

# Pinning the cosmic web to massive halos

Joanne Cohn

# Web tracer here: dark matter density

## Web finder: Disperse

Dark matter density in the Millennium simulation (Springel++05,Lemson++06)

N-body, 500 Mpc/h side box

Fixed time,  $z \sim 0.1$

Specifically using from it:

- Dark matter densities in  $256^3$  **pixels** (1.95 Mpc/h each)
- Gaussian smoothing 1.25 Mpc/h, 2 Mpc/h 2.5 Mpc/h, 5 Mpc/h

(Drawback) **old** Millennium cosmology:

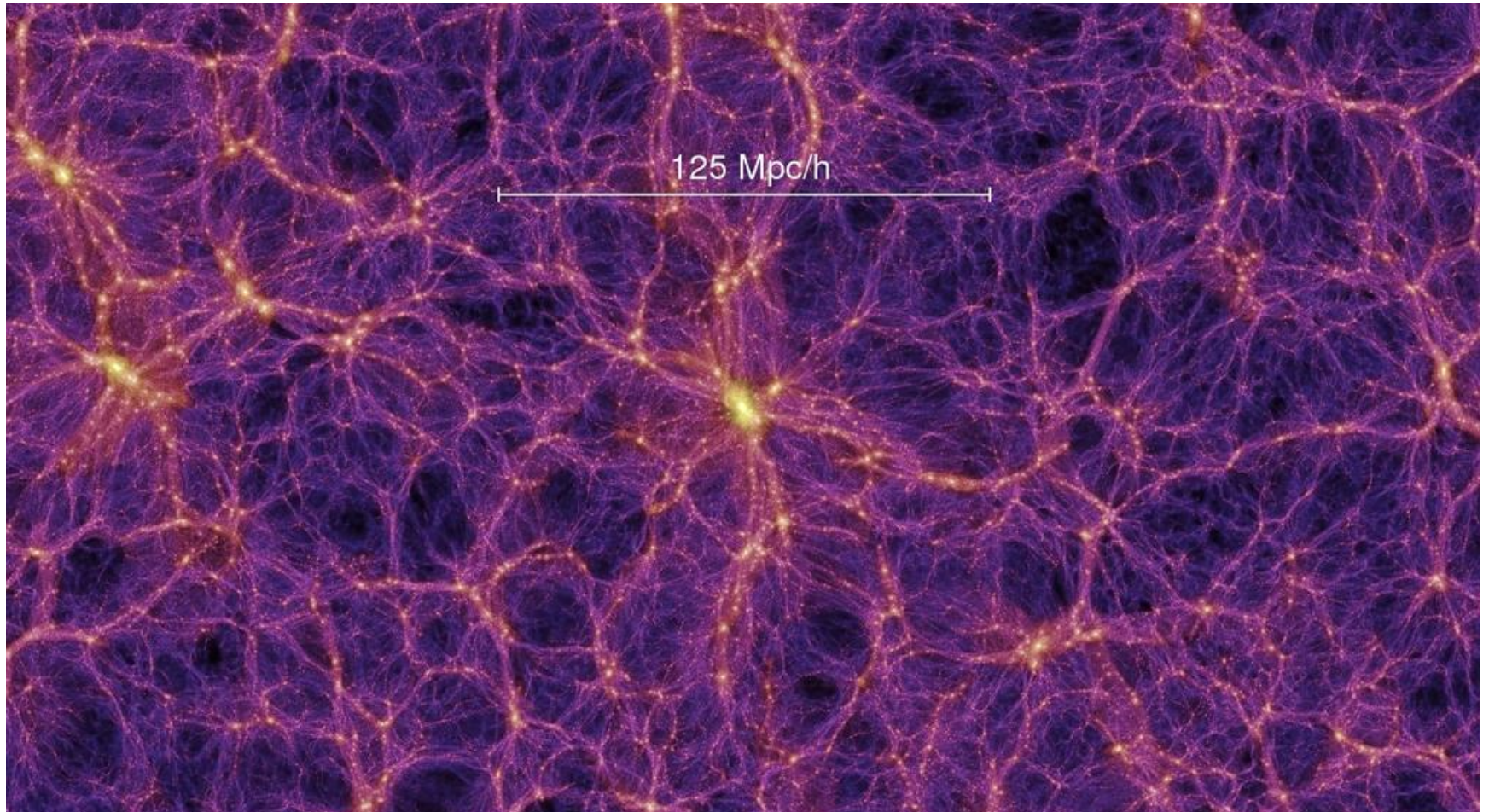
density rescaling to Planck Millennium unavailable, thus relevant galaxy observables unavailable. 😞

( $\Omega_m = 0.25$ ,  $\Omega_b = 0.045$ ,  $h = 0.73$ ,  $n=1$ ,  $\sigma_8 = 0.9$ )

Lengths < than **pixel scale** ( $\sim 2$  Mpc/h) not well described

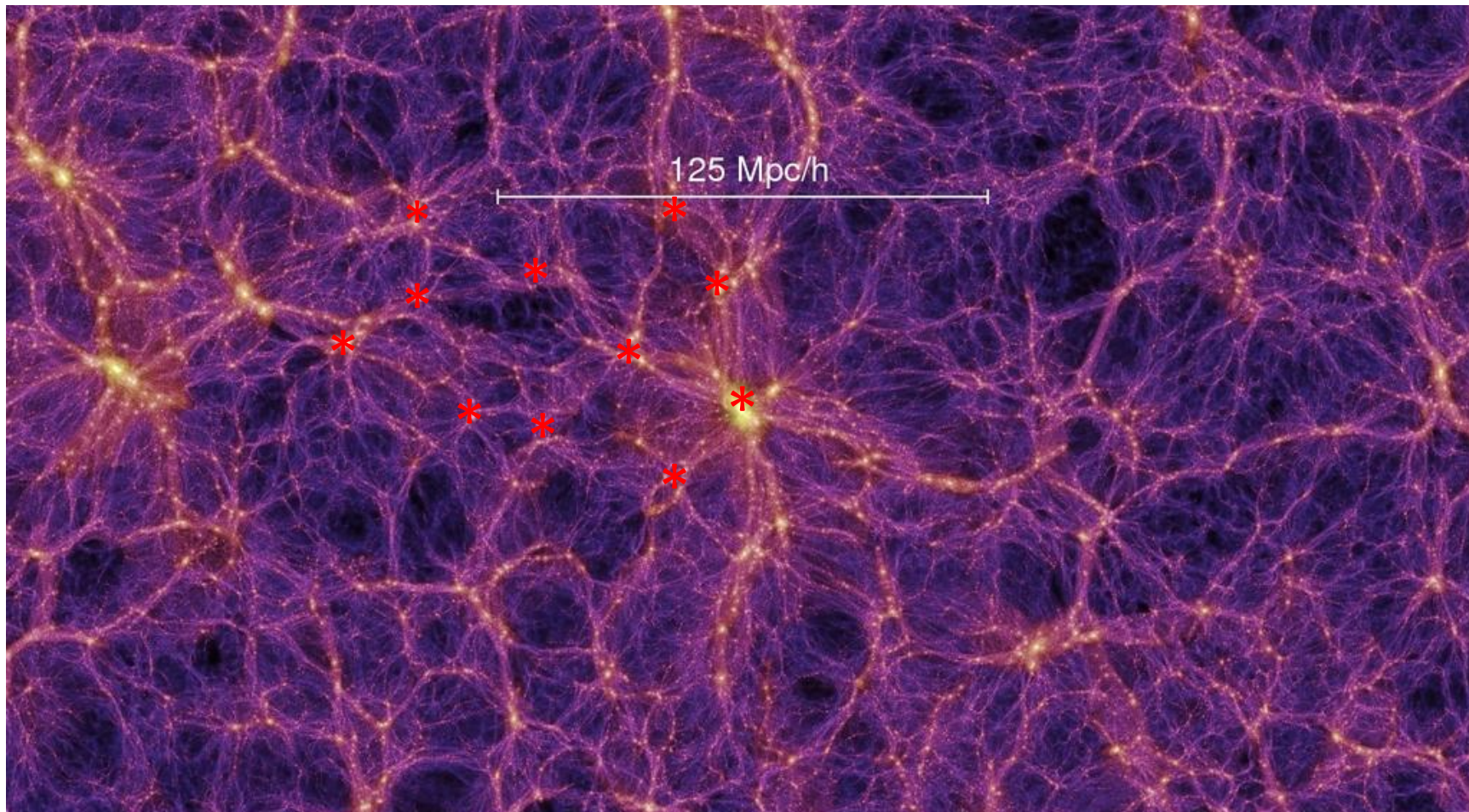
⇒ Web of interest will be at larger scales

# Cartoon idea





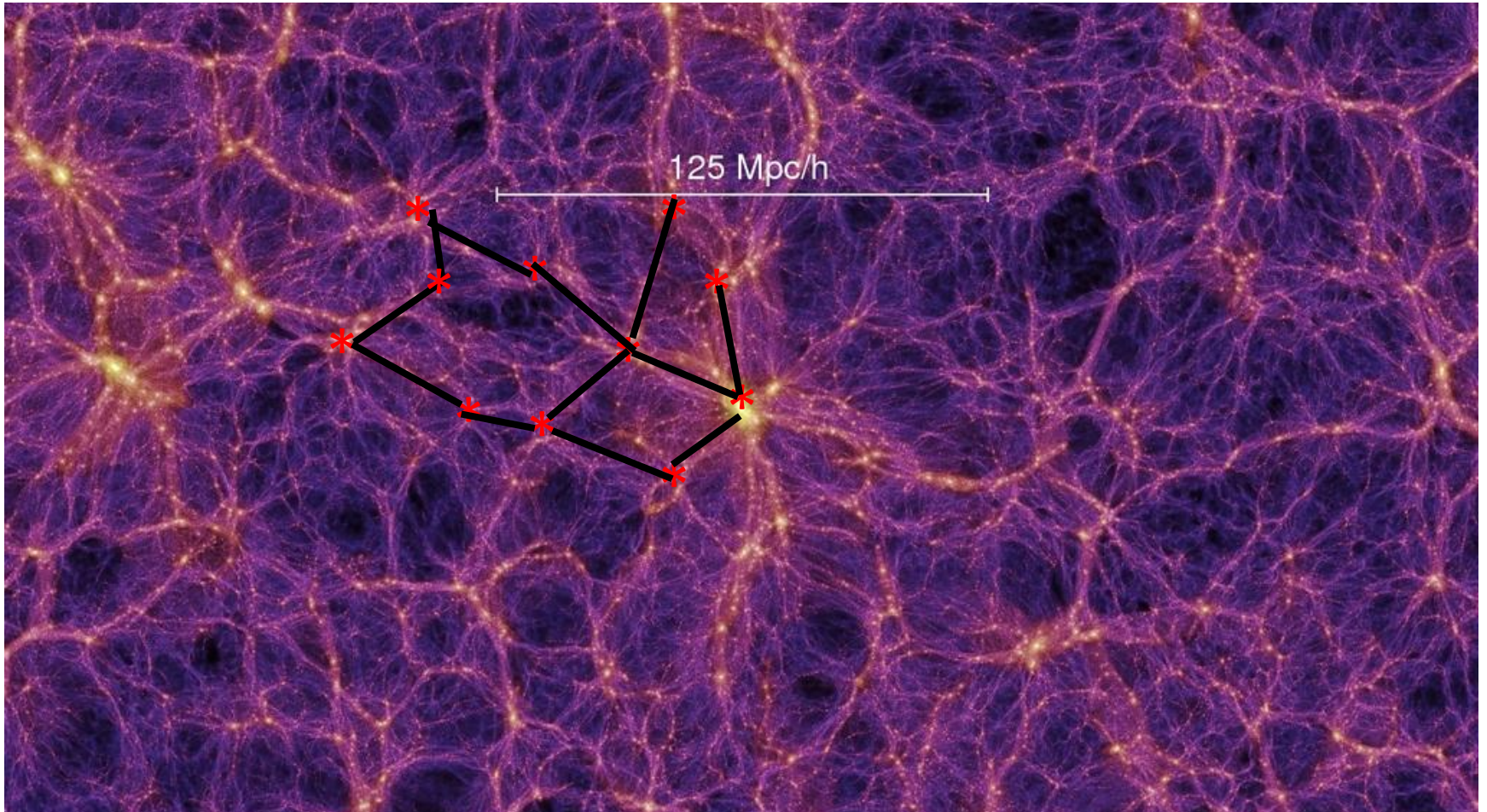
# Cartoon idea



★ = Massive nodes



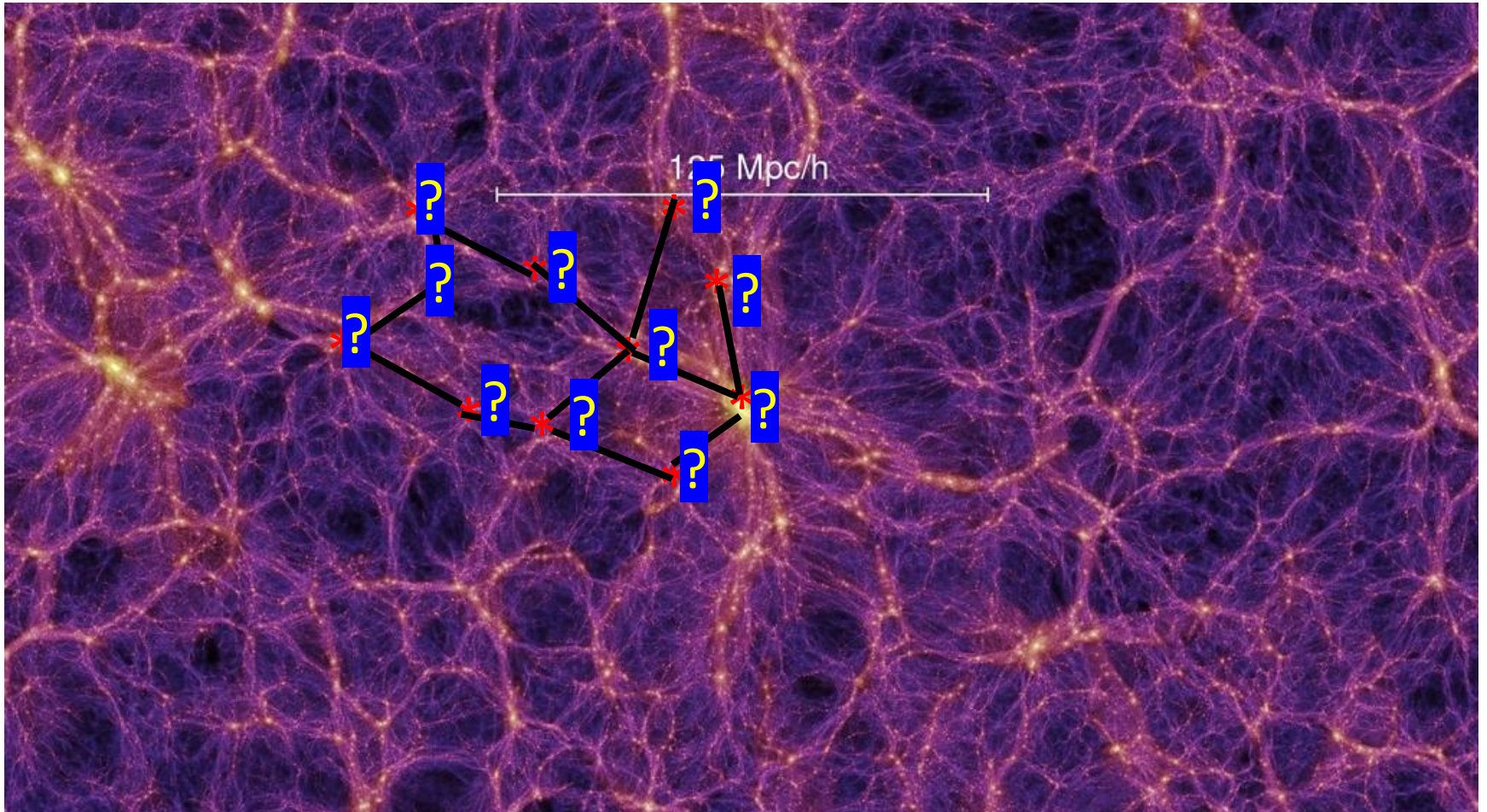
# Cartoon idea



★ = Massive nodes, — = filament  
(Note: some overdensities might be projection)



# Cartoon idea



**\*** = Massive nodes, — = filament **??** clusters ~ nodes?  
(Note: some overdensities might be projection)

# Often said clusters are nodes of cosmic web

Reasonable:

- For many finders, nodes are peaks in the density, like clusters
- both probe/affect larger scales around them
- in some finders, nodes are **required** to have large cluster like densities, e.g. Cautun++14, or nodes are **defined** to be clusters (& sometimes groups), e.g., Alpaslan++13
- clusters as (part of) node population may capture web-like features
  - *Anisotropy*: special directions to other clusters
  - *Connectivity*: cluster-cluster pairs might be filaments

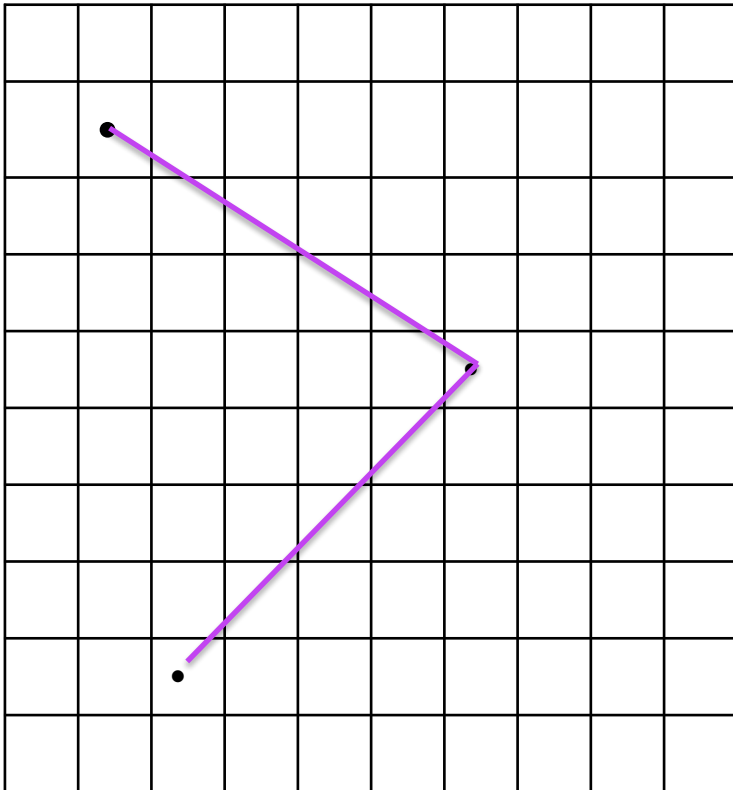
What *is* the correspondence between clusters and nodes?

[reductionist/rough question: how much do clusters capture of the web?

Variants of this asked many times, starting e.g. with Bond & Myers '96]

## Disperse based web(s)

- crit points
  - nodes-peaks
  - filaments have saddles in centers
- *no volumes*-lines and points
- based on critical points in **density**



### *One Simulation & One Finder*

#### *Different webs:*

different smoothings

1.25, 2, 2.5 (& 5) Mpc/h

different persistence [ncut-note added]

$1\sigma$ ,  $2\sigma$ ,  $3\sigma$

(~criteria to distinguish peaks)

Use these 9 webs hereon

(see momentarily that 5 Mpc/h smoothing case too degenerate)

*...What do they look like?*

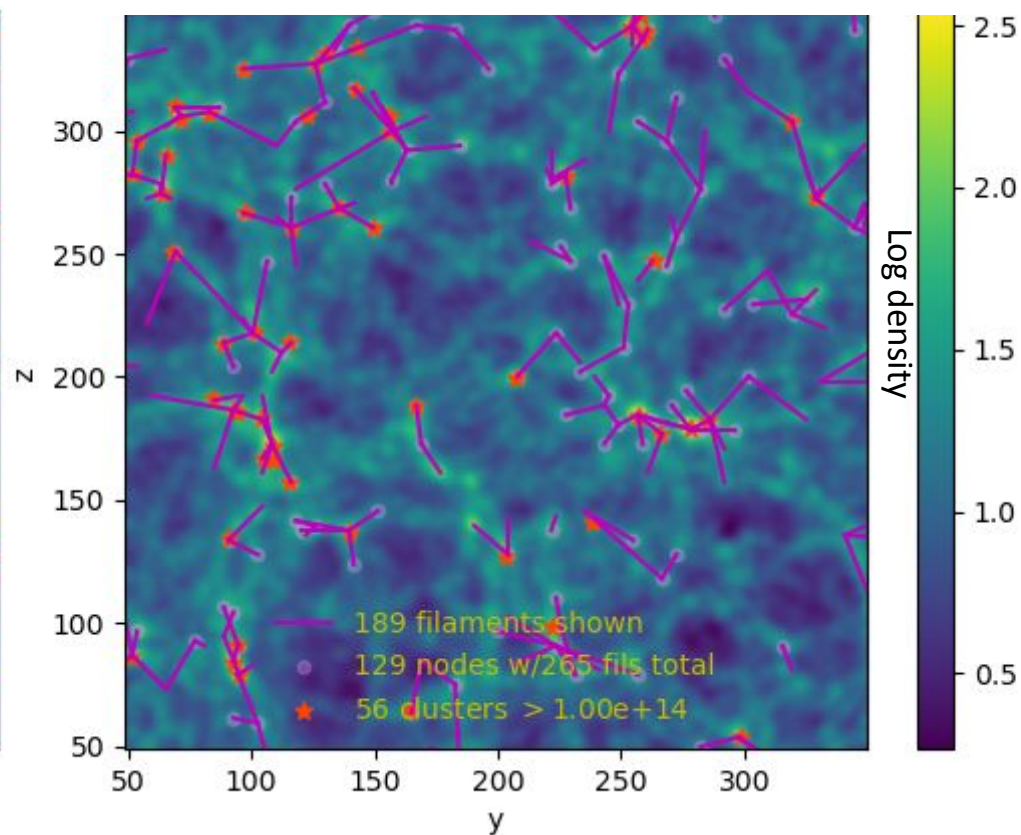
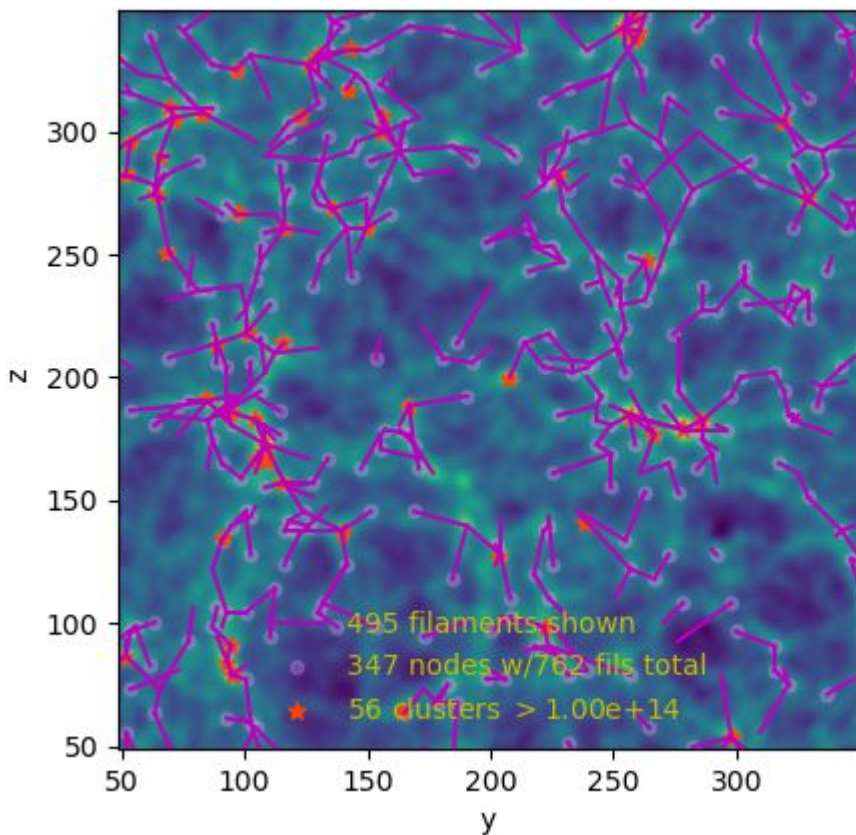


1 $\sigma$  persistence

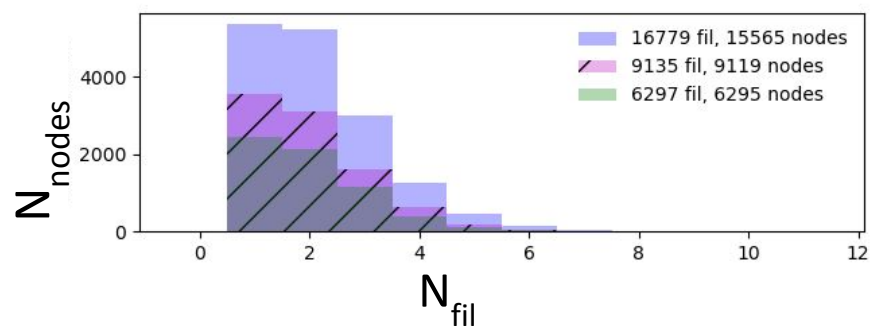
2 Disperse webs

3 $\sigma$  persistence

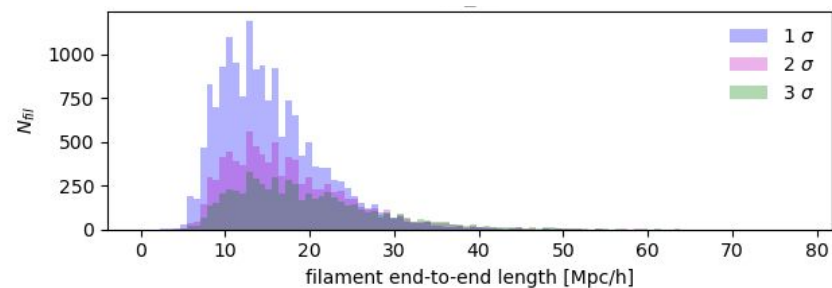
(2Mpc/h smoothing)



Connectivity (1 $\sigma$ ,2 $\sigma$ ,3 $\sigma$ )

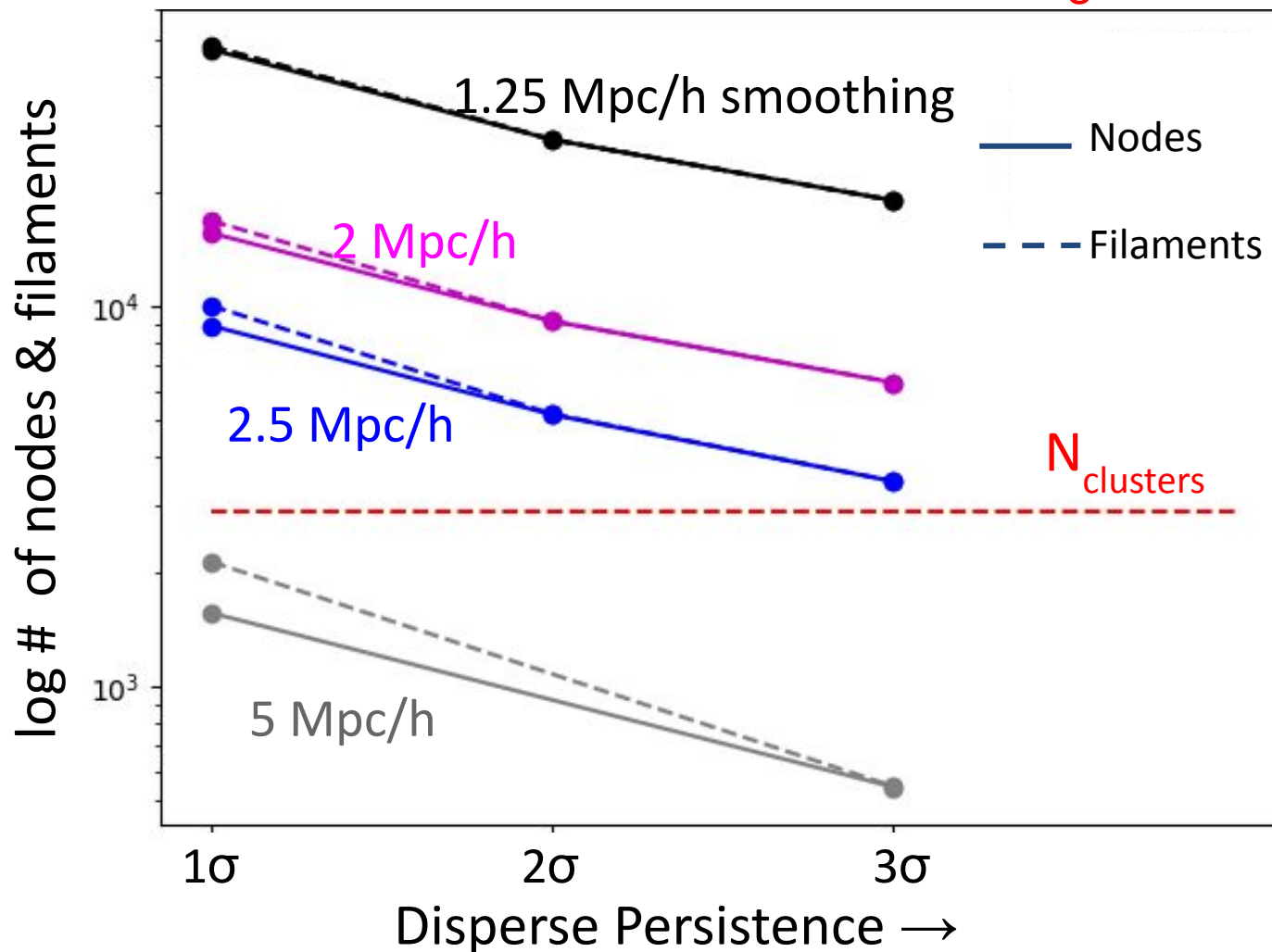


Filament lengths (1 $\sigma$ ,2 $\sigma$ ,3 $\sigma$ )



# Numbers of nodes & filaments for different webs

Compare to 2898 cluster ( $\geq 10^{14} M_{\odot}$ ) halos



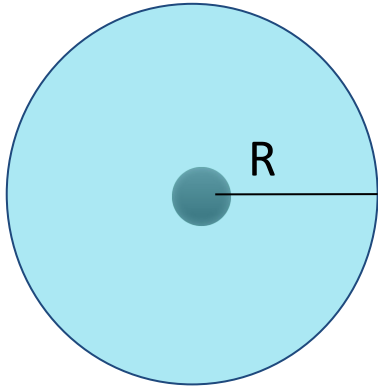
Aside from 5 Mpc/h (discard), **more nodes than clusters**, sometimes many more!



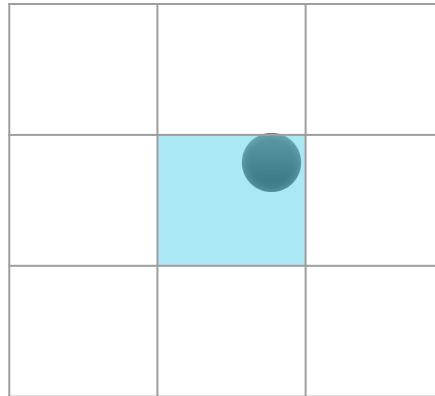
# cluster $\leftrightarrow$ node matching

Disperse identifies critical *points*

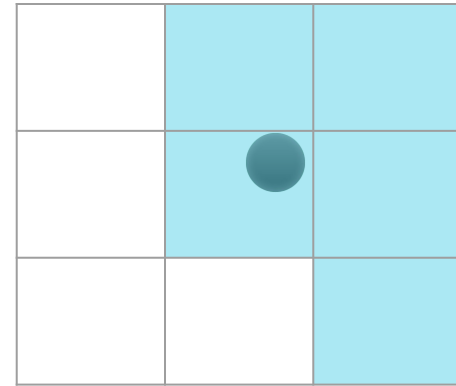
Assign *volume* to nodes\* and see if cluster centers are inside



$R \sim 2x$  smoothing  
"nearest/fixed"



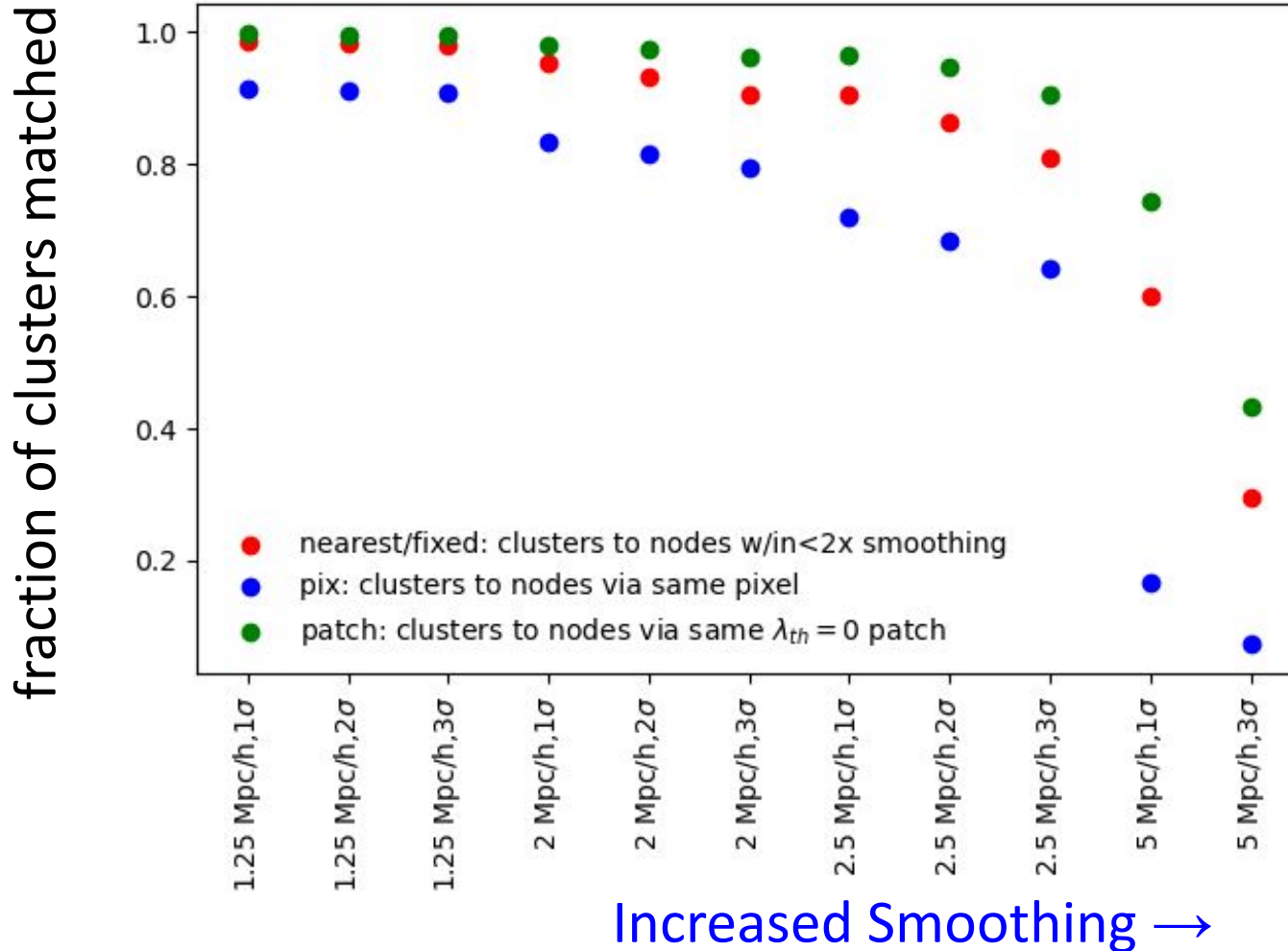
density pixel  
"pix"



Hessian patch with  $\partial_i \partial_j \varphi$  ev's  
+++ = node  
node = contiguous +++ patch  
"patch"

\*Could also try to put nodes "in" clusters, which have a natural radius

# Clusters matched to nodes?



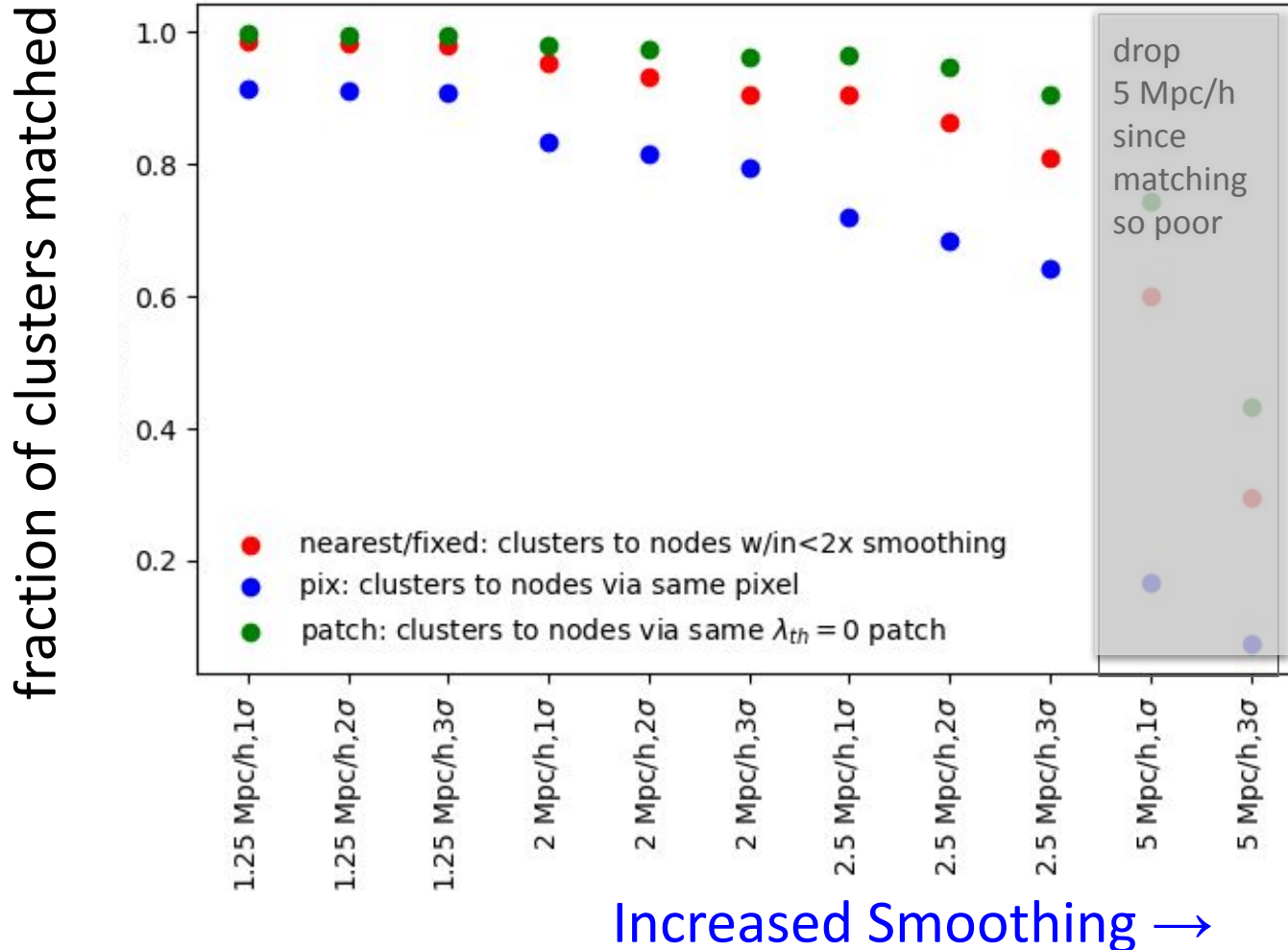
*Most clusters are matched*  
(~100%\* to 64%)  
depends on web

*Fewer matched as web smoothing ↑ persistence ↑*

\*missing only 9/2898



# Clusters matched to nodes?

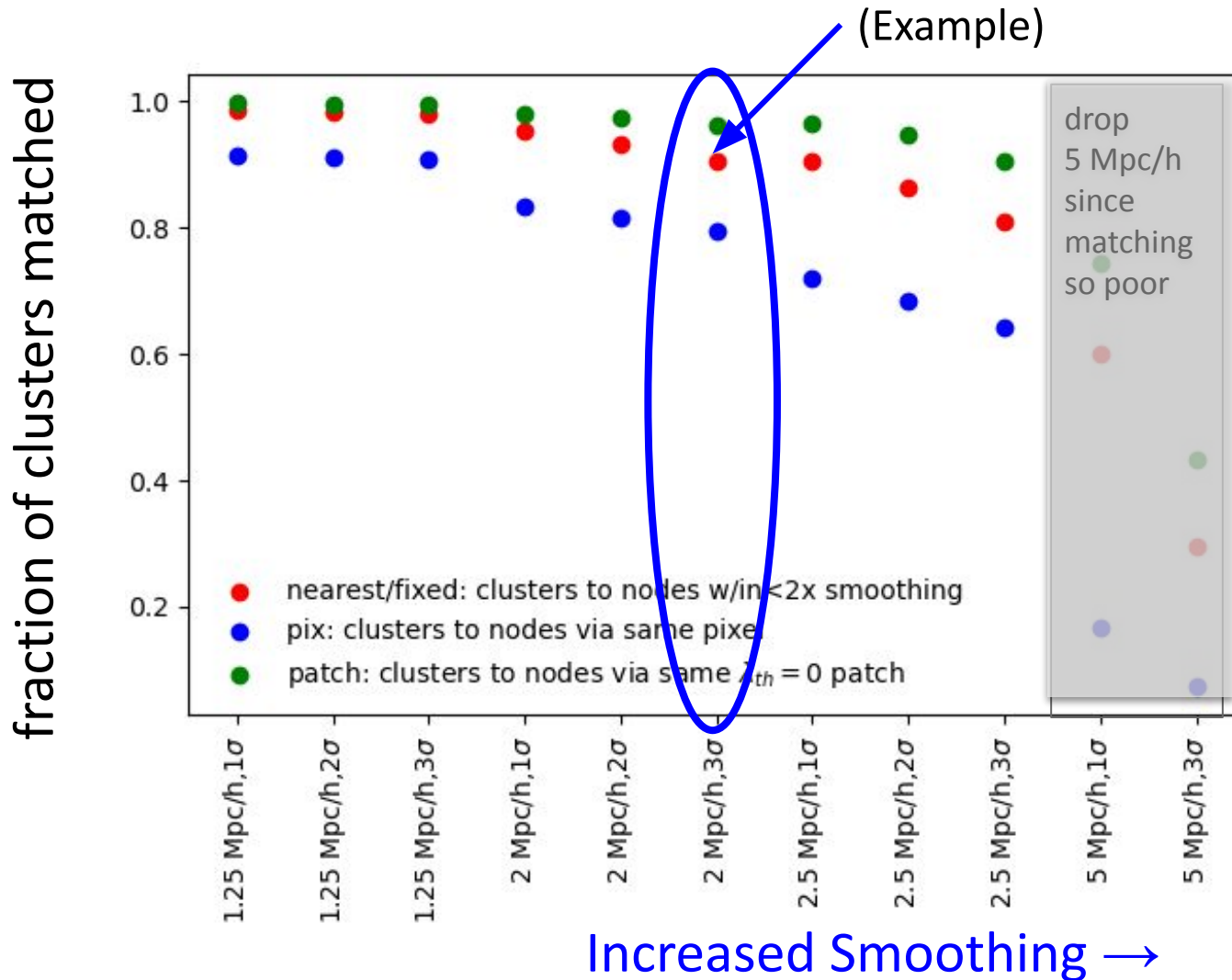


*Most clusters are matched*  
(~100%\* to 64%)  
depends on web

*Fewer*  
matched as web  
smoothing ↑  
persistence ↑

\*missing only 9/2898

# Clusters matched to nodes?



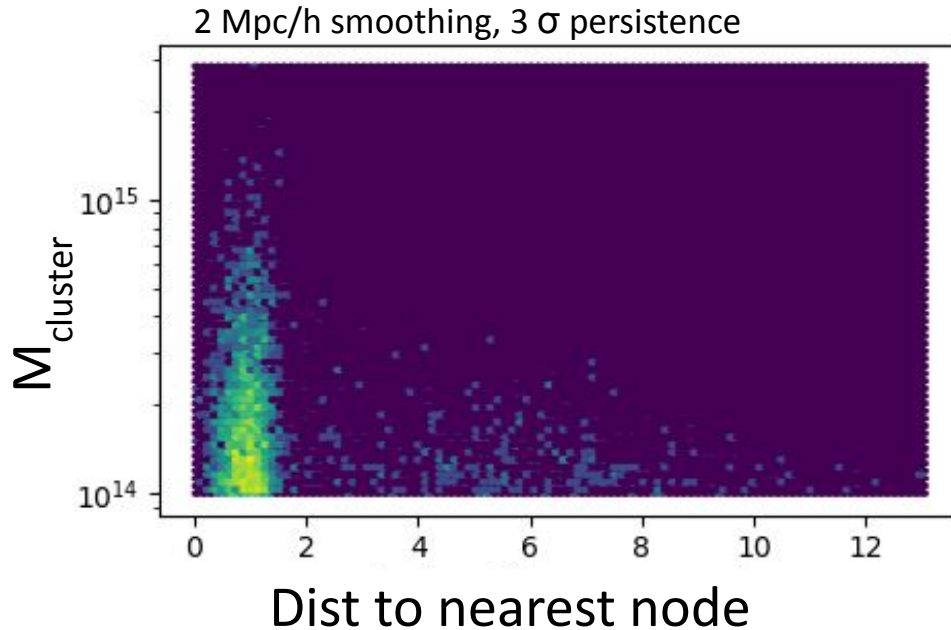
*Most clusters are matched*  
 (~100%\* to 64%)  
 depends on web

*Fewer*  
 matched as web  
 smoothing ↑  
 persistence ↑

\*missing only 9/2898



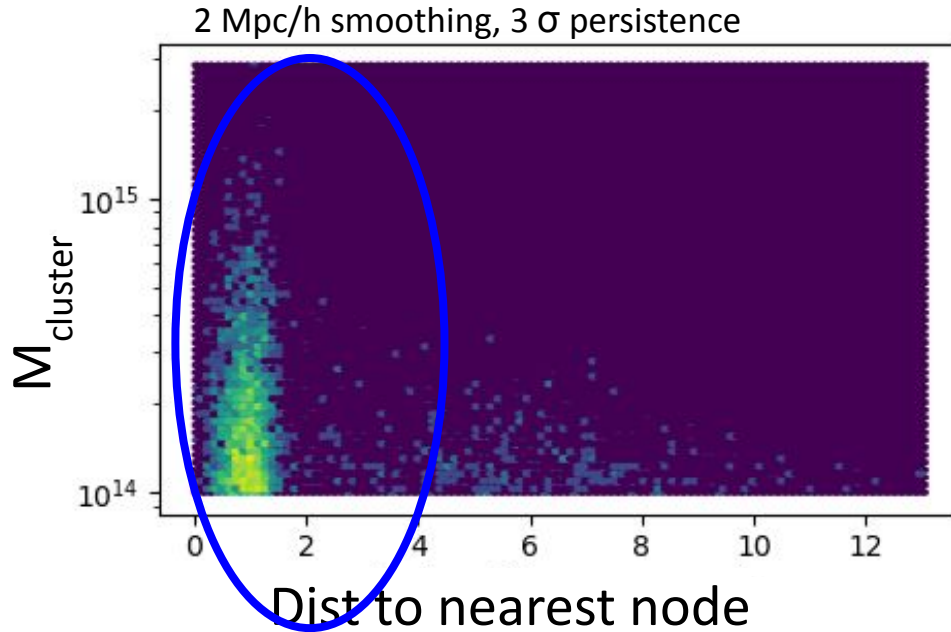
# Matching example: "nearest/fixed"



two populations:

- clusters near nodes-"matched"
- clusters not near nodes

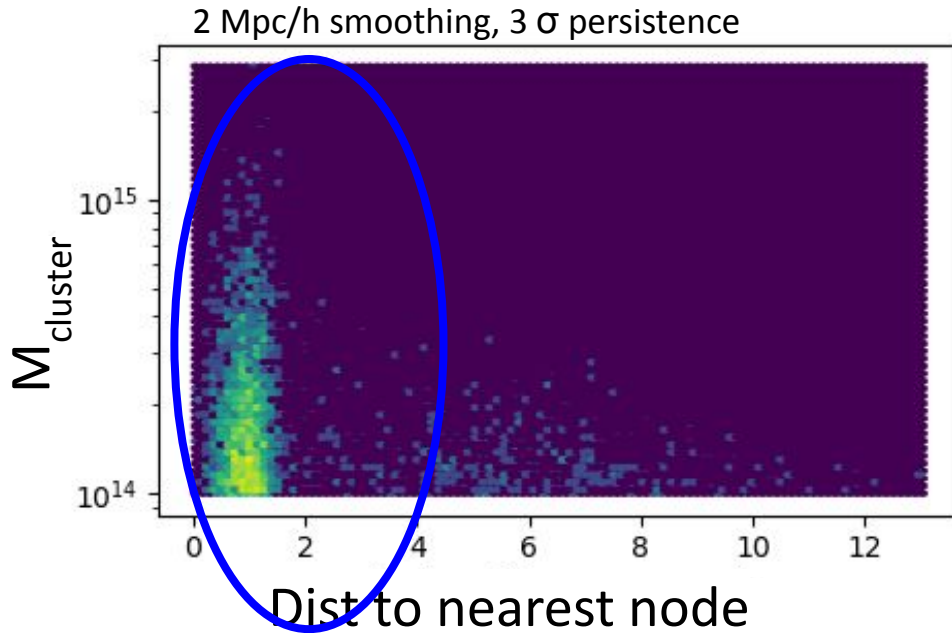
# Matching example: "nearest/fixed"



two populations:

- clusters near nodes-"matched"
- clusters not near nodes (272/2898)

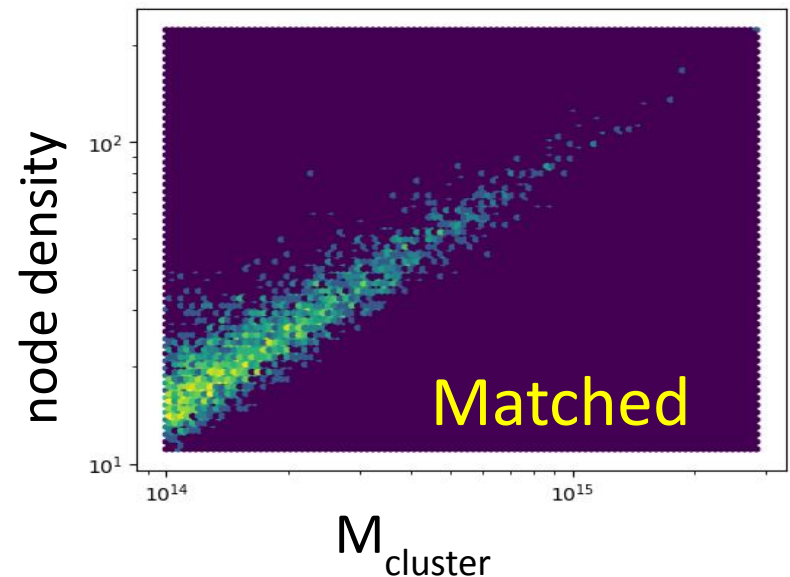
# Matching example: "nearest/fixed"



Matched clusters:  
cluster mass - node  
density relation



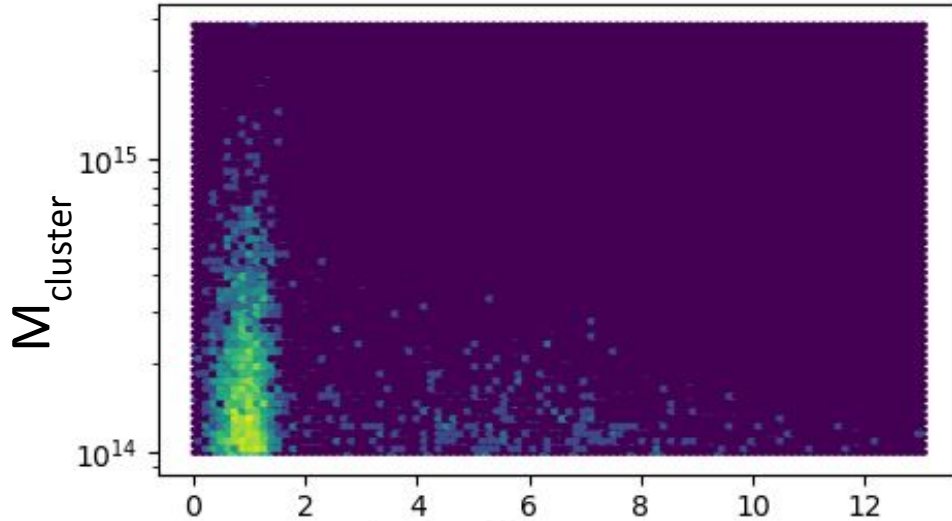
- two populations:
- clusters near nodes - "matched"
  - clusters not near nodes (272/2898)





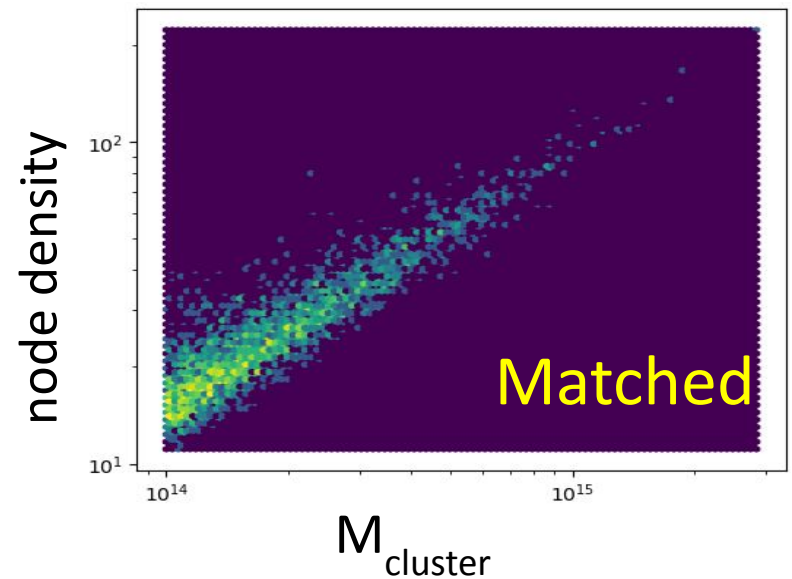
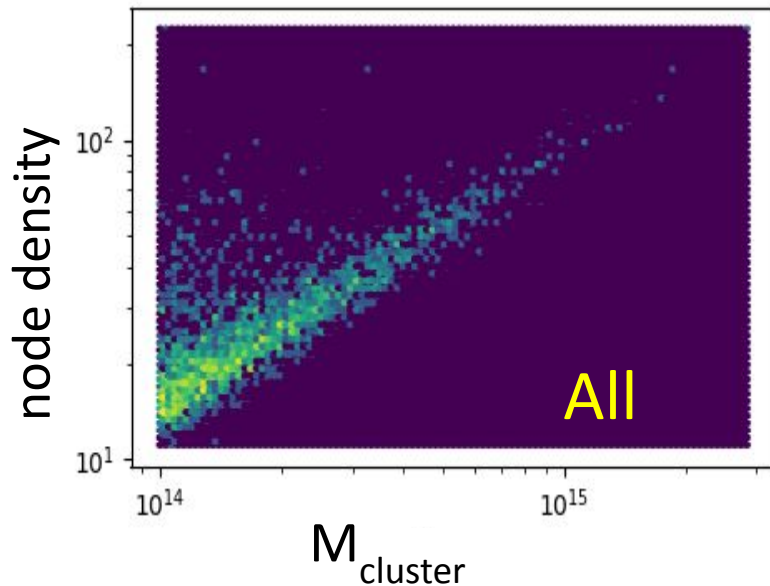
# Matching example: "nearest/fixed"

2 Mpc/h smoothing, 3  $\sigma$  persistence



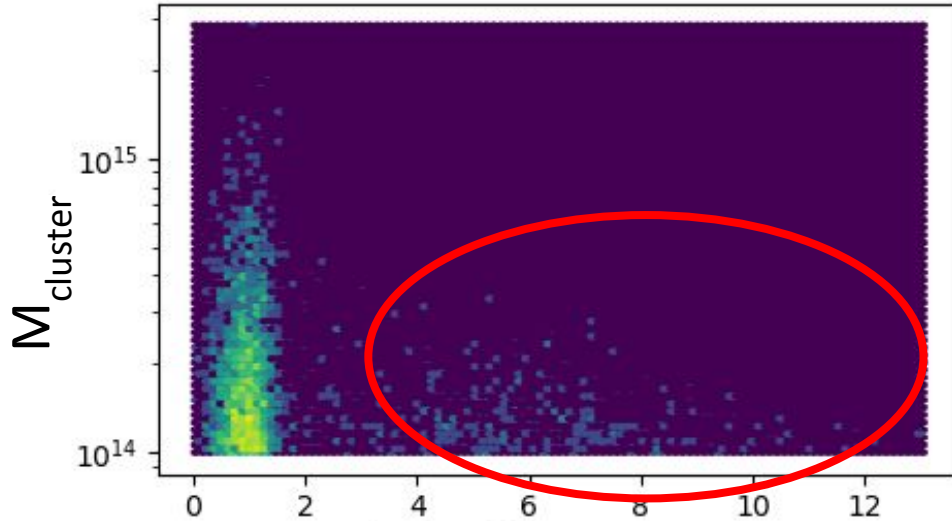
two populations:

- clusters near nodes-"matched"
- clusters not near nodes (272/2898)



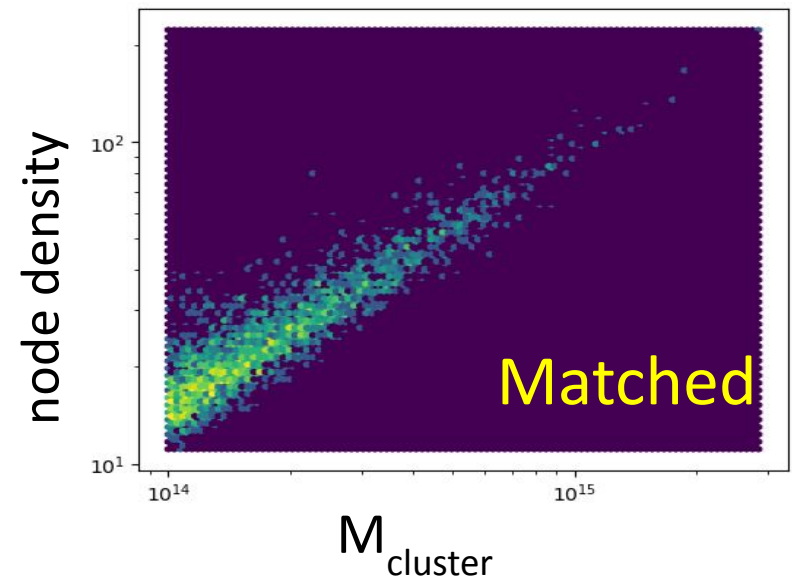
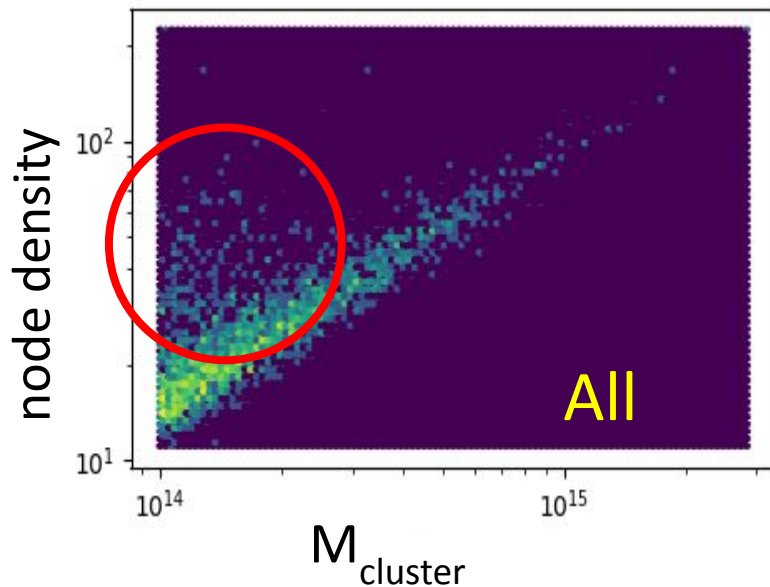
# Matching example: "nearest/fixed"

2 Mpc/h smoothing, 3  $\sigma$  persistence

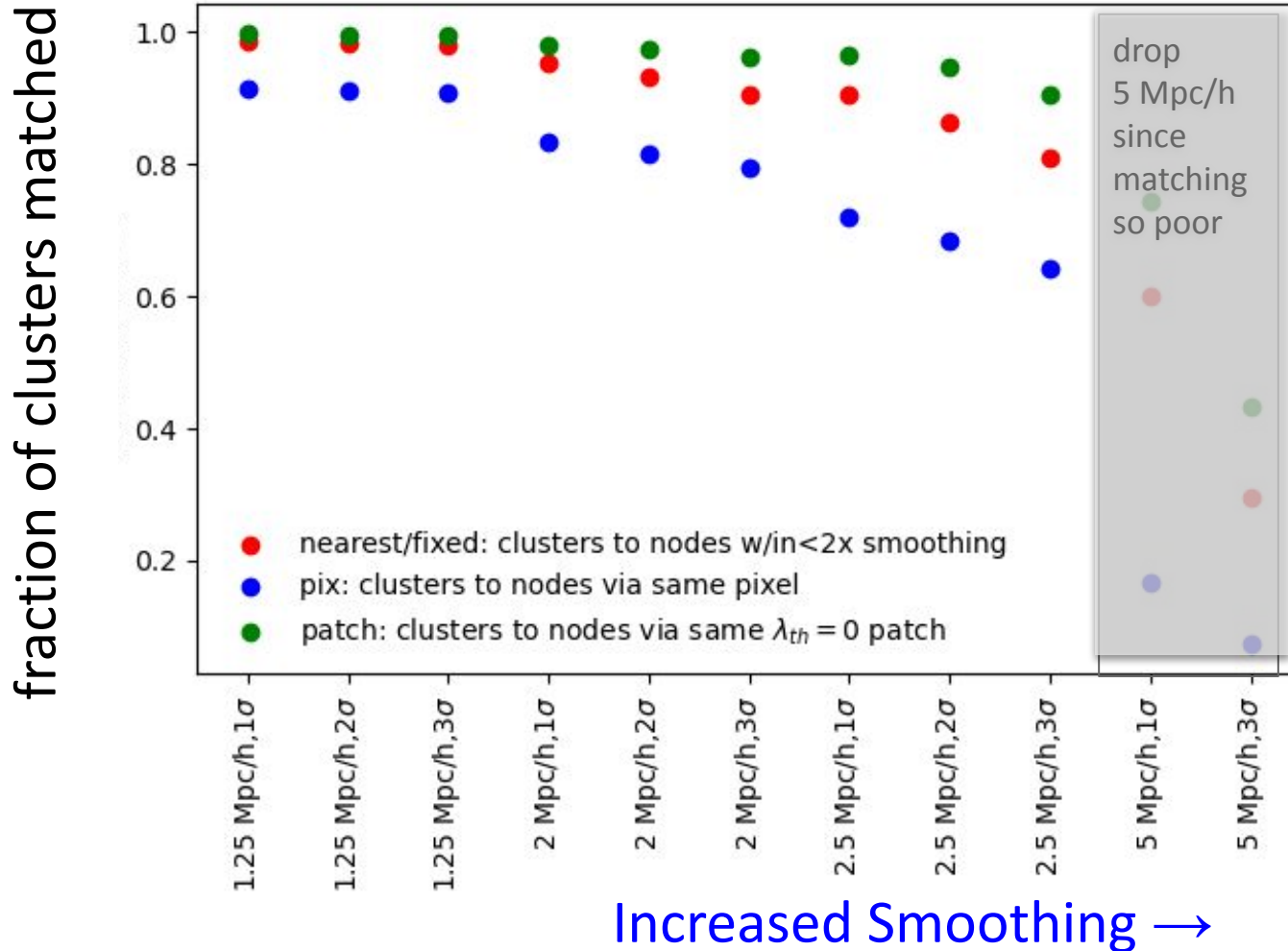


two populations:

- clusters near nodes—"matched"
- clusters **not near nodes—9% no nodes**



# Unmatched clusters more generally?



*Most clusters are matched*  
(~100%\* to 64%)  
depends on web

*Fewer*  
matched as web  
smoothing ↑  
persistence ↑

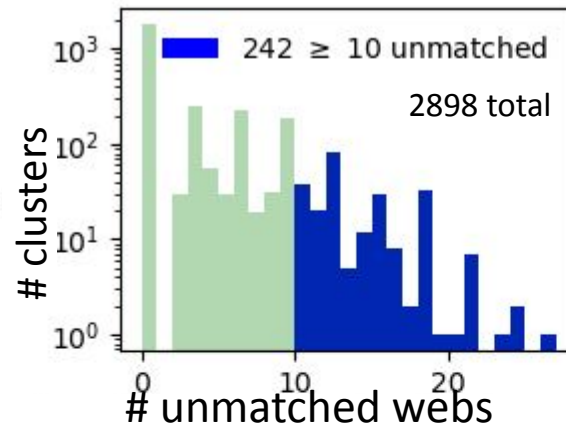
\*missing only 9/2898



# Unmatched clusters different webs/matching methods

Matched clusters: 64% -~100% - - 63% of clusters match every time  
[drop "pix" method 81%- ~100%] - - 78% of clusters match every time

"pix" -match same pixel, very restrictive, perhaps too much so

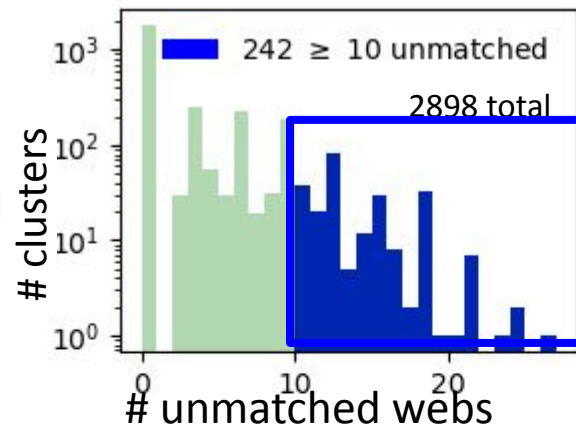


How many times each cluster is  
unmatched, in all web/matching  
combinations

# Unmatched clusters

## different webs/matching methods

Matched clusters: 64% -~100% - - 63% of clusters match every time  
[drop "pix" method 81%- ~100%] - - 78% of clusters match every time  
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How many times each cluster is  
unmatched, in all web/matching  
combinations

Take clusters unmatched  $\geq$  10 times

# Unmatched clusters

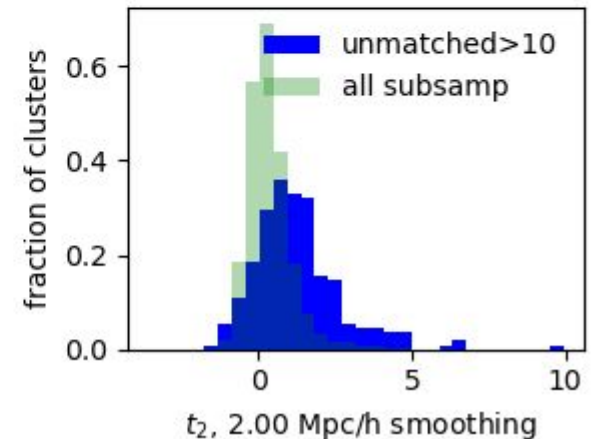
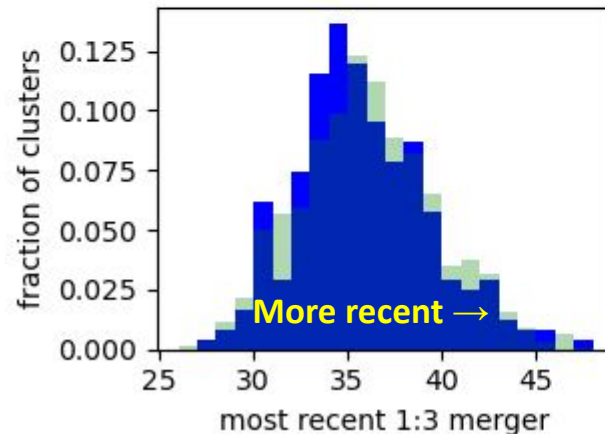
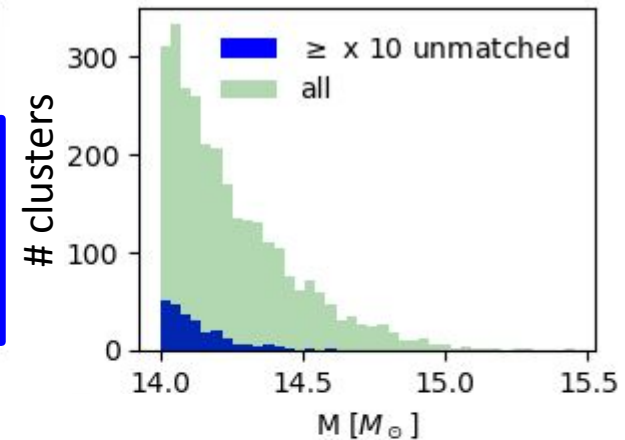
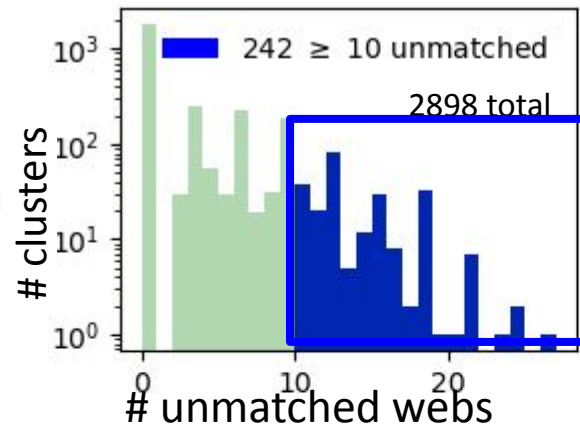
## different webs/matching methods

Matched clusters: 64% - ~100% - - 63% of clusters match every time  
 [drop "pix" method 81%- ~100%] - - 78% of clusters match every time

"pix" -match same pixel, very restrictive, perhaps too much so

frequently  
 unmatched  
 clusters tend to:

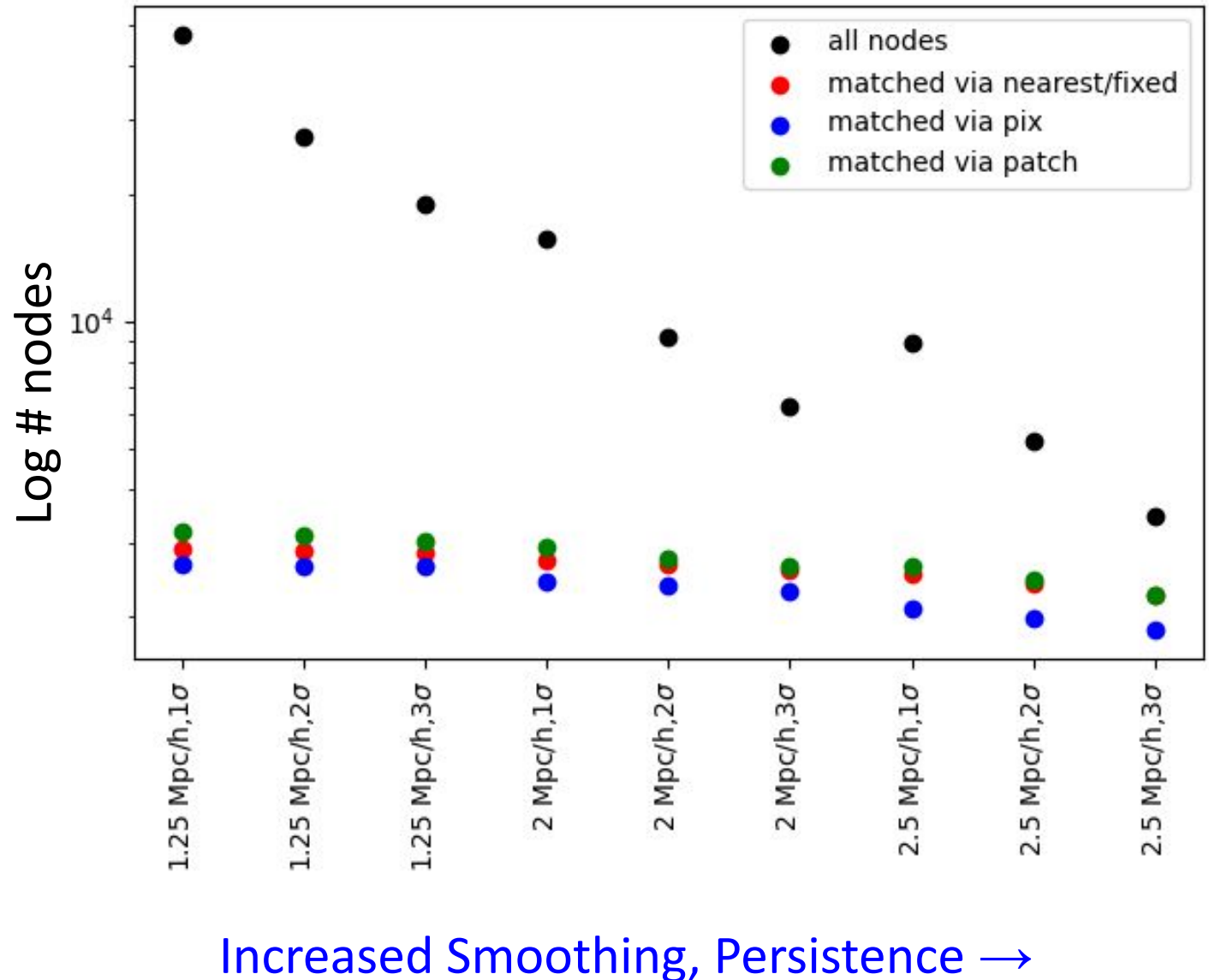
- have lower mass
- slightly less recent major mergers
- higher  $t_2 = \lambda_2 - \delta/3$





# Nodes: most are unmatched!

Most nodes are not matched to clusters

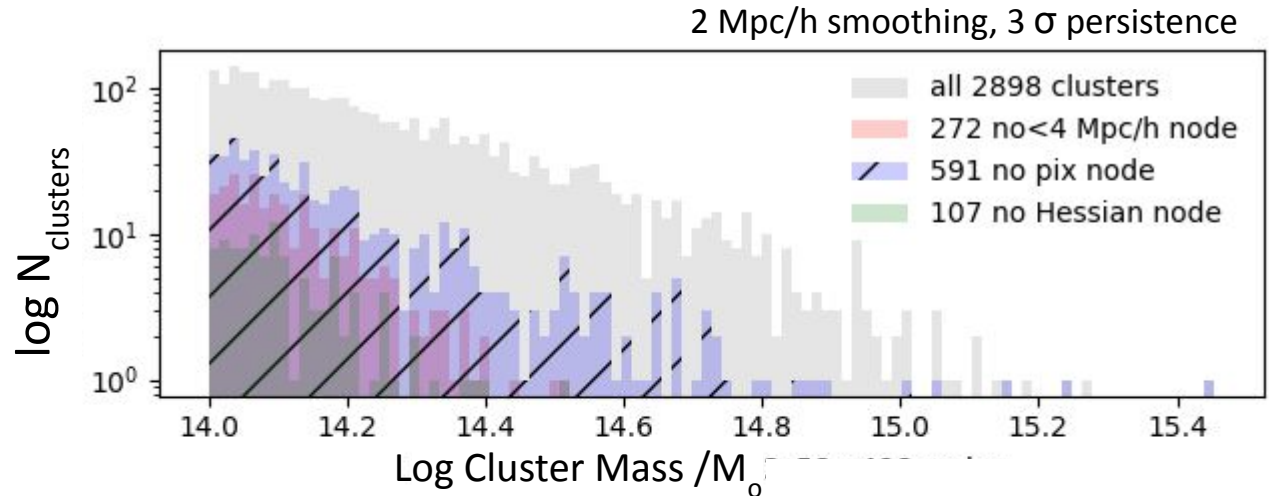


# A bit more about unmatched nodes

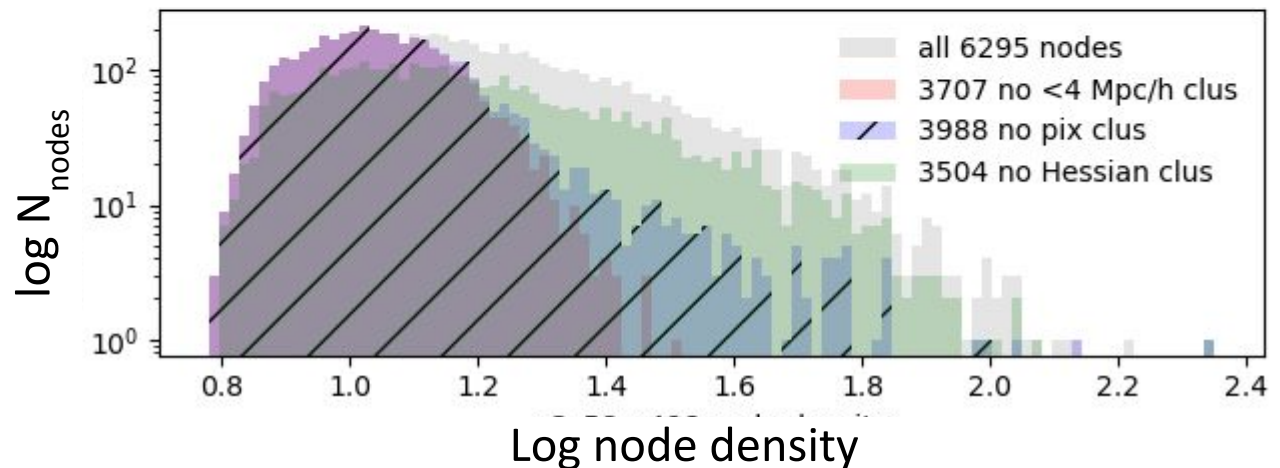
# nodes  $\gg$  # clusters  $>$  # matched clusters

For main example web  
& several matching  
methods:

**Unmatched clusters  
mostly low mass**



Unmatched *node*  
density distribution  
**not just low density**  
**[except for 2x  
smoothing]**  
**Hess has fewest  
unmatched but goes to  
highest density**



For these webs, now have (36 versions of)  
clusters  $\leftrightarrow$  nodes

How about

cluster pairs  $\leftrightarrow$  web filaments?

[connect clusters  $\leftrightarrow$  connect nodes]

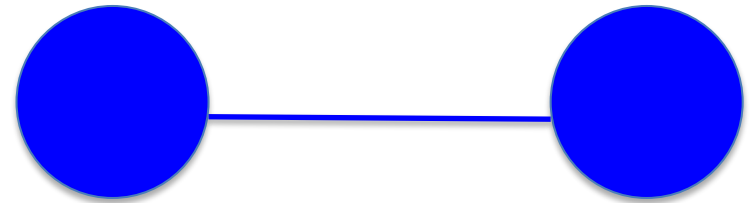
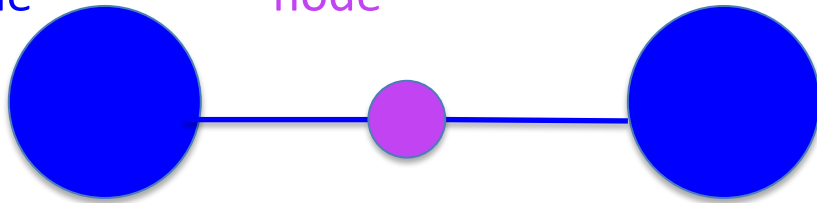
- Sometimes it's implicitly assumed that cluster pairs have filaments
- Here, take nodes matched to clusters
  - If two cluster matched nodes share a filament  $\rightarrow$  cluster pair has a filament
  - Interpolate through nodes not matched to clusters

# Truncated ('approximate') web

Connect nodes with non-matched node [  ] in between if angle  $> 120^\circ$  ; triples = 3 pairs, etc.

matched  
node

unmatched  
node



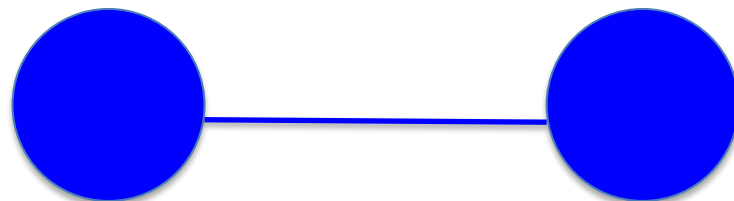
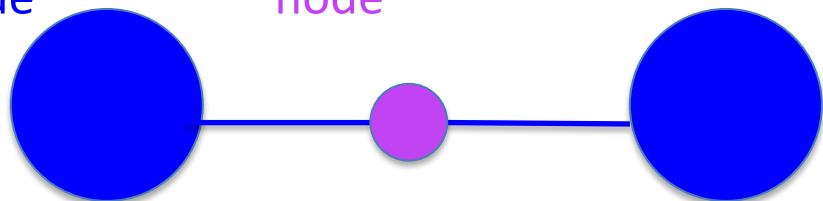


# Truncated ('approximate') web

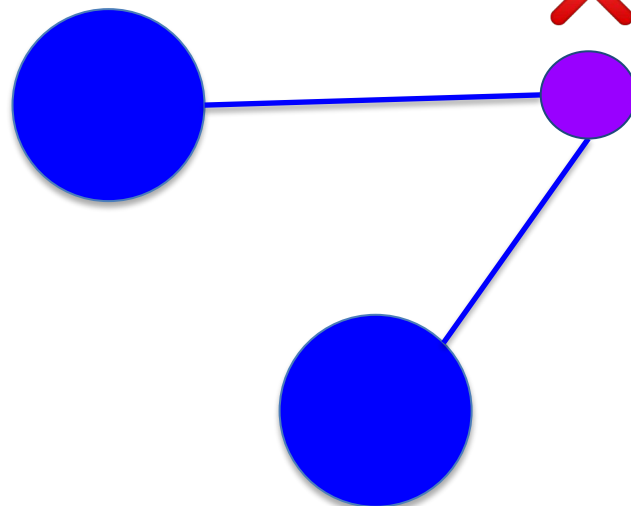
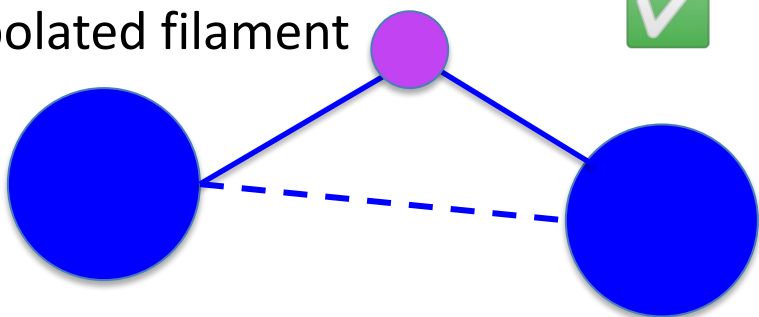
Connect nodes with non-matched node [  ] in between if angle  $> 120^\circ$  ; triples = 3 pairs, etc., can drop  $> 1$  in between.

matched  
node

unmatched  
node



Interpolated filament

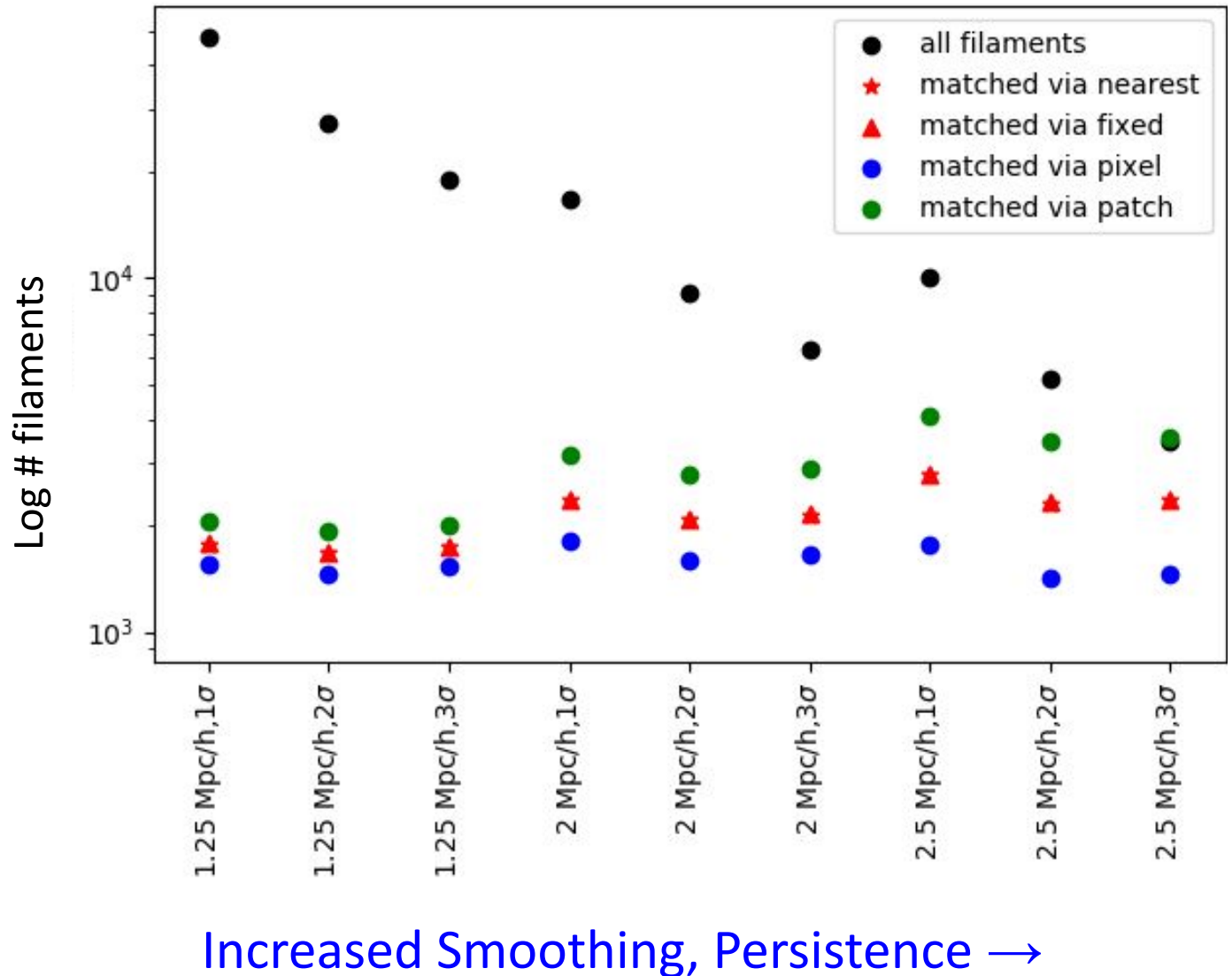


Interp  
Fraction  
of fils

	1.25 Mpc/h	2 Mpc/h	2.5 Mpc/h
	34%-50%	15%-40%	7%-35%

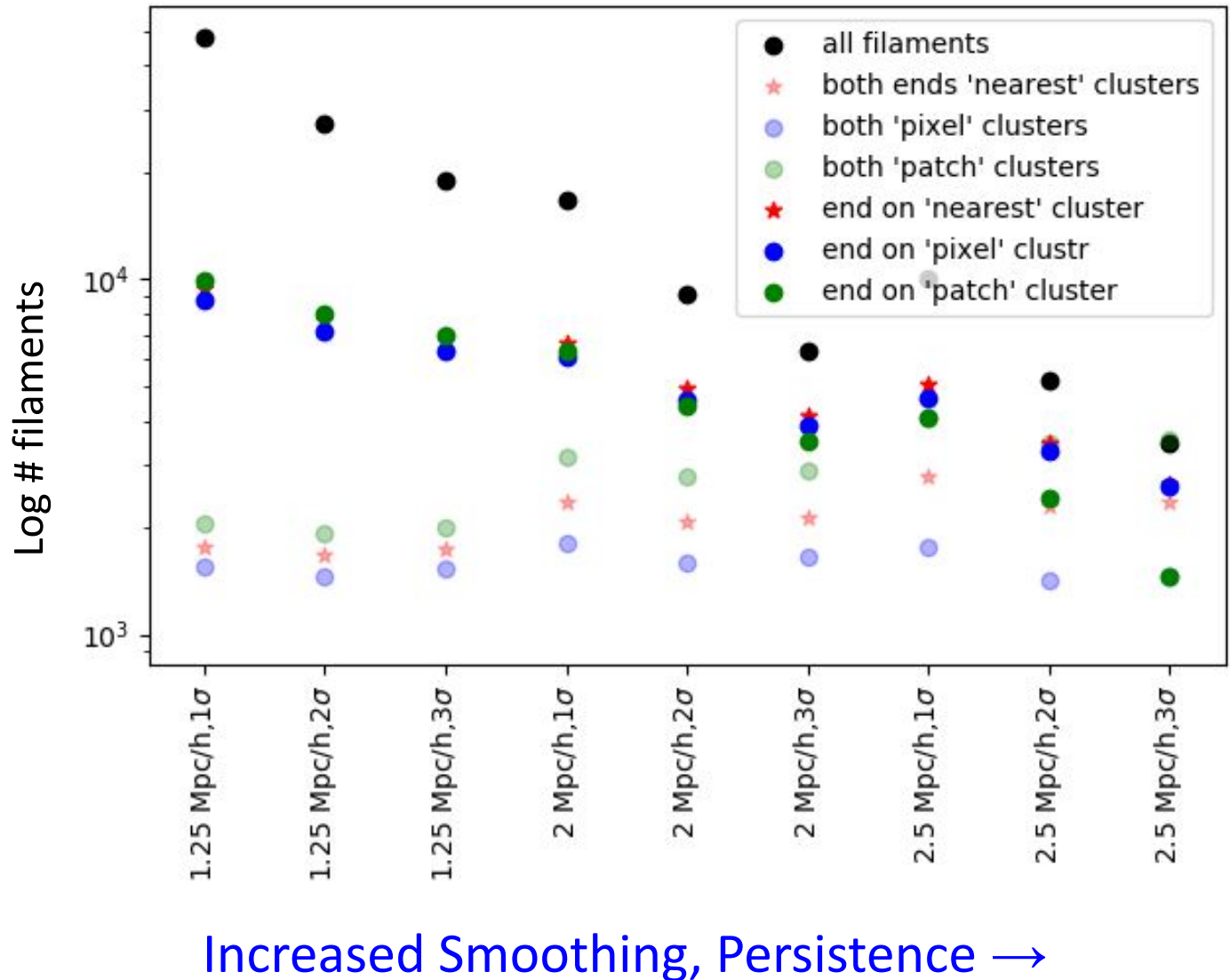
# Filament demographics after matching to cluster pairs

Most webs:  
most  
filaments  
are not  
matched  
to cluster  
pairs



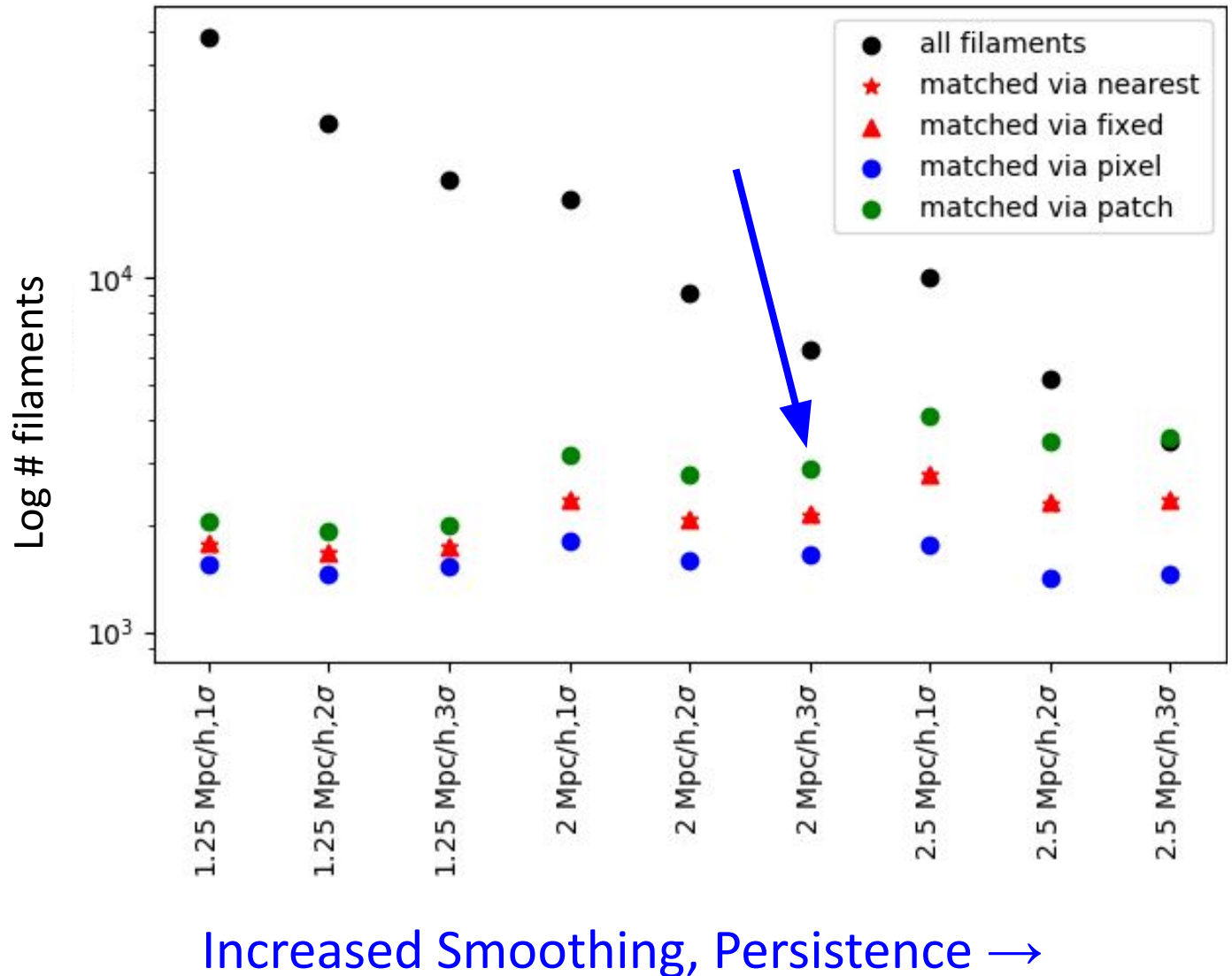
# Filament demographics after matching to cluster endpoints (aside)

Most webs:  
many  
filaments  
have at  
least one  
cluster  
matched  
endpoint



# Filament demographics after matching to clusters

Most webs:  
most  
filaments  
are not  
matched  
to cluster  
pairs

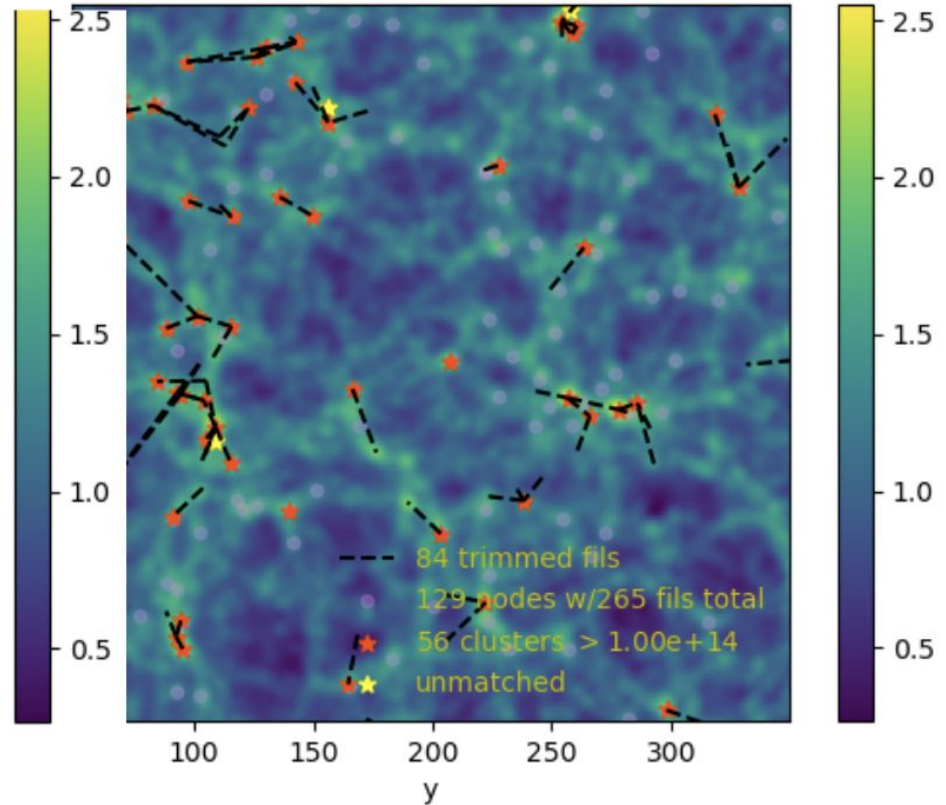
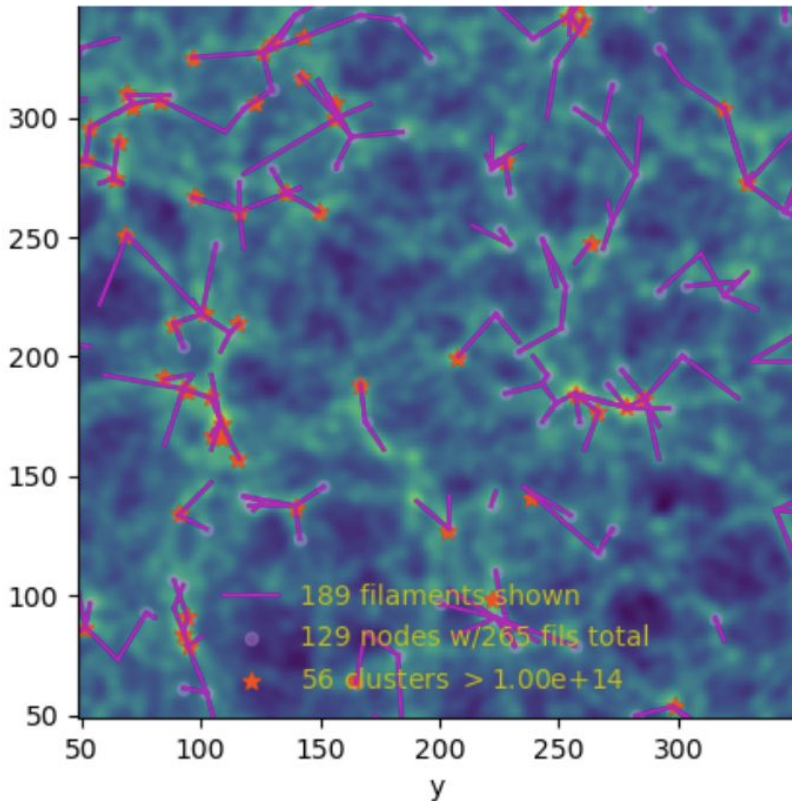




# Get very sparse web!

2 Mpc/h smoothing,  $3\sigma$  persistence

30 Mpc/h deep



**189 filaments originally**

— Disperse filaments

\* clusters w/nodes



**84 cluster-cluster filaments**

- - - cluster-cluster filaments

\* unmatched clusters

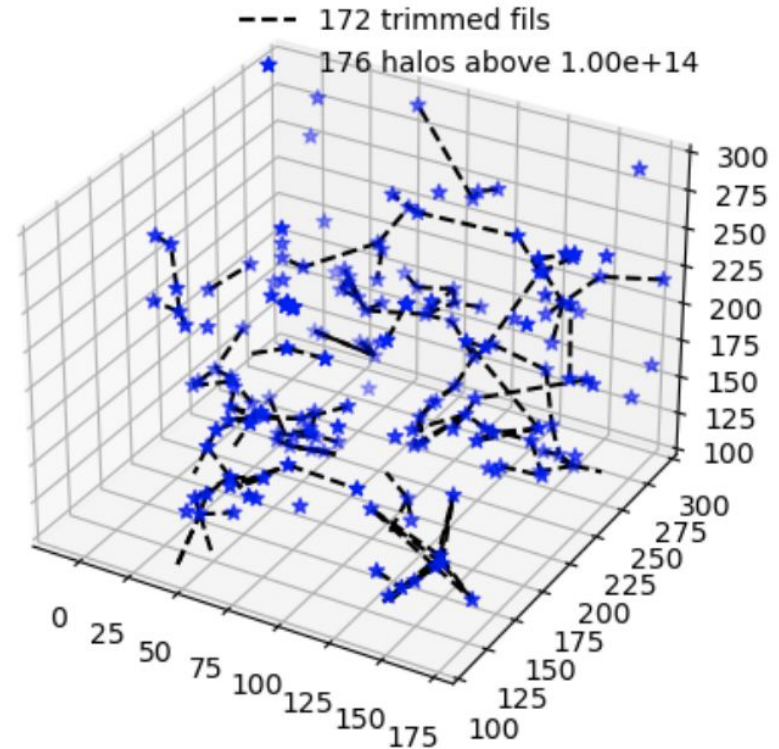
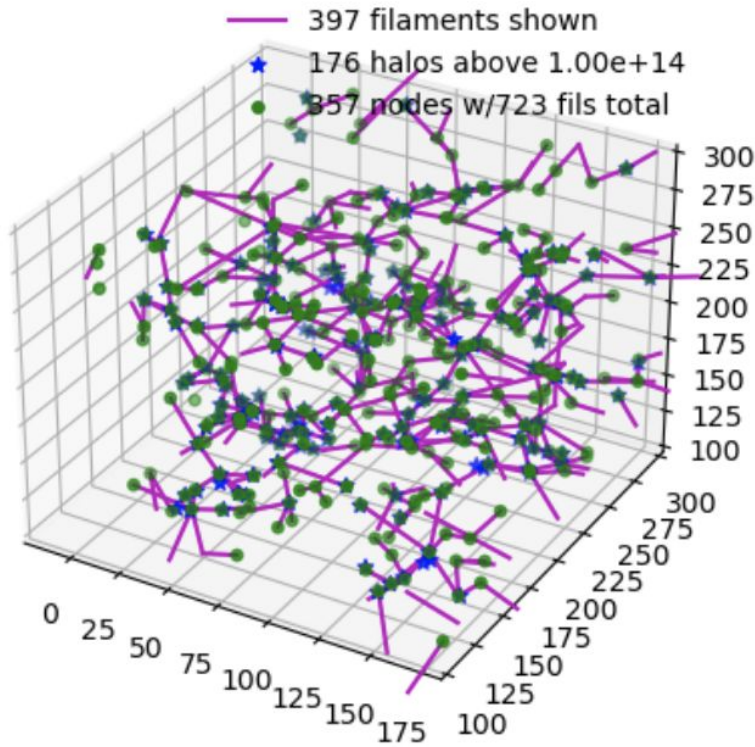
# Another larger scale view of same system ( $[200 \text{ Mpc}/h]^3$ )

\* Disperse Nodes

- Disperse Filaments

\* Clusters

- - - Cluster pairs with filaments



# Statistics of all cluster webs from this Disperse web

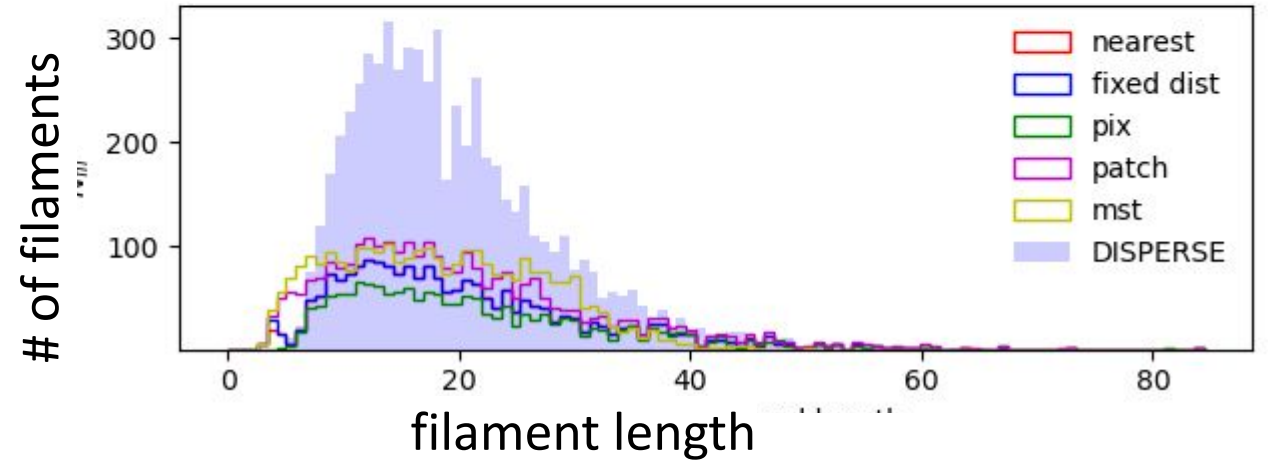
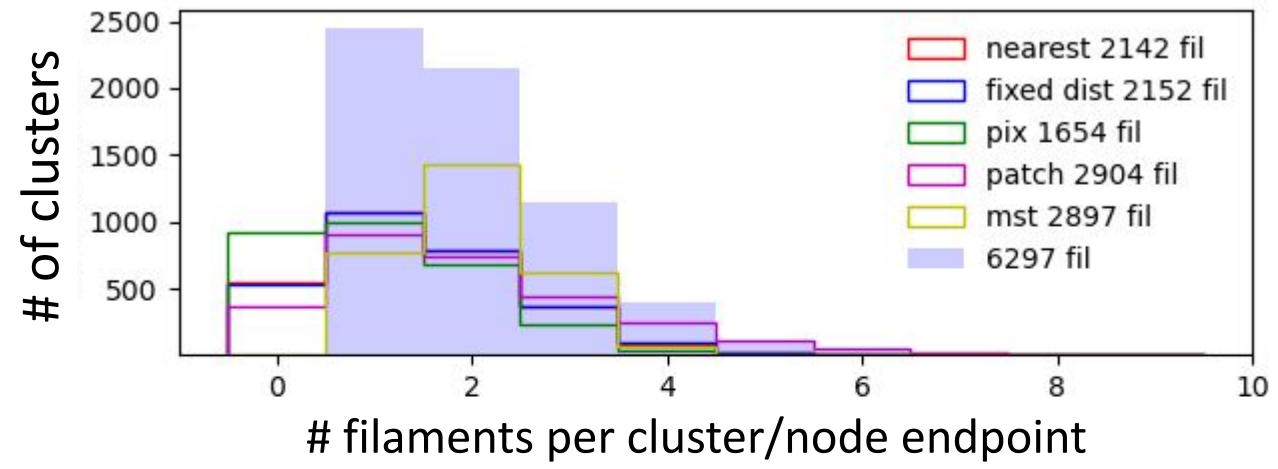
**Disperse** 

- more filaments (6297)
- all nodes get filaments

**Cluster webs:** (lines)

- 1654 - 2904 filaments
- some clusters no filaments
- higher fraction of long filaments
- high density (at saddle)
- filaments more often matched to cluster pairs

(2 Mpc/h smoothed, 3 persistence)



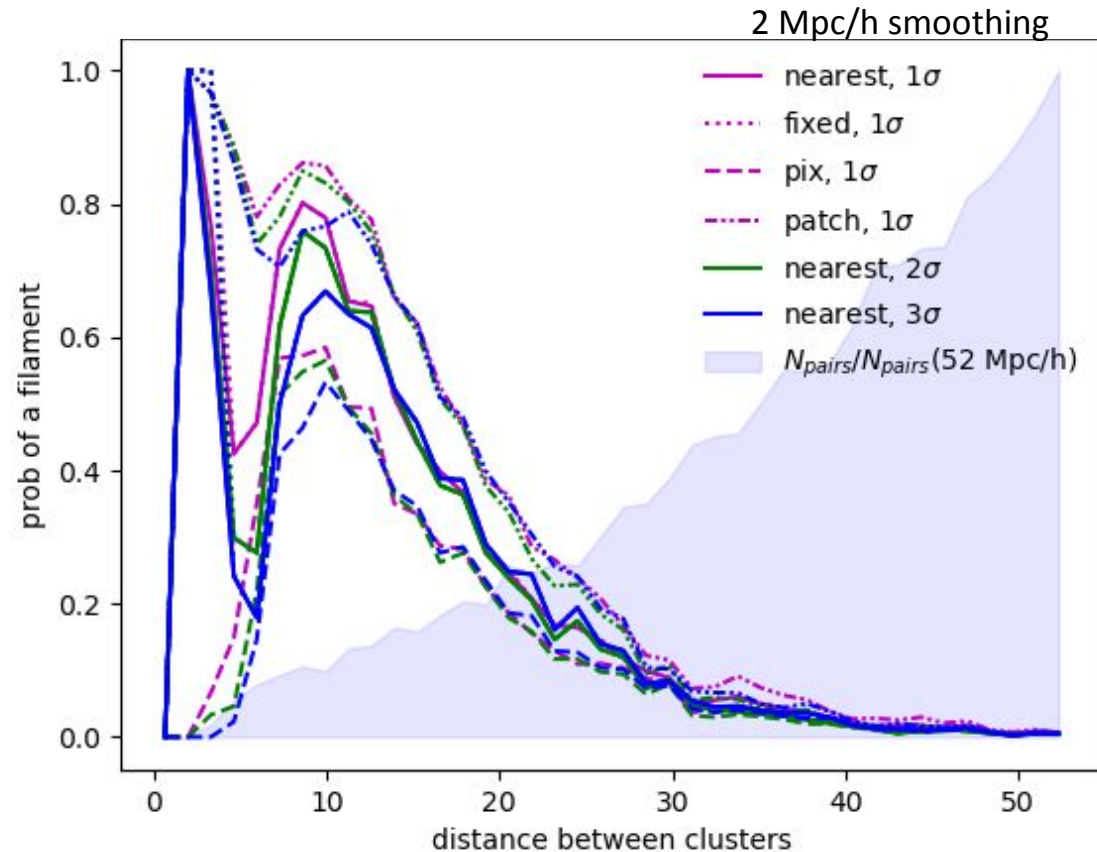
These are filament properties that match to cluster pairs, how about vice versa?

# Before: which clusters -> nodes?

# Now: which cluster pairs -> filaments?

A pair is more likely to have a Disperse filament if the clusters:

- are close together
- have long axes aligned with cluster pair axis
- using ML (later)
  - cluster is one of closest other clusters
  - have long axes aligned with each other



3 persistences shown here (3 webs)

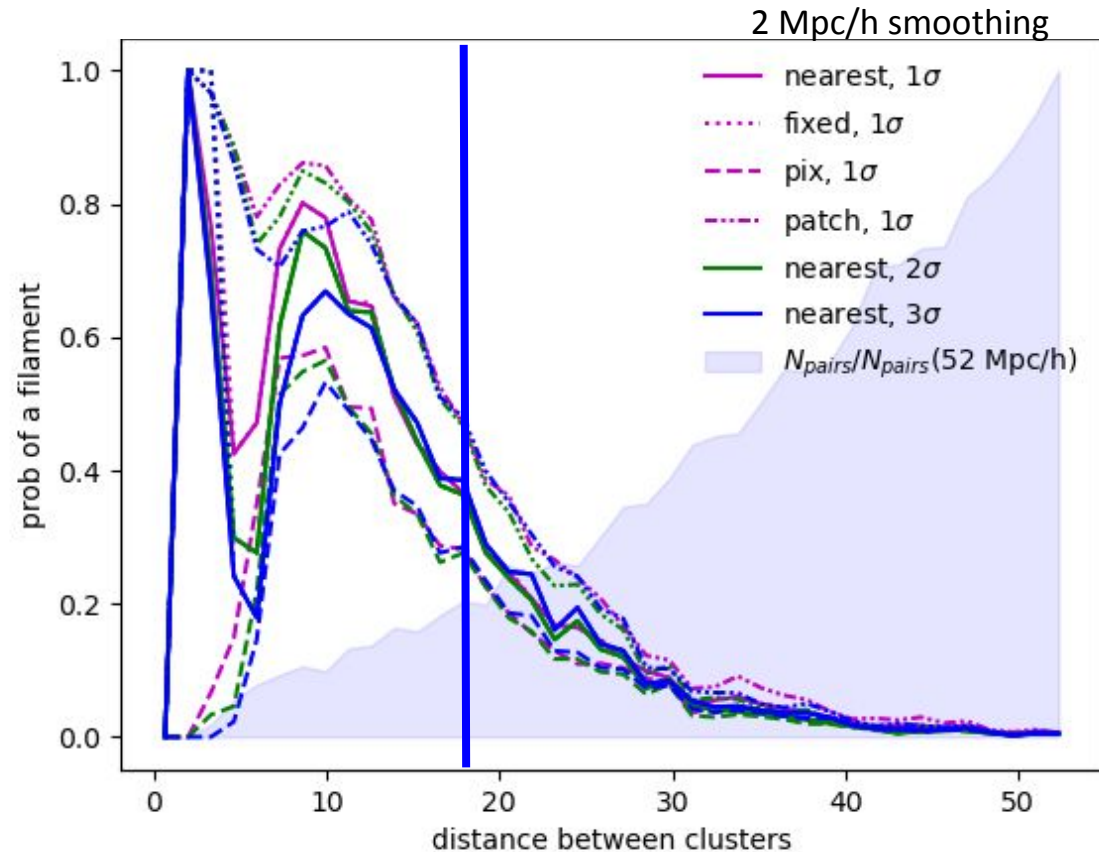


# Before: which clusters -> nodes?

# Now: which cluster pairs -> filaments?

A pair is more likely to have a Disperse filament if the clusters:

- are close together
- have long axes aligned with cluster pair axis
- using ML (later)
  - cluster is one of closest other clusters
  - have long axes aligned with each other



For this 2 Mpc/h smoothing, median length for filaments matched to cluster pairs is about 18 Mpc/h  
(all filaments, median length  $\sim$  16 Mpc/h)




# Profiles: on average, enhanced around cluster pairs (on axis)

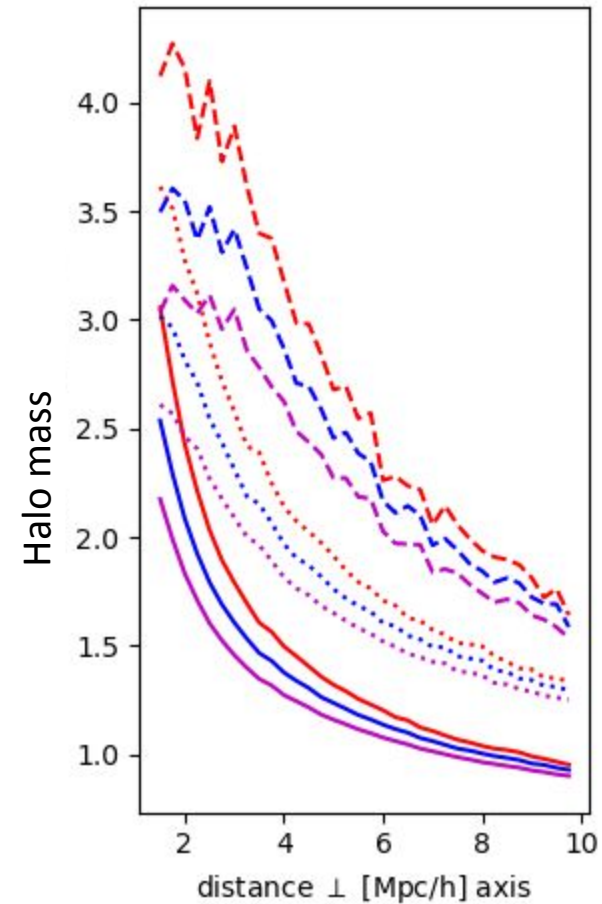
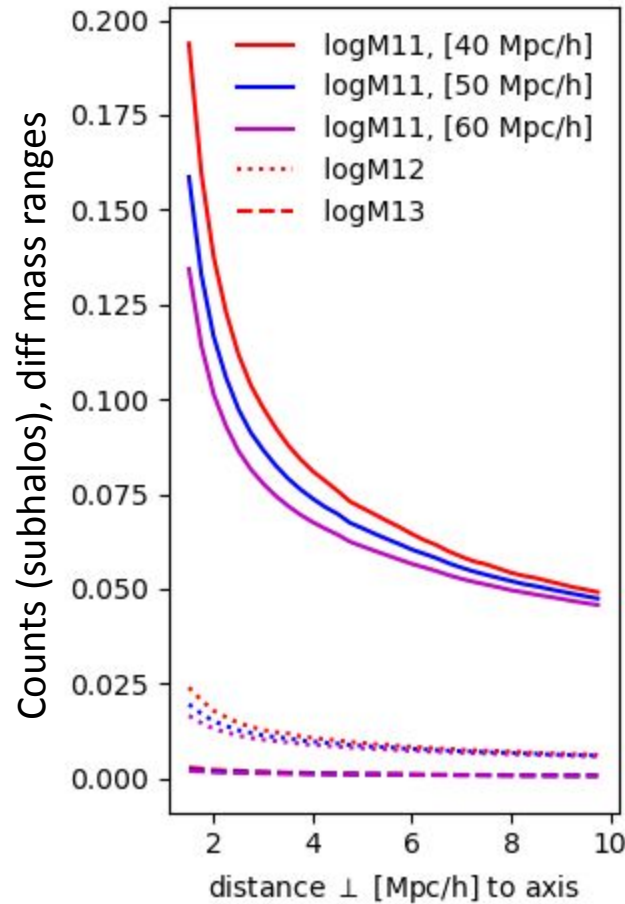
Counts (gal subhalos)

Mass (halo centers)

Pairs < 40, 50, 60 Mpc/h

subhalo/halo mass ranges

$10^{11} - 10^{12} M_{\odot}$    
 $10^{12} - 10^{13} M_{\odot}$    
 $10^{13} - 10^{14} M_{\odot}$  



# Profiles: density enhanced even more, on average, for filaments!

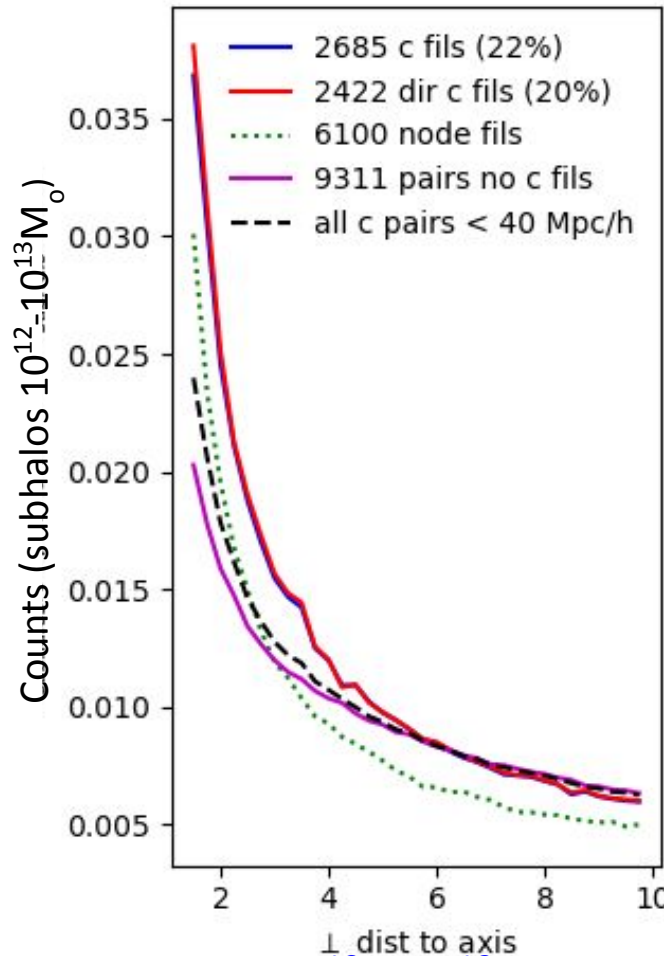
Different profiles:

- all cluster pairs
- filament pairs
- non-filament pairs
- nodes

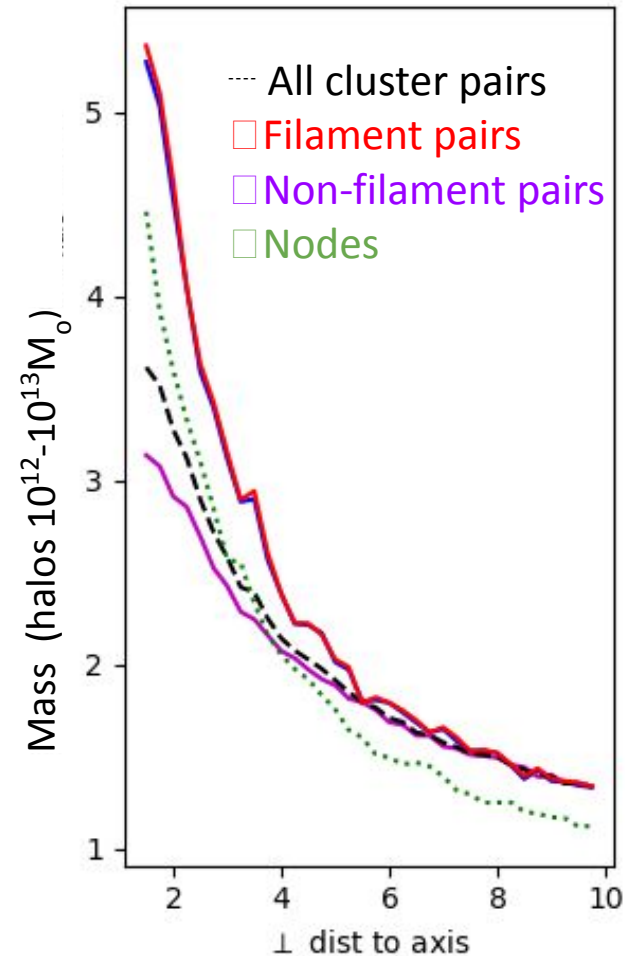
from 2 Mpc/h,  $3\sigma$   
persistence web

profile  $\sim 1/r$

Counts (gal subhalos)



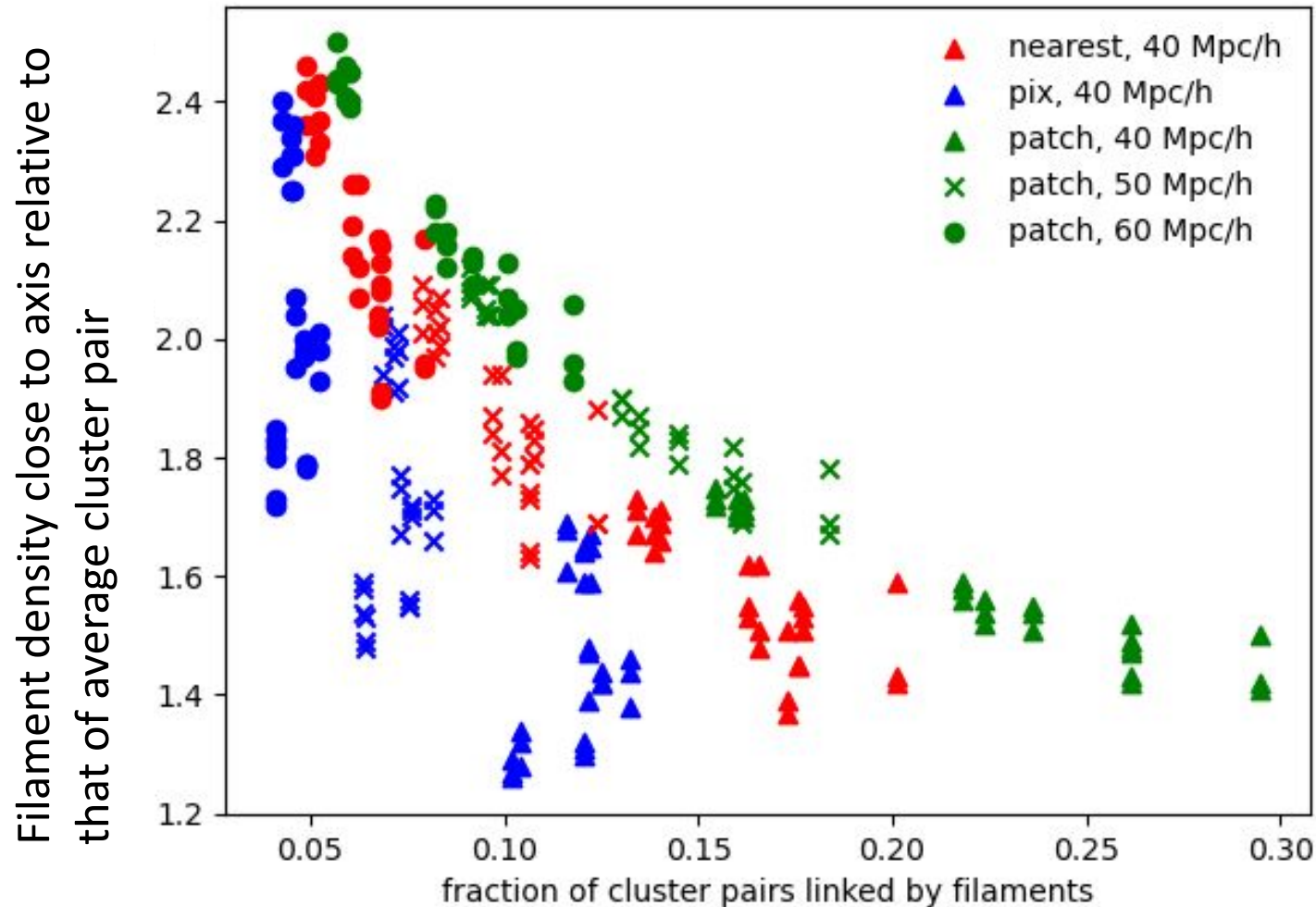
Mass (halo centers)



$10^{12} - 10^{13}M_{\odot}$ , pairs < 40 Mpc/h

# Filament density enhancement relative to all cluster pairs (@ max) for different webs, matching methods, max pair lengths

As might be expected, when *fewer cluster pairs* are assigned filaments, the cluster filament pair profile is *more enhanced* relative to all cluster pairs





# Different webs/matching →

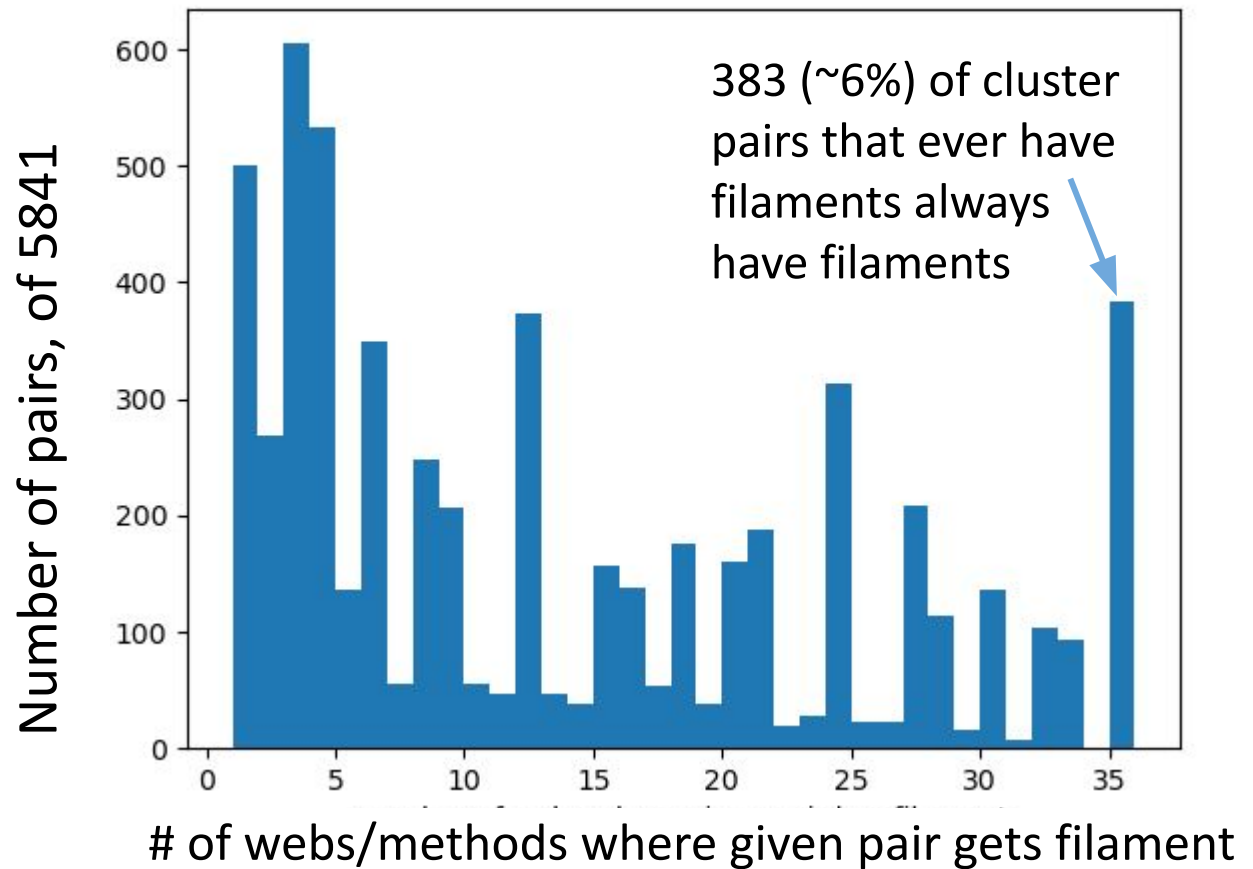
(Before: different clusters get nodes)

Here: different cluster pairs get filaments

Clusters to nodes:  
¾ of clusters  
always matched to  
nodes

Cluster pairs to  
filaments:  
< 1/10 pairs which  
always match to  
filaments

(383 of 1400-3500  
pairs always get  
filaments)



# Filaments as operation on cluster pairs

Large scale filaments in a web → map on cluster pairs

Have 11996, 20906, and 33842 pairs  $< 40$  Mpc/h, 50 Mpc/h, 60 Mpc/h, respectively

Easy to set up as ML problem:

- each pair gets 1 (filament) or 0 (no filament)
- out of box algorithms not very successful for these filaments
  - misclassified 6%-12% of cluster pairs
  - inputs: distance, cluster axes dot product, cluster axes dot product with long axis, cluster density, etc.  
(only use properties of cluster population)

# Clusters and other webs?

Beyond Disperse:

Sometimes hard to compare webs to each other

Change webs–cluster pairs are fixed, but connectivity and matching to nodes change

- Can use clusters & cluster pairs to compare webs to each other, fixed reference point
- Useful if consistent mapping to clusters used  
(doesn't have to be ones suggested here)

[Again, there are a ton of different web definitions, in part, because there are a ton of different web uses.]

# Directions

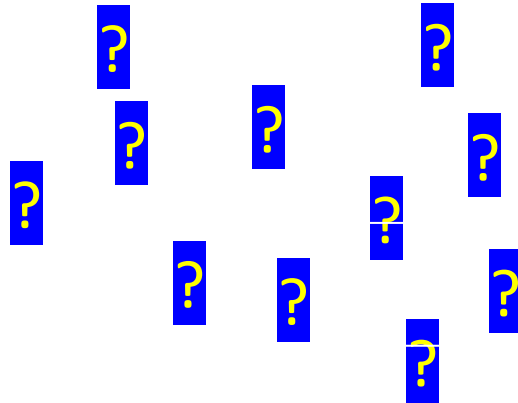
- More properties of this restricted web?
- Different webs:
  - Use level instead of persistence
  - Drop lower persistence webs when look for filaments that persist
- Cluster pairs do indicate where mass density will likely go
  - How much can one infer from pairs-> filaments, etc?\*
  - How much of rest of mass distribution? Shear field?
- Build up web? Go below cluster mass:
  - some halos will be most massive halo near a node—which ones?

\*Note: can reconstruct web from clusters other ways

- Use clusters to get initial conditions & evolve → everything  
(Bos, van de Weygaert, Kitaura, Cautun '16, esp. clusters; also via ic:  
Leclercq, Lavaux, Jasche, Wandelt '16)

Just trying reductionist approach here to see how far it can go....

# Cartoon idea

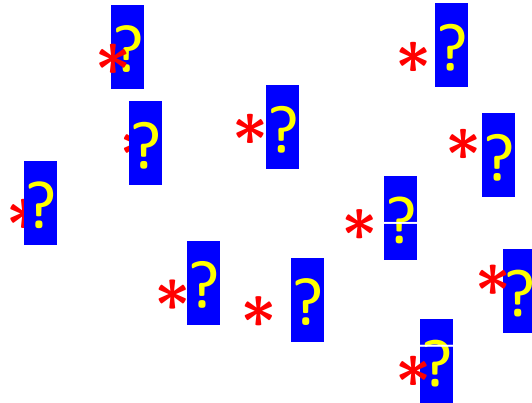


Start with clusters

\* = Massive nodes, — = filament ?? clusters  
(Note: some overdensities might be projection)



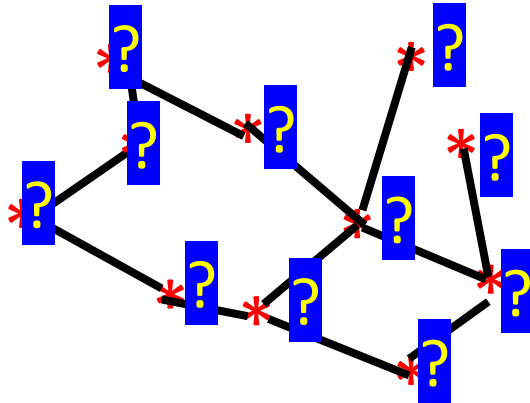
# Cartoon idea



Start with clusters  
Most massive *likely* to be  
nodes

\* = Massive nodes, — = filament ?? clusters  
(Note: some overdensities might be projection)

# Cartoon idea

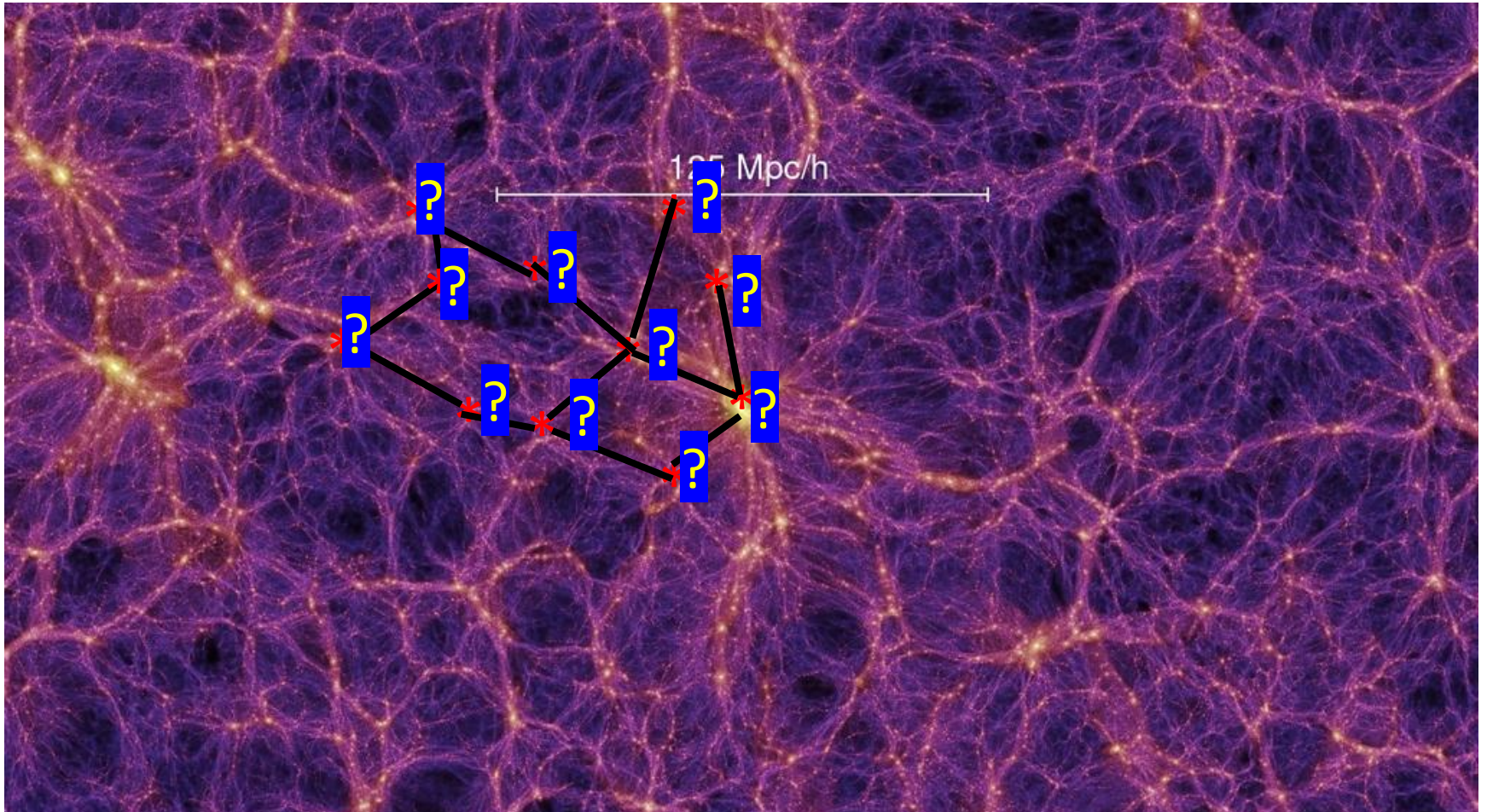


Start with clusters  
Most massive *likely* to be nodes  
Clusters close by often connected by filaments...  
But often not, and over half of the filaments aren't to close-by clusters

\* = Massive nodes, — = filament **??** clusters

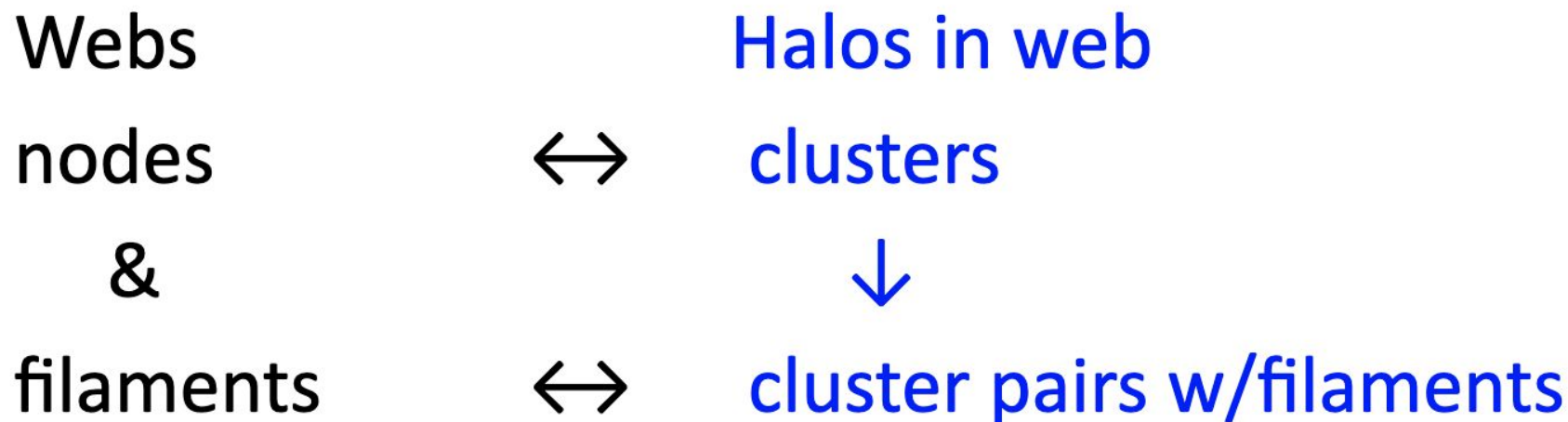
(Note: some overdensities might be projection)

# Cartoon idea



\* = Massive nodes, — = filament ?? clusters?  
(Note: some overdensities might be projection)

Started with:



Some points:

- Most, but not all clusters match to nodes, across different webs
  - high mass clusters more likely, cluster mass  $\sim$  node density
- Cluster pairs have enhanced average density profile, filament pairs even more so, but which cluster pairs are assigned filaments varies significantly as webs vary
- higher density nodes & filaments more likely to match to clusters & cluster pairs
- web restricted to clusters very sparse!

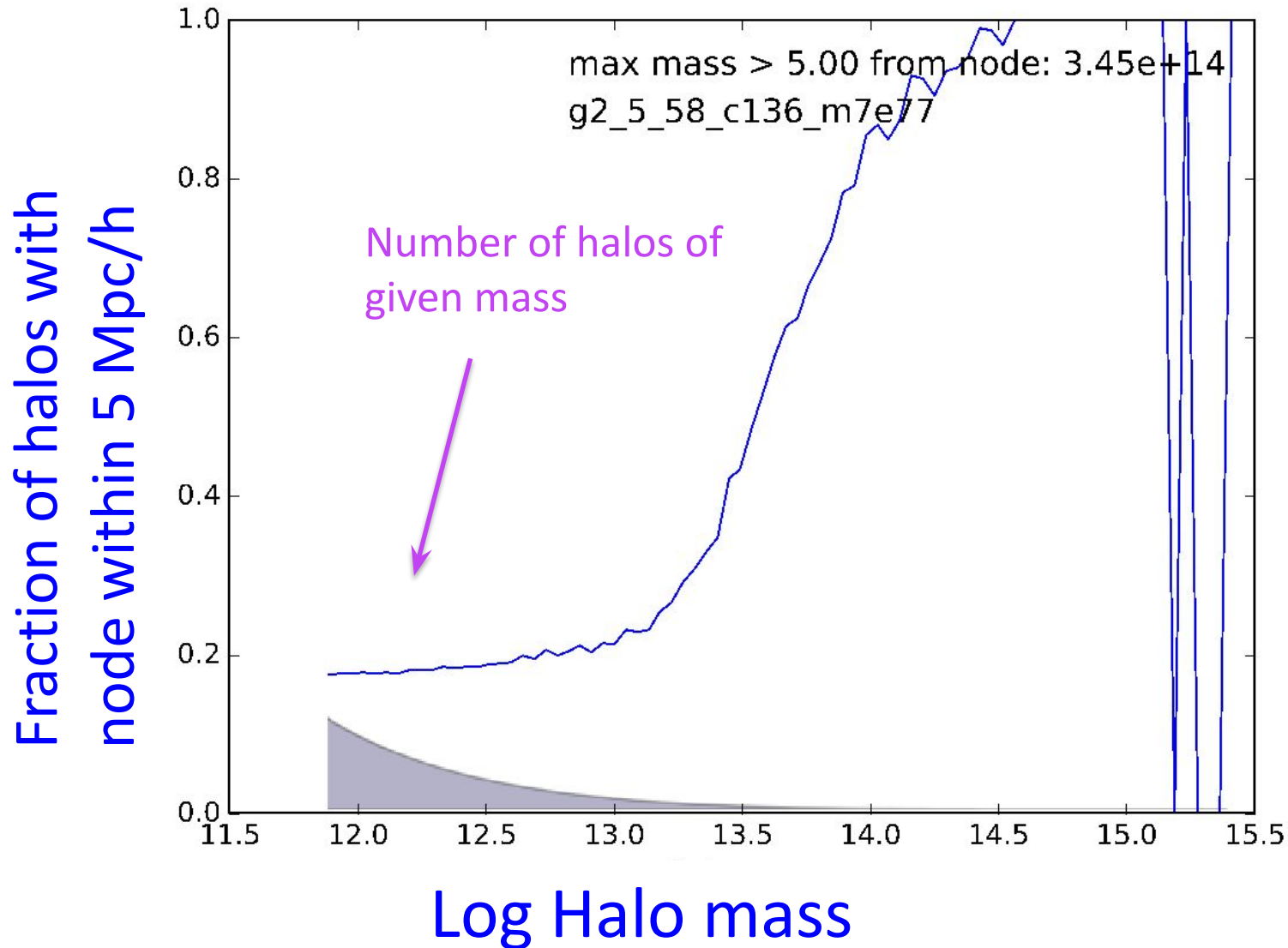
Thank you!



# Completeness?

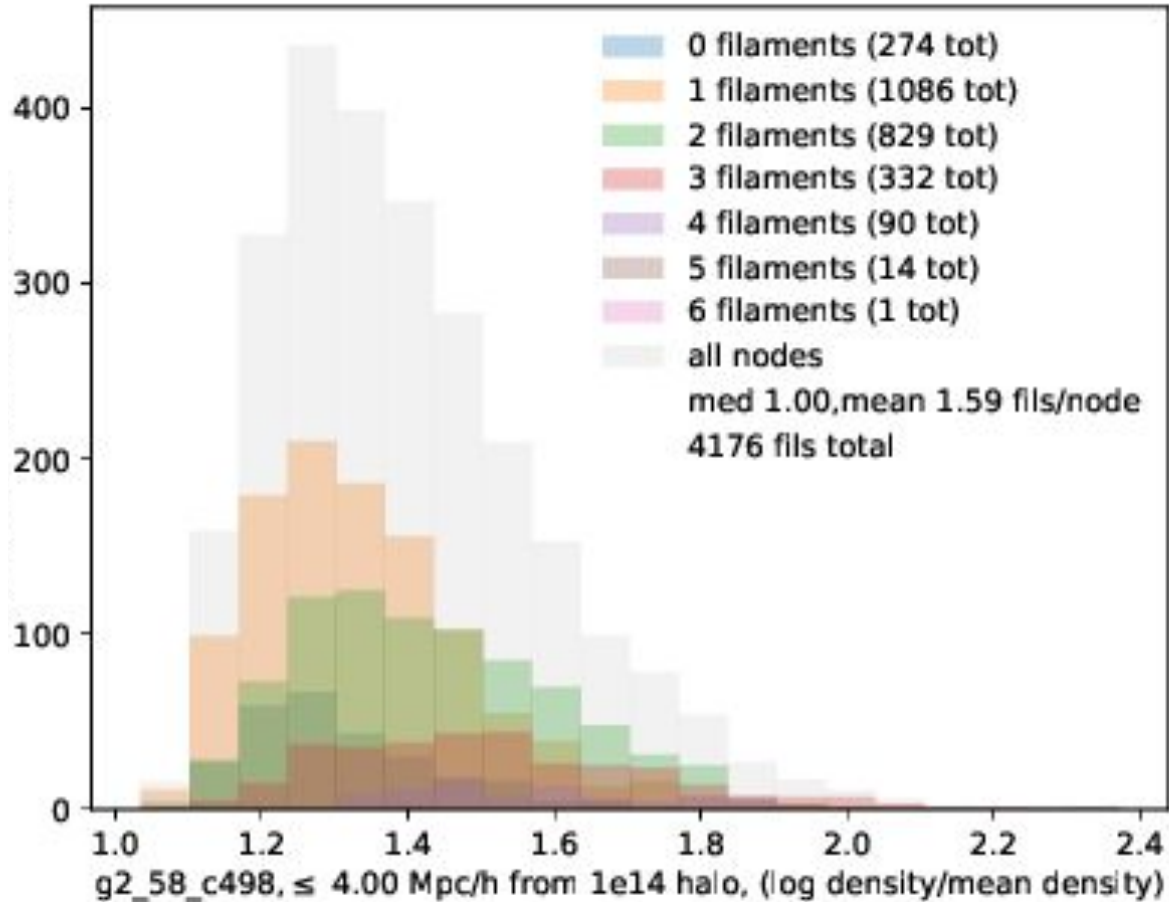
Fraction of halos with “nearby” node

(Disperse pixel based web, smoothing 2.5 Mpc/h)



# connectivity of “matched” nodes to other “matched” nodes **only**

Number of nodes (of 2588 matched)



log (pixel density/mean density)