2π pulse

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can be generalized to multi-photon transitions

three-photon photoassociation: Rb₂

Tomza, Goerz, Musiał, Moszynski, Koch, Phys Rev A 86, 043424 (2012)



- 1/*R*³ excited states
- multi-photon selection rules
- strong spin-orbit coupling
- crossing of ion-pair state

three-photon photoassociation: Rb₂

Tomza, Goerz, Musiał, Moszynski, Koch, Phys Rev A 86, 043424 (2012)

$$\hat{\mathbf{H}}_{pump}(t) = \begin{pmatrix} \hat{\mathbf{H}}^{a^{3}\Sigma_{u}^{+}}(R) & 0 & \boldsymbol{\epsilon}^{*}(t)^{3}\chi^{(3)}(\omega_{L}, R) & 0\\ 0 & \hat{\mathbf{H}}^{(5)^{1}\Sigma_{g}^{+}}(R) & \boldsymbol{\xi}_{3}(R) & A(R)\\ \boldsymbol{\epsilon}(t)^{3}\chi^{(3)}(R) & \boldsymbol{\xi}_{3}(R) & \hat{\mathbf{H}}^{(3)^{3}\Pi_{g}}(R) - \boldsymbol{\xi}_{4}(R) & \boldsymbol{\xi}_{5}(R)\\ 0 & A(R) & \boldsymbol{\xi}_{5}(R) & \hat{\mathbf{H}}^{(6)^{1}\Sigma_{g}^{+}}(R) \end{pmatrix}$$

•
$$\hat{\mathbf{H}}^{2S+1|\Lambda|} = \hat{\mathbf{T}} + V^{2S+1|\Lambda|}(R) + \omega_S^{2S+1|\Lambda|}(t,R) + \Delta_{\omega_L}$$

- $\chi^{(3)}(\omega_L, R)$ three-photon coupling
- ξ_j spin-orbit couplings
- *A*(*R*) non-adiabatic radial coupling

optimal control calculations in progress

poster next week

two-photon dump: Rb₂

Tomza, Goerz, Musiał, Moszynski, Koch, Phys Rev A 86, 043424 (2012)





- $\hat{\mathbf{H}}^{2S+1|\Lambda|} = \hat{\mathbf{T}} + V^{2S+1|\Lambda|}(R) + + \Delta_{\omega_L}^{np}$
- $d_i(R)$ transition dipole matrix elements
- *ξ_j* spin-orbit couplings
- *A*(*R*) non-adiabatic radial coupling

optimized two-photon dump: Rb₂

Tomza, Goerz, Musiał, Moszynski, Koch, Phys Rev A 86, 043424 (2012)



optimized two-photon dump: Rb₂



summary

multi-photon photoassociation of Rb₂

Tomza, Goerz, Musiał, Moszynski, Koch, Phys Rev A 86, 043424 (2012)

• multi-photon ionization:

problem of bandwidth, selection rules

• ion-pair state:

speed up excited state dynamics

- strong spin-orbit coupling: singlet-triplet conversion, efficient dumping
- optimal control can teach you how to take full advantage of complex dynamics

hot vs cold photoassociation





hot

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- photoassociation at large *R*
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González-Férez & Koch, Phys Rev A 86, 063420 (2012) = -620 resonance position (mK $S_0 + P_1$ 15 PA 10 5 $E_{coll} = 1 \,\mu K$ = 00 50 100 150 0 0.2 0.4 0.6 0.8 1.2 0 internuclear separation intensity (10^{10} W/cm²) (units of bohr radii)

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González-Férez & Koch, Phys Rev A 86, 063420 (2012)

intensity (10^{10} W/cm²)





non-resonant field control

Ağanoğlu, Lemeshko, Friedrich, González-Férez, Koch, arXiv:1105.0761 González-Férez & Koch, Phys Rev A 86, 063420 (2012)

$$\hat{\mathbf{H}} = \hat{\mathbf{T}} + V(\hat{\mathbf{R}}) + \frac{1}{2\mu\hat{\mathbf{R}}^2}\hat{\mathbf{J}}^2 - \frac{2\pi I}{c}\left(\Delta\alpha(\hat{\mathbf{R}})\cos^2\hat{\boldsymbol{\theta}} + \alpha_{\perp}(\hat{\mathbf{R}})\right)$$

coupling of field *I* to polarizability anisotropy $\Delta \alpha(\hat{\mathbf{R}})$

$$\begin{aligned} \alpha_{\perp}(\mathbf{\hat{R}}) &\approx 2\alpha_0 - 2\alpha_0^2/\mathbf{\hat{R}}^3 + 2\alpha_0^3/\mathbf{\hat{R}}^6 \\ \alpha_{\parallel}(\mathbf{\hat{R}}) &\approx 2\alpha_0 + 4\alpha_0^2/\mathbf{\hat{R}}^3 + 8\alpha_0^3/\mathbf{\hat{R}}^6 \end{aligned}$$

Silberstein's formula

non-resonant field control

Ağanoğlu, Lemeshko, Friedrich, González-Férez, Koch, arXiv:1105.0761

González-Férez & Koch, Phys Rev A 86, 063420 (2012)



use the non-resonant field to control the position of the shape resonance, bringing it close to $k_B T_{trap}$

enhancement of the pair density: ⁸⁸Sr₂



photoassociation

in the presence of a non-resonant field

$$\hat{\mathbf{H}} = \begin{pmatrix} \hat{\mathbf{T}} + V_g(\hat{\mathbf{R}}) & -\frac{1}{2}D(\hat{\mathbf{R}})\sqrt{\frac{I_{PA}}{2\epsilon_o c}}\cos\hat{\theta} \\ -\frac{1}{2}D(\hat{\mathbf{R}})\sqrt{\frac{I_{PA}}{2\epsilon_o c}}\cos\hat{\theta} & \hat{\mathbf{T}} + V_e(\hat{\mathbf{R}}) + \Delta_{PA} \end{pmatrix} \\ + \frac{\hat{\mathbf{J}}^2}{2\mu\hat{\mathbf{R}}^2} - \frac{2\pi I_{NR}}{c} \begin{bmatrix} \begin{pmatrix} \Delta\alpha_g(\hat{\mathbf{R}}) & 0 \\ 0 & \Delta\alpha_e(\hat{\mathbf{R}}) \end{pmatrix} \cos^2\hat{\theta} \\ & + \begin{pmatrix} \alpha_{\perp,g}(\hat{\mathbf{R}}) & 0 \\ 0 & \alpha_{\perp,e}(\hat{\mathbf{R}}) \end{pmatrix} \end{bmatrix}$$

photoassociation rates

- ensemble with Maxwell-Boltzmann velocity distribution
- isolated resonance
- weak PA laser

$$K_{v'}(I_{PA}, \Delta_{PA}, T) \approx \frac{4\pi^2 I_{PA}}{c} \frac{k_B T}{hQ_T} \\ \int_0^\infty \sum_{J=0}^\infty \sum_{M=-J}^J e^{-\frac{E}{k_B T}} \frac{\gamma_{v'} |D_{v'J'}(E)|^2}{(E - \Delta_{v'J'})^2 + (\gamma/2)^2} \frac{dE}{k_B T}$$

$$D_{v'J'}(E) = \langle \psi^{e}_{v'J'} | D(\mathbf{\hat{R}}) \cos \mathbf{\hat{\theta}} | \psi^{g}_{J}(E) \rangle$$

 $|\psi_I^g(E)\rangle$ modified by I_{NR}

photoassociation of Sr₂

Skomorowski, Moszynski, Koch, Phys Rev A 85, 043414 (2012)



effect of non-resonant light



enhancement of PA rate



enhanced PA rates by shape resonance control



envisioned scheme for PA

- slowly switching on the non-resonant field thermal cloud follows adiabatically
- Photoassociation in presence of non-resonant field PA laser finds enhanced pair density at relevant interatomic separations due to non-resonant field
- spontaneous decay

ground state molecules in hybridized levels

- slowly/suddenly switching off the non-resonant field ground state molecules in field-free levels
- Raman transfer to v = 0

into hybridized ground state levels



into hybridized ground state levels

followed by adiabatic switch off of non-resonant light



into hybridized ground state levels

followed by adiabatic switch off of non-resonant light



into hybridized ground state levels

followed by sudden switch off of non-resonant light



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- spontaneous decay ground state molecules in hybridized levels
- slowly/suddenly switching off the non-resonant field ground state molecules in field-free levels
- Solution Raman transfer to v = 0

Skomorowski, Moszynski, Koch, Phys Rev A 85, 043414 (2012)

outlook:

non-resonant light control of scattering

in collaboration with R. González-Férez, P. Julienne, J. Ye



- heating due to light scattering can be made small by using far off-resonant laser light (λ_{NR} = 10 μm)
- also scattering of higher partial waves will be affected

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non-resonant light control of scattering

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- heating due to light scattering can be made small by using far off-resonant laser light (λ_{NR} = 10 μm)
- also scattering of higher partial waves will be affected opening the way toward all-optical control of scattering!

summary

photoassociation as a binary reaction

• photoassociation:

coherent control out of scattering continuum

- initial thermal ensemble can be significantly altered by tuning scattering resonances
- here: non-resonant field control of shape resonances related: Feshbach-optimized photoassociation Pellegrini, Gacesa, Cóté, Phys Rev Lett 101, 053201 (2008)
- generally applicable

best for heavy atoms with large polarizabilities and large scattering lengths

take home messages

• photoassociation:

coherent control out of scattering continuum coherence distillation/Franck-Condon filtering

• coherent evolution after bond formation:

play all the games of coherent control

• low temperature:

initial thermal ensemble of high purity can be significantly altered by tuning scattering resonances