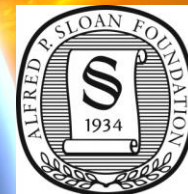
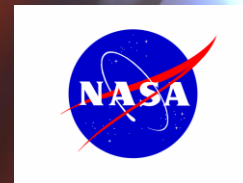
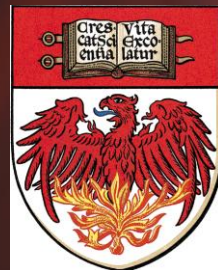


Small-Planet Densities and System Architectures through Photodynamic Variations

Daniel Fabrycky
University of Chicago



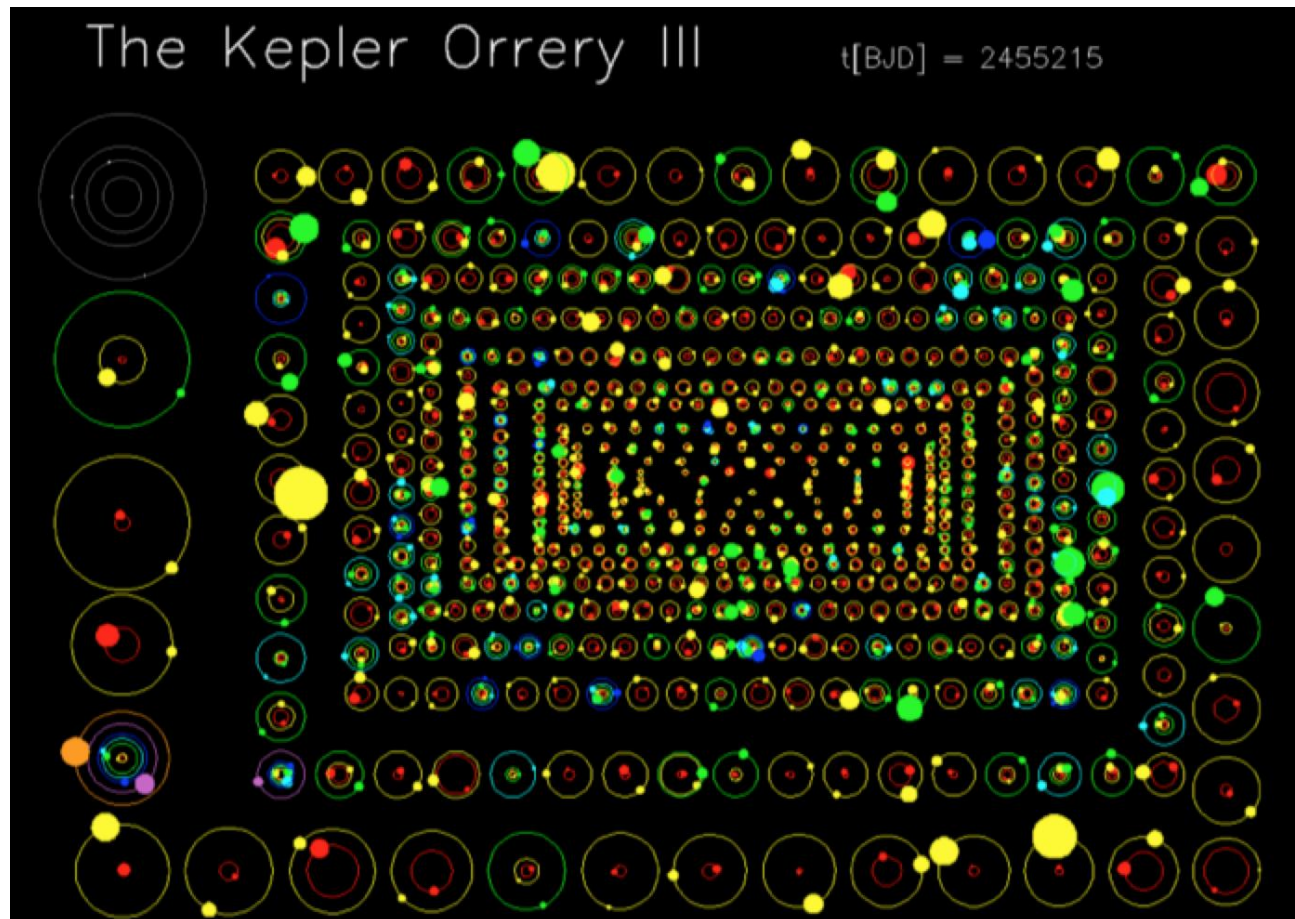
NASA Kepler Participating Scientist
Sloan Research Fellow

Image: Pyle/M

<https://www.youtube.com/watch?v=gnZVvYm6KKM>

or

<http://kepler.nasa.gov/multimedia/animations/orrery3/>



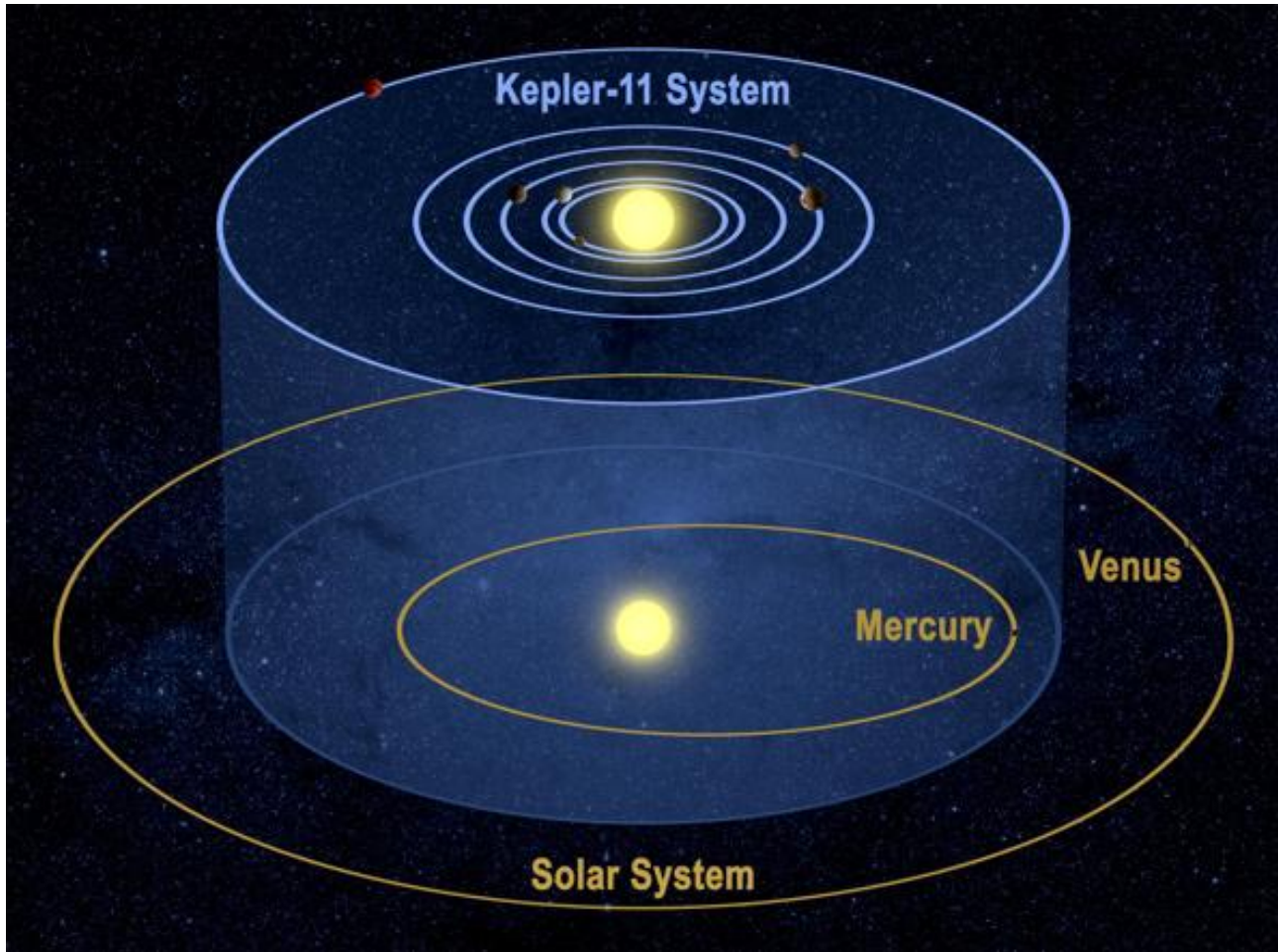
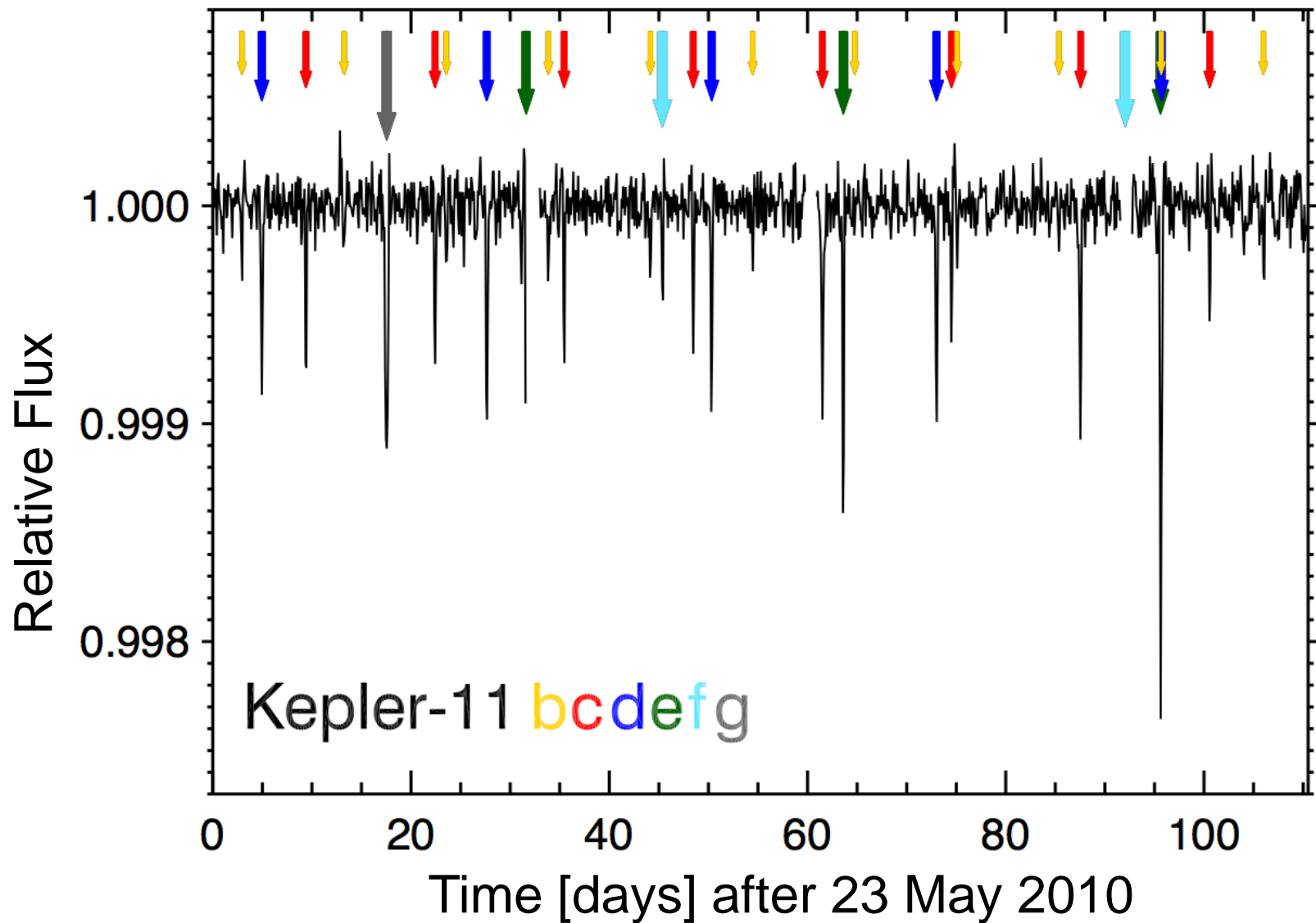


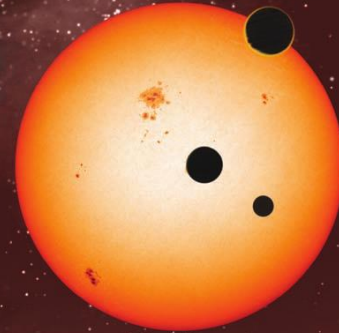
Image: NASA/Pyle

Kepler-11: Six Transiting Planets



nature

THE INTERNATIONAL WEEKLY JOURNAL OF SCIENCE



SIX NEW WORLDS

Kepler telescope's edge-on view of compact planetary system around Sun-like star **PAGE 53**

POLICY

DEEP-SEA MINING

Regulate now to protect hydrothermal vent species

PAGE 31

DRUG DISCOVERY

TAKING THE LEAD

Debating how to keep the pipelines flowing

PAGE 42

ADAPTIVE IMMUNITY

EARLY ORIGIN FOR A 'THYMUS'

Gill-based thymoid found in living-fossil lampreys

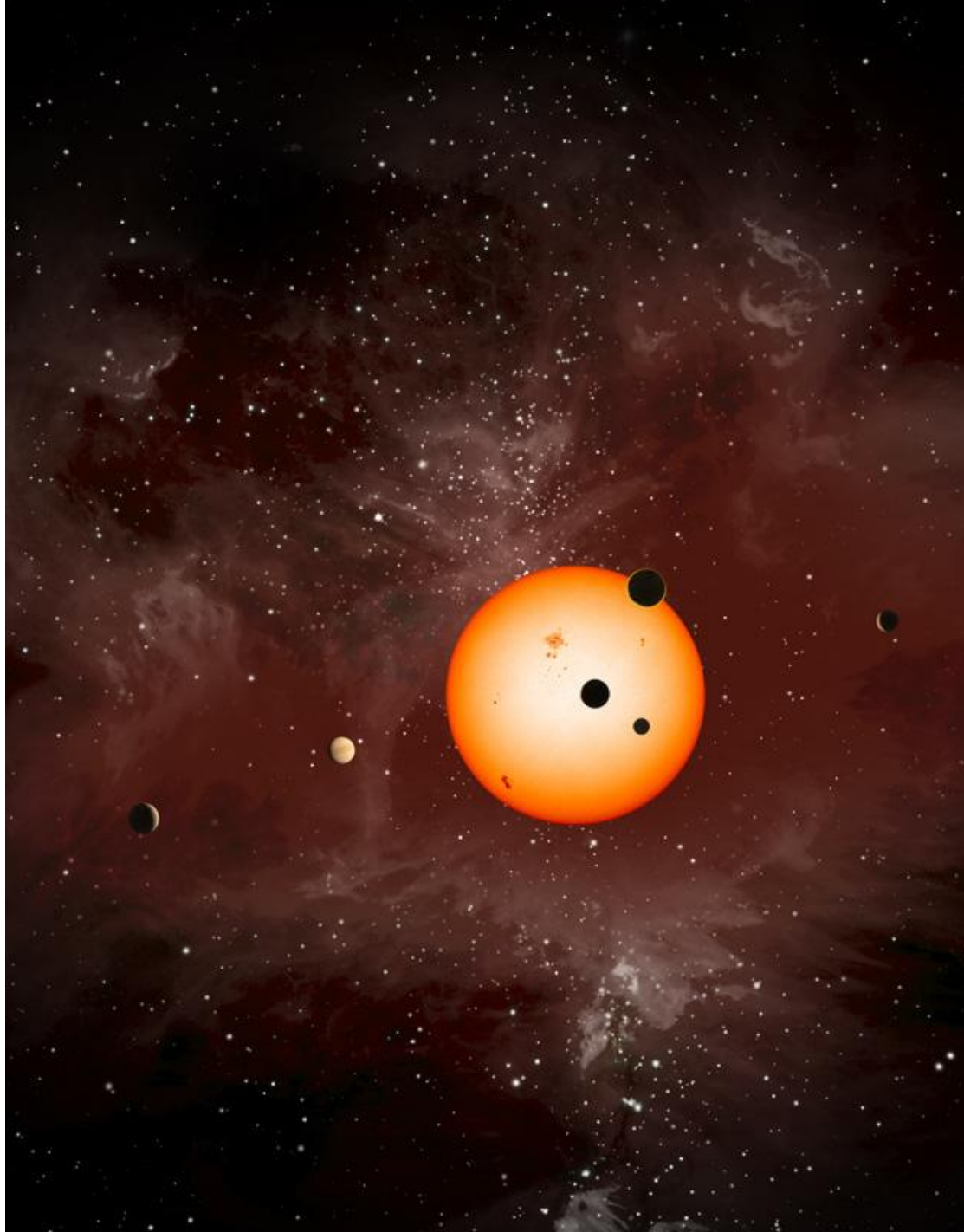
PAGE 90

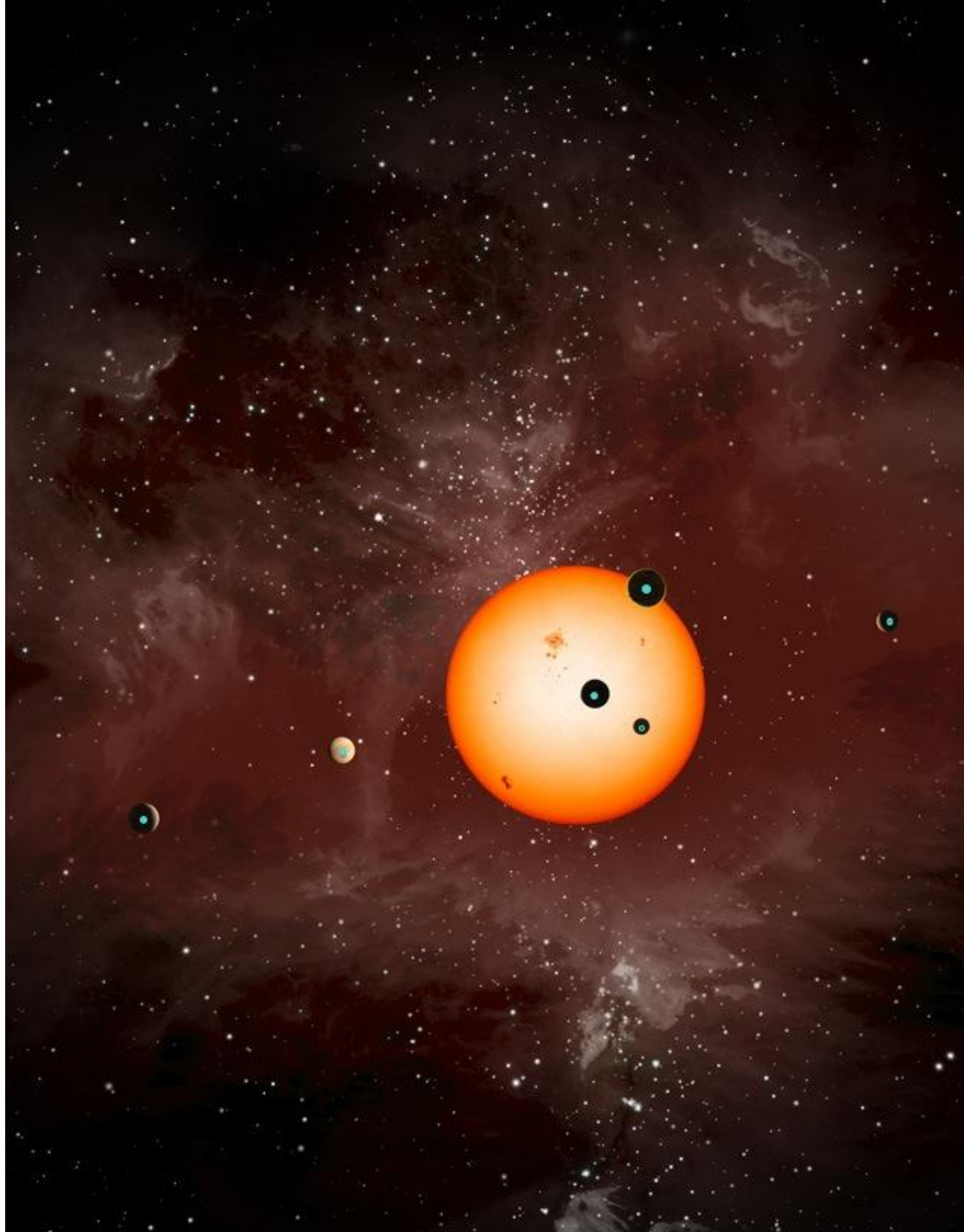
NATURE.COM/NATURE

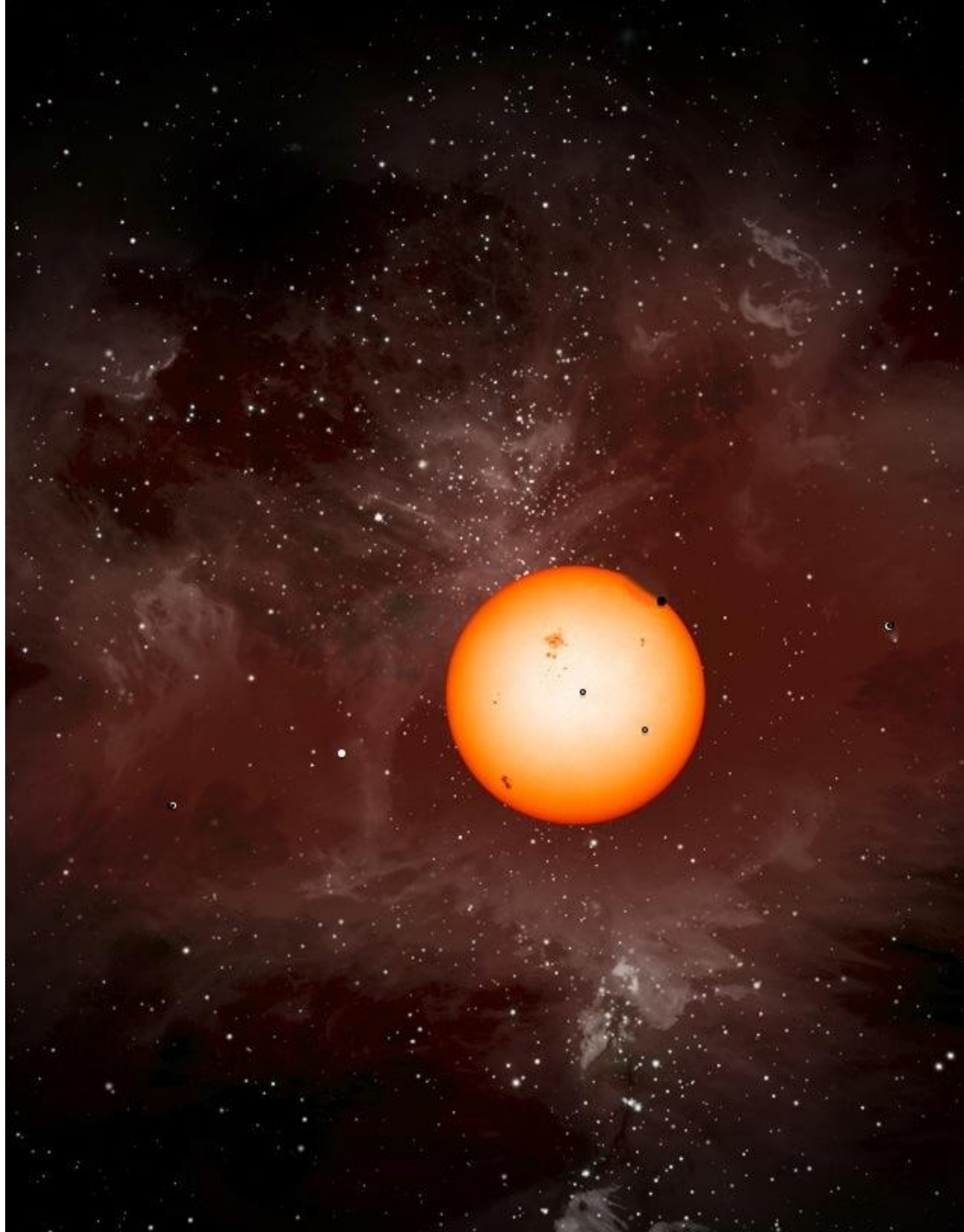
3 February 2011



Image: NASA/Pyle



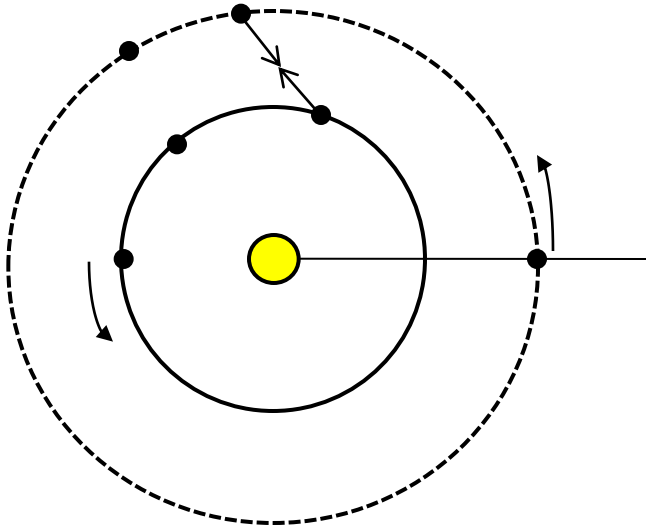




Outline: Small-Planet **Densities** and **System Architectures** through **Photodynamic** **Variations**

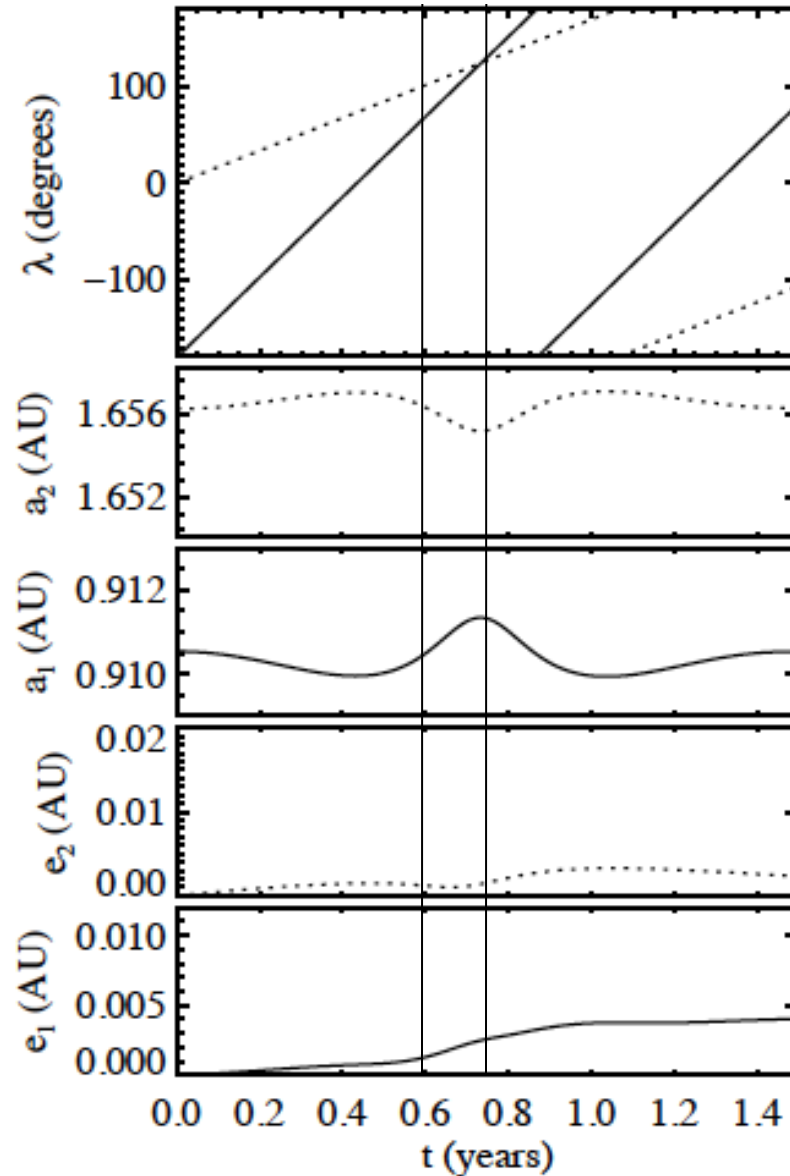
- Transit Timing Variations (TTV) → M_p “small”
1-6 M_E
2-8 R_E
- **Photometric** Approaches to **TTV**
- **Eccentricities** to Probe Formation
0.5-2 R_E
rocky

Dynamics: Orbital Timescales

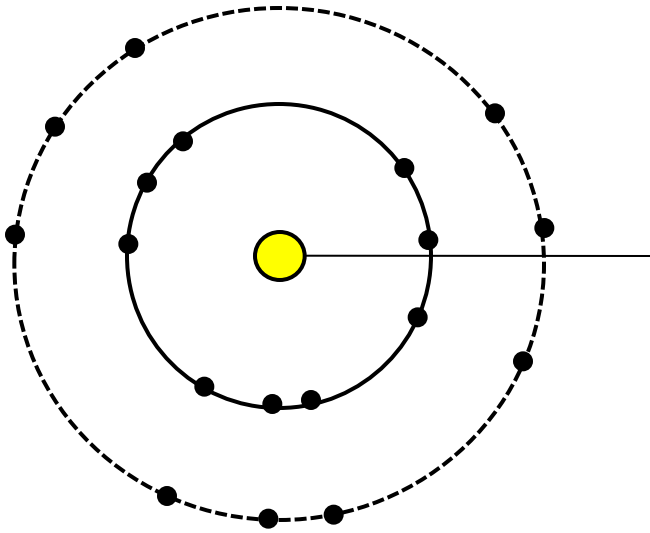


Transit timing variations

Agol et al. 2005,
Murray & Holman 2005



Dynamics: Secular Timescales



$$P_2/P_1 = 2.44$$

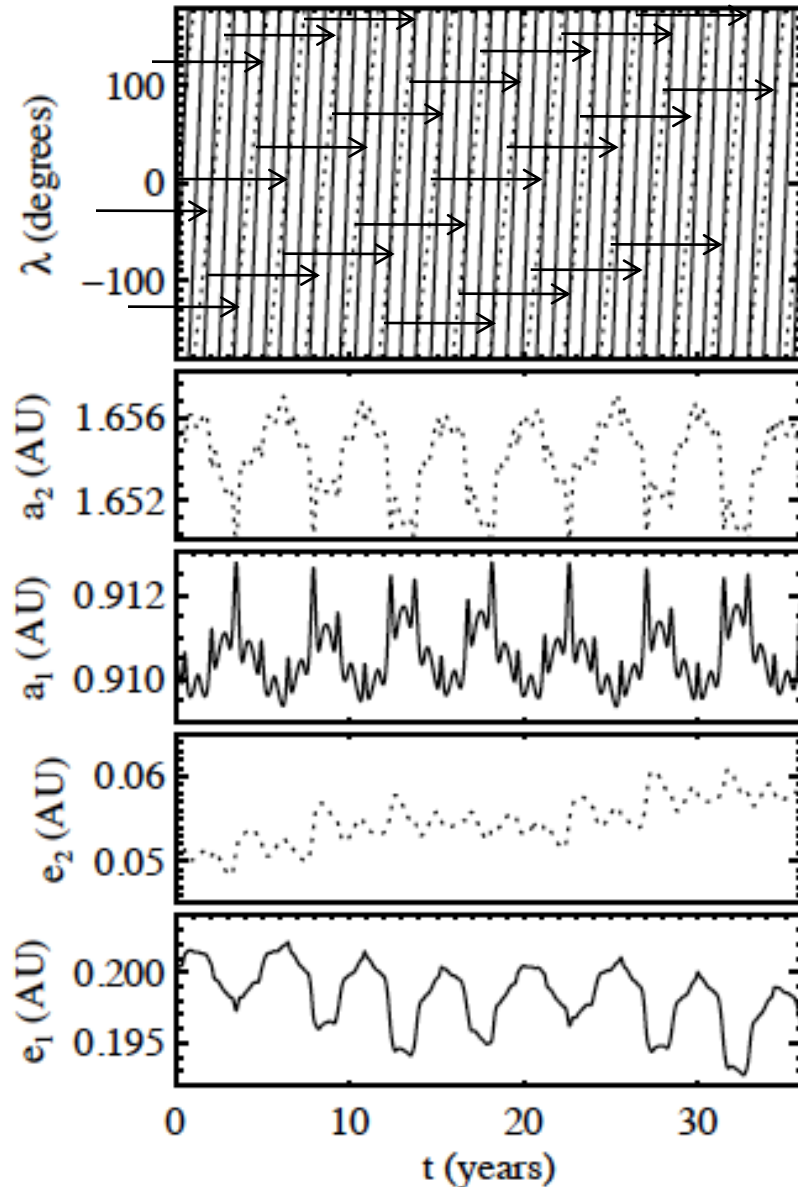
Non-resonant

→ “Chopping” timing signal
of Eric’s talk, next

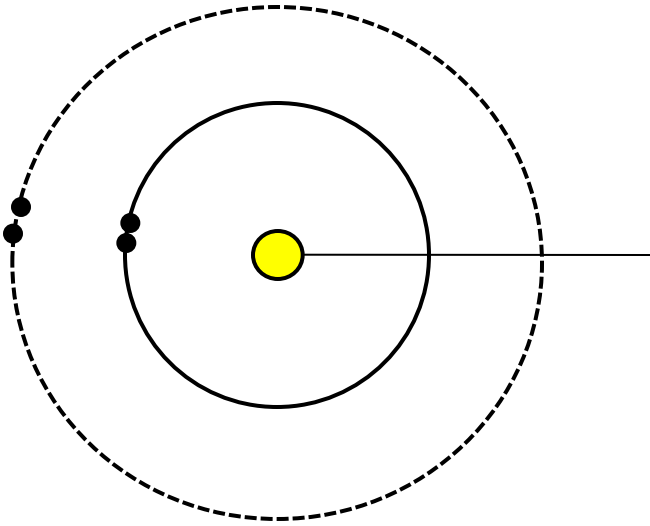
Transit timing variations

Agol et al. 2005,

Murray & Holman 2005



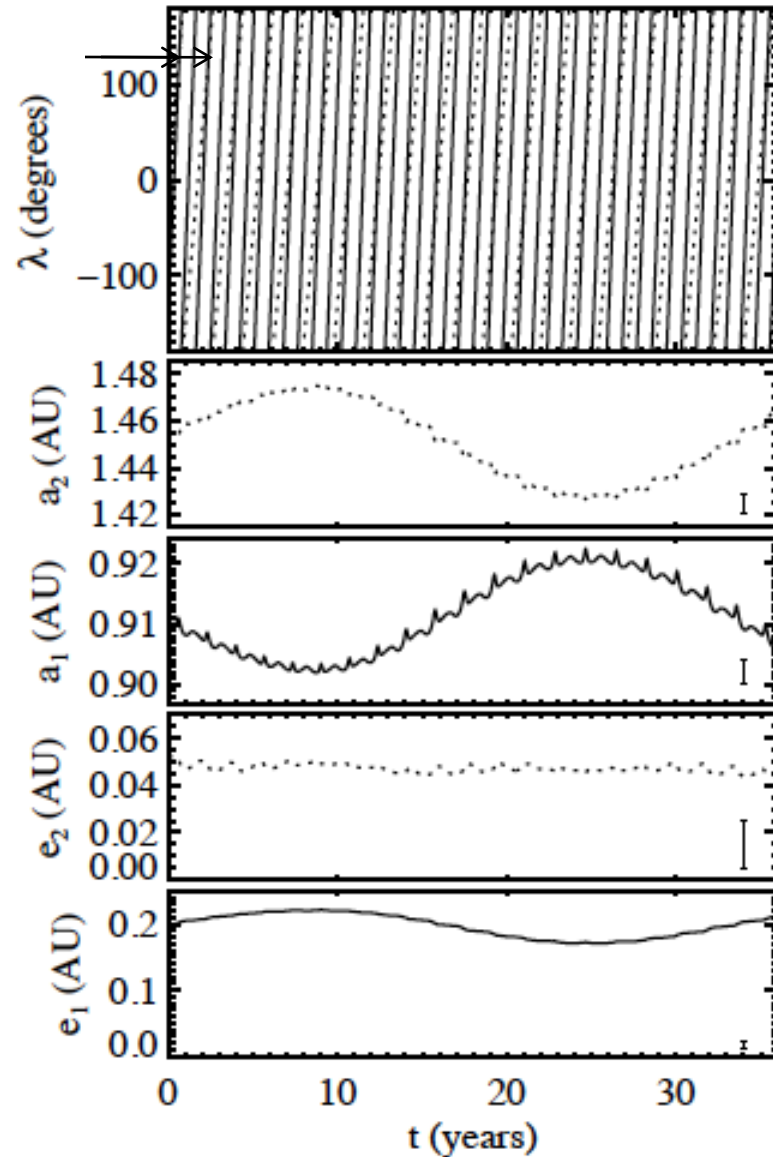
Dynamics: Resonant Orbits



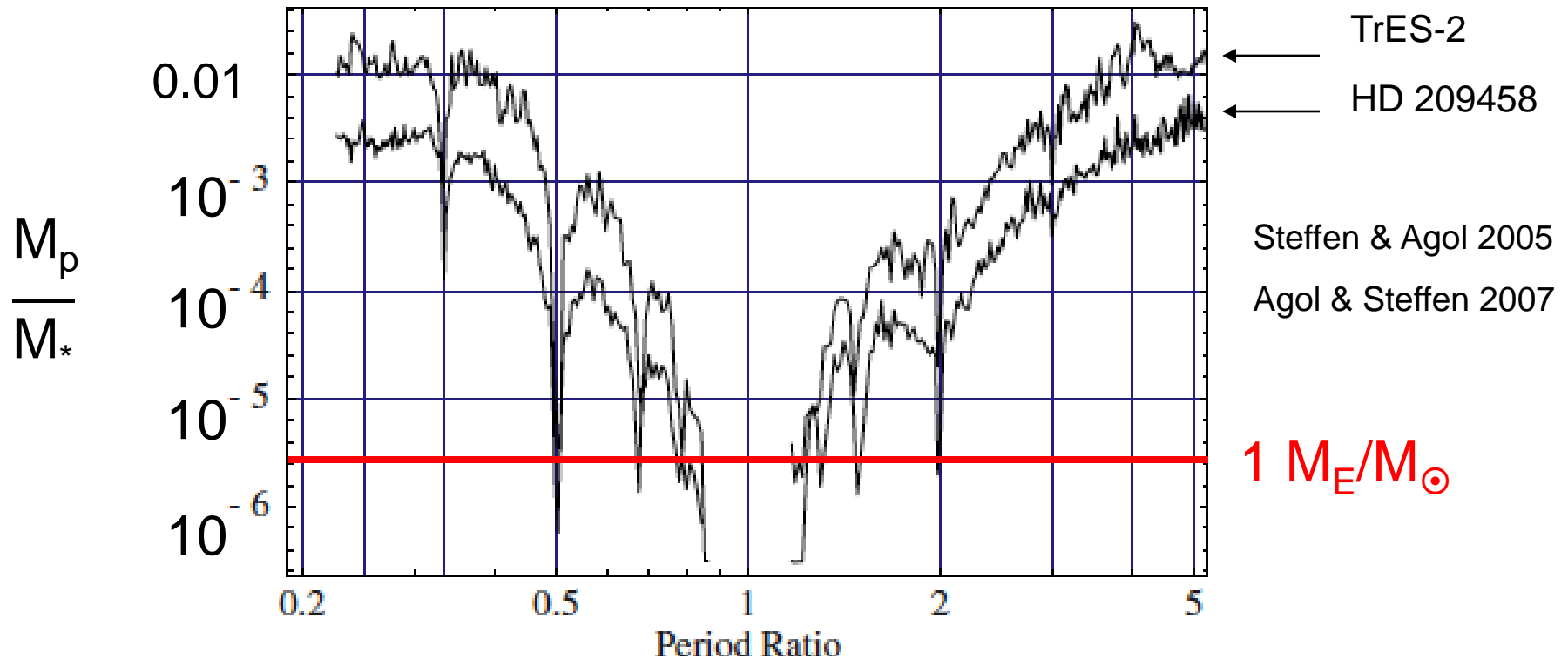
$$P_2/P_1 = 2.00$$

Transit timing variations

Agol et al. 2005,
Murray & Holman 2005



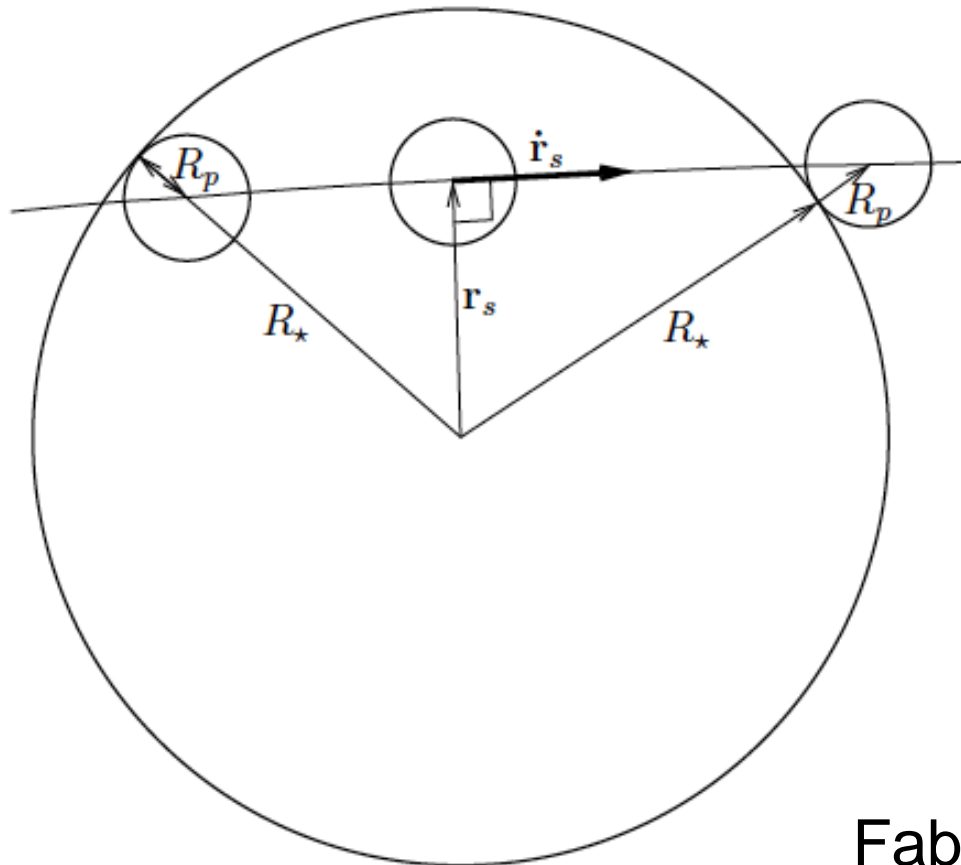
Sensitivity



TTV signal scales as orbital periods – *better* for relatively distant planets.

Dynamical Model of Transits

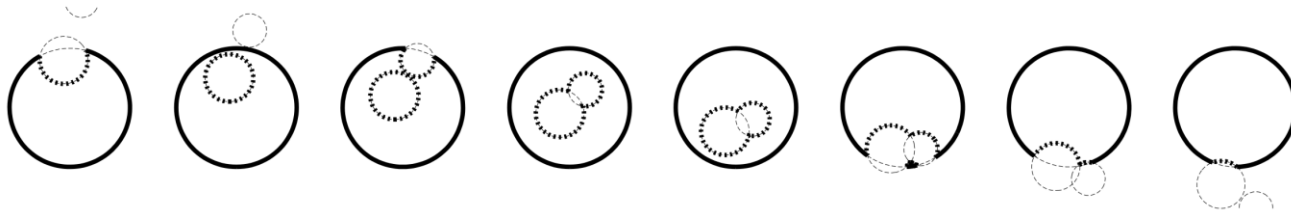
Use Newton's equations to integrate a 3-body system
Numerical transit times and radial velocities



Fabrycky (2010)

Transit Computation

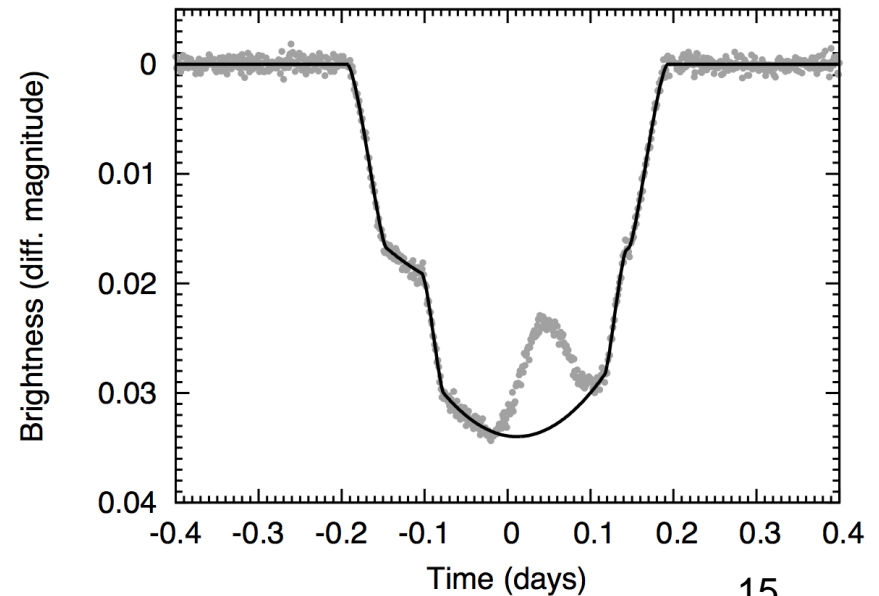
- Semi-analytical solutions, using basic limb darkening (Pal 2011)



$$I[\mu] = 1 - c_1(1 - \mu) - c_2(1 - \mu)^2$$

$$\mu = \mu[x, y] = (1 - (x^2 + y^2))^{\frac{1}{2}}$$

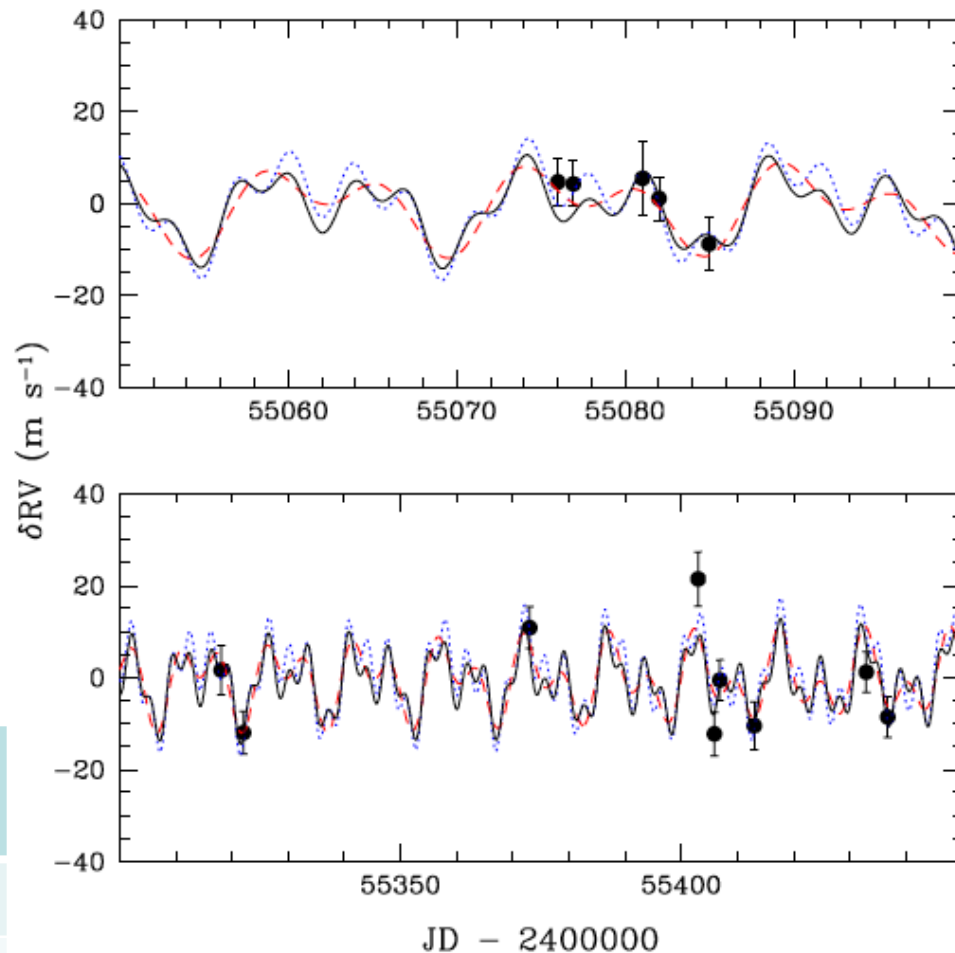
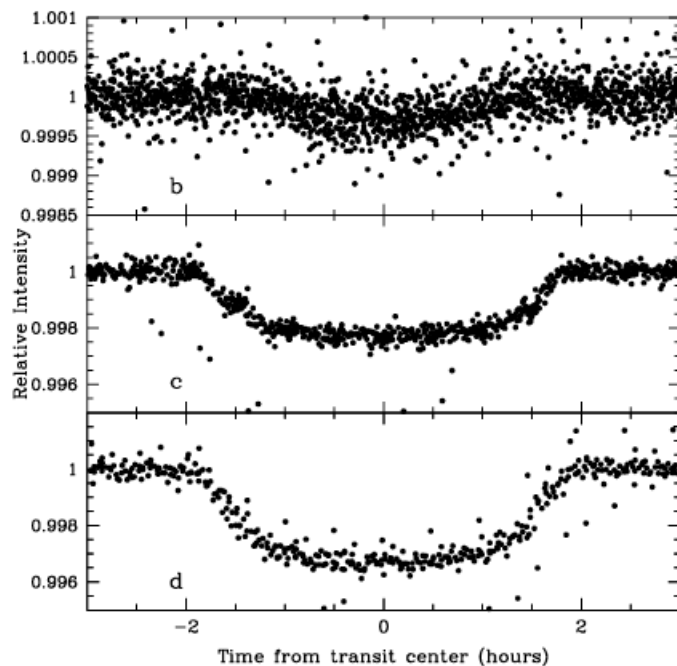
(slide courtesy UChicago graduate student Sean Mills)



“Ground truth”

- Neptune’s discovery
- Checking TTV masses by Radial Velocity
 - Kepler-18 (Multi-transiting)
 - KOI-142 (TTV discovery)
 - Lauren Weiss’ poster on Kepler-11

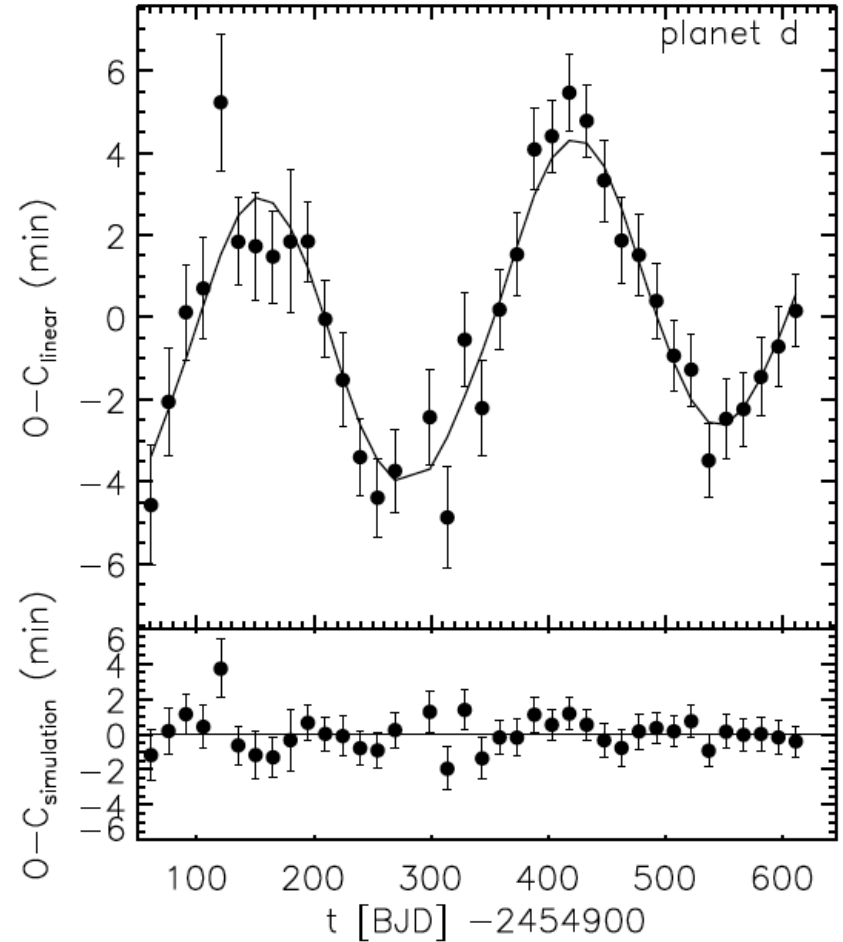
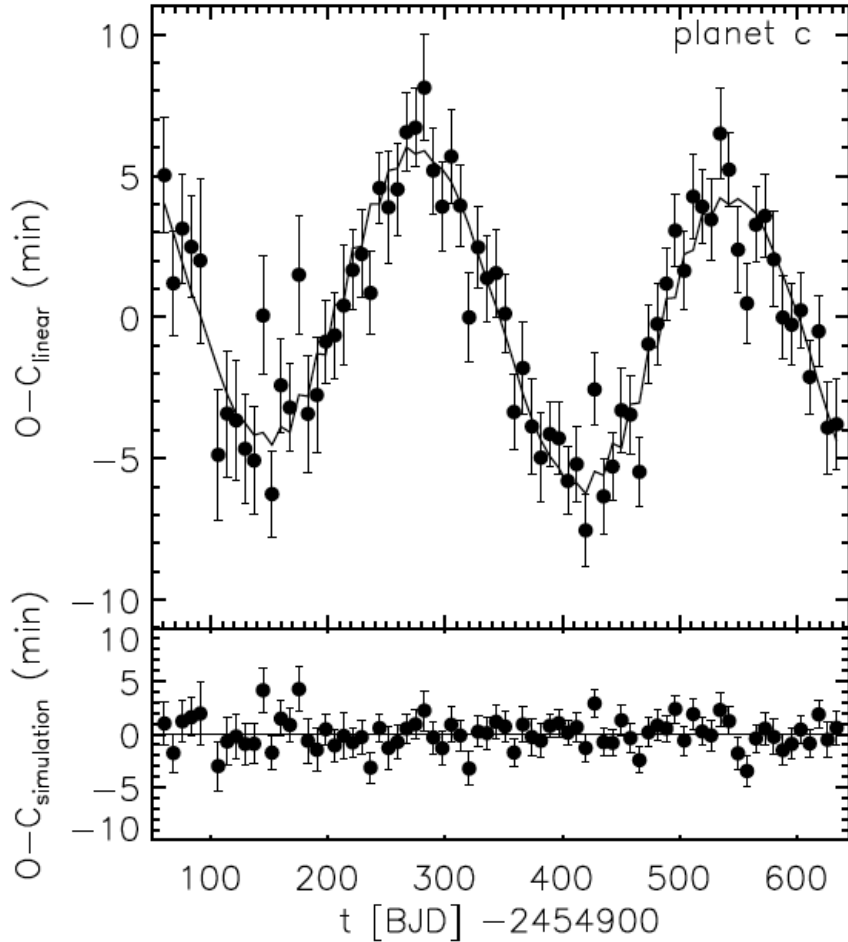
Kepler-18 (Cochran, Fabrycky, et al. 2011)



Planet	Period (days)	Mass (M_{Earth})
b	3.5	12 ± 5
c	7.6	15 ± 5
d	14.9	28 ± 7

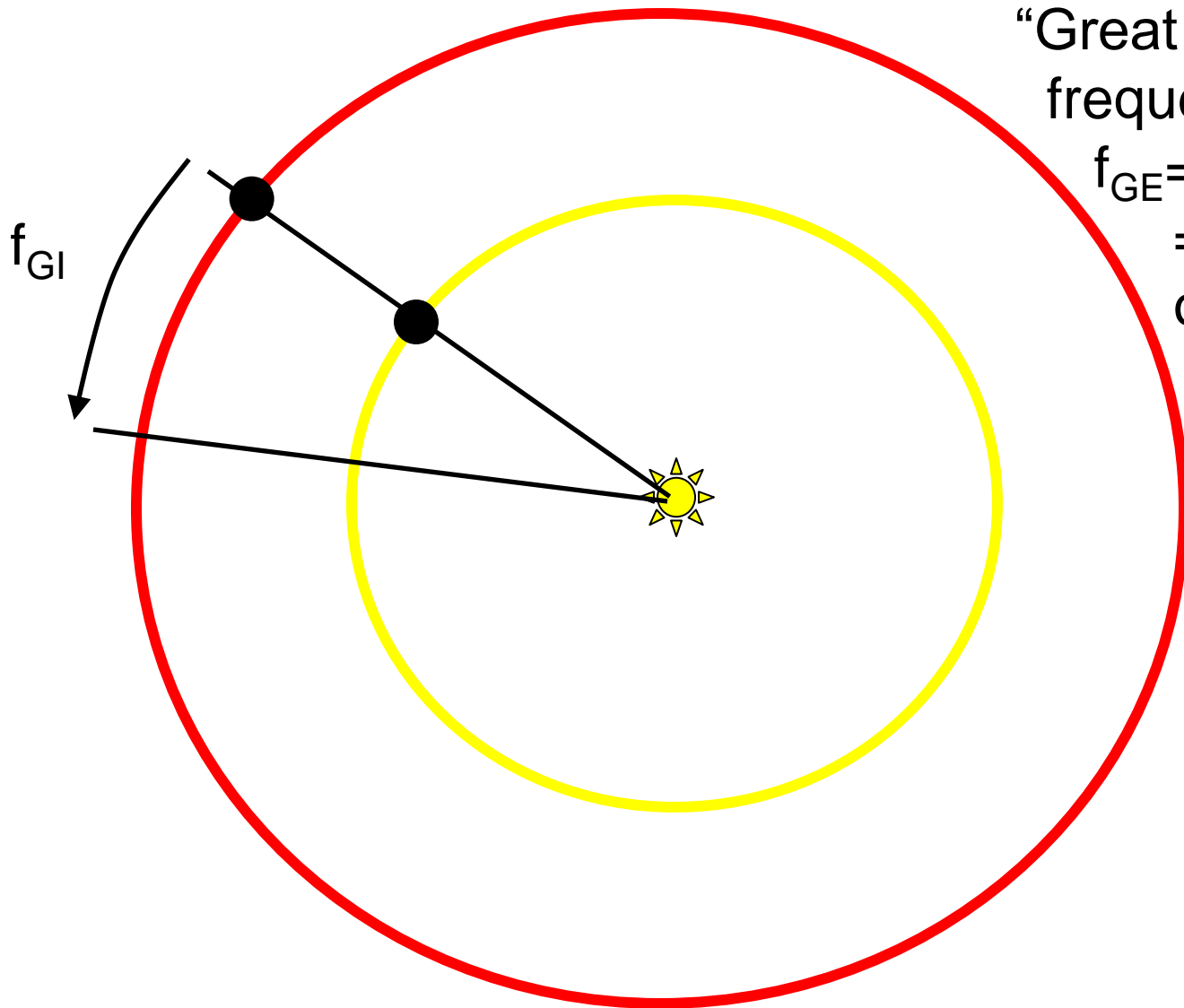
P = 7.6416 days

P = 14.8589 days



$$P/P = 1.944 \sim 2/1$$

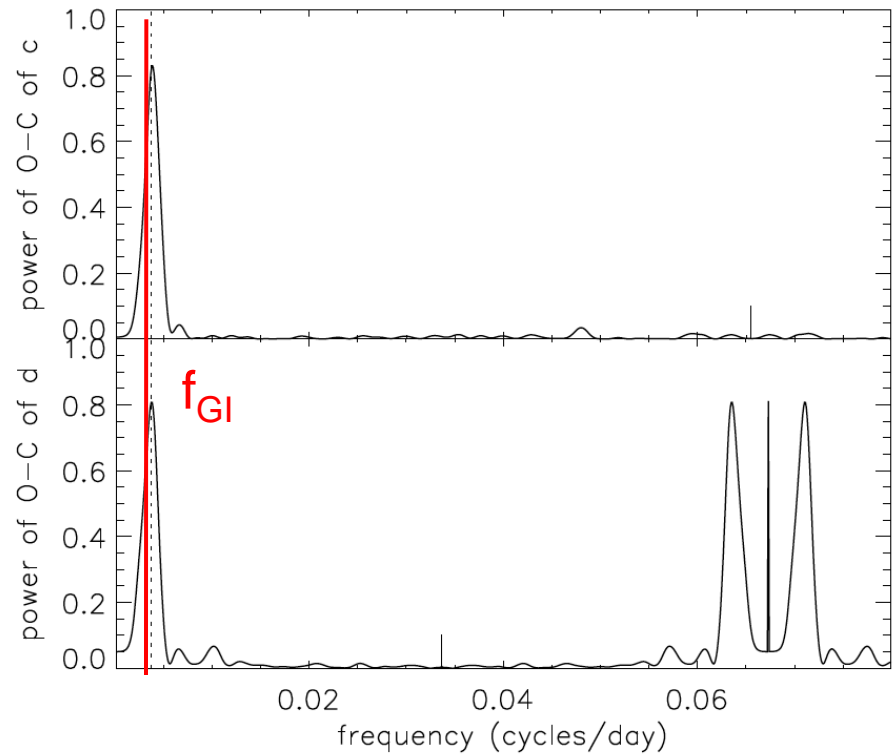
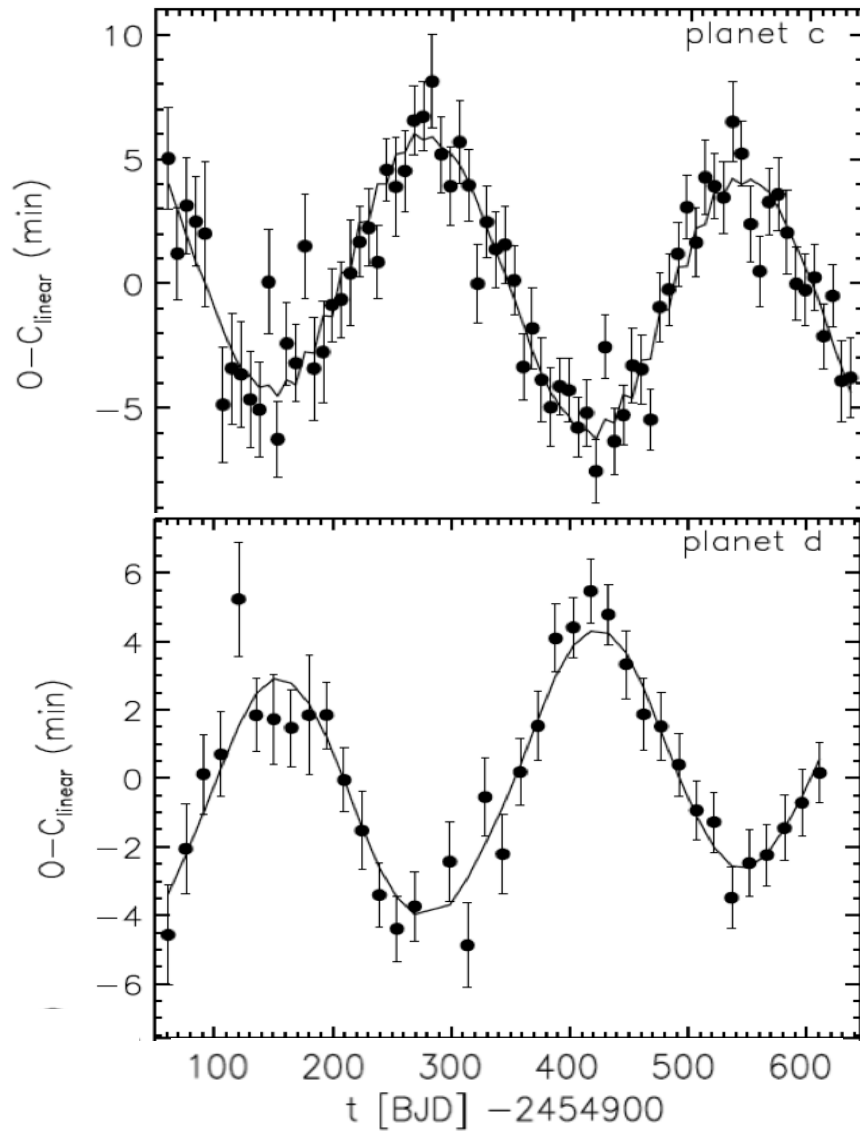
Fit adjusts: P , T_0 (phase), $e \cos w$, $e \sin w$, M_p of each planet



“Great Inequality”

frequency:

$$f_{GE} = 2/P - 1/P$$
$$= 0.0037 \text{ d}^{-1}$$
$$\text{or } 270 \text{ days}$$



The Great Inequality is observed!

Kepler-18 tests TTV masses

Planet	Period (days)	RV Mass (M_{Earth})	TTV Mass (M_{Earth})
b	3.5	12 ± 5	18 ± 9
c	7.6	15 ± 5	17.3 ± 1.7
d	14.9	28 ± 7	15.8 ± 1.3

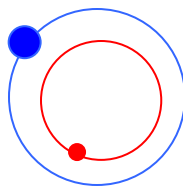
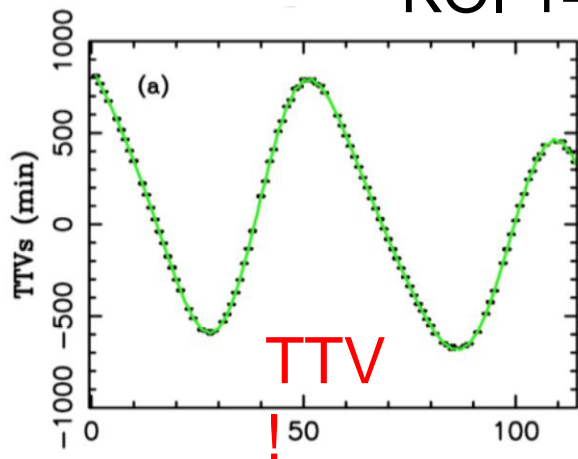
Other multi-transiting test?

Kepler-9: published RV dataset has 6 points for 3 planets, an insufficient test;

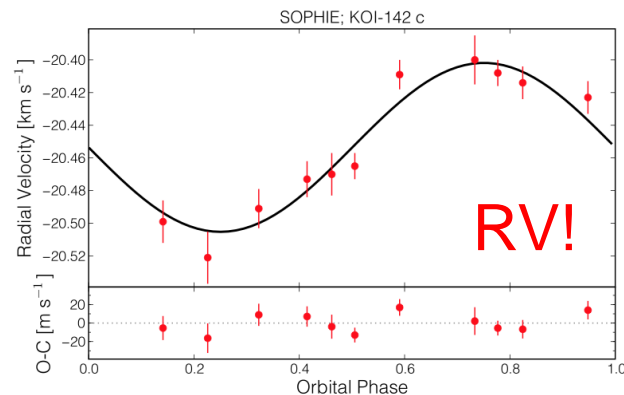
(see Dreizler & Ofir (2014), Borsato+14 for TTV mass)

TTV-discovered Planet, Checked by RV

- KOI-142 (Nesvorny et al. 2013)



Barros et al. (2014)



Fitted parameters

22.340 +/- 0.002

Orbital period, P [days]

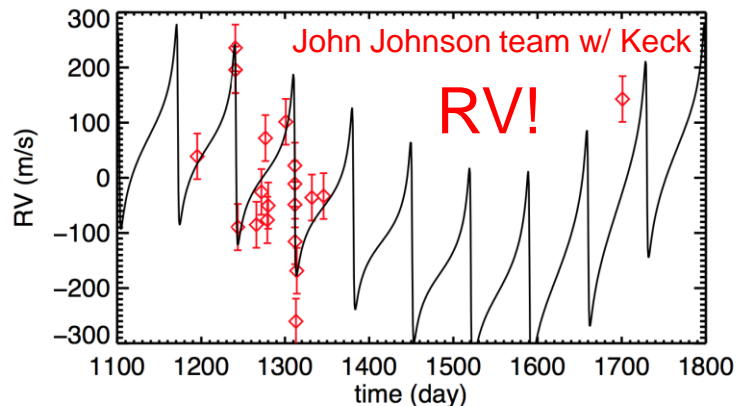
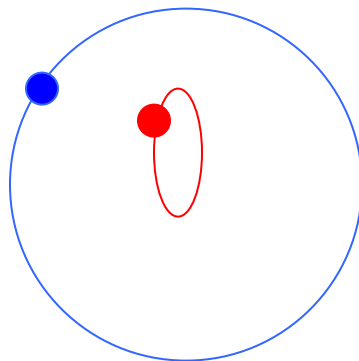
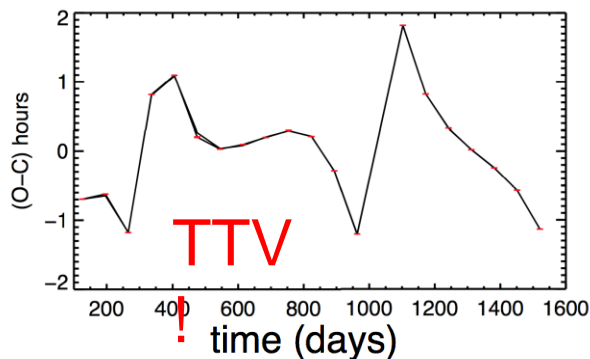
0.0559 +/- 0.0004

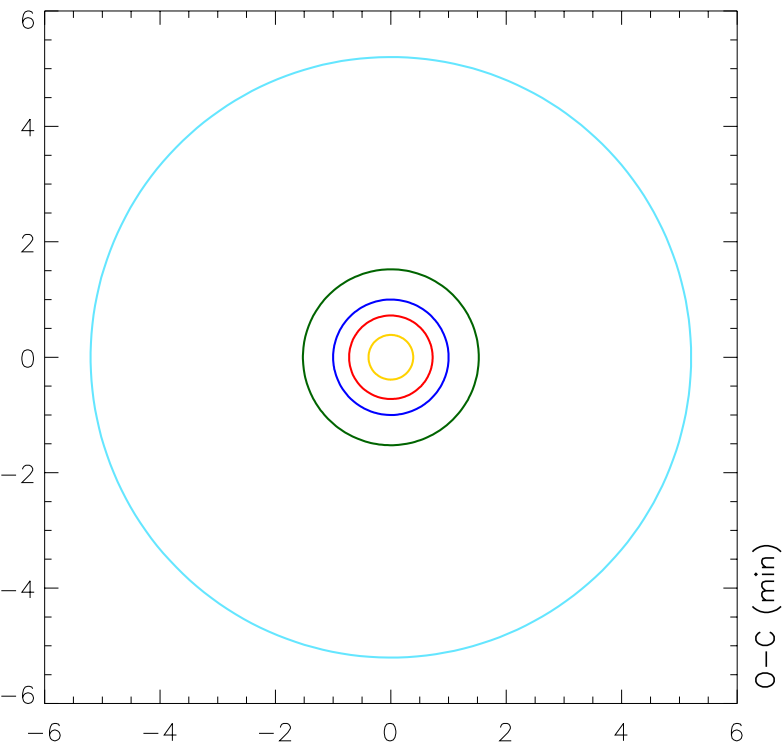
Orbital eccentricity

0.63 +/- 0.03

Minimum planet mass [M_J]

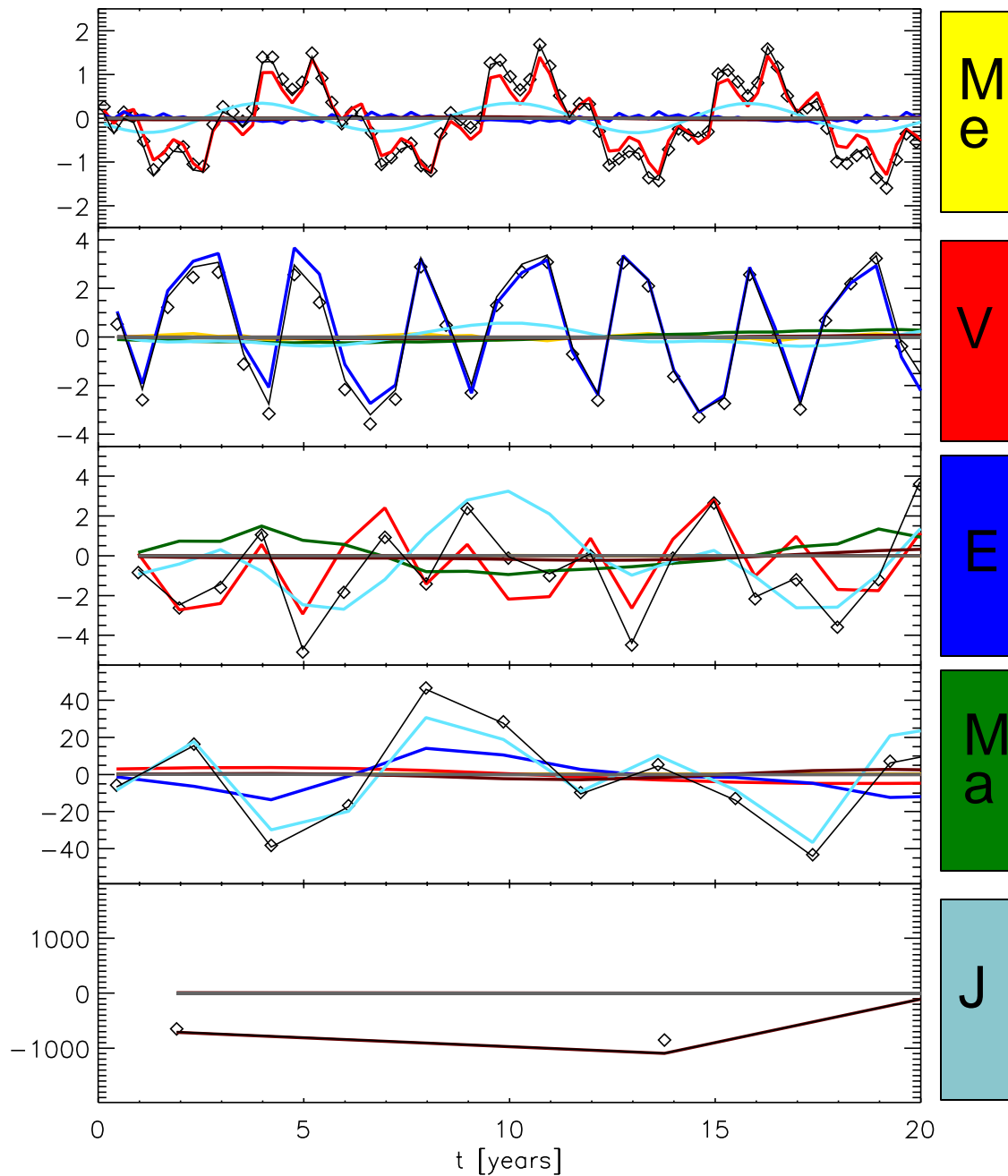
- KOI-1474 (Dawson et al. 2012, 2014)



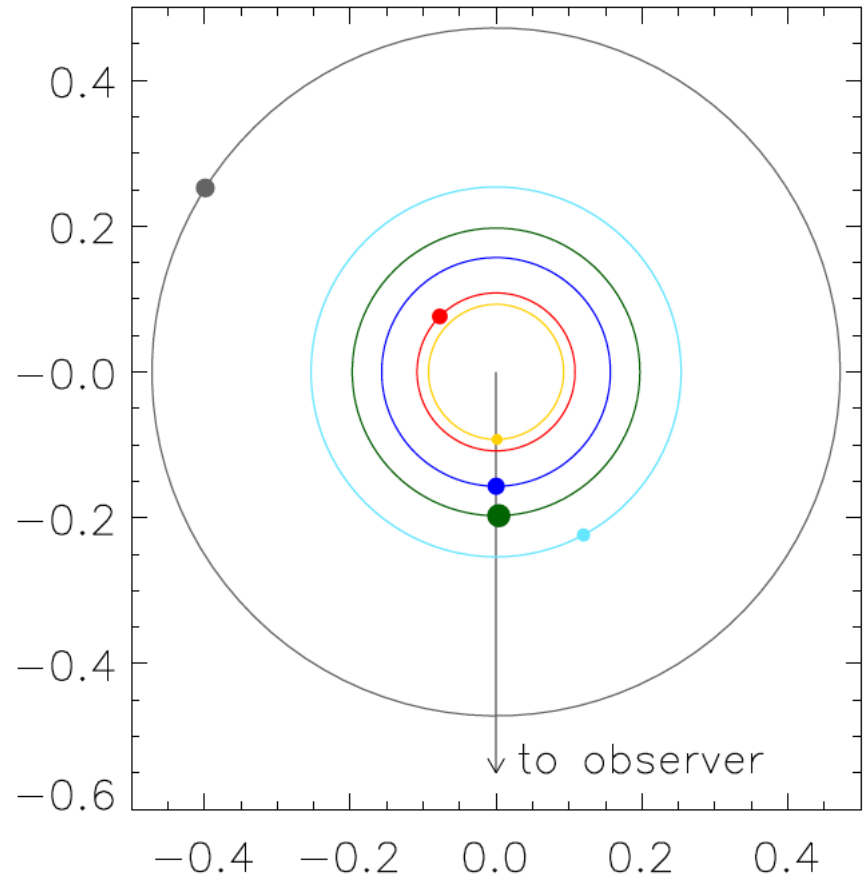
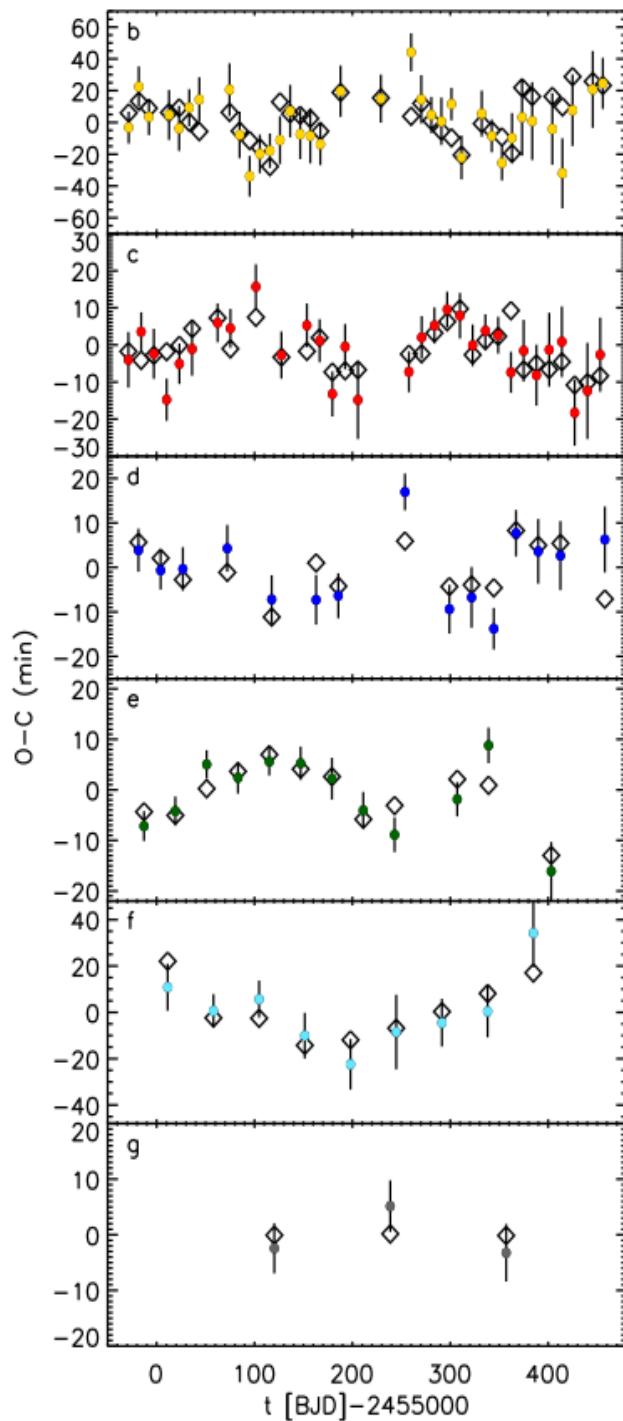


Mercury-through-Jupiter mutual perturbations.

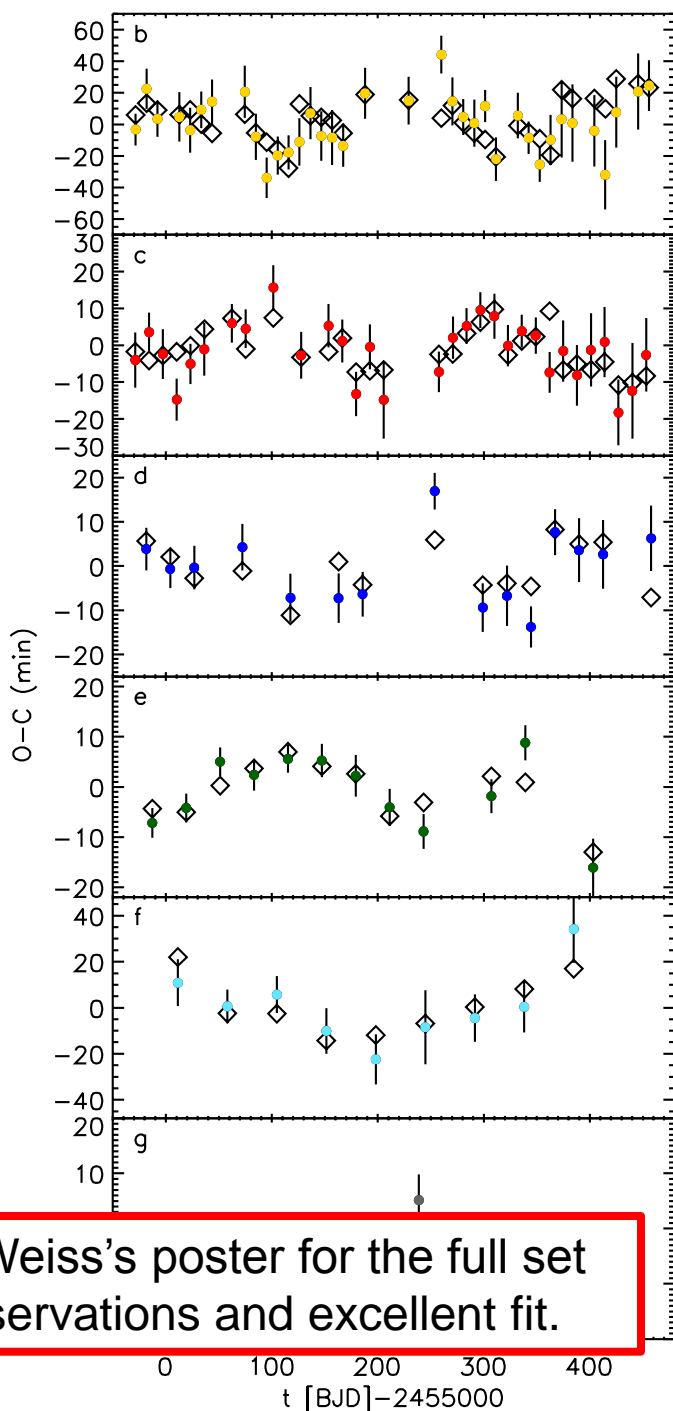
Concept: Holman & Murray 2005



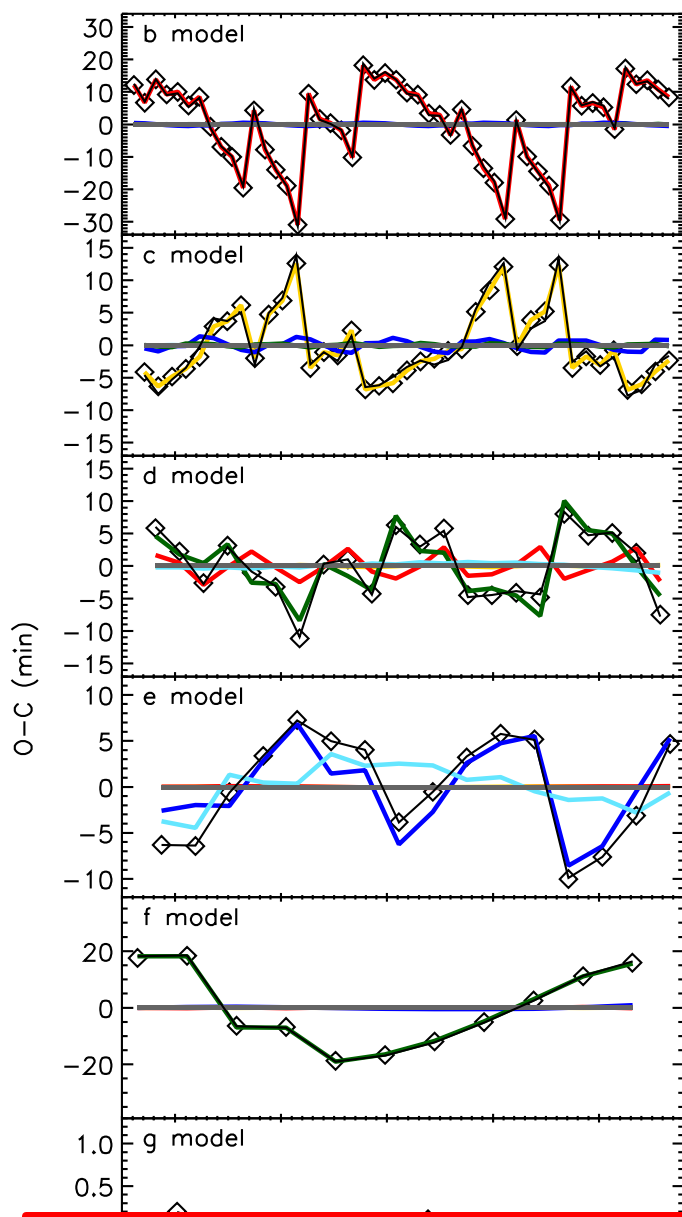
Kepler-11



Lissauer, Fabrycky, et al. 2011

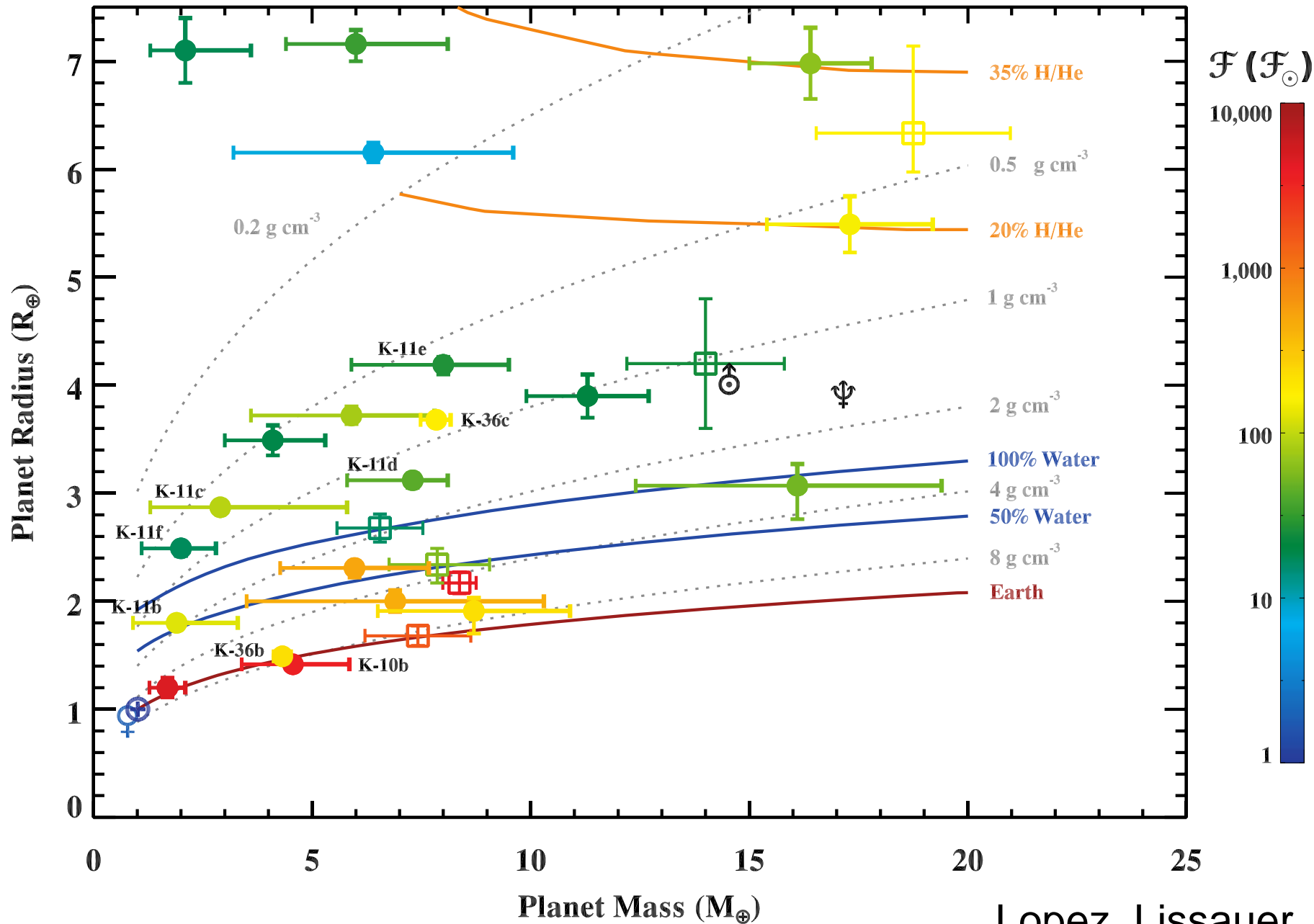


See Weiss's poster for the full set of observations and excellent fit.

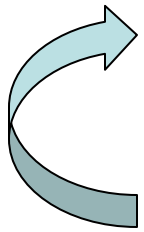
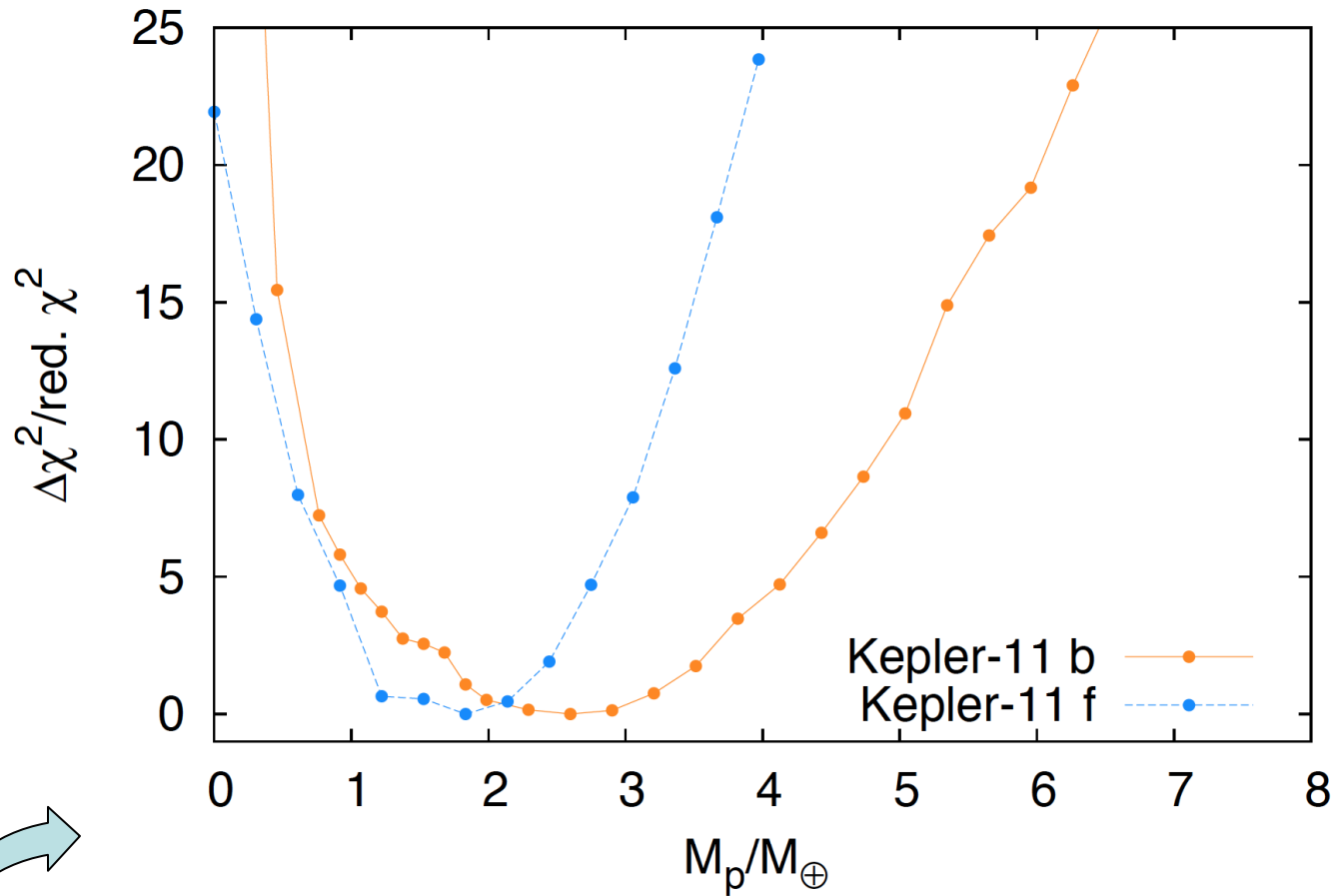


Measure *Radius* from the transit depth.
Measure *Mass* from the neighbor's transit timing.

From Earth-sized to Mini-Neptunes



“Have you tried taking the smallest two Kepler-11 planets, fixing them at higher masses, and actually seeing if you can't find a solution... that isn't offensive?” -
-Dave Charbonneau on Monday



Quick work by Daniel Jontof-Hutter!

(Lissauer, Jontof-Hutter, et al. 2013 updated analysis of Kepler-11)

More Extreme Sub-Neptunes

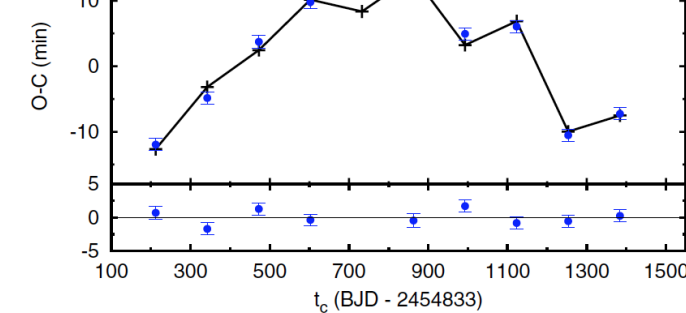
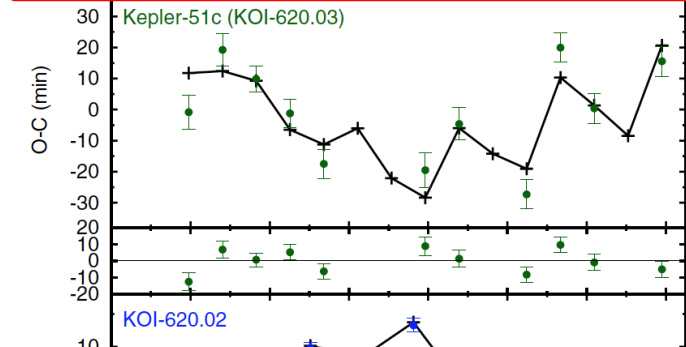
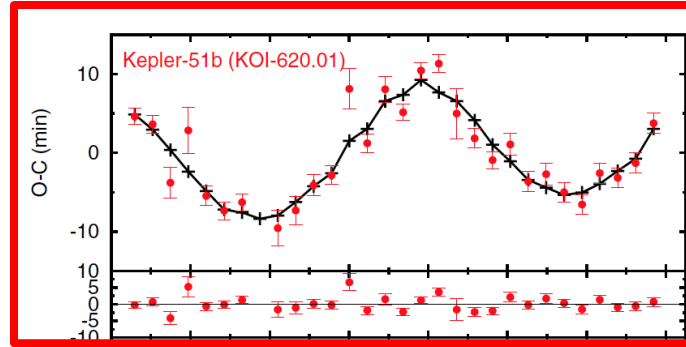
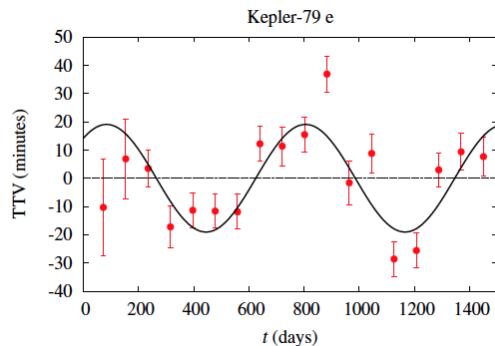
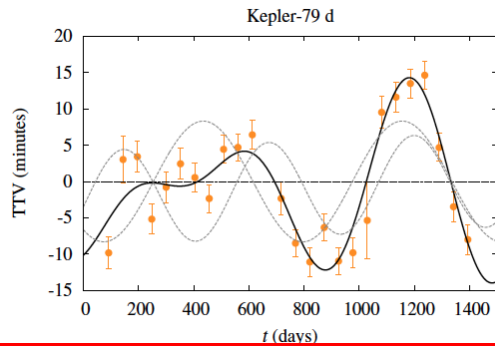
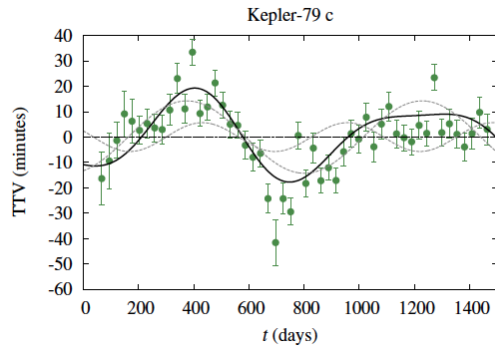
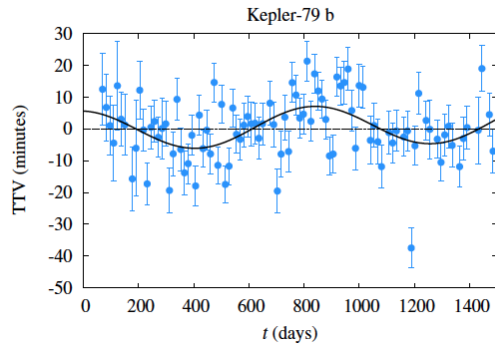
(don't ignore them – they're real!)

See Daniel Jontof-Hutter's poster and talk with him!

Kepler # Planet	T_{eq} (K)	TTV Mass (M_{Earth})	Transit Radius (R_{Earth})	Ref.
79 d	634	$6.0^{+2.1}_{-1.6}$	$7.16^{+0.13}_{-0.16}$	Jontof-Hutter + 2014
51 b	543	$2.1^{+1.5}_{-0.8}$	7.1 ± 0.9	Masuda 2014
87 c	403	6.4 ± 0.8	6.1 ± 0.3	Ofir + 2014

Same density as the architypical puffy hot Jupiter, TrES-4 (Sozzeti et al. 2015)

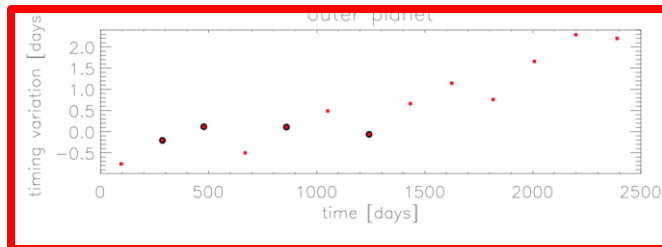
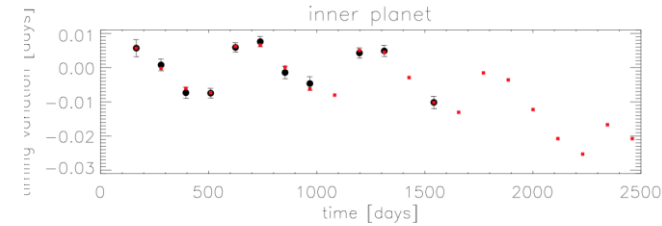
More Extreme Sub-Neptunes



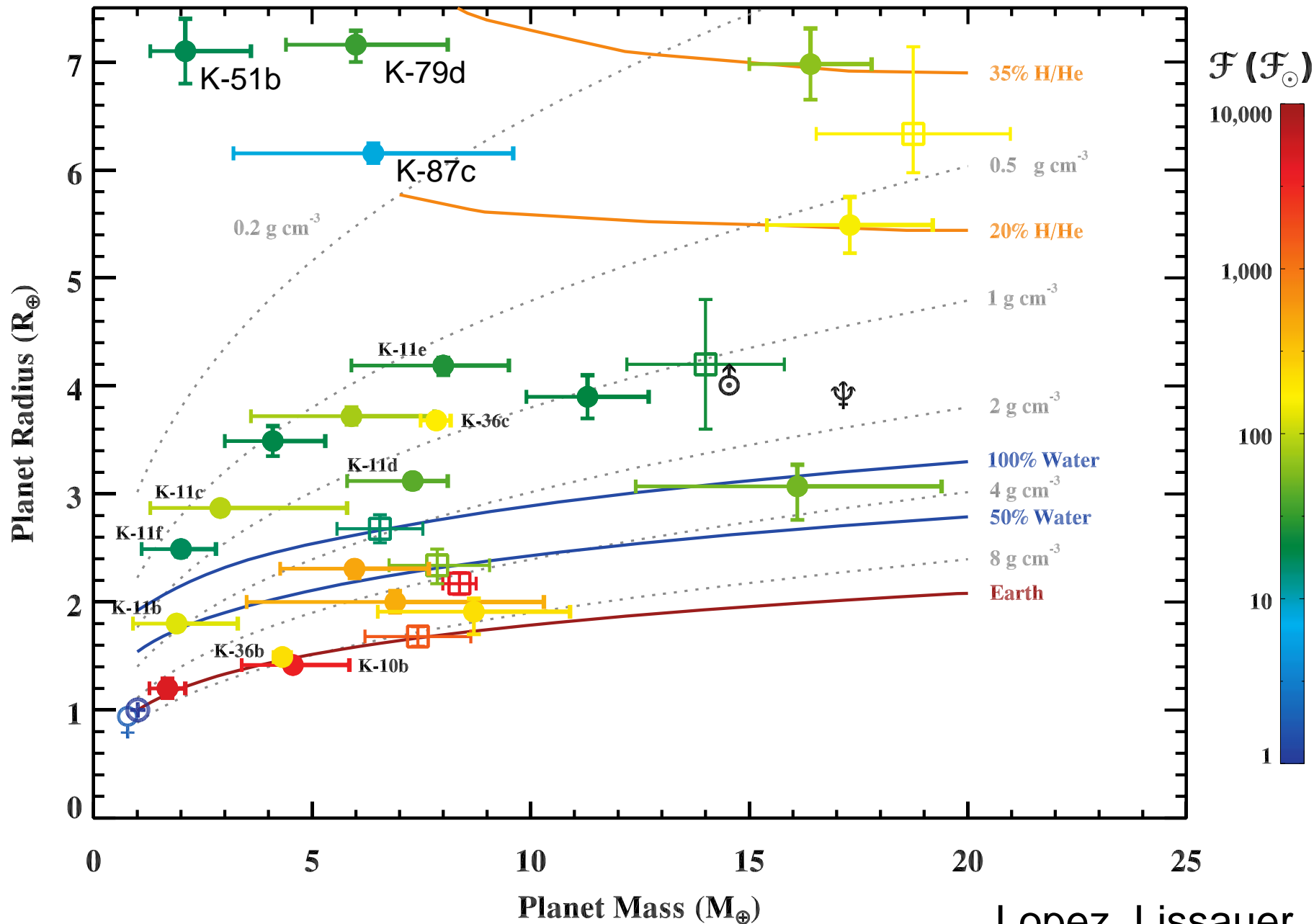
<< Jontof-Hutter+14

< Masuda 14

VV Ofir+14



From Earth-sized to Mini-Neptunes



Exoplanetary System Architectures

Basic facts:

- Planet number
- Masses
- Radii

Dynamical properties:

- Periods (n.b.: their ratios)
- Eccentricities
- Mutual Inclinations

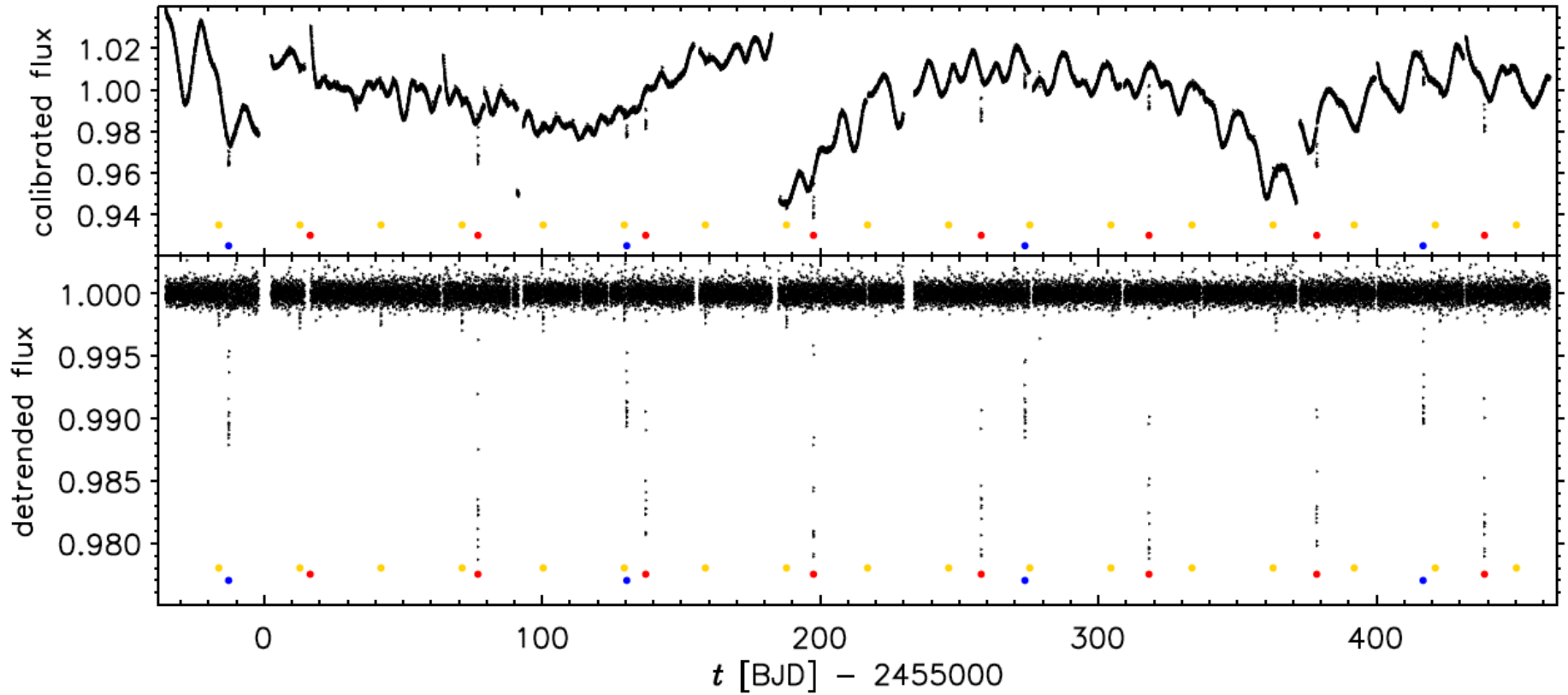
Transits	Radial Velocities
w/ TTV	✓
w/ TTV	✓
✓	
✓✓	✓
w/ TTV	✓
w/ TDV	

Clearinghouse of TTV and TDV curves: Mazeh et al. 2013

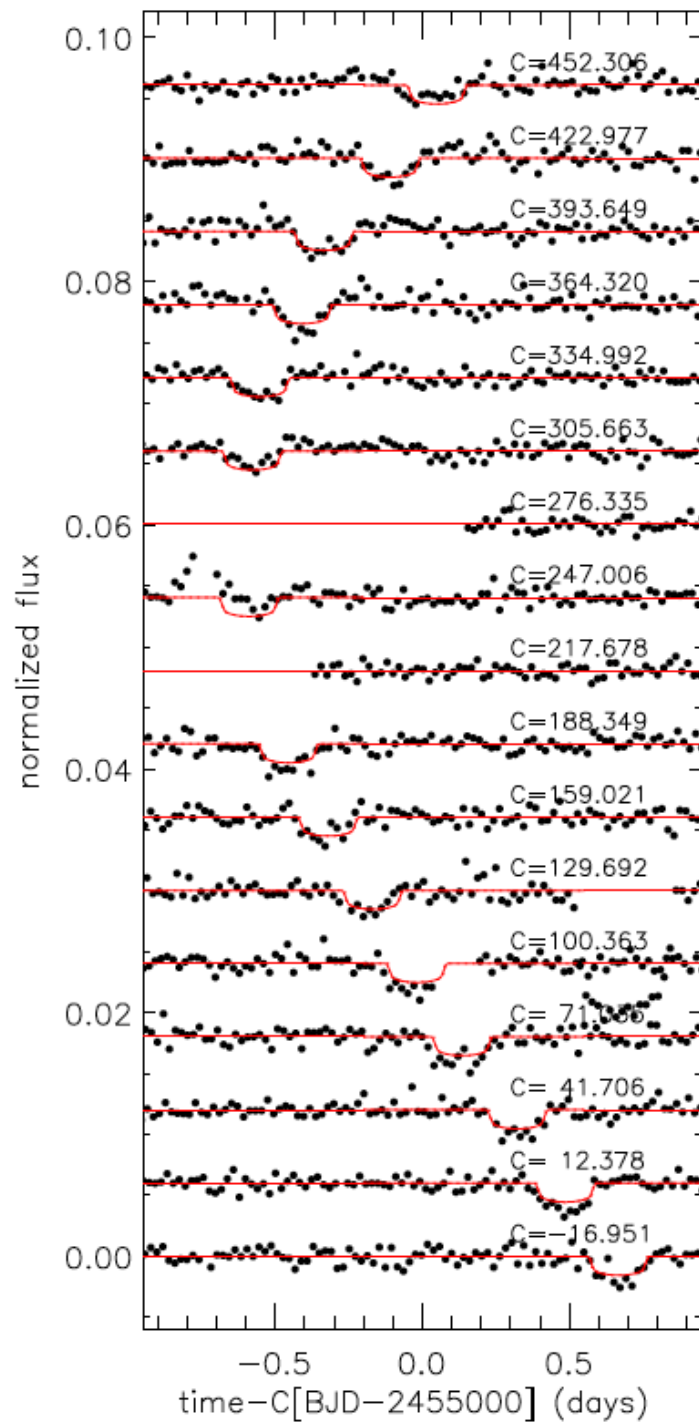
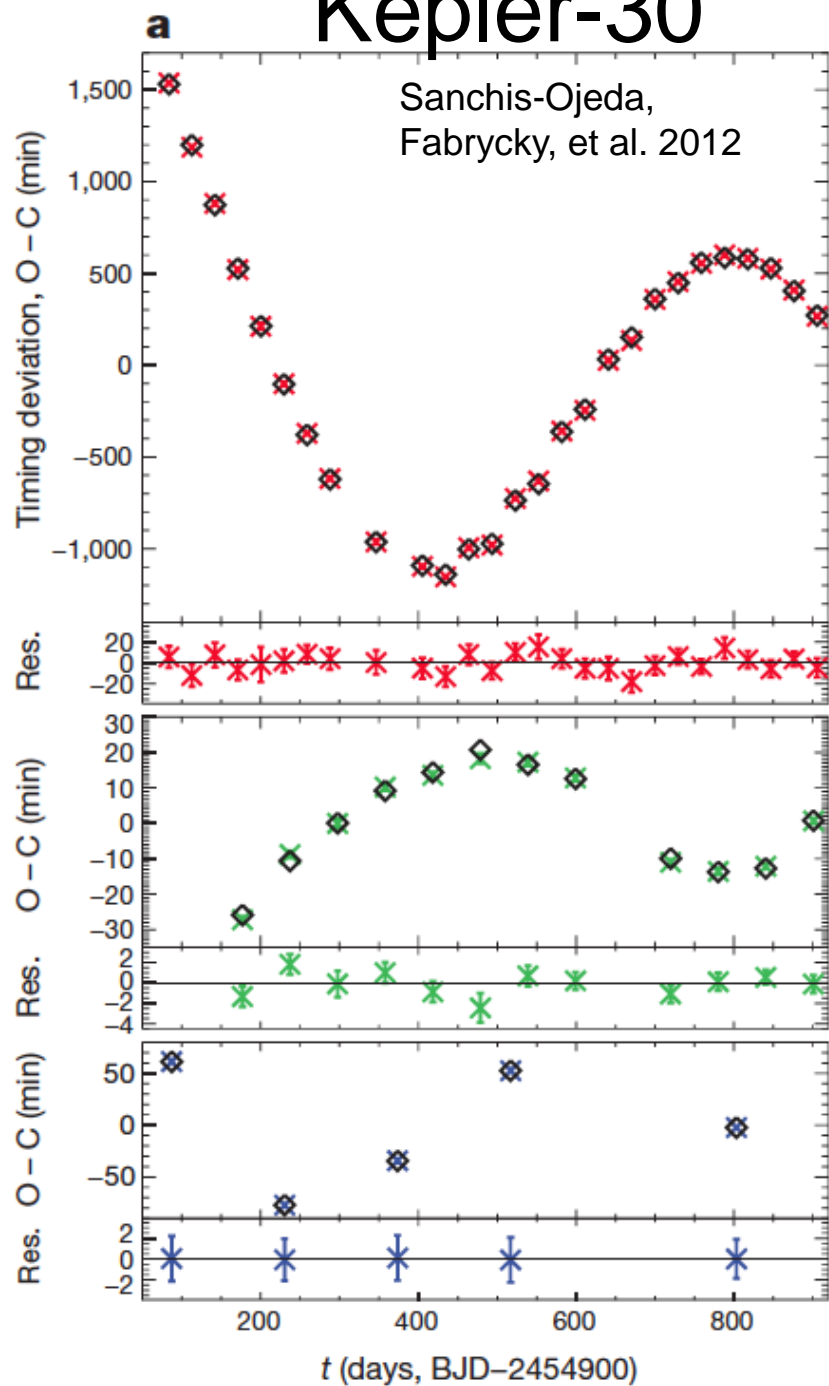
<ftp://wise-ftp.tau.ac.il/pub/tauttv/TTV>

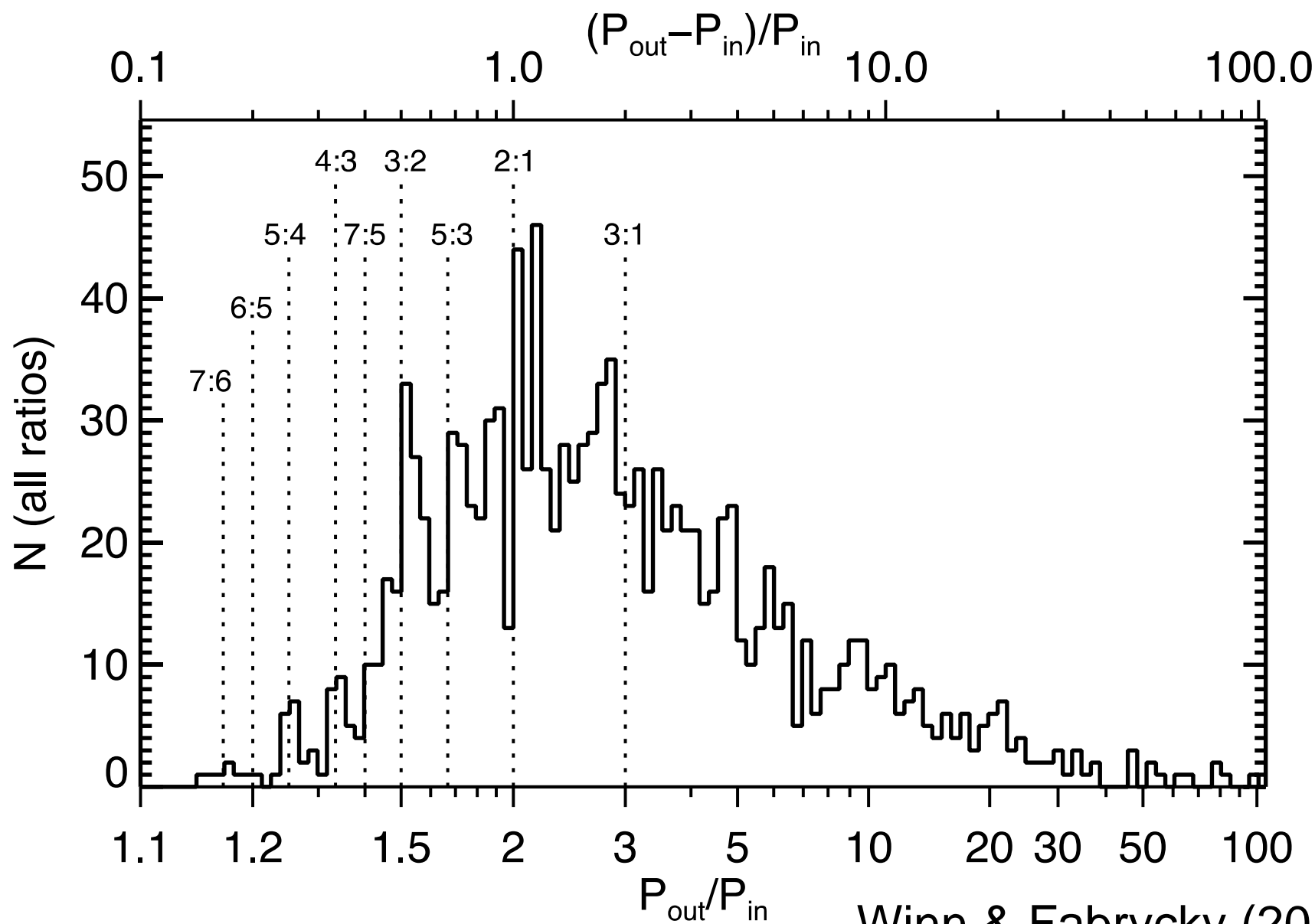
Version 112 sub-directory for the latest

Kepler-30



Kepler-30





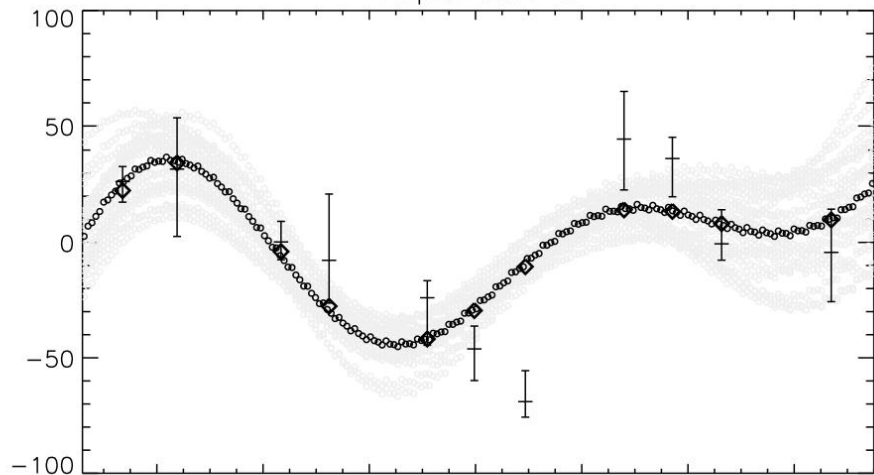
Winn & Fabrycky (2015)
 Following Fabrycky+14,
 “Architectures II”

A few Resonant chains

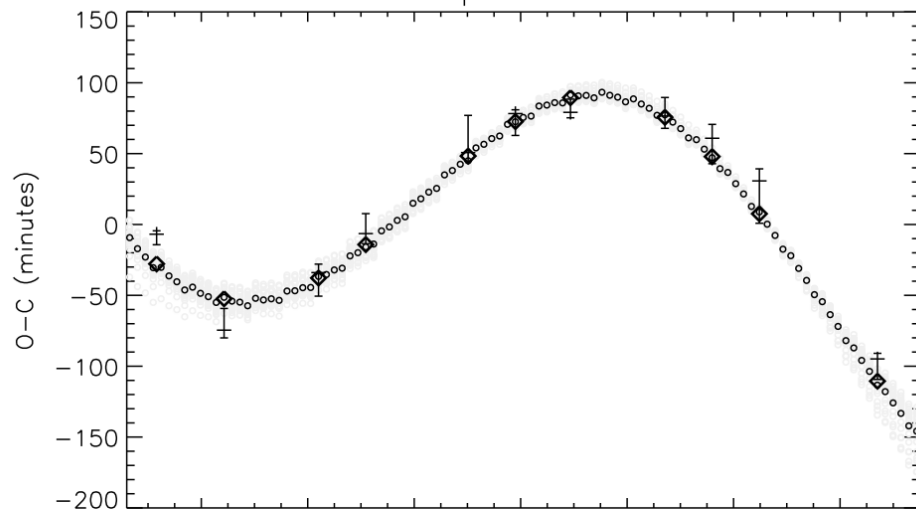
- Kepler-223 (KOI-730; 4:3, 3:2, 4:3)
- Kepler-60 (KOI-2086; 5:4, 4:3)
- Kepler-80 (KOI-500; 1.518, 1.518, 1.350)

KOI-730 TTVs, detected at last!

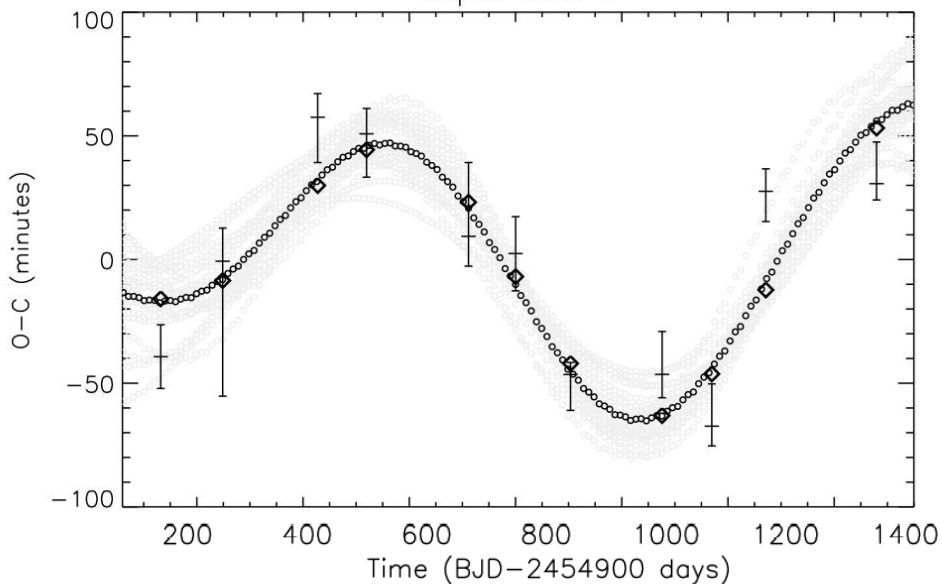
Kepler 223 b



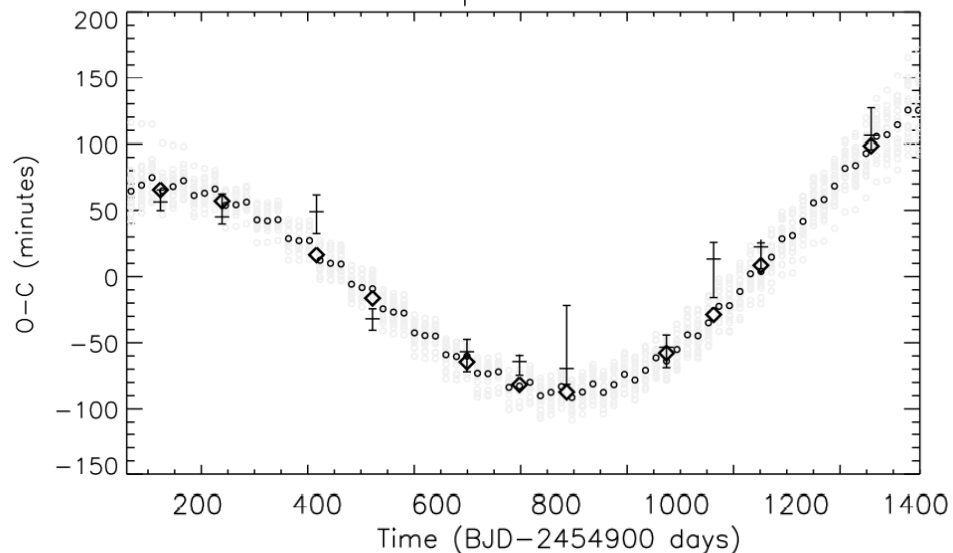
Kepler 223 d



Kepler 223 c



Kepler 223 e

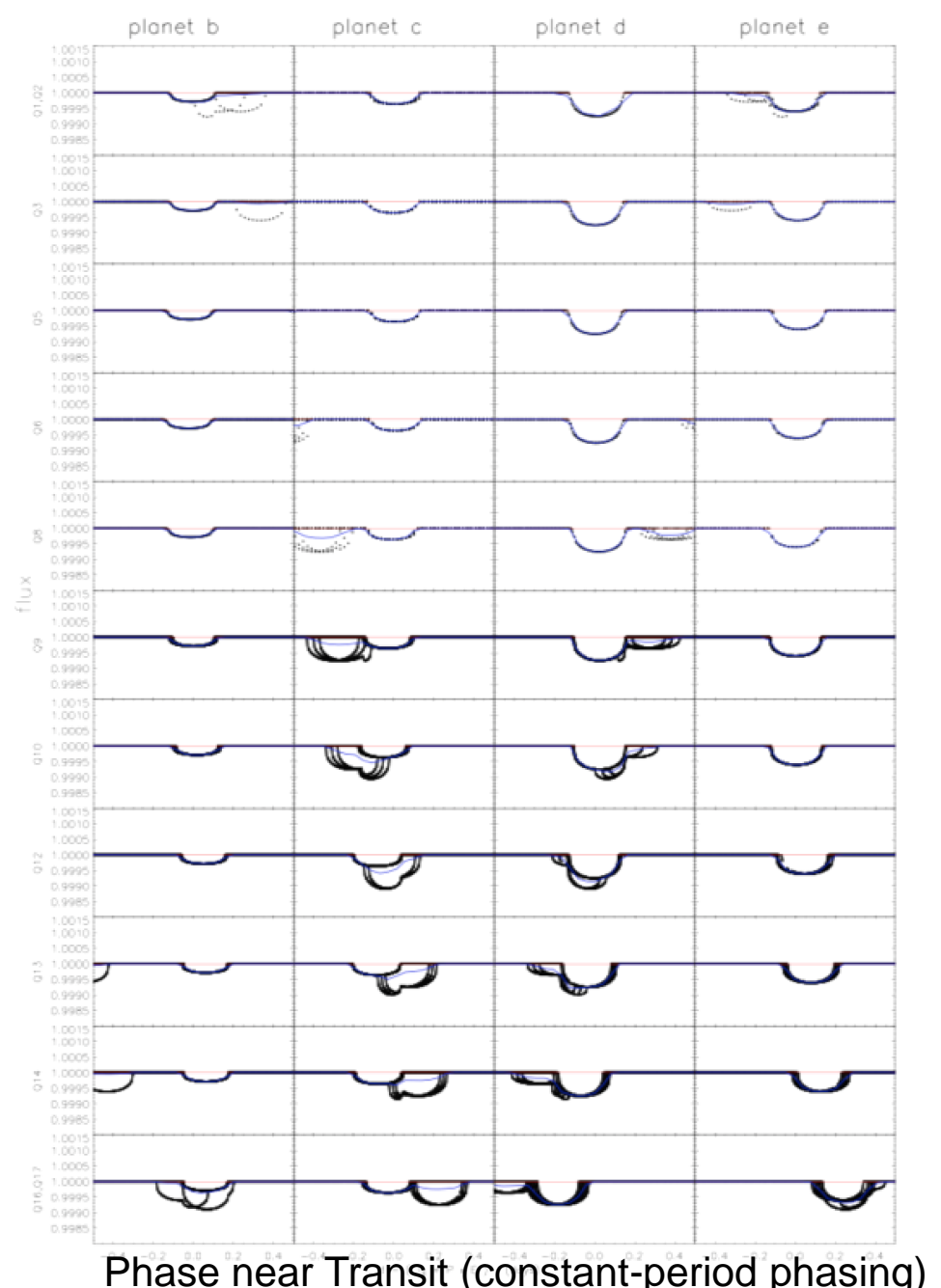
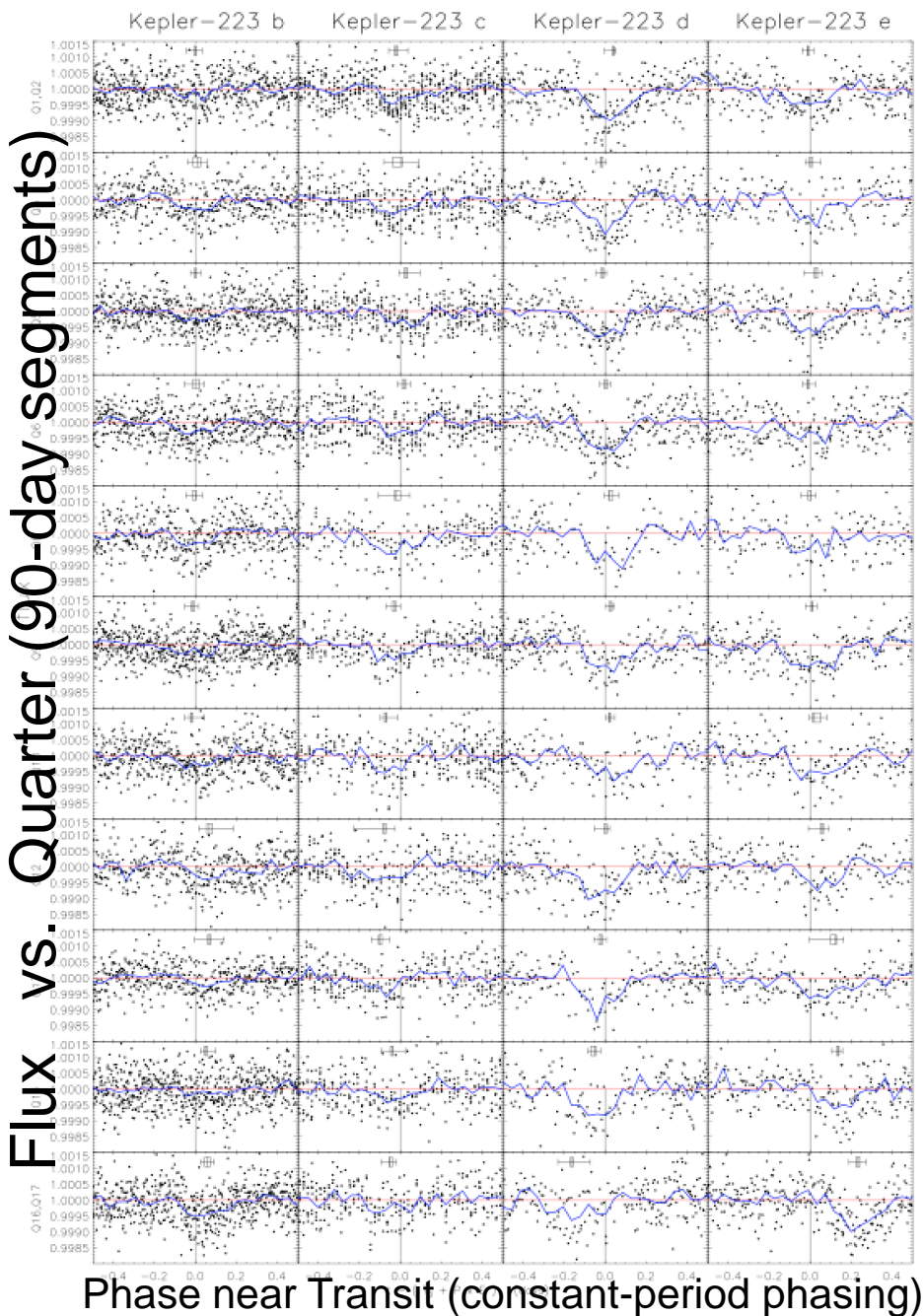


See Sean Mills' poster!

KOI-730

DATA

Photodynamic MODEL



Sinusoidal Photodynamics

- Work in progress: Fitting photometry of all multitransiting systems with transit phase

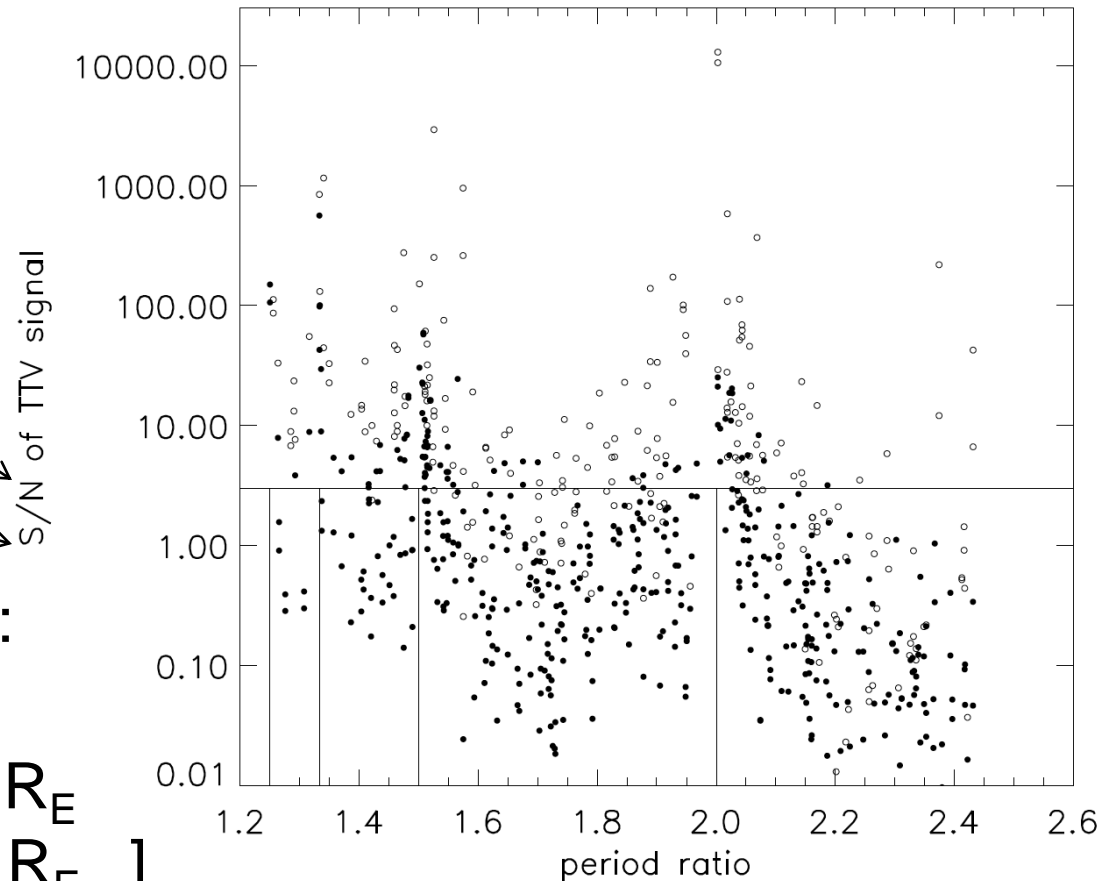
$$\Phi = T_0 + P \times E + A_{\text{ttv}} \sin(2\pi t/P_{\text{ttv}} + \phi_{\text{ttv}})$$

Carter et al. (2008)
[yes, idealized!]

Lithwick et al.
(2012)

[for plot amplitudes:
e=0,

$M_{p,e} = R_{p,e}^{3.7}$ ● $R_p < 2 R_E$
 $R_{p,e}^{2.06}$ ○ $R_p > 2 R_E$]



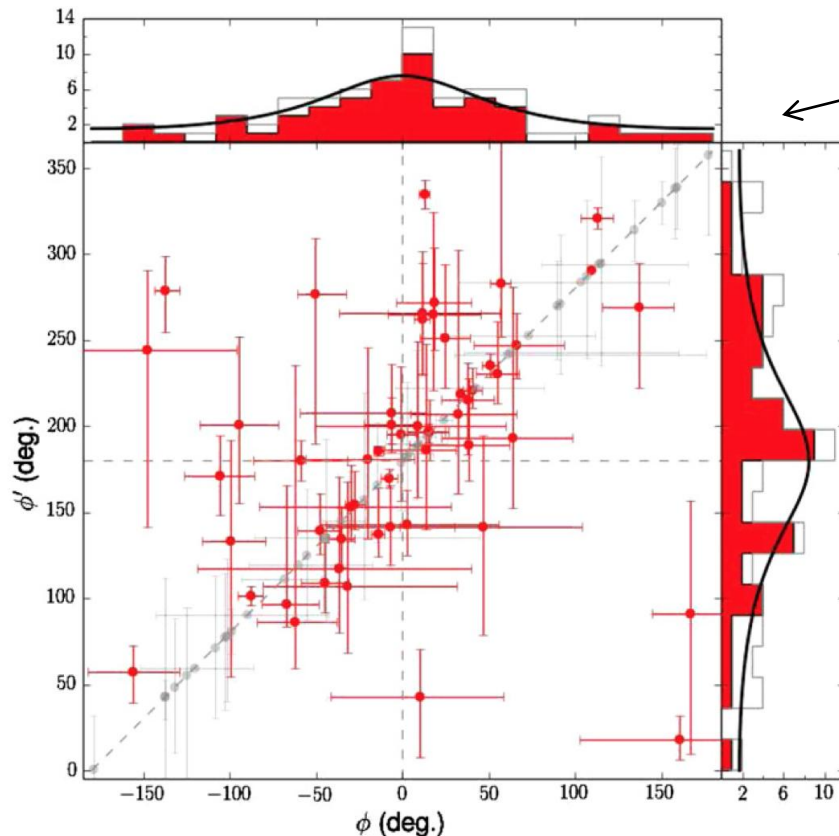
Eccentricities of Terrestrials?

- Planet formation options:
 - Within gas disk → low eccentricities
 - Giant Impacts → orbits cross, eccentricities much larger than the Hill sphere

caveat: there may be some damping on residual or secondary debris (e.g., Schlichting et al. 2012)

Eccentricities of Terrestrials?

- Planet formation options:
 - Within gas disk \rightarrow low eccentricities
 - Giant Impacts \rightarrow orbits cross, eccentricities much larger than the Hill sphere



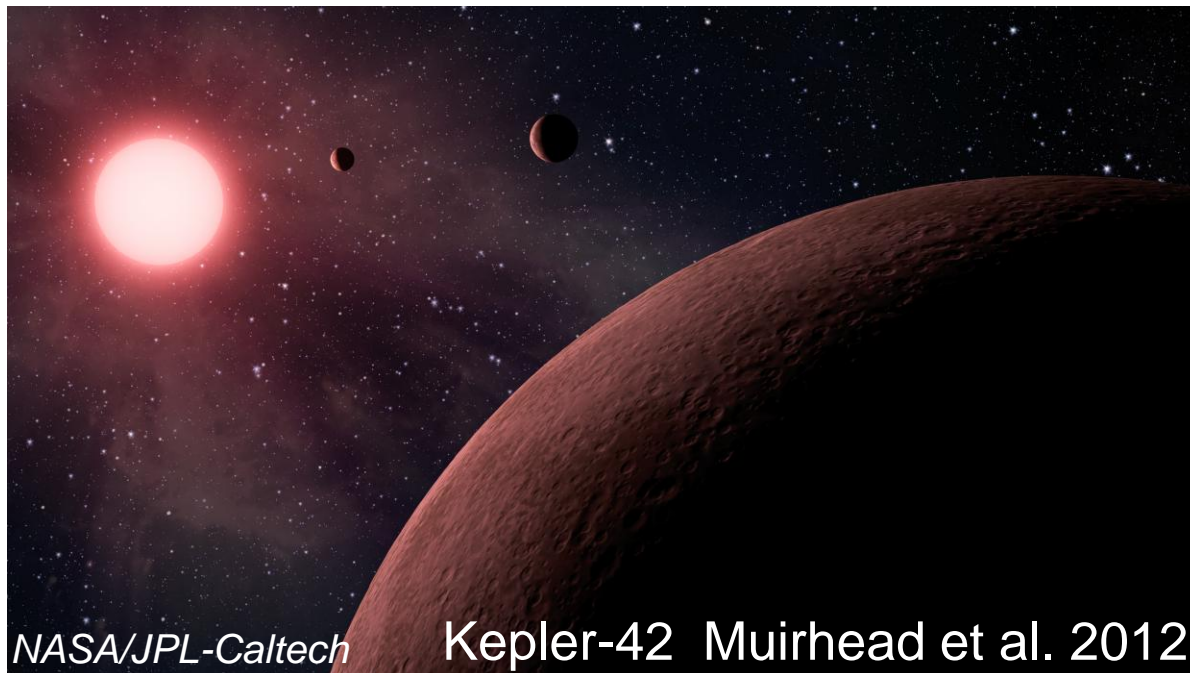
TTV phases of 54 systems:
Hadden & Lithwick (2014)
analyzing Mazeh+13 TTs.

Near - 2:1, 3:2, 4:3
resonant perturbation
relates: $\phi_{\text{ttv}} / e_{\text{free}}$

$$\sigma_e = \begin{cases} 0.017^{+0.009}_{-0.005}, & \text{for } R \text{ and } R' < 2.5 R_{\oplus} \\ 0.008^{+0.003}_{-0.002}, & \text{for } R \text{ and } R' > 2.5 R_{\oplus}. \end{cases}$$

Summary

- *Kepler* found a host of multiplanet systems.
- TTV masses reveal Super-Puffy Sub-Neptunes
- Photodynamics opens a new window on exoterrestrial planet formation



NASA/JPL-Caltech

Kepler-42 Muirhead et al. 2012