

# Optical Absorption Inside the Mott Gap

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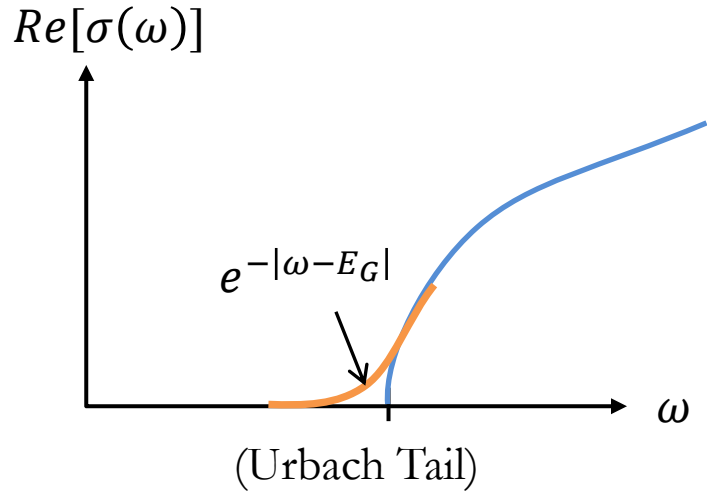
(in collaboration with Patrick Lee)

KITP Fragnets'12 – Tuesday October 23, 2012

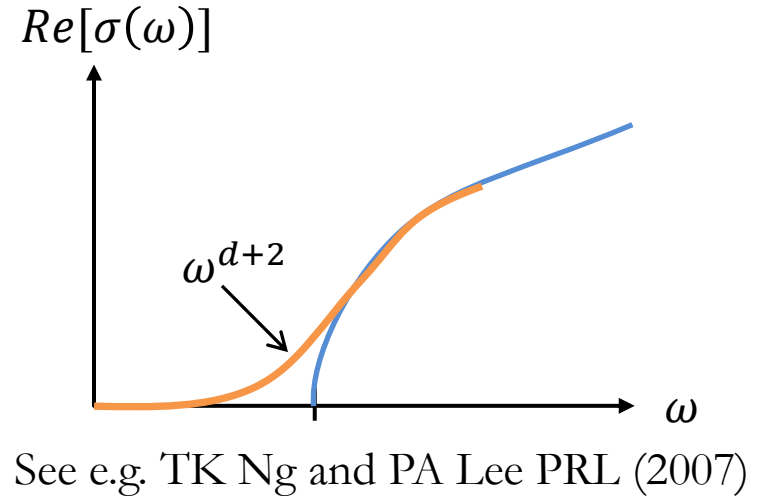


# Conductivity in Charge Insulators

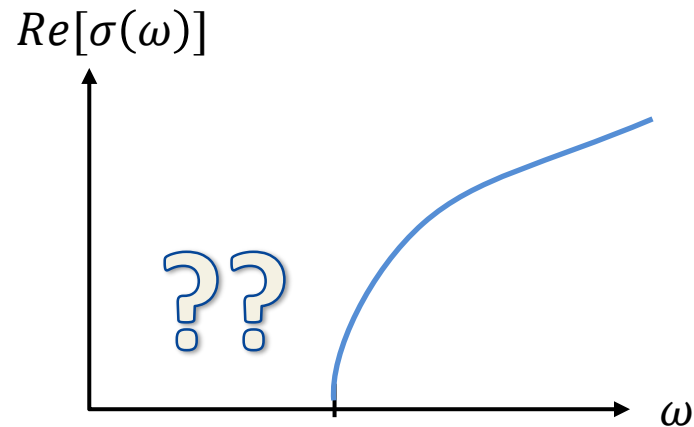
## Band Insulator



## Antiferromagnetic Insulator



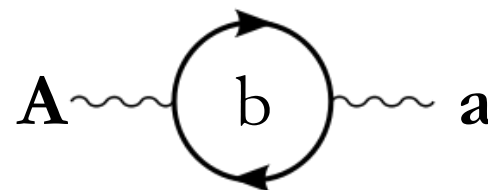
## Spin-Liquid Mott Insulator



# Effective Field Theory Description

$$c_\sigma = bf_\sigma$$

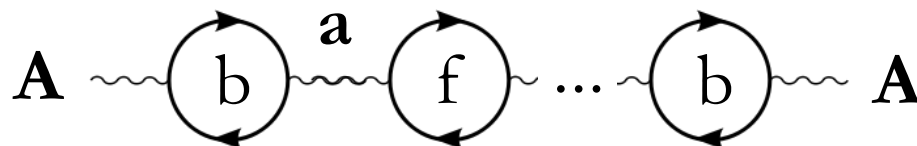
$$L = S_{0b} + S_{0f} + j_b \cdot (a + A) + j_f \cdot a$$



$$\int Db \Rightarrow L[a, A, f] = K_b(a + A)^2 + S_{0f} + j_f \cdot a$$

$$\int Df \Rightarrow L[a, A] = K_b(a + A)^2 + K_f a^2$$

$$\int Da \Rightarrow L[A] = \frac{K_b K_f}{K_b + K_f} A^2$$



$$\sigma_{\text{physical}} = \frac{\sigma_b \sigma_f}{\sigma_b + \sigma_f}$$

$$\text{Re}[\sigma] \approx \frac{\text{Im}[\sigma_b]^2}{\text{Re}[\sigma_f]}$$

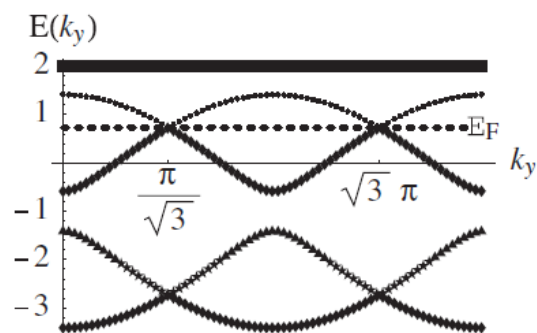
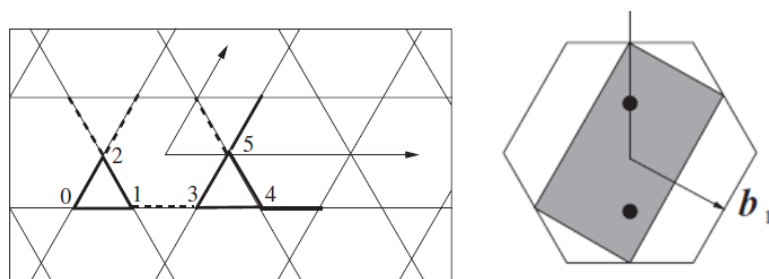
$$\omega^2 \left( \frac{\epsilon_c - 1}{4\pi} \right)^2$$

L. B. Ioffe and A. I. Larkin – *Gapless Fermions and Gauge Fields in Dielectrics*. PRB (1989)

TK Ng and PA Lee – *Power-Law Conductivity inside the Mott Gap: Application to [K-ET]*. PRL (2007)

# Fermionic Spin-Liquids

## Dirac Spin Liquid

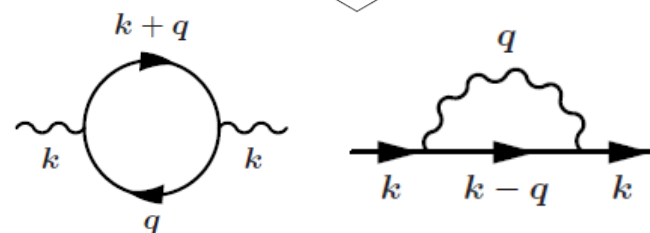
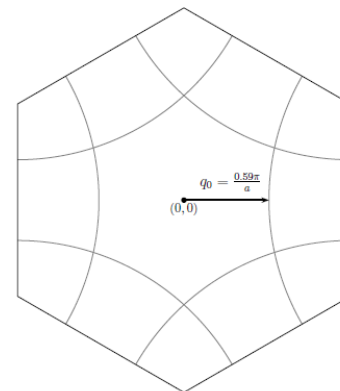


$$\sigma_f \sim \frac{\#e^2}{h}$$

$$\sigma_{electron} \sim \omega^2$$

See e.g. M. Hermele et al. PRB 2008

## Spinon Fermi-Surface

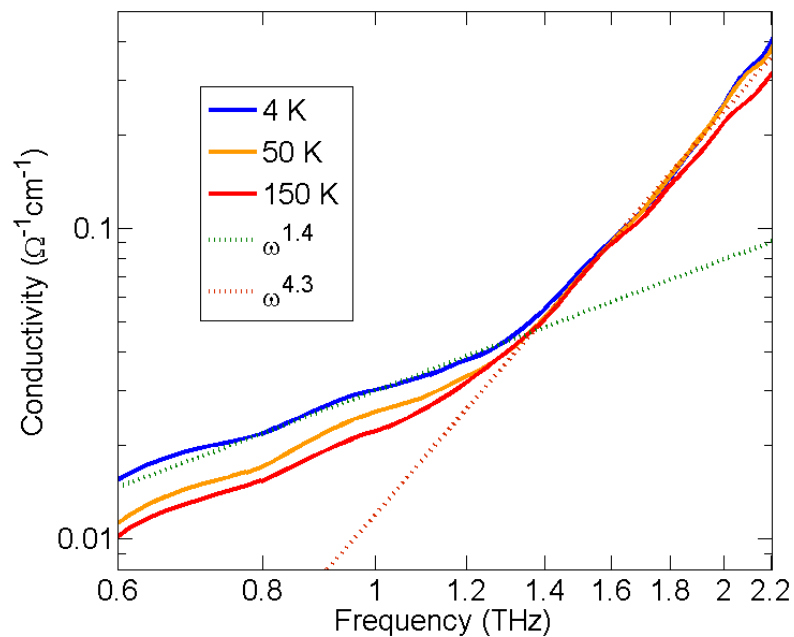
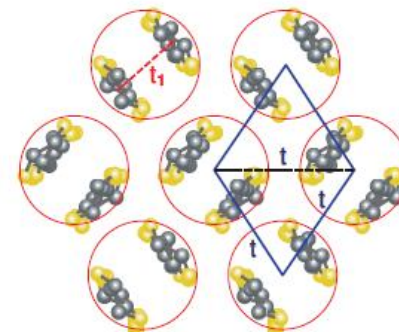
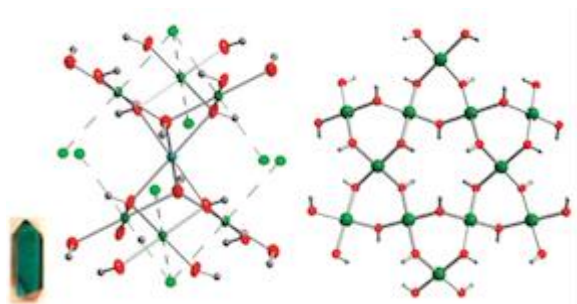


$$\sigma_f \sim \omega^{-4/3}$$

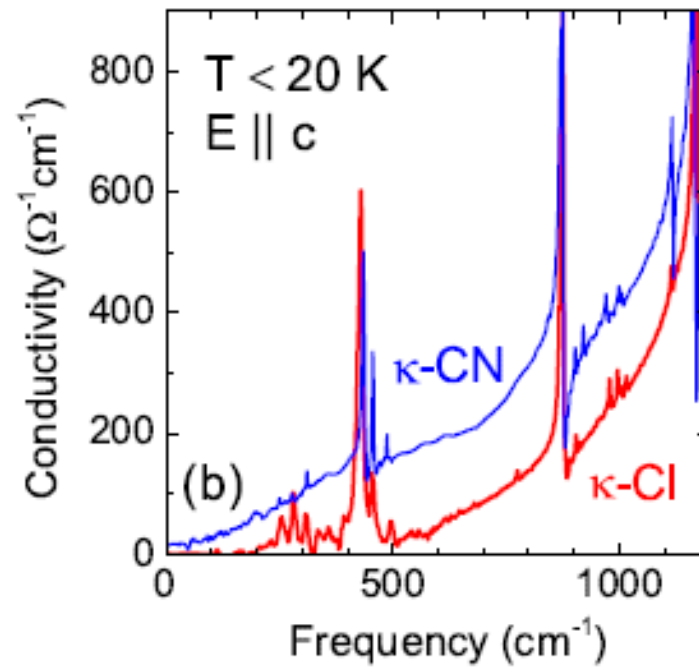
$$\sigma_{electron} \sim \omega^{3.33}$$

S.S. Lee and P.A. Lee PRL 2005  
C.Nave & P.A. Lee PRB 2007

# Experiments



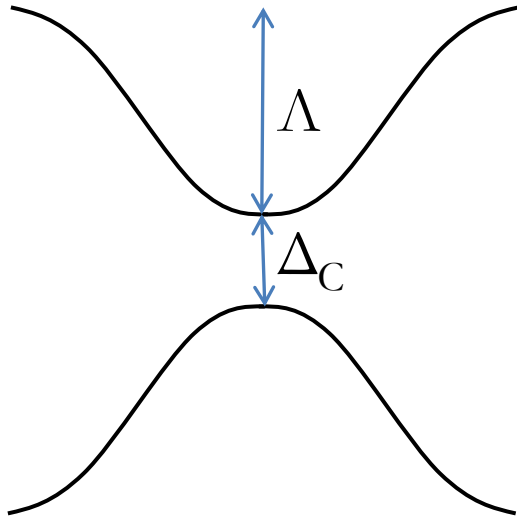
D. Pilon, J. Lui, A. Frenzel, Y. Lee, and N. Gedik  
(Unpublished)



Elsaesser et al. arXiv:1208.1664 (2012)

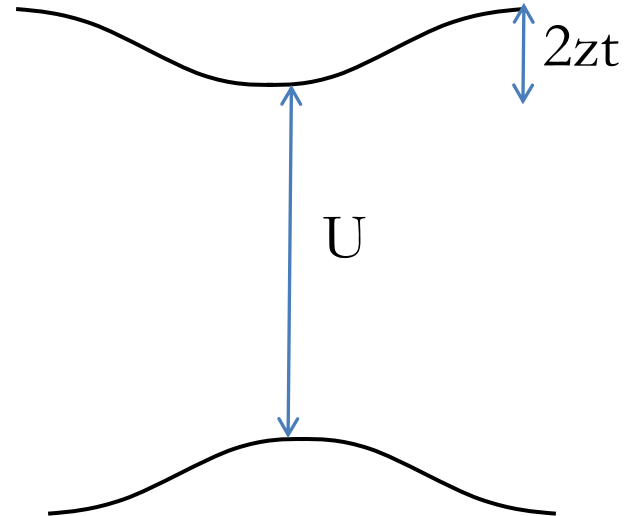
# Weak vs. Strong Mott Insulator

Weak Mott Insulator



$$\text{Im}[\sigma_b] \approx \frac{\#e^2}{h} \left( \frac{\omega}{\Delta_c} \right)$$

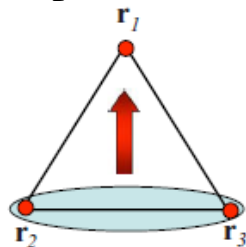
Strong Mott Insulator



$$\text{Im}[\sigma_b] \approx \frac{\#e^2}{h} \left( \frac{t}{U} \right)^3 \left( \frac{\omega}{t} \right)$$

$$\sigma(\text{Thz}) \sim 10^{-12} \Omega^{-1}$$

Compare to  $t/U$  expansion:  $\tilde{P}_y = 4\sqrt{3}ea(t/U)^3[\mathbf{S}_1 \cdot (\mathbf{S}_2 + \mathbf{S}_3) - 2\mathbf{S}_2 \cdot \mathbf{S}_3]$

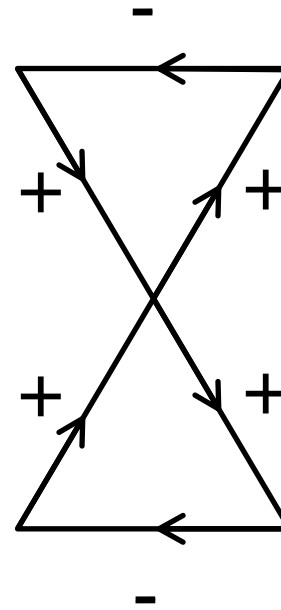
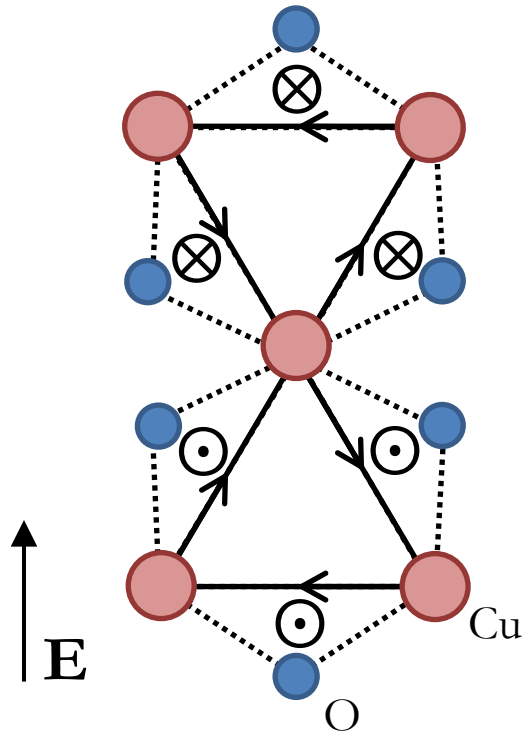


LN Bulaevskii, et al. PRB, 2008

# Other Mechanisms

DM Interactions

E-Field Modulation  
of DM

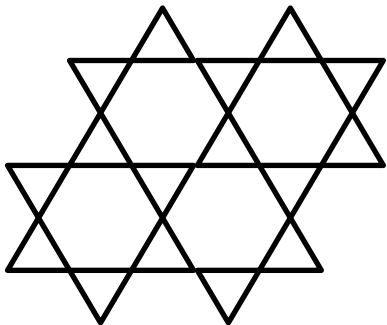


$$D_{ij} \cdot (\mathbf{S}_i \times \mathbf{S}_j) \Rightarrow i\lambda_{ij} \cdot (f_{ia}^+ \sigma_{ab} f_{jb}) + h.c.$$

$$(\mathbf{E}(t) \times \hat{z}) \cdot \mathbf{J}^{Sz}$$

$$\sigma \sim \omega^2$$

$$\sigma(\text{Thz}) \sim 10^{-9} \Omega^{-1}$$



# Thanks for your attention – Questions?

Thank you to:

- KITP – Hosting this Research/Program
- Patrick Lee – Many helpful conversations

