Probing the Early Universe with *Gravitational Waves* from Cosmic Strings



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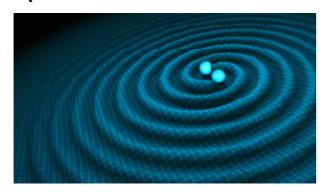


arxiv: 1711.03104 (PRD), 1808.08968 (JHEP)
YC with Marek Lewicki, David Morrissey and James Wells
work in prep, YC with Chia-Feng Chang

KITP workshop, Jul 5, 2019

Gravitational Waves: An Unprecedented Window to New Physics?

 LIGO discovery 2016:
 A new era of observational astronomy (blackholes, neutron stars...)





 New opportunities for probing new particle physics/ early universe cosmology?

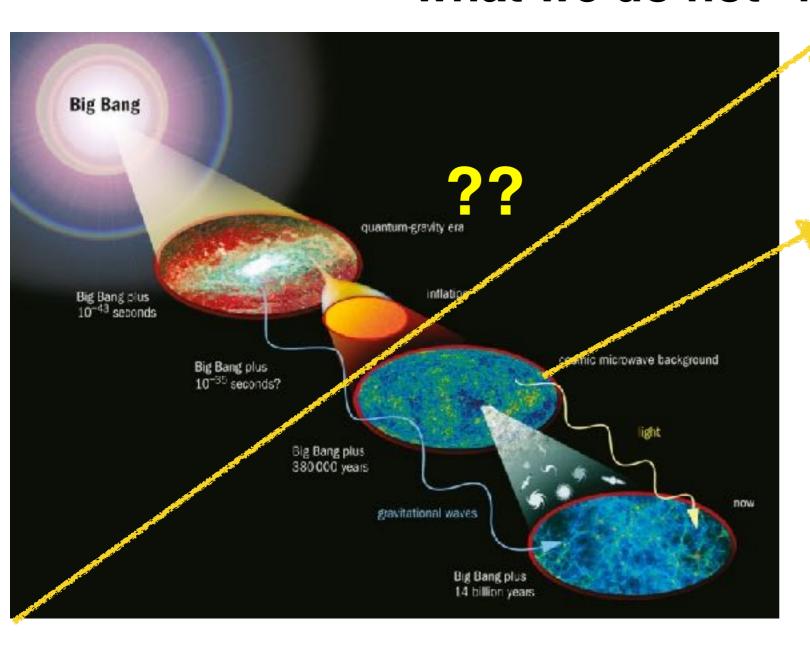


BSM Physics and GW

-what we know

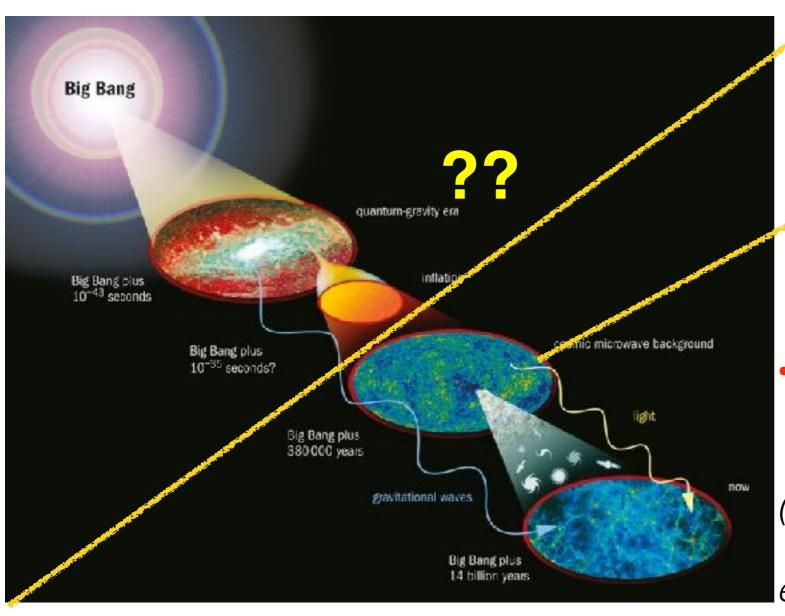
- Cosmological sources of GW:
 - Inflation
 - Preheating
 - 1st order phase transition: EWPT/EWBG
 - Cosmic strings ★: e.g. following a spontaneous U(1) symmetry-breaking (at any scale: γ', Z', U(1)_{B-L}, axion...) or superstring theory (arxiv: 1712.01168 by LIGO and Virgo collaboration)
- Dramatic events in the (pre-BBN) early universe
 - Effects on GW from BH/NS: axions, light bosons (e.g. Dimopoulos et al. 2016; Nelson et al. 2017)

-what we do not "know"



- The horizon of confidence: BBN (~1s-3 min after Big Bang)
- CMB light: a direct window back to ~400k yrs after the Big Bang

-what we do not "know"



- The horizon of confidence: BBN (~1s-3 min after Big Bang)
- CMB light: a direct window back to ~400k yrs after the Big Bang
- What happened before BBN?

Theory: standard cosmology; many unknowns!

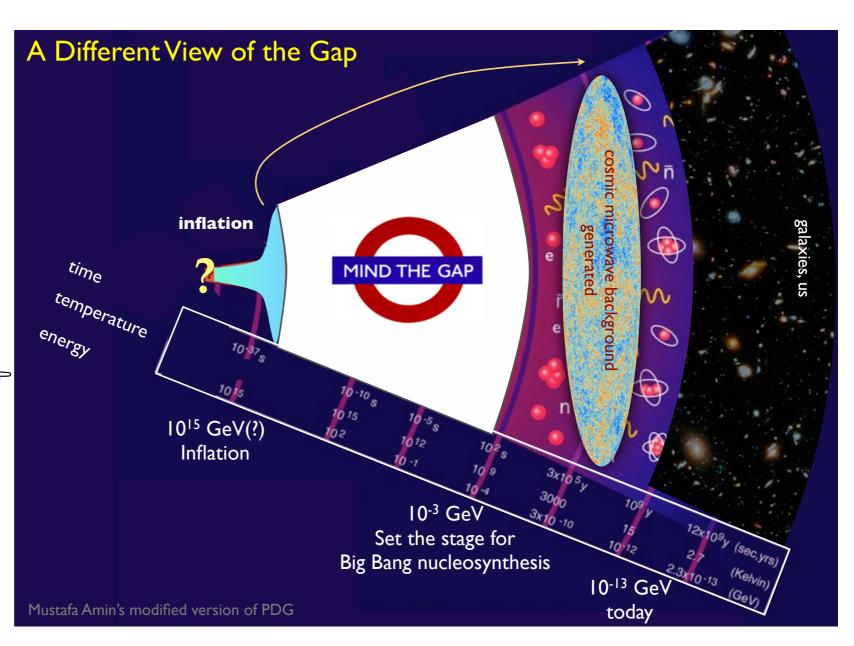
(scale of inflation/reheating? early matter domination (moduli)? early phase transitions? new d.o.f?...)

the Primordial Dark Age

(Boyle and Steinhardt 2005, Boyle and Buonanno 2007)

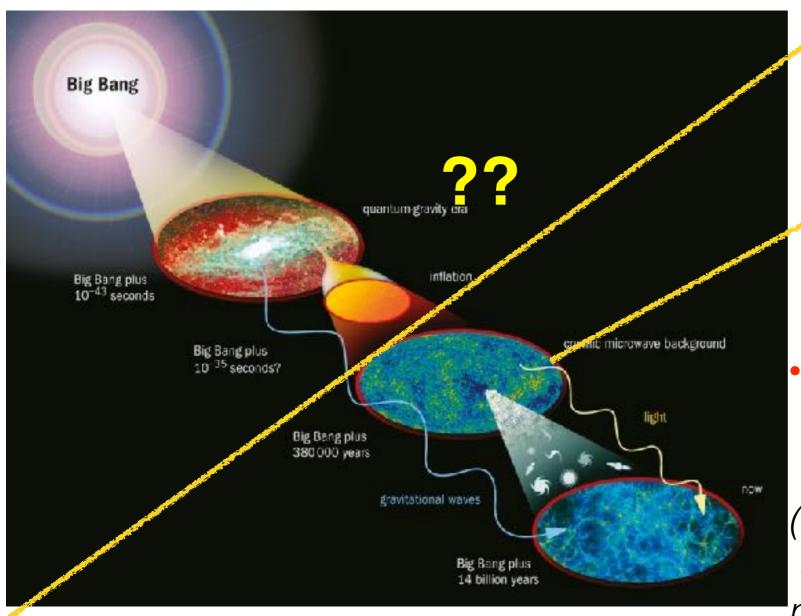
What happened within the first ~1 sec?

The gap amplified on Log scale of temperature $T(\alpha a^{-1})!$



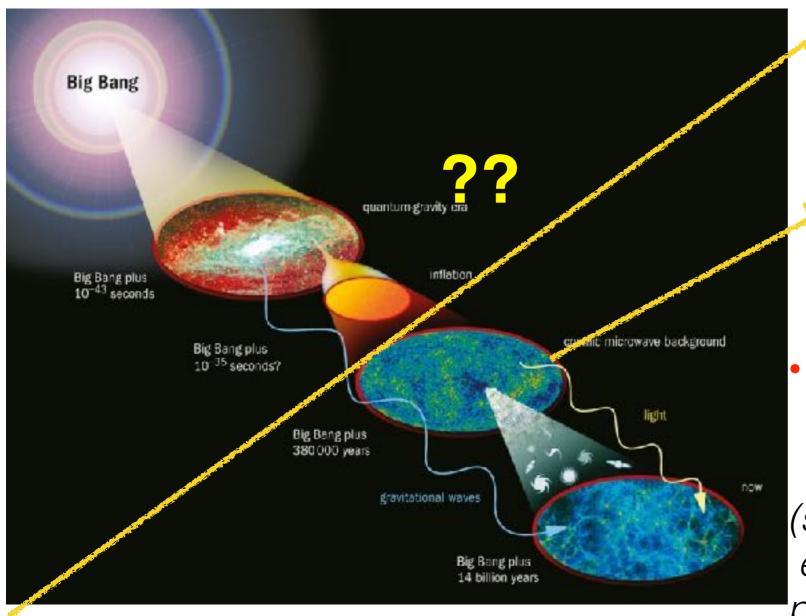
The Universe is RD with SM content from T_{eq} all the way back to the end of inflation: up to 24 orders of magnitudes on T scale! — IS IT??

-what we do not "know"



- The horizon of confidence: BBN (~1s-3 min after Big Bang)
- CMB light: a direct window back to ~400k yrs after the Big Bang
- What happened before BBN? standard cosmology, no observational proof... (scale of inflation/reheating? early matter domination? early phase transitions? new d.o.f?...)

-what we do not "know"

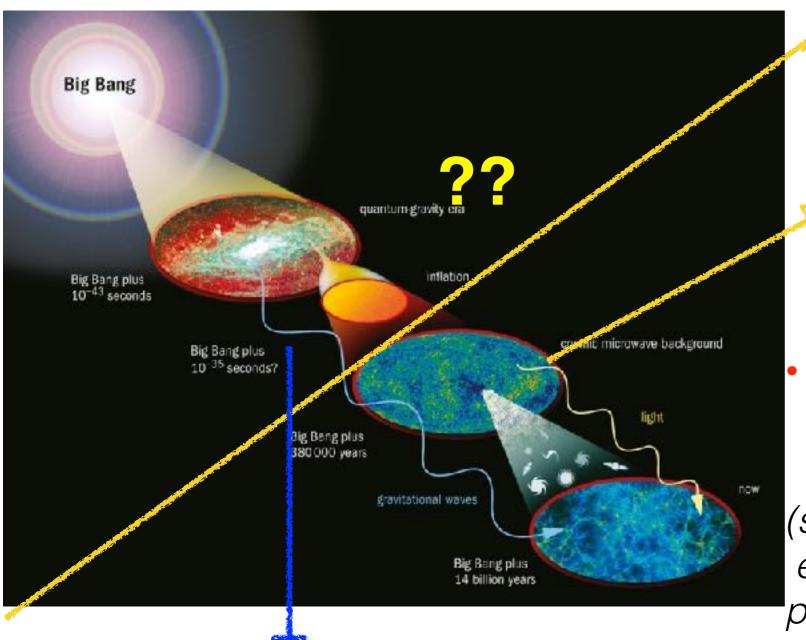


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Direct observational probe?
most effort so far: inflation. Thermal history?
Mission impossible?

-what we do not "know"



- The horizon of confidence: BBN
 (~1s-3 min after Big Bang)
- CMB light: a direct window back to ~400k yrs after the Big Bang
- What happened before BBN? standard cosmology, no observational proof...
 (scale of inflation/reheating? early matter domination? early phase transitions? new d.o.f?...)

GW: the window of hope?



Direct observational probe? most effort so far: inflation. Thermal history? Mission impossible?

Cosmic Archaeology with GWs from Cosmic Strings

(arxiv: 1711.03104, 1808.08968, YC with Lewicki, Morrissey and Wells)

- A direct probe of pre-BBN Universe with GWs

Outline

- A brief review on cosmic strings
- Test of standard cosmology: The time-frequency correspondence in the cosmic string GW spectrum
- Probe new phases of cosmic evolution (eq. of state)
- Probe new degrees of freedom (beyond LHC, CMB ΔN_{eff}!)
- Probe ALP DM models with GW from axion strings/DWs (work in prep with Chang)
- Discussion/Conclusion/Outlook

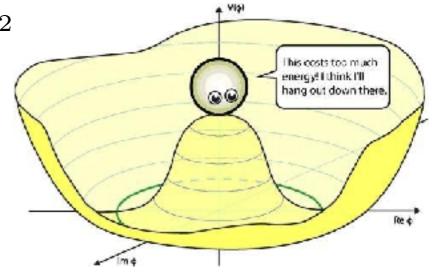
Cosmic Strings 101 (1)

- What are Cosmic strings? Stable one-dimensional topological defect, tension μ
- The origins of cosmic strings:
 - Predictions from superstring theory: fundamental (F-) string, D-string (Polchinski 2003-2008)
 - Vortex-like (soliton) solutions of field theory: e.g.
 spontaneous broken U(1) symmetry (gauge or global)

Charged complex scalar: $V = \lambda \left(\Phi^{\dagger} \Phi - \frac{v^2}{2} \right)^2$

Adding gauge field: Abelian Higgs model

$$\mathcal{L} = D_{\mu}\Phi D^{\mu}\Phi^{\dagger} - \frac{1}{4}F_{\mu\nu}F^{\mu\nu} - \lambda(\Phi^{\dagger}\Phi - v^2/2)^2$$

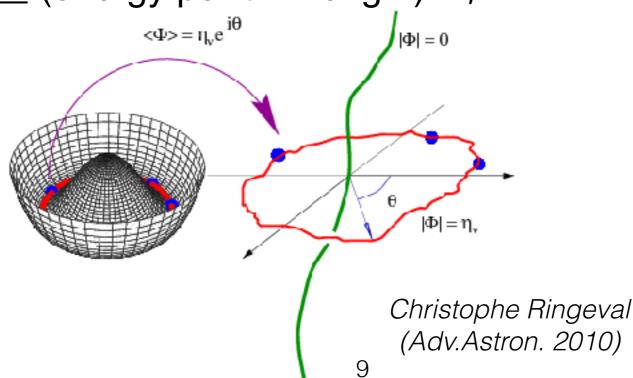


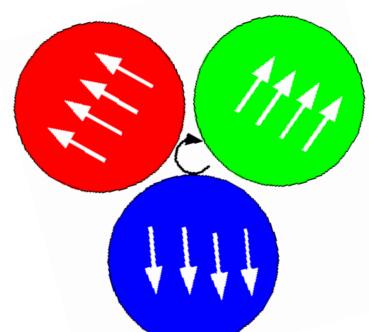
Cosmic Strings 101 (2)

- The familiar solution: $\langle \Phi \rangle = v/\sqrt{2}$ everywhere
- The string solution to abelian Higgs model

(position dependent, Nielsen and Olesen 1973; vortex in type-II superconductor, Abrikosov 1957)

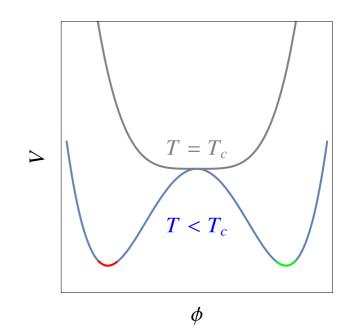
at
$$r \to \infty$$
 $\Phi \to \frac{v}{\sqrt{2}} \exp(iN\theta)$ $\langle \Phi \rangle = 0$ at the origin



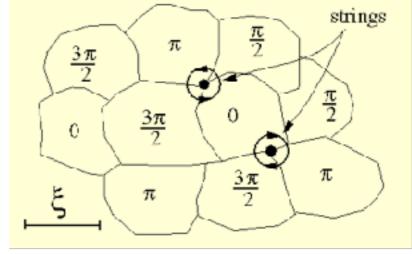


Formation of Cosmic Strings

- Formation: Kibble mechanism
 - Symmetry restoration at $T > T_c$
 - Spontaneous symmetry breaking at $T_{\sim}T_{c}$, but $\langle\Phi\rangle$ (phase!) cannot be correlated on scales larger than the finite horizon size $d_{H}\propto M_{p}/T^{2}$!



- Cosmic strings: non-trivial vacuum configuration,
 - necessarily formed at boundaries of causally disconnected domains.
 - "frozen in"

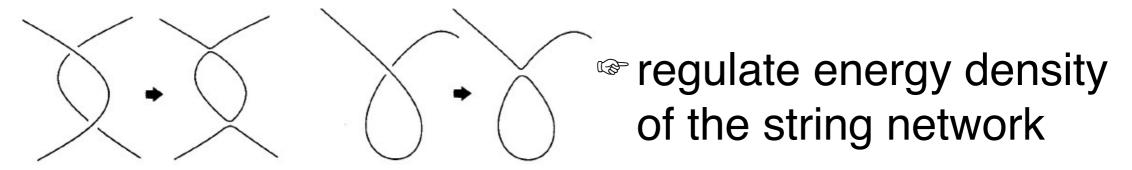


Evolution of Cosmic Strings

Static string network would redshift as:

$$ho_{\infty} \propto a^{-2}$$
 - dangerous! dominate universe today!

 Dynamics: strings inter-commute on collision, shed string loops that radiate away

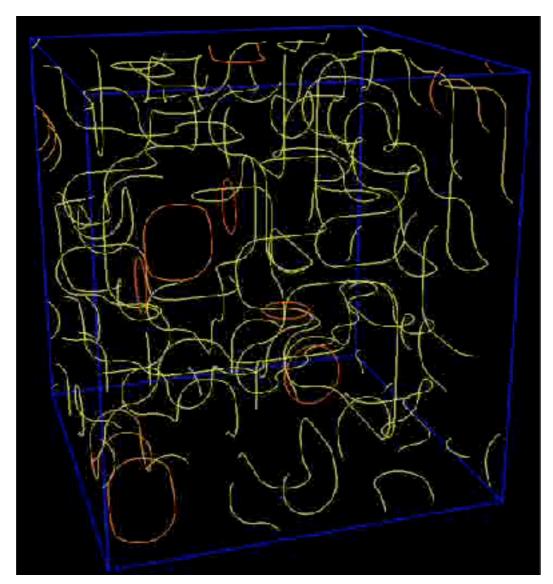


Total energy of the network eventually scales with background energy density (MD or RD):

$$\frac{\rho_{\infty}}{\rho_{\rm bkg}} \propto G \mu$$
 "safe" to have stable cosmic strings! (unlike domain walls, monopoles...)

How does a string network look like

- Per horizon volume:
 - O(1) horizon size long strings + copious string loops
 - -requires dedicated numerical simulations

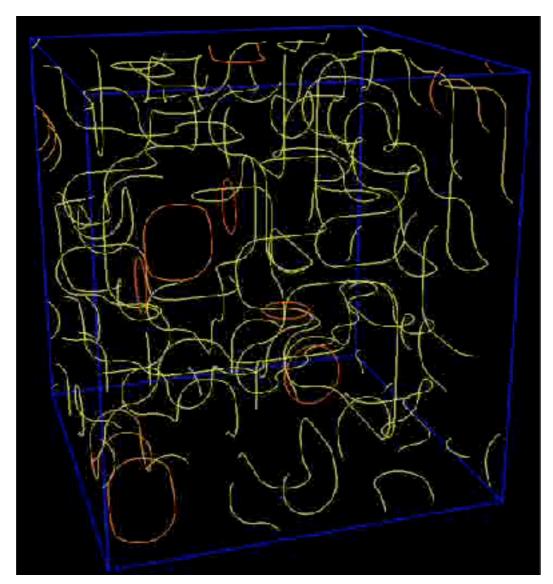


Simulation of a cosmic string network. Long strings are represented in yellow and cosmic string loops are shown in red.

© Cambridge cosmology group

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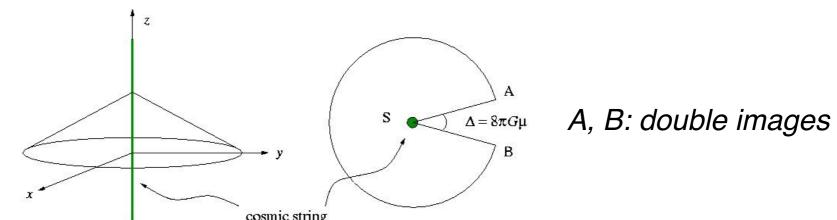
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Rich Phenomenology/Complementarity-1

- History: potentially provide primordial density perturbation for structure formation, CMB observation \rightarrow inflation dominates; CMB constraint: $G\mu \lesssim 10^{-7}$
- · Gravitational lensing: double image

conic space-time around a string: deficit angle $\Delta = 8\pi G\mu$



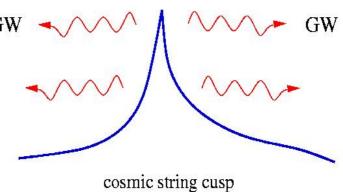
Potentially direct observational evidence: e.g. 2003 two seemingly identical galaxies very close together, 2005 found to be a pair of similar galaxies; double quasar Q0957+561A,B (1979); *future observations?...*

 Non-thermal production of matter from string decay: axions, gauge/Higgs fields, dark matter, cosmic ray...

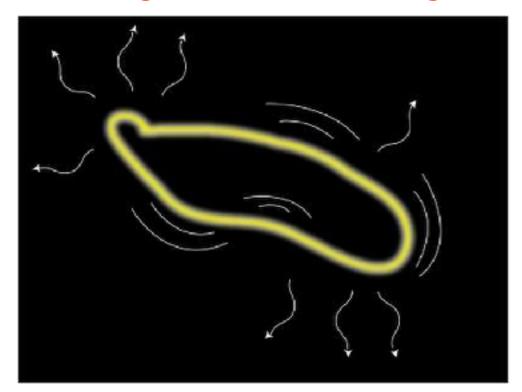
(e.g. YC w/Martin, Morrissey, Wells; YC w/Morrissey 2008; Vachaspati 2009; Long, Hyde, Vachaspati 2014, Long, Wang 2019...)

Rich Phenomenology/Complementarity-2

- Gravitational waves emitted from oscillating string loops
 - GW bursts from cusps on the loops



► Relic stochastic GW background: continuous emission throughout the string network history \bigstar (c.f. 1st order PT)



Credit: Matt DePies/UW.

⇒ spectrum spanning a <u>wide</u> frequency range

$$f \propto L^{-1}$$

$$dE/dt = \Gamma G \mu^{2}$$

$$(\Gamma \approx 50)$$

Stochastic GW Background from Cosmic Strings

We use a simplified loop size distribution (at formation) justified by recent simulation results:

$$l_i = \alpha t_i, \quad \alpha \approx 0.1$$

The loop formation rate per unit V per unit time (t):

$$n(l,t) = \frac{C_{\text{eff}}(t_i)}{\alpha^2 t_i^4} \frac{a^3(t_i)}{a^3(t)}$$

• After its creation, each loop radiates GW energy at a constant rate: dE

$$\frac{dE}{dt} = -\Gamma G \mu^2, \quad \Gamma \approx 50$$

Stochastic GW Background from Cosmic Strings

Consequently, the loop size decreases as

$$l = \alpha t_i - \Gamma G \mu \left(t - t_i \right)$$

The observed GW frequency today from a loop of size l

$$f = \frac{a(t)}{a(t_0)} \frac{2k}{l}$$

k=1 oscillation mode dominates

Stochastic GW Background from Cosmic Strings

Putting things together:

GW density per unit frequency seen today:

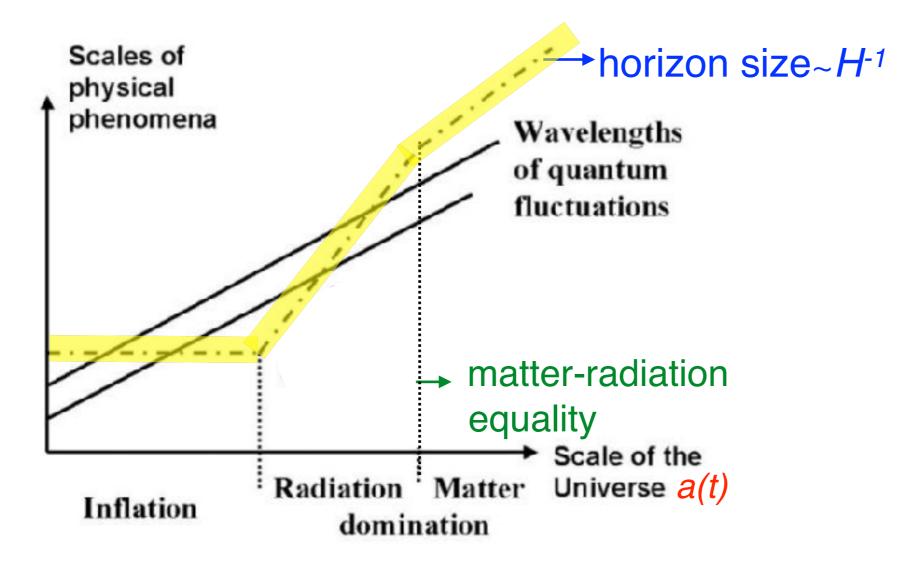
$$\Omega_{GW}(f) = \frac{f}{\rho_c} \frac{d\rho_{GW}}{df} = \sum_k \Omega_{GW}^{(k)}(f)$$

$$\Omega_{GW}^{(k)}(f) = \frac{1}{\rho_c} \frac{2k}{f} \frac{(0.1) \Gamma_k G \mu^2}{\alpha(\alpha + \Gamma G \mu)} \xrightarrow{\text{expansion parameter}} \times \int_{t_F}^{t_0} d\tilde{t} \frac{C_{eff}(t_i)}{t_i^4} \left[\underbrace{a(\tilde{t})}_{a(t_0)} \right]^5 \left[\underbrace{a(t_i)}_{a(\tilde{t})} \right]^3 \Theta(t_i - t_F)$$

-Evolution of cosmic bkg (state equation) encoded in $a(\tilde{t})$!

A Brief Review of Standard Cosmology

- Standard cosmology:
 - Inflation (?)
 - * Radiation domination (RD): primordial reheating (?) till $T_{eq} \sim eV$
 - ► Matter domination (MD): $T_{eq} \sim eV$ till today (Λ)(well tested \checkmark)

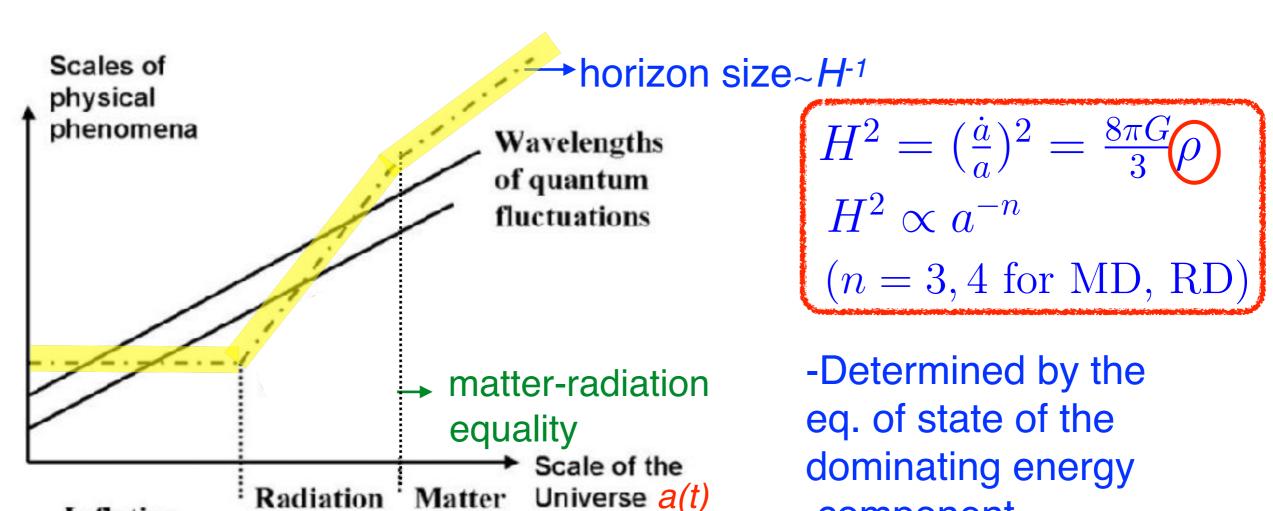


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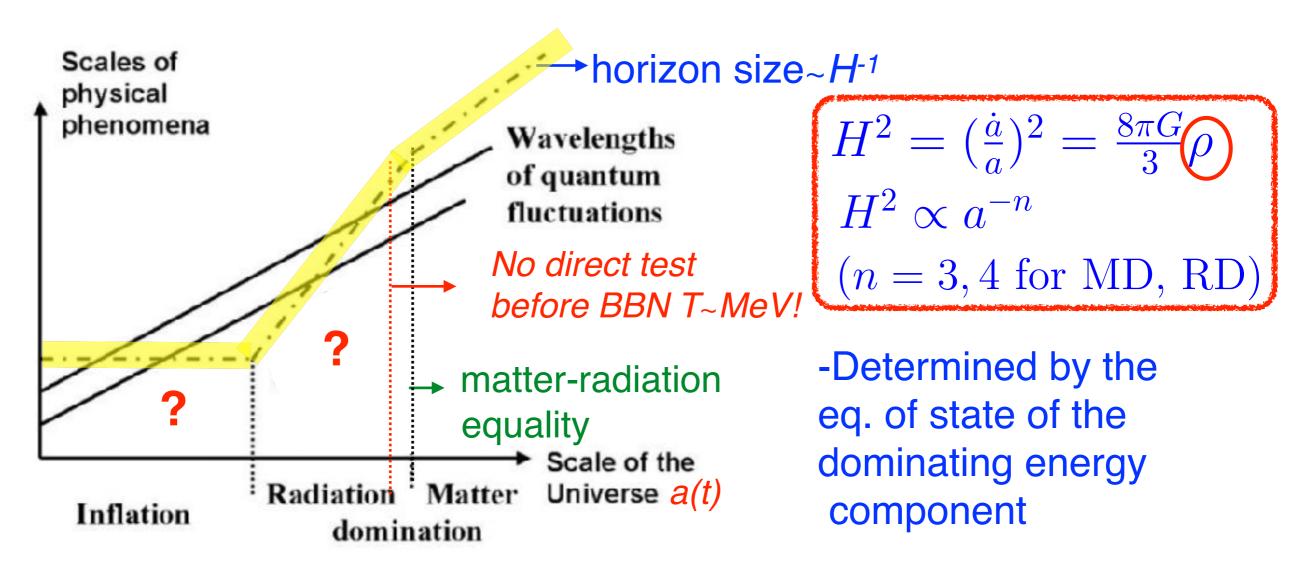


domination

component

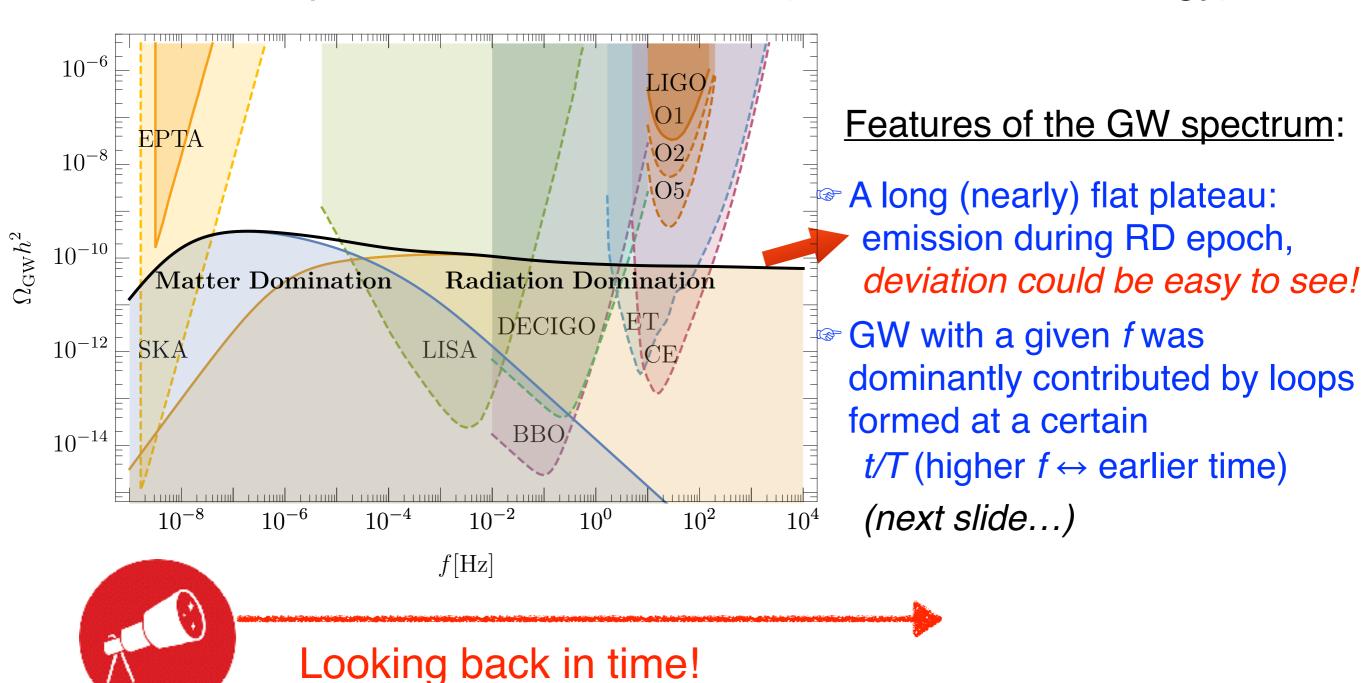
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Testing Standard Cosmology w/GW Spectrum from Cosmic Strings

• An example: $G\mu = 2 \times 10^{-11}$, $\alpha = 0.1$ (in standard cosmology)



The GW Frequency-Time (Temperature) Correspondence

arxiv: 1711.03104, 1808.08968, YC with Lewicki, Morrissey and Wells

Quantify/utilize the f-T correspondence

GW frequency \leftrightarrow temperature

GW with a given f was dominantly contributed by loops formed at a certain t/T

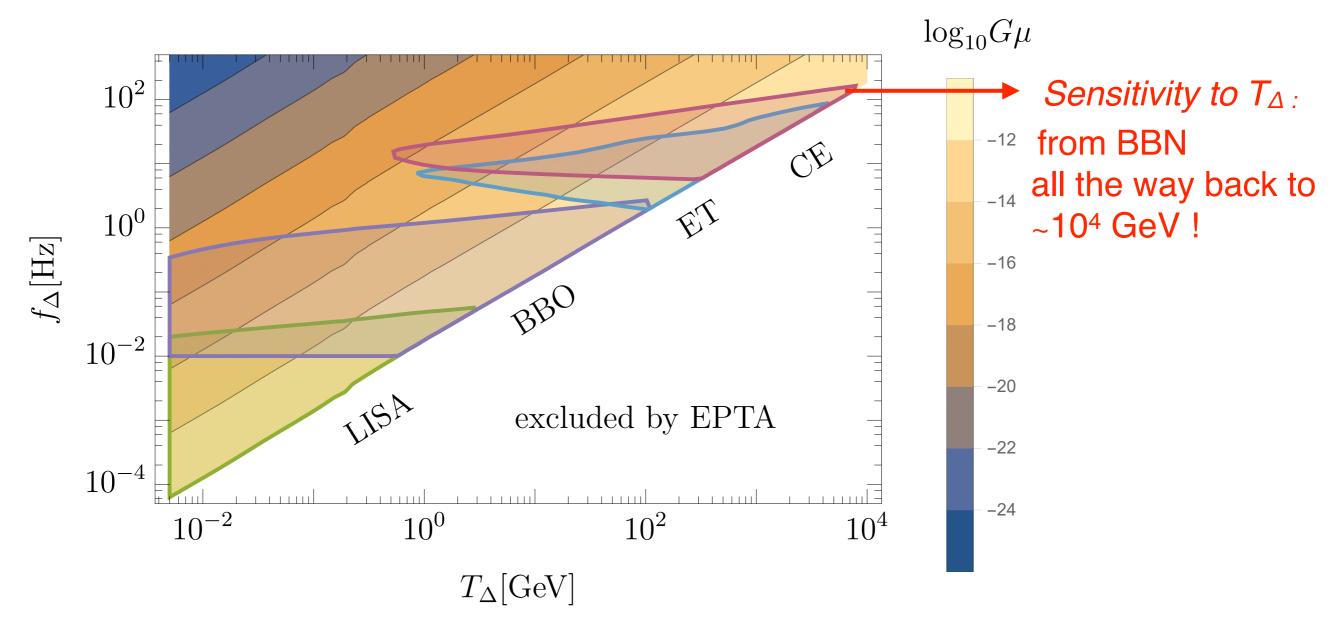
$$f_{\Delta} \simeq \sqrt{\frac{8}{z_{\rm eq}\alpha \Gamma G\mu}} \left[\frac{g_*(T_{\Delta})}{g_*(T_0)}\right]^{1/4} \left(\frac{T_{\Delta}}{T_0}\right) t_0^{-1}$$

Numerical fit:

$$f_{\Delta} = (8.67 \times 10^{-3} \,\text{Hz}) \, \left(\frac{T_{\Delta}}{\text{GeV}}\right) \left(\frac{0.1 \times 50 \times 10^{-11}}{\alpha \, \Gamma(G\mu)}\right)^{1/2} \left(\frac{g_*(T_{\Delta})}{g_*(T_0)}\right)^{\frac{8}{6}} \, \left(\frac{g_{*S}(T_0)}{g_{*S}(T_{\Delta})}\right)^{-\frac{7}{6}}$$

Experimental Detection Prospects

(f-T correspondence)



• Fig.: f_{Δ} required to test the standard cosmology up to radiation T_{Δ} for a range of $G\mu$, α =0.1. Shaded regions: signal within detection sensitivity by the corresponding GW detector.

Probing New Phases in Cosmological Evolution

Probing New Phases in Cosmological Evolution

- Standard cosmology: the Universe is RD from T_{eq} all the way back to the end of inflation—IS IT??
 - often taken for granted, but no direct observational support for pre-BBN era! Important to test: re-assure or surprise...
- New cosmology are well motivated: e.g.
 - Early matter-domination (ends with a reheating phase): a long-lived massive particle, oscillation of a scalar field in ϕ^2 potential (moduli); e.g. SUSY, baryogenesis, the end of inflation...
 - A "kination" period: n>4 in $H^2\propto a^{-n}$, a stiff component, redshifts faster than radiation! e.g. oscillation of a scalar field in a non-renormalizable potential-quintessence models for DE/ inflation, axion model... $V(\phi)\propto \phi^N,\, n=6N/(N+2)$

Rising interest recently: effects of EMD/kination on DM physics...

Probing New Phases in Cosmic History with Cosmic String GWs

 Consider a general cosmology: we assume the Universe dominated by a single component

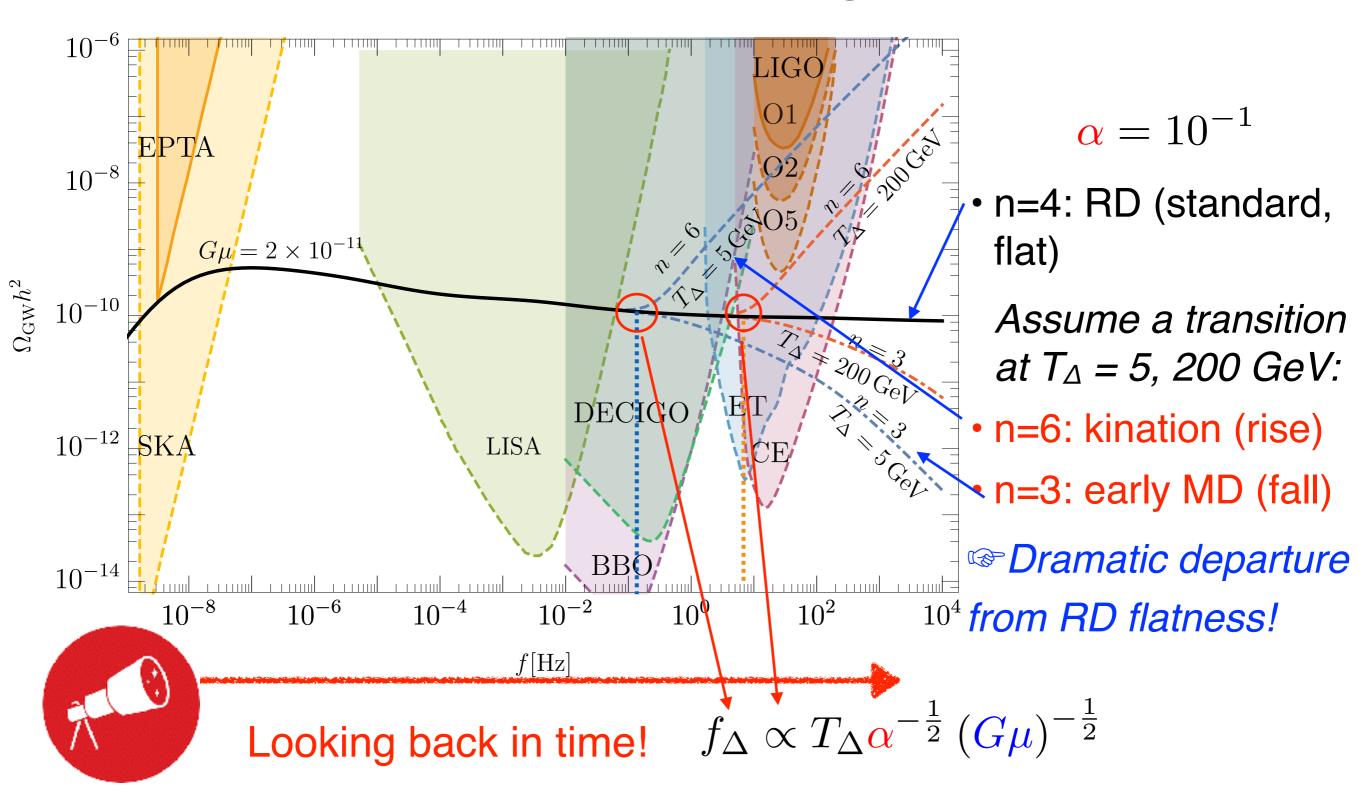
$$H^2 \propto a^{-n}$$
 $a(\tilde{t}) \propto \tilde{t}^{\frac{2}{n}}$ parametrized by n

$$\Omega_{GW}(f) \propto \begin{cases} f^{\frac{8-2n}{2-n}} & n > 10/3 \\ f^{-1} & n \leq 10/3 \end{cases}$$
 n=4: RD flatness explained!

• GW spectrum with a departure from RD at t_{\triangle} ? Model the transition:

$$\rho(t) = \begin{cases} \rho_{st}(t) & ; t \ge t_{\Delta} \\ \rho_{st}(t_{\Delta}) & \left[\frac{a(t_{\Delta})}{a(t)}\right]^{n} & ; t < t_{\Delta} \end{cases}$$

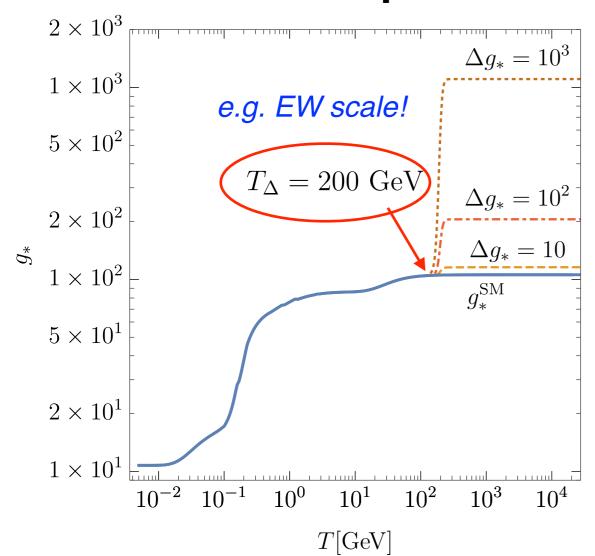
Probing New Phases in Cosmic History with Cosmic String GWs



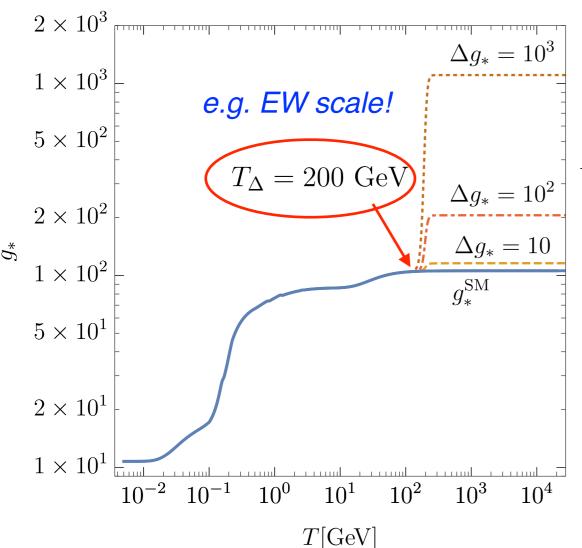
Probing New (Massive) Degrees of Freedom

- Additional d.o.f's: <u>ubiquitous</u> in BSM theories, maybe hundreds of them! (DM, SUSY, RS, hidden valley, twin Higgs, clockwork, NNaturalness...)
- Massive d.o.f's: in form of radiation in the early Universe (g_*), beyond the reach of CMB (ΔN_{eff}) or LHC
 - GW spectrum may provide a way!

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$\Delta g_* = 10^3$ Friedman equation:

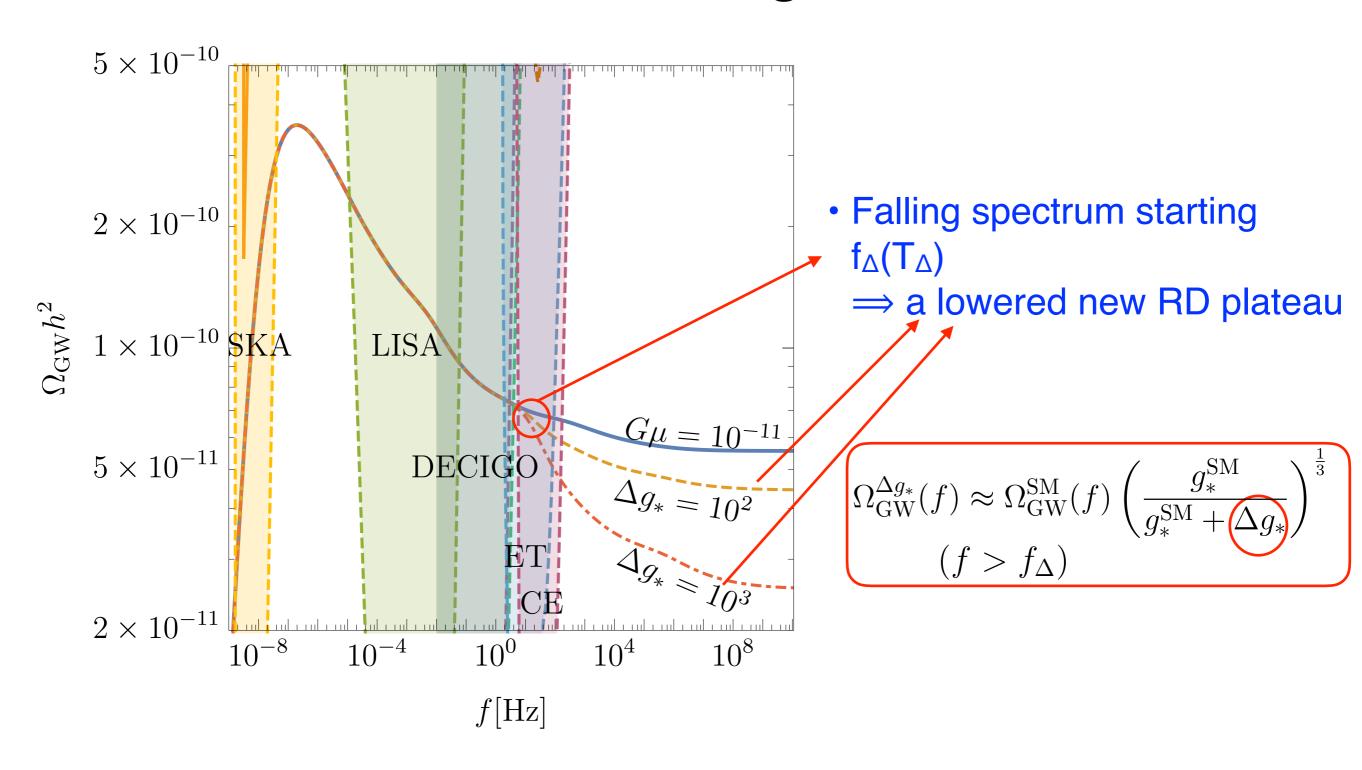
$$\Delta g_* = 10^2$$

$$H^2 \equiv \left(\frac{\dot{a}}{a}\right)^2 = H_0^2 \left[\Delta_R(a) \Omega_R \left(\frac{a}{a_0}\right)^{-4} + \Omega_M \left(\frac{a}{a_0}\right)^{-3} + \Omega_\Lambda\right]$$

dominates in RD era

$$\Delta_R(a) = \frac{g_*(a)}{g_*(a_0)} \left(\frac{g_{*S}(a_0)}{g_{*S}(a)}\right)^{4/3}$$

—the source of g_* dependence



(work in prep with Chia-Feng Chang)

— An interesting twist when switch gear to a global U(1)...

- Axion-like particle (ALP) DM: ultra-light (pseudo-)goldstone boson from a global U(1)_{PQ} breaking, leading alternative to WIMP paradigm, a lot of interest/effort recently; QCD axion, generic (hidden) ALPs also motivated (e.g. string axiverse)
- A relatively under-developed aspect of ALP studies: implication of ALP topological defects

ALP cosmic strings/domain walls: indispensable companion of ALP particles for $U(1)_{PQ}$ breaking after inflation, independent of ALP-SM interaction

 $^{\square}$ Can significantly affect Ω_{DM} prediction + potential new probes

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ALP cosmic strings/domain walls: indispensable companion of ALP particles for $U(1)_{PQ}$ breaking after inflation, independent of ALP-SM interaction

- $^{\odot}$ Can significantly affect Ω_{DM} prediction + potential new probes
- A natural inspiration from the gauge string story:



GW signature from axion cosmic strings?

(complementary, could be the smoking gun for "hidden" ALPs...)

- GW signature from global/axion cosmic strings: an overlooked, yet potentially important discovery channel
- Why Overlooked? "too small" by naive estimate Sub-dominant relative to goldstone emission:

$$P_{\rm GW} \sim \Gamma G \mu^2 \ll P_g \sim \Gamma_g \eta^2$$

 $\mu \sim \eta^2 \log (L/\delta)$ correlation length: $L \sim H^{-1}$, string core width: $\delta \sim \eta^{-1}$

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- BUT: rare decay mode can be discovery mode! (e.g. Higgs discovery, axion/goldstone search strategy model dependent...)
 - + GW detector sensitivity will keep improving...

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- BUT: rare decay mode can be discovery mode! (e.g. Higgs discovery, axion/goldstone search strategy model dependent...)
 + GW detector sensitivity will keep improving...
- The effect of pre-BBN cosmology? OR: probe pre-BBN universe with GW spectrum from axion strings? (non-standard cosmology and axion DM: Poulin, Smith, Grin, Kawal, Kamionkowski arxiv:1806.10608, A. Nelson and Xiao arxiv: 1807.07176)

(work in prep with Chia-Feng Chang)

Challenges:

- Very limited literature: even for pure global U(1)
 (GW spectrum from global strings: Battye and Shellard 1996, needs update!)
- More complex for axion strings: cosmic strings + domain walls
- Ongoing development of global string simulation

(work in prep with Chia-Feng Chang)

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 (GW spectrum from global strings: Battye and Shellard 1996, needs update!)
- More complex for axion strings: cosmic strings + domain walls
- Ongoing development of global string simulation
- Our ongoing study: global → QCD axion → ALPs
 - Preliminary result (global) small, but observable!
 - Also advance understanding of Ω_{DM} due to topological defects

Discussion:Confronting Detection Challenges

Astrophysical foreground

(With assumptions) LIGO expect to detect stochastic GW bkg from unresolved binary mergers (peak: $\Omega \sim 10^{-9}$ at $f \sim 10^{3}$ Hz), possibly overwhelm primordial signals...

Solutions:

- Optimized statistical strategy to identify/subtract astro bkg
 LIGO (arXiv:1712.00688)
- Improved resolution to resolve/remove astro bkg with future detectors (@ LISA, ET/CE, BBO) → down to Ω~10⁻¹³ or even better
 - Important newly developing research area!

(Analogy: CMB foreground removal, DM indirect detection)

Discussion: Confronting Detection Challenges

Work in progress with Barry Barish and Simeon Bird: distinguish cosmogenic/primordial sources stochastic GW background from astro-foreground...

Distinguish from other primordial GW sources

- Characteristic flat plateau at high f, difficult to mimic by most other sources (e.g. GW from 1st order PT has peaky structure—split power law)
- Exception: GW from minimal inflation has a RD flat plateau, BUT much smaller amplitude, rising at low f

Conclusion

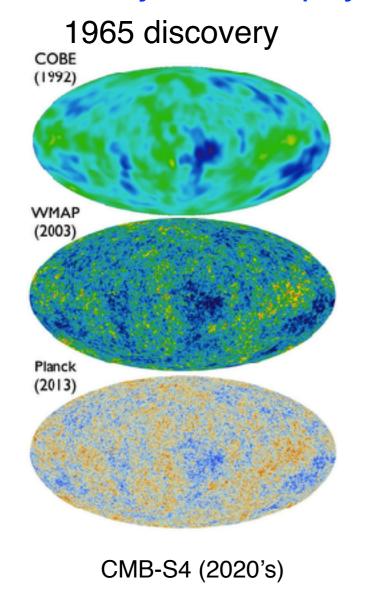
- Cosmic strings: generically motivated (U(1) breaking, axion, superstring...); a strong, well-understood source of GWs that can serve as a "standard candle" for probing very early Universe
 - a unique and powerful tool for reconstructing a timeline for pre-BBN cosmic history (the f-T correspondence)
- In principle we could probe the expansion rate of the Universe even above $T_{\sim} 10^4 \; GeV$ using GW from cosmic strings!
 - Probe new phases (eq. of state) of early Universe
 - Probe (massive) BSM d.o.f's using GW (beyond CMB, LHC)
- GWs from axion strings/domain walls may be the smoking gun for dark matter...

Outlook

Beyond cosmic strings:

An inspirational benchmark for exploiting the full potential of GW as a new tool for probing particle physics and cosmology beyond the horizon of our current knowing

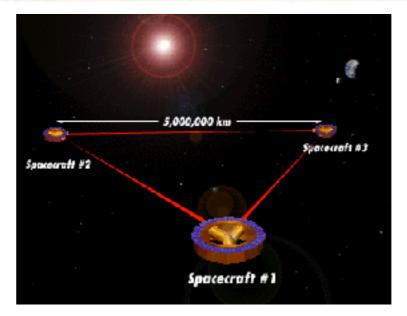
The history of CMB physics



How far can GW take us?



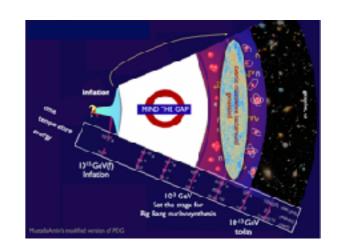
2016 LIGO discovery



Future GW experiments in sight: LISA, BBO, DECIGO, ET, CE, TianQin, Taiji...

KITP Program Jan 6-Mar 13 2020:

From Inflation to the Hot Big Bang



Coordinators: Peter Adshead, Yanou Cui, Raphael Flauger, and Scott Watson Scientific Advisors: Robert Brandenberger, Andrei Linde, and Raman Sundrum

https://www.kitp.ucsb.edu/activities/inflation20, (waitlist...)

Associated conference: https://www.kitp.ucsb.edu/activities/inflation-c20
Feb 3-6 2020, registration deadline Jan 5 2020





HERE again, in winter...

Thank you!