

# Near-field radiative heat radiation in many-body systems: non-reciprocity, topology, etc.

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## Introduction

Heat transfer in two-body systems

## Near-field heat transfer in many-body systems

Framework and overview

## Non-Reciprocity

Hall effect for thermal radiation (revisited)

Heat flux rectification with non-reciprocal surface waves

## Boltzmann vs. Landauer

## Topology

Su-Schrieffer-Heeger model

Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

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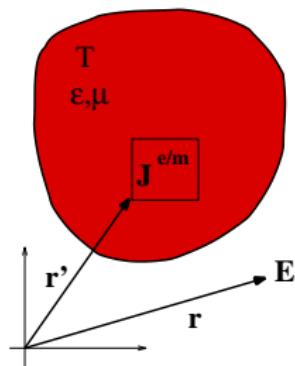
Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

## Summary

# Rytov's fluctuational electrodynamics

- Maxwell's eqs. + fluct. source currents



$$\langle \mathbf{J} \rangle = \mathbf{0}$$

- Fluctuating fields

$$E_\alpha(\omega, \mathbf{r}) = i\omega\mu_0 \int_V d^3r' G_{\alpha\beta}^{EE}(\mathbf{r}, \mathbf{r}') J_\beta(\mathbf{r}', \omega)$$

- Fluctuation-dissipation theorem

$$\langle J_\alpha(\mathbf{r}, \omega) J_\beta^*(\mathbf{r}', \omega') \rangle = \Theta(\omega, T) 2\omega\epsilon_0 [\text{Im}(\epsilon_{\alpha\beta}) \delta(\mathbf{r} - \mathbf{r}')] 2\pi\delta(\omega - \omega')$$

- Mean energy of a harmonic oscillator

$$\Theta(\omega, T) := \frac{\hbar\omega}{2} + \frac{\hbar\omega}{e^{\hbar\omega/k_B T} - 1}$$

# Field correlation functions

- Correlation functions (applying the FDT)

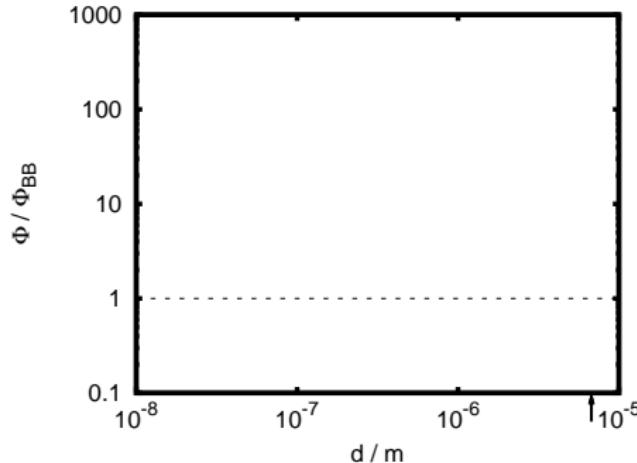
$$\langle E_\alpha(\mathbf{r}, t) E_\beta(\mathbf{r}', t') \rangle = \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} e^{i\omega(t-t')} 2\mu_0^2 \omega^3 \Theta(\omega, T) \int_V d^3 r'' \\ \times \left( \epsilon_0 G^{EE}(\mathbf{r}, \mathbf{r}'') \epsilon''(\mathbf{r}'') G^{EE\dagger}(\mathbf{r}', \mathbf{r}'') \right)_{\alpha\beta}$$

$$\langle E_\alpha(\mathbf{r}, t) H_\beta(\mathbf{r}', t') \rangle = \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} e^{i\omega(t-t')} 2\mu_0^2 \omega^3 \Theta(\omega, T) \int_V d^3 r'' \\ \times \left( \epsilon_0 G^{EE}(\mathbf{r}, \mathbf{r}'') \epsilon''(\mathbf{r}'') G^{HE\dagger}(\mathbf{r}', \mathbf{r}'') \right)_{\alpha\beta}$$

etc.

- Equilibrium: FDT 1. kind (G.S. Agarwal, Phys. Rev. A 11, 230 (1975))
- Stress tensor: Casimir force (Lifshitz, JETP 2, 73 (1956))
- Poynting vector: Rad. heat transfer (Polder, van Hove, PRB 4, 3303 (1971))

# Consequences for radiative heat flux



$\Phi_{BB}$  = blackbody value

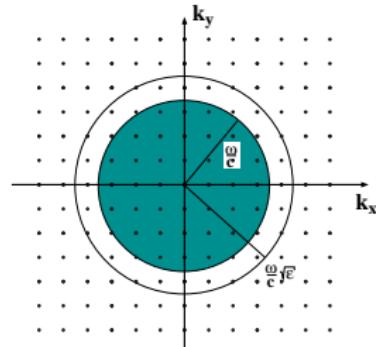
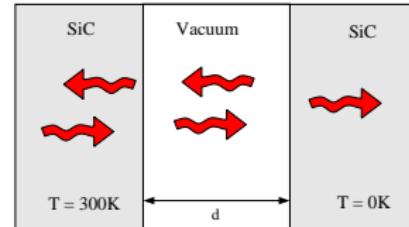
Polder and van Hove, PRB **4**, 3303 (1971)  
Pendry, J. Phys. **11** 6621 (1999)  
Volokitin and Persson, RMP **79**, 1291 (2007)

**Landauer:**

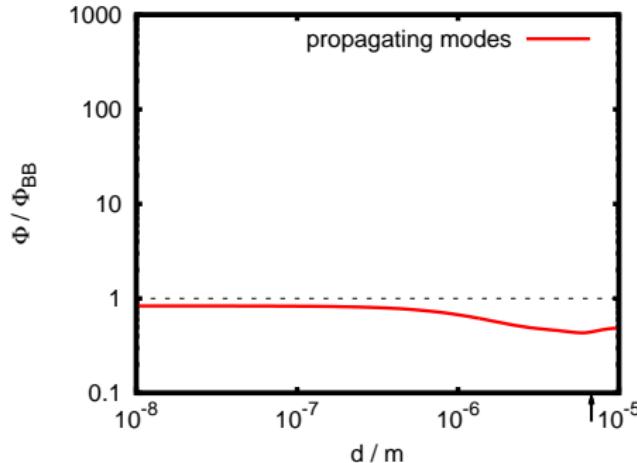
SAB, Rousseau, Greffet, PRL **105**, 234301 (2010)  
Ben-Abdallah and Joulain, PRB **82**, 121419 (R) (2010)

**Limits:**

Basu, Zhang, JAP **105**, 093535 (2009)  
Miller et al., PRL **115**, 204302 (2015), Venkataram et al., PRL **124**, 013904 (2020)



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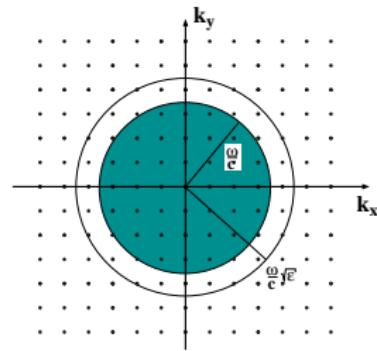
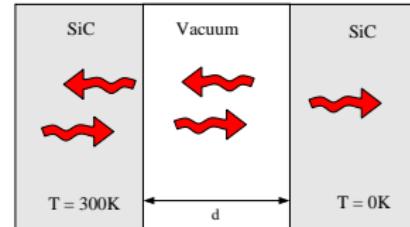
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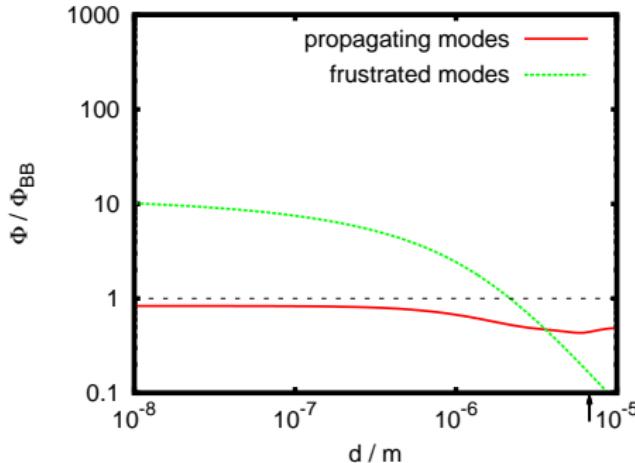
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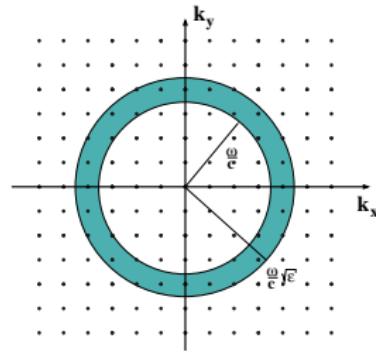
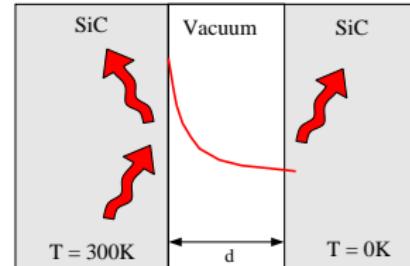
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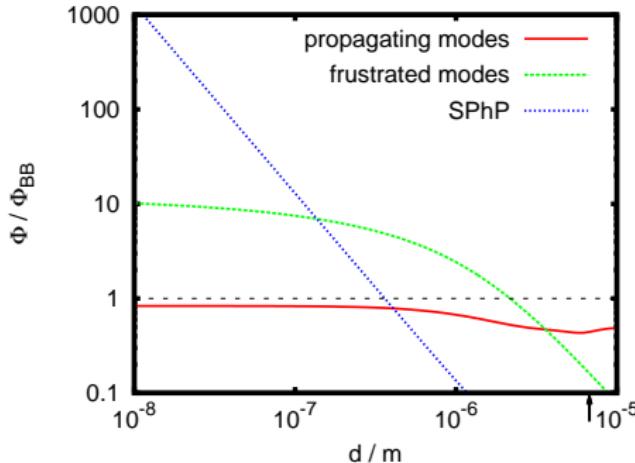
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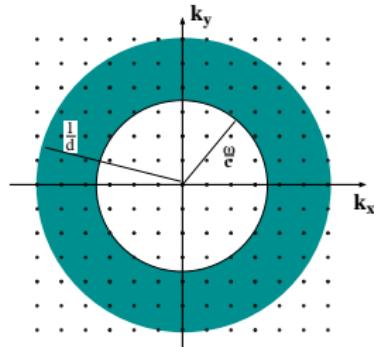
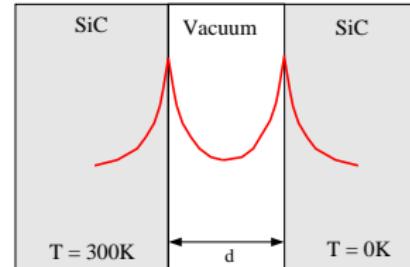
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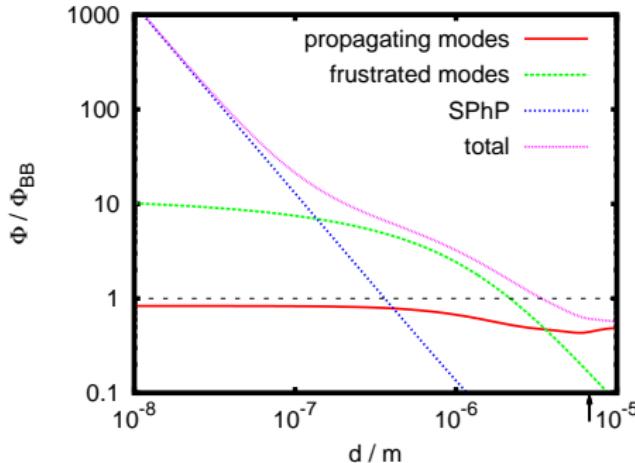
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NHT: non-reciprocity, topology, etc.



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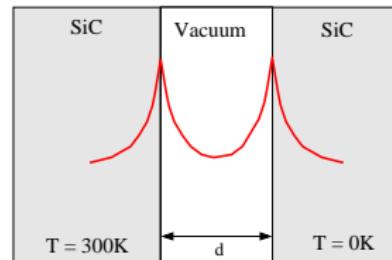
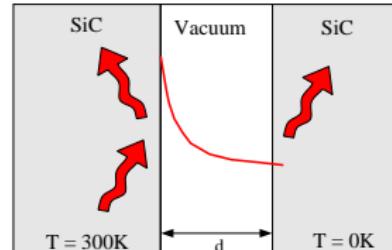
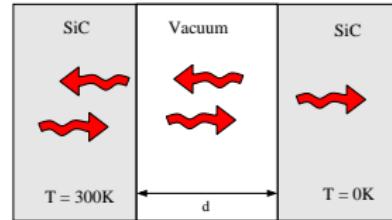
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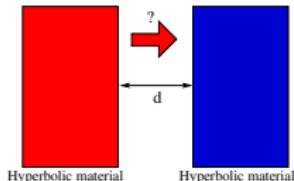
Miller et al., PRL **115**, 204302 (2015) , Venkataram et al., PRL **124**, 013904 (2020)



# Two-body near-field heat transfer

## Enhancement:

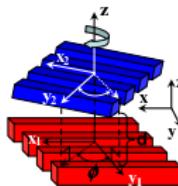
### Hyperbolic materials



Nefedov, Simovski, PRB **84**, 195459 (2011)  
SAB et al., Opt. Expr. **19**, A1088 (2011)  
SAB et al., PRL **109**, 104301 (2012)  
SAB et al., PRL **115**, 174301 (2015)

## Modulation:

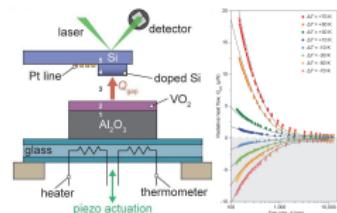
### mech., elec., magn.



SAB et al., APL **98**, 243102 (2011)  
van Zwol et al., PRB **83**, 201404(R) (2011)  
Huang et al., APL **105** 244102 (2014)  
Ekeroth et al., ACS Phot. **5**, 705 (2018)

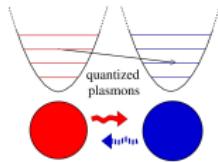
## Thermotronics:

### Phase-change Diode



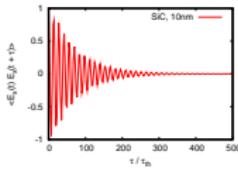
Otey et al., PRL **104**, 154301 (2010)  
Ben-Abdallah, SAB, APL **103**, 191907 (2013)  
Fiorino et al., ACS Nano **12**, 5774 (2018)

## Quantum models



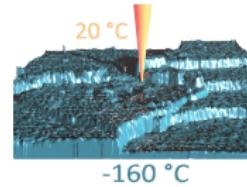
Janowicz et al., PRA **68**, 043823 (2003)  
SAB, Agarwal, JOSAB **30**, 700 (2013)  
Barton, J. Stat. Phys. **165**, 1153 (2016)  
Wang, Peng EPL **118**, 24001 (2017)

## Fluctuations



Golyk et al., PRB **88**, 155117 (2013)  
SAB, Ben-Abdallah, PRB **97**, 201406(R) (2018)  
Herz, SAB, EPL **127**, 44001 (2019)  
Herz et al., EPL **130**, 44003 (2020)

## Experiments



Kittel et al., PRL **95**, 224301 (2005)  
Kittel et al., APL **93**, 193109 (2008)  
Kloppstech et al., Nat. Comm. **8**, 14475 (2017)

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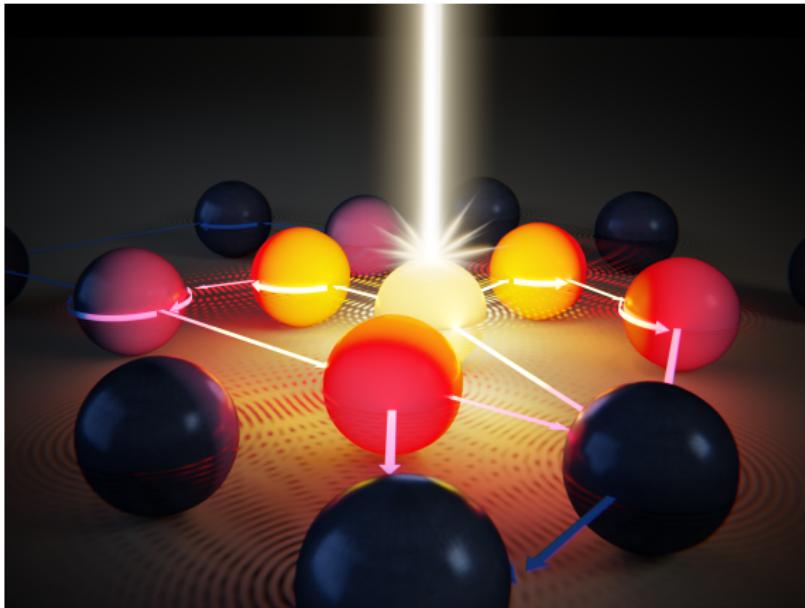
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Summary

# Thermal near-field radiation in many-body systems



Ben-Abdallah, SAB, Joulain, PRL **107**, 107, 114301 (2011)

...  
Messina, Antezza PRA **84**, 042102 (2011)

Krüger, Bimonte, Emig, Kardar, PRB **86**, 115423 (2012)

...  
SAB, Messina, Venkataram, Rodriguez, Cuevas, Ben-Abdallah, Rev. Mod. Phys. **93**, 025009 (2021)

# Thermal near-field radiation in many-body systems

- Power exchanged between particles with polarizability  $\underline{\underline{\alpha}}$

$$\langle P_i \rangle = \sum_{j \neq i}^N 3 \int_0^\infty \frac{d\omega}{2\pi} \left( [\Theta(\omega, T_j) - \Theta(\omega, T_i)] \mathcal{T}_{ji}(\omega) \right)$$

- Mean energy of harmonic oscillator

$$\Theta(\omega, T) = \frac{\hbar\omega}{e^{\hbar\omega/k_B T} - 1} \quad \langle P_1 \rangle = 3 \left( \frac{\pi^2 k_B^2 T}{3h} \right) \bar{T}_{12} \Delta T_{12}$$

- Transmission coefficient (proportional to absorptivity  $\frac{\underline{\underline{\alpha}} - \underline{\underline{\alpha}}^\dagger}{2i}$ )

$$\mathcal{T}_{ij}(\omega) = \frac{4}{3} \text{ImTr} \left[ \mathbf{T}_{ij}^{-1} \frac{\underline{\underline{\alpha}} - \underline{\underline{\alpha}}^\dagger}{2i} (\mathbf{T}_{ij}^{-1})^\dagger \underline{\underline{\alpha}}^{-1\dagger} \right]$$

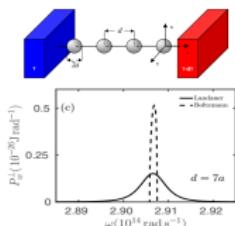
- 'Transfer matrix'

$$\mathbf{T}_{ij} = \delta_{ij} \mathbb{1} - (1 - \delta_{ij}) k_0^2 \underline{\underline{\alpha}} \mathbb{G}_{ij}^E$$

- Access to all observables: mean Poynting vector, energy density, etc.

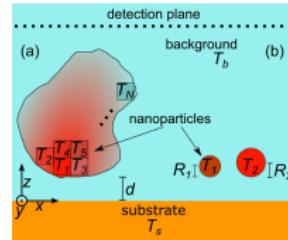
# Application of many-body theory

## Boltzmann vs. Landauer



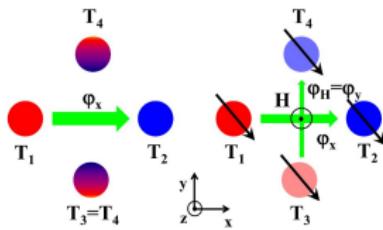
Ben-Abdallah, et al., PRL **111**, 174301 (2013)  
Kathmann et al., PRB **98**, 115434 (2018)

## Coupled dipole method



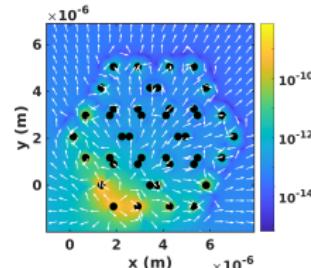
Herz, SAB, PRB **105**, 205422(2022)

## Non-Reciprocal systems



Ben-Abdallah, PRL **116**, 084301 (2016)  
Ott et al., J. Phot. En. **9**, 032711 (2019)  
Ott et al., PRB **101**, 241411(R) (2020)

## Topological systems



Ott, SAB, PRB **102**, 115417 (2020)  
Ott, SAB, IJHMT **190**, 122796(2022)

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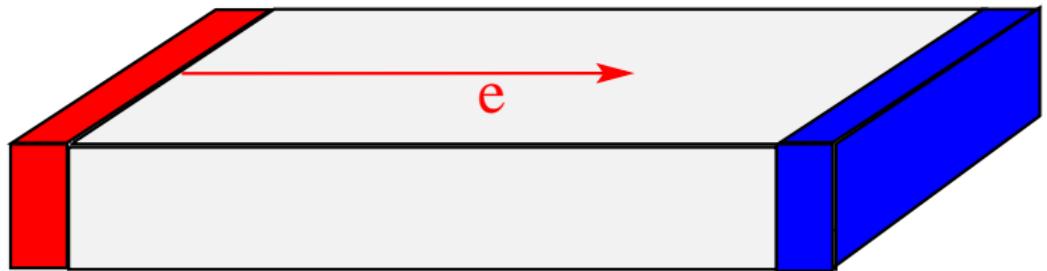
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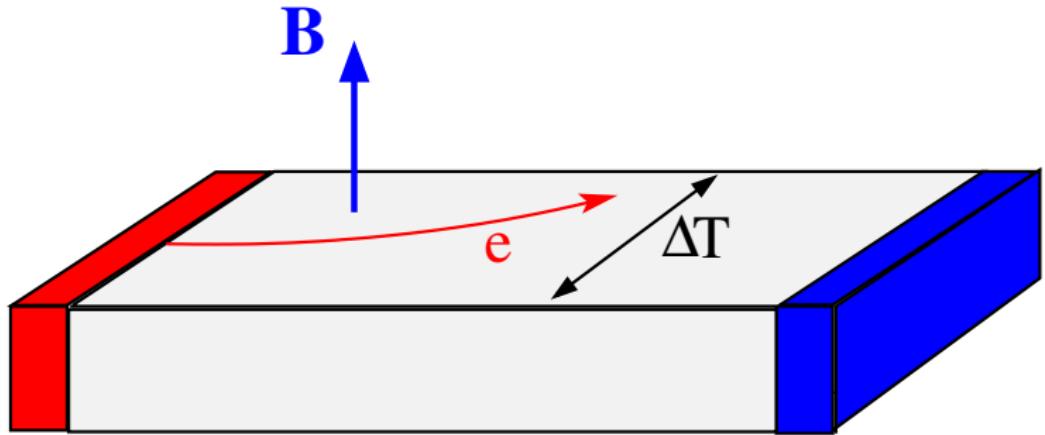
## Summary

# Righi-Leduc or thermal Hall effect



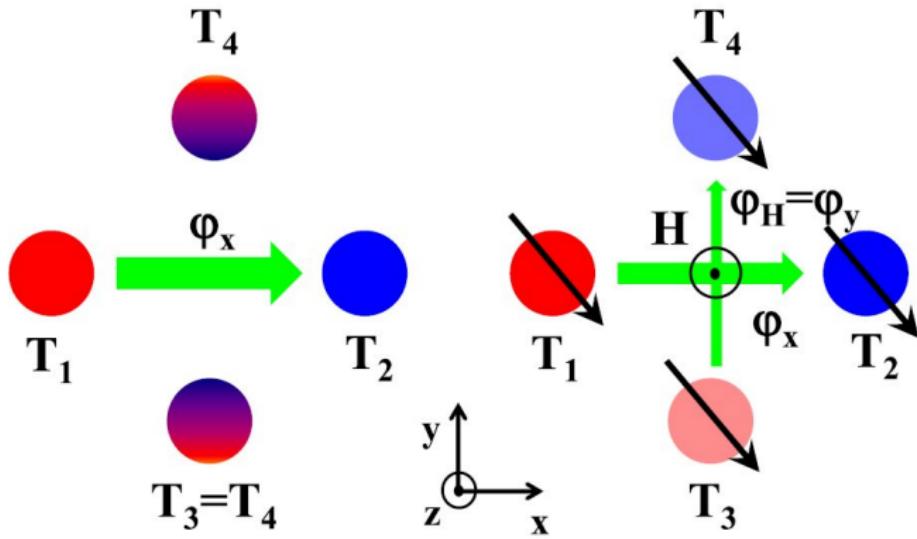
A. Righi, Mem. Acc. Lincei 4, 433 (1887); M. A. Leduc, J. Phys. 2e série 6, 378 (1887)

# Righi-Leduc or thermal Hall effect



A. Righi, Mem. Acc. Lincei 4, 433 (1887); M. A. Leduc, J. Phys. 2e série 6, 378 (1887)

# Hall effect for thermal radiation



How can the photon trajectories be bent?

Ben-Abdallah, PRL 116, 084301 (2016)

# Fluctuational fields around a nanoparticle

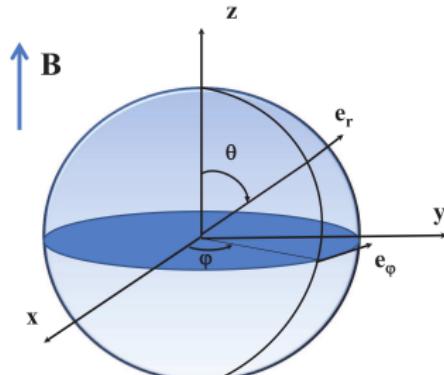
- Fluctuational fields

$$\vec{E}_{\text{fl}} = \omega^2 \mu_0 \mathbb{G}^E(\vec{r}, \vec{r}', \omega) \cdot \vec{p}_{\text{fl}}(\omega, t)$$

$$\vec{H}_{\text{fl}} = \omega^2 \mu_0 \mathbb{G}^H(\vec{r}, \vec{r}', \omega) \cdot \vec{p}_{\text{fl}}(\omega, t)$$

- Fluctuation-dissipation theorem of second kind

$$\langle \vec{p}_{\text{fl}} \otimes \vec{p}_{\text{fl}}^* \rangle = \frac{2\epsilon_0}{\omega} \Theta(\omega, T_p) \frac{1}{2i} (\underline{\underline{\alpha}} - \underline{\underline{\alpha}}^\dagger)$$



- Polarizability (spherical particle)

$$\underline{\underline{\alpha}} = 4\pi R^3 (\underline{\underline{\epsilon}} - \mathbb{1})(\underline{\underline{\epsilon}} + 2\mathbb{1})^{-1}$$

- Non-reciprocal permittivity ( $\underline{\underline{\alpha}}^t \neq \underline{\underline{\alpha}}$ ,  $\underline{\underline{\epsilon}}^t \neq \underline{\underline{\epsilon}}$ )

$$\underline{\underline{\epsilon}} = \begin{pmatrix} \epsilon_1 & -i\epsilon_2 & 0 \\ i\epsilon_2 & \epsilon_1 & 0 \\ 0 & 0 & \epsilon_3 \end{pmatrix} \quad \Rightarrow \quad \underline{\underline{\alpha}} = \begin{pmatrix} \alpha_1 & \alpha_{12} & 0 \\ -\alpha_{12} & \alpha_1 & 0 \\ 0 & 0 & \alpha_3 \end{pmatrix}$$

Ott, Ben-Abdallah, SAB, PRB 97, 205414 (2018)

# Heat flux, momentum, angular momentum, and spin

- Mean poynting vector

$$\langle \vec{S}_\omega \rangle = 2\text{Re} \langle \vec{E}_{\text{fl}} \times \vec{H}_{\text{fl}}^* \rangle$$

- Canonical linear momentum density

$$\langle \vec{P}_\omega \rangle = \frac{1}{\omega} \text{Im} \left( \frac{\epsilon_0}{2} \langle \vec{E}_{\text{fl}}^*(\nabla) \vec{E}_{\text{fl}} \rangle + \frac{\mu_0}{2} \langle \vec{H}_{\text{fl}}^*(\nabla) \vec{H}_{\text{fl}} \rangle \right)$$

- Angular momentum density

$$\langle \vec{L}_\omega \rangle = \vec{r} \times \langle \vec{P}_\omega \rangle$$

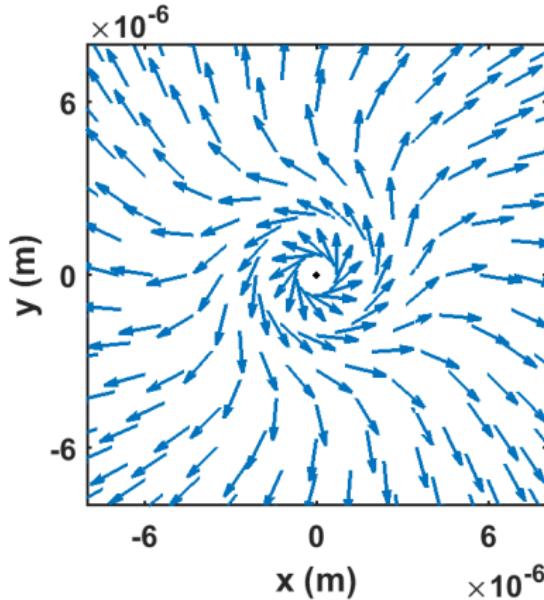
- Spin angular momentum density

$$\langle \vec{S}_{d\omega} \rangle = \frac{1}{\omega} \text{Im} \left( \frac{\epsilon_0}{2} \langle \vec{E}_{\text{fl}}^* \times \vec{E}_{\text{fl}} \rangle + \frac{\mu_0}{2} \langle \vec{H}_{\text{fl}}^* \times \vec{H}_{\text{fl}} \rangle \right)$$

Bliokh and Nori, Phys. Rep. **592**, 1 (2015)

Ott, Ben-Abdallah, SAB, PRB **97**, 205414 (2018)

# Poynting vector around one InSb nanoparticle



- Polarizability

$$\underline{\underline{\alpha}} = 4\pi R^3 (\epsilon - 1)(\epsilon + 2\mathbb{I})^{-1}$$

- Applied magnetic field

$$\underline{\underline{\alpha}} = \begin{pmatrix} \alpha_1 & \alpha_{12} & 0 \\ -\alpha_{12} & \alpha_1 & 0 \\ 0 & 0 & \alpha_3 \end{pmatrix}$$

- Non-reciprocal

$$\underline{\underline{\alpha}}^t \neq \underline{\underline{\alpha}}$$

$$S_\varphi(\omega) = \frac{\Theta(\omega, T_p) k_0^3}{2\pi^2 r^2} \operatorname{Re}(\alpha_{12}) \left( \frac{1}{k_0 r} + \frac{1}{k_0^3 r^3} \right)$$

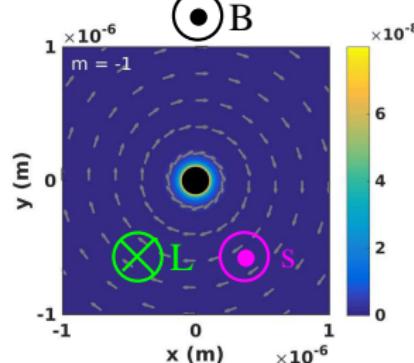
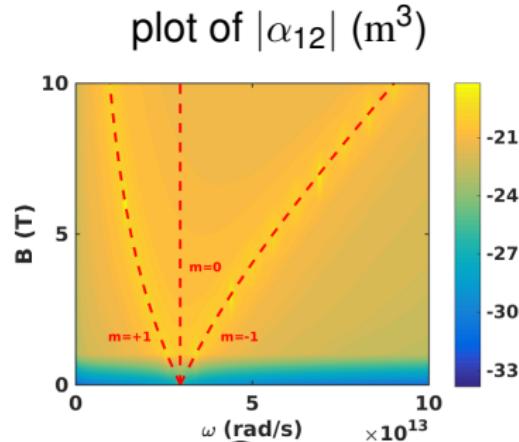
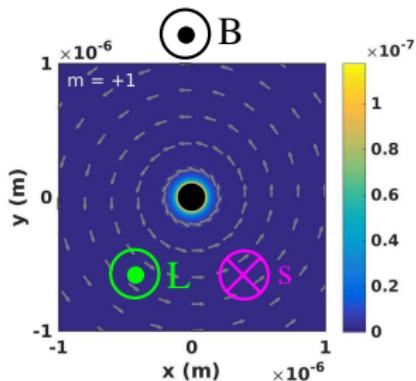
Ott, Ben-Abdallah, SAB, PRB **97**, 205414 (2018)

# Dipolar resonances, ( $I = 1$ , $m = -1, 0, +1$ )

- Dipolar resonances

$$\omega_{m=0} = \sqrt{\frac{\epsilon_\infty \omega_p^2}{\epsilon_\infty + 2}}$$

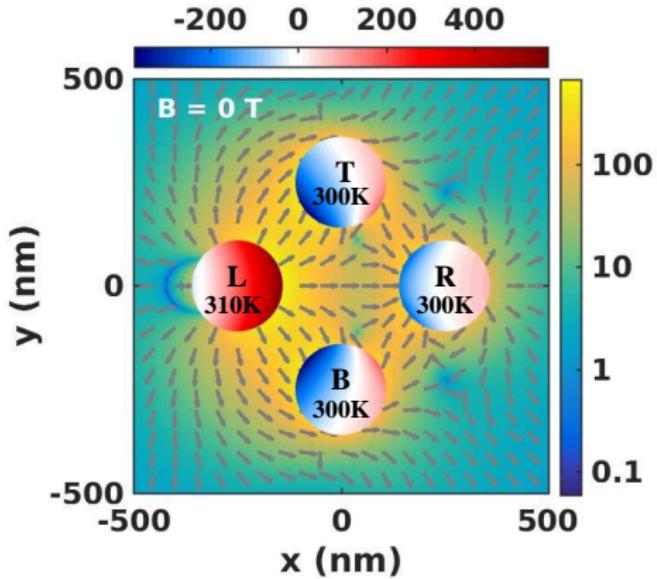
$$\omega_{m=\pm 1} = \sqrt{\frac{\epsilon_\infty \omega_p^2}{\epsilon_\infty + 2} + \frac{\omega_c^2}{4}} \mp \frac{\omega_c}{2}$$



spin, angular momentum, heat flux **persist** in equilibrium  
[see also M.G. Silveirinha, PRB 95, 115103 (2017)]

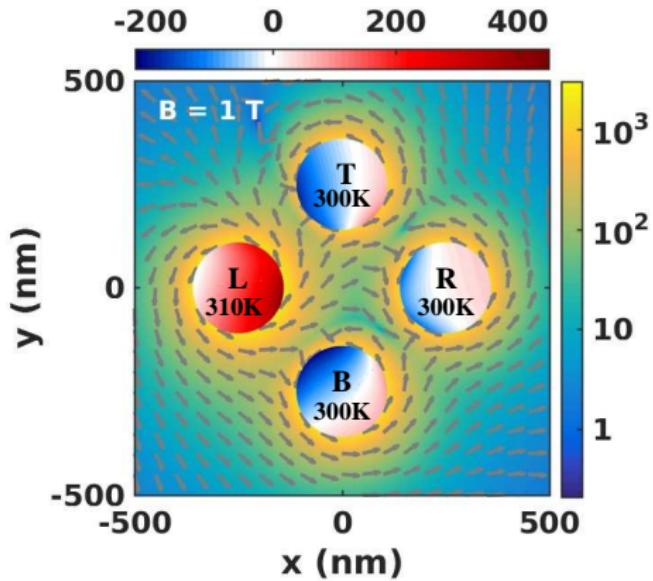
Ott, Ben-Abdallah, SAB, PRB 97, 205414 (2018)

# Heat flux and emitted/received power ( $R = 100$ nm, $d = 500$ nm)



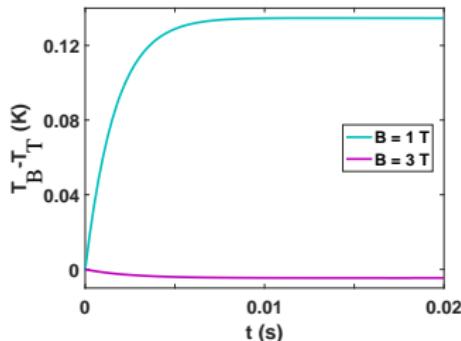
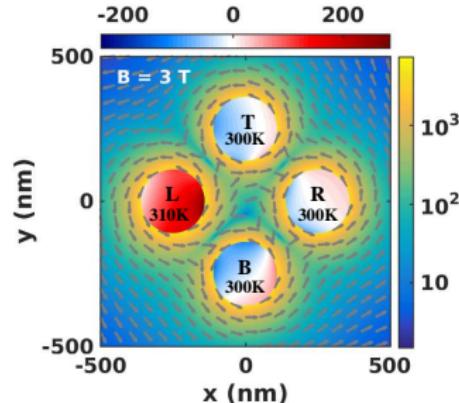
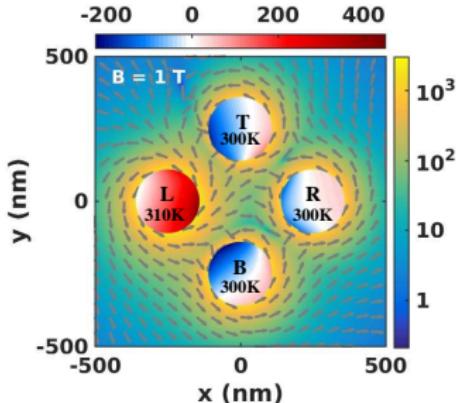
Ott, Messina, Ben-Abdallah, SAB, J. Photon. Energy 9, 032711 (2019)

# Heat flux and emitted/received power ( $R = 100$ nm, $d = 500$ nm)



Ott, Messina, Ben-Abdallah, SAB, J. Photon. Energy 9, 032711 (2019)

# Photonic thermal Hall effect



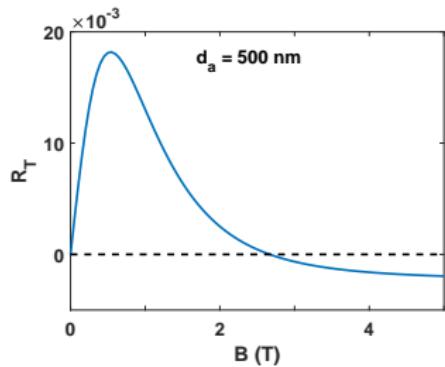
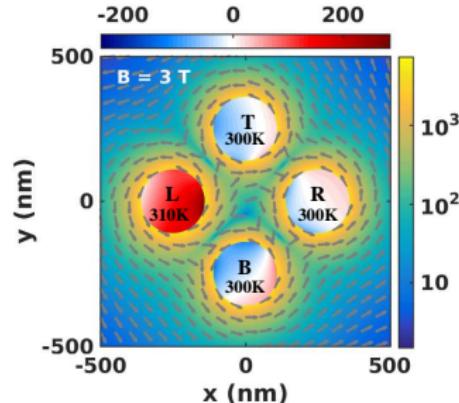
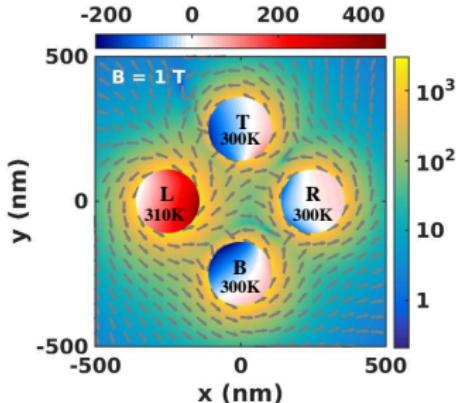
“Righi-Leduc coefficient”

$$R_T = \frac{T_B^{(st)} - T_T^{(st)}}{T_L - T_R} = \frac{G_{LB} - G_{BL}}{G_{LB} + G_{BL} + 2G_{BT}}$$

Ott, Messina, Ben-Abdallah, SAB, J. Photon. Energy **9**, 032711 (2019)

Anomalous Hall effect for Weyl semi metals: Ott, SAB, Ben-Abdallah, PRB **101**, 241411(R) (2020)

# Photonic thermal Hall effect



“Righi-Leduc coefficient”

$$R_T = \frac{T_B^{(st)} - T_T^{(st)}}{T_L - T_R} = \frac{G_{LB} - G_{BL}}{G_{LB} + G_{BL} + 2G_{BT}}$$

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## Introduction

Heat transfer in two-body systems

## Near-field heat transfer in many-body systems

Framework and overview

## Non-Reciprocity

Hall effect for thermal radiation (revisited)

Heat flux rectification with non-reciprocal surface waves

## Boltzmann vs. Landauer

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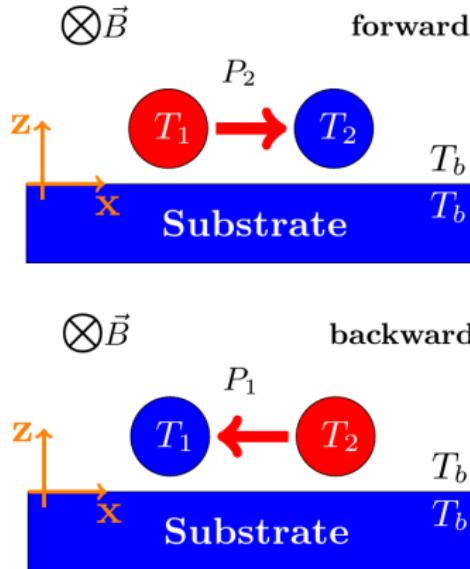
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Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

## Summary

# Heat flux diode with non-reciprocal surface waves



Ott, Messina, Ben-Abdallah, SAB, APL **114**, 163105 (2019)

Ott, SAB, PRB **101**, 155428 (2020)

Enhancement by surface:

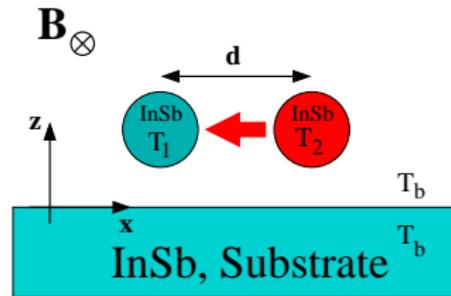
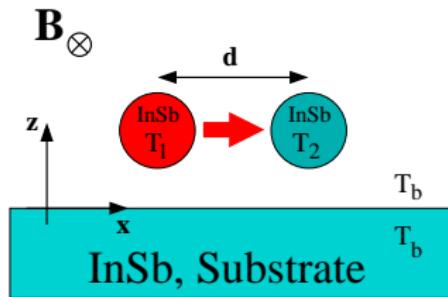
Sääskilathi et al., PRB **89**, 134301 (2014)

Asheichy et al., PRB **96**, 155402 (2017)

Dong et al., PRB **97**, 075422 (2018)

Messina et al., PRB **97**, 165437 (2018)

# Rectification and non-reciprocity



$$P_2 = 3 \int_0^\infty \frac{d\omega}{2\pi} [\Theta(T_1) - \Theta(T_2)] \mathcal{T}_{12}$$

$$\mathcal{T}_{12} = \frac{4}{3} k_0^4 \text{Tr} [\underline{\chi} \mathbb{G}_{12} \underline{\chi} \mathbb{G}_{12}^\dagger]$$

$$P_1 = 3 \int_0^\infty \frac{d\omega}{2\pi} [\Theta(T_2) - \Theta(T_1)] \mathcal{T}_{21}$$

$$\mathcal{T}_{21} = \frac{4}{3} k_0^4 \text{Tr} [\underline{\chi} \mathbb{G}_{21} \underline{\chi} \mathbb{G}_{21}^\dagger]$$

- No rectification if

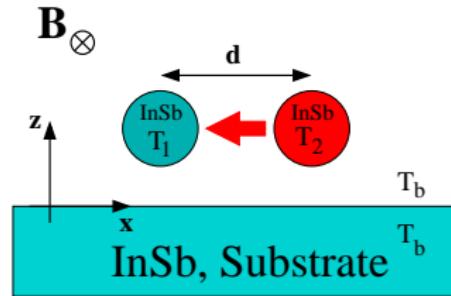
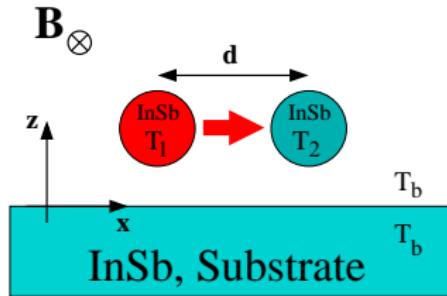
$$\mathbb{G}_{12} = \mathbb{G}_{21} \quad \text{or} \quad \mathbb{G}_{12} = \mathbb{G}_{21}^t$$

- Non-reciprocal substrate

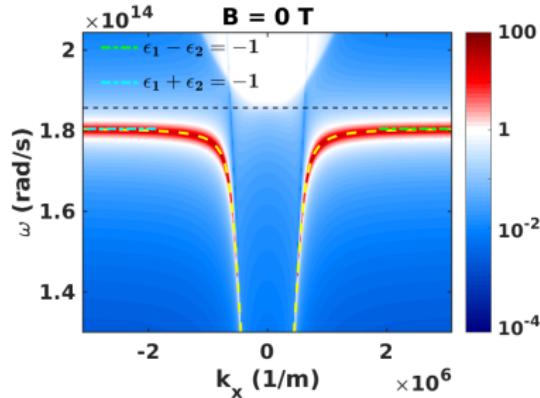
$$r_{pp}(k_x) \neq r_{pp}(-k_x) \Rightarrow \mathbb{G}_{12} \neq \mathbb{G}_{21}^t$$

Ott, Messina, Ben-Abdallah, SAB, APL **114**, 163105 (2019); Ott, SAB, PRB **101**, 155428 (2020)

# Rectification and non-reciprocity

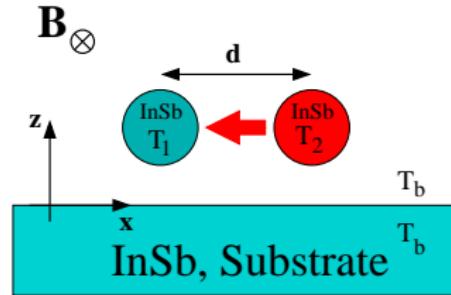
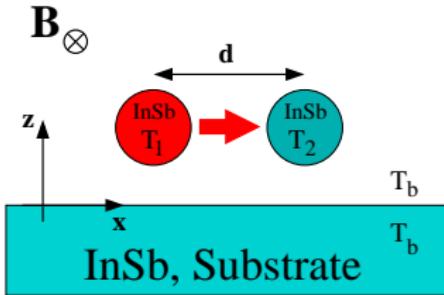


$$r_{pp}(k_x) = r_{pp}(-k_x)$$



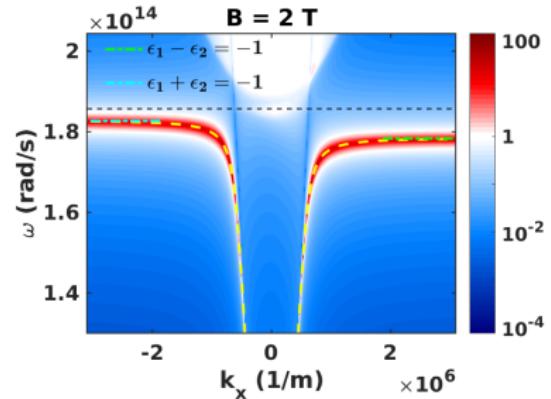
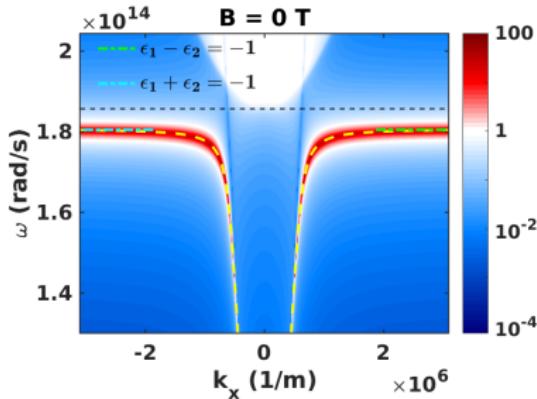
Ott, Messina, Ben-Abdallah, SAB, APL **114**, 163105 (2019); Ott, SAB, PRB **101**, 155428 (2020)

# Rectification and non-reciprocity



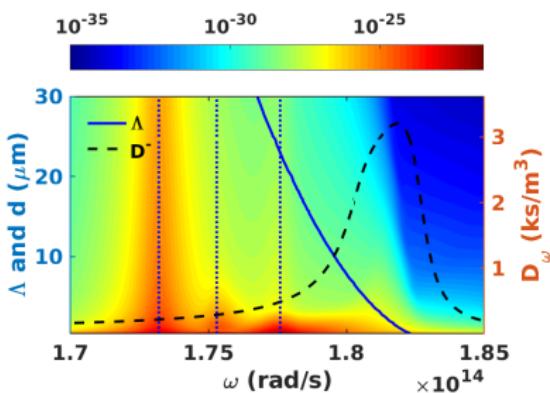
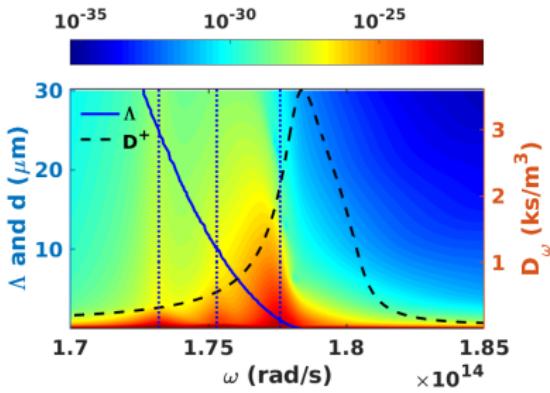
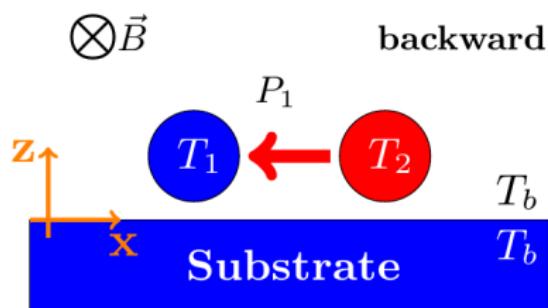
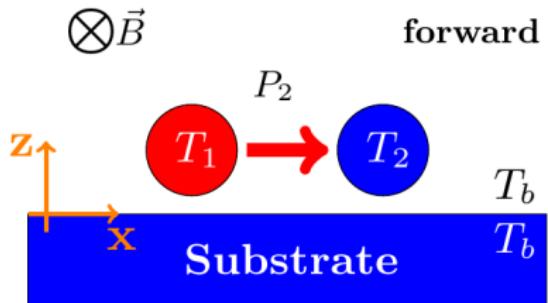
$$r_{pp}(k_x) = r_{pp}(-k_x)$$

$$r_{pp}(k_x) \neq r_{pp}(-k_x)$$



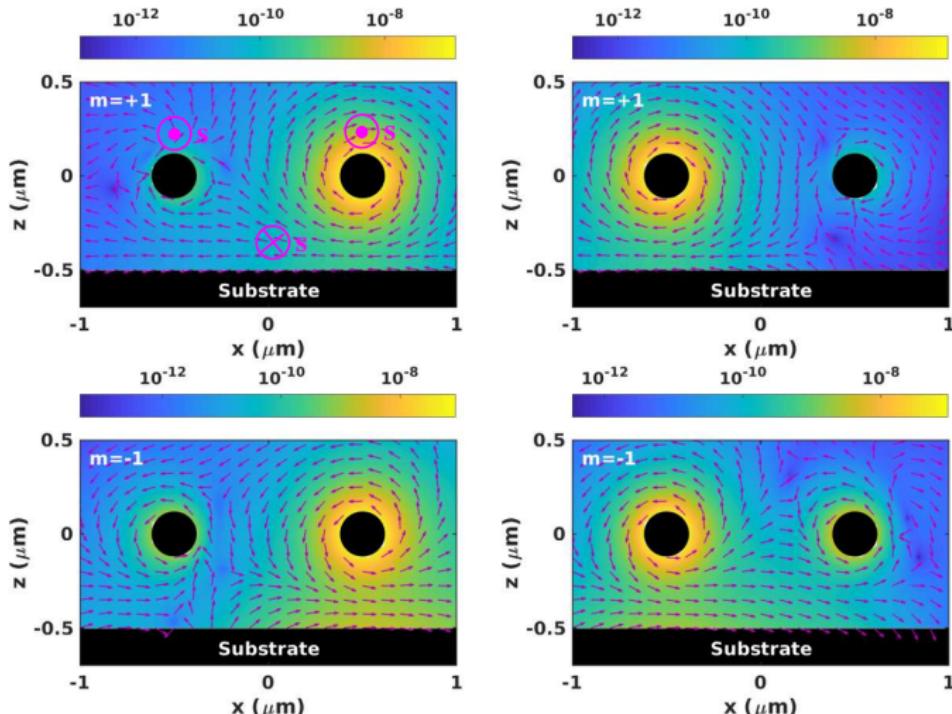
Ott, Messina, Ben-Abdallah, SAB, APL **114**, 163105 (2019); Ott, SAB, PRB **101**, 155428 (2020)

# Heat flux diode (doped InSb, $R = 100$ nm, $z = 5R$ , 2T)



Ott et al., APL **114**, 163105 (2019)  
Ott, SAB, PRB **101**, 155428 (2020)

# Coupling of dipolar and surfaces modes

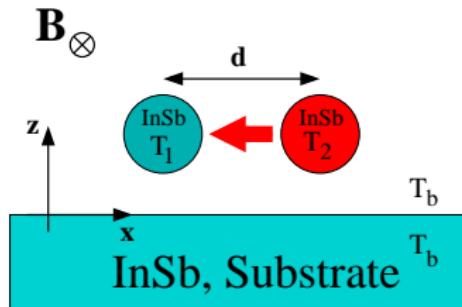
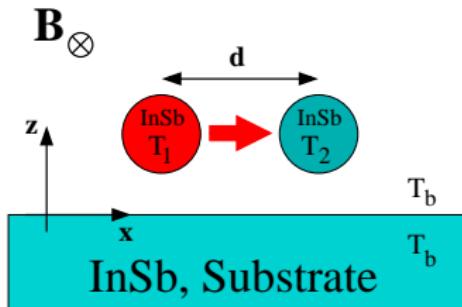


Ott et al., APL **114**, 163105 (2019)

Ott, SAB, PRB **101**, 155428 (2020)

spin-momentum locking:  
Bliokh et al., Science **348**, 1448 (2015);  
Van Mechelen,Jacob, Optica **3**, 118 (2016)

# Rectification coefficient ( $R = 100\text{nm}$ , $z = 500\text{nm}$ )

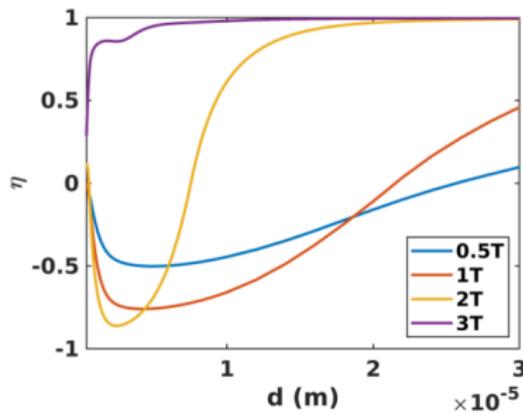


- Rectification coeff.

$$\eta = \frac{P_1 - P_2}{\max(P_1, P_2)}$$

n-doping  
( $n = 1.4 \times 10^{19} \text{ cm}^{-3}$ )

Ott et al., APL **114**, 163105 (2019)  
Ott, SAB, PRB **101**, 155428 (2020)



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## Near-field heat transfer in many-body systems

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Su-Schrieffer-Heeger model

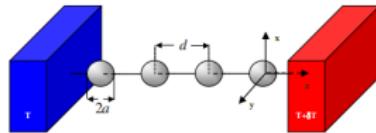
Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

## Summary

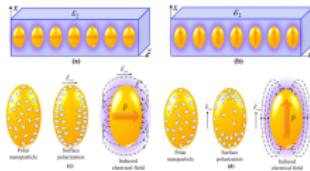
# Boltzmann equation approach for plasmonics

## Chain of nanoparticles



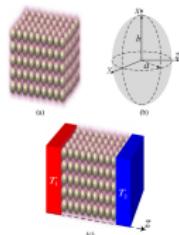
Ben-Abdallah, PRB **77**, 075417 (2008)

## Spheroidal nanoparticles



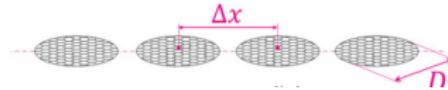
Ordonez-Miranda et al., PRB **92**, 115409 (2015)

## Plasmonic crystal



Ordonez-Miranda et al., PRB **93**, 035428 (2016)

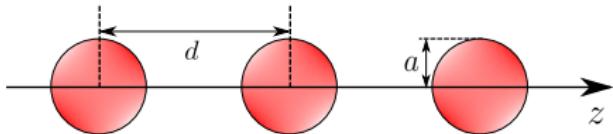
## Graphene disks



Ramirez, McGaughey, PRB **96**, 165428 (2017)

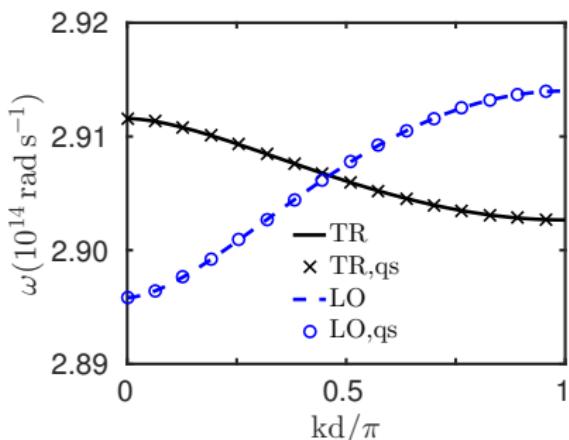
# hBN nanoparticle chain ( $a = 25\text{nm}$ , $d = 100\text{nm}$ )

- Heat current density



$$j = \frac{1}{LA} \sum_k (f_k - f_k^0) v_{g,k} \hbar \omega_k$$

- Boltzmann equation



$$\frac{\partial f_k}{\partial t} + v_{g,k} \frac{\partial f_k}{\partial z} = -\frac{f_k - f_k^0}{\tau_k}$$

- Transferred power ( $\frac{dT}{dz} \approx \frac{\Delta T}{L}$ )

$$P_d = Aj = \int \frac{d\omega}{2\pi} \Theta_{1N} \frac{2}{L} (2\Lambda_\omega^\perp + \Lambda_\omega^\parallel)$$

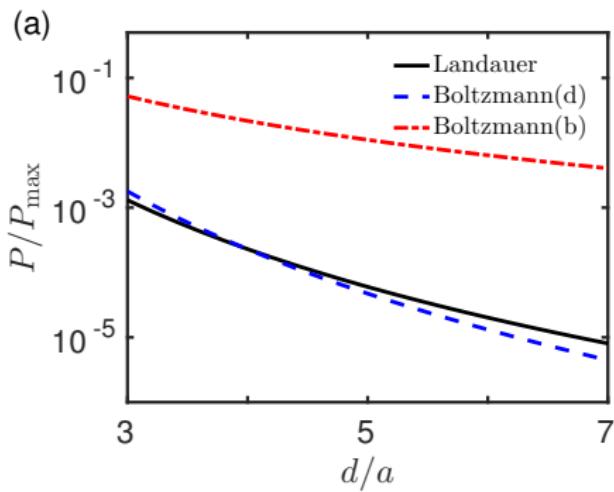
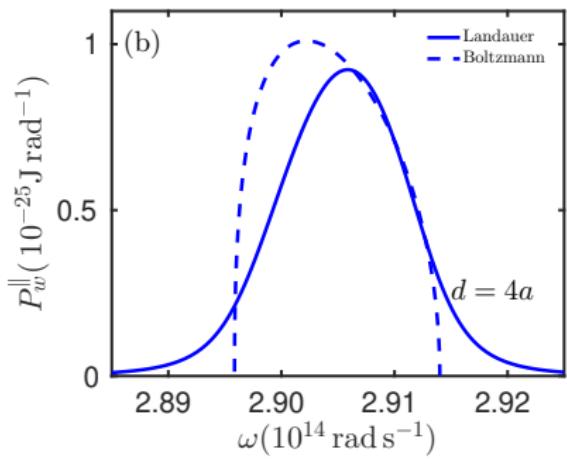
- Propagation length [ $\exp(-i\omega t)$ ]

$$\Lambda_\omega = \left| \frac{d\omega'}{dk} \frac{1}{2\omega''} \right|$$

Kathmann, Messina, Ben-Abdallah, SAB, PRB **98**, 115434 (2018)

# Boltzmann vs. Landauer (hBN, $a = 25\text{nm}$ )

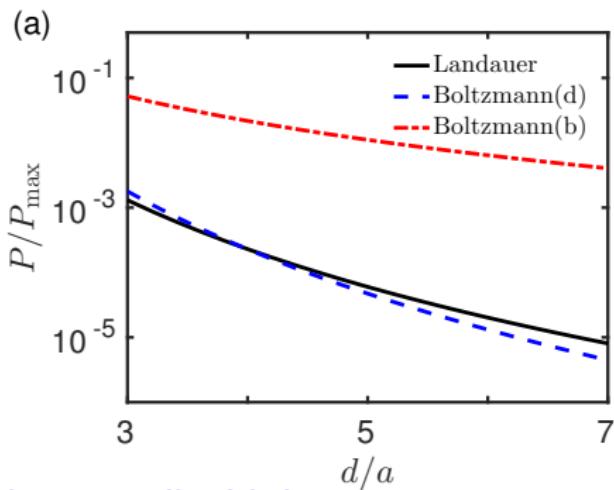
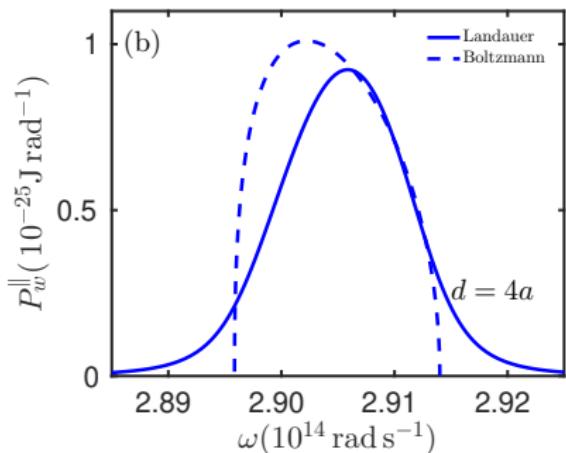
- Spectral transferred power
- Full transferred power



Kathmann, Messina, Ben-Abdallah, SAB, PRB **98**, 115434 (2018)

# Boltzmann vs. Landauer (hBN, $a = 25\text{nm}$ )

- Spectral transferred power
- Full transferred power



Boltzmann approach is in general not applicable!

see also Tervo et al, JQSRT 246, 106947 (2020)

Kathmann, Messina, Ben-Abdallah, SAB, PRB 98, 115434 (2018)

## Introduction

Heat transfer in two-body systems

## Near-field heat transfer in many-body systems

Framework and overview

## Non-Reciprocity

Hall effect for thermal radiation (revisited)

Heat flux rectification with non-reciprocal surface waves

## Boltzmann vs. Landauer

## Topology

Su-Schrieffer-Heeger model

Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

## Summary

## Introduction

Heat transfer in two-body systems

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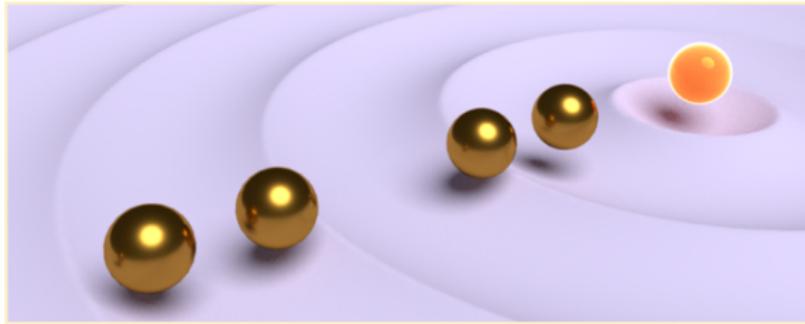
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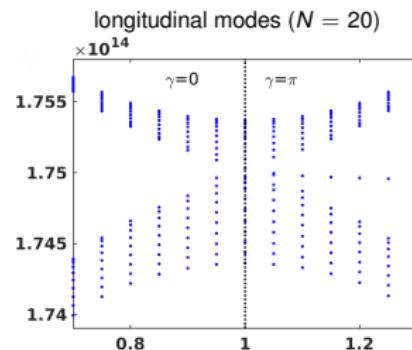
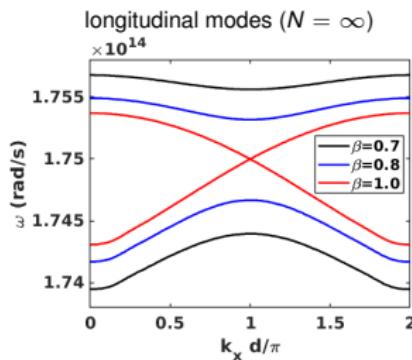
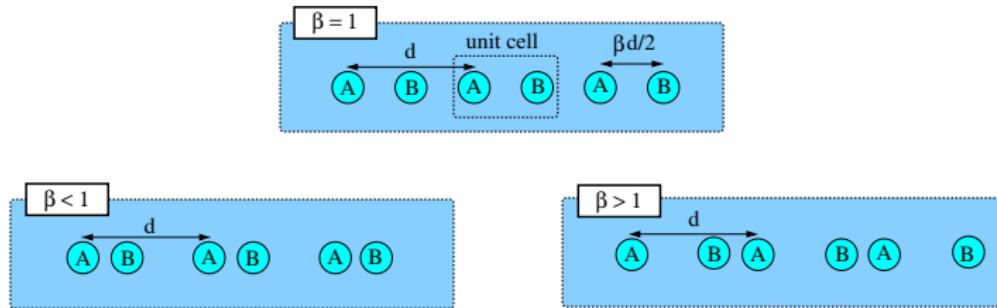
# Su-Schrieffer-Heeger model in plasmonics



Ling et al, Opt. Expr. **23**, 2021 (2015)  
Downing, Weick, PRB **95**, 125426 (2017)  
Pocock et al., ACS Photonics **5**, 2271 (2018)

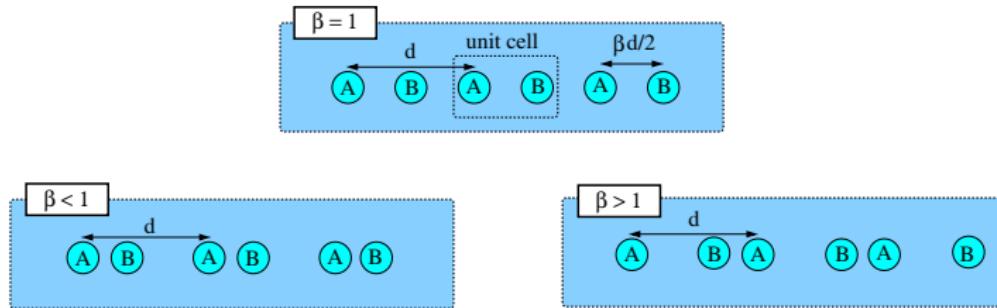
...

# Nanoparticle chains ( $R = 100\text{nm}$ , $d = 1\mu\text{m}$ )

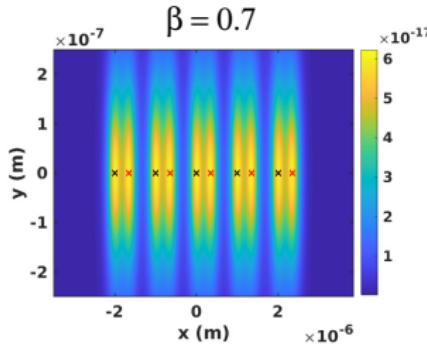


Ott, SAB, PRB **102**, 115417 (2020)

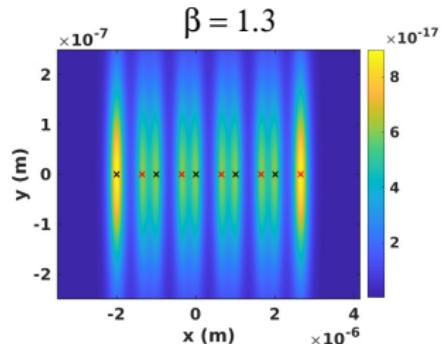
# Nanoparticle chains ( $R = 100\text{nm}$ , $d = 1\mu\text{m}$ )



spectral energy density ( $z = 300 \text{ nm}$ ,  $\text{Js/m}^3$ ,  $N = 10$ )



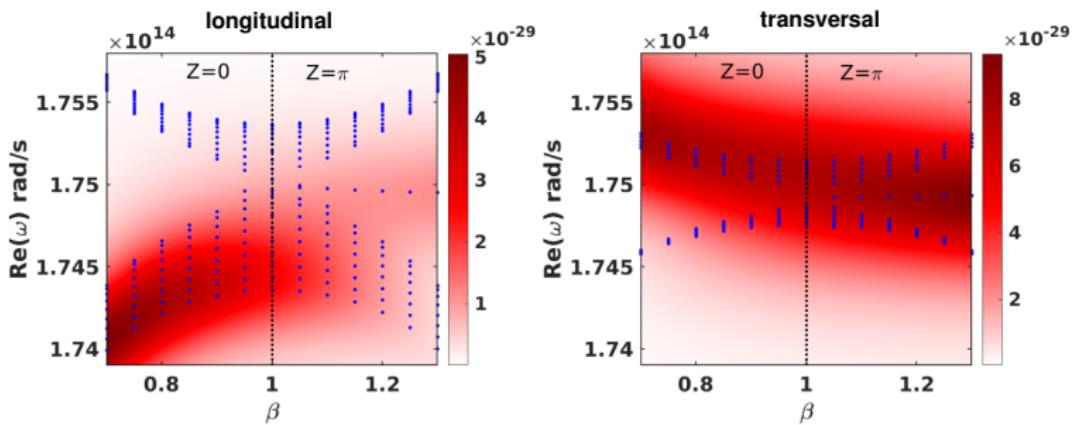
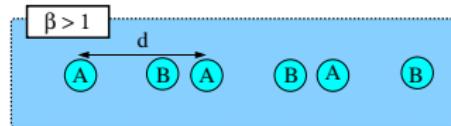
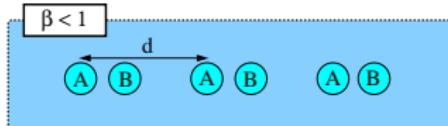
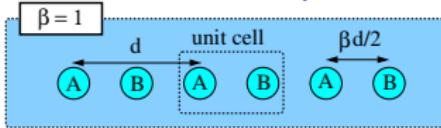
spectral energy density ( $z = 300 \text{ nm}$ ,  $\text{Js/m}^3$ ,  $N = 10$ )



Ott, Kittel, An, SAB, PRB **104**, 165407(2021)

# Spectral heat flux in SSH chains

( $R = 100\text{nm}$ ,  $d = 1\mu\text{m}$ ,  $N = 20$ )



Ott, SAB, PRB 102, 115417 (2020)

## Introduction

Heat transfer in two-body systems

## Near-field heat transfer in many-body systems

Framework and overview

## Non-Reciprocity

Hall effect for thermal radiation (revisited)

Heat flux rectification with non-reciprocal surface waves

## Boltzmann vs. Landauer

## Topology

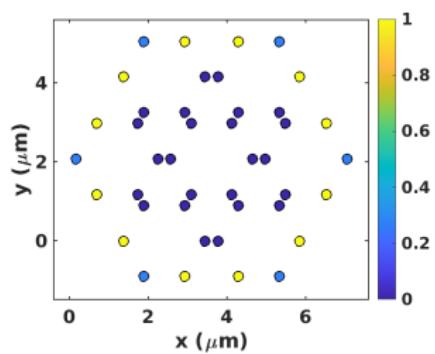
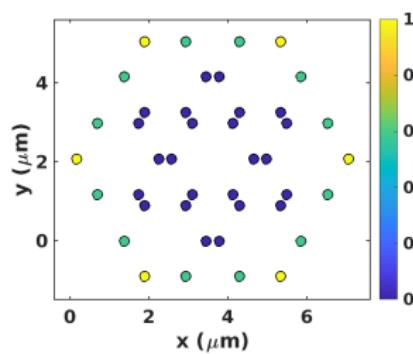
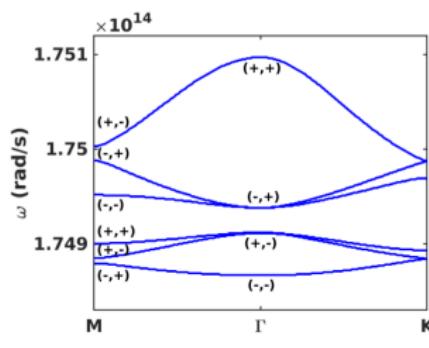
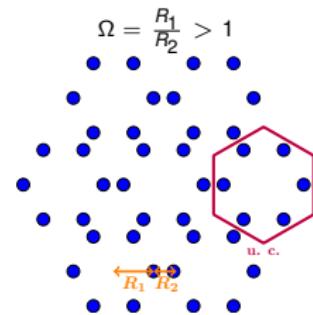
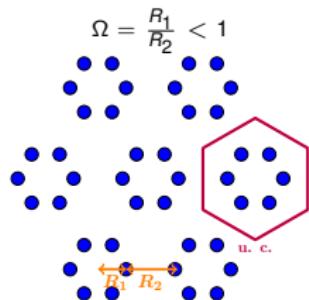
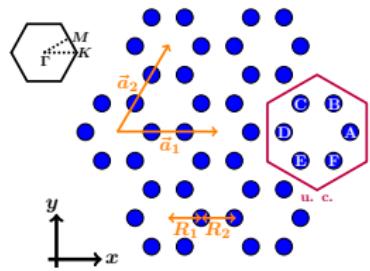
Su-Schrieffer-Heeger model

**Honeycomb lattice**

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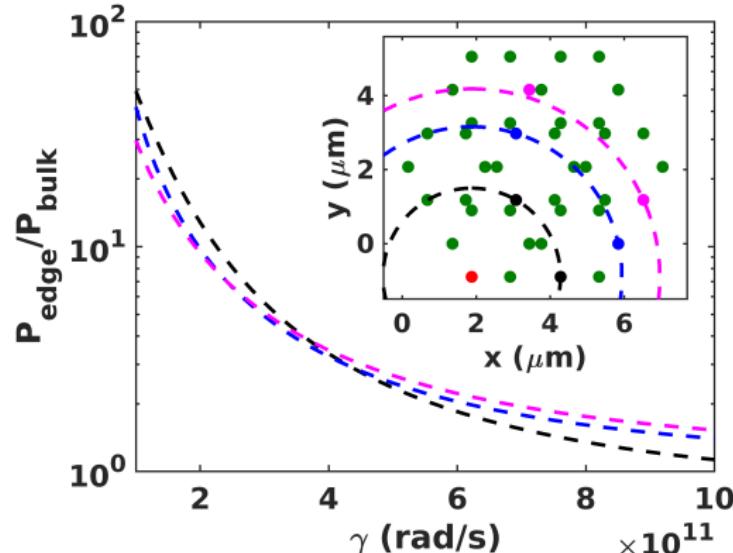
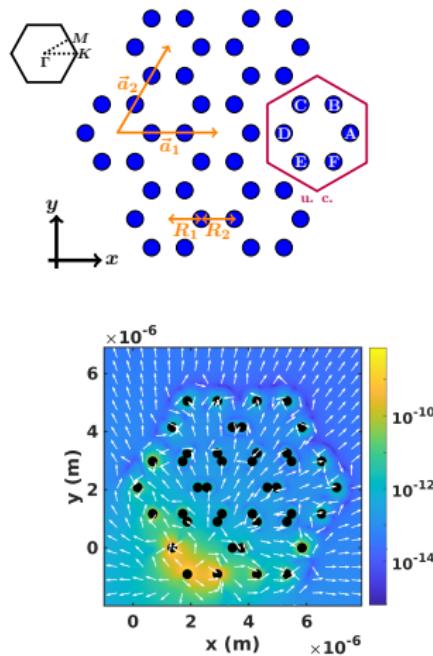
## Summary

# Edge and corner modes ( $R = 100\text{nm}$ , $d = 1\mu\text{m}$ )



Ott, SAB, Int. J. Heat & Mass Transf. **190**, 122796(2022)

# Edge mode heat transfer ( $R = 100\text{nm}$ , $d = 1\mu\text{m}$ )



Ott, SAB, Int. J. Heat & Mass Transf. **190**, 122796(2022)

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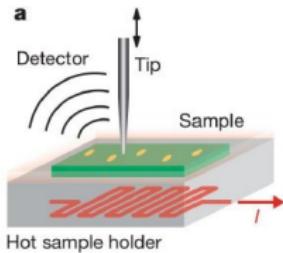
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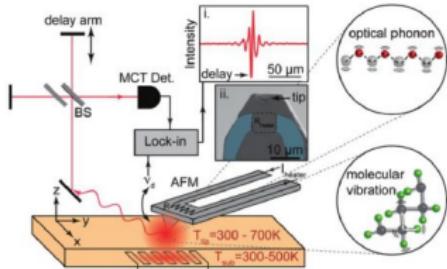
# Near-field thermal imaging

## Thermal radiation tunneling microscope



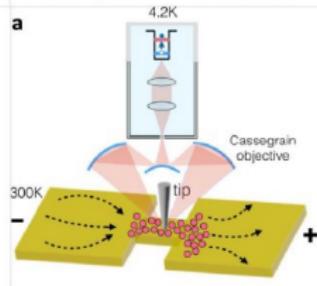
De Wilde et al., Nature 444, 740 (2006)

## Thermal infrared near-field spectroscopy



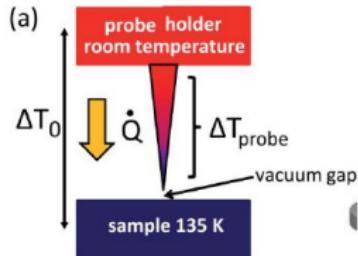
Jones, Raschke, Nano Lett. 12, 1475 (2012)

## Scanning noise microscope



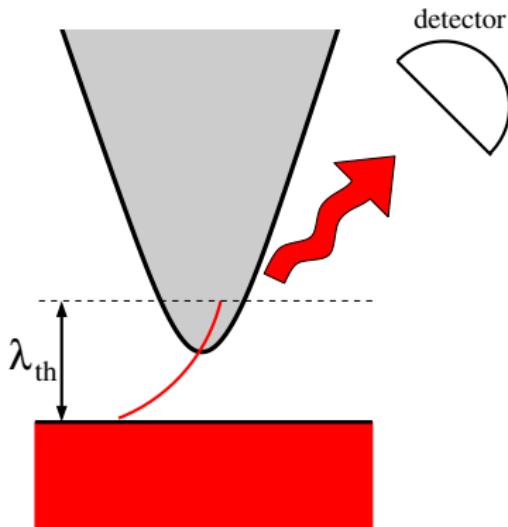
Weng,..,SAB,.., Science 360, 775 (2018)

## Near-field scanning thermal microscope



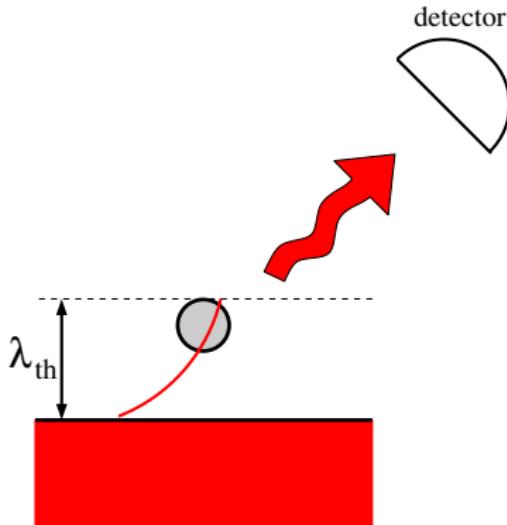
Kittel,..,SAB,.., PRL 95, 224301 (2005)

# Theoretical model



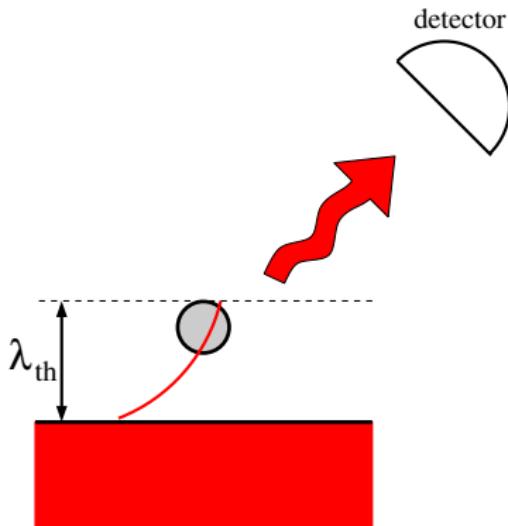
Joulain et al., JQSRT **136**, 1 (2014)  
Herz et al., PRAppl **10**, 044051 (2018)  
Herz, SAB, JQSRT **266**, 107572 (2021)

# Theoretical model

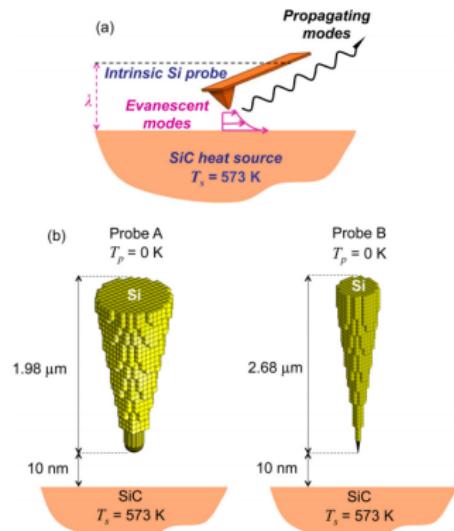


Joulain et al., JQSRT **136**, 1 (2014)  
Herz et al., PRAppl **10**, 044051 (2018)  
Herz, SAB, JQSRT **266**, 107572 (2021)

# Theoretical model



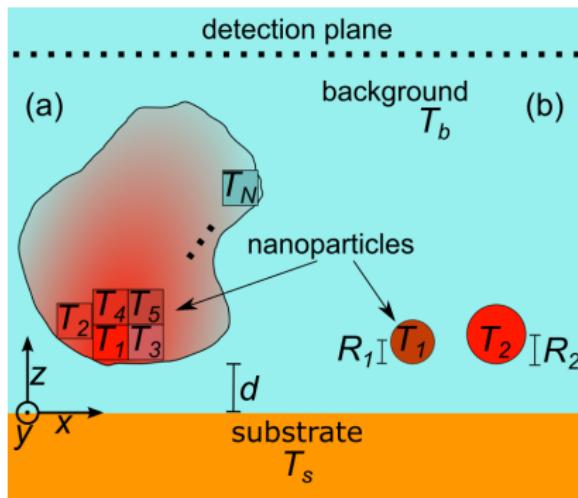
## Discrete Dipole Approximation



Joulain et al., JQSRT **136**, 1 (2014)  
Herz et al., PRAppl **10**, 044051 (2018)  
Herz, SAB, JQSRT **266**, 107572 (2021)

Edalatpour et al., JQSRT **133**, 364 (2014)  
Edalatpour, Francoeur, PRB **94**, 045406 (2016)  
Ekeroth et al., PRB **95**, 235428 (2017)

# Coupled dipole method for far-field thermal radiation

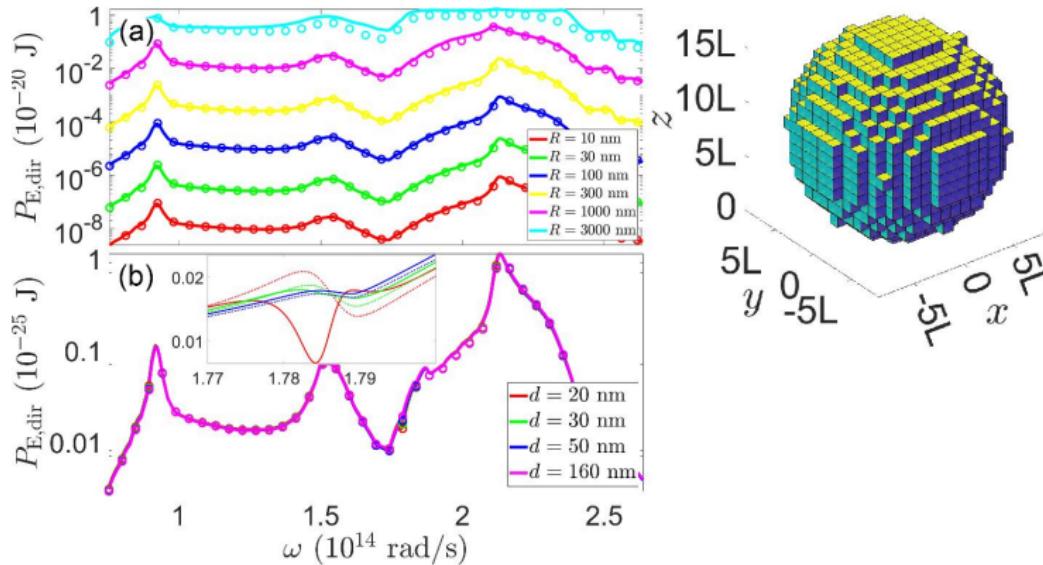


- Fields of  $N$  coupled dipoles + environment
- Electric and magnetic moments
- Local temperatures
  - $T_i$  for each particle
  - $T_s$  for substrate
  - $T_b$  for background
- Power in detection plane

$$\begin{aligned} P &= \int dx \int dy \langle S_z \rangle \\ &= P^{\text{sub}} + P^{\text{dir}} + P^{\text{abs}} + P^{\text{sc}} \end{aligned}$$

Herz, SAB, PRB **105**, 205422(2022)

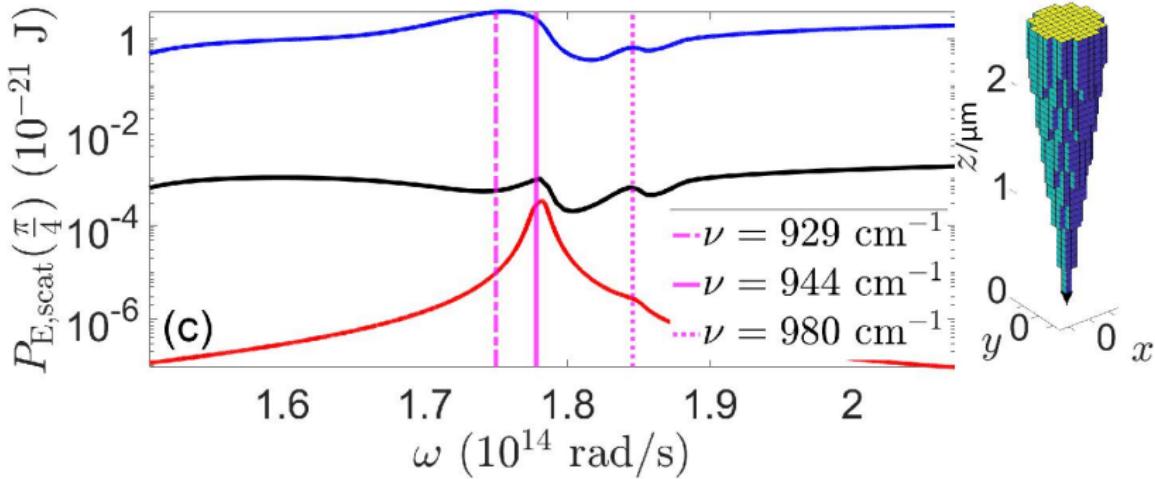
# Direct thermal radiation, SiO<sub>2</sub> sphere ( $N = 2553$ ) (vacuum and SiC substrate)



- Vacuum: agreement with  
Kattawar, Eisner, Appl. Opt. **9**, 2685 (1970) / Ekeroth et al., PRB **95**, 235428 (2017)
- SiC-substrate: coupling with surface waves

Herz, SAB, PRB **105**, 205422(2022)

# Scattering by Si tip above SiC substrate ( $N = 5388$ )



- DDA-results agree with Edalatpour, Francoeur, PRB **94**, 045406 (2016)
- dipole model reproduces most prominent features

## Introduction

Heat transfer in two-body systems

## Near-field heat transfer in many-body systems

Framework and overview

## Non-Reciprocity

Hall effect for thermal radiation (revisited)

Heat flux rectification with non-reciprocal surface waves

## Boltzmann vs. Landauer

## Topology

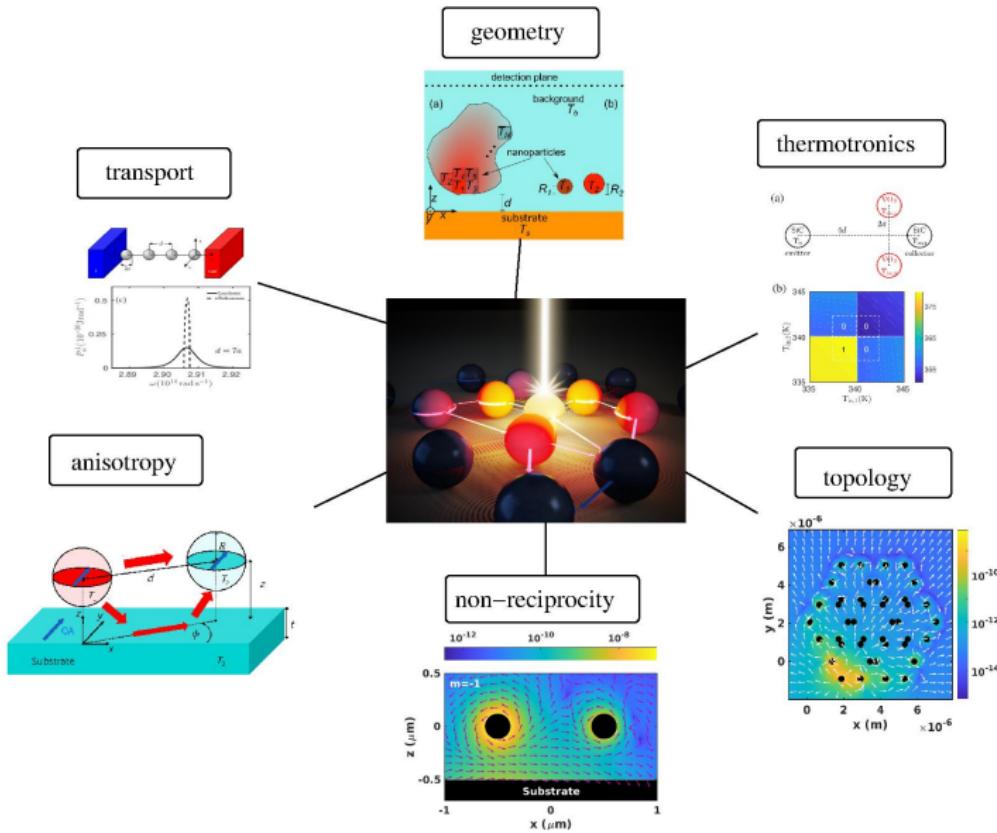
Su-Schrieffer-Heeger model

Honeycomb lattice

## Coupled-dipole method for far-field thermal radiation

## Summary

# Summary



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