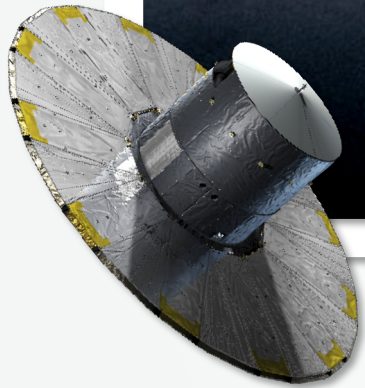


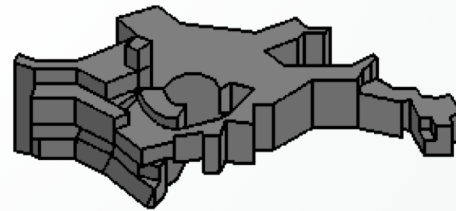
„In the Balance: Stasis and Disequilibrium in the Milky Way“  
KITP, Santa Barbara, 1. April 2018



# THE GALACTIC DISC & BAR IN ACTION-ANGLE SPACE AS SEEN BY GAIA DR2

Wilma Trick (MPA, Garching/Munich)

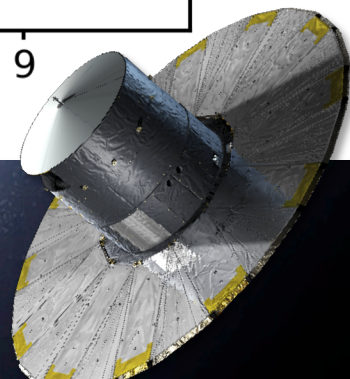
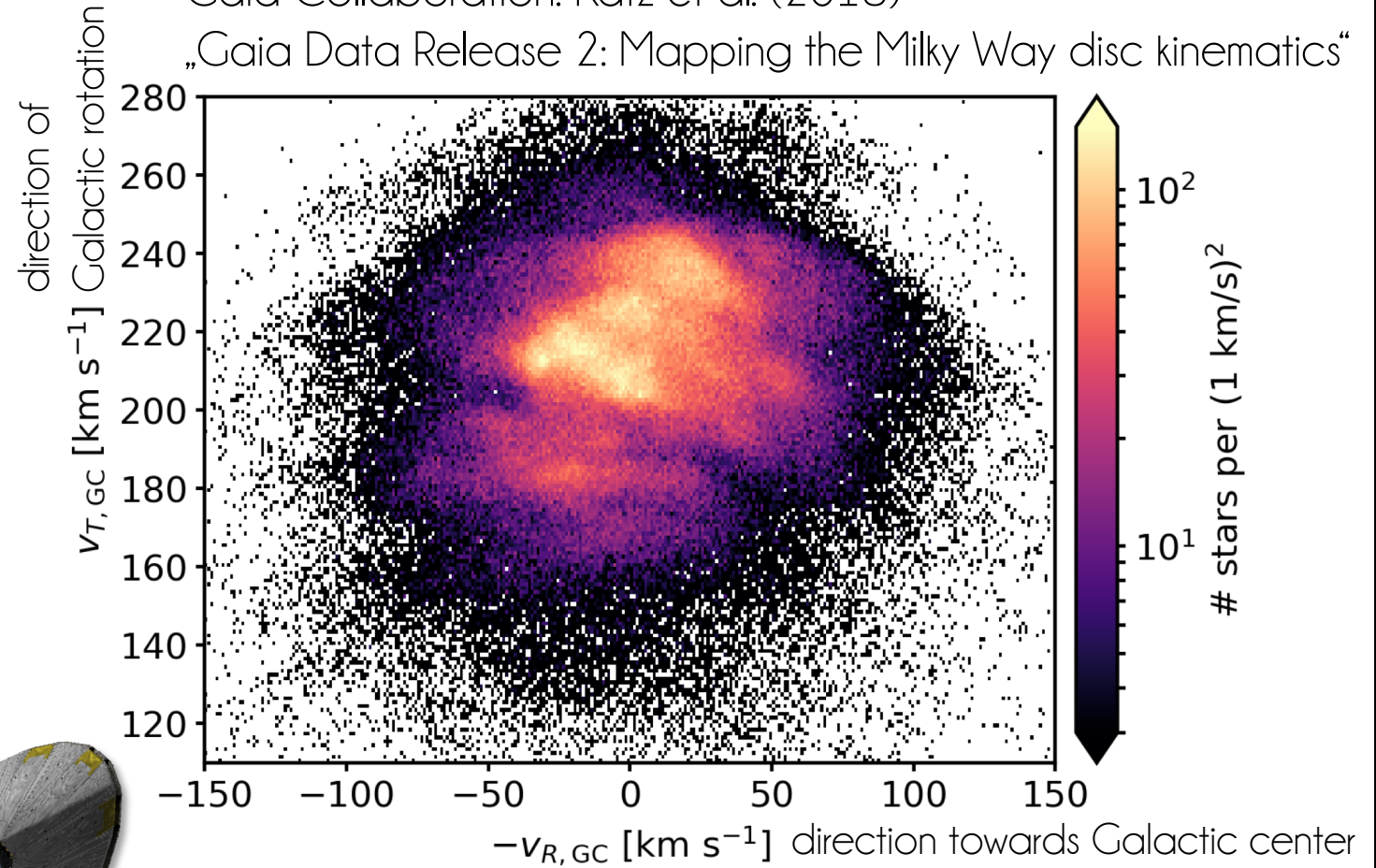
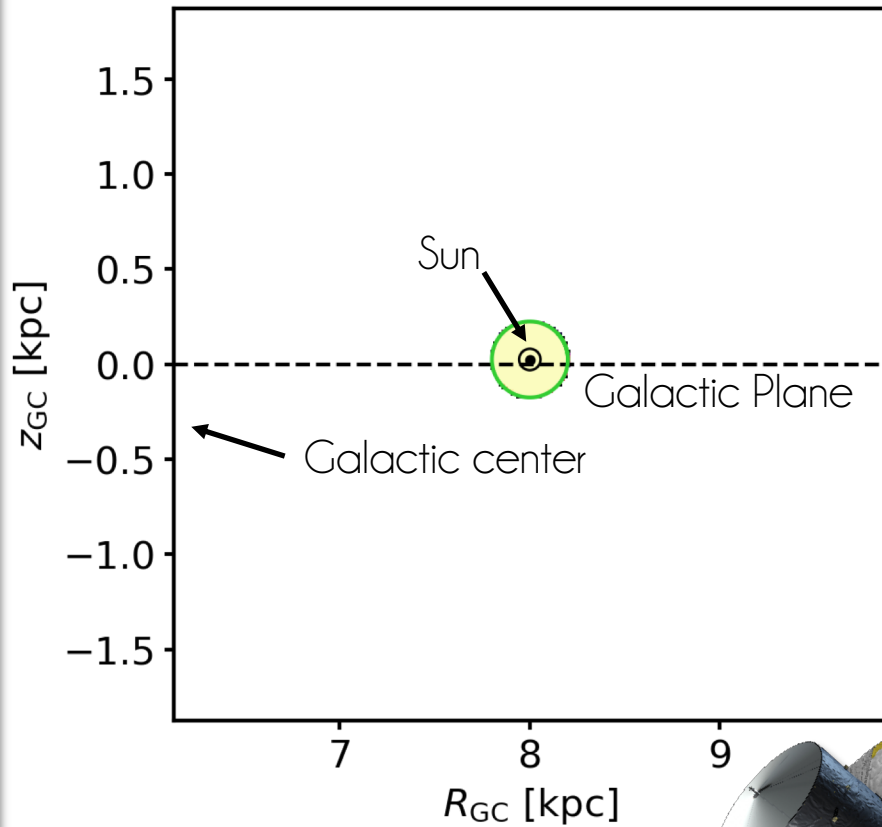
Johanna Coronado (MPIA Heidelberg), Francesca Fragkoudi (MPA Garching),  
Jason Hunt (Uni Toronto), Ted Mackereth (Uni Birmingham),  
Hans-Walter Rix (MPIA Heidelberg), Jerry Sellwood (Uni Arizona),  
Simon White (MPA Garching), Jo Bovy (Uni Toronto)



# THE IN-PLANE MOTIONS OF THE SOLAR NEIGHBOURHOOD: GAIA DR2

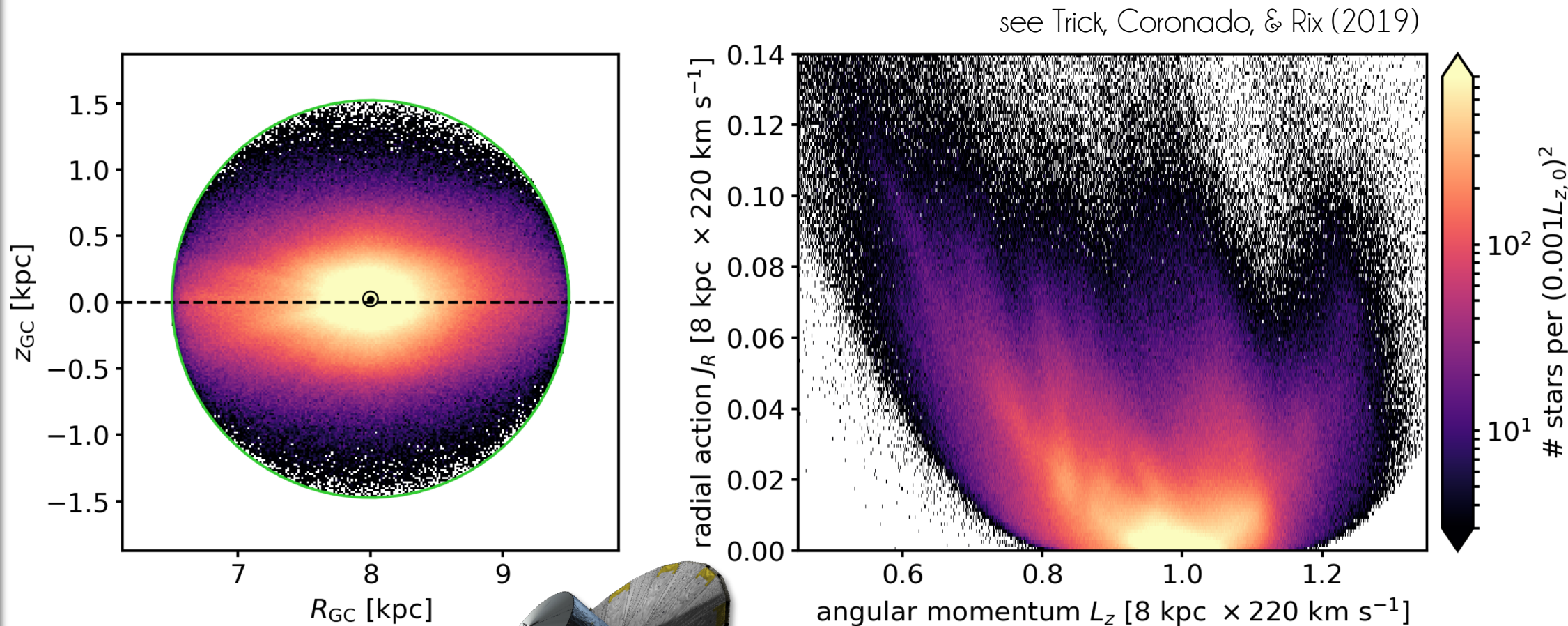
Gaia Collaboration: Katz et al. (2018)

„Gaia Data Release 2: Mapping the Milky Way disc kinematics“

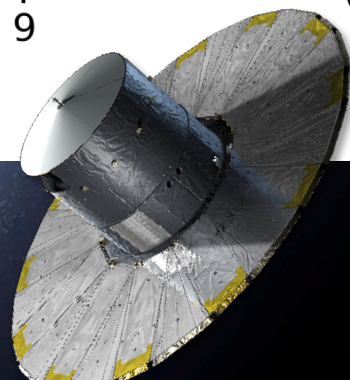




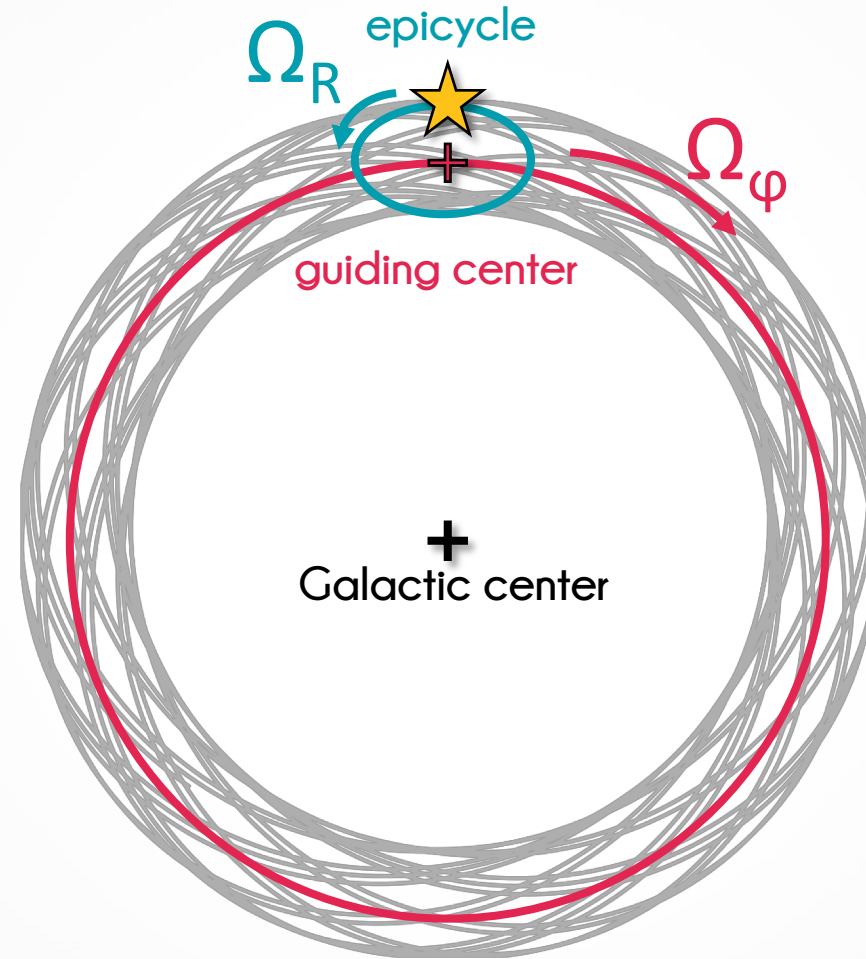
# THE IN-PLANE MOTIONS OUT TO 1.5 KPC: GAIA DR2 IN ACTION SPACE



Stars in the Gaia DR2 / RVS sample within 1.5 kpc, most stars have `parallax_over_error` > 20  
→ 5% distance error



# DISK ORBITS IN THE EPICYCLE APPROXIMATION



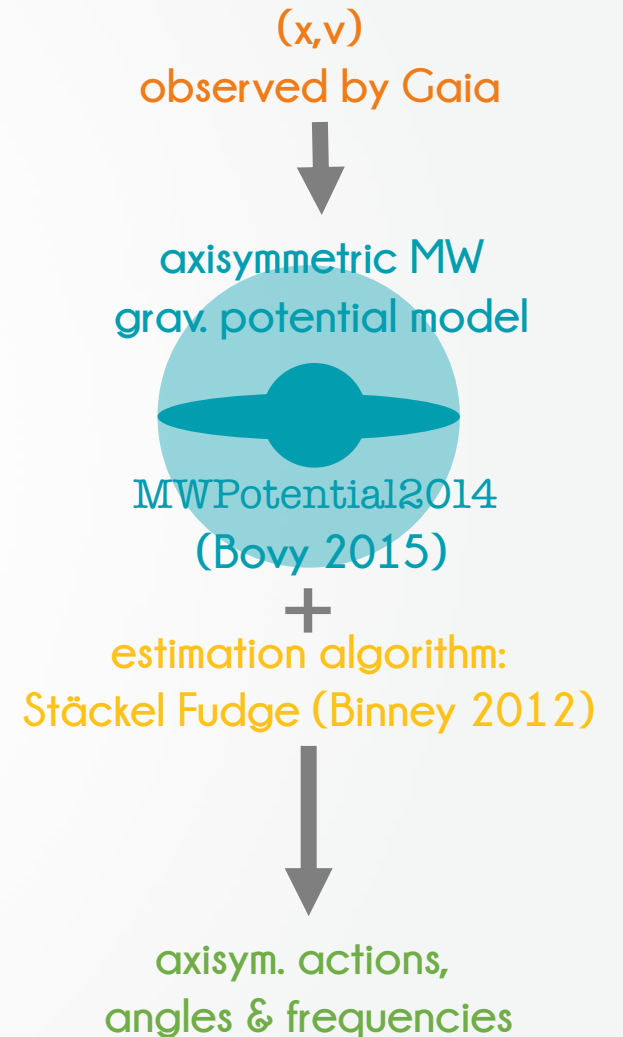
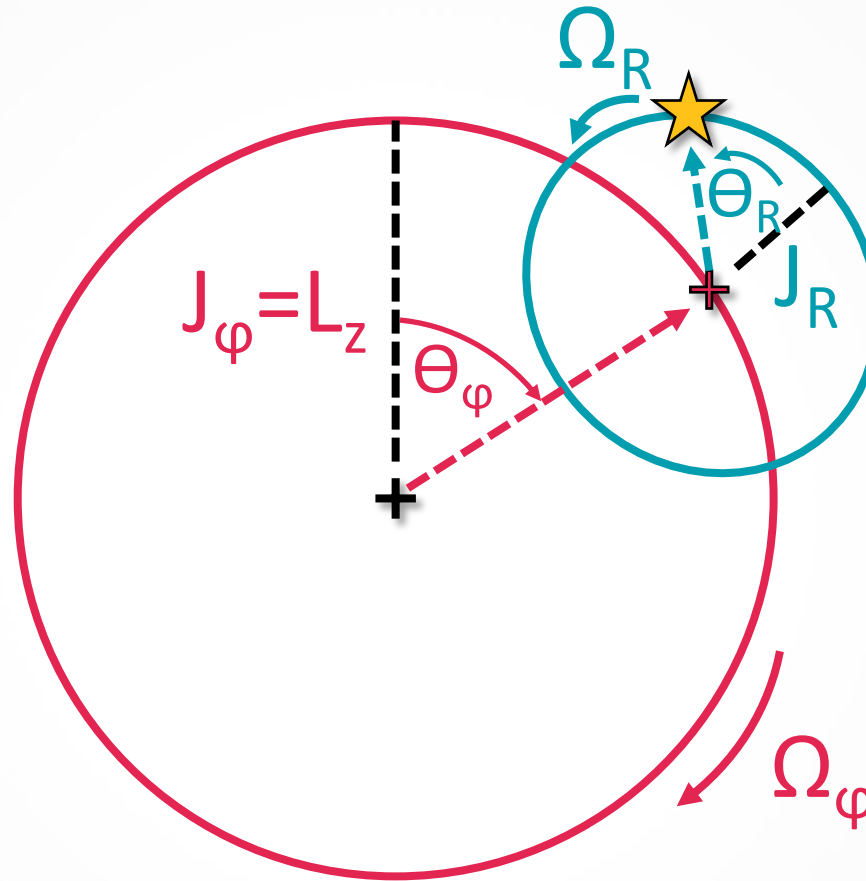


# ACTION-ANGLE COORDINATES (EXPLAINED WITH EPICYCLES)

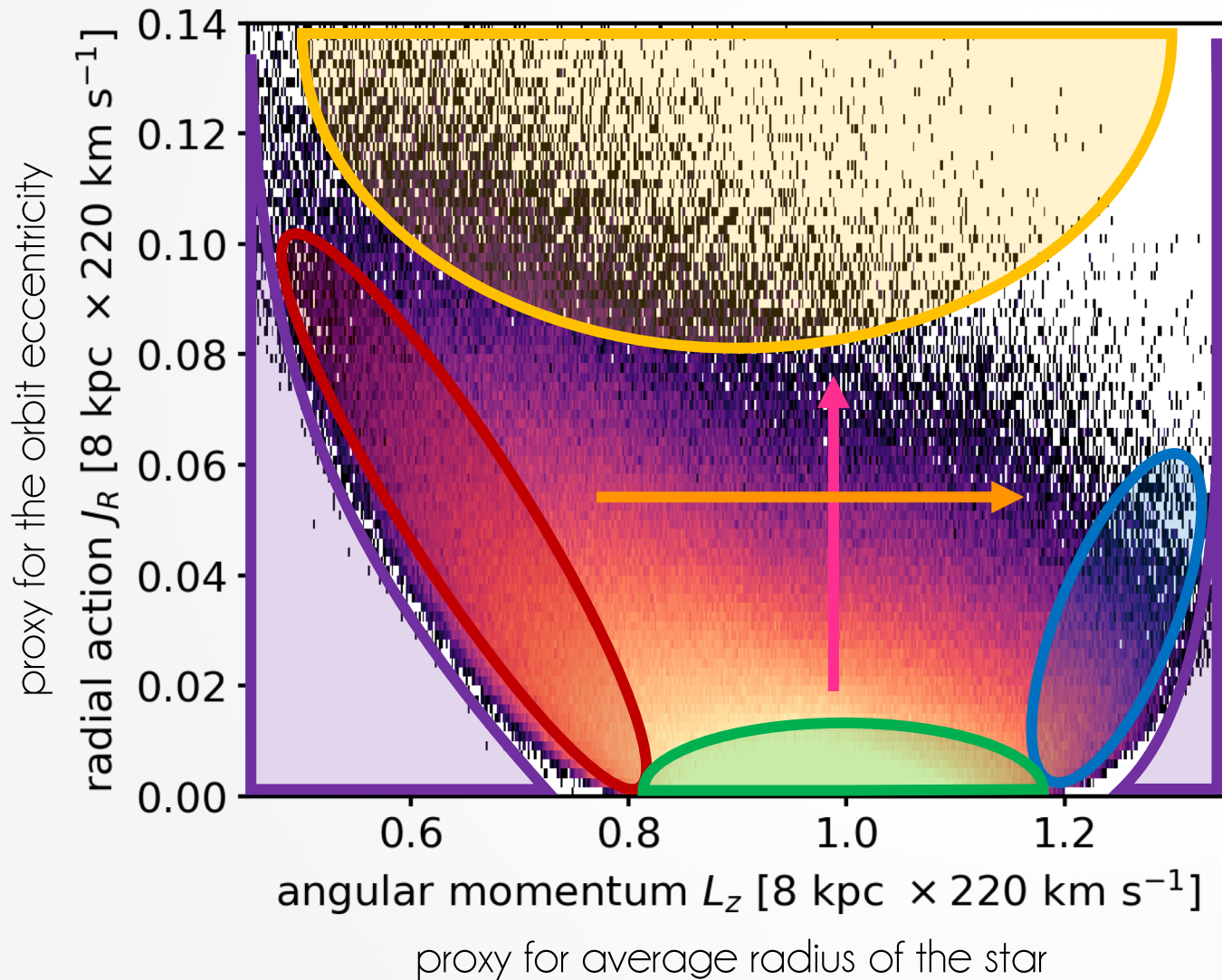
size of circle  
→ actions  $J$   
→ „label“ one orbit

position on circle  
→ angles  $\theta = \Omega \cdot t$

fundamental  
frequencies  $\Omega$



# UNDERSTANDING ACTION SPACE



## Interpretation:

Stars on...

- ... near-circular orbits with  $R \in R_\odot \pm 1.5$  kpc
- ... rare, highly eccentric orbits

## Population effects:

- radially decreasing stellar density
- radial velocity dispersion

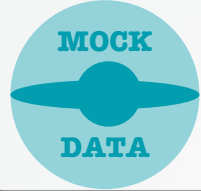
## Selection effects:

Stars...

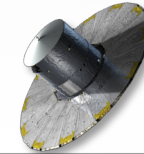
- ... close to pericenter
- ... close to apocenter
- ... on orbits that do not reach into the survey volume (exist, but are not observed)



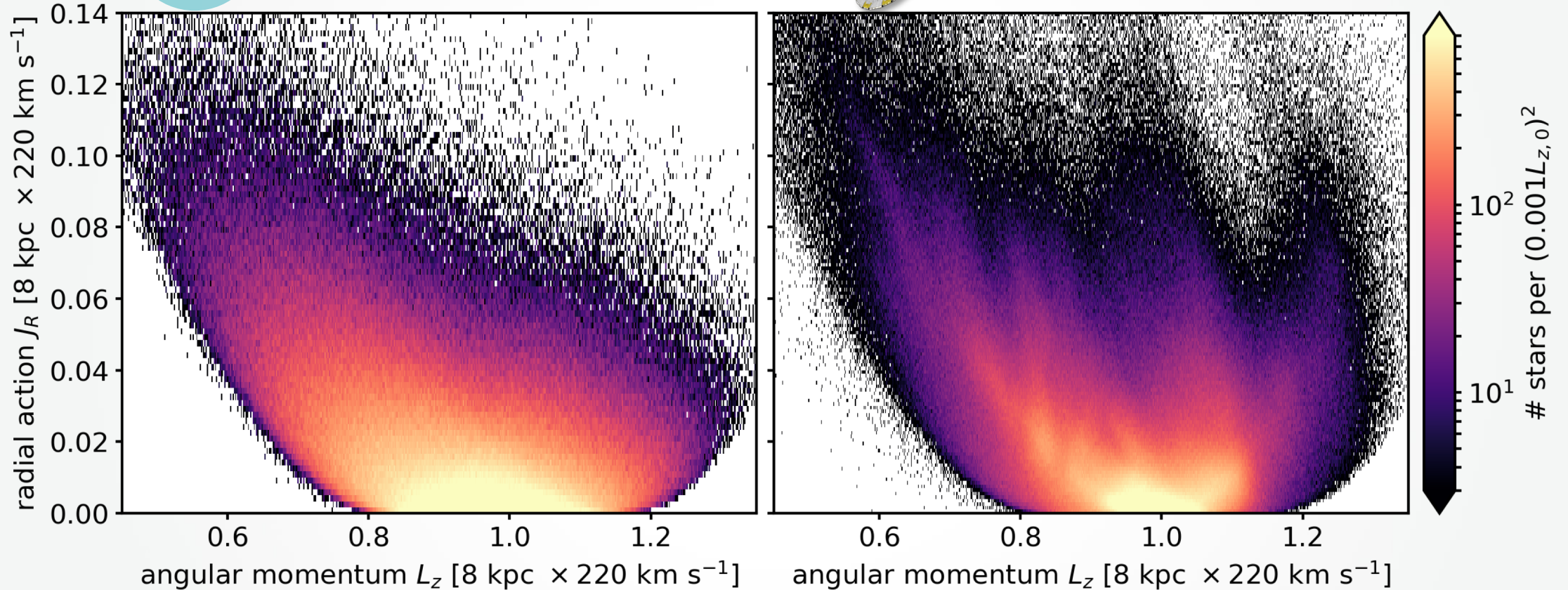
# THE IN-PLANE MOTIONS OUT TO 1.5 KPC: GAIA DR2 IN ACTION SPACE



Axisymmetric mock data



Gaia DR2 data



Mock data model:

- MWPotential2014 (Bovy 2015)
- quasi-isothermal distribution function for the stellar disk (Binney & McMillan 2011)
- spherical survey volume around the Sun,  $r=1.5$  kpc (Trick et al. 2016)

see Trick, Coronado, & Rix (2019)

# THE WAY FORWARD

Gaia DR2 🤖

## The Goal with Gaia:

axisymmetric **action-based dynamical modeling** of the MW disk

- grav. **potential** (e.g. dark matter)
- chemo-orbital distr. of disk stars
- as baseline for perturbation theory

### Axisym. actions & DFs:

Binney 12; Binney & McMillan 11; Sanders & Binney 15

### RoadMapping modeling:

my PhD thesis, Trick+ 16,17; Bovy & Rix 13;

Similar approach: Piffl+ 15

action-based modeling  
incl. perturbations:

Monari+ 16,17,19; Binney 18

## Understanding action sub-structure:

- 1) **Data**: Properties of the substructure
- 2) **Theory**: signatures of underlying mechanisms – e.g. **resonances**
- 3) **Qualitative**: „labelling“ the features by perturber (bar, spiral arm, satellite fly-by)
- 4) **Quantitative**: dynamical **modeling** using informed guess & improved models

### Resonances in...

#### ...velocity space:

e.g. Binney & Lacey 88; De Simone 04; Quillen+ 03,05; Antoja+ 2011; Fux+ 01; Monari et al. 17, Fragkoudi,...,Trick+ 19

#### ...axisym. action space:


e.g. Sellwood & Binney 02; Sellwood 10; McMillan 11; Fouvy+ 15a,b; Sellwood, Trick+ 19

of velocity space with Hipparcos or Gaia DR1:

e.g. Dehnen 00; Minchev+ 10; Antoja+ 15; Monari+ 17

...simpler middle ground using **axisymmetric actions**, angles & frequencies...?





PART 2:  
THE EXTENDED ORBIT SUB-STRUCTURE  
OF THE GALACTIC DISK  
AS SEEN BY GAIA DR2

Hipparcos volume



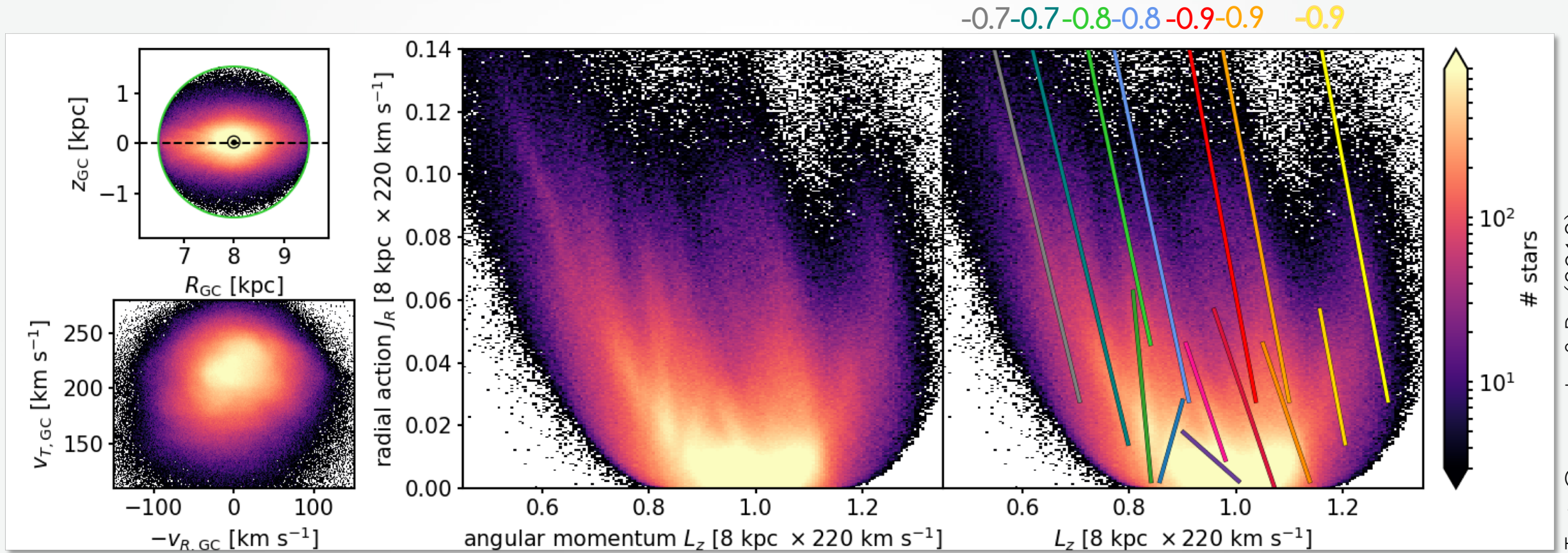
volume of Gaia DR2 / RVS  
with good parallaxes

Trick, Coronado, & Rix (2019)



# OUTSIDE OF THE SOLAR NEIGHBOURHOOD: THE EXTENDED ORBIT STRUCTURE

Gaia DR2 in Action Space



Trick, Coronado, & Rix (2019)

high  $J_R$ :

- 1) overdensities along linear lines
- 2) parallel pairs

low  $J_R$ :

- 1) different slopes
- 2) one with positive slope

estimated slopes  $\Delta J_R / \Delta L_z$

-1.8 0.6 -0.5 -0.5 -0.9  
-0.15 -0.5



# THE SOLAR NEIGHBOURHOOD: MOVING GROUPS

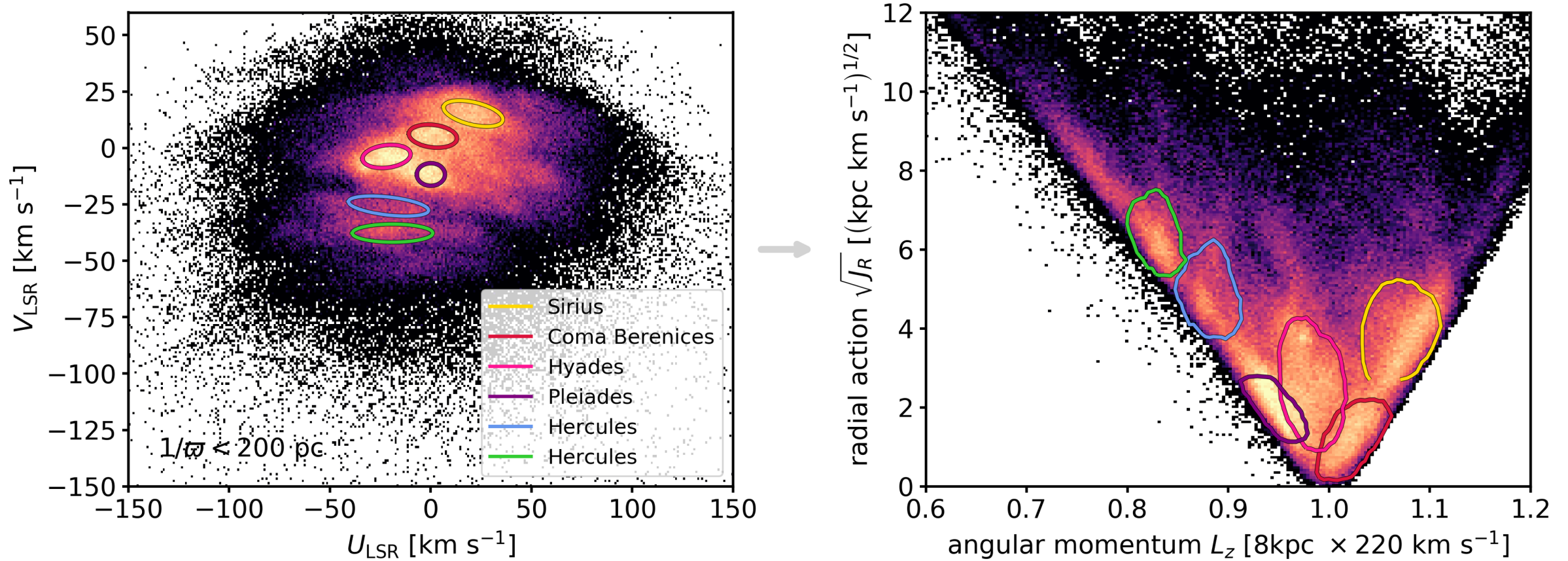


figure from Trick, Coronado & Rix (2019)

# THE SOLAR NEIGHBOURHOOD: MOVING GROUPS & ARCHES

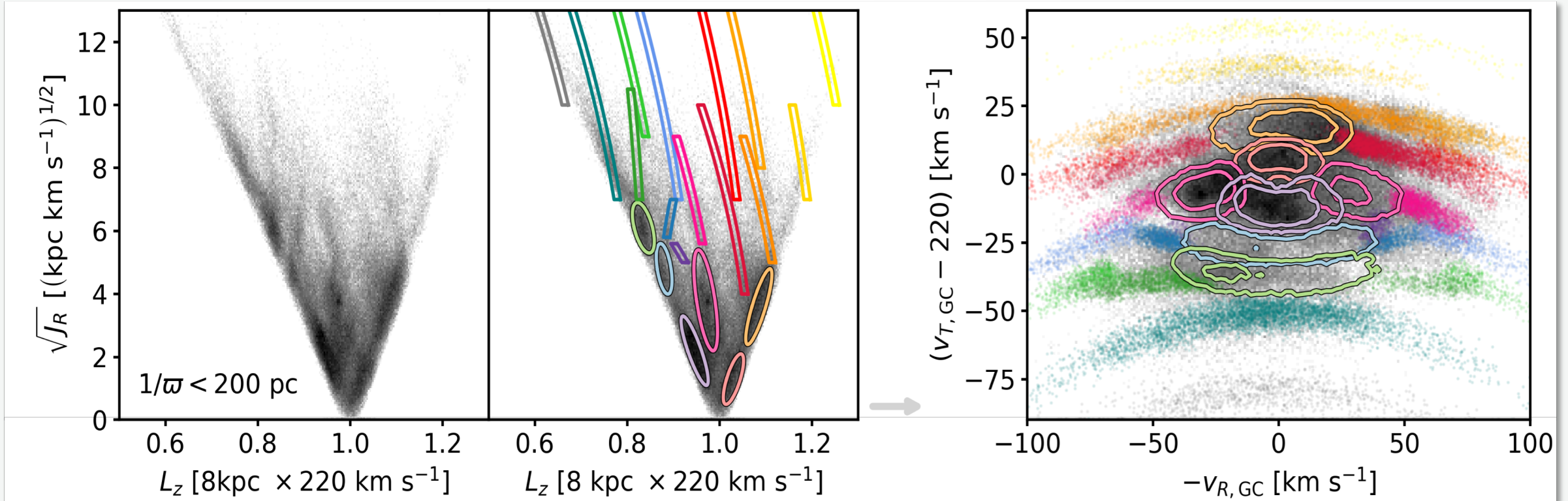


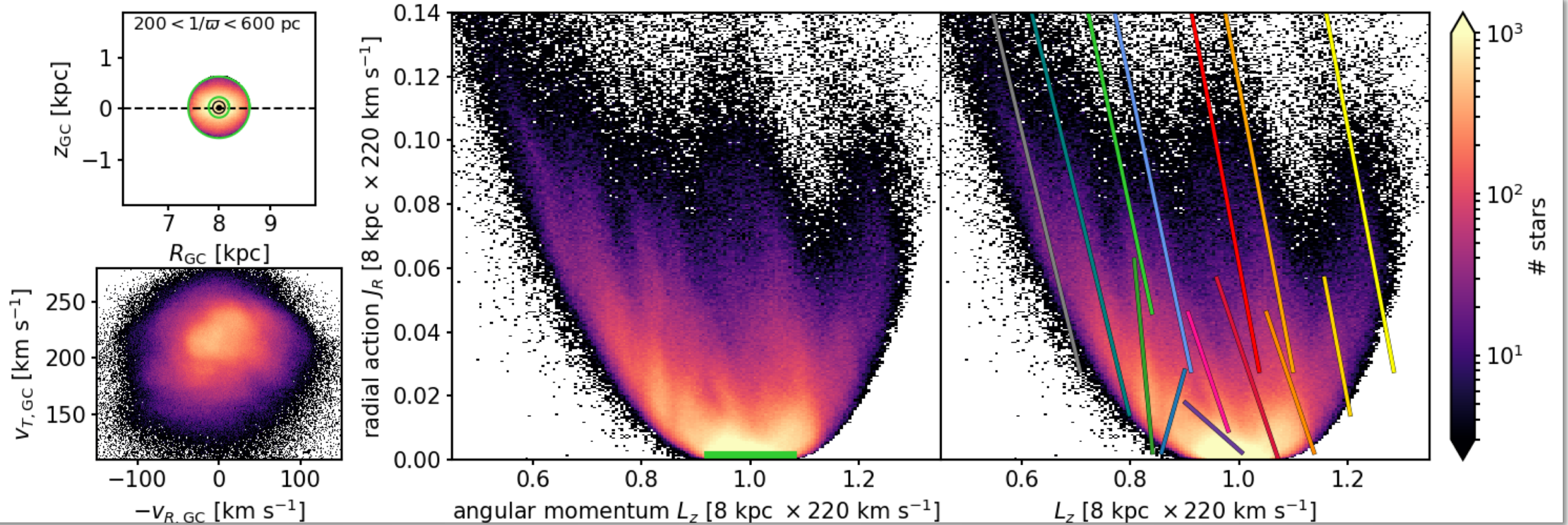
figure from Trick, Coronado & Rix (2019)

In the Solar neighbourhood, the lines in action space correspond to the **arches in velocity space** discovered by Gaia Collaboration: Katz et al. (2018) and Kawata et al. (2018).

**BUT:** More nicely visible in action space. 😊

**NOTE:** Asymmetric numbers of stars in positive and negative radial velocity

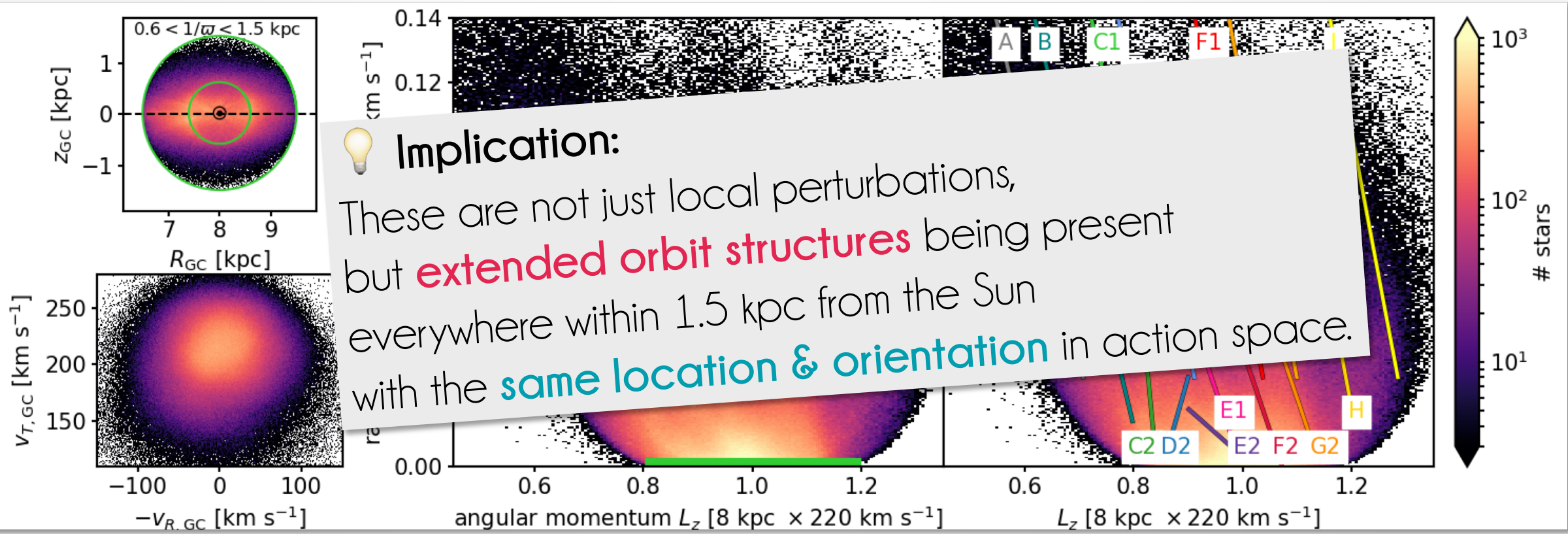
# OUTSIDE OF THE SOLAR NEIGHBOURHOOD: THE EXTENDED ORBIT STRUCTURE



Trick, Coronado, & Rix (2019)



# OUTSIDE OF THE SOLAR NEIGHBOURHOOD: THE EXTENDED ORBIT STRUCTURE

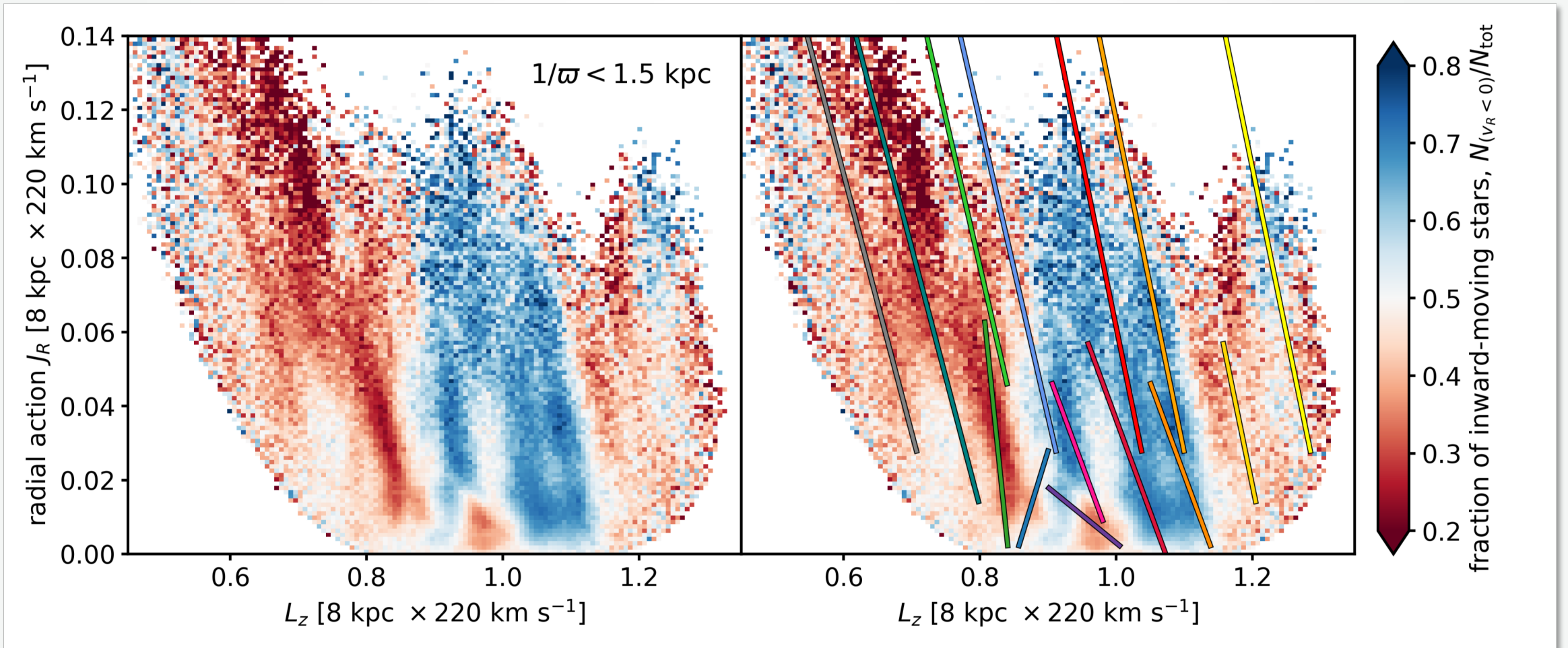


Trick, Coronado, & Rix (2019)

The moving groups are the local, selection function affected manifestation of this extended orbit structure.

# PROPERTIES OF THE EXTENDED ORBIT STRUCTURE

- 1) stars are not phase-mixed along orbits  $\rightarrow$  large-scale analogue to asymmetry in  $(v_R, v_T)$  plot
- 2) strongest asymmetries related to action-space overdensities







PART 3:

WHAT DO „AXISYMMETRIC ACTIONS“  
TELL US ABOUT THE GALACTIC BAR?



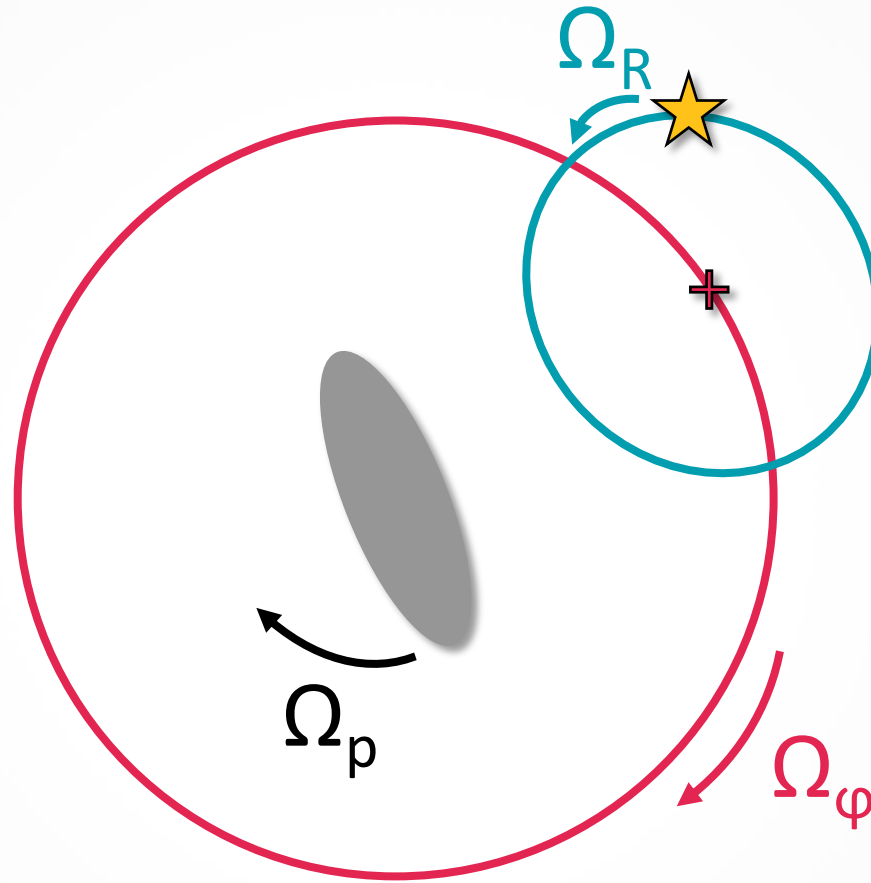
Paper to be submitted soon...





# RESONANCES IN A NON-AXISYMMETRIC GALAXY

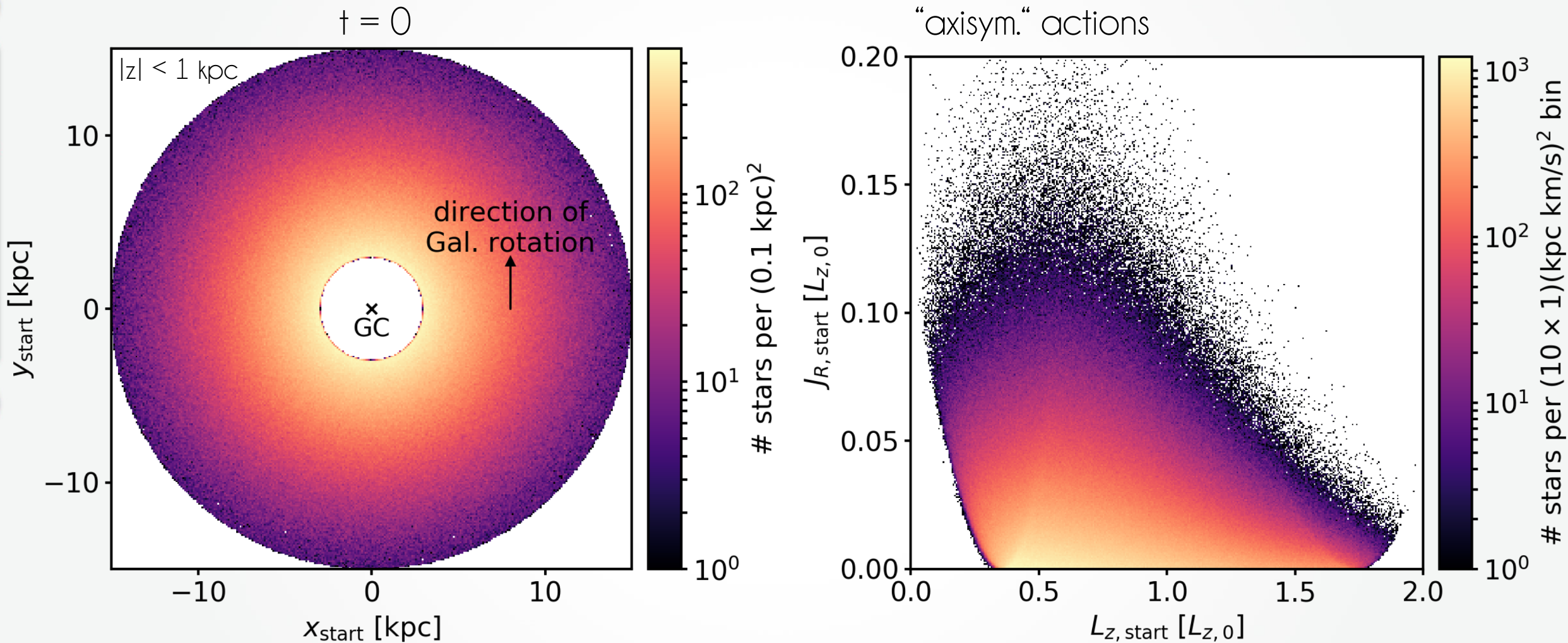
$$m \cdot (\Omega_p - \Omega_\varphi) - l \cdot \Omega_R = 0$$



m-fold symmetric perturbation  
e.g.  $m = 2$  is strong for bar

- $l = 0$ : Co-rotation resonance (CR)
- $l = +1$ : Outer Lindblad resonance (OLR)
- $l = -1$ : Inner Lindblad resonance (ILR)

# CREATE MOCK DATA STARS IN MW POTENTIAL

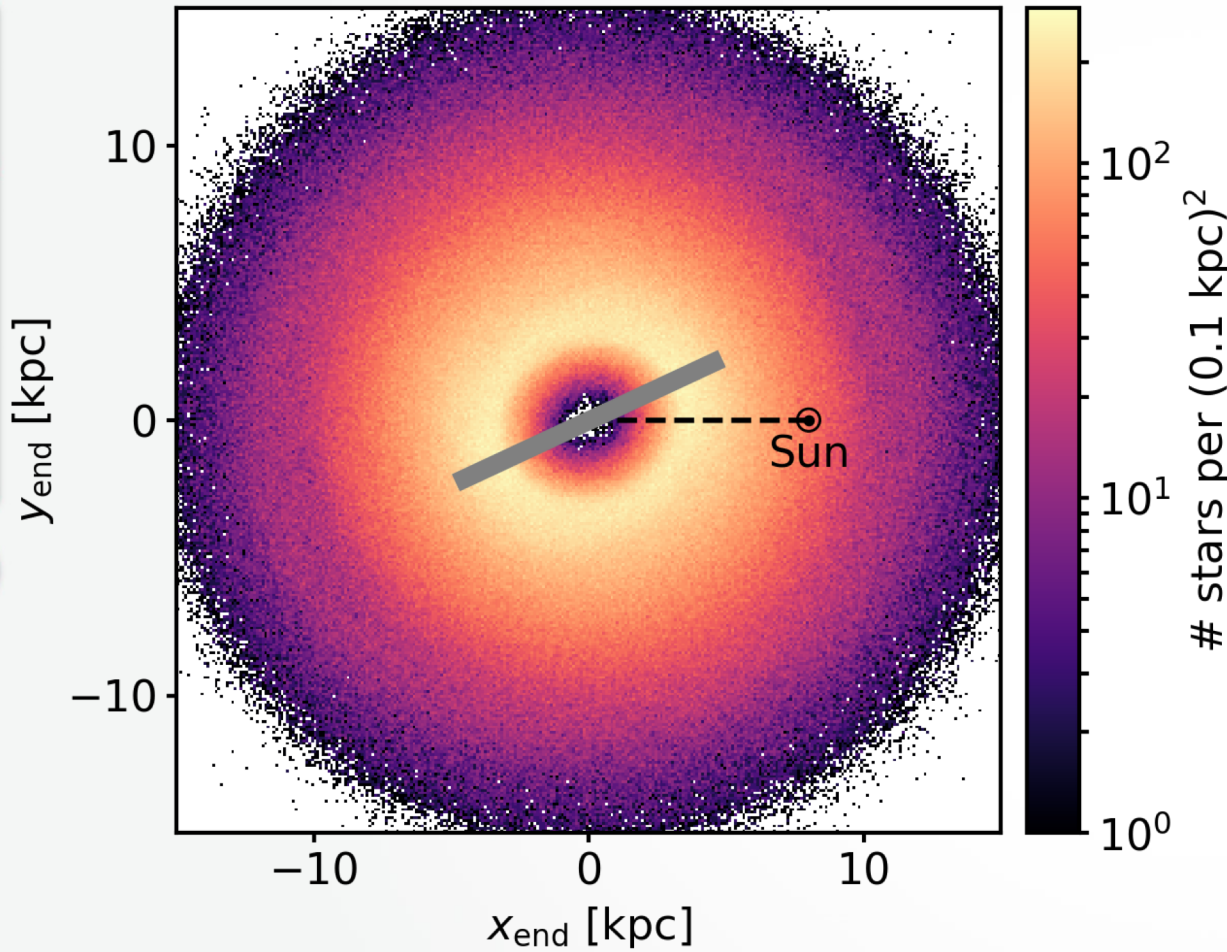


axisymmetric MWPotential2014 (Bovy 2014)

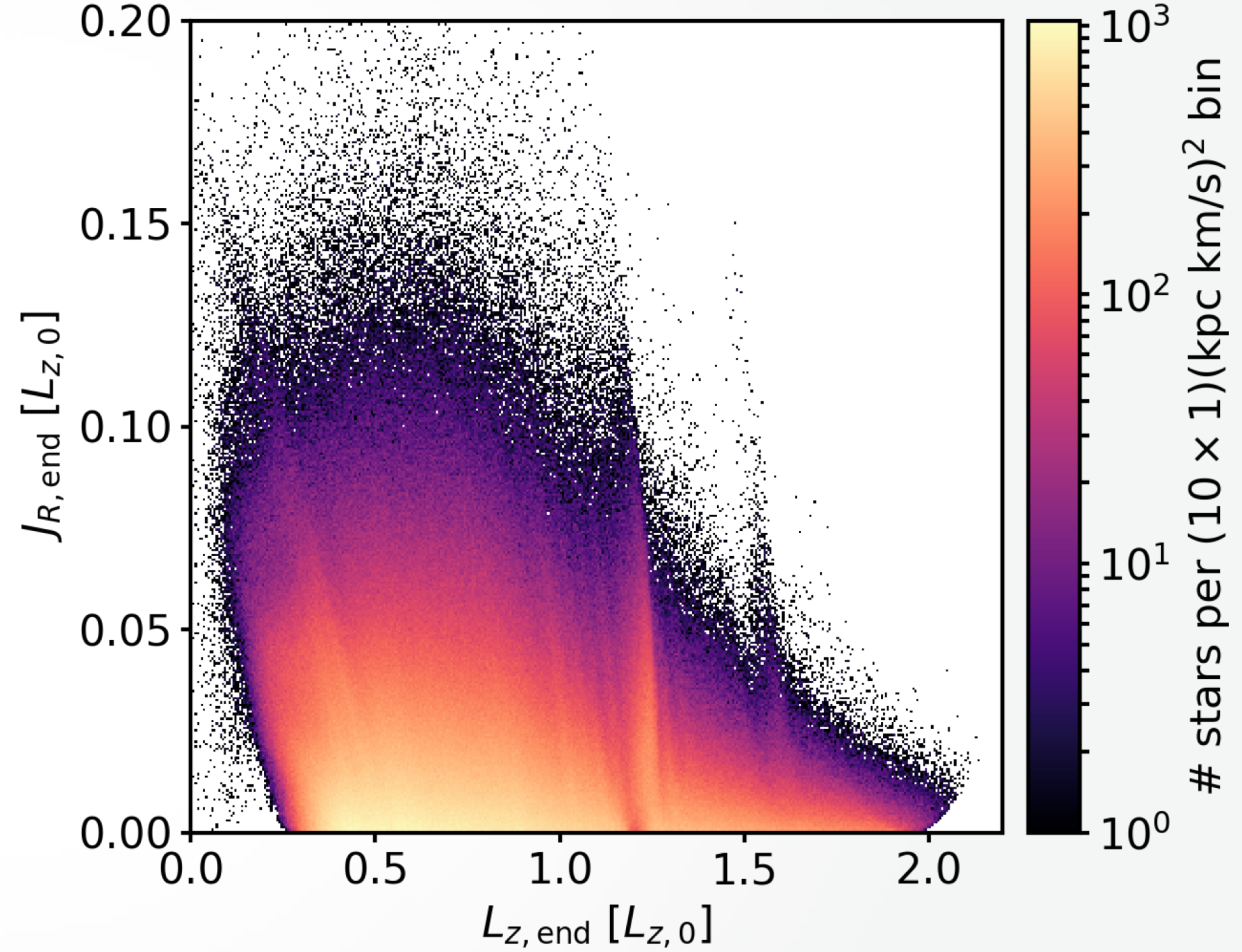
quasi-isothermal distribution function (Binney & McMillan 2011)

# INTEGRATE MOCK STARS IN BAR POTENTIAL

$t = 10$  bar periods = 1.8 Gyr



“axisym.” actions

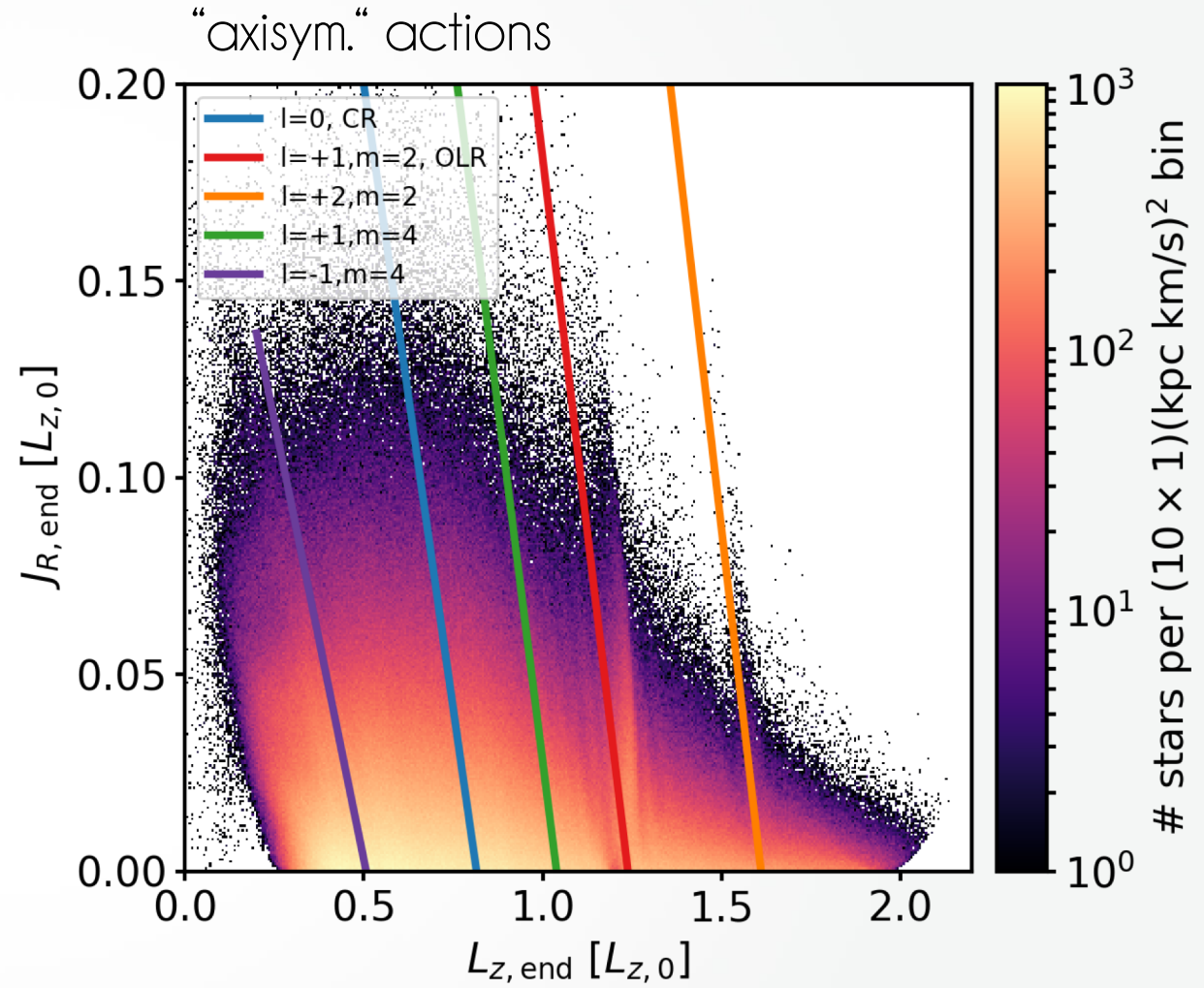
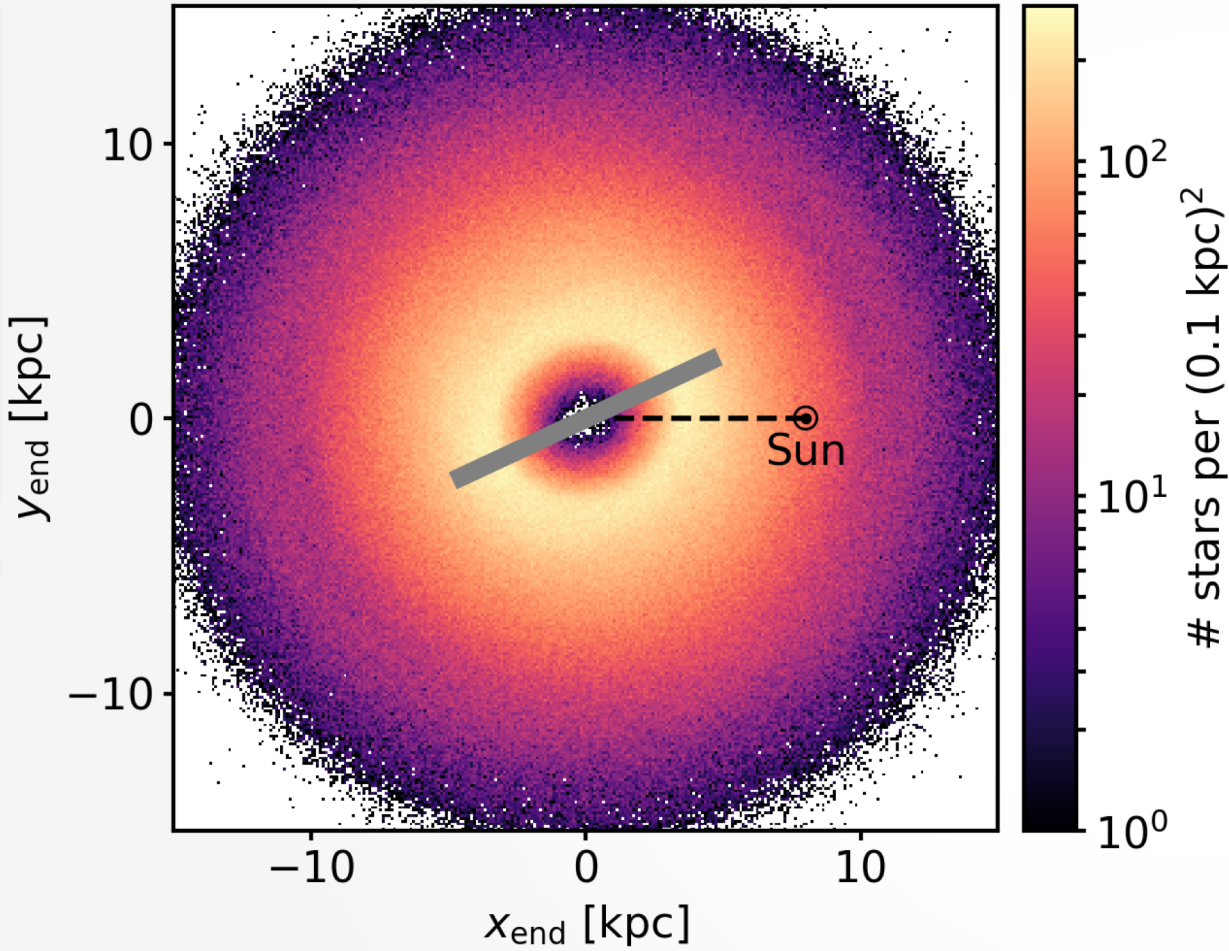


MW pot + „Dehnen“ bar,  
pattern speed:  $\Omega_p = 35 \text{ km/s/kpc}$



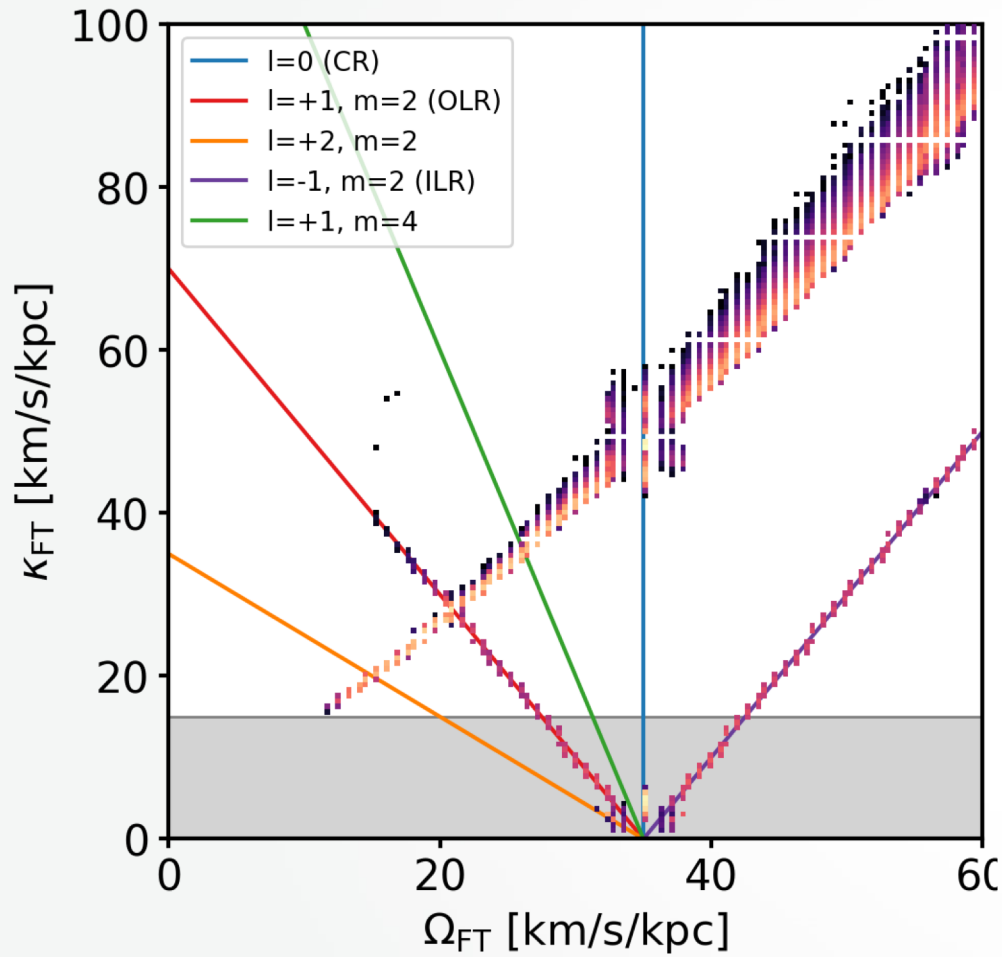
# RESONANCE LINES BASED ON AXISYM. FREQUENCIES

$t = 10$  bar periods = 1.8 Gyr

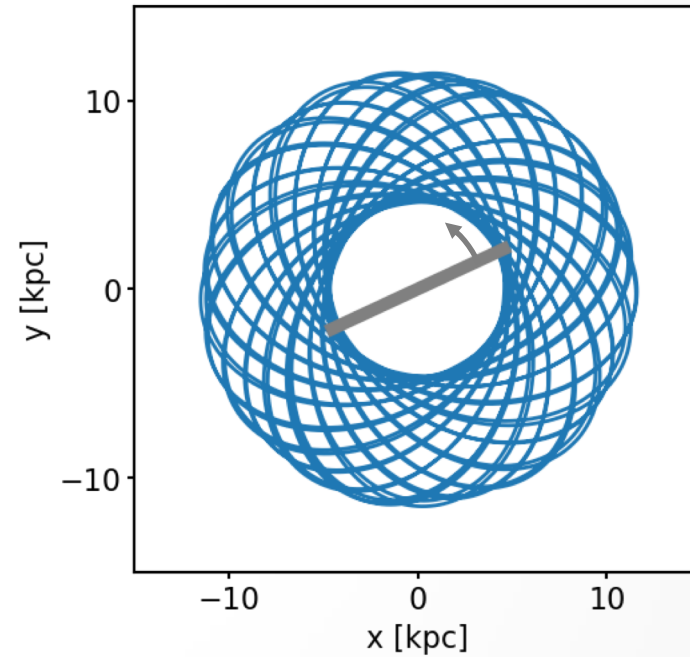


Resonance condition:  $m \cdot (\Omega_p - \Omega_\phi) - l \cdot \Omega_R = 0$   
 pattern speed:  $\Omega_p = 35 \text{ km/s/kpc}$

# SELECTING STARS IN RESONANCE WITH THE BAR



$$m \cdot (\Omega_p - \Omega_{FT}) - l \cdot \kappa_{FT} \sim 0$$



Fourier transform spatial coord. to get „real“ fundamental frequencies:

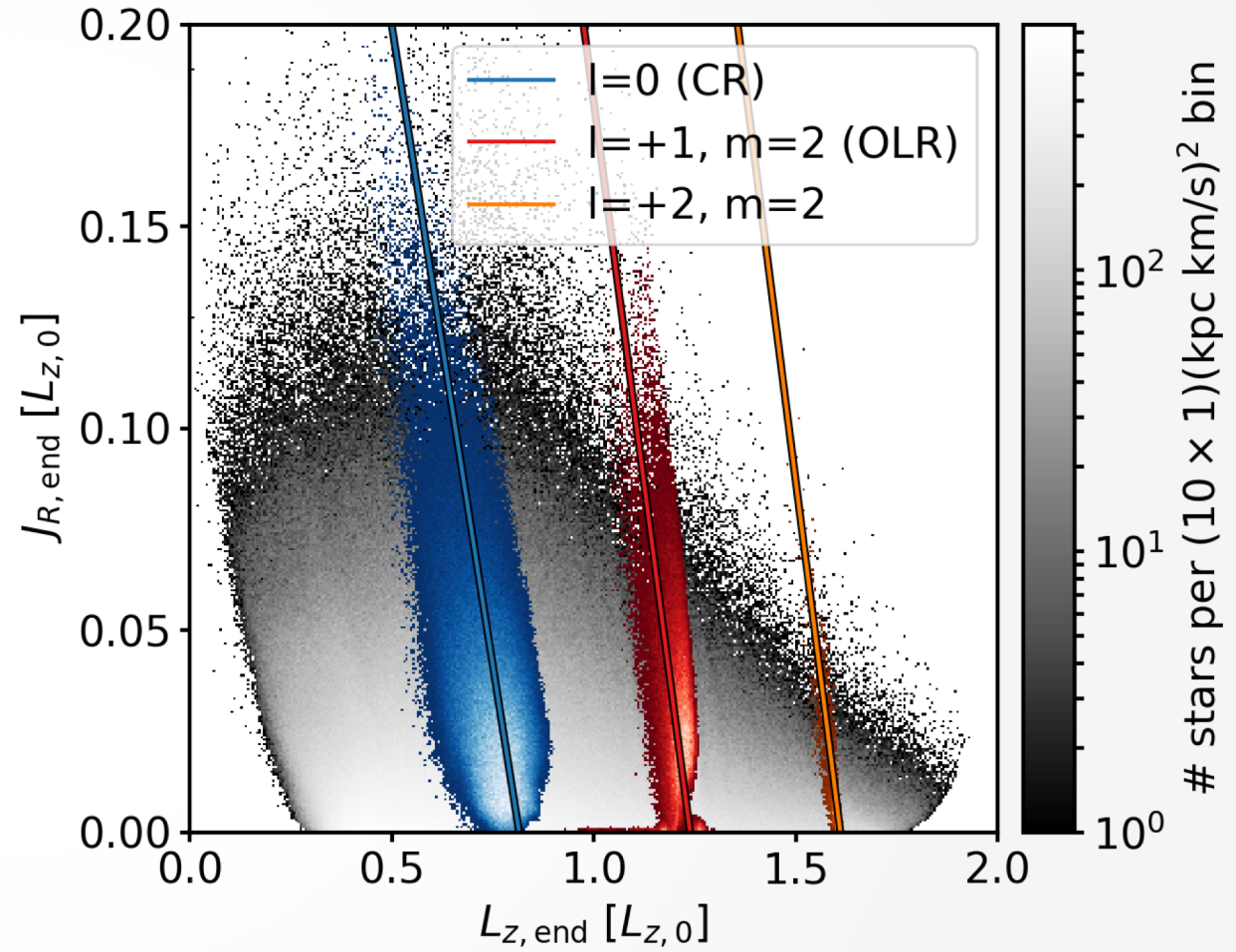
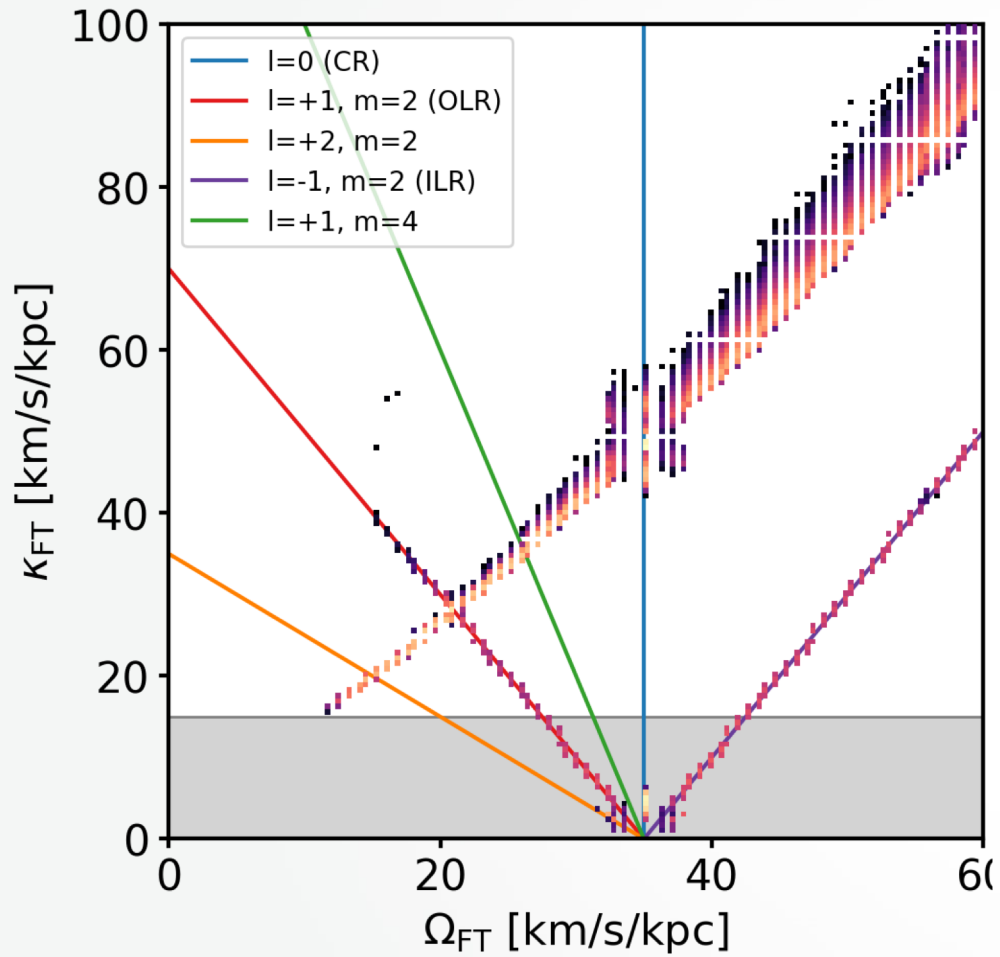
$R(t)$   
 → epicycle  $\kappa_{FT}$

$\cos(\phi)(t)$   
 → circular  $\Omega_{FT}$

see also Fragkoudi et al (2019)

# LOCATION OF „TRULY” RESONANT STARS

... versus the axisymmetric resonance lines



$$m \cdot (\Omega_p - \Omega_{FT}) - l \cdot \kappa_{FT} \sim 0$$



# EFFECT OF RESONANCES ON "AXISYMMETRIC ACTIONS"

„Scattering“ (i.e. lasting changes)  
in axisym. action space

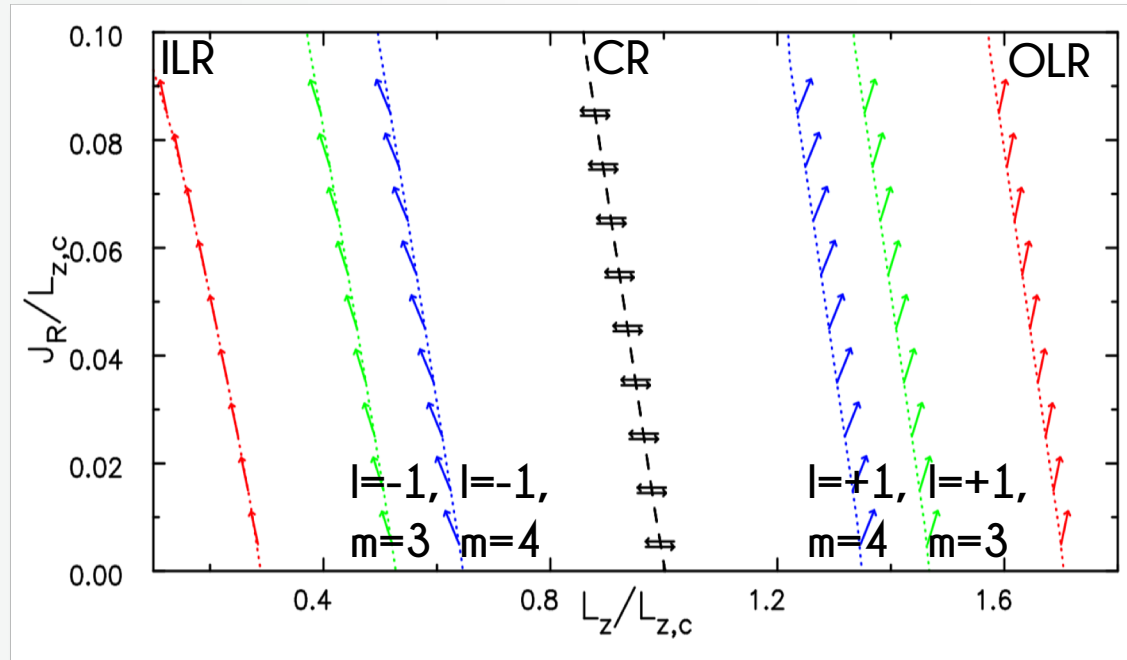
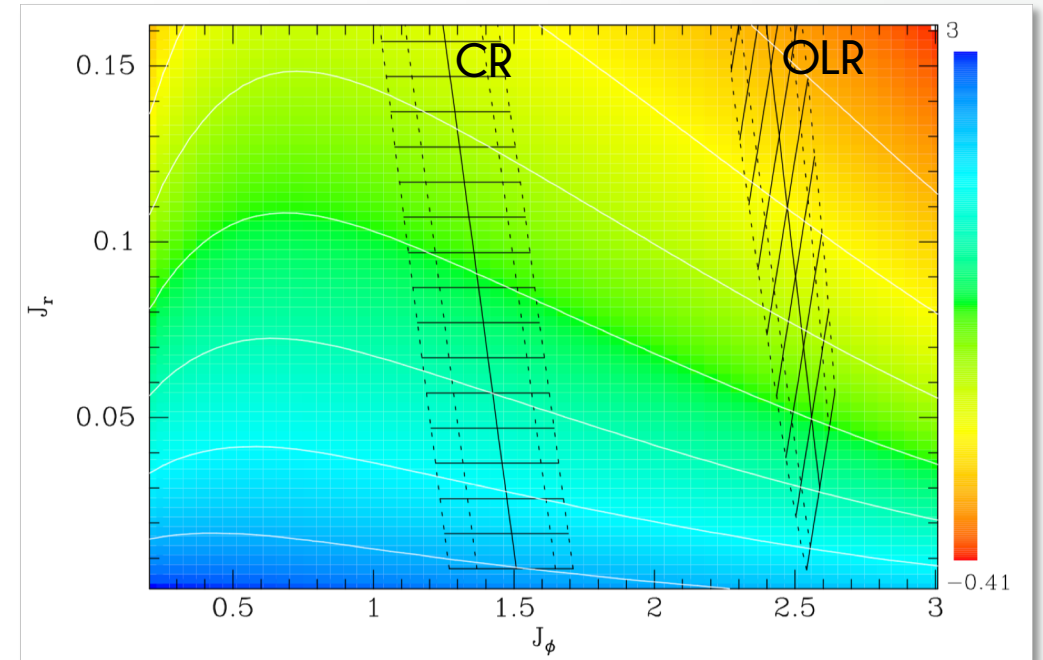


figure taken from Sellwood, Trick et al. (2019),  
see also Sellwood & Binney (2002), Lynden-Bell & Kalnajs (1972)

from conservation of Jacobi energy:

$$E_J = E - \Omega_p \times L_z = \text{const.} \rightarrow \Delta J_R = l/m \Delta L_z$$

„Oscillation“ around resonance lines  
in axisym. action space



Binney (2018)

from perturbing axisymmetric orbital tori  
(actions & angles) in a bar potential

# LOCATION OF SOLAR VOLUME WITH RESPECT TO THE BAR

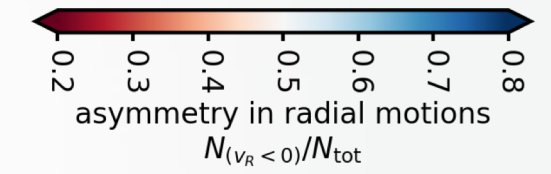
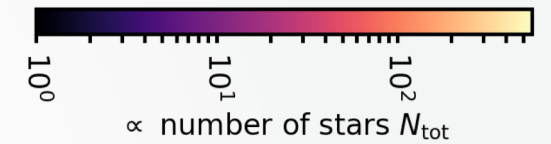
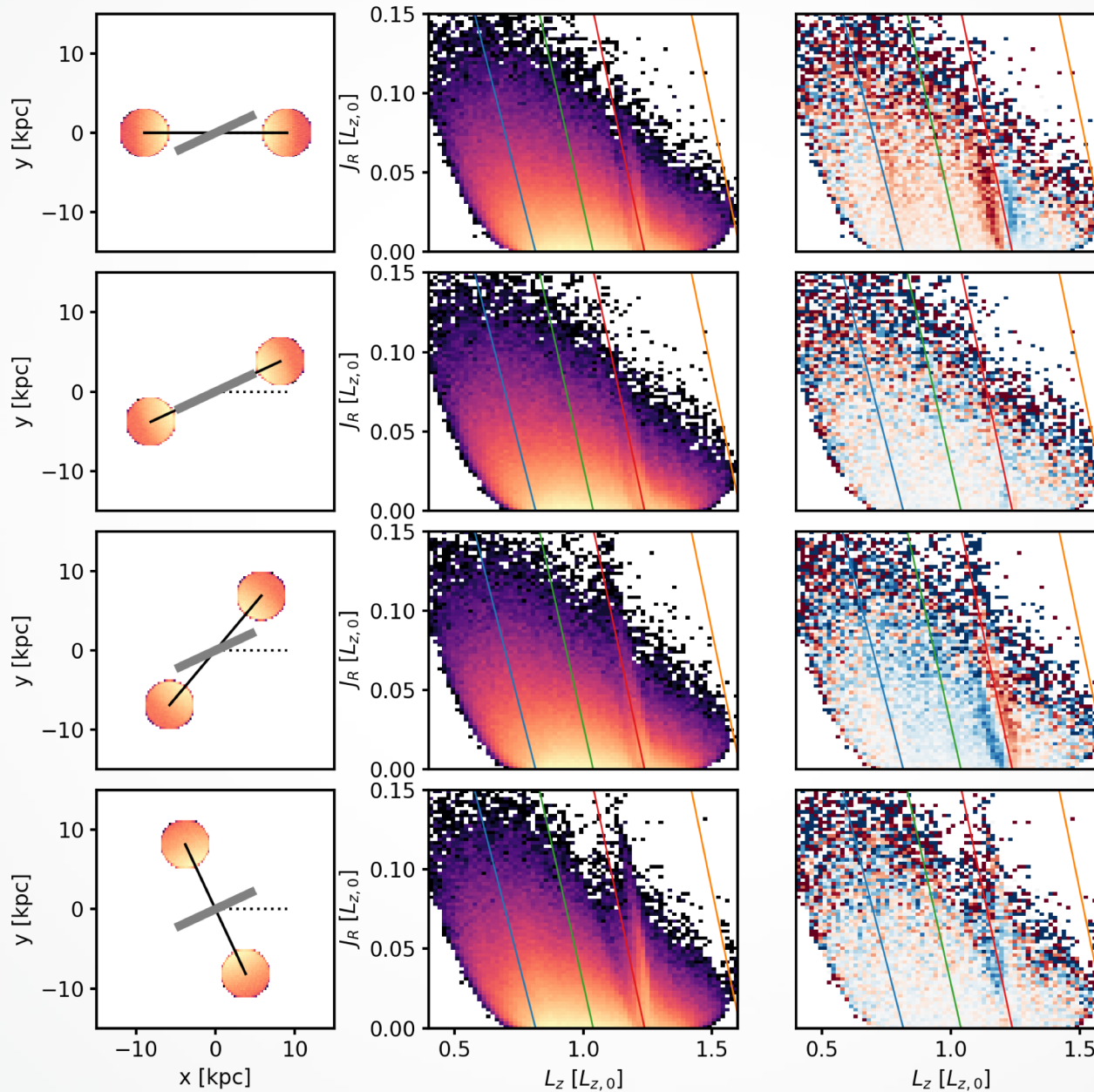
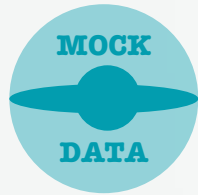
Orbit integration

time:

10 bar periods

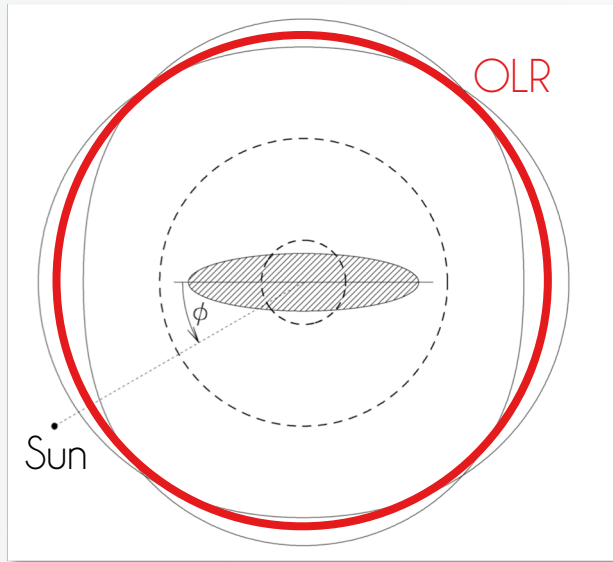
= 1.8 Gyr

Bar resonances & axisym. Actions



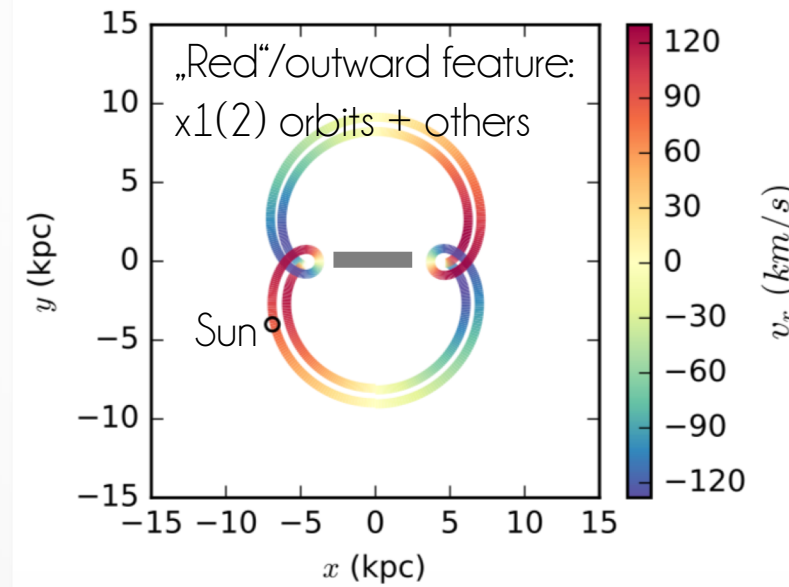
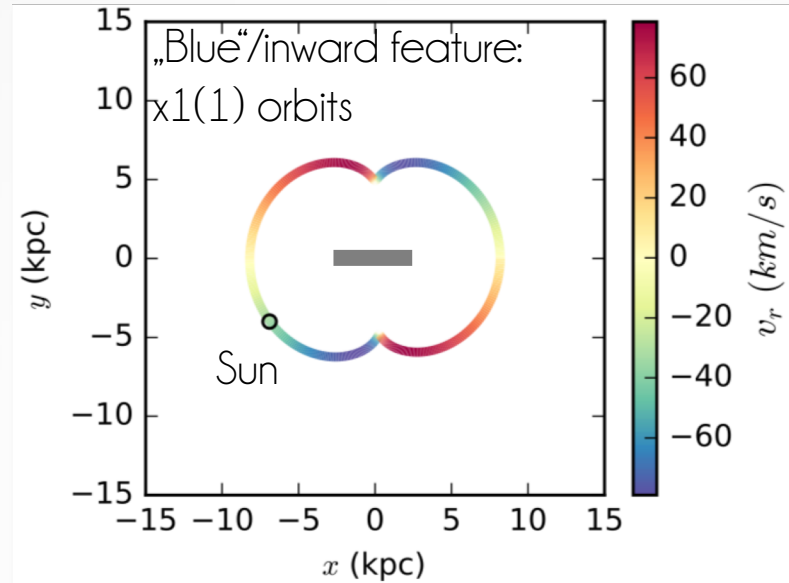
- CR
- OLR
- $l=+2, m=2$
- $l=+1, m=4$

# THE OUTWARD-INWARD (RED-BLUE) SIGNATURE OF THE OLR

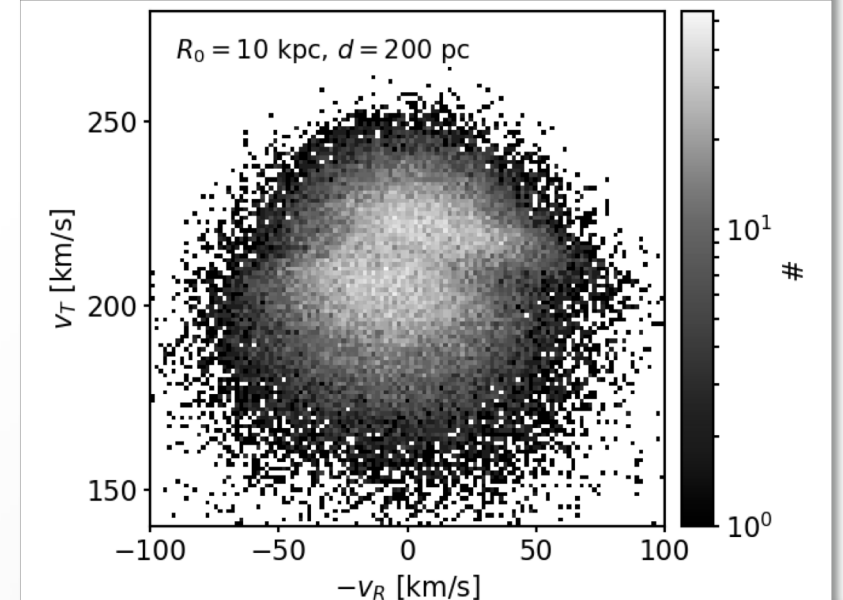
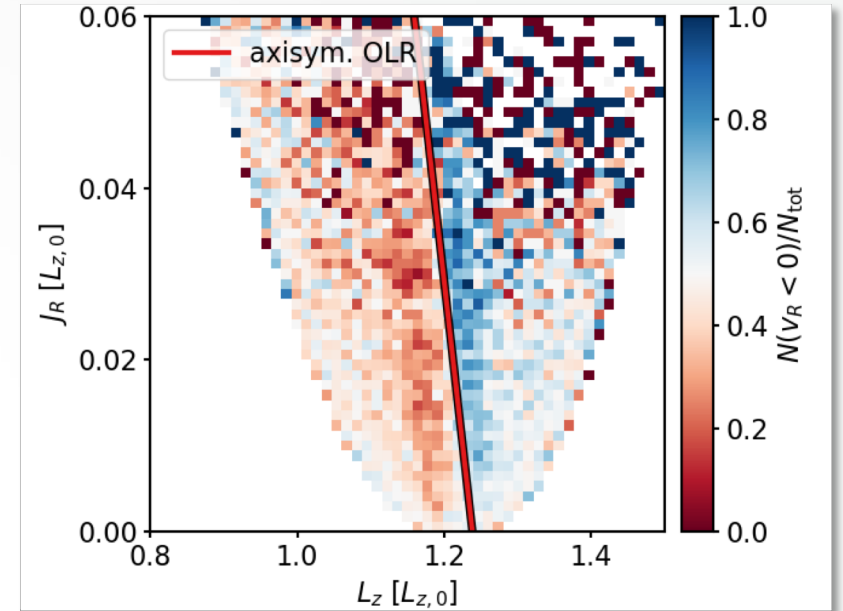


Dehnen (2000)

Orbits flip their orientation at the axisym. OLR line.



Fragkoudi,...,Trick,... et al. (2019)

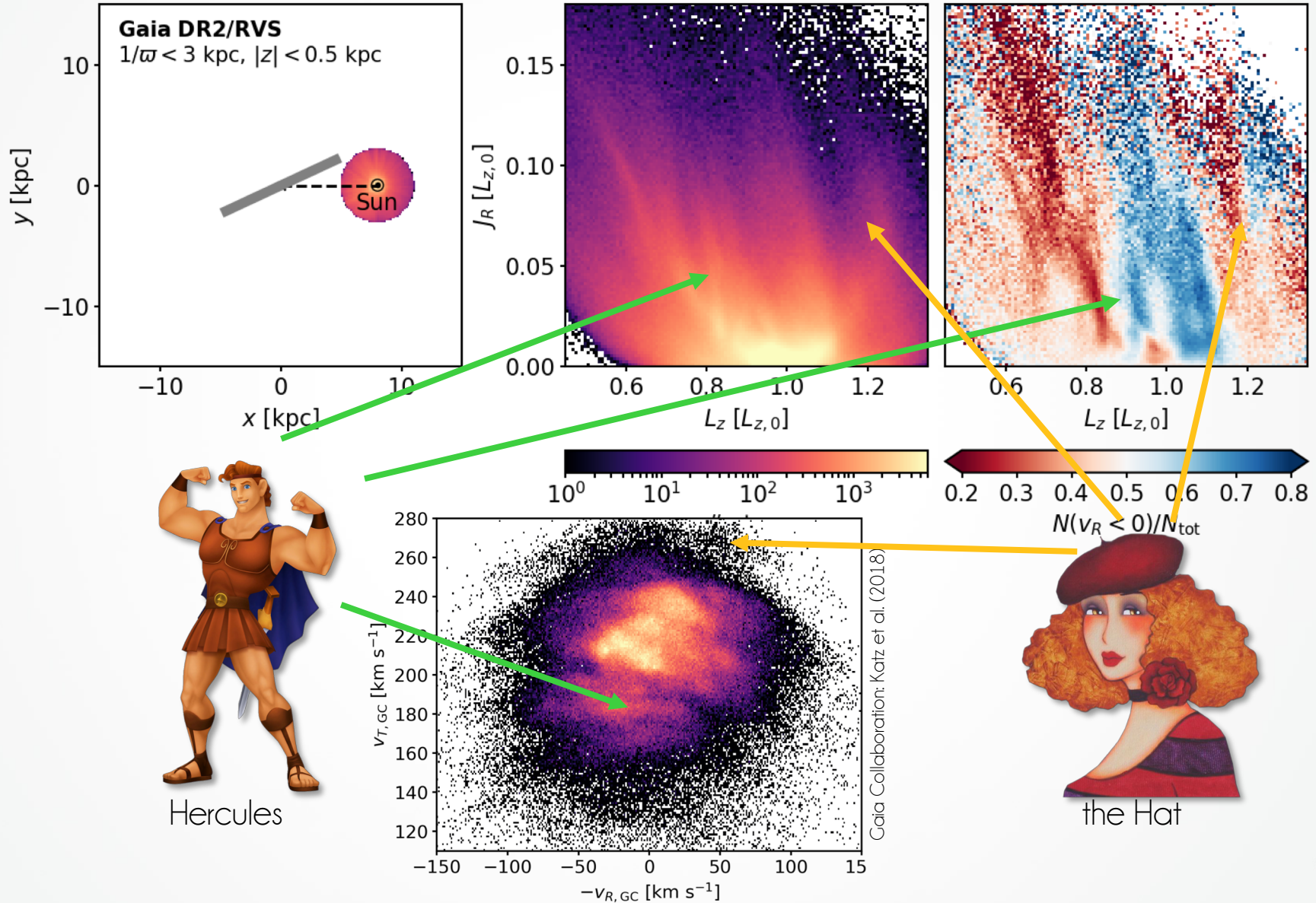
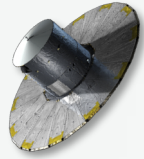


Trick et al. (in prep.)



# COMPARING GAIA DR2 TO THE MODEL

Bar resonances & axisym. Actions



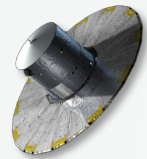
Hercules



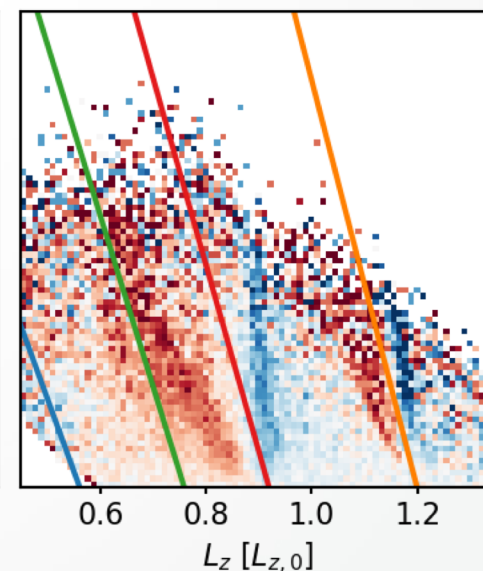
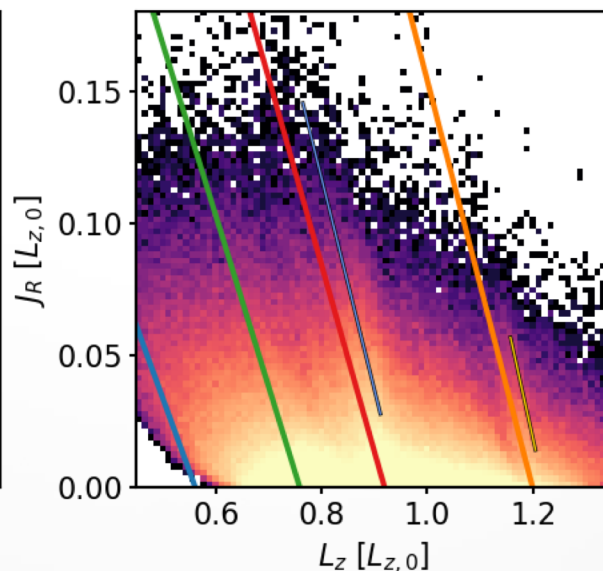
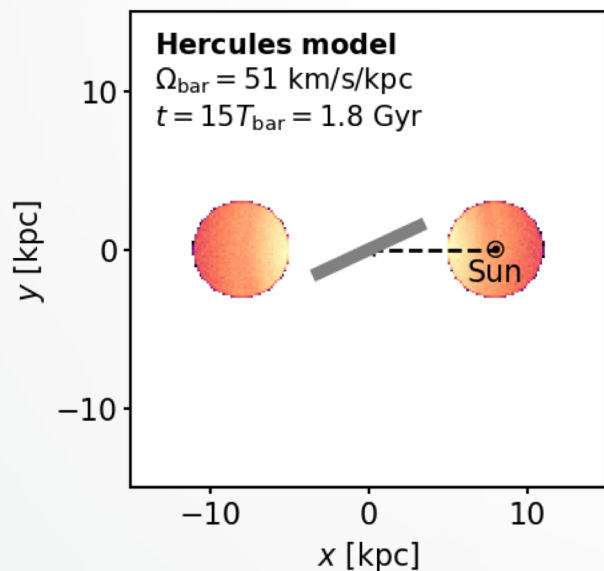
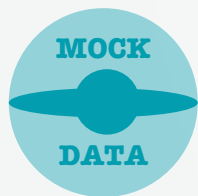
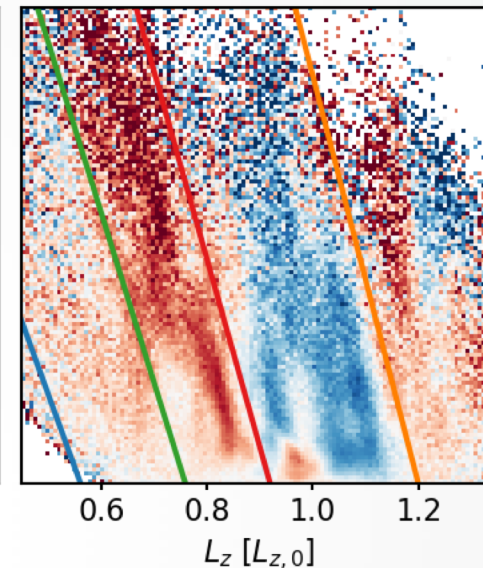
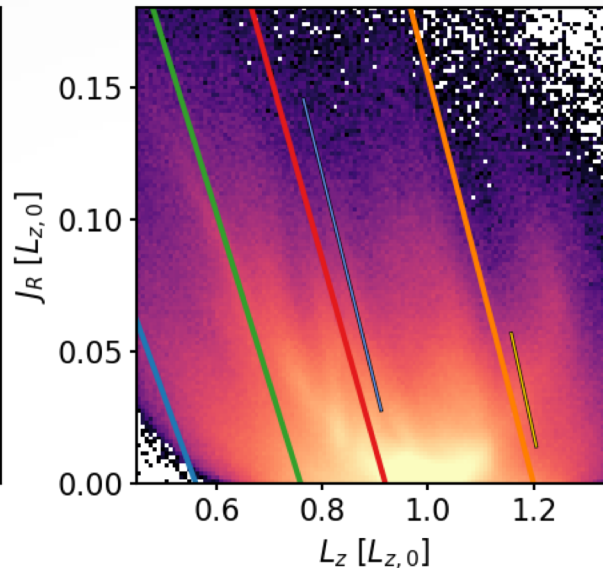
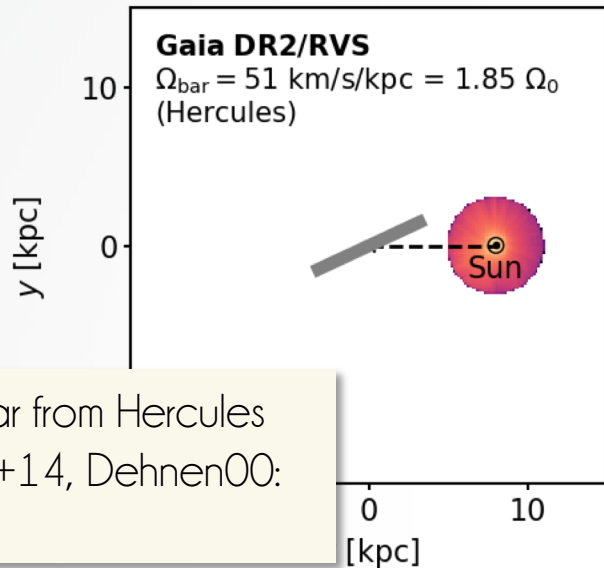
the Hat

# ASSUMING BAR OLR IS NEAR HERCULES

Bar resonances & axisym. Actions



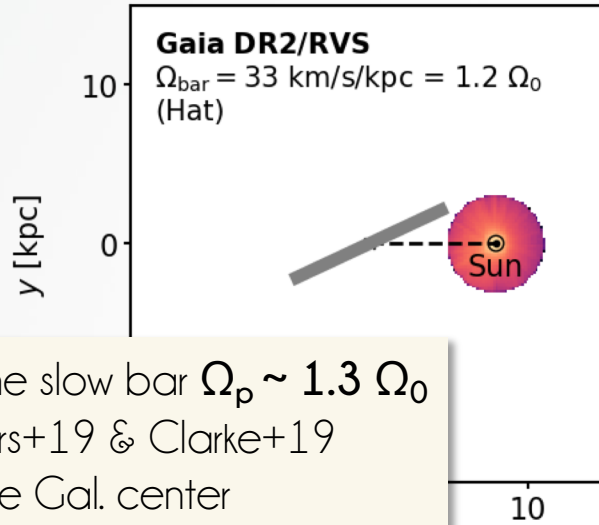
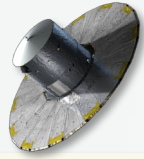
very close to fast bar from Hercules modeling by Antoja+14, Dehnen00:  
 $\Omega_p \sim 1.8 \Omega_0$



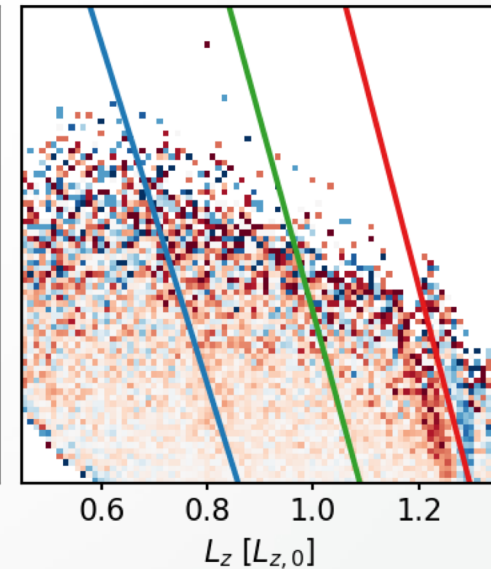
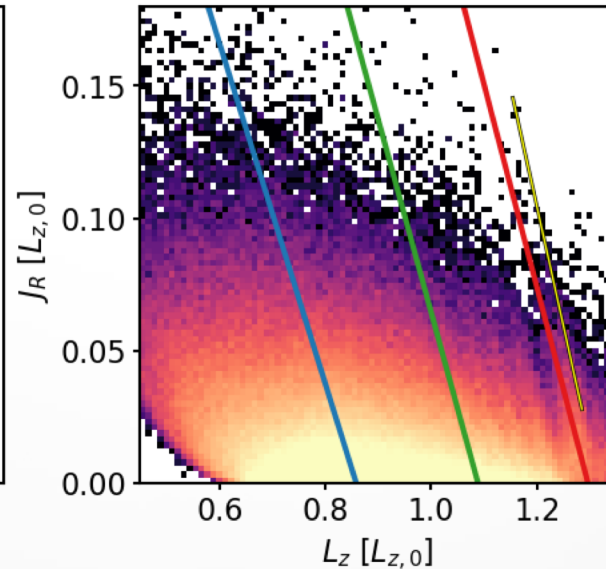
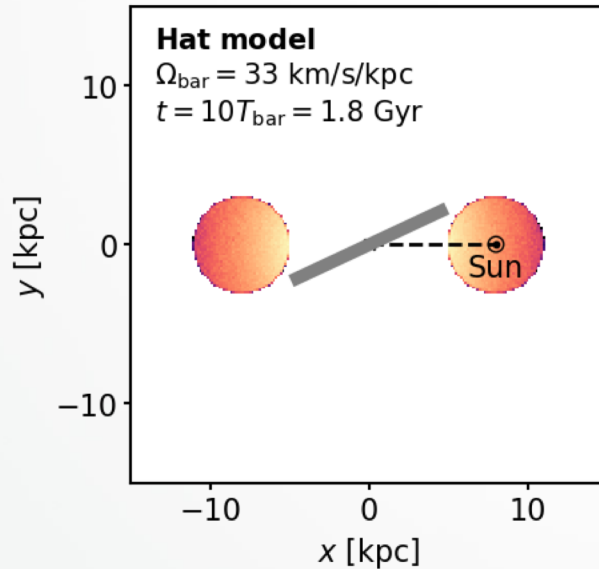
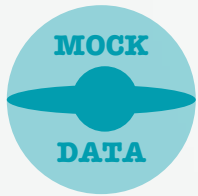
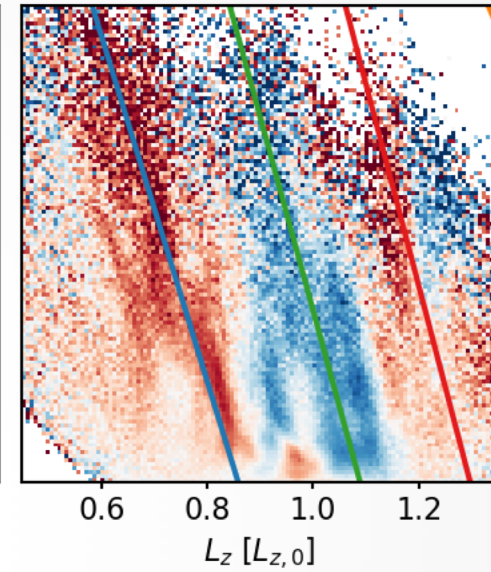
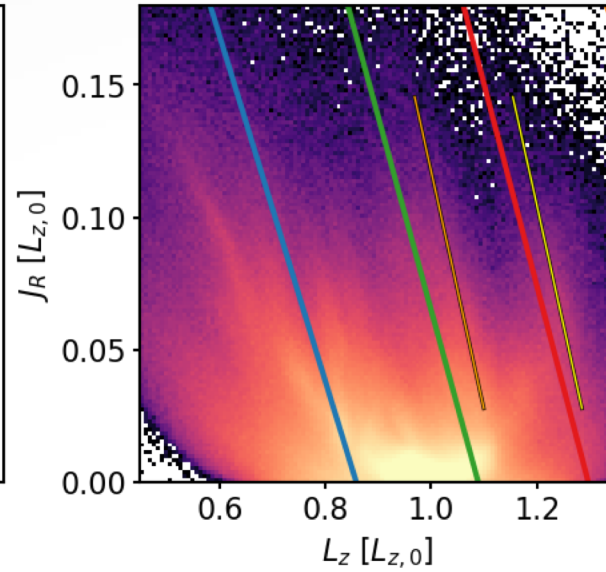
- CR
- OLR
- $l=+2, m=2$
- $l=+1, m=4$

# ASSUMING BAR OLR IS NEAR THE HAT

Bar resonances & axisym. Actions



slightly lower than the slow bar  $\Omega_p \sim 1.3 \Omega_0$   
 as found by Sanders+19 & Clarke+19  
 from kinematics in the Gal. center  
 (similar labeling of action space in Monari+18)



- CR
- OLR
- $l=+2, m=2$
- $l=+1, m=4$





PART 4:  
CONSTRAINTS FROM THE „AXISYM.  
ANGLES“ ON THE GALACTIC BAR

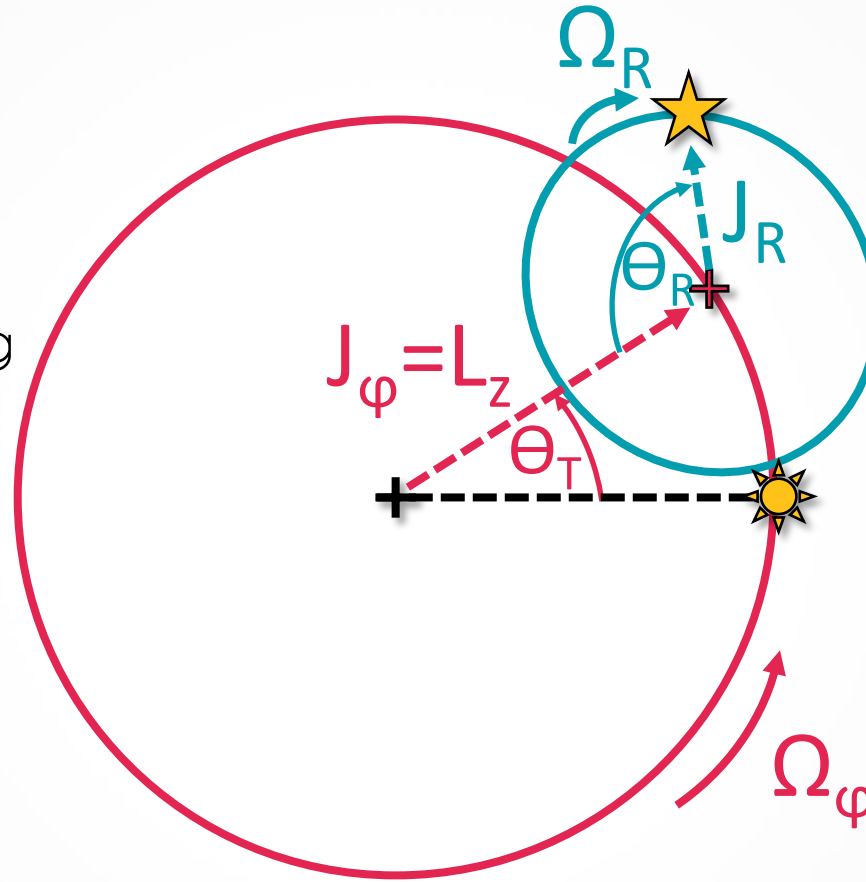


Work in progress...



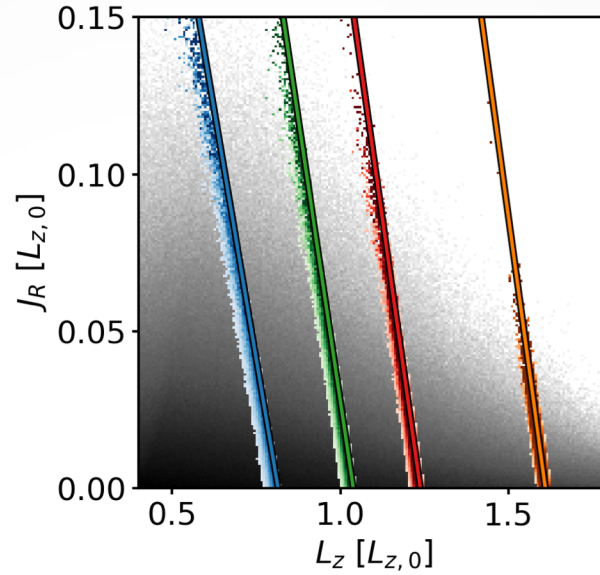
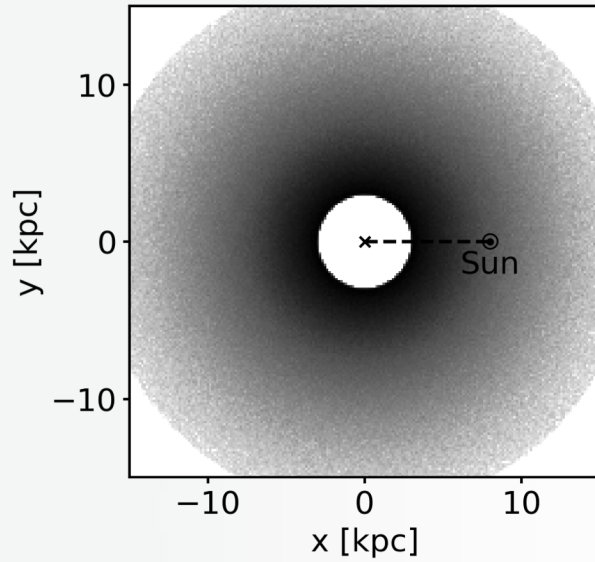
# ANGLE COORDINATES (EXPLAINED WITH EPICYCLES)

- $\theta_R = 0:$  pericenter
- $\theta_R > 0:$  outward moving
- $\theta_R = \pm\pi:$  apocenter
- $\theta_R < 0:$  inward moving



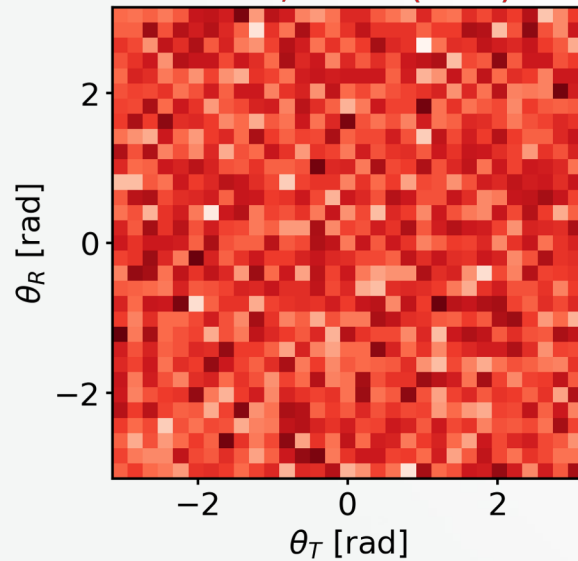
$\theta_T = 0:$  azimuth of the Sun

# ANGLE SPACE OF AXISYMMETRIC MOCK DATA

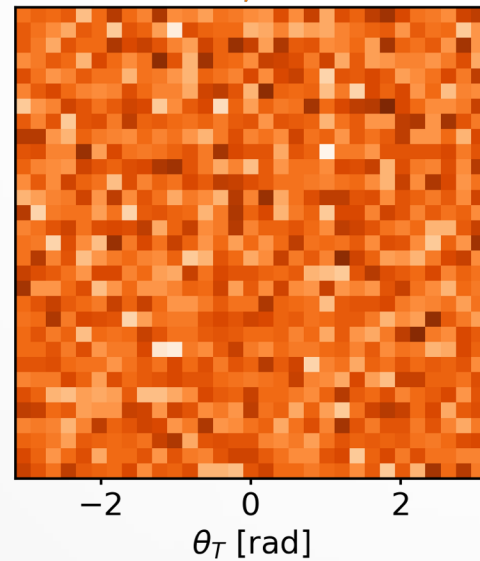


- Time: **before the bar**
- Stars: **along resonance lines**

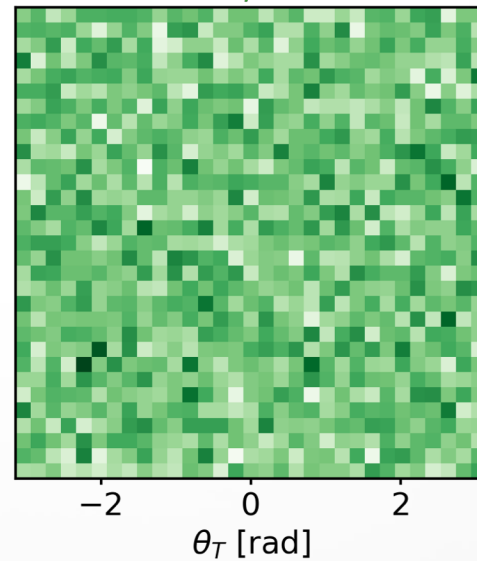
$l=+1, m=2$  (OLR)



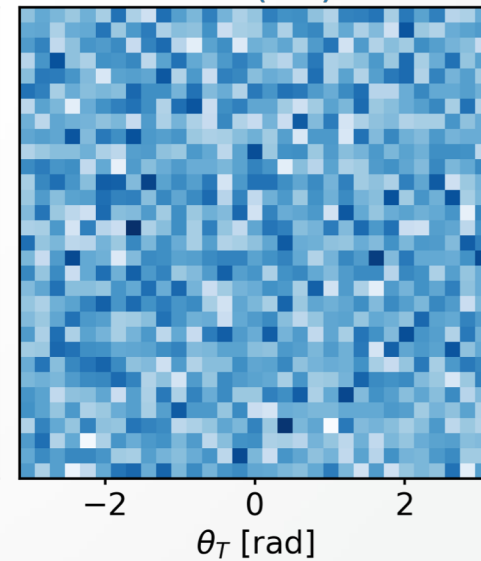
$l=+2, m=2$



$l=+1, m=4$



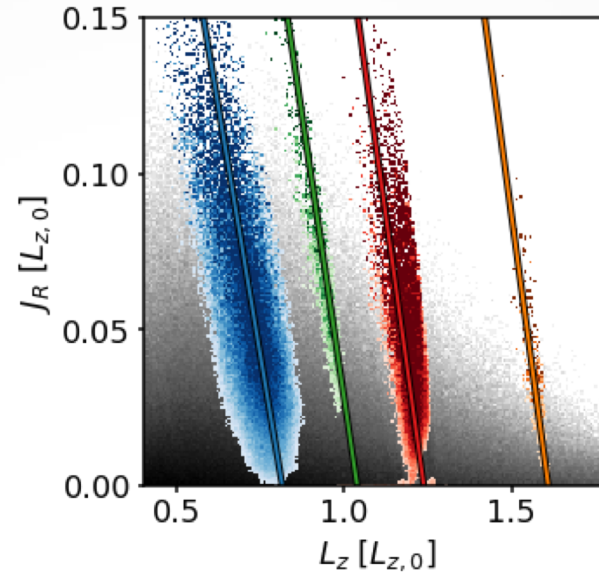
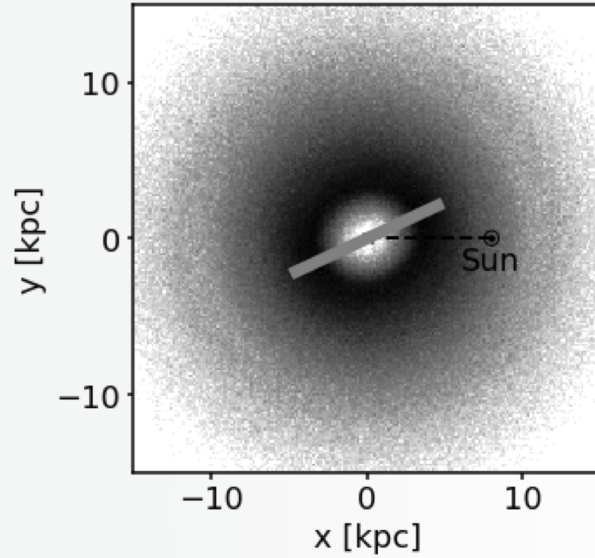
$l=0$  (CR)



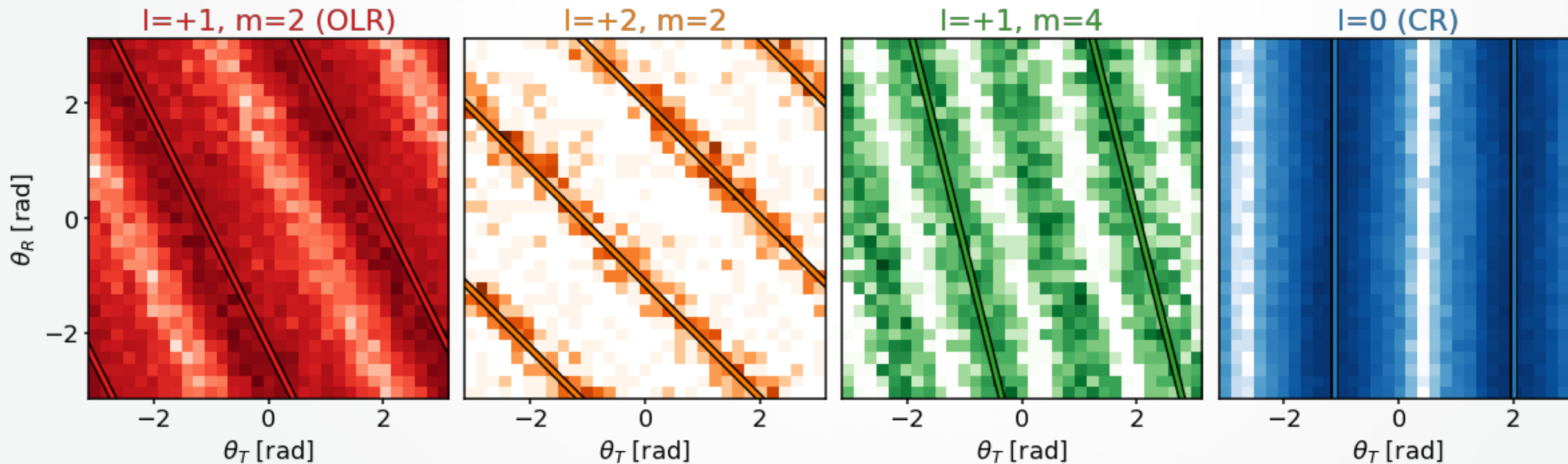


# ANGLE SPACE FOR STARS INTEGRATED IN BAR POTENTIAL

- Time: "today"
- Stars: "real" resonant stars

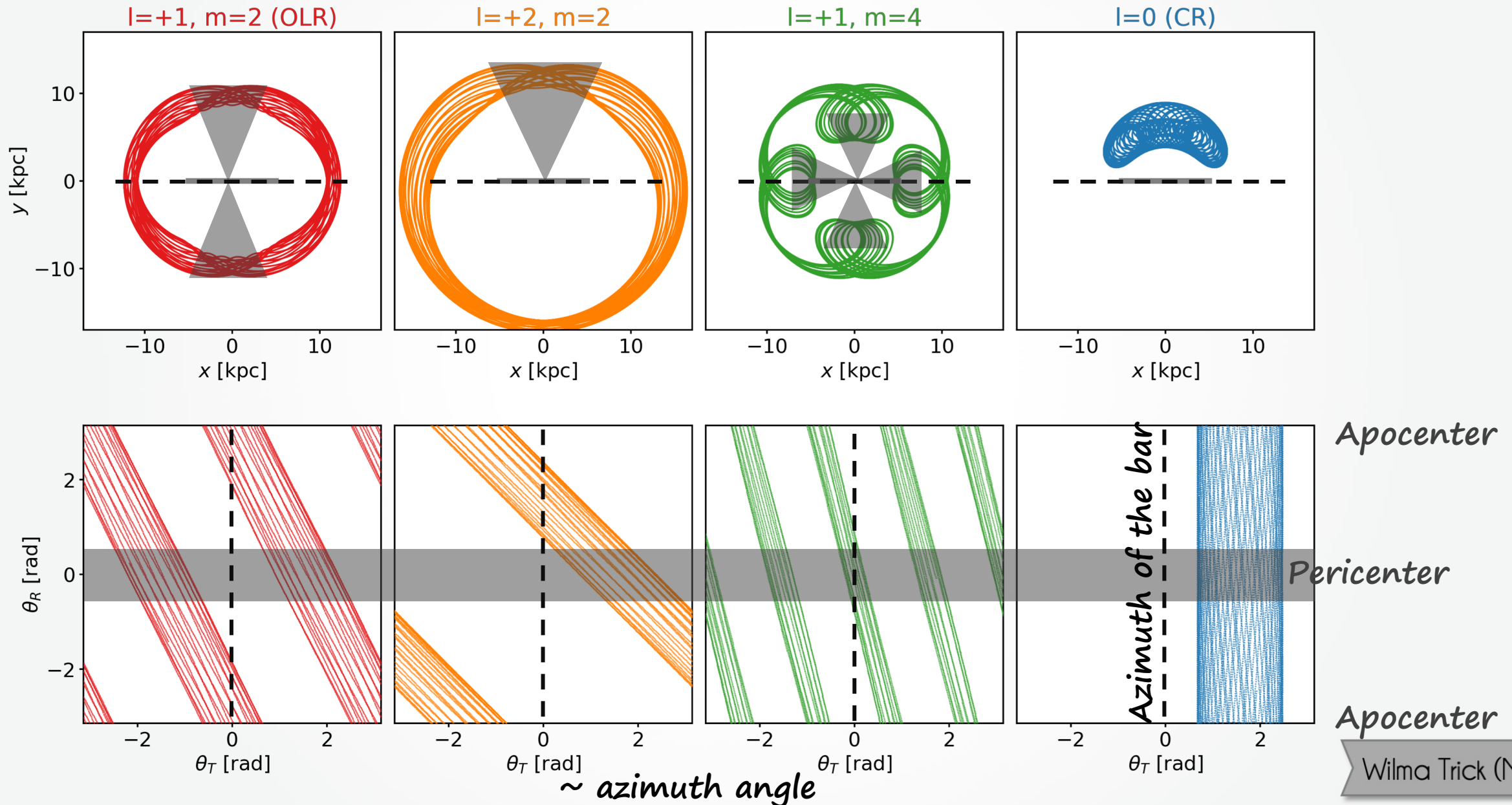


angle distribution follows predicted slope:  $-m/l$   
 --> use to decide which resonance?!

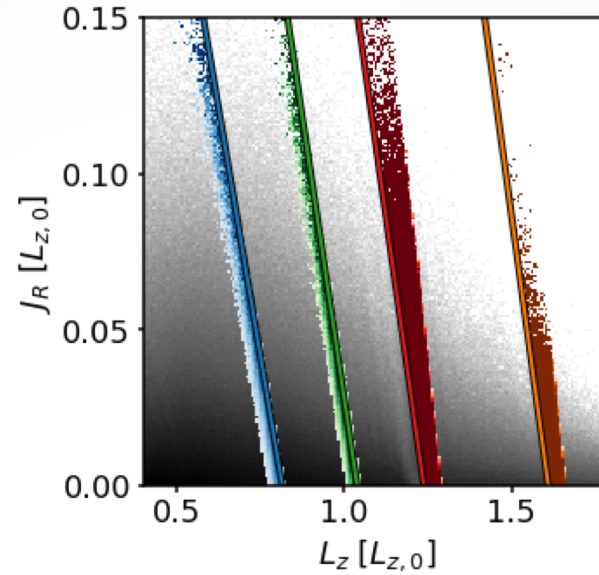
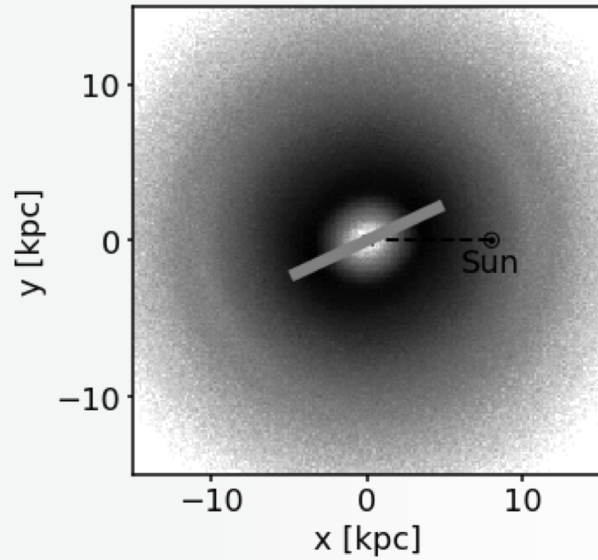


see also Sellwood (2010)

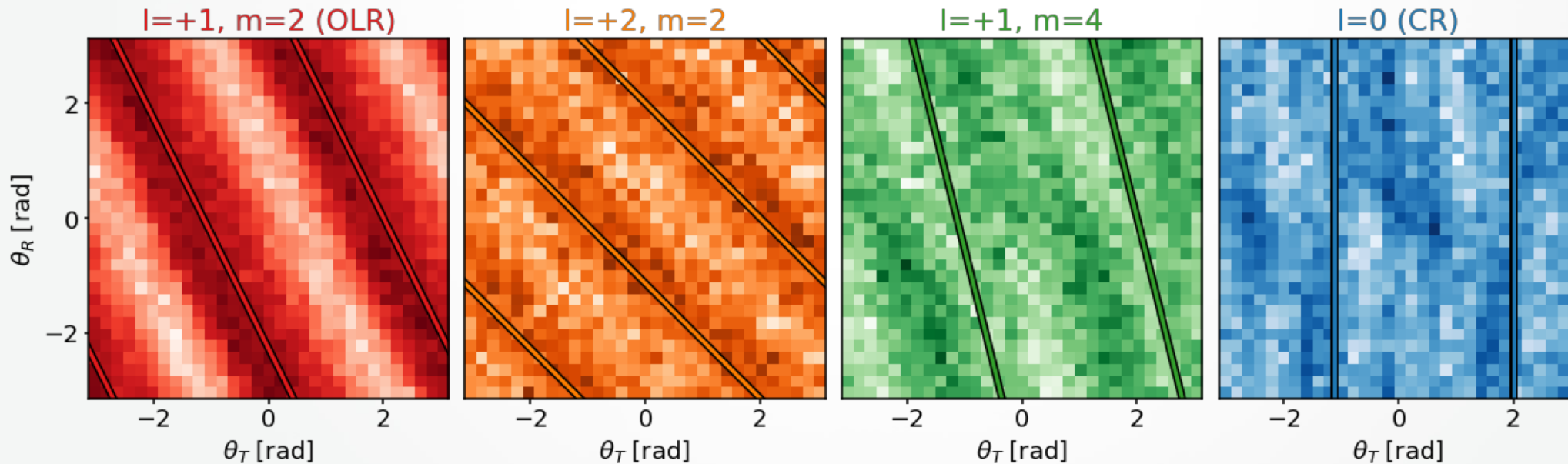
# RESONANT ORBITS IN ANGLE SPACE



# ANGLE SPACE FOR STARS SELECTED AT THE RESONANCES

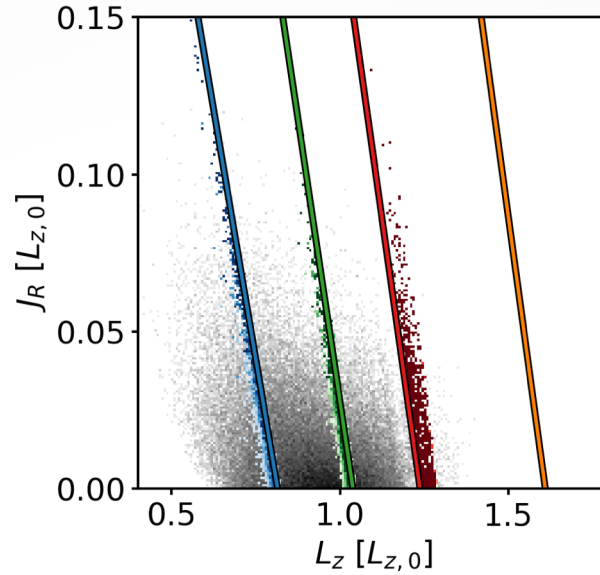
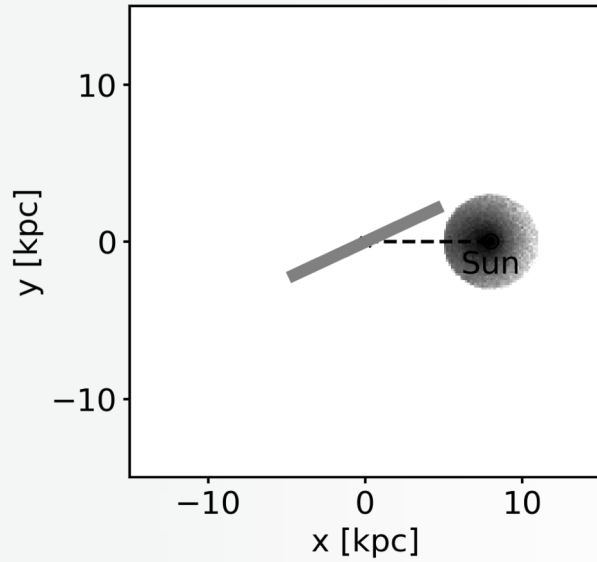


- Time: "today"
- Stars: selected by hand in action space → hoping to capture resonant stars

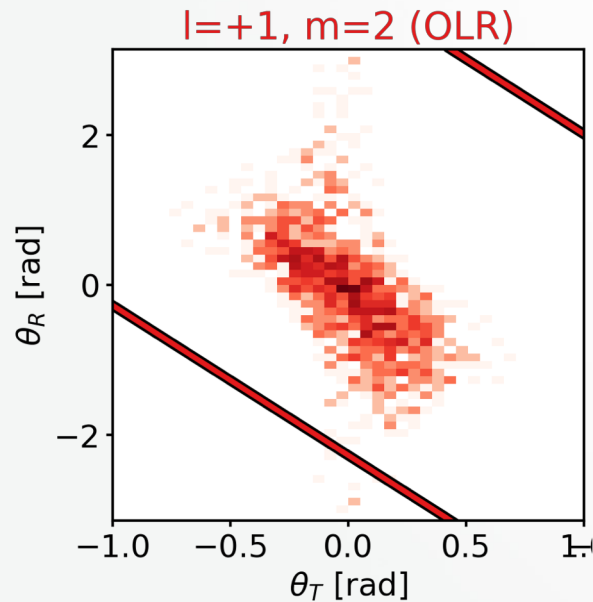




# ANGLE SPACE & SELECTION EFFECTS



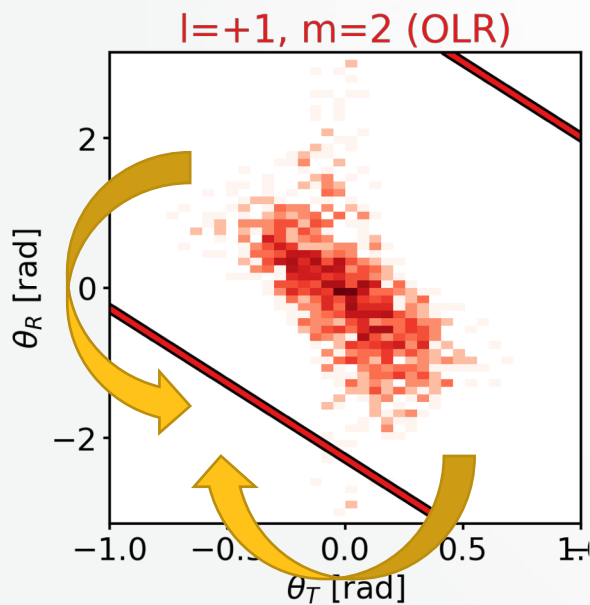
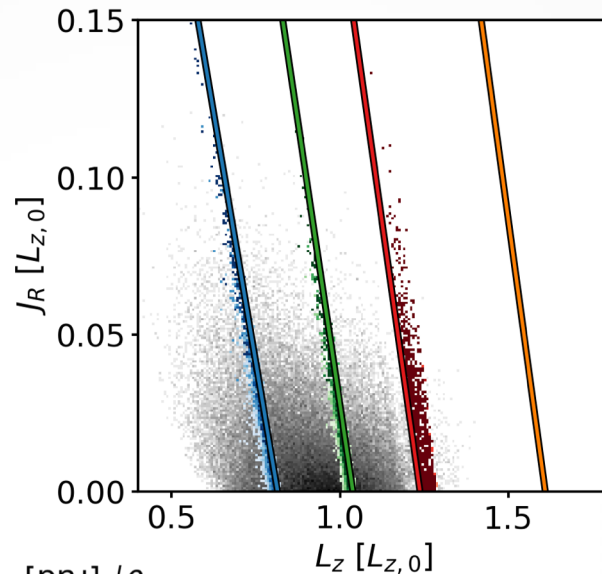
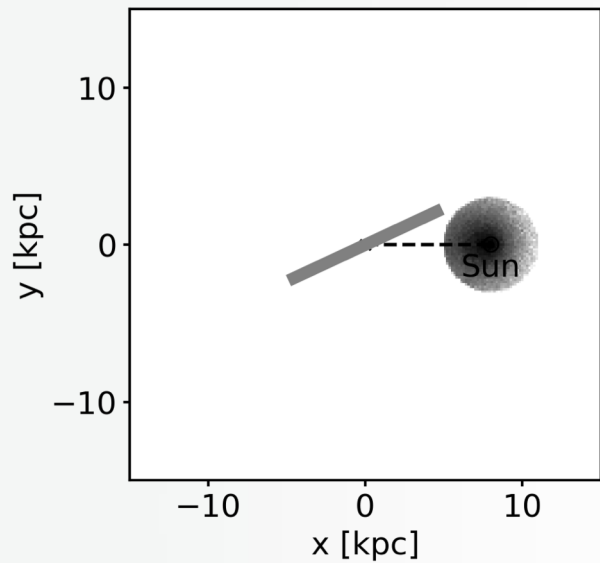
- Time: “today”
- Stars: **picked by hand in action space**
- Selection: **3 kpc sphere + exponential decrease of completeness with distance from Sun**



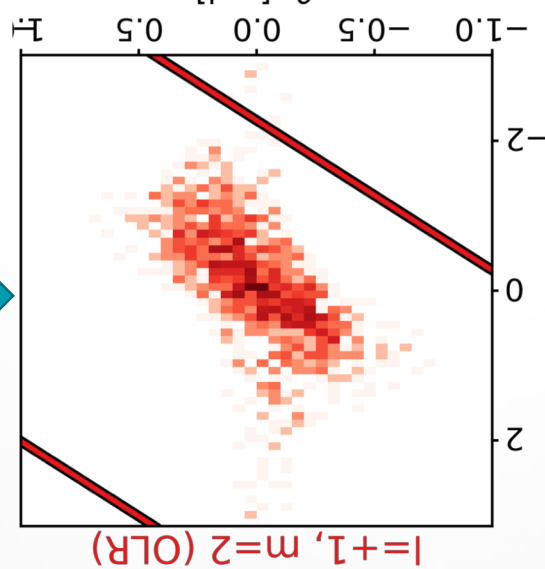
see also  
McMillan (2013)

# IDEA: HOW TO DEAL WITH THE SELECTION EFFECTS

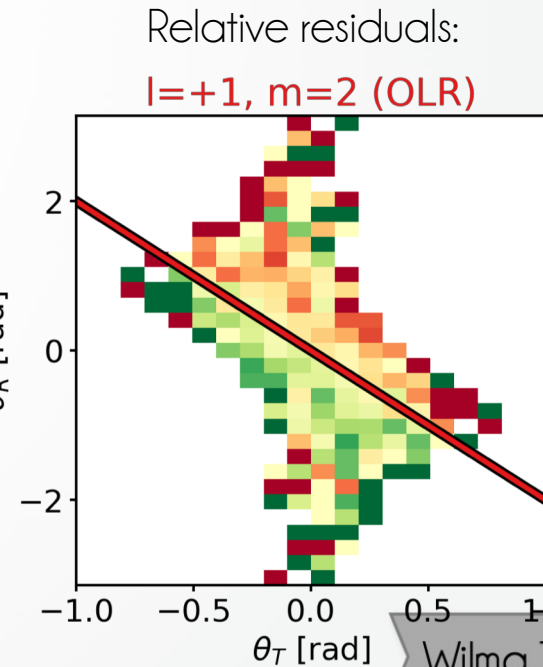
Bar resonances & axisym. Angles



mirror

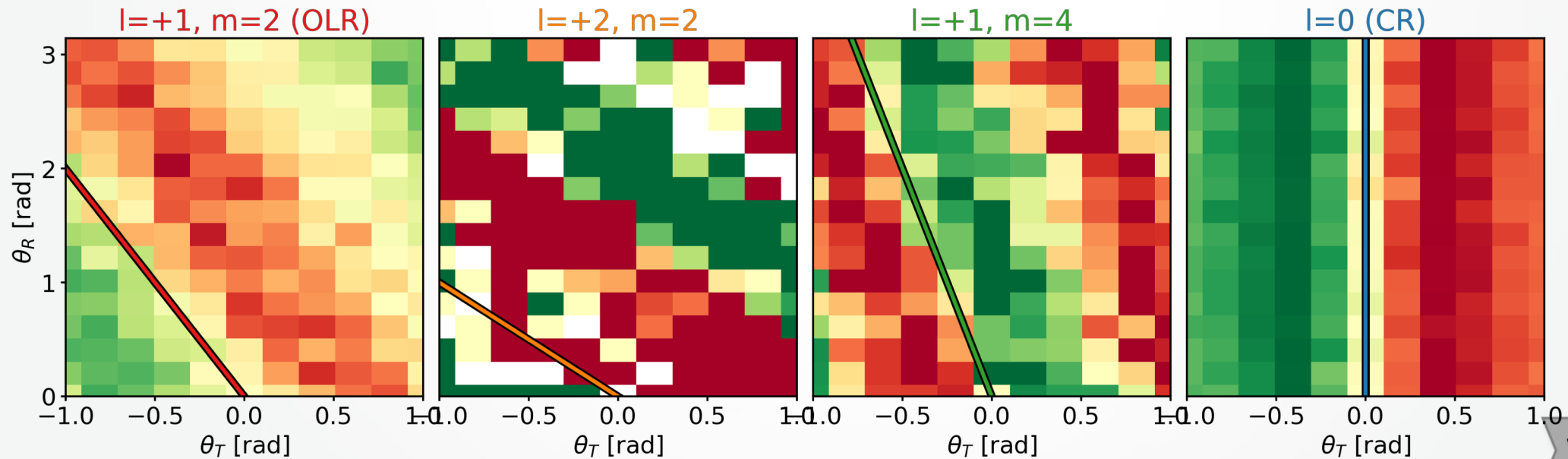
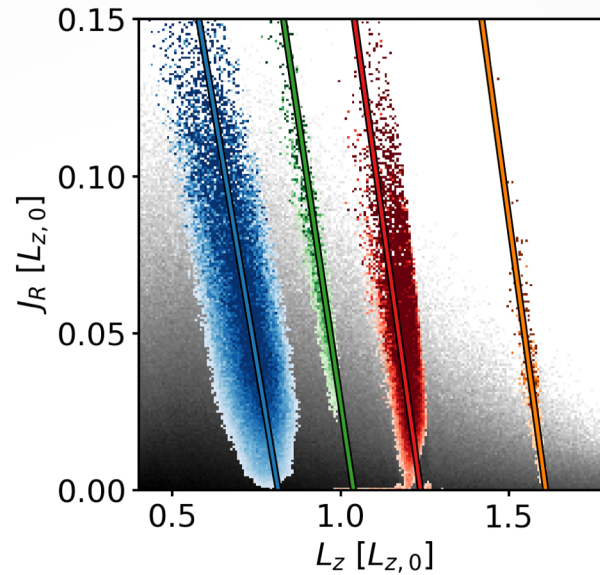
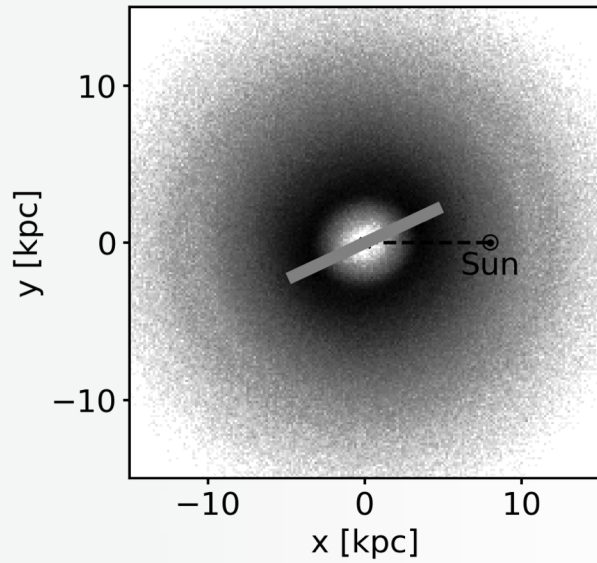


subtract



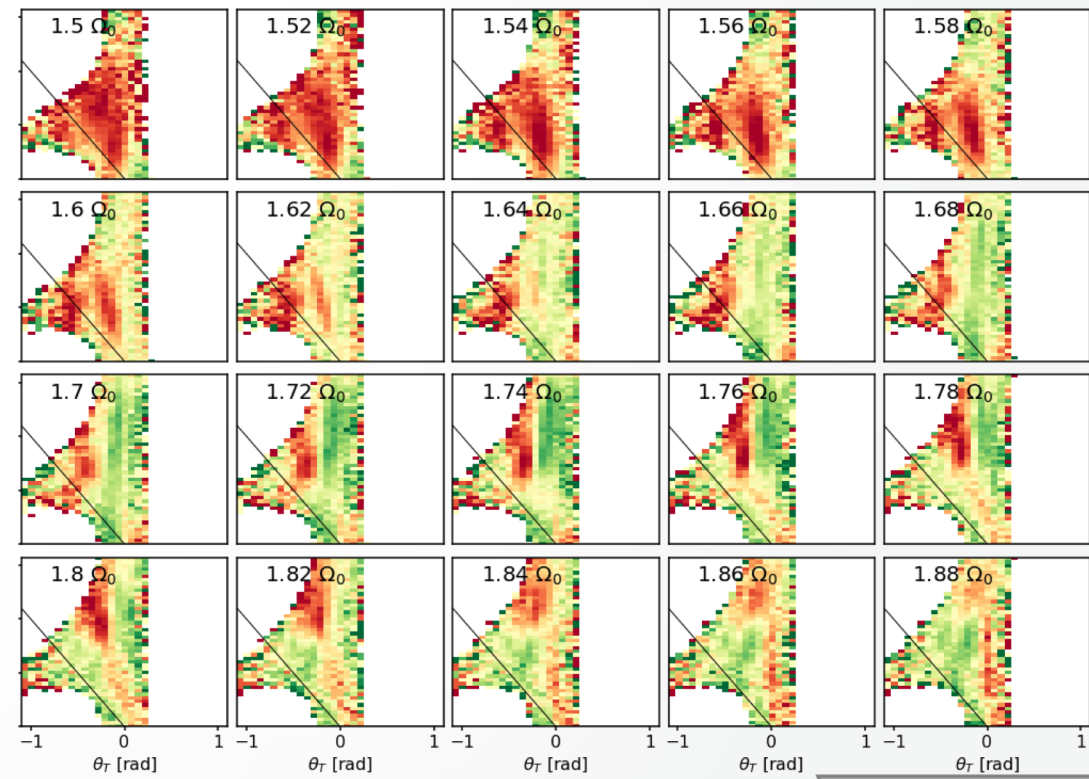
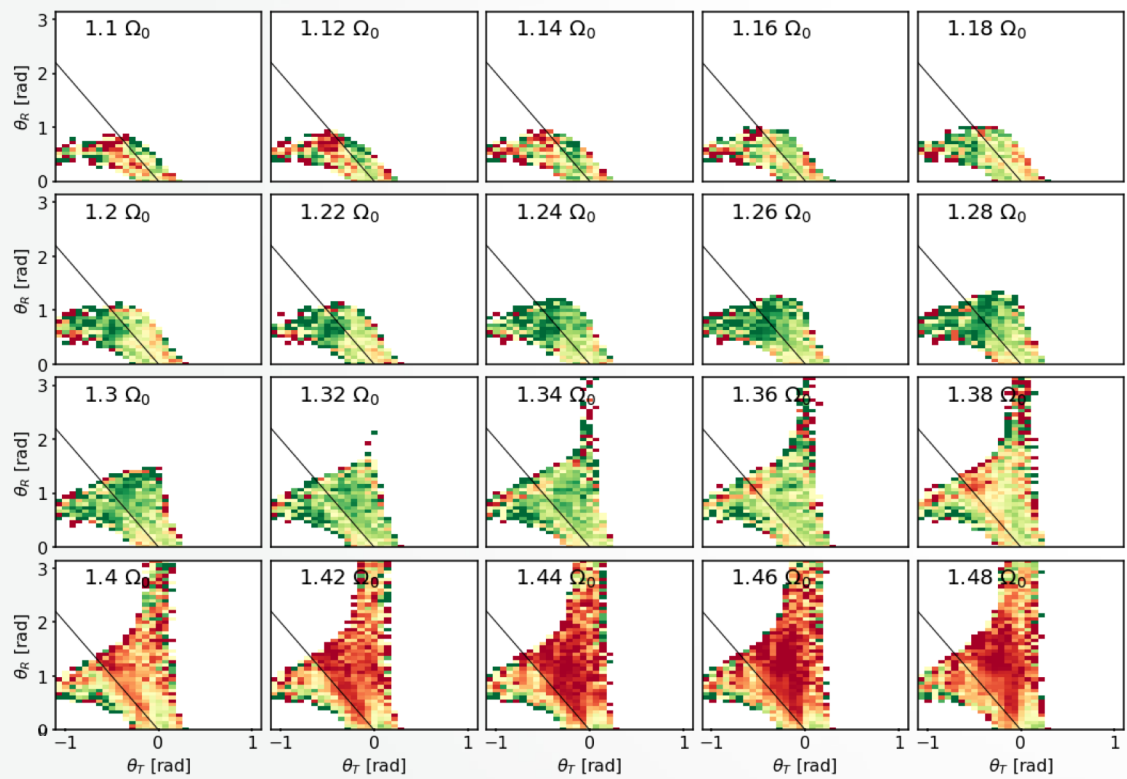
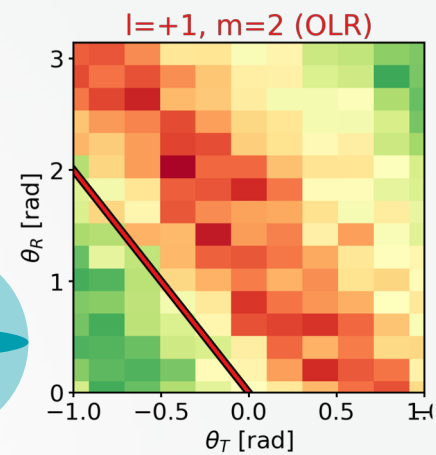
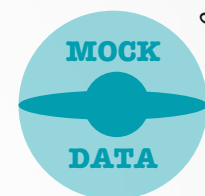
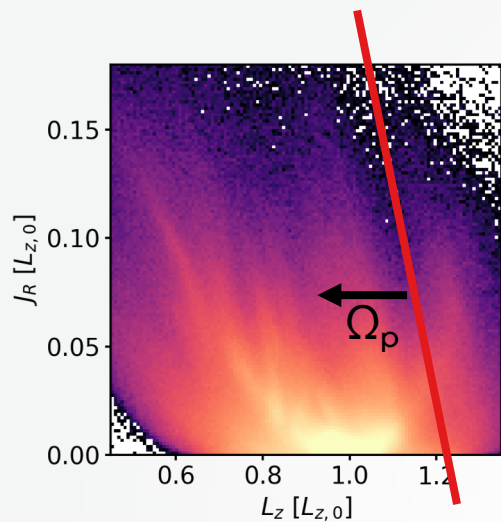
# IDEA: HOW TO DEAL WITH THE SELECTION EFFECTS

Bar resonances & axisym. Angles





# ANGLE SPACE AT THE OLR ASSUMING A PATTERN SPEED



# CROWDSOURCING THE BAR'S PATTERN SPEED FROM THE AXISYMMETRIC ANGLES

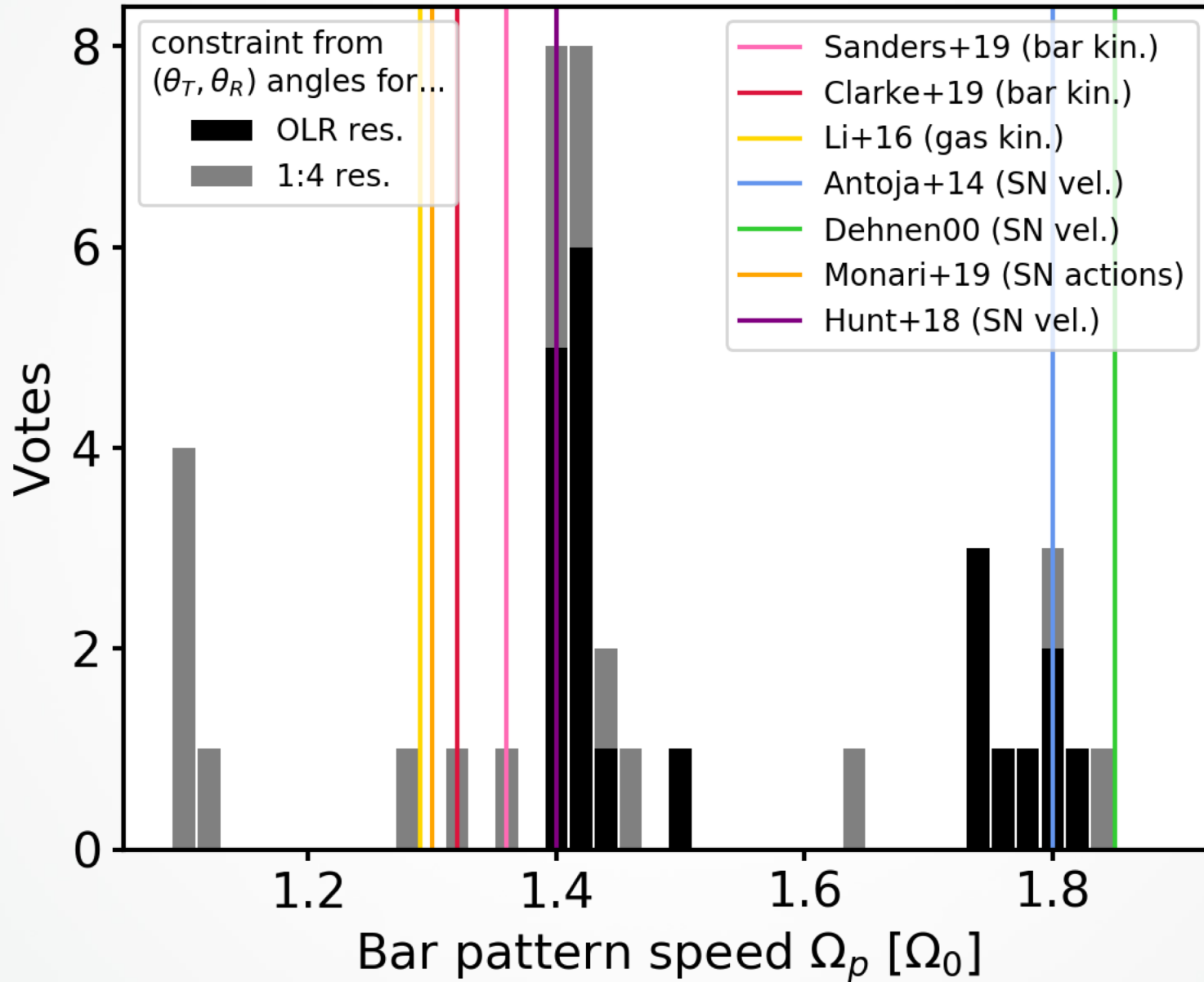


<https://goo.gl/n2omwv>



The screenshot shows a Google Docs document with a starry background. The title is "Crowdsourcing the Bar's Pattern Speed from Angle Space". The text explains the goal of determining the pattern speed of the bar by selecting the angle plane that best matches a model expectation. It includes a note about the (0,0) point and a "THANK YOU!!!" message. Below the text is a grid of 11 panels, labeled A1 through A10, each showing a different angle plane. A legend panel at the top left of the grid shows a heatmap with a diagonal line and labels for  $l=+1, m=2$  (OLR) and "ideal model expectation: line through (0,0) with slope -2, separates 'green' and 'red'". A red arrow points from the legend to panel A3. A note on the right says "This is the Gaia DR2/RVS data! (The outer envelopes are selection effects, please ignore)".

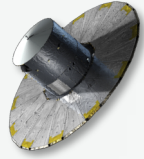
# CROWDSOURCING THE BAR'S PATTERN SPEED FROM THE AXISYMMETRIC ANGLES



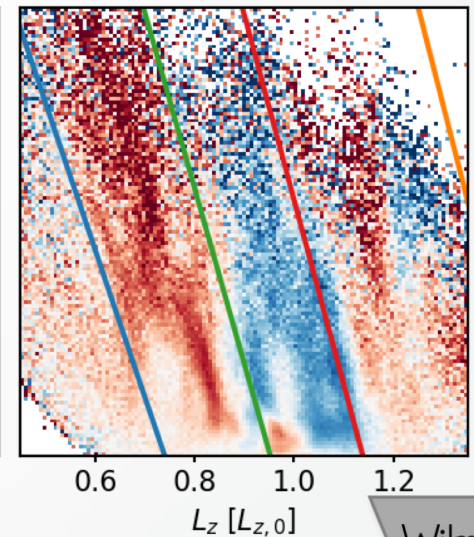
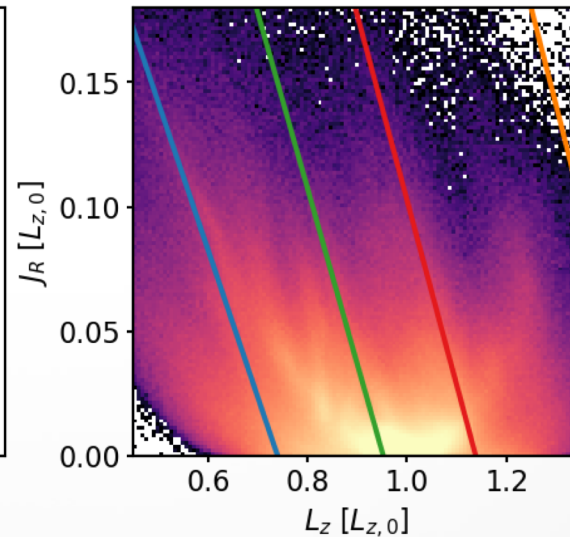
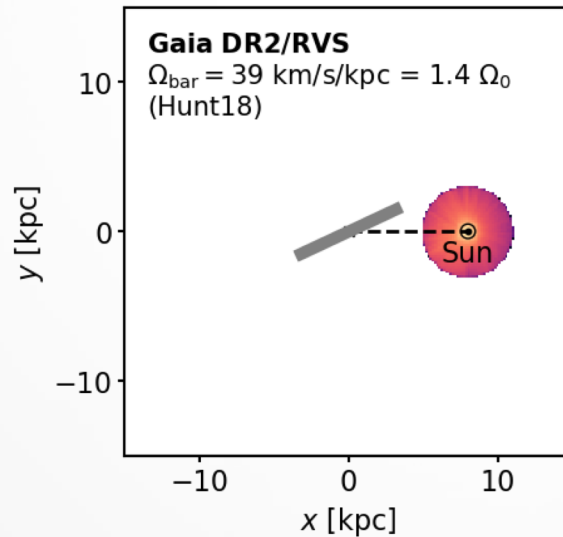
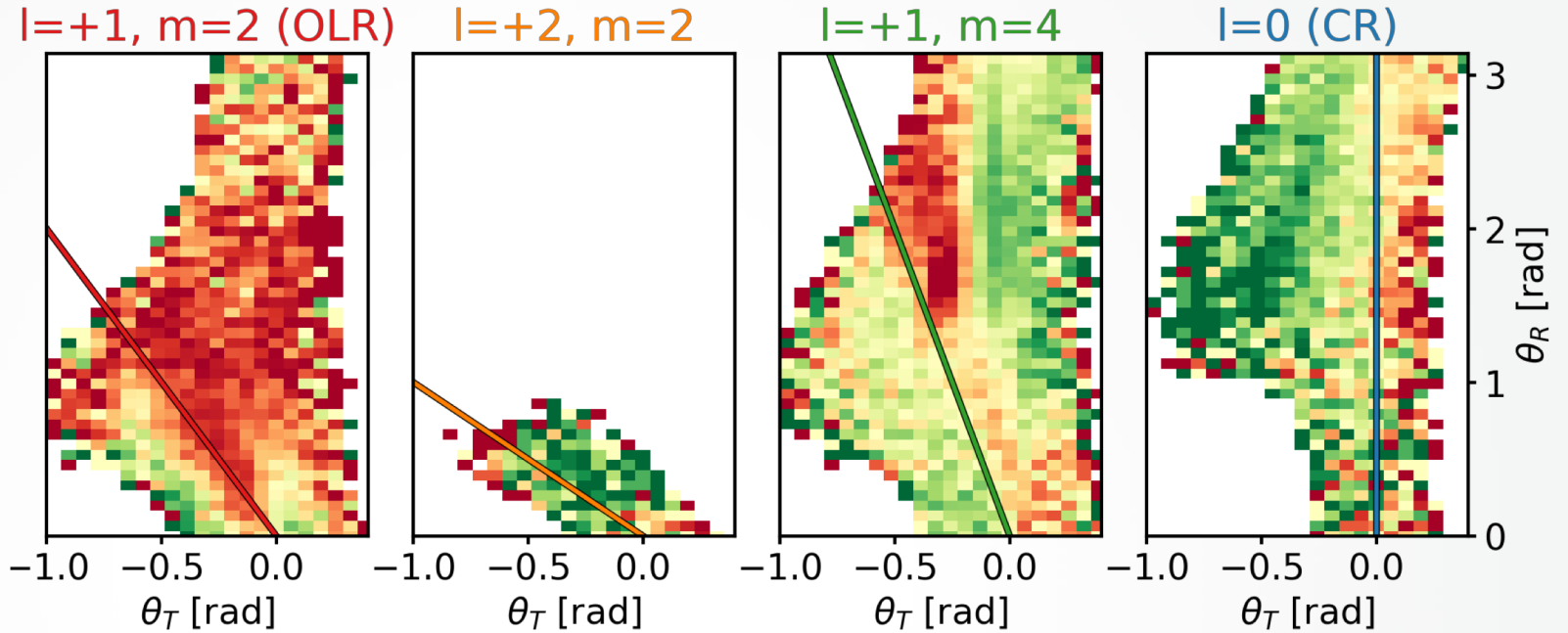


# CROWDSOURCING THE BAR'S PATTERN SPEED FROM THE AXISYMMETRIC ANGLES

Bar resonances & axisym. Angles



very close to model by Hunt+18  
(Hercules caused by 1:4 bar res.):  
 $\Omega_p \sim 1.4 \Omega_0$



- CR
- OLR
- $l=+2, m=2$
- $l=+1, m=4$

# SUMMARY: THE BAR IN GAIA DR2'S ACTION-ANGLES

■ The space of axisymmetric actions ( $L_z, J_R$ ) of Gaia DR2 reveals...

... a system of **orbit sub-structure that extends out to 1.5 kpc** from the Sun

... asymmetric radial motions

*Trick, Coronado, & Rix (2019)*

■ The **OLR** of the bar is expected to cause an „outward-inward“ feature in action space.

*Fragkoudi, [...], Trick et al. (2019)*

Simple comparison to the **Gaia DR2 data proposes two bar models close to the existing** fast (e.g. Antoja et al. 2014) and slow (e.g. Portail et al. 2015) bar models.

*Trick, Fragkoudi, Hunt, Sellwood, Mackereth, White et al. (to be submitted)*

■ The space of axisymmetric angles ( $\Theta_T, \Theta_R$ ) in Gaia DR2 **surprisingly prefers the bar model by Hunt et al. (2018).**

*Trick et al. (in preparation)*

■ I am optimistic that **dynamical modeling with axisymmetric actions / angles / frequencies** can and will be still super interesting after Gaia DR2. 😊👍