

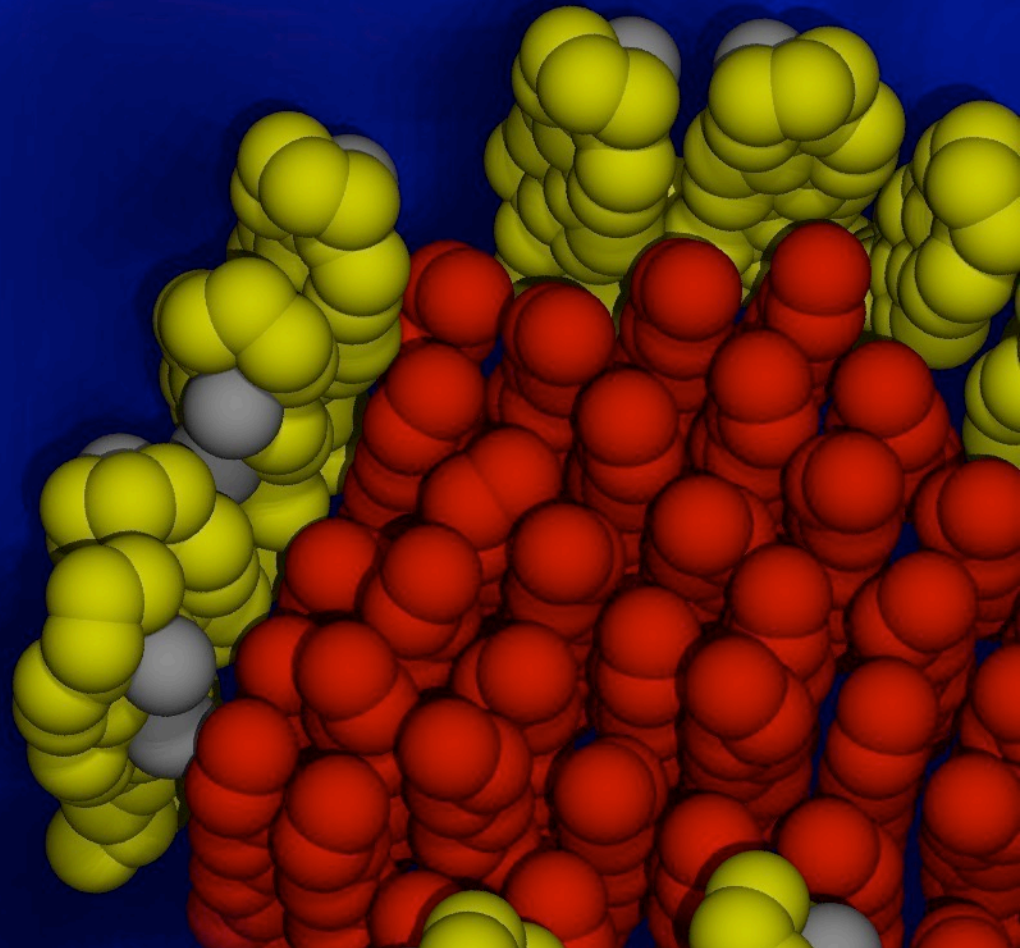
Surface viscosity and subdiffusion in membrane simulations

Ed Lyman

*Dept of Physics and Astronomy and Dept of Chemistry and
Biochemistry, Univ of Delaware*

KITP FILMS21

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Viscosity is a *fundamental concept* in membrane biology — Here's why!

Homeoviscous adaptation (Sinensky):¹

Cells actively regulate lipid *composition* in order to maintain membrane fluidity

Why?

Viscosity controls the rates of events in membranes, such as diffusion of electron carriers in respiration²

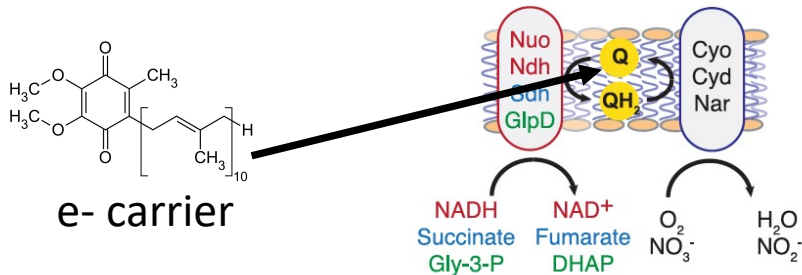
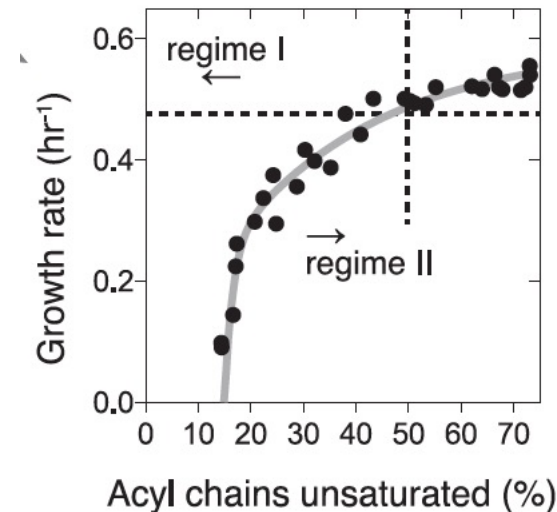


TABLE 2. *The viscosity of E. coli lipid extracts from cells grown at different temperatures*

Temperature of growth (°C)	Temperature of measurement (°C)	τ (nsec)	η (poise)
15	15	2.8	1.8
30	30	2.7	1.9
37	37	2.6	1.8
43	43	2.7	2.0
43	15	13.8	15



[1] Sinensky *PNAS* 71:522(1974)

[2] Budin et al, *Science* 362:1186(2019)



Viscosity is a *fundamental concept* in membrane biology — Here's why!

Homeoviscous adaptation (Sinensky):¹

Cells actively regulate lipid *composition* in order to maintain membra

Increasing chain unsaturation



Why?

Viscosity controls the rates of events in membranes, such as diffusion of electron carriers in respiration²

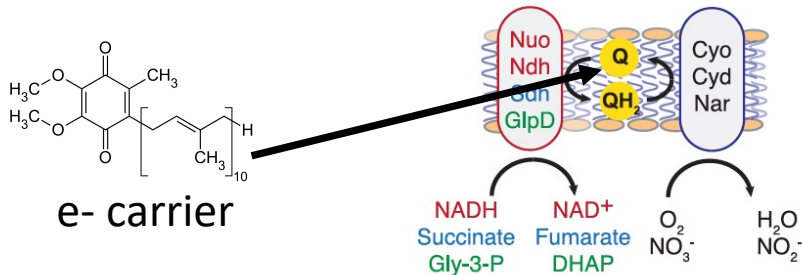
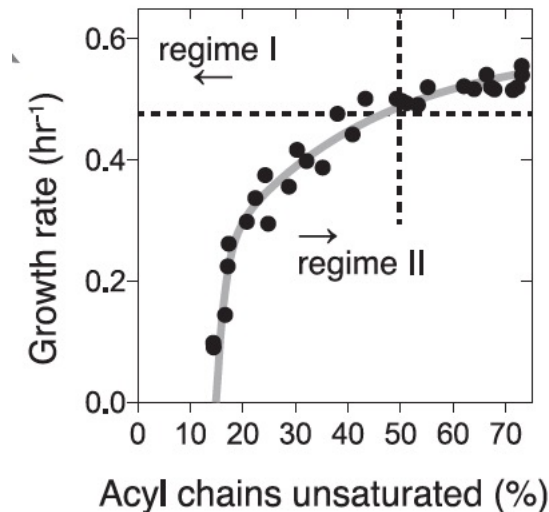


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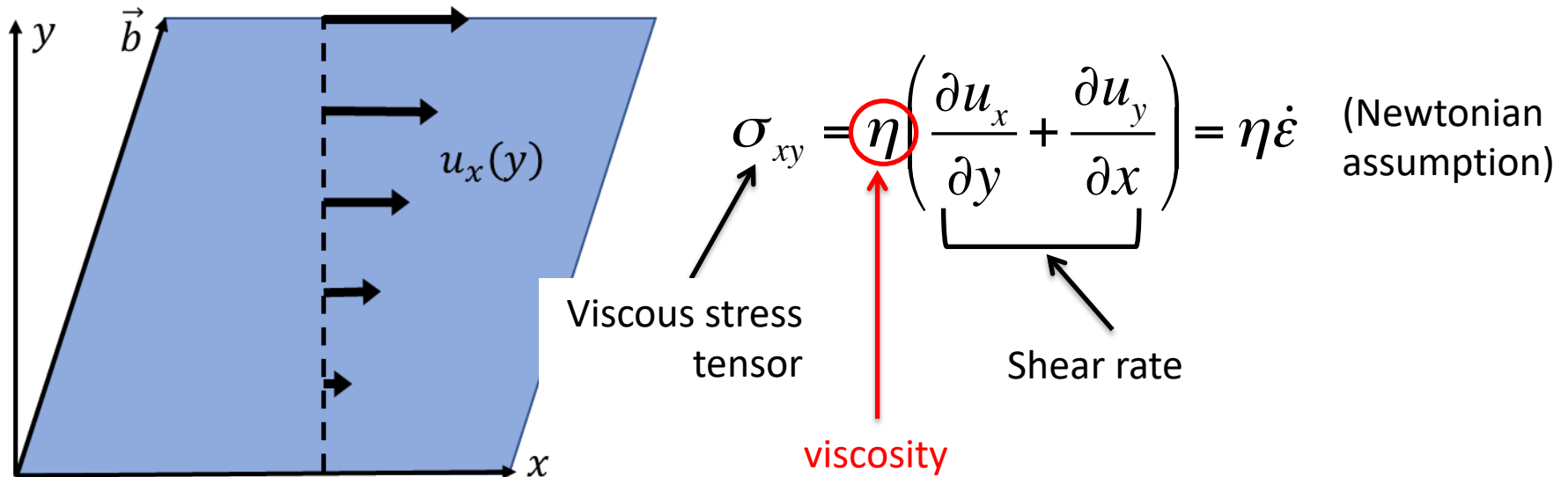
Outline

- Lipid viscosities obtained by a nonequilibrium method, non-Newtonian behavior at high shear
- (Lots of) viscosities obtained from equilibrium fluctuations
- Subdiffusion in the L_o phase, and some rampant speculation



Shear viscosity: Definition and units

Consider a simple fluid subjected to a shearing deformation, resulting in a velocity gradient:



Units:

In 3D: $[\sigma_{xy}] = \frac{[\text{Force}]}{[\text{area}]}$



$[\eta] = \frac{[\text{force}][\text{time}]}{[\text{area}]}$

$[\dot{\epsilon}] = [\text{time}]^{-1}$

In 2D: $[\sigma_{xy}] = \frac{[\text{Force}]}{[\text{distance}]}$



$[\eta] = \frac{[\text{force}][\text{time}]}{[\text{distance}]}$

Shear viscosity of some alkanes and aliphatic alcohols

Carbons	Alkanes	Alcohols
4		2.5*
6	0.2*	
8	0.386	3.5*
10	0.5*	
12	1.06	9.0*
14	1.0*	
16	2.1	9 or 27

- Units are cP
- Aliphatic alcohols are about 9x more viscous than the corresponding alkane
- Hexadecanol comparison is complicated by higher melting temp (50 C) and inconsistency in the literature. One source says 53 cP at 75 C. Another says 9 cP at 53 C.

Consider a thin (4-5 nm) slab of 16 carbon chains: $(h) \times (\eta_{\text{hex}}) = \eta_{\text{m}}$

This would give a surface viscosity for DPPC of $4.5 \times (10)^{-11}$ Pa-m-sec

(Multiply by 10^3 to get P-cm)

*from Yamaguchi, *JCP* 146:094511(2017) at 25 C

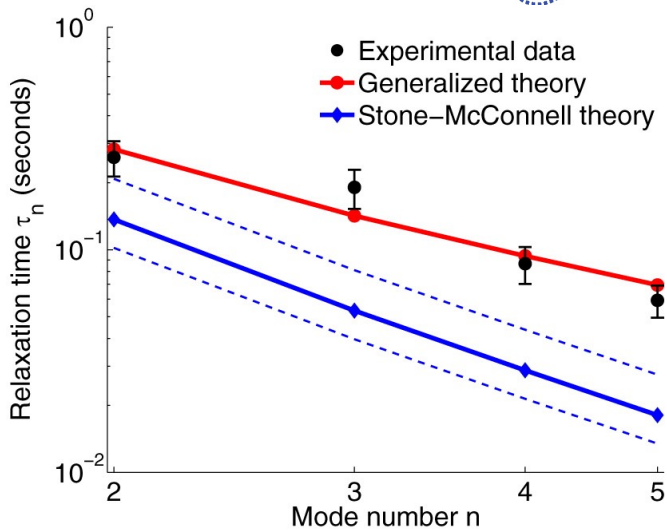
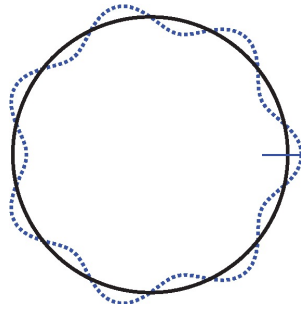
*from (sources cited in) Venable, Krämer, Pastor *Chem Rev* 119:5954(2019)



Membrane viscosity: Some experimental numbers

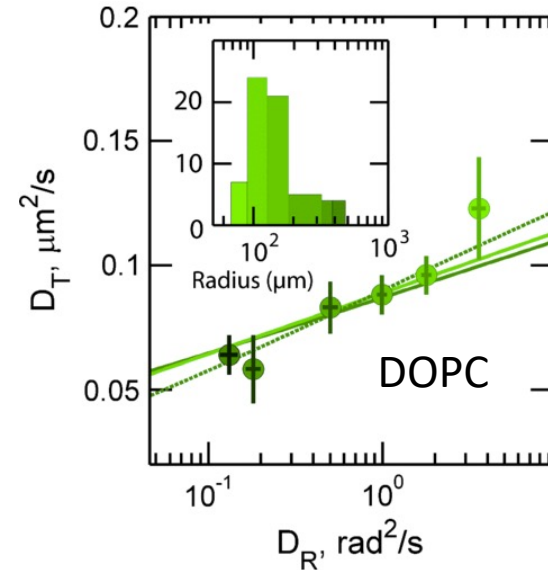
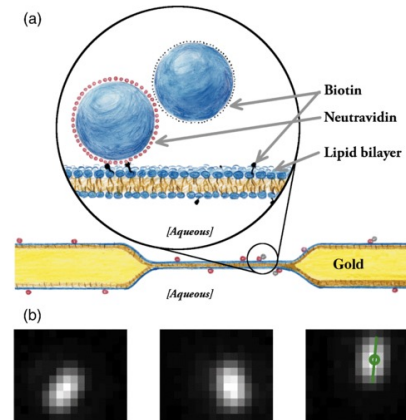
Domain flicker spectroscopy:

DPPC:DiPhy:chol



$$\eta = 4 \times 10^{-9} \text{ Pa} \cdot \text{m} \cdot \text{sec}$$

Fits to SDHPW:



^aBLM, DOPC:

$$\eta = (15.9 \pm 2.3) \times 10^{-9} \text{ Pa} \cdot \text{m} \cdot \text{sec}$$

^bGUV, L₀ phase:

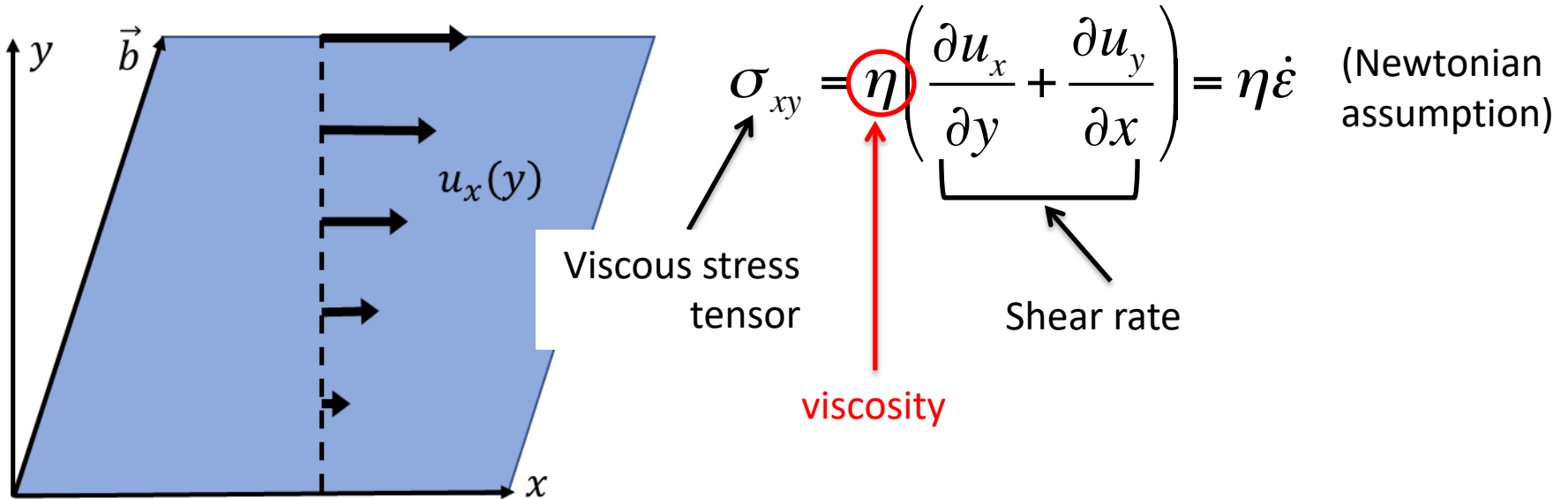
$$\eta = (5 - 10) \times 10^{-9} \text{ Pa} \cdot \text{m} \cdot \text{sec}$$

[a]Hormel...Parthasarathy PRL 112:188101(2014)

[b]Cicuta, Keller, Veatch J Phys Chem B 111:3328(2007)



Measuring surface viscosity of lipid forcefields: NE box deformation protocol



The protocol for surface viscosity:

- Apply a box deformation to achieve diff shear rates
- Average P_{xy}

Stress tensor obtained from pressure (virial) tensor

$$\sigma_{xy} = -\langle P_{xy} \rangle$$

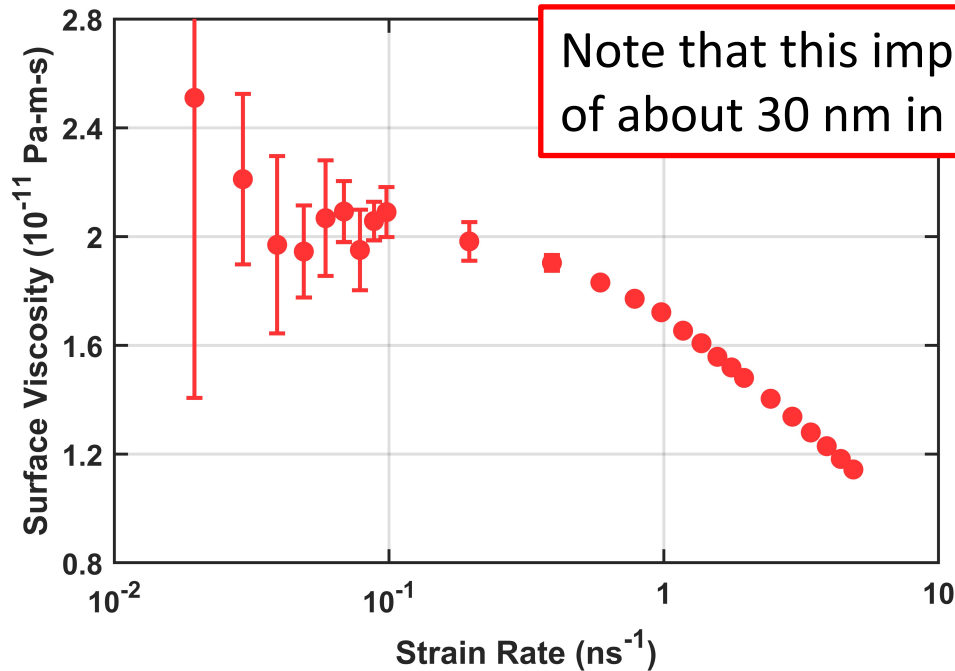


Martini DPPC Shear Viscosity

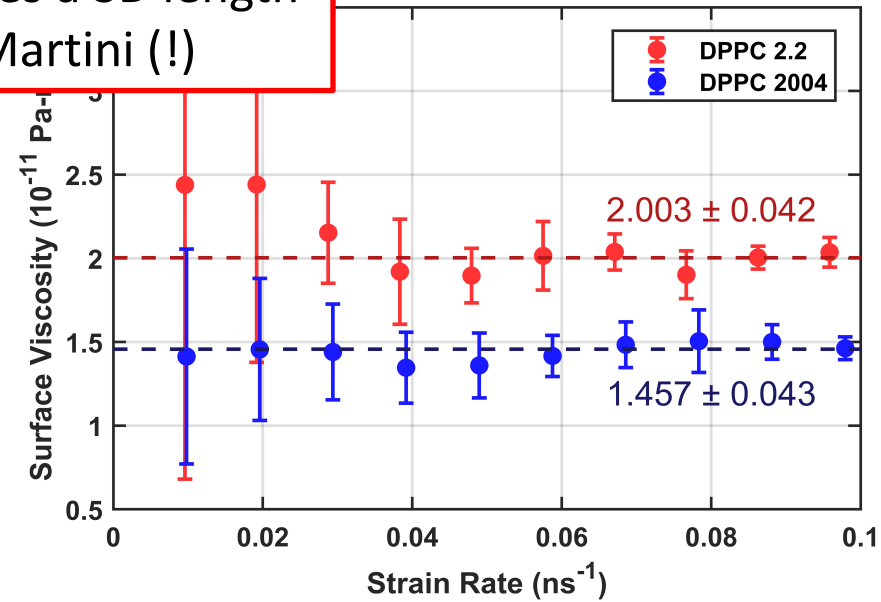


Andrew Zgorski

- Surface viscosity depends on Martini version
- Values are (nearly) in agreement with earlier report by den Otter (1.2×10^{-11}) for v. 2004
- Value for v.2.2 is in agreement with ind calc using Einstein relation: $(2.23 \pm 0.21) \times 10^{-11}$



Note that this implies a SD length of about 30 nm in Martini (!)

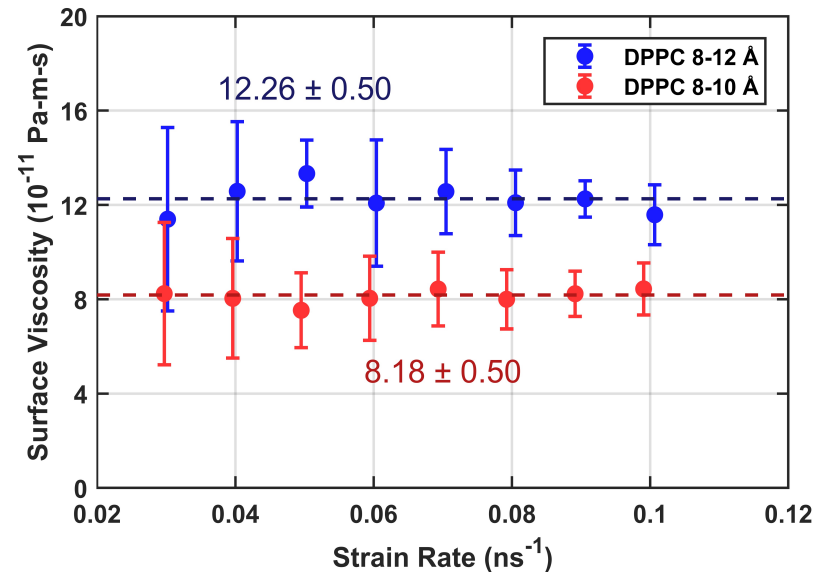
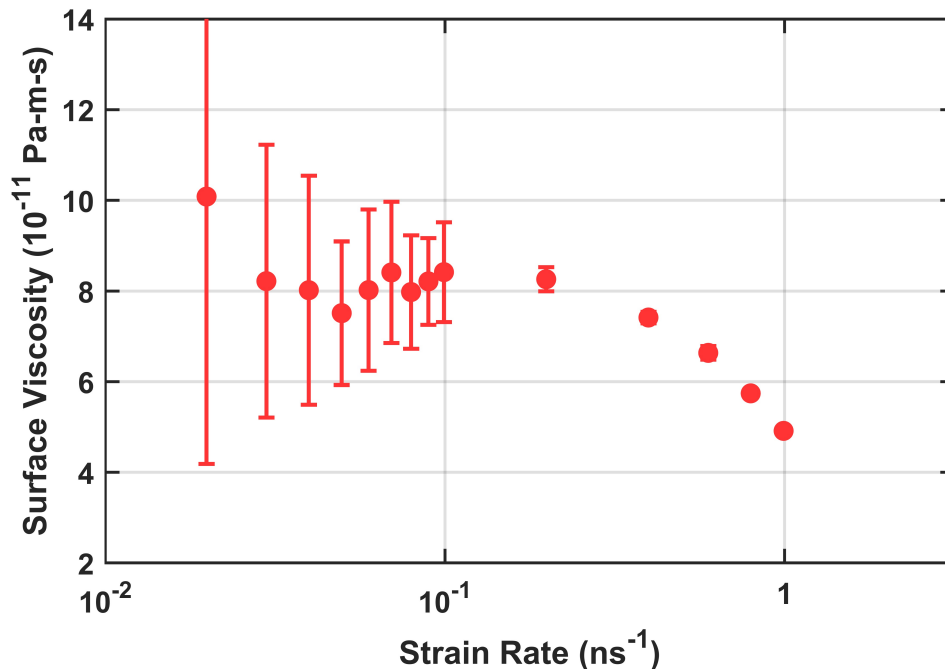


- 10 x 10 nm membranes, 10 replicas run for 10 usec in NPT, then system rescaled to the average box size and equilibrated under NVT
- 820 nsec production runs, 3 runs at each strain rate



C36 (all-atom) DPPC Shear Viscosity

- Surface viscosity depends on LJ cutoff (ca. 50% difference)
- Simulated values ($8-12 \times 10^{-11}$ P-cm) are below expt. values by a factor of 200 or so. (oi)



- 10 x 10 nm membranes, relaxed and rescaled to the average box size and equilibrated under NVT for 10 nsec
- $\langle P_{xy} \rangle$ converged to < 1.5 bar after 20 nsec
- 5 x 25 nsec production runs to obtain visc at ea. strain rate



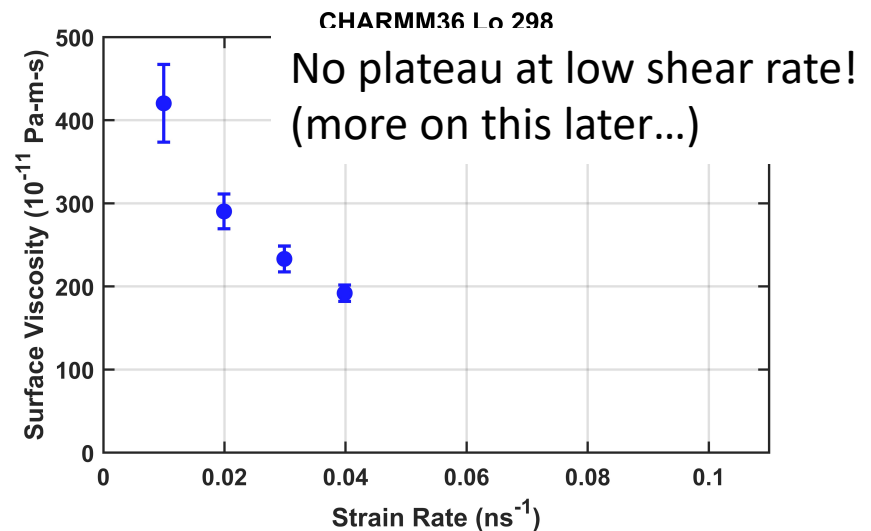
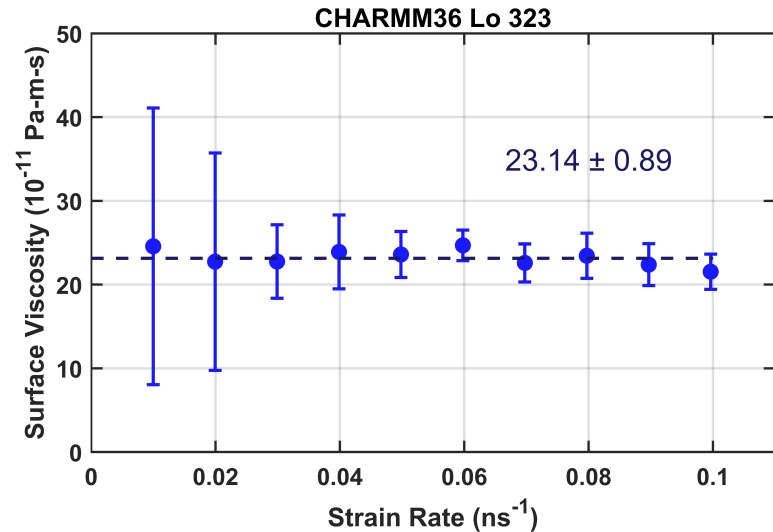
All-atom lipids: A surprise for cholesterol rich membranes

$T_{sim} = 323$

$T_{sim} = 303$

$T_{sim} = 323$

Membrane Composition	Surface Viscosity (10^{-11} Pa-m-s) = (10^{-8} P*cm)
DPPC (8-10)	8.18 ± 0.50
DPPC (8-12)	12.26 ± 0.50
DOPC (8-12)	19.68 ± 0.69
PSM (8-12)	48.8 ± 1.2
L_o (8-12)	23.83 ± 0.92 (T = 323K)
L_o (8-12)	??? (T = 298K)
L_d (8-12)	9.39 ± 0.47 (T = 323K)
L_d (8-12)	40.6 ± 1.0





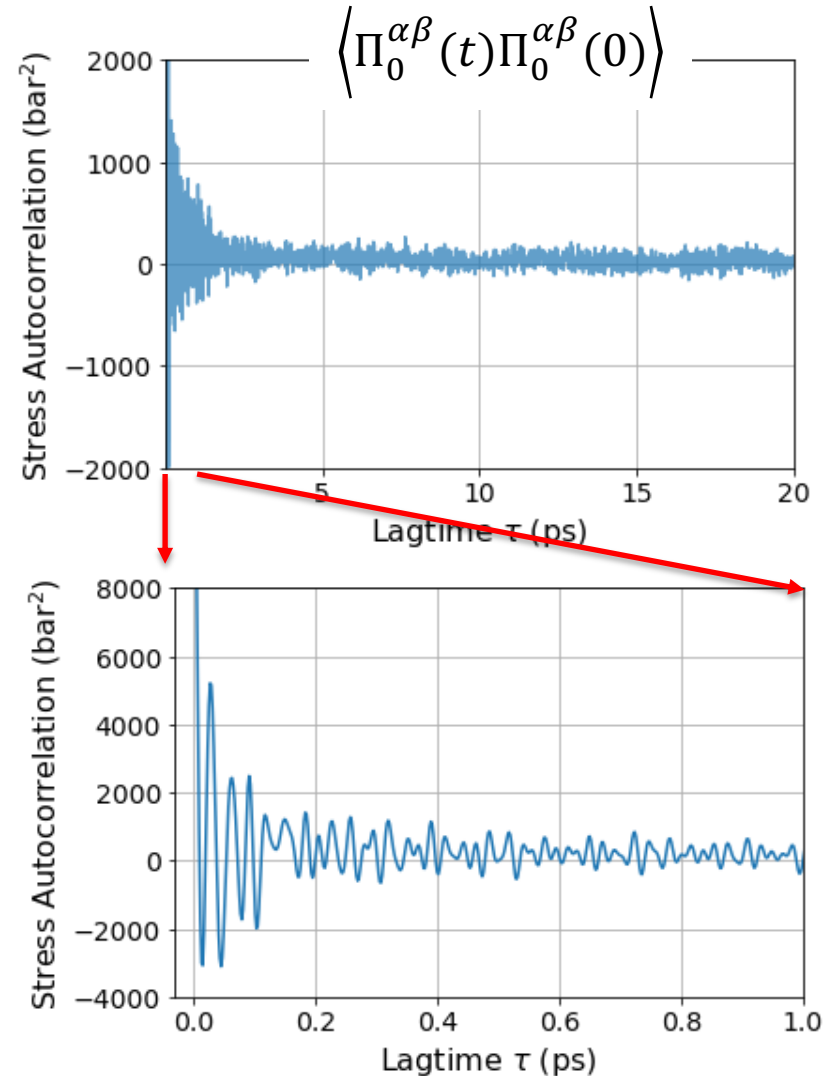
An equilibrium protocol. Or, how to blow a bunch of cycles chasing a number

A Green-Kubo relation for shear viscosity:

$$\eta = \frac{\beta}{V} \int_0^\infty \left\langle \Pi_0^{\alpha\beta}(t) \Pi_0^{\alpha\beta}(0) \right\rangle dt$$

Notes:

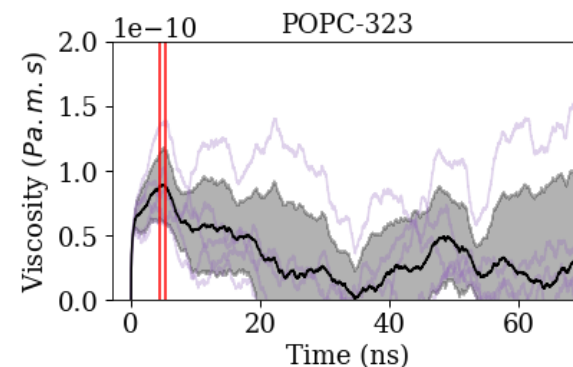
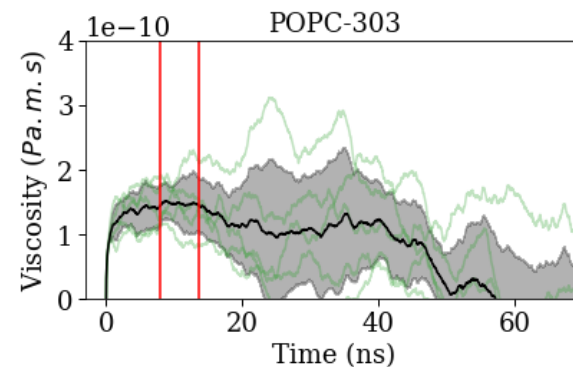
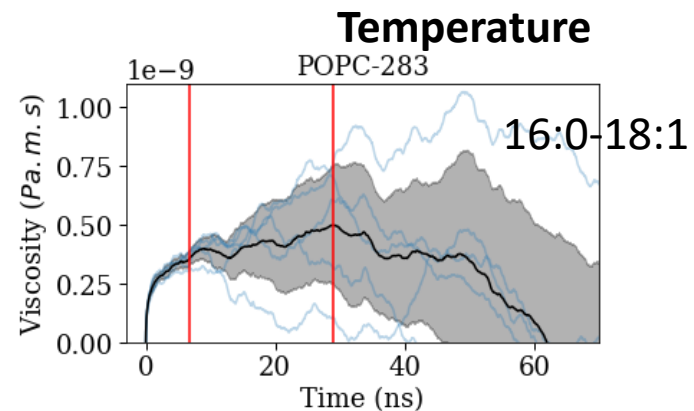
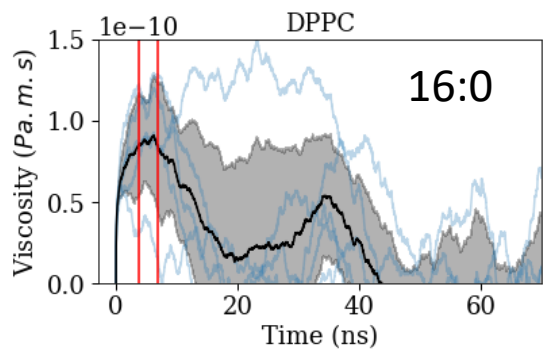
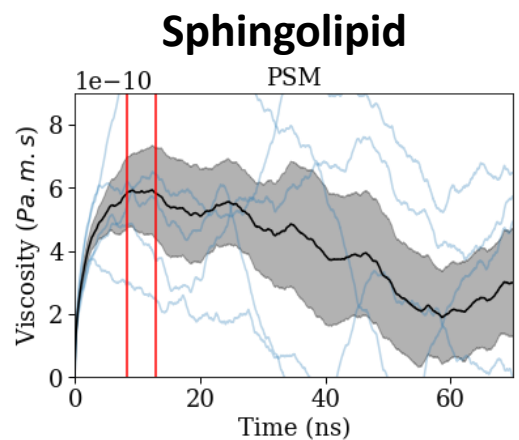
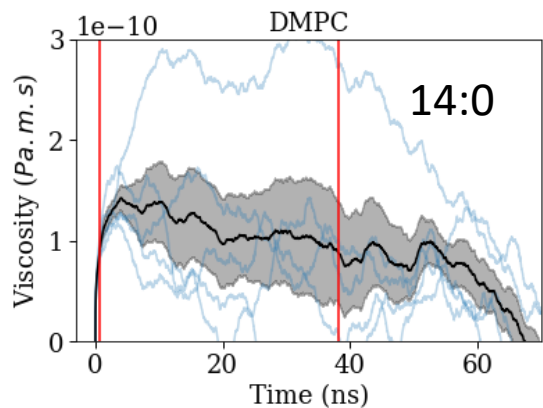
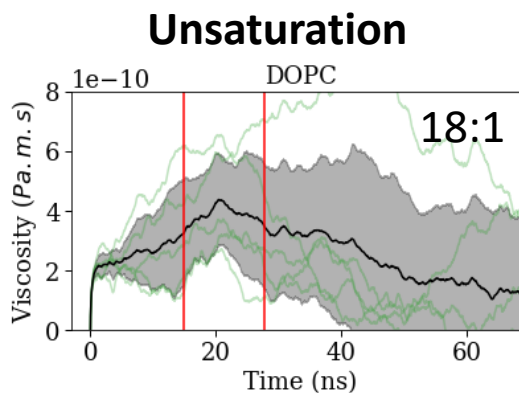
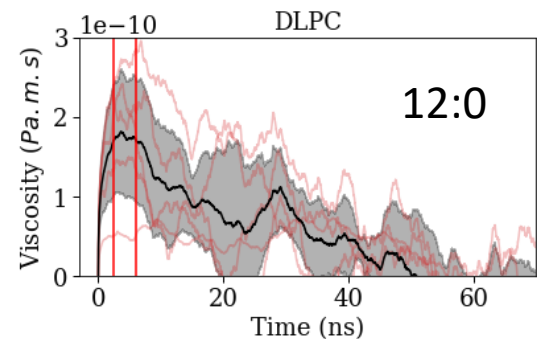
- “0” subscript reminds us that we have taken a $k \rightarrow 0$ limit
- $\Pi_0^{\alpha\beta}$ is the atomic stress tensor here. We use NVT conditions to avoid artifacts
- To get membrane surface viscosity, α, β in the plane and $\alpha \neq \beta$.
- We get $\Pi_0^{\alpha\beta}$ from the pressure tensor, so from G-K we get the system viscosity (membrane + water)





G-K integrals

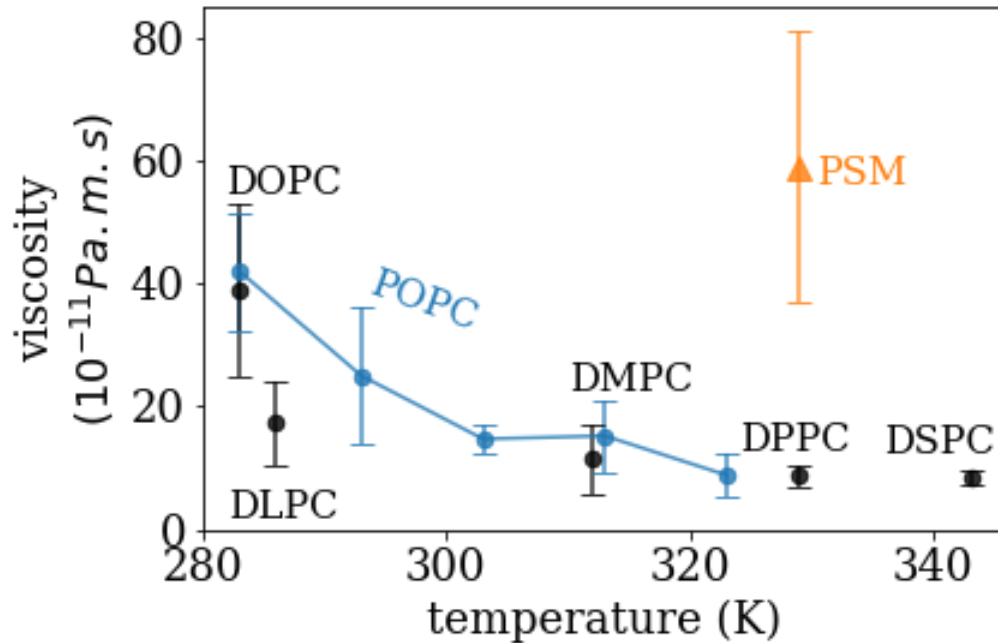
Chain length



Shea Fitzgerald and EL, unpublished



Equilibrium viscosity results, summary



Lipid	T_m	T_{sim}	η (10^{-11}) Pa-m-sec
DLPC 12:0	271	286	17.3 ± 6.8
DMPC 14:0	297	312	11.4 ± 5.7
DPPC 16:0	314	329	8.7 ± 1.7
DSPC 18:0	327	343	8.5 ± 1.1
DOPC 18:1	256	283	39 ± 14
PSM	314	329	59 ± 22
POPC 16:0-18:1	271	283	42.0 ± 9.6
POPC 16:0-18:1	271	293	25 ± 11
POPC 16:0-18:1	271	303	14.7 ± 2.5
POPC 16:0-18:1	271	313	15.2 ± 5.8
POPC 16:0-18:1	271	323	8.8 ± 3.4

Non Equil results:

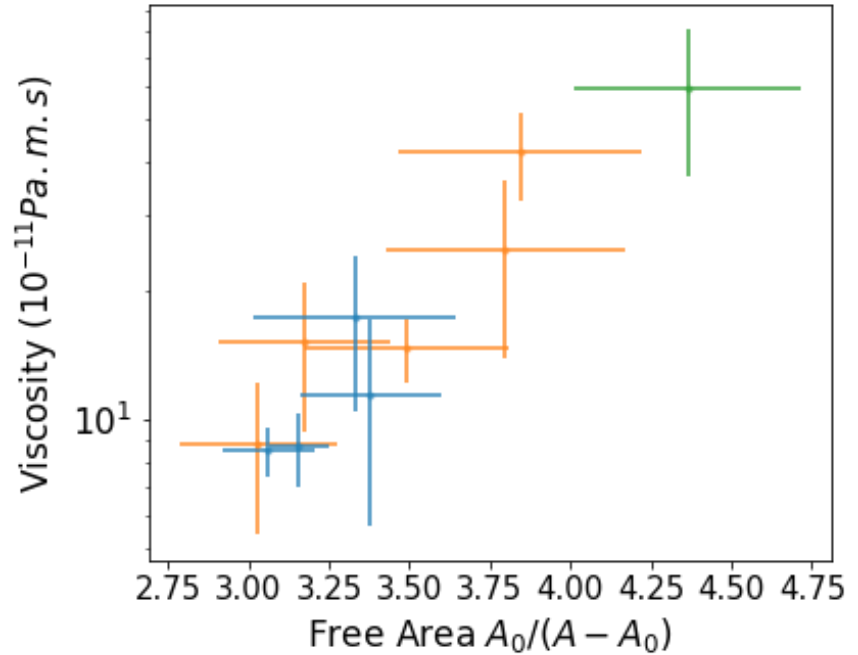
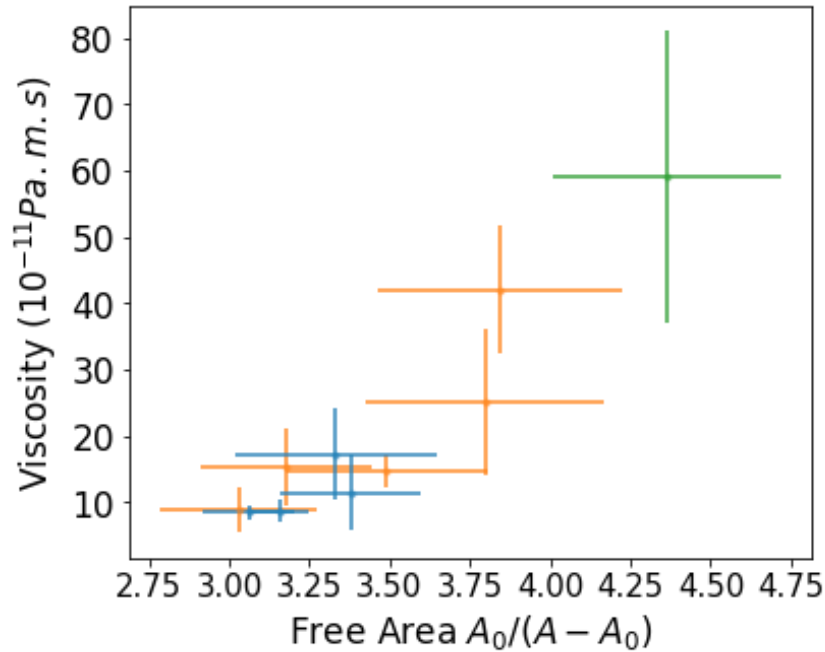
DPPC @ 323: 12.26 ± 0.5

PSM @ 323: 48.8 ± 1.2



Does “free area” explain membrane viscosity?

If the error bars are big enough --- sure!



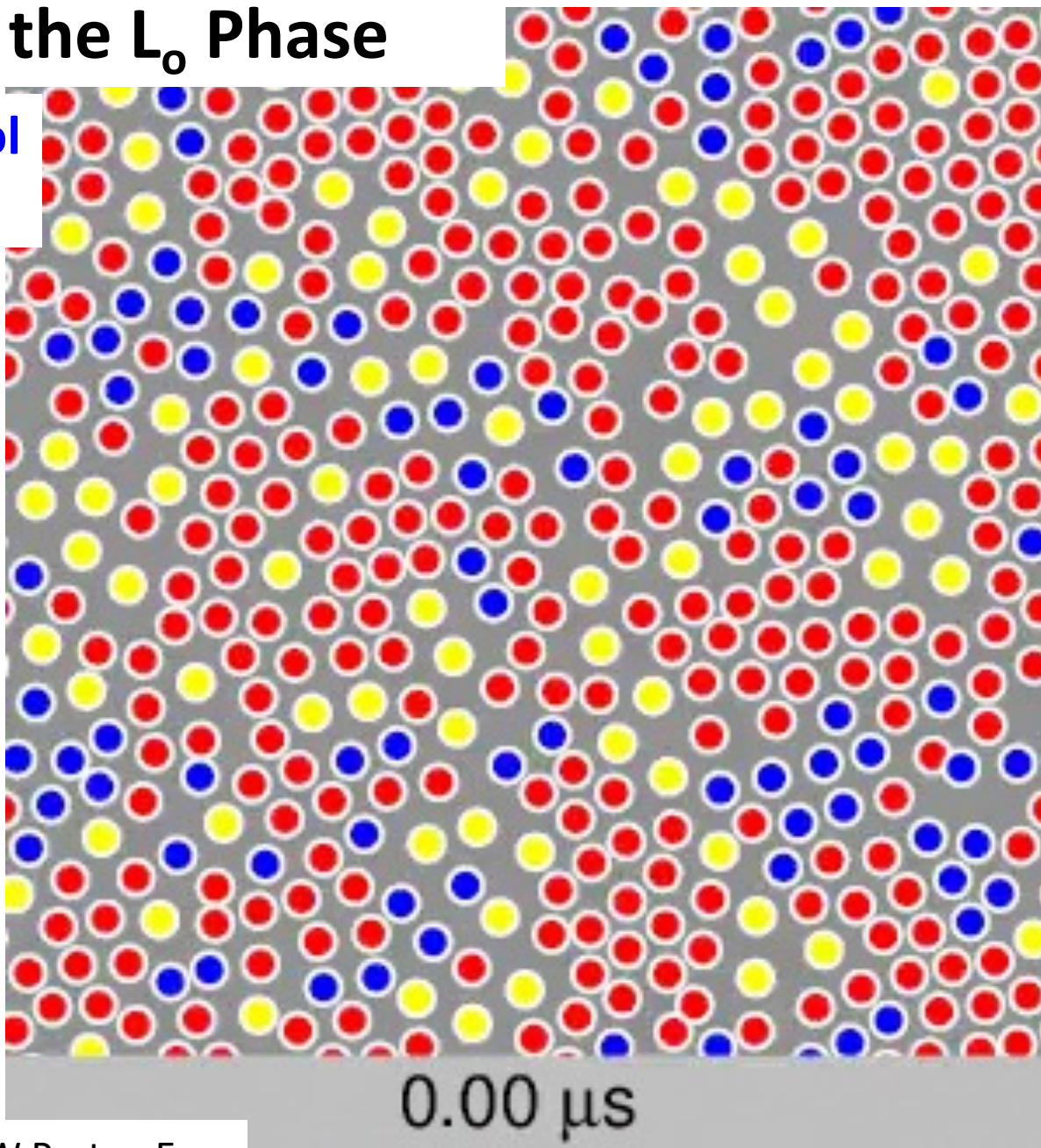


Dynamics of the L_0 Phase

DPPC/DOPC/Chol
0.55/0.15/0.30

Top view, one leaflet
 L_0 phase composition

- **Yellow:** CHOL
- **Blue:** DOPC chain
- **Red:** DPPC chain



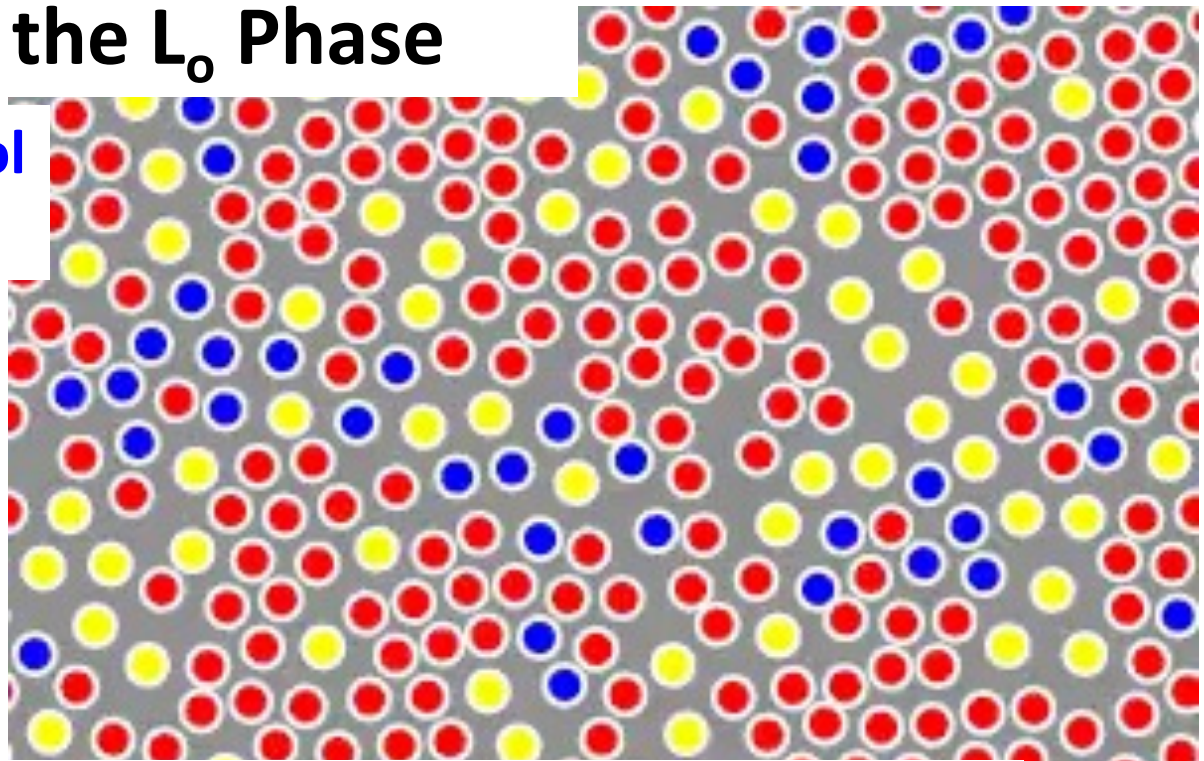


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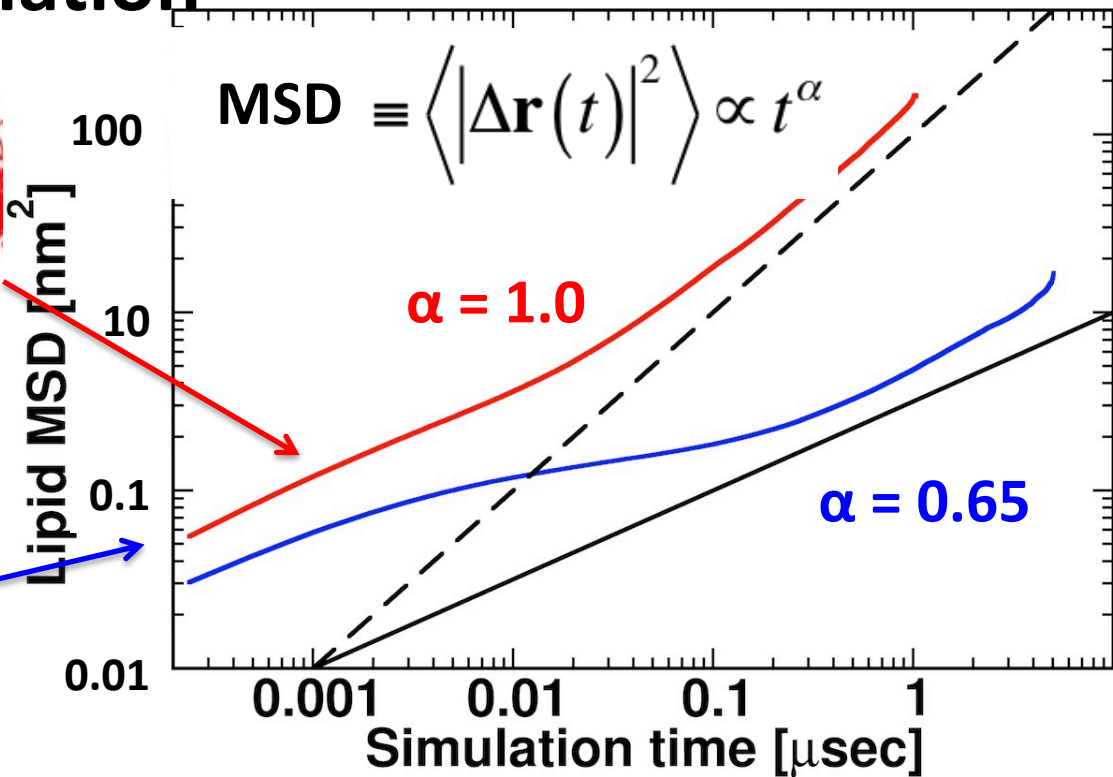
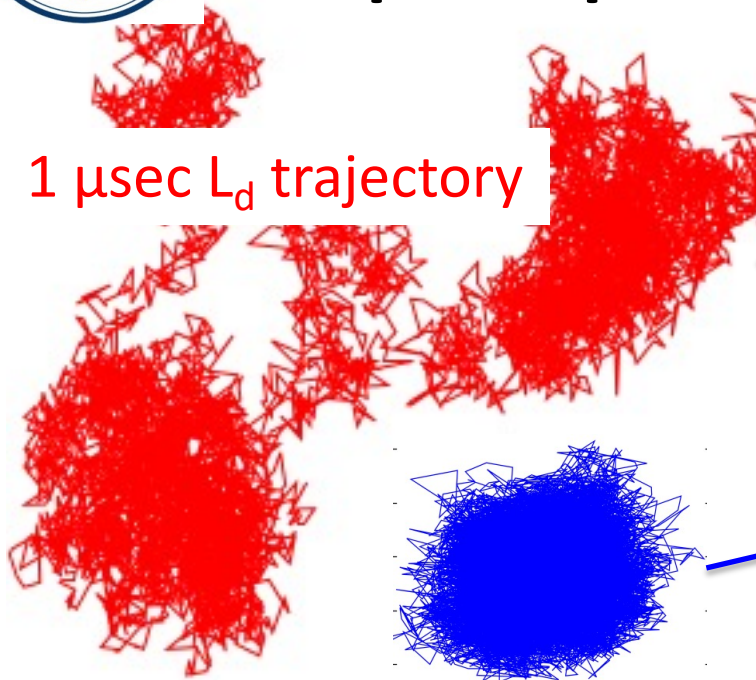
Take home messages:

- L_0 dynamics are slow and collective
- L_0 structure is itself inhomogeneous —
Implication for partitioning?





The turnover to Newtonian behavior: Some rampant speculation

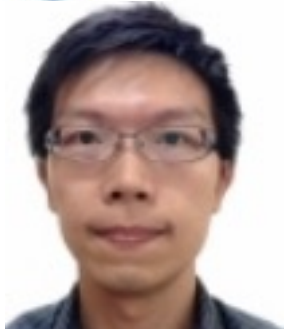


iSCAT SPT of a lipid moving **from L_d to L_o**

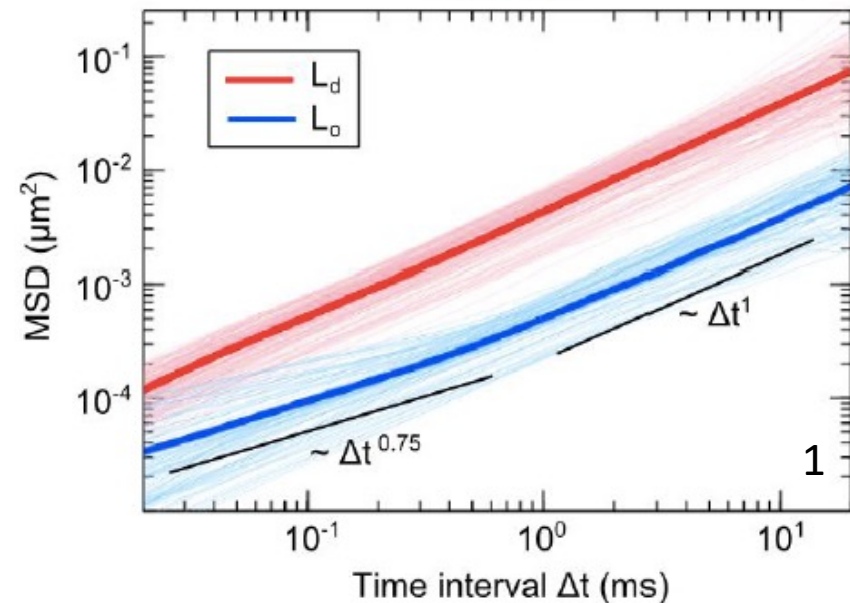
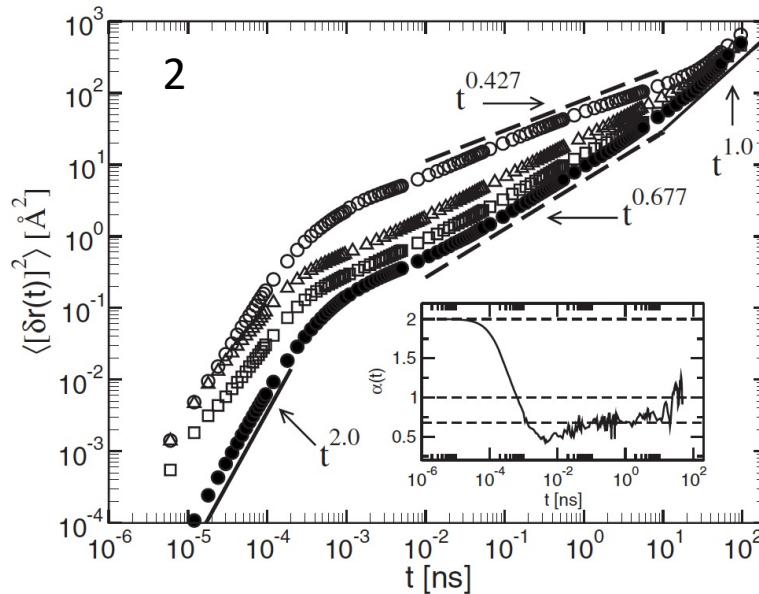
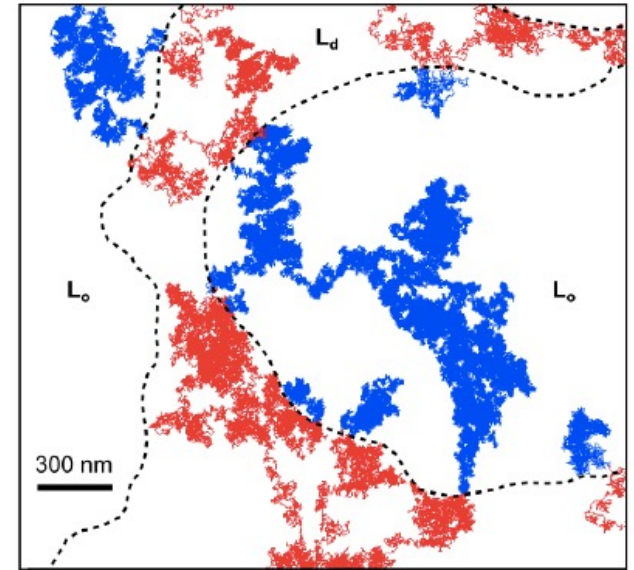
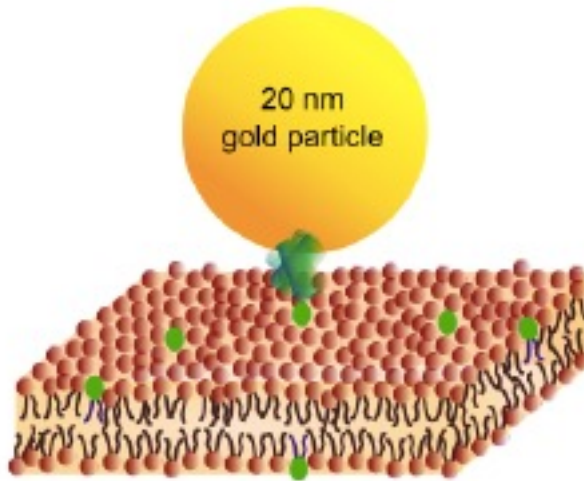
Hsieh et al Optics in the Life Sciences (2015)



Lipid subdiffusion in the L_o phase: iSCAT SPT



Chia-Lung Hsieh,
Academia



[1] Wu, ...Chia-Lung Hsieh *Sci Rep* 2016

[2] Flenner et al, *PRE* 79:011907(2009)



Summary

- Surface viscosities in all-atom simulations are at least 10x lower than experimental measurements --- Why?
- The DPPC/DOPC/Chol L_0 phase at 295 does not plateau at accessible shearing rates — is this a signature of longer timescale elastic to viscous crossover?
- Interpreting lipid diffusion with the PSD yields a lipid hydrodynamic radius of 0.15 nm



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Itay Budin (UCSD)



Shea Fitzgerald

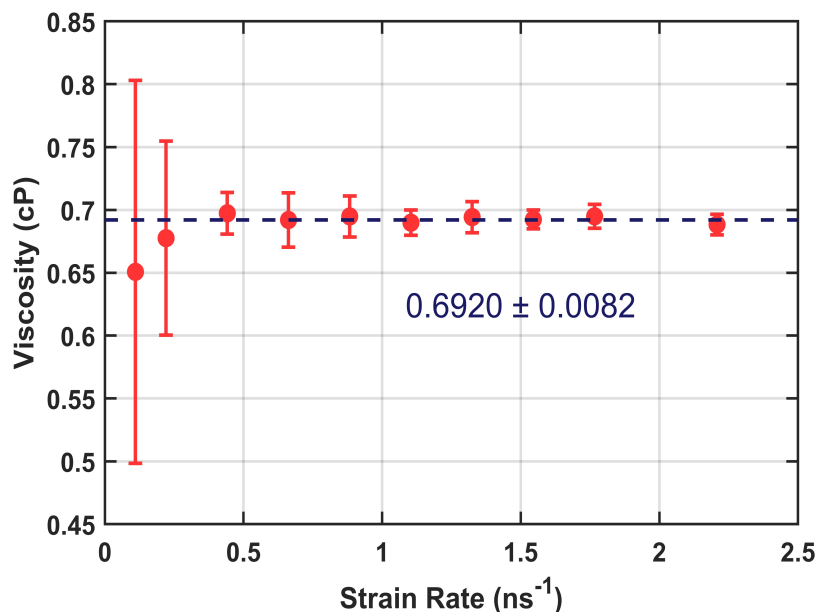


Alison Leonard



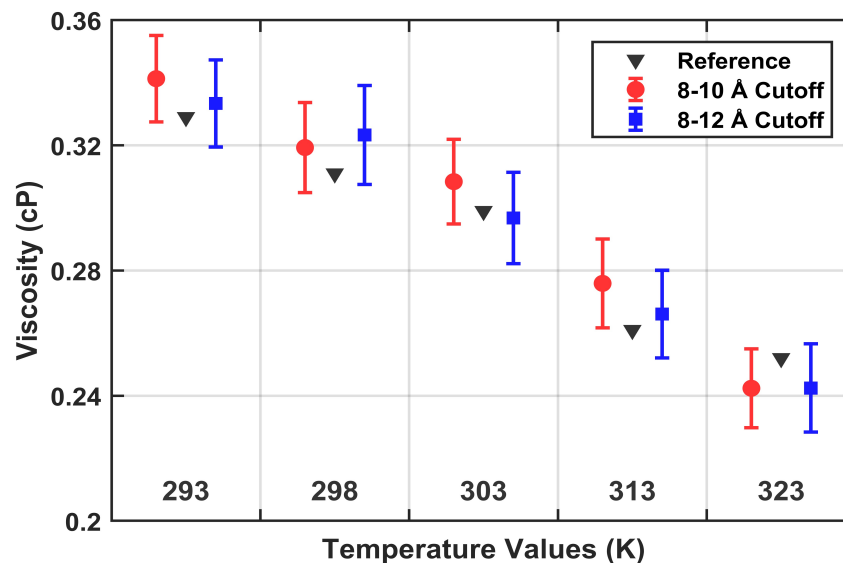
Testing the box deformation protocol

Martini “water”



- 3 independent replicas (420 nsec ea) at each strain rate
- 6100 vdW particles
- Agrees w/ ind. Measurement obtained from Green-Kubo

Tip3p



- 5 independent replicas 12 nsec ea) at each strain rate (0.2-4 nsec⁻¹)
- 4074 waters
- Agrees w/ ind. Measurement obtained from Green-Kubo¹

[1] Venable et al J Phys Chem B 114:12501 (2010)
A Zgorski, R Pastor, EL JCTC 15:6471(2019)



$\alpha < 1$... let me count the ways

The MSD does not fully characterize the probability distribution

$$\delta r^2(t) \equiv \int [\mathbf{r}(t)]^2 P(\mathbf{r}, t) d^2 r$$

There are **at least three** distinct microscopic processes relevant to biology that all yield $\alpha < 1$!!

Fractional Brownian Motion (FBM)



Memory



Viscoelastic Stuff

Continuous Time Random Walk (CTRW)



Long-tailed waiting time distribution



Binding to "traps"

Laplace Process



Fractal support



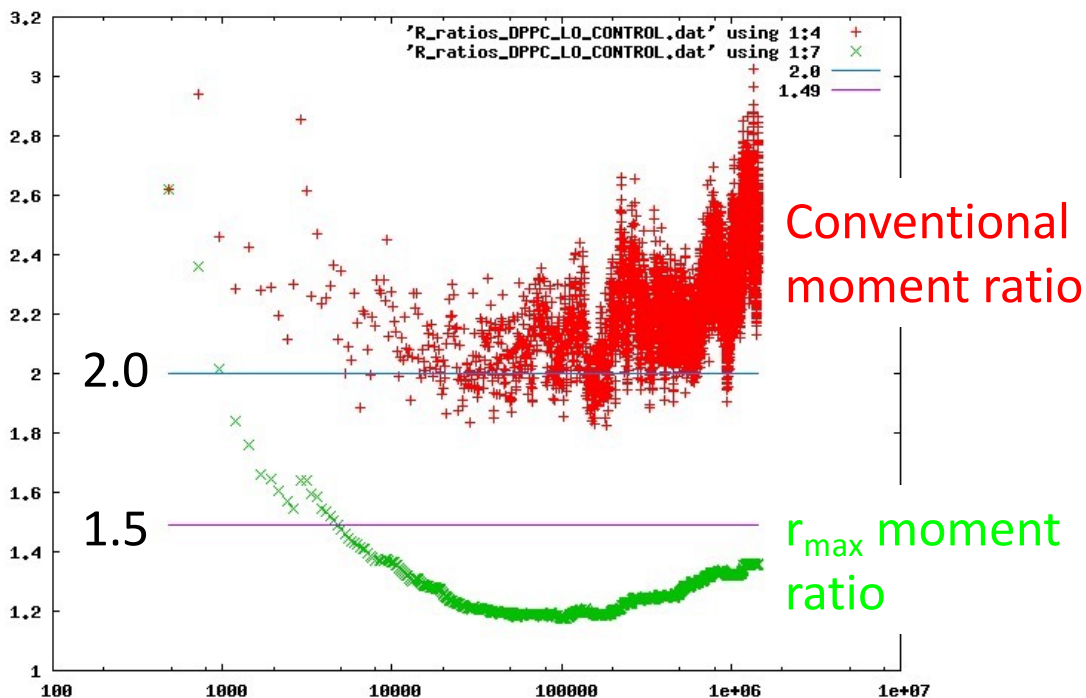
Crowding



Displacement statistics distinguish FBM and CTRW¹

$$\frac{\langle |\Delta \mathbf{r}(t)|^4 \rangle}{\langle |\Delta \mathbf{r}(t)|^2 \rangle^2} = 2 \text{ for FBM (in 2D)}$$
$$> 2 \text{ for CTRW}$$
$$< 2 \text{ for Laplace}$$

$$\frac{\langle |\Delta \mathbf{r}_{\max}(t)|^4 \rangle}{\langle |\Delta \mathbf{r}_{\max}(t)|^2 \rangle^2} < 1.49 \text{ for FBM}$$
$$> 1.49 \text{ for CTRW}$$
$$< 2 \text{ for Laplace}$$



We think that FBM is a signature of the L_0 phase² (on 20 nm lengthscales)

[1] Tejedor et al *Biophys J* **98**:1364(2010)

[2] Jeon et al PRL **109**:188103(2012)



What criteria must a simulation fulfill? A manifesto

A molecular simulation approach should:

- Retain sufficient chemical detail to resolve lipids and membrane proteins
- Be tractable for actin compartment spatiotemporal scales
- Be faithful to the dynamics of membrane lateral transport

How big is big enough?

- For Martini 2.2: $L_{SD} = \frac{2 \times 10^{-8} \text{ P} \cdot \text{cm}}{0.69 \text{ cP}} \cong 30 \text{ nm}$
- For c36: $L_{SD} = \frac{20 \times 10^{-8} \text{ P} \cdot \text{cm}}{0.3 \text{ cP}} \cong 660 \text{ nm}$



What criteria must a simulation fulfill? A manifesto

A molecular simulation approach should:

The image shows the cover of a Biophysical Journal article. The title is "From Dynamics to Membrane Organization: Experimental Breakthroughs Occasion a 'Modeling Manifesto'". The authors are Edward Lyman, Chia-Lung Hsieh, and Christian Eggeling. The journal is Biophysical Journal, and the article is part of the Biophysical Perspective series. The Biophysical Society logo is also visible.

Biophysical Journal
Biophysical Perspective

Biophysical Society

**From Dynamics to Membrane Organization:
Experimental Breakthroughs Occasion a “Modeling
Manifesto”**

Edward Lyman,^{1,2,*} Chia-Lung Hsieh,³ and Christian Eggeling^{4,5,6}

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Saffman-Delbruck and q2D hydrodynamics: Long ranged and counter-intuitive

Hydrodynamics for membranes:

- Low Re number \rightarrow Navier-Stokes linearize
- Incompressible (both membrane and water)
- 2D fluid coupled to 3D bulk, $\eta_m \sim 1000 \times \eta_w$

A new length
scale appears:

$$L_{SD} = h \frac{\eta_m}{\eta_w}$$

Mobility scales with
log radius:

$$\mu = \frac{1}{4\pi h \eta_m} \left(\ln \left(\frac{2L_{SD}}{a} \right) - \gamma \right)$$

