



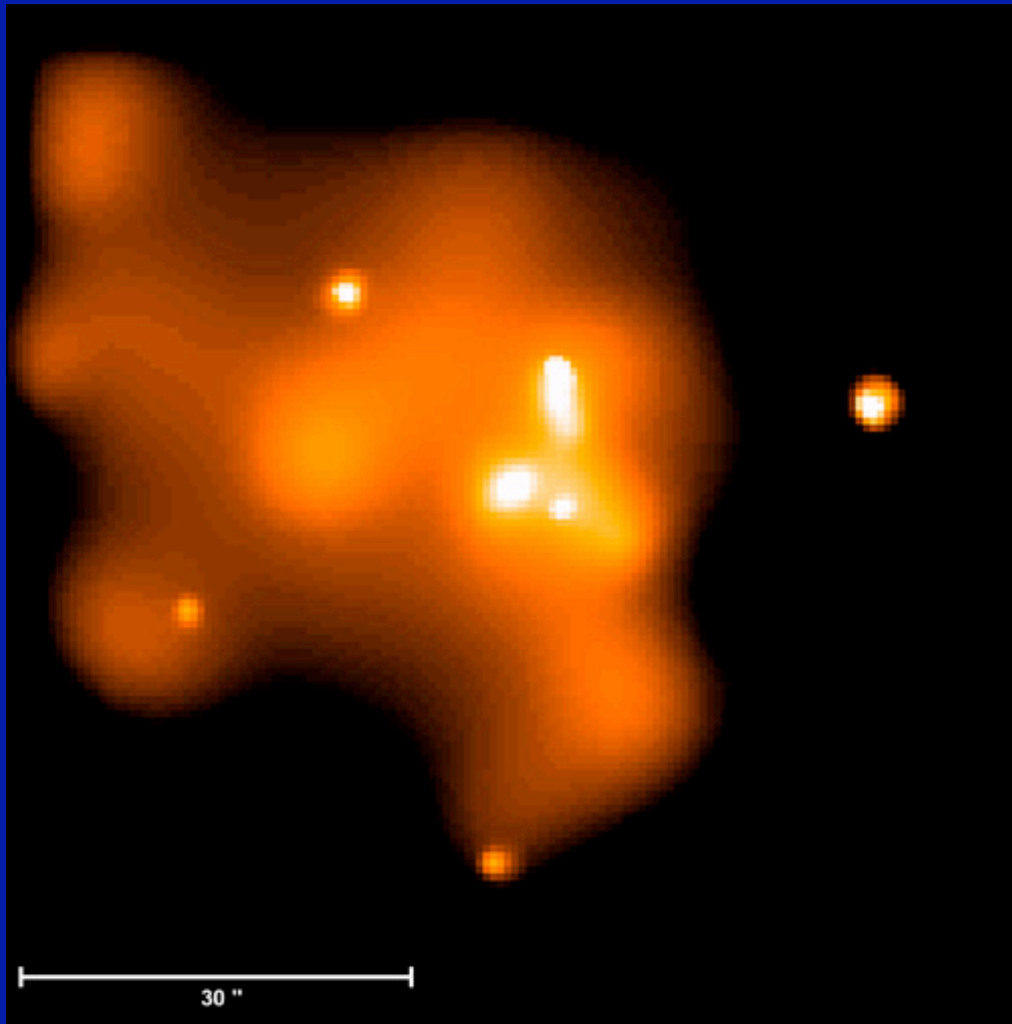
Models of Accretion Flows in Kinetic Theory

(+ a wee bit of MHD)

Eliot Quataert
(UC Berkeley)

Collaborators: Prateek Sharma, Greg Hammett, Bill Dorland, Jim Stone
Josh Goldston, Karin Sandstrom

The (In)Applicability of MHD?



Observed Plasma

($\sim 1'' \sim R_{\text{Bondi}} \sim 10^5 R_{\text{S}}$)

$T \sim \text{few keV}$ $n \sim 100 \text{ cm}^{-3}$

e-p thermalization time \sim **2000 yrs**

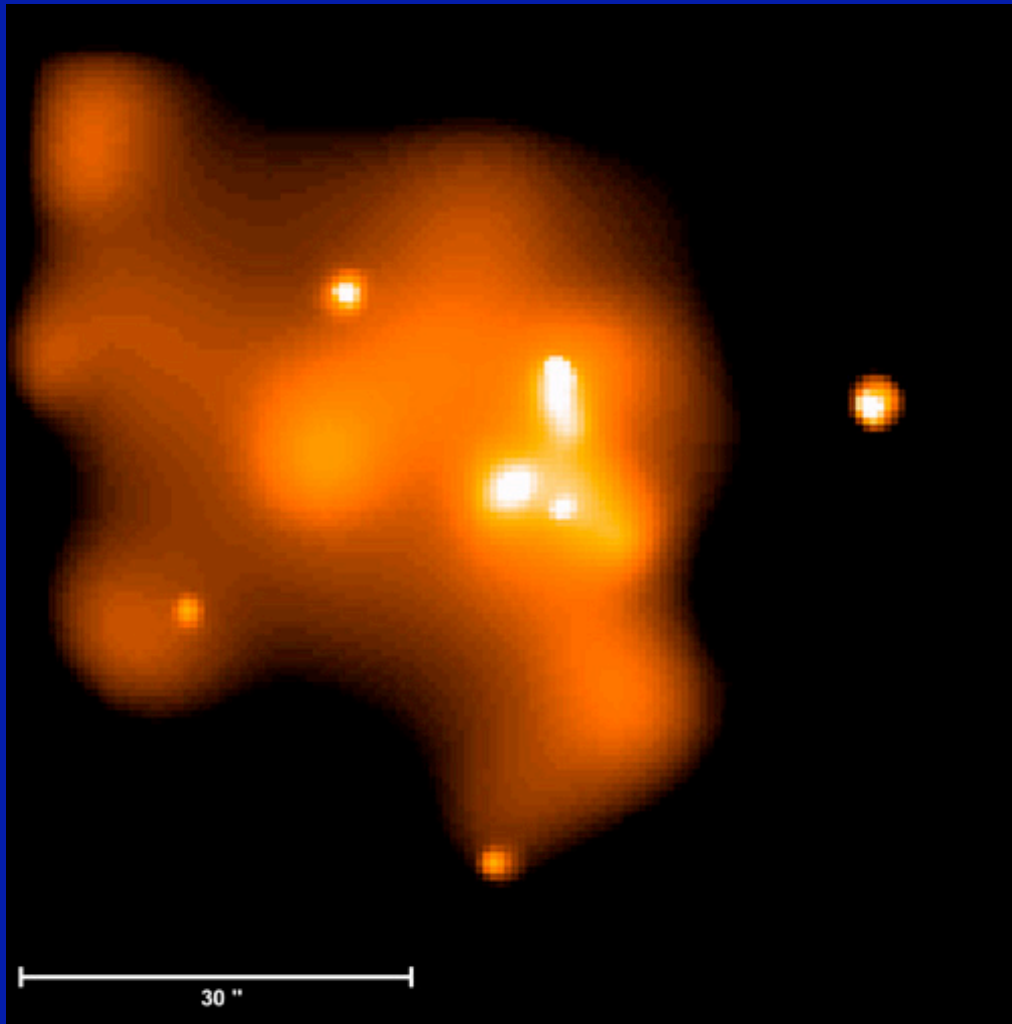
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inflow time $\sim R_{\text{Bondi}}/c_{\text{S}} \sim$ **100 yrs**

\Rightarrow

T_{electron} measured by X-rays
need not equal T_{proton}
(complicates inference of R_{Bondi})

The (In)Applicability of MHD?



Estimated Conditions
Near the BH

$$\begin{aligned}T_p &\sim 10^{12} \text{ K} \\T_e &\sim 10^{11} \text{ K} \\n &\sim 10^6 \text{ cm}^{-3}\end{aligned}$$

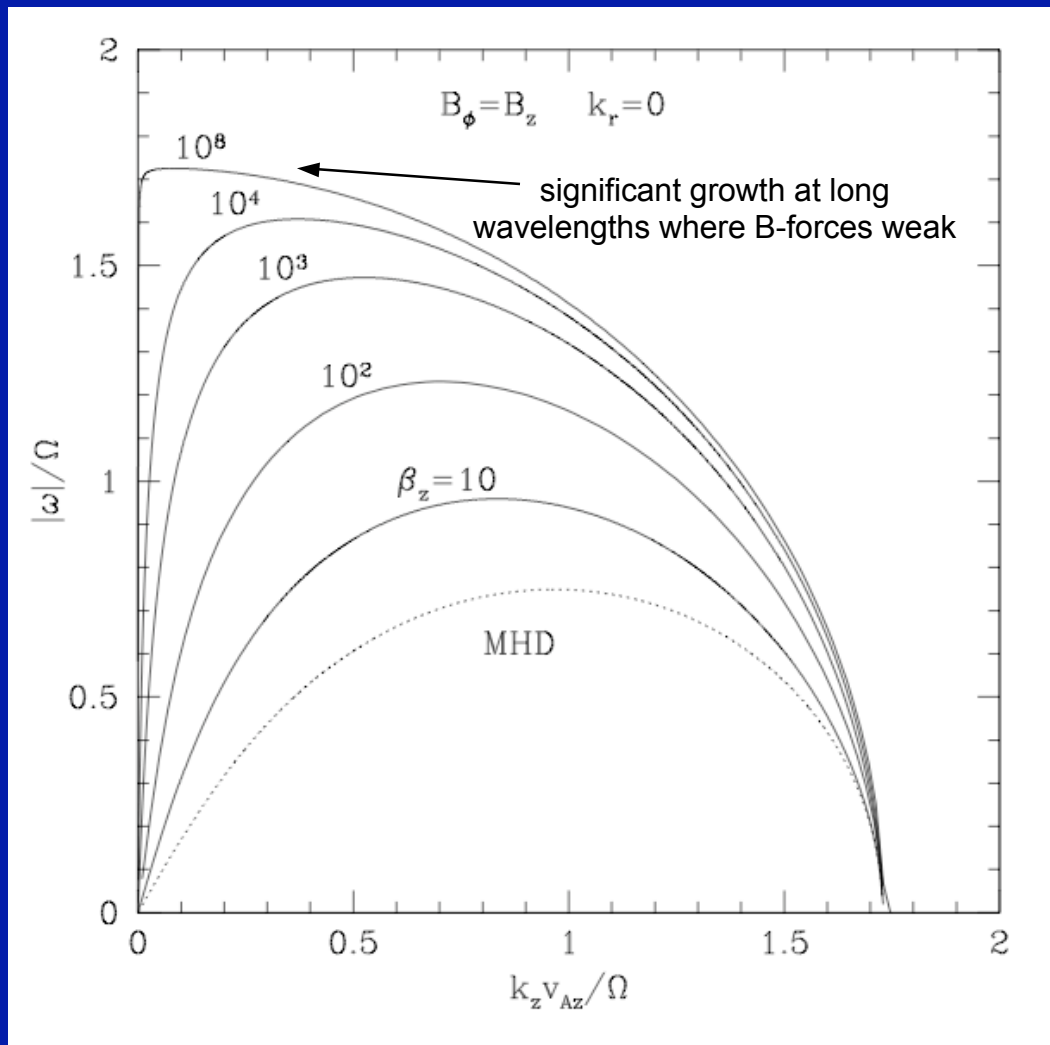
proton mfp \sim kpc $\gg \gg R_s$



We need to understand
accretion of a magnetized
collisionless plasma



The MRI in a Collisionless Plasma

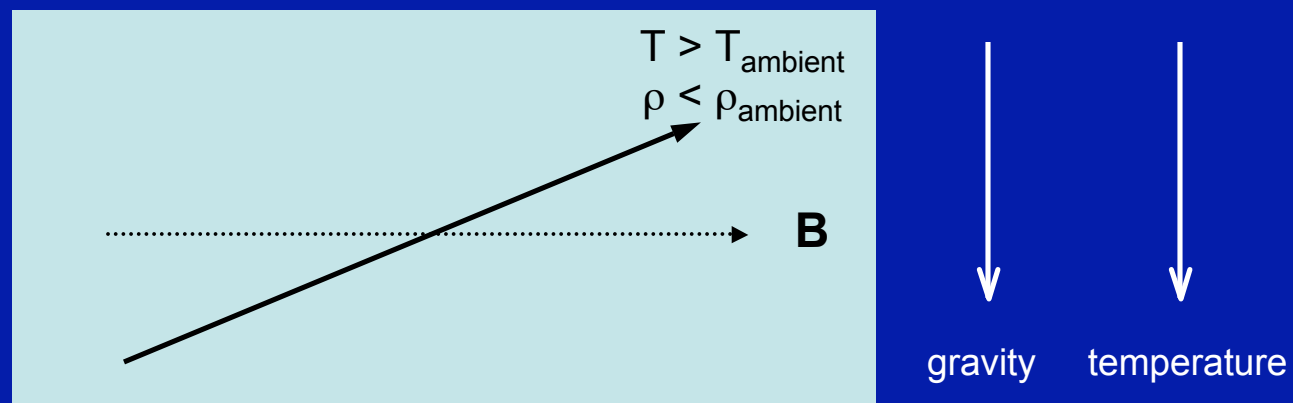


angular momentum transport
via anisotropic pressure (viscosity!)
in addition to magnetic stresses

Collisionless Convection

(Balbus 2000; Karin Sandstrom & EQ 200N)

- Convection (Buoyancy) May be Dynamically Impt in Hot, Thick Disks
- Schwarzschild Criterion for Instability in Hydro & MHD ($\beta \gg 1$): **$ds/dr < 0$**



$$t_{\text{conduction}} < t_{\text{buoyancy}} \Rightarrow \nabla_{\parallel} T \approx 0 \quad (\text{temp constant along field lines})$$

“Convection” if **$dT/dr < 0$**

**Hydro & MHD Simulations Do
Not Capture the Correct Physics
of Dynamical Instabilities in
Hot Collisionless RIAFs
(neither MRI nor Convection)**

Goal: Kinetic Simulations

Kinetic-MHD

(e.g., Kulsrud 1983)

- Large-scale Dynamics of collisionless plasmas: expand Vlasov equation retaining “slow timescale” & “large lengthscale” assumptions of MHD
- Particles efficiently transport heat and momentum along field-lines

$$\begin{aligned}\frac{\partial \rho}{\partial t} + \nabla \cdot (\rho \mathbf{V}) &= 0, \\ \rho \frac{\partial \mathbf{V}}{\partial t} + \rho (\mathbf{V} \cdot \nabla) \mathbf{V} &= \frac{(\nabla \times \mathbf{B}) \times \mathbf{B}}{4\pi} - \nabla \cdot \mathbf{P} + \mathbf{F}_g, \\ \frac{\partial \mathbf{B}}{\partial t} &= \nabla \times (\mathbf{V} \times \mathbf{B}), \\ \mathbf{P} &= p_{\perp} \mathbf{I} + (p_{\parallel} - p_{\perp}) \hat{\mathbf{b}} \hat{\mathbf{b}},\end{aligned}$$

Evolution of the Pressure Tensor

$$\rho B \frac{d}{dt} \left(\frac{p_{\perp}}{\rho B} \right) = -\nabla \cdot (\hat{\mathbf{b}} q_{\perp}) - q_{\perp} \nabla \cdot \hat{\mathbf{b}}$$

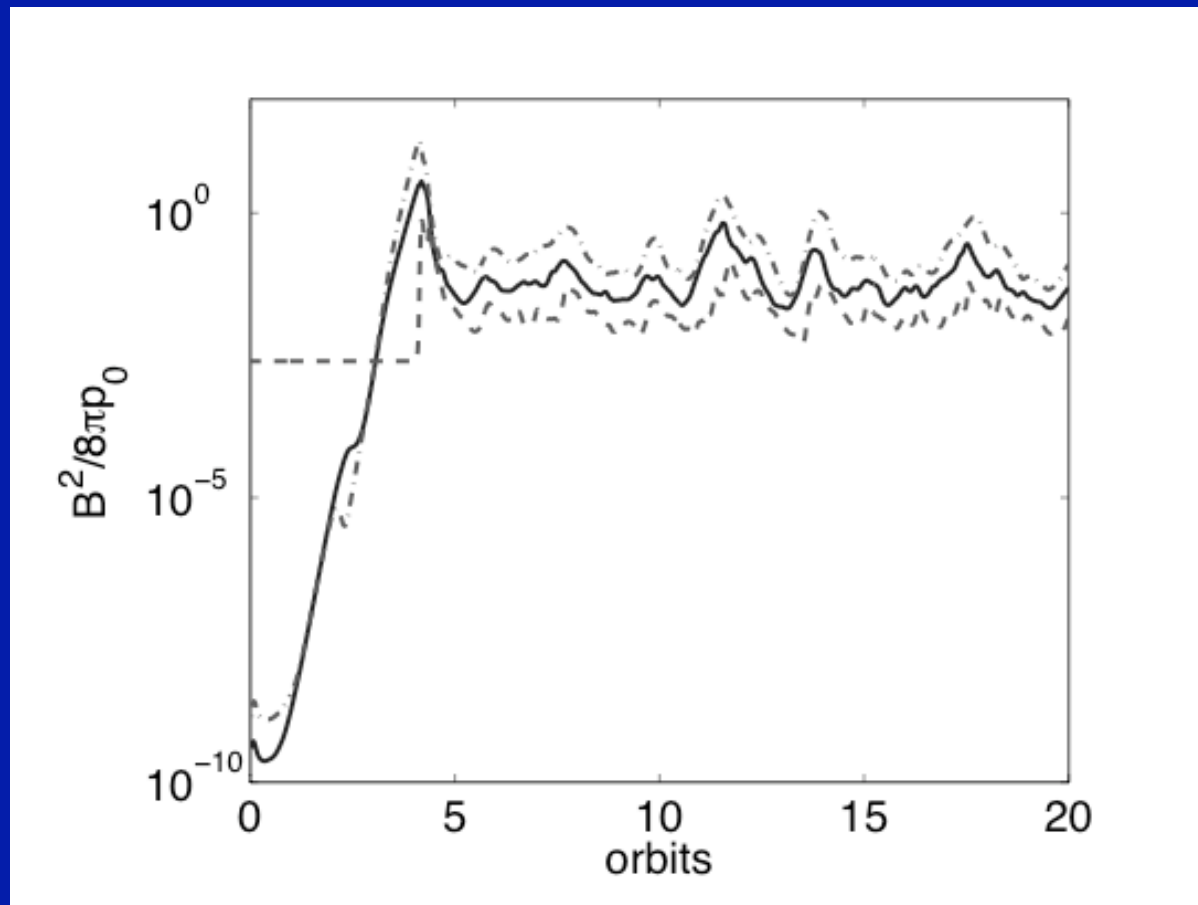
adiabatic invariance
of $\mu \sim mv_{\perp}^2/B \sim T_{\perp}/B$

$$\frac{\rho^3}{B^2} \frac{d}{dt} \left(\frac{p_{\parallel} B^2}{\rho^3} \right) = -\nabla \cdot (\hat{\mathbf{b}} q_{\parallel}) + 2q_{\perp} \nabla \cdot \hat{\mathbf{b}},$$

$$q \approx \frac{nv_{th}}{|k_{\parallel}|} \nabla_{\parallel} T$$

Closure Models
(Approximations) for the
Heat Flux (temp gradients
along fields wiped out
on \sim a crossing time)

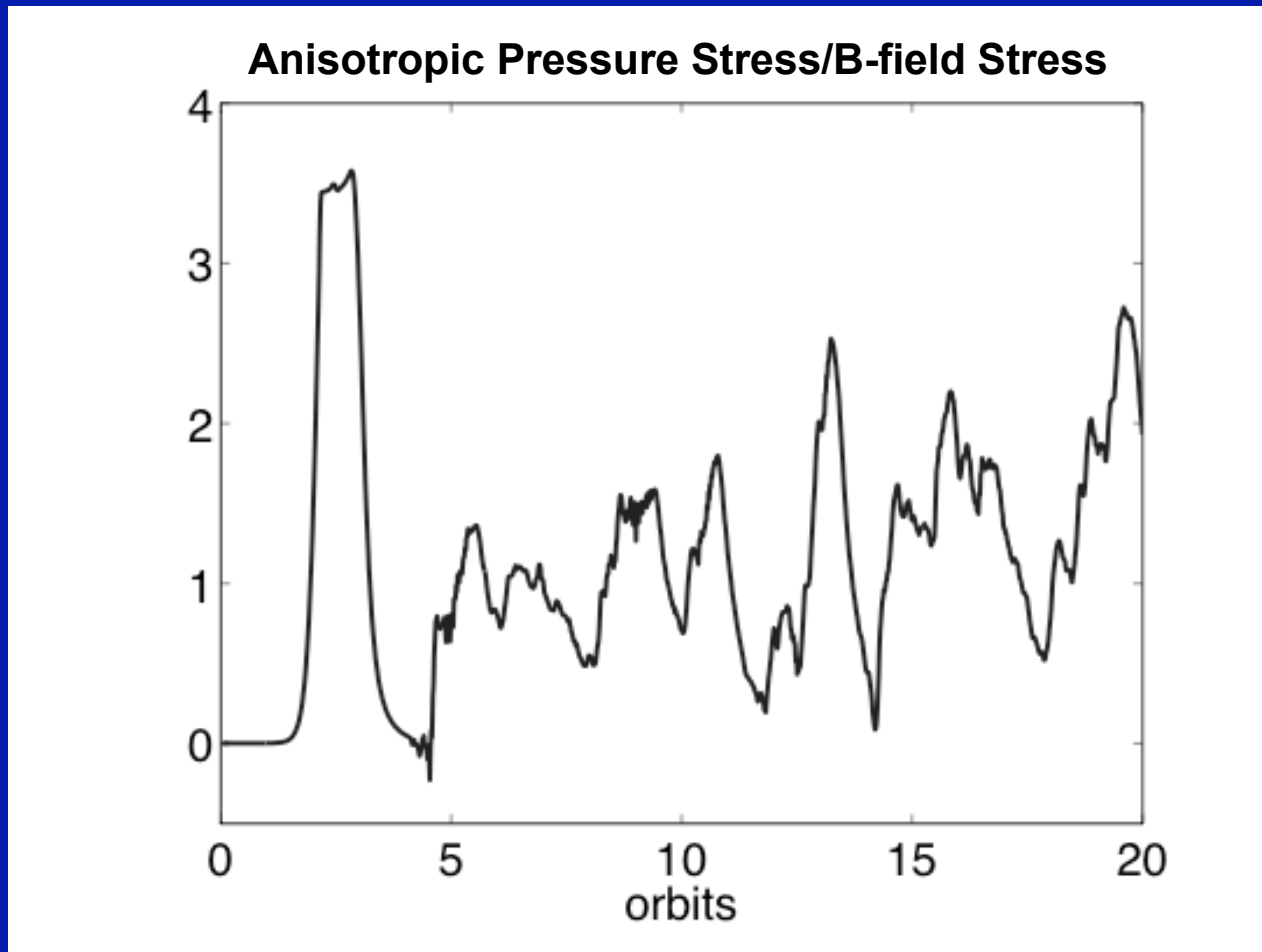
Local Simulations of the Kinetic MRI



**Non-linear Evolution
Depends Critically
On Isotropization
Of Pressure Tensor
via small-scale
Kinetic Instabilities**

Sharma et al. in prep

Angular Momentum Transport



**Anisotropic Stress
~ Maxwell Stress**

Local Rate of
Angular Momentum
Transport Enhanced
(by factor ~ 2)

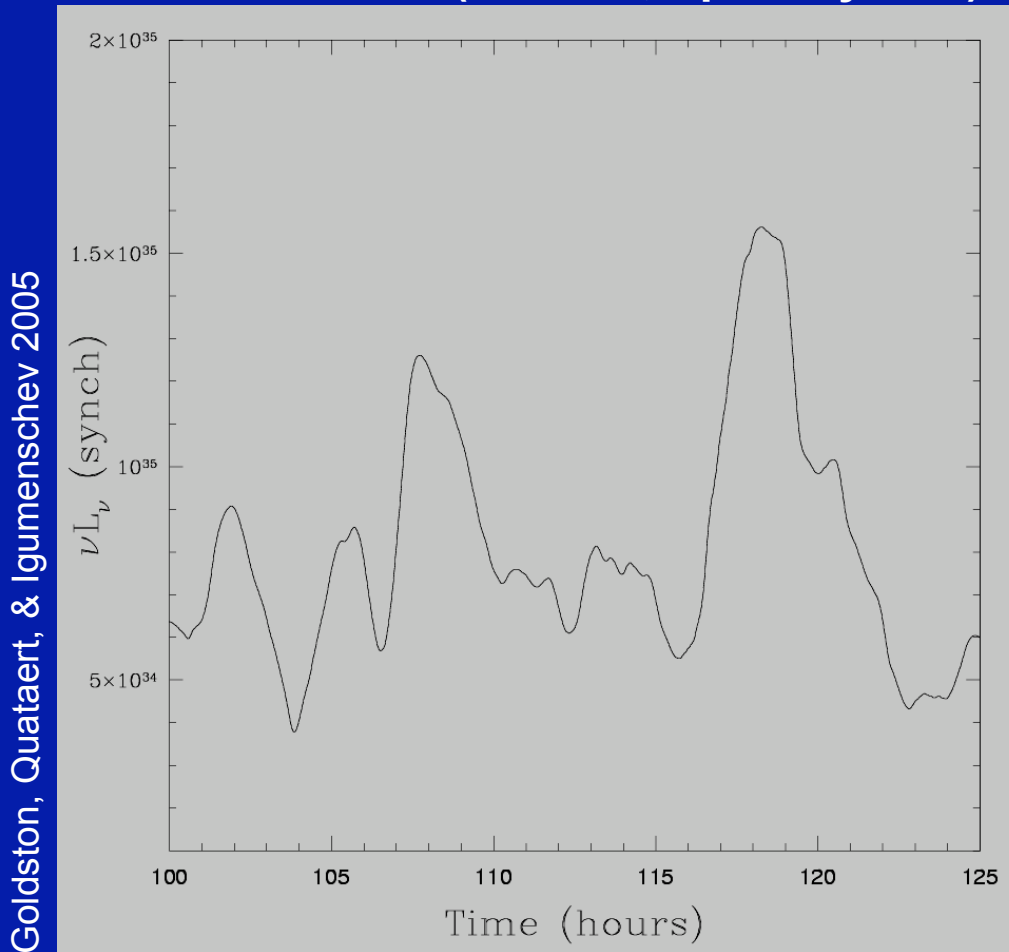
Global Dynamics
In Collisionless Limit
Remains to Be Explored

Sharma et al. in prep

Connecting Simulations To Observations

Synchrotron Emission in Global **MHD** Sims of RIAFs

1mm/300 GHz (thermal; optically thin)



At high (optically thin) frequencies, factors of ~ few-5 variability on ~ hour timescales (~ orbital period near BH)

How Quantitative Can we Be?

- IR & X-ray 'Flaring' Depends on e- DF: **Plasma Physics Weather?**
- Electron Heating & Acceleration Remain Poorly Understood
- **electron conduction time \ll inflow time, electron cooling time**
- \Rightarrow conduction strongly influences T_e & thus the radiation we see
- (maybe submm better bec. \sim thermal population of e⁻s?)

Summary

- Accretion Flow onto Sgr A* is Collisionless: $mfp/R_s \sim 10^9!$
- Instabilities that Determine Accretion Flow Dynamics Qualitatively Different in Collisionless Plasmas (MRI, Convection)
- Local Simulations of Kinetic MRI Similar to MHD with Enhanced Transport due to Anisotropic Pressure Stresses
- Radiation from MHD Simulations Similar to Observations of SgrA*
 - Caution Required Re. Quantitative Comparisons (Electron DF?)