

# Spin 1/2 on the kagome lattice: “from theory to experiments and back”.

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LPTMC

Université Pierre et Marie Curie  
Paris



## Paris Univ. P&M Curie

- L. Messio
- B. Bernu
- P. Viot
- J. C. Domenge
- F. Brieuç

## Saclay Ipht CEA

- L. Messio
- G. Misguich

## Grenoble CNRS

- O. Cepas

## Hong Kong

C. M. Fong, P. W. Leung

## Grenoble CEA & ILL

- B. Fåk

## Orsay LPS

- F. Bert
- E. Kermarrec
- P. Mendels

## London (UCL) :

- R. H. Colman
- A. S. Wills

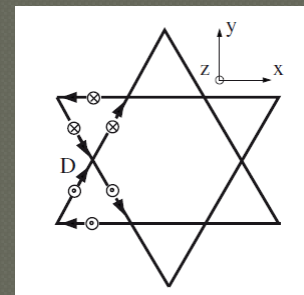
# Outline

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- A point of view on the properties of herbertsmithite
- Kapellasite:
  - A new gapless Spin Liquid.
  - *B. Fåk, et al. PRL 109, 037208 (2012)*
    - Polymorph of herbertsmithite
    - Slightly different crystallography
    - Notably different physics

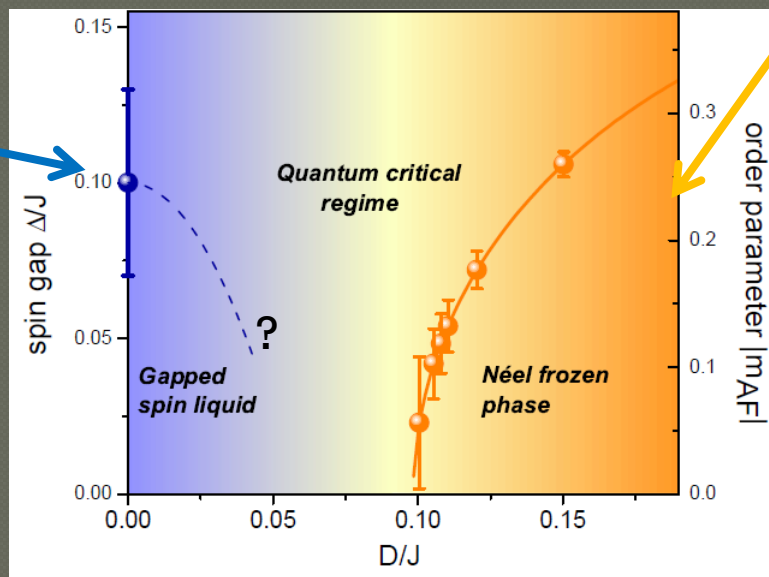
# Quantum phase transition induced by Dzyaloshinskii-Moriya interactions

$$H = \sum_{\langle i,j \rangle} [JS_i \cdot S_j + \mathbf{D}_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j)]$$



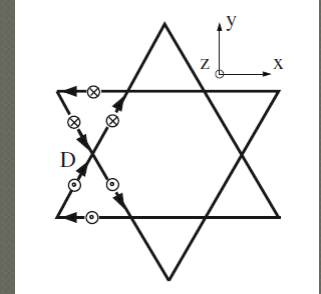
Jiang ..., '08  
Yan, ... '12  
Depenbrock '12

O. Cepas... PRB 78 '08

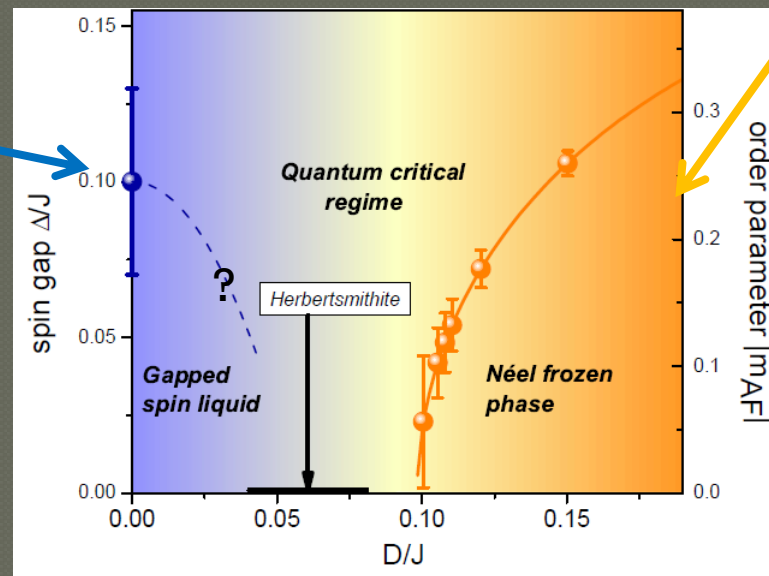


# Quantum phase transition induced by Dzyaloshinskii-Moriya interactions

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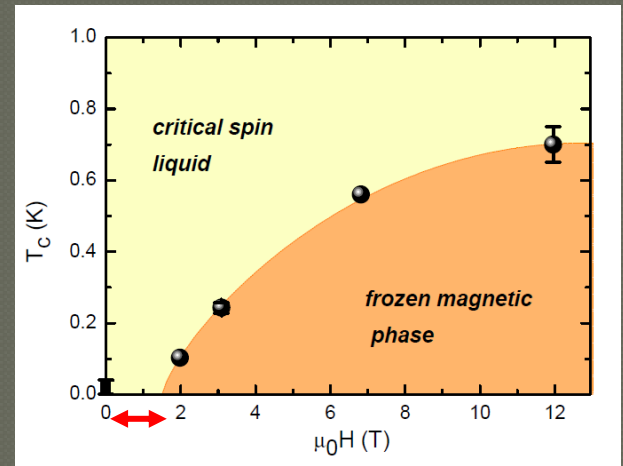
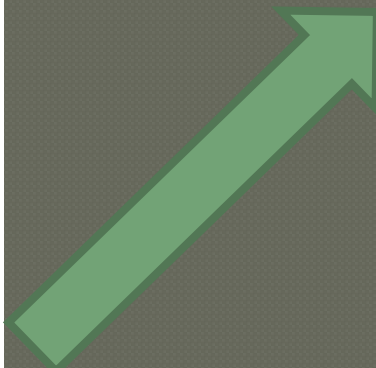
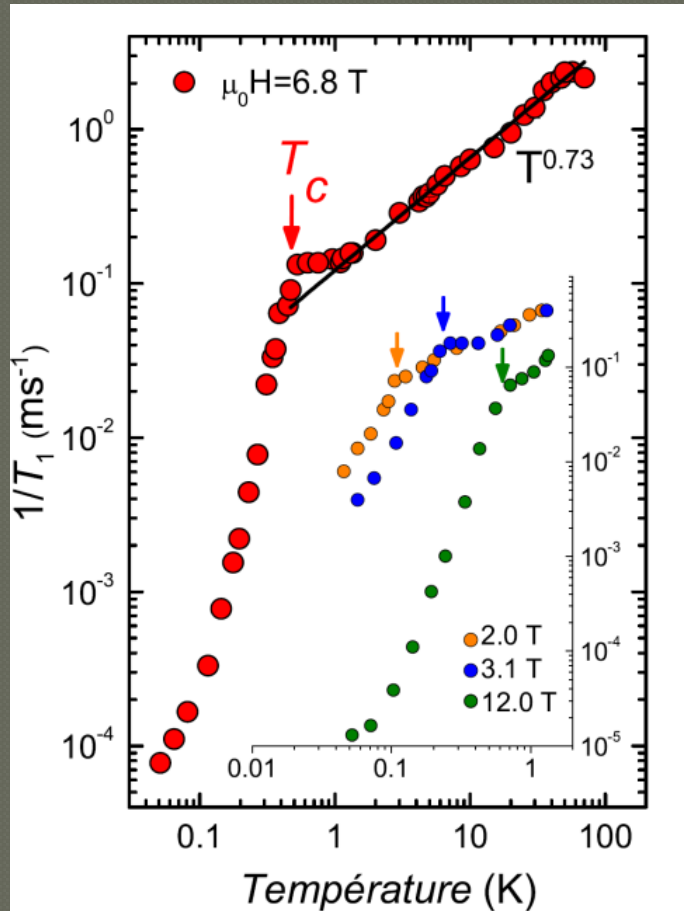
Jiang, '08  
Yan, '12  
Depenbrock '12



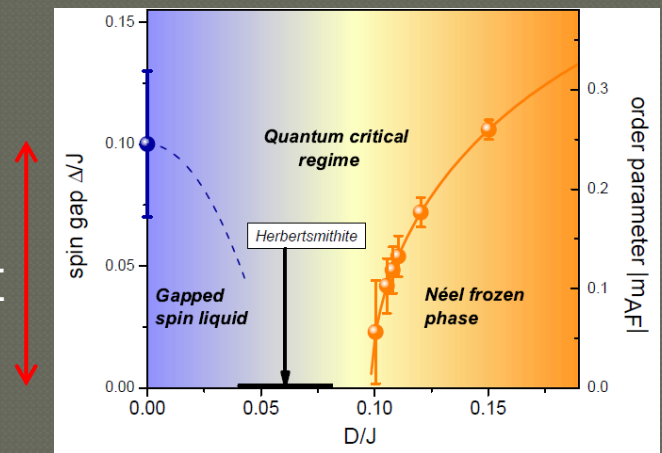
O. Cepas... PRB 78 '08

Zorko ... PRL 101 '08, El Shawish... PRB 81 '10.

# Effect of a magnetic field on Herbertsmithite ( $1/T_1$ NMR)



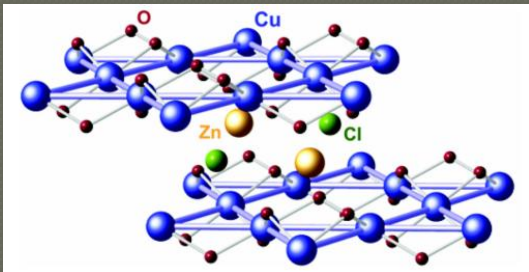
$\sim 20 \text{ K}$



M. Jeong et al: PRL 107, 237201 (2011)

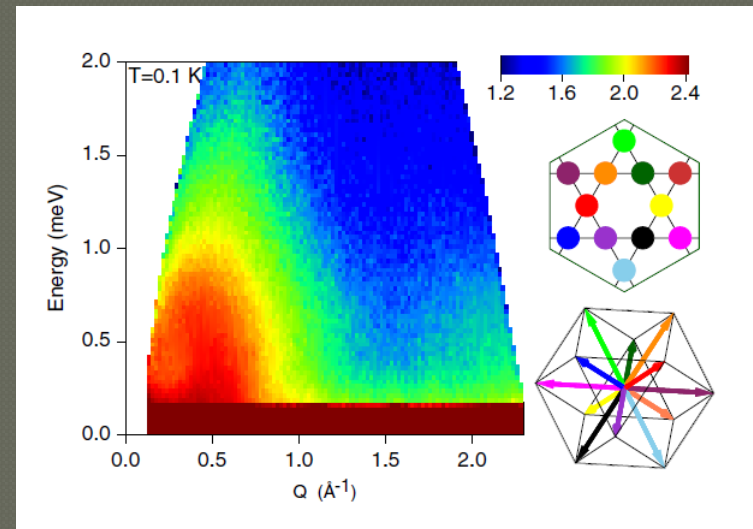
# Kapellasite: a new gapless SL

- A metastable polymorph of herbertsmithite
  - slightly different crystallography
- Fluctuating down to 20 mK ( $\mu$ SR, INS)



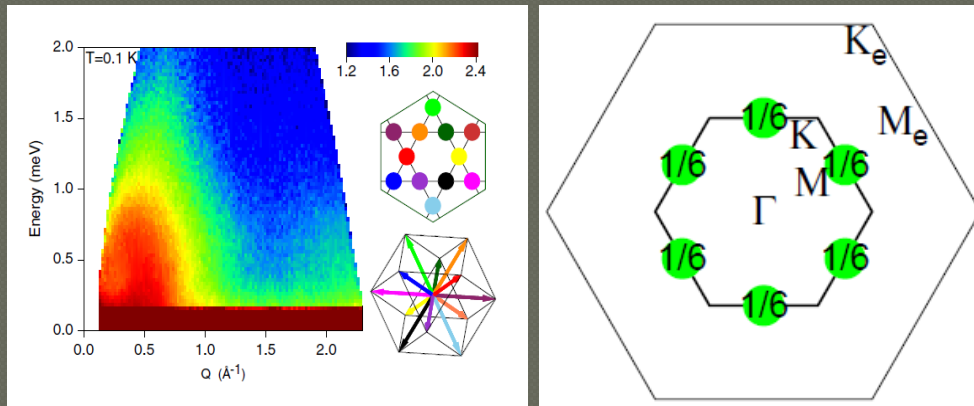
Synthesis:

R. H. Colman, et al.,  
Chem. Mater.  
20, 6897 (2008) and  
22, 5774 (2010).



B. Fåk, et al. PRL 109, 037208 (2012)

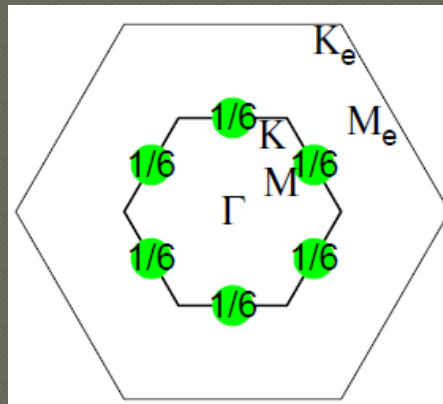
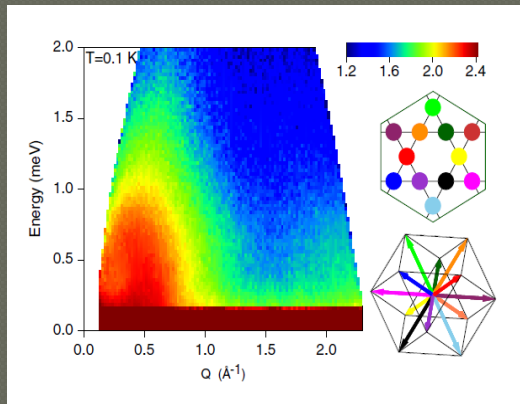
# When INS meets PSG analysis



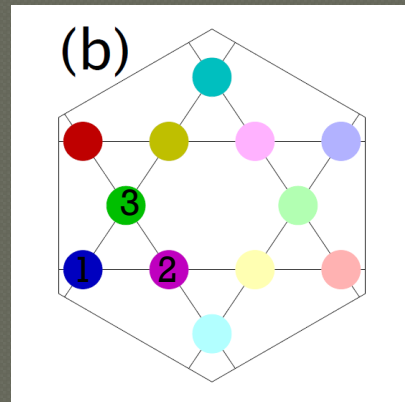
L. Messio PRB 83 (2011)  
5 AF “regular” states  
on the kagome lattice  
Only cuboc2 SRO can fit INS



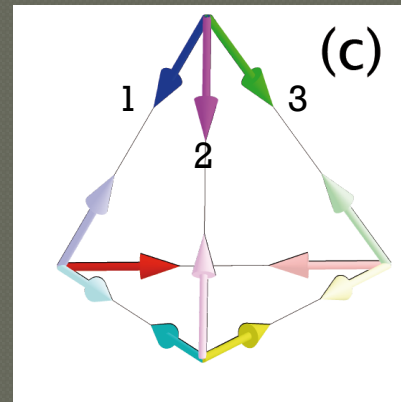
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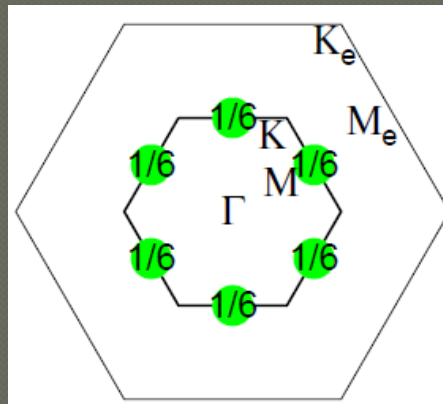
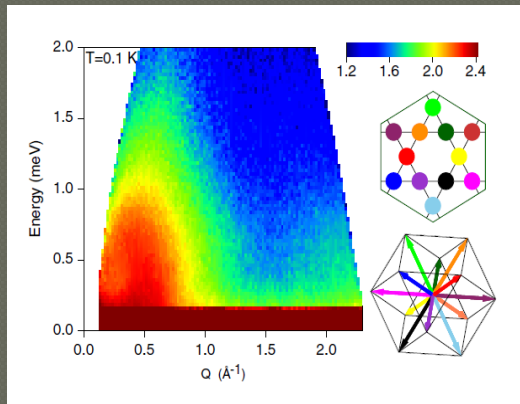


Magnetic unit cell

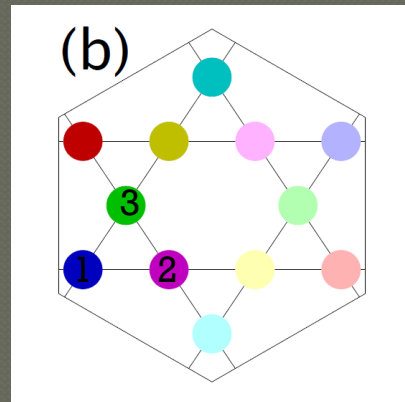


Short range 3D chiral  
disposition of spins

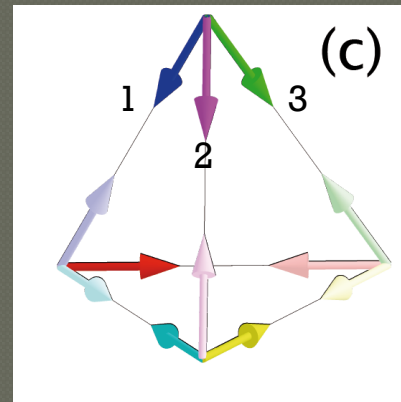
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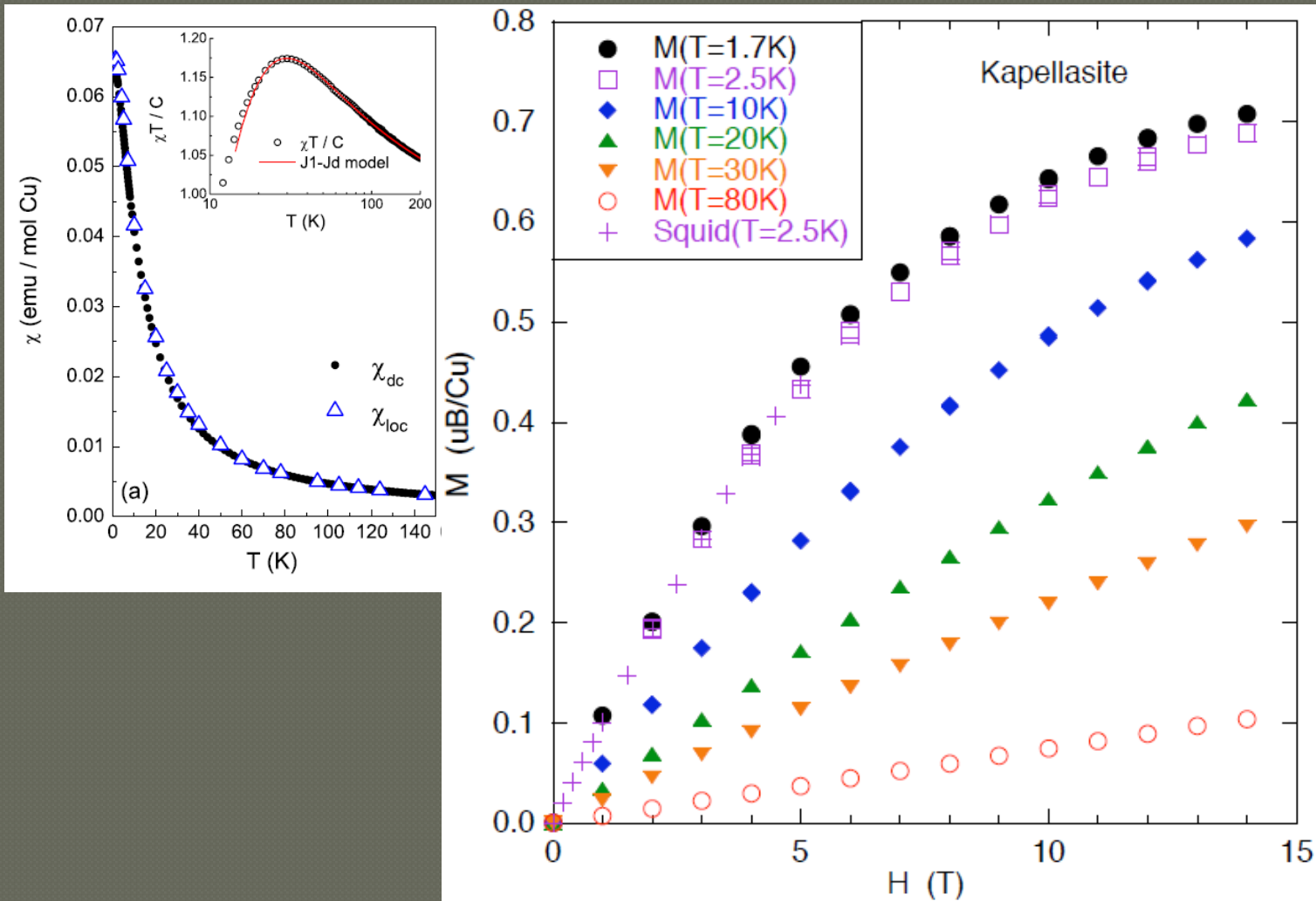
Short range 3D chiral  
 disposition of spins

Chirality:

$$\sigma = \frac{S_1 \cdot (S_2 \times S_3)}{|S_1 \cdot (S_2 \times S_3)|}$$

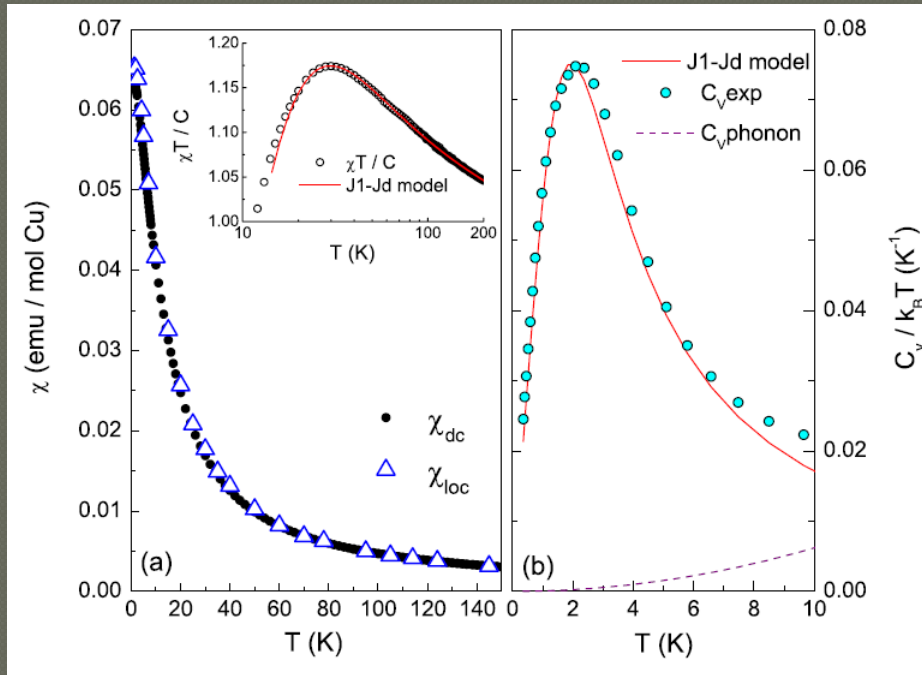
# From experiments to model by HT series

B. Bernu, E. Kermarec, et al.. 2012

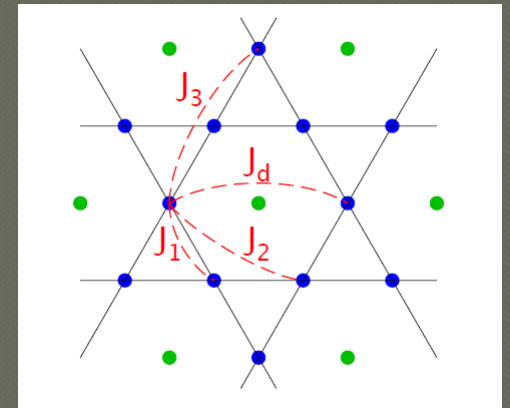


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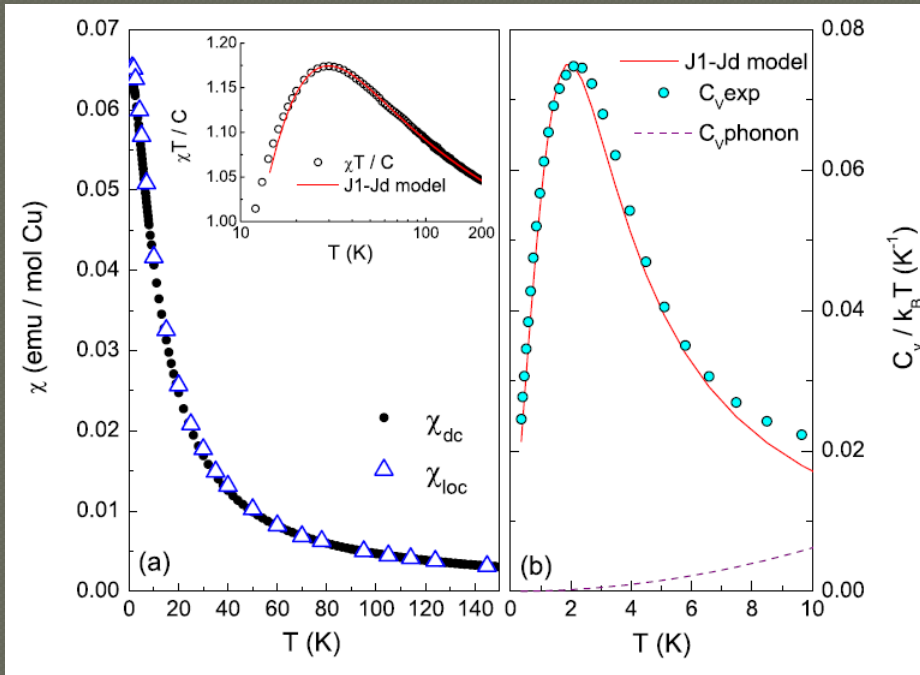
$$H = \sum_{i,j} J_{i,j} S_i \cdot S_j$$



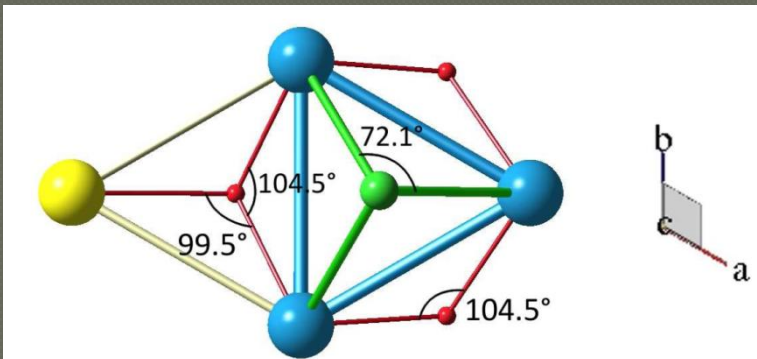
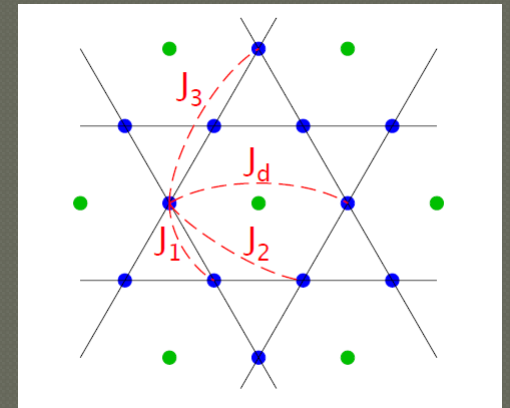
Ferro  $J_1$  competing  
with AF  $J_2$  or/and  $J_d$   
 $J_1 = -12.4K$ ,  $J_2 = -3K$ ,  $J_d = +14.8K$

# From experiments to model by HT series

B. Bernu, E. Kermarec, et al.. 2012

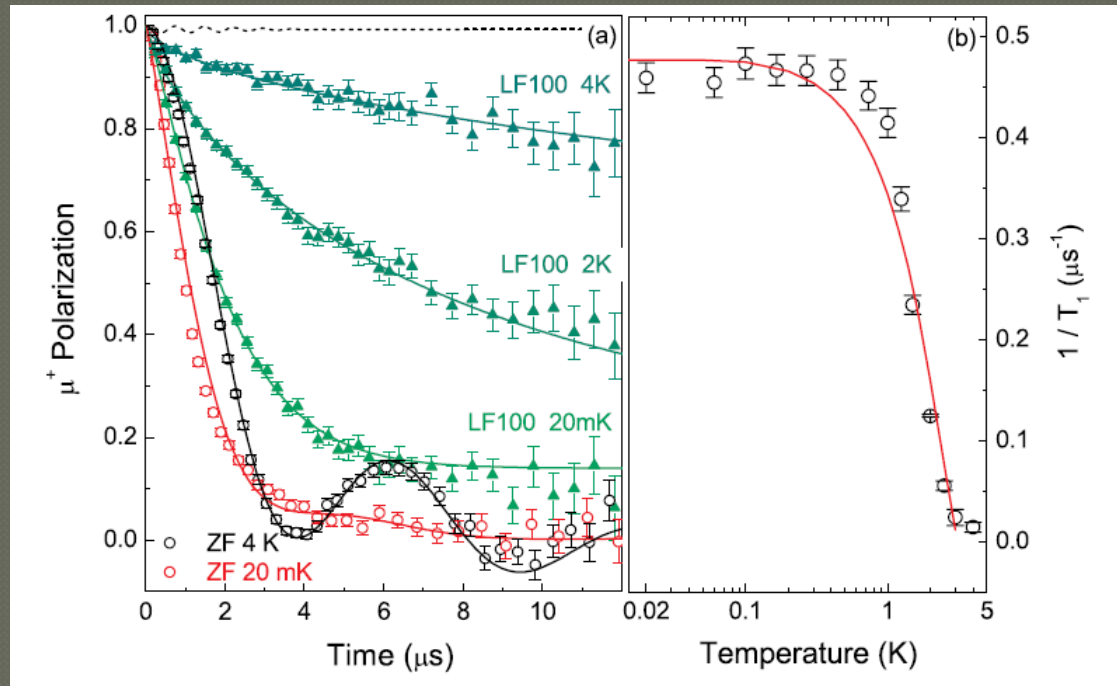


$$H = \sum_{i,j} J_{i,j} S_i \cdot S_j$$



Ferro  $J_1$  competing with AF  $J_2$  or/and  $J_d$   
 $J_1 = -12.4\text{K}$ ,  $J_2 = -3\text{K}$ ,  $J_d = +14.8\text{K}$

# $\mu$ SR relaxation (local low frequency fluctuations)



Right:  $1/T_1$  (low temperature plateau)

Experiments (circles) and SBMF calculations (red line).

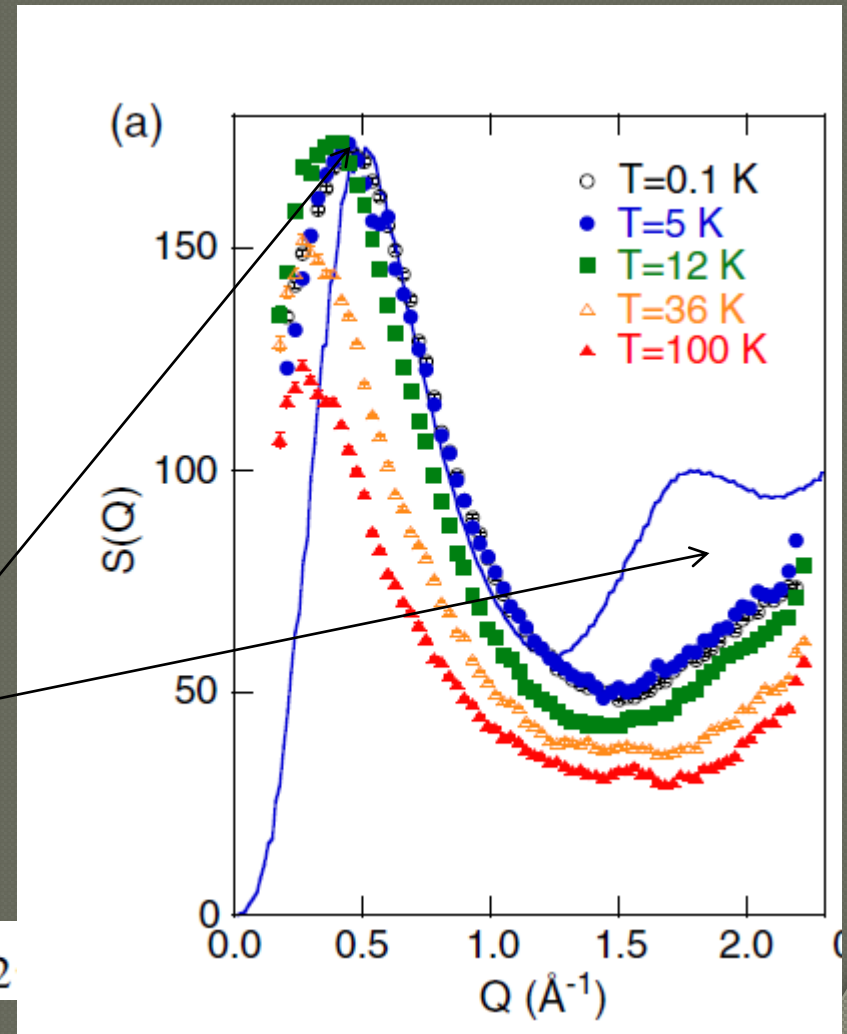
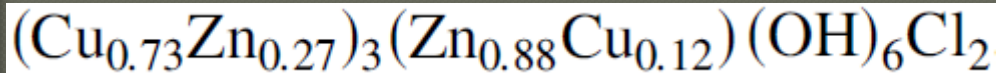
No adjustable parameters (except the absolute value)

# Powder averaged INS

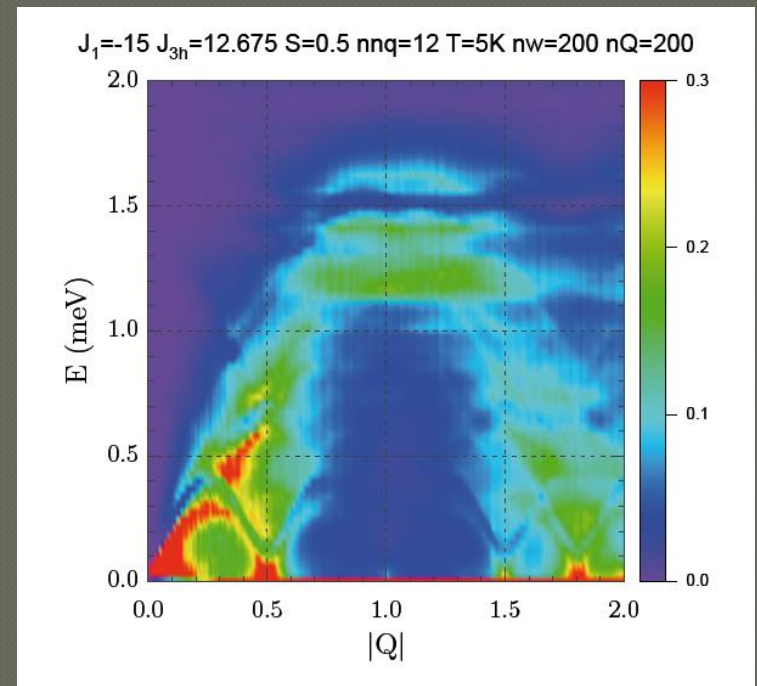
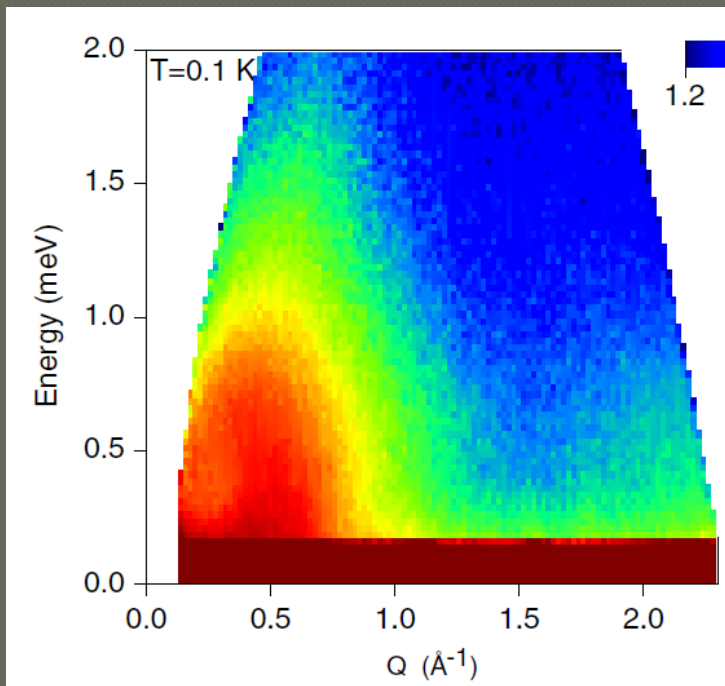
Wave-vector dependence of the inelastic magnetic scattering integrated over the energy range  $0.4 < E < 0.8$  meV.

Blue line SBMF calculations.  
No adjustable parameters

2 features may be due to Zn substitutions on Cu sites ?



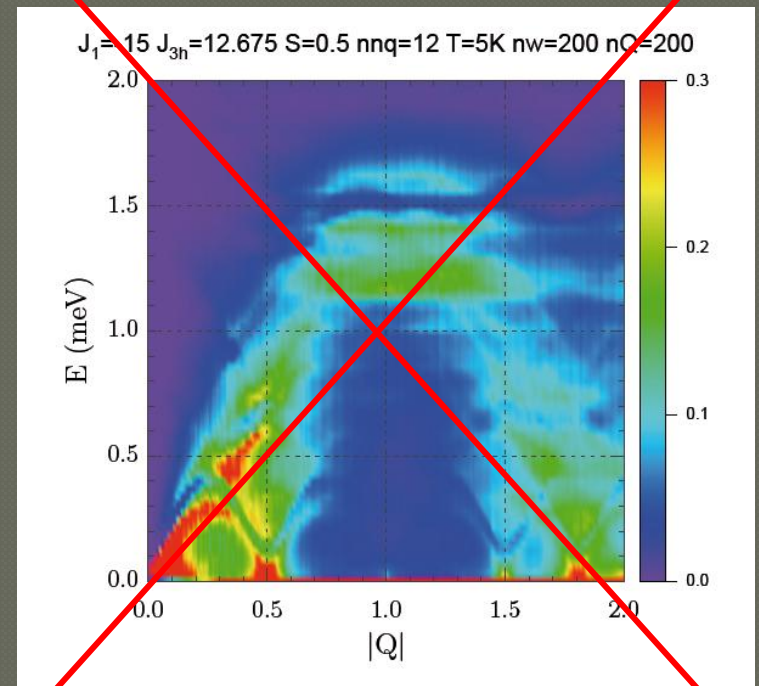
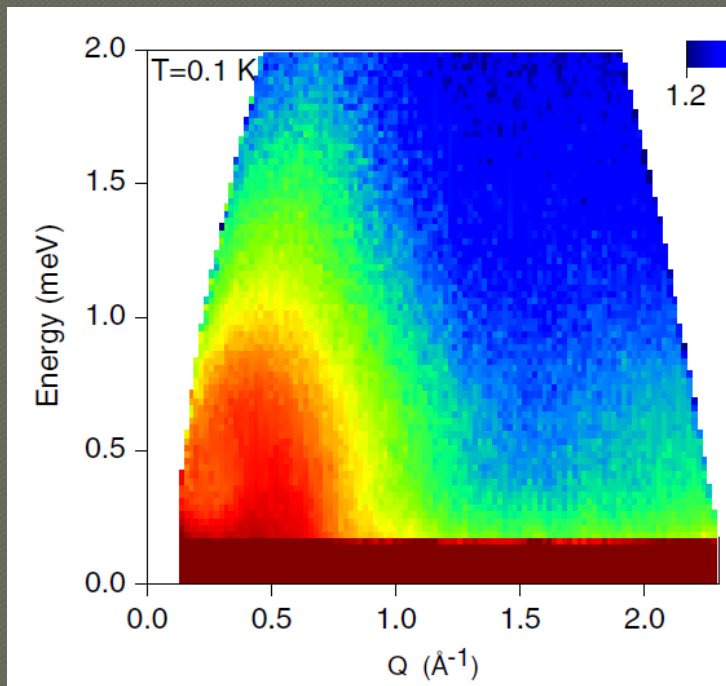
# Dynamical correlations



Schwinger bosons calculation

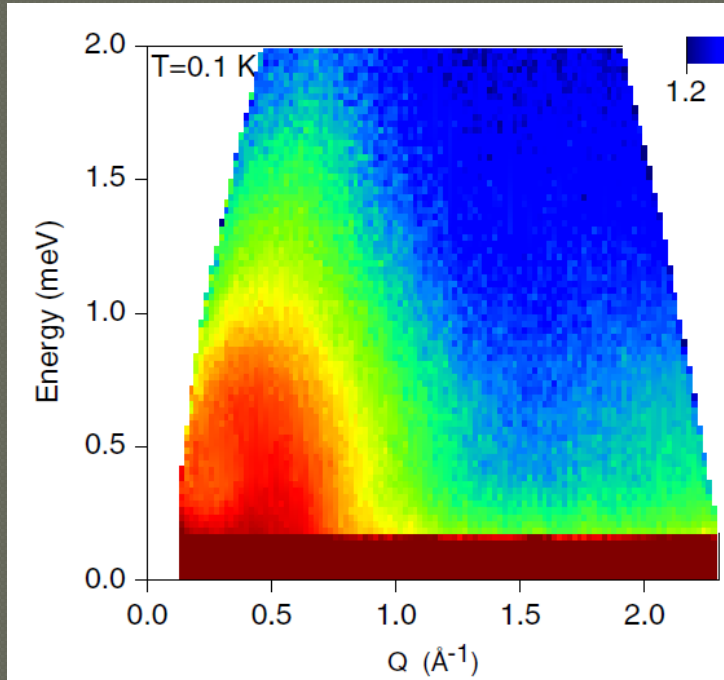


# Dynamical correlations



Are not damped spin waves of the SR order!

# INS

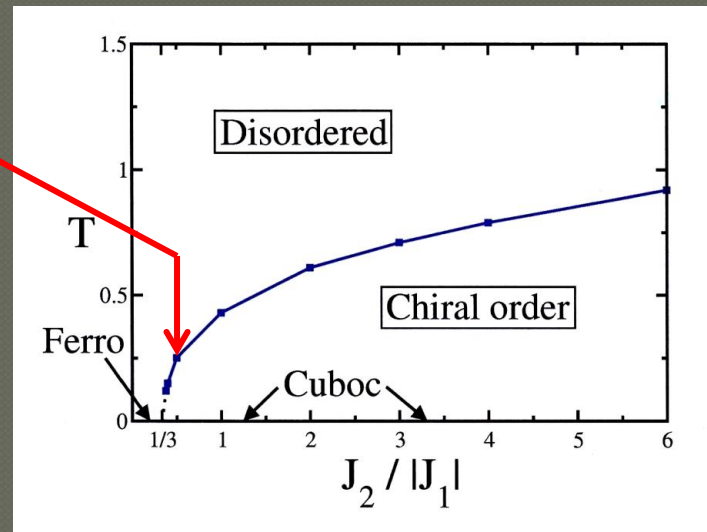


- ✓ Continuum of spinons excitations...
- ✓ Wanted: a fermionic description of spinons!
- ✓ Is it a chiral spin liquid?

# The classical cuboc2 phase diagram

- Chiral order parameter  $\rightarrow$  low temperature time reversal symmetry breaking phase

kapellasite



- Restoration of time reversal symmetry through a (weak) first order thermal phase transition  
*Domenge et al: PRB 78 2008*

# Summary of part II

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- Kapellasite appears experimentally as a true Spin Liquid: gapless and dynamic down to 20 mK in spite of disorder ( $J/1000$ )
- Kapellasite is not in the same spin liquid phase as herbertsmithite. Very far from any critical point.
- A good model with competing interactions has been obtained.
- In the classical limit this model describes a chiral phase. Does the classical chiral phase survive quantum fluctuations? If Yes it might be measured through RIXS (*Ko and Lee PRB 84 2011*)

# Outline

- A Quantum phase transition induced by Dzyaloshinskii-Moriya int. (*Cepas PRB 2008*) can explain the critical properties of herbertsmithite.
- Kapellasite: A new, different, gapless Spin Liquid. *B. Fåk, et al. PRL 109, 037208 (2012)*
  - Polymorph of herbertsmithite
  - Dynamical down to 20 mK
  - A good realization of a  $J_1$ - $J_2$ - $J_d$  model on the kagomé lattice with a ferromagnetic  $J_1$  (*Bernu 2012*)
- A chiral Spin Liquid?
  - The classical model has a chiral ground state (*Domenge PRB 2008, Messio PRB 2011*) and a weak first order phase transition at non zero temperature.
  - Does the chiral properties of the classical phase survive quantum fluctuations?



# Conclusion of this first part

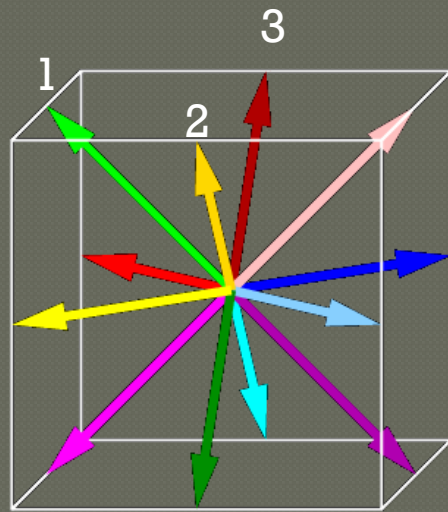
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- Critical properties of Herbertsmihte can be explained by the presence of a near-by Quantum Critical Point induced by Dzyaloshinskii-Moriya interactions.
- This nearby presence also explains why a small magnetic field is enough to push the system to a frozen phase.

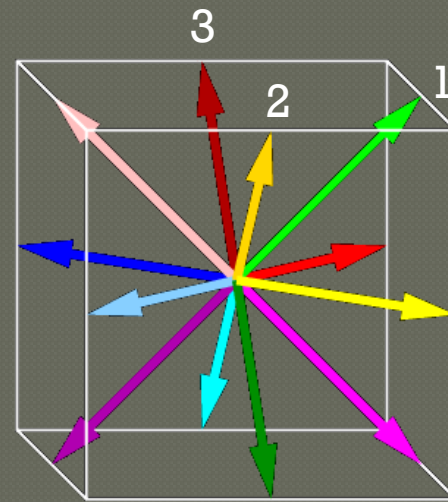
# The classical cuboc2 phase

- A chiral order parameter

$$\sigma = \frac{S_1 \cdot (S_2 \times S_3)}{|S_1 \cdot (S_2 \times S_3)|}$$



$$\sigma = +1$$



$$\sigma = -1$$



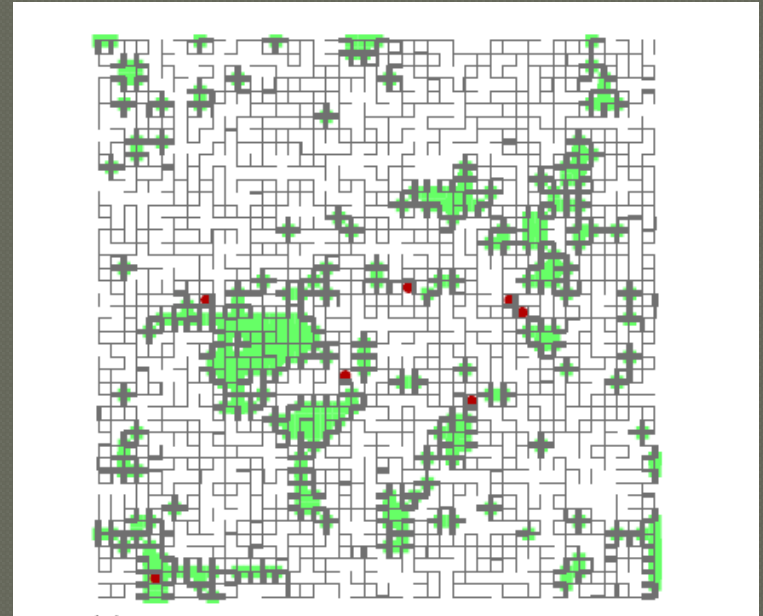
# First order phase transition mechanism

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Snapshot of a spin chirality configuration near the phase transition:

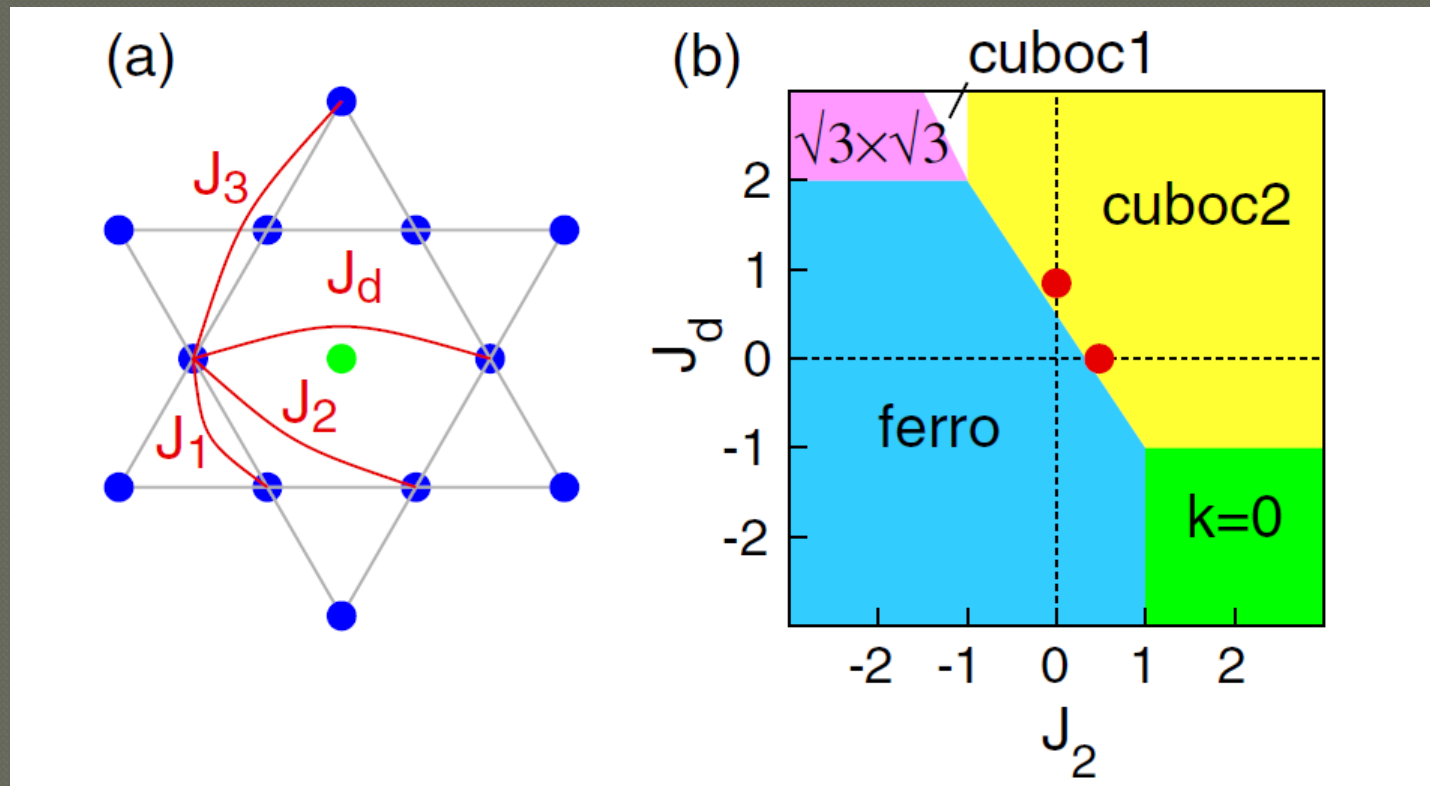
*$Z_2$  vortices (brown points) nucleate in the domain walls of chirality (white/green boundaries) and modify the domain wall energy*

*Messio et al. PRB 78*



# The classical cuboc2 phase

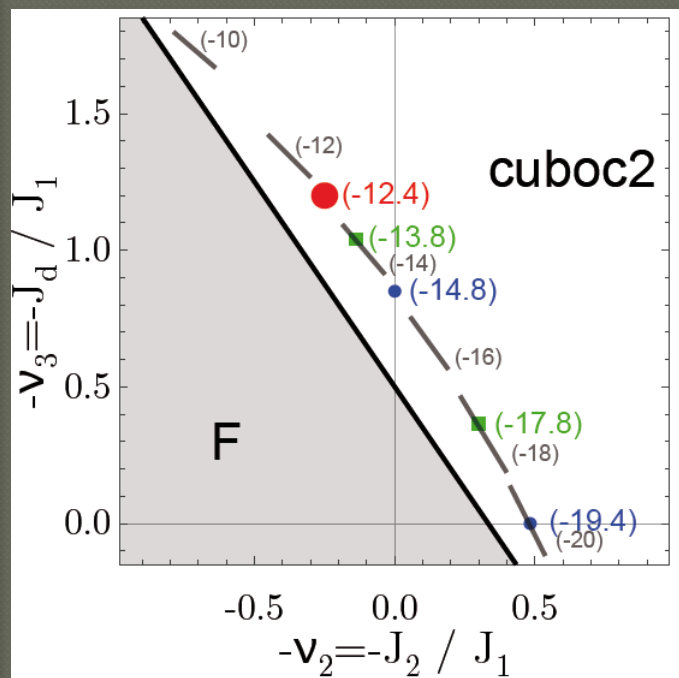
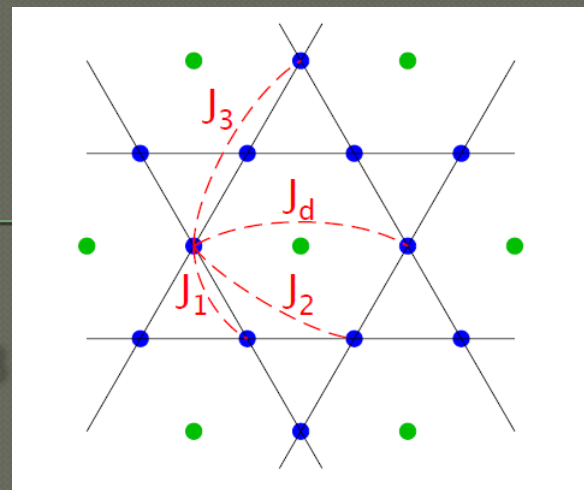
A large range of parameters with  $J_1$  ferro



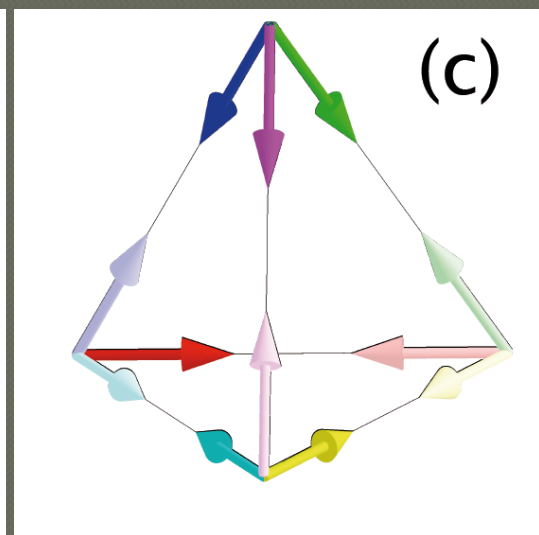
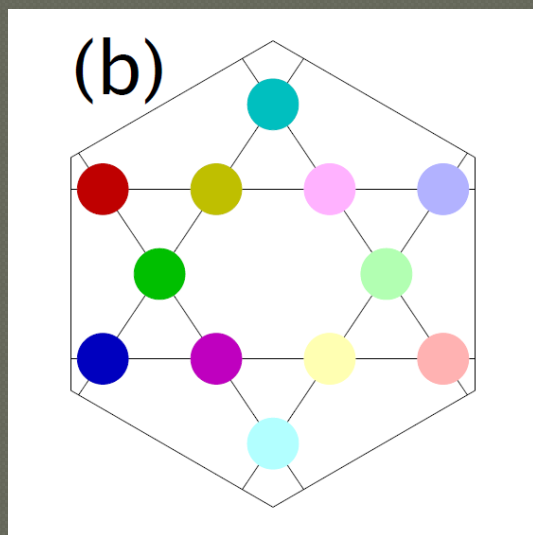
# HT series (B. Bernu 2012)

Competing exchange int.

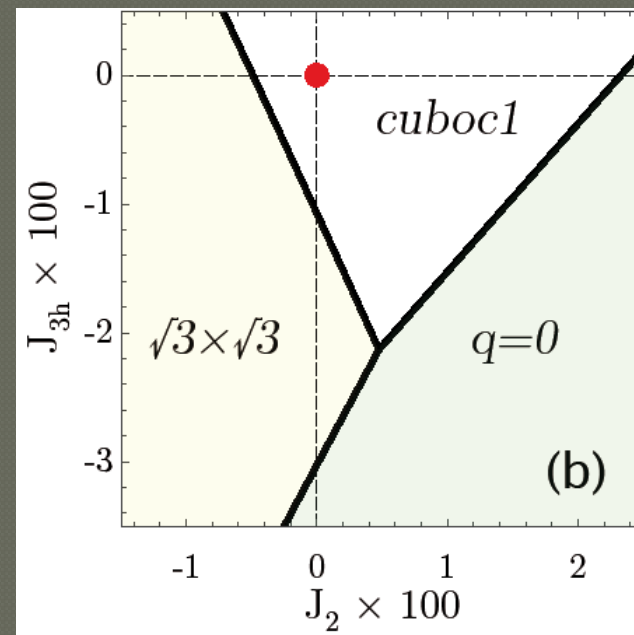
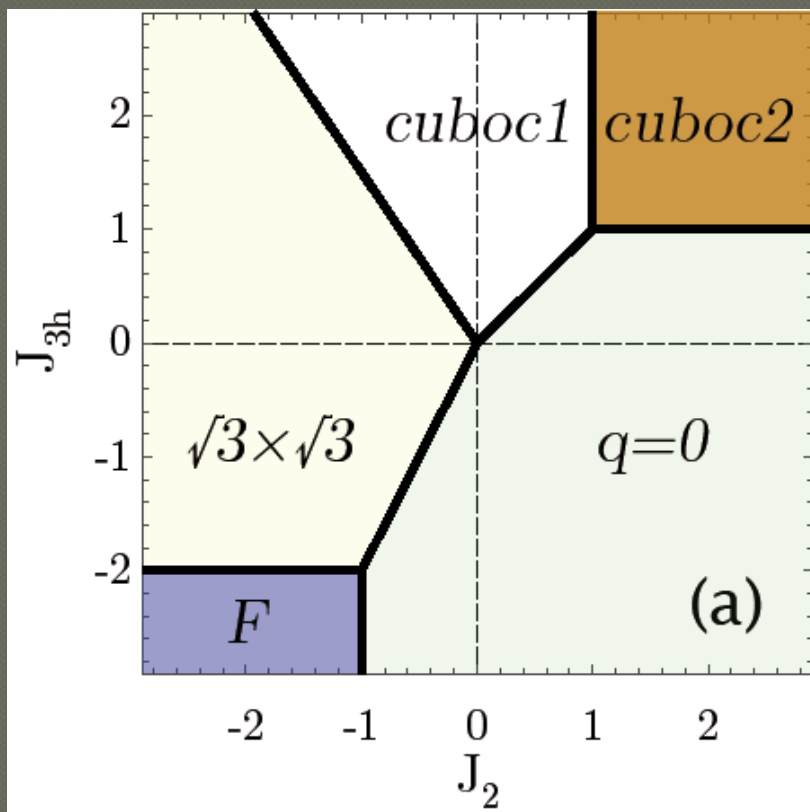
Best set of values  $J_1 = -12.4\text{K}$ ,  $J_2 = -5\text{K}$ ,  $J_d = +14.8$

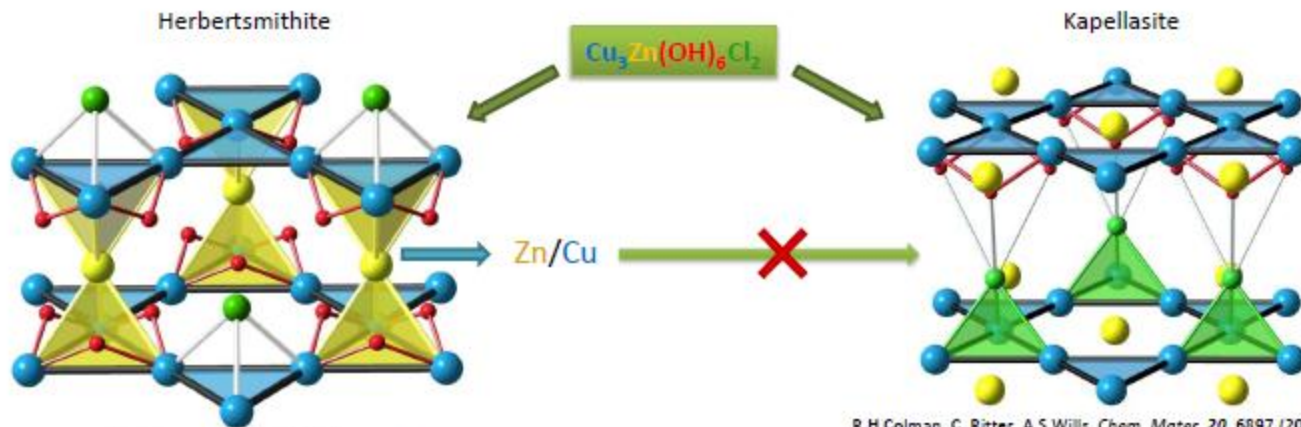


Classical phase diagram

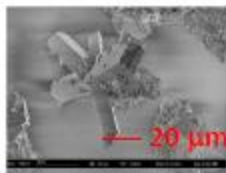


Classical order parameter



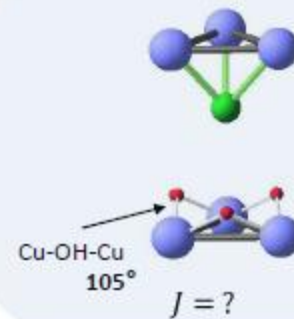
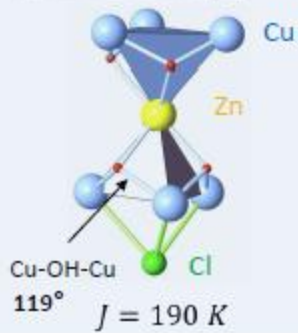
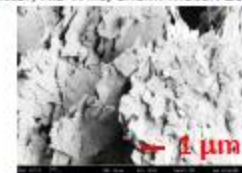


R.H Colman, C. Ritter, A.S Wills, Chem. Mater. 20, 6897 (2008)

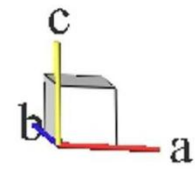


2D structure: weak OH—Cl hydrogen bondings

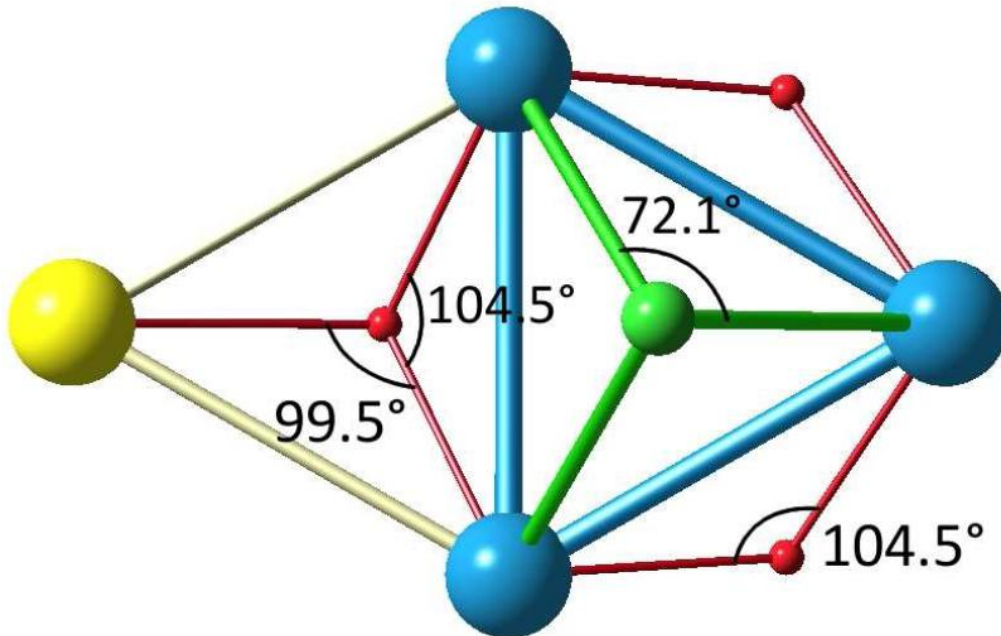
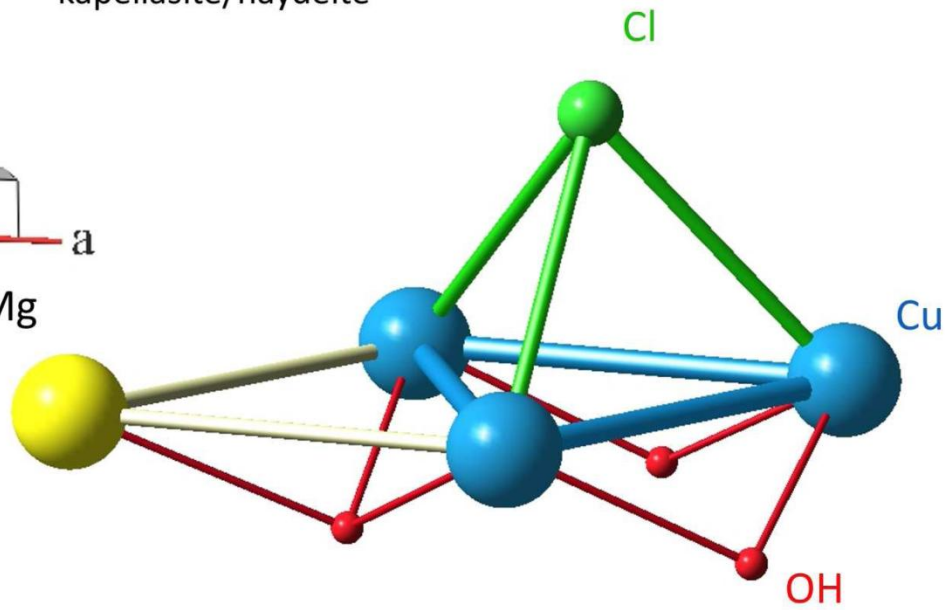
Cu—OH—Cu = 105°: Reduced first nn interaction, importance of further nn interactions !



kapellasite/haydéite



Zn/Mg



Zn

