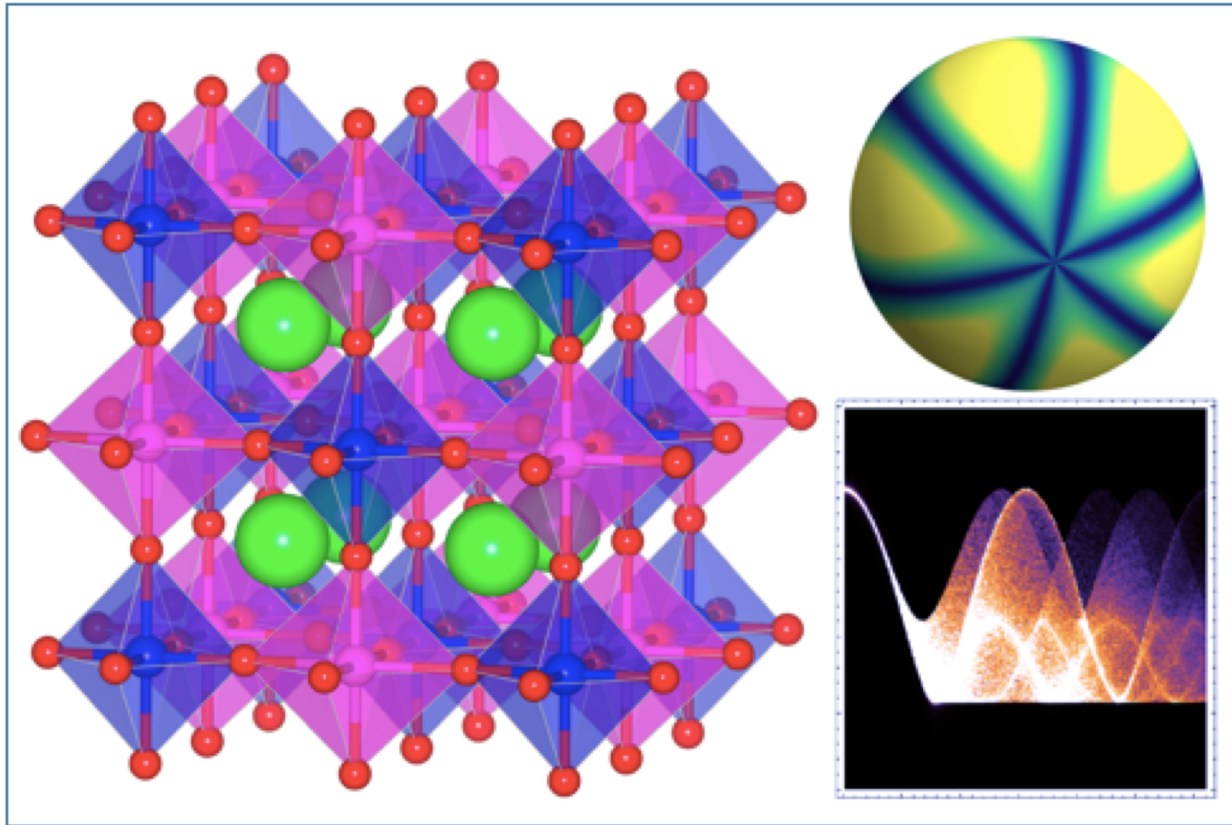


Octupolar order in a d-orbital Mott insulator



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7 Oct 2020



UNIVERSITY OF
TORONTO



NSERC
CRSNG



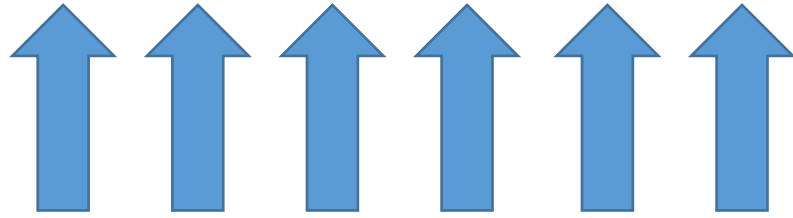
ICTS

INTERNATIONAL
CENTRE *for*
THEORETICAL
SCIENCES

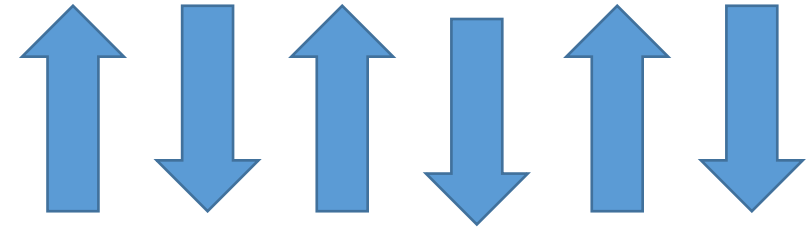
TATA INSTITUTE OF FUNDAMENTAL RESEARCH

Multipolar orders

Dipolar order

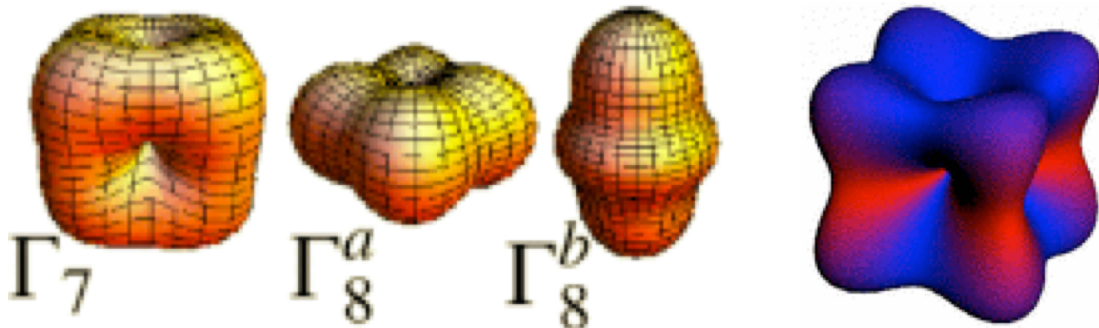


Ferromagnetism
Easily manifest



Antiferromagnetism
Probe: Neutron diffraction
Neutron: dipole interaction

Multipolar orders



SOC drives complex spin and orbital density distributions
“**Hidden order**”: URu_2Si_2 , NpO_2

Mostly 5f heavy fermions

Energy scales in 5f v/s 5d systems

5f (actinides)

Hubbard $U \sim 1-2\text{eV}$

Spin orbit coupling $\sim 1-2\text{eV}$

Hund's coupling $\sim 0.5\text{eV}$ (?)

Crystal field splittings $\sim 10-100\text{meV}$

[write crystal field potential in terms of J]

Well-separated J levels

5d systems

Hubbard $U \sim 1-2\text{eV}$

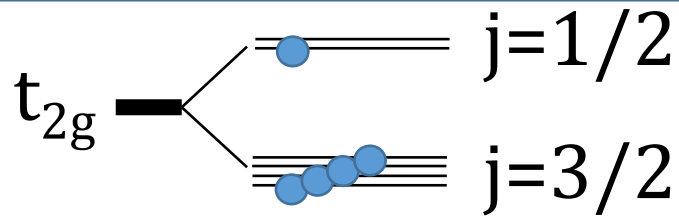
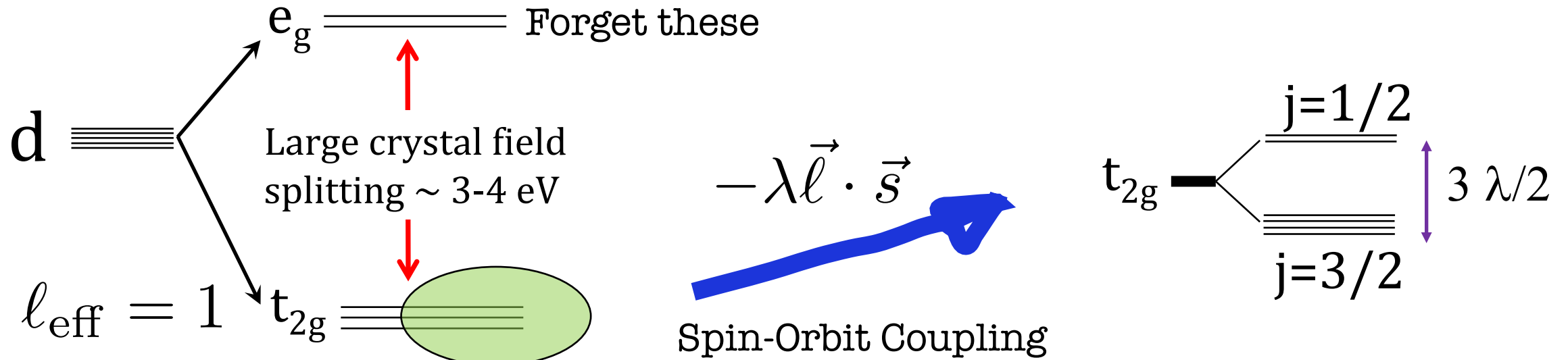
Crystal field splittings $\sim 2-3\text{eV}$

[write crystal field potential in terms of L]

SOC $\sim 0.4\text{eV}$; Hund's coupling $\sim 0.25\text{eV}$

Well-separated orbitals

d-orbitals: “atomic limit”



Sr₂IrO₄, Na₂IrO₃, Li₂IrO₃

B. J. Kim, et al, PRL 2008

B. J. Kim, et al, Science 2009

Y. Singh, P. Gegenwart PRB 2010

G. Jackeli and G. Khaliullin, PRL 2009

Most well studied limit

- ❖ “Relativistic” Mott insulator
- ❖ Superconductivity in doped Sr₂IrO₄?
- ❖ Kitaev physics in edge-shared geometries

d-orbitals: “atomic limit”

===== $j=1/2$

=====
=====
===== $j=3/2$
●

===== $j=1/2$

=====
=====
===== $j=3/2$
●●

===== $j=1/2$

=====
=====
===== $j=3/2$
●●●

===== $j=1/2$

=====
=====
===== $j=3/2$
●●●●

Ba₂NaOsO₆, Ba₂MgReO₆

Chen, Pereira, Balents, PRB (2010)
C. Svoboda, Trivedi, Randeria (2017)
L. Lu, et al, Nat. Comm. (2017)
D. Hirai, Z. Hiroi, JPSJ (2019)
D. Hirai, et al, arXiv:2004.13928

Recent work

- ❖ $j=3/2$ Mott insulator
- ❖ Nnbr orbital repulsion?
- ❖ Quadrupolar+Dipolar



This talk

D. D. Maharaj, et al, PRL (2020)
AP, et al, PRB (2020)
S. Voleti, et al, PRB (2020)



Ongoing work

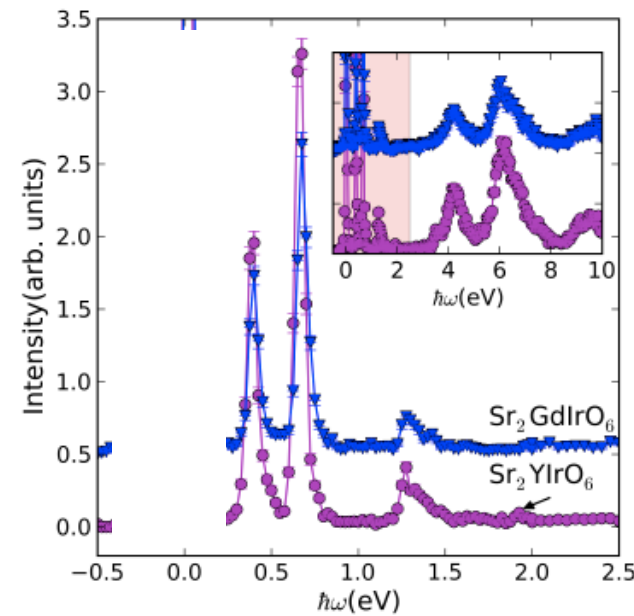
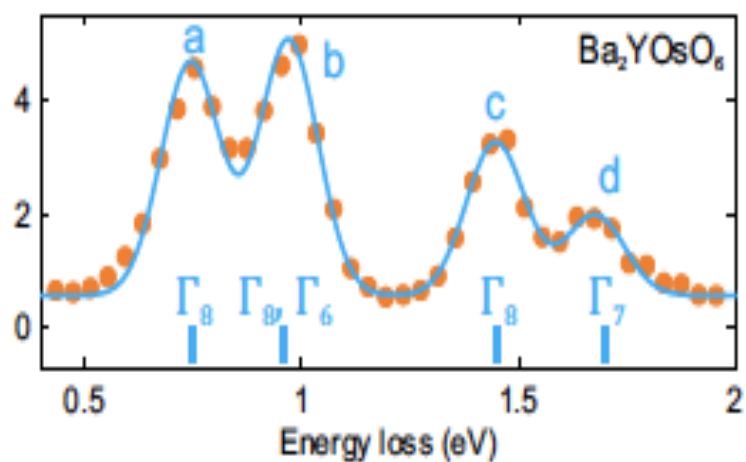
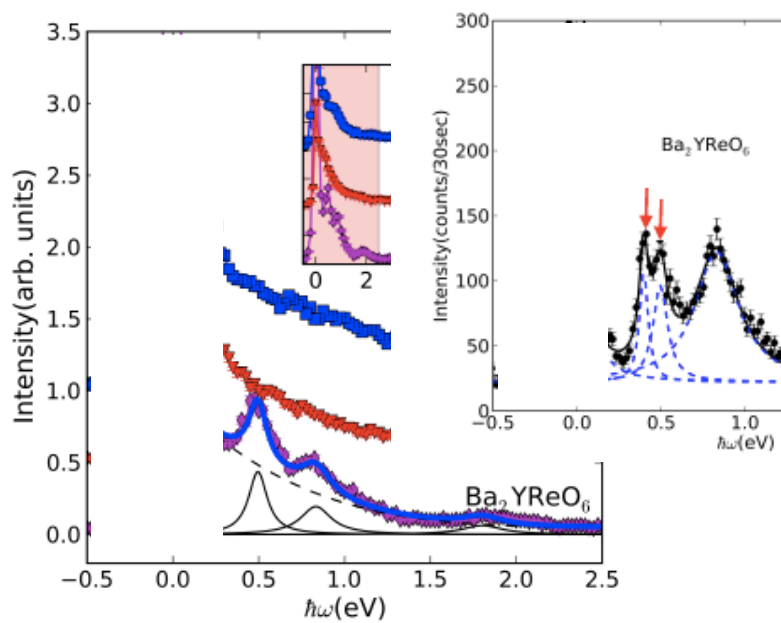
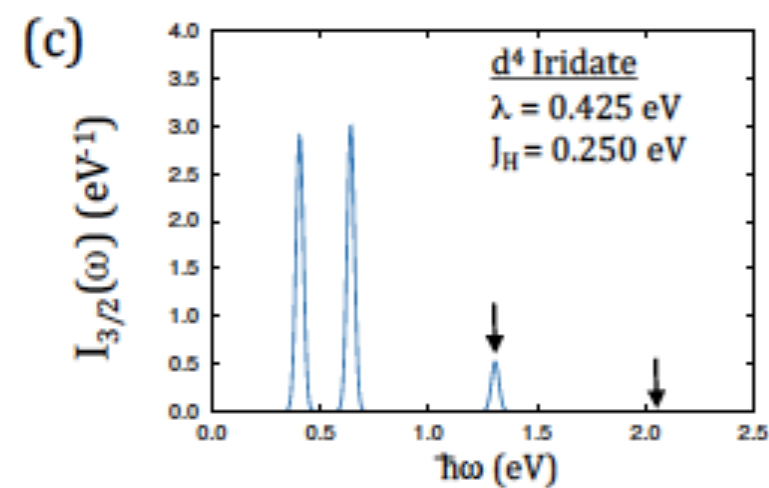
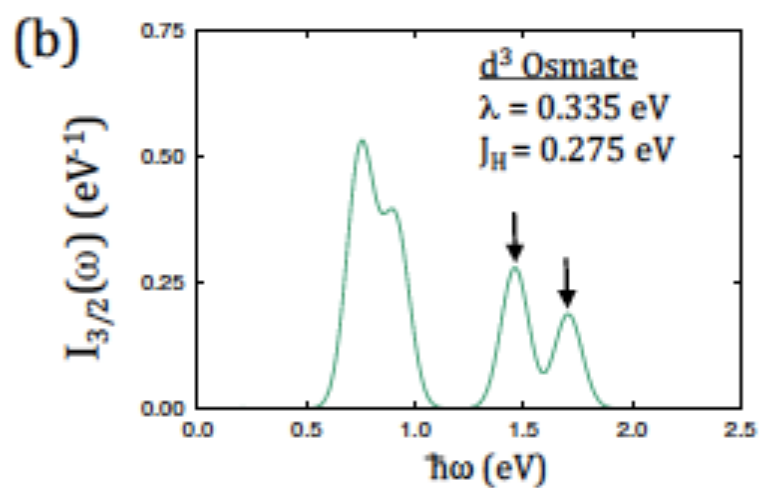
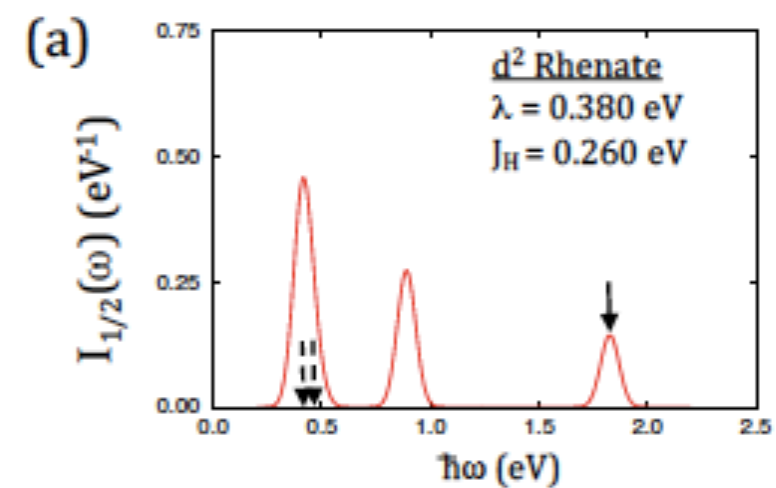
Ba₂YIrO₆, Sr₂YIrO₆

G. Khaliullin, PRL (2013)
G. Cao, et al, PRL (2014)
T. Dey, et al, Buchner, PRB (2016)
Svoboda, Randeria, Trivedi (2017)
A. Paramakanti, et al, PRB (2018)

Recent work

- ❖ Fully occupied $j=3/2$ orbital
- ❖ Mott insulator with $J_{\text{eff}}=0$
- ❖ Excitonic magnetism?

Exact diagonalization for RIXS



Ground state degeneracies

d^1 4-fold degenerate: $j=3/2$

d^2 5-fold degenerate: $J=2$

d^3 4-fold degenerate: $J=3/2$

d^4 0-fold degenerate: $J=0$

d^5 0-fold degenerate: $j=1/2$

Candidates for
multipolar orders

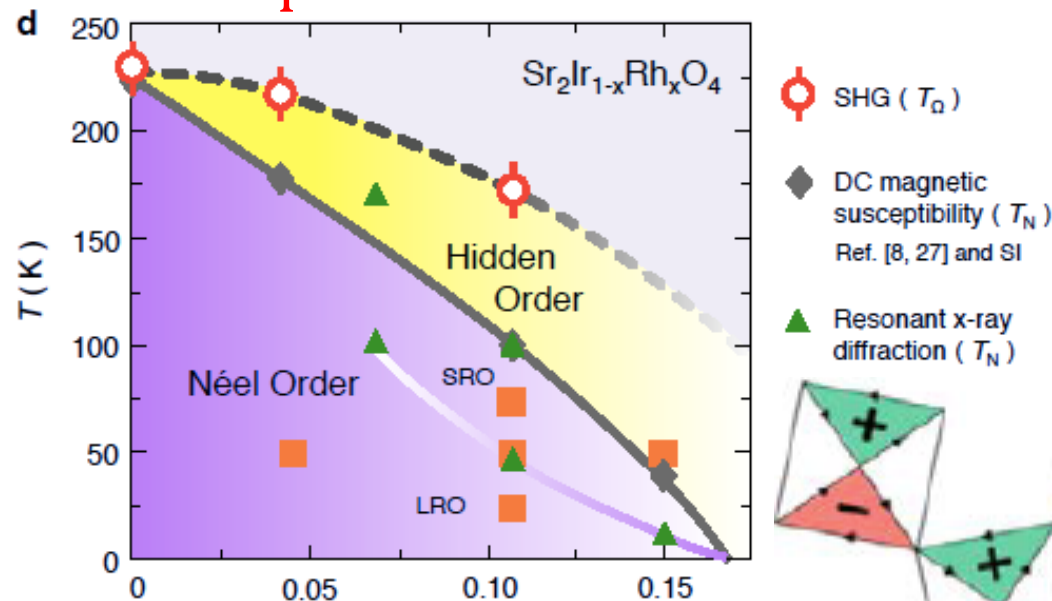
Multipolar symmetry breaking in d-orbitals

Inversion breaking -> SHG

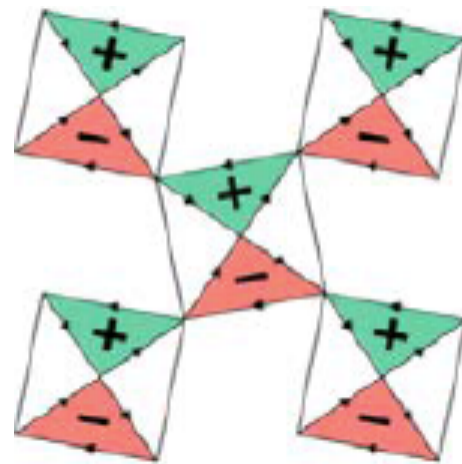
Parity-breaking transition

Toroidal moment?

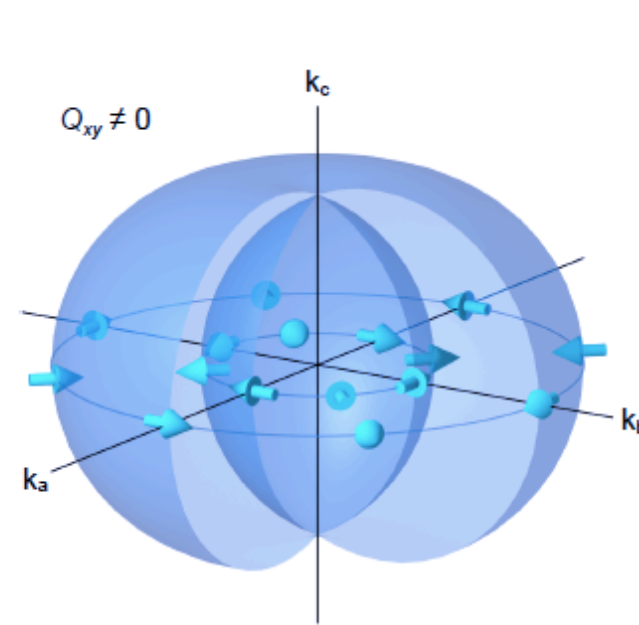
Loop current order?



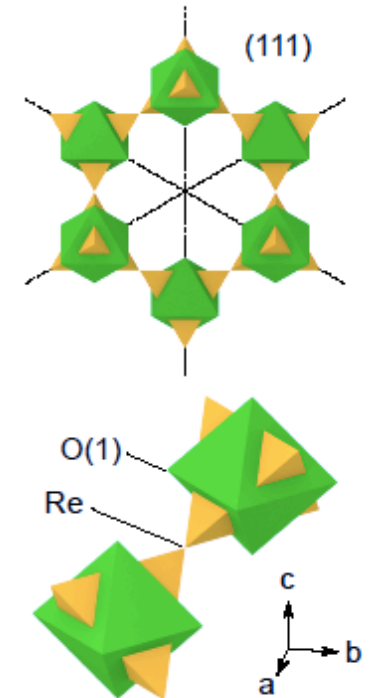
L. Zhao, et al,
Nat. Phys. (2016)



A Multipolar Nematic Order



B Cubic $\text{Cd}_2\text{Re}_2\text{O}_7$



$$Q_{xy} \propto (k_x S_y + k_y S_x)$$

Parity-breaking quadrupolar order

Liang Fu, PRL (2015)

J. W. Harter, et al, Science (2017)

Quadrupolar+Dipolar ordering in d-orbitals

Rodrigo, Chen, Balents (PRB 2010)
Chen, Balents (PRB 2011)

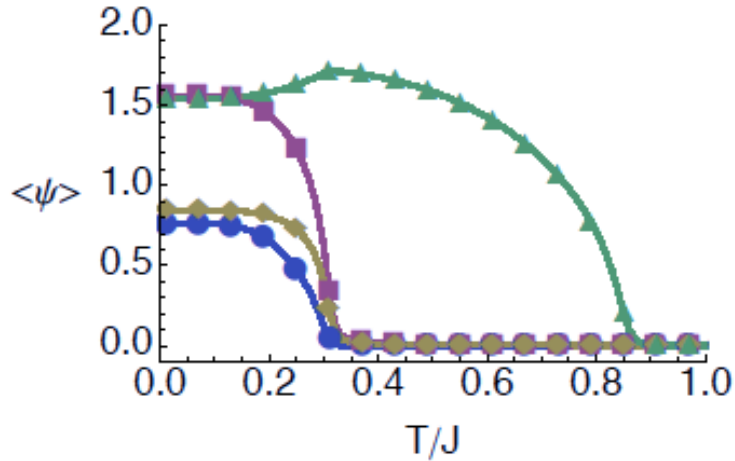
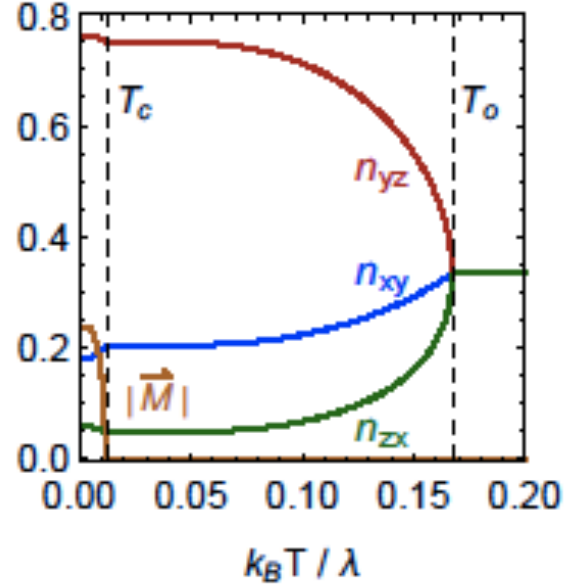


FIG. 9. (Color online) Temperature dependence of order parameters for $J'/J = 0.3$, $V/J = 0.3$. For these parameters, there is a continuous normal to quadrupolar transition, at $T/J \approx 0.85$, followed by a continuous quadrupolar to FMI10 transition at $T/J \approx 0.33$. The four order parameters plotted are: squares (red online) $\langle (T_{A,\alpha} - T_{B,\alpha})/2 \rangle$, circles (blue online) $\langle (Q_A^{3z^2} + Q_B^{3z^2})/2 \rangle$, diamonds (yellow online) $\langle (j_A + j_B)/2 \rangle$, and triangles (green online) $\langle (Q_A^{x^2-y^2} - Q_B^{x^2-y^2})/2 \rangle$.

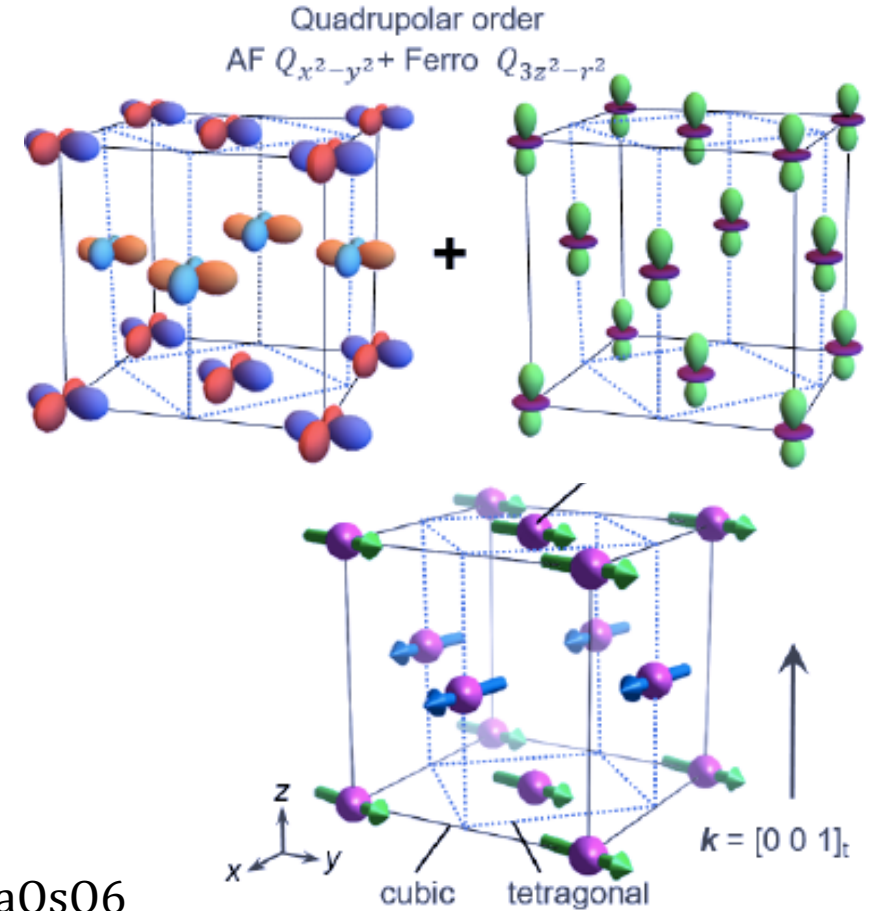
Svoboda, Randeria, Trivedi
[+ W. Zhang] (arXiv:2017)



L. Lu, et al, Nat. Comm. (2017): Ba2NaOsO6

D. Hirai, Z. Hiroi, JPSJ (2019): Ba2MgReO6

D. Hirai, et al, arXiv:2004.13928: Ba2MgReO6

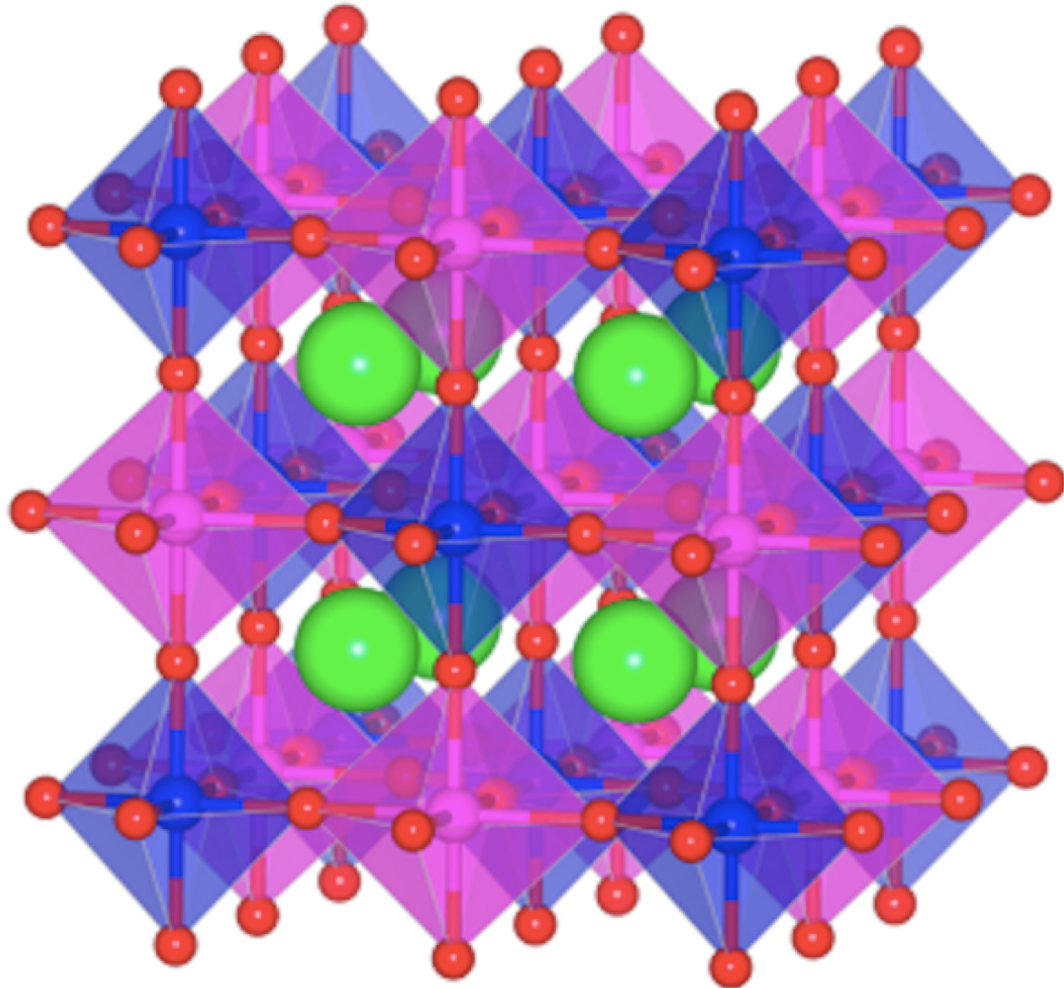


TQ = 33K (seen from non-resonant XRD)

TN = 18K (seen from resonant XRD and polarization analysis)

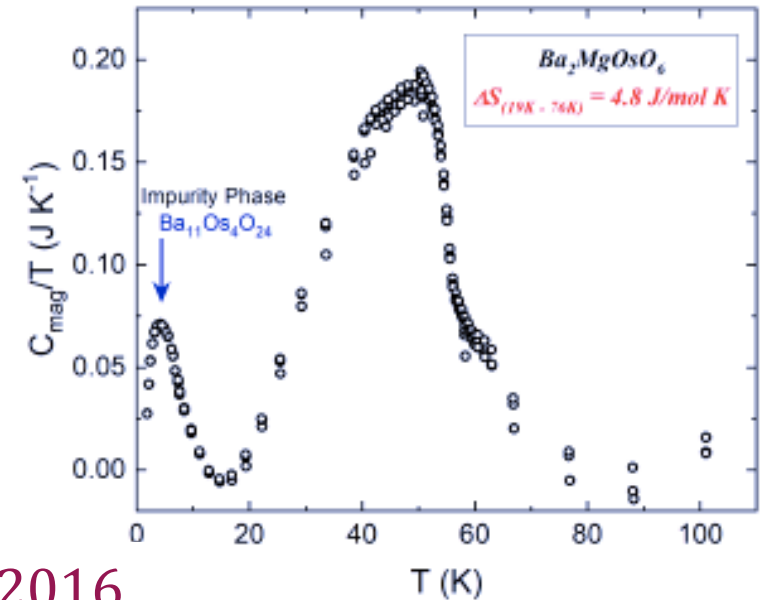
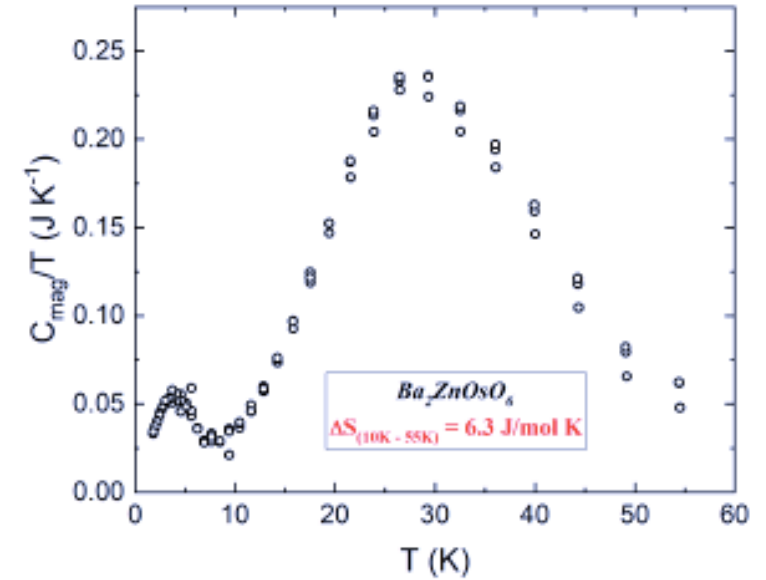
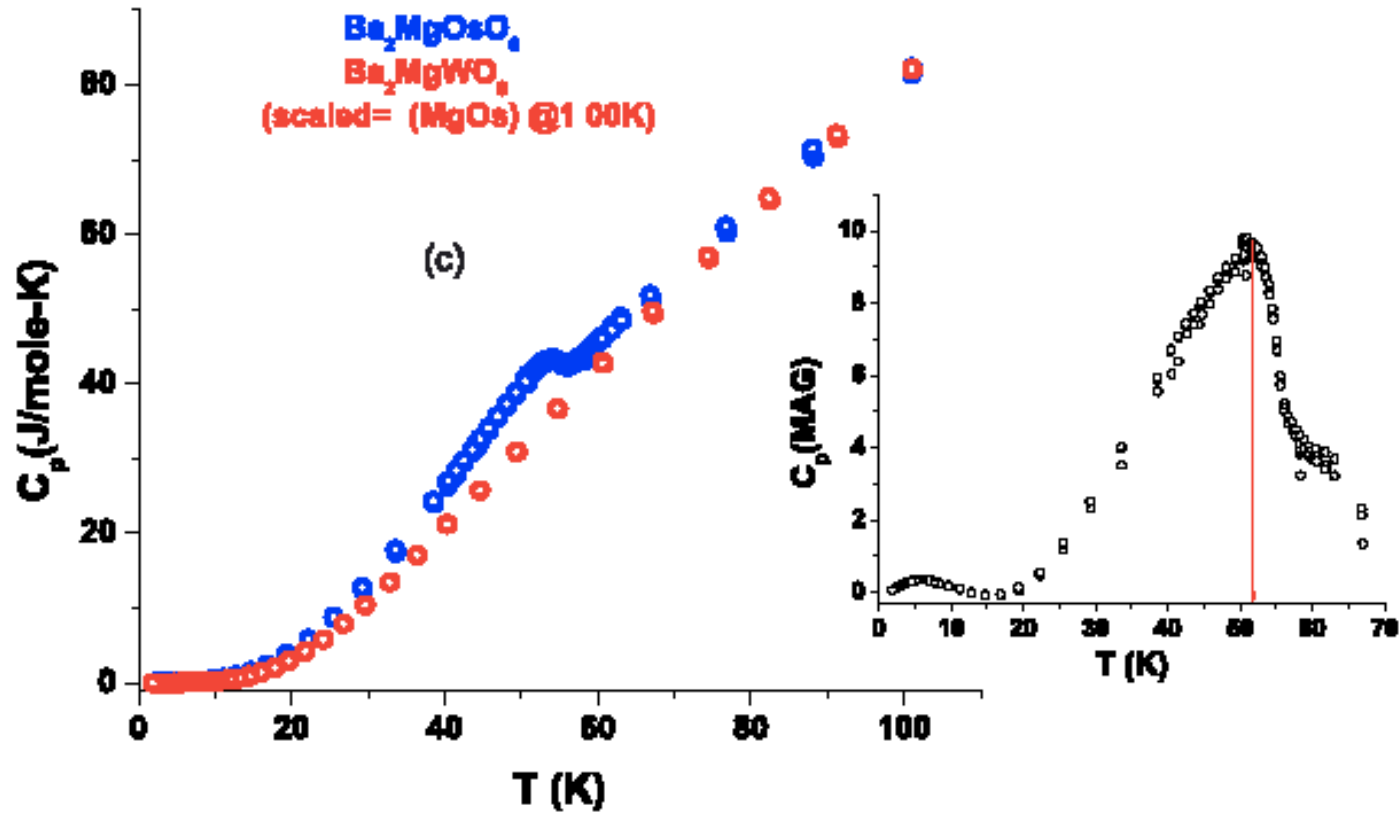
Ordered double perovskites with SOC

Mott insulator with $J=2$ spins



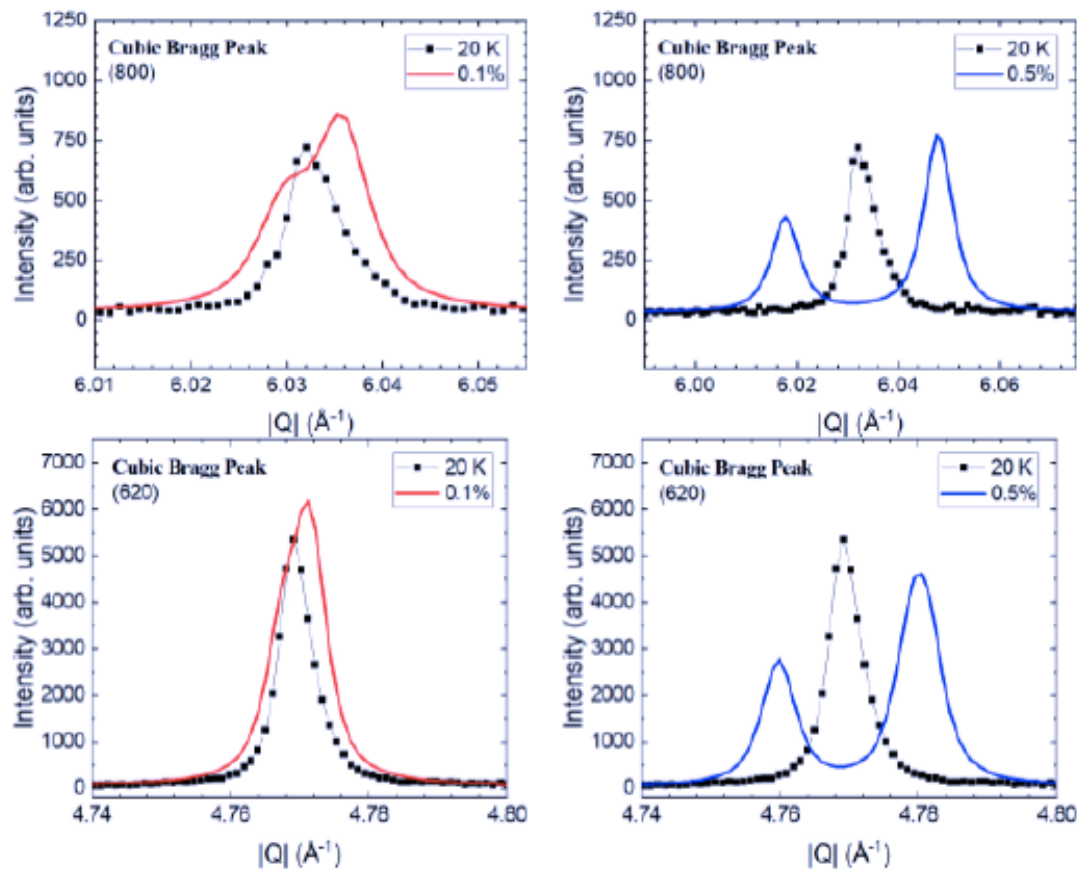
Os⁵⁺: $5d^2$ in checkerboard pattern (FCC lattice)

Thermodynamics: Specific heat and entropy



- Phase transition at $T \sim 30-50K$
- Entropy recovered $\ll R \ln(5)$: Not $J=2$?
- $R \ln(2) \sim 5.8$ J/mol-K; $R \ln(3) \sim 9.1$ J/mol-K

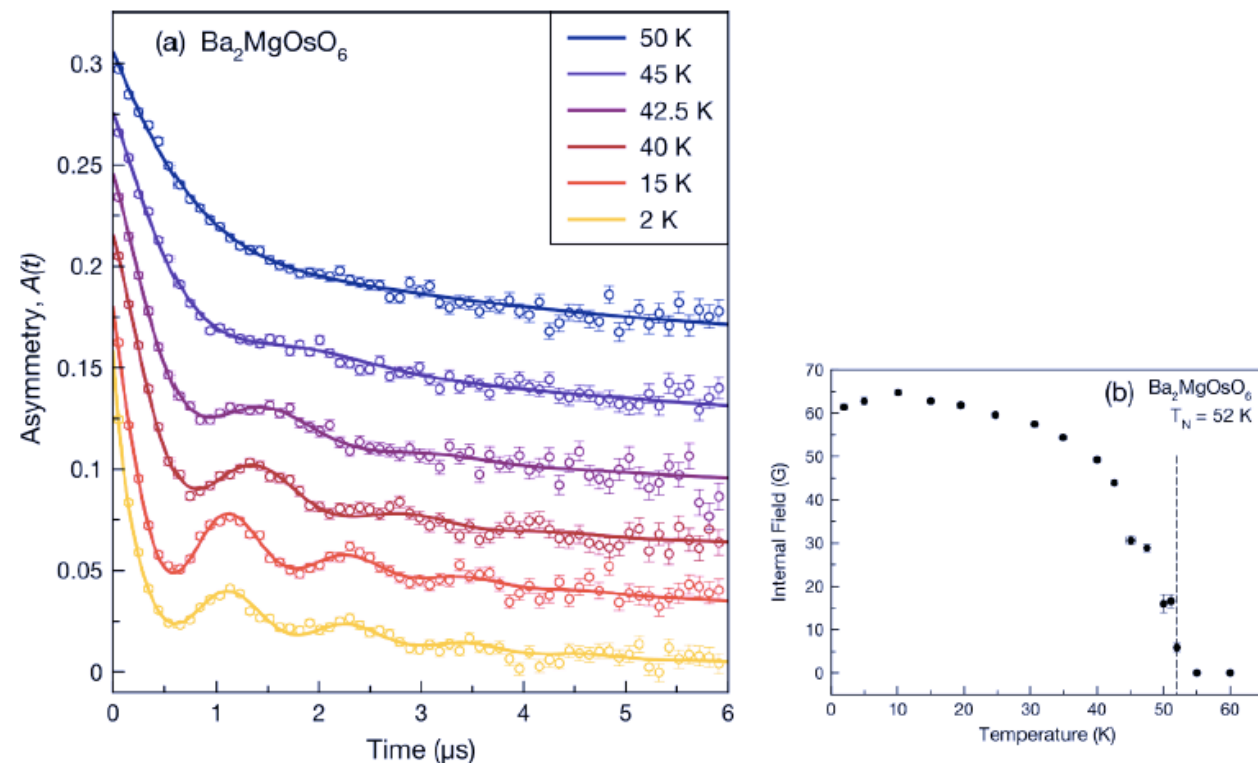
Xray diffraction



Perfectly cubic, $Fm\bar{3}m$
($<0.1\%$ distortion)

D. D. Maharaj, et al, PRL (2020)

μSR



Signature of time-reversal
symmetry breaking

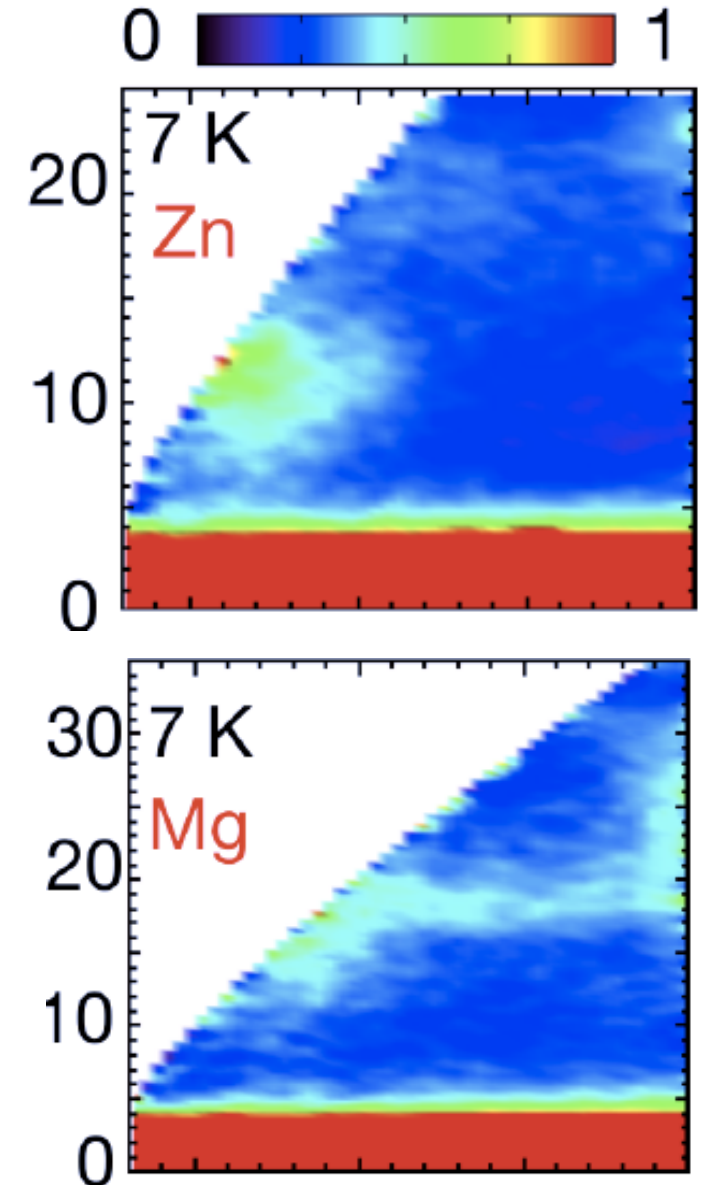
C. M. Thompson, et al, JPCM (2014)

Susceptibility, neutron diffraction, neutron scattering

System	T^*	θ_{CW}	μ_{ord}
$\text{Ba}_2\text{CaOsO}_6$	49	$-156.2(3)$	$< 0.11\mu_B$
$\text{Ba}_2\text{MgOsO}_6$	51	$-120(1)$	$< 0.13\mu_B$
$\text{Ba}_2\text{ZnOsO}_6$	30	$-149.0(4)$	$< 0.06\mu_B$

- Moderate frustration
- No sign of ordered moment!
- Spin gap in inelastic scattering

D. D. Maharaj, et al, PRL (2020)



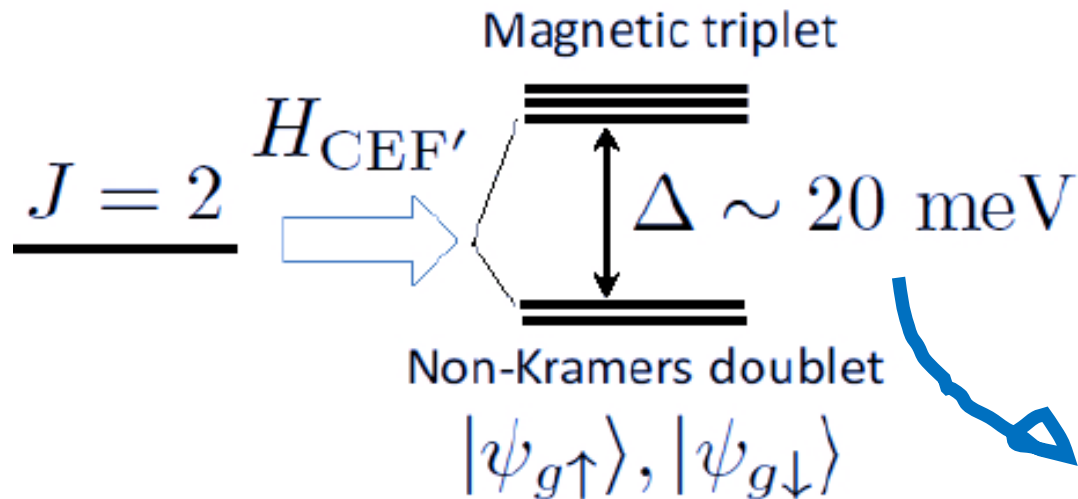
Puzzles

- ❑ Entropy recovered across $T^* \ll R \ln(5)$
- ❑ No sign of a second transition at higher T
- ❑ Remains cubic down to $T \ll T^*$
- ❑ Time reversal breaking via mSR
- ❑ No sign of magnetic Bragg peaks
- ❑ Spin gap in neutron scattering ~ 10 meV

The correct “atomic limit”

New Idea:

- $J=2$ splits in octahedral environment
- Unresolved in RIXS



- ✓ Spin gap
- ✓ No dipole order
- ✓ Entropy: $R \ln(2)$

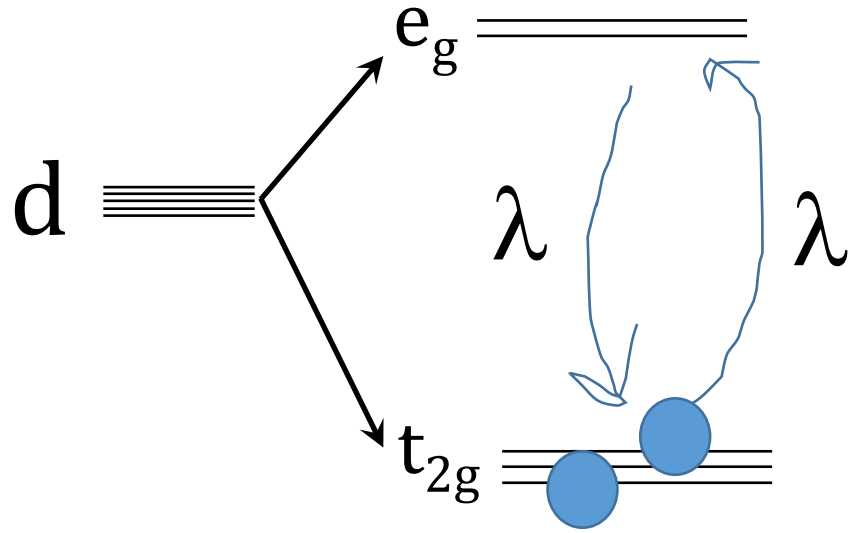
$$|\psi_{g,\uparrow}\rangle = |0\rangle$$

$$|\psi_{g,\downarrow}\rangle = \frac{1}{\sqrt{2}}(|2\rangle + |-2\rangle)$$

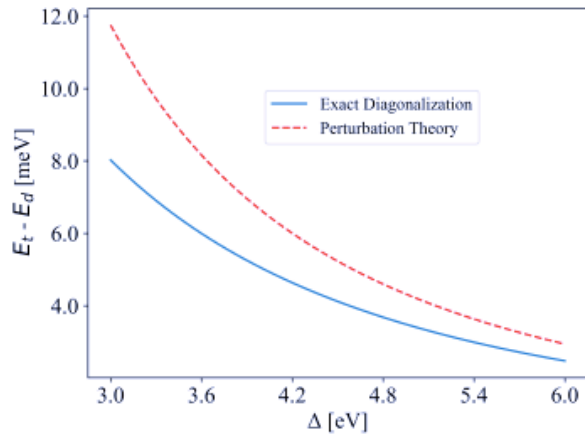
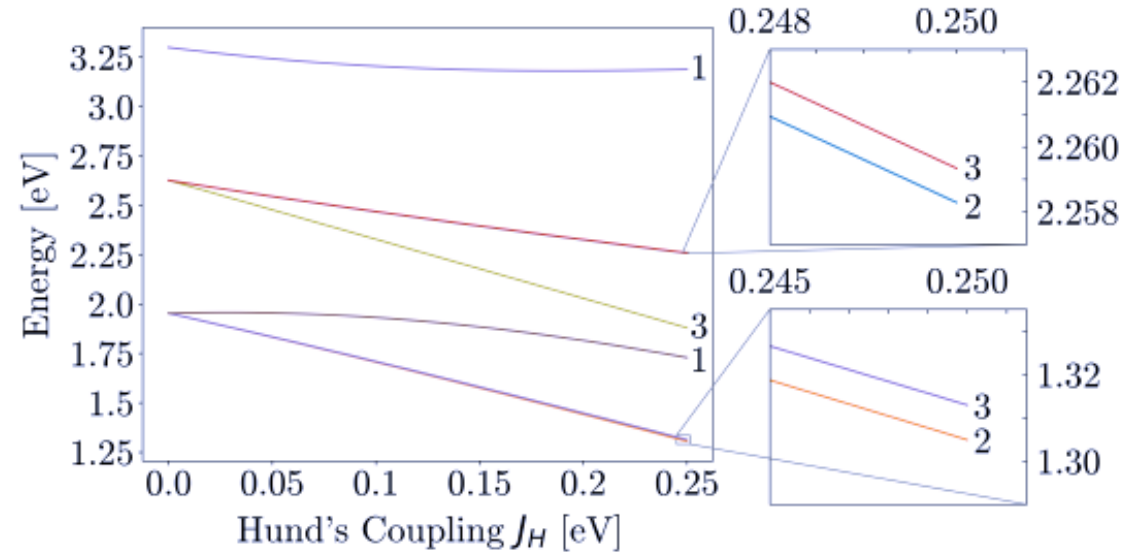
Splitting originates from t_{2g} - e_g coupling!

Cannot blindly drop e_g orbitals - Might be crucial for low energy physics!

The correct “atomic limit”



$$\Delta \sim O(J_H \lambda^2 / V)$$



$$H_{\text{CEF}} = -V_{\text{eff}} (\mathcal{O}_{40} + 5\mathcal{O}_{44})$$

$$\mathcal{O}_{40} = 35J_z^4 - (30J(J+1) - 25)J_z^2 + 3J^2(J+1)^2 - 6J(J+1),$$

$$\mathcal{O}_{44} = \frac{1}{2}(J_+^4 + J_-^4).$$

Exchange interactions

$$\tau_x \propto J_x^2 - J_y^2$$

$$\tau_z \propto 3J_z^2 - J^2$$

$$\tau_y \propto \text{Sym} [J_x J_y J_z]$$

“XY” Quadrupolar
charge density

Ising magnetic
octupole

$$H_{\text{eff},xy}^{(1)} = \sum_{\langle ij \rangle_{xy}} (-\gamma_0 \tau_{ix} \tau_{jx} + \gamma_1 \tau_{iz} \tau_{jz})$$

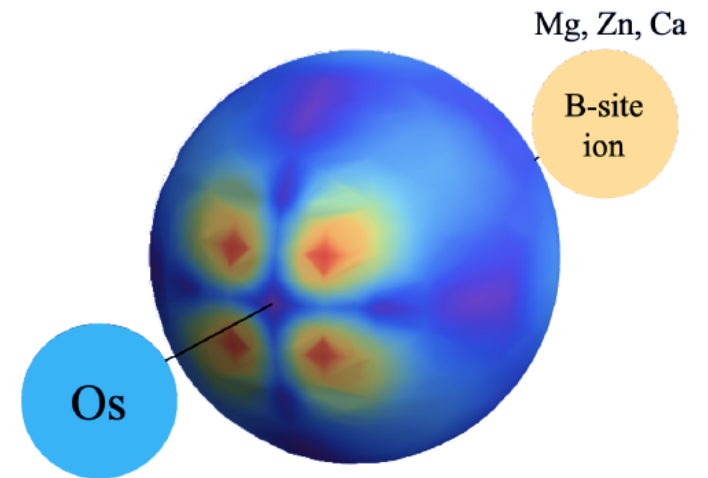
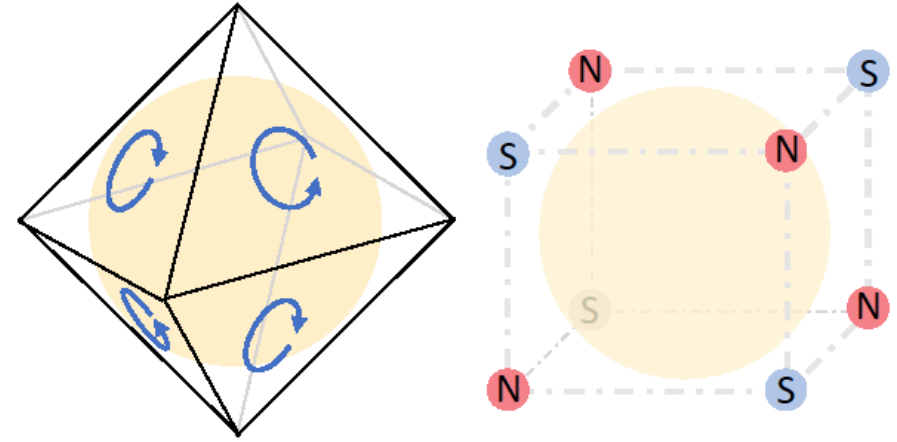
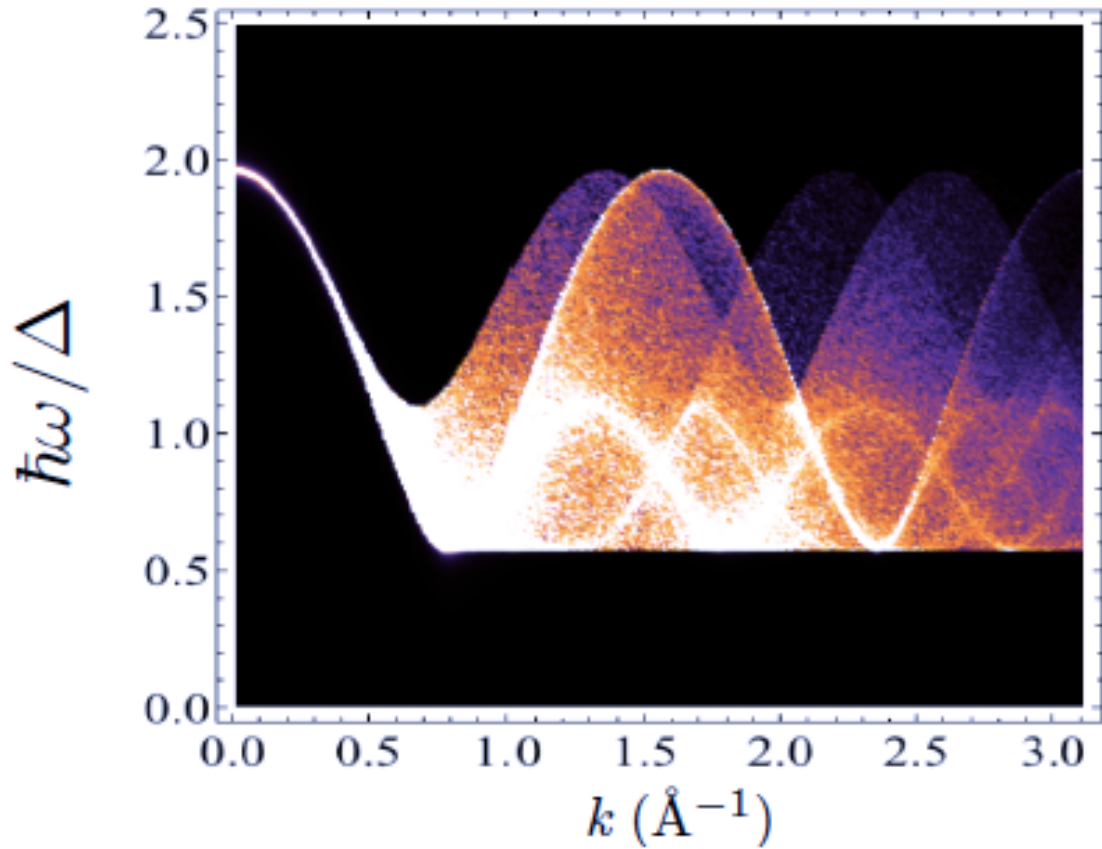
$$H_{\text{eff},xy}^{(2)} = -\frac{1}{2\Delta} \sum_{\langle ij \rangle_{xy}} (\gamma_m \vec{J}_i \cdot \vec{J}_j + \gamma_2 \rho_{i,xy} \rho_{j,xy})^2$$

$$H_{xy}^{\text{Quad}} = \sum_{\langle ij \rangle_{xy}} \left[\left(-\gamma_0 + 6 \frac{\gamma_m \gamma_2}{\Delta}\right) \tau_{ix} \tau_{jx} + \left(\gamma_1 - \frac{9}{8} \frac{\gamma_2^2}{\Delta}\right) \tau_{iz} \tau_{jz} \right]$$

$$H_{\text{Oct}}^{(2)} = -6 \frac{\gamma_m \gamma_2}{\Delta} \sum_{\langle ij \rangle} \tau_{iy} \tau_{jy}$$

✓ Leads to ferro-octupolar coupling from cross-term

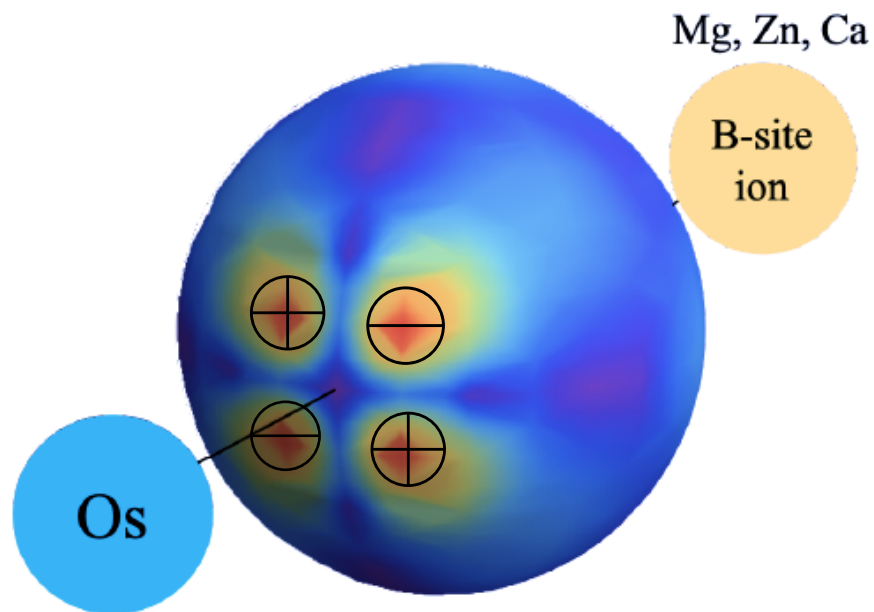
Ferro-octupolar order: Neutron Scattering, μ SR



✓ Spin-gapped magnetic exciton

✓ Loop current order, $B \sim 30\text{G}$

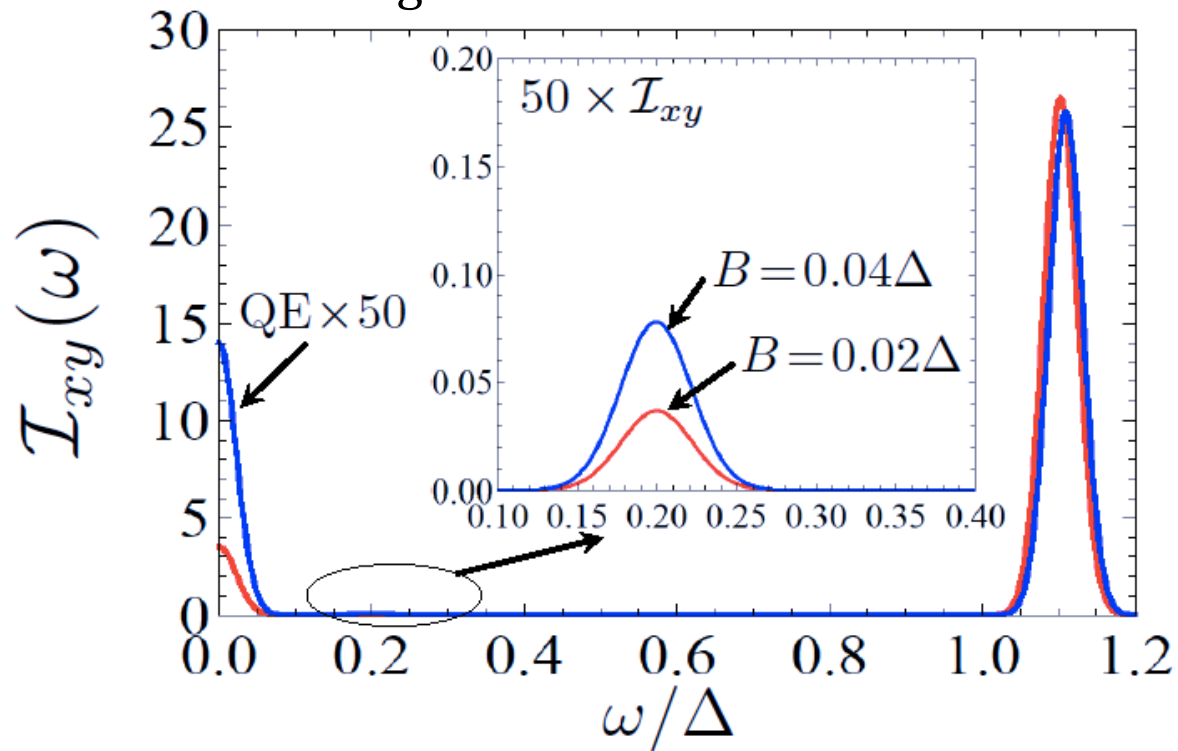
Predictions for NMR, Raman scattering



- Oxygen NMR should not see T^* transition
- Break C_4 symmetry \rightarrow NMR signal

AP, D. D. Maharaj, Bruce Gaulin, PRB 2020
S. Voleti, et al, PRB 2020

B_{2g} Raman scattering

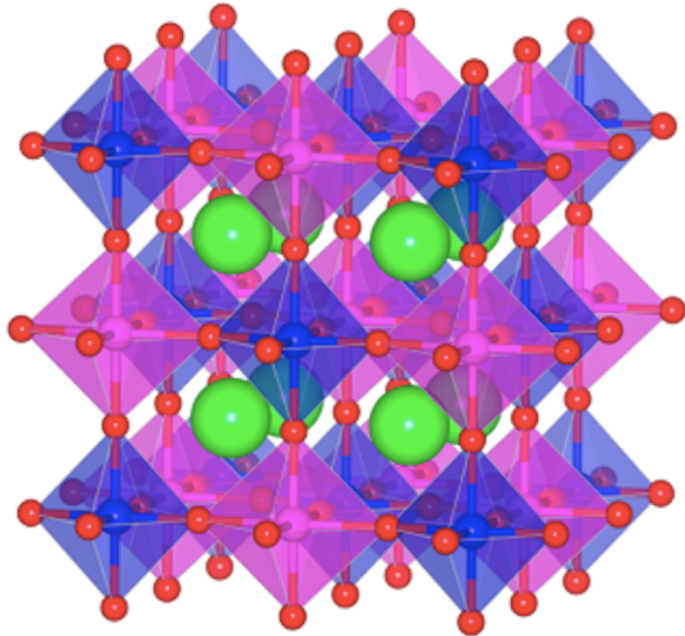


- Field B_z induces Q_{xy} quadrupolar order
- New quasielastic peak
- New transition between split doublet

- ❖ $\text{Ba}_2\text{MgOsO}_6$
- ❖ $\text{Ba}_2\text{CaOsO}_6$
- ❖ $\text{Ba}_2\text{ZnOsO}_6$

Octupolar order

- ✓ Entropy recovered across $T^* \sim R \ln(2)$
- ✓ Remains cubic down to $T \ll T^*$
- ✓ Time reversal breaking via mSR
- ✓ No sign of magnetic Bragg peaks
- ✓ Spin gap in neutron scattering $\sim 10 \text{ meV}$



Old parallel: complex eg orbital order (J. van den Brink, D. Khomskii PRB 2001)

Collaborators and references



Bruce Gaulin



Dalini Maharaj



Sreekar Voleti



Graeme Luke

- ❖ D. D. Maharaj, G. Sala, M. B. Stone, E. Kermarrec, C. Ritter, F. Fauth, C. A. Marjerrison, J. E. Greedan, AP, Bruce Gaulin, PRL 124, 087206 (2020)
- ❖ AP, D. D. Maharaj, Bruce Gaulin, PRB 101, 054439 (2020)
- ❖ S. Voleti, D.D. Maharaj, Bruce Gaulin, Graeme Luke, AP, PRB 101, 155118 (2020)

Summary and open issues

- First candidate for d-orbital octupolar order?
- High T_c octupolar symmetry breaking
- Predictions for NMR and Raman scattering
- **Elasticity** (A. Patri, Nat Comm 2019; M. Sorensen, I. Fisher arXiv:2020)

- Can we dynamically “switch” the Ising order?
- Can doping lead to fluctuating loop currents?
- Are multipolar orders useful for anything?

