#### To Send or Receive but not Both:

The role of cis-interactions between Notch and Delta

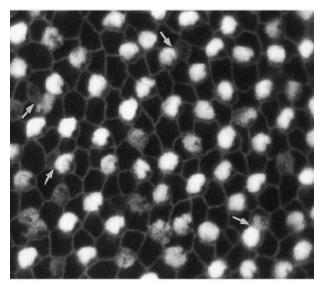
Computational Morphodynamics, KITP 2009

David Sprinzak

Elowitz Lab, California Institute of Technology

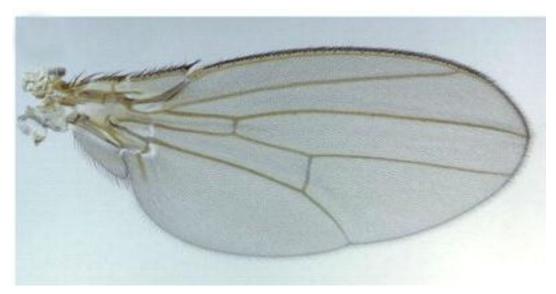
#### Fine Grained Developmental Pattern Formation

#### Inner ear development (chick)



Goodyear and Richardson, J. Neurosci 1997

#### Wing Vein Patterning (Drosophila)



Lai et al, Development 2005

### THE THEORY OF THE GENE

 $\mathbf{B}\mathbf{Y}$ 

#### THOMAS HUNT MORGAN

Professor of Biology, California Institute of Technology formerly Professor of Experimental Zoölogy in Columbia University

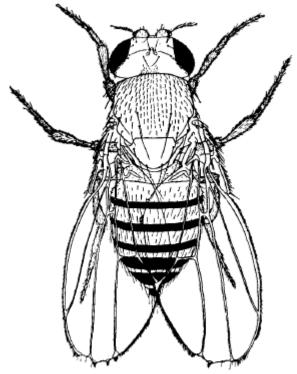


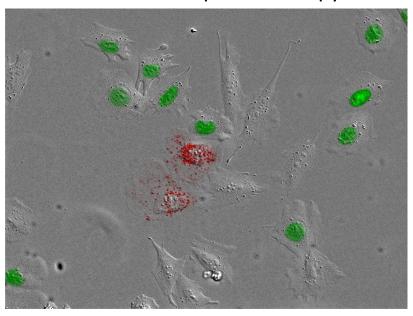
Fig. 44.

Notch-wing, a dominant sex-linked, recessive lethal of Drosophila melanogaster.

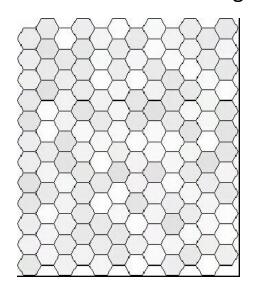
# How do the molecular properties of the Notch-Delta signaling system affect developmental patterning?

### Approach: combine quantitative time lapse microscopy and mathematical modeling

Quantitative time laps microscopy



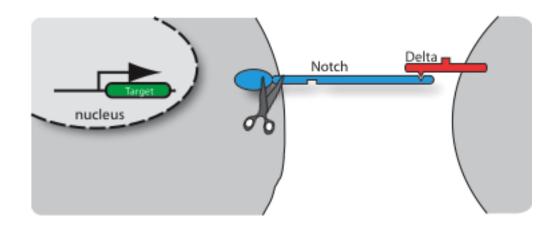
Mathematical modeling



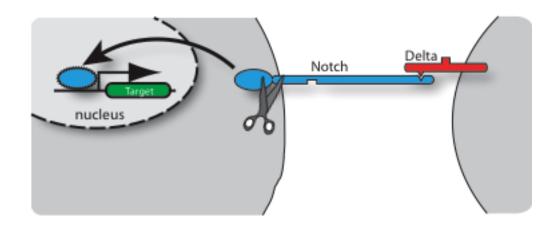
Use synthetic approach:

- Synthetic constructs (Notch-Gal4)
- Study dynamics in mammalian cell culture system

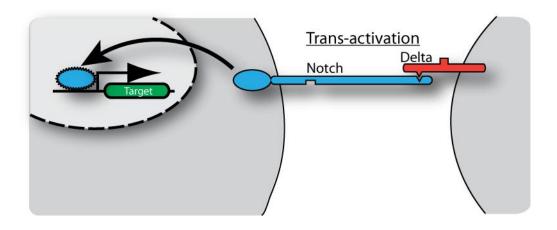
#### Delta trans-activates Notch



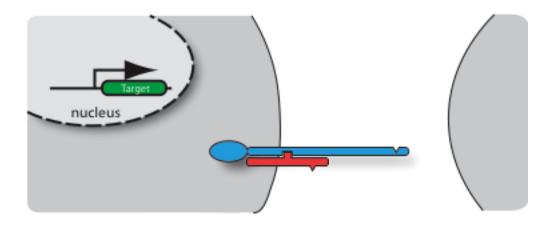
#### Delta trans-activates Notch



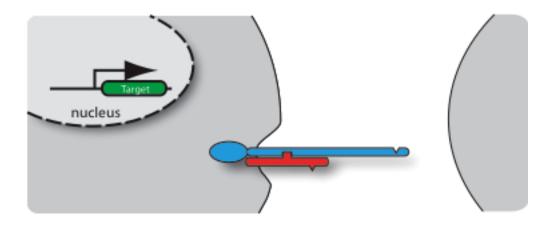
#### Delta Trans-activates Notch



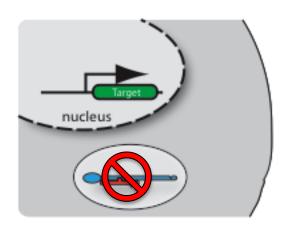
#### Delta cis-inhibits Notch

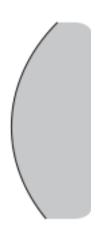


#### Delta cis-inhibits Notch

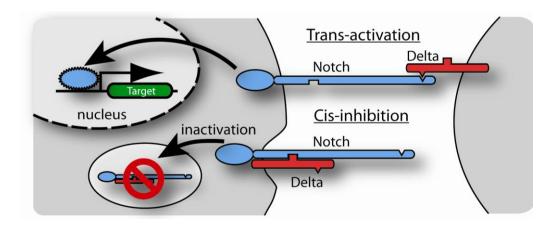


#### Delta cis-inhibits Notch



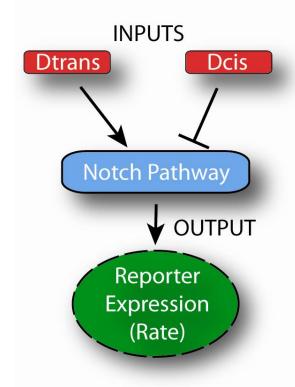


#### Notch and Delta interact in cis and in trans



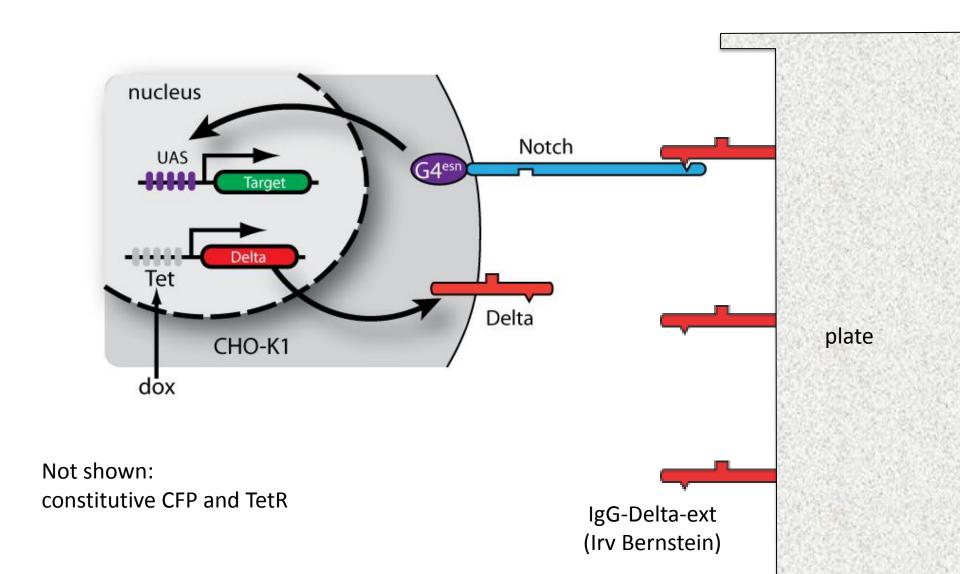
(Diagram is only schematic - cis and trans interaction occur in the same Notch domain)

### How do the Notch pathway integrates these two inputs?

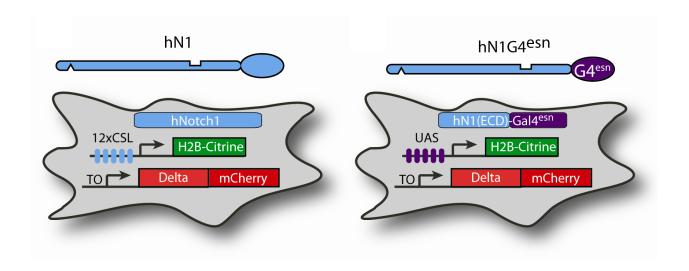


Why do you need such a mechanism?

### Platform for analyzing Notch response to cis and trans Delta



### System for analyzing Notch response to cis and trans Delta

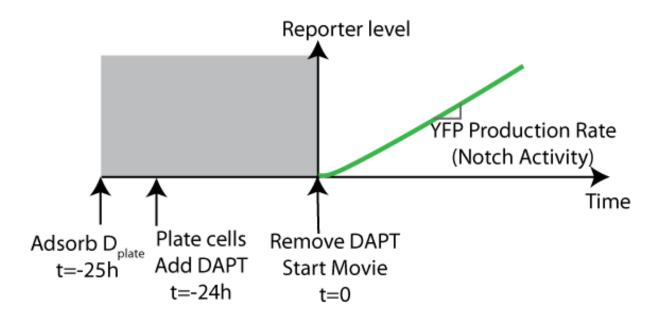


Base cell line: CHO-K1

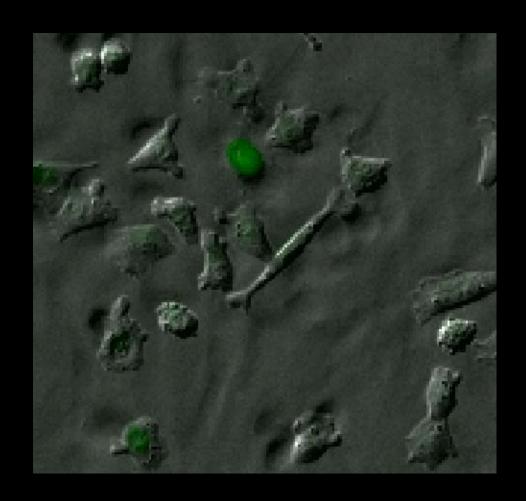
Not shown: TetR, CMV-H2B-Cerulean

rDll1 (from Gerry Weinmaster) 12xCSL (from Urban Lendahl) hN1 (from Jon Aster)

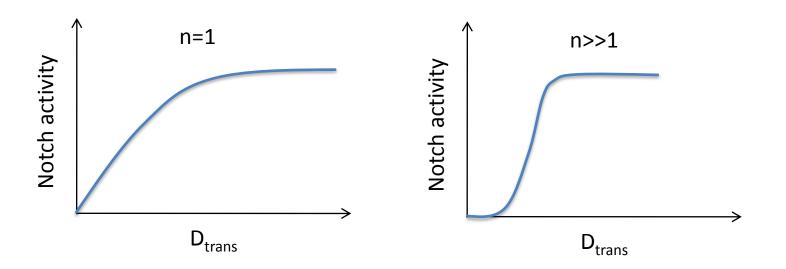
### Notch response to trans-activation



### Notch response to trans-activation

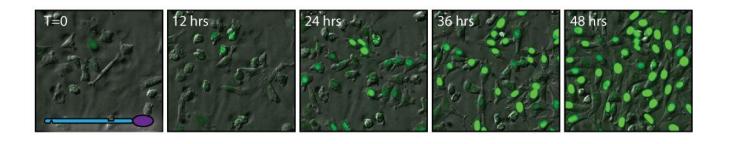


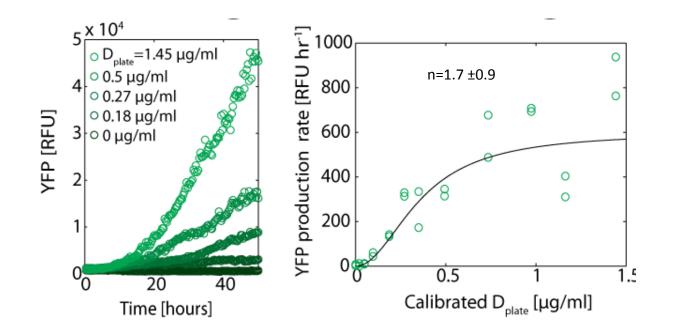
### What is the cooperativity of Notch response to trans-Delta?



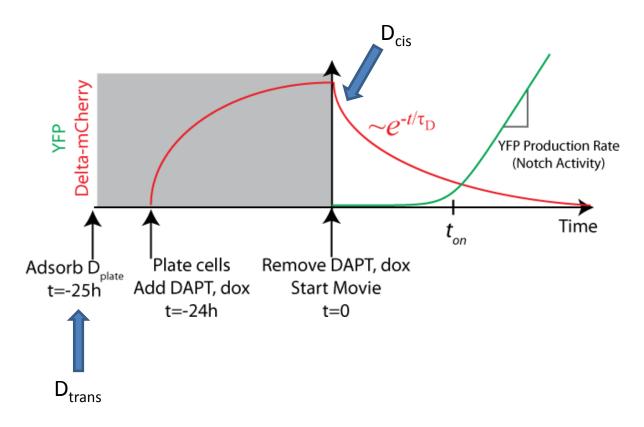
From modeling of Lateral Inhibition expect >2

## Notch response to trans-activation is graded

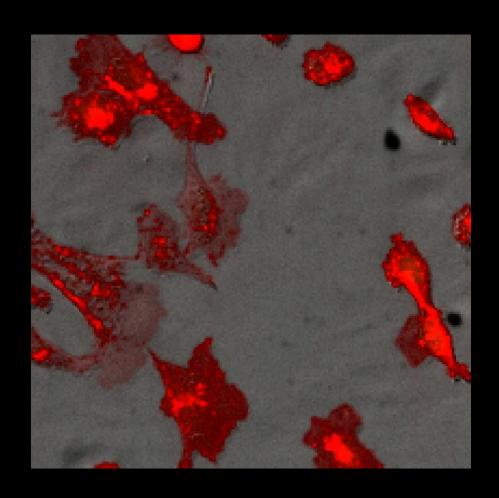




### Measuring Notch response to cis and trans Delta

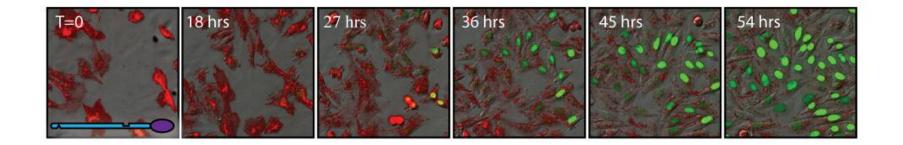


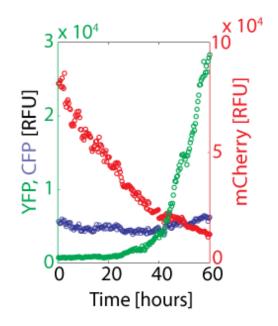
### Notch activity in response to cis-Delta



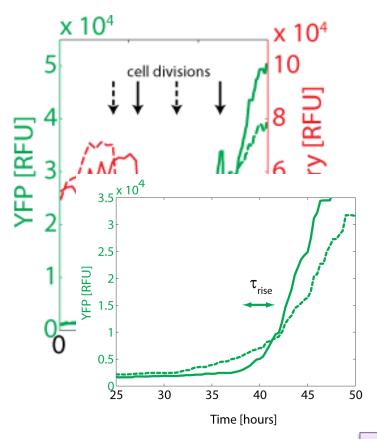
Red – Delta Green – Notch response

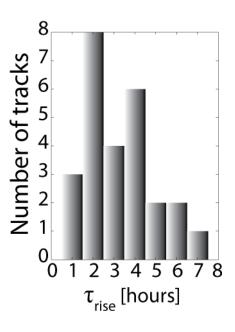
### Cis-Delta exhibits sharp response





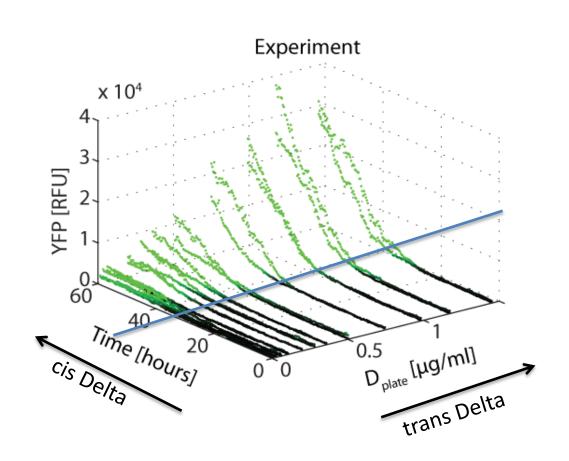
### And even sharper in single cells...





Effective cooperativity  $\approx \tau_{Delta\ decay} / \tau_{rise} \approx 12$ 

### Response of Notch signaling to both cis and trans Delta



### What have we got?

- Graded response to trans-Delta
- Sharp response to cis-Delta
- Threshold for cis-Delta independent of trans-Delta

#### Mathematical model

Trans-activation reaction:

**Notch ICD** 

$$N + D_{trans} \rightleftharpoons [ND_{trans}] \rightarrow S$$

Cis-inhibition (mutual inactivation) reaction:

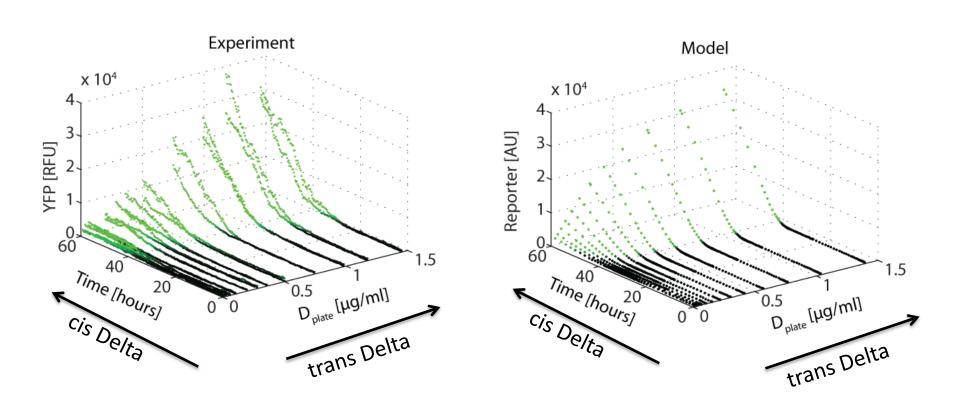
$$N + D_{cis} \rightleftharpoons [ND_{cis}] \rightarrow \phi$$

N and  $D_{cis}$  are also produced and degraded at constant rate

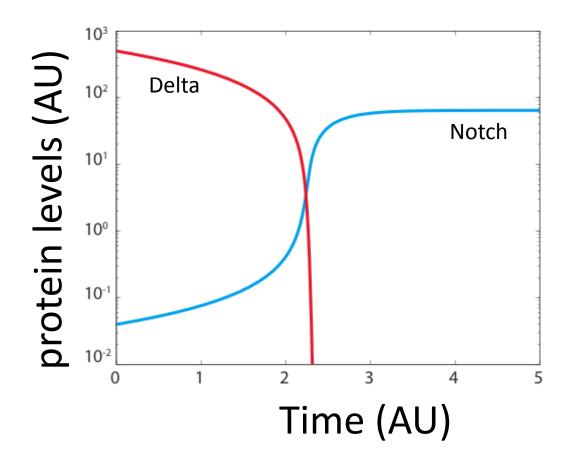
#### Mathematical model

$$\begin{split} \frac{dN}{dt} &= \beta_N - \gamma N - \frac{ND_{cis}}{k_C} - \frac{ND_{trans}}{k_t} \\ \frac{dD_{cis}}{dt} &= \beta_D - \gamma D_{cis} - \frac{ND_{cis}}{k_C} \\ \frac{dS}{dt} &= \frac{ND_{trans}}{k_t} - \gamma_S S \end{split}$$

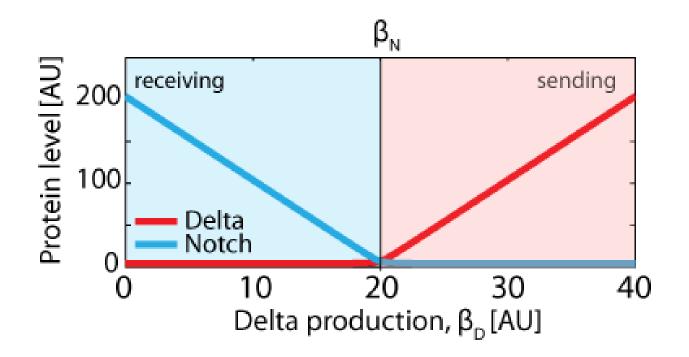
### Model captures main experimental observations



## Mutual inactivation of Notch and Delta leads to an ultrasensitive response

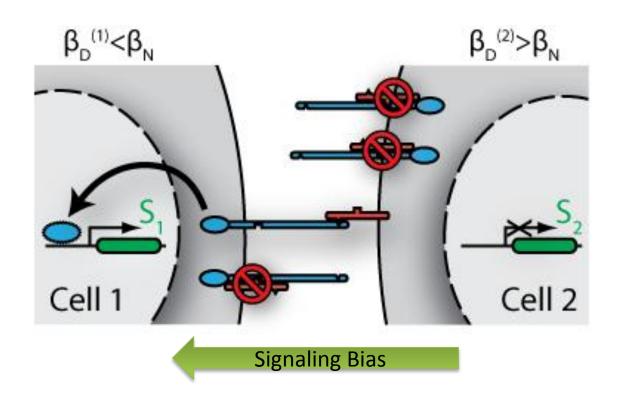


### A signaling switch 'Sender' or a 'receiver' but not both

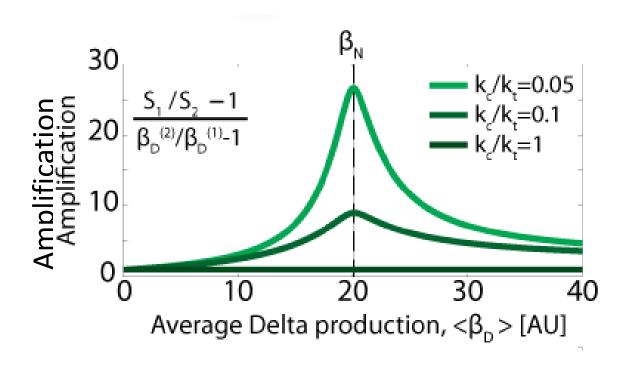


An inherent property of the Notch-Delta signaling Without any transcriptional feedback!

### Signaling bias in two neighboring cells



### Mutual inactivation amplifies differences between cells

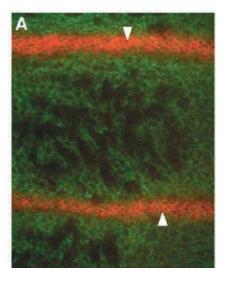


## Implications for Pattern formation: Sharp boundary in the wing vein

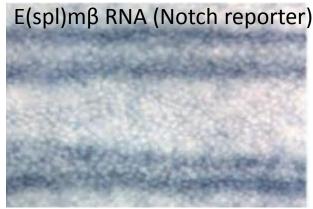


Notch (green)

Delta (red)

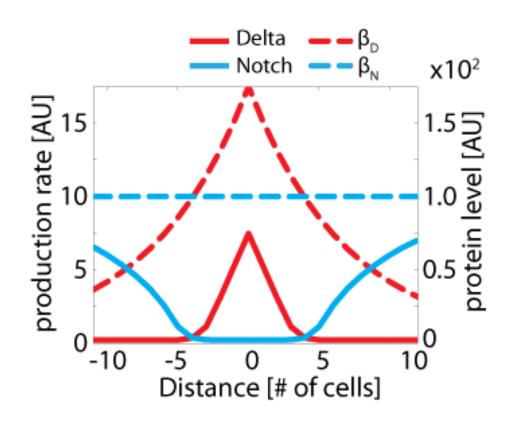


Huppert et al. (1997)

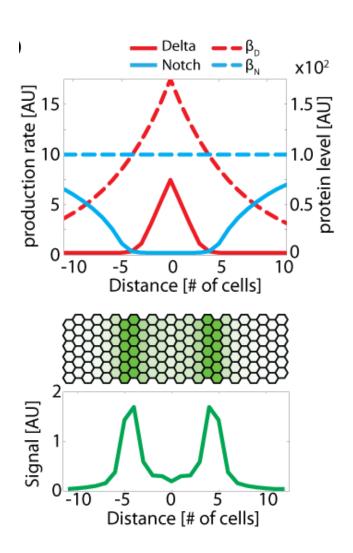


de Celis et al. (1997)

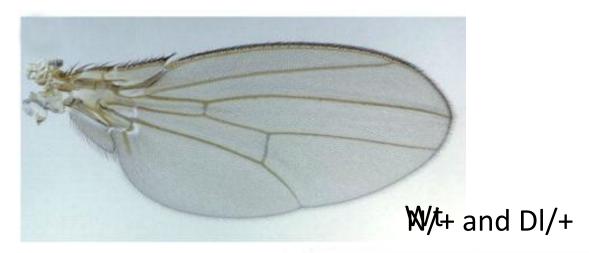
### Sharp boundary in the wing vein

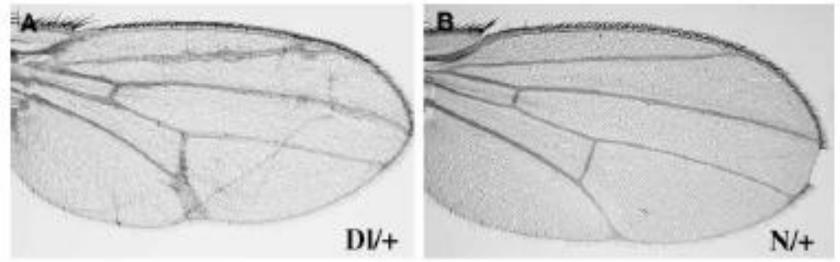


### Sharp boundary in the wing vein



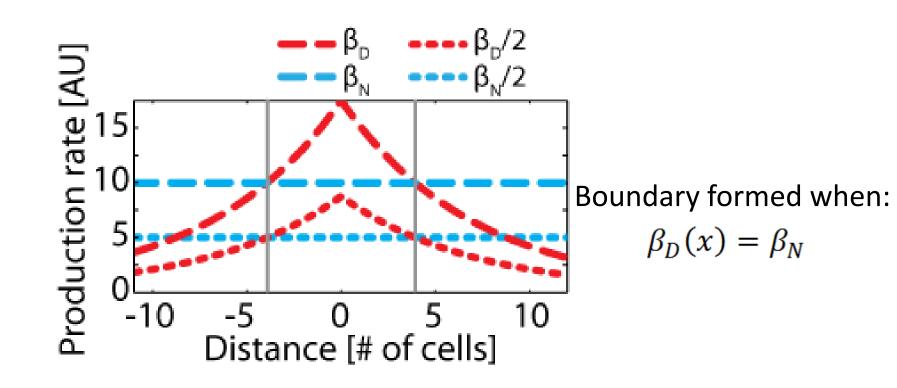
## Model explains gene dosage phenotypes



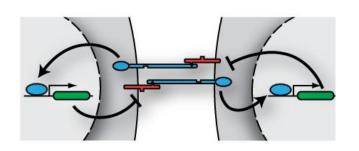


de Celis and Bray (2000)

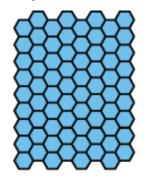
## Model explains gene dosage phenotypes

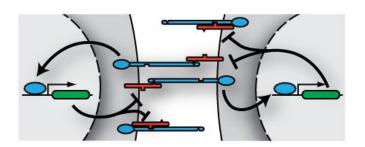


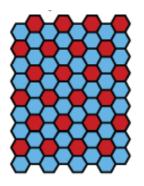
# Lateral Inhibition with Mutual Inactivation mechanism circumvent the need for cooperativity



Requires n>2

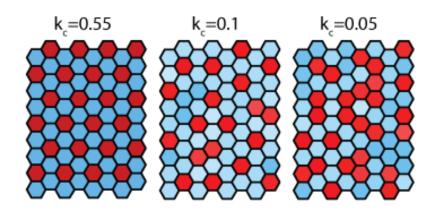






Work with n=1!

## And generates a new spectrum of patterns



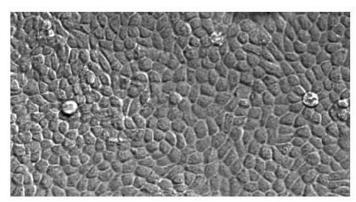
#### Summary

- Mutual inactivation of Notch and Delta results in an ultrasensitive signaing switch: A cell is either a 'sender' or 'reciever'
- This intrinsic property of the Notch pathway amplifies differences between neighboring cells without additional feedback.
- Major implication in patterning processes

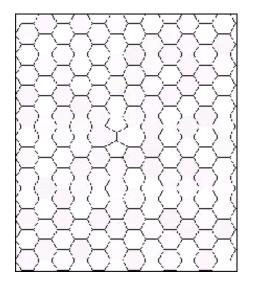
Mutual inactivation mechanism?

## Interaction between morphology and signaling

#### Role of Disorder



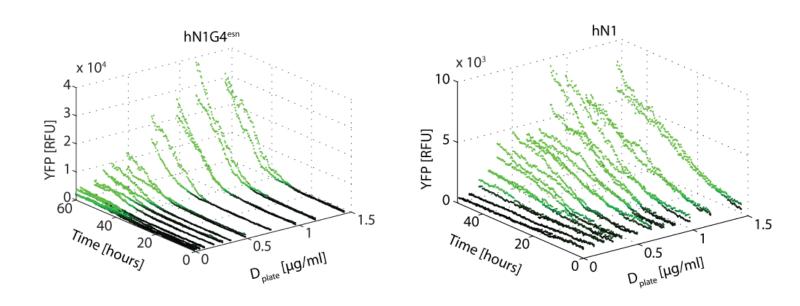
Confluent MDCK cells



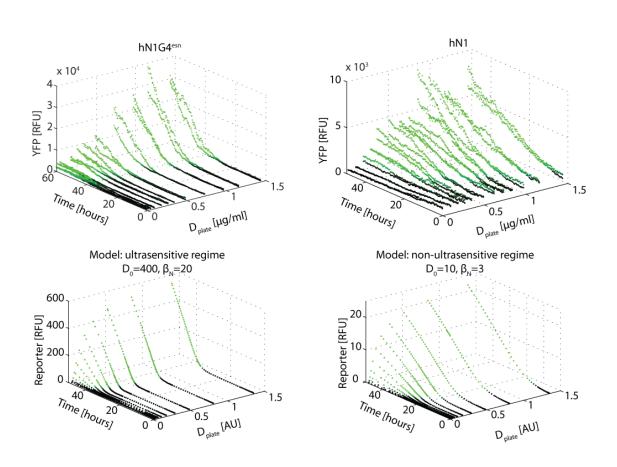
# Examples of active interaction between signaling and morphology

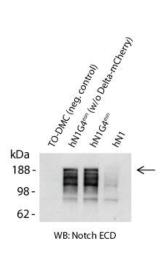
## Response of Notch signaling to both cis and trans Delta

hN1 vs hN1G4<sup>esn</sup>



### Model explains qualitative difference between measurements





#### Acknowledgments











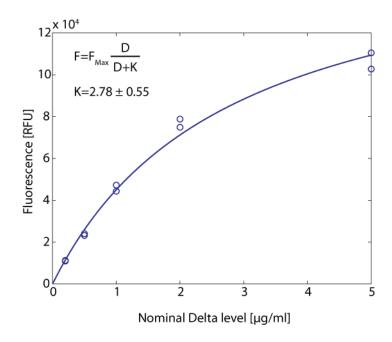
Jordi Garcia-Ojalvo

#### Special thanks

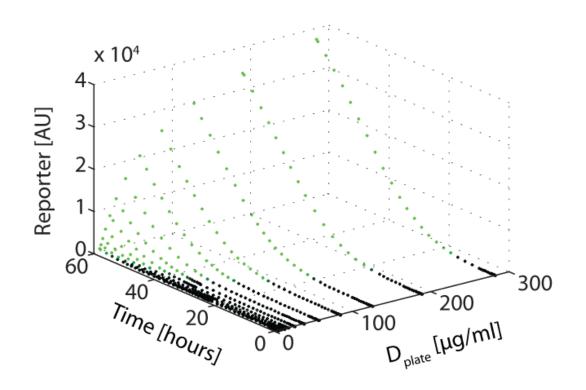
Gerry Weinmaster and the Weinmaster lab

Irv Bernstein
Jon Aster

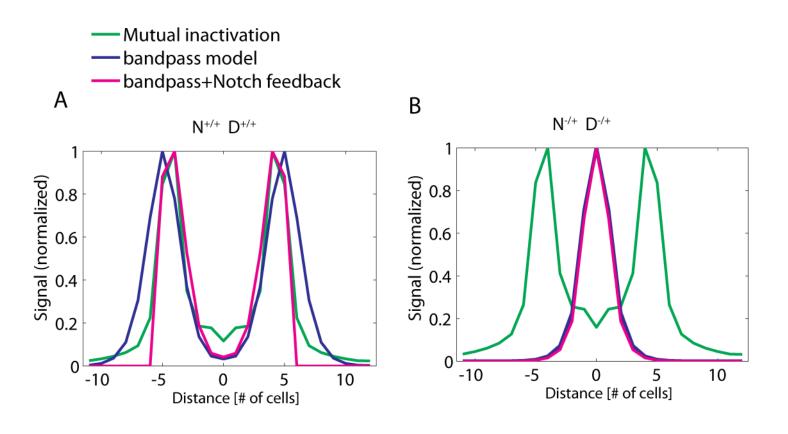
#### Plate bound Delta calibration



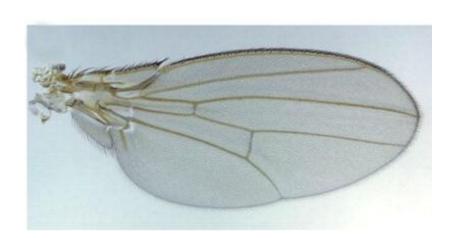
#### Catalytic model

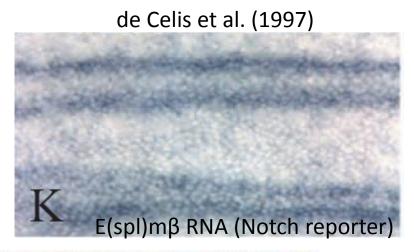


## Alternative models for boundary formation

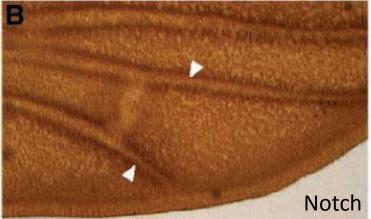


## Implications in Pattern formation 1: Sharp boundary in the wing vein



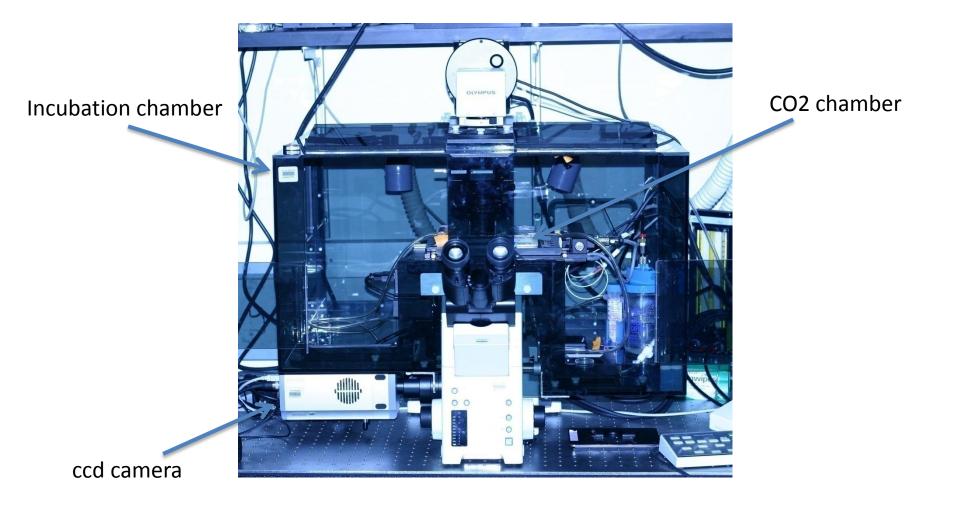






Huppert et al. 1997

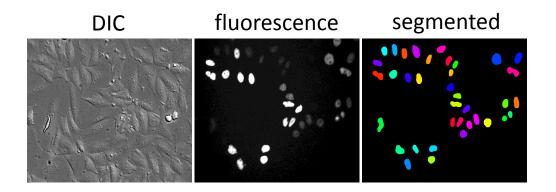
#### Quantitative time lapse microscopy using fluorescent protein reporters



#### Fully automated setup:

Allows taking time lapse microscopy movies over extended times (several days)

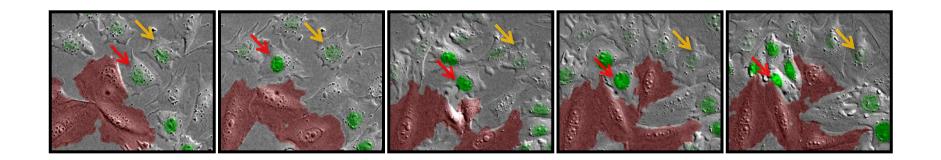
#### Automated segmentation and tracking

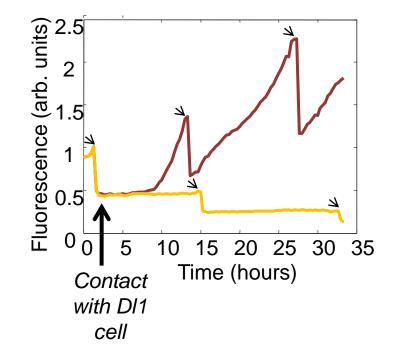


Developed automated image analysis routine:

- ➤ Identify (segments) single nuclei.
- ➤ Track nuclei through time lapse movie.
- ➤ Identify cell division and keeps track of lineage relations.

#### Quantitative analysis of Notch-Delta Signaling





#### **Conclusions:**

- We can track the dynamics of activation.
- We measure a time delay of a few hours between contact and transcriptional response.