



*Structure and  
Evolution of Solar  
System Giant Planets*

*Dave Stevenson*

*Caltech*

KITP Exoplanets, March 30, 2010

# Why should you Care?

(about a tiny fraction of all planets- the ones in our solar system)

- We have a far greater prospect of understanding them in detail because of better data (including in situ data) - gravity, magnetic field, heat flow, composition (including noble gases and isotopes)
- Some of this better understanding informs us about general processes (not just the vagaries of our solar system) and calibrates our models (e.g. equation of state)
- Our planets teach us humility... our incomplete understanding is in large part because planets are complicated... planetary science will never yield to the astronomical low dimensional representations (such as the H-R diagram).

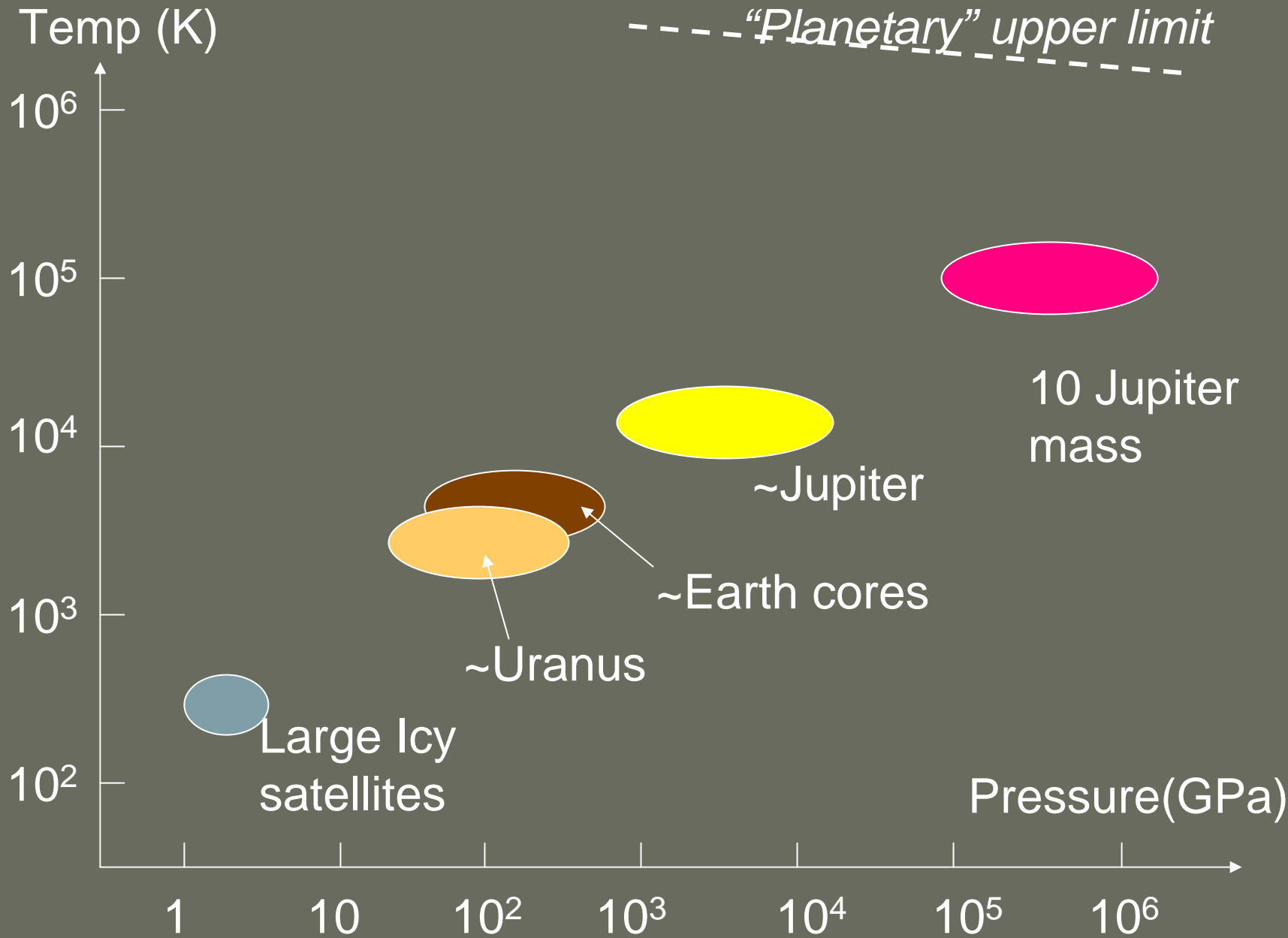
# Pressures of Relevance

- At 1 Mbar,  $PV_{\text{ion}} \sim 1\text{eV}$

- $P_{\text{typical}} \sim 1\text{Mbar} \cdot (M/M_{\text{earth}})^2 \cdot (R_{\text{earth}}/R)^4$

or  $P_{\text{typical}} \sim 10\text{Mbar} \cdot (M/M_{\text{Jupiter}})^2 \cdot (R_{\text{Jup}}/R)^4$

Pressures much higher than 10 Mbar occur in SuperJupiters (common) but hydrogen is “simple” at these extreme pressures (and relevant temperatures)?



# *Cosmic (~Solar) Abundances*

<b>Element</b>	<b>Number Fraction</b>	<b>Mass Fraction</b>
H	0.92	0.71
He	0.08	0.27
O	$7 \times 10^{-4}$	0.011
C	$4 \times 10^{-4}$	0.005
Ne	$1.2 \times 10^{-4}$	0.002
N	$1 \times 10^{-4}$	0.0015
Mg	$4 \times 10^{-5}$	0.001
Si	$4 \times 10^{-5}$	0.0011
Fe	$3 \times 10^{-5}$	0.0016

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-But these characterizations are very misleading at high P and T

## Mass-Radius Relationships

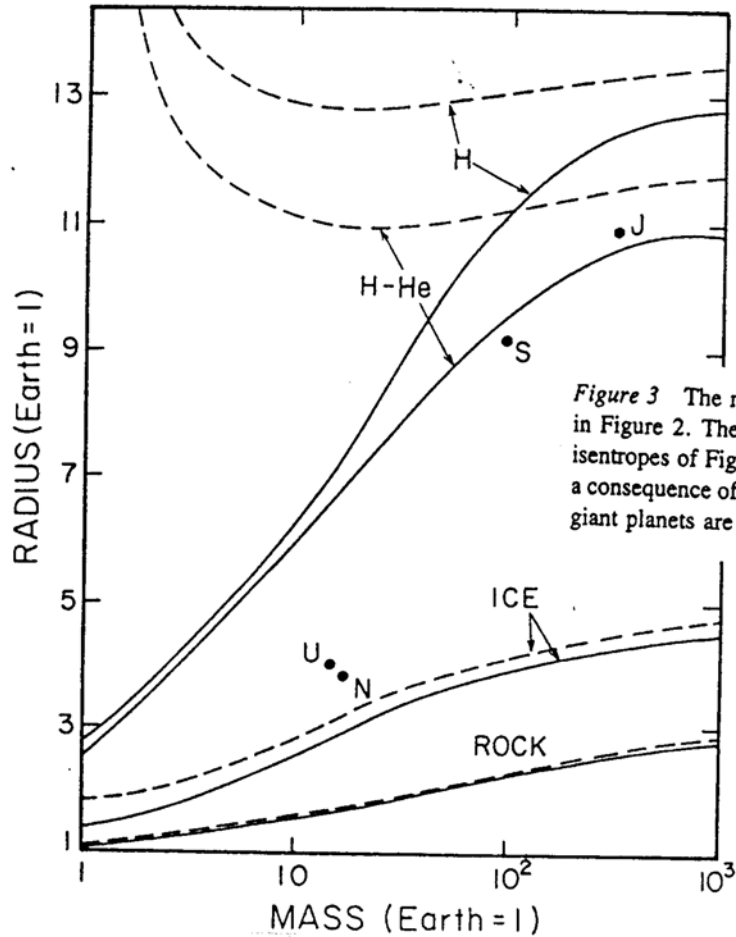


Figure 3 The mass-radius relationship for self-gravitating bodies of the same compositions as in Figure 2. The solid lines are for cold matter ( $T = 0$  K); the dashed lines correspond to the isentropes of Figure 2. The insensitivity of radius or mass for hydrogen and hydrogen-helium is a consequence of the approximate validity of  $P \propto \rho^2$  (see text for discussion). The positions of the giant planets are labelled by J, S, U, and N.

Stevenson (1982)

A reworking of Zapolsky & Salpeter (1969),  
adding isentropic models

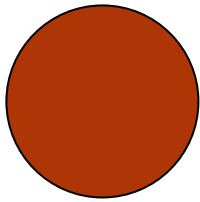
# Some Significant Facts for Our Solar System

- Jupiter & Saturn are mostly gas. (So they must have formed in the presence of a nebula).
- Jupiter may have a dense core & Saturn almost certainly has a dense core. Both are enriched in heavy elements throughout.
- Jupiter and Saturn release substantially more energy than they receive from the Sun.. Primarily a consequence of steady cooling.
  - Contraction is a consequence of cooling , not an energy source in itself.
  - Possibly also some differentiation.
- Uranus and Neptune resist simple characterization. Contrary to what is sometimes claimed, they are not necessarily ice rich. (You could build them out of Plutos or Tritons plus a modest amount of gas.) Not layercakes!



# Why might a Planet have a Core?

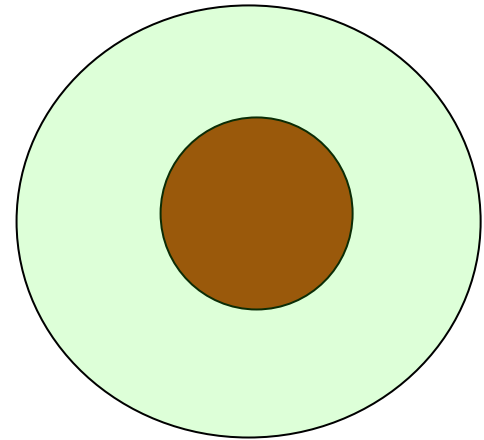
Bottom Up



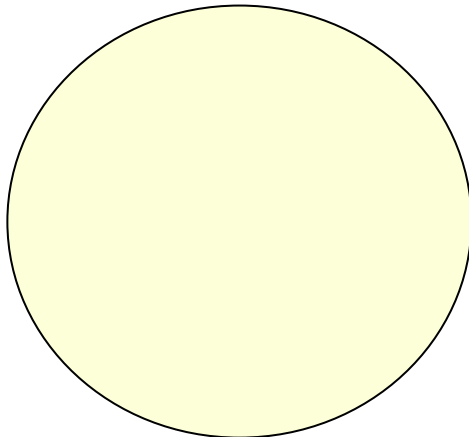
Popular Giant  
Planet Picture



Accrete gas



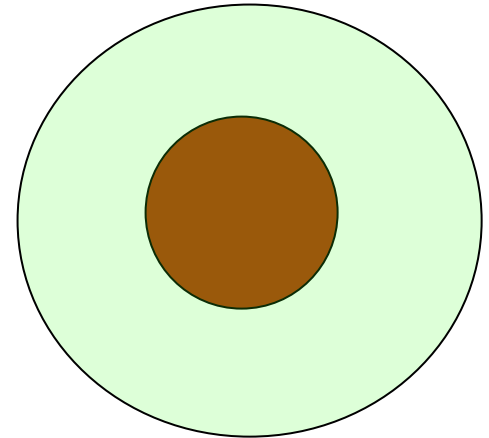
Top Down



Well established  
Terrestrial Planet  
Picture

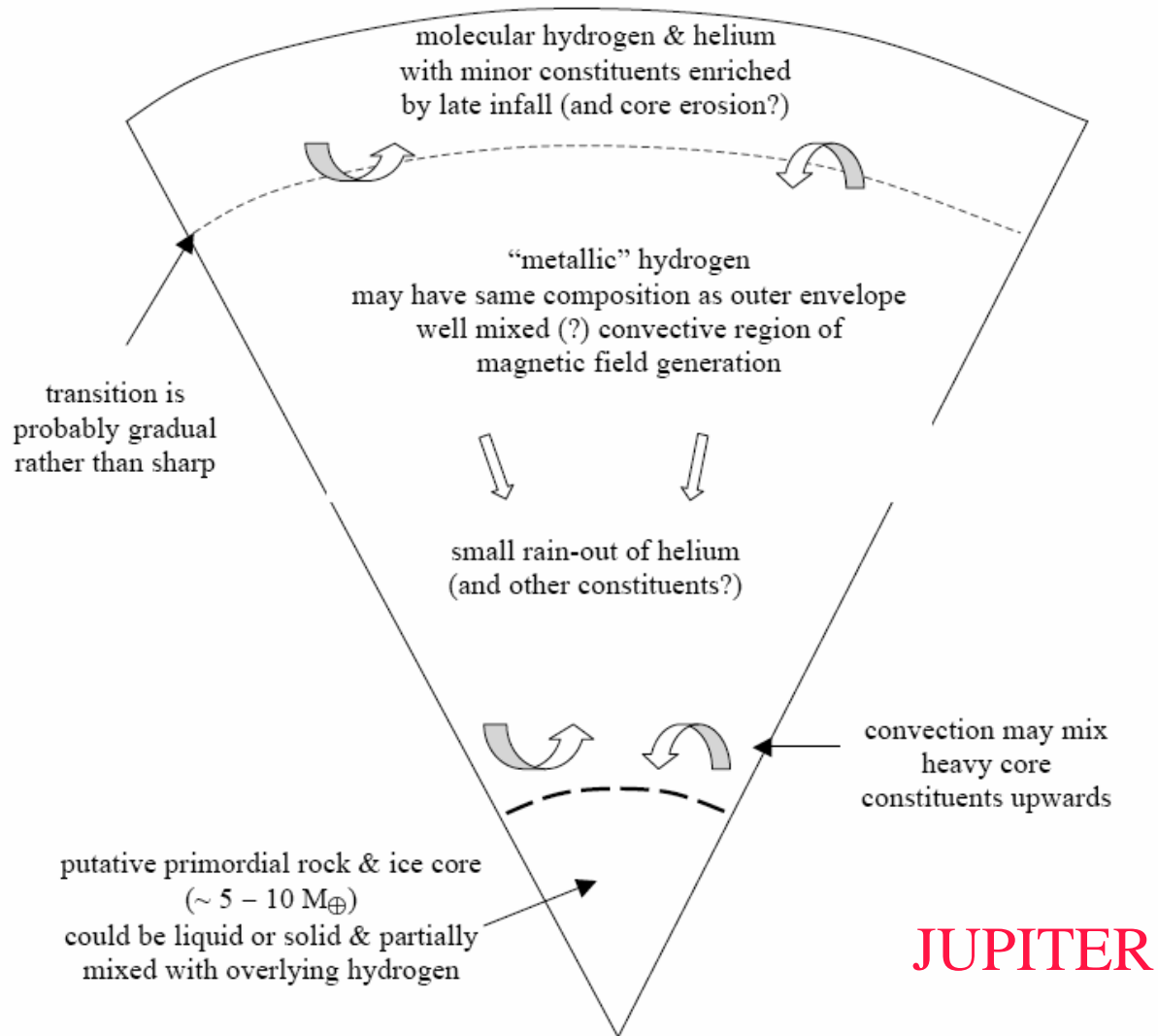


Differentiate



# There are some major problems with giant planet models

- Equation of state uncertainties
  - Theory of pure end-members still not converging with other information
  - Mixtures not well understood. Our usual concepts of relevant materials break down at high P and T.
  - Experiments are difficult
- Unreasonable reliance on parsimony.
  - Concepts of “cores” are based on false analogies (e.g., Earth’s core or behavior of materials at low P and T)
  - Ideas of planet formation do not necessarily lead to simple separation of materials according to density.
- Absence of the most valuable technique: Seismology



# Current State of Jupiter Modeling

- Until a few years ago, the state of the art relied heavily on EOS from Saumon, Chabrier and van Horn (a “chemical approach”). Used extensively by Guillot. But enough uncertainty that one could not say whether Jupiter has a core.
- More recent modeling use density functional approach to the EOS for hydrogen (also some work on mixtures)
- Latest models yield just as much variation in core mass as previous work! (Few to 15 Earth masses).
  - Primary reason is different assumptions about the composition (number of layers)
- Is the molecular to metallic phase transition first order? This may be the wrong thing to focus on since it must be at most a small entropy and density jump.
  - No current evidence of a first order transition.
- Insolubility of helium is now quite well established (this is a first order phase transition).
- Layering, if present, can arise from how the planet was assembled.

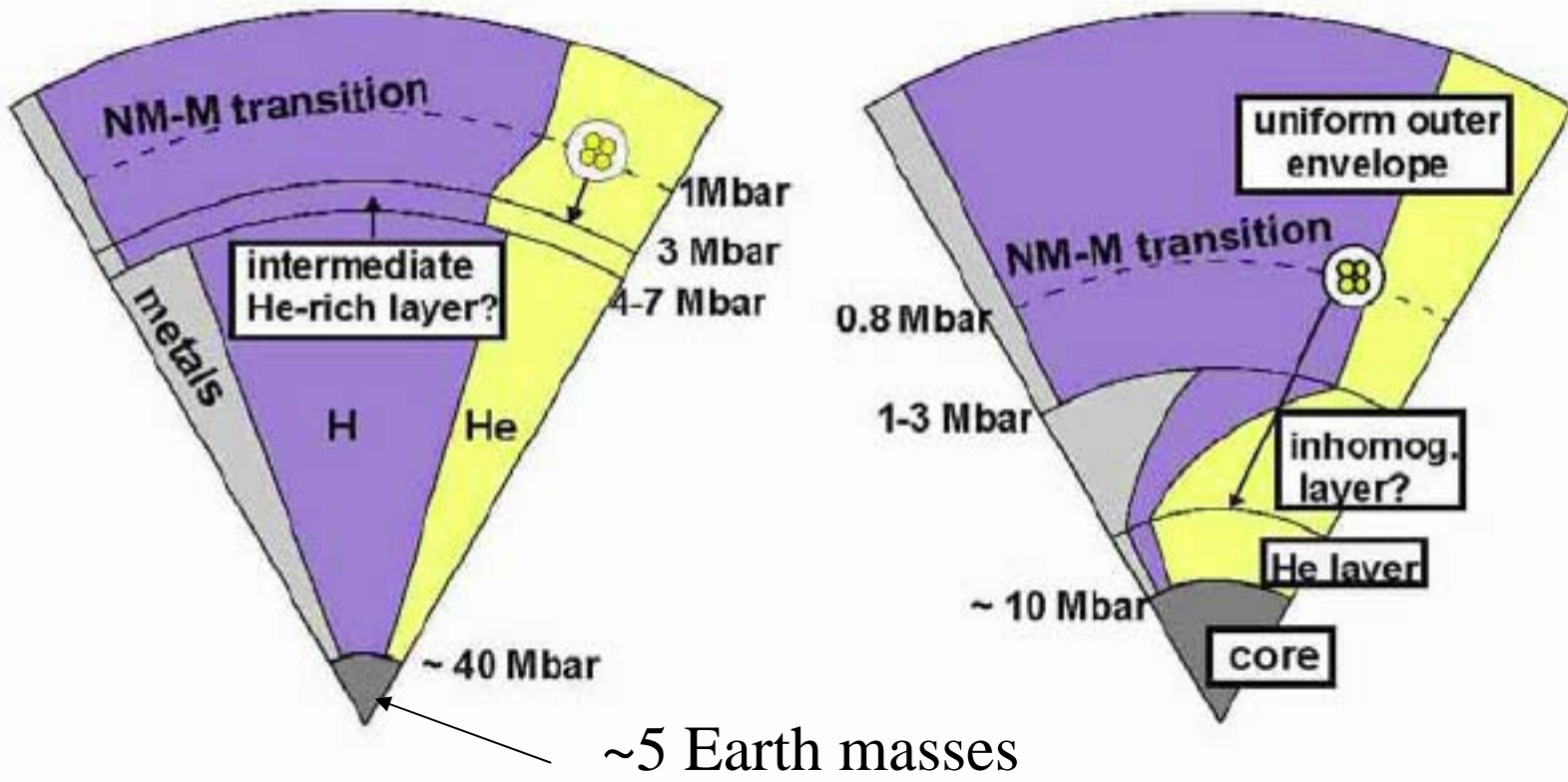


Figure 2: 4-layer interior models of Jupiter (left) and Saturn (right).

Nettelmann et al,  
2008...

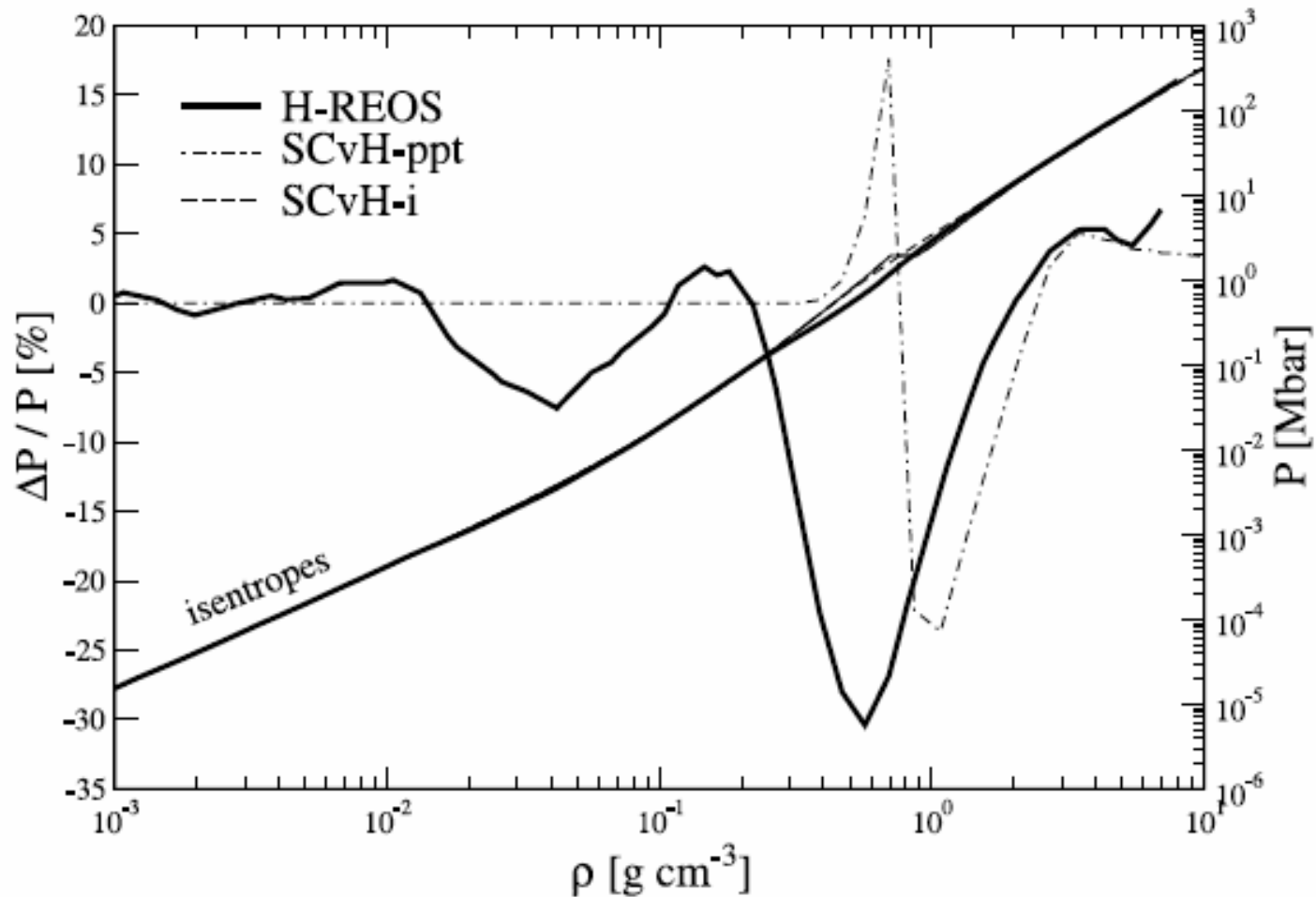


FIG. 6.—Hydrogen adiabats for Jupiter, determined by  $T = 165$  K at  $P = 1$  bar, computed with three different hydrogen EOSs: H-REOS, SCvH-i, and SCvH-ppt. The scale on the right shows absolute pressures, and the scale on the left shows relative differences in pressure with respect to the SCvH-i-adiabat.

# Where do we go with the EOS Issue?

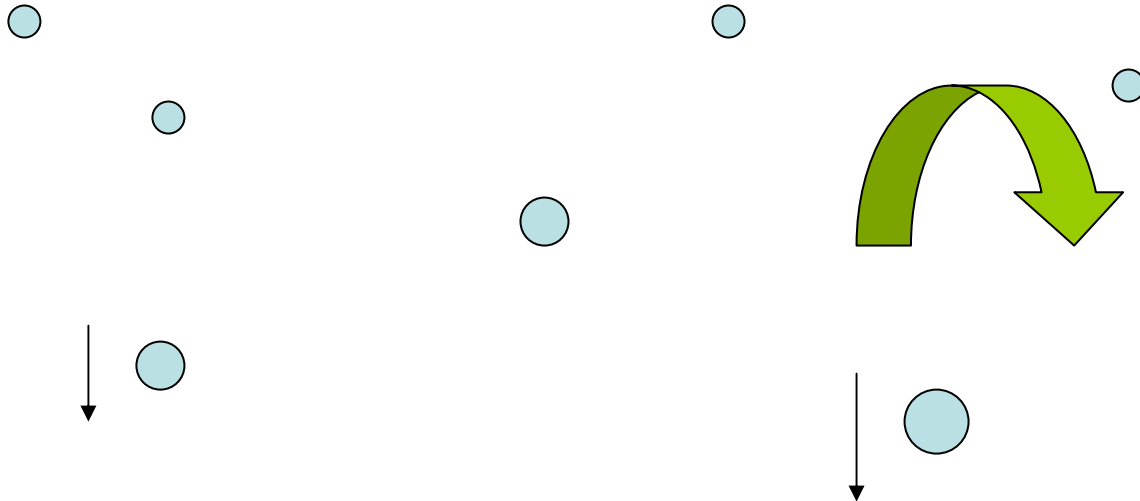
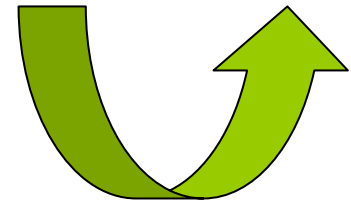
- Experiments at NIF (Livermore) might help
  - Need to use precompressed and cryogenic targets.
- High pressure calibration is a problem!
- The failure of theory at relatively low pressure ( $\sim 0.5$  Mbar) needs to be better understood
- But some reason for optimism on the timescale of the next big influx of information- the Juno mission (launch in 2011, arrival in 2016)

**Helium** Raindrops form at ~ million atmospheres (15000km depth)....

**Neon** partitions into the droplets,

**Argon** does not

Observations now agree with quantum mechanical calculations







## Sequestration of Noble Gases in Giant Planet Interiors

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The Galileo probe showed that Jupiter's atmosphere is severely depleted in neon compared to protosolar values. We show via *ab initio* simulations of the partitioning of neon between hydrogen-helium phases that the observed depletion can be explained by the sequestration of neon into helium-rich droplets within the postulated hydrogen-helium immiscibility layer of the planets interior. We also demonstrate that this mechanism will not affect argon explaining the observed lack of depletion of this gas. This provides strong indirect evidence for hydrogen-helium immiscibility in Jupiter.

DOI: [10.1103/PhysRevLett.104.121101](https://doi.org/10.1103/PhysRevLett.104.121101)

PACS numbers: 96.30.Kf, 31.15.es, 64.75.Bc, 96.15.Kc

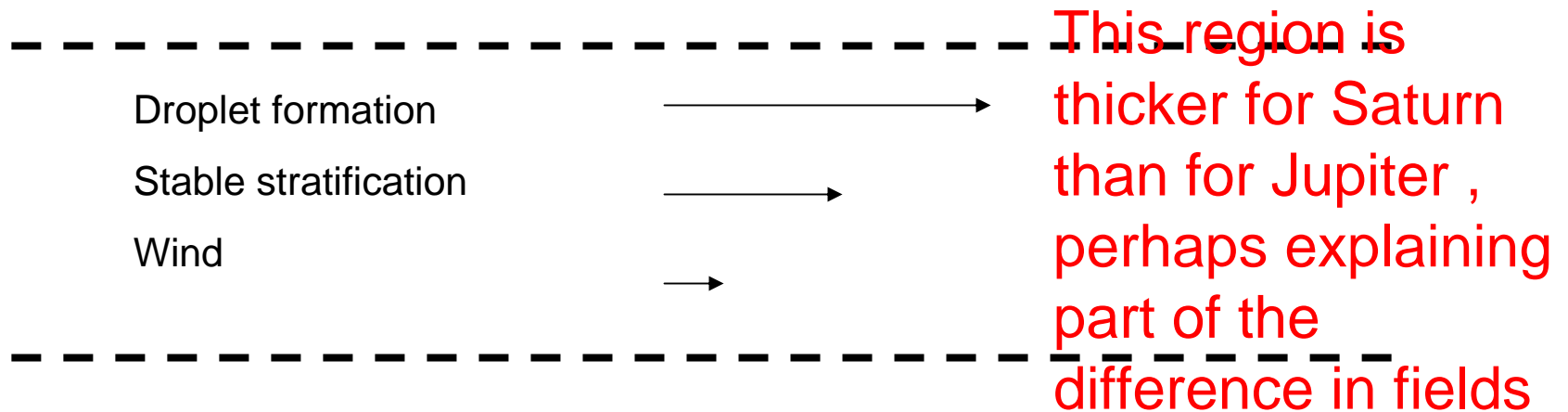
## NOBLE GASES in JUPITER

Neon is a Jupiter thermometer.. The observed depletion requires a temperature of  $\sim 5000\text{K}$  at the raindrop formation location

He	10% depletion	Insolubility
Ne	Factor of $\sim 10$ depletion	Partitioning into He raindrops
Ar, Kr, Xe	Factor of $\sim 3$ enrichment	Sticky

# ELECTROMAGNETIC SKIN EFFECT

Field with reduced dipole tilt



Field with dipole tilt

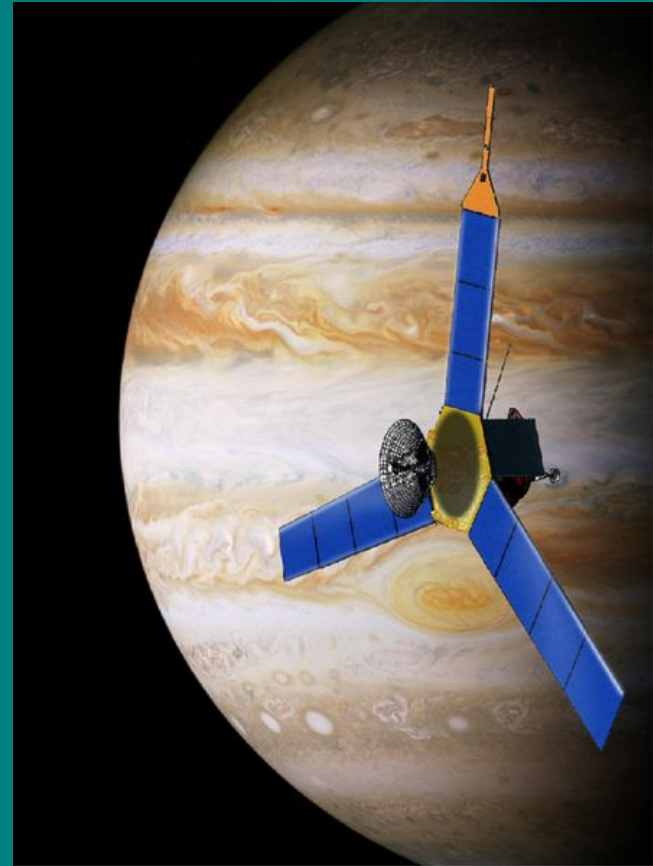
QuickTime™ and a  
TIFF (Uncompressed) decompressor  
are needed to see this picture.

Spin- axisymmetrization of Saturn's magnetic  
field may also be indirectly a consequence of  
helium rain-out

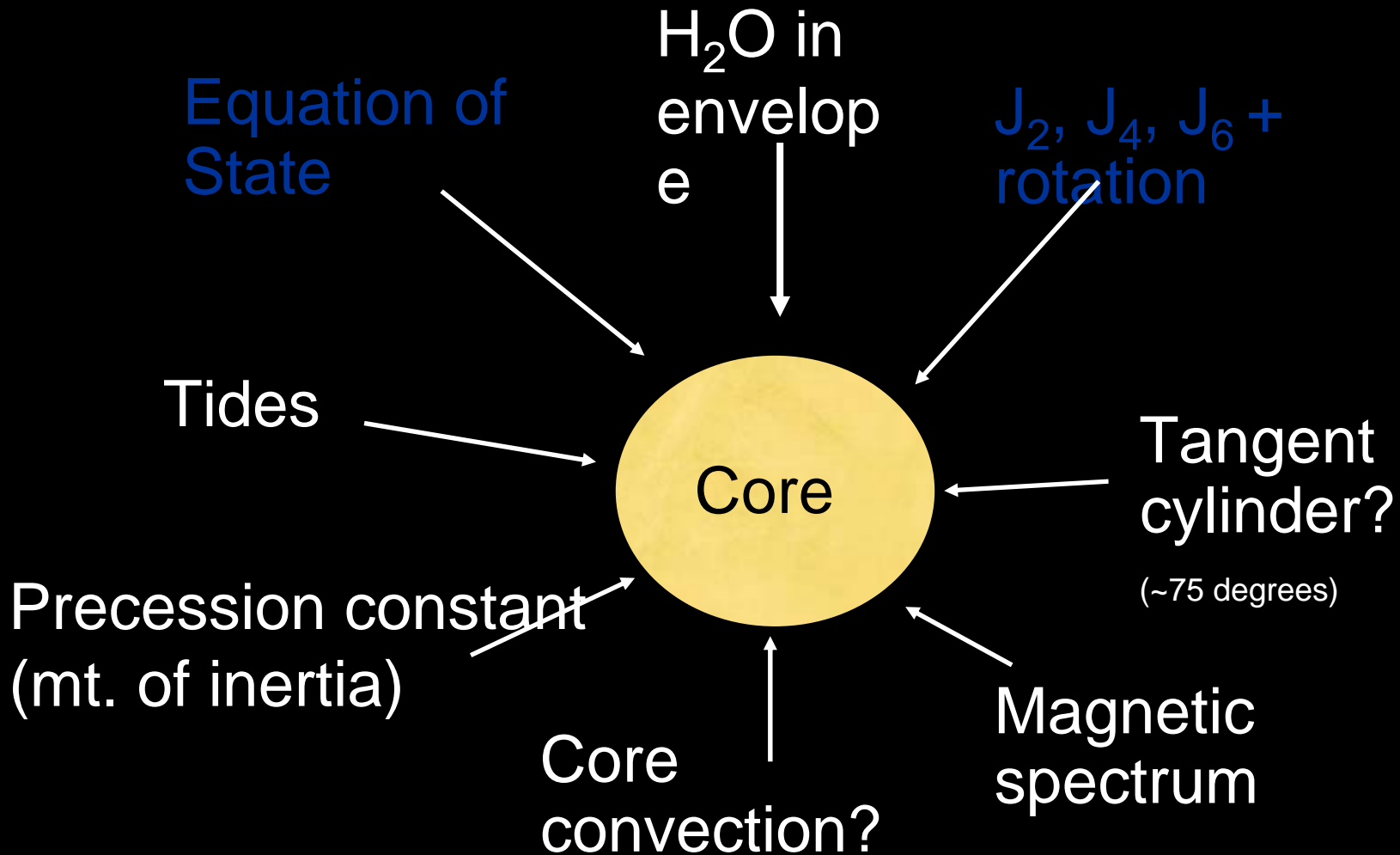
Stanley, GRL, 2010

# Juno

- Launch in 2011, arrive in 2016
- Microwave sounding..  
Mainly to find water
- Exquisitely accurate determination of gravity and magnetic field



Determination of Core Existence/Mass:  
Juno Approach



# Why U&N Matter

- Essential part of understanding planetary origin and evolution.
  - “Naked” Jupiter and Saturn cores
  - Formed in presence of nebula (since contain some gas)
  - Exist in other planetary systems
- Distinctively different! Magnetic fields are dominated by  $(l,m) = (2,0)$  and  $(1,1)$ 
  - Not isentropic? Some stable stratification

## Cosmogonical Considerations Regarding Uranus

A. G. W. CAMERON

*Center for Astrophysics, Harvard College Observatory and Smithsonian Astrophysical Observatory,  
Cambridge, Massachusetts 02138*

Received September 13, 1974

The cosmogony of Uranus is discussed within the context of a picture in which solid condensed materials accumulate to form a large body, which then acquires significant amounts of gas from the primitive solar nebula. Of prime cosmogonical importance is the tilt of the equatorial plane of the planet and of the plane of the satellite orbits by  $98^\circ$  with respect to the plane of the planetary orbit. The tilt of the planet can easily occur as a result of a major collision during the formation process; it seems most likely that the tilt of the satellite orbits requires that they were formed from a gaseous disc rotating about the planet after the tilt of the planetary rotational axis had occurred. Possible methods for tilting this gaseous disc are discussed. A strong early magnetic field may have helped in this and may have played an essential role in slowing down the spin of the planet to the present observed value. These processes may have produced significant compositional differences between the satellites of Uranus and those of Jupiter and Saturn.



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## Observed parameters

Parameter	Uranus	Neptune
Mass ( $10^{29}$ g)	0.868	1.024
Equatorial radius (km)	$25,559 \pm 4$	$24,764 \pm 20$
Rotation period (hrs)	$17.24 \pm 0.01$	$16.11 \pm 0.05$
$J_2 \times 10^6$	$3516 \pm 3$	$3538 \pm 9$
$J_4 \times 10^6$	$-31.9 \pm 5$	$-38 \pm 10$
Mean density (g/cc)	1.27	1.64

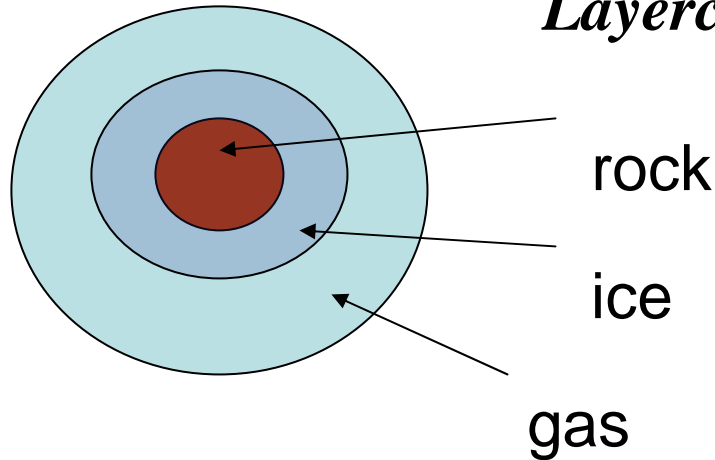
These are uncertain  
(especially for Neptune)

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Much higher than Saturn....Sufficient to infer a large amount of elements heavier than H and He

## *Layercake Model for U or N*

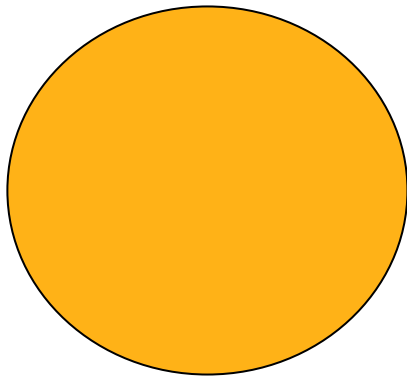


This model fails to give the right  $J_2$  (moment of inertia is too small).

This model also fails to give the right heat flow... too much heat after 4.5 Ga.

May also not give the right magnetic field?

*Fully mixed Model for U&N ....**Not ridiculous a priori because ice , rock and gas may mix in all proportions at high P and T and the energy of accretion is sufficient to mix it up***



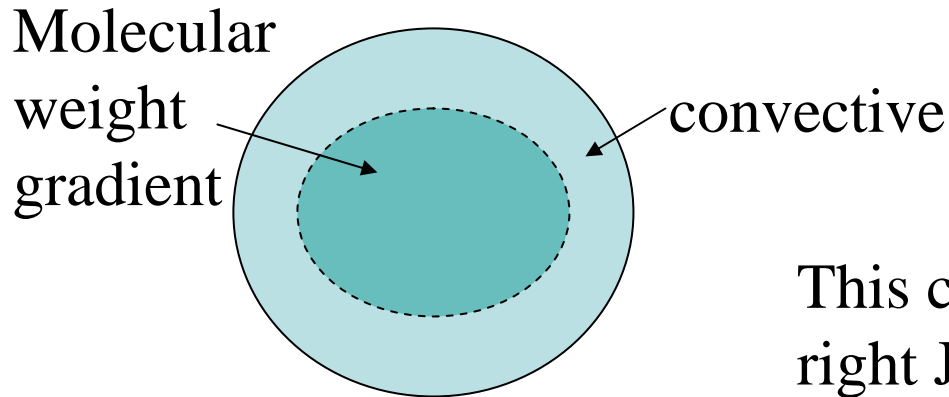
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This model also gives wrong deep atmosphere (even after allowing for cloud formation).

May also not give the right magnetic field?

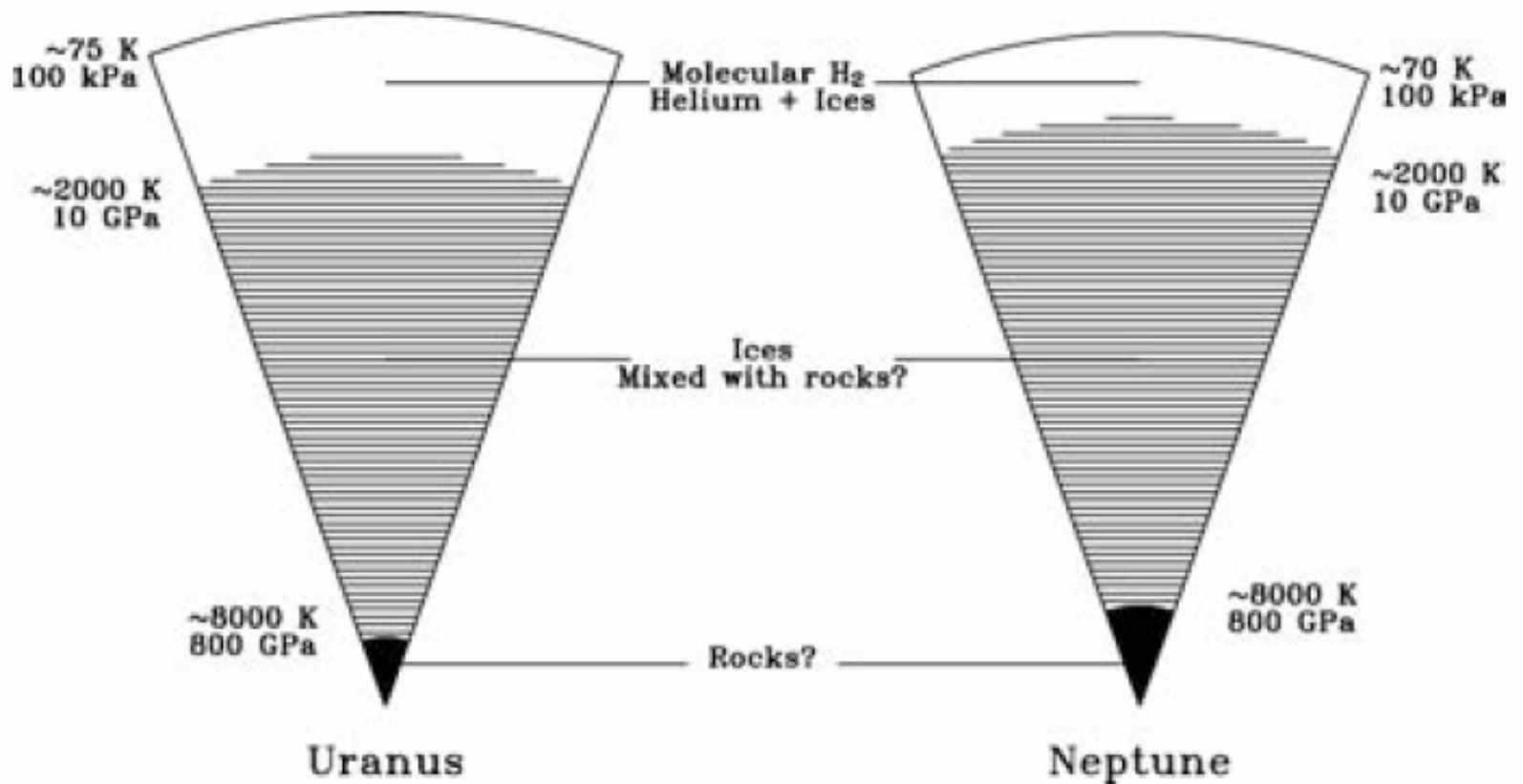
## *The “Correct” Model?*



This can be adjusted to get the right  $J_2$ . It has a gravitational energy  $\sim -0.79GM^2/R$

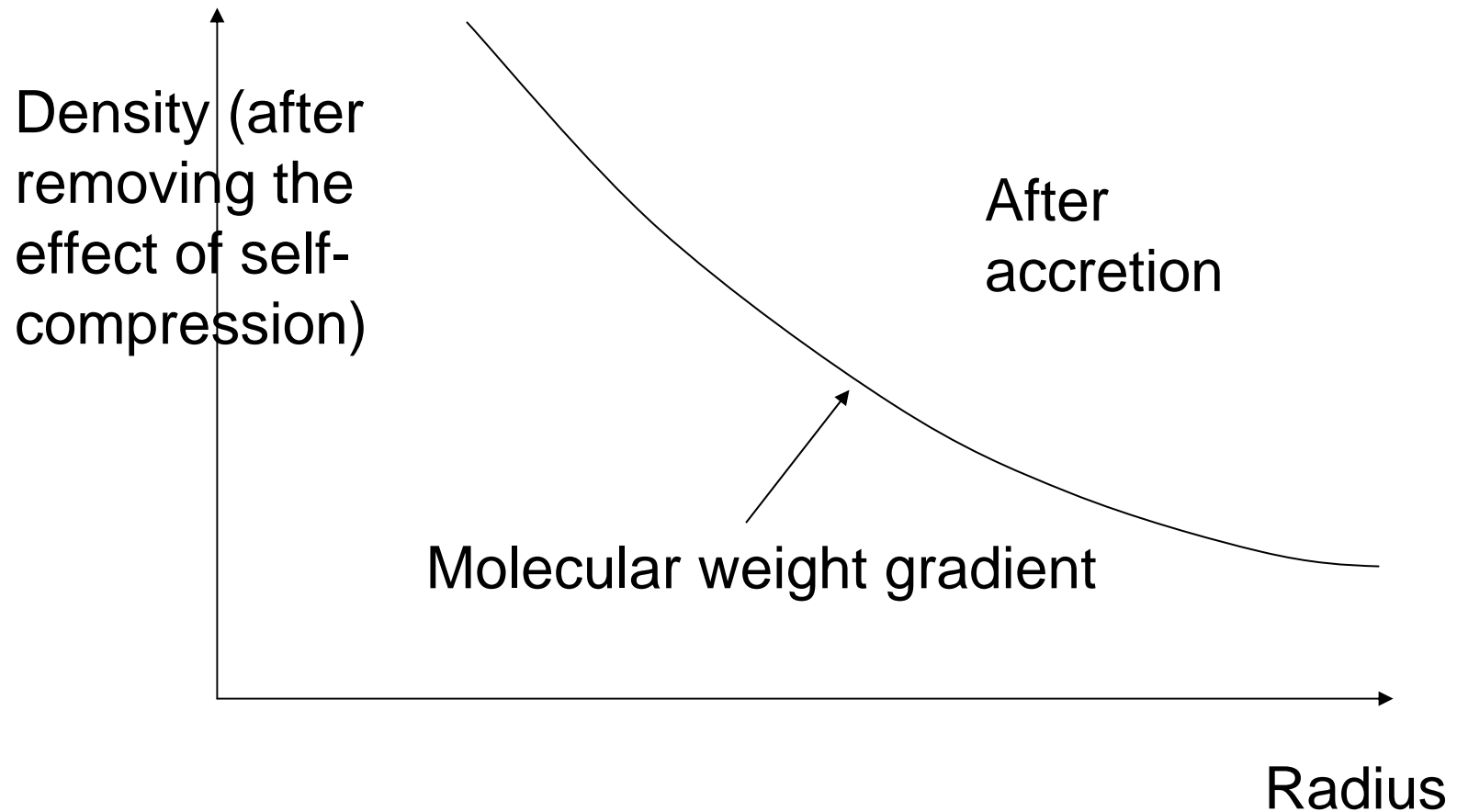
This can also be adjusted to get the right heat flow (assuming the heat from the deeper region is unable to escape.. Deep U & N are very hot!.....over 10,000K)

This may also give an distinctive environment for the dynamo.. a shell bounded below by a non-convecting but fluid, convective deeper region.



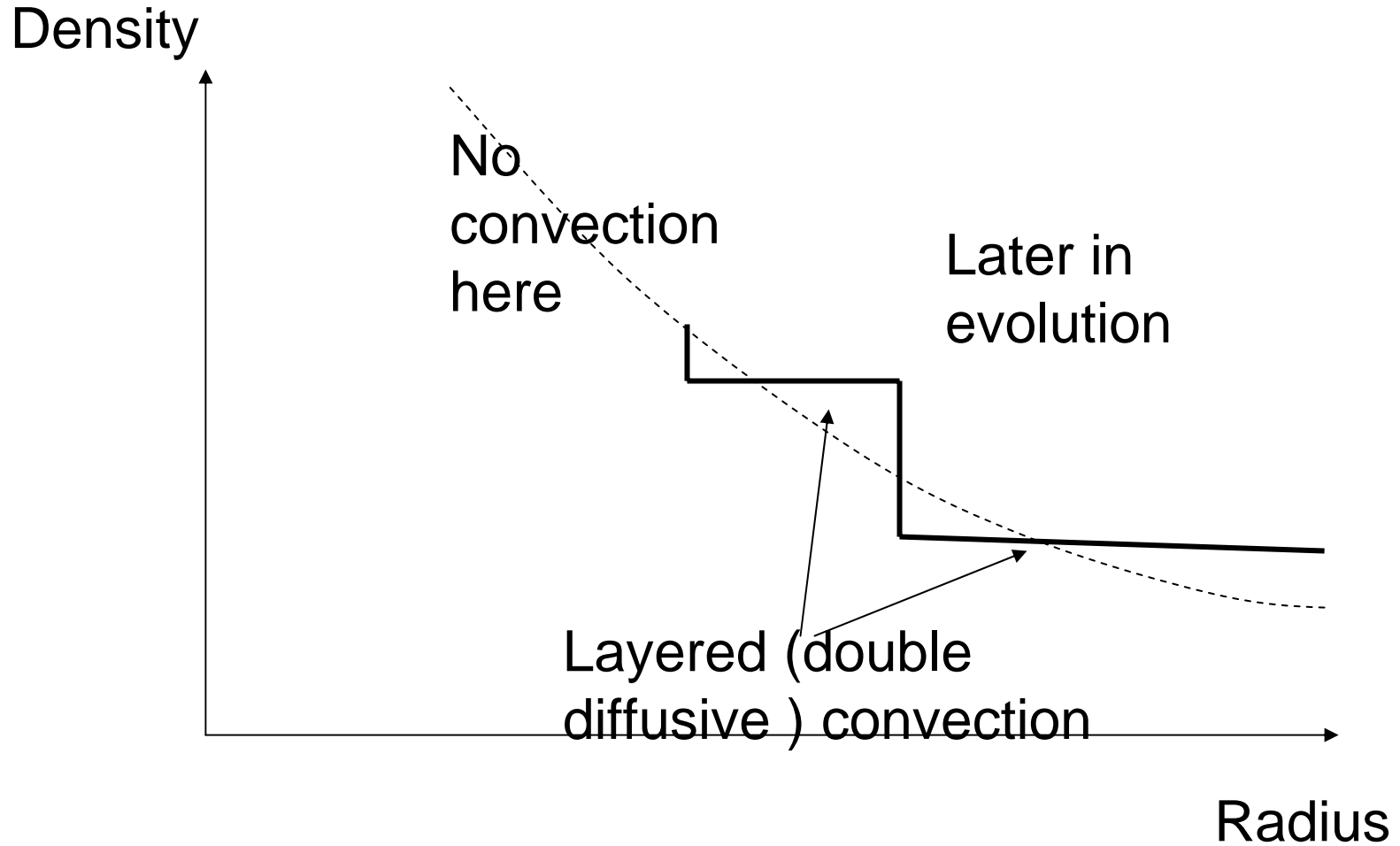
**Figure 9** Schematic representation of the interiors of Uranus and Neptune. Adapted from Guillot 1999b.

# What is a plausible scenario?

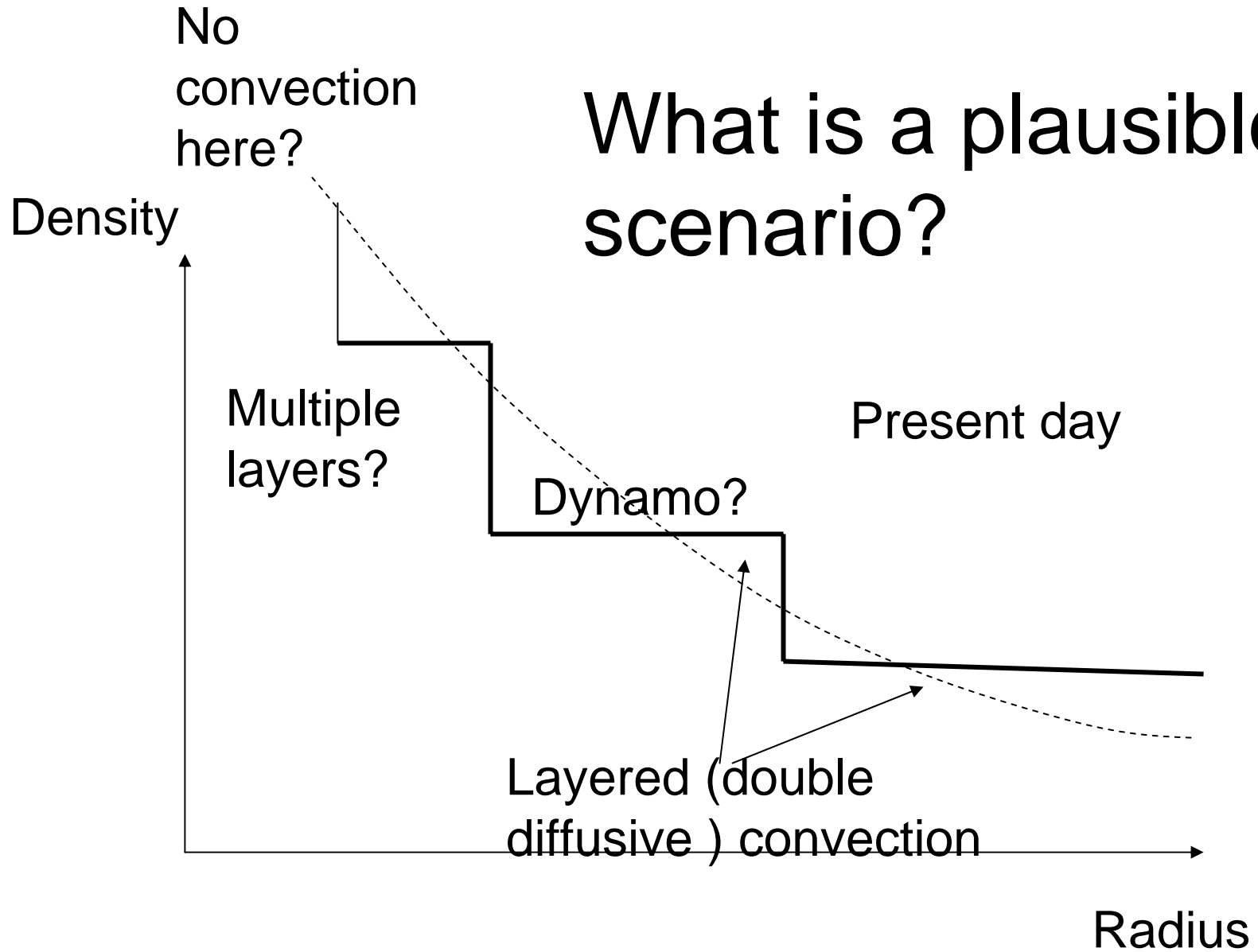




# What is a plausible scenario?



# What is a plausible scenario?



# Main Conclusions

- Our planets can tell us about things that are beyond anything you could hope to learn outside our solar system
- Jupiter and Saturn have cores
- But the picture is not a simple one. The “core” is messy. Uranus and Neptune indicate this.
- Role for traumatic events? (giant impacts, embryo merging)

# Future Work

- Hydrogen Equation of state.
- Thermodynamics of mixtures
- Juno & Probes.
- More realistic accretion models including orbital migration (the argon problem), etc.
- Uranus and Neptune!

“Measure what is measurable, and make measurable what is not so.”

-Galileo Galilei



The End

