



Strange Bosons in Strange Metals

Catherine Pépin, (IPhT, CEA-Saclay)



A. Banerjee



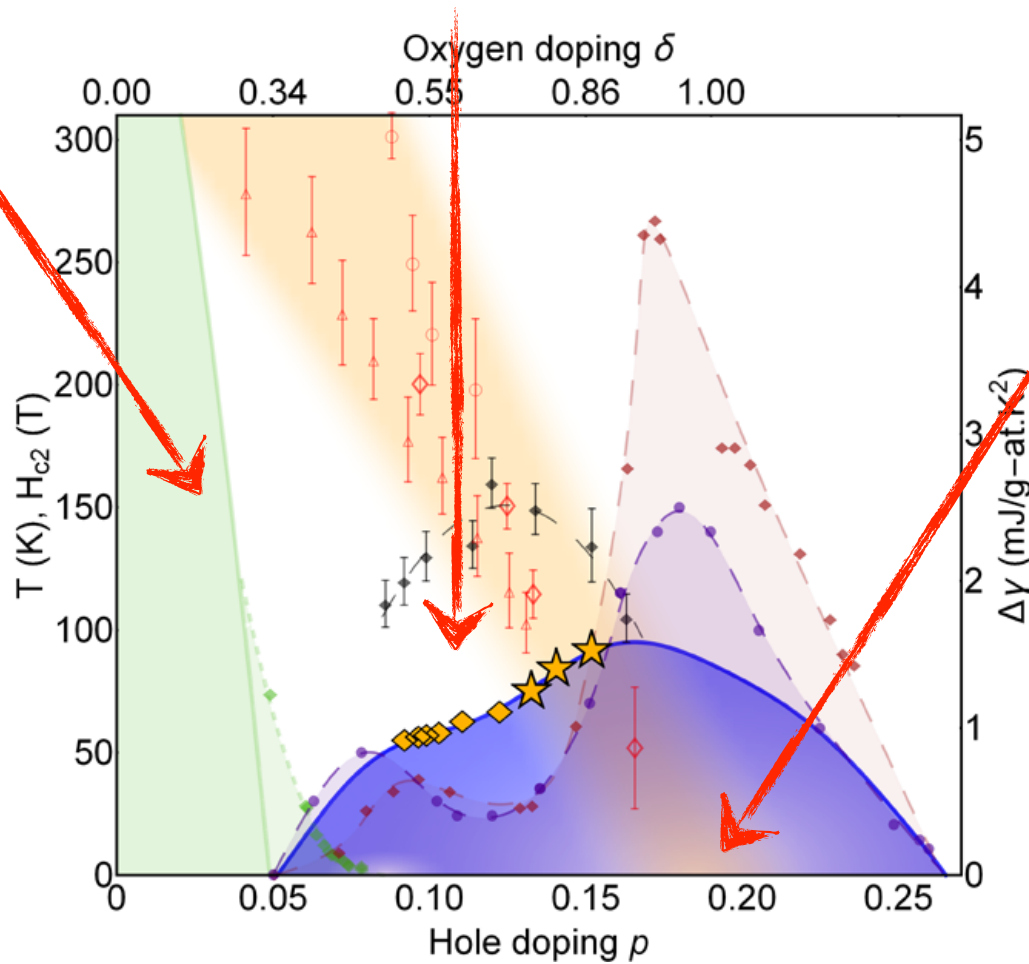
S. Sarkar & M. Grandadam

Correlated20, KITP, Oct. 13th, 2020

Mott transition

Fluctuations

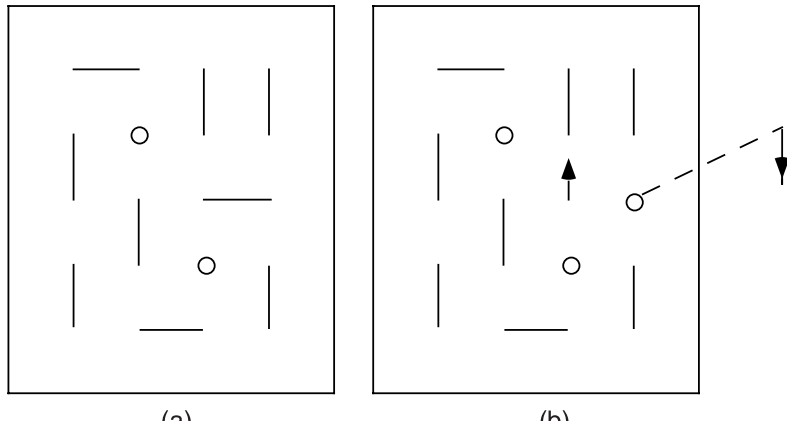
QCP under the dome



Ramshaw, 2015

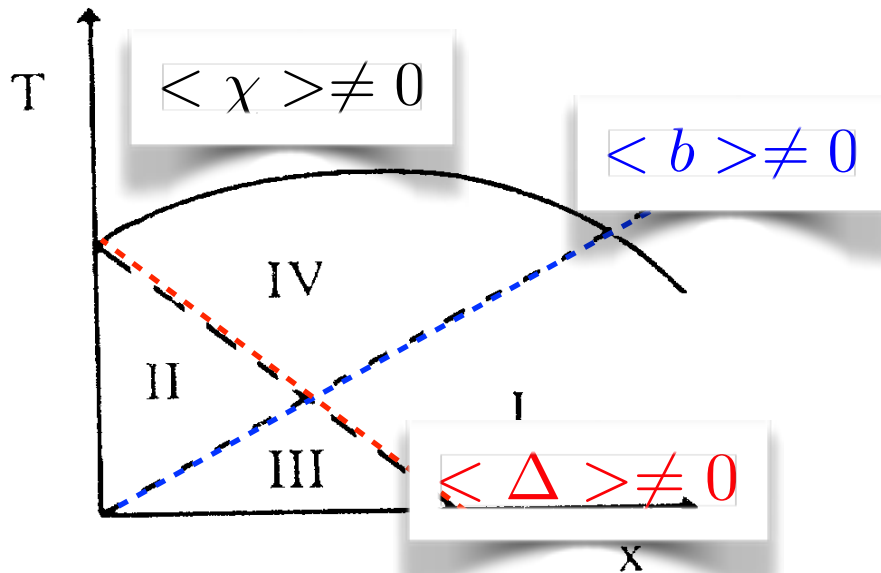
1. The context of strong coupling : doping a Mott insulator

Resonating Valence Bond (RVB) : pairs form and fluctuate



$$\chi_{ij} = \sum_{\sigma} \langle f_{i\sigma}^{\dagger} f_{j\sigma} \rangle,$$

$$\Delta_{ij} = \langle f_{i\uparrow} f_{j\downarrow} - f_{i\downarrow} f_{j\uparrow} \rangle.$$



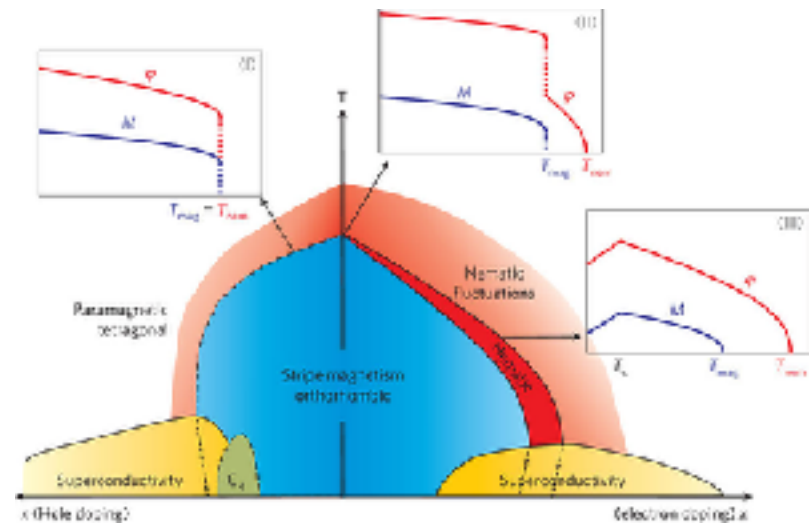
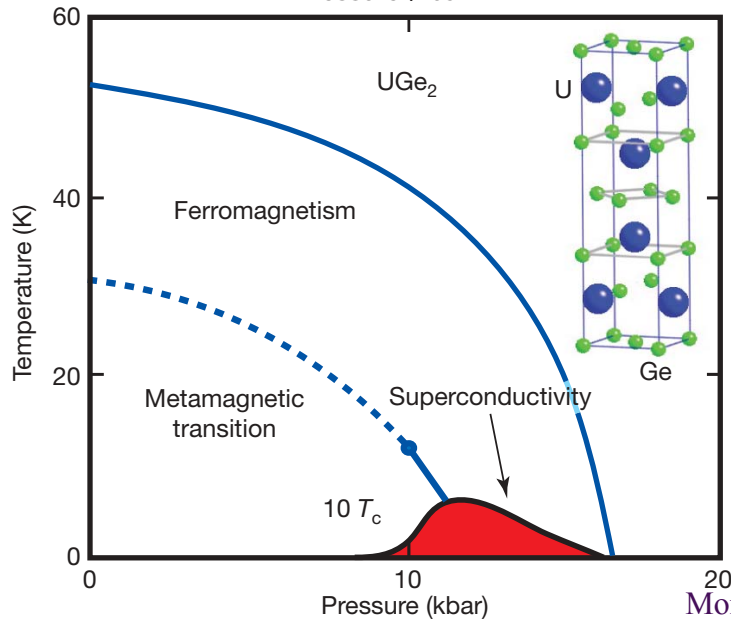
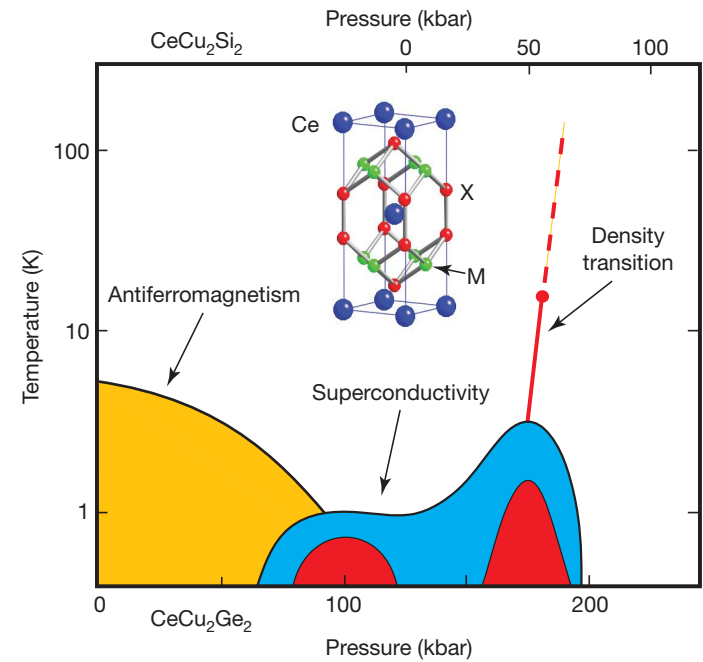
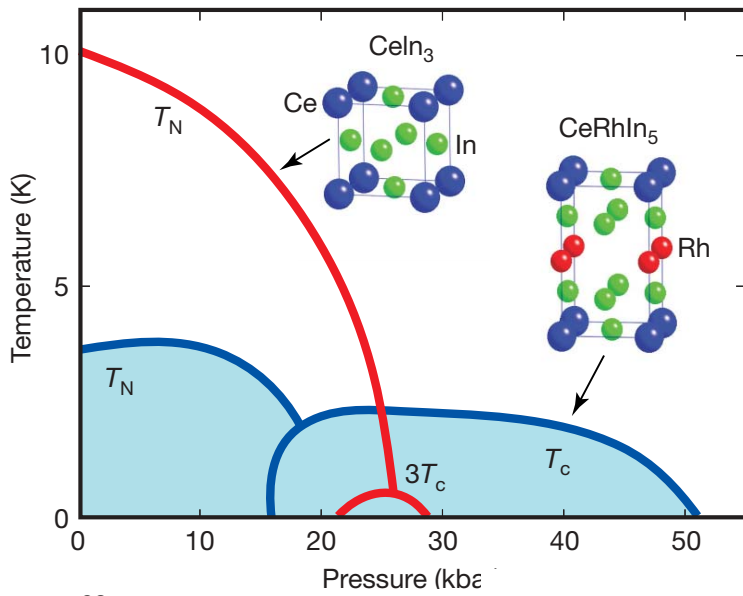
$$c_{i\sigma}^{\dagger} = f_{i\sigma}^{\dagger} b_i$$

Spinon

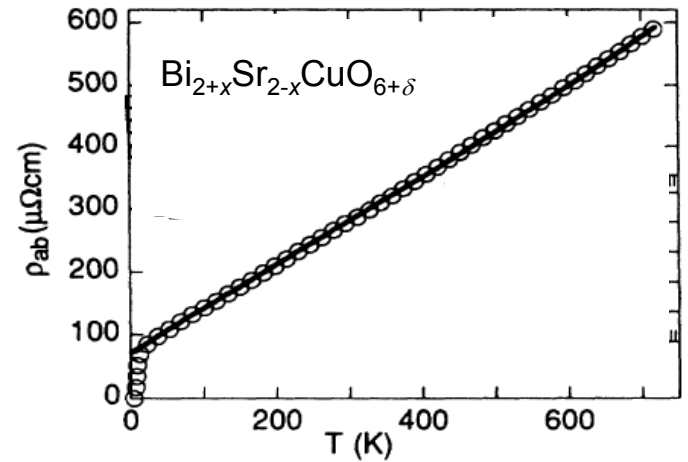
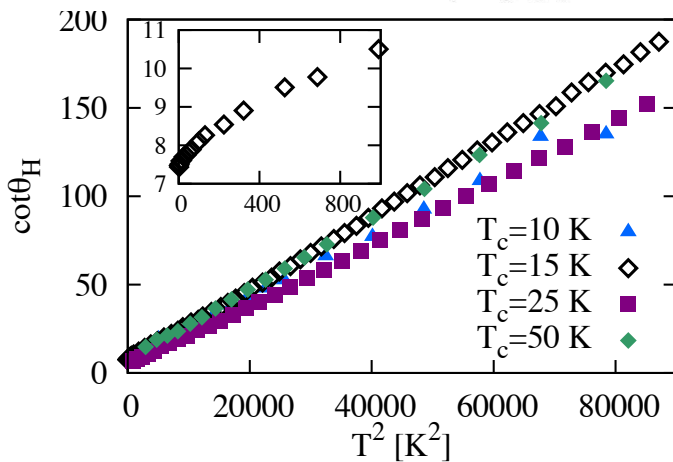
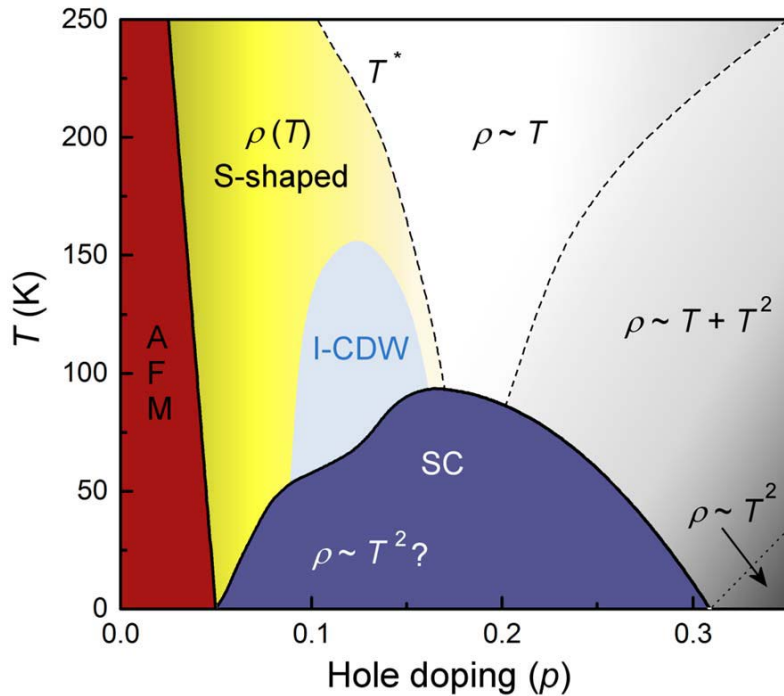
Holon

$$f_{i\uparrow}^{\dagger} f_{i\uparrow} + f_{i\downarrow}^{\dagger} f_{i\downarrow} + b_i^{\dagger} b_i = 1.$$

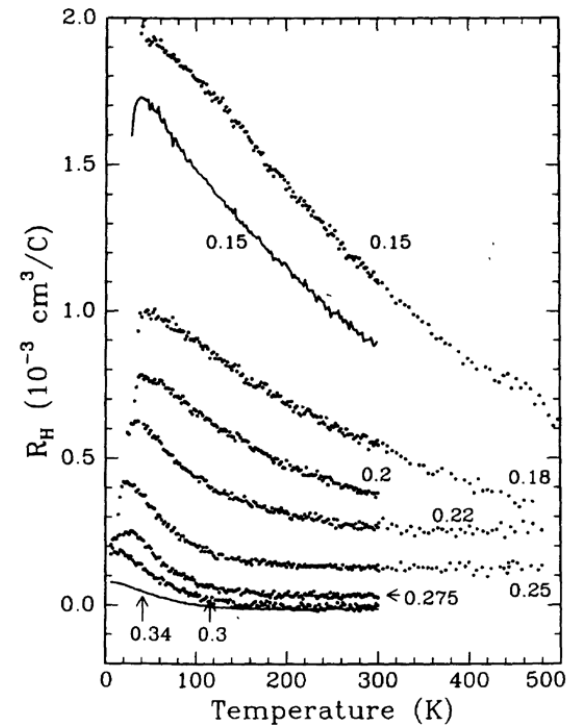
2. QCP under the SC dome



Most strongly Correlated QCP ?

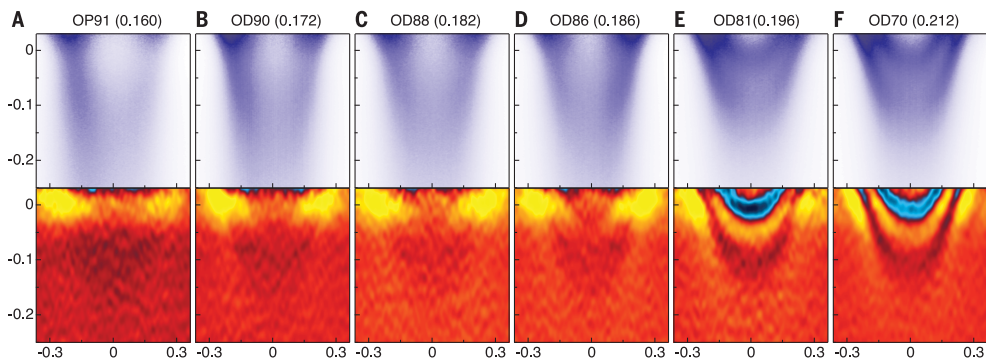
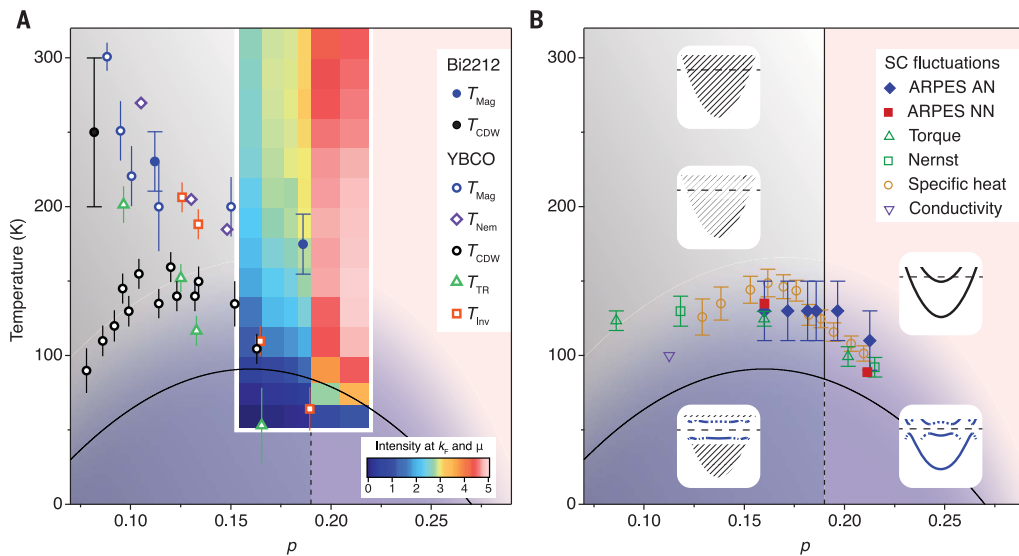


Martin *et al.*, *Phys. Rev. B* (1990)

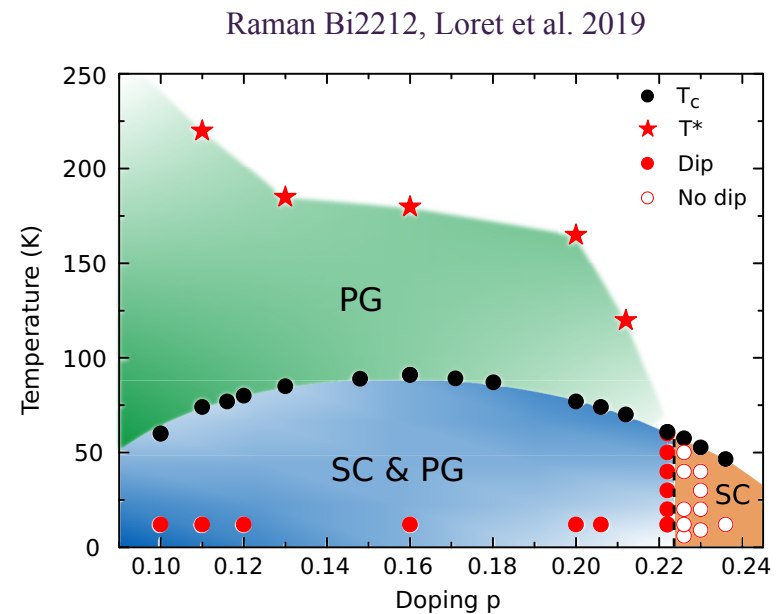


Hwang *et al.*, *PRL* **72** 2636 (94)

QCP questionned : an abrupt change at p^* ?



ARPES Bi2212, Chen et al. 2019



3. Fluctuations

TABLE 1 Phase stiffness and T_{θ}^{\max} for various superconductors

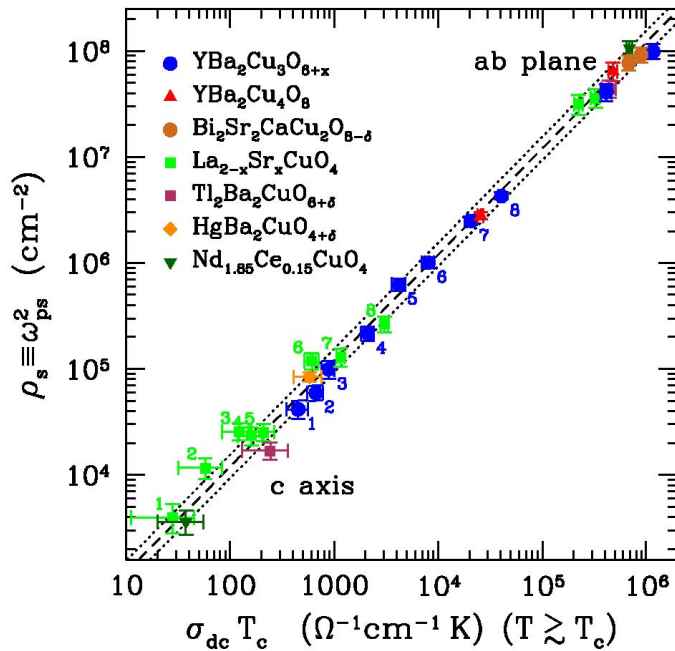
Material	l (Å)	λ (Å)	T_c (K)	V_0 (K)	T_{θ}^{\max}/T_c	Ref.
Pb	830	390	7	6×10^5	2×10^5	17
Nb ₃ Sn	60	640	18	2×10^4	2×10^3	18
UBe ₁₃	140	11,000	0.9	10^2	3×10^2	19, 20
LaMO ₆ S ₈	200	7,000	5	4×10^2	2×10^2	12, 21
B _{0.6} K _{0.4} BiO ₃	40	3,000	20	5×10^2	50	12
K ₃ C ₆₀	30	4,800	19	10^2	17	22, 23
(BEDT) ₂ Cu(NCS) ₂	15.2	8,000	8	15	1.7	24
Nd _{2-x} Ce _x Cu ₂ O _{4+δ}	6.0	1,000	21	4×10^2	16	25
Tl ₂ Ba ₂ CuO _{6+δ}	11.6	2,000	80	2×10^2	2	26, 27
	11.6	1,800	55	2×10^2	3.6	26, 27
Bi ₂ Sr ₂ CaCu ₂ O ₈	7.5	1,850	84	140	1.5	28, 29
Bi ₂ Pb _x Sr ₂ Ca ₂ Cu ₃ O ₁₀	5.9	1,850	105	110	0.9	28
	8.9	1,850	105	160	1.4	28
La _{2-x} Sr _x CuO _{4+δ}	6.6	3,700	28	30	1	30
	6.6	2,200	38	85	2	30
YBa ₂ Cu ₃ O _{7-δ}	5.9	1,600	92	145	1.4	31
YBa ₂ Cu ₄ O ₈	6.8	2,600	80	65	0.7	31

$$V_0 = \frac{(\hbar c)^2 a}{16\pi e^2 \lambda^2(0)}$$

$$T_{\theta}^{\max} \simeq V_0$$



Emery Kivelson 95



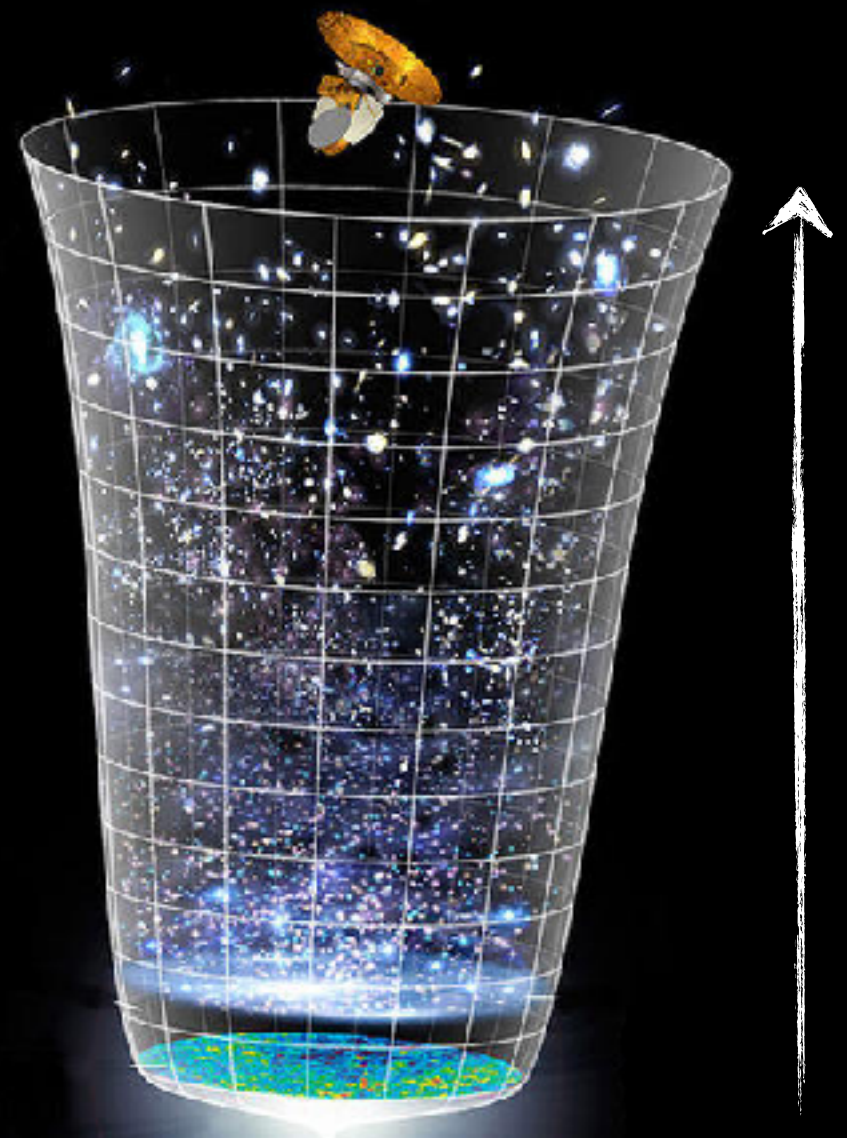
Uemura's plot

C. Holmes et al, 2004

Amplitude
Fluctuations ▶

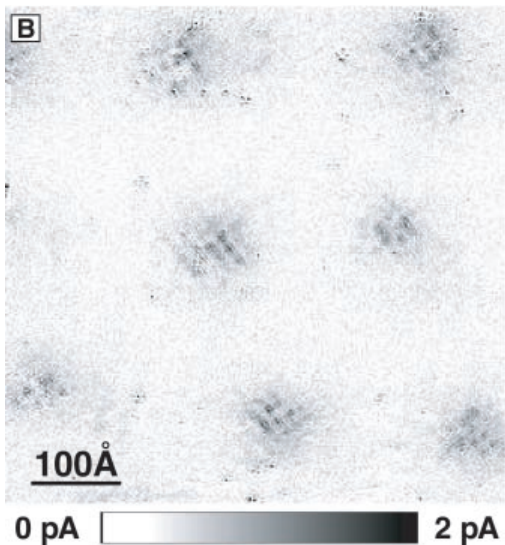
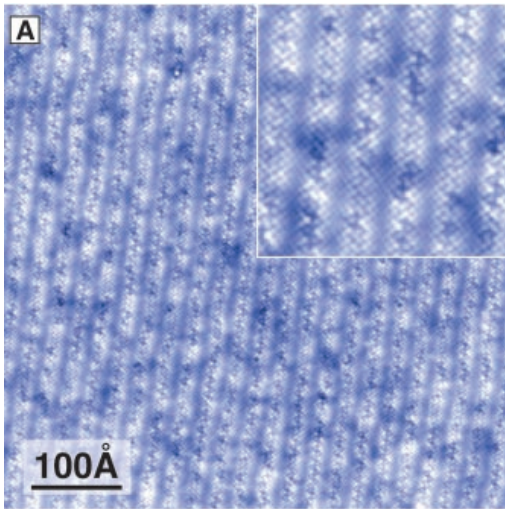
Phase
fluctuations ▶

Condensate ▶



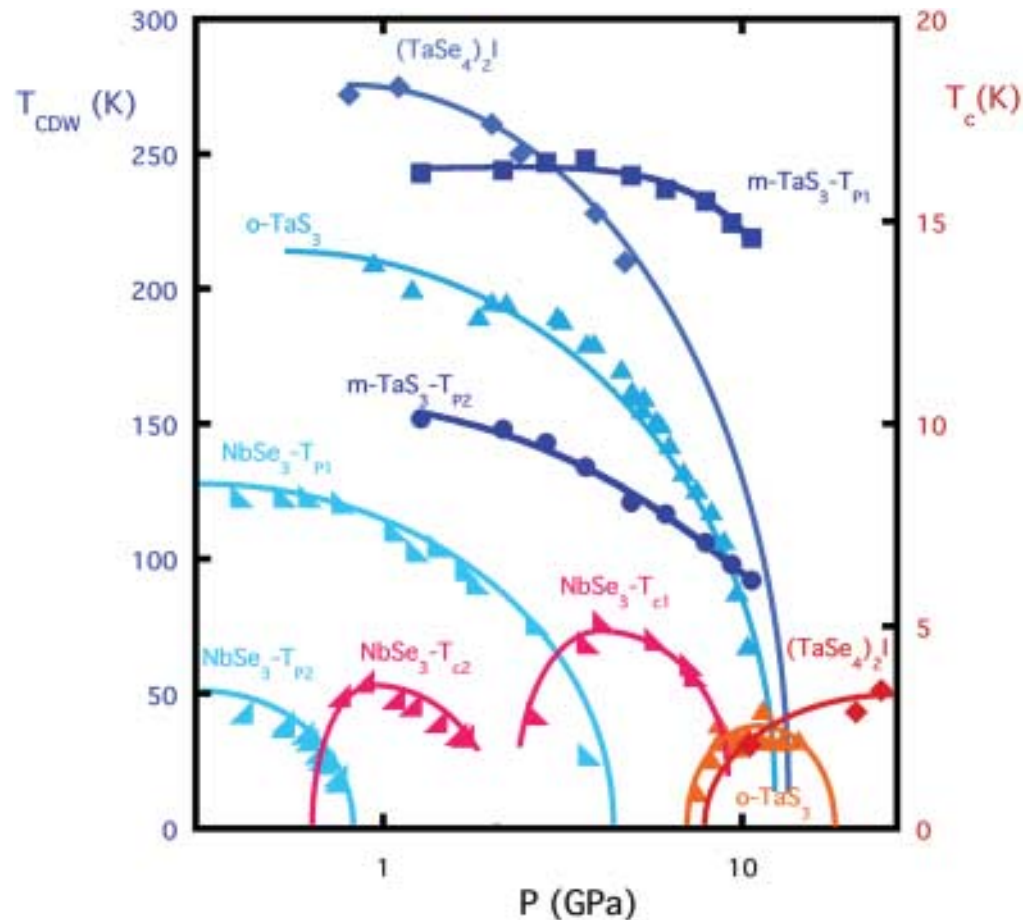
Presence of competing orders

Charge modulations in strong competition with SC state

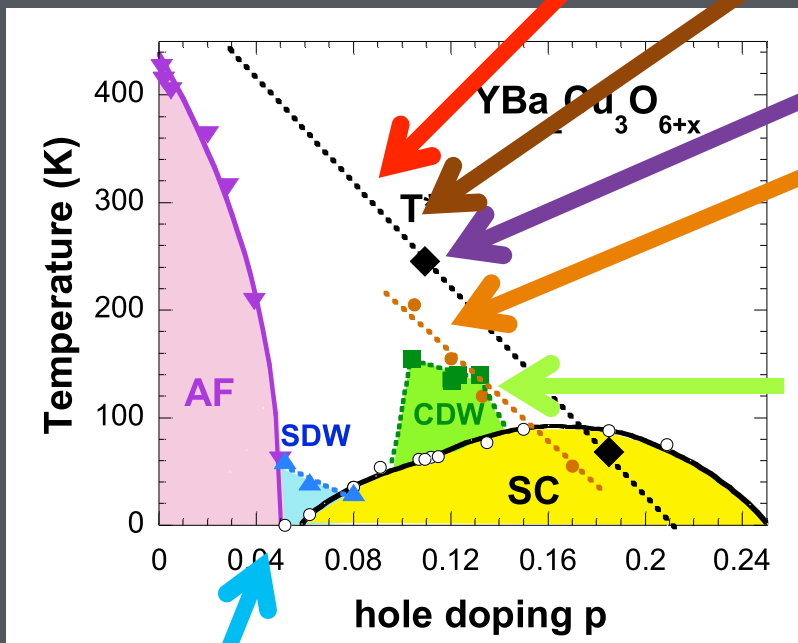


Hoffman, 2002

Kapitulnik, 2002



Charge order Landscape



- Nematicity
- Inversion symmetry
- loop currents

anomalous Kerr effect $T_k < T^*$

Xia, PRL 2008

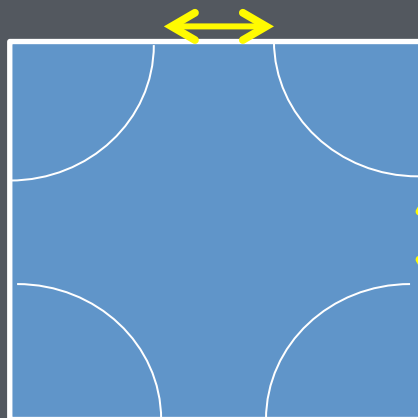
Incipient CDW – $T_m < T^*$

- $Q^* = (\delta, 0)$ and $(0, \delta)$ with $\delta \sim 0.3$

Chang, Nature Phys. 2012
Ghiringhelli, Science 2012

glassy SDW : $T_{SDW} \ll T^*$
(neutron, μ SR, RMN)

Haug, New J. Phys. 2010
T. Wu et al., PRB 2013



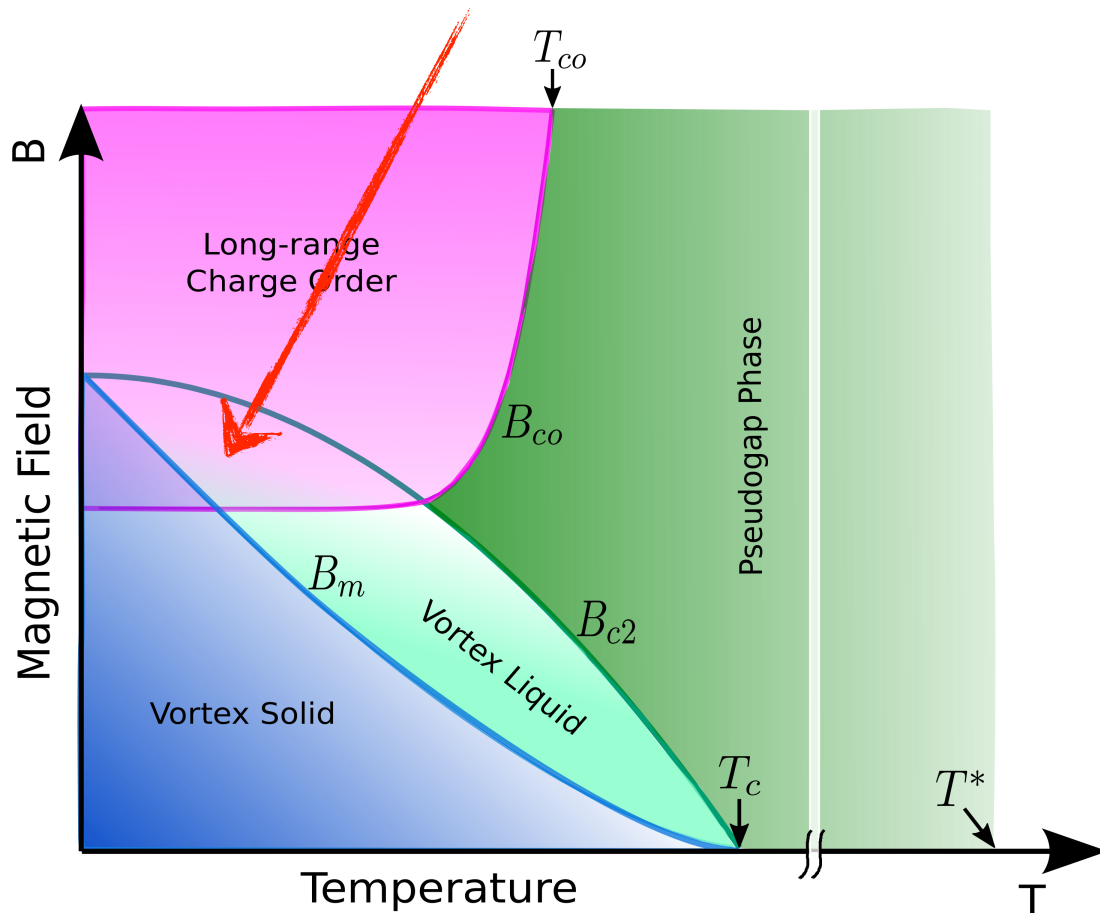
Stable CDW under magnetic field & Fermi surface reconstruction
(NMR, quantum oscillation, ultrasound)

D. LeBoeuf, Nature 2007.
T. Wu et al., Nature 2011.
D. LeBoeuf et al., Nature Physics 2011.

Quest for PDW in the phase diagram : is it observed, or maybe not ?

s-wave PDW or supersolid phase modulations
at 4 lattice sites

Coherent with STM (Hamidian et al. 2016)

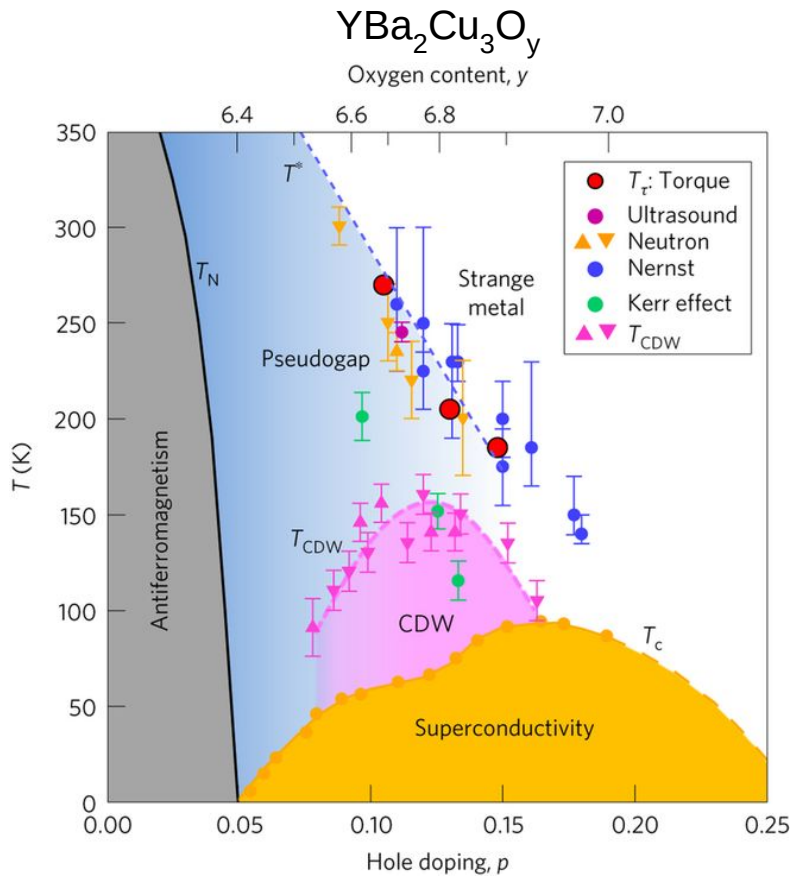


Field induced results
Show d-wave PDW
modulated
At 8 lattice spacings
Cf PA Lee's theory
(Edkins 2018)

So far X-ray didn't see
anything

Fractionalization of a PDW

The phase diagram



Slave-boson method :

$$c_{i,\sigma} = b_i f_{i,\sigma}^\dagger$$

Charge (holon)

Spin (spinon)

Constraint :

$$b_i b_i^\dagger + \sum_{\sigma} f_{i,\sigma} f_{i,\sigma}^\dagger = 1$$

Fictitious gauge transformation :

$$\begin{cases} f_{i\sigma} \rightarrow e^{i\theta} f_{i\sigma} \\ b_i \rightarrow e^{i\theta} b_i \end{cases}$$

Fractionalization of a Pair Density Wave

Modulated particle-particle pair : $\Delta_{ij}^{PDW} = \langle c_{i,\sigma} c_{j,\bar{\sigma}} e^{i\mathbf{Q}\cdot\mathbf{r}_{ij}} \rangle$

PDW fractionalization : $\Delta_{ij}^{PDW} = [\Delta_{ij}, \chi_{ij}^*]$

$$\Delta_{ij}^* \Delta_{ij} + \chi_{ij}^* \chi_{ij} = 1$$

Uniform particle-particle pair : $\Delta_{ij} = \langle c_{i,\sigma} c_{j,\bar{\sigma}} \rangle \longrightarrow$ Charge (2)

Modulated particle-hole pair : $\chi_{ij} = \langle c_{i,\sigma}^\dagger c_{j,\sigma} e^{i\mathbf{Q}\cdot\mathbf{r}_{ij}} \rangle \longrightarrow$ Translation symmetry

Phase transformation :

$$\begin{cases} \Delta_{ij} \rightarrow e^{i\theta} \Delta_{ij} \\ \chi_{ij} \rightarrow e^{i\theta} \chi_{ij} \end{cases}$$

Ansatz : $|PG\rangle = \left(\hat{\chi}_{ij} + \hat{\Delta}_{ij} \right) |0\rangle + \text{constraint}$

The phase diagram

Emerging gauge field : confining transition

$$S = \frac{1}{2} \int d^2x \sum_{a,b=1}^2 |\omega_{ab}|^2, \text{ with } \omega_{ab} = z_a \partial_\mu z_b - z_b \partial_\mu z_a,$$

$$z_1 = \Delta, z_2 = \chi, z_1^* = \Delta^*, z_2^* = \chi^*.$$

$$T = T^*$$

θ gets to fluctuate

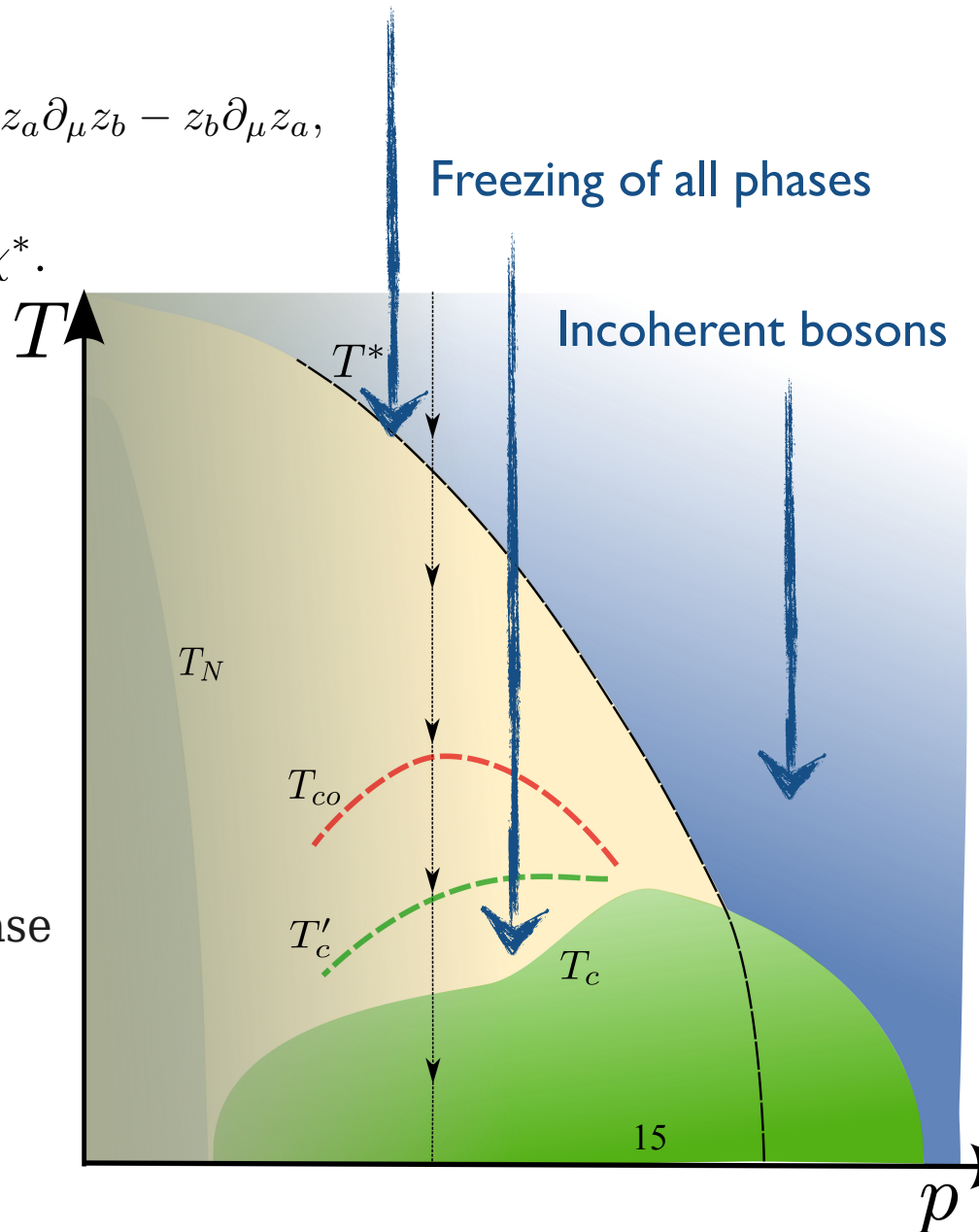
We obtain the constraint

$$|\Delta_{ij}|^2 + |\chi_{ij}|^2 = (E^*)^2$$

$$T = T_c$$

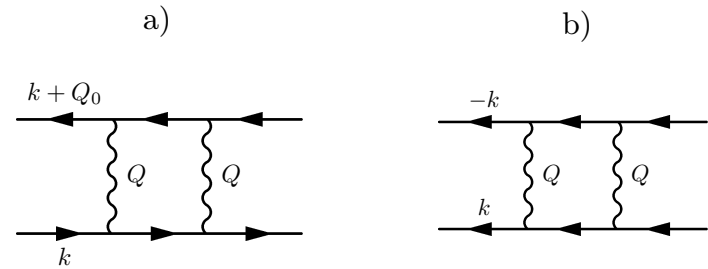
ϕ gets frozen and we have global phase coherence.

Meissner effect.



Why the system would want to do this ?

$$H = \sum_{i,j,\sigma} c_{i,\sigma}^\dagger t_{ij} c_{j,\sigma} + J \sum_{\langle i,j \rangle} \mathbf{S}_i \cdot \mathbf{S}_j + V \sum_{\langle i,j \rangle} n_i n_j$$



$$\chi_{ij} = \frac{1}{2} \langle c_{i\sigma}^\dagger c_{j\sigma} \rangle \quad \Delta_{ij}^* = \langle c_i^\dagger \uparrow c_j^\dagger \downarrow \rangle$$

Mean-field decoupling

$$\Delta_k = \sum_{\sigma} \sigma c_{k,\sigma} c_{-k,\bar{\sigma}}$$

$$\chi_k^Q = \sum_{\sigma} c_{k,\sigma}^\dagger c_{k+Q,\sigma}$$

$$\Psi_{ij} = (\hat{\Delta}_{ij}, \hat{\chi}_{ij})^t \quad |\Psi_{ij}| = E^*$$

Energy scales :

$$\Delta_k \sim 3J - V$$

$$\chi_k^Q \sim 3J + V$$

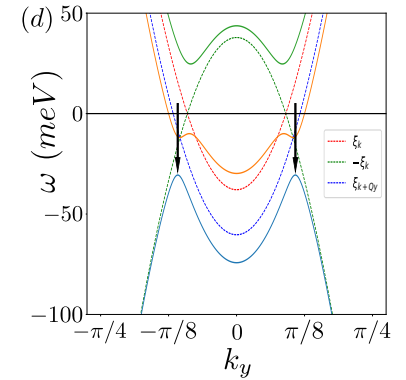
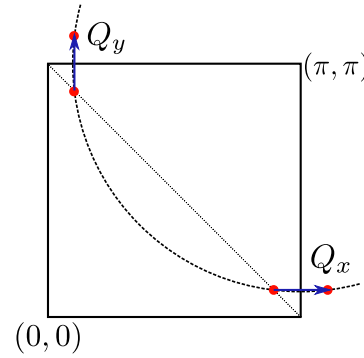
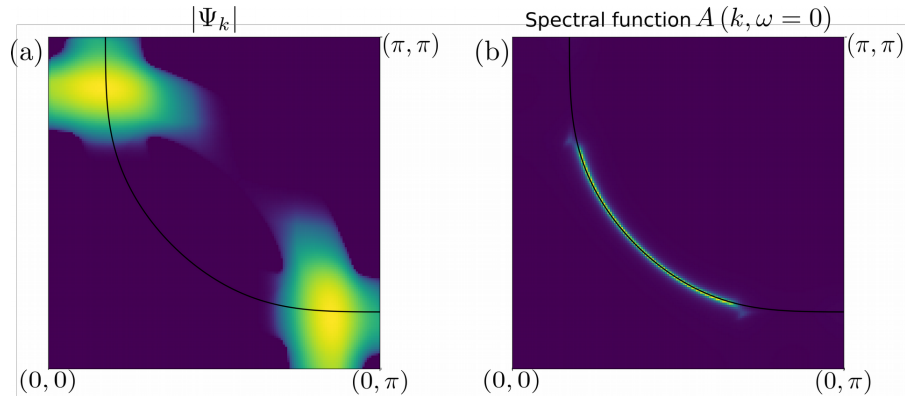
Condensation energy

$$E_{PG} = \frac{1}{2\tilde{J}} |\Psi_{k=k_F}|^2 = 0.017 \text{ eV},$$

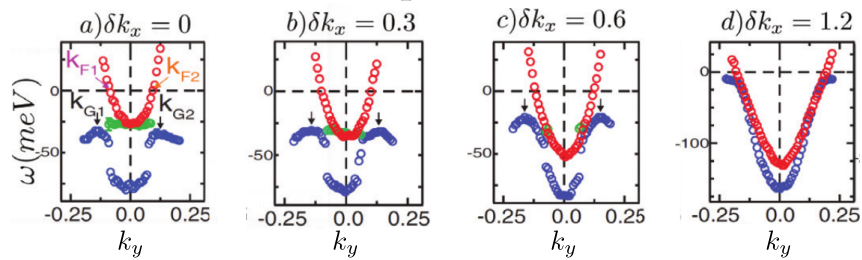
$$E_{SC} = \frac{1}{2J_-} |\Delta_{k=k_F}|^2 = 0.014 \text{ eV},$$

$$E_{CDW} = \frac{1}{2J_+} |\chi_{k=k_F}|^2 = 0.011 \text{ eV}.$$

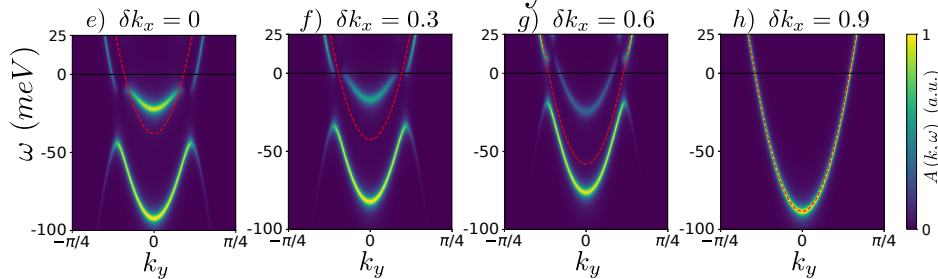
Opening a gap in the Fermi surface



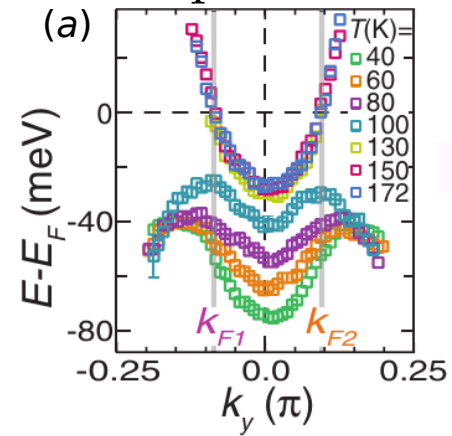
Experiment



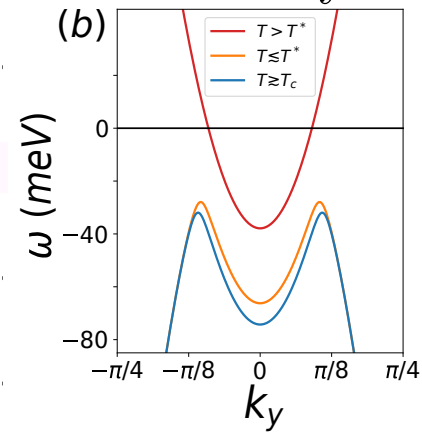
Theory



Experiment

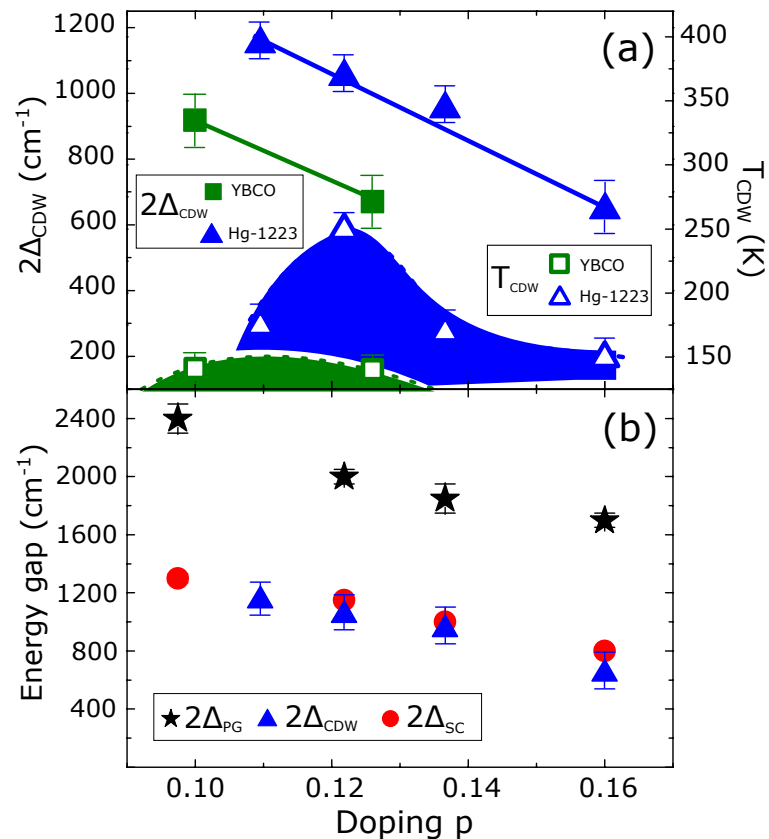
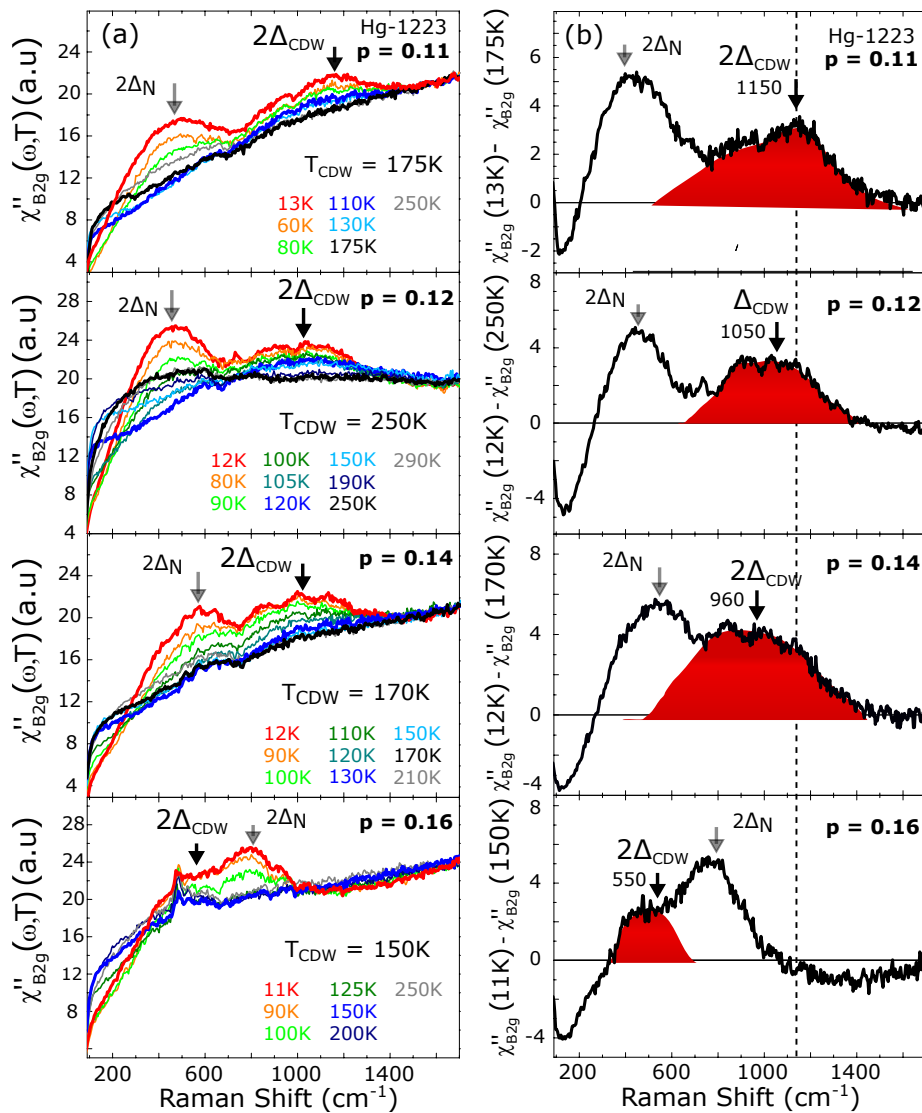
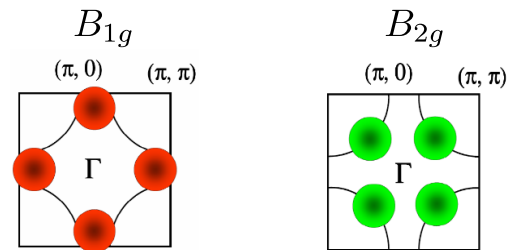


Theory



Raman Scattering B_{2g} , $T < T_{co}$

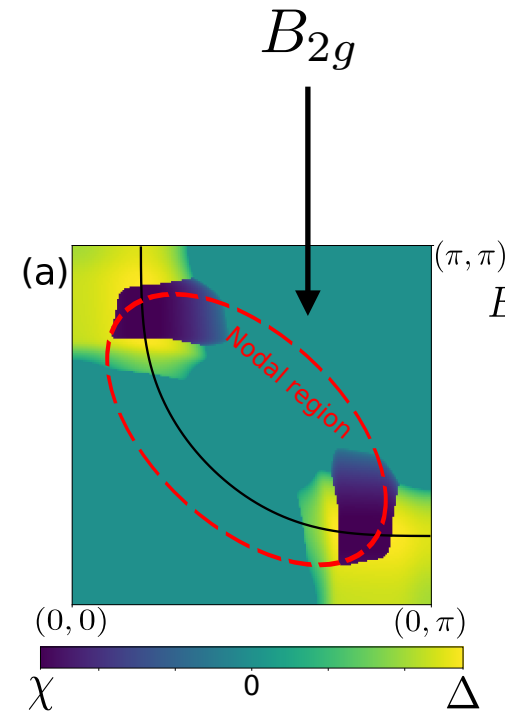
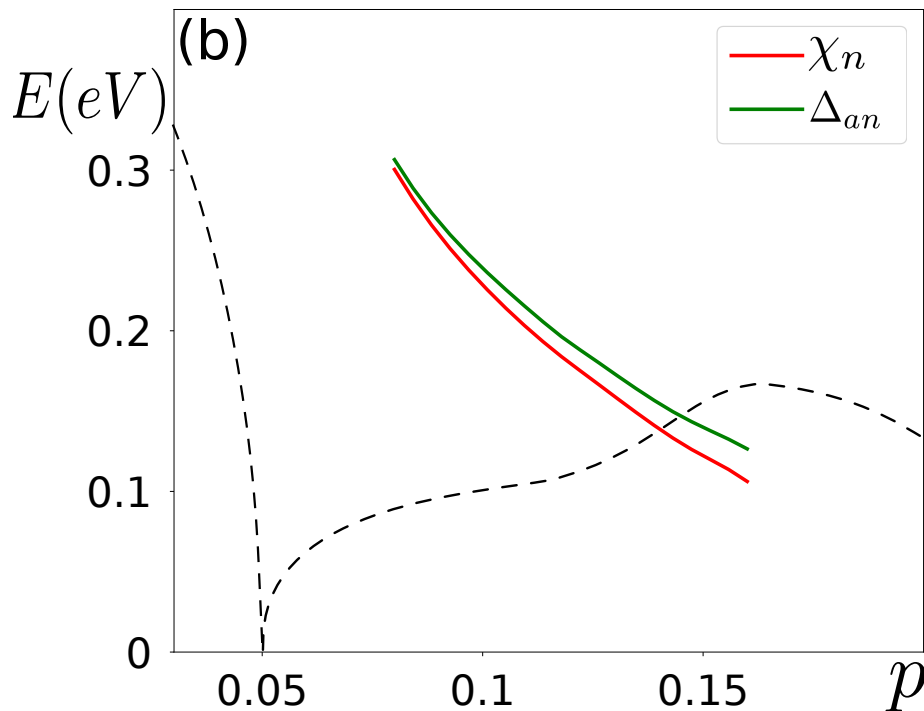
Loret et al. Nat. Physics (2019)



Solving gap equations

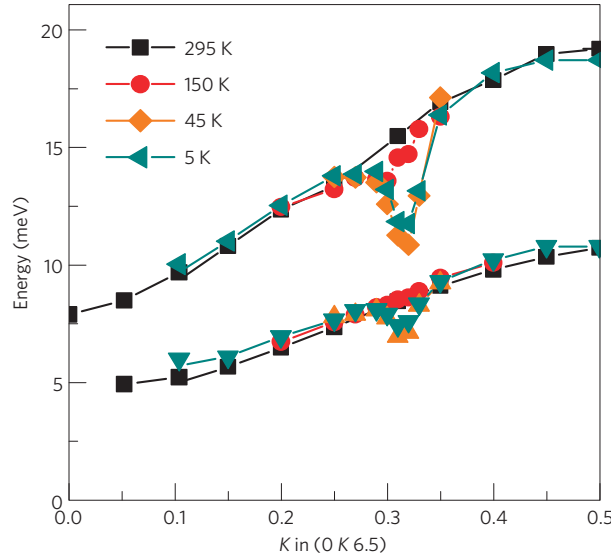
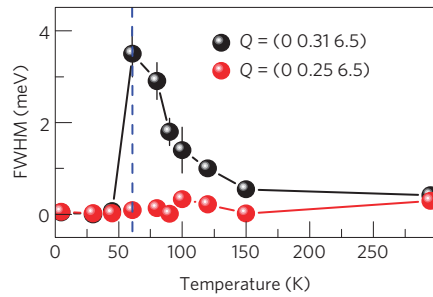
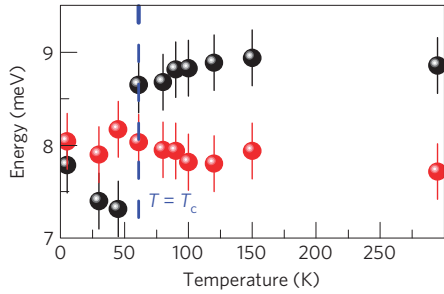
$$\Delta_{k,\omega} = -\frac{1}{\beta} \sum_{q,\Omega} \frac{J_-(q, \Omega) \Delta_{k+q}}{(\omega + \Omega)^2 - \xi_{k+q}^2 - \Delta_{k+q}^2},$$

$$\chi_{k,\omega} = -\frac{1}{\beta} \sum_{q,\Omega} \frac{J_+(q, \Omega) \chi_{k+q}}{(\omega + \Omega - \xi_{k+q})(\omega + \Omega - \xi_{k+Q+q}) - \chi_{k+q}^2},$$



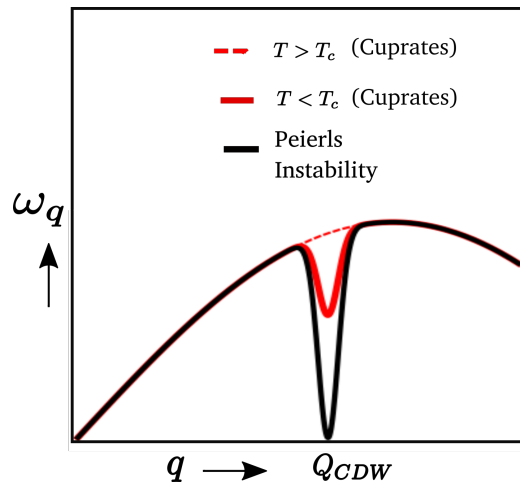
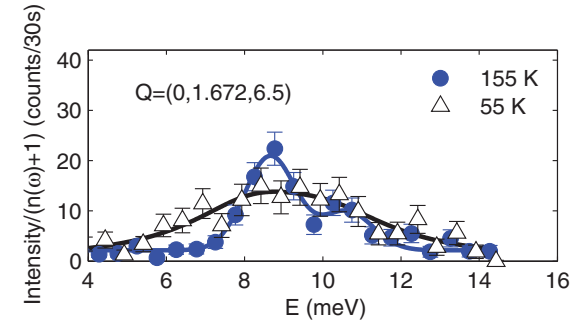
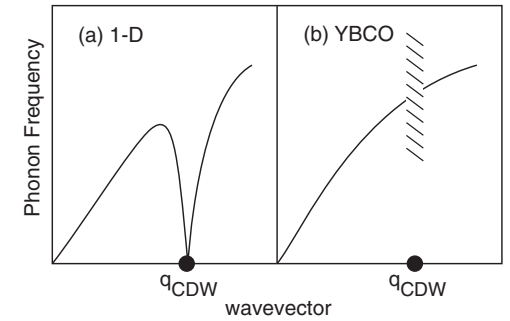
Same order of magnitude for
 Δ and χ

Anomalous softening of phonons

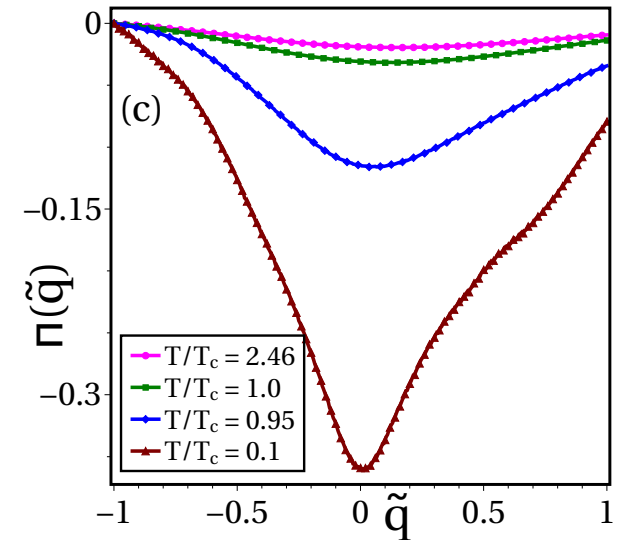


Le Tacon, 2013

Blackburn, 2013



- *Phases lock at T_c*
- *Fluct. Quench at T_c*



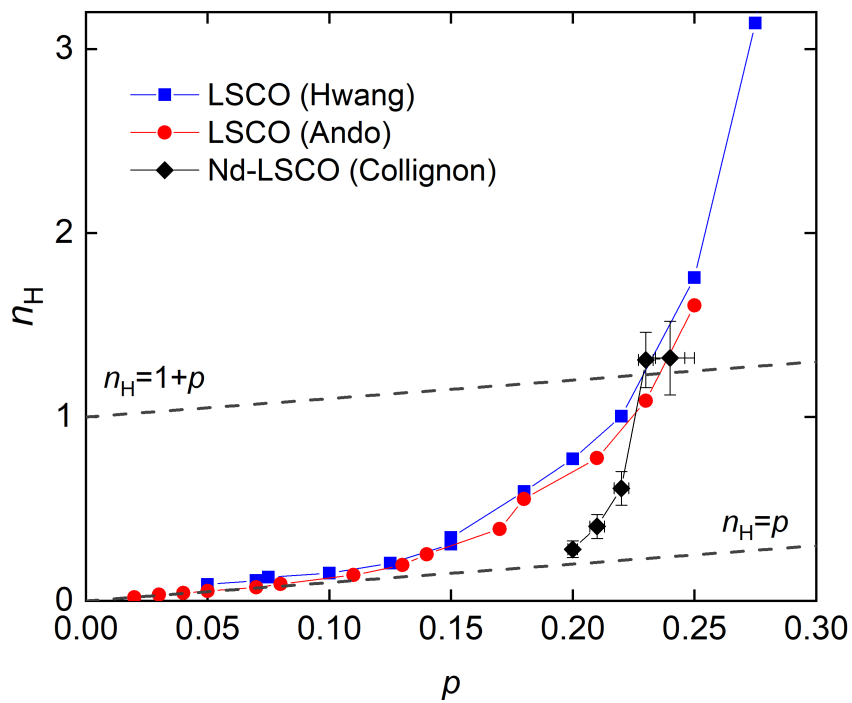
S. Sarkar et al. (2020)

Transport in the Strange Metal

Recent controversy

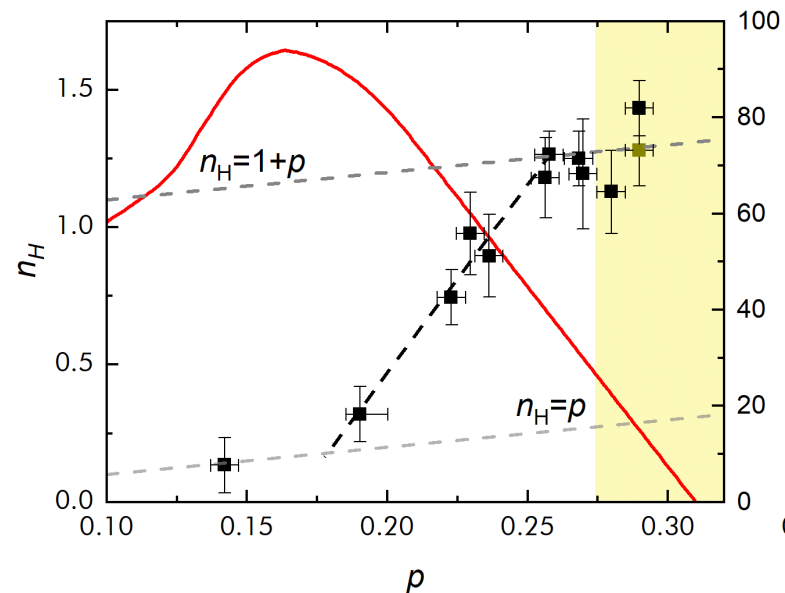
Spectral weight missing in the Strange Metal regime?

Another type of carrier?

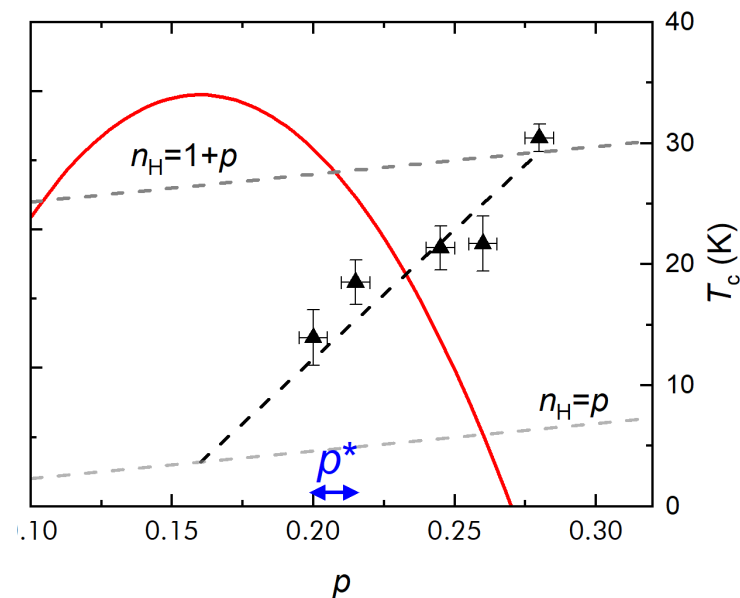


Prutzke et al. 2019

Tl2201

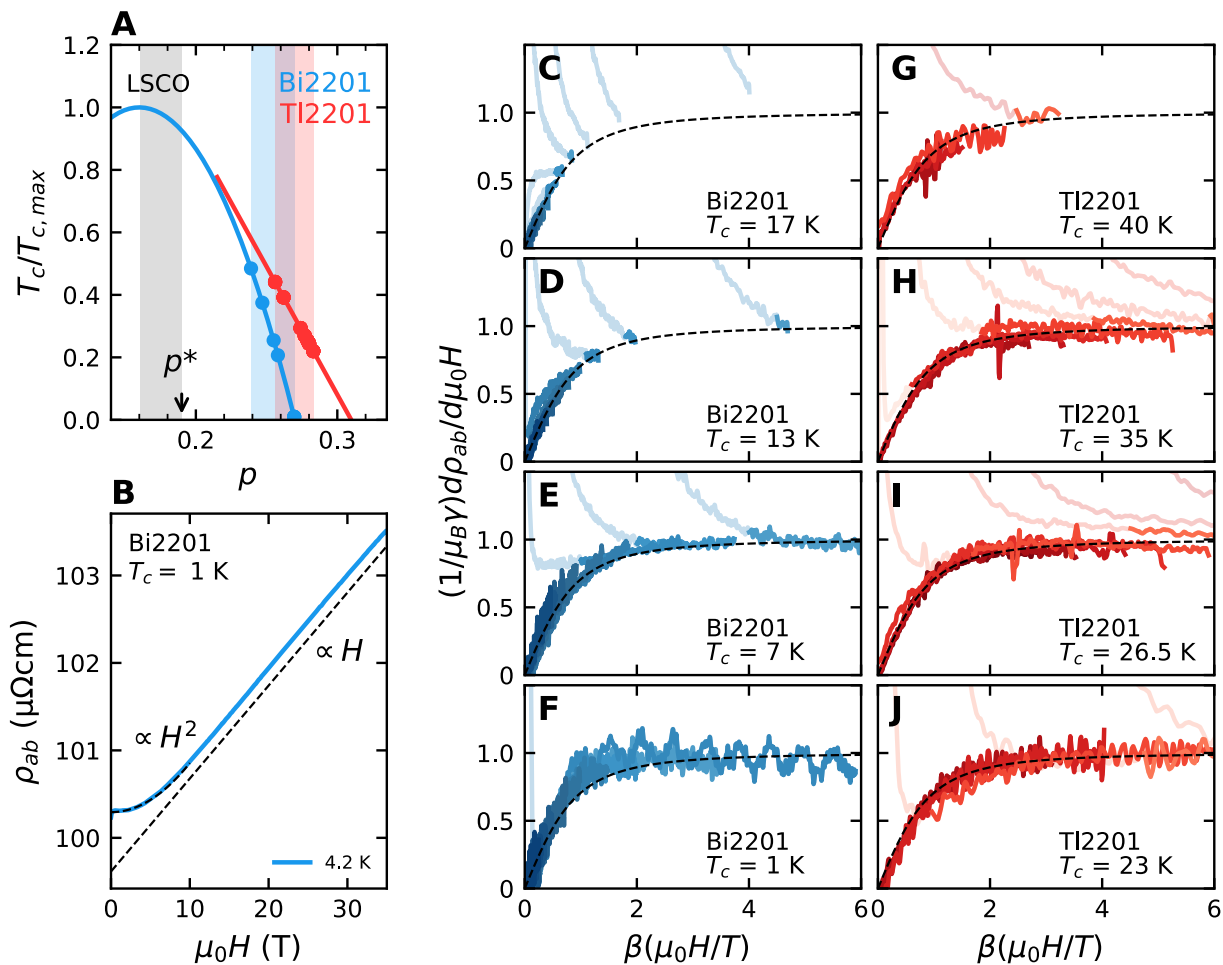


Bi2201



\mathcal{H}/T scaling in the SM phase

$$\rho(H, T) - \rho(0, 0) = \sqrt{(\alpha k_B T)^2 + (\gamma \mu_B \mu_0 H)^2}$$

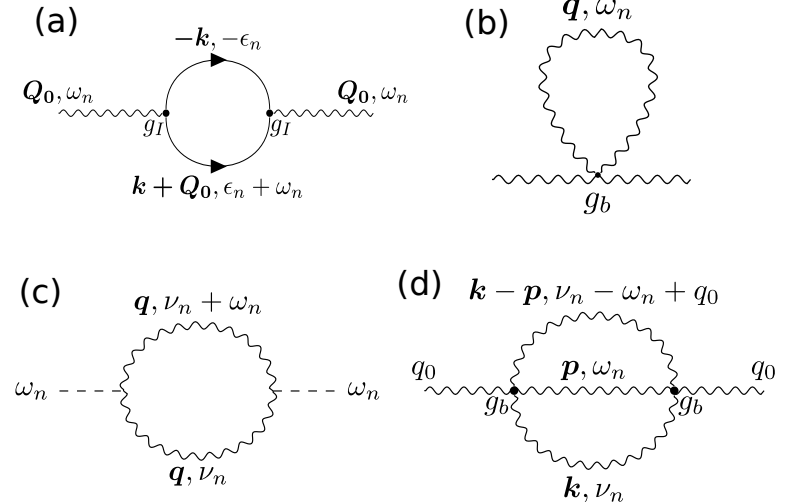
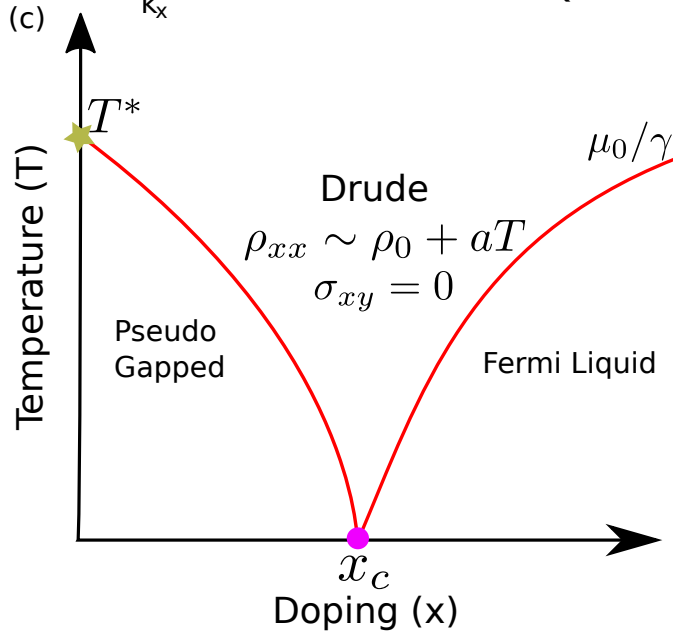
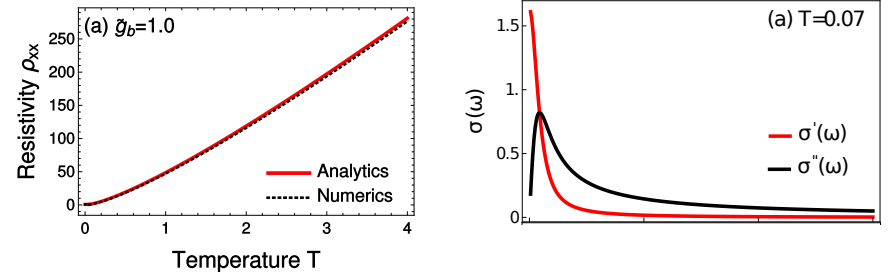
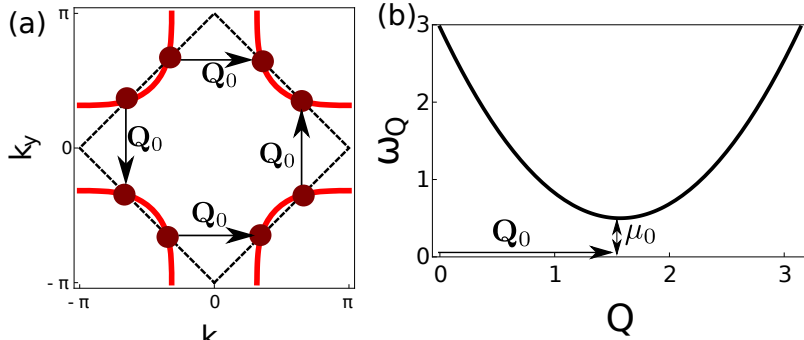


- *Isotropic*
- *Incoherent*
- $\sigma_{xy} = 0$
- *Planckian limit*

Our proposal: Charged bosons in the Strange Metal phase

$$D^{-1}(\mathbf{q}, i\omega_n) = \gamma |\omega_n| + \mathbf{q}^2 + \mu(T)$$

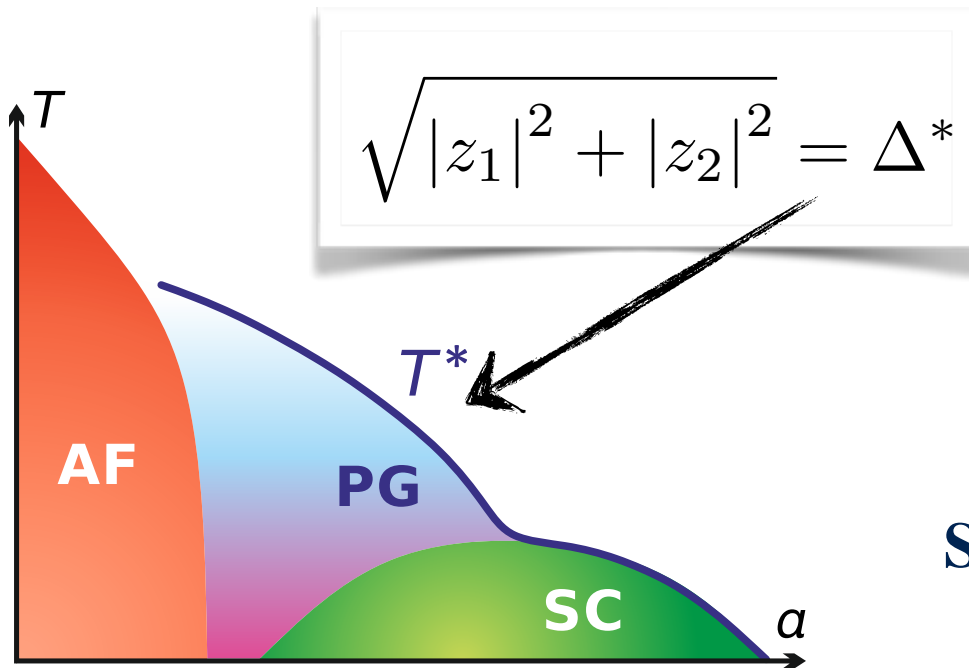
$$\sigma_{xx}(i\omega \rightarrow \omega + i\delta) = \frac{\sigma_0^b \tau}{\left(1 - i\frac{\gamma\omega}{2\mu}\right)},$$



Analogy with $SU(2)$ emergent symmetry

Eight hot spots, attractive Hubbard model at 1/2 filling... and beyond ?

$$\psi = (z_1, z_2) \quad \mathcal{L}_{CP^1} = \frac{1}{2g} |D_\mu \psi|^2 + V(\psi)$$



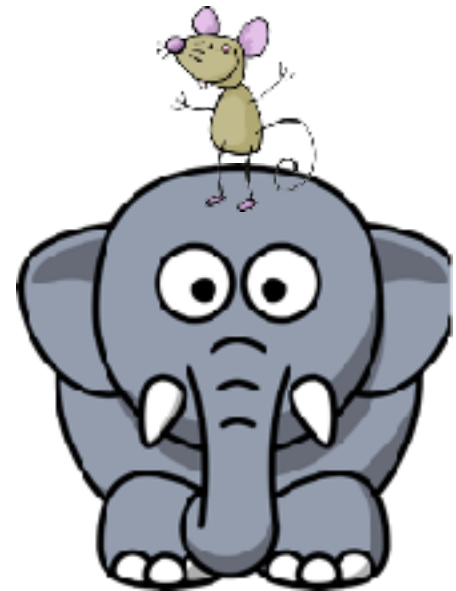
$$\psi \rightarrow e^{i\theta} \psi$$

$SU(2)$ chiral model protected by a Pseudo Spin Higgs mechanism !

Sachdev et al (2013)
Efetov, Meier, CP (2013)

Conclusions

- Charge orders are a key players in cuprate physics: natural competitor of superconductivity
- For the first time observation of a precursor in the charge channel (as well as in the SC channel), which follow T^* , not T_c or T_{co}
- New idea of fractionalizing a PDW or a more complex boson
- Entangling particle-hole and particle-particle pairs at T^*
- Explains recent Raman and phase coherence in STM
- ARPES : back-bending, poles in self-energy (cf. DMFT studies)
- Can a charge-2 boson explain the mystery of strange metal and Hall resistivity ?



Discussions of the data and a few Refs

Yvan Sidis, J. C. Séamus Davis, Mohammad Hamidian,

Alain Sacuto, Henri Alloul, Nigel Hussey

[Anurag Banerjee](#), [Maxence Grandadam](#), [Hermann Freire](#), [Catherine Pépin](#) [arXiv:2009.09877](#)

[Saheli Sarkar](#), [Maxence Grandadam](#), [Catherine Pépin](#) [arXiv:2009.02975](#)

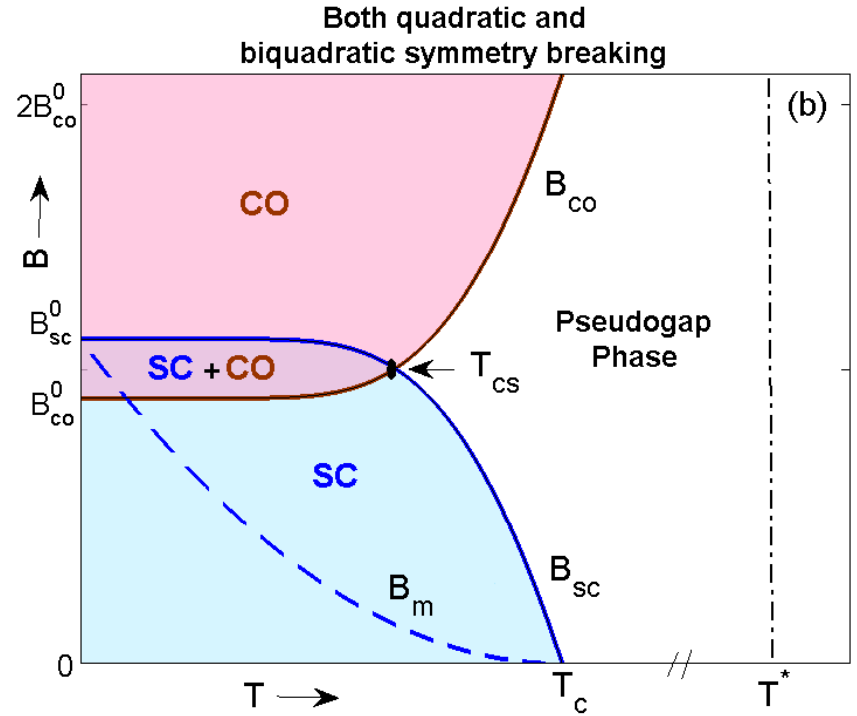
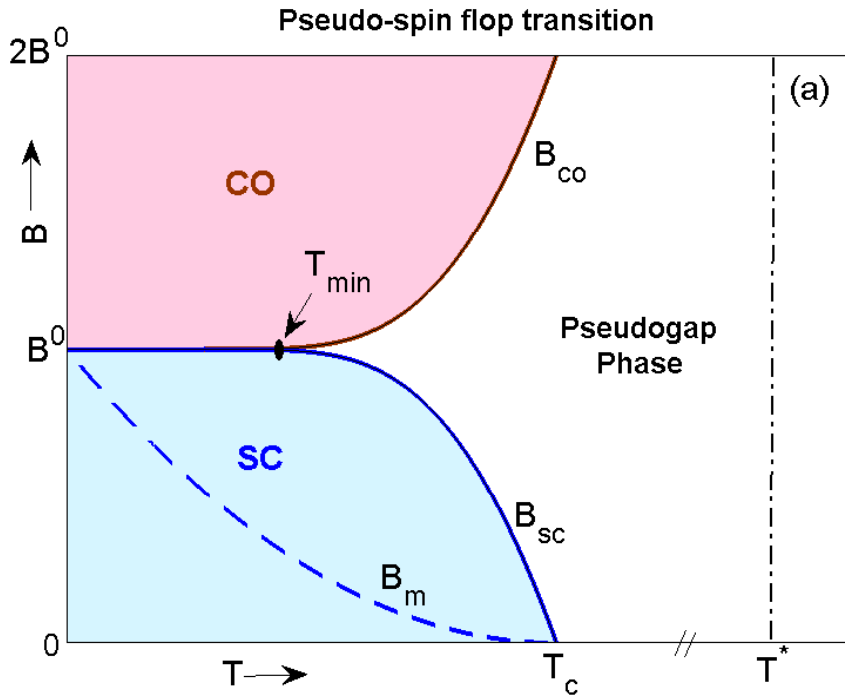
[Maxence Grandadam](#), [Debmalya Chakraborty](#), [Xavier Montiel](#), [Catherine Pépin](#) [arXiv:2002.12622](#)

[D. Chakraborty](#), [M. Grandadam](#), [M. H. Hamidian](#), [J. C. S. Davis](#), [Y. Sidis](#), [C. Pépin](#) [arXiv:1906.01633](#)

[Saheli Sarkar](#), [Debmalya Chakraborty](#), [Catherine Pépin](#) [arXiv:1906.08280](#)

[C. Pépin](#), [D. Chakraborty](#), [M. Grandadam](#), [S. Sarkar](#) [arXiv:1906.10146](#)

O(3) Non Linear Sigma Model

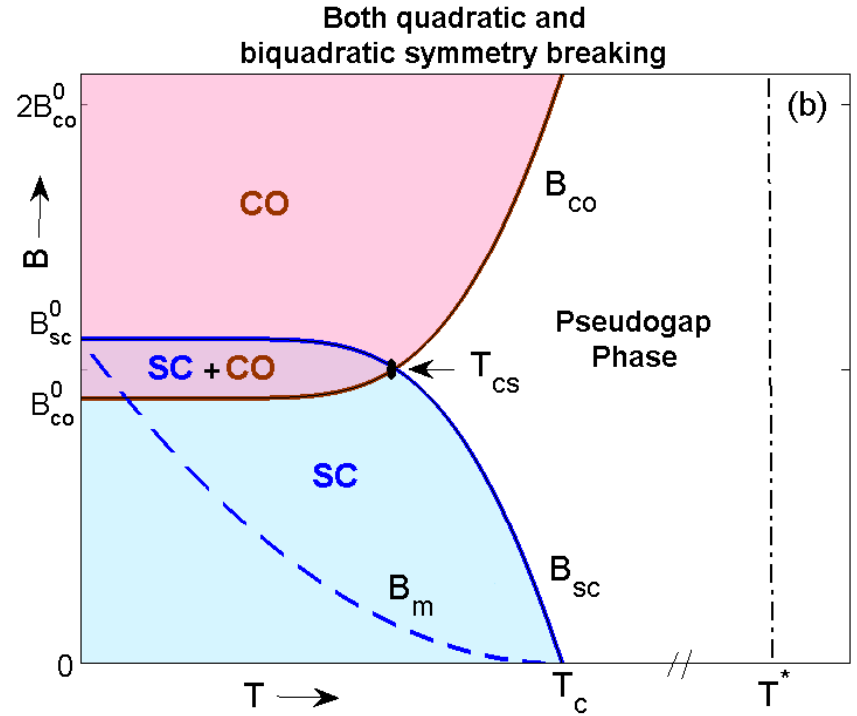
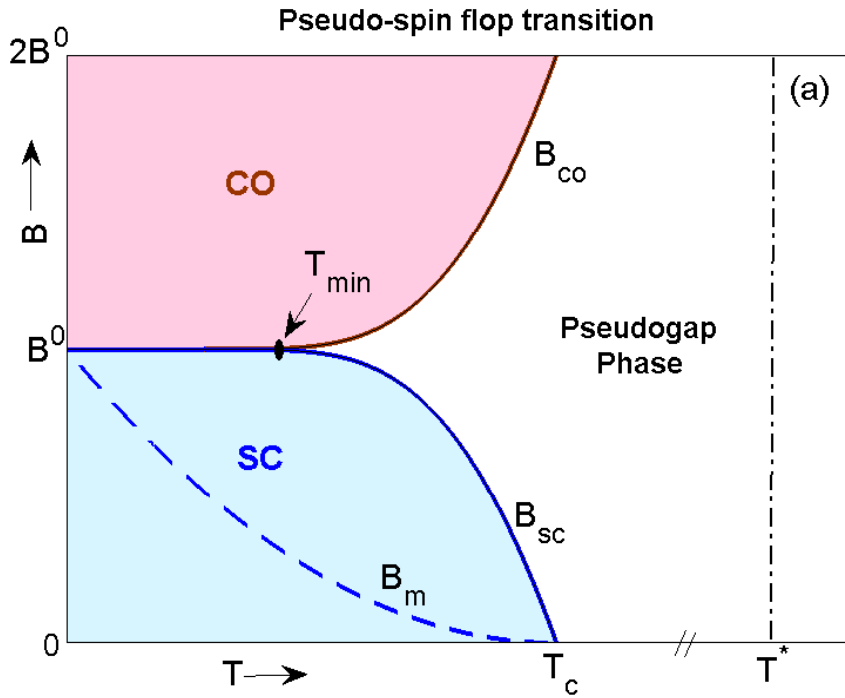


$$\frac{F}{T} = \frac{1}{t_0} \int \text{tr}[\nabla u^\dagger \nabla u + \kappa_0 \tau_3 u^\dagger \tau_3 u] dR$$

$$\frac{F_{bq}}{T} = \frac{1}{t_0} \int z_0 \left\{ (\text{tr}[\tau_3 u^\dagger \tau_3 u])^2 - 1 \right\} dR$$

D. Chakraborty et al. PRB (2018)

O(3) Non Linear Sigma Model



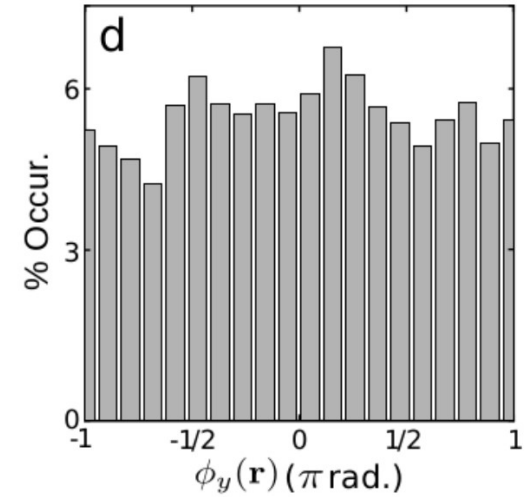
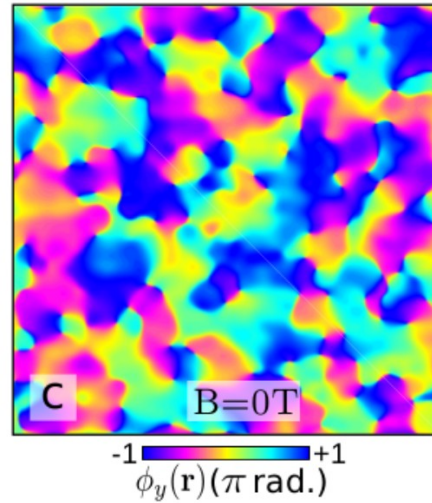
$$\frac{F}{T} = \frac{1}{t_0} \int \text{tr}[\nabla u^\dagger \nabla u + \kappa_0 \tau_3 u^\dagger \tau_3 u] dR$$

$$\frac{F_{bq}}{T} = \frac{1}{t_0} \int z_0 \left\{ (\text{tr}[\tau_3 u^\dagger \tau_3 u])^2 - 1 \right\} dR$$

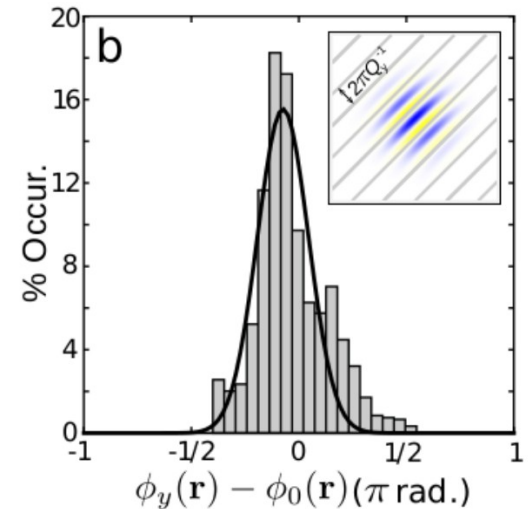
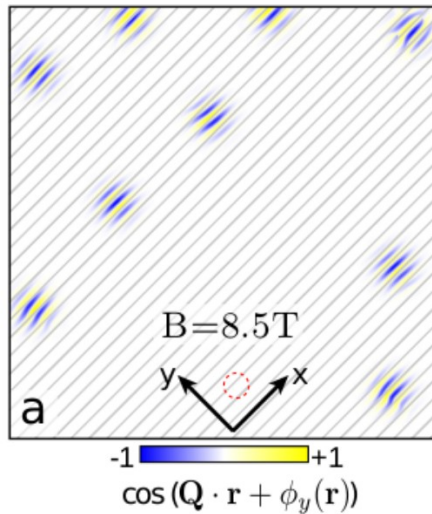
D. Chakraborty et al. PRB (2018)

STM measurement of charge density modulation : $Re(\chi_{ij}) = \hat{d}|\chi_{ij}|\cos(\mathbf{Q} \cdot \mathbf{r} + \phi(\mathbf{r}))$

$B = 0 T$ random phase distribution :

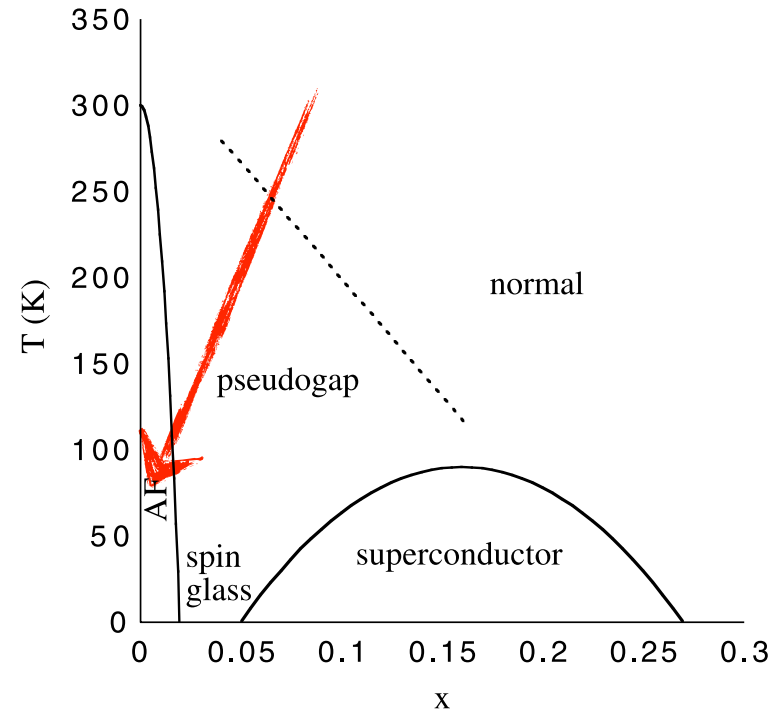
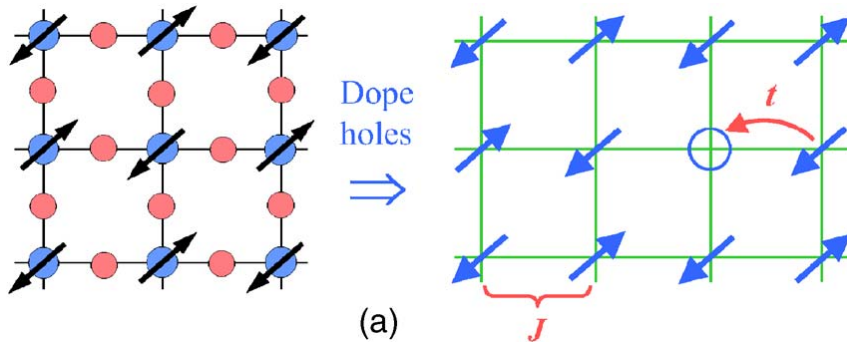


$B \neq 0 T$ centered distribution :



The context of strong coupling : doping a Mott insulator

Resonating Valence Bond (RVB)



$$H = P \left[- \sum_{\langle ij \rangle, \sigma} t_{ij} c_{i\sigma}^\dagger c_{j\sigma} + J \sum_{\langle ij \rangle} (\mathbf{S}_i \cdot \mathbf{S}_j - \frac{1}{4} n_i n_j) \right] P$$

Anderson, Lee, Nagaosa, Rice etc...

P: projection on no double occupancy

^{89}Y NMR Evidence for a Fermi-Liquid Behavior in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$

H. Alloul, T. Ohno,^(a) and P. Mendels

Physique des Solides, Université de Paris-Sud, 91405 Orsay, France

(Received 15 May 1989)

We report NMR shift ΔK and T_1 data of ^{89}Y taken from 77 to 300 K in $\text{YBa}_2\text{Cu}_3\text{O}_{6+x}$ for $0.35 < x < 1$, from the insulating to the metallic state. A Korringa law and therefore a Fermi-liquid picture is found to apply for the spin part K_s of ΔK . The spin contribution $\chi_s(x, T)$ to χ_m is singled out, as the T variation of ΔK scales linearly with the macroscopic susceptibility χ_m . This implies that $\text{Cu}(3d)$ and $\text{O}(2p)$ holes do not have independent degrees of freedom. Their hybridization, which has a σ character, hardly varies with doping. These results put severe constraints on theoretical models of high- T_c cuprates.

PACS numbers: 74.70.Vy, 75.20.En, 76.60.Cq, 76.60.Es

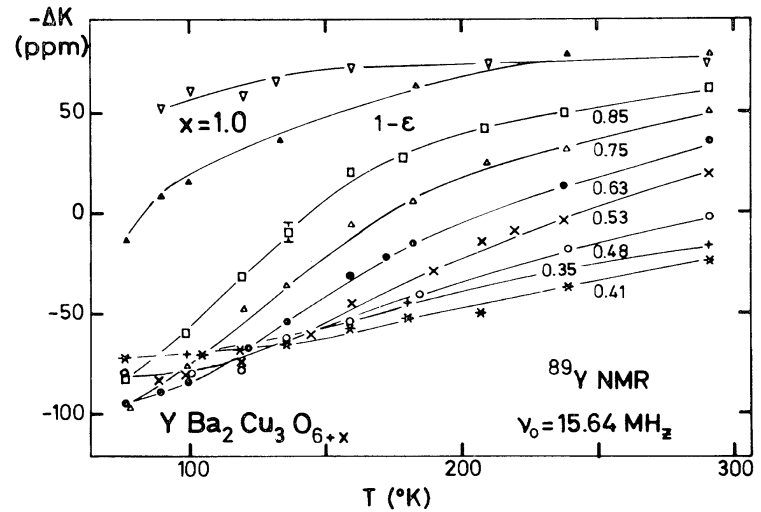
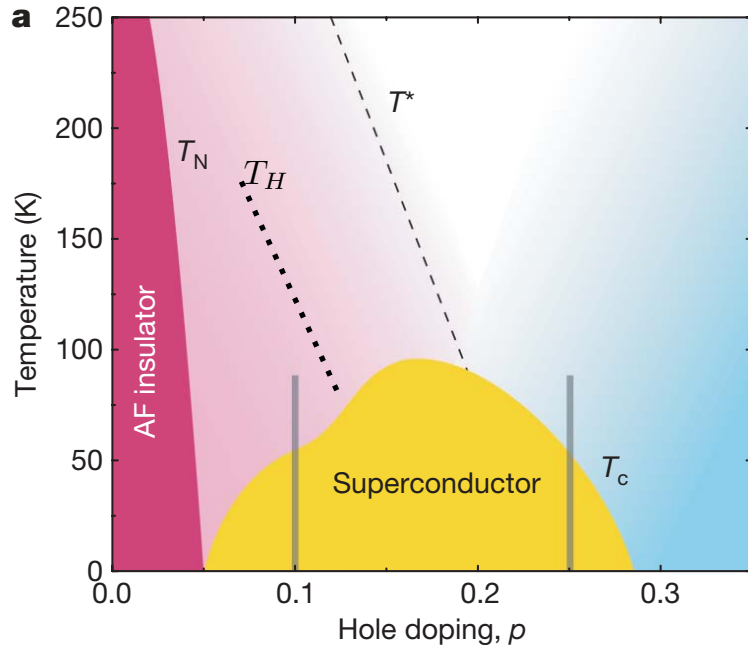
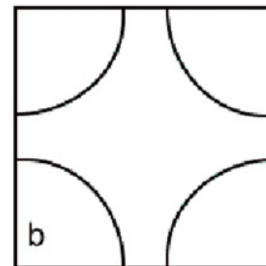
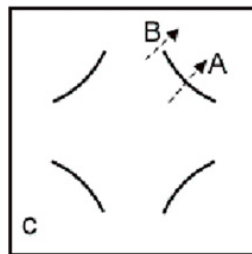
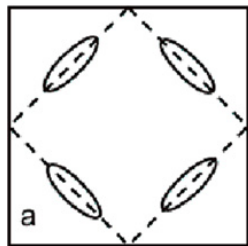
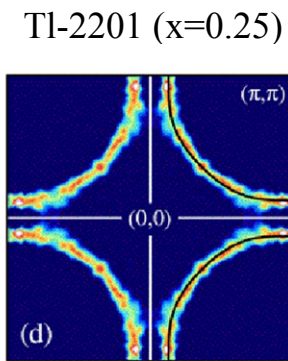
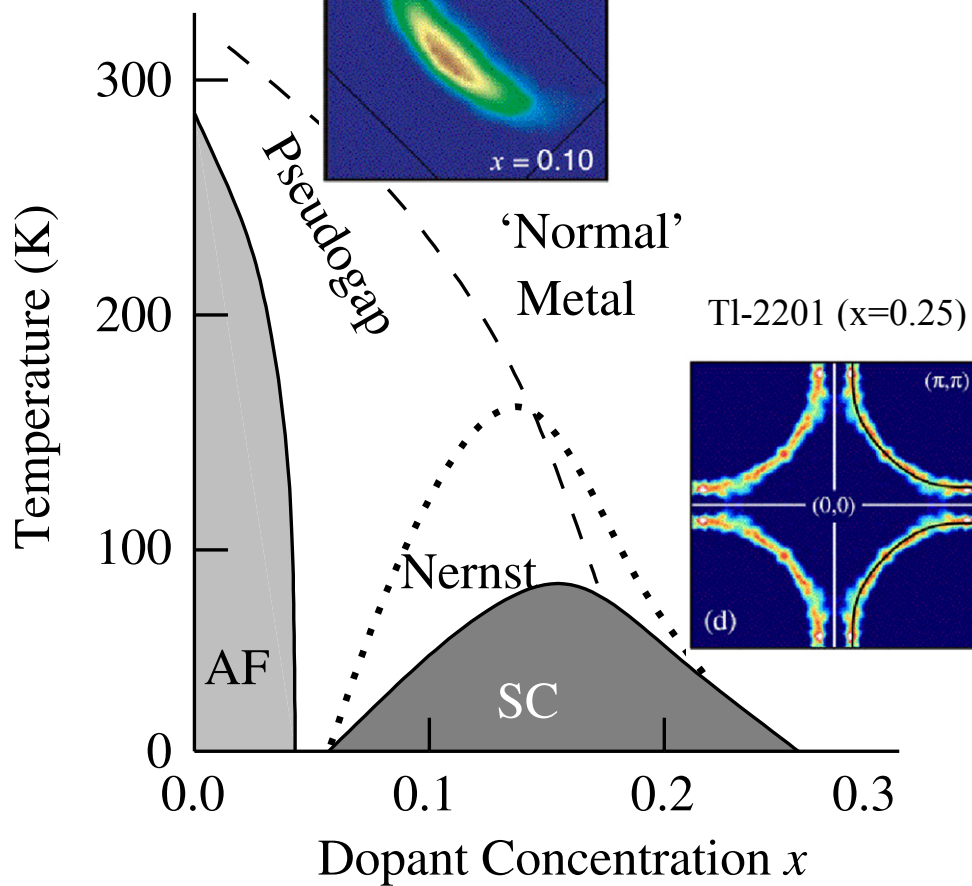
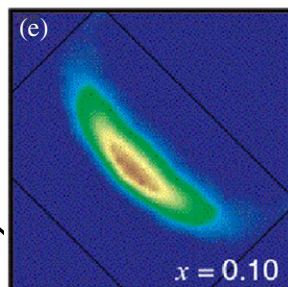


FIG. 1. The shift ΔK of the ^{89}Y line, referenced to YCl_3 plotted vs T , from 77 to 300 K. The lines are guides to the eye.



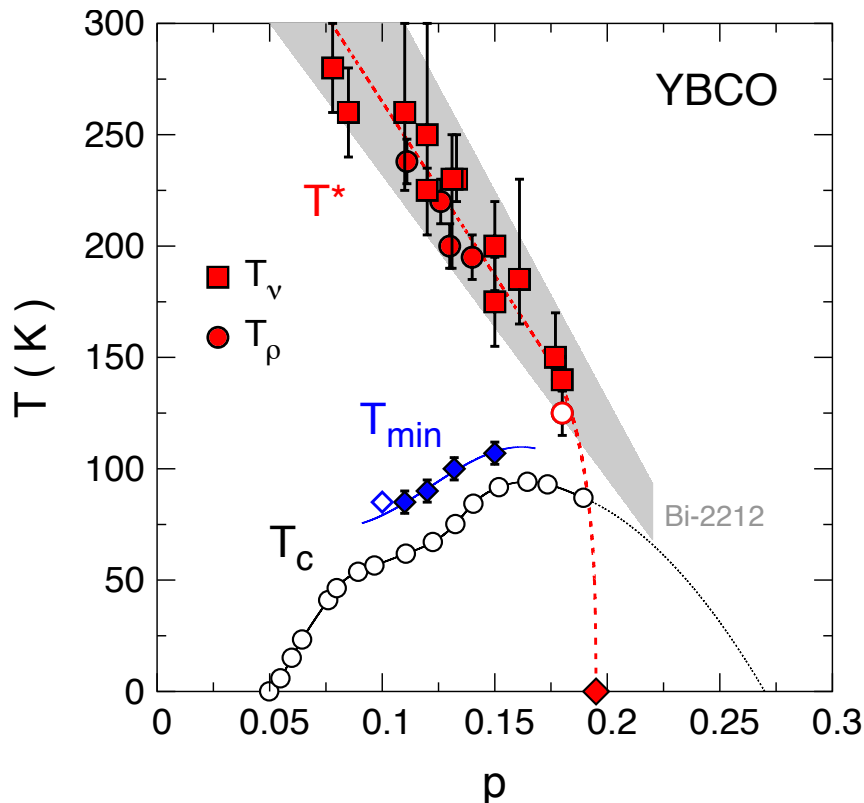
NaCOCl ($x=0.1$)



The extend of the Cooper pairs **phase fluctuations** regime
 Nernst effect (Ong, Behnia), transport (Rullier-Albenque,
 Sebastian), Squid spectroscopy (Lesueur)...

The presence of a partner to SC pairing inhibits the
 visibility of phase fluctuations in transport and Nernst
 effect (Orgard, 2017)

Cyr-Choignière et al , (2017)



Hsu et al , (2017)

