

# Progress Towards a Theory of the IMF

Mark Krumholz (ANU)

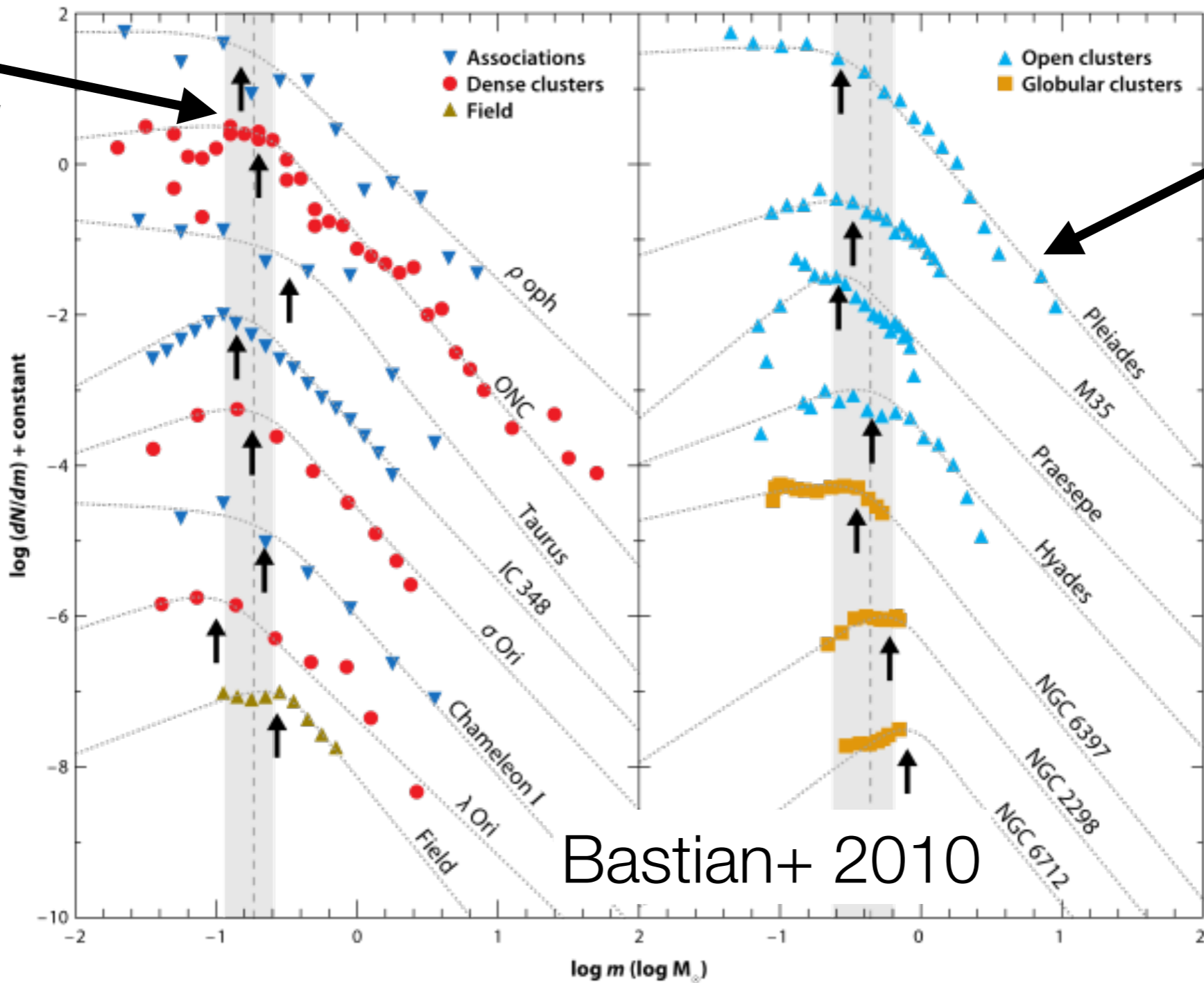
# Explaining the Low-Mass IMF

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- The isothermal conundrum
- Possible solutions
  - The galactic approach: ordinary or turbulent Jeans mass
  - The small-scale approach: equation of state and radiative feedback models
- Concluding thoughts

# What We'd Like to Explain

Not a powerlaw



Powerlaw

Bastian+ 2010

# Why This Matters

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- Stars have a distinctive mass scale (few x 0.1 M<sub>⊙</sub>)
- Classical explanation: this mass reflects the Jeans mass in the star-forming cloud

$$M_J \approx \frac{c_s^3}{\sqrt{G^3 \rho}} \approx 0.3 M_{\odot} \left( \frac{T}{10 \text{ K}} \right)^{3/2} \left( \frac{n}{10^5 \text{ cm}^{-3}} \right)^{1/2}$$

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# The Isothermal Conundrum

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$$\begin{aligned}\frac{\partial \rho}{\partial t} &= -\nabla \cdot (\rho \mathbf{v}) \\ \frac{\partial}{\partial t}(\rho \mathbf{v}) &= -\nabla \cdot (\rho \mathbf{v} \mathbf{v}) - c_s^2 \nabla \rho + \frac{1}{4\pi} (\nabla \times \mathbf{B}) \times \mathbf{B} - \rho \nabla \phi \\ \frac{\partial \mathbf{B}}{\partial t} &= -\nabla \times (\mathbf{B} \times \mathbf{v}) \\ \nabla^2 \phi &= 4\pi G \rho\end{aligned}$$

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 \end{aligned}$$

- Dimensionless numbers unchanged by  $\rho_0 \rightarrow x\rho_0$ ,  $L \rightarrow x^{-1/2}L$ ,  $B_0 \rightarrow x^{-1/2}B_0$ , but mass changes by  $M \rightarrow x^{-1/2}M$
- Implication: isothermal gas has no mass scale!

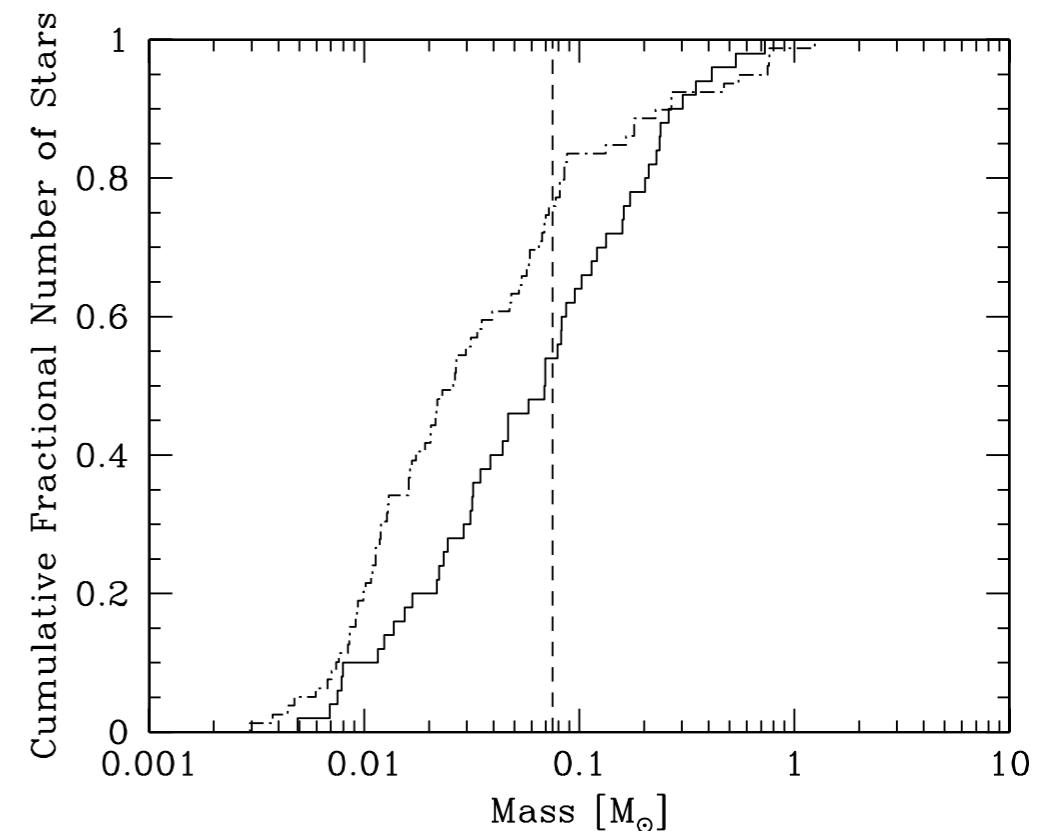
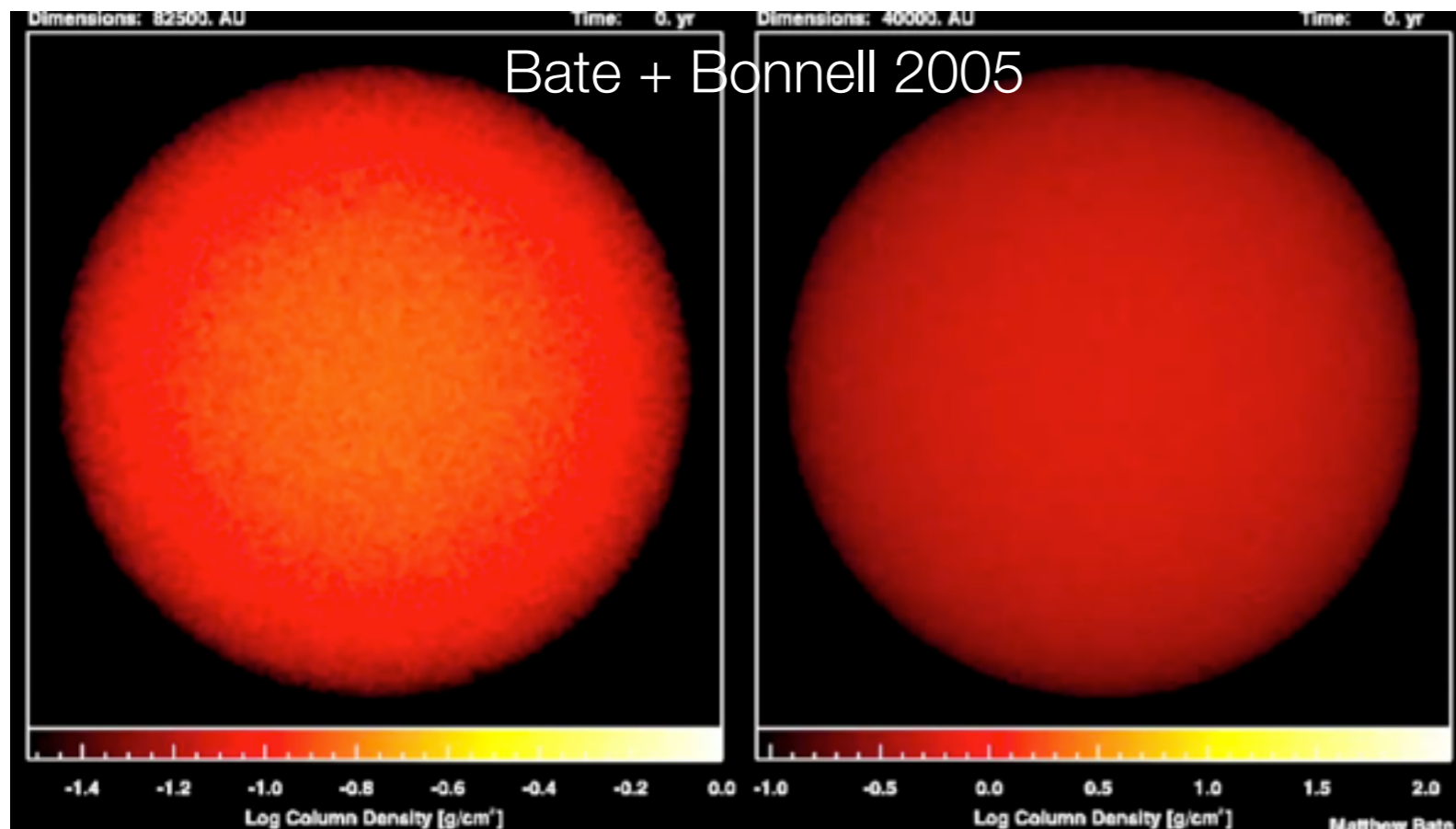
# How Do We Get Out of This?

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- Need to bring in extra physics beyond self-gravitating isothermal MHD turbulence to explain low mass IMF
- Three basic approaches
  - IMF set by the large-scale properties of the galaxy
  - IMF set by deviations from isothermal behavior due to dust-gas coupling and/or opacity effects
  - IMF set by local radiative feedback processes

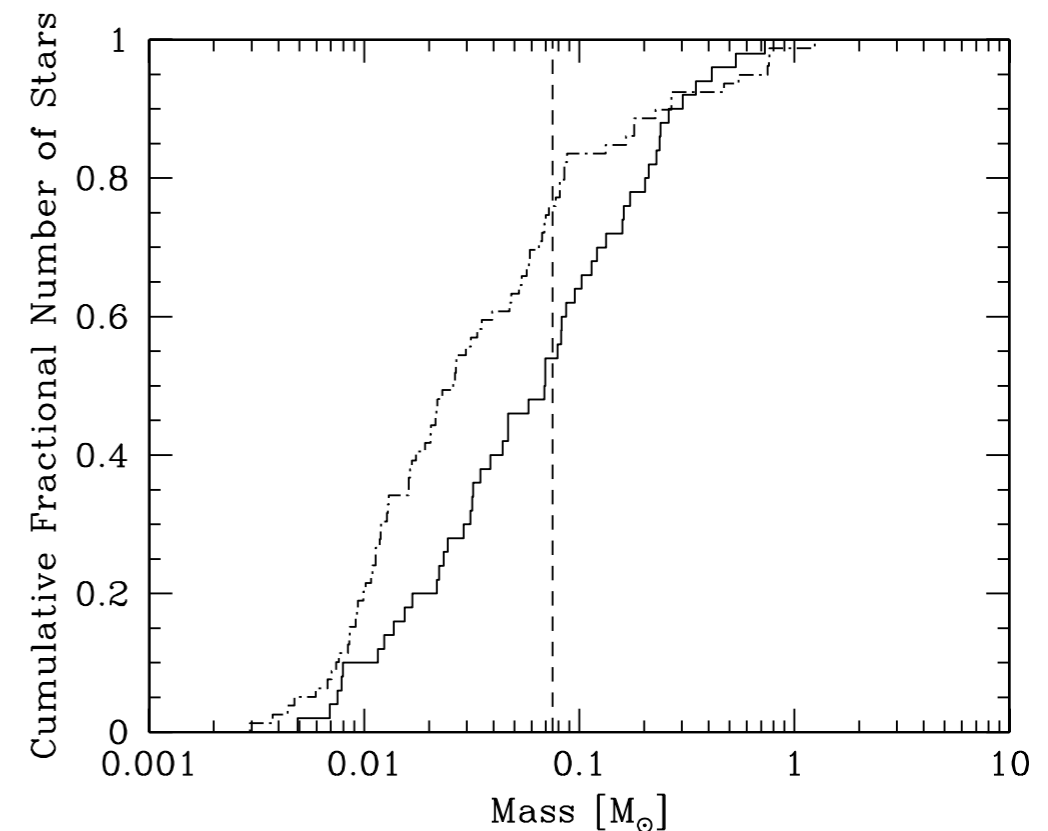
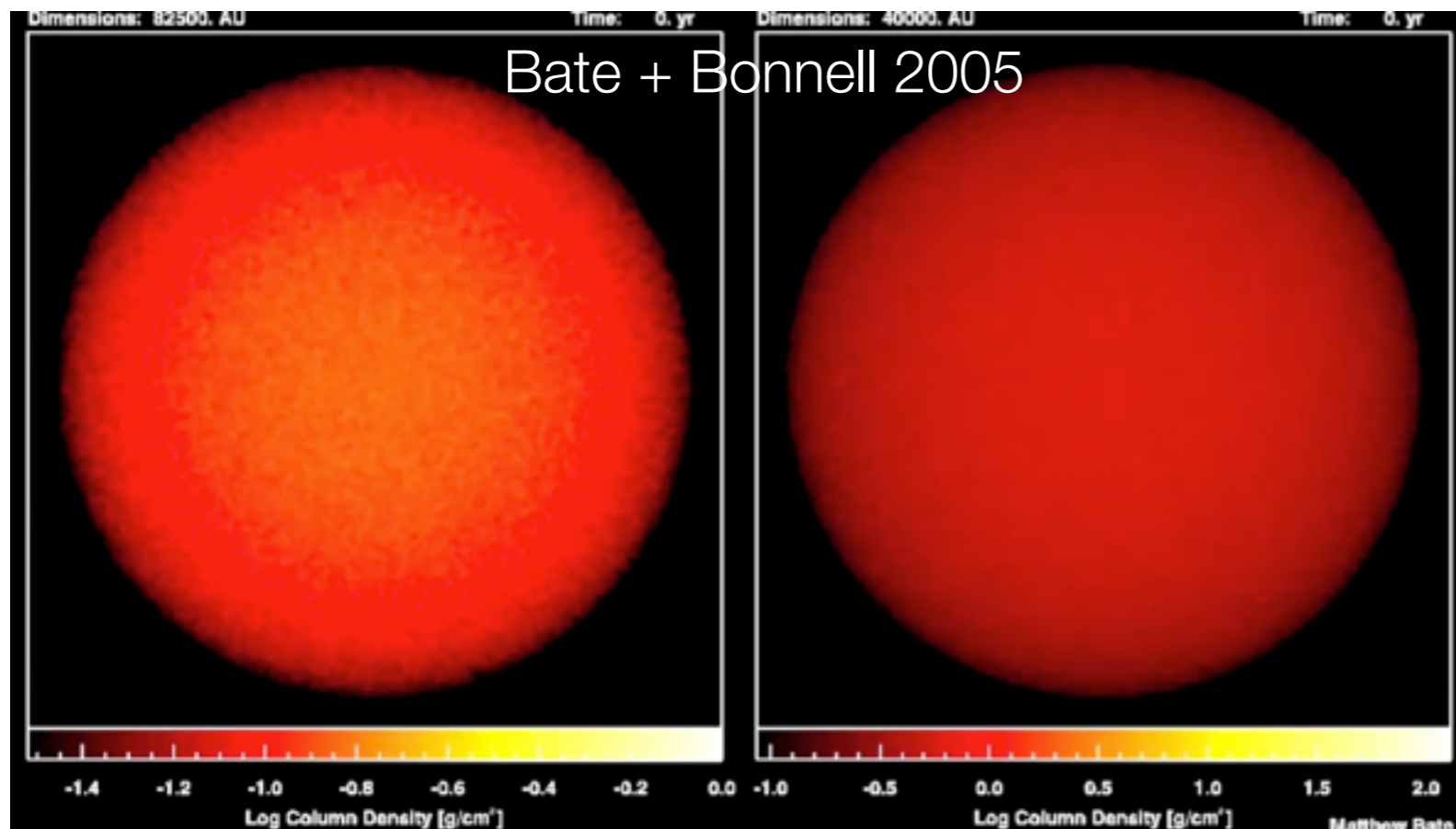
# Galactic Hypothesis v1: The Jeans Mass

- Conjecture: IMF peak  $\sim$  Jeans mass at GMC mean density (Bate + Bonnell 2005; Tumlinson 2007; Narayanan & Dave 2012, 2013)
- Implies top-heavy IMF at high SFR, high  $z$  due to high gas temp



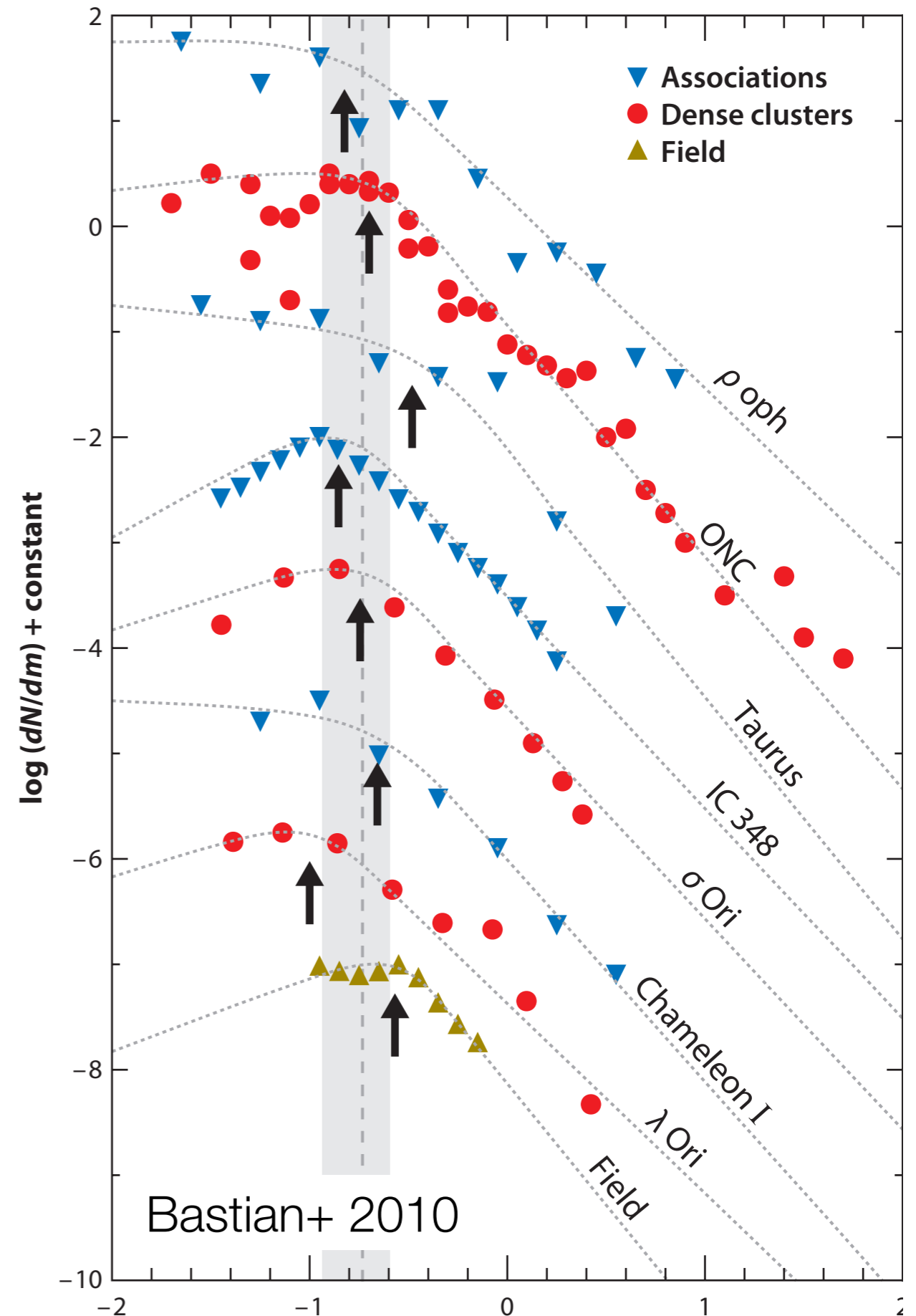
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# Problems with Jeans Mass Hypothesis

- Densities vary widely in local SF regions, e.g.,
  - Taurus:  $\approx 60$  stars  $\text{pc}^{-3}$  (Hartman 2002)
  - ONC:  $\sim 20,000$  stars  $\text{pc}^{-3}$  (Hillenbrand + Hartmann 1998)
- Factor of  $\sim 300$  density variation should produce factor of  $\sim 20$  IMF variation
- NOT OBSERVED!



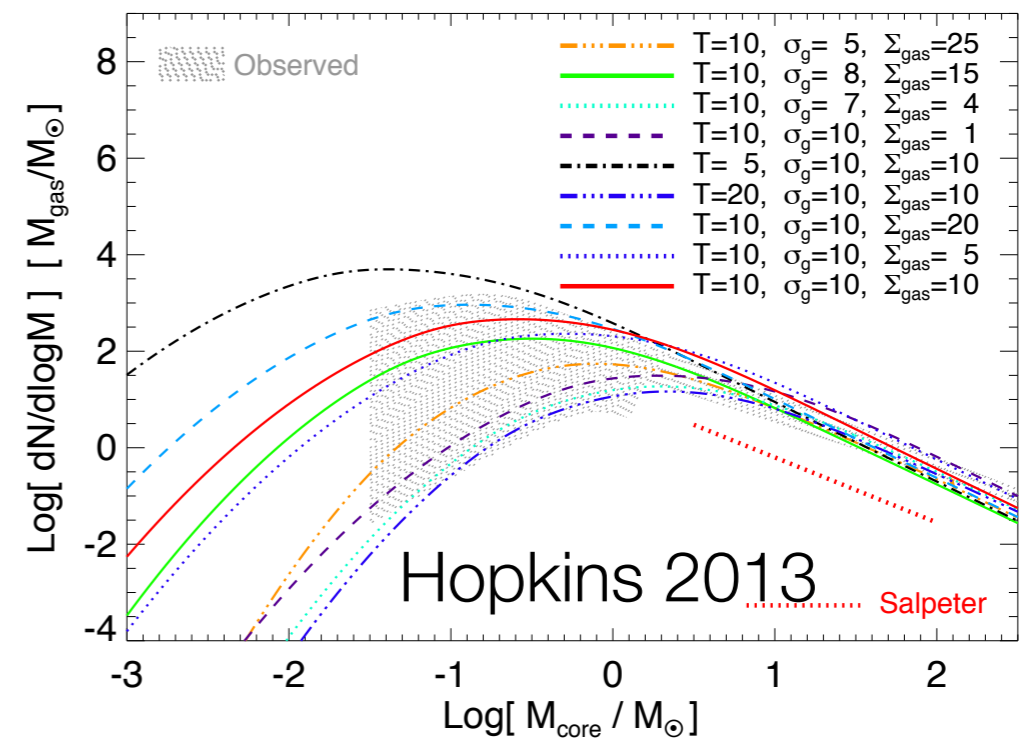
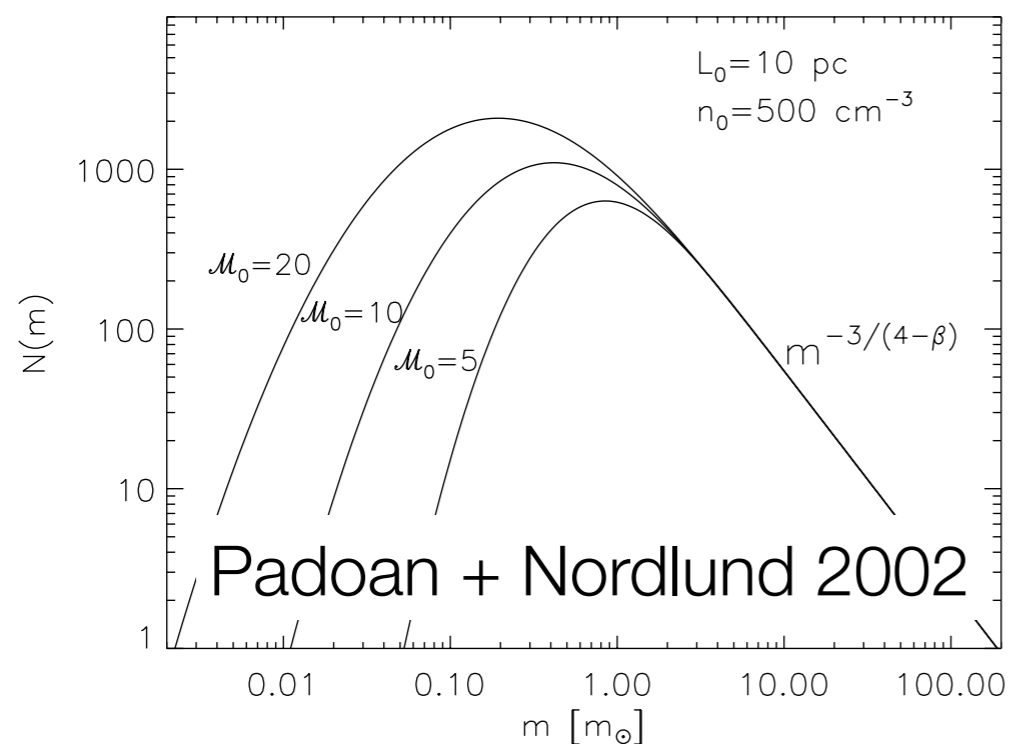
# Galactic Hypothesis v2: Turbulent Jeans Mass

- Conjecture: IMF peak occurs because collapse suppressed by thermal pressure below a critical mass  $\sim$  Jeans mass at median density (Padoan + Nordlund 2002; Hennebelle + Chabrier 2008, 2009; Hopkins 2012, 2013)

- Critical mass is

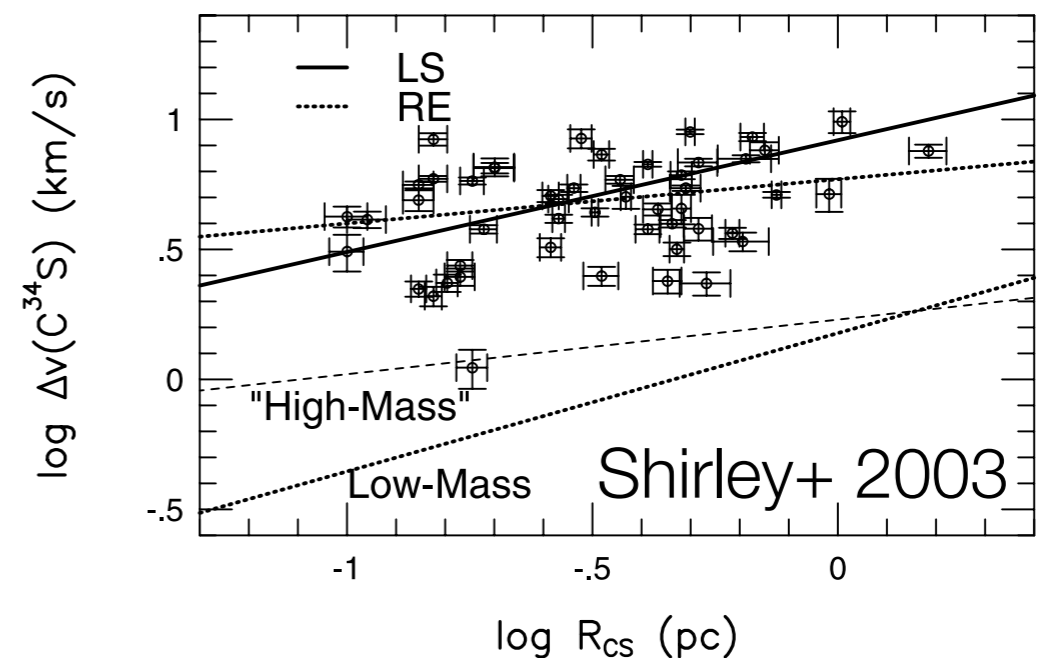
$$M_{\text{crit}} \approx \frac{M_J(\rho_0)}{\mathcal{M}} \approx \frac{c_s^2}{G\sigma_{\text{pc}}} \approx \frac{c_s^2}{G^2\Sigma}$$

LWS normalization  $\swarrow$   
 $\searrow$  GMC surface density



# Turbulent Jeans Mass Predictions and Problems

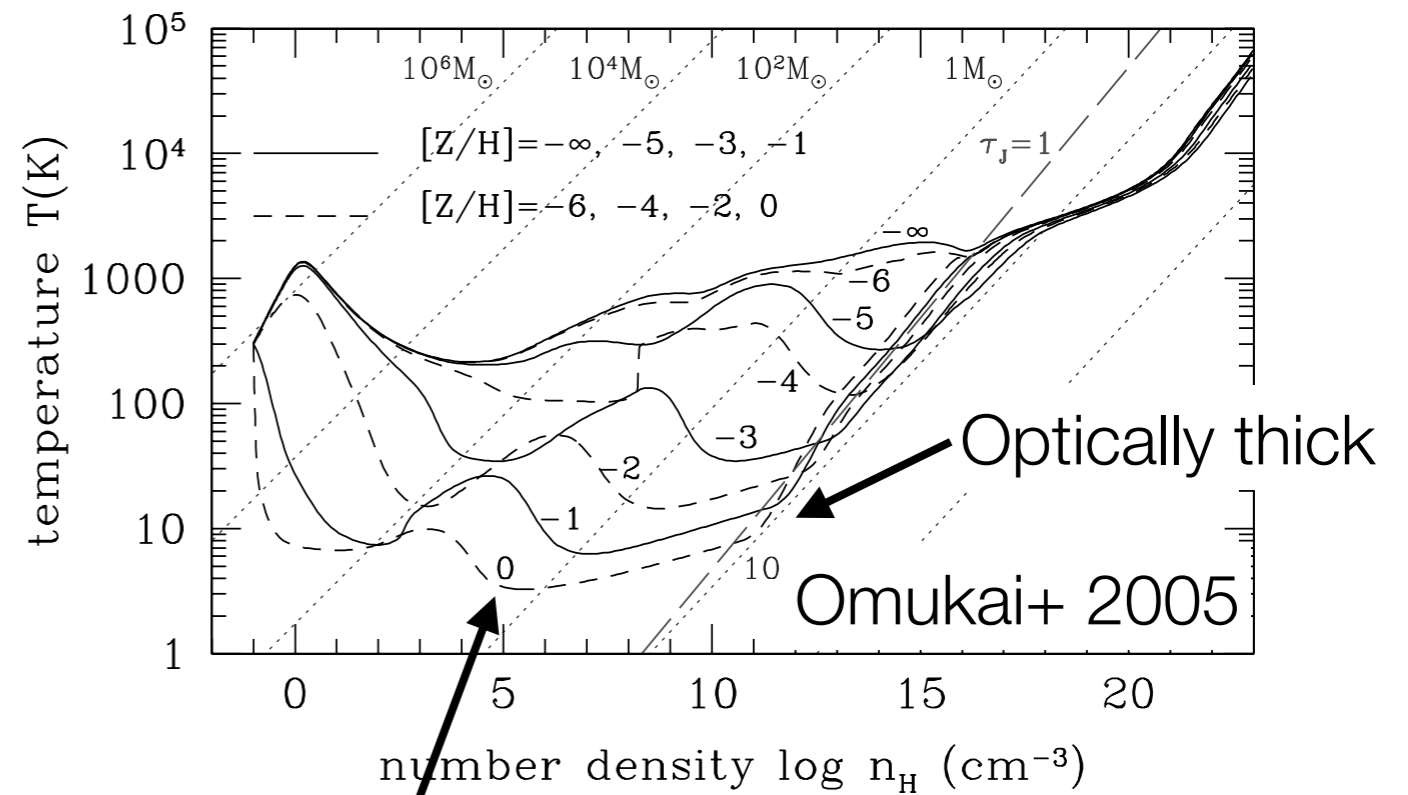
- Prediction: characteristic mass depends on temperature / linewidth-size normalization OR GMC surface density
- Predicts less variation than normal Jeans mass hypothesis due to cancellation: higher  $T \leftrightarrow$  higher  $\sigma_{\text{pc}}, \Sigma$
- Biggest variation likely in starbursts, but not yet calculated in detail; depends on  $T$  vs.  $\Sigma$
- May have problems in high-mass SF-regions:  $\sigma_{\text{pc}}$  higher by a factor of 10,  $T$  is not



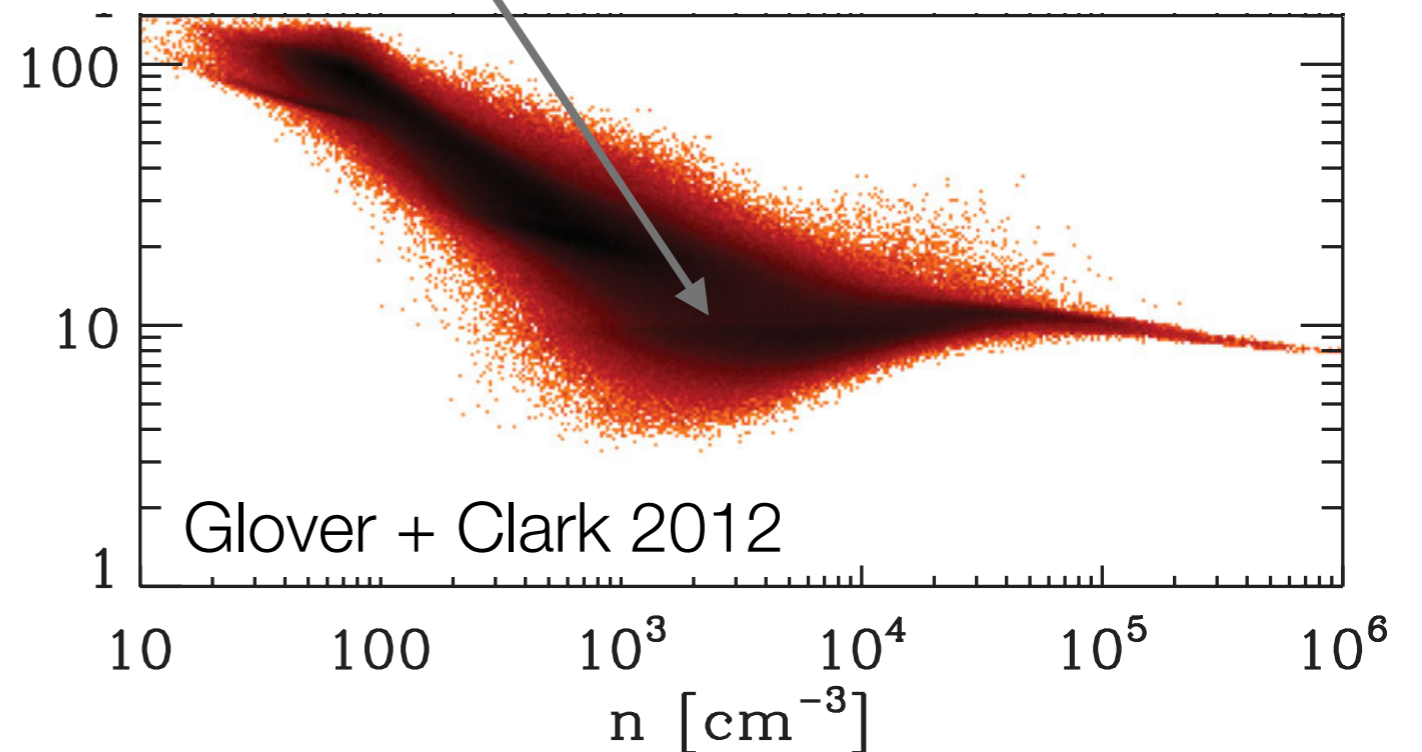


# The Non-Isothermal EOS Hypothesis

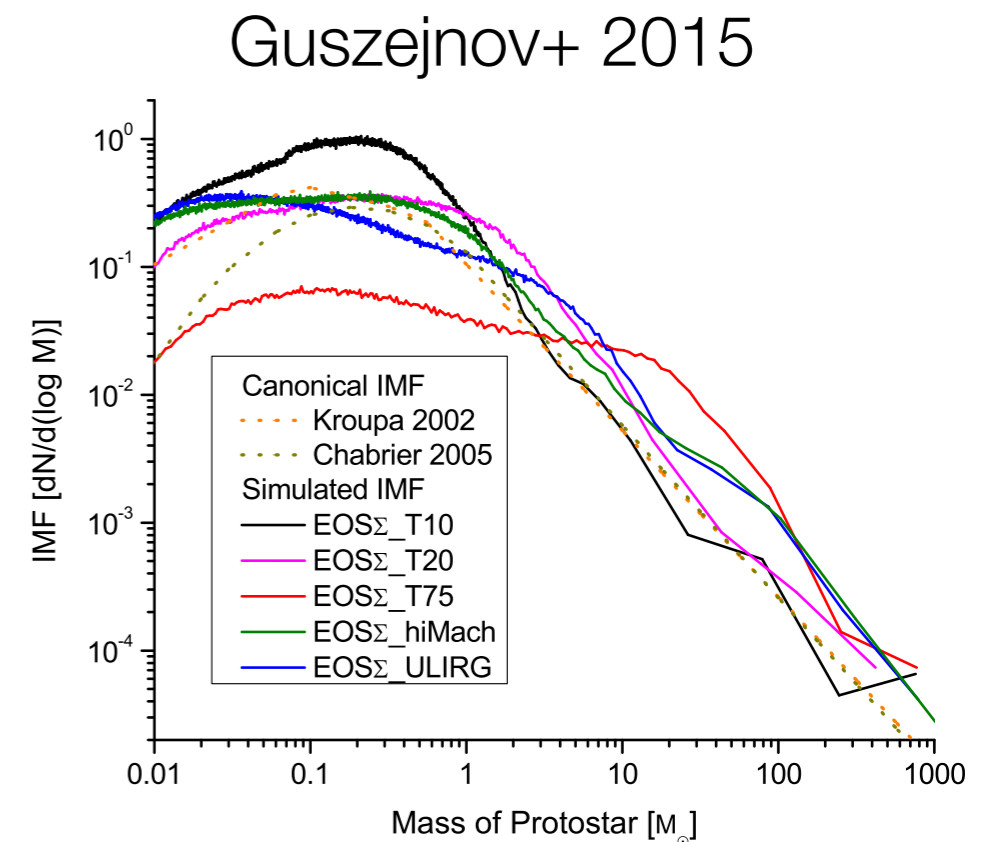
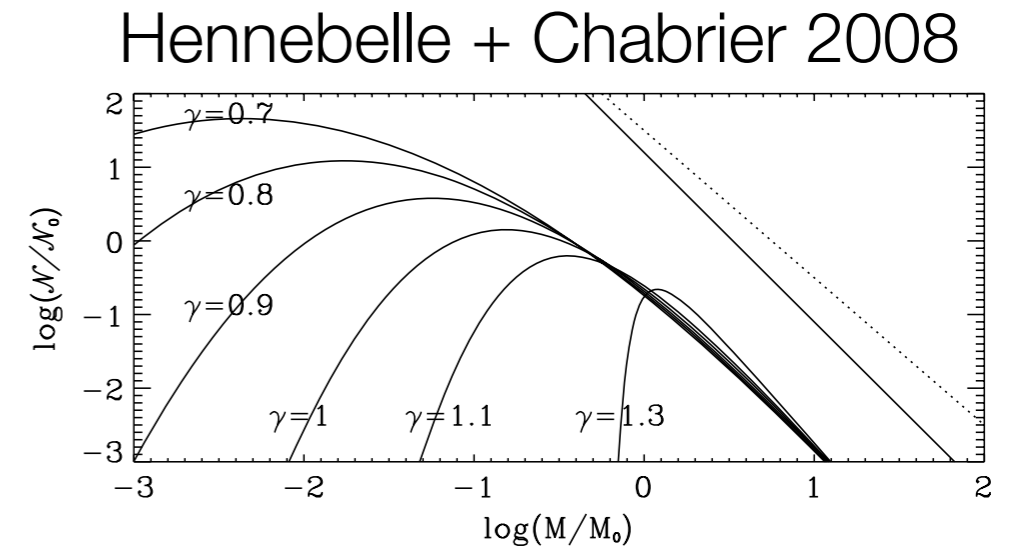
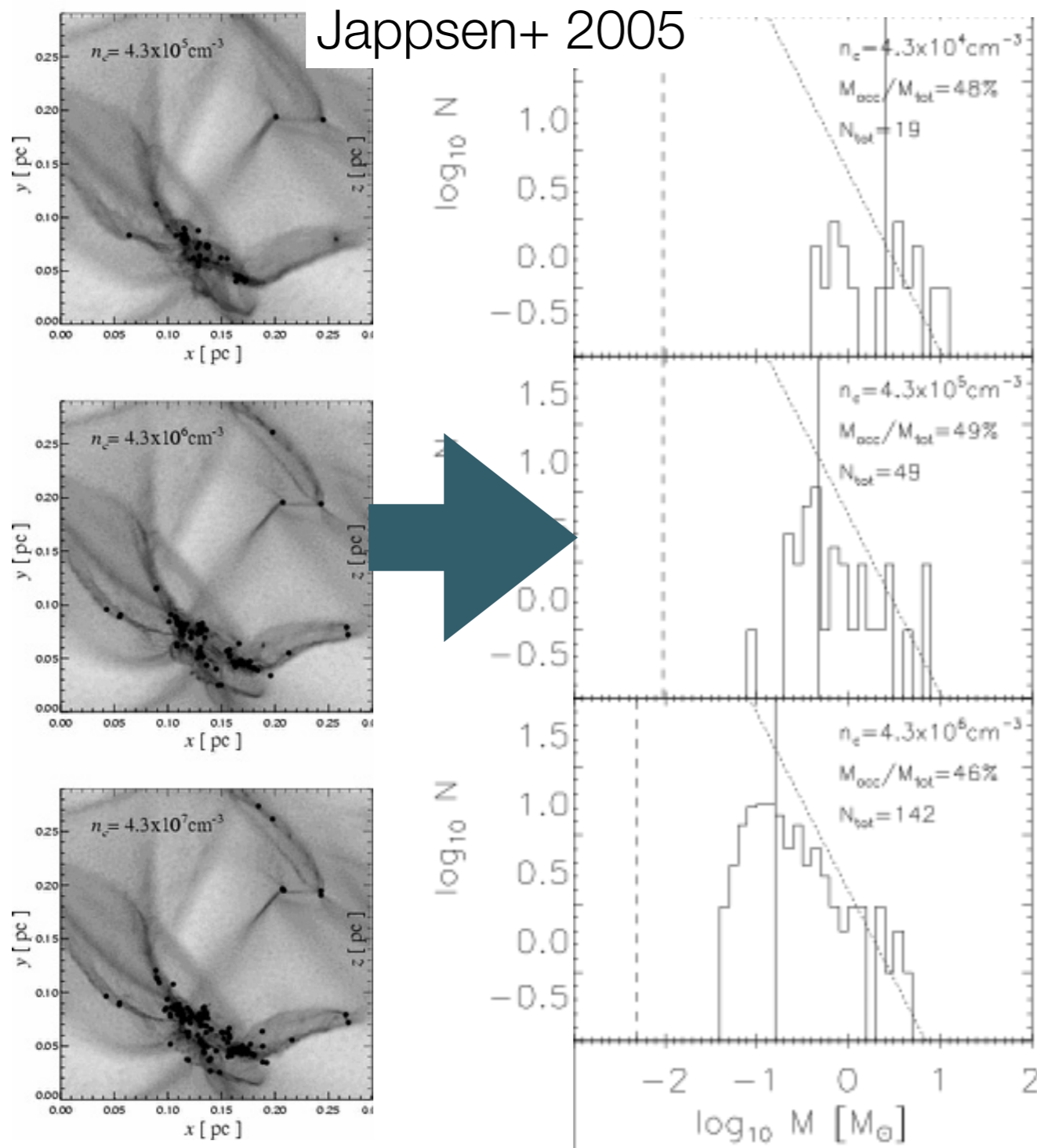
- Gas not perfectly isothermal:
  - Dust-gas coupling imperfect below  $\sim 10^5 \text{ pc}^{-3}$
  - Gas becomes optically thick at  $\sim 10^{10} \text{ pc}^{-3}$
- EOS has near-discontinuities in  $\gamma$  at these densities
- Conjecture: stellar mass scale set by  $M_J$  at such a discontinuity (Larson 2005; Omukai+ 2005; Bonnell+ 2006; Elmegreen+ 2008; Guszejnov & Hopkins 2015)



Dust-gas coupling

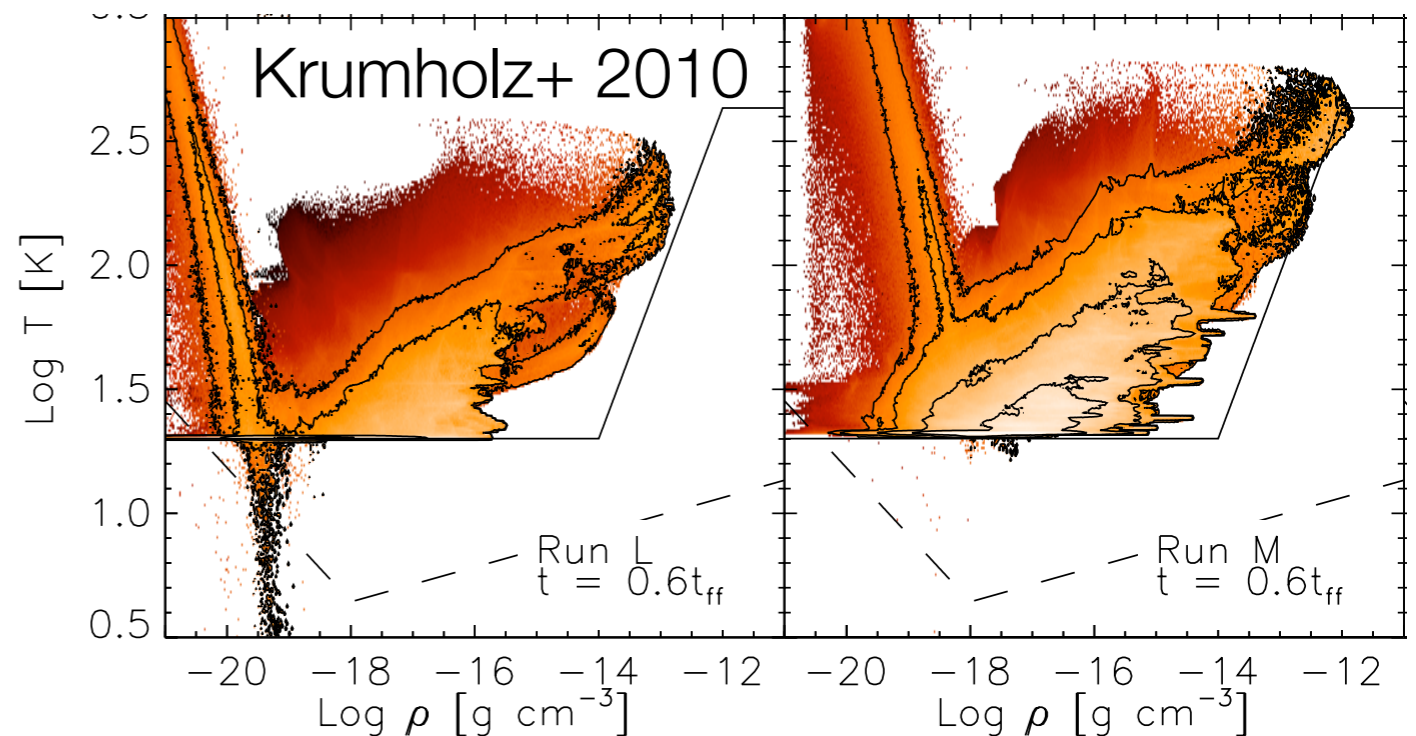
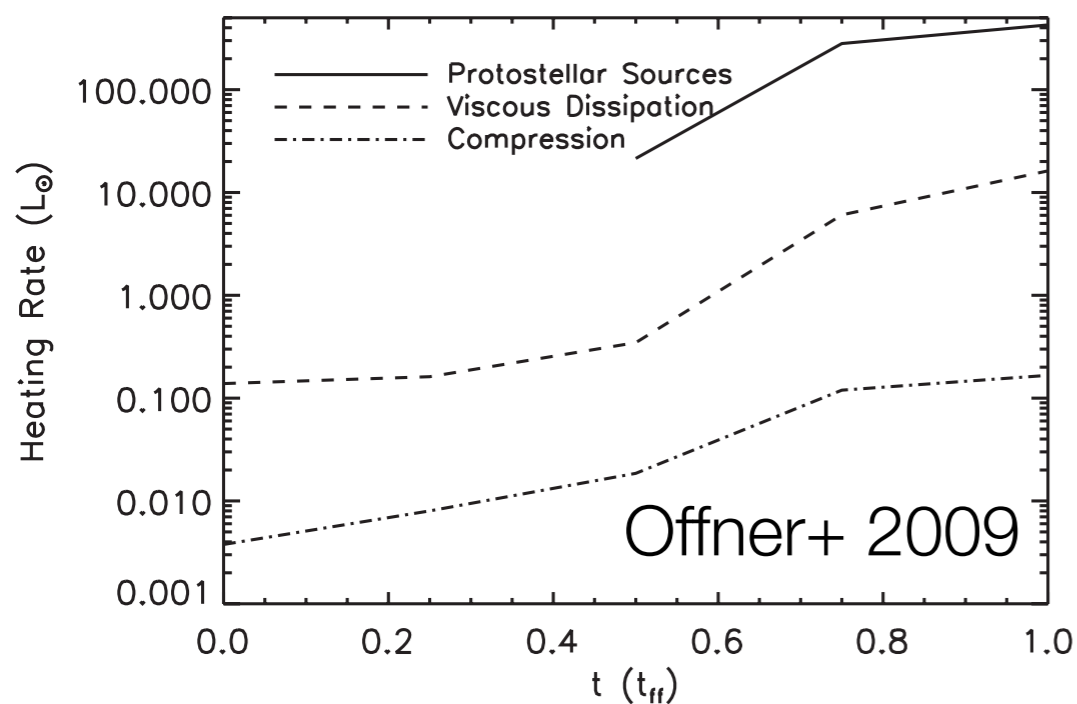


# Simulations and Models for the Non-Isothermal EOS Hypothesis



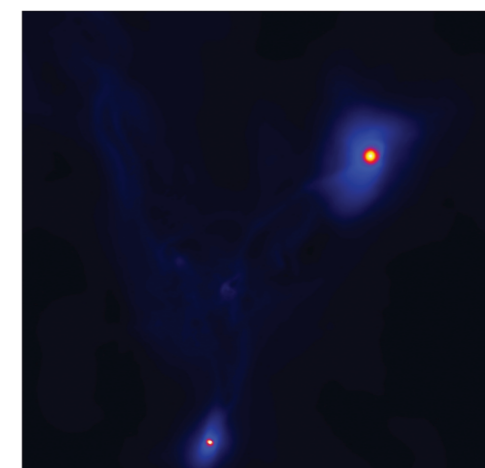
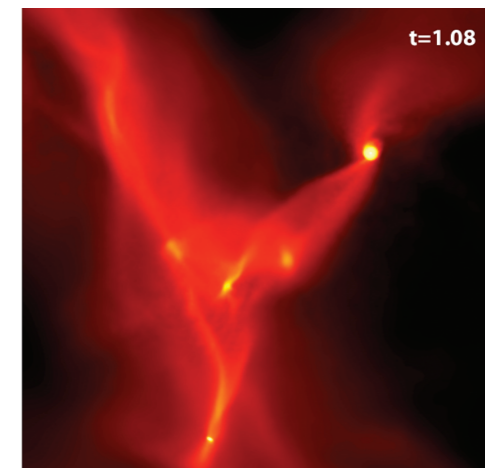
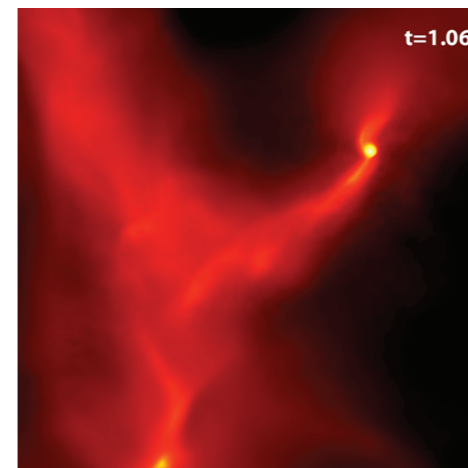
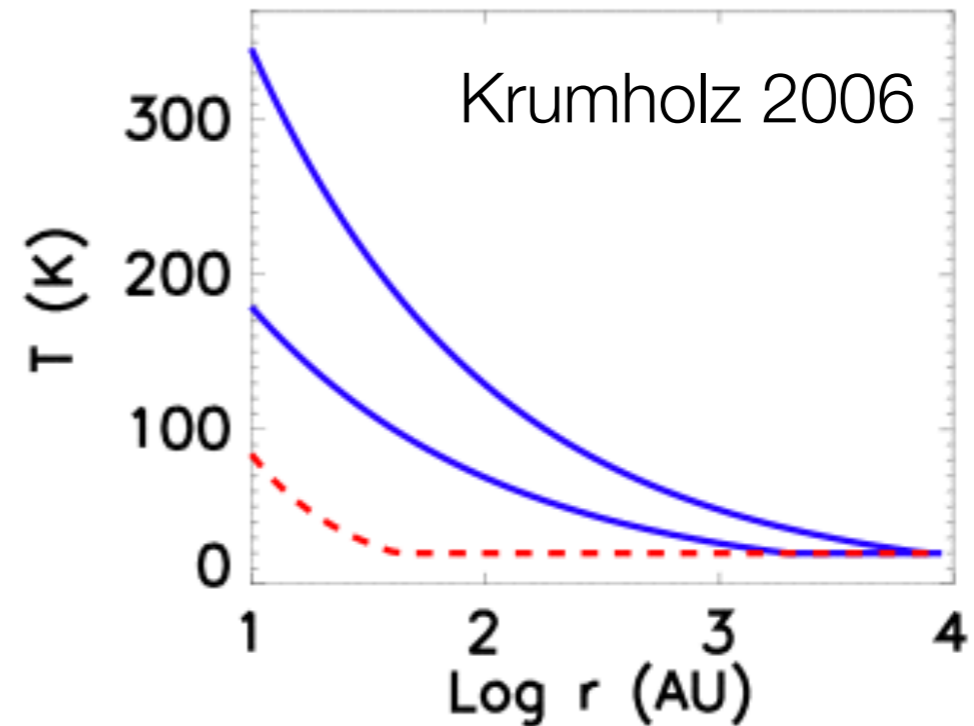
# Problems with the Non-Isothermal EOS Hypothesis

- IMF in BD regime exquisitely sensitive to assumed EOS
- Proposed EOS's not a good fit once stars turn on, since these dominate the energy budget
- Not possible to describe  $T$  vs.  $\rho$  with a single function once this happens



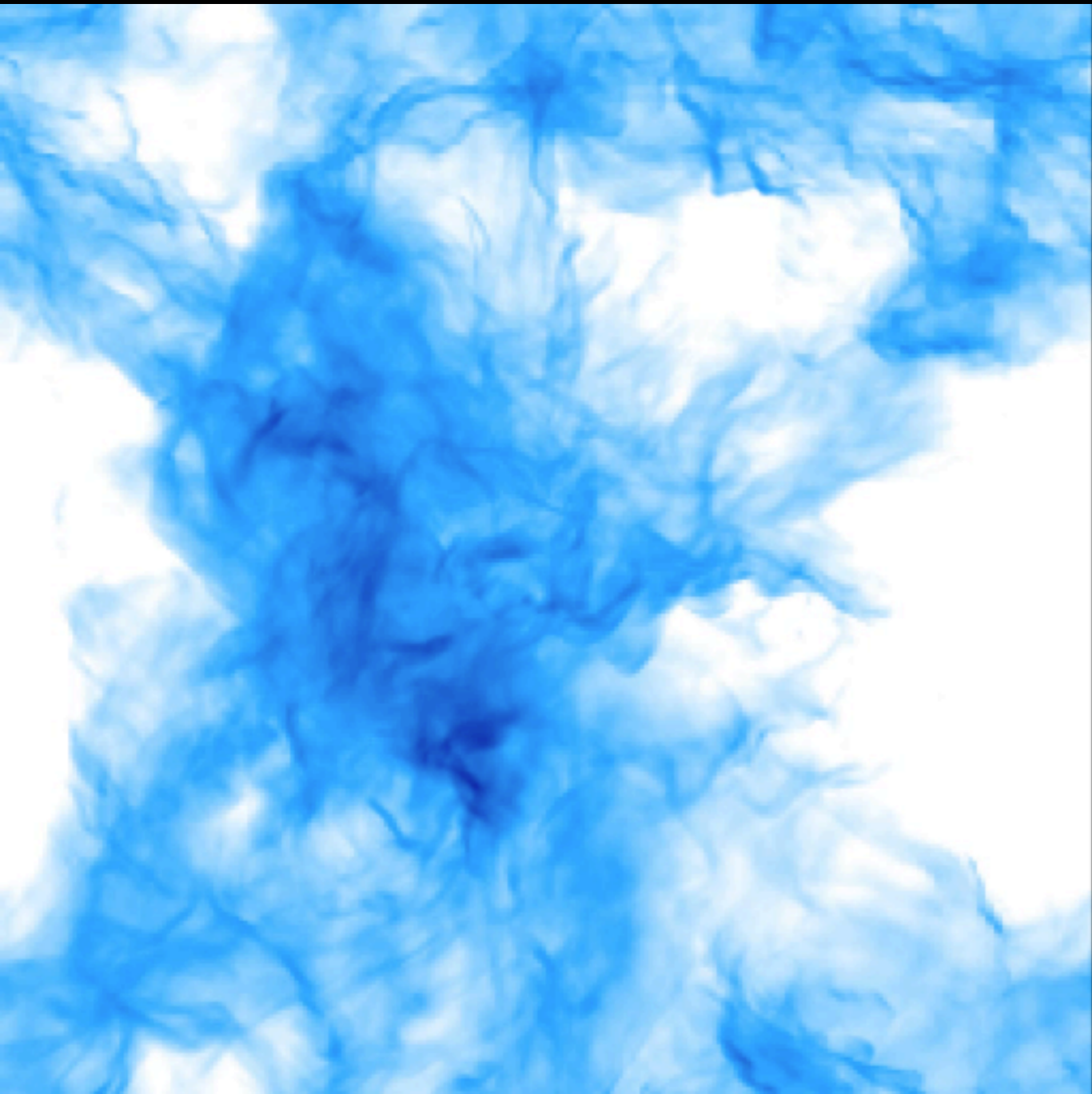
# The Radiation Hypothesis

- Stars heat up the gas around them via accretion luminosity
- Heating is immediate, as soon as a collapse object forms
- Heating raises Jeans mass, chokes off fragmentation in a region around each star
- Conjecture: mass of heated region determines characteristic mass of IMF (Krumholz 2006, 2011; Offner+ 2009; Bate 2009, 2014)



# Testing the Radiation Hypothesis

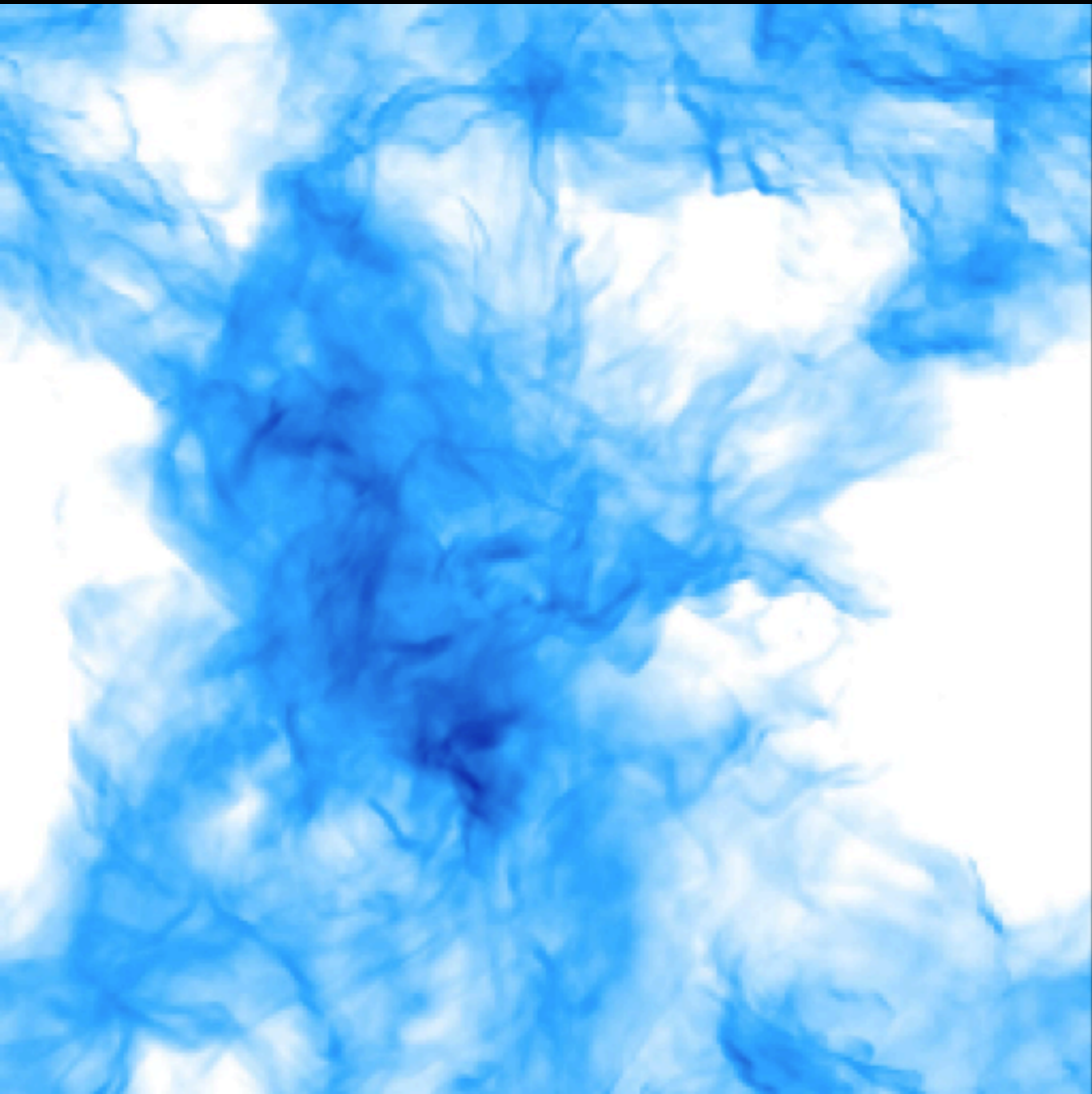
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Krumholz+ 2012

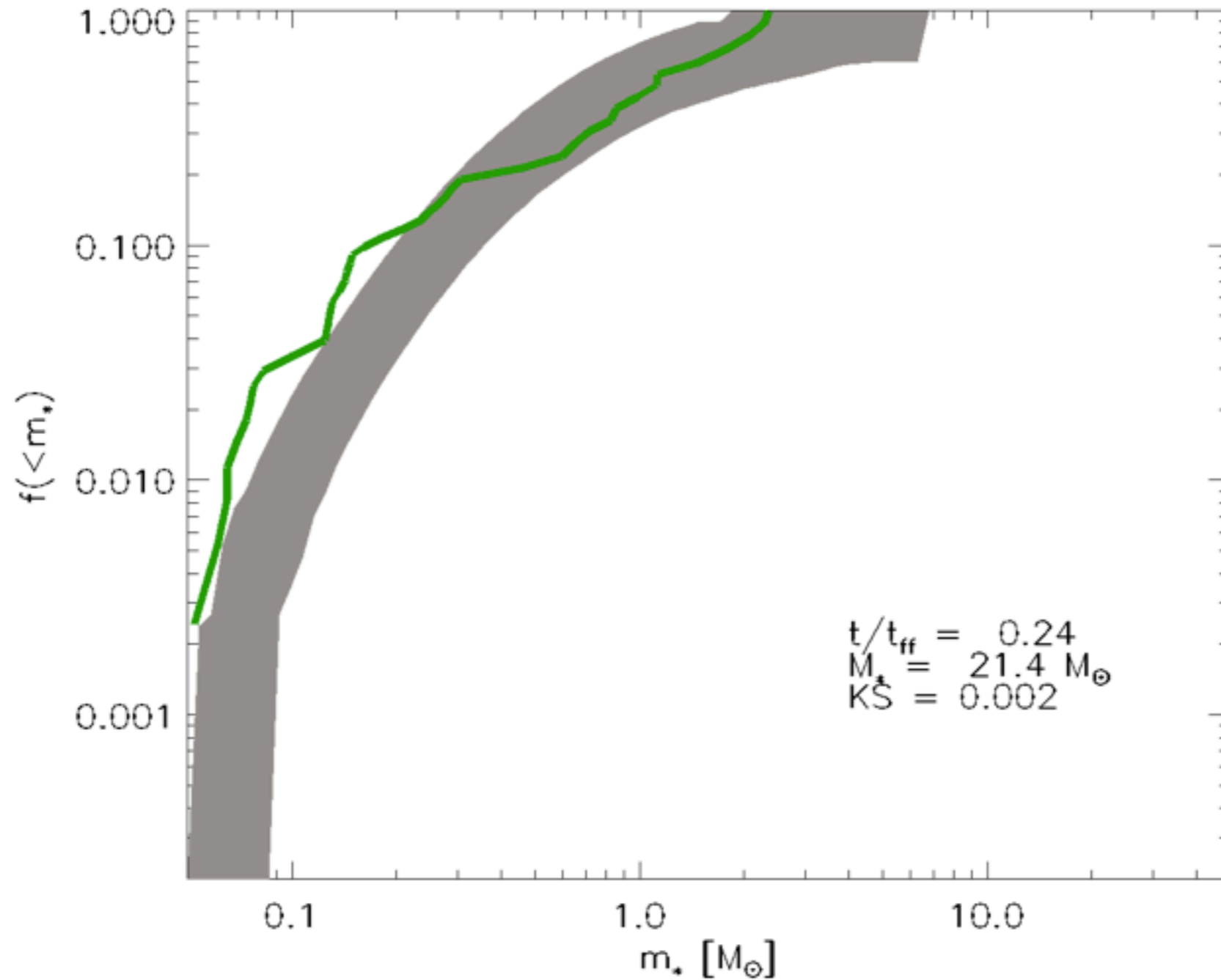
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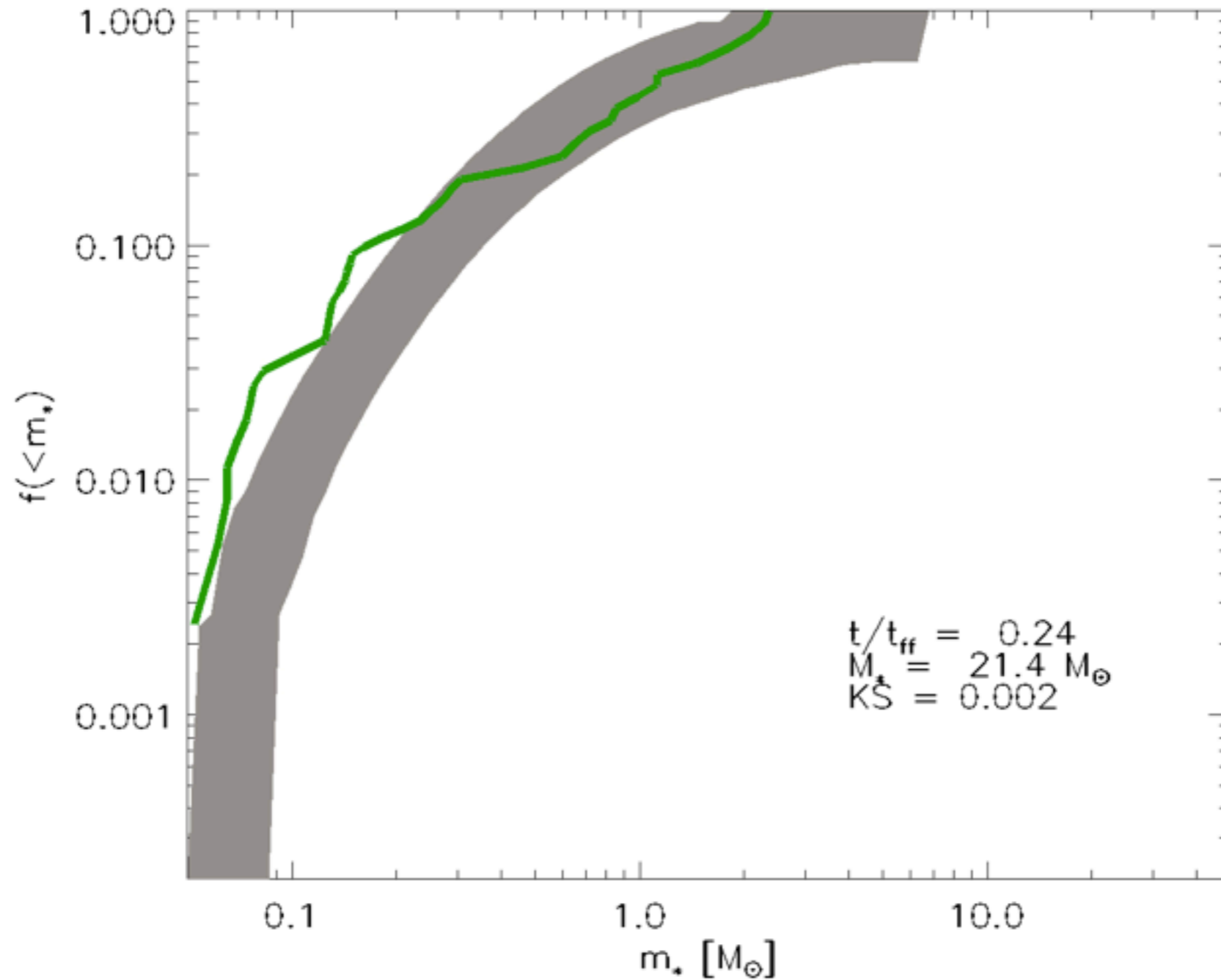
Krumholz+ 2012

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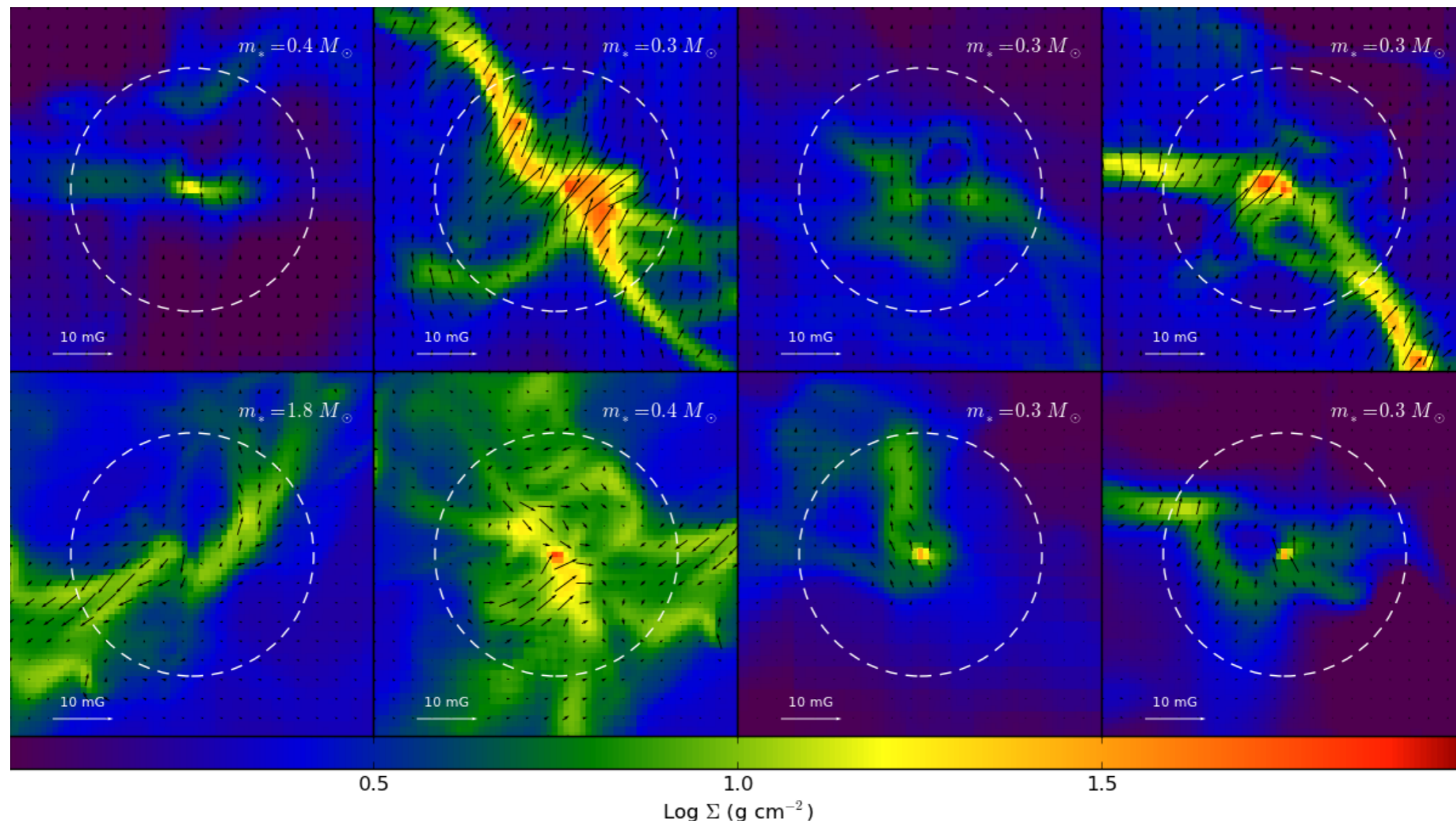


Krumholz+ 2012



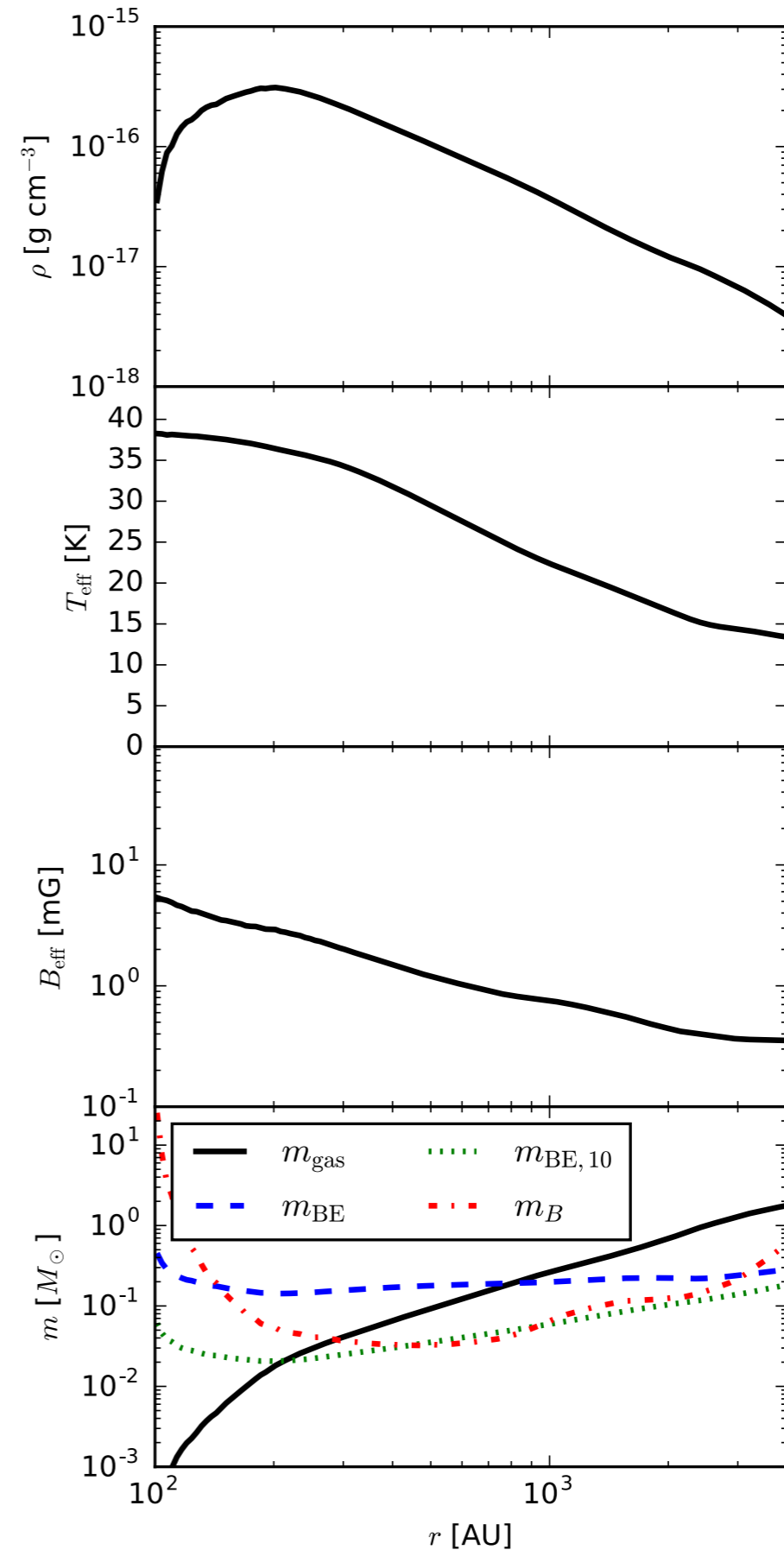
# How Does Radiation Work? A Detailed View

- Examine all stars formed in radiation-MHD simulations so we can compare radiative and magnetic effects (Myers+ 2014, Cunningham+ 2016)



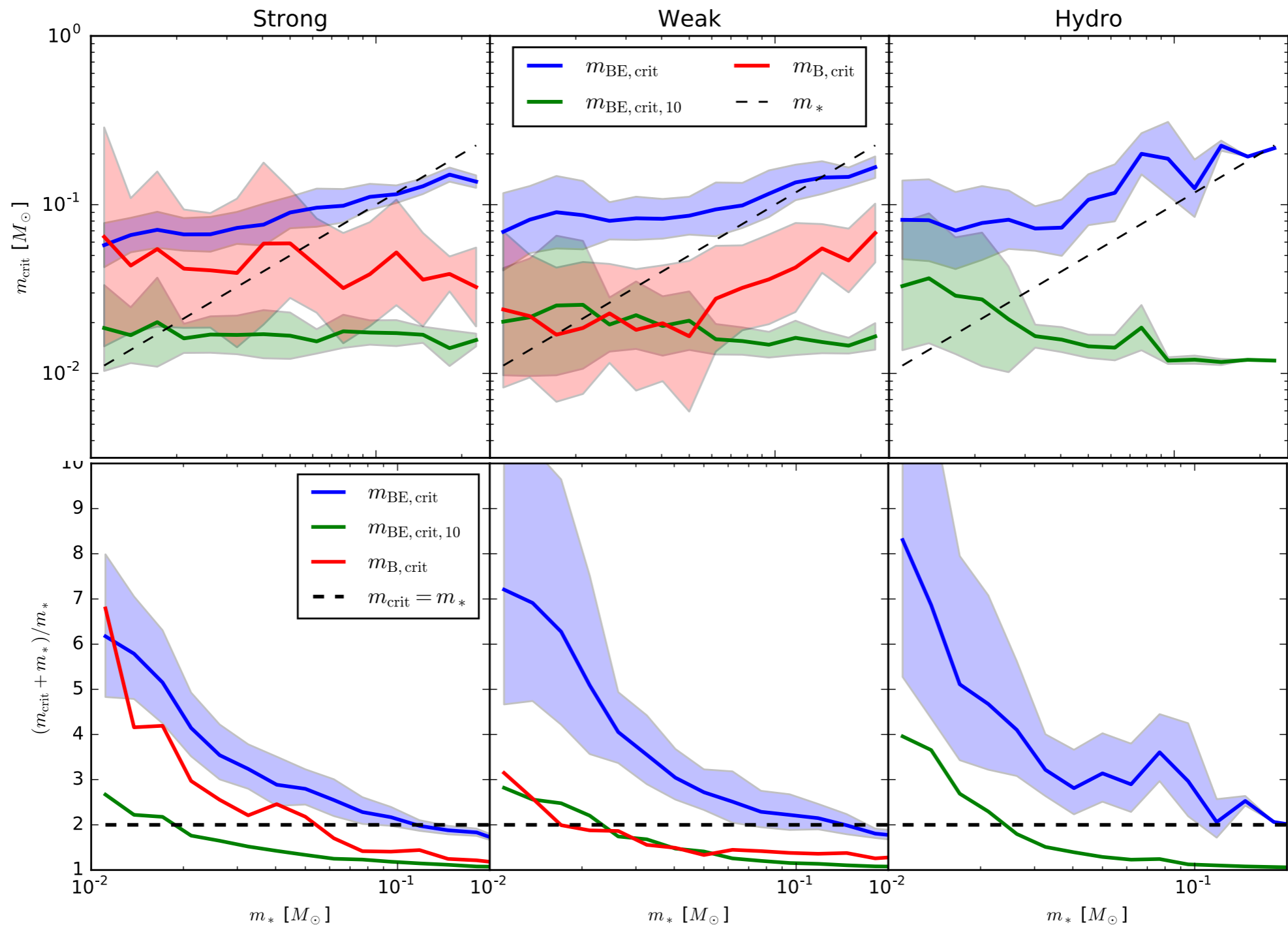
# Dissecting Radiation Feedback

- Examine concentric shells around each star at each time
- Compare gas mass  $m_{\text{gas}}$  to:
  - $m_{\text{BE}}$  — thermal pressure support
  - $m_{\text{BE},10}$  — thermal pressure support we would have had without radiation feedback
  - $m_{\text{B}}$  — magnetic support
- Mass of stabilized region set by  $m_{\text{gas}} = \max(m_{\text{BE}}, m_{\text{B}})$

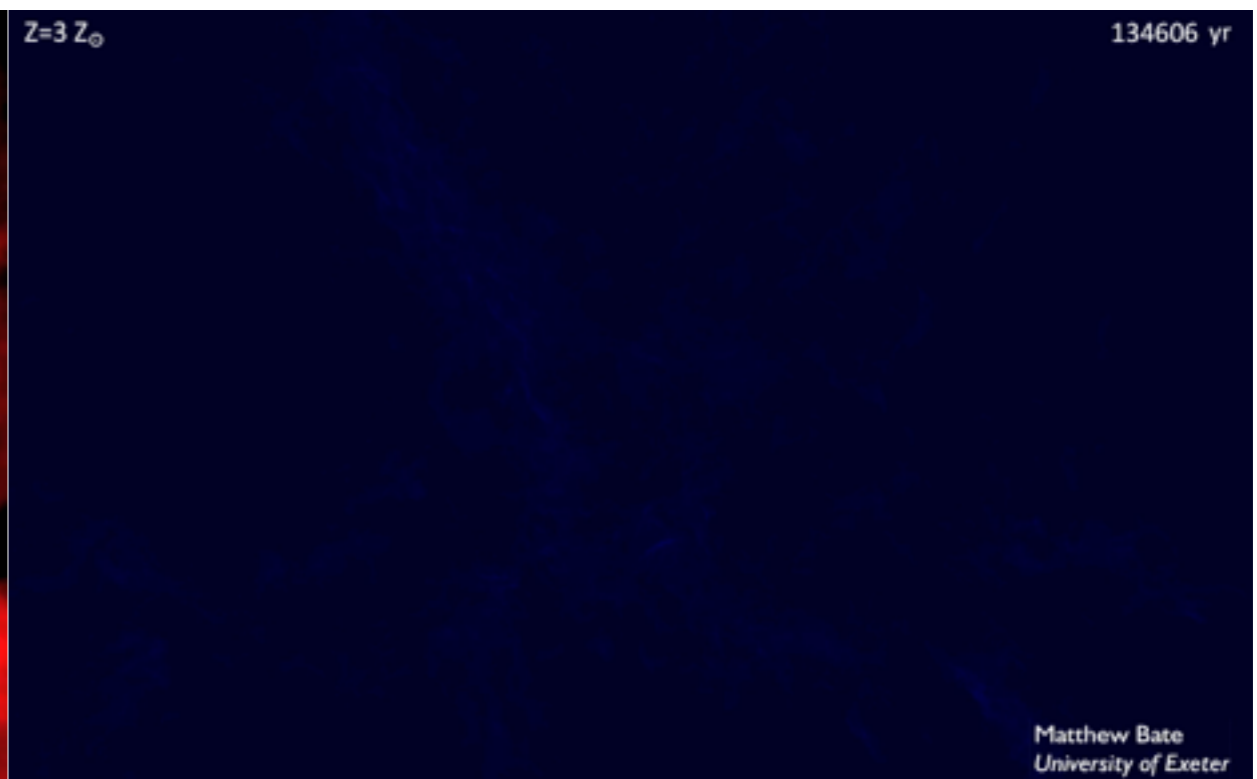
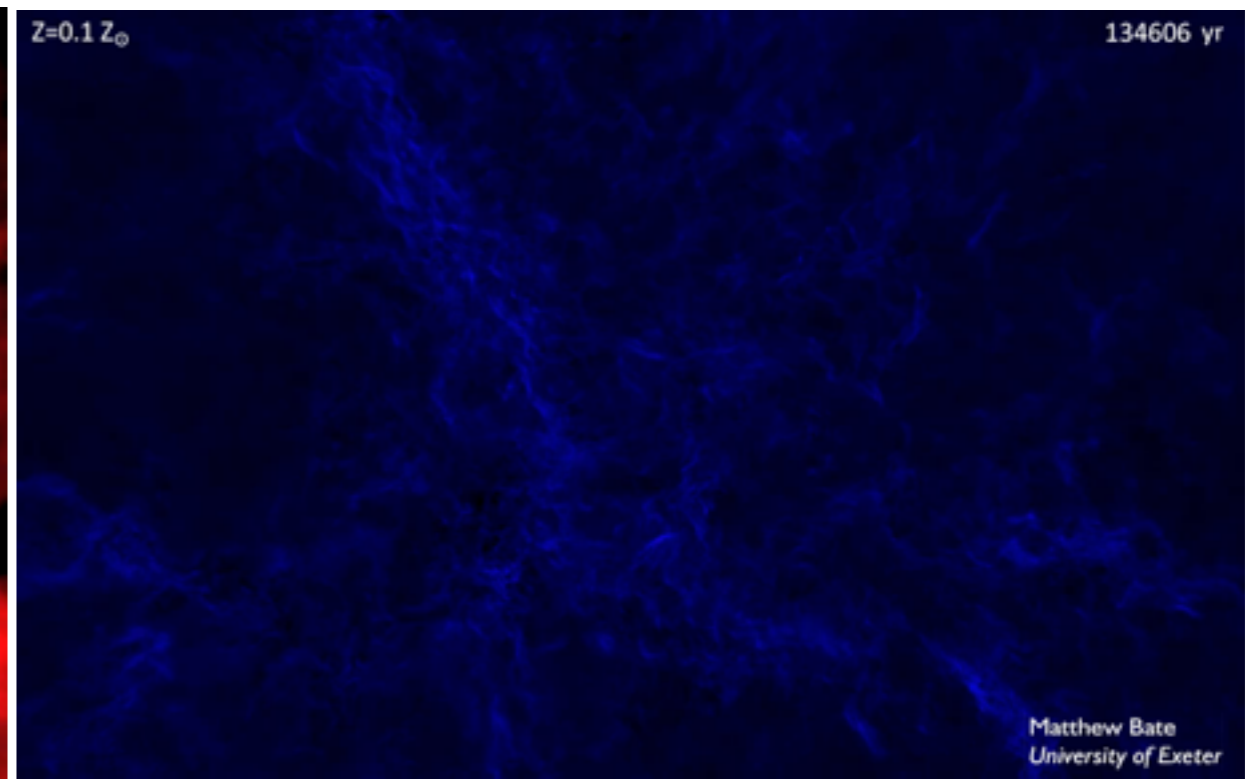


Krumholz+ 2016

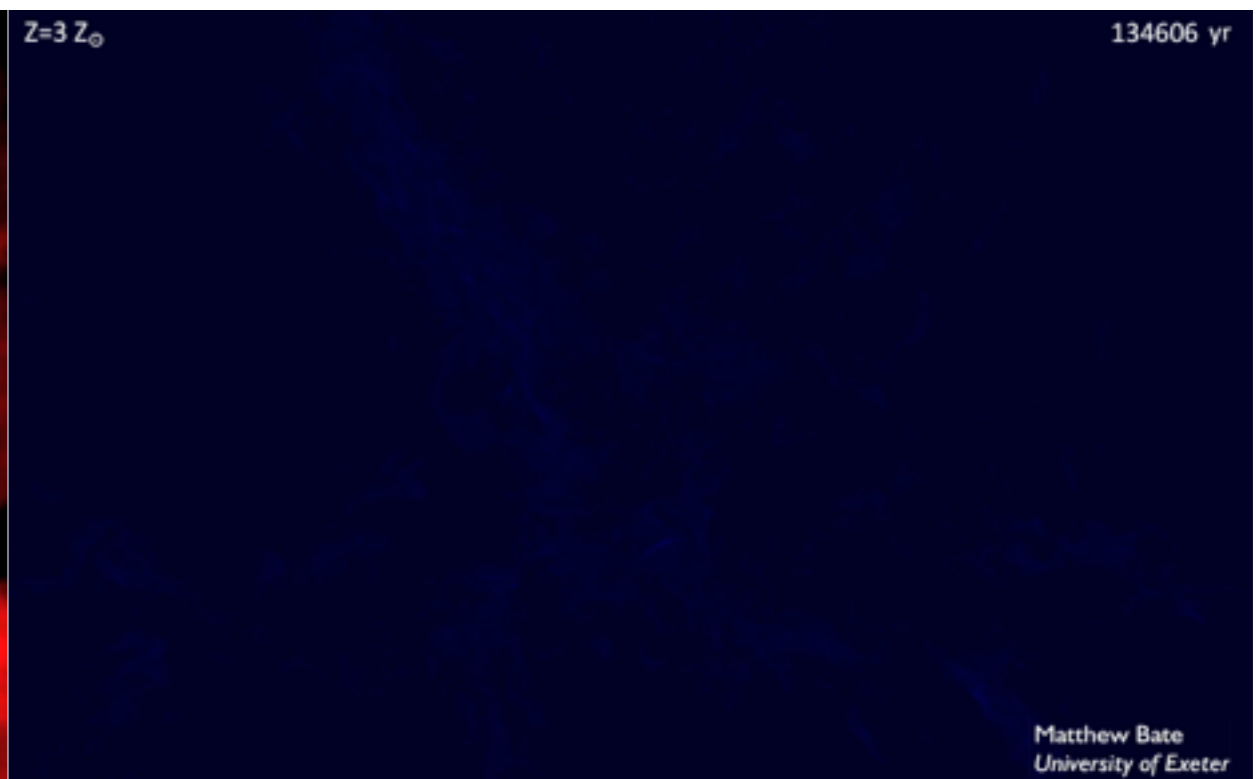
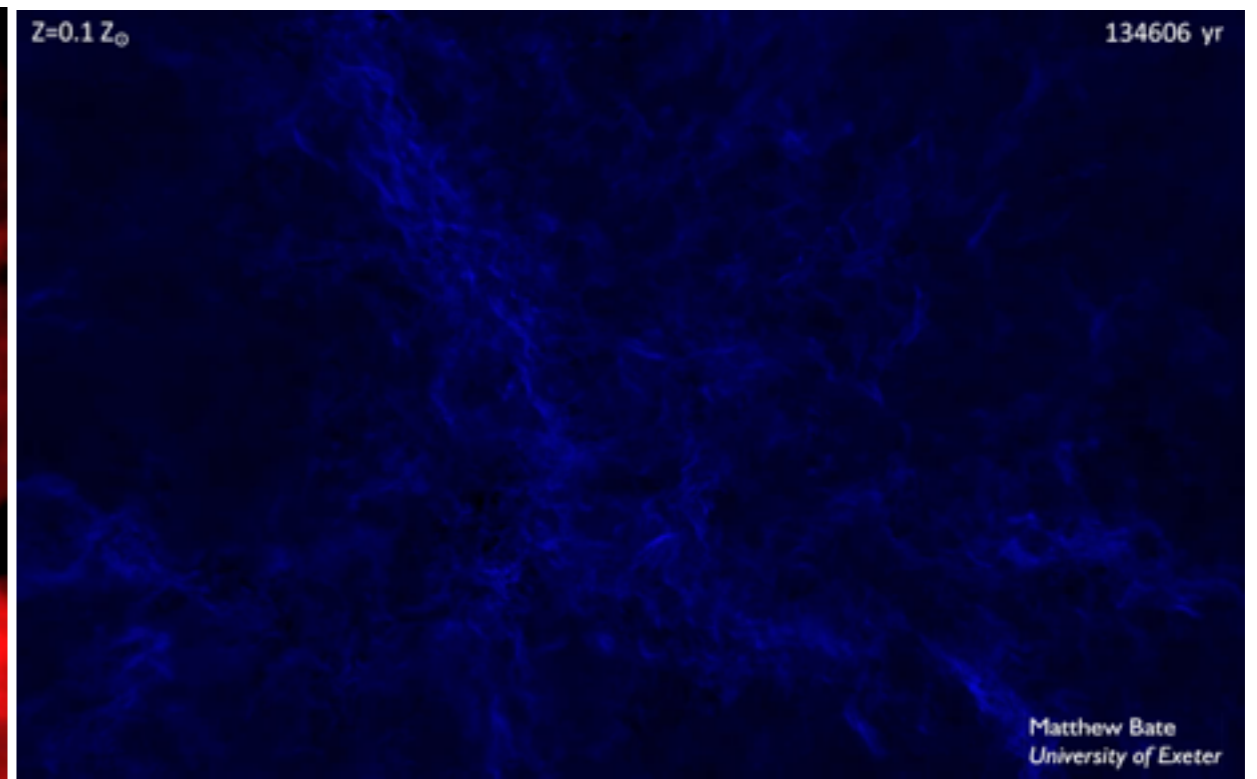
# Gas Stabilization by Radiative Feedback



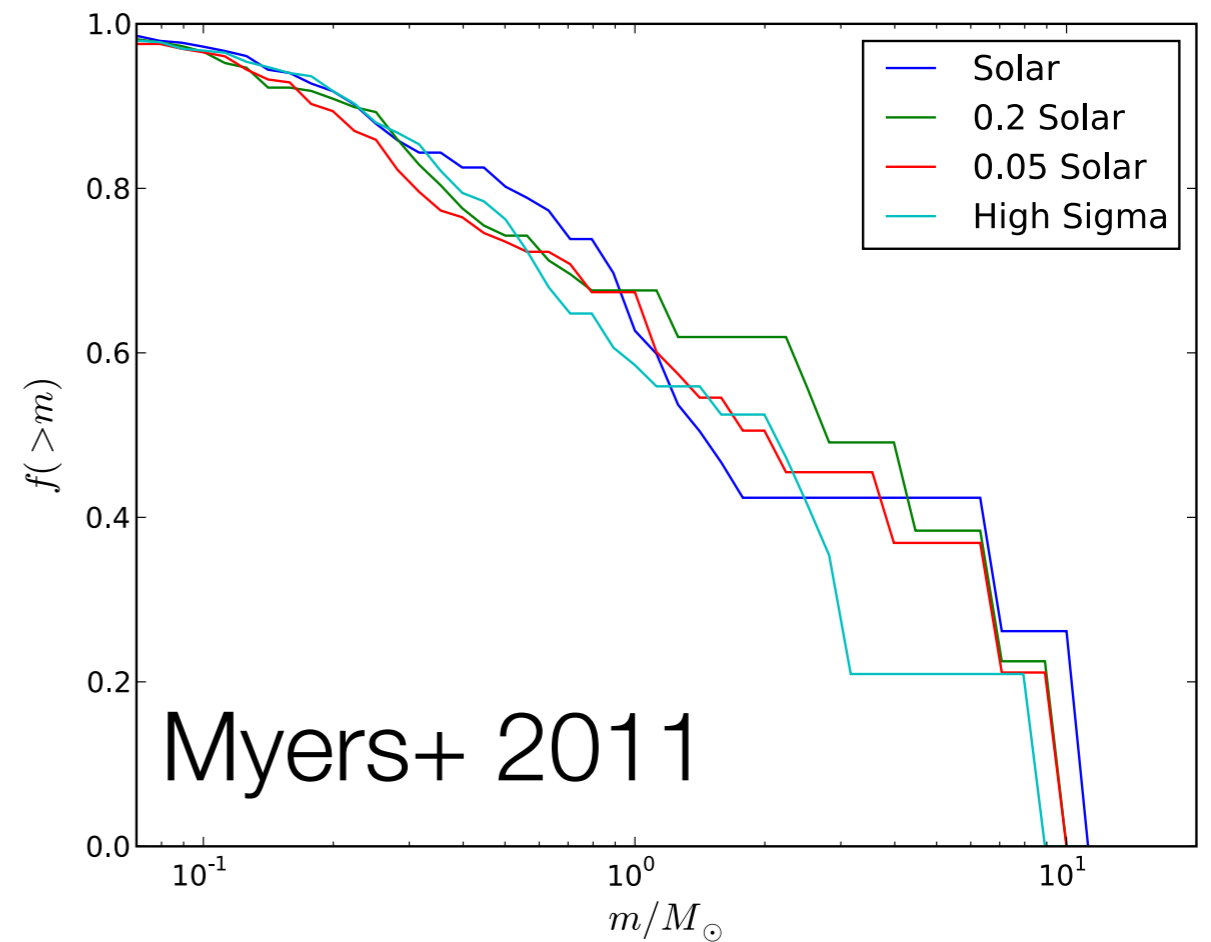
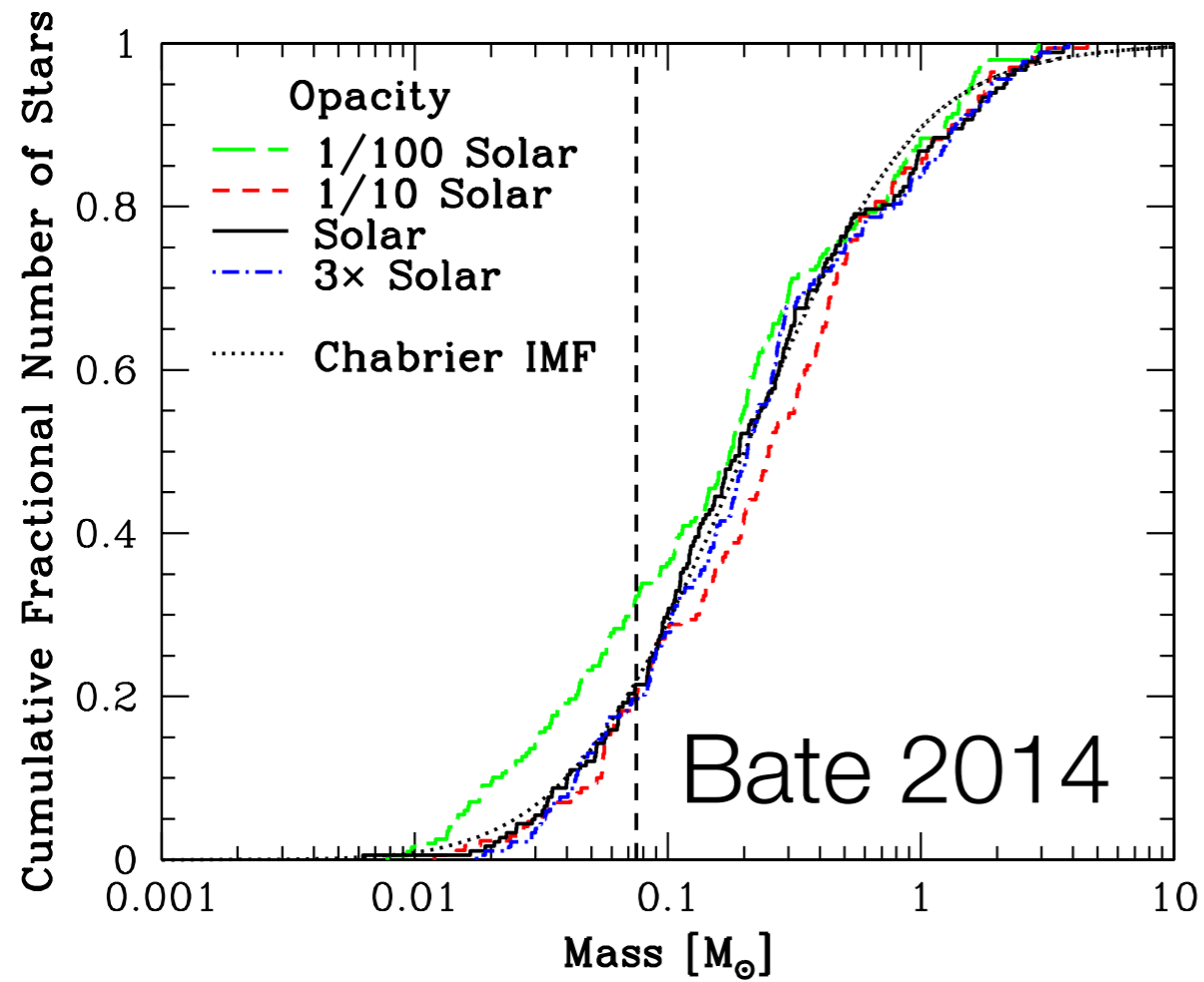
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# Extending the Radiation Hypothesis

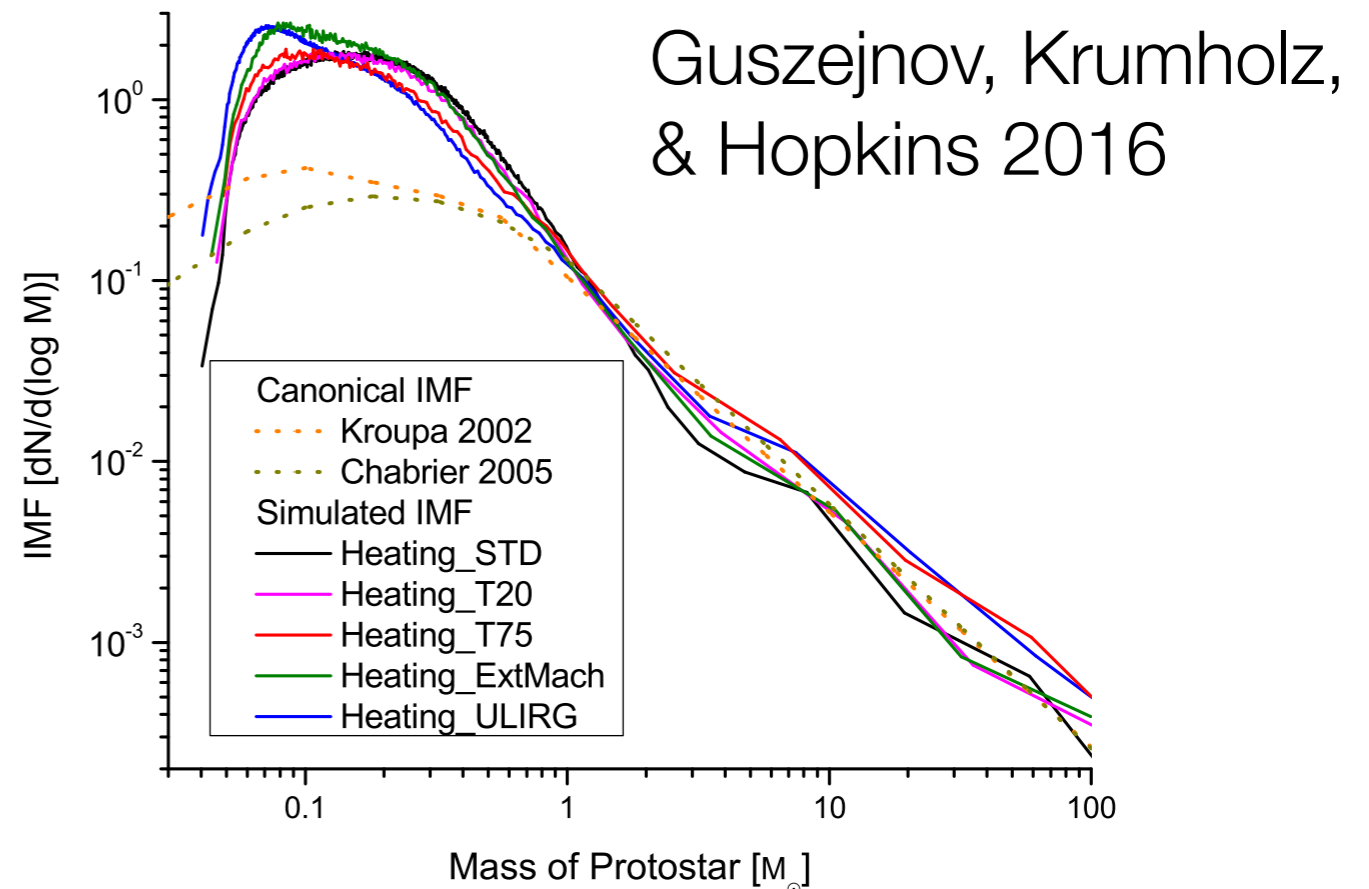
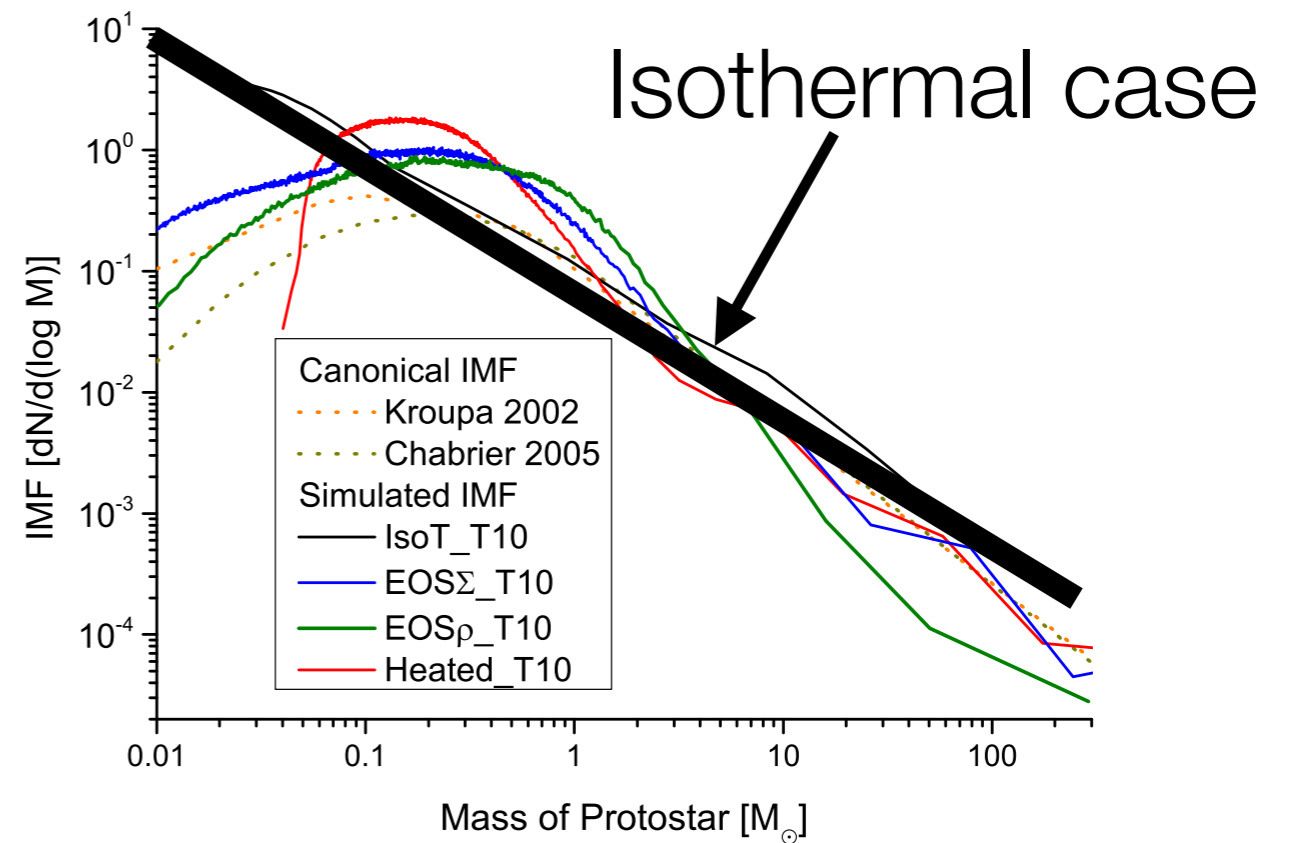
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- Accretion luminosity set by surface escape speed, which in turn is set by  $T_{\text{core}}$ , which D burning fixes to  $\sim 10^6$  K
- Escape speed can therefore be written approximately in terms of fundamental constants
- Analytically solve for size of heated region and characteristic mass, with almost no dependence in interstellar parameters (Krumholz 2011):

$$M_* \approx 0.15 \left( \frac{P/k_B}{10^6 \text{ K cm}^{-3}} \right)^{-1/18} M_\odot$$

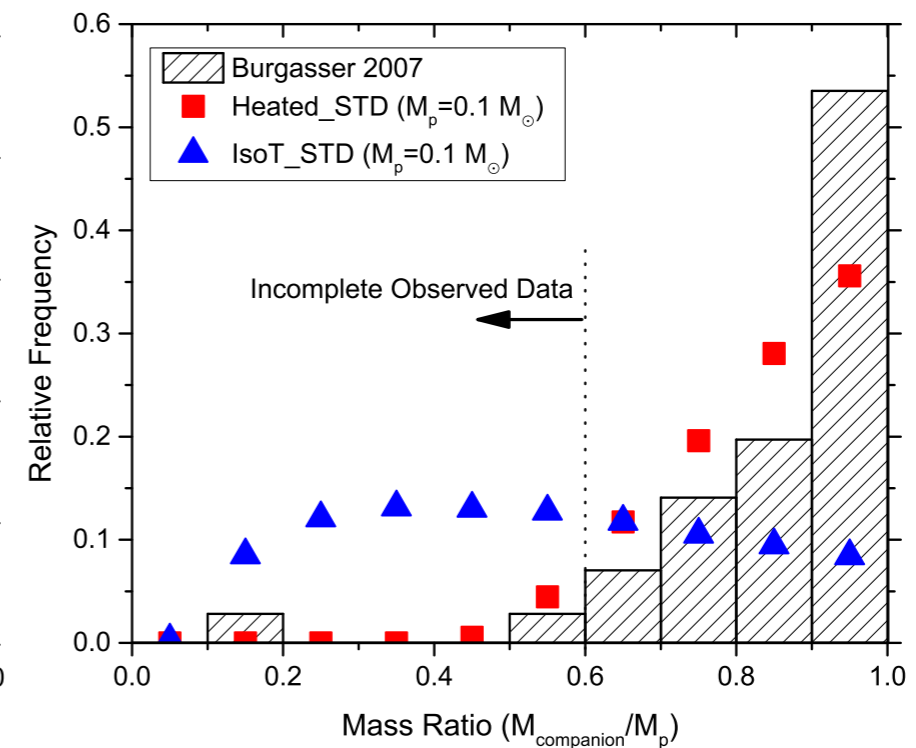
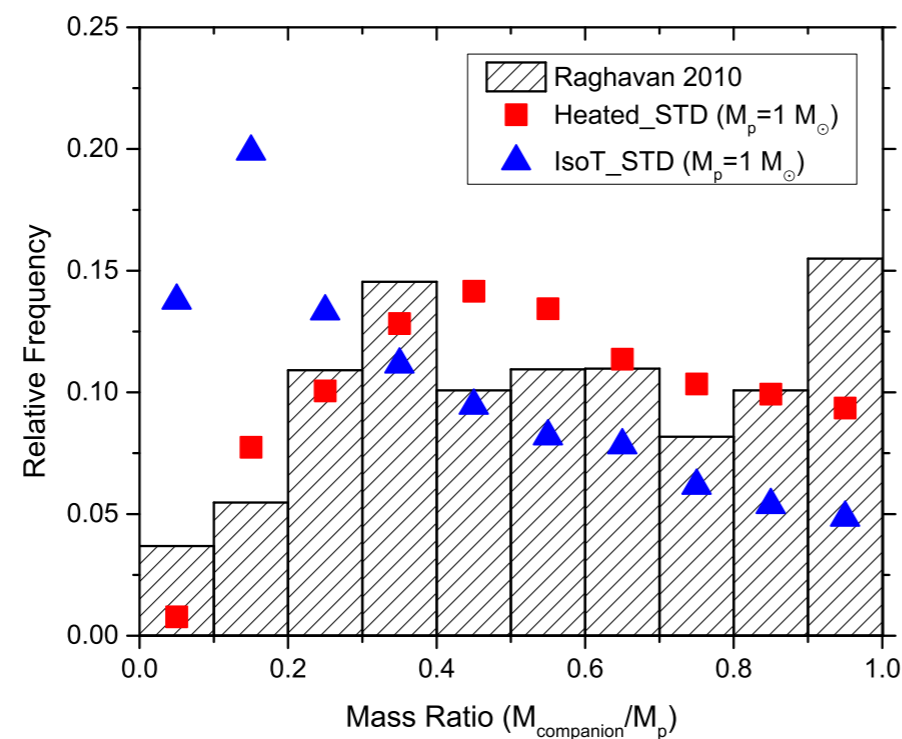
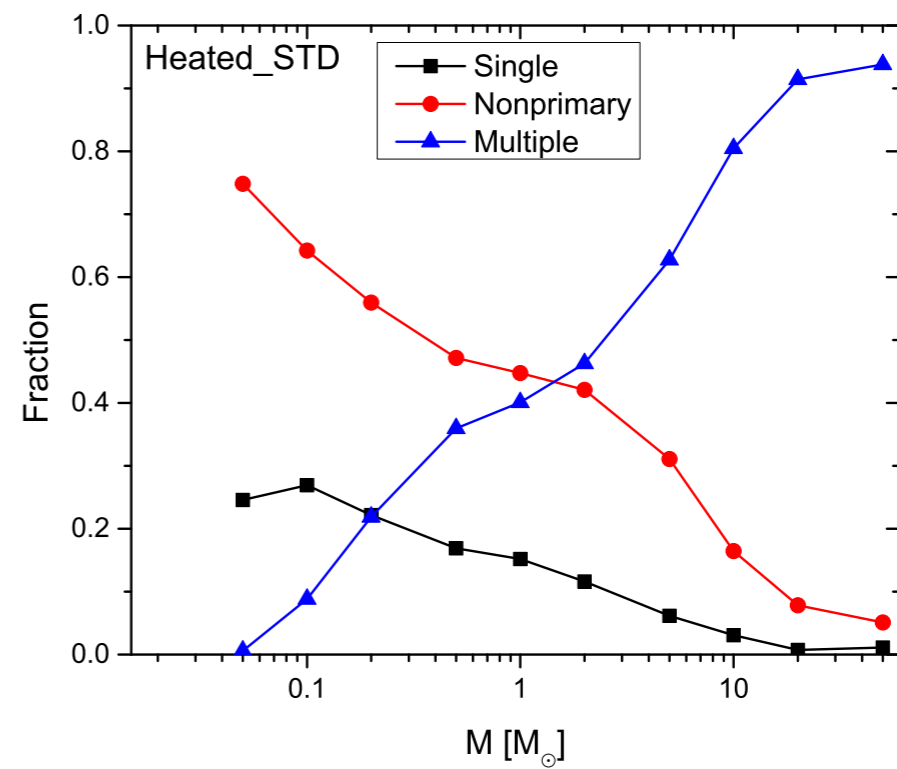
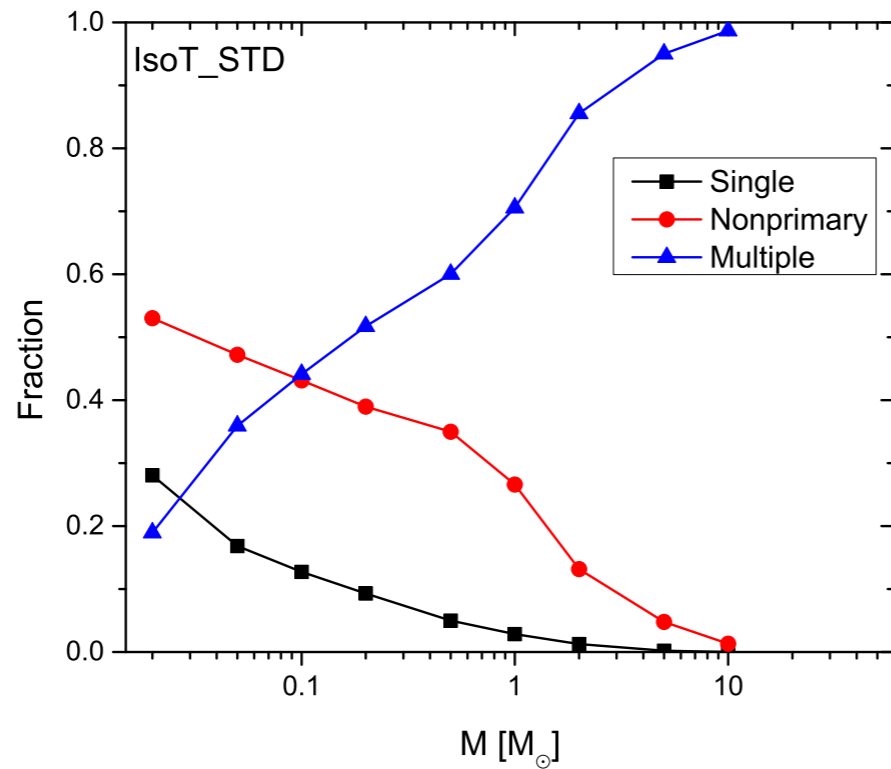
# Radiation In a (Semi-)Analytic Model

- Use excursion set-like model based on Hopkins+ fragmentation tree
- Add local radiative heating: in any collapsing region, use temperature computed from Krumholz+ 2011 formalism
- Vary environment:
  - Background  $T = 10, 20, 75$  K
  - Mach number = 6 - 30
  - $\Sigma = 10 - 3000 M_{\odot} \text{ pc}^{-2}$
- Compare to isothermal, EOS not including radiation





# Semi-Analytic Model Also Gets Binaries Right



# Implications and Possible Problems for the Radiation Hypothesis

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- Suggests (very slightly) bottom-heavy IMF in the highest pressure star-forming environments
- Not clear yet what sets the shape of the IMF below the feedback break
- Probably need to extend models to include disk fragmentation — not currently captured, appear to have too few brown dwarfs in analytic model as compared to simulations

# Summary

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- Non-powerlaw part of the IMF must be controlled by deviations from isothermal behavior
- Two possibilities:
  - Important deviations are at galactic scale; apparent lack of IMF variation is due to convenient cancellation
  - Important deviations are at  $\ll 1$  pc scale, due to stellar feedback or dust-gas coupling; predicts at most weak IMF variation in very high pressure / density regions