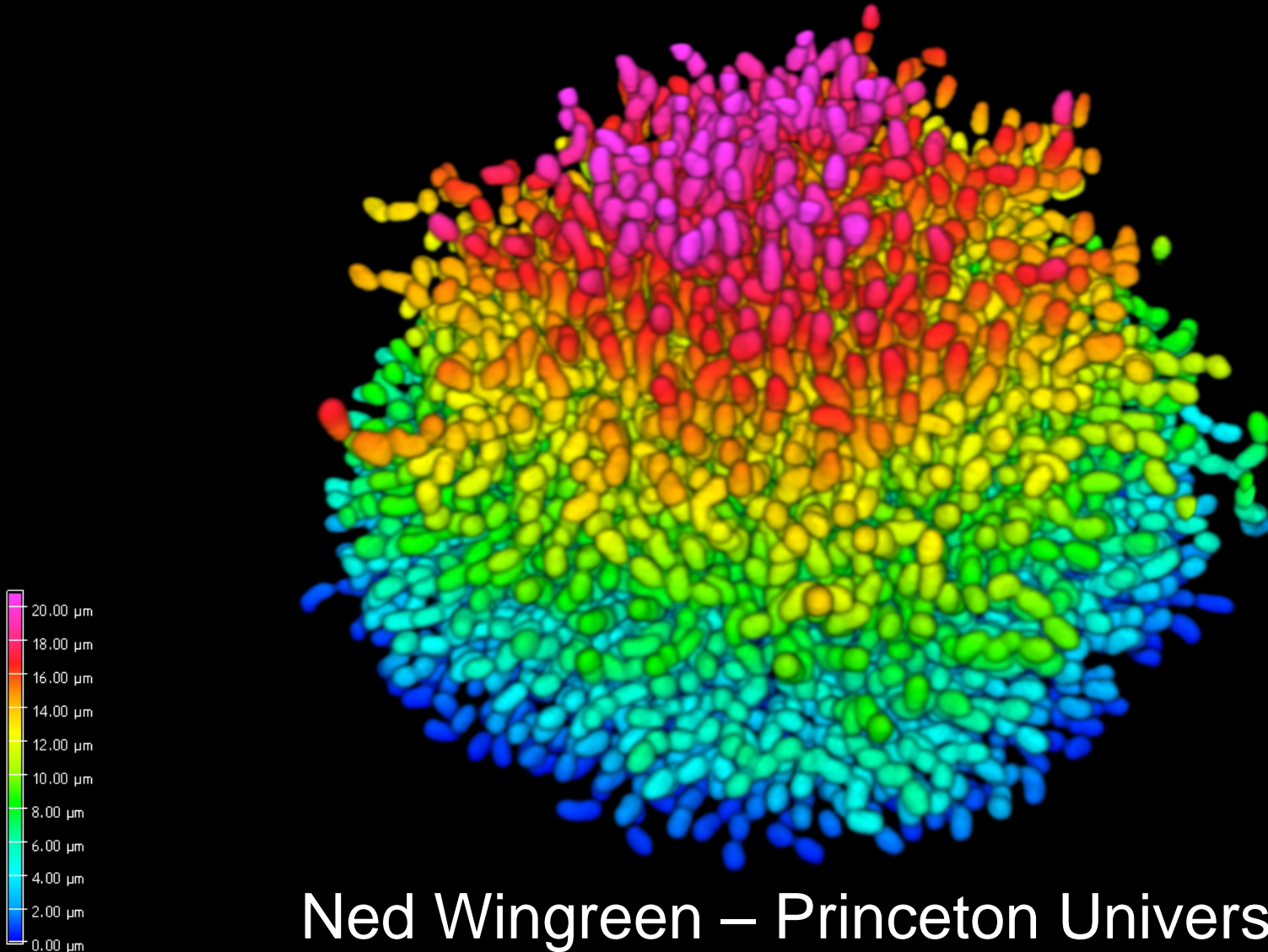


# Building a biofilm the *Vibrio cholerae* way



Ned Wingreen – Princeton University

# NOTICE.

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## PREVENTIVES OF **CHOLERA!**

Published by order of the Sanatory Committee, under the sanction of the Medical Council.

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### **BE TEMPERATE IN EATING & DRINKING!**

*Avoid Raw Vegetables and Unripe Fruit !.*

**Abstain from COLD WATER**, when heated, and above all from *Ardent Spirits*, and if habit have rendered them indispensable, take much less than usual.

### **SLEEP AND CLOTHE WARM !**

 **DO NOT SLEEP OR SIT IN A DRAUGHT OF AIR,**  
**Avoid getting Wet !**

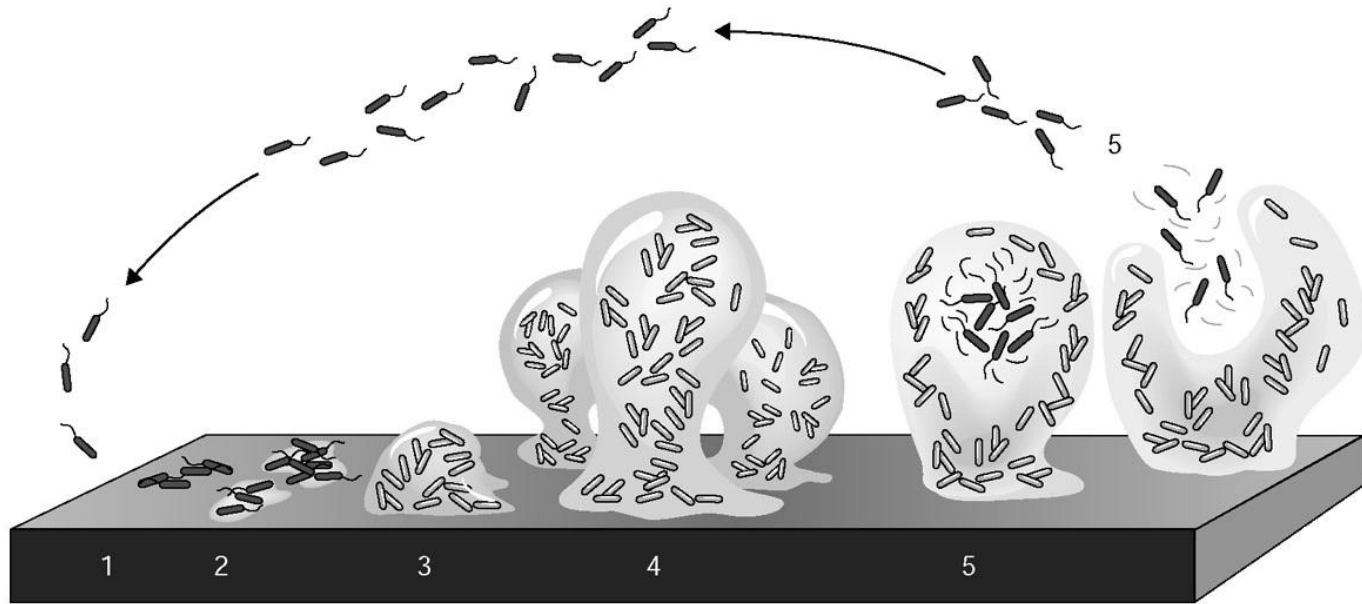
**Attend immediately to all disorders of the Bowels.**

**TAKE NO MEDICINE WITHOUT ADVICE.**

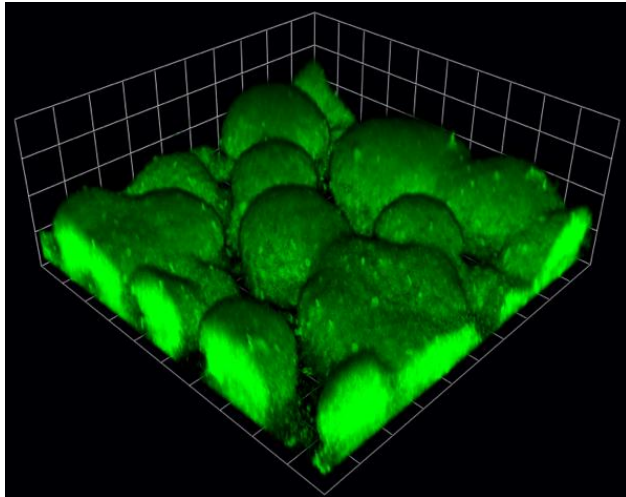
Medicine and Medical Advice can be had by the poor, at all hours of the day and night, by applying at the Station House in each Ward.

**CALEB S. WOODHULL, Mayor**  
**JAMES KELLY, Chairman of Sanatory Committee.**

# How to form a 3D biofilm?



Adapted from Stoodley (2001)



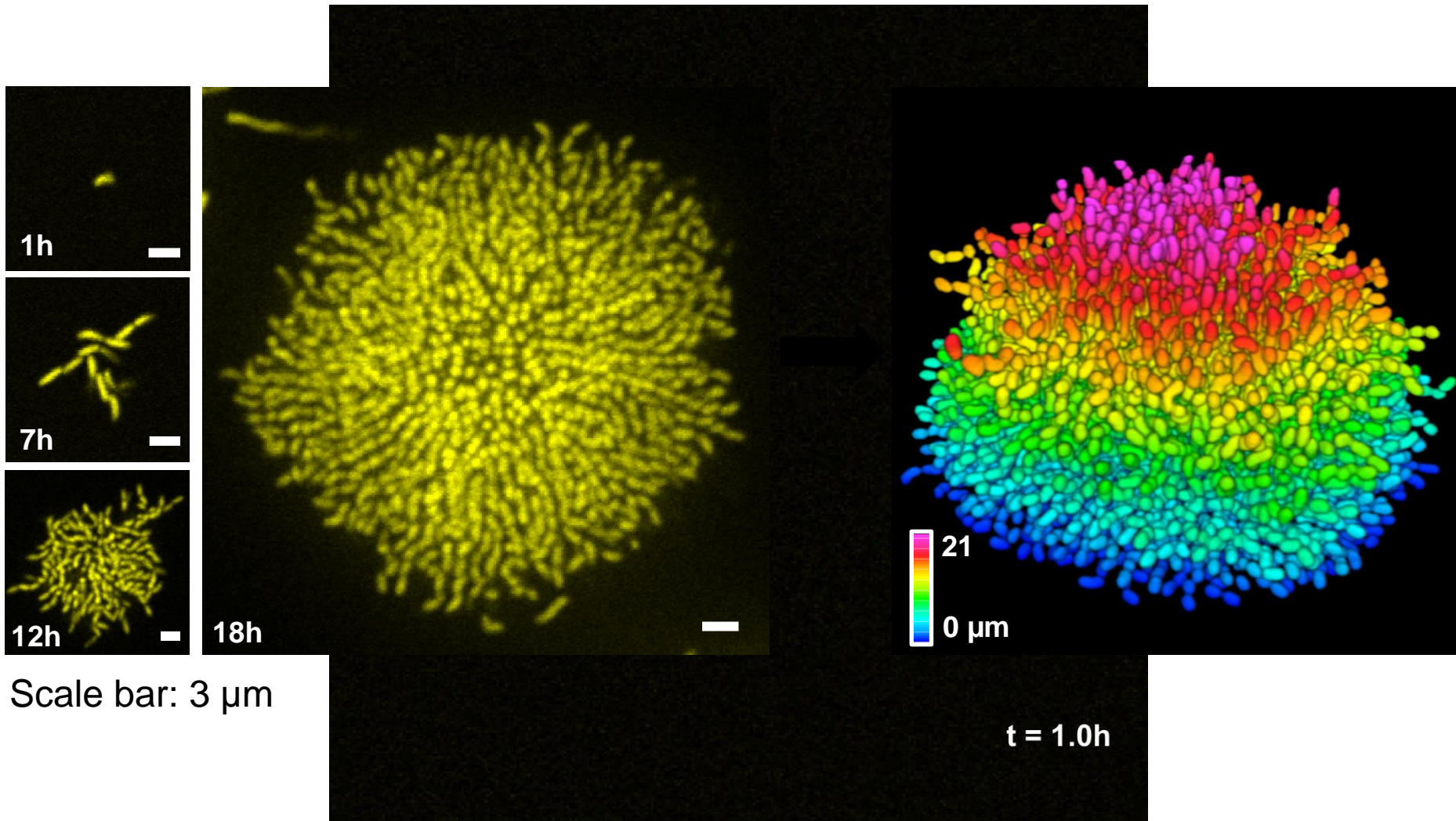
Harwood *et al.* (2005)



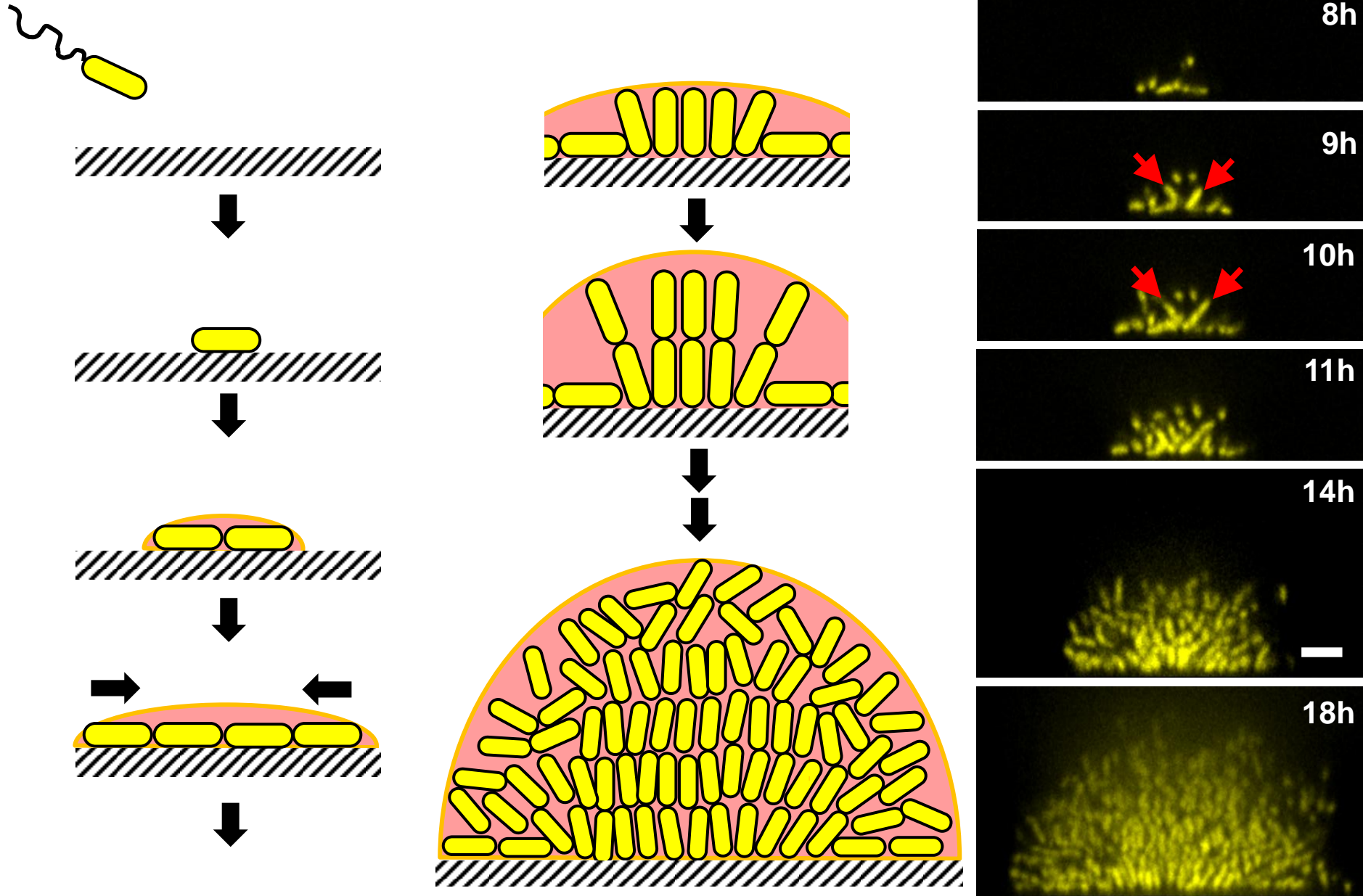
[www.idynamics.org](http://www.idynamics.org)



# Biofilm formation cell-by-cell



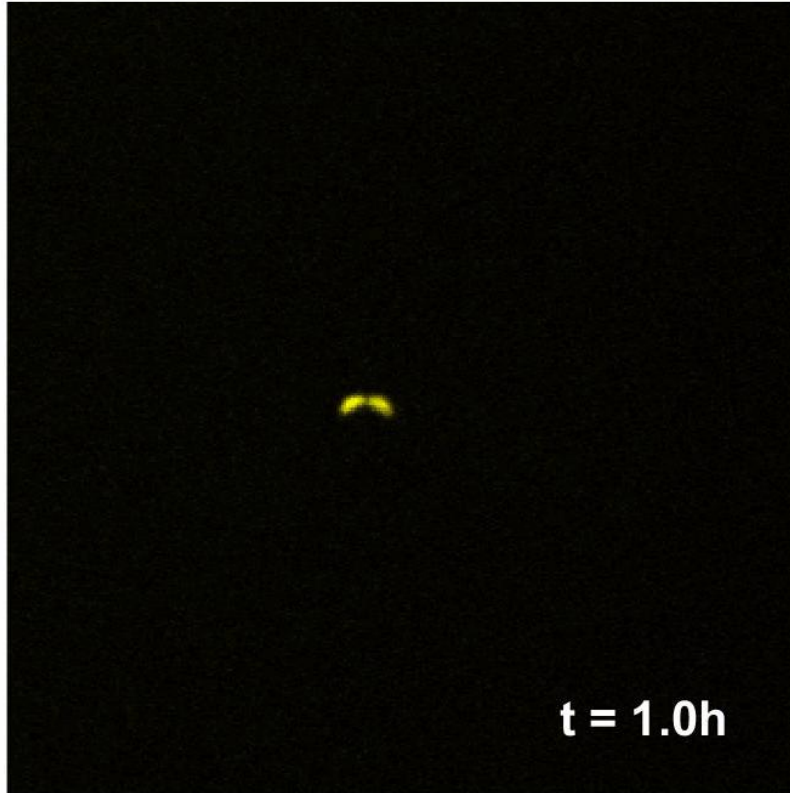
# Schema for *V. cholerae* biofilm growth



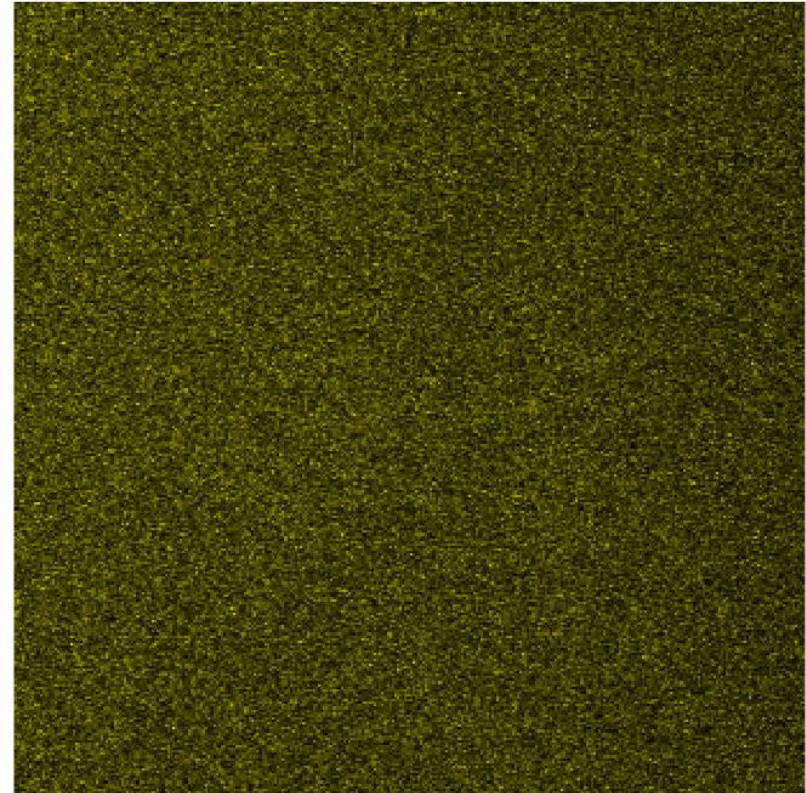


# Role of cell-to-surface adhesion

At the surface



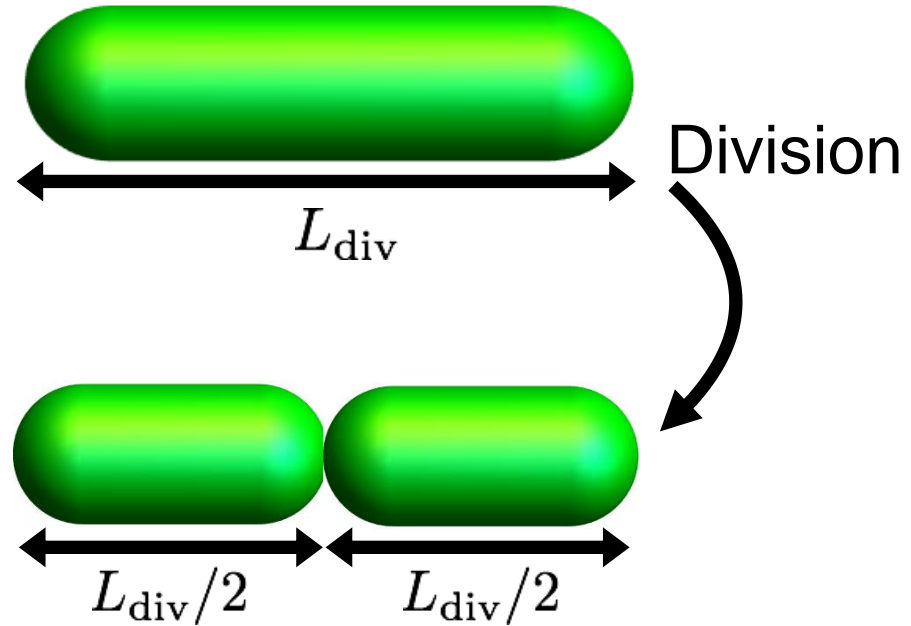
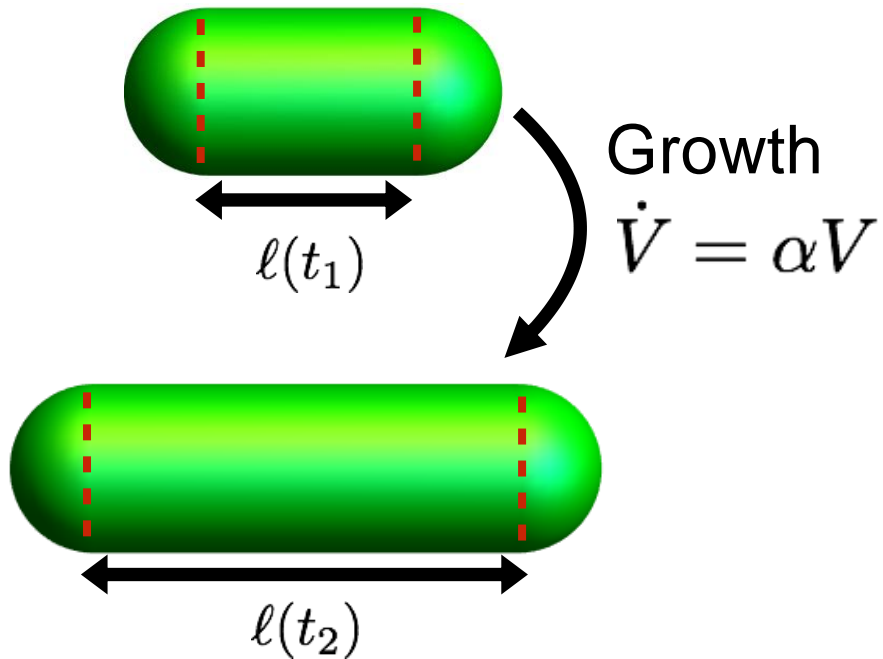
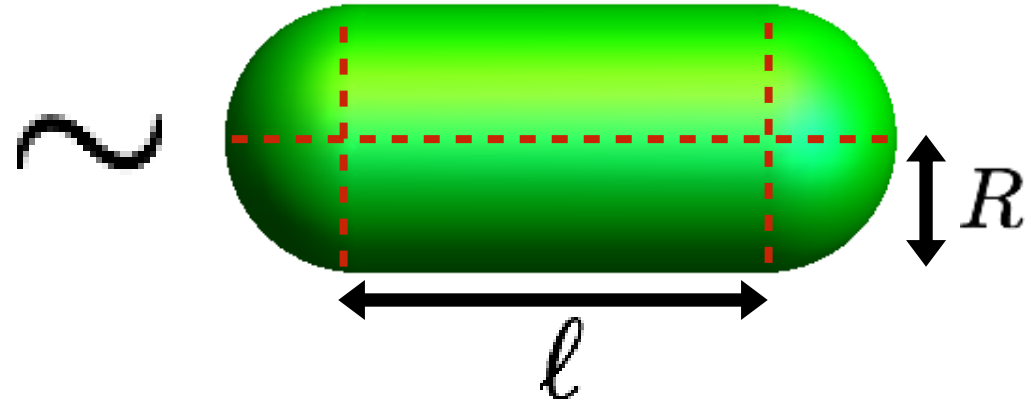
5 microns above the surface



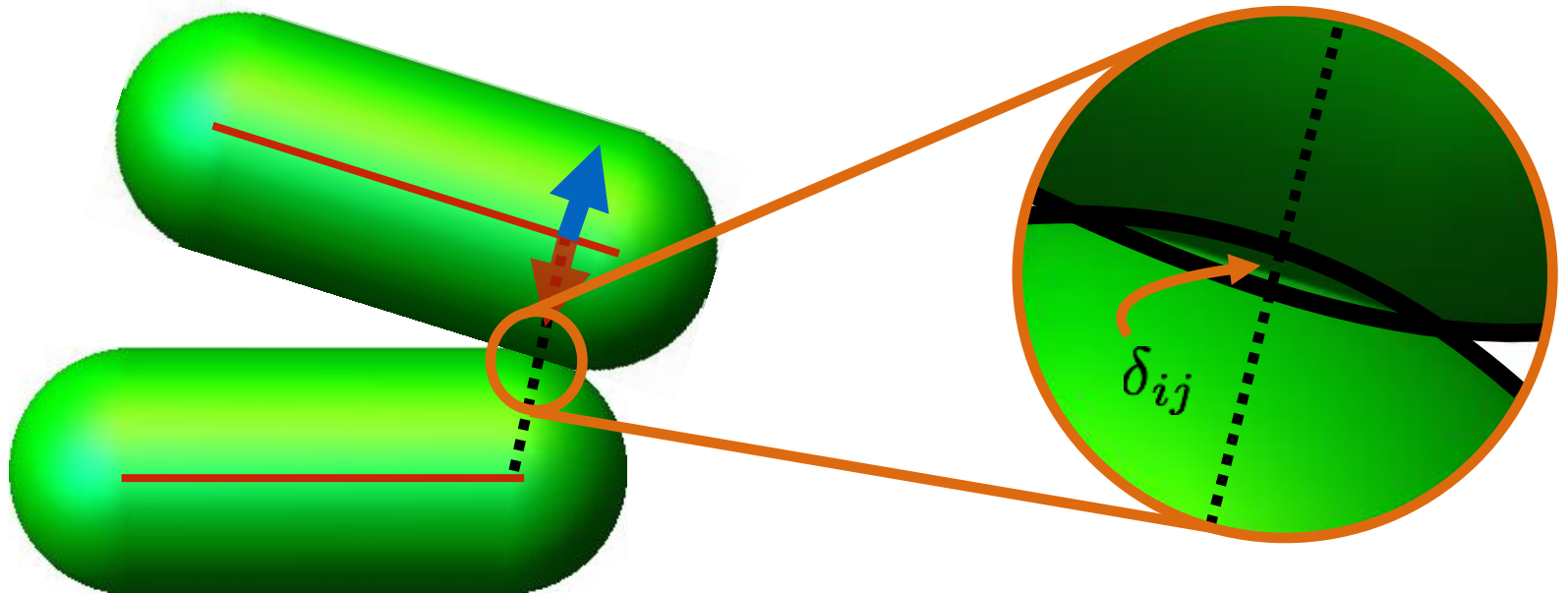
---

$\Delta bap1 \Delta rbmC$  mutant

# Agent based simulation



# Cell-cell interaction



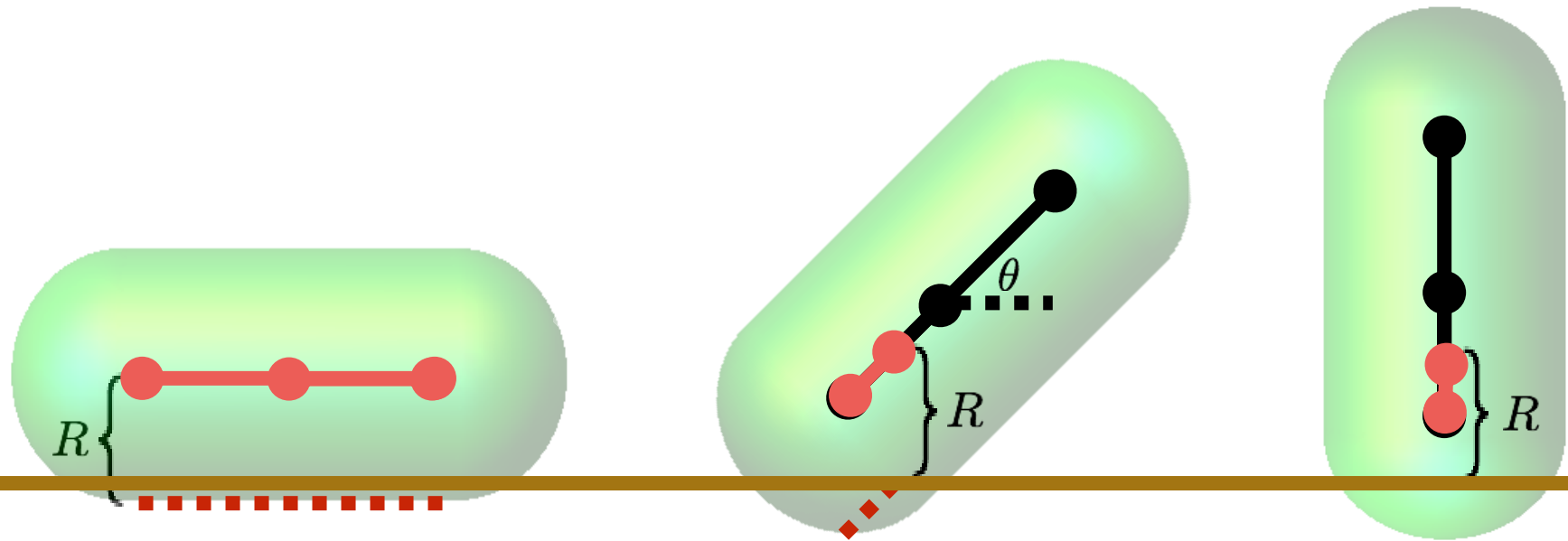
**Repulsion** due to  
elastic energy

**Attraction** due to  
adhesive energy

$$E_{\text{cell-cell}} = E_0 R^{1/2} \delta_{ij}^{5/2} - A_0 R^{-1} \delta_{ij}$$

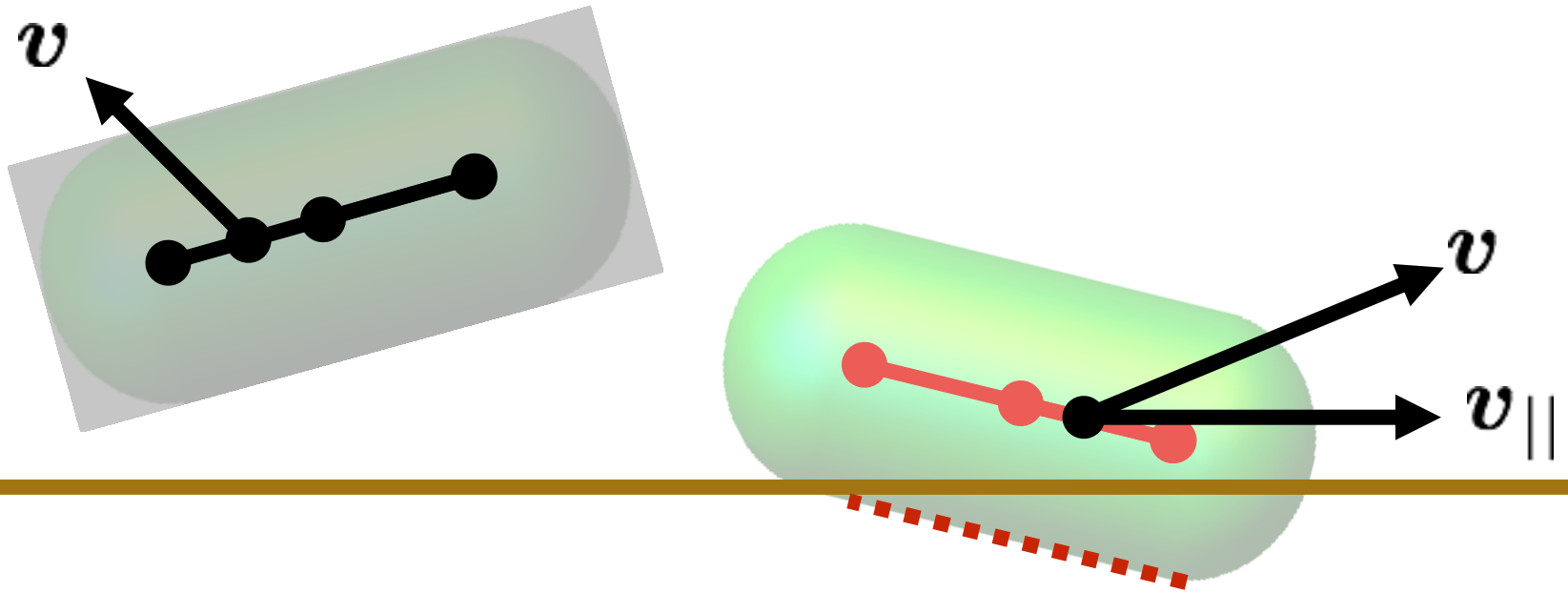


# Cell-surface interaction interpolates between cylindrical and spherical contacts



$$\delta_{\text{eff}}^{5/2} = \delta_{ij}^2 \cos^2(\theta) + R^{1/2} \delta_{ij}^{3/2} \sin^2(\theta)$$

# Viscous drag



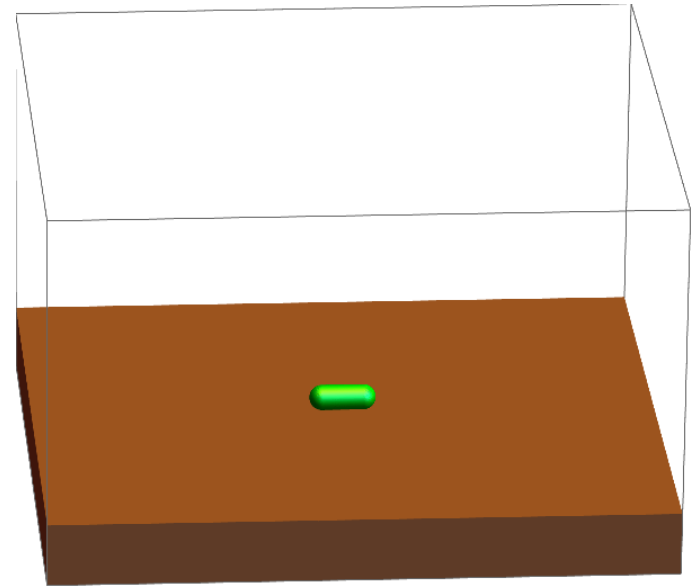
$$\mathbf{F}_{\text{drag}} = \nu_0 \mathbf{v} + \nu_1 A_{\text{eff}} \mathbf{v}_{||}$$

Ambient  
drag

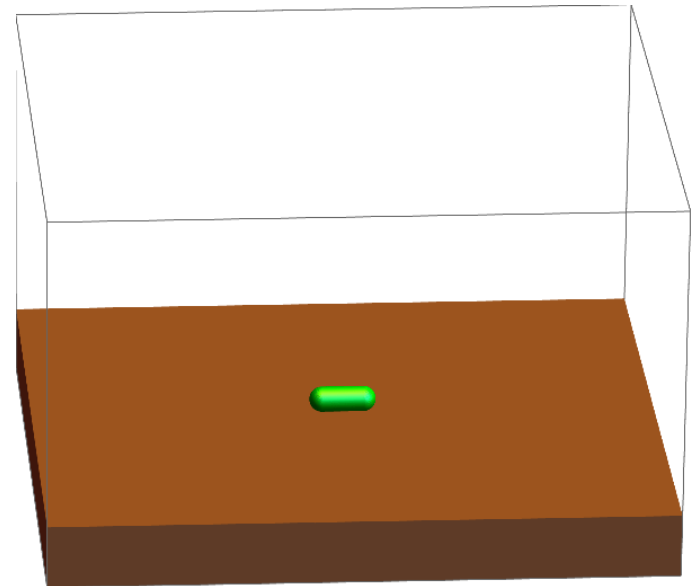
Surface  
drag

# Surface interaction facilitates 3D growth

Ambient  
drag only

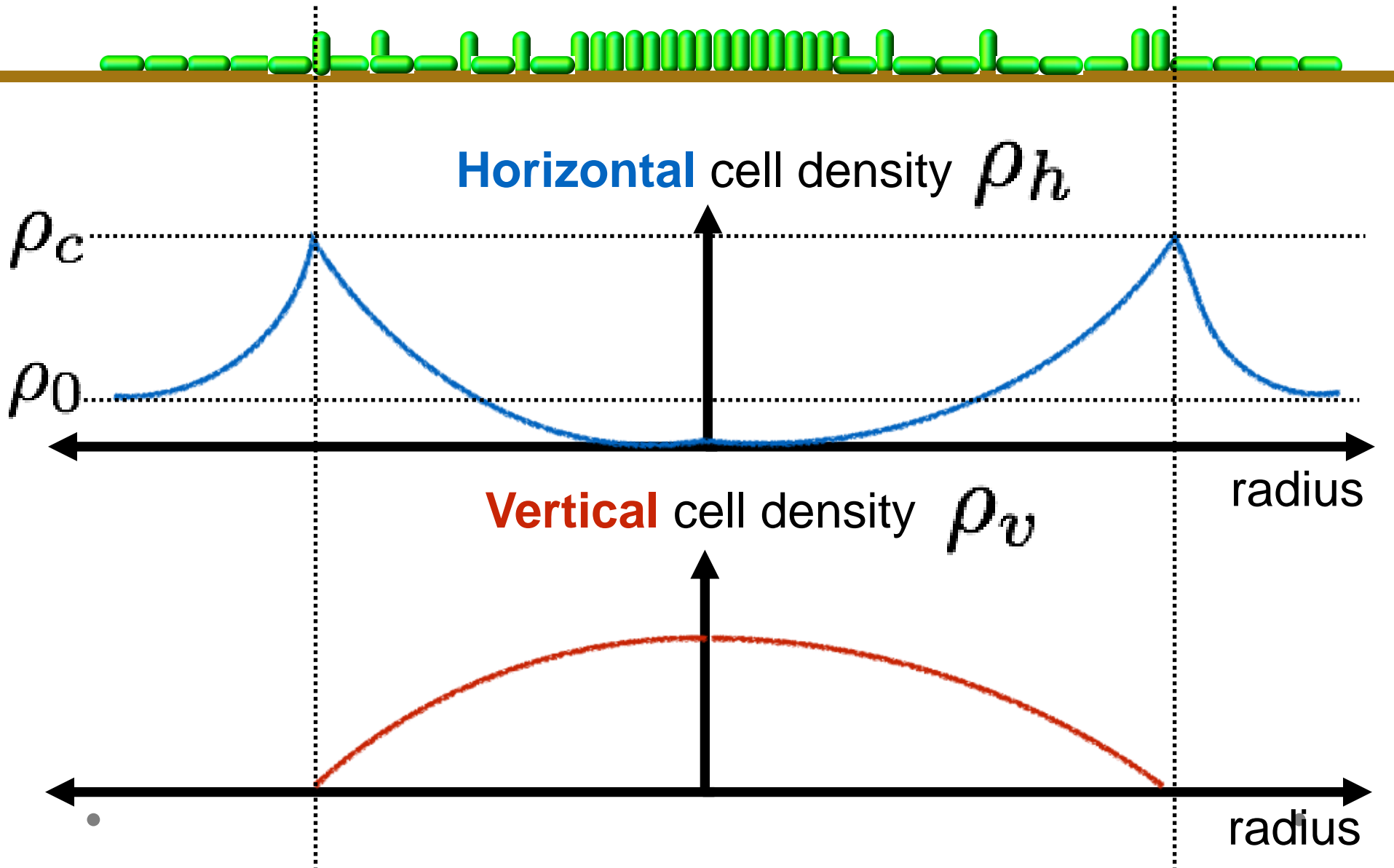


Ambient drag  
plus surface  
drag





# Continuum model for “verticalization”



# Continuity equations for horizontal and vertical cells

**Horizontal** cells

$$\dot{\rho}_h + \nabla \cdot (\rho_h \mathbf{v}) = \alpha \rho_h$$

Cell flux

growth  
rate

pop-up rate  
("verticalization")

$$\dot{\rho}_v = \beta \Theta(p - p_c) \rho_h$$

**Vertical** cells

# Cells push on their neighbors

Approximation: pressure  $\sim$  cell density (above packing density)

$$p = \begin{cases} \lambda(\rho_h + \xi\rho_v - \rho_0) & \text{if } \rho_h + \xi\rho_v > \rho_0 \\ 0 & \text{otherwise} \end{cases}$$

Force balance:  $-\eta\rho_h\mathbf{v}_h = \nabla p$



# Equations of motion

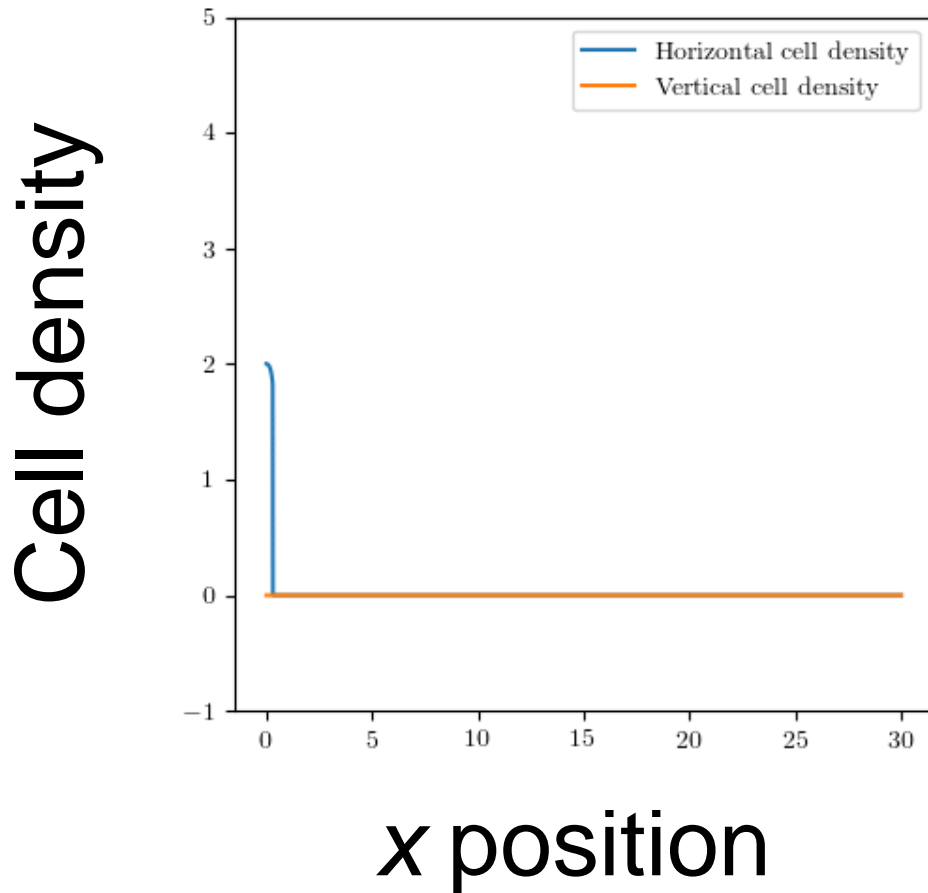
**Horizontal** cells

$$\dot{\rho}_h = \gamma \nabla^2 (\rho_h + \xi \rho_v) + [\alpha - \beta \Theta(p - p_c)] \rho_h$$

**Vertical** cells

$$\dot{\rho}_v = \beta \Theta(p - p_c) \rho_h$$

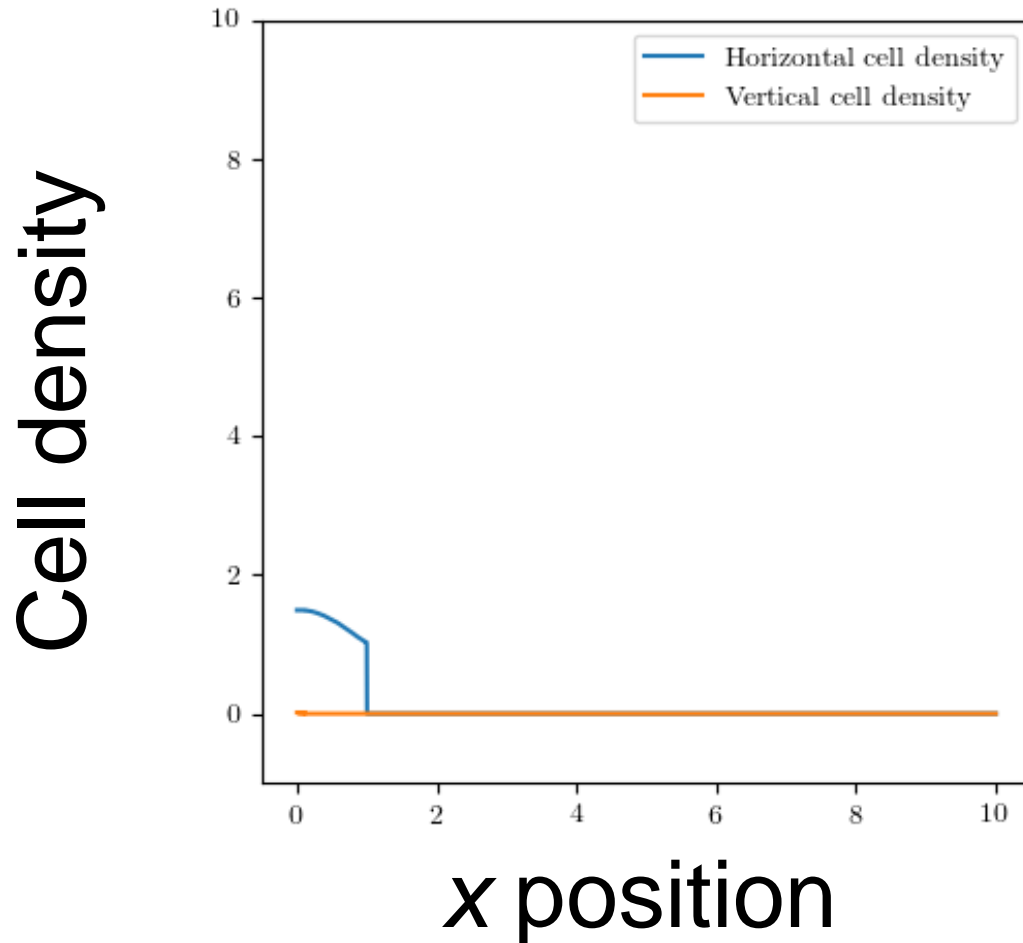
# Numerical solution yields moving front



- Traveling "shark fin" of horizontal cells
- Front moves with constant speed

Can we predict the speed and shape?

If verticalization is fast  $\rightarrow$  “isobaric” regime



Isobaric regime if

$$\alpha/\beta < 1 - \xi$$

$\alpha$  = growth rate

$\beta$  = verticalization rate

$\xi$  = ratio of vertical to horizontal footprint



# Cell length influences colony shape

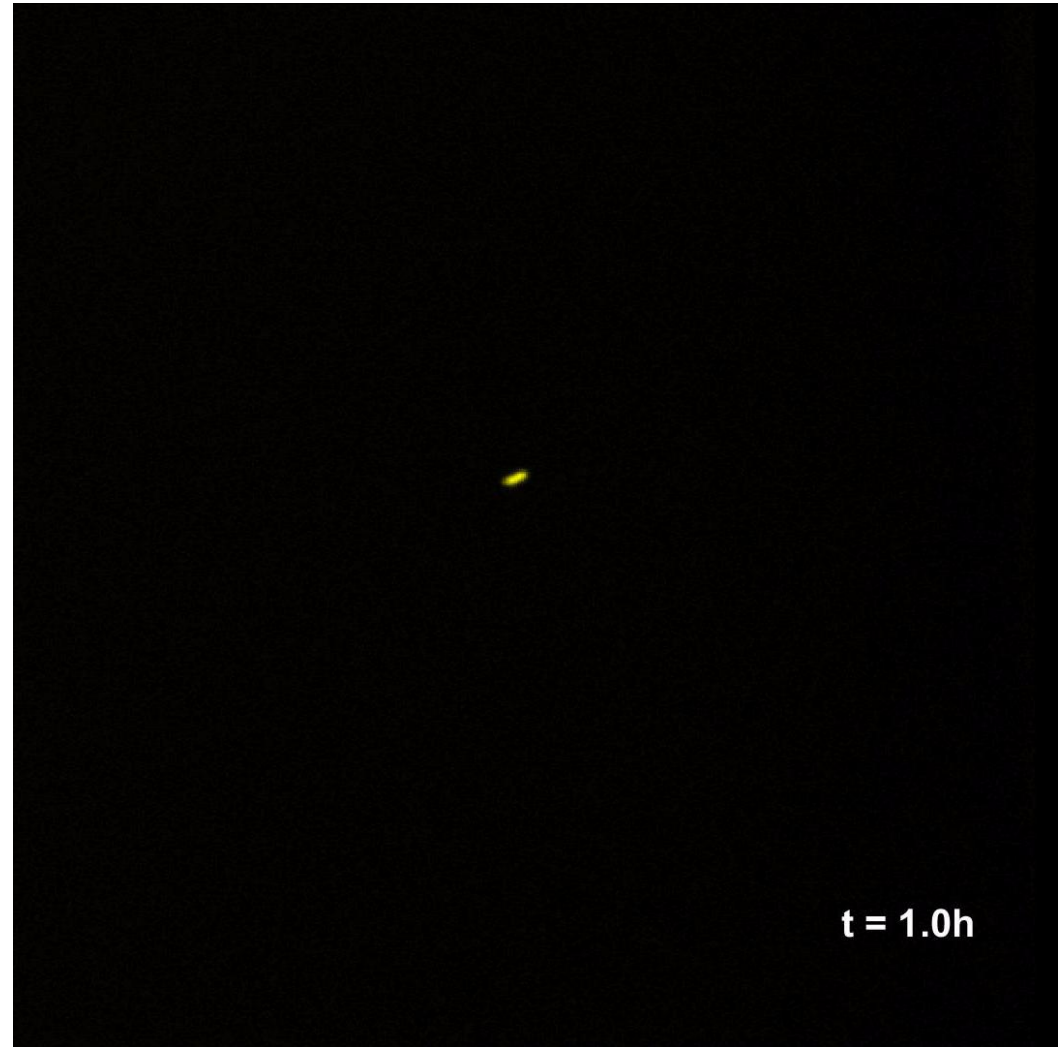
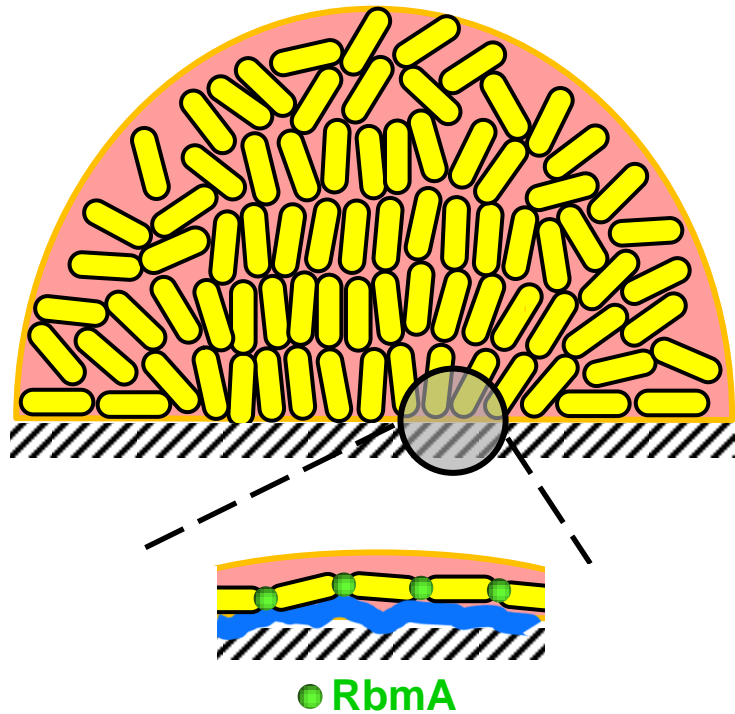


$$L_{\text{div}} = 3$$



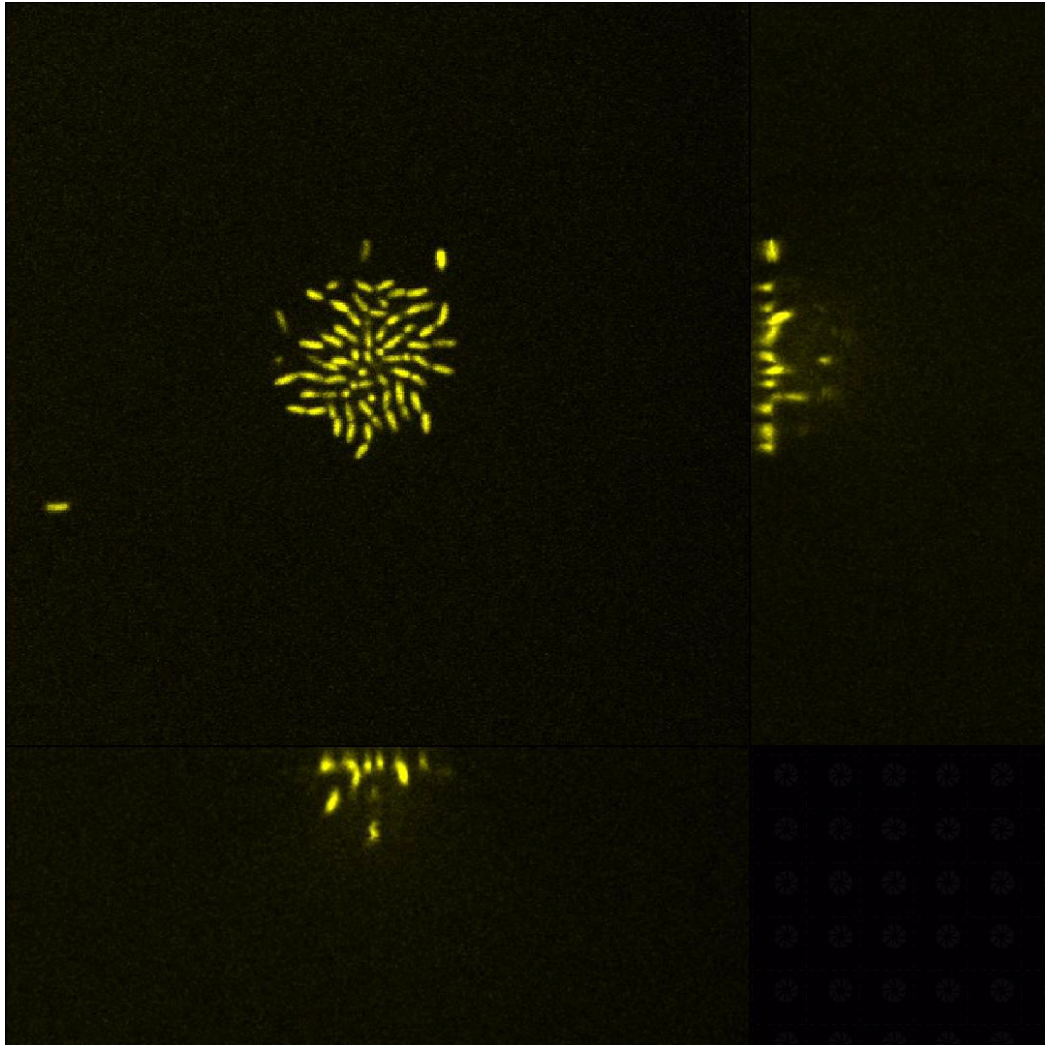
$$L_{\text{div}} = 7$$

# Role of cell-to-cell adhesion



$\Delta rbmA$  mutant

# A different mode of biofilm growth



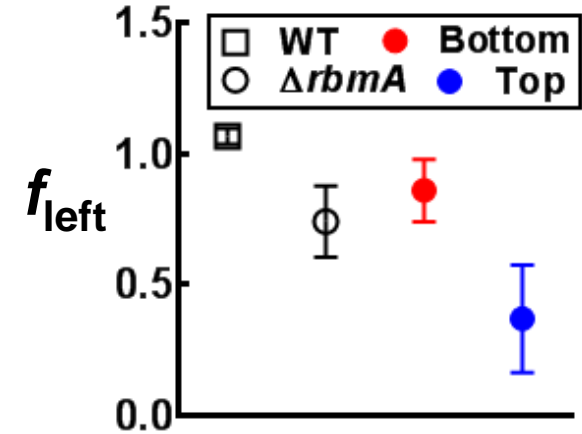
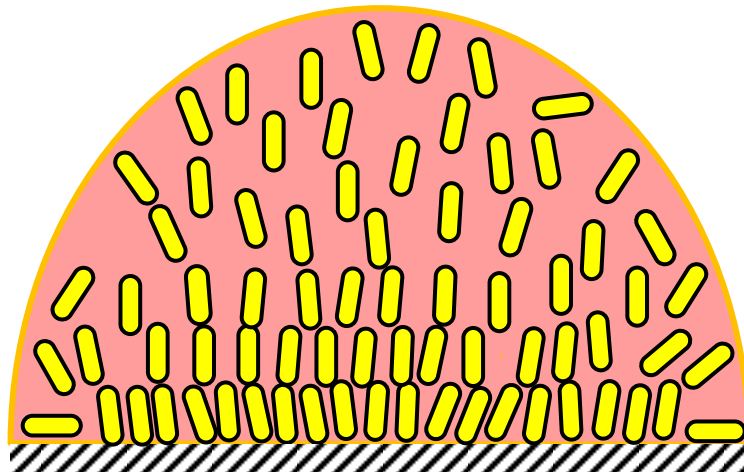
# Resistance to mechanical perturbation

Perturbation  
←→

RbmA<sup>+</sup>

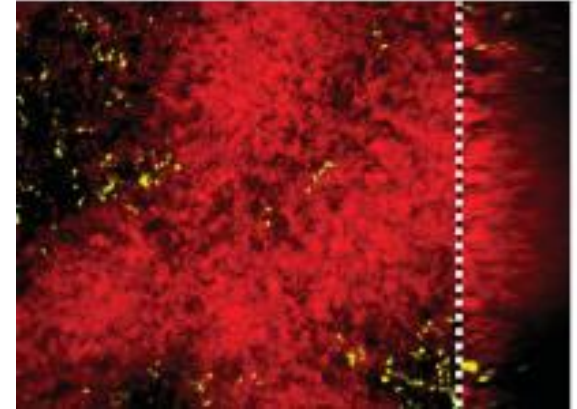
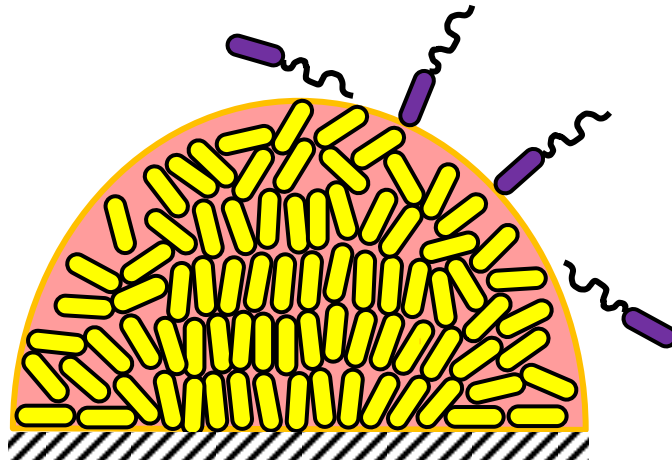


RbmA<sup>-</sup>

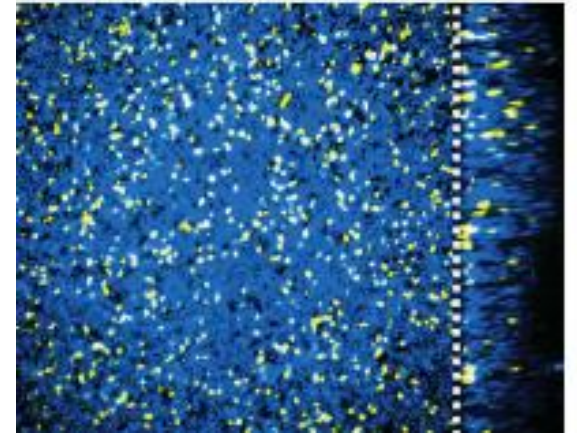
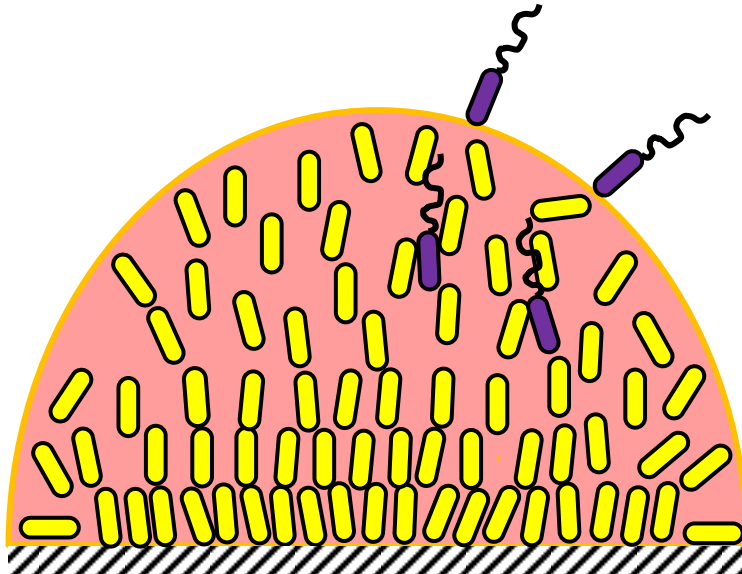


# Resistance to invasion

RbmA<sup>+</sup>

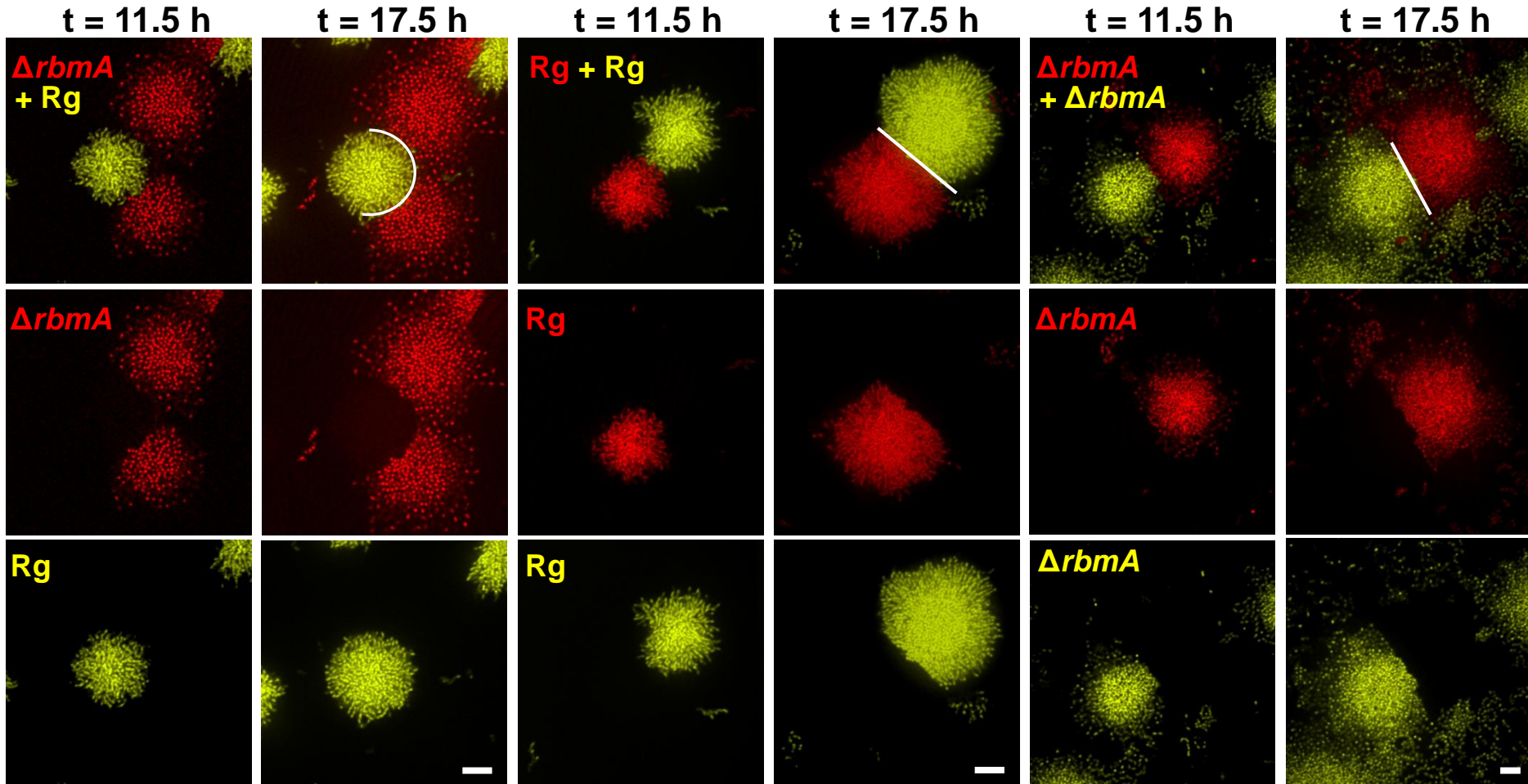


RbmA<sup>-</sup>



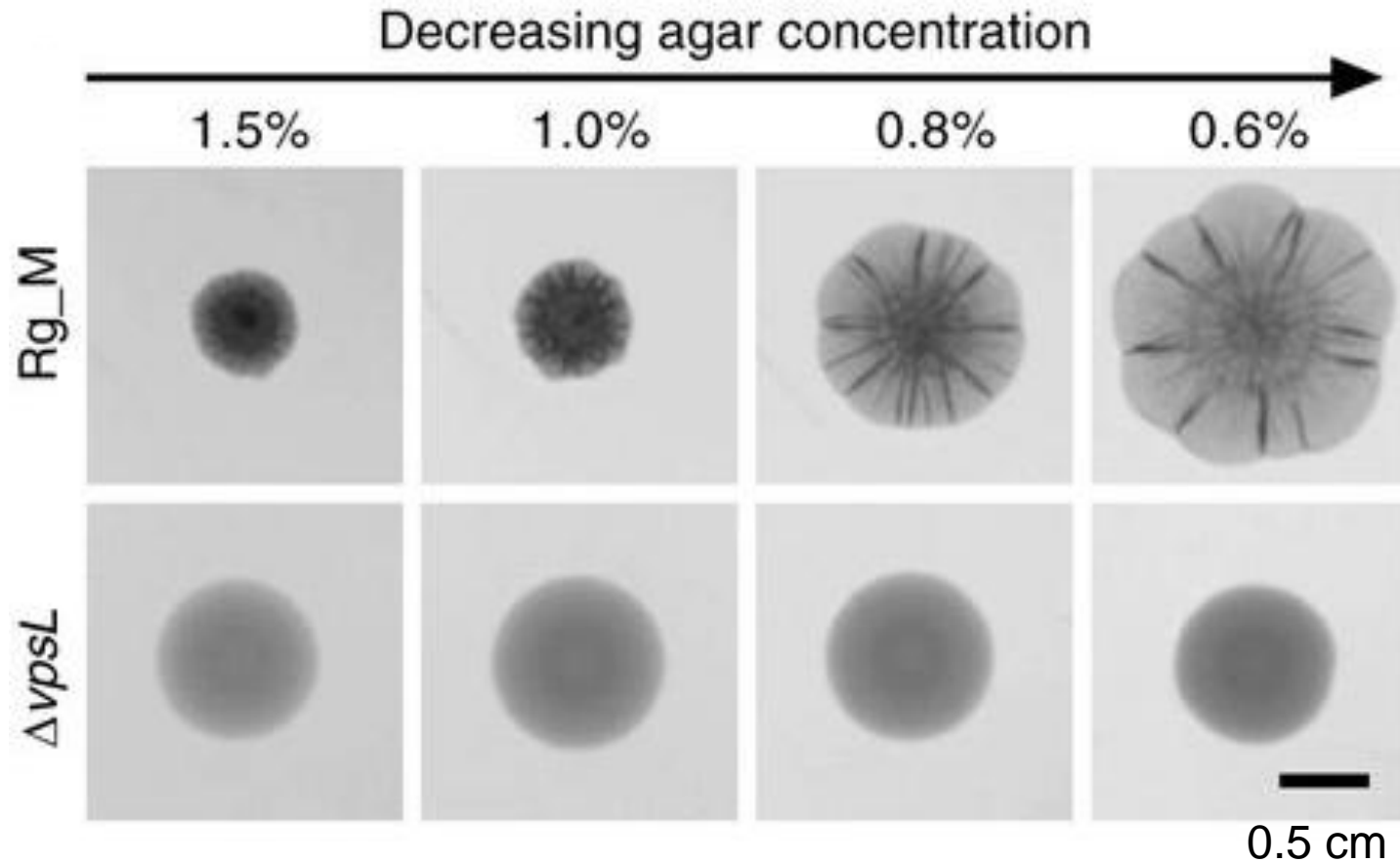


# Contact between two clusters

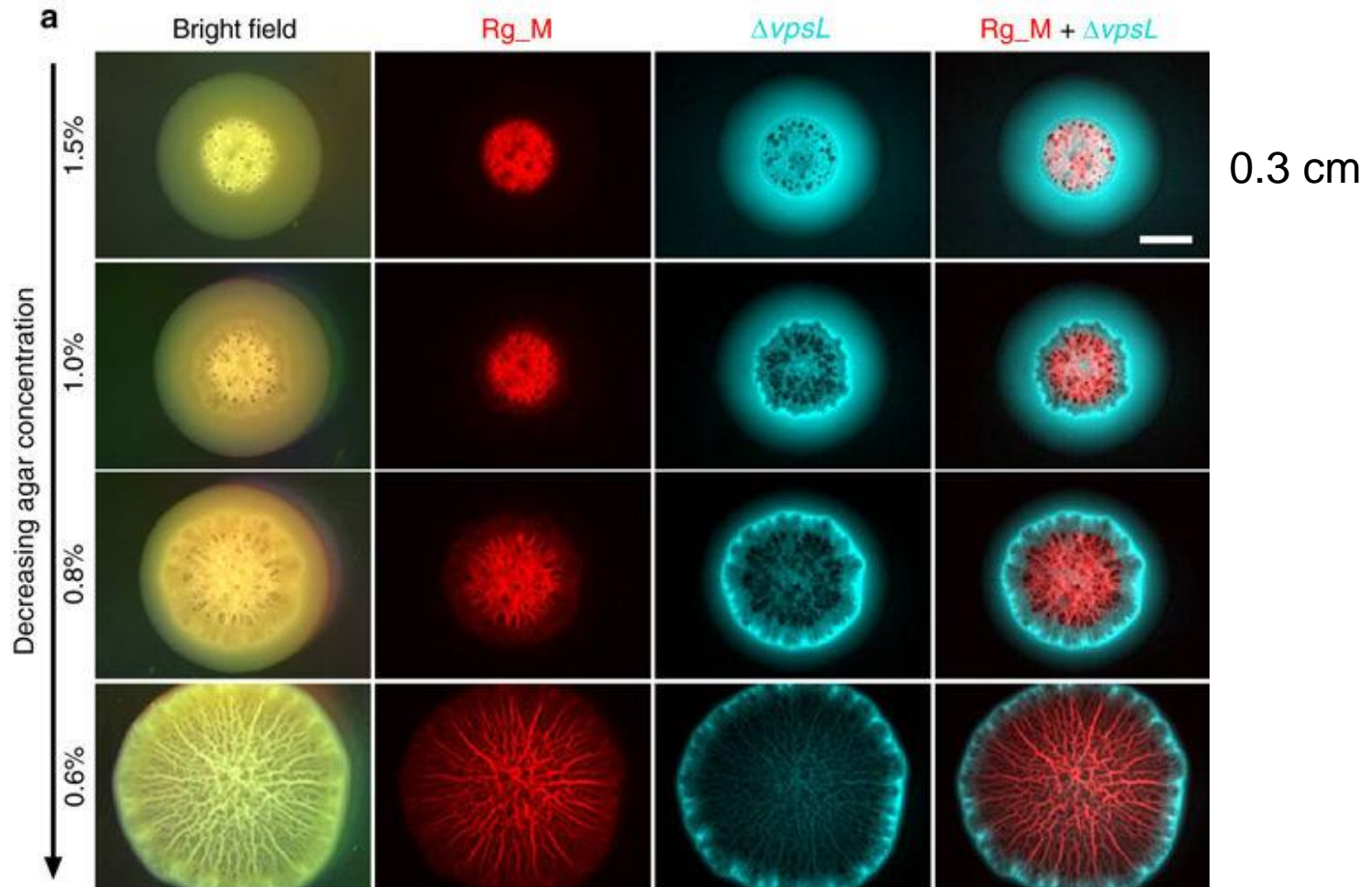




# Osmotic pressure drives biofilm expansion



# Osmotic swelling enables matrix producer to exclude non-producer



# Summary

- Biofilms are ubiquitous – bacteria live in communities
- Single-cell imaging reveals single founder, 2D → 3D transition, and internal order
- Agent-based and continuum modeling reveal mechanism of verticalization, influence of cell size, etc.
- *V. cholerae* biofilms control territory:
  - Resist invasion
  - “Bulldoze” competitors
  - Exploit osmotic swelling

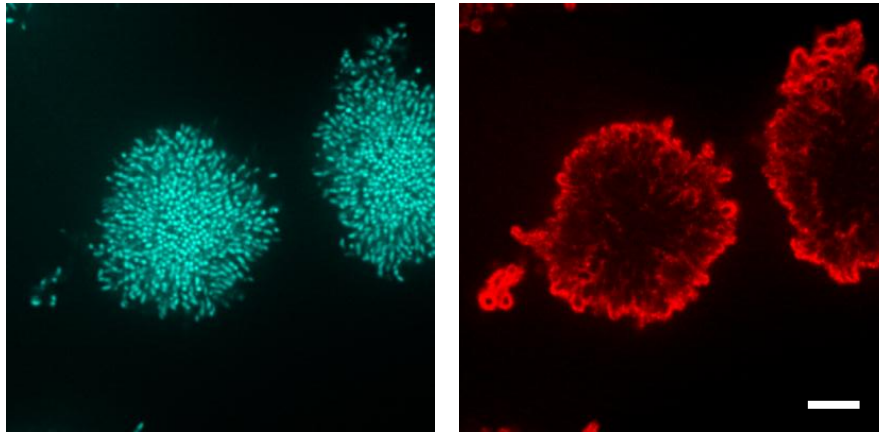
Drescher *et al.*, PNAS (2016)

Yan *et al.*, PNAS (2016)

Yan *et al.*, Nature Comm (2017)

# Future directions

- Role of cell curvature?
- Role of the matrix “envelope”?



- Quorum sensing & gene expression
- How do different species build biofilms?
- Implications for disease

# Acknowledgements

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Transformative Technology Fund



# Colocalization of matrix components

