### A new kind of science?

Ilya Nemenman

KITP, UCSB

Ilya Nemenman, KITP Colloquium, March 12, 2003

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- To see if *traditional* science can help with the new one. (It probably can.)
- To see implications of new science to traditional one (thus to ours, as scientists, well-being). (Probably very few: New science is not predictive).

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- Analyze social, ownership, and scientific conduct issues connected to some results.
- Analyze other people reviews and opinions.

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Chapter 10-12 The concept of computation.(Philosophical, but little scientific value.)







Looks random, at least partially



Evolves to a simple fixed point.



#### Moves points to the right.

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Superposition of nested structures. Randomness with structure.



#### Semi-random behavior.



Intricate behavior - interacting structures.

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## **Other simple programs**

- 2-d, 3-d cellular automata (cf. *Game Of Life*)
- Multicolor, long range or memory cellular automata
- Mobile automata and Turing machines
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- Numbers for generating structure, randomness, or complexity
  - arithmetic operations in different bases (remember linear congruential random number generators)
  - ★ recursive sequences, continued fractions (roots, etc.), networks
  - $\star$  primes and important constants (e is nested,  $\pi$  is not)
  - ⋆ iterated maps and chaos

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# **Observations**

- Different types of behavior are possible, from very simple to very complex, or to very random (But what is *complex* or *random*?)
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- For constrained systems (time reversal, symmetry, etc.) more complex rules are needed
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- Nothing interesting happens for finite systems and in 0+1 dimensional systems (Smells like stat. mech.)
- Not a single example of continuous system shown (continuous CA are <u>not</u> good)

• Exhaustive search and computer simulations

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With its strong emphasis on simple laws and measurements of numbers, physics has normally tended to define itself to avoid complexity.

 Should focus on discrete simple systems and on evolution, rather than constraints.

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- Computer simulations needed for finding positions of gas molecules in the room, but these features are not predictive, and we do not study them because it *does not make sense* (though see below)
- Nothing is simpler than a harmonic oscillator, but a lot of them make QFT (and us). (The analogy with QFT can possibly be made more precise – ordered, random, critical phases. Governed by strength of couplings, and thus by predictability and information transmission.)

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## **Problems**

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 One must talk about ensembles of possible initial conditions – complexity is a function of the rule and a typical set of initial conditions. Example: usually random CA30 may behave like:



### **Possible solution**

There exists complexity classification scheme (Bialek, Nemenman, Tishby, 2001) based on predictability – mutual information between past and future.

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- Entropies show distinction in extensive part (just a multiplies), and also in subextensive one (qualitative – zero vs. growing function)
- Predicting future is impossible in CA30 – too fast information spread
- May be viewed as learning initial conditions

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• This makes CA classification ambiguous

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- Mathematica's Random[Integer] uses CA30

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# How to distinguish cases?

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#### (How does this help?)

• There's probably not enough randomness to case type 1 behavior (But electron moving 1cm at the nearby star is felt  $10^{-5}$  sec later.)

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  ... not necessary... to have a formal definition of complexity."
- Not rigorous definition

 $\dots$  [T]he greatest complexity lies  $\dots$  in systems that neither stabilize..., nor exhibit close to uniform randomness forever.

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- Logical depth the number of computations; CA's are complex in this measure.

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- Do not solve equations (constraints); simulate evolution rules
  - ... [W]henever the behavior is of significant complexity its most plausible explanation tends to be some explicit process of evolution, not the explicit satisfaction of constraints.
- Programs as models as good as equations as models
  - ... [T]raditional matematic[s] ... say[s] that the motion of a planet is governed by ... differential equations. But one does not imagine that this means that the planet itself contains a device that explicitly solves [them].

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- Prediction works we are not hit by moving trucks (Wolfram would probably argue that these are all simple cases)

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- Can explain things a posteriori this is not predictive science

### Simple programs in biology



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#### Reaction-diffusion process

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- in practice no entropy decrease is seen since we start with low entropy states (!)
- The Second Law is an important and quite general principle—but it is not universally valid.

## Space-time

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- multiway universes may sample different histories
- How is this all testable?

• Relativity: one step in network –  $\ell_P, t_P$ ;

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- Can recover time dilation and other spatial properties
- Cannot get  $E = mc^2$  and other non-spatial aspects

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- Akin to stable structures in cellular automata
- Gravity is changing the pattern of connections and getting curvature – the number of nodes within a given distance from the center depends on the Ricci scalar

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- Randomness of Quantum Mechanics is intrinsically generated
- EPR-type problems may be overcome by "threads that continue to connect particles" (But no details are given.)
- Some interesting properties of physics are obtained

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- There are universal computers among almost all very simple ones

- Everything is computation (e. g., motion of fluid solving Navier-Stokes equation)
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- There are universal computers among almost all very simple ones
- Threshold for universality is low possibly all class 4 CA's are in it (localized structures allow controlled information transmission)

I suspect that in almost any case where we have seen complex behavior ... it will ... be possible to show that there is universality.

#### Universal cellular automata



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#### • Related to Gödel's undecidability (does the pattern die out?)

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- Maybe we should ask about all possible input-output relations? If mutual information between them can get infinite, we can encode all computations and get universality

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- "... most of the core processes needed for general human-like thinking will be able to be implemented with rather simple rules."
- There is not intelligence substantially better than ours
- Free will is described
- Bleak human future

## Last addition to understanding ANKOS

- Most systems are irreducible, but random only instrinsically
- Most systems are as complex as they get
- They cannot be predicted at all
- Traditional science is useless for them
- But aside from stating the uselessness, ANKOS does no better.