

Controlling near-field thermal energy for conversion devices and sensing

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Contributors

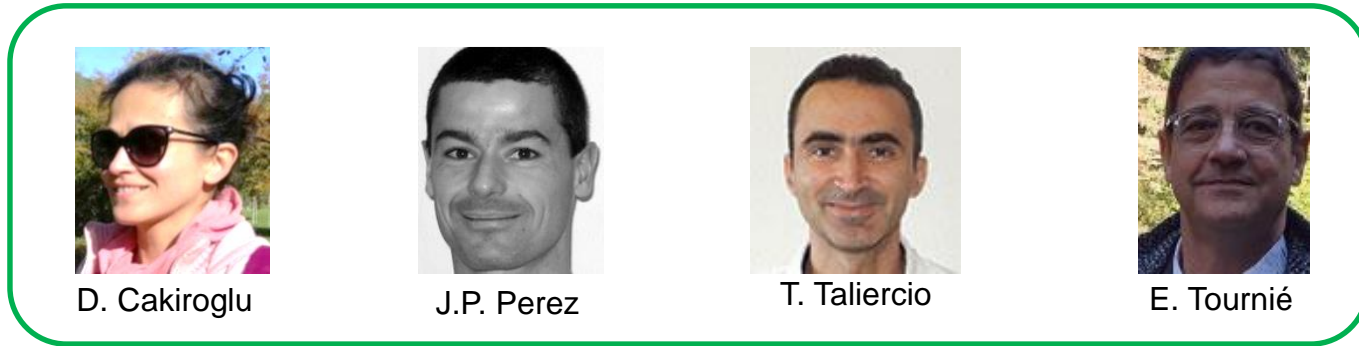
PhD
students



Post-docs



colleagues at
CETHIL



colleagues at
IES Montpellier

Outline

I. Context

II. Near-field thermal radiation vs T

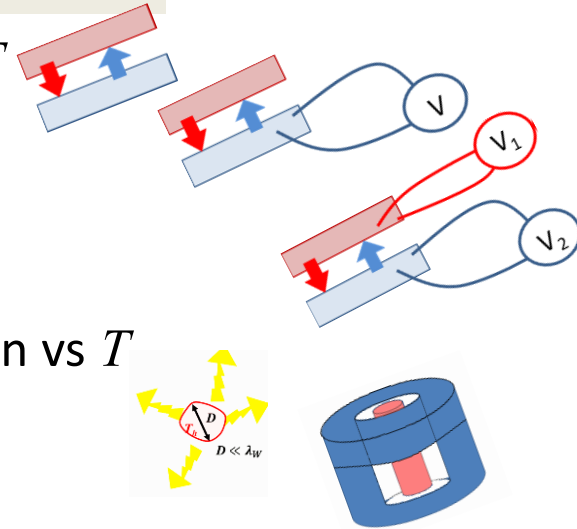
III. Near-field thermophotovoltaics

IV. Near-field thermophotonics

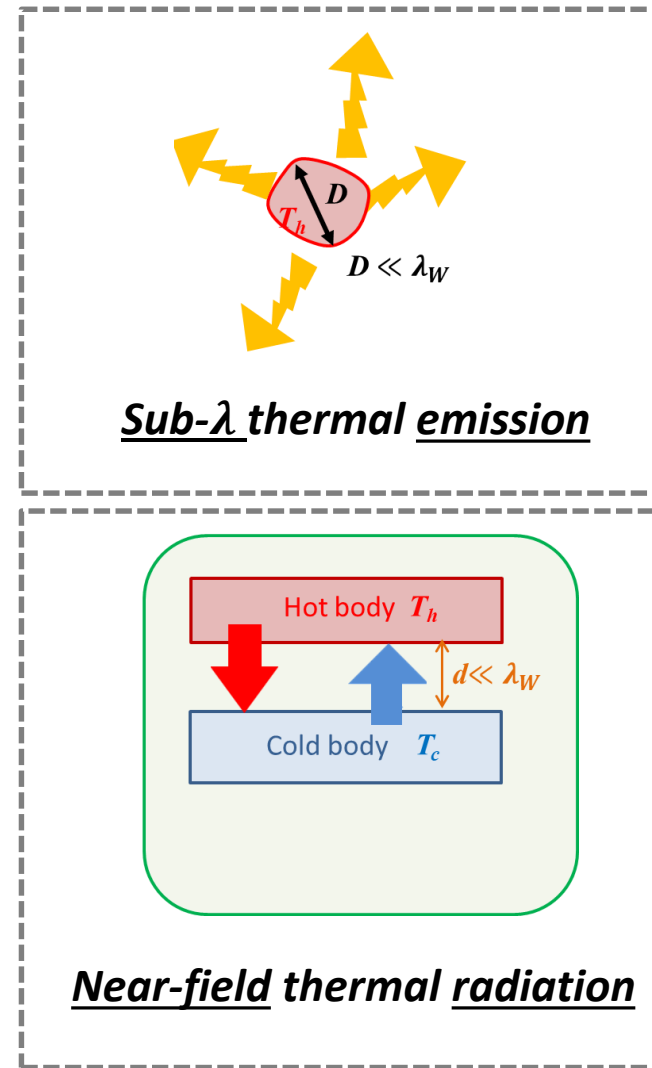
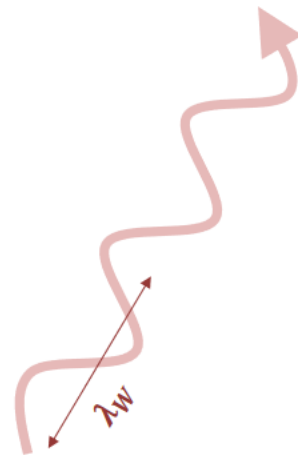
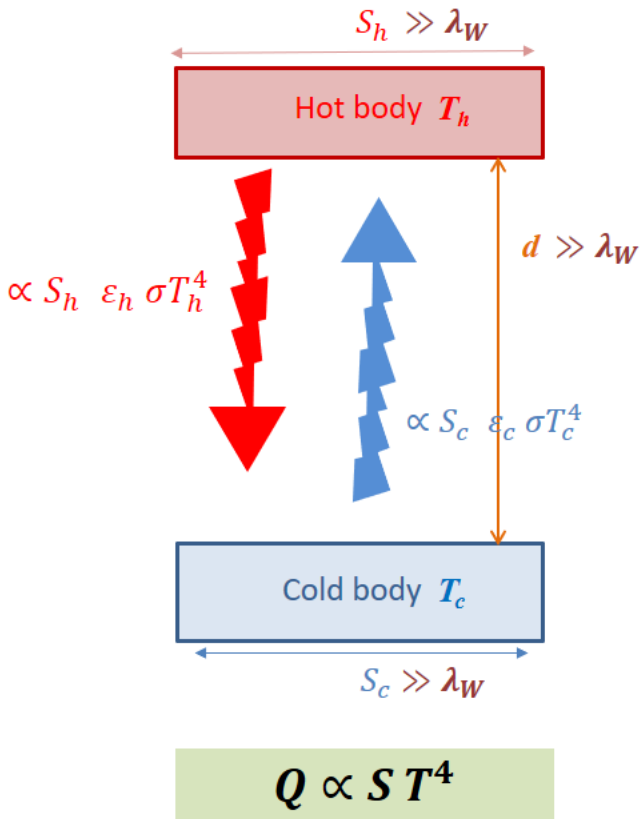
V. Sub-wavelength thermal emission vs T

VI. Concentric cylinders

VII. Some prospects



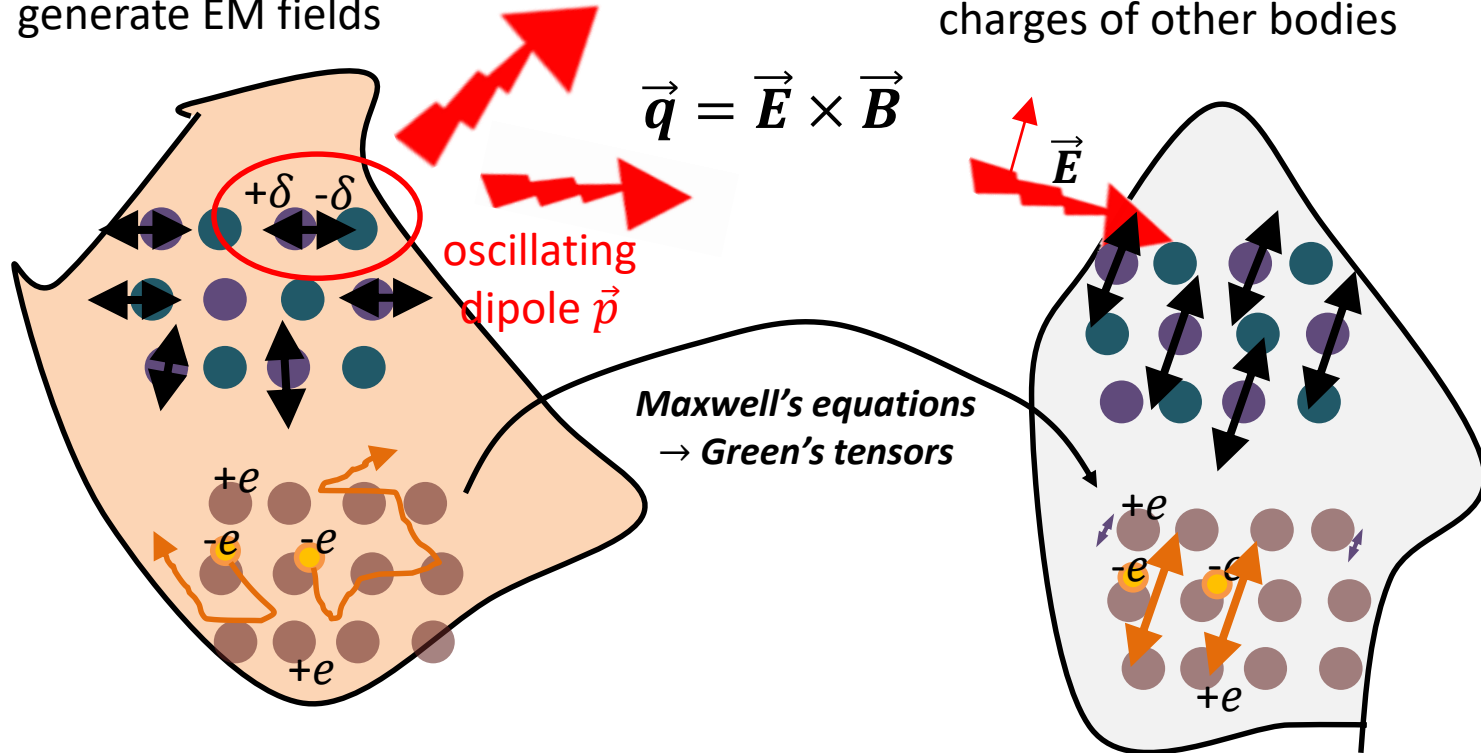
Thermal radiation involving small sizes...



Back to basics...

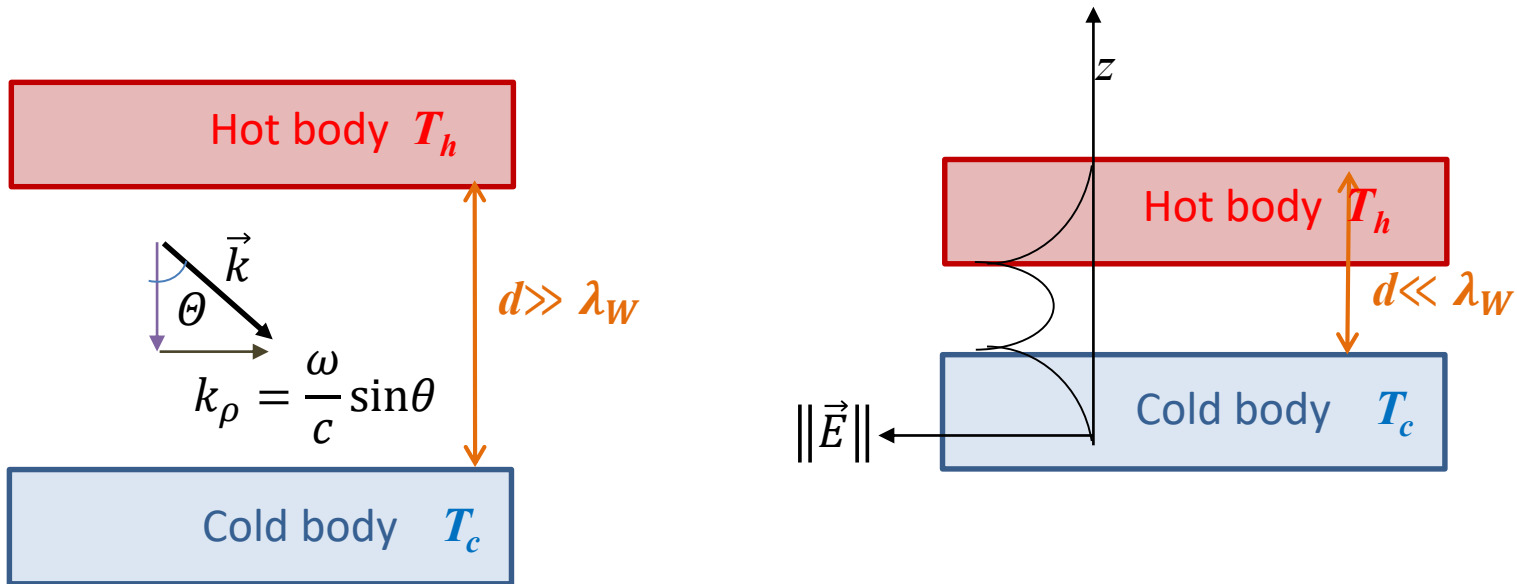
Random motion of charges generate EM fields

These fields act on charges of other bodies



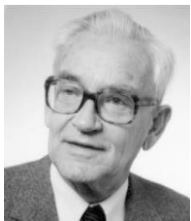
FDT + Maxwell's equations = Fluctuational Electrodynamics

Fundamentals: thermal radiation between 2 surfaces



$$q = \sum_{pol=TE,TM} \int d\omega \frac{\omega^2}{4\pi^2 c^2} \hbar\omega \left(\frac{1}{e^{\hbar\omega/T_{hot}} - 1} - \frac{1}{e^{\hbar\omega/T_{cold}} - 1} \right) \left[\int_0^{\frac{\omega}{c}} dk_\rho \tau_{prop}^{pol}(\omega, k_\rho) + \int_{\frac{\omega}{c}}^\infty dk_\rho \tau_{evan}^{pol}(\omega, k_\rho) \right]$$

Planck's law
 $e(\omega)$
(generalized)
emissivity
photon
tunneling
at nanoscale



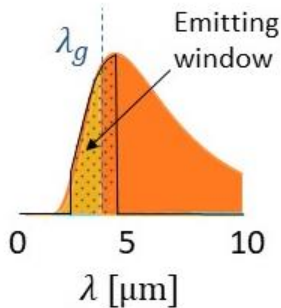
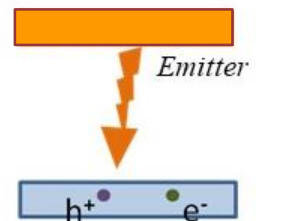
Polder & Van Hove, PRB (1971)

$$x = \frac{\hbar\omega}{k_B T} = \frac{cst}{\lambda T} \longrightarrow d \cdot T$$

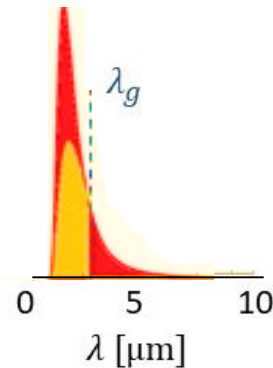
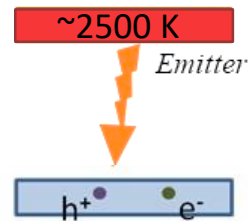
$$\tau_{evan}^{pol}(\omega, k_\rho) \propto e^{-2|k_z|d}$$

Converting thermal energy into electrical power...

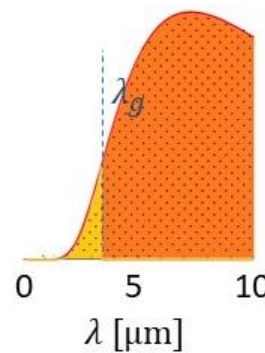
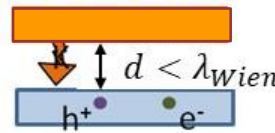
Thermo-
photovoltaics



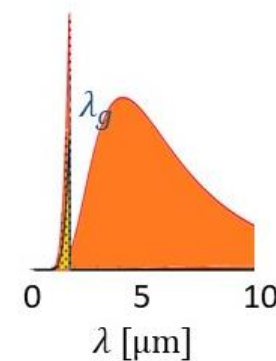
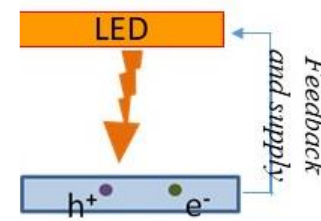
High-temperature
TPV



Near-field TPV



Thermophotonics



Hybrid
devices

TPV
+
TE
TI
etc.

~~Planck's law~~

~~$$n(\omega, T) = \frac{1}{\frac{\hbar\omega}{e^{k_B T} - 1}}$$~~

~~$$q_{max} = \sigma T^4$$

$$h_{max} = \frac{q}{\Delta T} = 4\sigma T^3$$~~

...breaking Planck/Bose-Einstein limits

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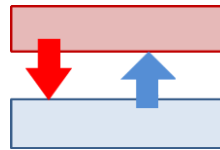
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IV. Near-field thermophotonics

V. Sub-wavelength thermal emission vs T

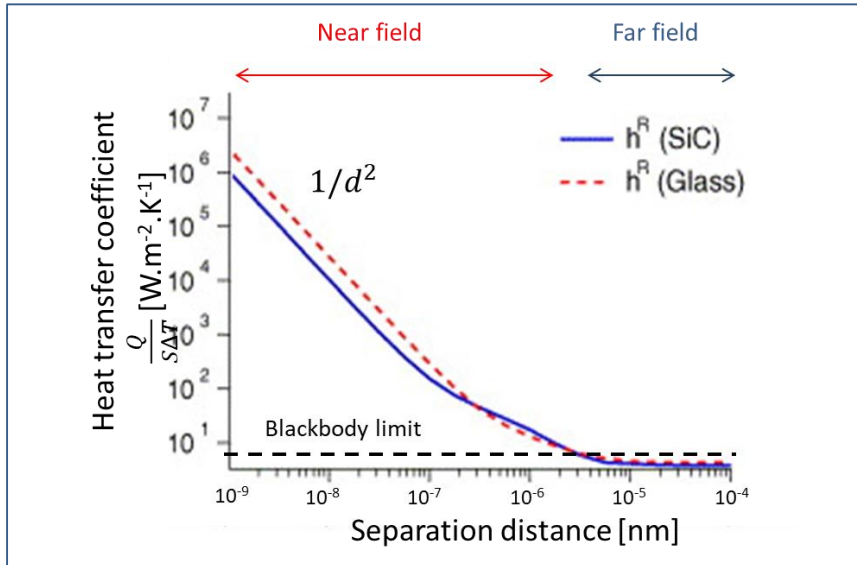
VI. Concentric cylinders

VII. Some prospects

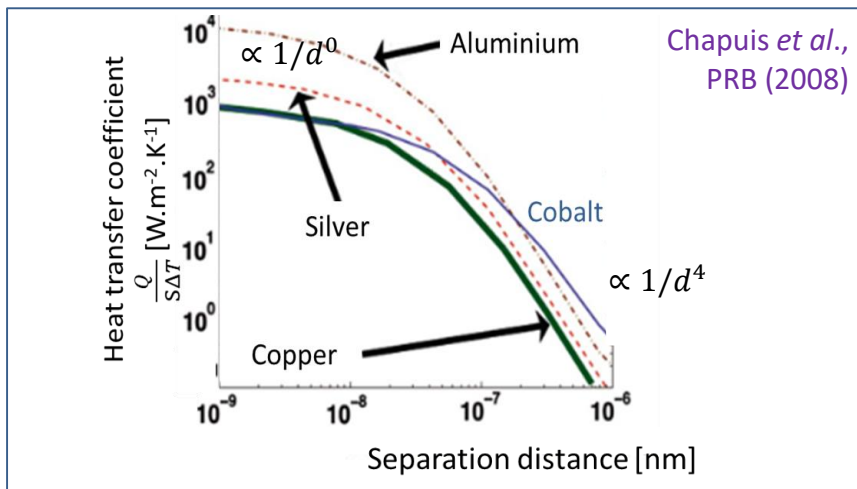
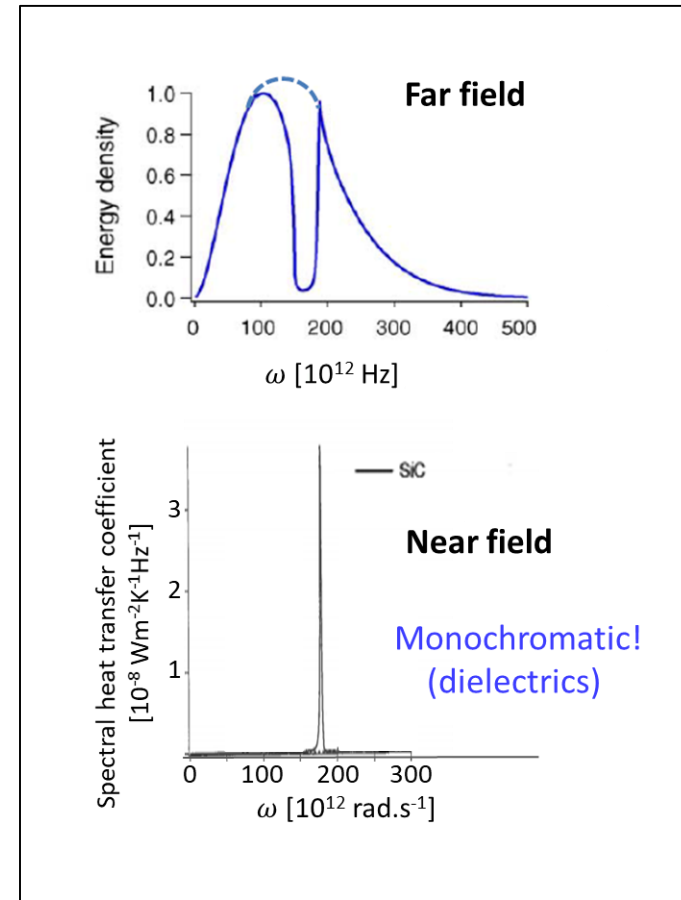


Features of near-field transfer between surfaces

Mulet *et al.*, MTE (2002)



From Shchegrov *et al.*, PRL (2000)

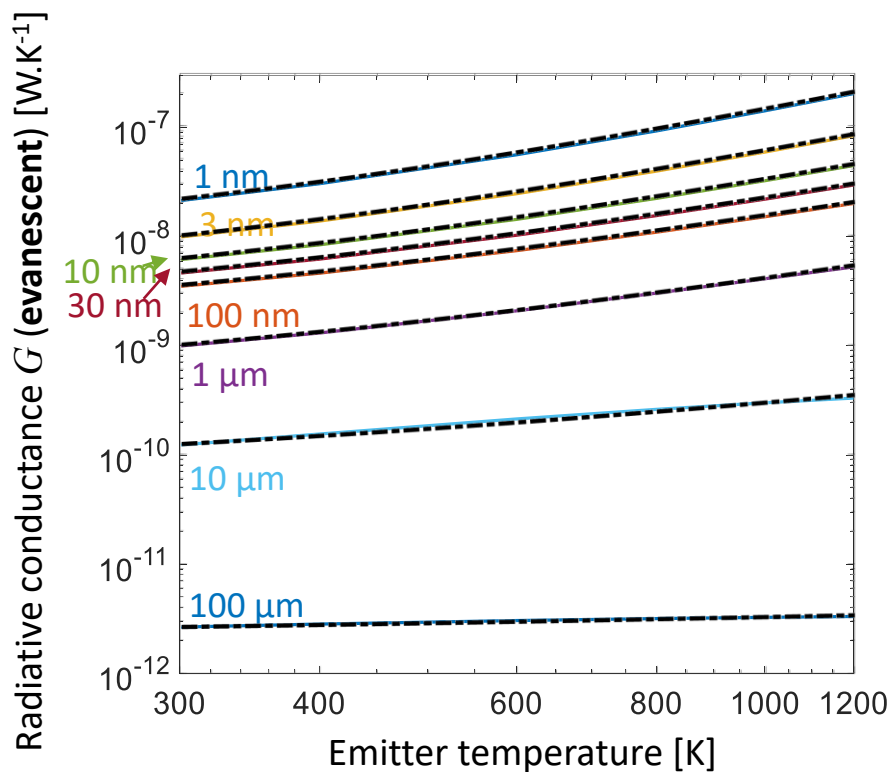


Modification of spectrum

Effect of temperature?

Enhancement of heat flux

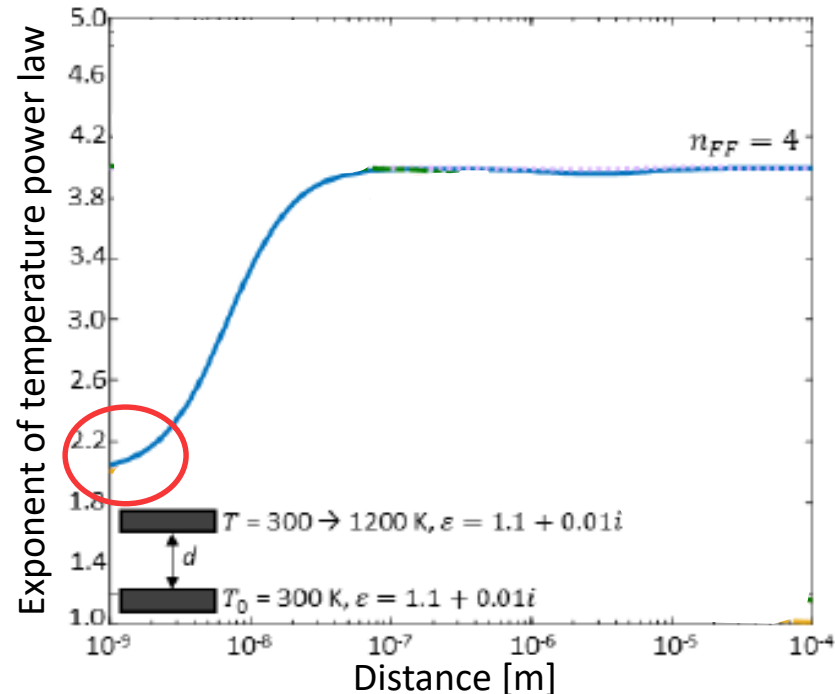
Stefan-Boltzmann's law in near field?



$$q = \sigma T^4 \longrightarrow q \propto T^2$$

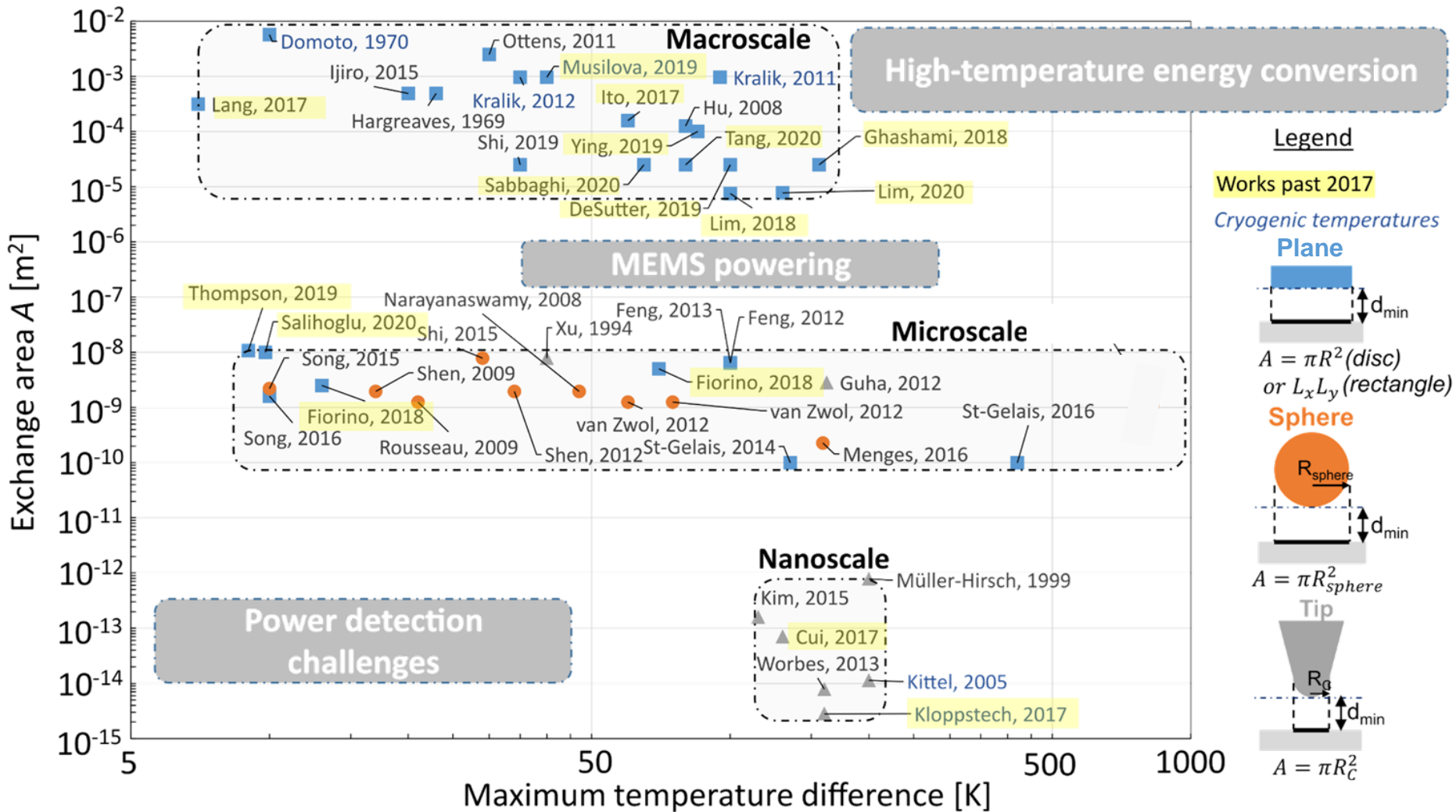
$$G = \frac{Q}{\Delta T} = \underset{\text{pre-factor}}{C\sigma} \frac{T^n - T_0^n}{T - T_0}$$

exponent

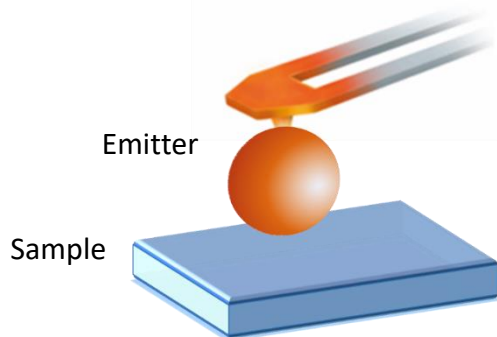
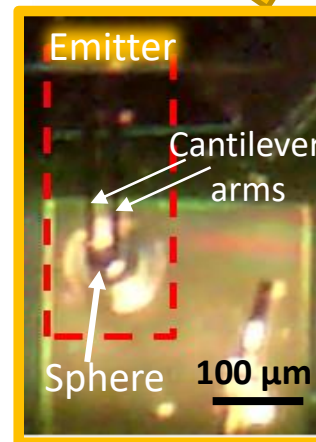
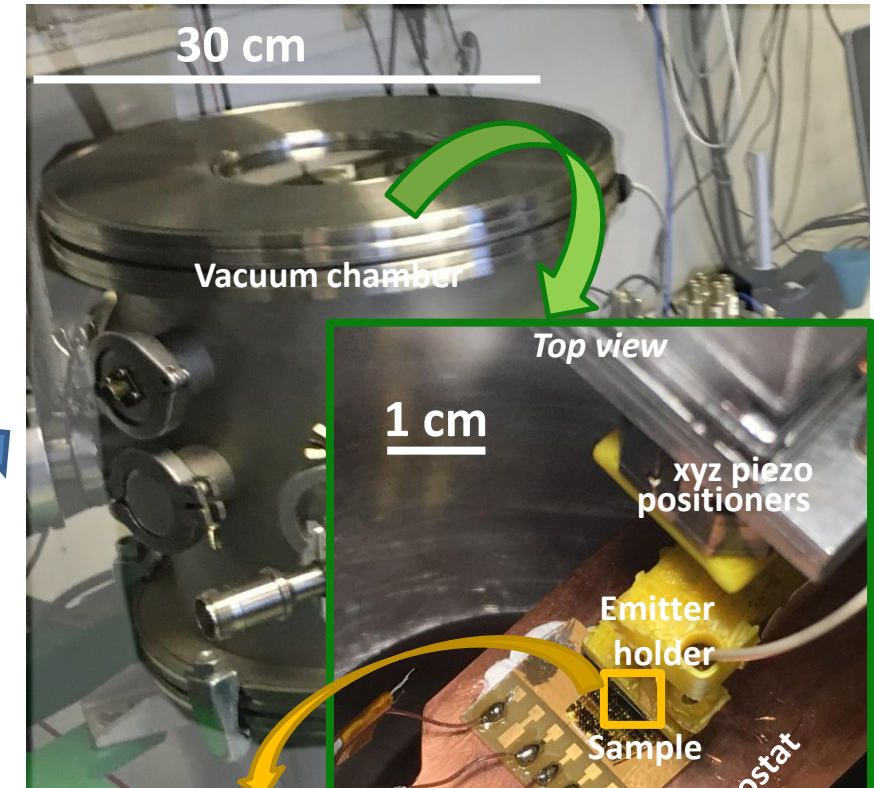
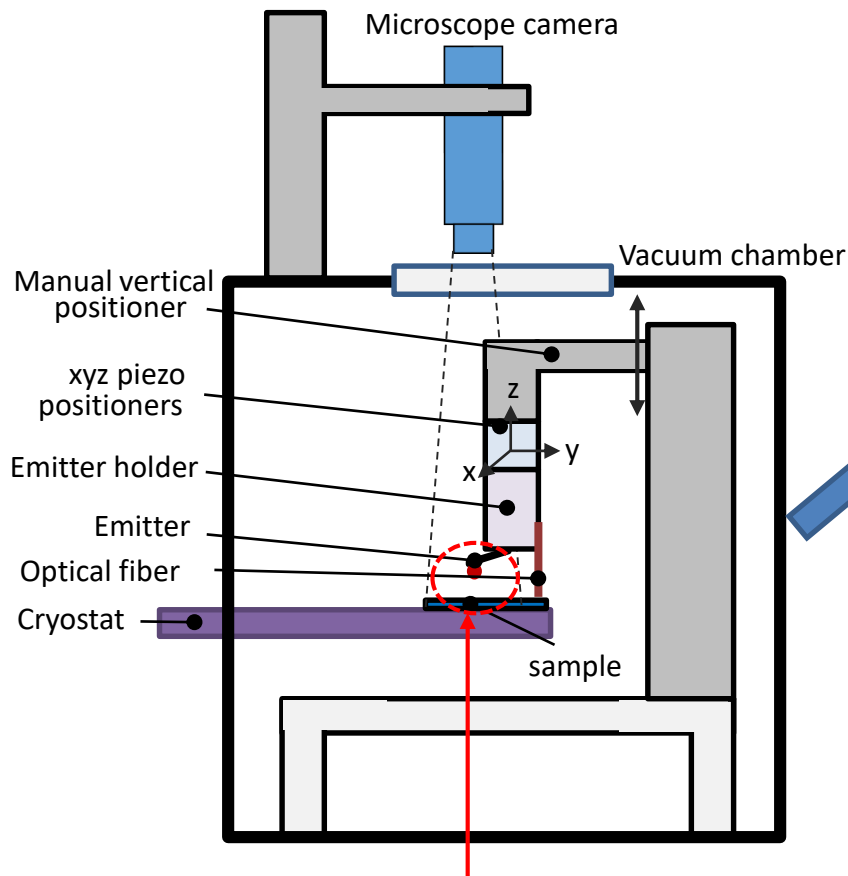


Temperature exponent seems different

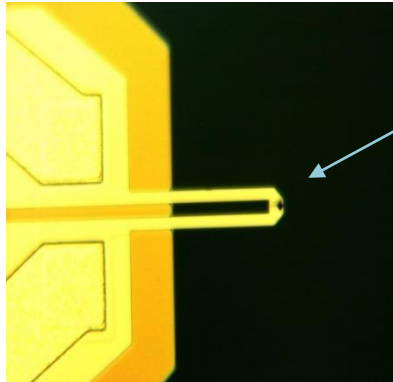
>40 experiments in the last decade



Our microsphere near-field experiment

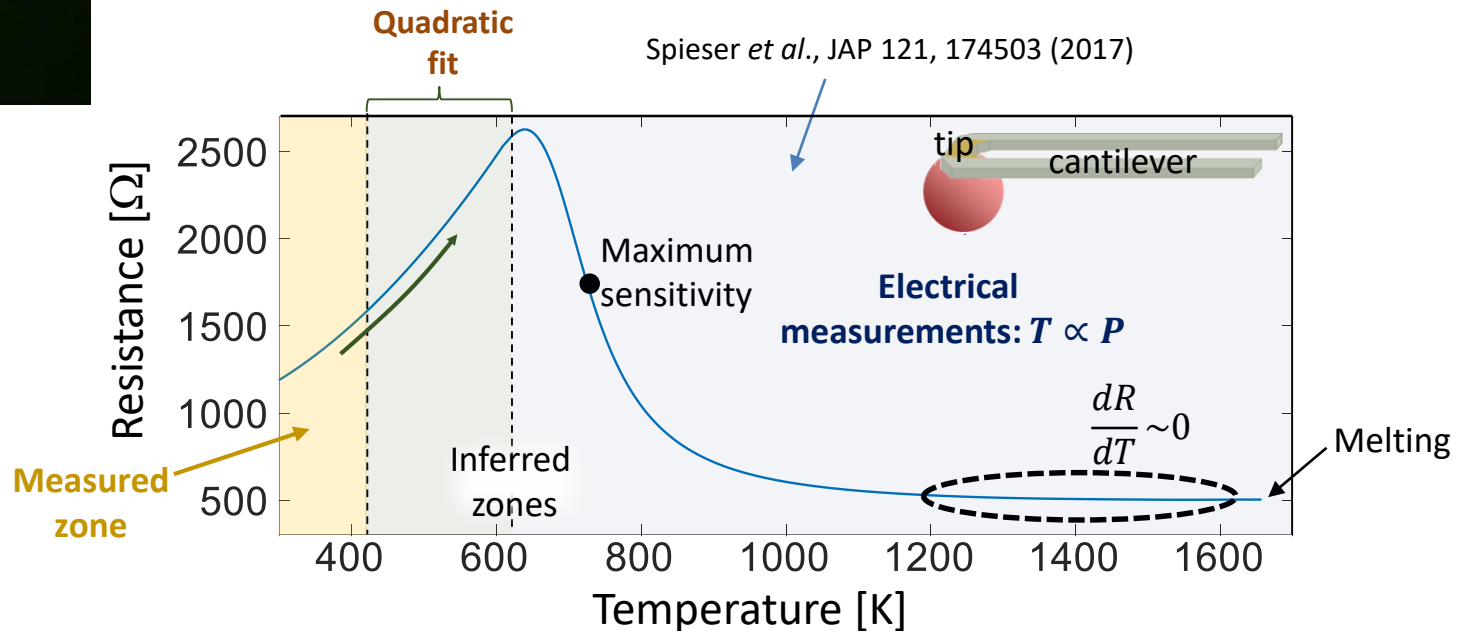


Measurement of emitter temperature: $R(T)$



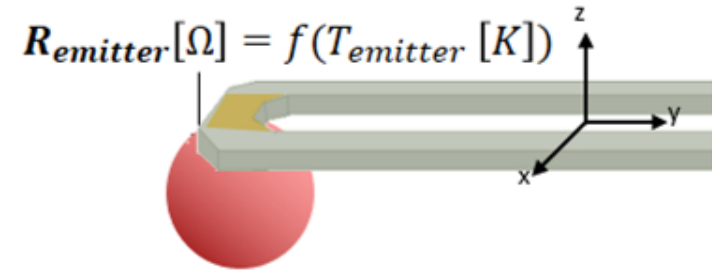
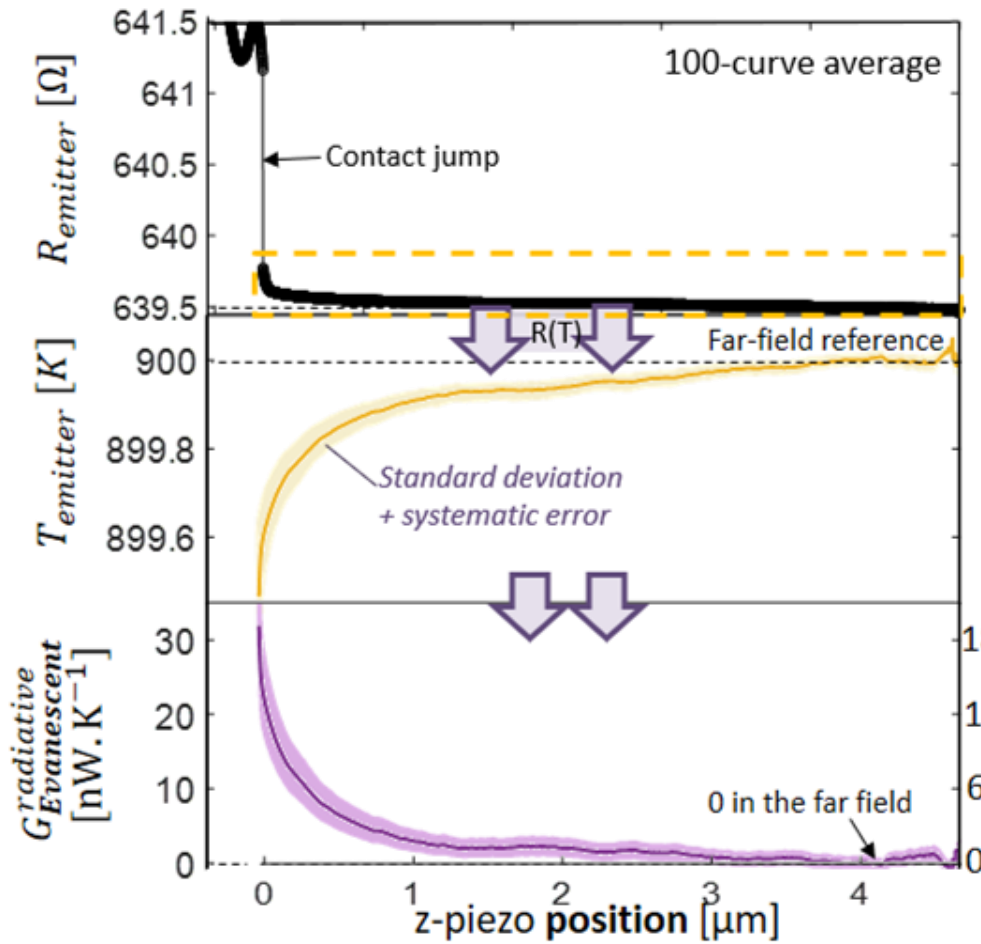
self-heating RI^2

→ Resistive thermometry



Better calibration: Piqueras et al.

Approach curves and radiative heat transfer



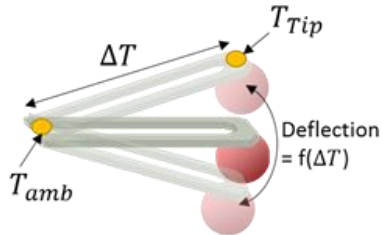
Sample vacuum

$$\frac{\Delta G_{tot}}{G_{tot}} = \frac{\Delta P}{P} - \frac{\Delta \theta}{\theta}$$

$$G_{NF} = G_{tot} \left[(T_{ref} - T) \left(\frac{1}{\theta} - \alpha \right) + 2 \frac{I - I_{ref}}{I} \right]$$

Distance uncertainties

- Temperature gradient



Measured by AFM

Negligible for small temperature variations

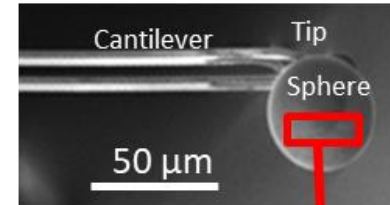
- Attraction forces



Measured by AFM

3 nm

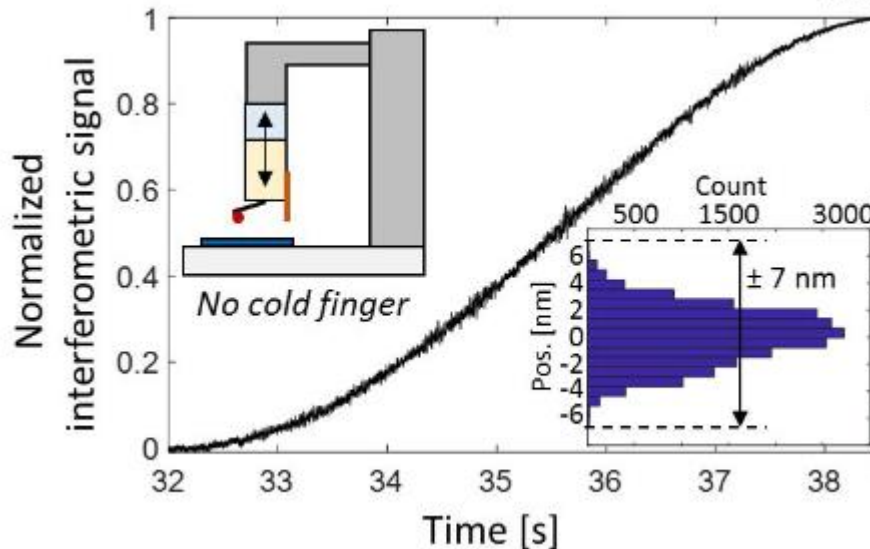
- Roughness



Measured by AFM

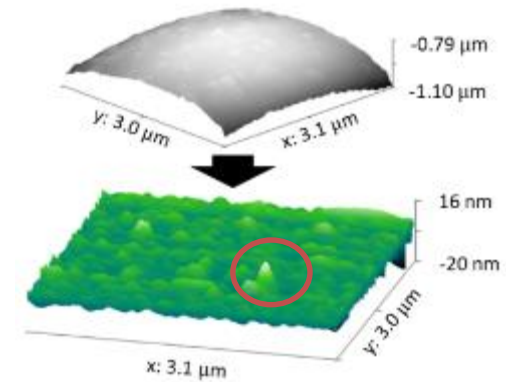
max = 30 nm

- Mechanical vibrations → measured by interferometry



Maximum measured amplitude = 7 nm

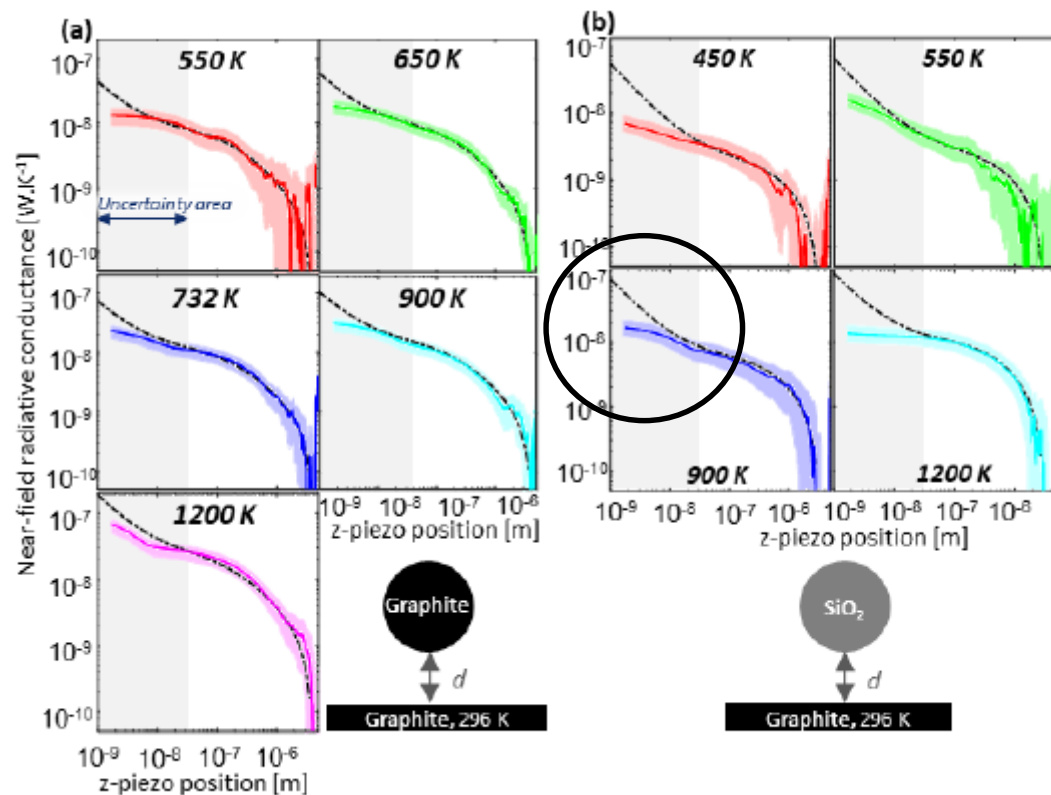
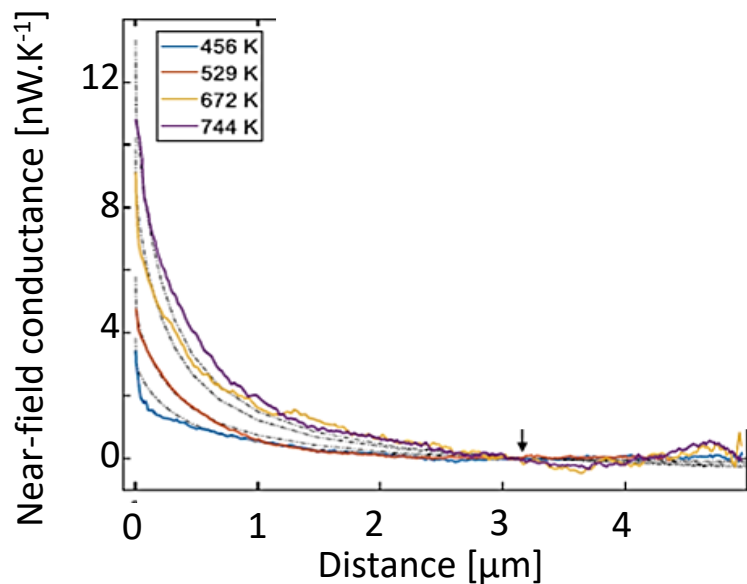
for sample at room temperature



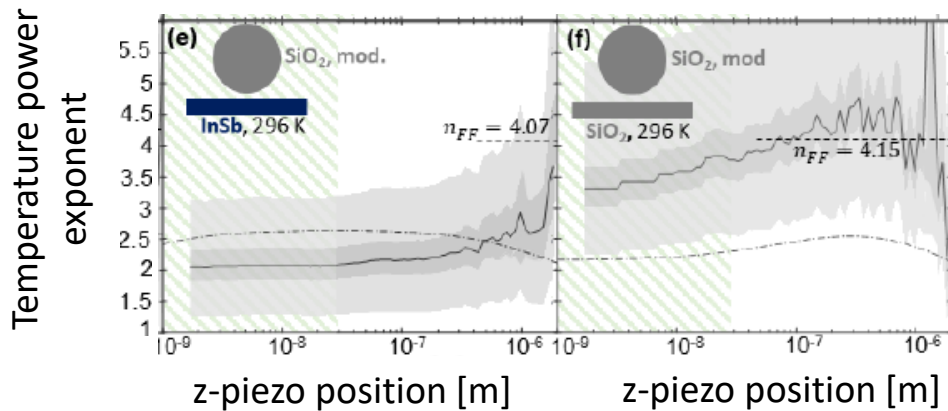
~~rms~~ sparse peaks!

≈ 30 nm

Approach curves as a function of temperature



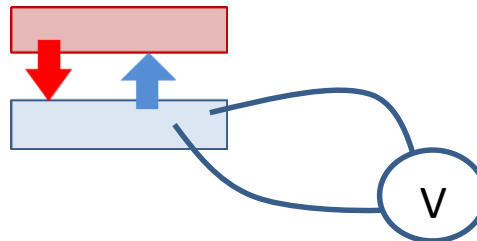
Temperature exponent in near field



Sphere-substrate configuration	ΔT_{max} [K]	Maximum conductance at ΔT_{max} [nW.K ⁻¹]	Temperature power law exponent of the near-field radiative conductance		
			Far-field (calculated)	$d = 100$ nm	
				Calculated	Measured
Graphite-SiO ₂	477	4.9 ± 1.0	4.30	2.88	2.84 ± 0.31
Modified SiO ₂ -SiO ₂	493	7.4 ± 1.5	4.15	2.46	4.11 ± 0.42
Modified SiO ₂ -InSb	904	7.6 ± 2.1	4.07	2.61	2.21 ± 0.27
Graphite-InSb	448	10.8 ± 2.1	4.18	3.01	3.67 ± 0.39
Modified SiO ₂ -Graphite	904	16.7 ± 3.3 (at $\Delta T = 604$ K)	4.30	2.89	2.80 ± 0.36
Graphite-Graphite	904	68.9 ± 13.7	4.32	2.82	2.92 ± 0.31

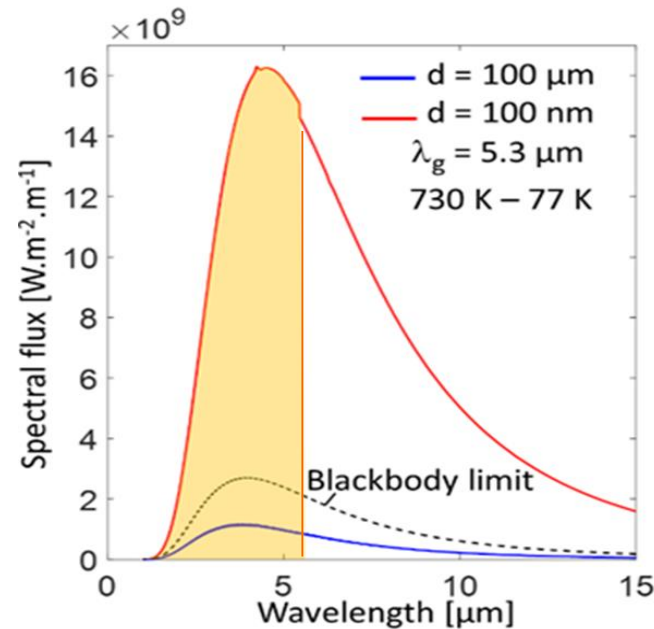
Softening of temperature dependence in near field

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Efficient near-field thermophotovoltaic conversion?

no experiment with efficiency above 1% in 2020...



Work	Cell	E_g [eV]	Emitter T [K]	Efficiency [%]	P [W.cm^{-2}]
Bhatt <i>et al.</i> ³ , Nat. Com. 2020	Ge	0.67 at 300 K	880	0.003 estimated	$1.3 \cdot 10^{-6}$
Inoue <i>et al.</i> ² , Nano Lett. 2019	InGaAs	0.73 at 300 K	1065	0.98 estimated	$7.5 \cdot 10^{-4}$
Fiorino <i>et al.</i> ¹ , Nat. Nano 2018	InAsSb	0.35 at 300 K	655	0.015 estimated	$3.4 \cdot 10^{-5}$
Mittapaly <i>et al.</i> ¹ , Nat. Com. 2021	InAsSb	0.35 at 300 K	1250	~8	0.5
Lucchesi et al., 2019	InSb	0.23 at 77 K	~700		

Near-field TPV cell design

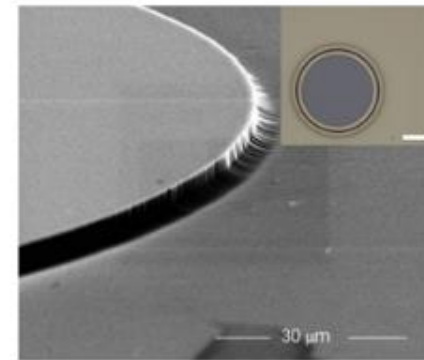
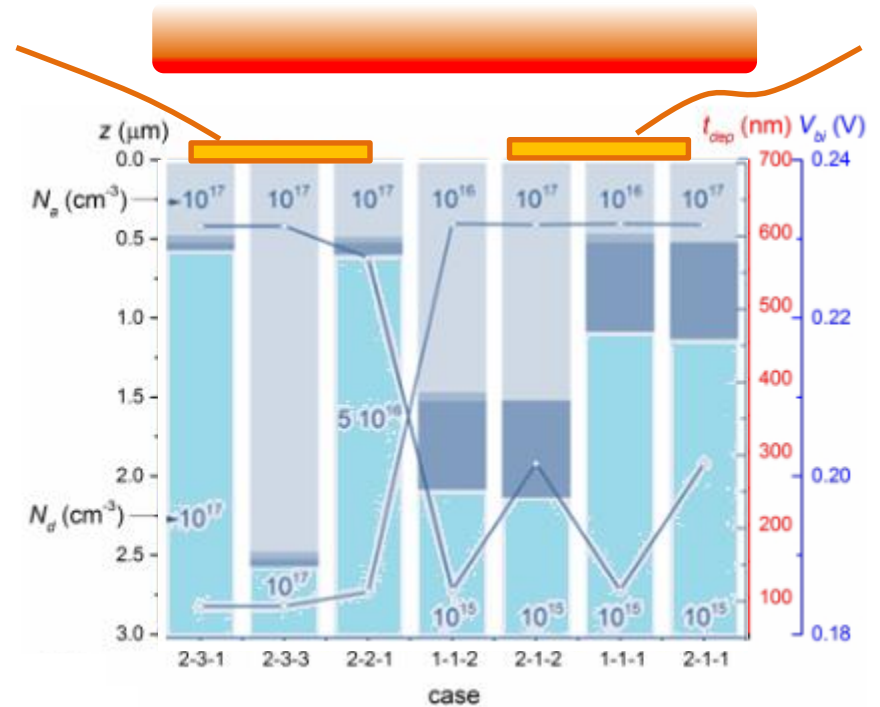
$$\frac{dE}{dz}(z) = -\frac{e}{\epsilon}(n(z) - p(z) + N_a(z) - N_d(z))$$

Poisson

$$\left. \begin{aligned} \frac{dJ_n}{dz}(z) &= -e(R(z) - G(z)) \\ \frac{dJ_p}{dz}(z) &= e(R(z) - G(z)) \end{aligned} \right\} \text{Continuity}$$

$$\left. \begin{aligned} J_n &= e \cdot n(z)\mu_n E(z) + e \cdot D_n \frac{dn}{dz}(z) \\ J_p &= e \cdot p(z)\mu_p E(z) - e \cdot D_p \frac{dp}{dz}(z) \end{aligned} \right\} \text{Drift-diffusion}$$

- Non-linearities
 - Coupled equations
- **iterative** process

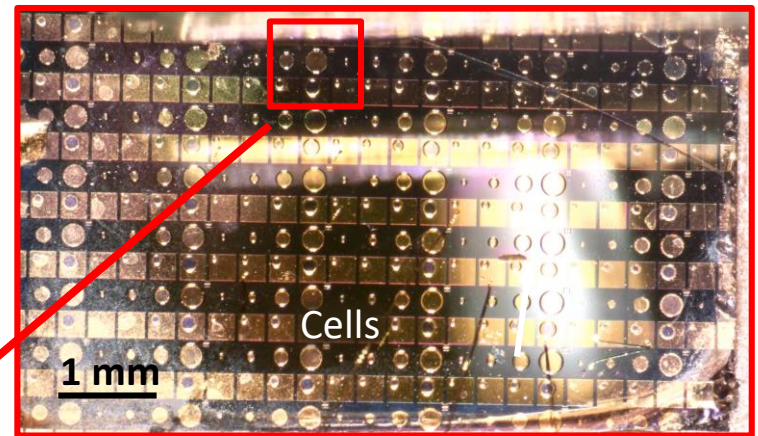
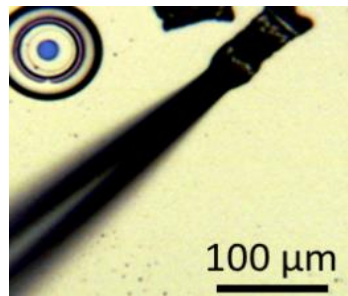
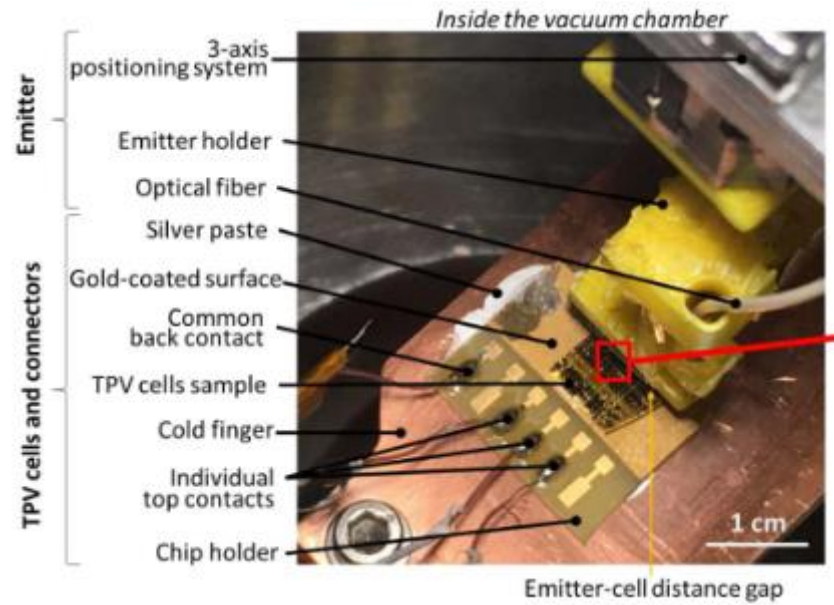
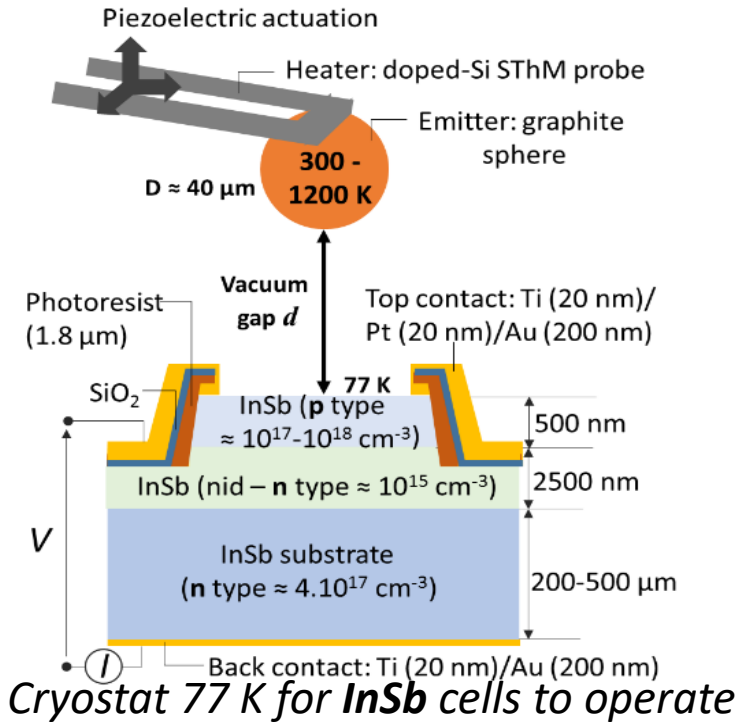


Mesa geometry

see also Francoeur et al.,
Tervo et al., and Feng et al.

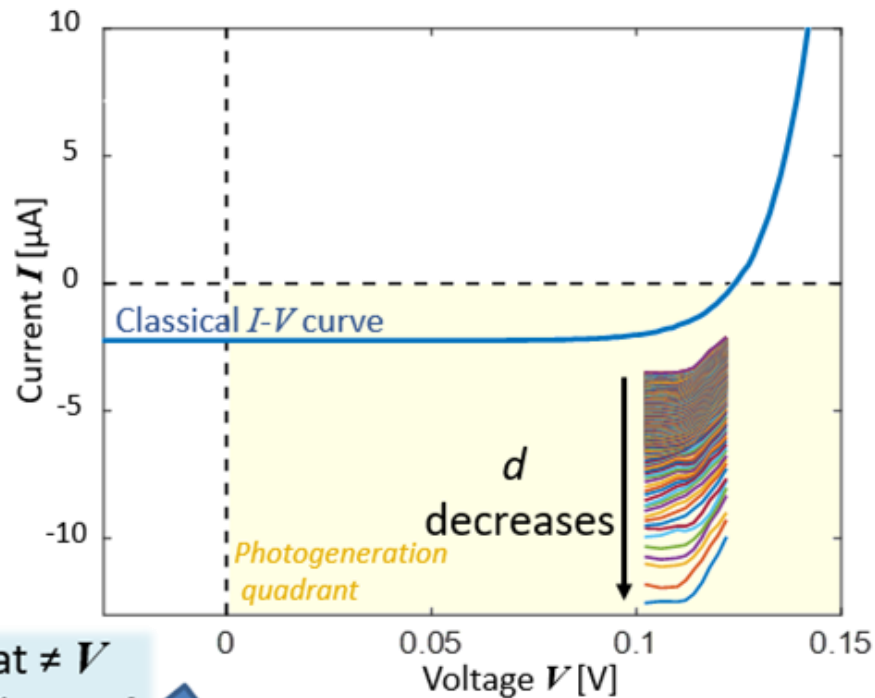
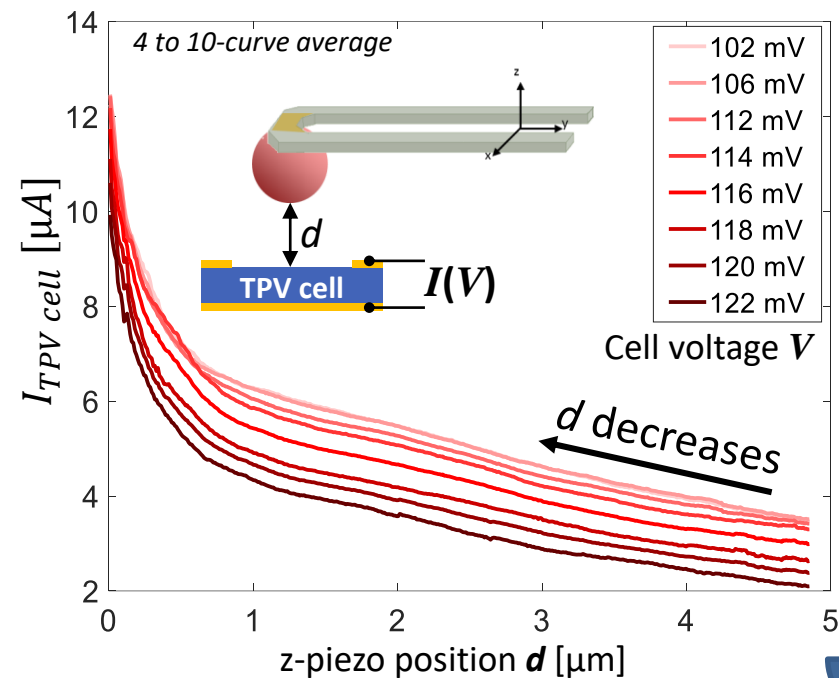
Vaillon et al., Optics Express 24, 347515 (2019)
Cakiroglu et al., Sol. Mat. 203, 110190 (2019)

Near-field TPV cell design



Output power measurement as a function of distance

Fixed V , $I(d)$ measurements

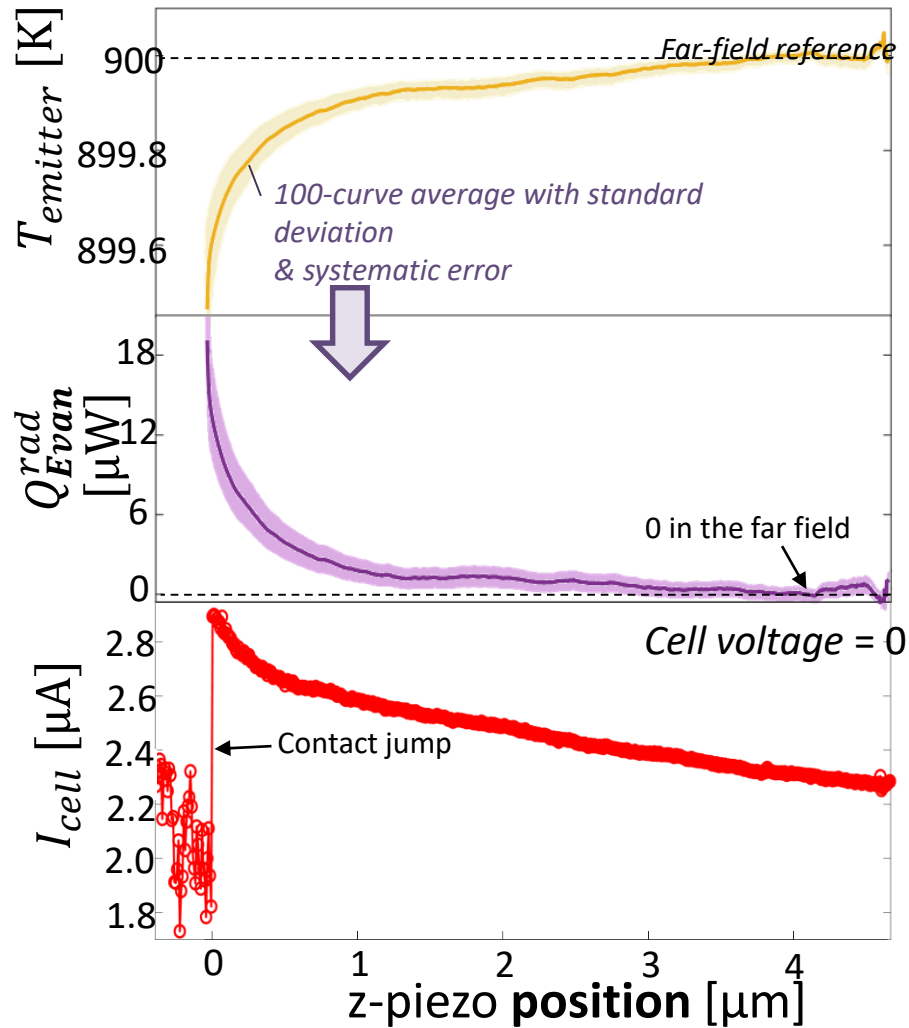


$I(d)$ at $\neq V$
 $\rightarrow I(V)$ at $\neq d$

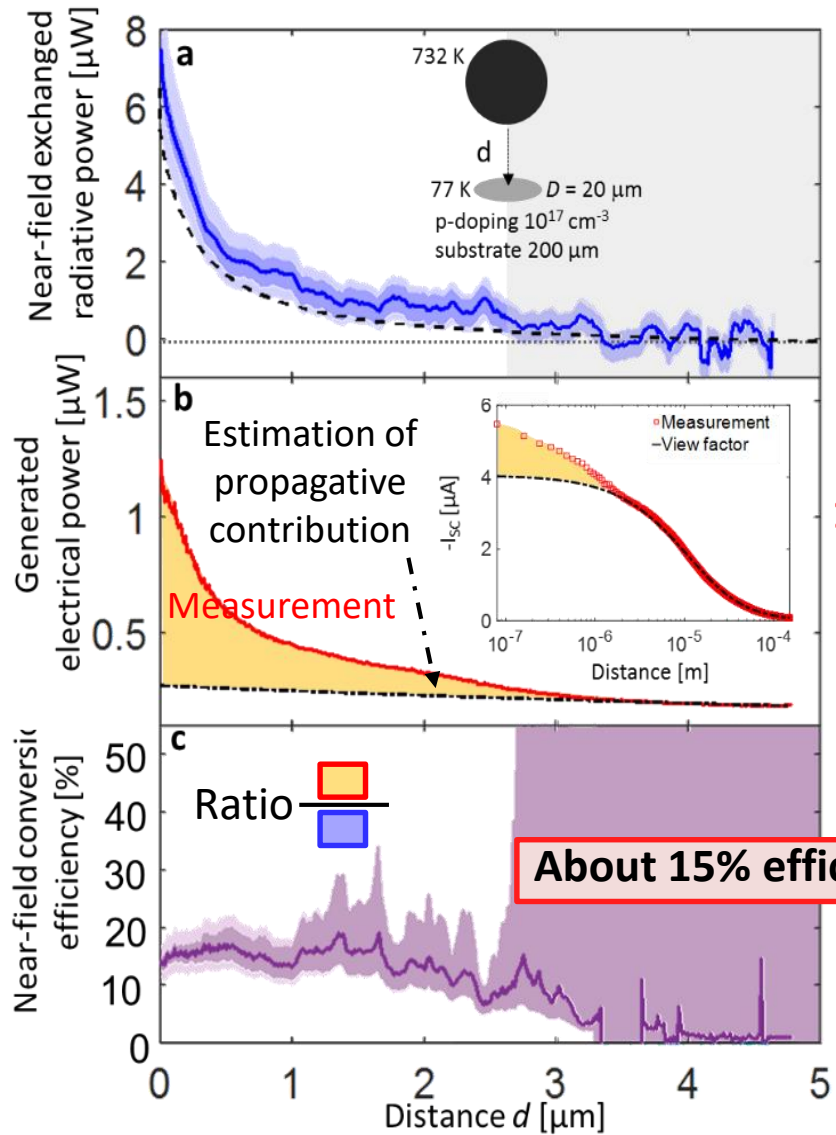
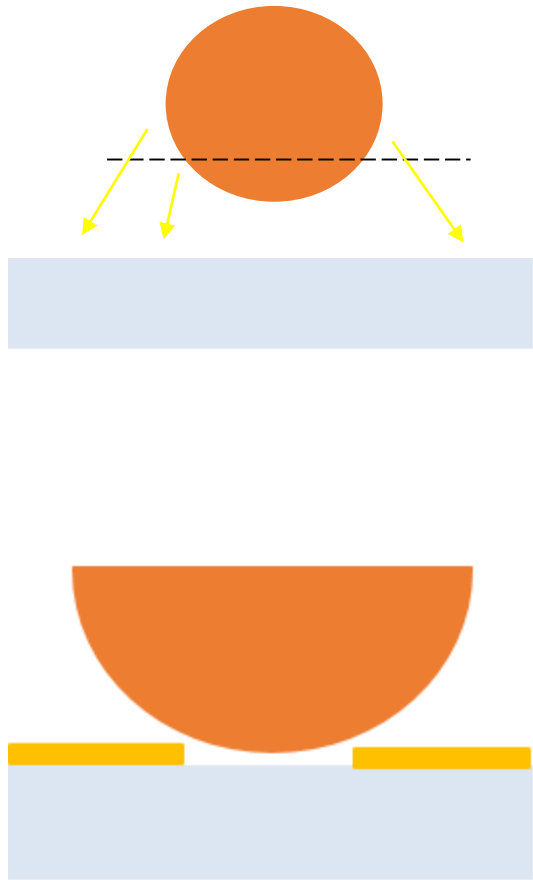
\rightarrow Reconstruction of $I(V) = f(d)$

\rightarrow Maximum power as a function of distance

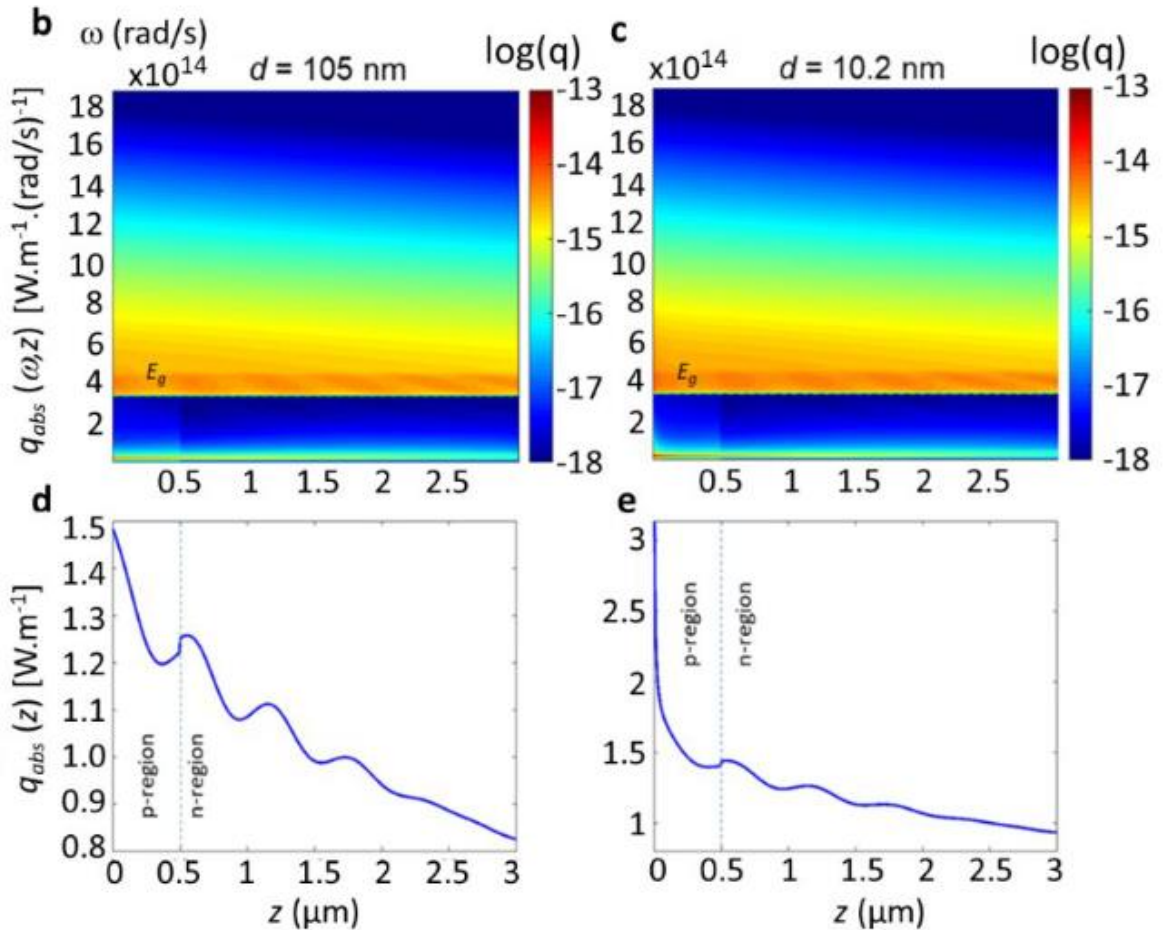
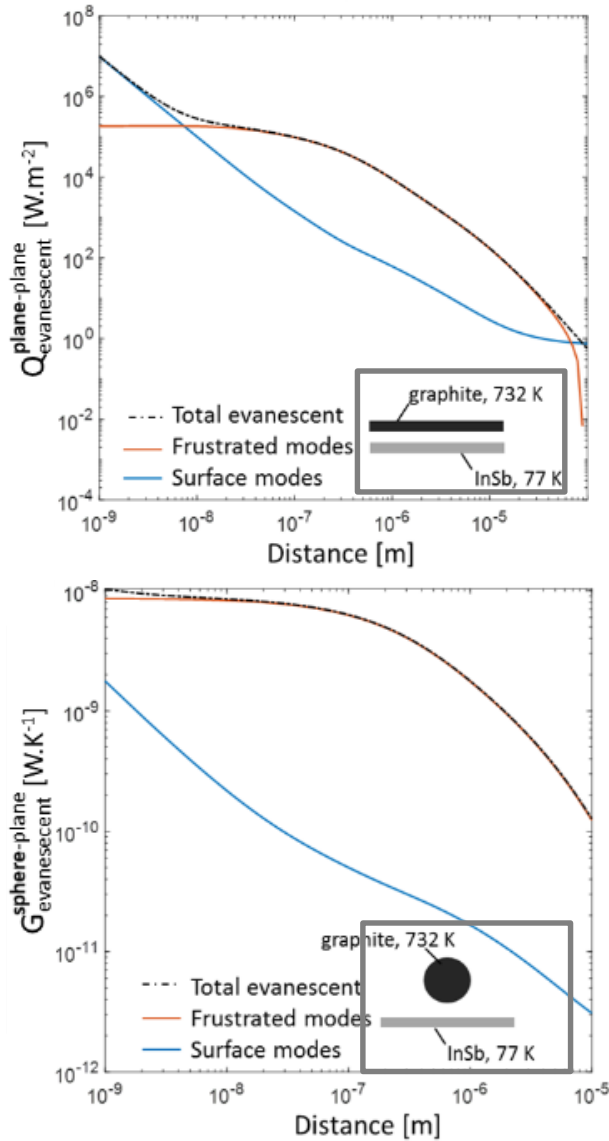
Contact determination...



Near-field thermophotovoltaic conversion

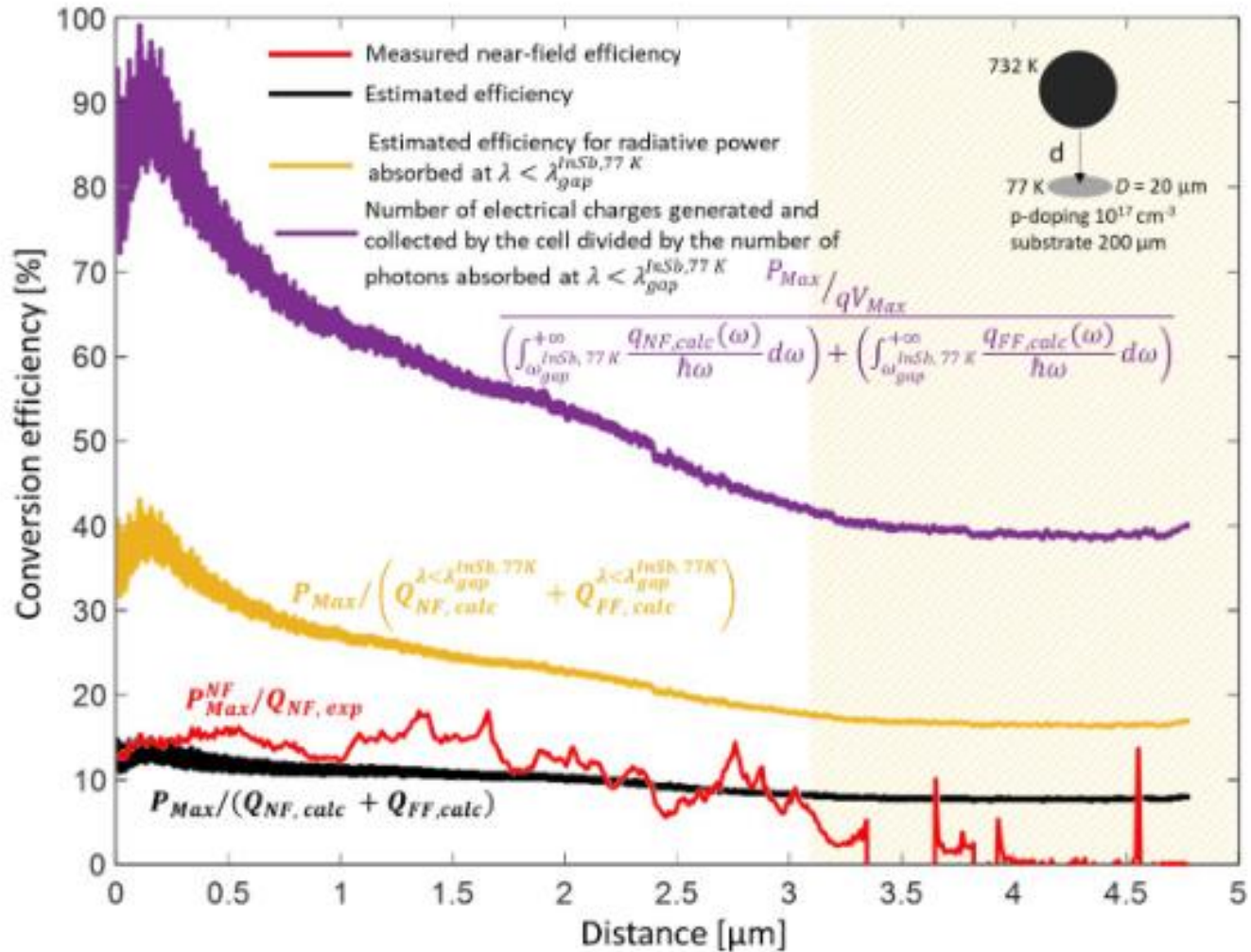


Which modes contribute?



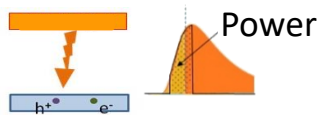
Frustrated modes!

Photon conversion into electron-hole pairs



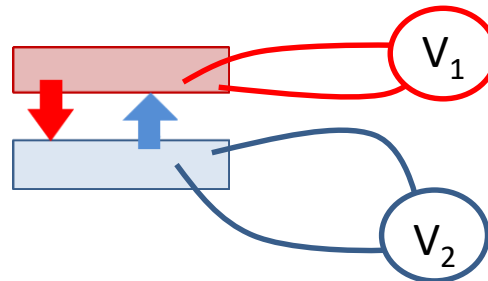
Current SoA for near-field thermophotovoltaics

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Lucchesi et al., 2019	InSb	0.23 at 77 K	~700	14.1 ± 2.9 <i>measured</i> <i>(near-field)</i>	0.75

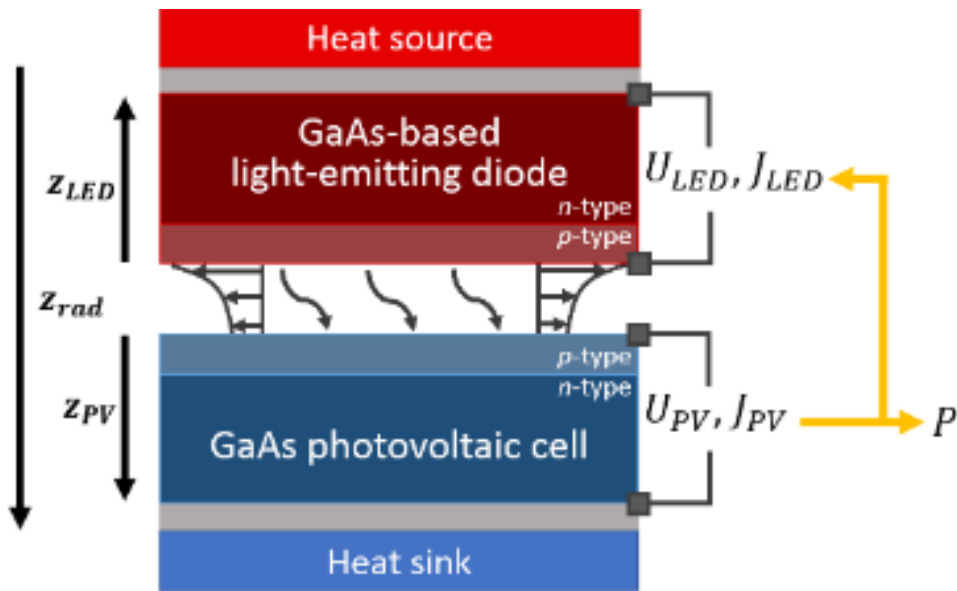


- Low-bandgap semiconductors allow for both high efficiency and high power output
- **Need now to be developed at room temperature**

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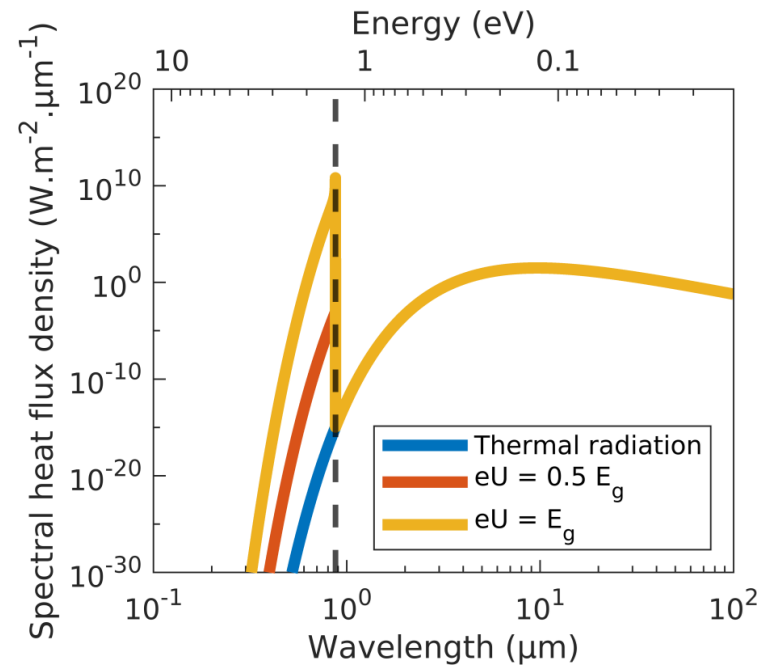
Controlling also the emitter spectrum... thermophotonics (TPX)



Harder & Green, SST(2003)
see also Oksanen et al.

Near-field: see Zhao *et al.* Nano Lett. 18, 5224 (2018)

Modified Planck's law



$$n^0(\omega, U, T) = \begin{cases} \left[e^{\frac{\hbar\omega}{k_B T}} - 1 \right]^{-1} & , \hbar\omega < E_g \\ \left[e^{\frac{\hbar\omega - eU}{k_B T}} - 1 \right]^{-1} & , \hbar\omega \geq E_g \end{cases}$$

Nonidealities: Internal Quantum Efficiency

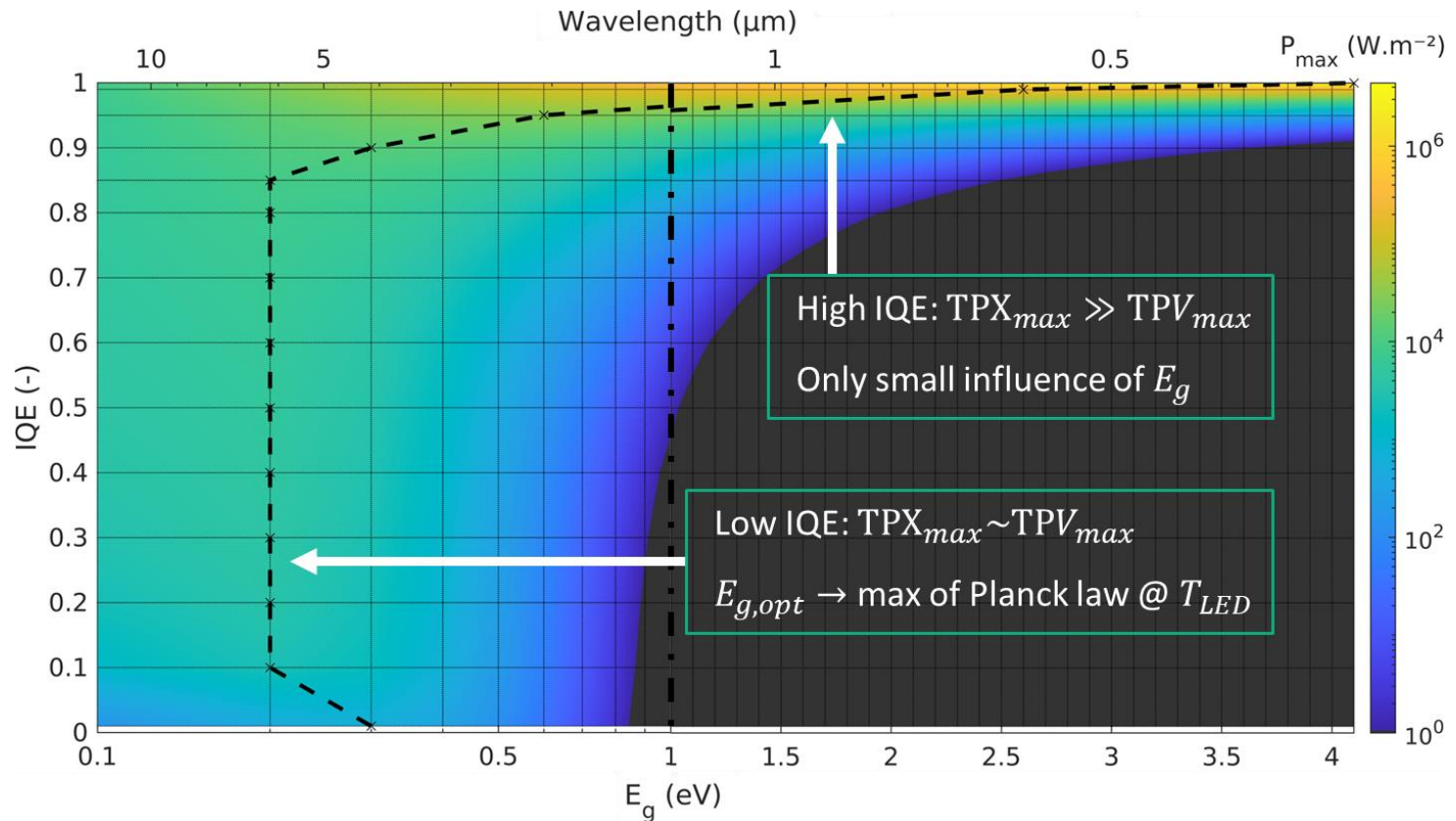
$$J = e \left(\gamma_{net} - \frac{1 - IQE}{IQE} (\gamma_{em}^U - \gamma_{em}^0) \right)$$

$\gamma_{abs} - \gamma_{em}$

LED (600 K)

PV cell (300 K)

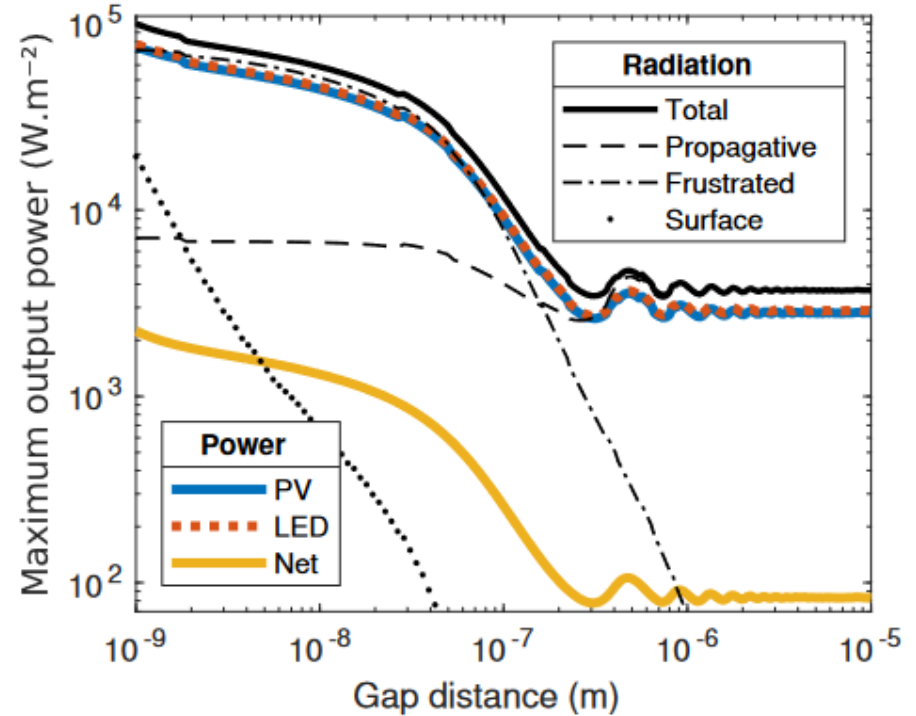
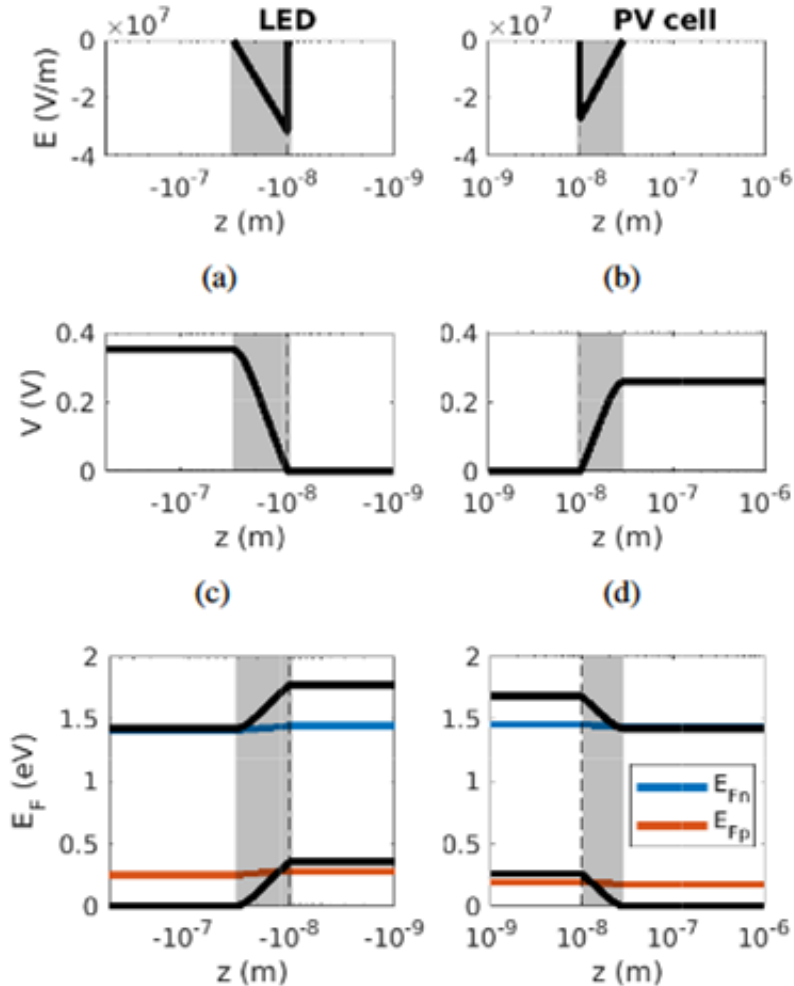
$d = 10 \text{ nm}$
 $\varepsilon = 10 + i$



→ Thermal frequencies not required if IQE is high

Drift-diffusion equation in both LED and PV devices

High doping: simplifications

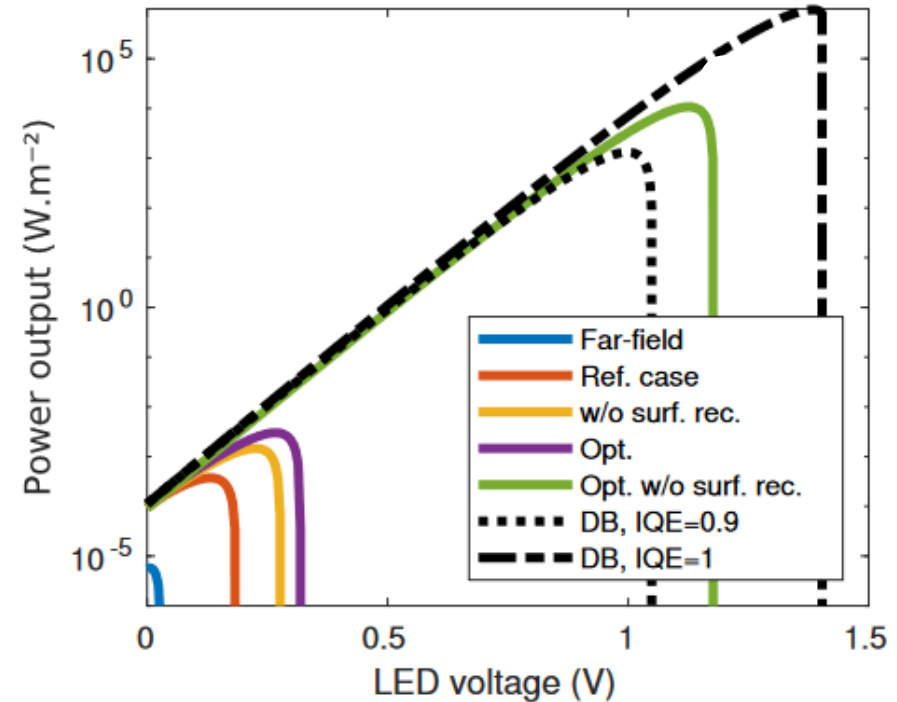
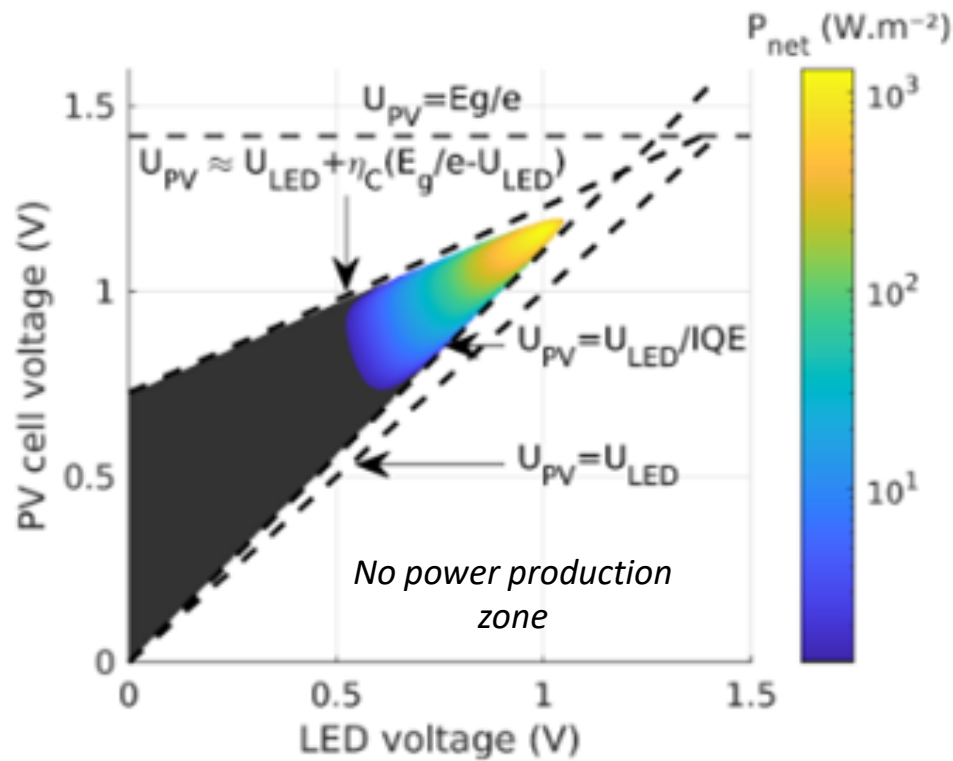


Huge flux emitted and converted, only a fraction is harvested

Performances of PN GaAs-based NF-TPX devices

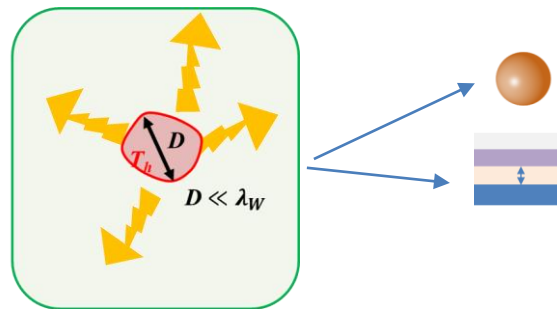
$$E_g = 1.4 \text{ eV}$$

High doping

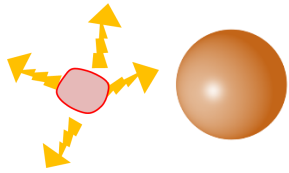


- Managing electrical losses and recombinations is critical
- Increasing the depleted zone in pin junctions

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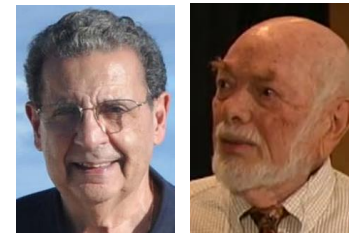


Thermal emission of a sphere



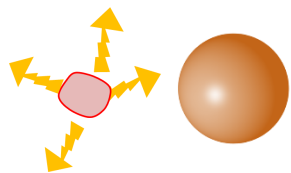
$$Q = \int_0^\infty d\omega \frac{\hbar\omega}{e^{\frac{\hbar\omega}{k_B T}} - 1} \underbrace{\frac{2}{\pi} \sum_{P=E,M} \sum_{l=1}^\infty (2l+1) [\operatorname{Re}(T_l^P) - |T_l^P|^2]}_{\mathfrak{I}(\omega)} \quad \sim \text{Mie}$$

$$e_{\text{eff,tot}} = \frac{Q_s}{\sigma T^4 4\pi R^2}$$



Kattawar & Eisner, Appl. Optics 9 (1970)
 Krüger et al., PRB 86 (2012)

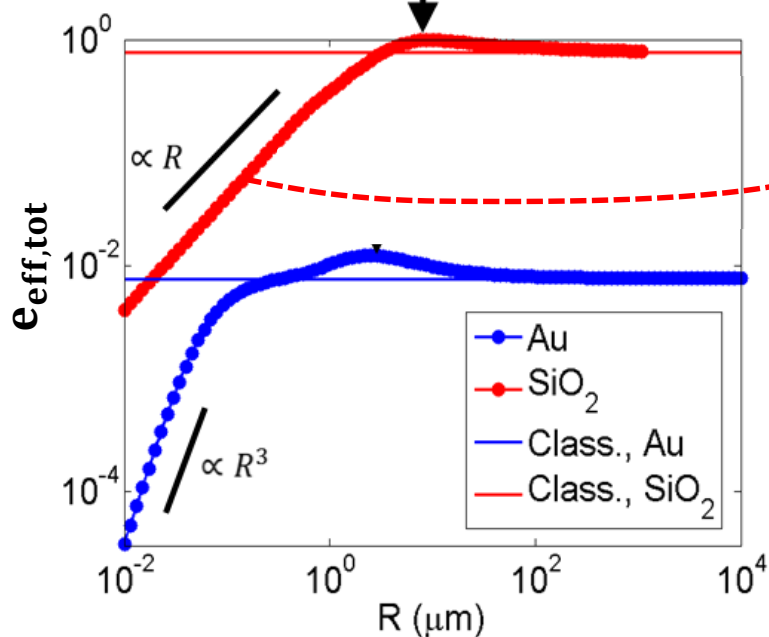
Thermal emission of a sphere



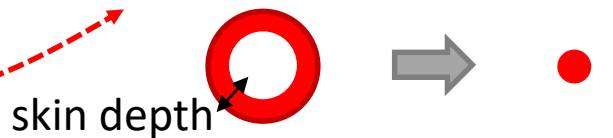
$$Q = \int_0^\infty d\omega \frac{\hbar\omega}{e^{\frac{\hbar\omega}{k_B T}} - 1} \underbrace{\frac{2}{\pi} \sum_{P=E,M} \sum_{l=1}^\infty (2l+1) [\text{Re}(T_l^P) - |T_l^P|^2]}_{\mathfrak{I}(\omega)}$$

$$e_{\text{eff,tot}} = \frac{Q_s}{\sigma T^4 4\pi R^2}$$

$e_{\text{eff,tot}} > 1$



$Q_s \propto R^2 \rightarrow R^3$: volume emission

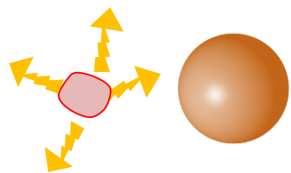


$Q_s \propto R^5$
magnetic dipole



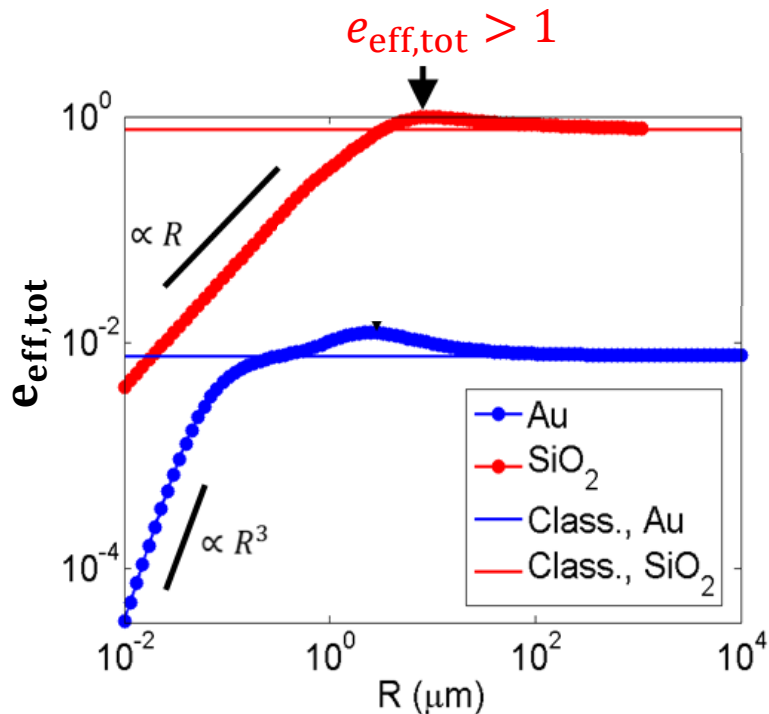
strong electromagnetic effects

Thermal emission of a sphere

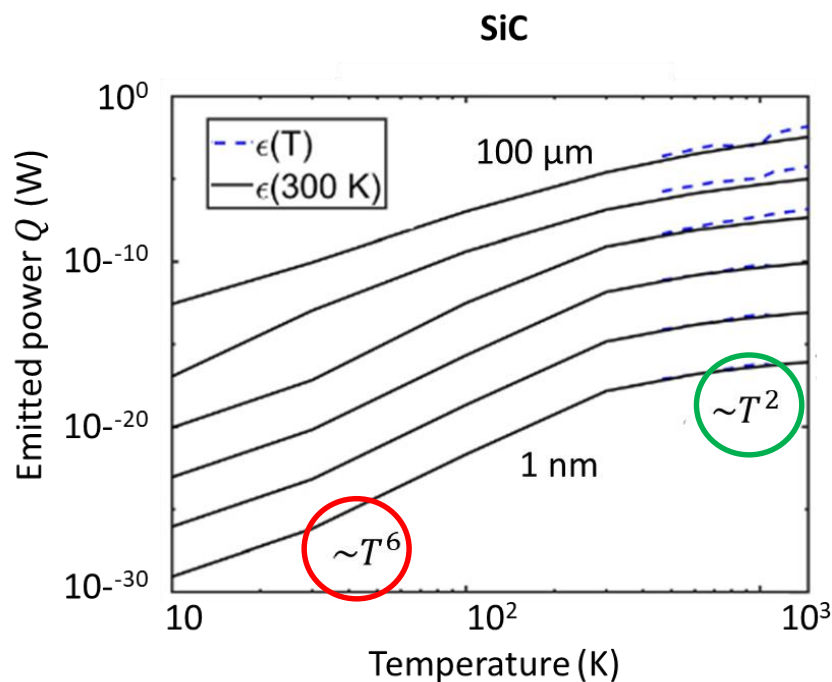


$$Q = \int_0^\infty d\omega \frac{\hbar\omega}{e^{\frac{\hbar\omega}{k_B T}} - 1} \underbrace{\frac{2}{\pi} \sum_{P=E,M} \sum_{l=1}^\infty (2l+1) [\text{Re}(T_l^P) - |T_l^P|^2]}_{\mathfrak{I}(\omega)}$$

$$e_{\text{eff,tot}} = \frac{Q_s}{\sigma T^4 4\pi R^2}$$



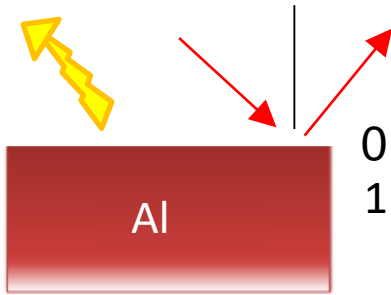
Size dependence different than for large objects



Temperature dependence different than predicted by Stefan-Boltzmann's law

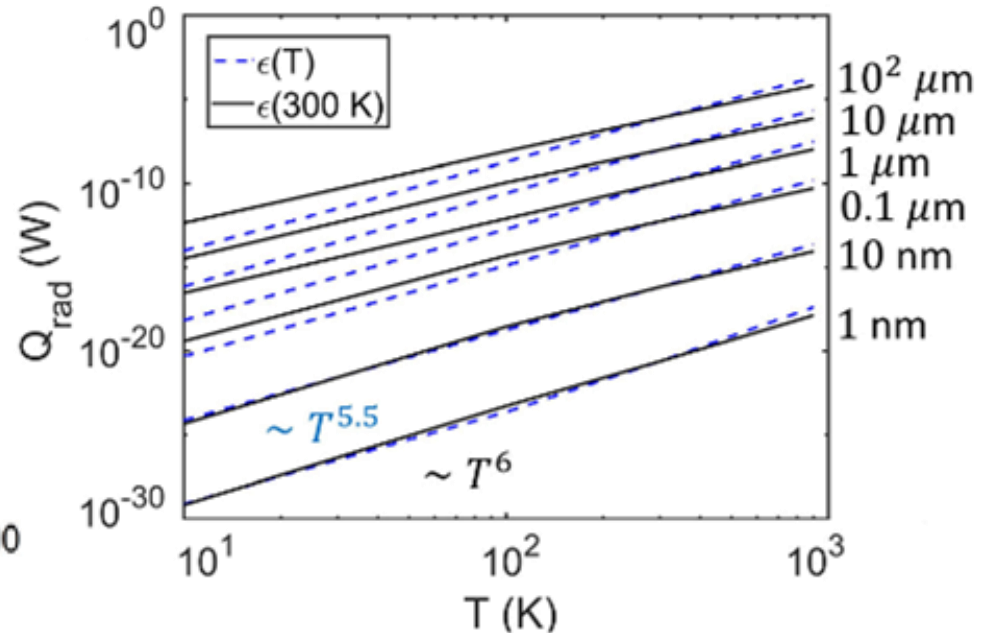
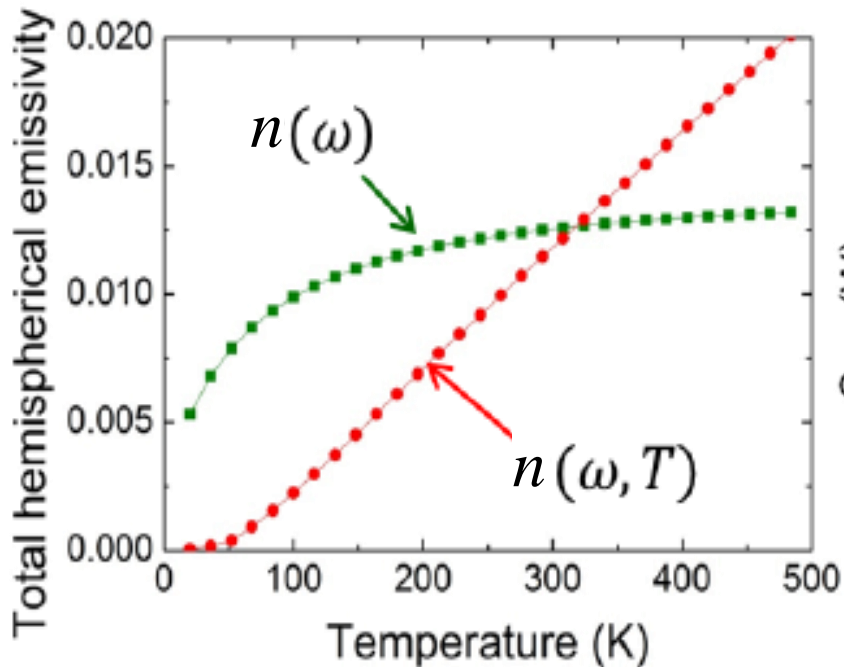
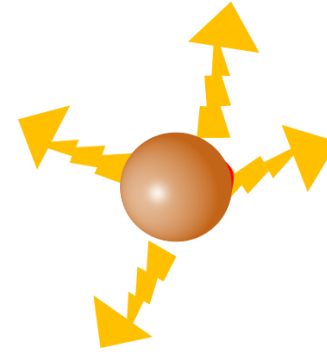
Temperature dependence of permittivity

Case of metals

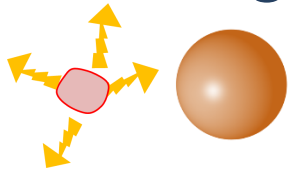


$$\epsilon(\omega) = 1 - \frac{\omega_p^2}{\omega(\omega + i\Gamma)}$$

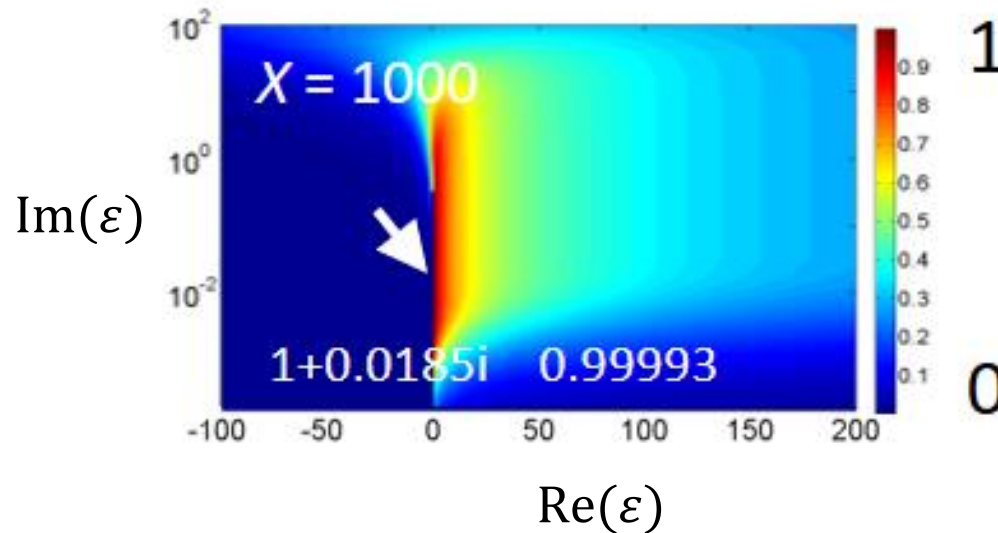
$$\omega_p^2 = \frac{Ne^2}{m^* \epsilon_0} \quad \Gamma = \frac{Ne^2 \rho}{m^*}$$



Optimizing thermal emission with Mie resonances

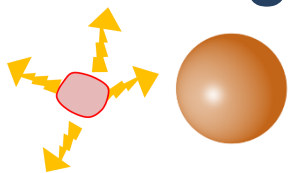


Emissivity of a large sphere

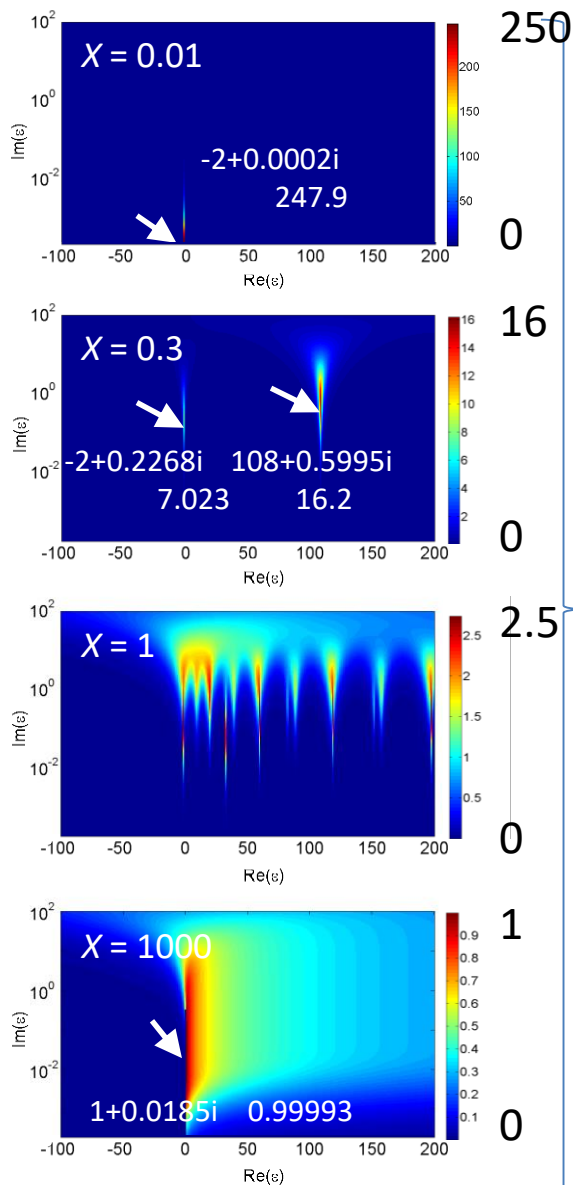


Blackbody = non-reflective medium that absorbs all radiation

Optimizing thermal emission with Mie resonances



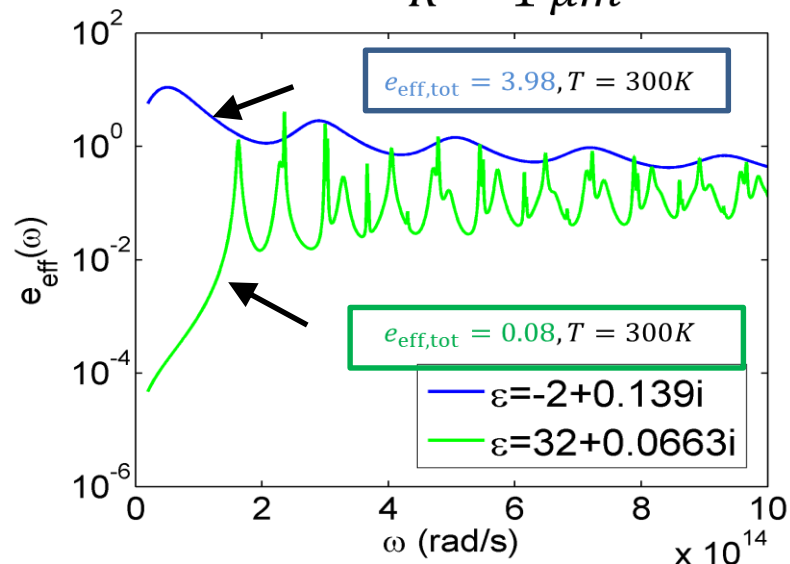
$$\text{Re}(\epsilon) \approx -2$$



$$\text{Re}(\epsilon) \approx 1$$

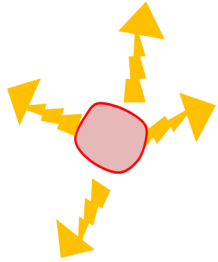
ϵ supposed constant

$$R = 1 \mu\text{m}$$



Dipole resonance more efficient because 'broadband'

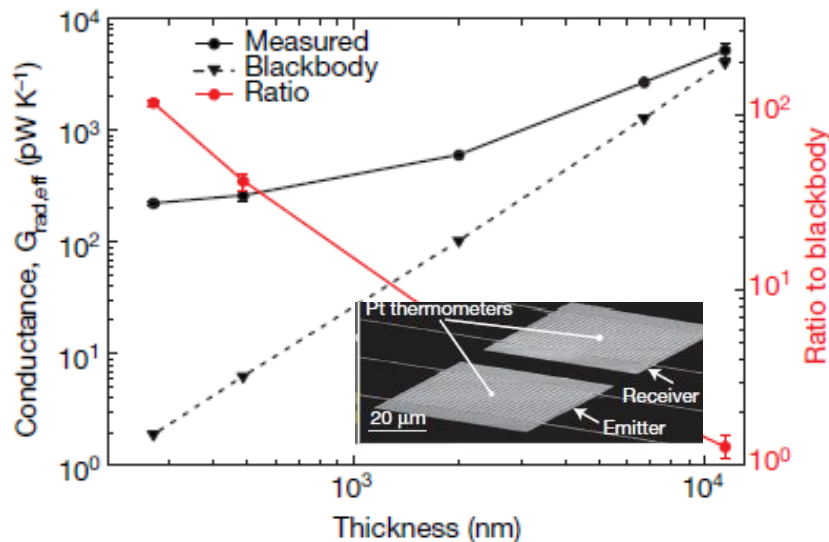
Recap for sub- λ finite objects



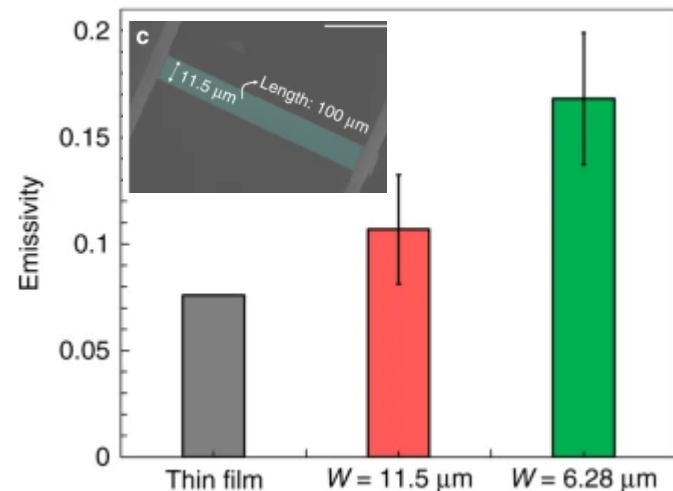
- Effective emissivity can be larger than 1
- $S T^4$ incorrect over large ranges of size/temperature
- Dipole resonance more broadband-compatible than Mie geometric ones
- Is it possible to tune the temperature-dependance and increase it for large surfaces with sub- λ elements?

Recent measurements involve also the shape of the objects

Heat transfer between suspended calorimeters



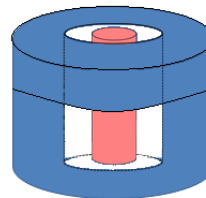
Thermal emission from ribbons



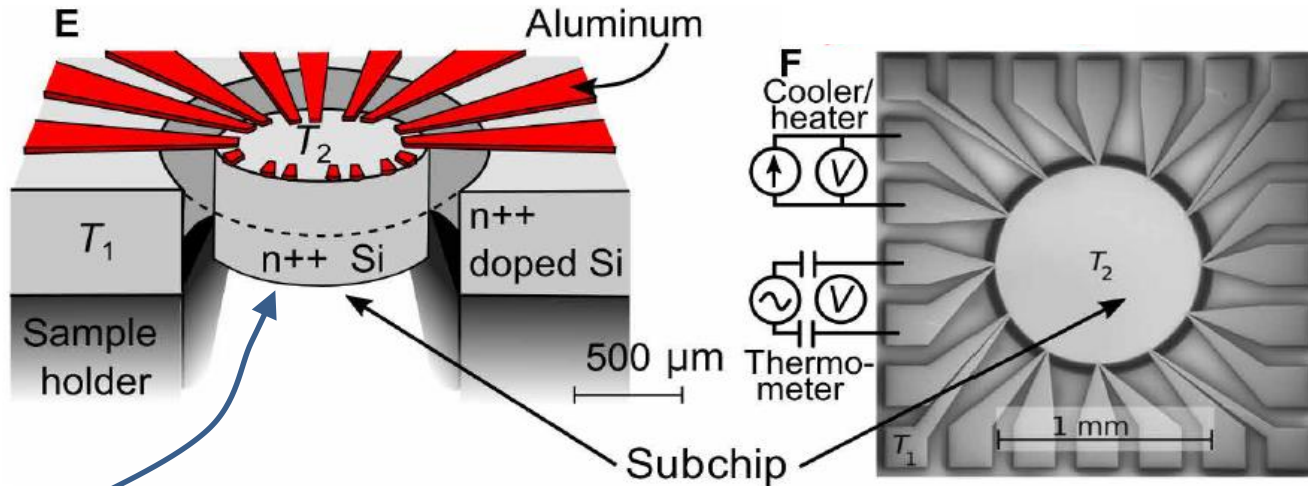
Thompson *et al.*, Nature 561 (2018)

Shin *et al.*, Nat. Com 10 (2019)

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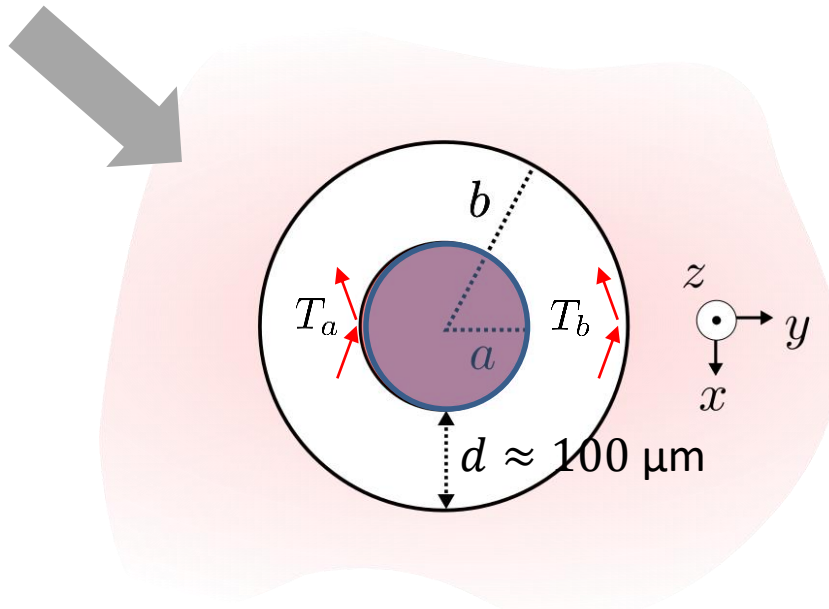


Refrigeration device: concentric cylinders



Cold zone

Mykkänen et al., Sci. Adv. 6, eaax9191 (2020)

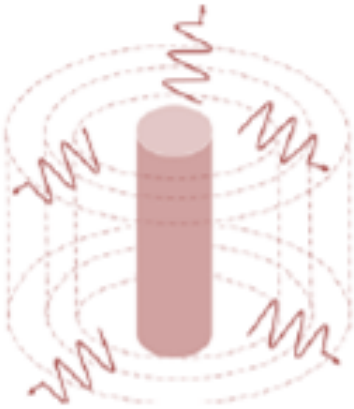


$$T < 1 \text{ K}$$

$$\lambda_{th} > 3 \text{ mm}$$

Thermal radiation is a parasitic heating channel

Electromagnetic modes for cylindrical objects

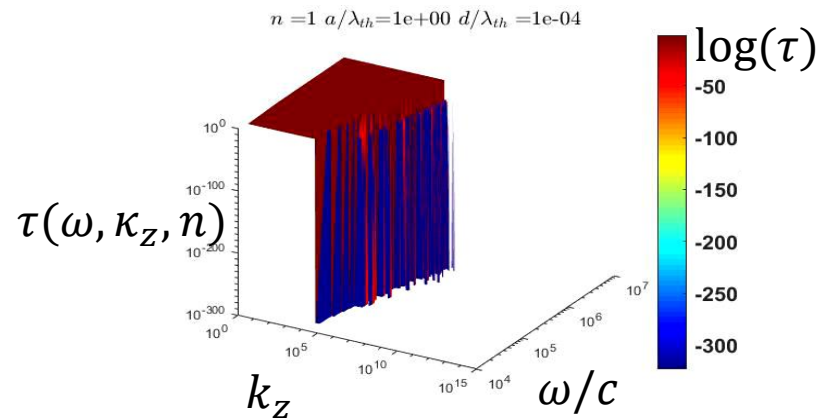
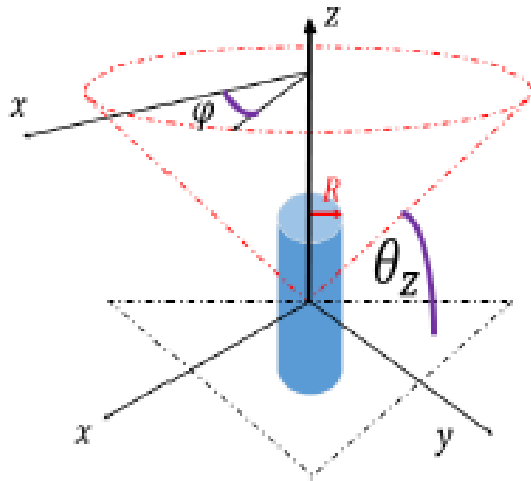


- Cylindrical waves $\cos(n\varphi), \sin(n\varphi)$
- Waves act as plane waves along z-axis $e^{ik_z z}$
- Polarizations are **coupled**

Golyk et al. PRE 85 (2012)

$$\left\{ \begin{array}{l} \text{E/N-polarization } E_{\parallel z} \\ \text{H/M-polarization } H_{\parallel z} \end{array} \right.$$

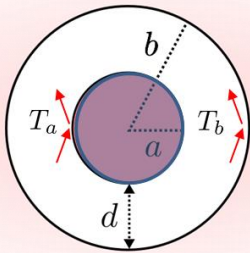
$$\begin{Bmatrix} E \\ H \end{Bmatrix} = f \left\{ \begin{Bmatrix} J_n(\kappa_\rho \rho) \\ H_n^{(1)}(\kappa_\rho \rho) \end{Bmatrix} \left\{ e^{ik_z z} \right\} \begin{Bmatrix} \cos(n\varphi) \\ \sin(n\varphi) \end{Bmatrix} \right\}$$



Radiative heat transfer from inner to outer cylinder

Trace formula for unbounded medium

vs Krüger al., PRB B 86, 115423 (2012)



Unbounded Green's tensor

$$\mathcal{T}(\omega) = -\frac{2}{\pi} \text{Tr} \text{Im} \left\{ (1 + \mathbf{G}_0 \mathbf{T}_b) \frac{1}{1 - \mathbf{G}_0 \mathbf{T}_a \mathbf{G}_0 \mathbf{T}_b} \mathbf{G}_0 \cdot \left[\text{Im}\{\mathbf{T}_a\} - \mathbf{T}_a \text{Im}\{\mathbf{G}_0\} \mathbf{T}_a^* \right] \frac{1}{1 - \mathbf{G}_0^* \mathbf{T}_a^* \mathbf{G}_0^* \mathbf{T}_b^*} \right\}$$

Heaviside

$$= -\frac{2}{\pi} H(k_0 - k_z) \text{Re} \left\{ W_{PP}(1 + W_{PP} + L_{PP} + D_{PP})^* + W_{P'P}(L_{P'P} + W_{P'P} + D_{P'P})^* \right\}$$

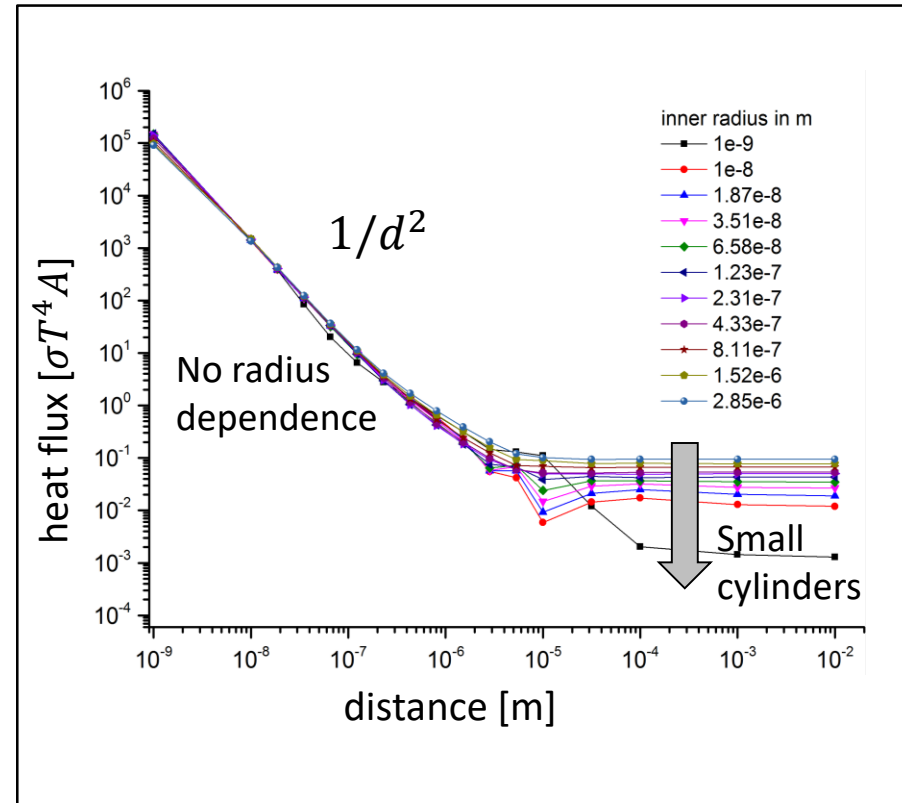
Polarizations

$$- \frac{1}{\pi} \text{Re} \left\{ W_{PP} C_{PP}^* + L_{PP}(1 + D_{PP})^* + W_{P'P} C_{P'P}^* + L_{P'P} D_{P'P}^* \right\}$$

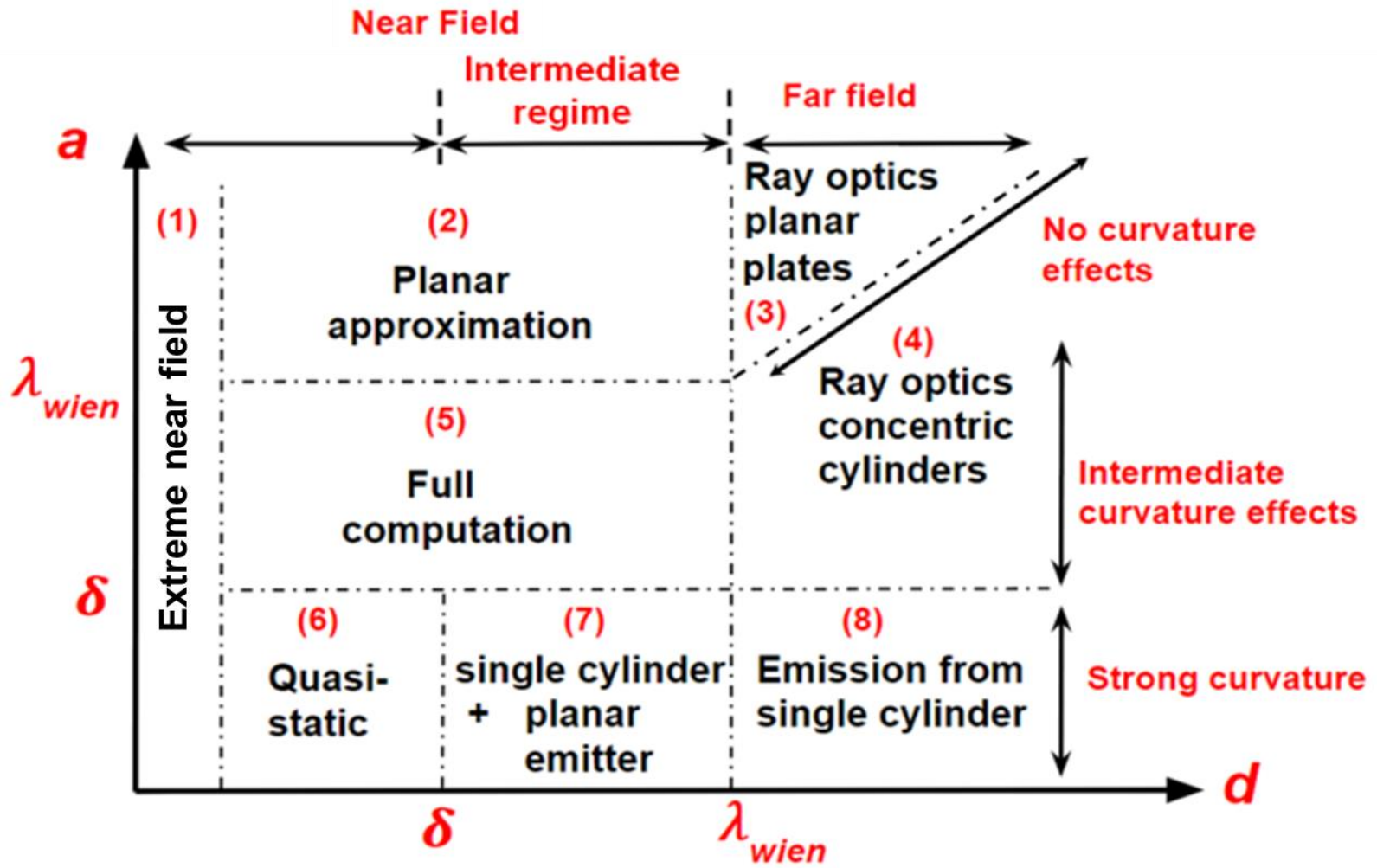
C, D, L, W :

Coefficients expressed in terms of ratios of cylindrical Bessel functions (poles & singularities...)

$$\mathcal{T}_{MM}^a = -\frac{J_n(\kappa_\rho, 0a)}{H_n(\kappa_\rho, 0a)} \frac{\Delta_1^a \Delta_4^a - K_a^2}{\Delta_1^a \Delta_2^a - K_a^2} \quad \Delta_1^a = \frac{1}{\kappa_{\rho, Aa}} \frac{J'_n(\kappa_\rho, Aa)}{J_n(\kappa_\rho, Aa)} - \frac{1}{\epsilon_A \kappa_{\rho, 0a}} \frac{H_n^{(1)}(\kappa_\rho, 0a)}{H_n^{(1)}(\kappa_\rho, 0a)}$$



Regime map vs (a, d) and (λ, δ)



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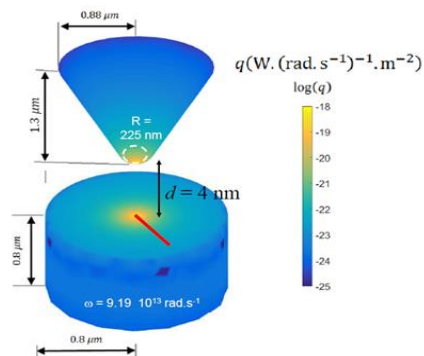
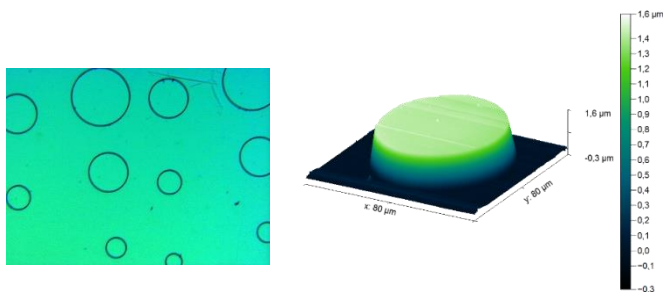
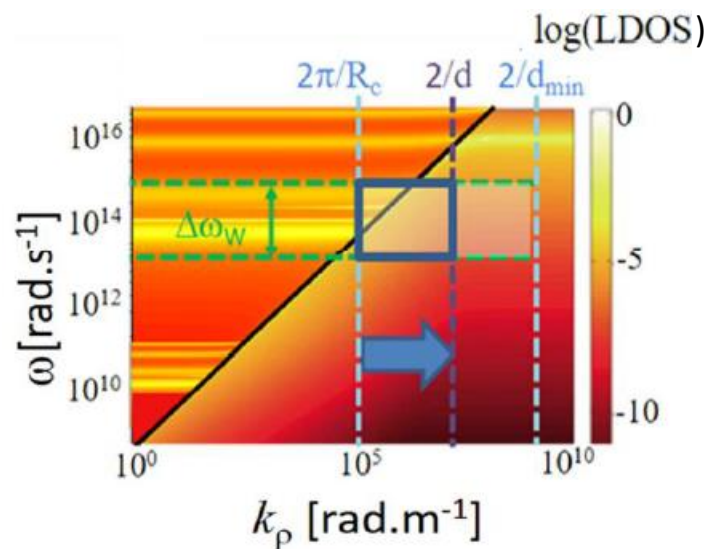
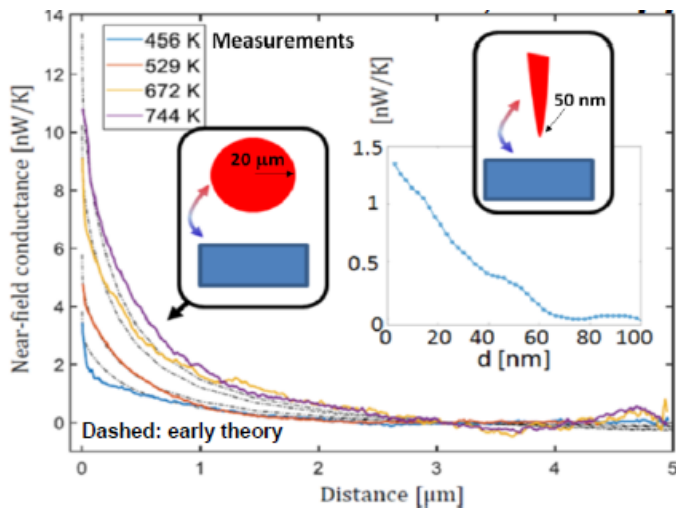
Spectroscopy without spectroscope?

Near-field radiative 'spectroscopy'

(θ, ω)

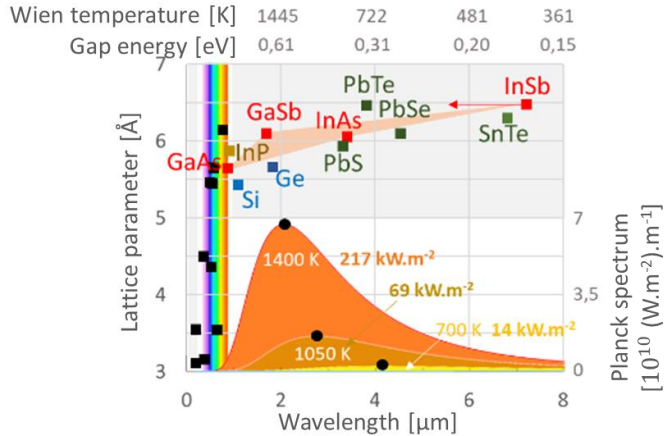


(d, T)



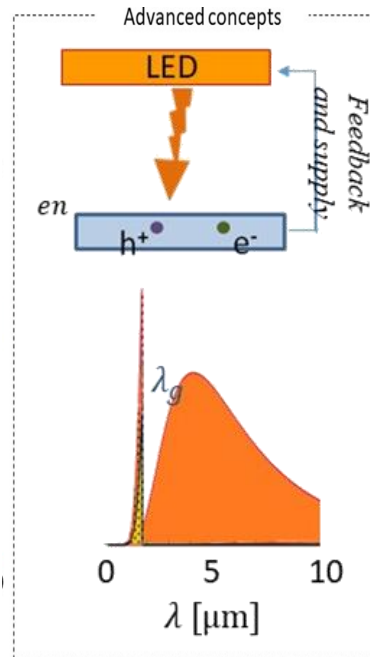
Energy-conversion devices

Near-field thermophotovoltaics



- Room temperature cells
- Higher operating temperature
- Smaller distances

Near-field thermophotonics

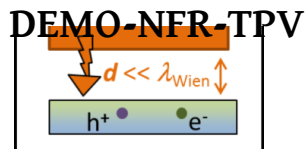


- Refrigeration
- Implementation...
- Moving to IR?

Other near-field thermo-electric phenomena

Thermionics and coupling with near-field thermal radiation

Acknowledgements



BQR REDCAV

ATTSEM



BQR THERMOS



Thermal Radiation to Electrical
Energy conversion (TREE)



Announcement:

'Special Topic' issue in APL

'Thermal radiation at nanoscale and applications'

AIP Applied Physics Letters

Deadline for submission: July 2022

Guest Editors: P.-Olivier Chapuis, CNRS & INSA Lyon, France
Bong Jae Lee, KAIST, South Korea
Alejandro Rodriguez, Princeton, USA