



# Spins and mechanics in diamond

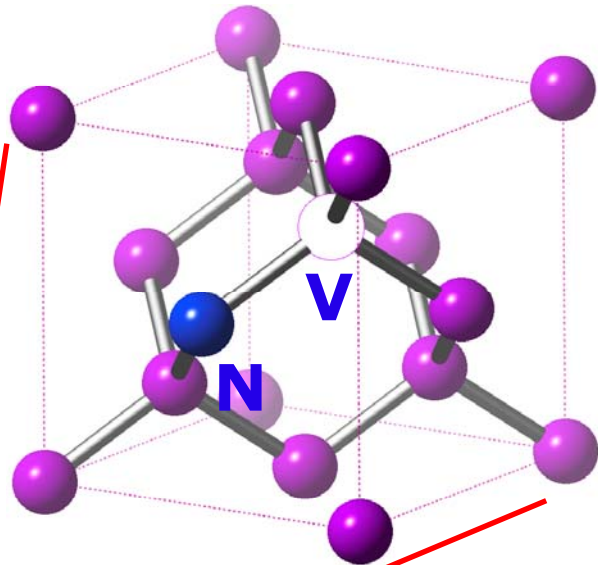
KITP  
Nov 3, 2015

**Donghun Lee, Kenny Lee, Preeti Ovardchaiyapong, Jeff Cady**

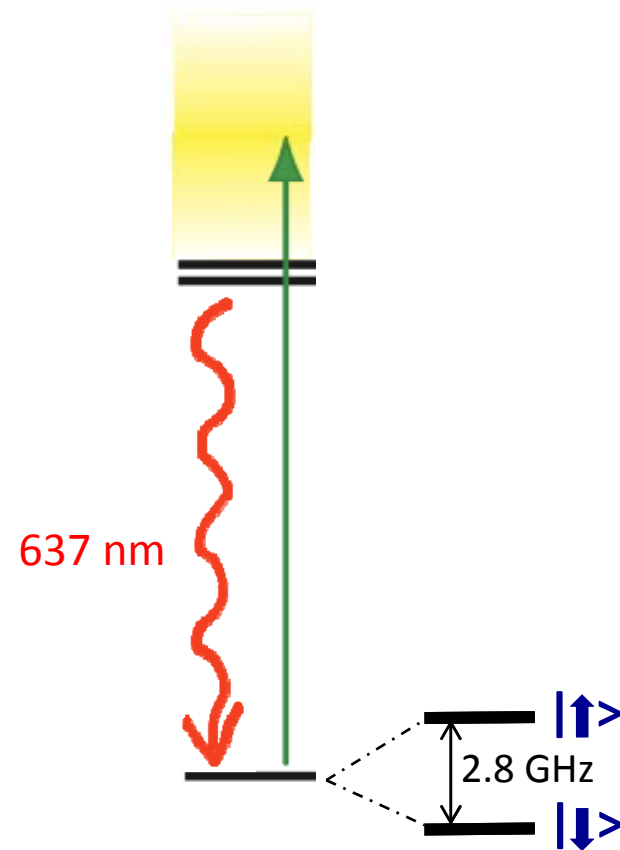
**Ania Jayich**  
UC Santa Barbara

# Nitrogen-vacancy centers in diamond

- A defect in the diamond lattice.
- Has an associated electronic spin and an optical transition
- Marries solid state and atomic physics



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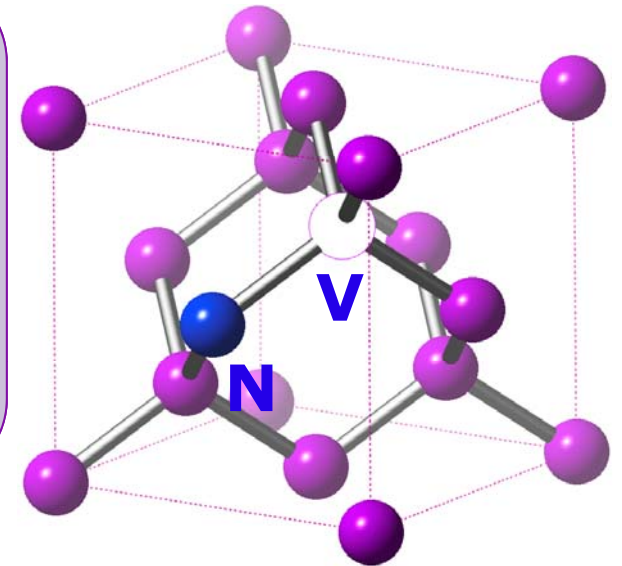


David D. Awschalom, Diamond Age of Spintronics. *Scientific American* (October 2007).

# Nitrogen Vacancy Centers in Diamond

Interesting for quantum devices

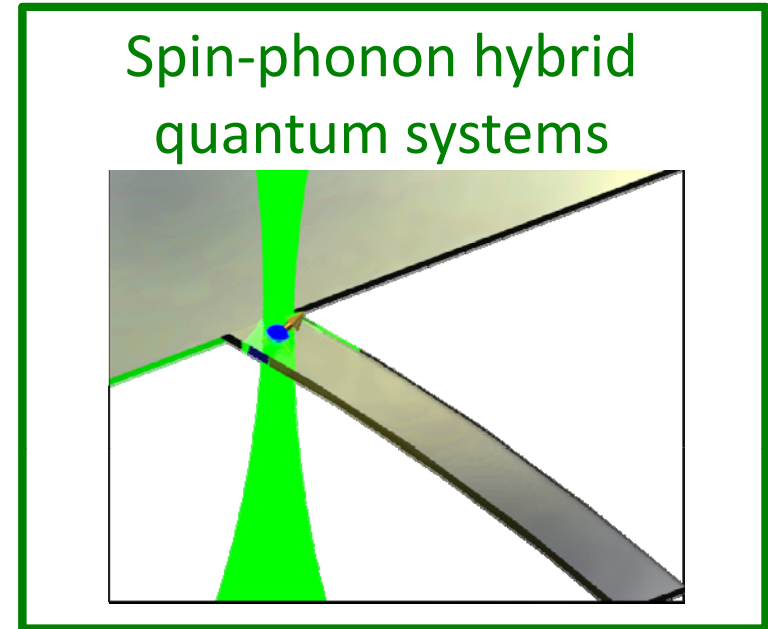
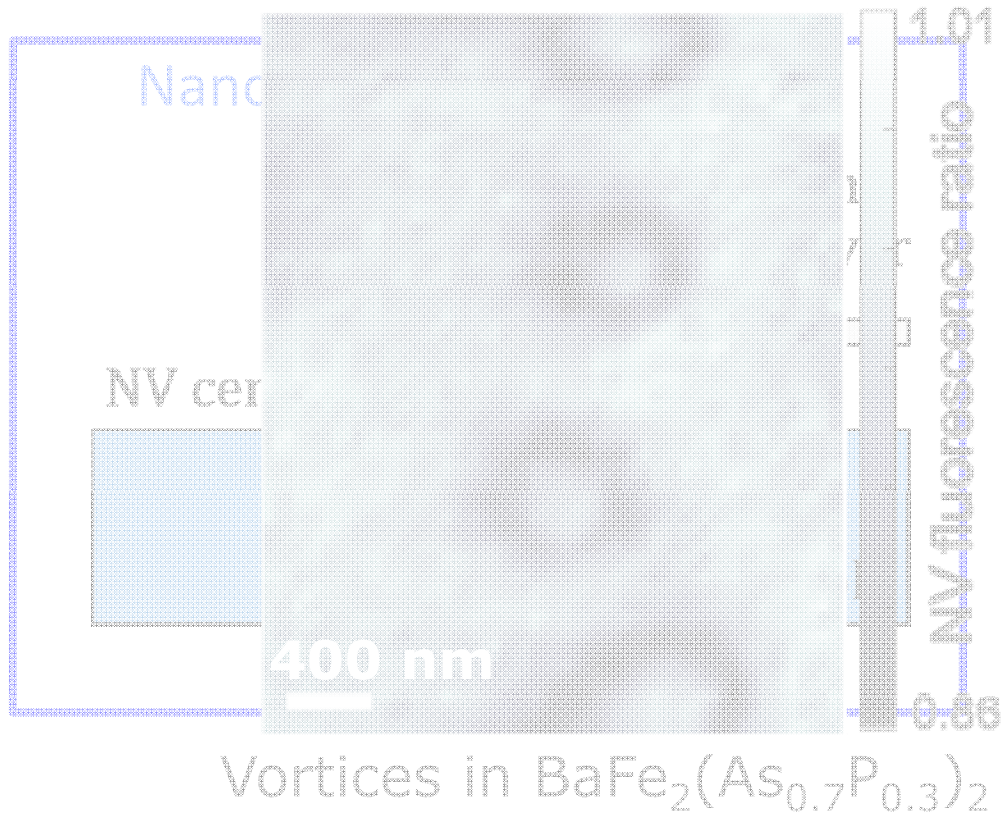
- Long ( $\sim 5$  ms) spin coherence times at 300 K
- Solid-state system
- Spin state can be optically initialized, coherently controlled with microwaves, and optically readout



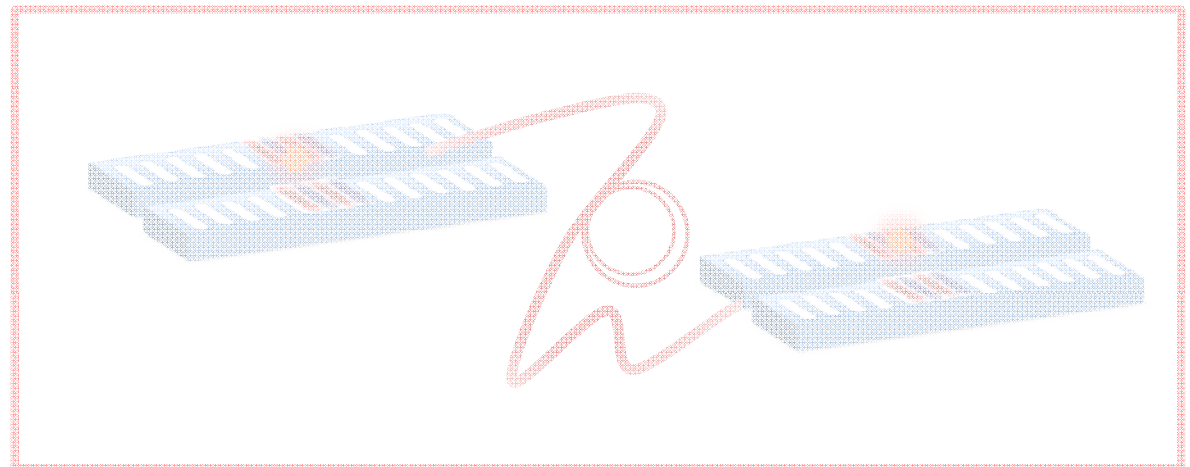
## Applications

- magnetometry \*\*
- quantum information processing \*
- single photon sources
- fluorescent biomarkers
- electrometry, thermometry

# Jayich research group thrusts



Spin-photon hybrid quantum systems:



# Mechanical coupling to spin: motivation

## ◆ Enhanced control of NV spin state

- Strain tuning of NV<sup>-</sup> zero phonon line

Electric field tuning

Tamarat *et al*, *NJP* **10**, 045004 (2008)  
Basset *et al.*, *PRL* **107**, 266403 (2011)

- Enhanced spin state control

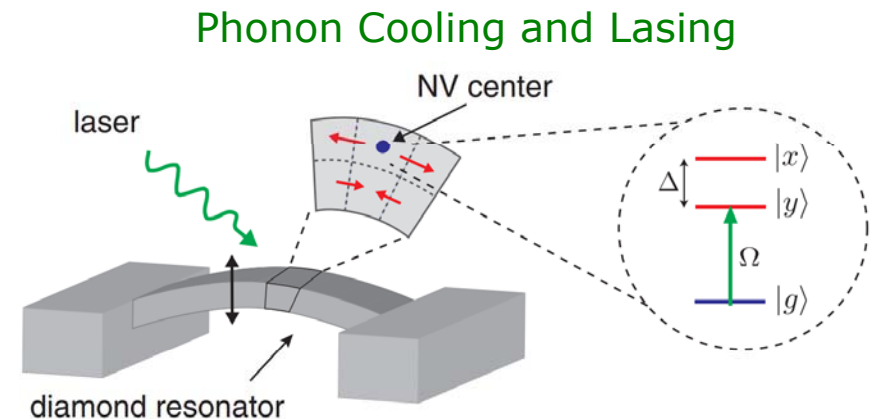
E. R. MacQuarrie, *et al Optica* **2**, 233 (2015)

## ◆ Transduction of quantum information

- Phonons can mediate spin-spin or spin-photon interactions

Rabl *et al*, *Nature Physics* **6**, 602 (2010)

- Quantum control of mechanical resonator



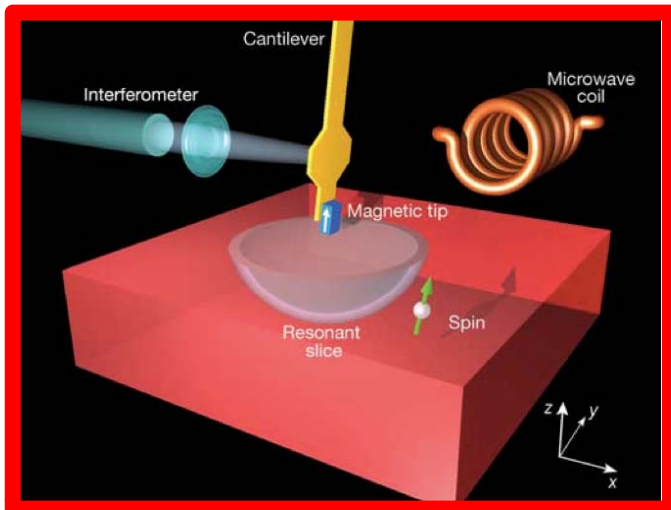
Kepesidis *et al.*, *PRB* **88**, 064105 (2013).

## ◆ Strain and phonons play an important role for NVs as quantum memories

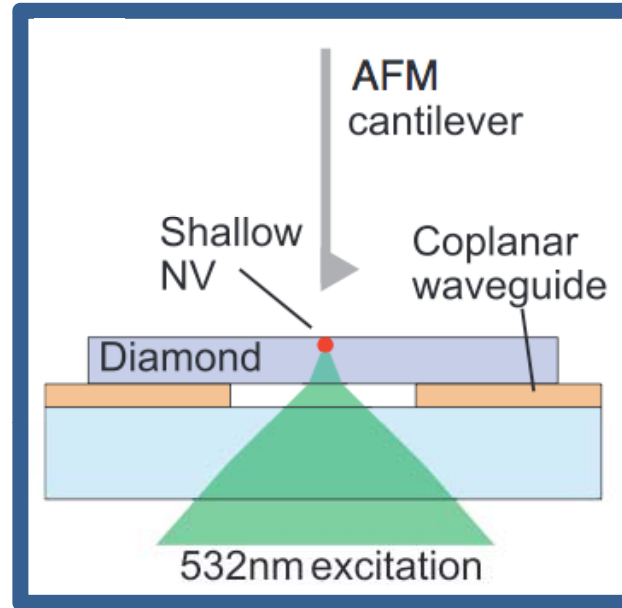
M.L. Goldman, *et al Phys. Rev. Lett.* **114**, 145502 (2015).



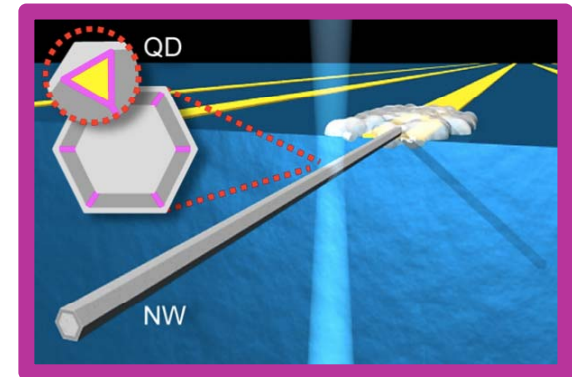
# Variety of spin-mechanical systems



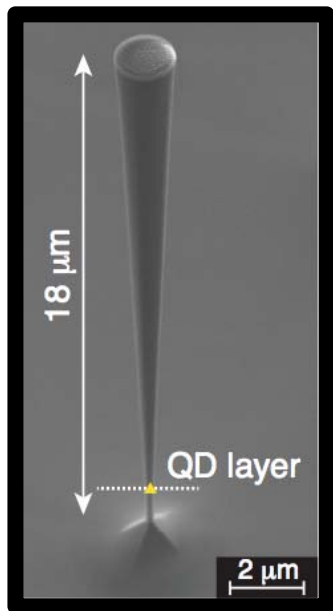
Rugar et al, Nature **430**,329 (2004)



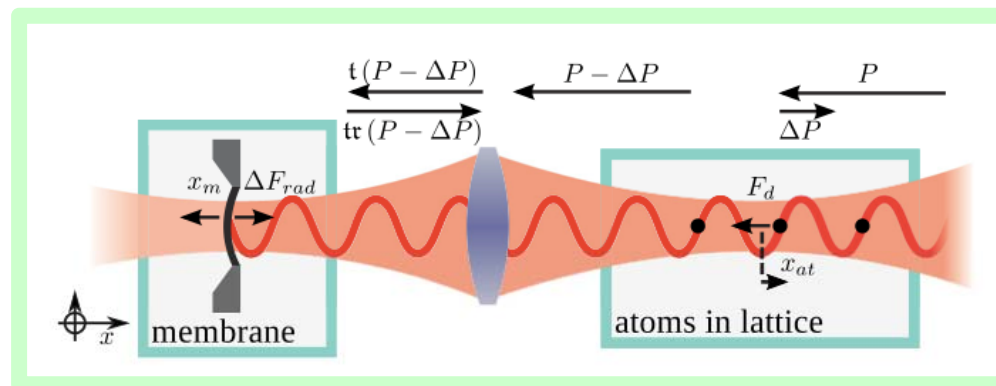
Kolkowitz et al, Science **335**, 1603 (2012)



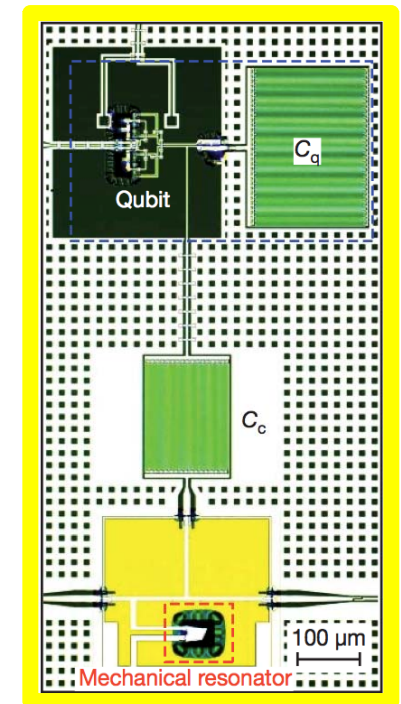
Montinaro, et al, Nano Lett. **14**, 4454 (2014)



Yeo et al, Nature Nano **9**, 106 (2014)



Camerer et al, PRL **107**, 223001 (2011),

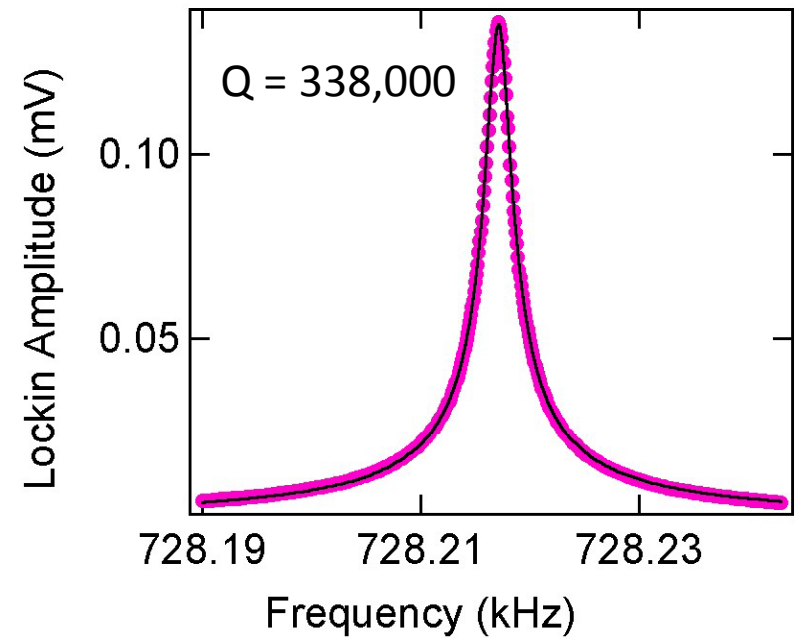


O'Connell et al, Nature **464**, 697 (2010)

# The diamond platform: benefits and challenges

## Benefits:

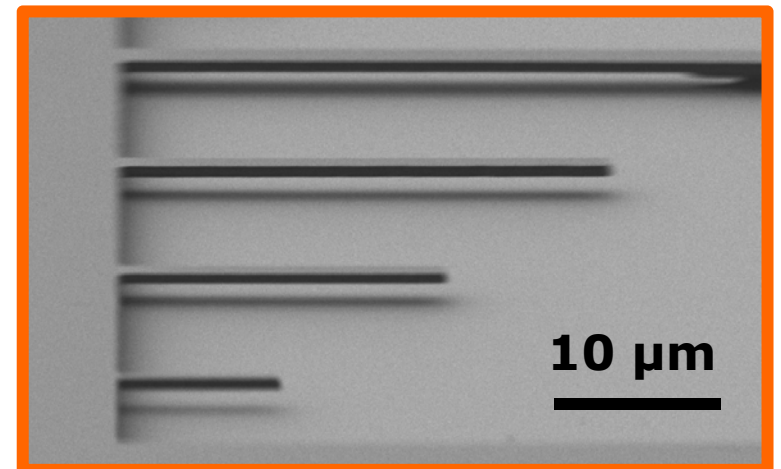
- Long NV spin coherence times
- Low intrinsic mechanical dissipation
- Integrated, monolithic structure



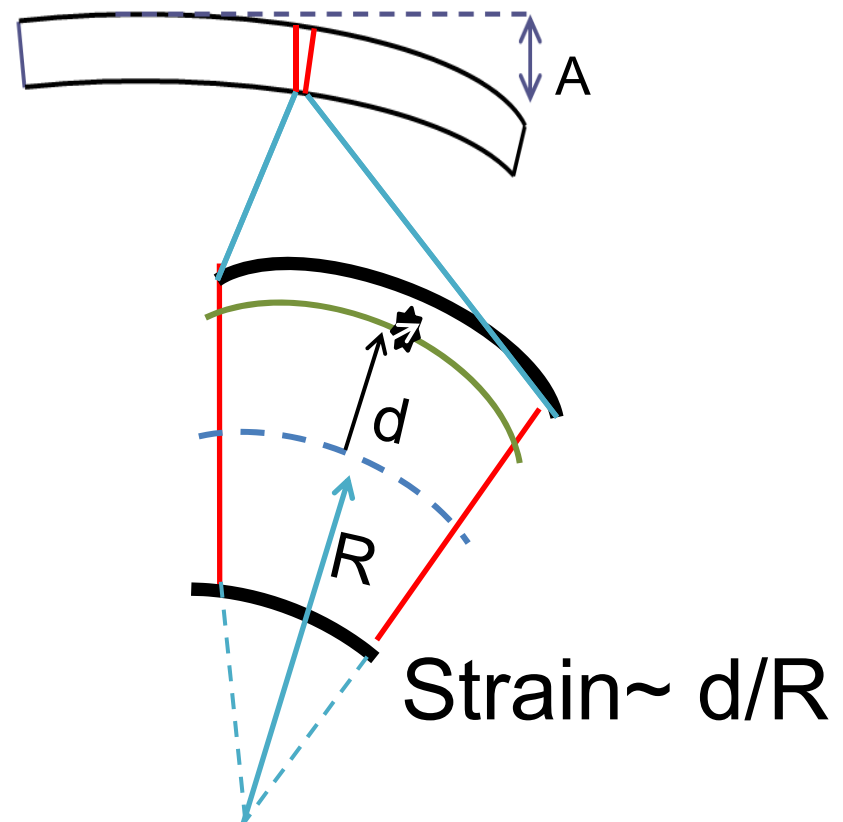
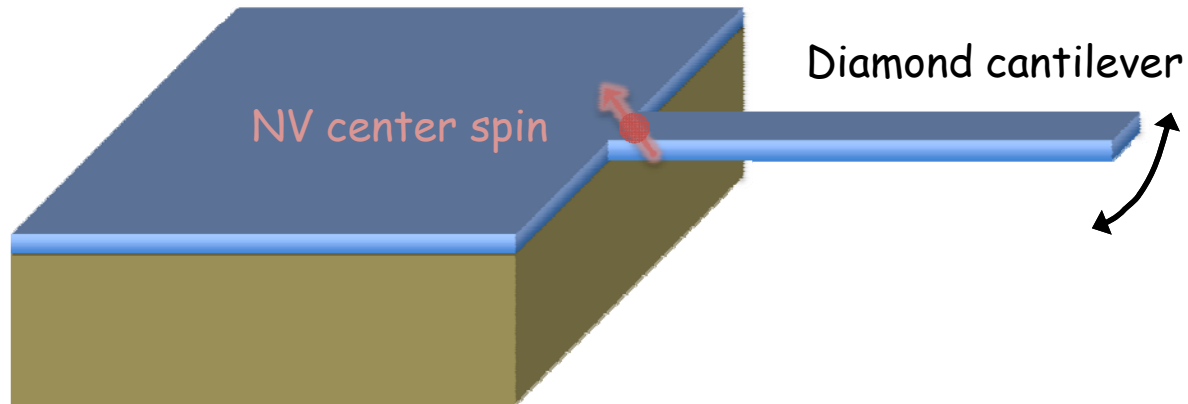
Ovartchayapong *et al*, *APL* **101**, 163505 (2012)

## Challenges:

- Diamond nanofabrication was immature
- NV strain interaction was not well characterized



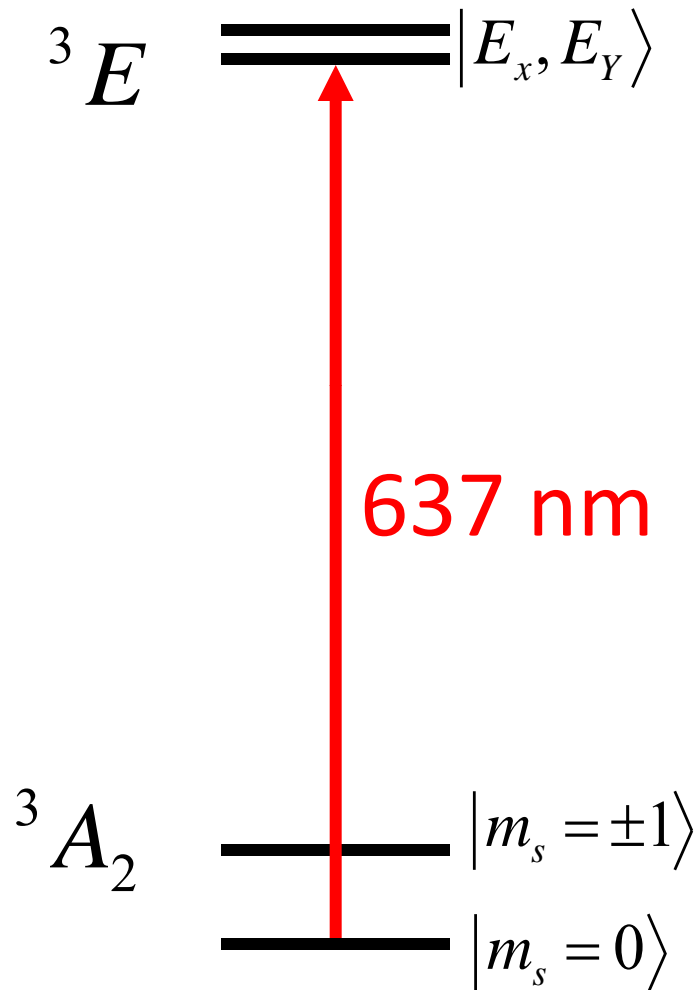
# Strain-mediated coupling



- Can control strain with NV depth and amplitude of bending
- Can control angle of strain with respect to NV axis
- Highly controlled platform for strain application



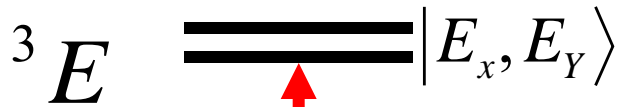
# Ground and excited state NV strain coupling



- Excited state:
  - Large strain coupling (1 PHz/strain)
  - Useful for coupling to photons
  - Good for quantum control (cooling)
- Ground state:
  - Long spin coherence time (ms) – good for storage
  - Useful for spin squeezing<sup>1</sup>
  - Relatively small (GHz/strain) coupling

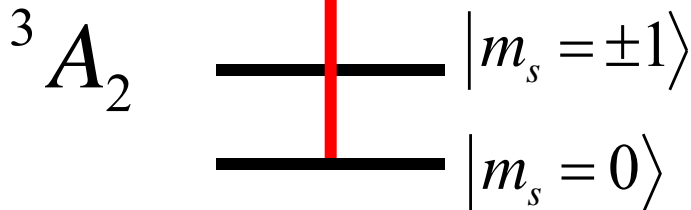
<sup>1</sup>S. Bennett, *et al*, *PRL* **110**, 156402 (2013).

# Ground and excited state NV strain coupling

${}^3E$    $|E_x, E_Y\rangle$

- Excited state:
  - Large strain coupling (1 PHz/strain)
  - Useful for coupling to photons
  - Good for quantum control (cooling)

637 nm

${}^3A_2$    $|m_s = \pm 1\rangle$   
 $|m_s = 0\rangle$

- Ground state:
  - Long spin coherence time (ms) – good for storage
  - Useful for spin squeezing<sup>1</sup>
  - Relatively small (GHz/strain) coupling

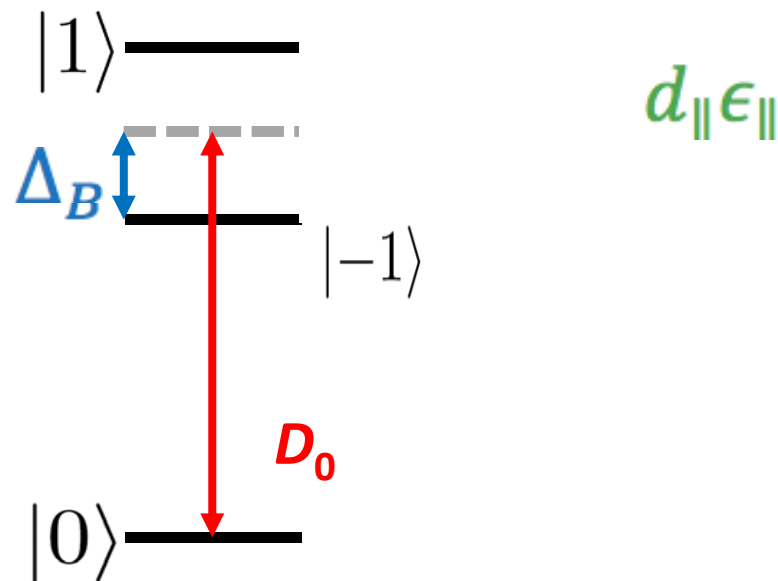
<sup>1</sup>S. Bennett, *et al.* *PRL* **110**, 156402 (2013).

# Strain interaction with NV ground state

$$H_{NV} = (D_0 + d_{\parallel}\epsilon_{\parallel})S_z^2 + \mu_B g \vec{S} \cdot \vec{B} - \frac{d_{\perp}\epsilon_{\perp}}{2} (S_+^2 + S_-^2)$$

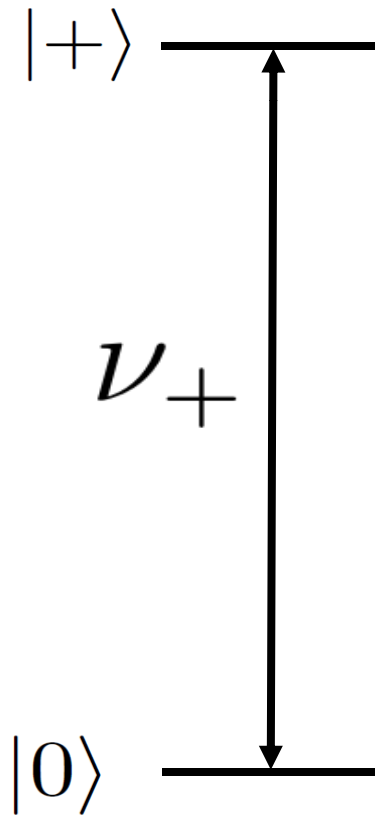
- Simple picture equates strain to electric field
- $d_{\parallel}$  and  $d_{\perp}$ : strain susceptibilities,  $\epsilon_{\parallel}$  and  $\epsilon_{\perp}$ : strain
- Strain parallel to NV axis shifts  $D$  (crystal field splitting)
- Perpendicular strain mixes  $|+1\rangle$  and  $|-1\rangle$

Ground state energy level structure in presence of strain and magnetic field:



# Defining the spin qubit

$$\nu_+ = D_0 + d_{\parallel}\epsilon_{\parallel} + \sqrt{(\gamma_{NV}B_z)^2 + (d_{\perp}\epsilon_{\perp})^2}$$



AC **parallel** strain modulates  
at **cantilever frequency**!

AC **perpendicular** strain  
modulates at  $\sim$  **twice cantilever  
frequency**!

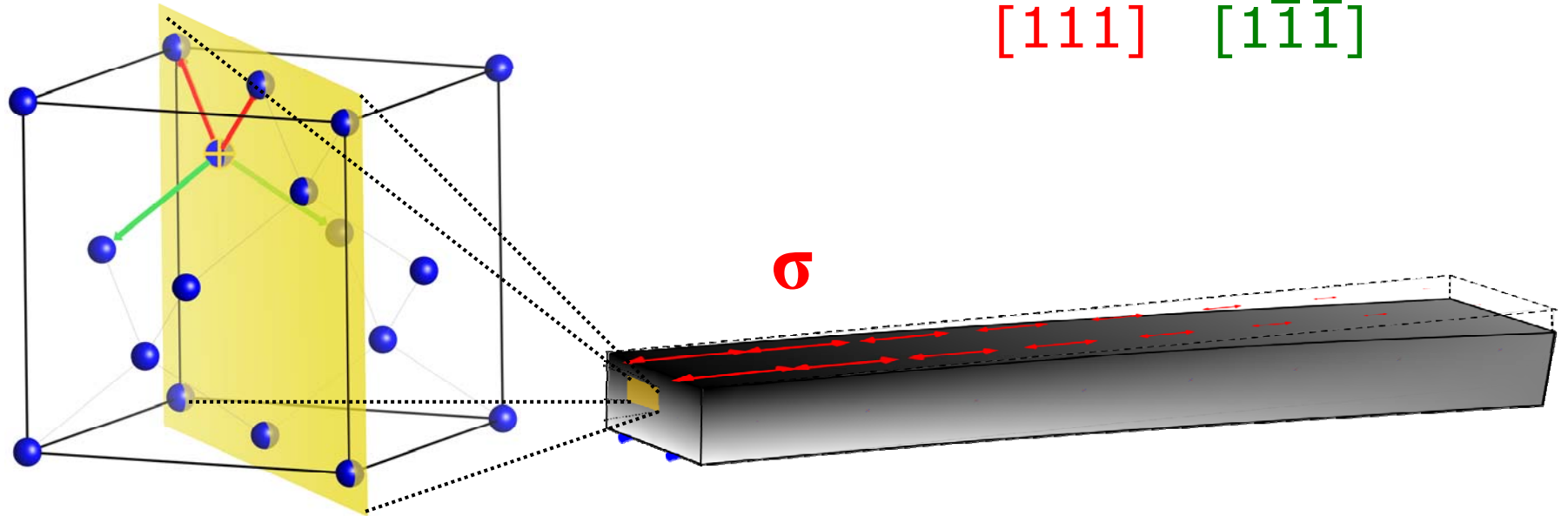
# Sensing strain with directionality

**Red class:**  
perpendicular strain  
is predominant

4 possible NV  
orientations:

$[111]$      $[\bar{1}\bar{1}\bar{1}]$

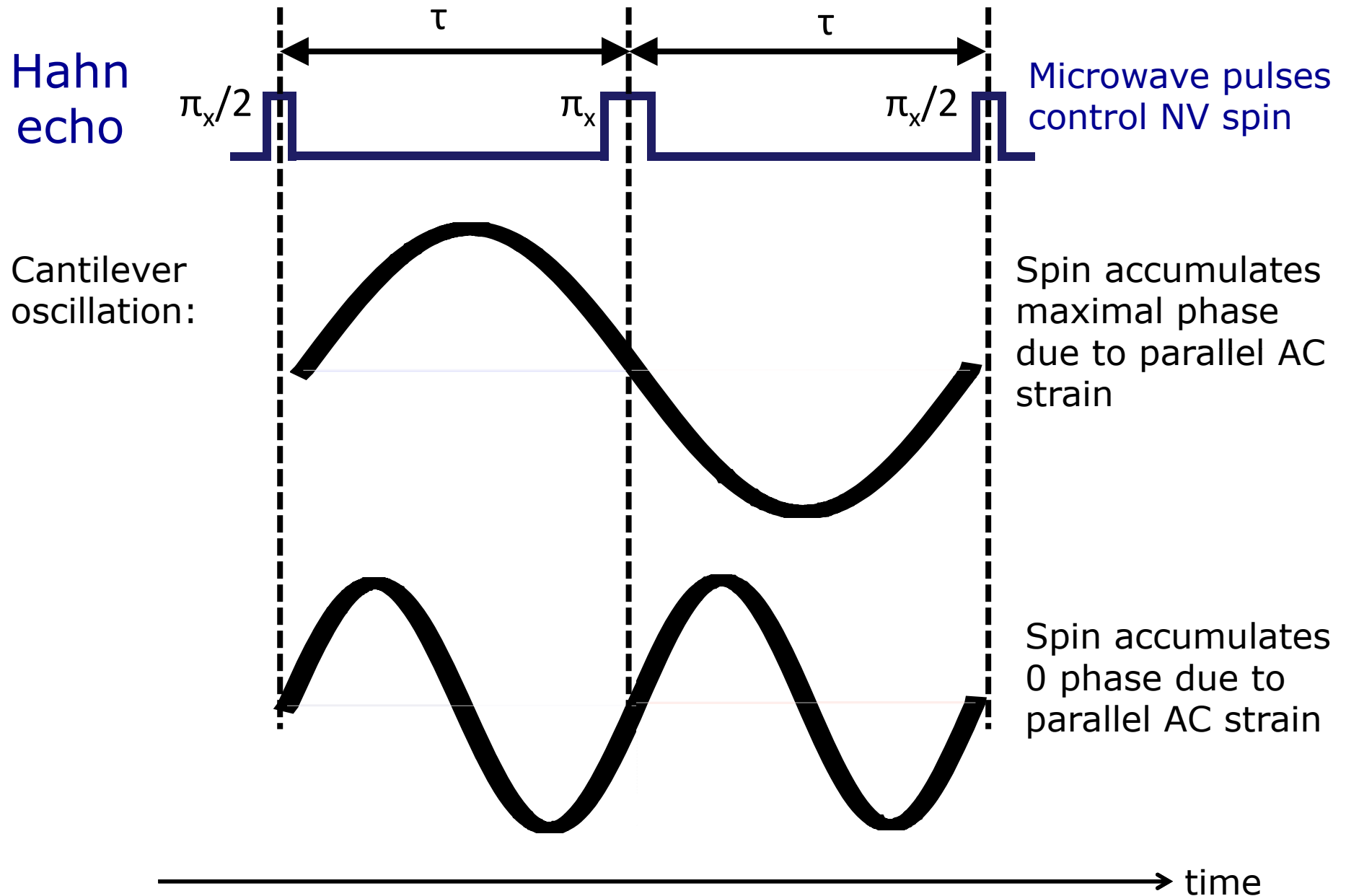
$[\bar{1}\bar{1}1]$      $[1\bar{1}\bar{1}]$



**Green class:** parallel  
strain is predominant

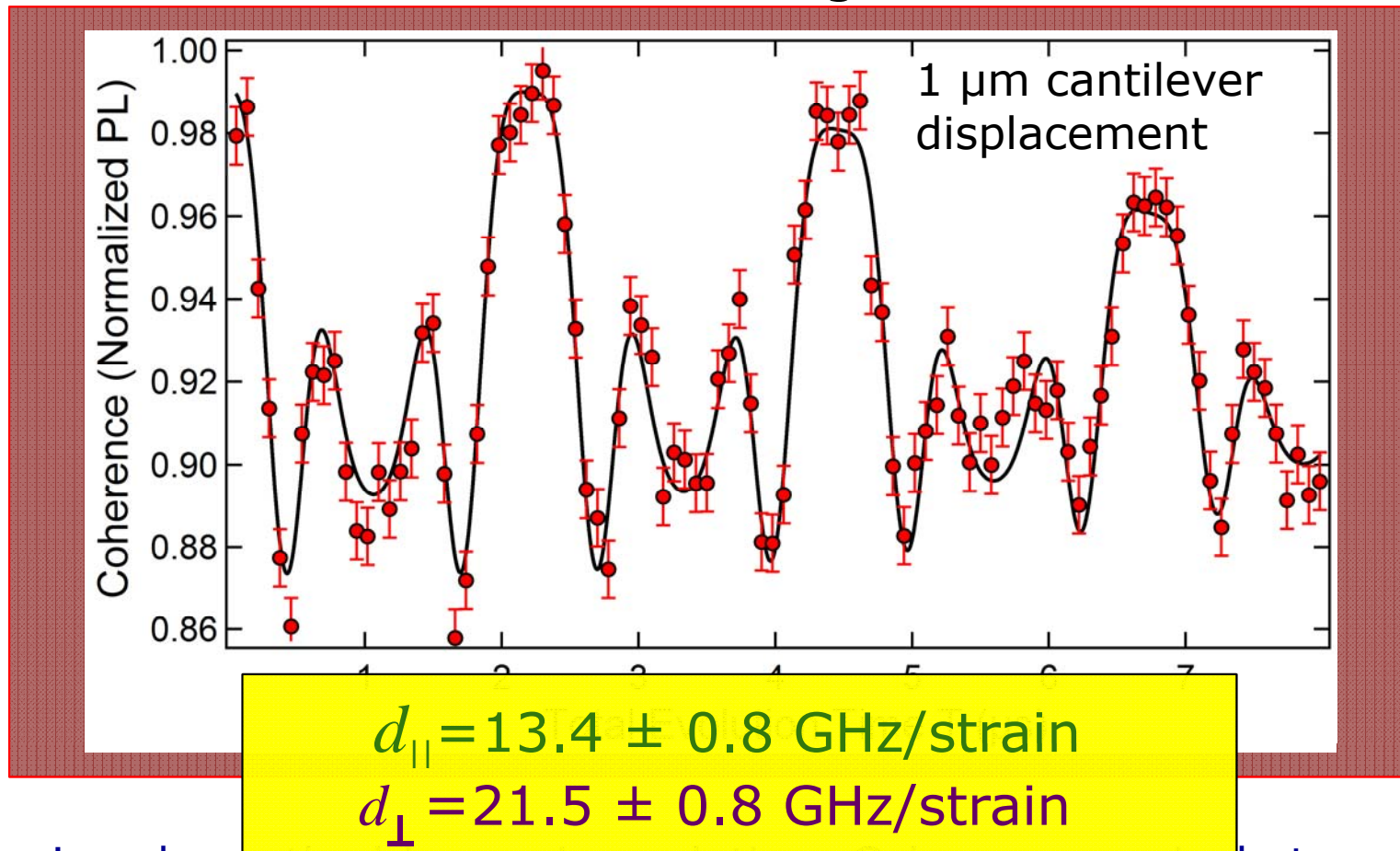


# Quantum control to reveal strain coupling



# Coherent detection of strain coupling

## Hahn Echo Signal

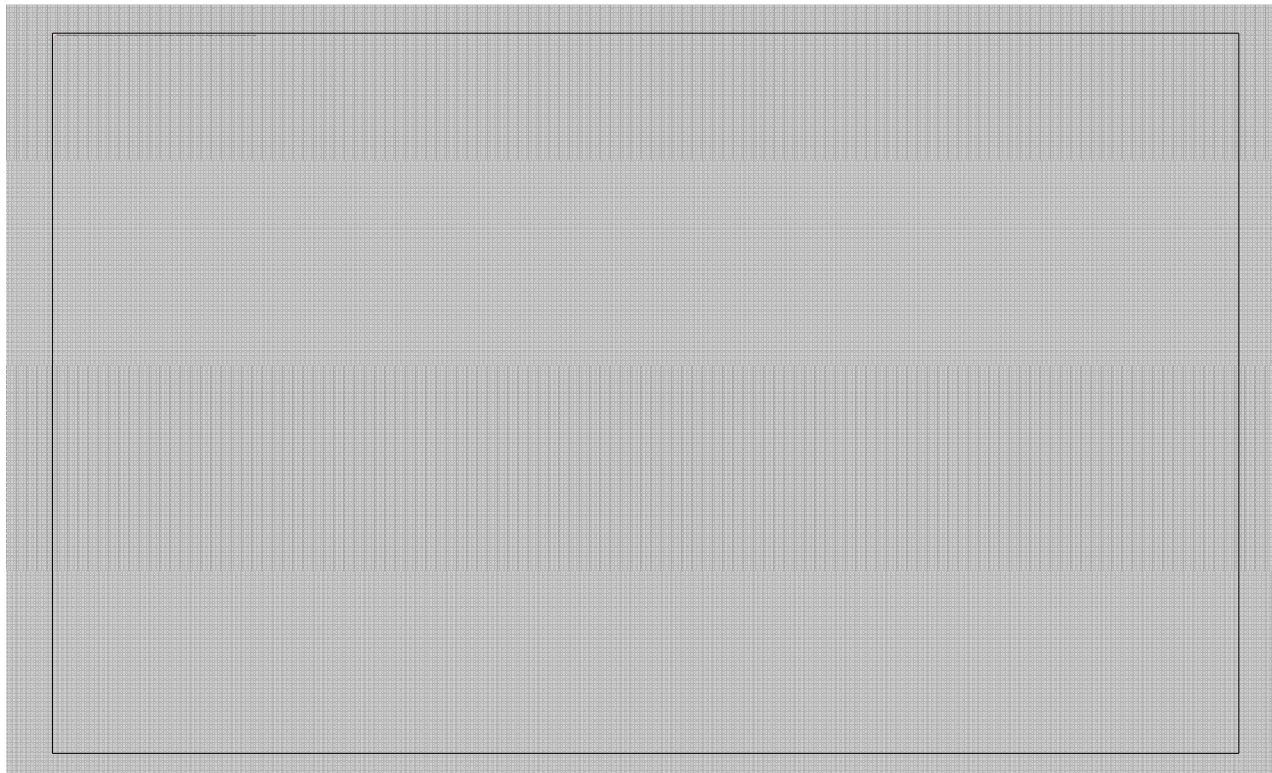
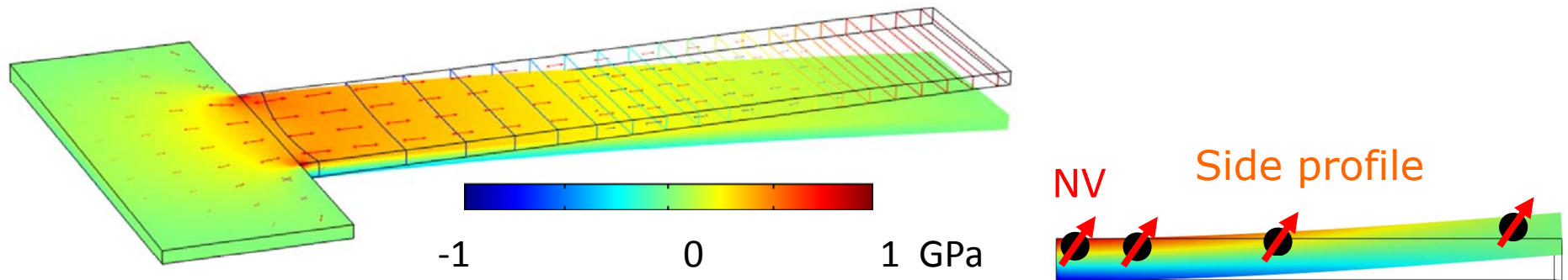


- AC strain coherently drives spin evolution: Coherence revival at  $\tau = 2\pi/\omega_{\text{cant}}$
- Parallel strain modulates qubit frequency at the resonator frequency

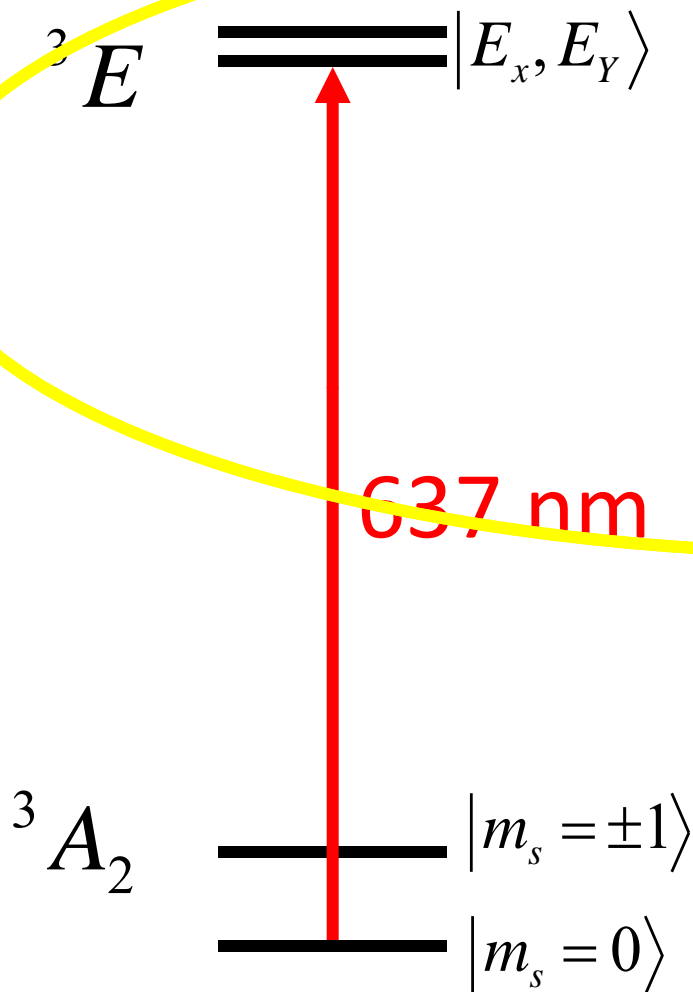
P. Ovartchayapong *et al*, *Nature Communications* **5**, 4429 (2014)  
Related work: Tessier *et al*, *PRL* 133, 020503 (2014)

# Nanoscale strain imaging along cantilever

Stress profile along cantilever:



# Ground and excited state NV strain coupling

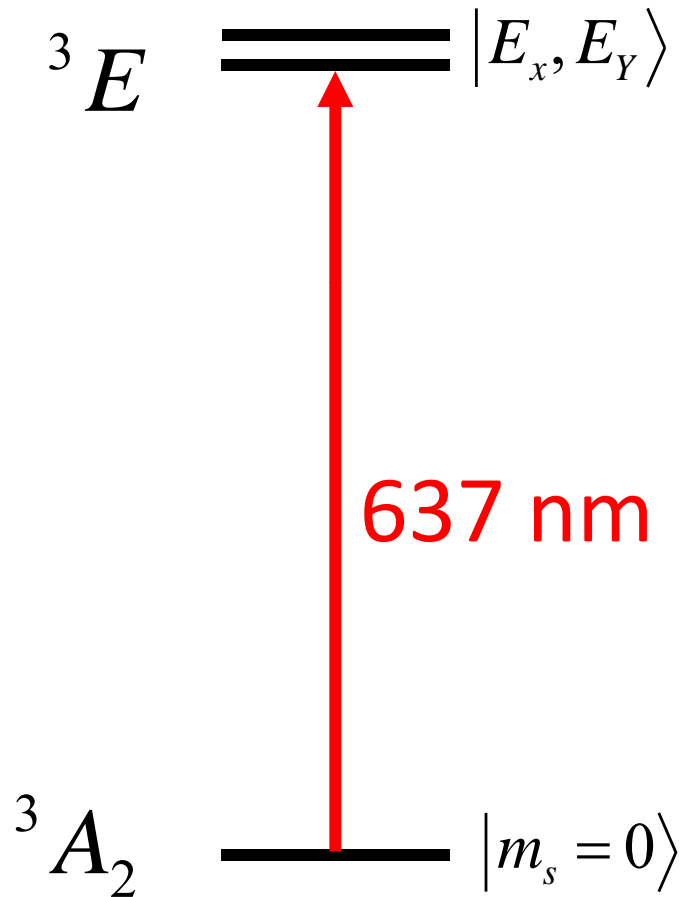


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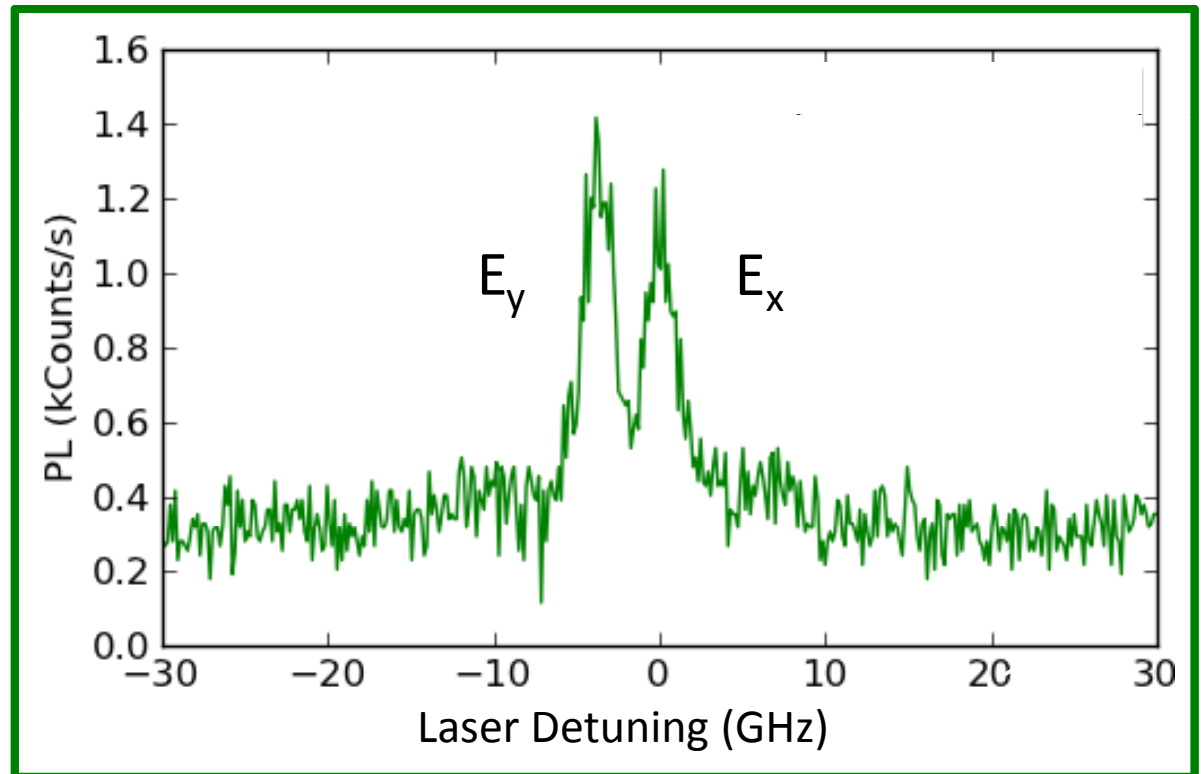
<sup>1</sup>S. Bennett, *et al*, *PRL* **110**, 156402 (2013).

# Excited state spectroscopy of NV in cantilever

- Resonant excitation of NV center at 5 K

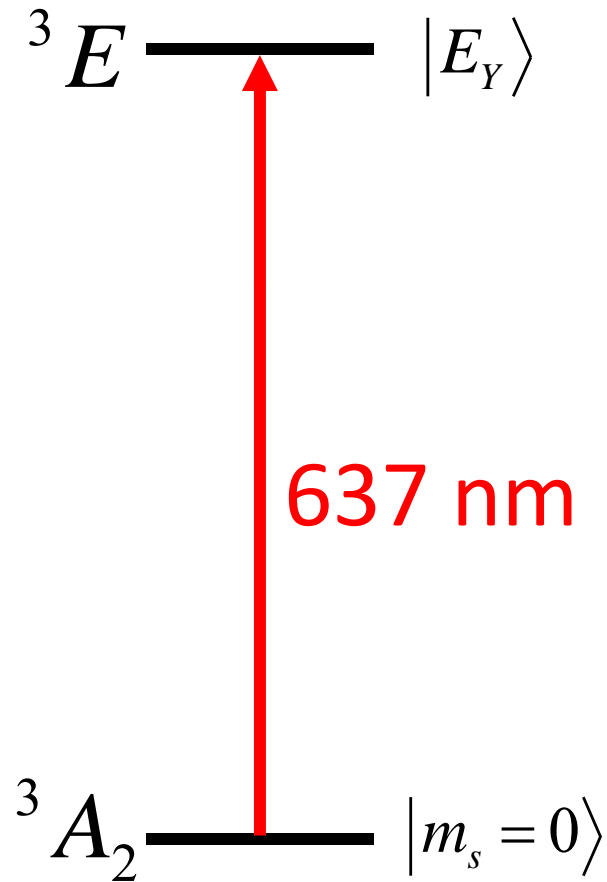


Photoluminescence excitation spectrum:

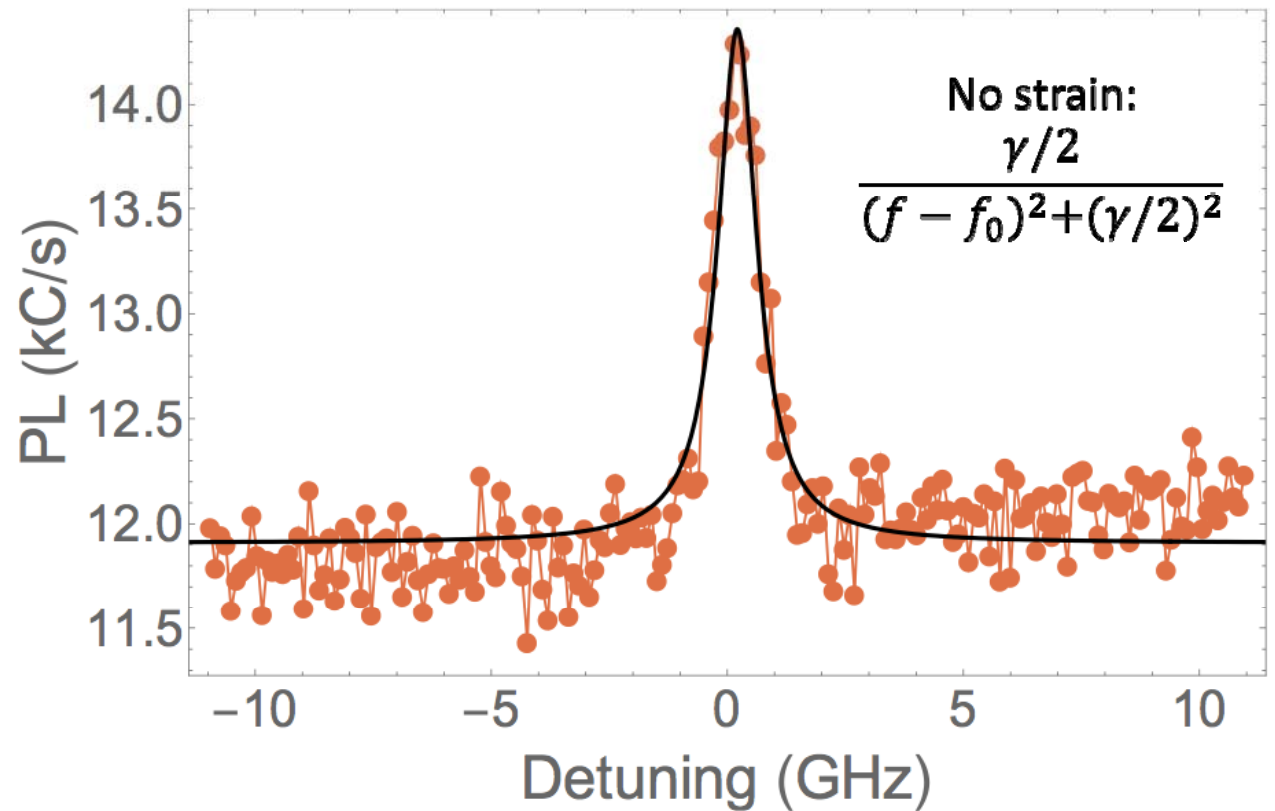




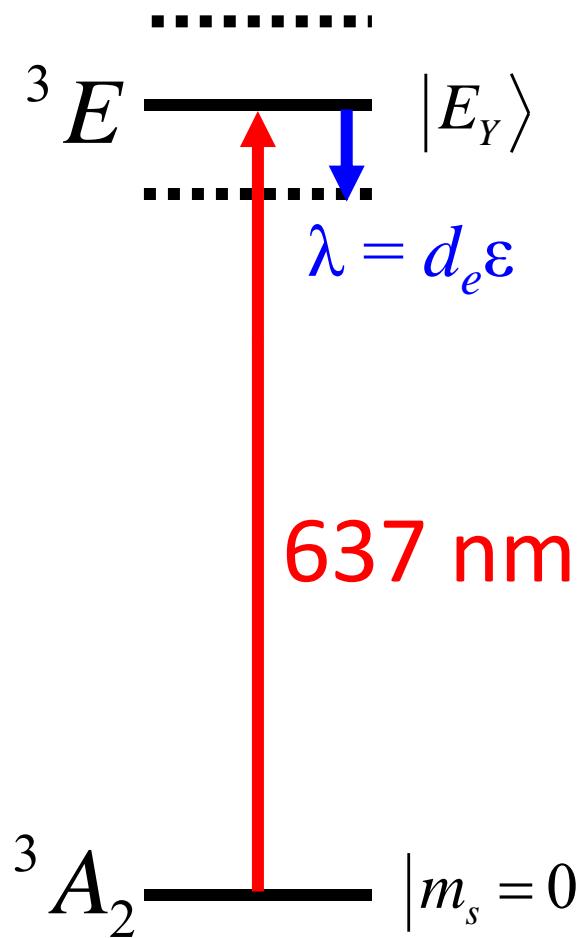
# Excited state spectroscopy of NV in cantilever



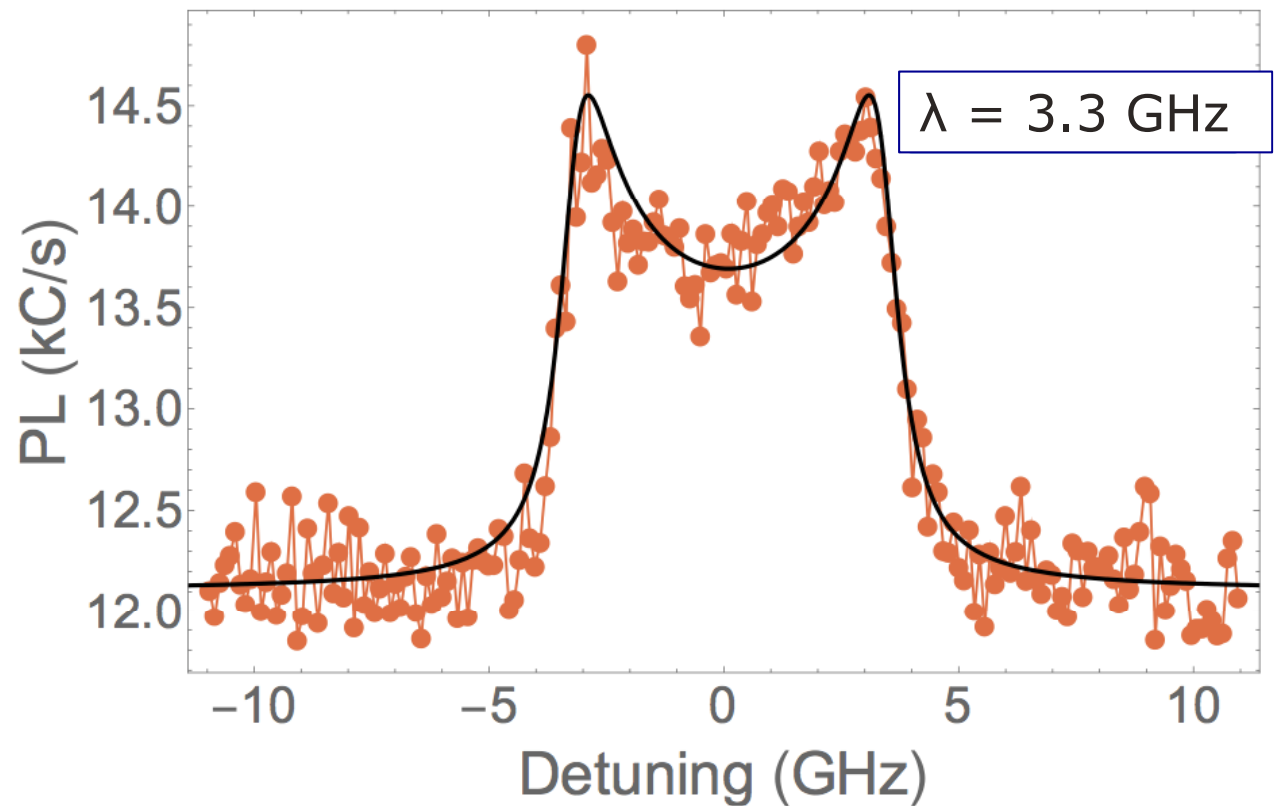
Photoluminescence excitation spectrum for stationary cantilever:



# Strain induced modulation of NV excited state

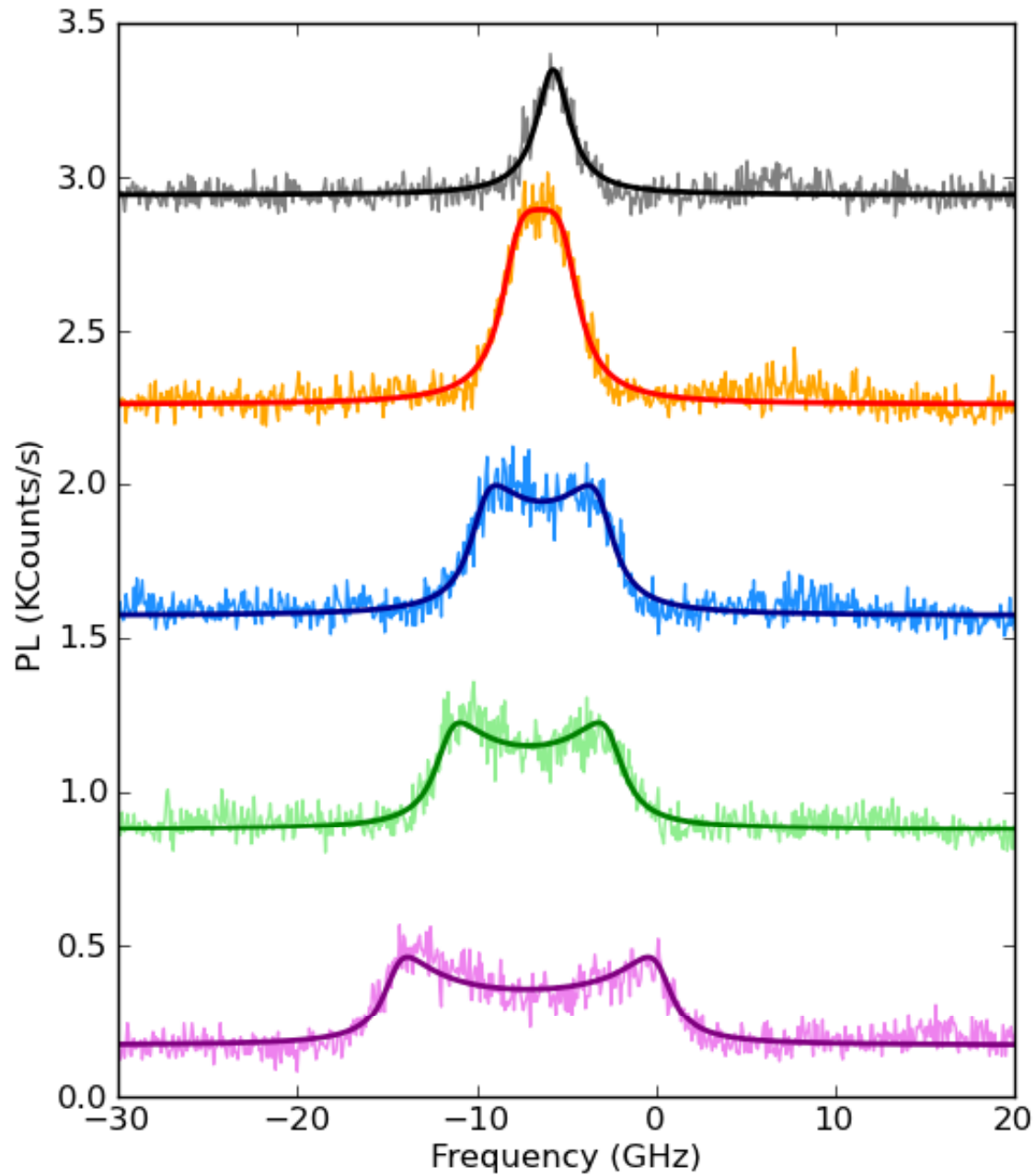


Photoluminescence excitation spectrum in the presence of 6 nm cantilever drive:

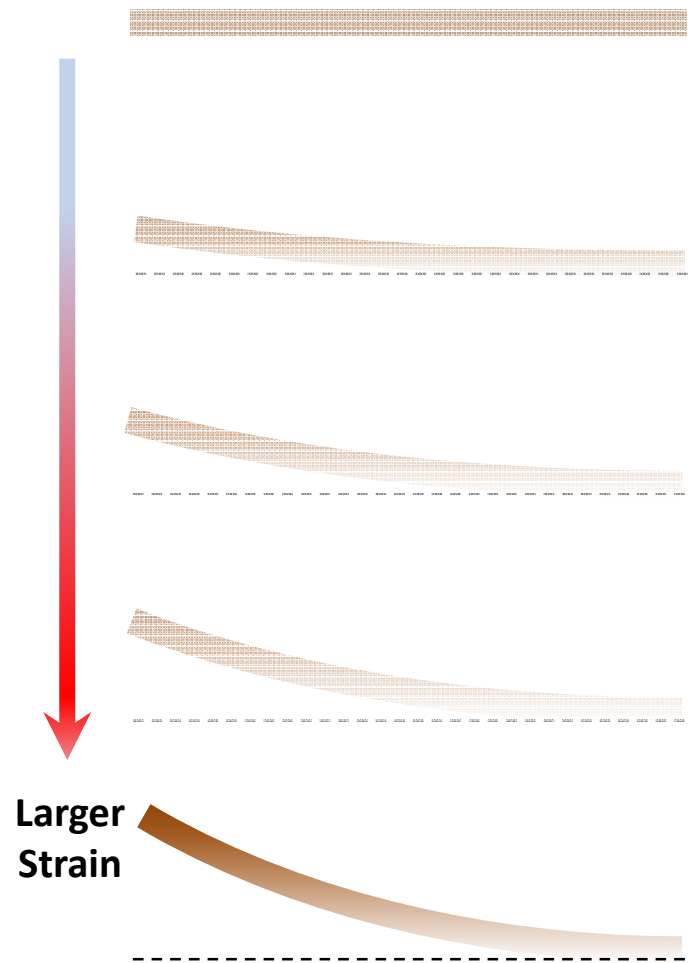


Fit: 
$$\int_0^t dt \frac{\gamma/2}{\{f - f_0 + \lambda \sin(2\pi f_m t)\}^2 + (\gamma/2)^2}$$

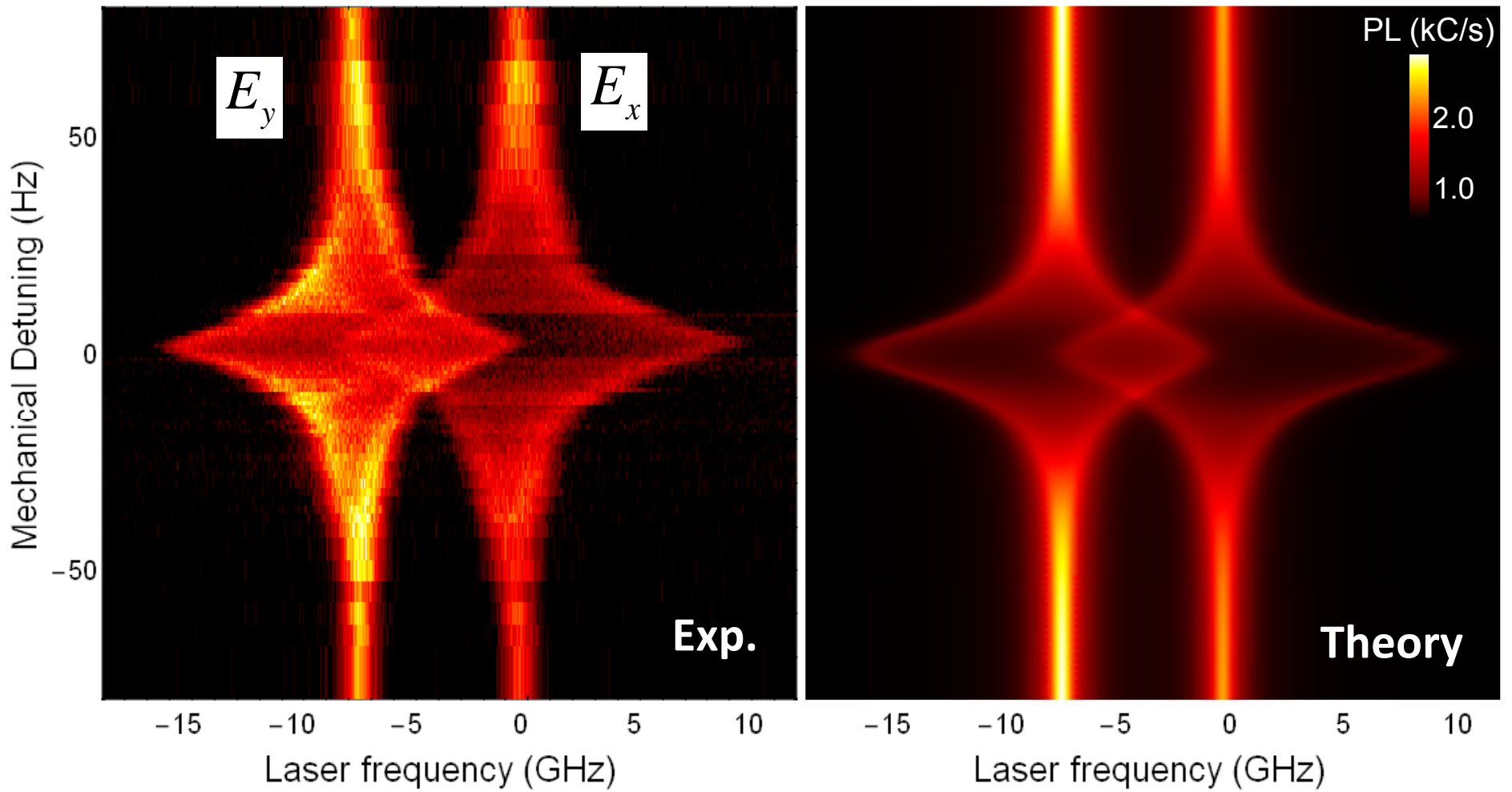
# Strain induced modulation of NV excited state



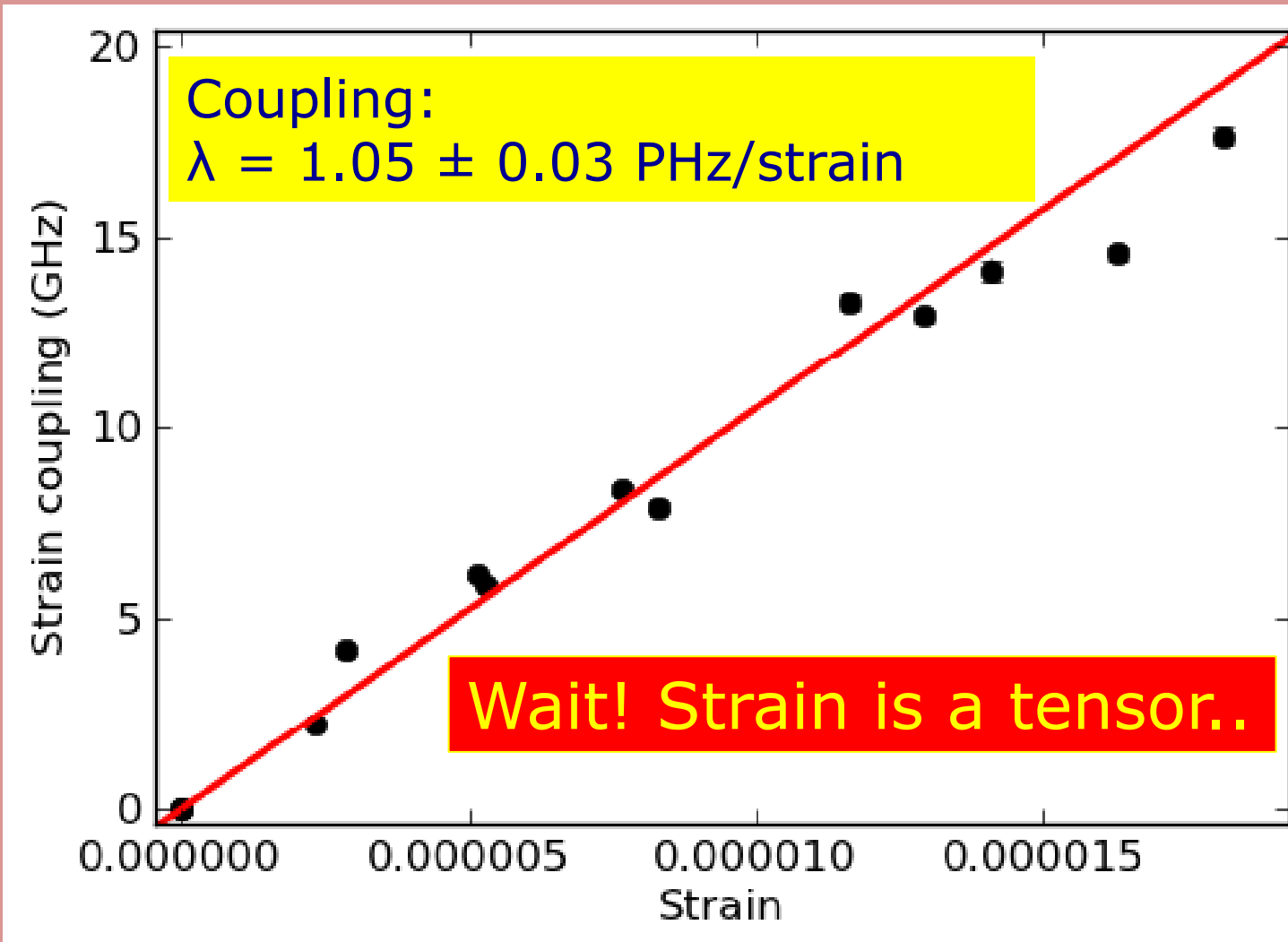
Cantilever motion



# Mechanical modulation of optical transitions



## Strain coupling to NV excited state





## But strain is a tensor...

Strain tensor:

$$\epsilon = \begin{pmatrix} \epsilon_{xx} & \epsilon_{xy} & \epsilon_{xz} \\ \epsilon_{xy} & \epsilon_{yy} & \epsilon_{yz} \\ \epsilon_{xz} & \epsilon_{yz} & \epsilon_{zz} \end{pmatrix}$$

NV-strain coupling characterized by 4 parameters:

$\lambda_1, \lambda_2$ :  $A_1$  symmetry

$\lambda_3, \lambda_4$ : E symmetry

$E_x, E_y$  energies:

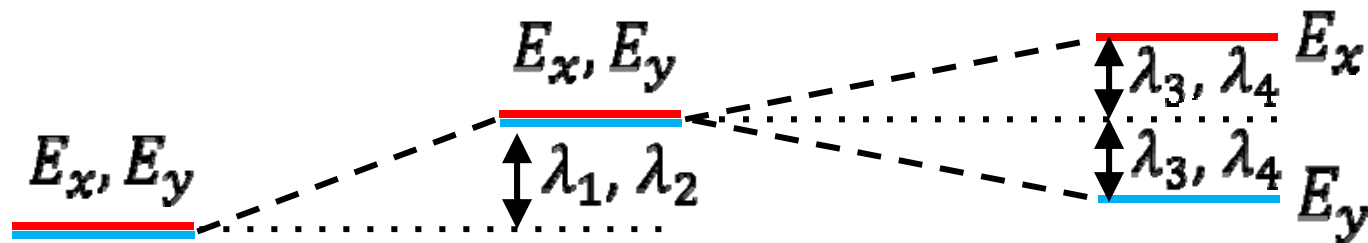
$$E_{x,y} = \lambda_1 \epsilon_{zz} + \lambda_2 (\epsilon_{xx} + \epsilon_{yy}) \pm$$

$$\sqrt{\{\lambda_3 (\epsilon_{xx} - \epsilon_{yy}) + \lambda_4 (\epsilon_{xz} + \epsilon_{zx})\}^2 + \{\lambda_3 (\epsilon_{xy} + \epsilon_{yx}) + \lambda_4 (\epsilon_{xz} + \epsilon_{zx})\}^2}$$

No strain

Strain ( $A_1$  symmetry)

Strain (E symmetry)



## But strain is a tensor...

Strain tensor:

$$\epsilon = \begin{pmatrix} \epsilon_{xx} & \epsilon_{xy} & \epsilon_{xz} \\ \epsilon_{xy} & \epsilon_{yy} & \epsilon_{yz} \\ \epsilon_{xz} & \epsilon_{yz} & \epsilon_{zz} \end{pmatrix}$$

NV-strain coupling  
characterized by 4 parameters:

$\lambda_1, \lambda_2$ :  $A_1$  symmetry

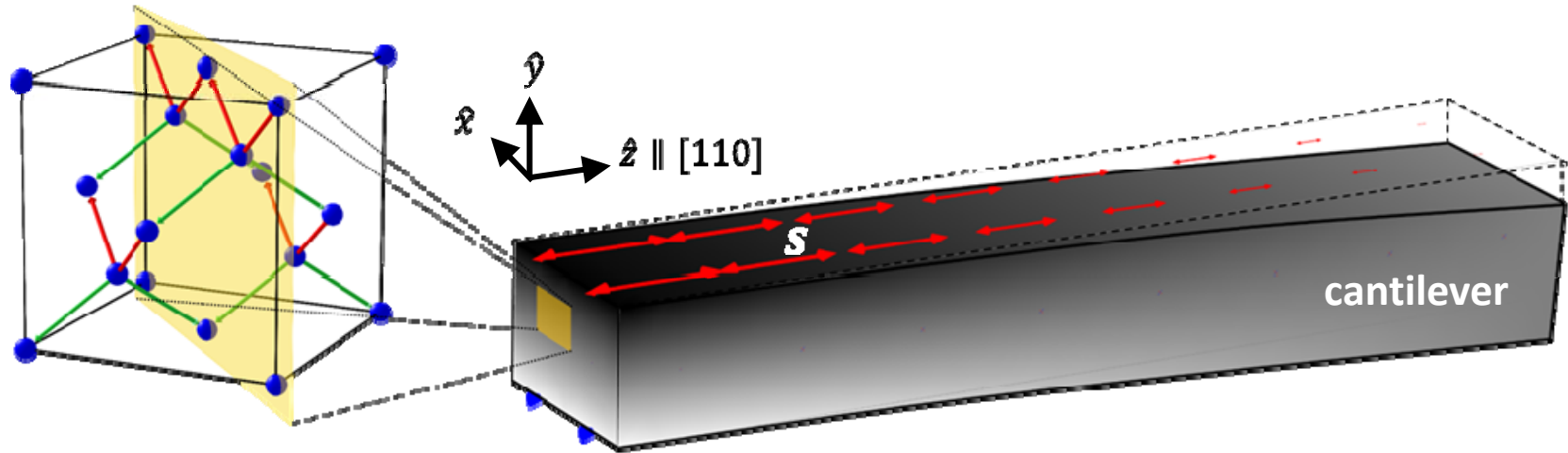
$\lambda_3, \lambda_4$ : E symmetry

- We want to measure  $\lambda_1, \lambda_2, \lambda_3$ , and  $\lambda_4$  carefully!

We utilize:

- Both  $E_x$  and  $E_y$  transitions
- Different NV orientations
- Photon polarization

# Strain tensors for two groups of NVs



Strain tensor in  
cantilever  
coordinate system:

$$\epsilon^c = \begin{pmatrix} -\nu s & 0 & 0 \\ 0 & -\nu s & 0 \\ 0 & 0 & s \end{pmatrix}$$

$s$  : strain along cantilever axis  
 $\nu$  : Poisson ratio, 0.11

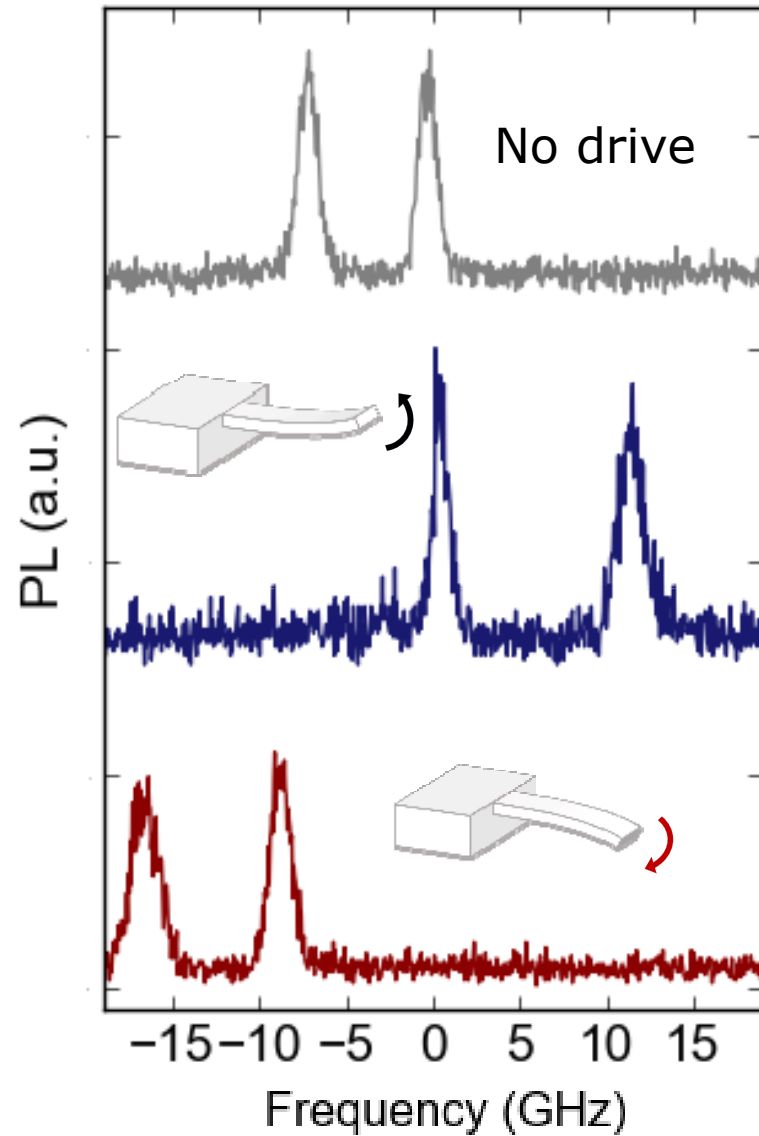
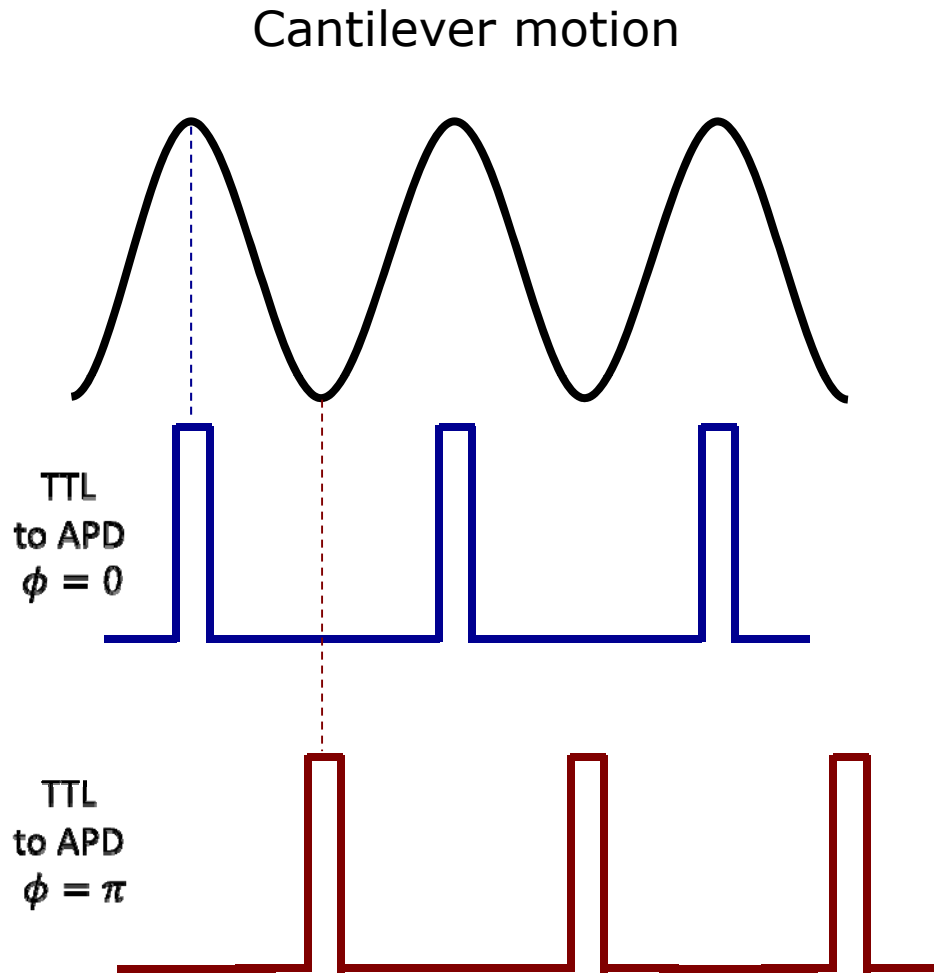
Strain tensor in NV coordinate  
NV axis  $\parallel [\bar{1}\bar{1}\bar{1}], [111]$

$$\epsilon^{NV} = \begin{pmatrix} \frac{s}{3}(1-2\nu) & 0 & -\frac{\sqrt{2}s}{3}(1+\nu) \\ 0 & -\nu s & 0 \\ -\frac{\sqrt{2}s}{3}(1+\nu) & 0 & \frac{s}{3}(2-\nu) \end{pmatrix}$$

Strain tensor in NV coordinate  
NV axis  $\parallel [\bar{1}\bar{1}\bar{1}], [111]$

$$\epsilon^{NV} = \begin{pmatrix} -\nu s & 0 & 0 \\ 0 & s & 0 \\ 0 & 0 & -\nu s \end{pmatrix}$$

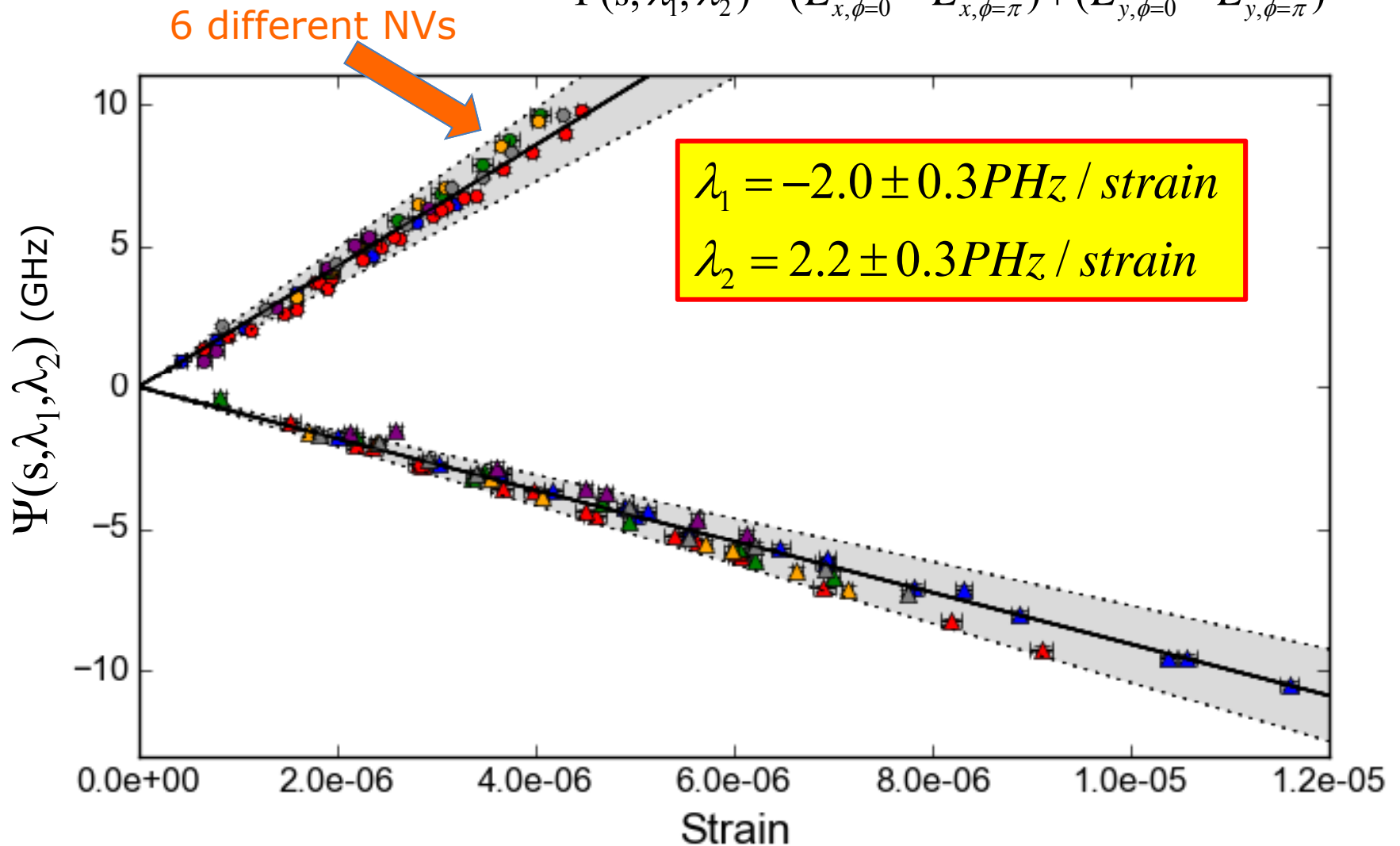
# Stroboscopy: a quasi-DC measurement



## Extracting $A_1$ -symmetric coupling parameters ( $\lambda_1$ and $\lambda_2$ )

- Constructed a quantity that only depends on  $\lambda_1$  and  $\lambda_2$ :

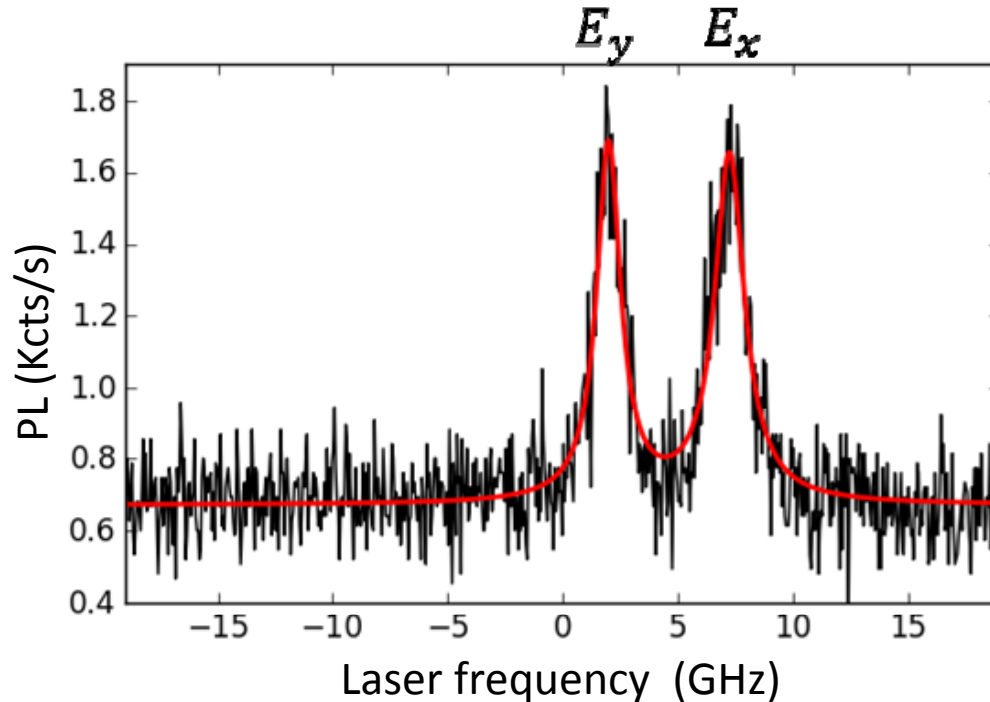
$$\Psi(s, \lambda_1, \lambda_2) = (E_{x,\phi=0} - E_{x,\phi=\pi}) + (E_{y,\phi=0} - E_{y,\phi=\pi})$$





## Role of intrinsic strain

- Without cantilever motion, the NV experiences intrinsic strain:



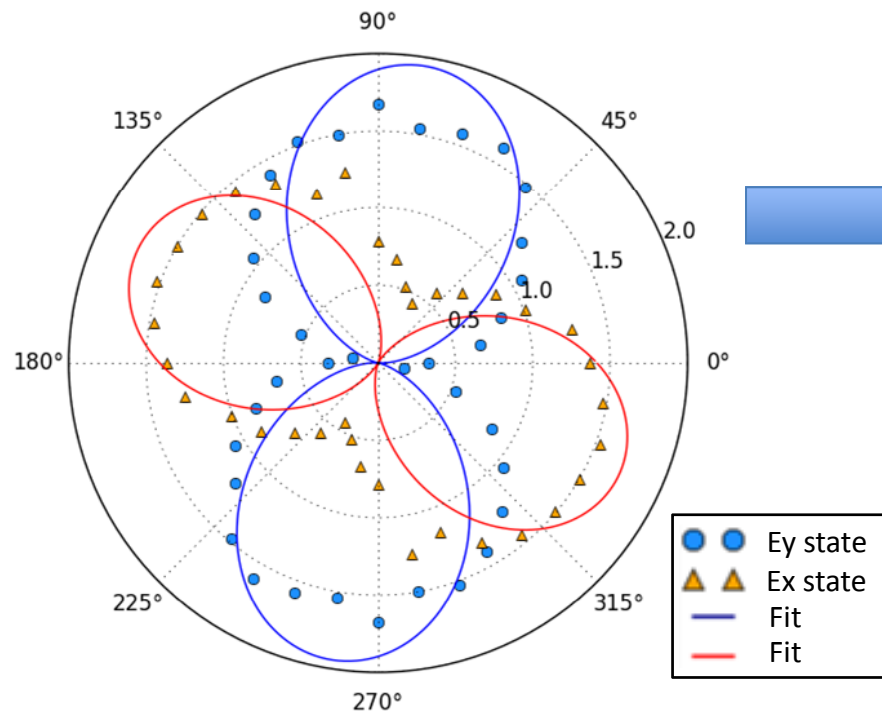
- But direction of the intrinsic strain (E-type) is important for  $\lambda_3$  and  $\lambda_4$ !

$$E_{x,y} = \lambda_1 \epsilon_{zz} + \lambda_2 (\epsilon_{xx} + \epsilon_{yy}) \pm \sqrt{\{\lambda_3 (\epsilon_{xx} - \epsilon_{yy}) + \lambda_4 (\epsilon_{xz} + \epsilon_{zx}) + V_{E1}\}^2 + \{\lambda_3 (\epsilon_{xy} + \epsilon_{yx}) + \lambda_4 (\epsilon_{xz} + \epsilon_{zx}) + V_{E2}\}^2}$$

- How do we know the direction of the intrinsic strain??

# Polarization and strain

Polarization angle of  $E_x$  and  $E_y$  states:

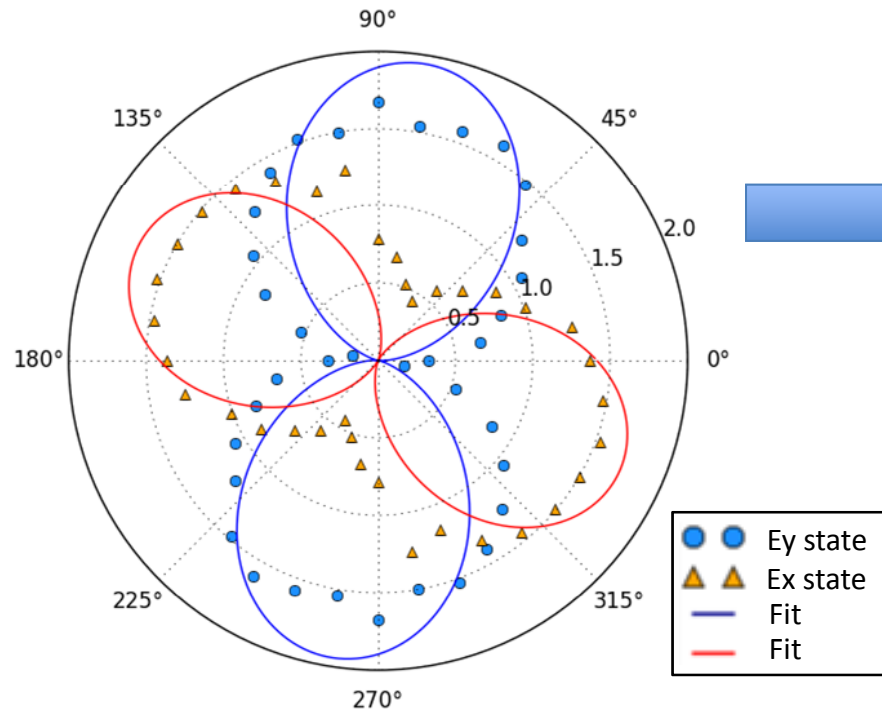


$$\theta = \frac{1}{2} \arctan(V_{E2}/V_{E1})$$

Still only gives us a ratio..

# Polarization and strain

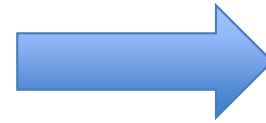
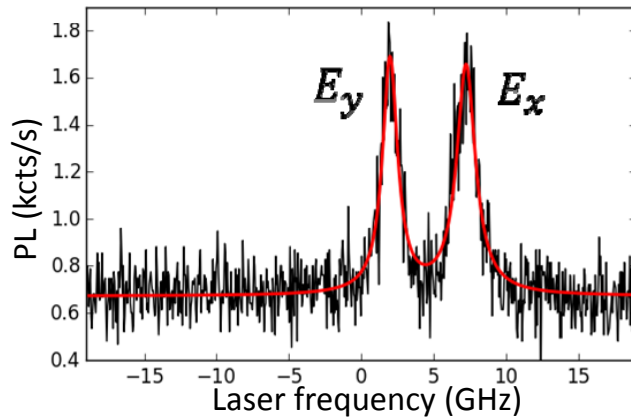
Polarization angle of  $E_x$  and  $E_y$  states:



$$\theta = \frac{1}{2} \arctan(V_{E2}/V_{E1})$$

Still only gives us a ratio..

Intrinsic strain splitting:

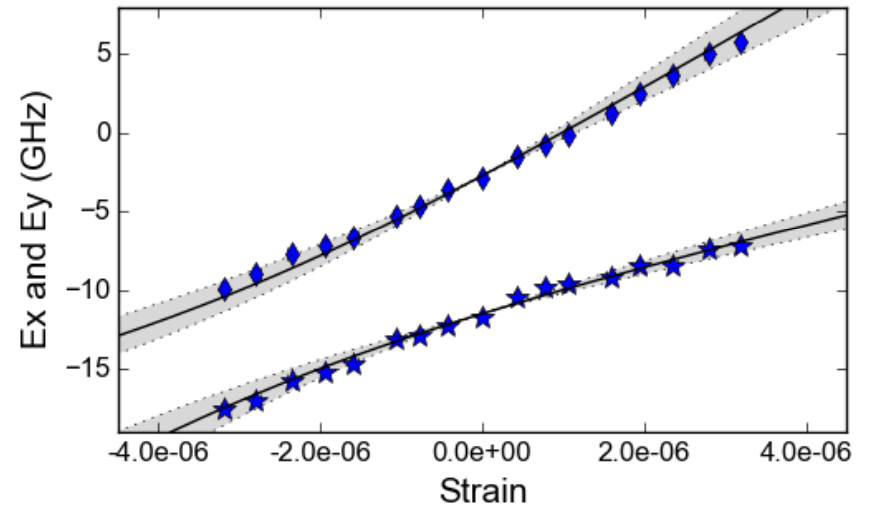
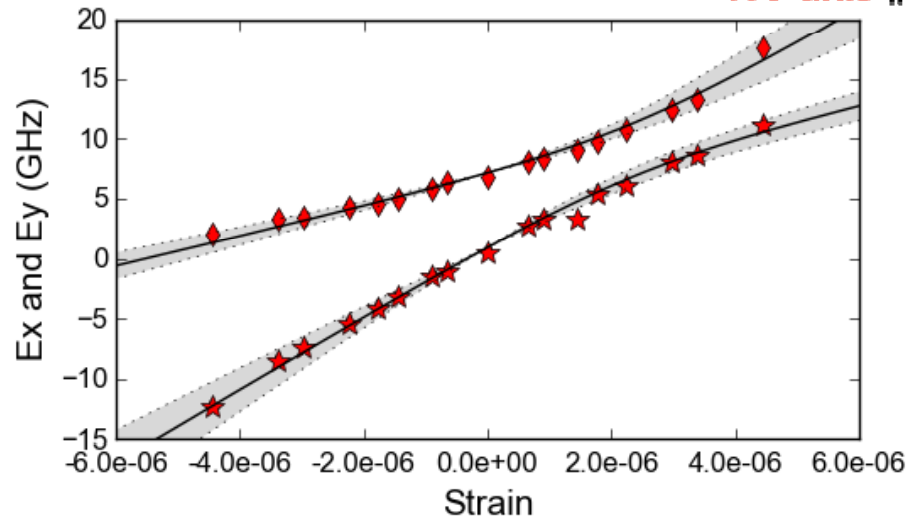


$$E_x - E_y = 2\sqrt{V_{E1}^2 + V_{E2}^2}$$

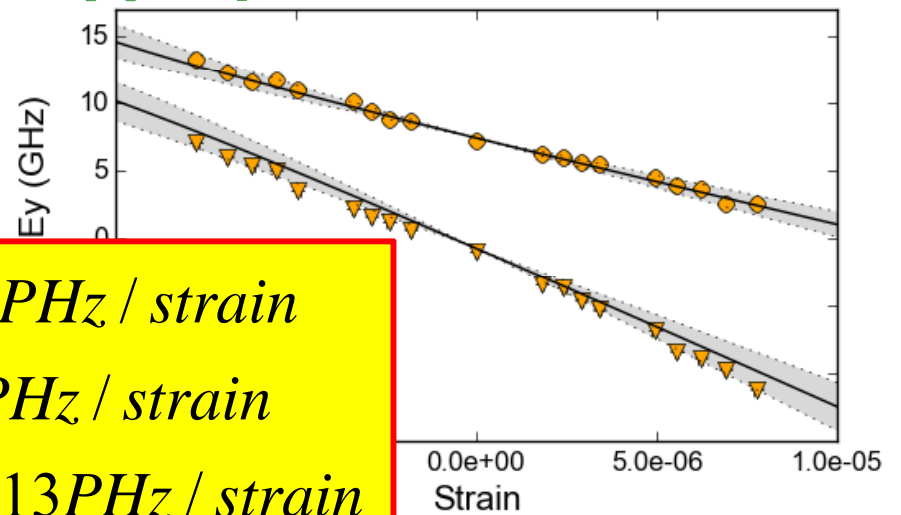
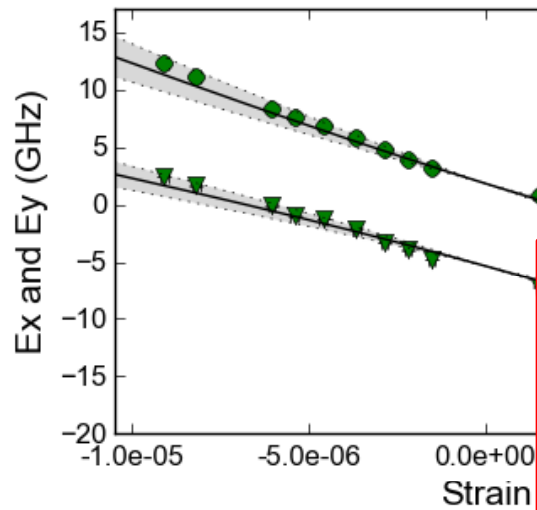
Now, we know  $V_{E1}$  and  $V_{E2}$ !!

## Extracting $\lambda_3$ and $\lambda_4$

NV axis  $\parallel$   $[1\ 1\ 1]$ ,  $[1\ 1\ 1]$



NV axis  $\parallel$   $[1\ 1\ 1]$ ,  $[1\ 1\ 1]$



$$\lambda_1 = -2.0 \pm 0.3 \text{ PHz} / \text{strain}$$

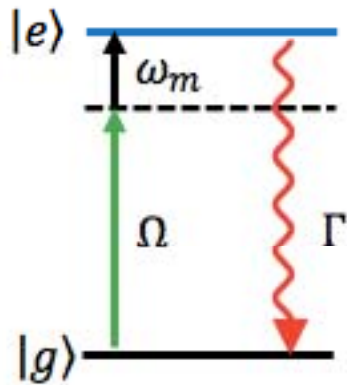
$$\lambda_2 = 2.2 \pm 0.3 \text{ PHz} / \text{strain}$$

$$\lambda_3 = -0.85 \pm 0.13 \text{ PHz} / \text{strain}$$

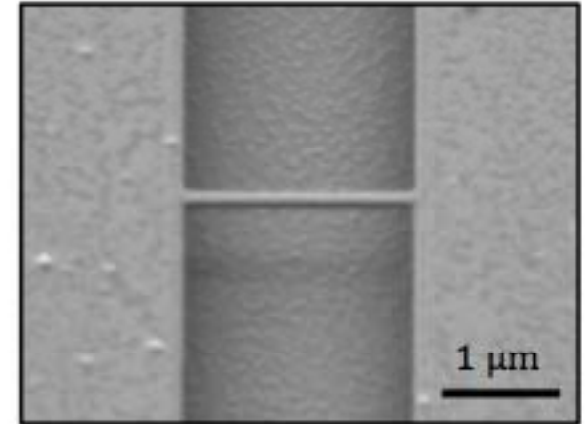
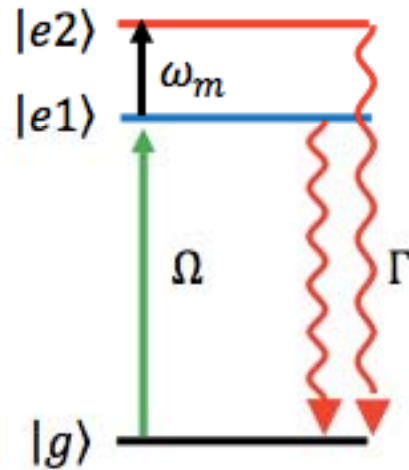
$$\lambda_4 = 0.02 \pm 0.01 \text{ PHz} / \text{strain}$$

# Toward phonon cooling

## Off-resonant cooling



## Resonant cooling



Kepesidis *et al.*, *PRB* **88**, 064105 (2013).

$$\tilde{\Gamma}_{off} \approx \frac{\lambda_{off}^2}{\Gamma} \frac{\Omega^2}{\omega_m^2}$$

$$\tilde{\Gamma}_{on} \approx \frac{\lambda_{on}^2}{\Gamma} \frac{4\Omega^2}{\Gamma^2}$$

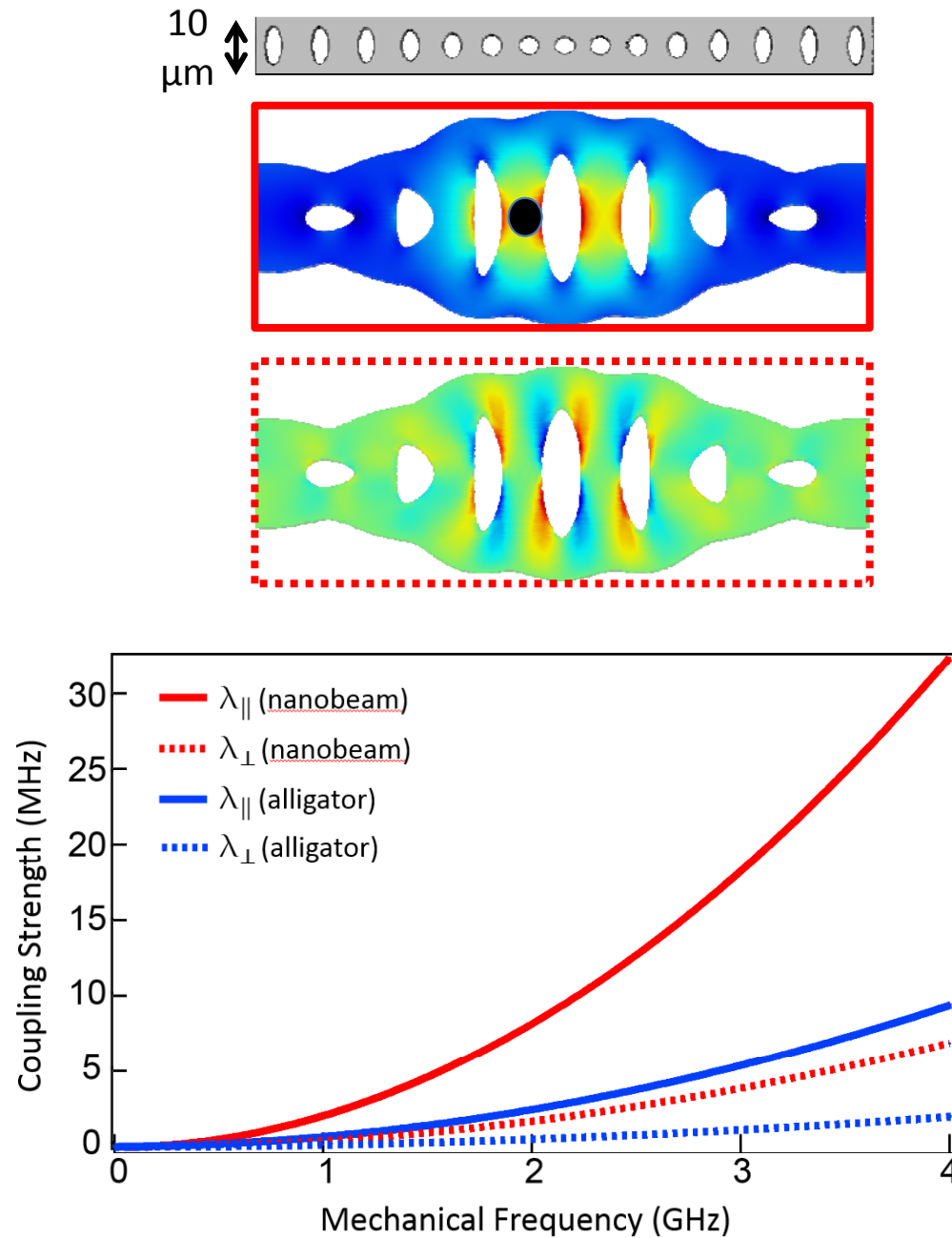
$$n_{off} \approx \frac{\gamma N_{th}}{\tilde{\Gamma}_{off}} \approx 4$$

$$n_{on} \approx \frac{\gamma N_{th}}{\tilde{\Gamma}_{on}} \approx 0.9$$

## System parameters:

- $2 \mu\text{m} \times 100 \text{ nm} \times 50 \text{ nm}$
- $Q = 5 \times 10^5$
- $T = 4 \text{ K}$
- $\lambda_{off} = 1 \text{ PHz/strain}$
- $\lambda_{on} = 1 \text{ PHz/strain}$
- $\Omega = 100 \text{ MHz}$
- $\Gamma = 500 \text{ MHz}$

# Strain coupling in diamond mechanical crystals



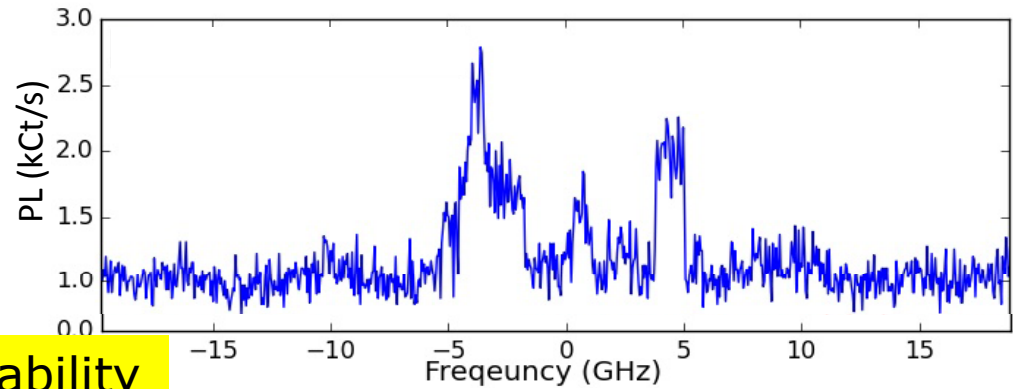
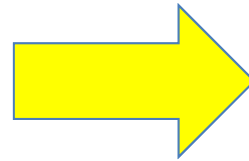
$$f_0 = 500 \text{ MHz}$$

$$T = 4 \text{ K}, Q = 10^5:$$

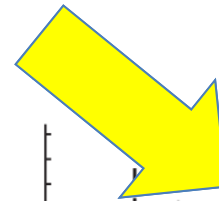
$$n_f < 1$$

# Challenge: NV quantum memories/spin-photon entanglement

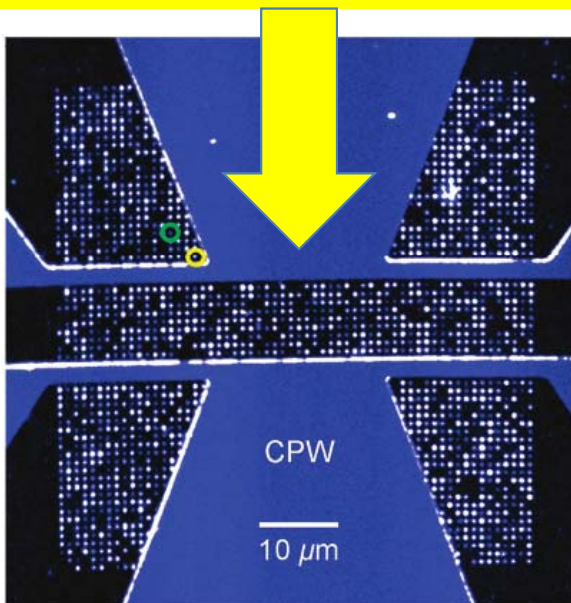
Challenge: NV spectral diffusion



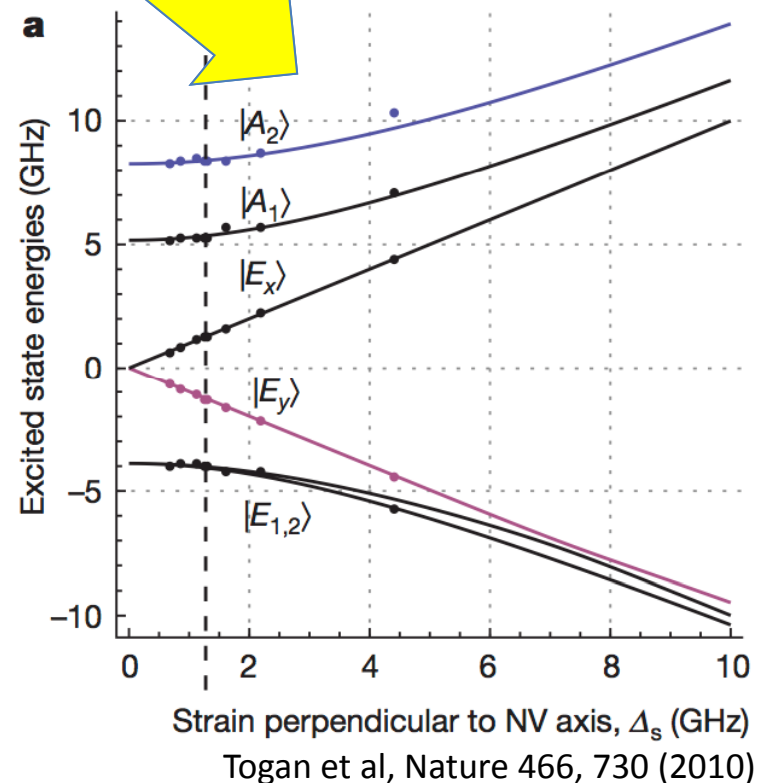
Challenge: indistinguishability of NV's due to local strain



Challenge: deterministic placement of NV's

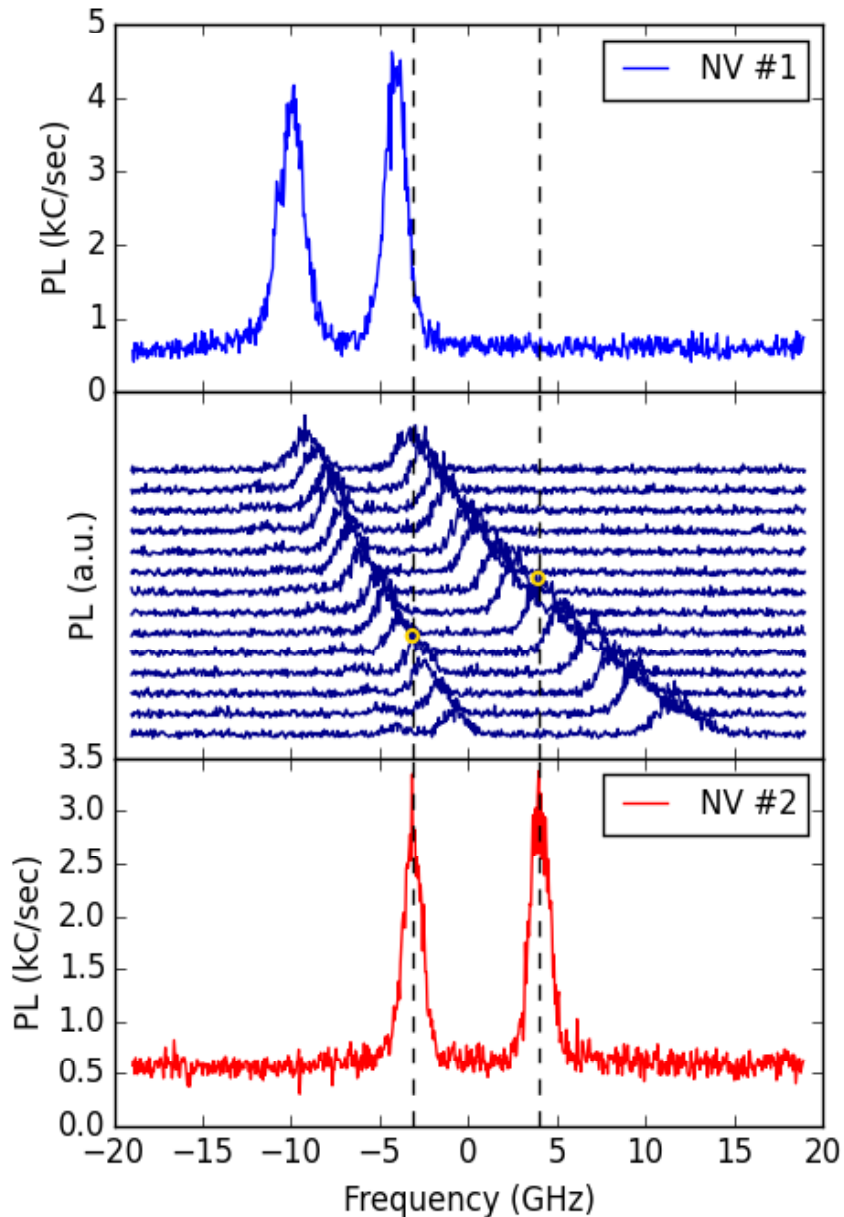


D. Toyli *et al.* *Nano Lett.* **10** (2010)





# Strain tuning two NVs into resonance



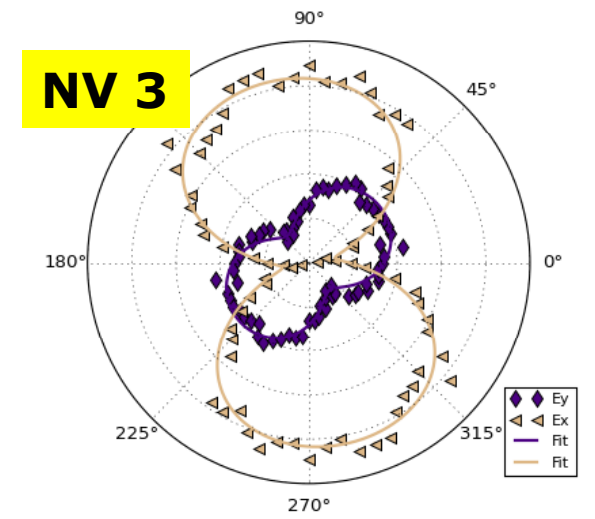
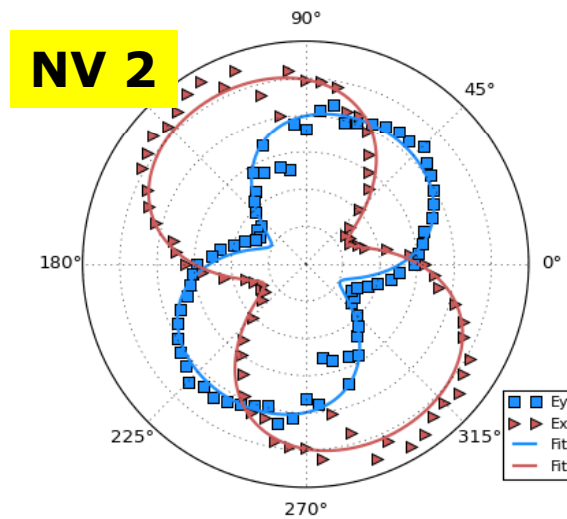
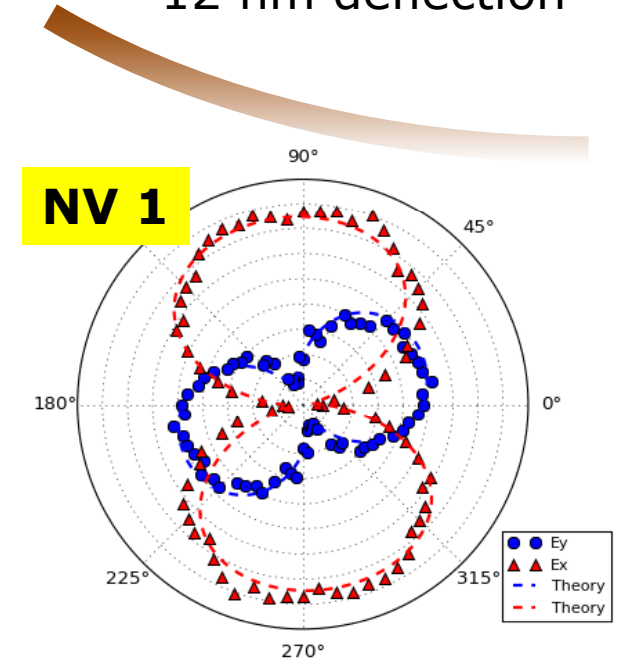
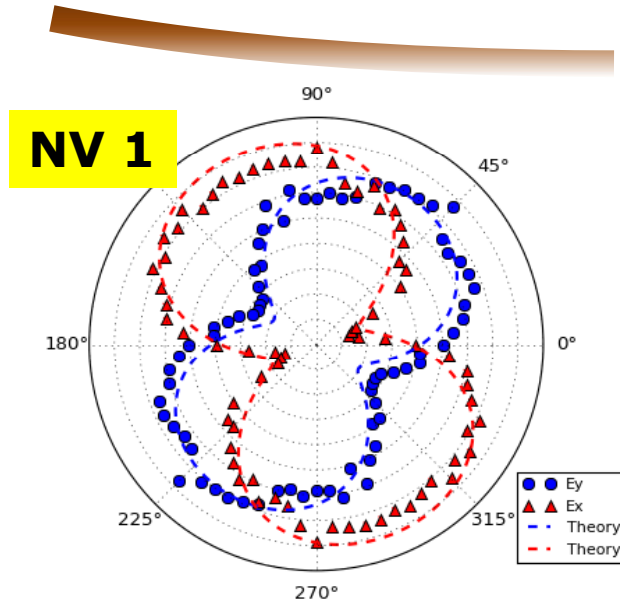
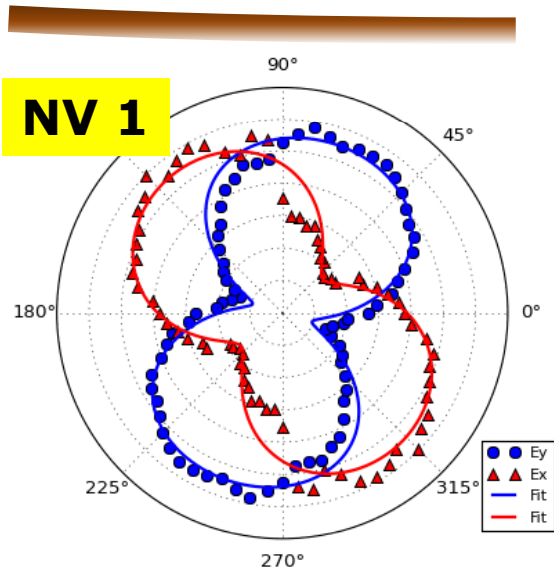
- NV#1 and NV#2 are initially distinguishable due to strain inhomogeneities in crystal
- Increasing cantilever oscillation amplitude (data is only taken at one extremum of cantilever motion)
- Matched optical transition energies of NV#1 and NV#2 through motionally-induced strain

# On-chip strain control of polarization state

0 nm deflection

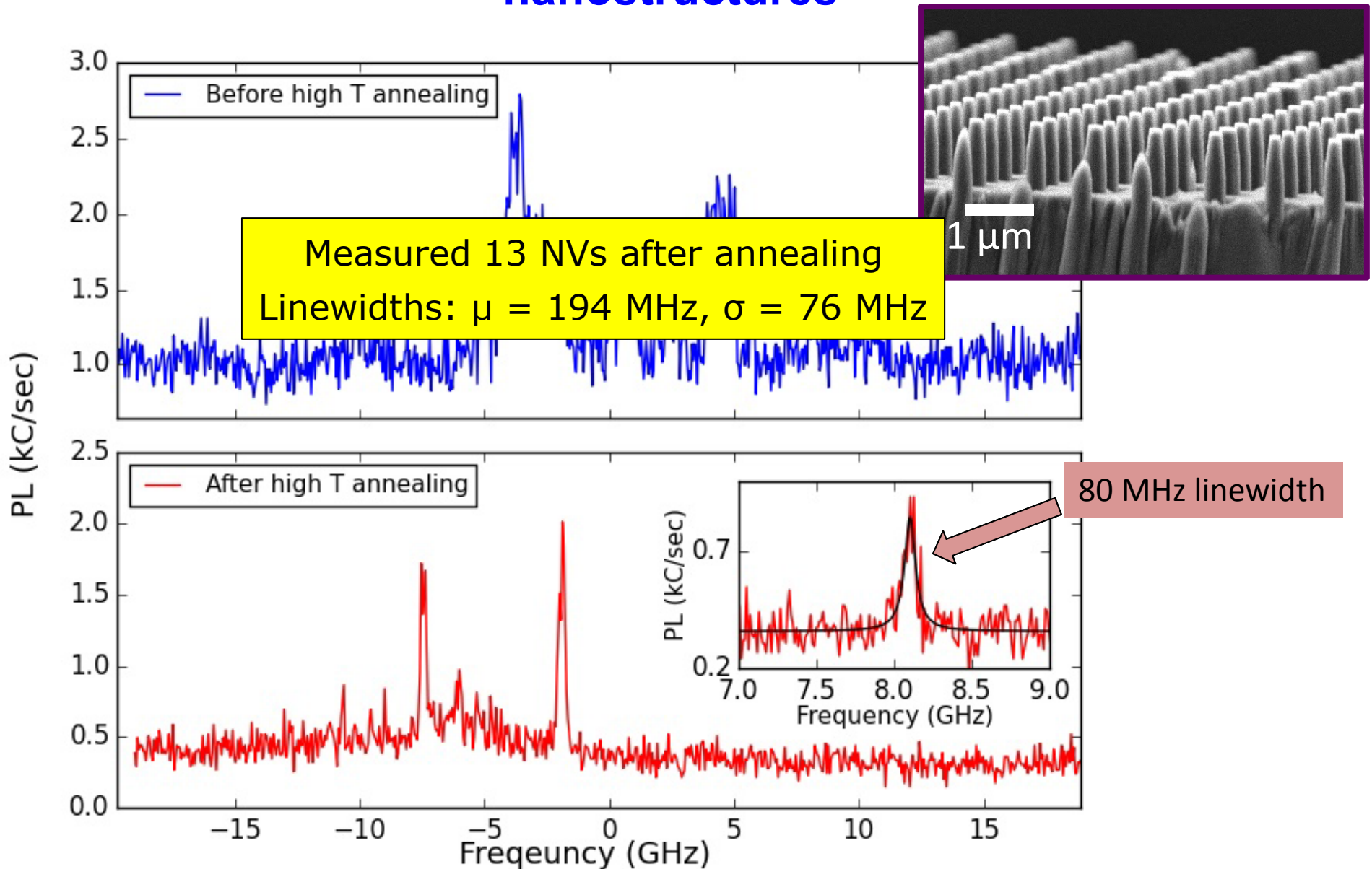
3 nm deflection

12 nm deflection



- Emitted photon polarization depends on intrinsic strain

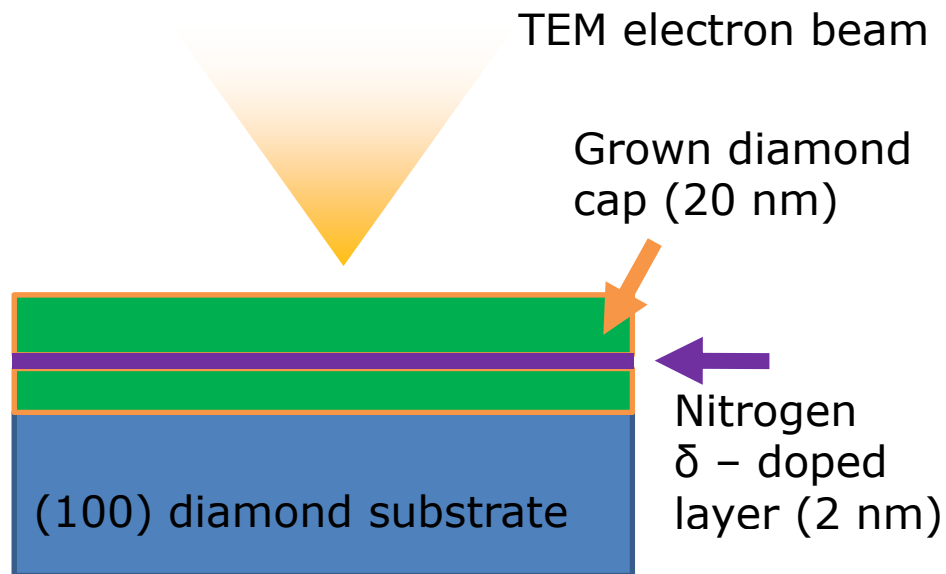
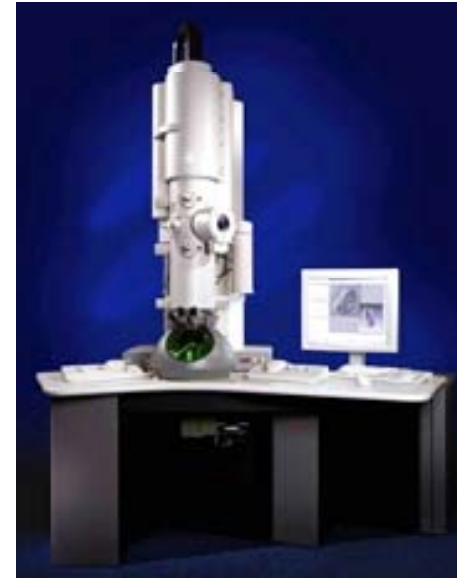
# Suppressing spectral diffusion in nanostructures



# Nanoscale localization of NV centers

- Vacancies introduced via transmission electron microscope (TEM) allows for

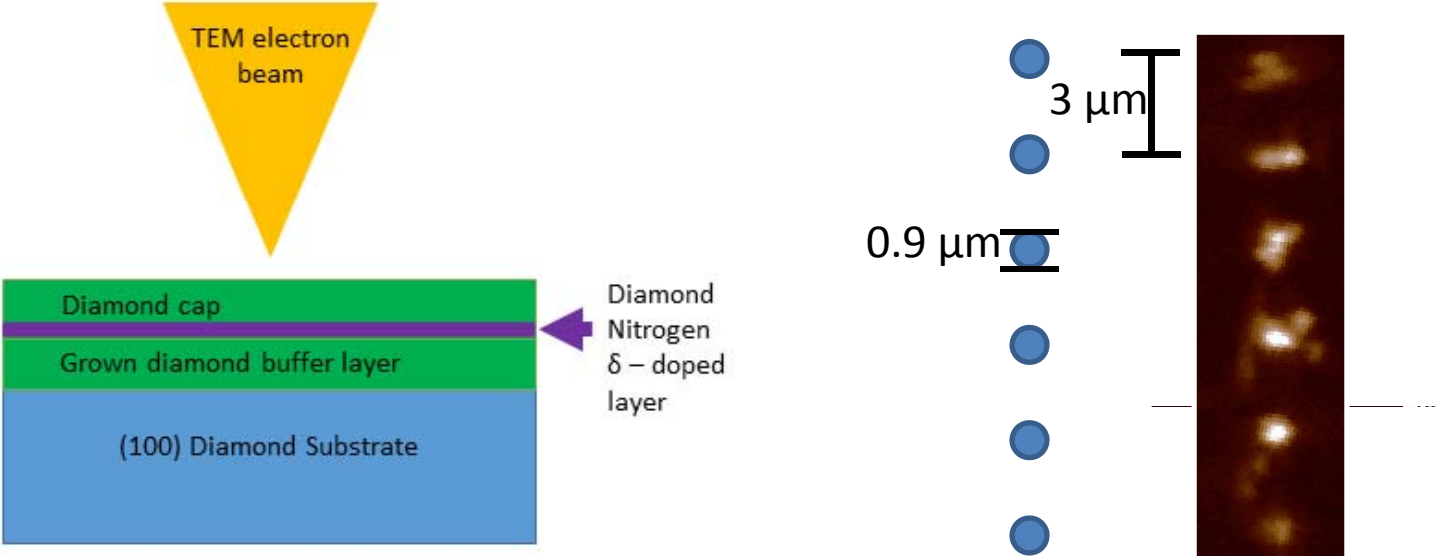
3-d nanoscale NV localization



- Can finely tune dose, flux, and energy of electrons
- Can focus electron beam to give nanoscale spatial resolution

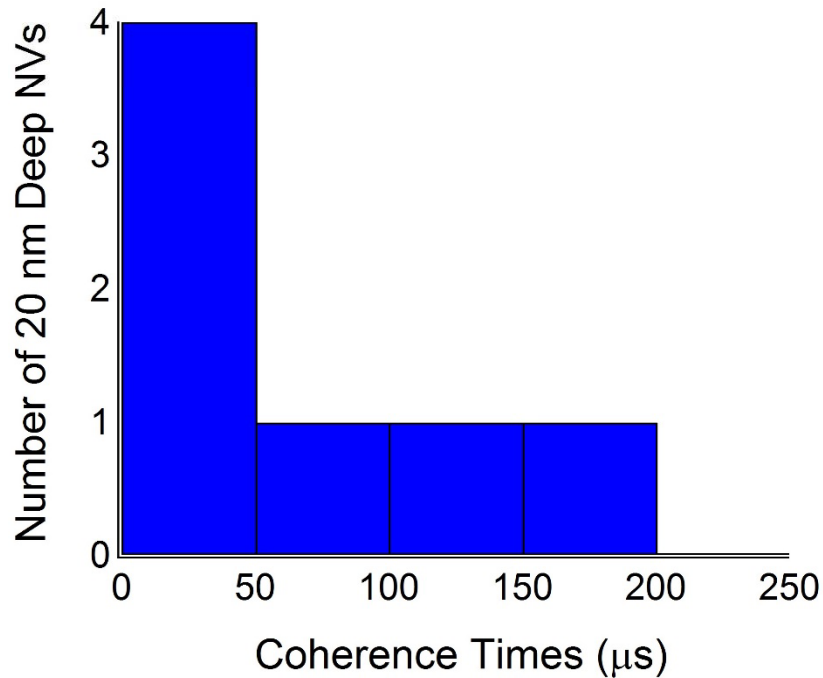
Ohno, *et al*, *APL* **101**, 082413 (2012)  
Myers *et al*, *PRL* **113**, 027602 (2014)  
McLellan *et al*, *in preparation*

# Patterned, highly coherent NV centers



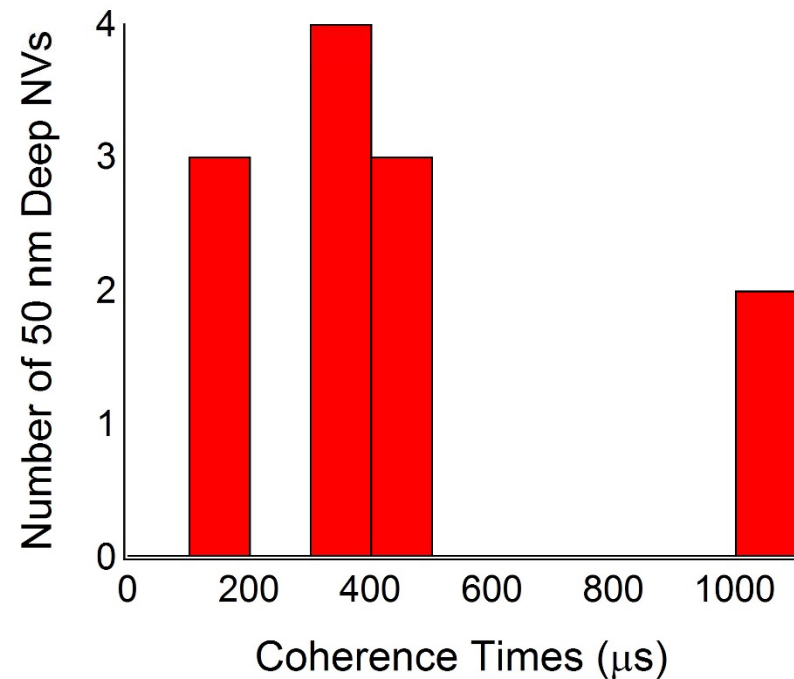
# Coherence time spread

## 20 nm deep NV coherence times



- $T_{2,avg} = 65 \mu s$

## 50 nm deep NV coherence times



- $T_{2,avg} = 442 \mu s$

Coherence times are long, even at the highest NV densities with  $> 10 \text{ NV's}/\mu\text{m}^2$



# Summary

- Strain coupling to ground spin states and excited orbital states
- Tunable control over energy and polarization via strain
- Annealing to significantly reduce spectral diffusion
- Deterministic patterning of highly coherent NV centers

