

# STELLAR ROTATION & ACTIVITY

## FROM THE SURFACE TO THE INTERIOR MEASURED BY COROT AND *KEPLER*

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Special thanks to:

K. Auguston, J. Ballot, A. Bonanno, A.S. Brun, T. Ceillier, A. Lanza, S. Mathur, T. Metcalfe, J. van Saders, D. Salabert & J. Tayar

## ➤ I- Introduction

- Why study the dynamics of other stars and their magnetism?
  - Closer look to solar-like stars
  - Using long time series high-precision photometry from space

## ➤ II- Stellar Dynamics

- Rotation
- Magnetism

## ➤ III- Surface magnetic activity proxy

- Definition photospheric magnetic proxy: Sph
  - Based on reliable surface rotation rates
  - Surface magnetic activity of solar analogs

## ➤ IV- Stellar magnetic cycles

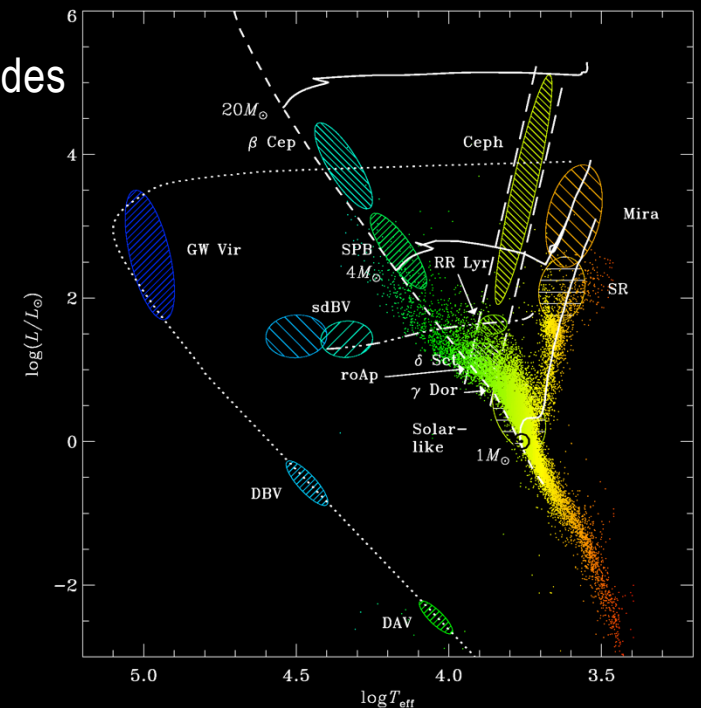
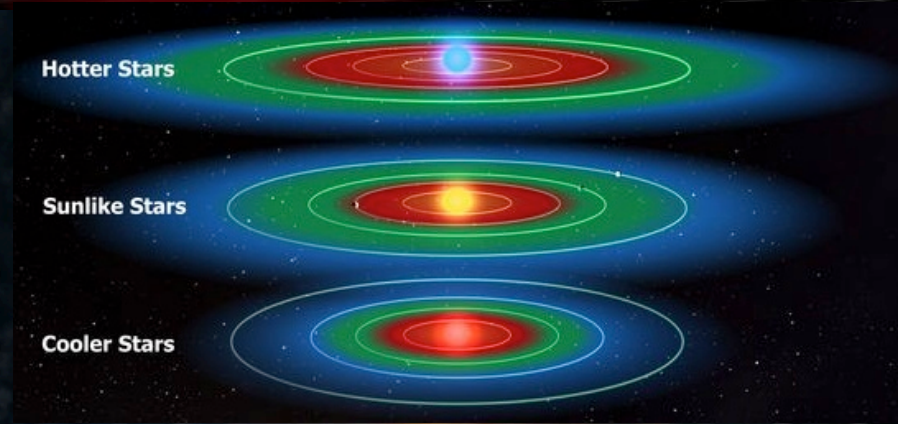
- F-stars: Fast rotating, shorter cycles
- Using seismology



# I-Introduction

## ➤ Why study the dynamics of other stars and their magnetism?

- Are the dynamics of the Sun particular or its properties are common?
- Put the Sun in a broader, evolutionary context
- Solar-stellar connection
- Star-planet interaction: Habitability
- Validate gyrochronology
- Dynamical stellar evolution codes





## ➤ What can offer high-precision photometry (HPP) to better understand stellar dynamics & magnetism ?

- HPP observations can potentially give access to:
  - Surface (differential?) rotation of hundred to thousand stars [e.g. McQuillan et al. 2013, 2014; Nielsen et al. 2013; Reinhold & Reiners 2013, 2015; García et al. 2014]
  - Internal (differential) rotation through seismology [e.g. Beck et al. 2012; Deheuvels et al. 2012, 2014; Mosser et al. 2012; Pia di Mauro et al. subm.]
- Convection properties
  - Characteristic time scale and velocities of convection (granulation) [e.g. Mathur et al. 2011; Kallinger et al. 2014]
    - other scales:
      - e.g. Faculae in active stars [e.g. Karoff et al. 2013]
- Internal structure (through seismology)
  - Size of the convective envelope [e.g. Mathur et al. 2012; Mazumdar et al. 2014; Metcalfe et al. 2014]
  - Probing (or not) the existence of internal magnetic fields
- Activity cycles
  - Through the analysis of long time series (activity proxies) [e.g. García et al. 2010; Mathur et al. 2013, 2014]
    - Or asteroseismology [e.g. García et al. 2010; Régulo et al. submitted]

# IIa-Stellar Dynamics:

## Rotation



# II-EFFECTS OF INTERNAL ROTATION

## ➤ Why studying the rotation of stars?

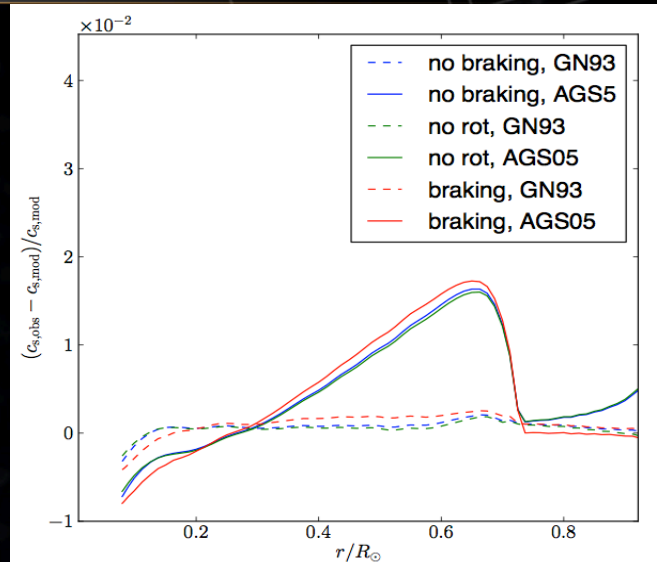
- It changes stellar evolution:
  - Angular momentum transfer
  - Mixing
- It also changes seismic variables:

Model no rotation       $V_i = 150 \text{ km s}^{-1}$

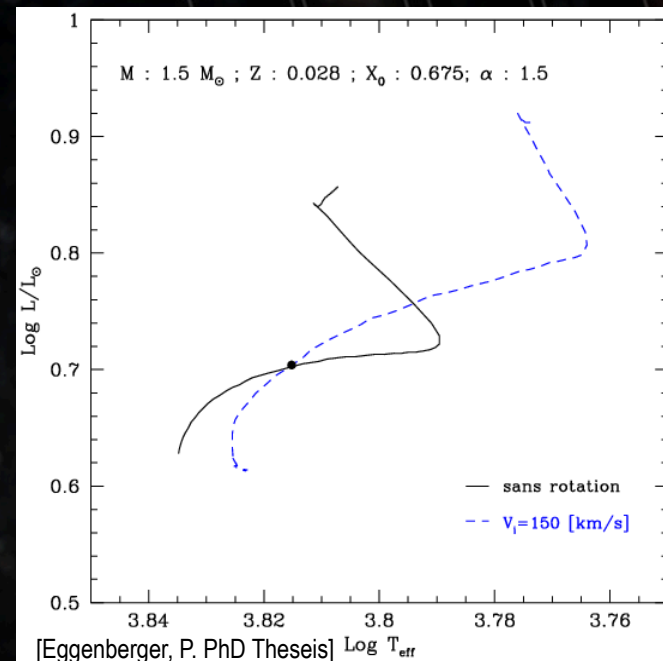
$\Delta\nu$       70.40  $\mu\text{Hz}$       69.94  $\mu\text{Hz}$

$\delta\nu_{02}$       5.07  $\mu\text{Hz}$       5.76  $\mu\text{Hz}$

- When rotation is considered in models:
  - Modify p-mode frequencies
  - high orders (surface effects?)

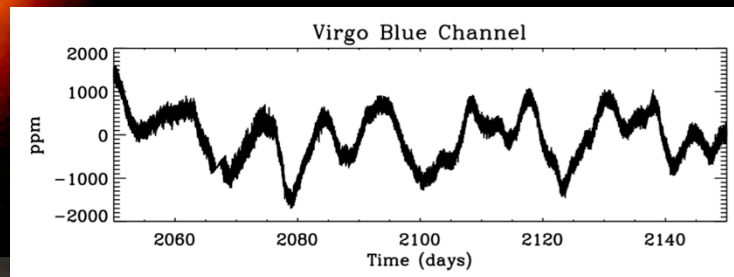
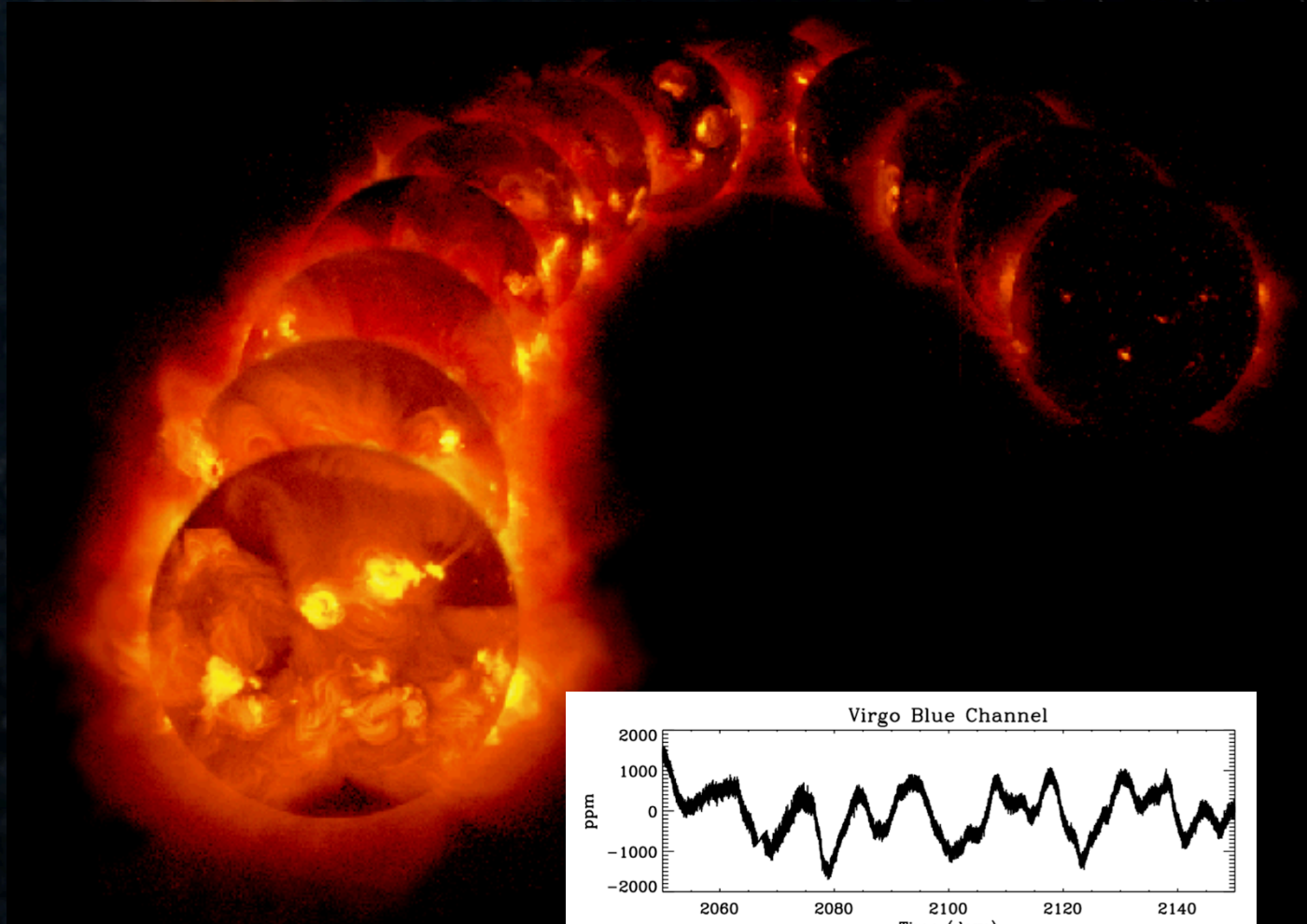


[Marques, et al. 2012; Turck-Chièze et al. (2010)...]



[Eggenberger, P. PhD Theseis]

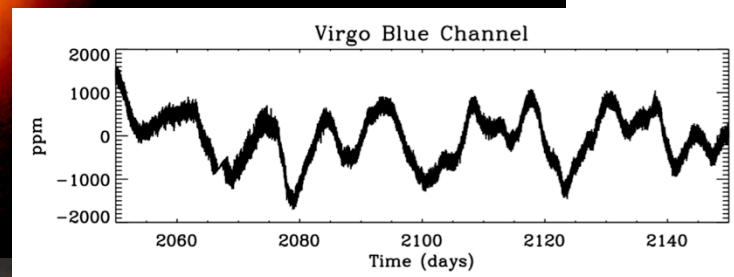
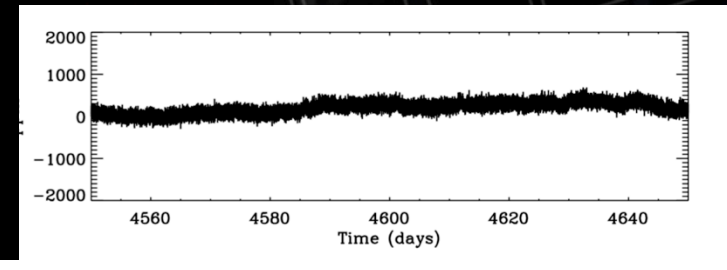
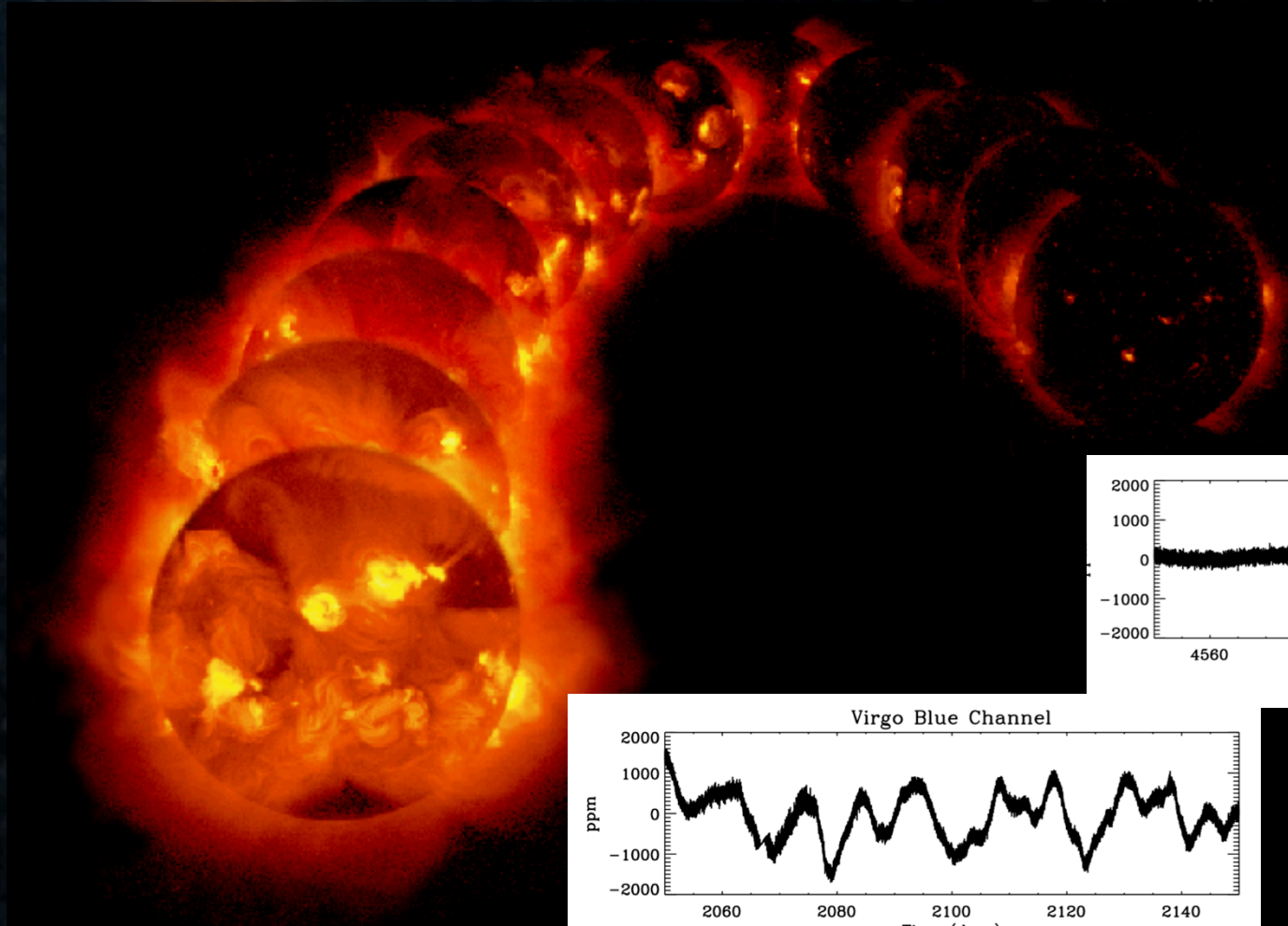
- When a star is magnetically active
  - Starspots crossing the visible disk of stars induce a modulation in the light curve



Solar Activity Maximum



- When a star is magnetically active
  - Starspots crossing the visible disk of stars induce a modulation in the light curve

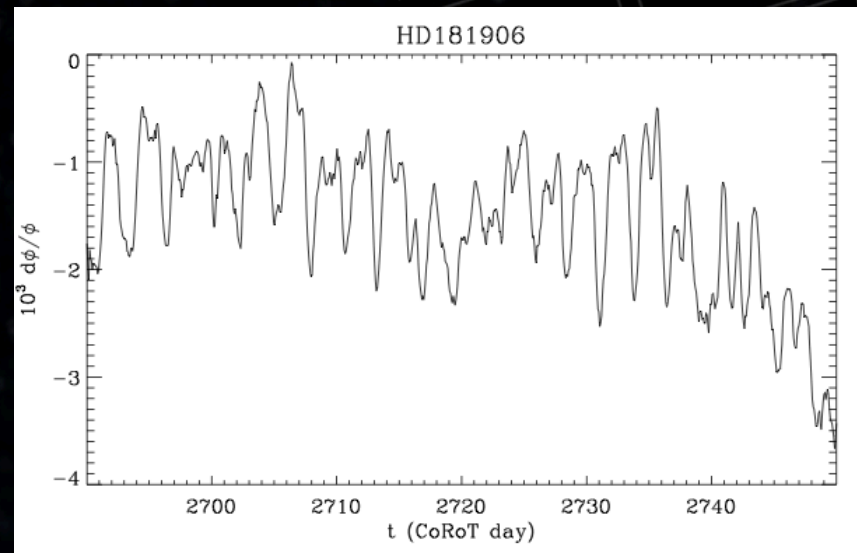
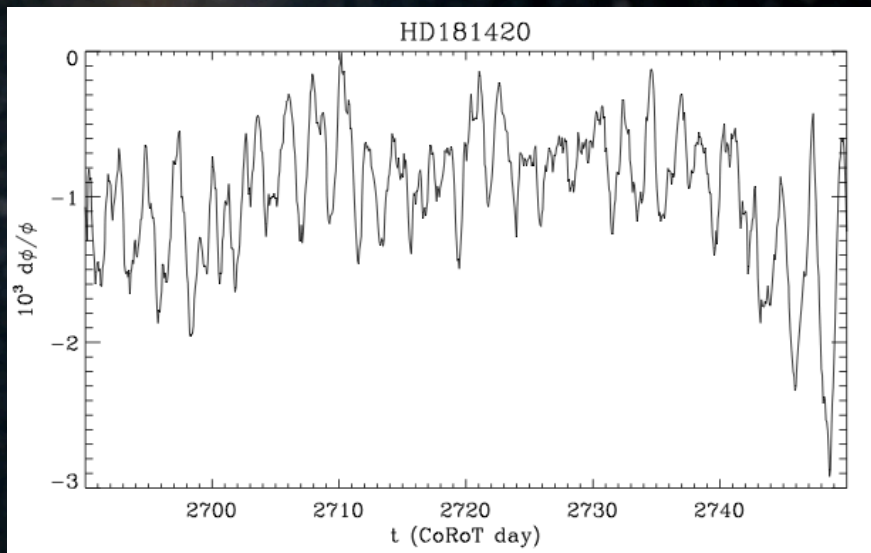


Solar Activity Minimum

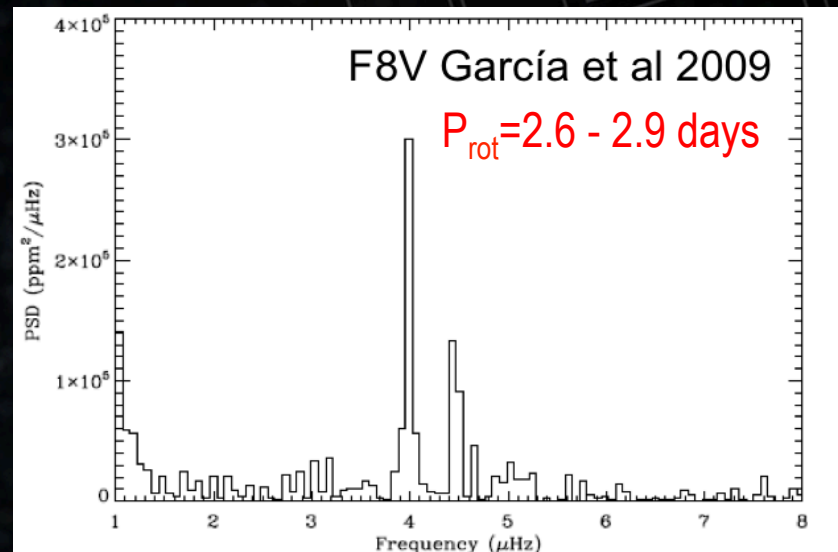
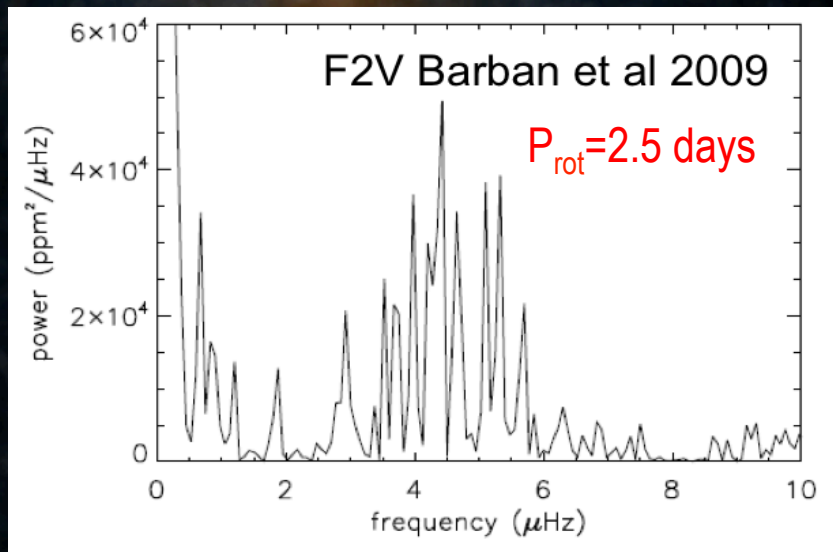
Solar Activity Maximum

# II-SURFACE ROTATION

## ➤ Examples of two CoRoT F Stars



## ➤ Analysis of the low-frequency range of the periodogram





# II-SURFACE ROTATION

## ➤ Techniques based on the analysis of the low-frequency part of the Periodogram

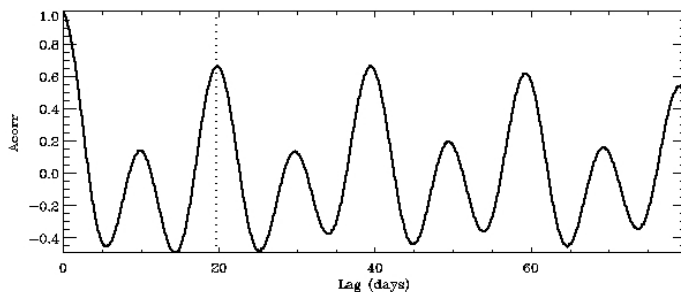
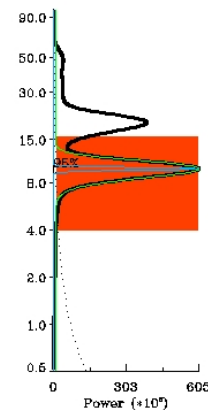
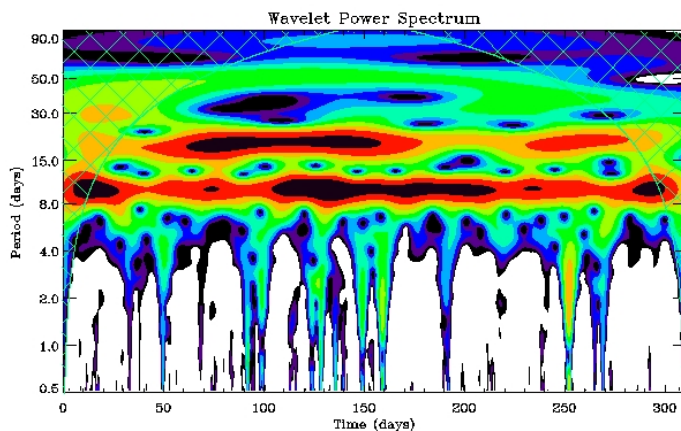
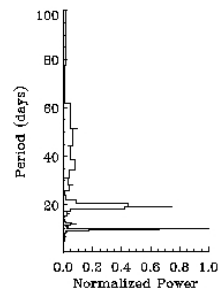
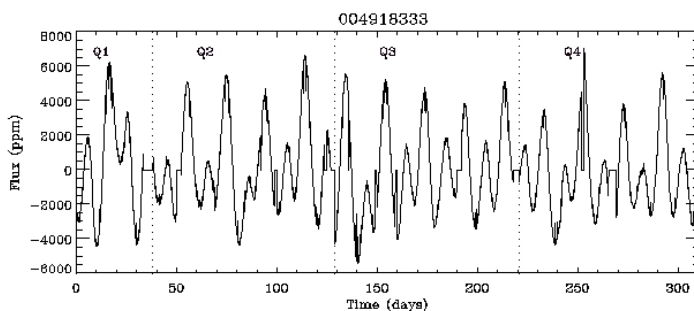
### ■ Problem:

- $2^{\text{nd}} > 1^{\text{st}}$  harmonic
- Check half of  $P_{\text{rot}}$

## ➤ Autocorrelation

### ■ Powerful for capturing the correct $P_{\text{rot}}$

- When there are two well defined
  - active longitudes



$$\begin{aligned} \nu_{\text{rot}} &= 1.18 \mu\text{Hz} \\ P_{\text{rot}} &= 9.8 \text{ days} \\ P_{\text{rot}}^1 &= 9.8 \pm 0.6 \text{ days} \end{aligned}$$

$$\langle \text{ACF} \rangle = 19.7 \text{ days}$$

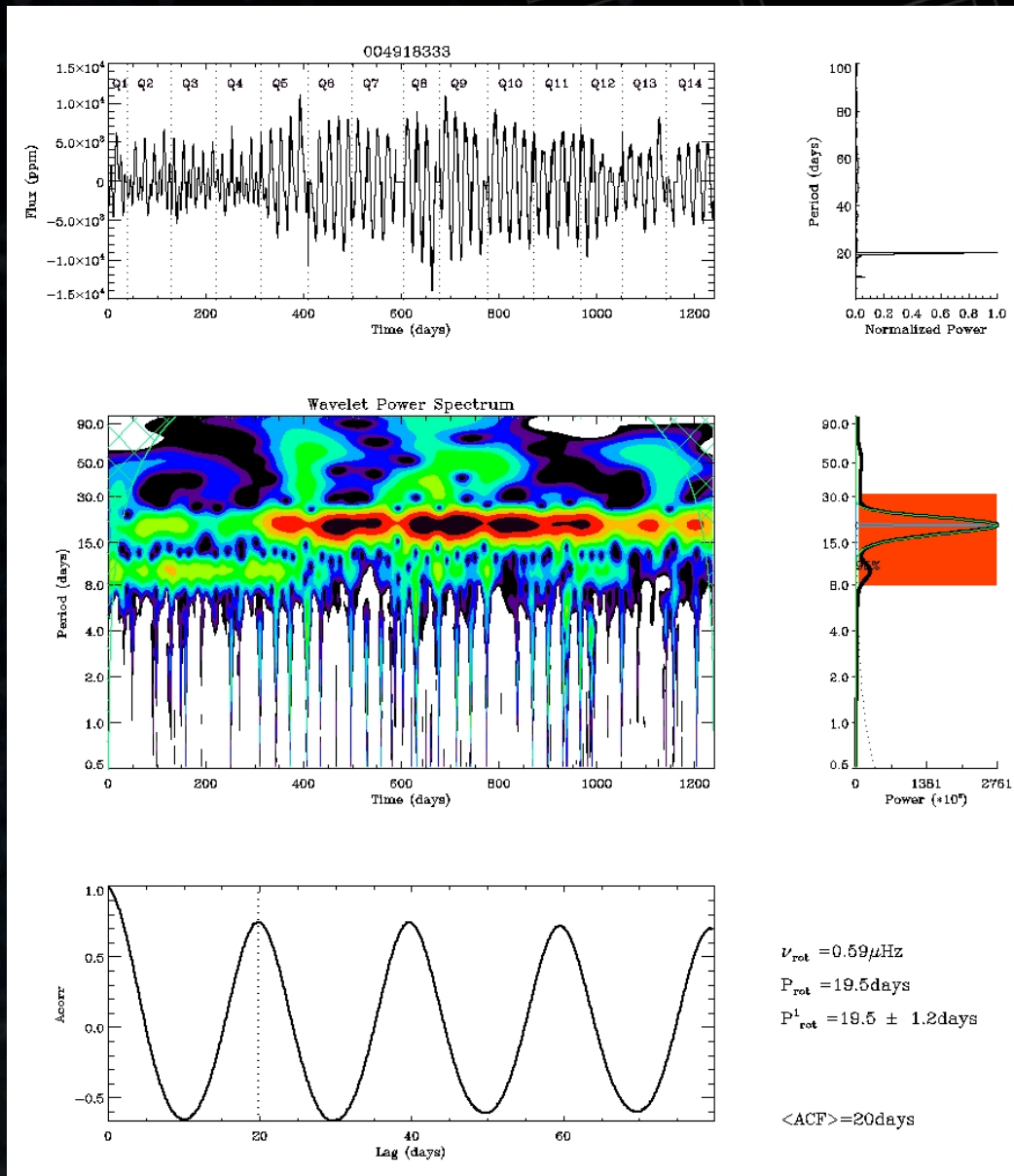
# II-SURFACE ROTATION

## ➤ Techniques based on the analysis of the low-frequency part of the Periodogram

- Problem:
  - $2^{\text{nd}} > 1^{\text{st}}$  harmonic
  - Check half of  $P_{\text{rot}}$
- Using all the available data
  - Could solve it !!

## ➤ Autocorrelation

- Powerful for capturing the correct  $P_{\text{rot}}$ 
  - When there are two well defined
    - active longitudes



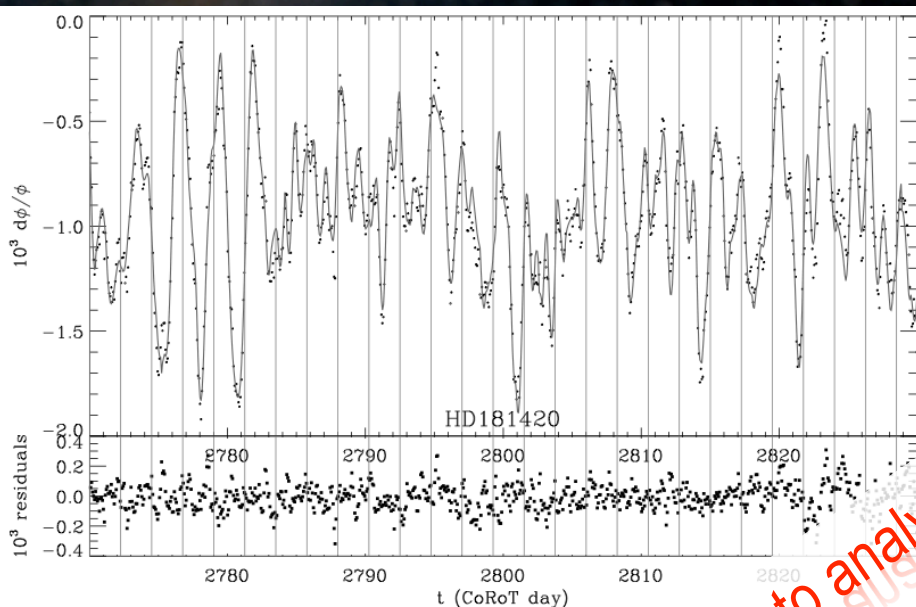


# II-SURFACE ROTATION

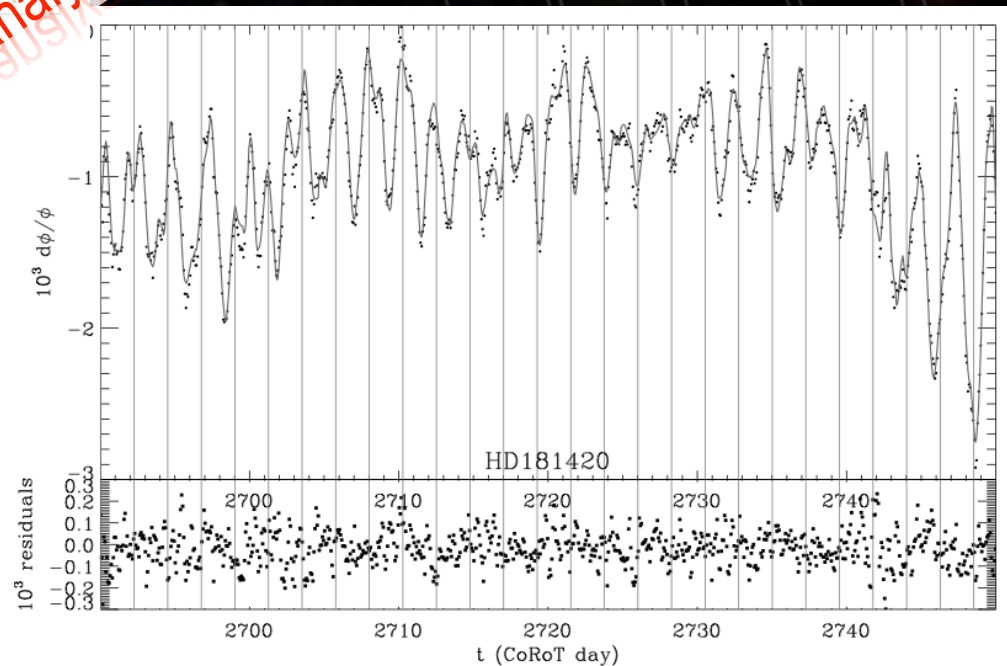
## ➤ Spot modelling

- Robust estimation of:
  - Average rotation
  - Spot lifetime
- More uncertain estimation of:
  - Time and distribution of spots
  - Inclination of the star
  - Differential rotation

Very time consuming to analyse hundred to thousand stars



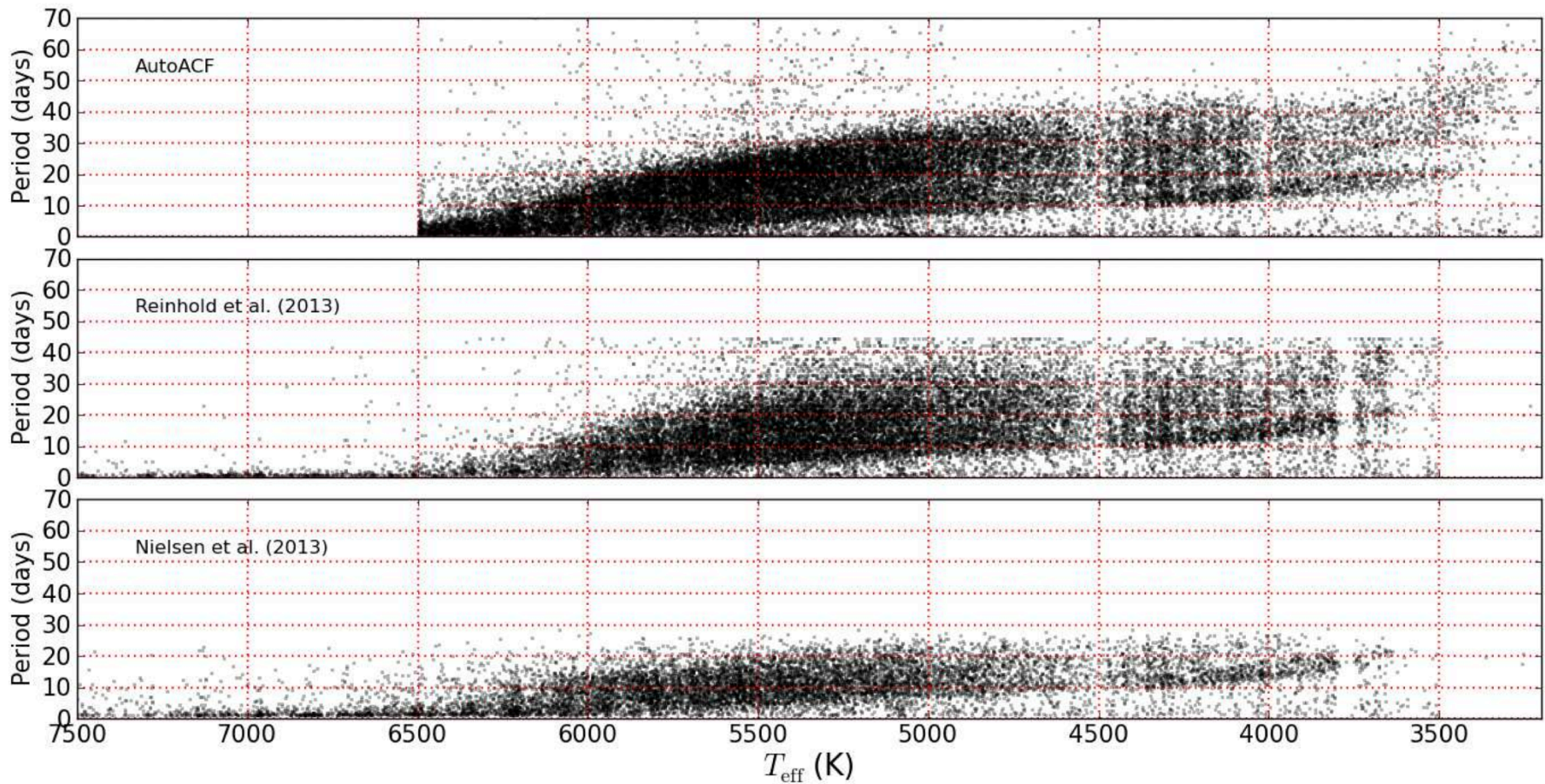
[Mosser et al. 2009]



[see also e.g. Frohlich et al. 2012; Lanza et al. 2014, Bonano et al. 2015]

# II-SURFACE ROTATION

	AutoACF	<a href="#">Reinhold et al. (2013)</a>	<a href="#">Nielsen et al. (2013)</a>
Total Number	34,030	24,124	12,515
AND AutoACF	—	20,009	10,381
AND <a href="#">Reinhold et al. (2013)</a>	20,009	—	9,292
AND <a href="#">Nielsen et al. (2013)</a>	10,381	9,292	—

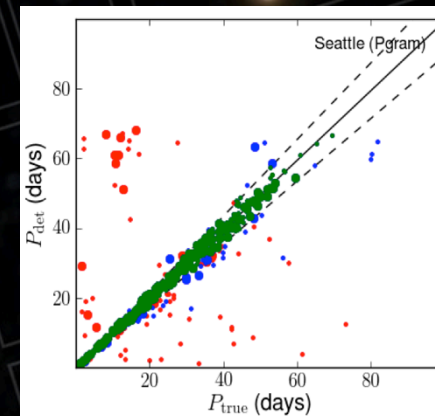
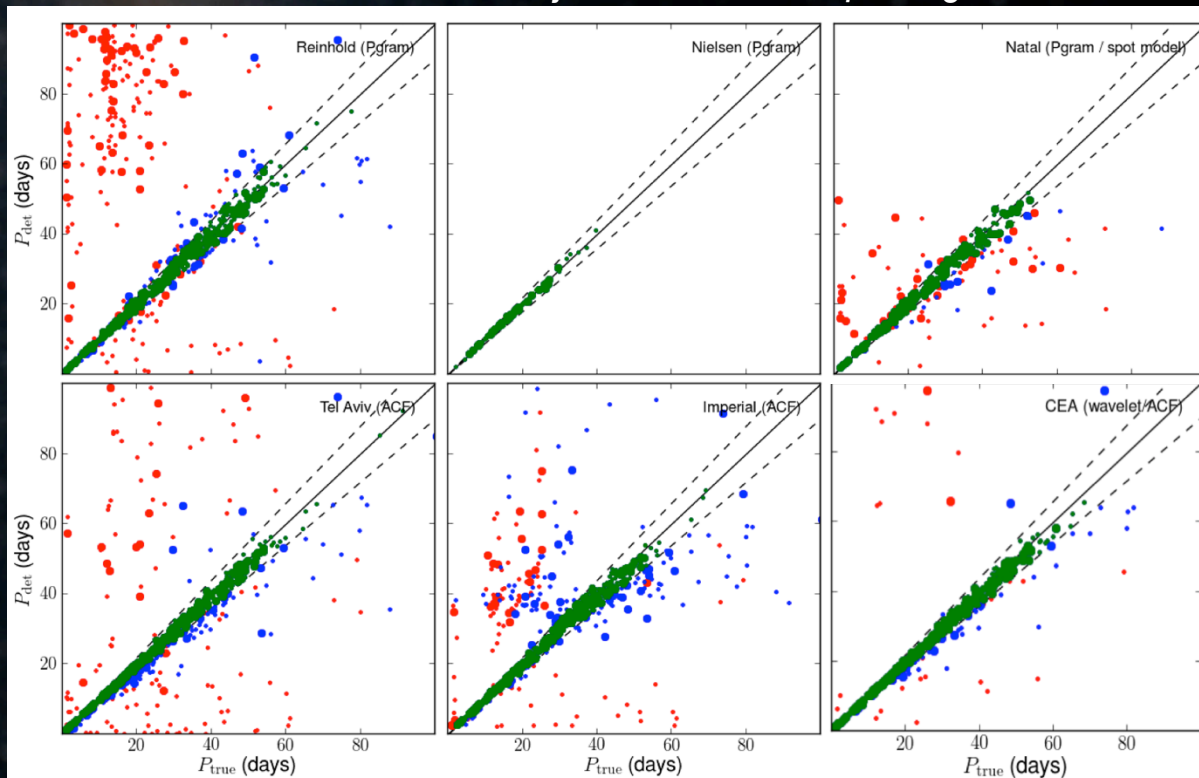




# II-VALIDATING $P_{\text{ROT}}$

## ➤ Through Simulations:

- 1000 simulated stars injected on real *Kepler* light curves

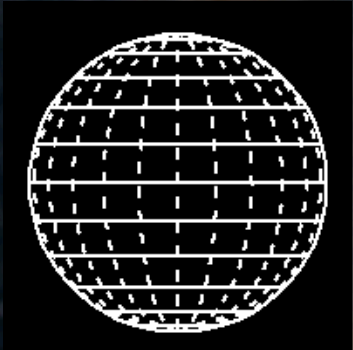


[Aigrain et al. Subm.]

Method	% det	Noisy % good	% ok	% det	Noise-free % good	% ok	solar No. det	No. ok
Blind teams								
Reinhold (Periodogram)	82	67	76	87	65	77	4	2
Nielsen (Periodogram)	16	100	100	15	100	100	0	0
Natal (Periodogram / spot model)	27	69	76	72	80	85	5	2
Tel Aviv (ACF)	100	68	80	100	75	90	5	4
Imperial (ACF)	95	71	87	98	73	88	5	4
Non-blind teams								
Seattle (Periodogram)	68	81	88	75	84	90	0	0
CEA (Wavelets / ACF)	78	88	95	82	92	99	2	2

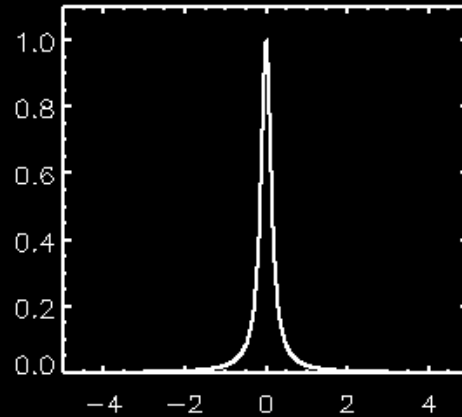
# II-INTERNAL ROTATION

$$\Omega = 0,0$$

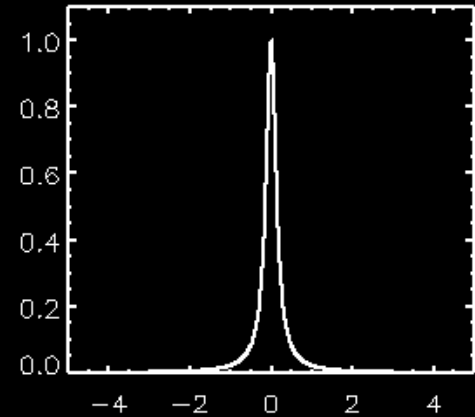


$$i = 90^\circ$$

$\ell=1$  mode



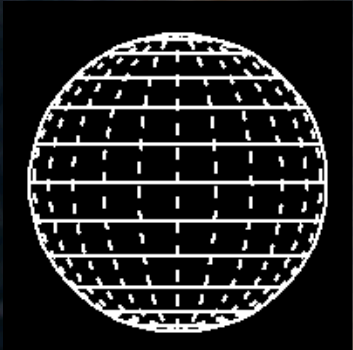
$\ell=2$  mode





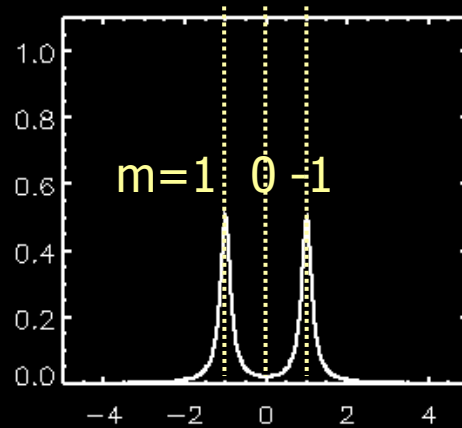
# II-INTERNAL ROTATION

$$\Omega = 1,0$$

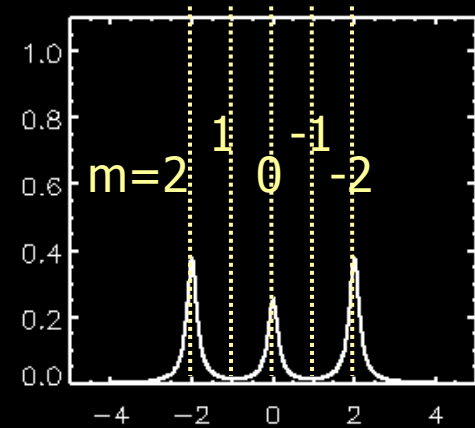


$$i = 90^\circ$$

$\ell=1$  mode

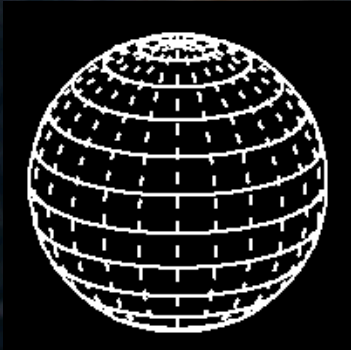


$\ell=2$  mode



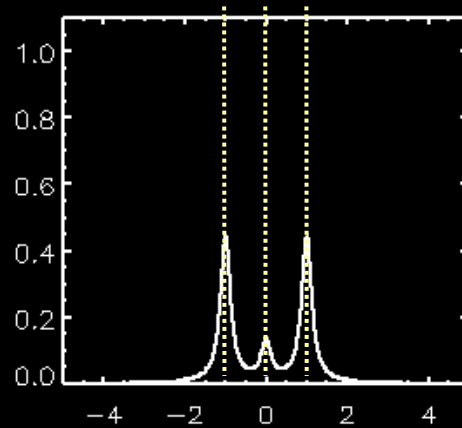
# II-INTERNAL ROTATION

$$\Omega = 1,0$$

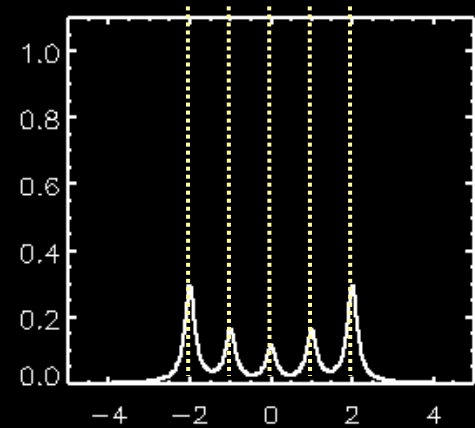


$$i = 70^\circ$$

$\ell=1$  mode



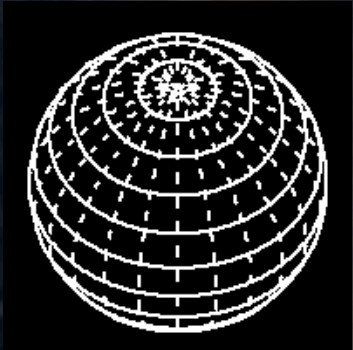
$\ell=2$  mode





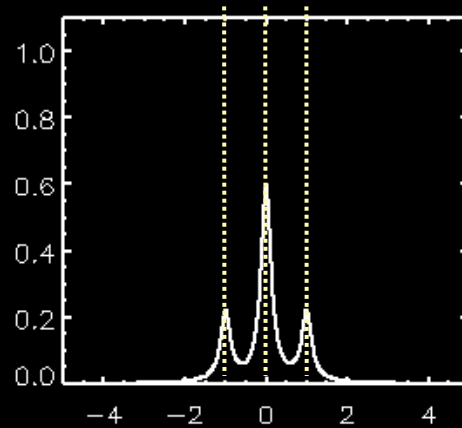
# II-INTERNAL ROTATION

$$\Omega = 1,0$$

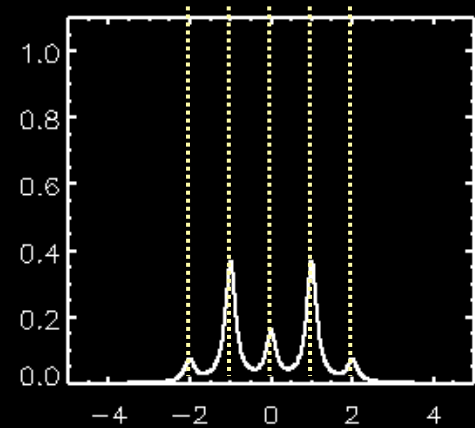


$$i = 40^\circ$$

$\ell=1$  mode

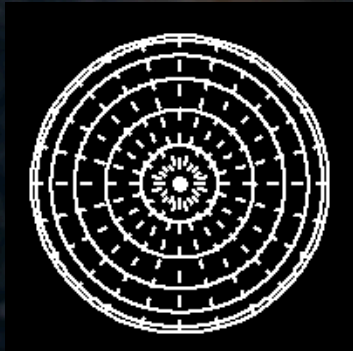


$\ell=2$  mode



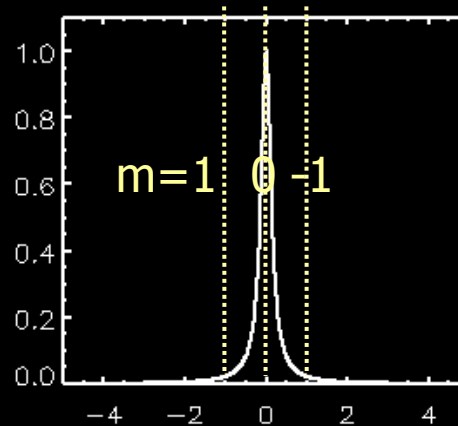
# II-INTERNAL ROTATION

$$\Omega = 1,0$$

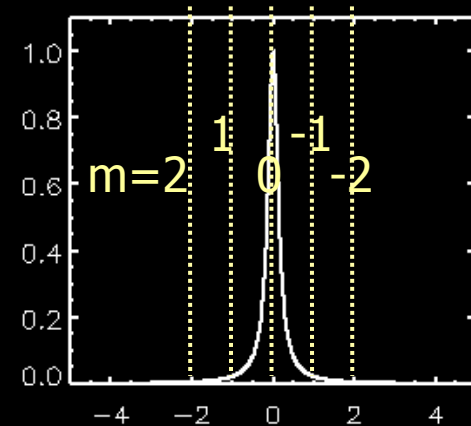


$$i = 0^\circ$$

$\ell=1$  mode



$\ell=2$  mode



## ➤ Strong correlation between angle and splitting

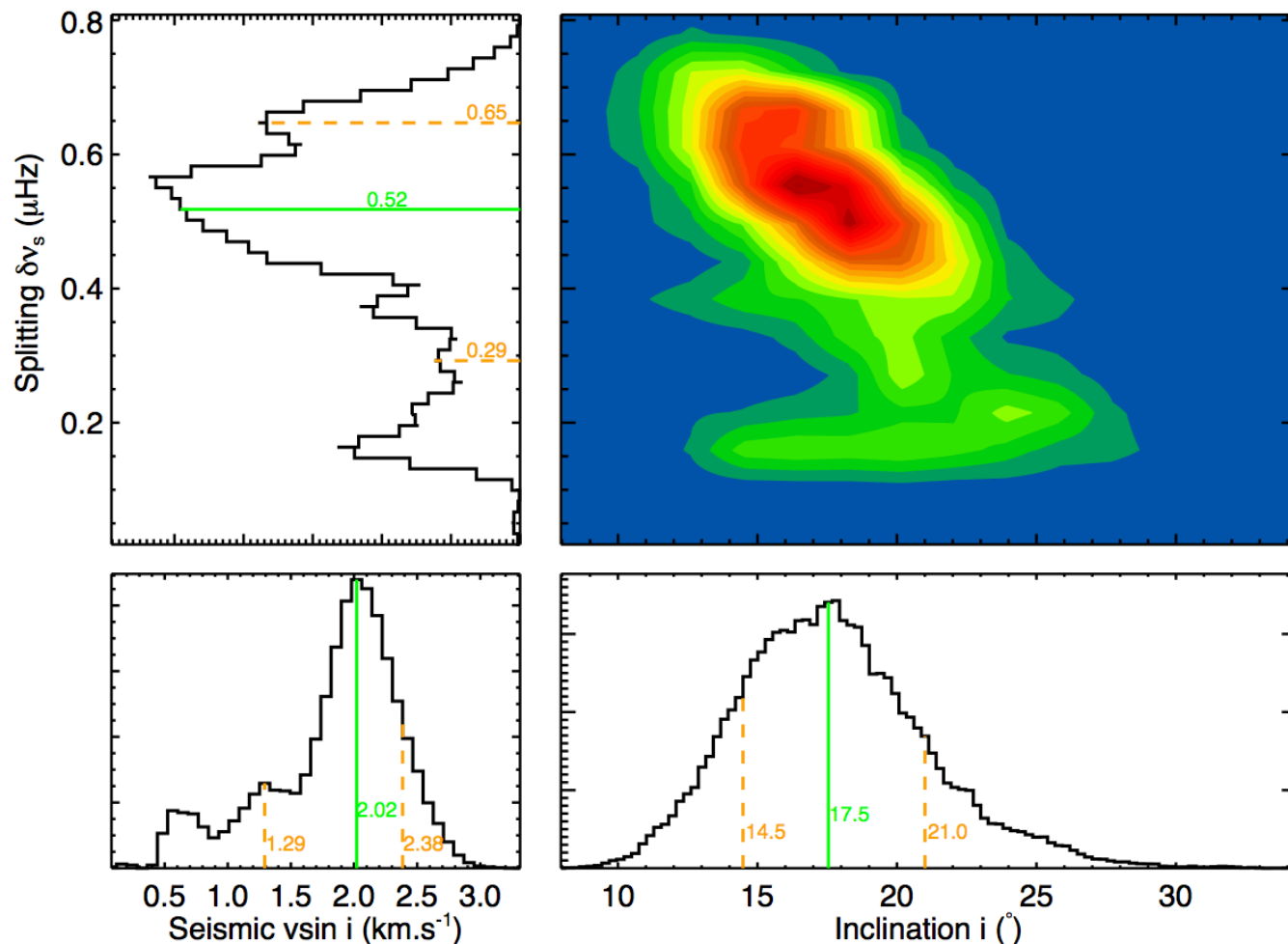
- We need to fit the stellar inclination angle and the rotational splitting together

[Ballot et al. 2006]

[Adapted from J. Ballot 2010]



# II-INTERNAL ROTATION (MS)



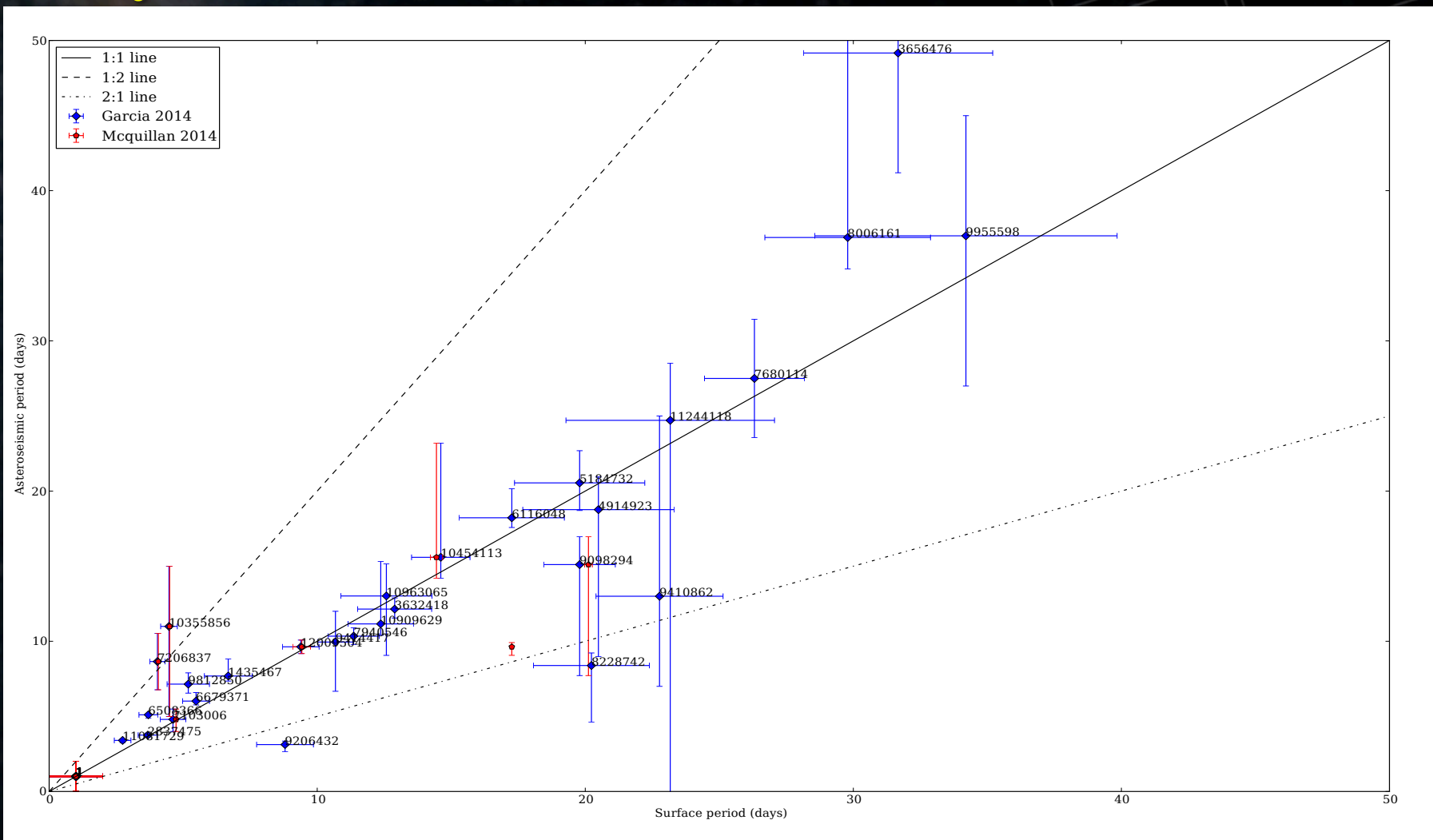
[García et al. 2014; see also Gizon et al. 2013; Davies et al. 2015, Benomar et al. submitted]

**Asteroseismic inclinations put constraints on star-planet systems dynamics**

[Chaplin et al. 2013 for some Kepler results on Kepler-50 and Kepler-65; Huber et al. 2013 for Kepler-56]

# III-VALIDATING $P_{\text{ROT}}$

## ➤ Using seismic inferences



## ➤ Inferred p-mode rotational splittings are a good proxy of surface rotation

[Davies, Garcia et al. in preparation]

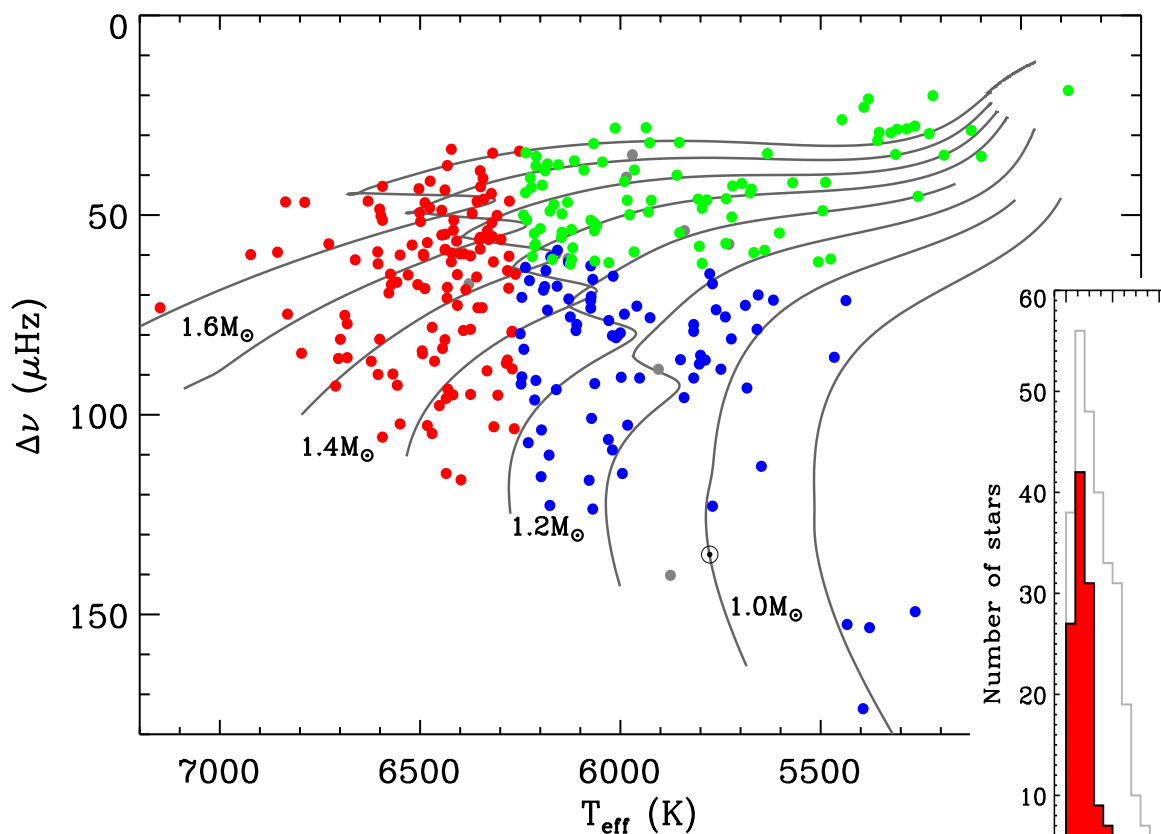
- Both inferences agree inside the error bars for most of the stars

[Lund et al. 2015; Benomar et al. in preparation]

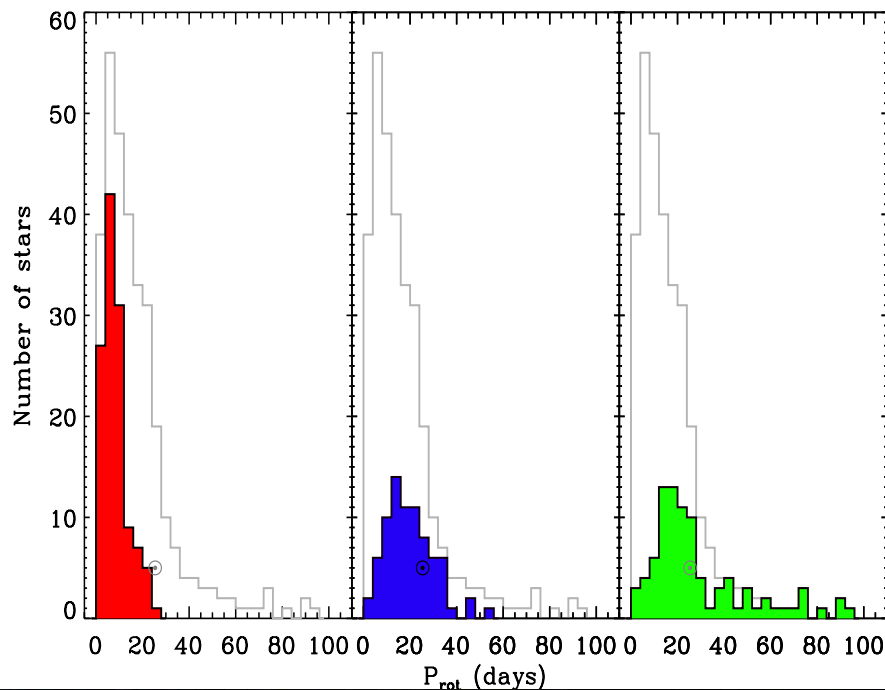


# II-SURFACE ROTATION (S-L STARS)

- ~540 solar-like stars showing p-mode oscillations have been measured (1 month) [Chaplin et al. 2014]
  - Reliable surface rotation rates and photospheric magnetic index obtained for 310 stars
- Stars in which pulsations are measured
  - Low surface activity (biased sample) [Garcia et al. 2010; Chaplin et al. 2011]



[García et al 2014]

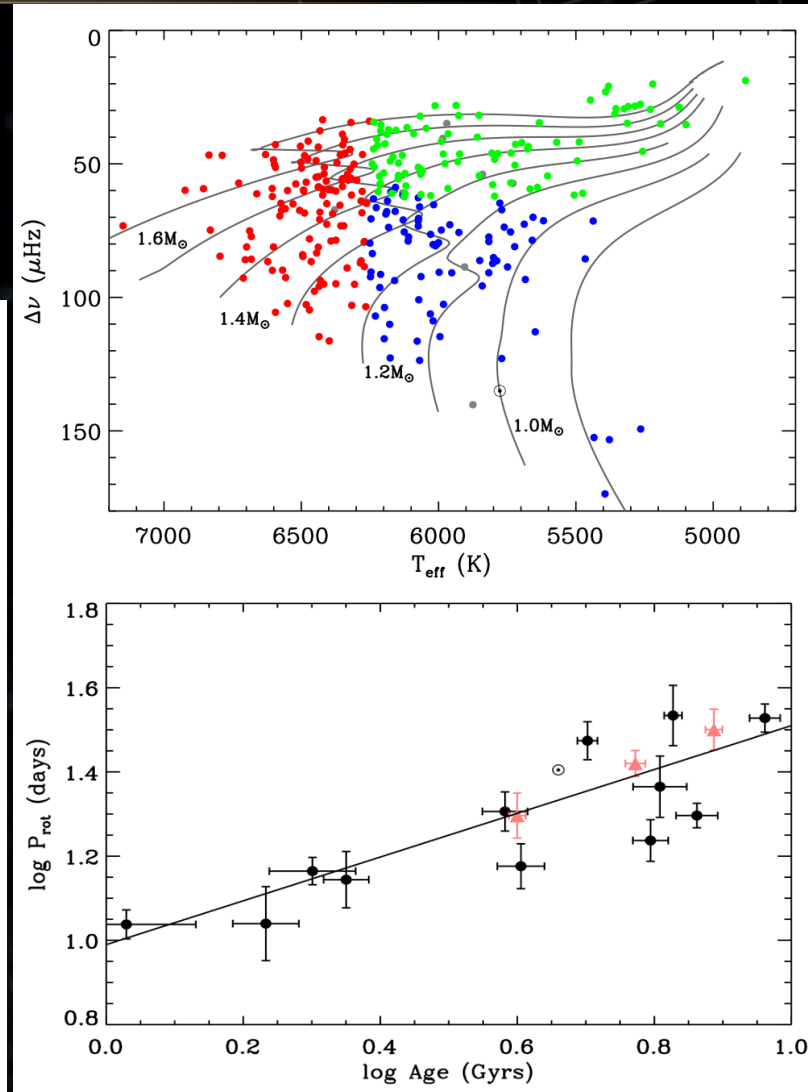
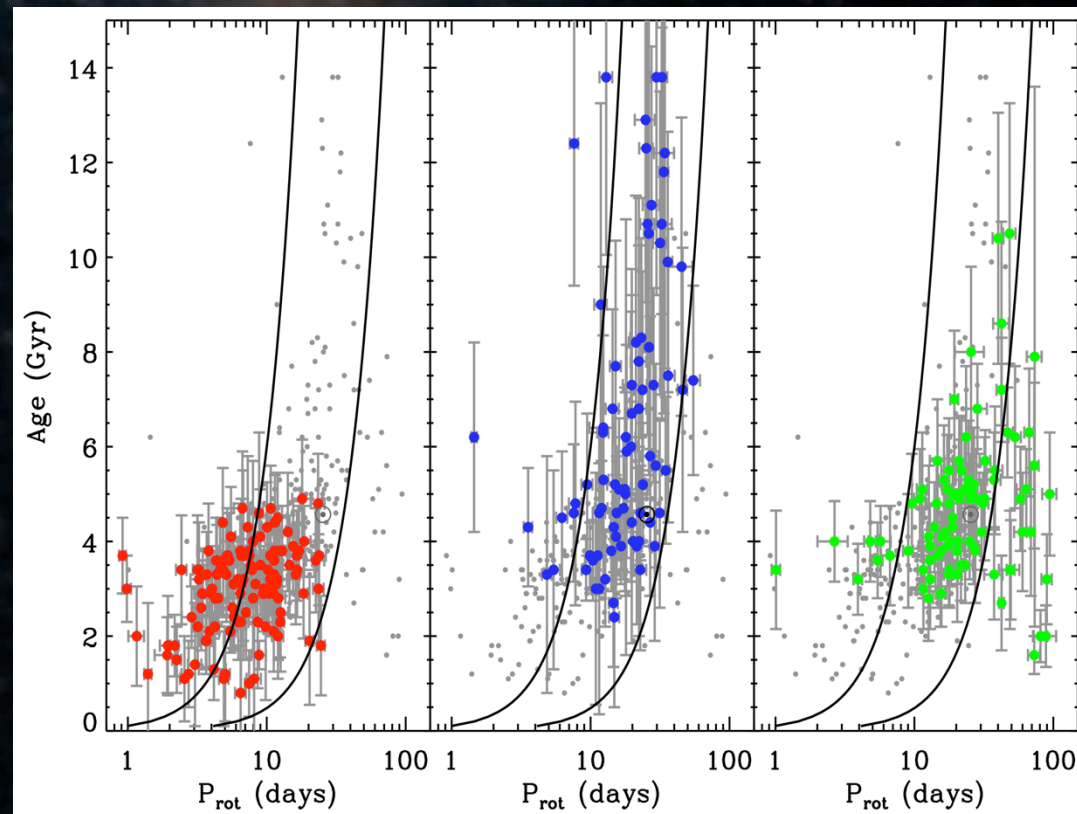


# II-SURFACE ROTATION

- Towards asteroseismically calibrated age-rotation relations. Gyrochronology of field stars

- Biased sample

[García et al. 2014]



$$\log P_{\text{rot}} = (0.52 \pm 0.06) \log(t) + (0.99 \pm 0.04).$$

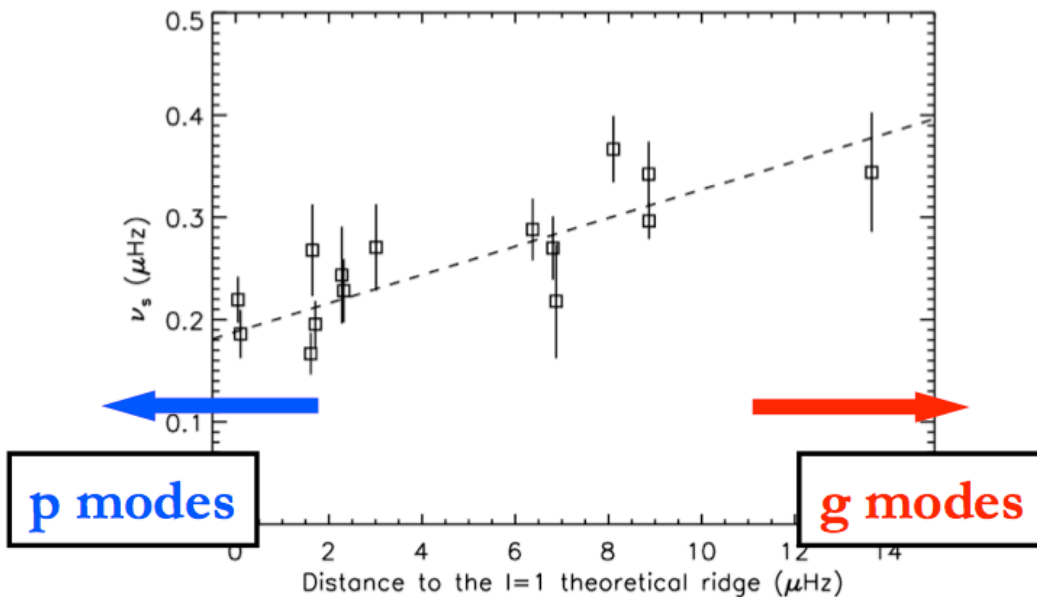
[Freqs from Appourchaux et al. 2012, models from Mathur et al. 2012 & Metcalfe et al. 2014]



# II-INTERNAL ROTATION

➤ Mixed modes allow us to study the internal dynamics

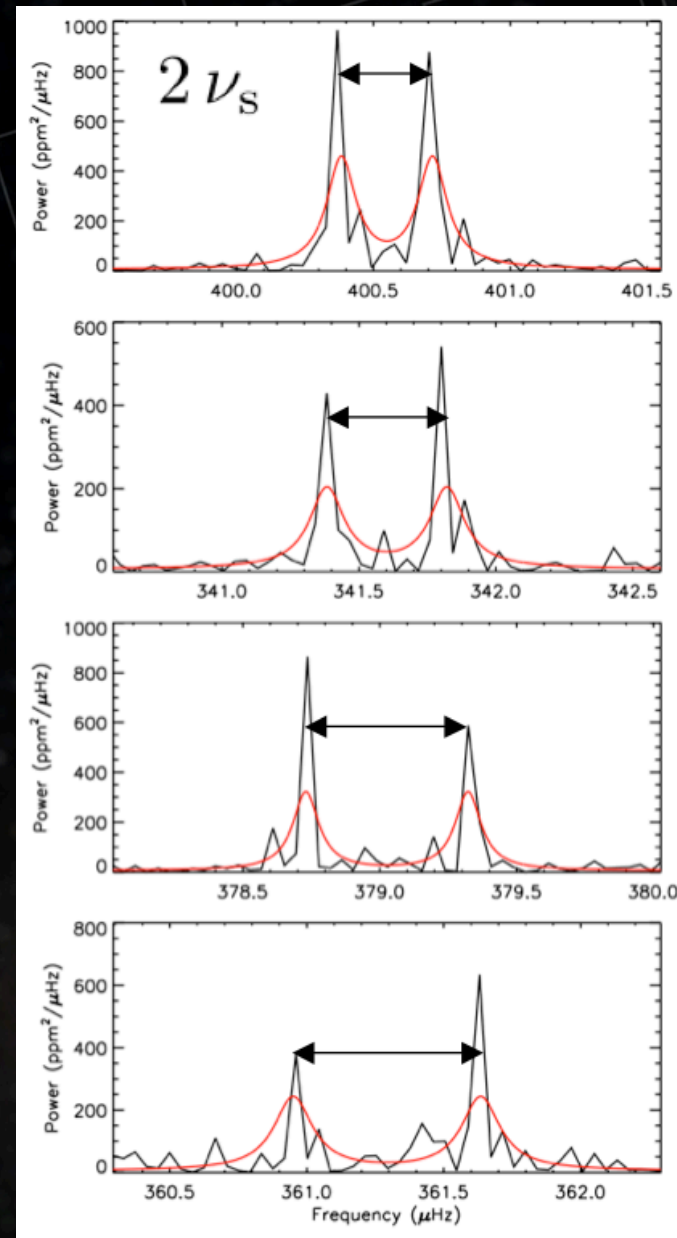
- g-dominated mixed modes:
  - Sensitive to the deep radiative interior
- P-dominated modes
  - Sensibility weighted towards the outer layers



suggests that  $\Omega_{\text{core}} > \Omega_{\text{surface}}$

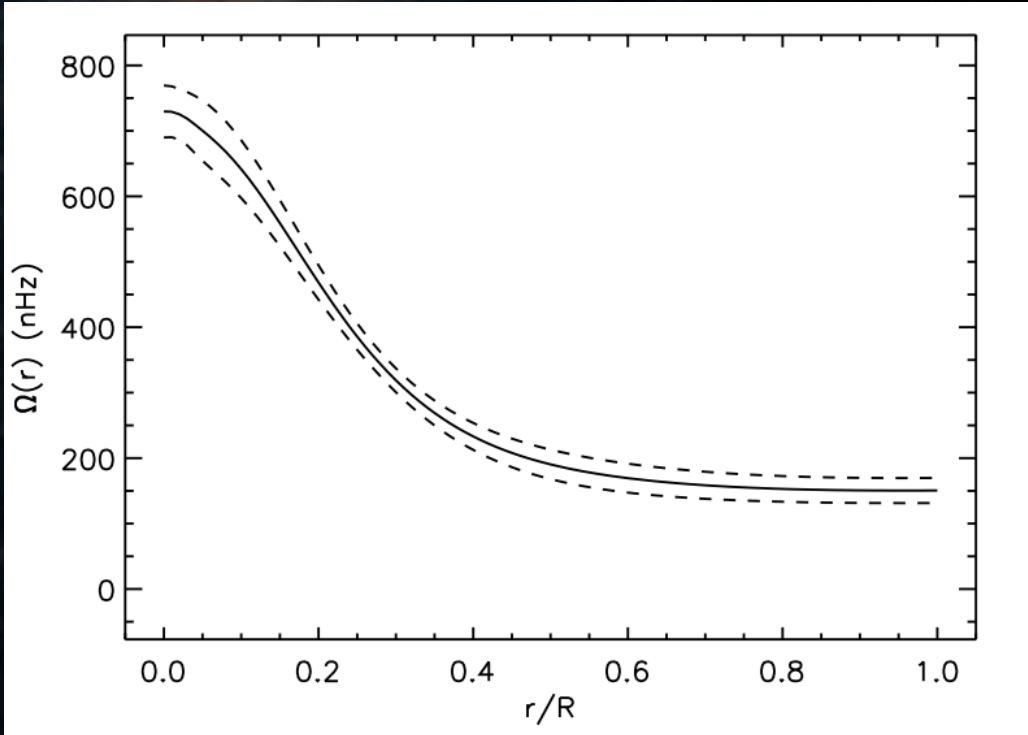
[Deheuvels, Garcia, et al. 2012]

see also Beck et al. 2012



# II-INTERNAL ROTATION (SUBGIANTS)

- Mixed modes allow us to study the internal dynamics
  - g-dominated mixed modes:
    - Sensitive to the deep radiative interior
  - P-dominated modes
    - Sensibility weighted towards the outer layers



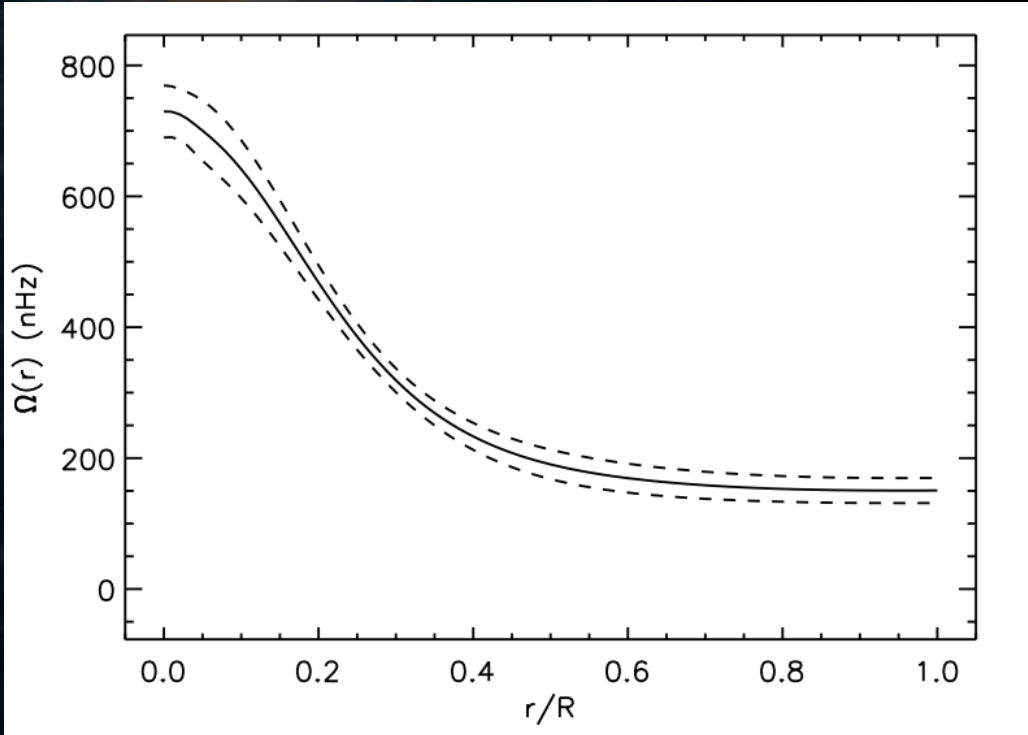
[Deheuvels, Garcia et al. 2012]



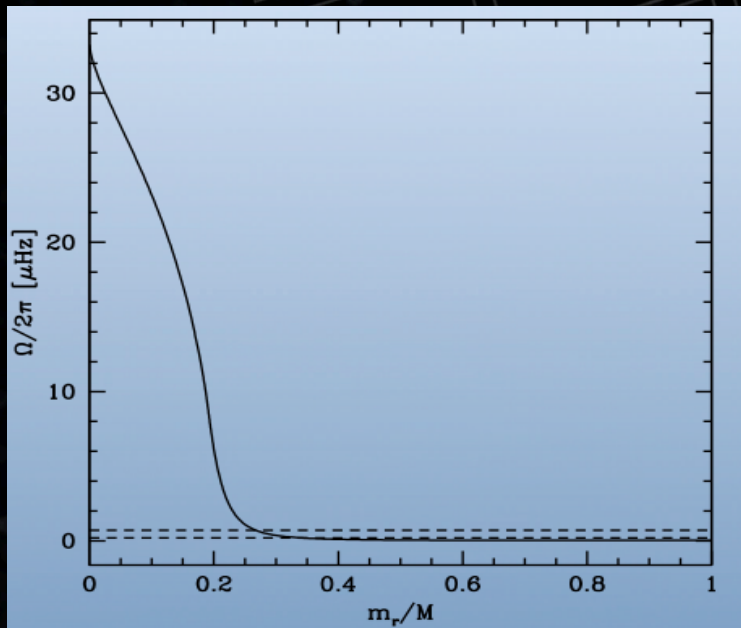
# II-INTERNAL ROTATION (SUBGIANTS)

➤ Mixed modes allow us to study the internal dynamics

- g-dominated mixed modes:
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- P-dominated modes
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[Deheuvels, Garcia et al. 2012]



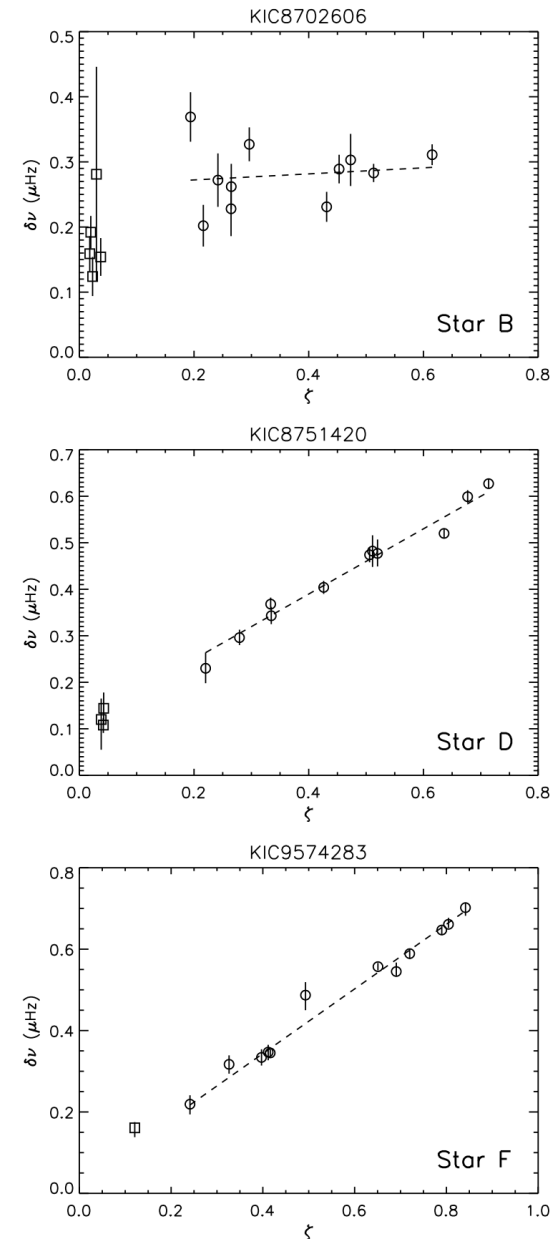
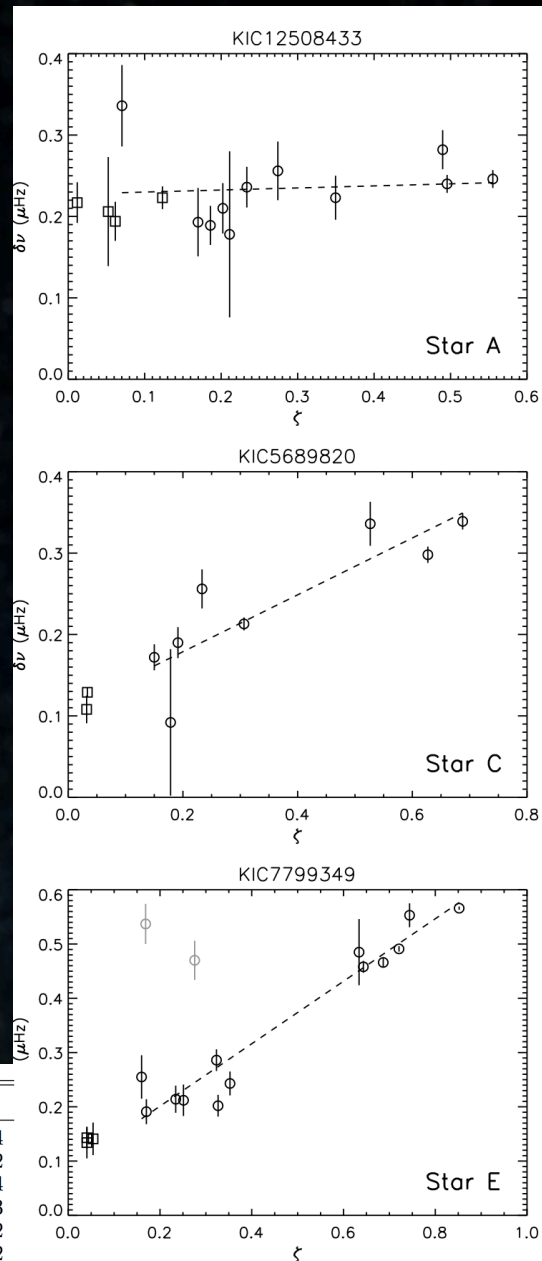
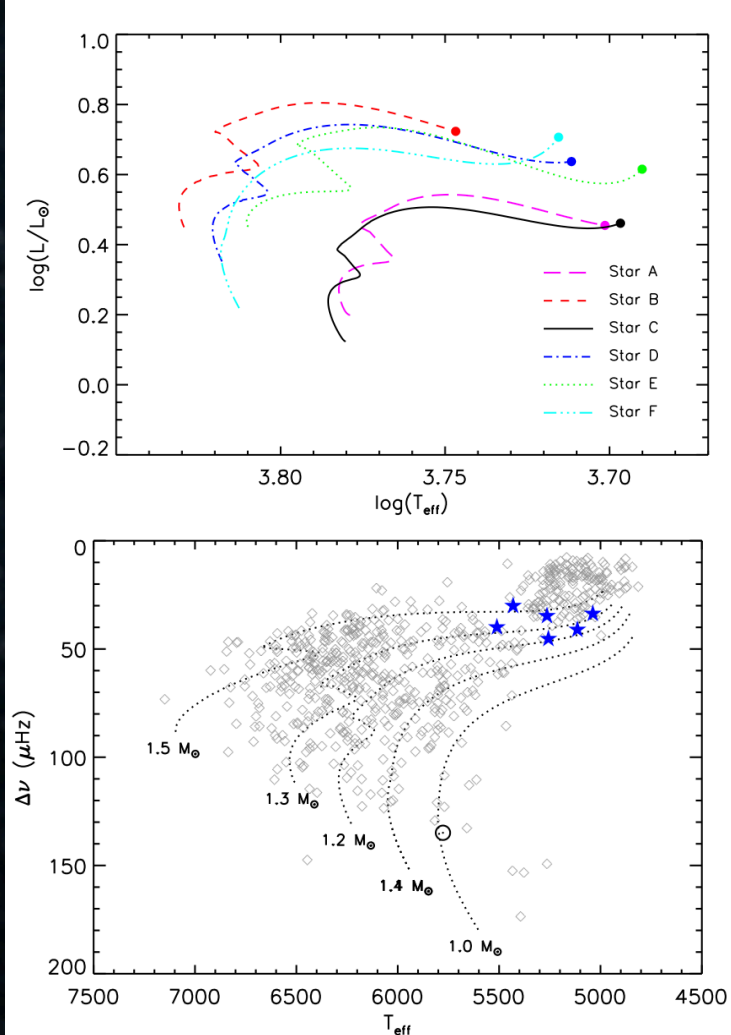
[Ceillier et al. 2013]

See also Eggenberger et al. 2012; Marques et al. 2013

# II-INTERNAL ROTATION (SUBGIANTS)

[Deheuvels et al. 2014]

## ➤ 6 Subgiant/early RGBs



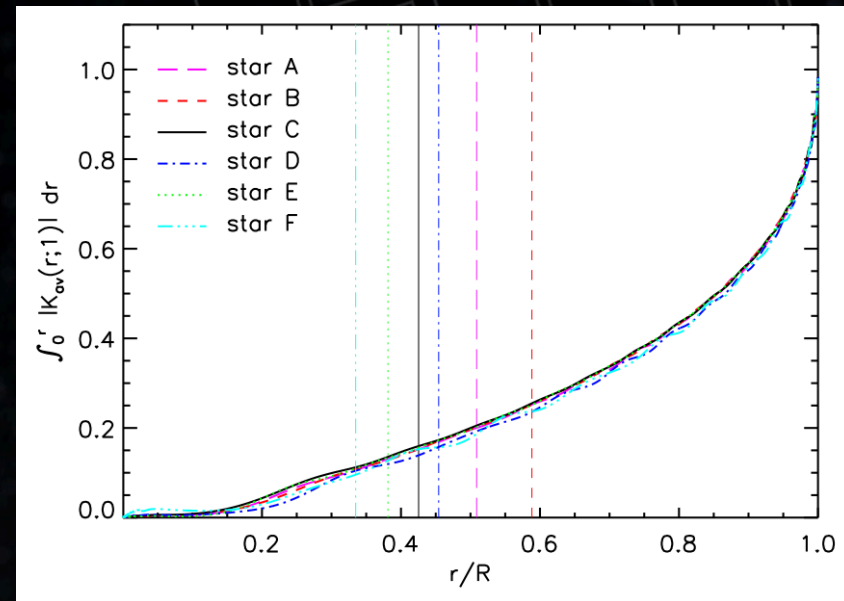
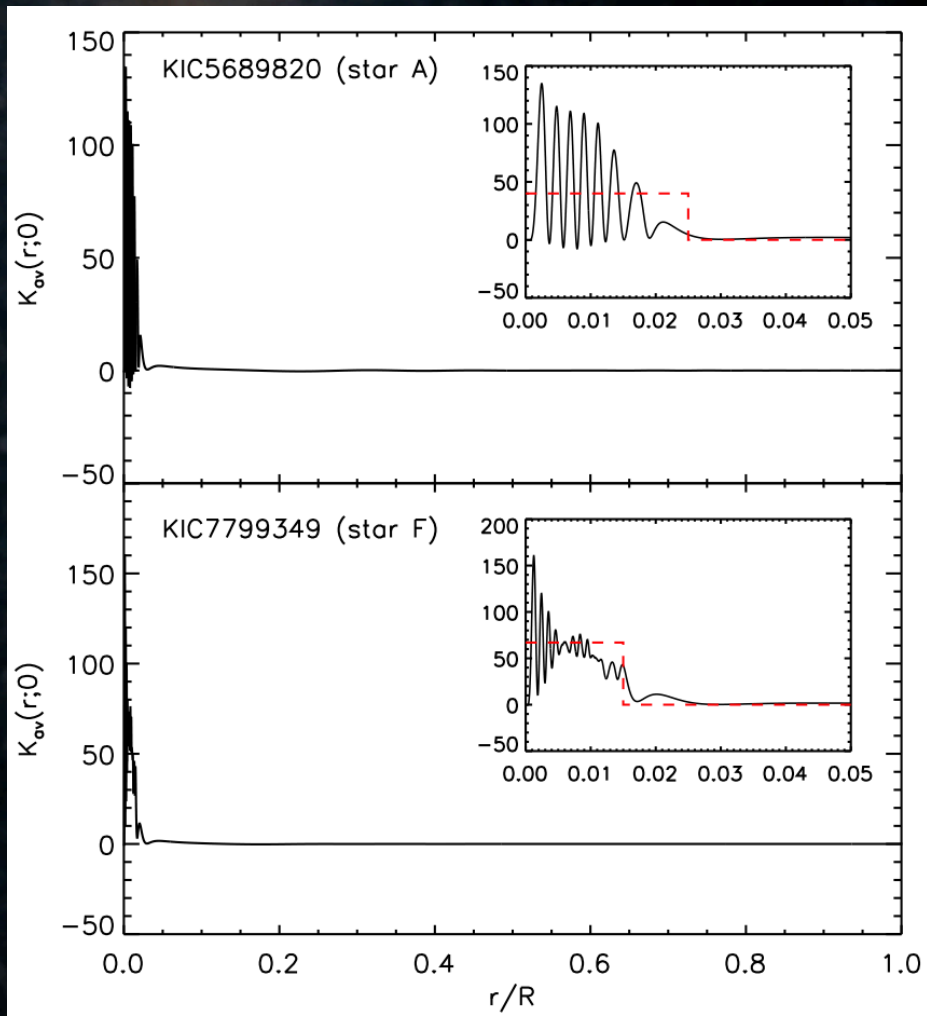
Star	Ref. letter	$\Delta\nu$ ( $\mu\text{Hz}$ )	$\nu_{\text{max}}$ ( $\mu\text{Hz}$ )	$M$	$R$	$\log g$
KIC12508433	A	$45.3 \pm 0.2$	$793 \pm 21$	$1.20 \pm 0.16$	$2.20 \pm 0.10$	$3.83 \pm 0.04$
KIC8702606	B	$39.9 \pm 0.4$	$664 \pm 14$	$1.27 \pm 0.15$	$2.44 \pm 0.11$	$3.77 \pm 0.02$
KIC5689820	C	$41.0 \pm 0.3$	$695 \pm 15$	$1.11 \pm 0.16$	$2.29 \pm 0.12$	$3.76 \pm 0.04$
KIC8751420	D	$34.7 \pm 0.4$	$598 \pm 14$	$1.50 \pm 0.20$	$2.83 \pm 0.15$	$3.71 \pm 0.03$
KIC7799349	E	$33.7 \pm 0.4$	$561 \pm 8$	$1.33 \pm 0.14$	$2.77 \pm 0.12$	$3.68 \pm 0.02$
KIC9574283	F	$30.0 \pm 0.5$	$455 \pm 8$	$1.24 \pm 0.17$	$2.92 \pm 0.17$	$3.60 \pm 0.02$



# II-INTERNAL ROTATION (SUBGIANTS)

[Deheuvels et al. 2014]

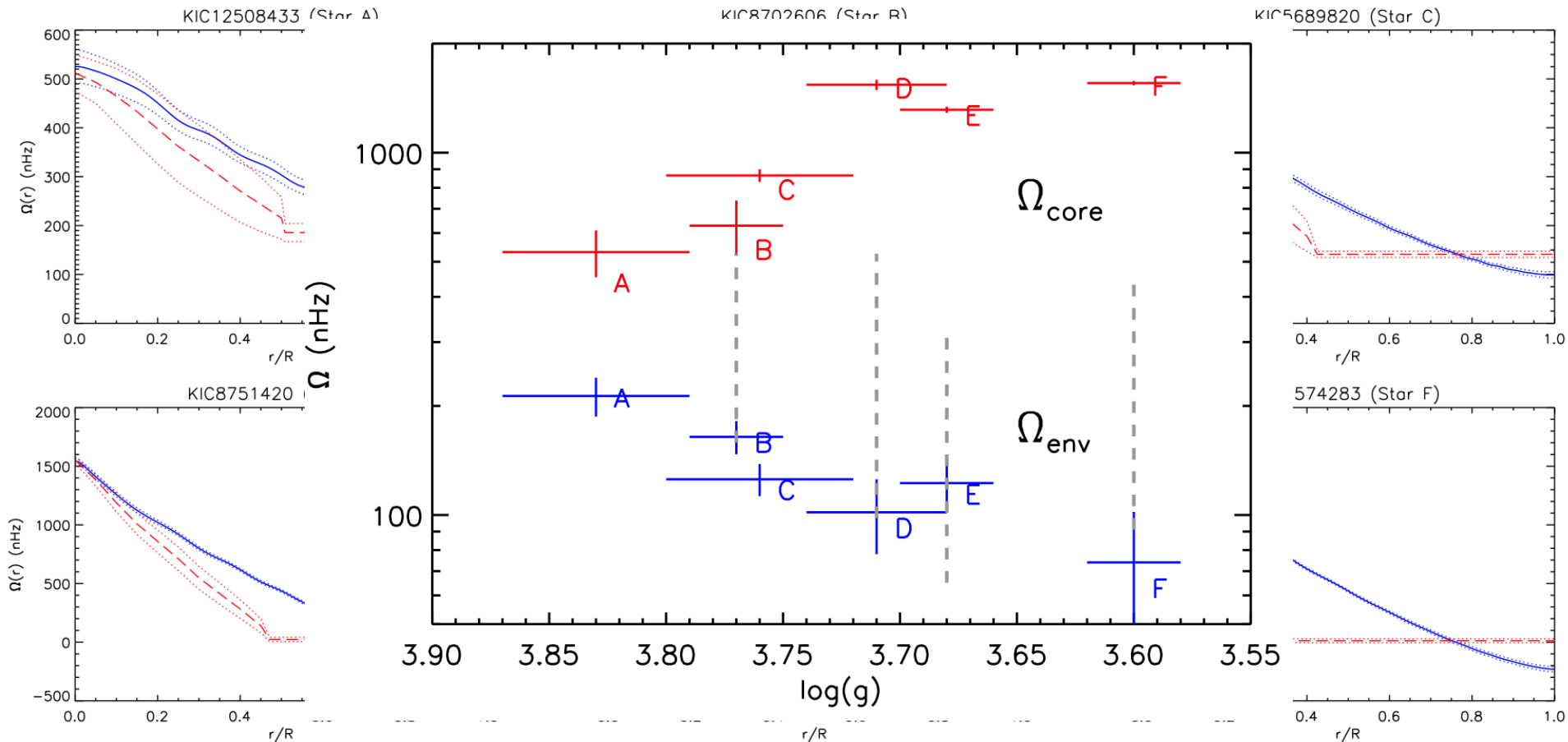
## ➤ 6 Subgiant/early RGBs



# II-INTERNAL ROTATION (SUBGIANTS)

[Deheuvels et al. 2014]

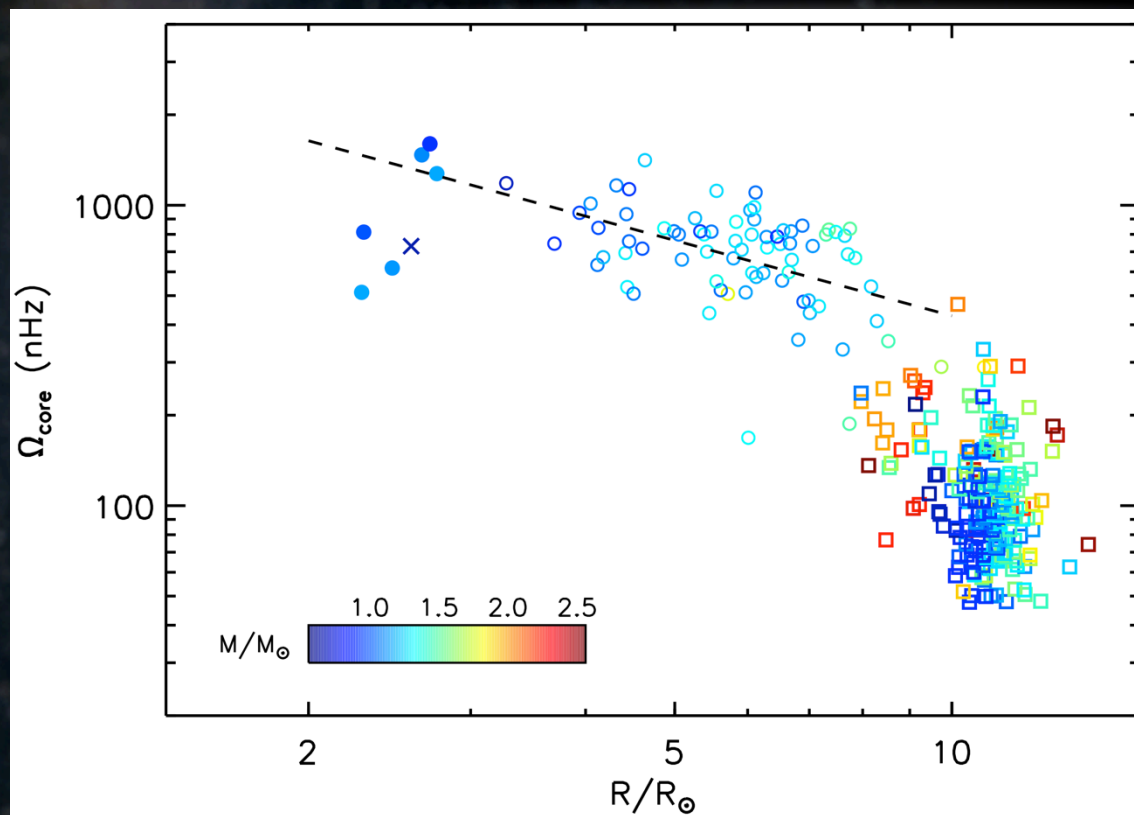
## ➤ 6 Subgiant/early RGBs



The trend with the seismic  $\log g$  suggests that the core spins in the subgiant phase



# II-INTERNAL ROTATION



[Mosser et al. 2012  
Filled circles from Deheuvels et al. 2014]

- Ensemble analysis used to obtain a proxy of the rotation rate of the deep radiative interior
- During RGB (circles):
  - The core of the stars during RGB spins down!
  - Efficient AM transport to counterbalance the core contraction and not efficient during subgiant phase
- Change from RGB to the clump (squares) can be related to the expansion of the non-degenerate helium burning core.
  - It can not explain all the reduction
    - significant transfer of internal angular momentum from the inner to the outer layers.

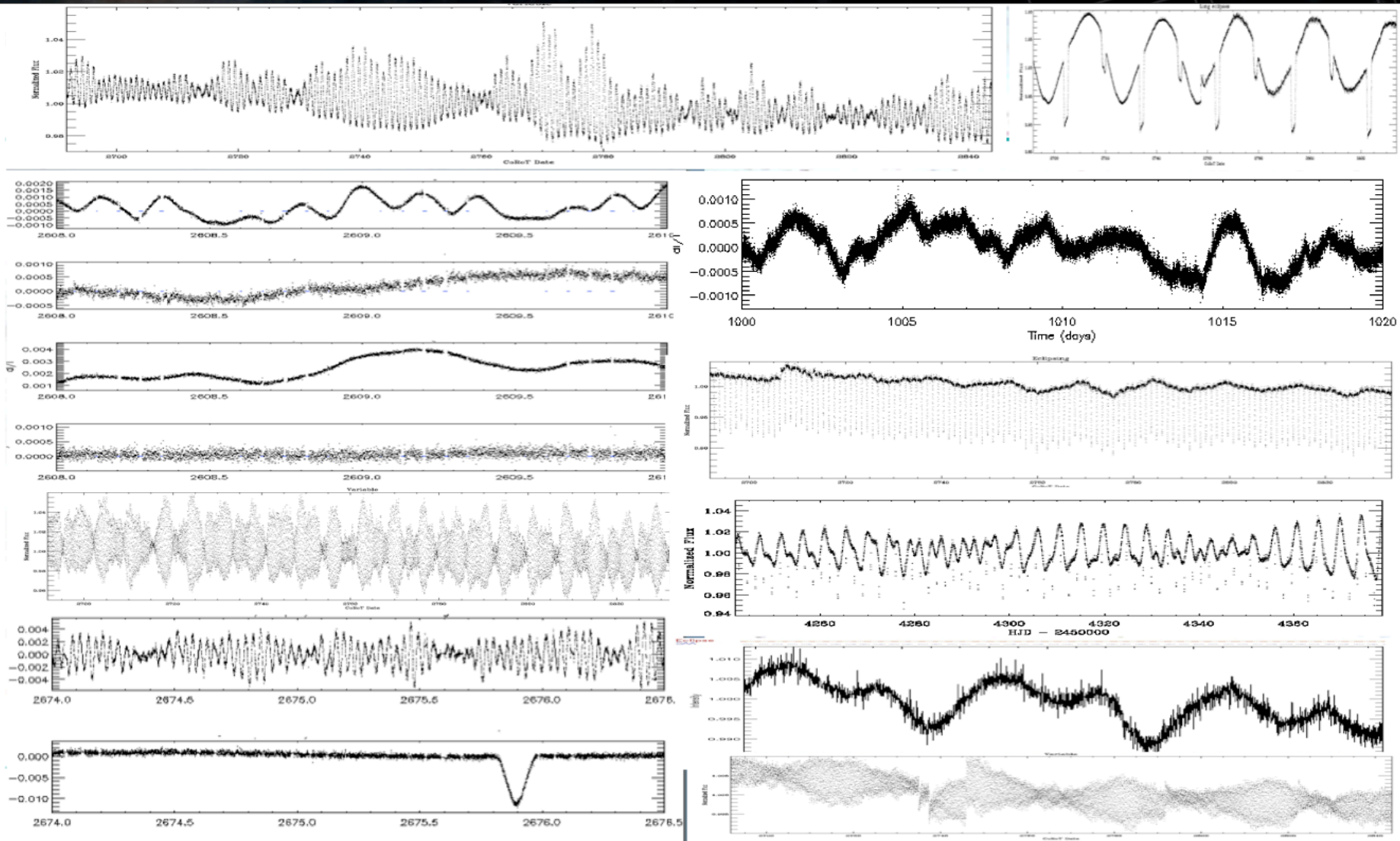
[Iben 1971; Sills & Pinsonneault 2000]

# I Ib-Stellar Dynamics:

## Magnetic variability



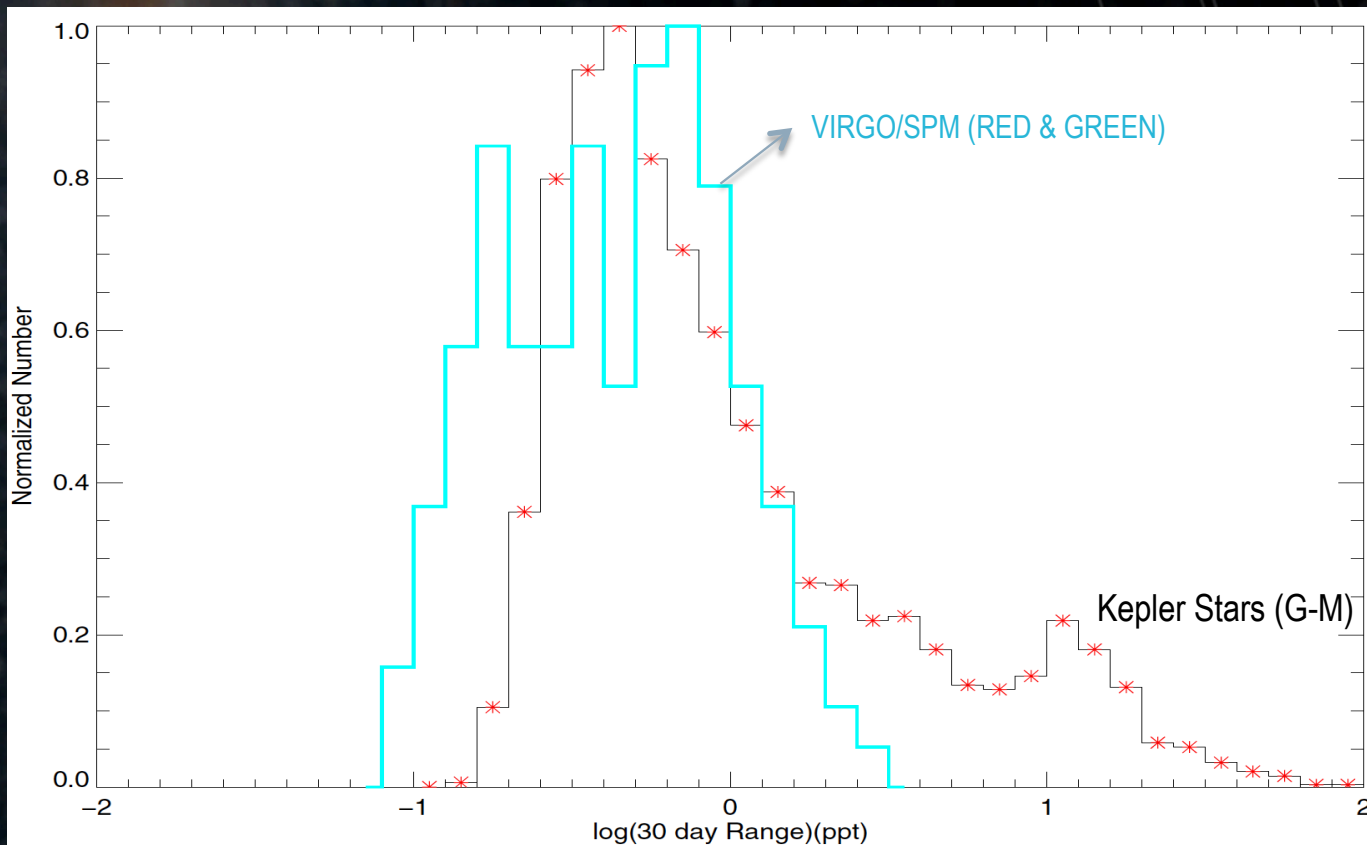
# II-STELLAR VARIABILITY



# II-STELLAR VARIABILITY

## ➤ To study the photometric variability of a star:

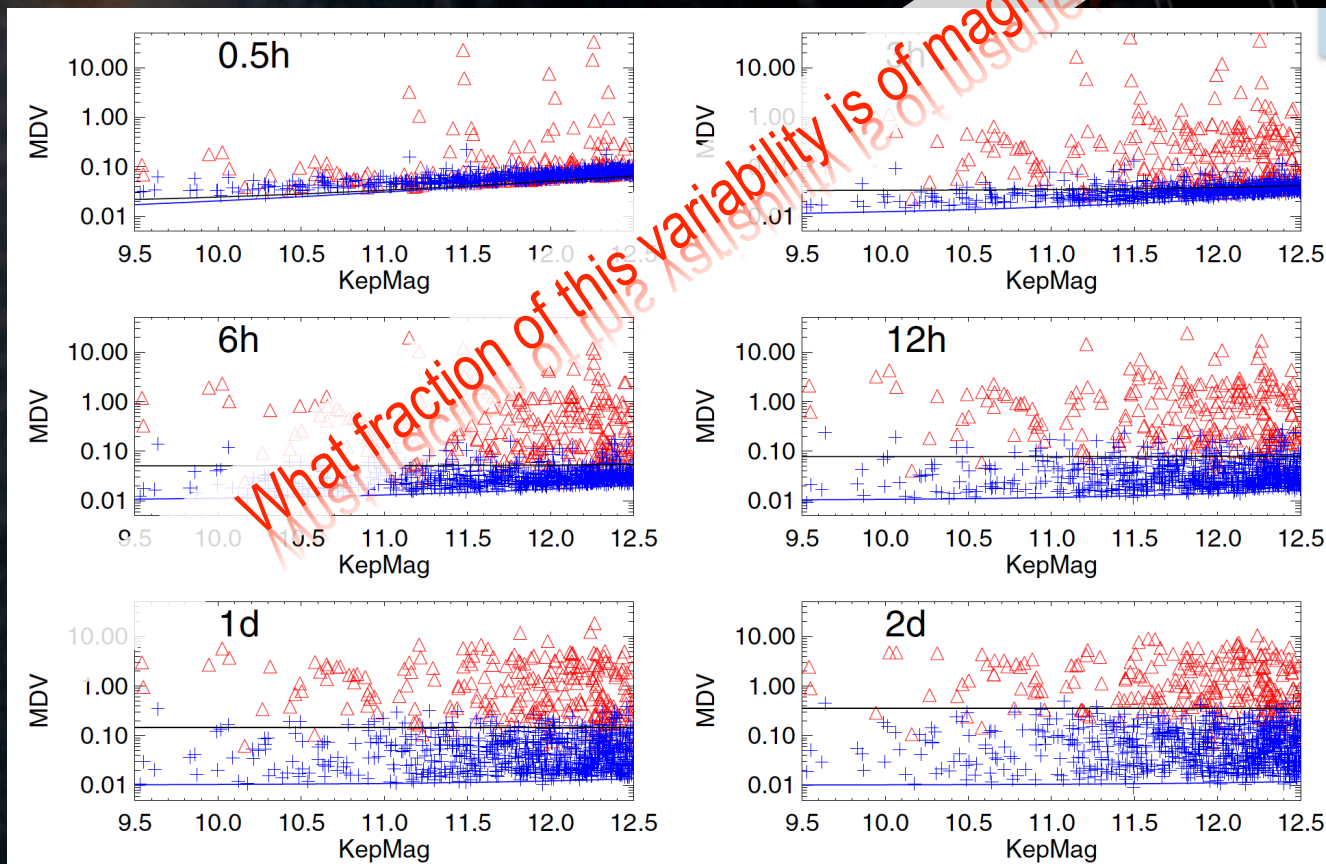
- It is common to parameterize it at a given time
  - E.g. MDV ( $t_{\text{bin}}$ ) (Median Differential Variability), Range, etc
    - Median of the bin-to-bin variability for bins of a given timescale  $t_{\text{bin}}$
  - This methodology is good to compare variability of stars at different timescales



# II-STELLAR VARIABILITY

## ➤ To study the photometric variability of a star:

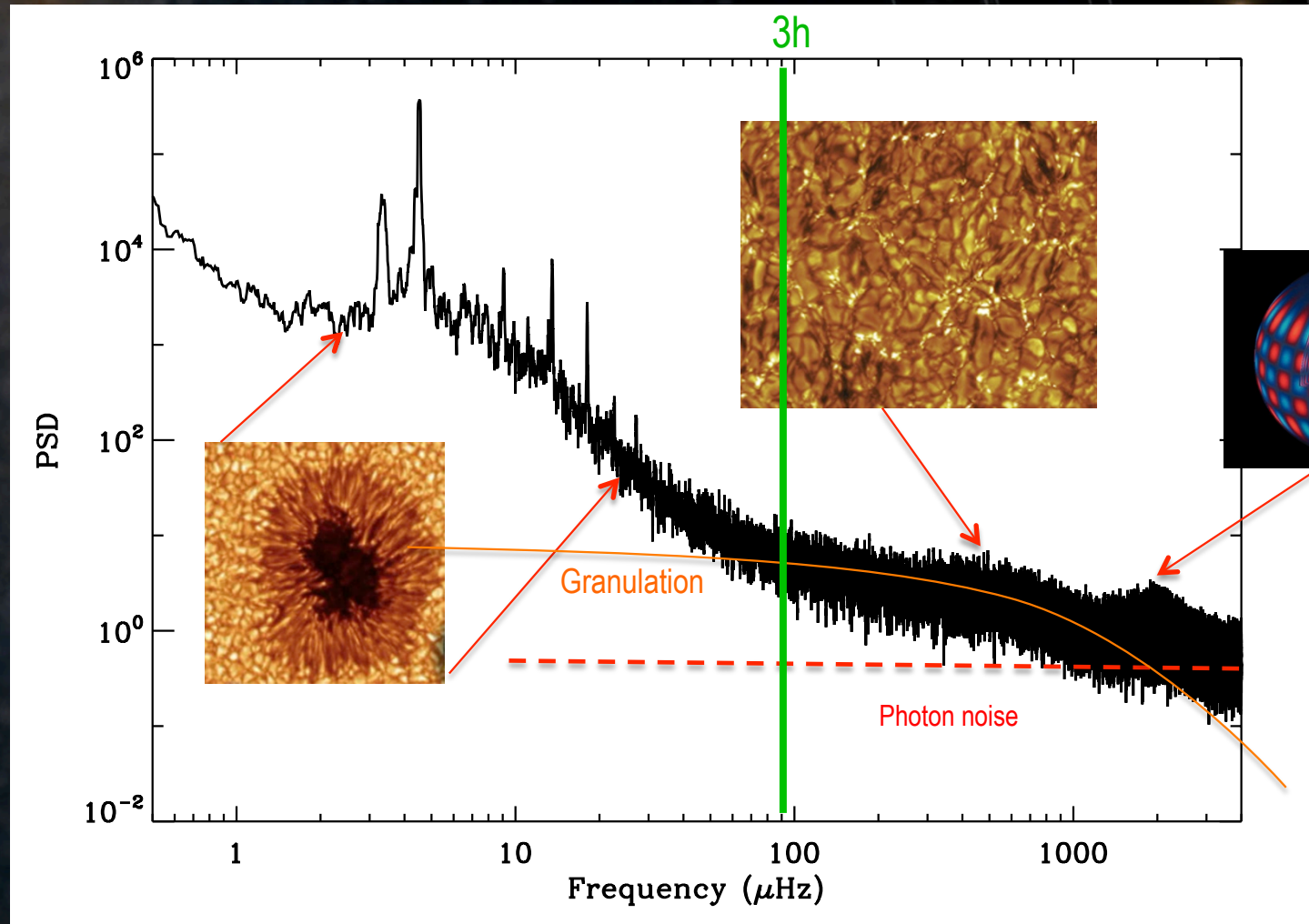
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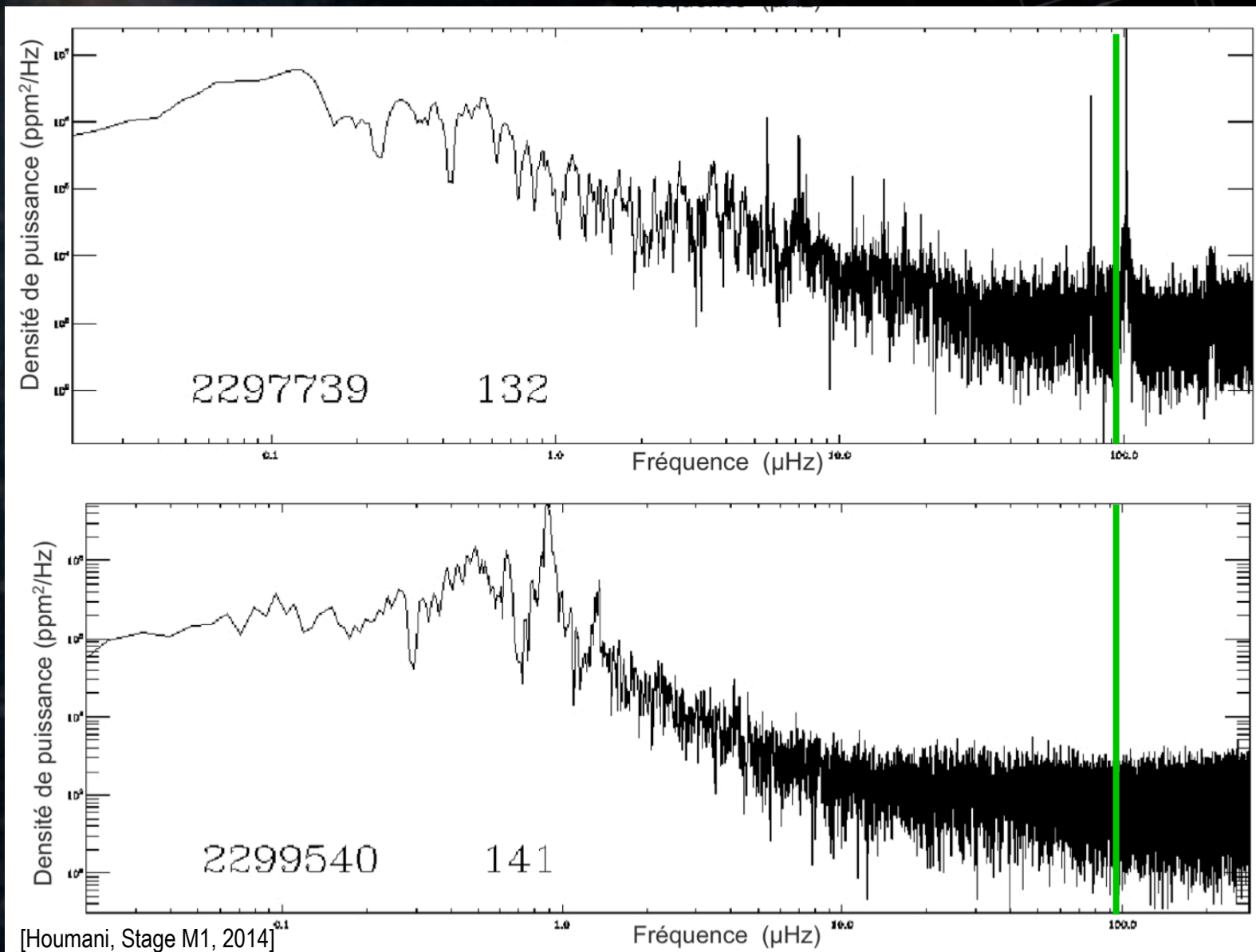
# II-STELLAR VARIABILITY

- Example of the PSD of a Solar-Like star



# II-STELLAR VARIABILITY

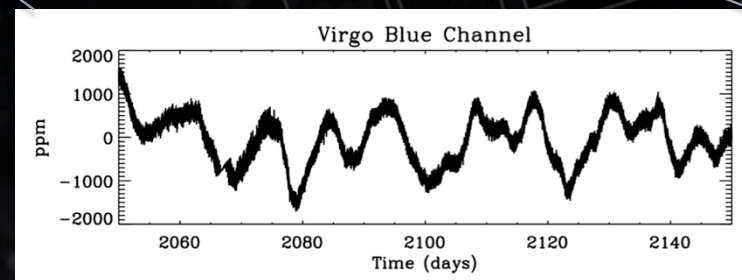
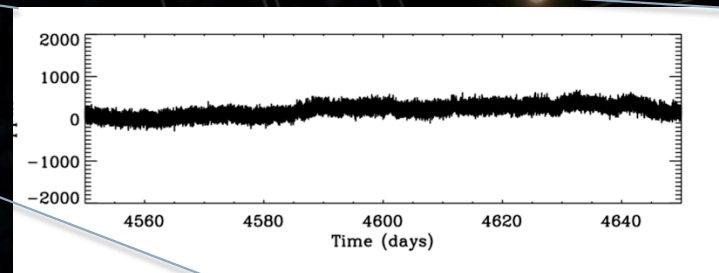
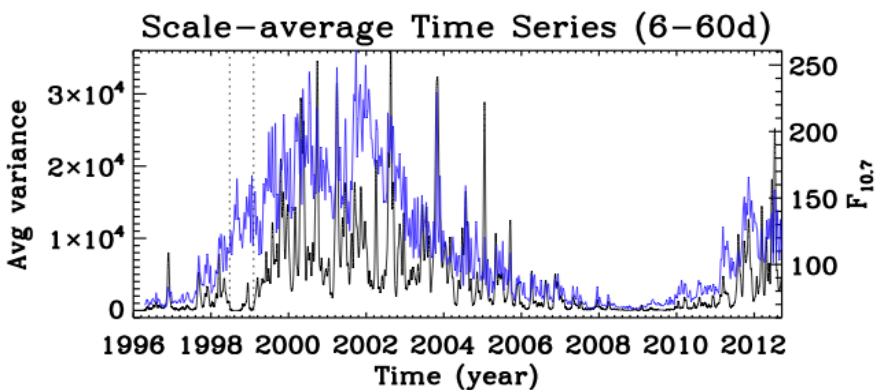
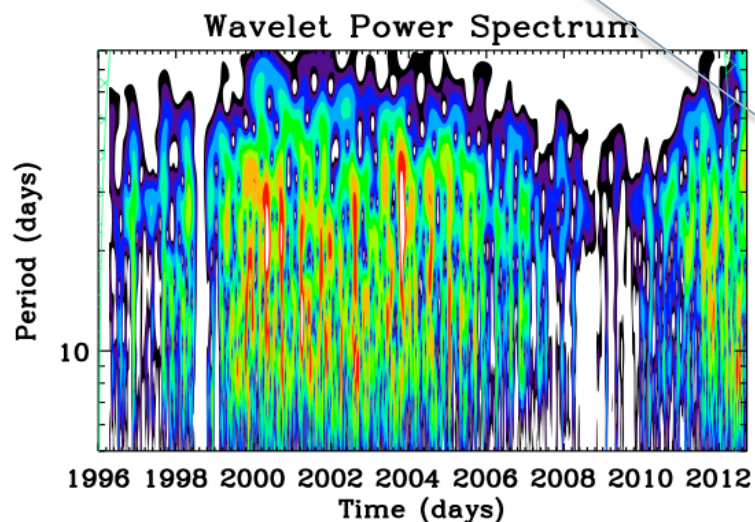
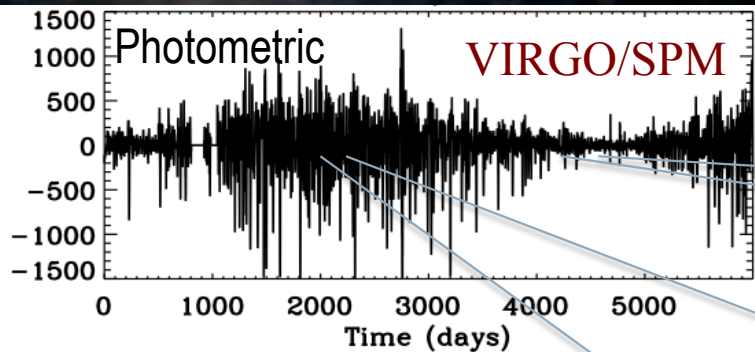
- Example of other type of pulsators (F, M)



# III-Surface Magnetic Activity proxy



# II-MAGNETIC ACTIVITY & ROTATION



[García, Salabert, Mathur et al. 2013]

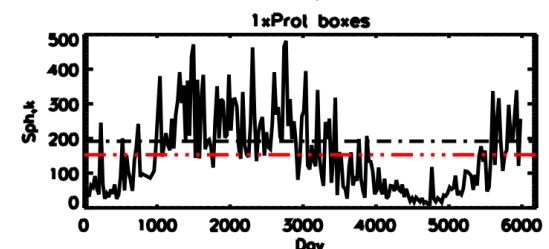
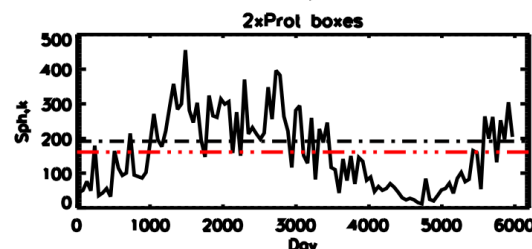
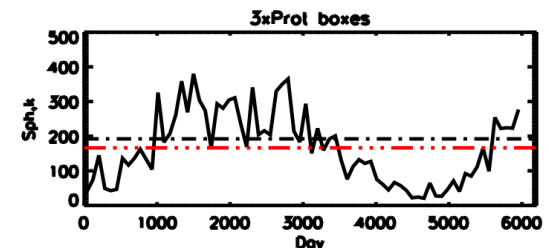
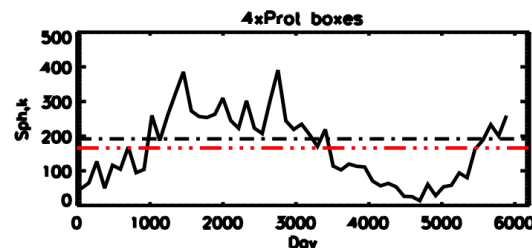
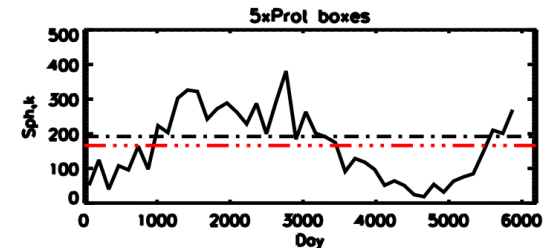
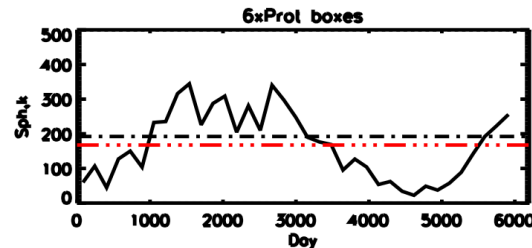
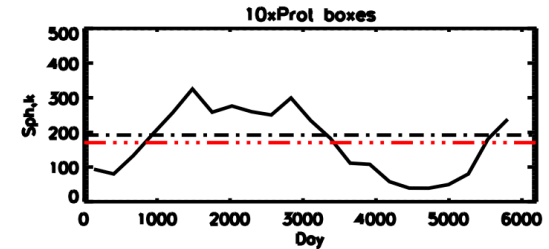
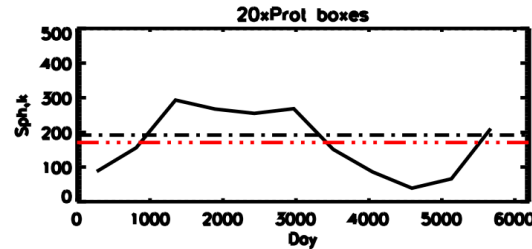
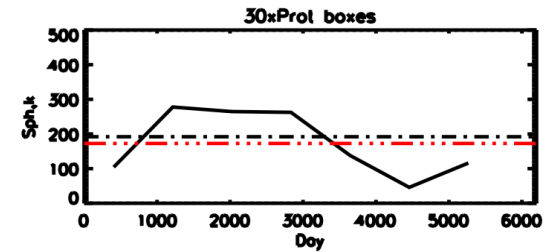
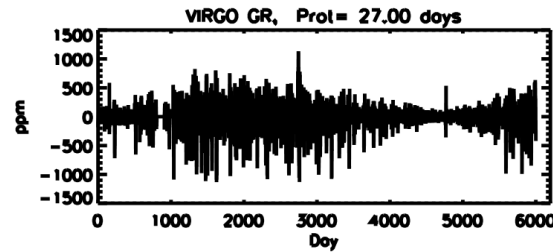
➤  $S_{ph}$

- Standard deviation  
of the light curve

[García et al. 2010; Chaplin et al. 2011;  
Campante et al. 2013]

- $K \times P_{rot}$ 
  - In general  $k=5$

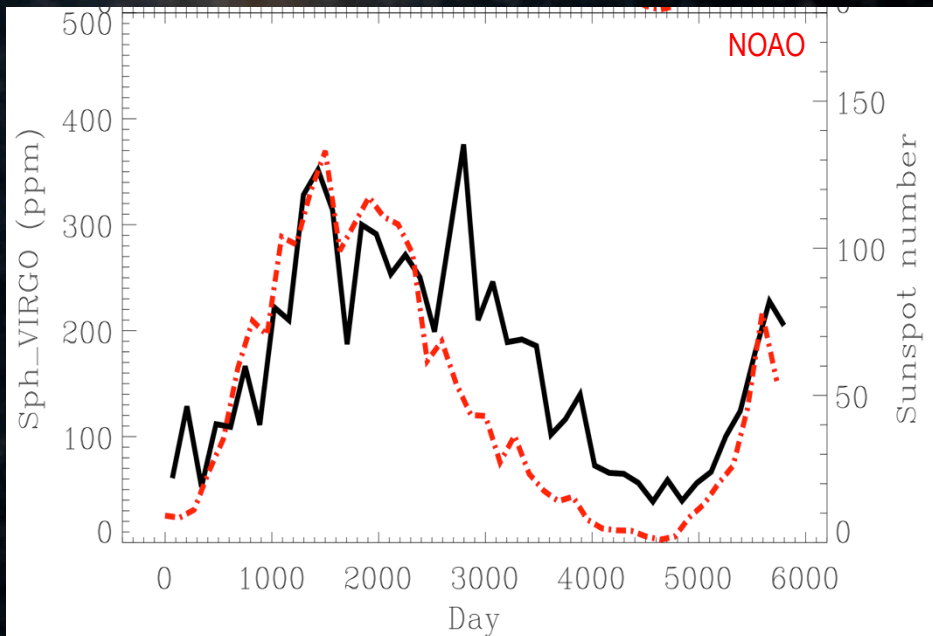
[Mathur, Salabert, García, et al. 2014]



# III-SURFACE MAGNETIC ACTIVITY PROXY

## ➤ Solar $S_{ph}$ (VIRGO/SPM)

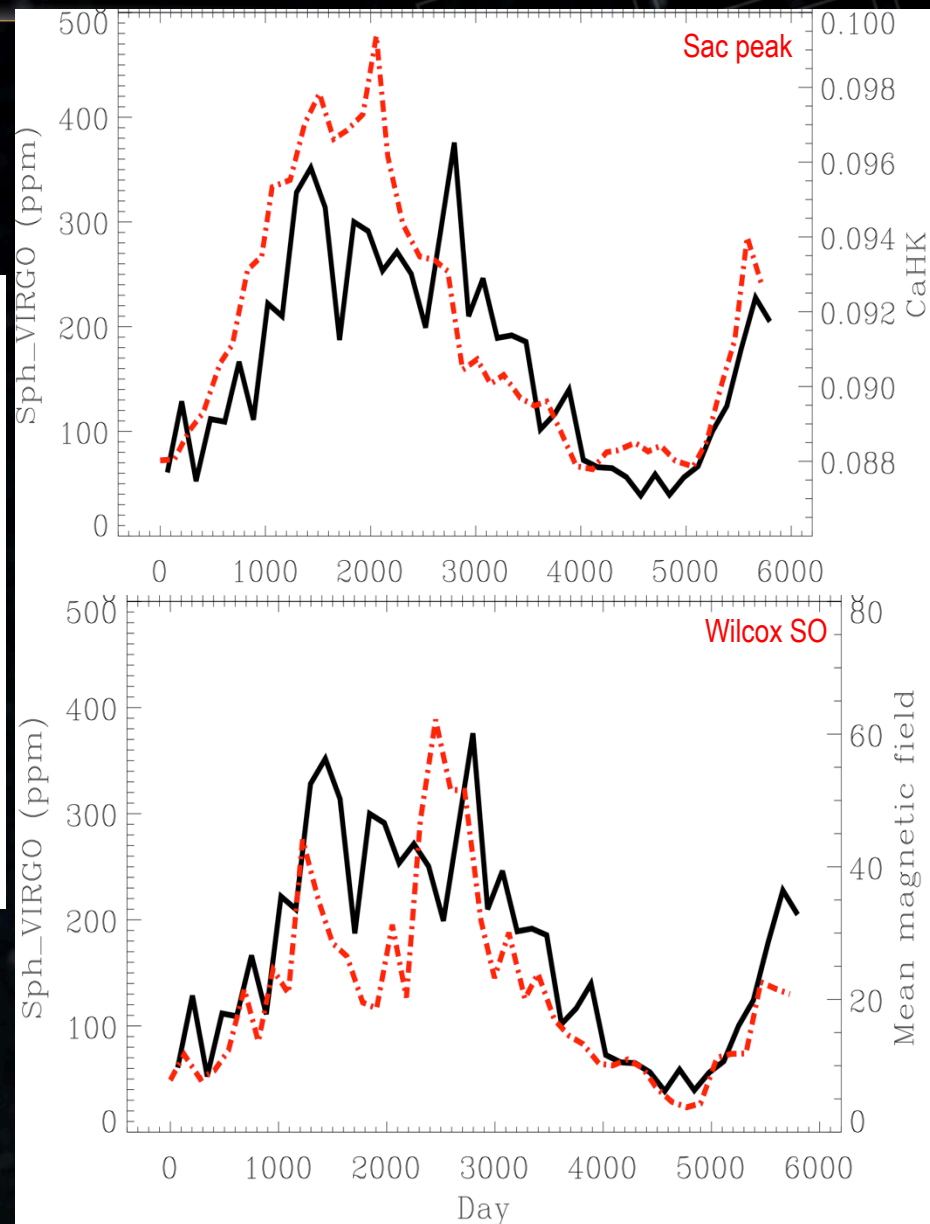
- Comparison with other solar indexes



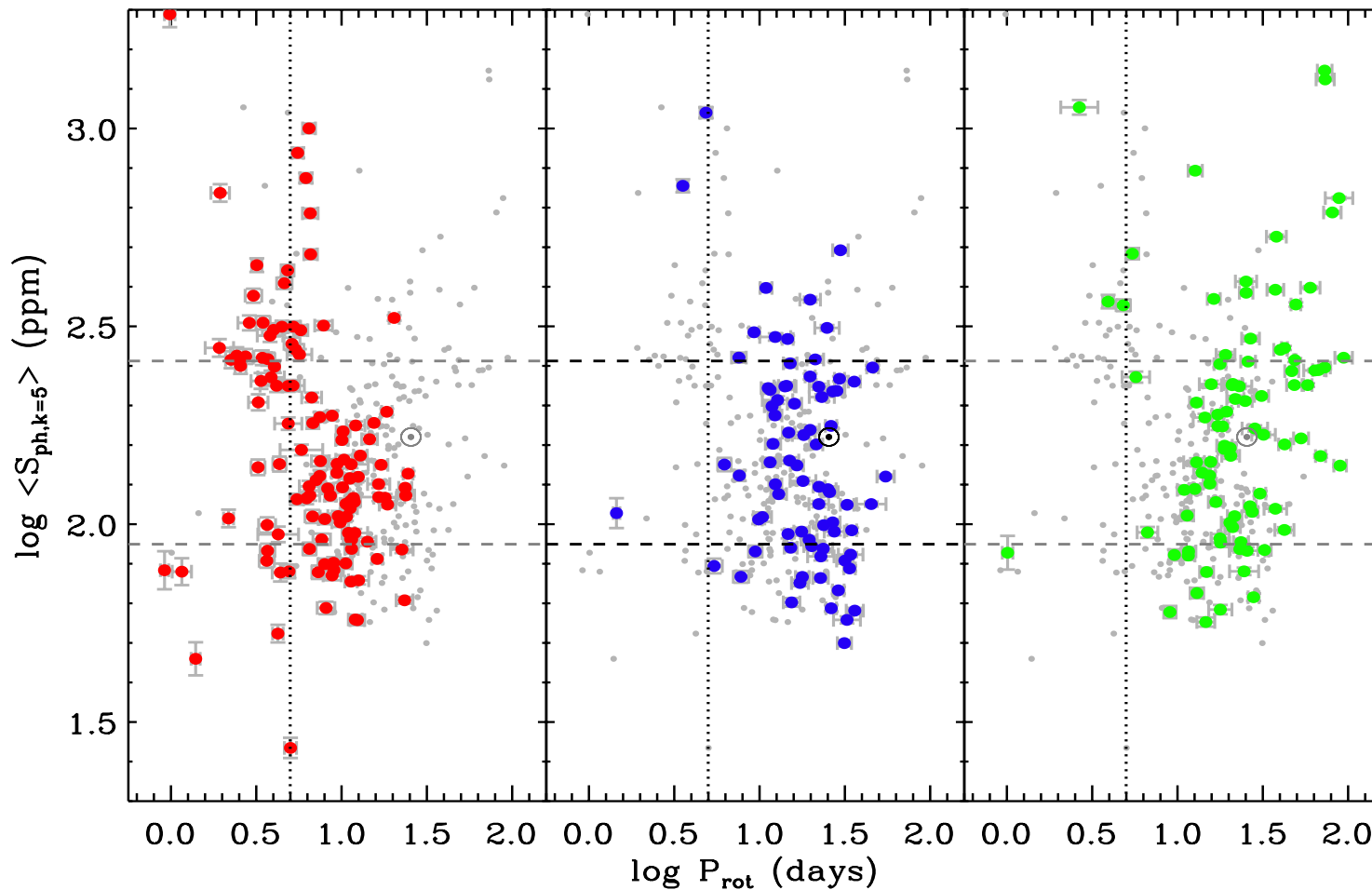
GOLF proxy also available



[Salabert, García, Roth, et al. in prep]







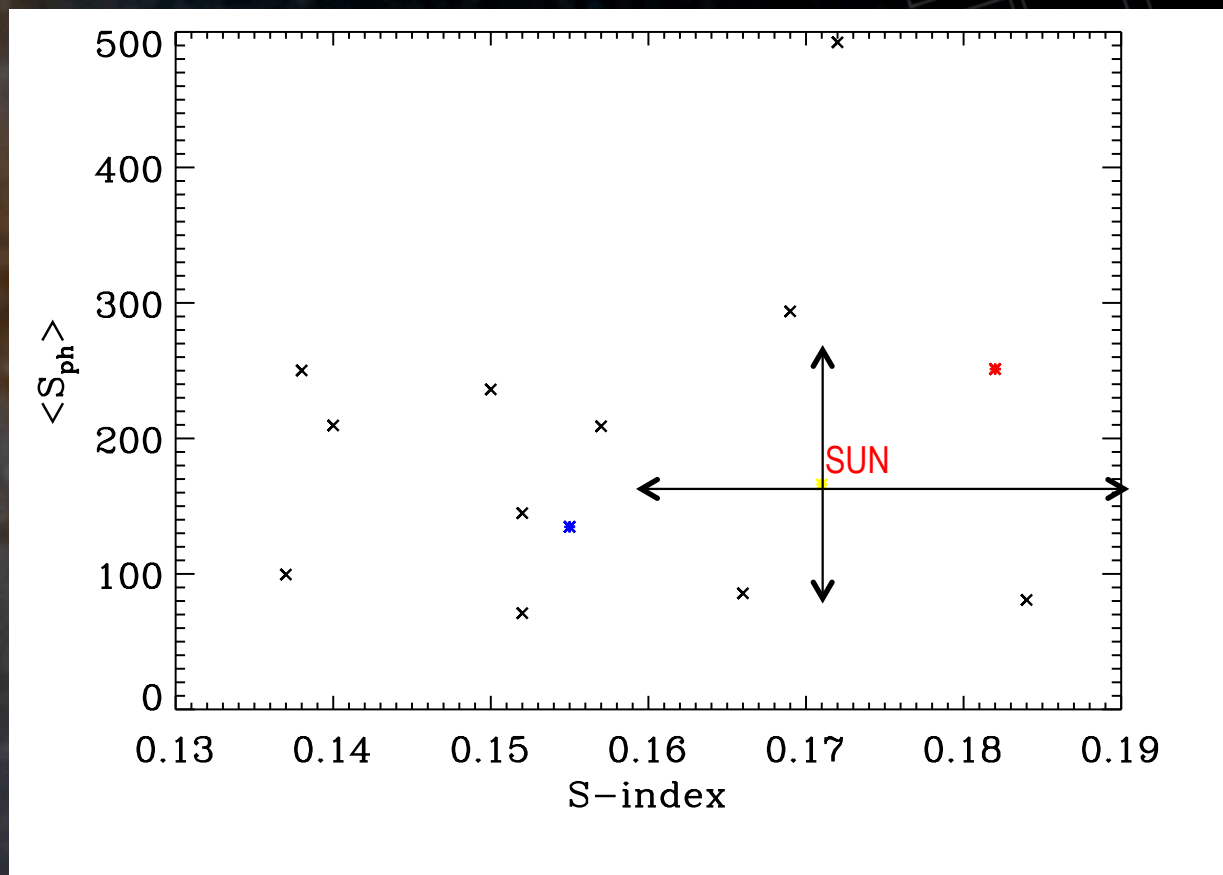
## ➤ The photospheric magnetic activity of the pulsating solar-like stars

[García et al. 2014]

- Compatible with the solar magnetic activity during the solar cycle (61.5%)

➤ S-index from NOT (Karooff et al. 2013) observations in 2009, 2010, and 2011

- $S_{ph}$  and Ca HK covering different periods of time
- $S_{ph}$  sensible to the stellar inclination angle
- $S_{ph}$  underestimate maximum activity in comparison to Ca HK



[Mathur et al. 2014]

# IV-Stellar magnetic cycles



# IV-STELLAR MAGNETIC CYCLES

## ➤ Activity cycles are the consequence of:

- Interaction between
  - Rotation, convection & magnetic fields

## ➤ There is a relation between:

$$P_{\text{cyc}}/P_{\text{rot}} = \Omega / \Omega_{\text{cyc}} = C \text{Ro}^q$$

[e.g. Thomas & Weiss 2008]

- with  $\text{Ro} = P_{\text{rot}}/\tau_c$ , the Rosby number
- $\tau_c$  the convective turnover time
- $q$  changing from 0.25 to 1

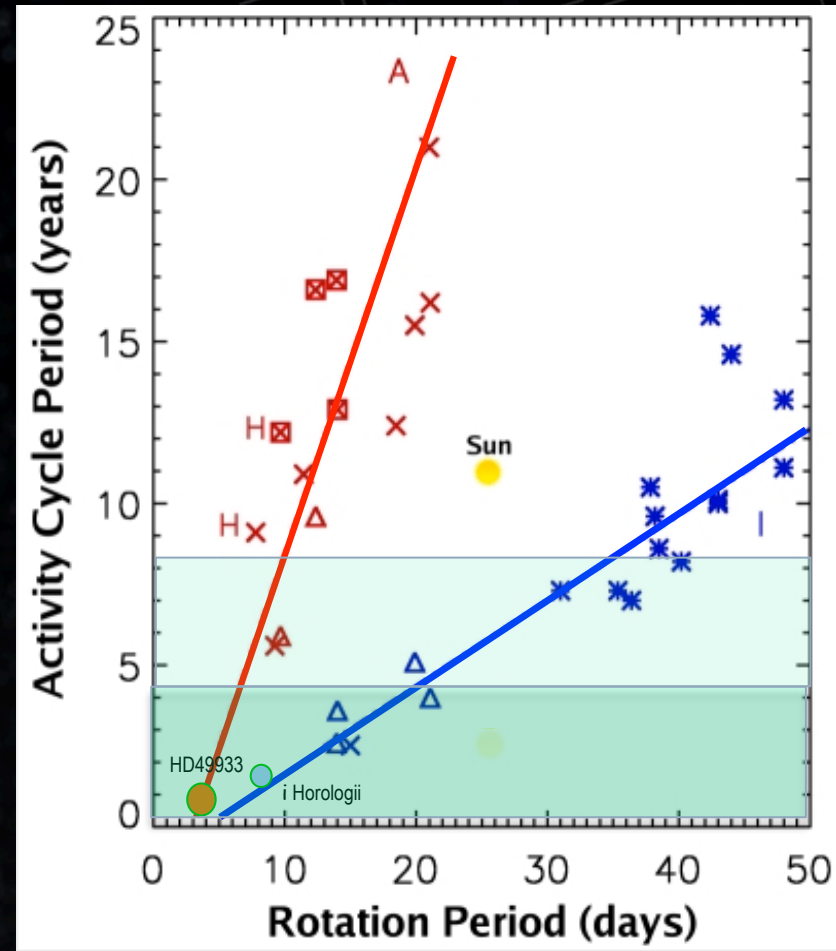
[e.g. Ossendrijver 1997; Saar 2002; Jouve et al. 2010]

## ➤ Stellar activity cycles:

- Two branches
- The position of the Sun
  - Between both branches

## ➤ Faster rotators

- Stronger magnetic activity amplitudes
- Rarely have regular cycles

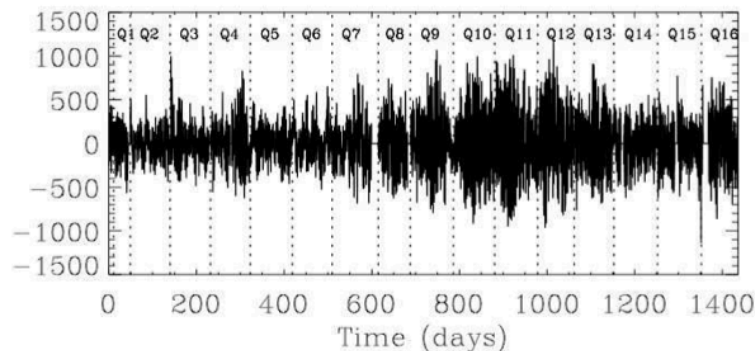


[Adapted from Bohm-Vitense, 2007]

[Benevolenskaya 1995, Fletcher et al. 2010]

# IV-STELLAR MAGNETIC CYCLES

KIC3733735

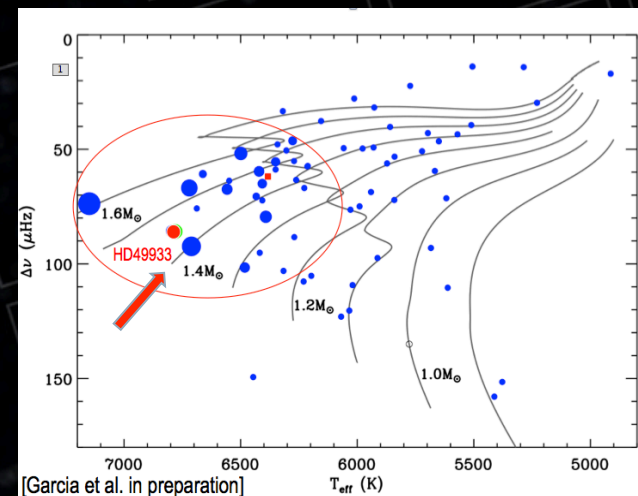


$P_{\text{rot}} = 2.5\text{d}$   
 $\langle S_{\text{ph}} \rangle = 250 \text{ ppm}$   
 $i \sim 30^\circ$

Asteroseismology:

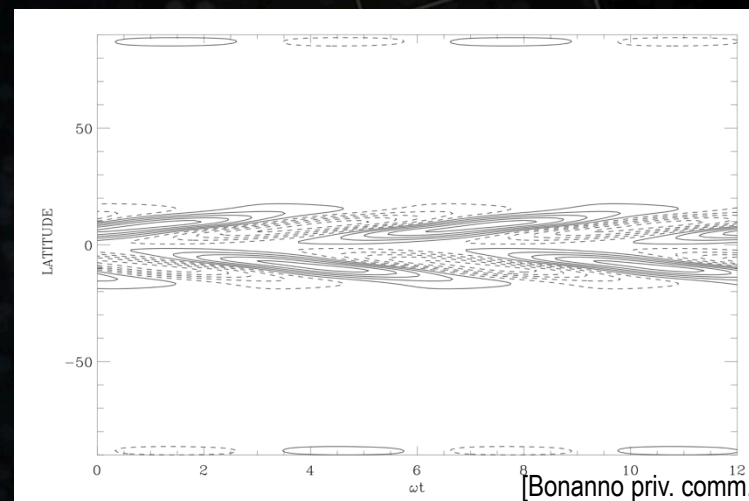
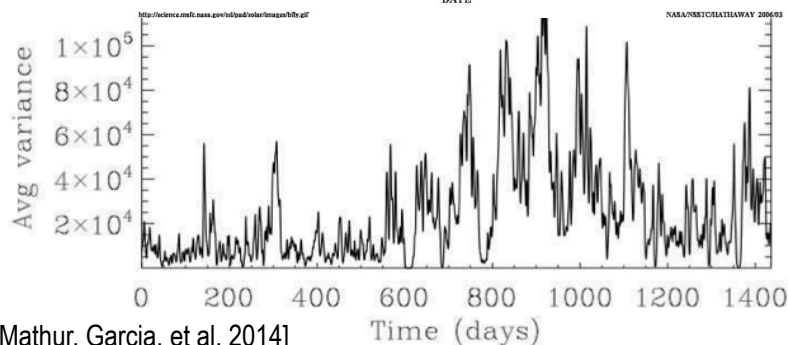
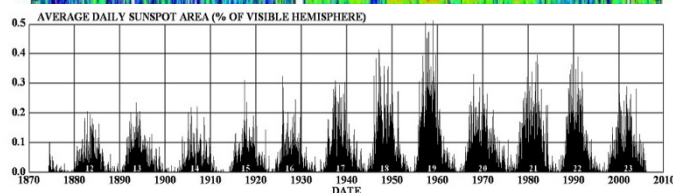
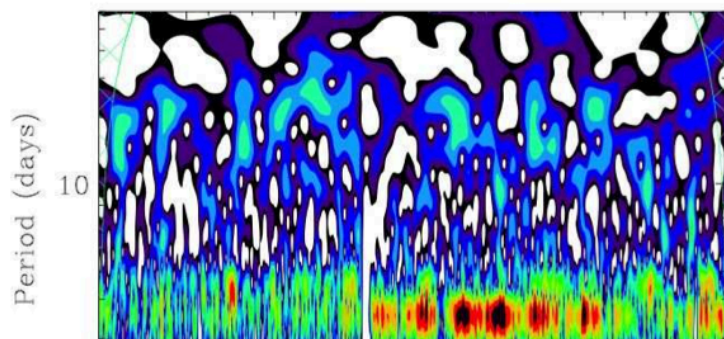
$M \sim 1.4 M_{\odot}$

DCZ  $\sim 1\%$



We observe:

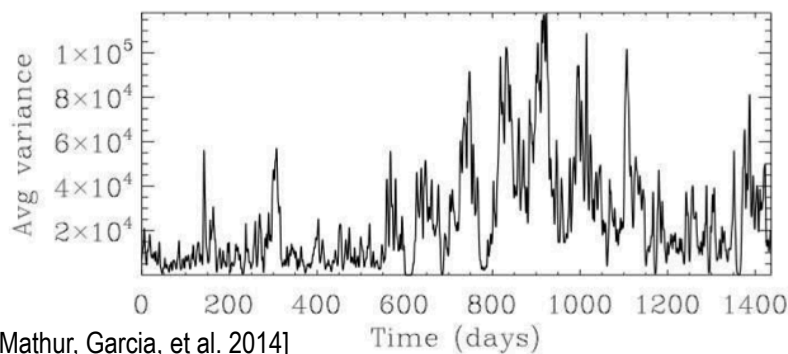
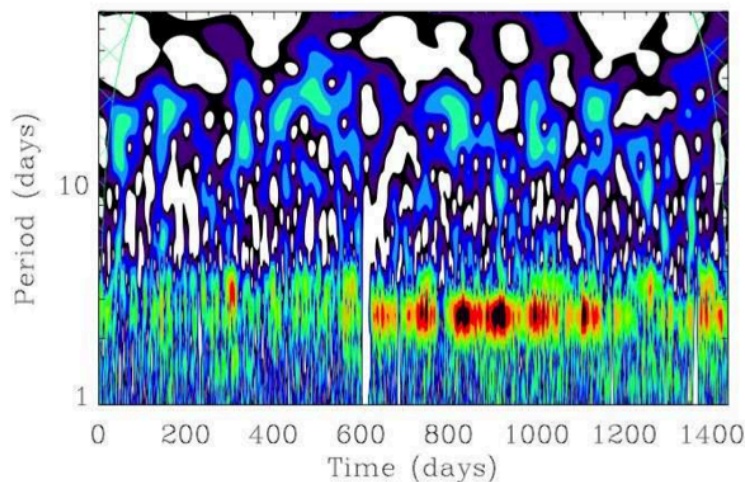
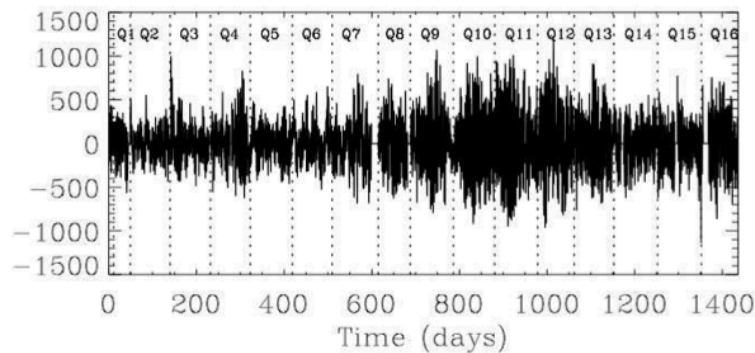
- Magnetic Cycle like behavior
- Presence of Active longitudes during maximum activity
- Mean field advection dominated model:



[Bonanno priv. comm.]



# IV-STELLAR MAGNETIC CYCLES



[Mathur, Garcia, et al. 2014]

$P_{\text{rot}} = 2$

$\langle S_{\text{ph}} \rangle$

$i \sim 30^\circ$

Aster

$M \sim 1.5$

DCZ

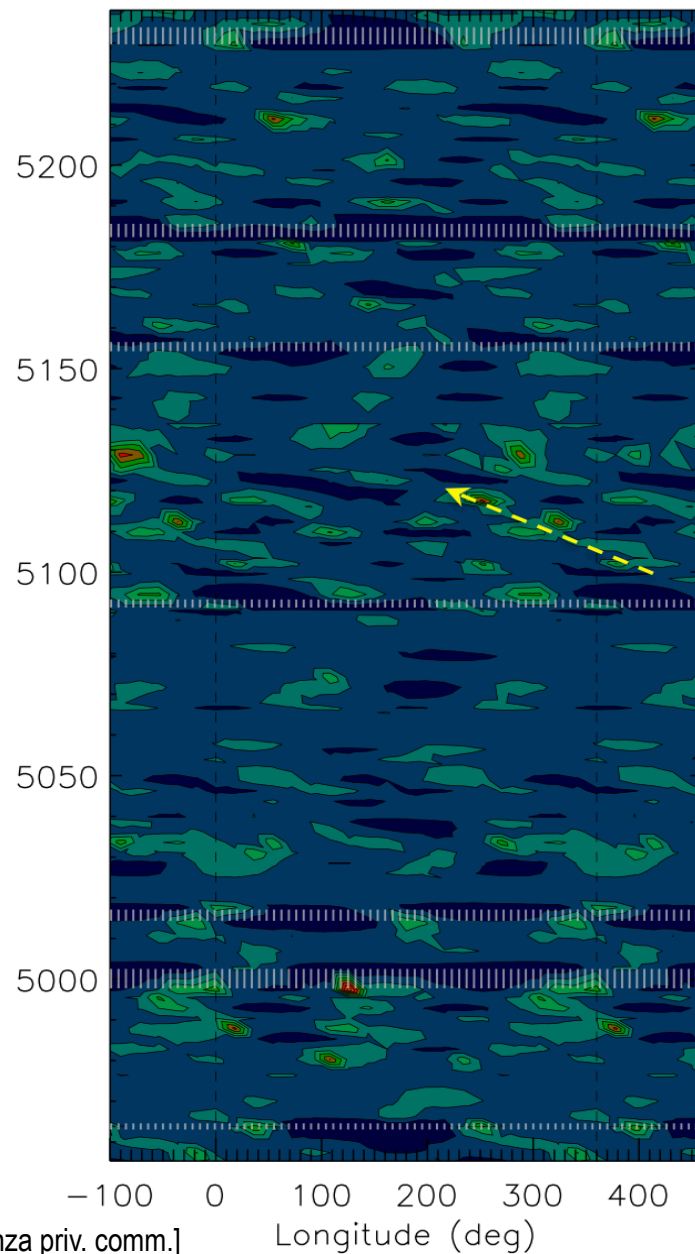
We

- M

- R

- M

Time (BJD - 2450000.0)



[Lanza priv. comm.]

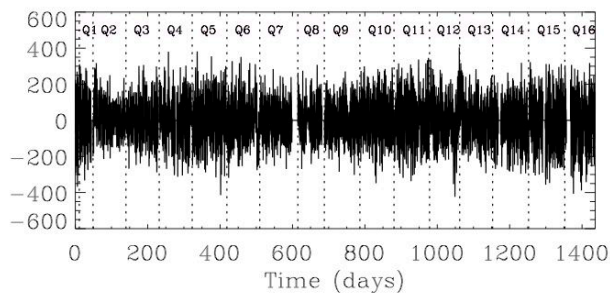
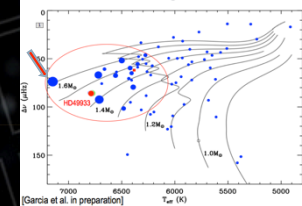


m activity





# IV-STELLAR MAGNETIC CYCLES



KIC9226926

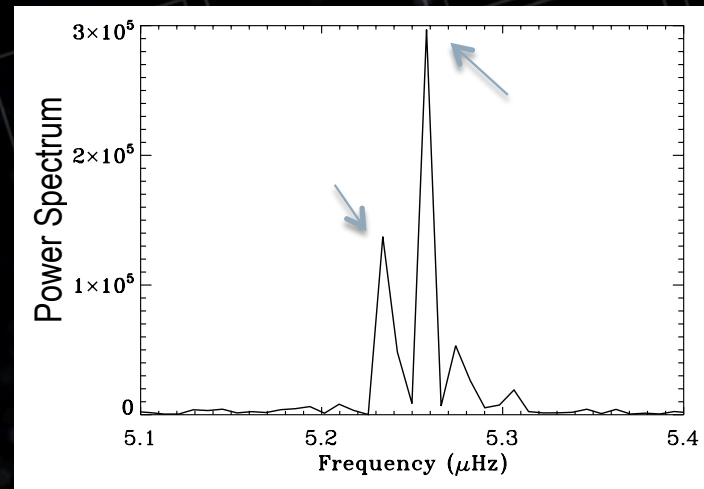
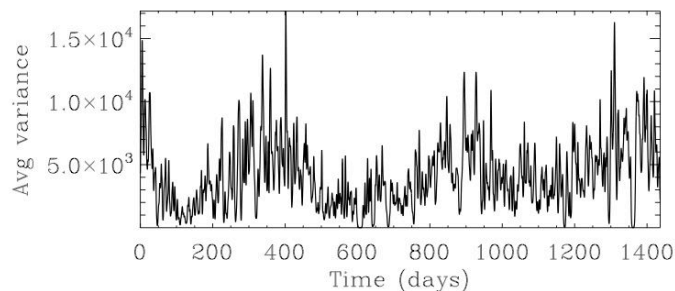
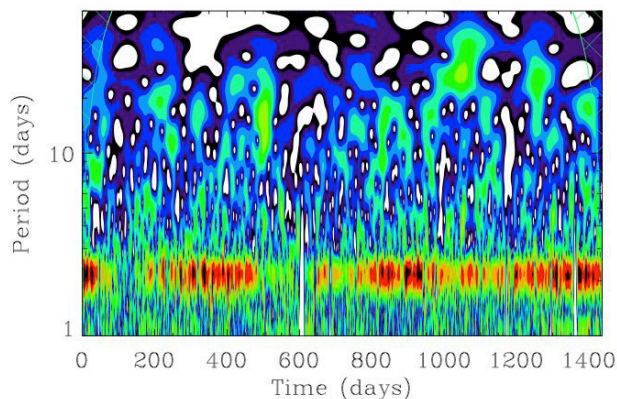
$P_{\text{rot}} = 2.2 \text{ d}$

$\langle S_{\text{ph}} \rangle = 104 \text{ ppm}$

Asteroseismology:

$M \sim 1.4 M_{\odot}$

DCZ  $\sim 1\%$

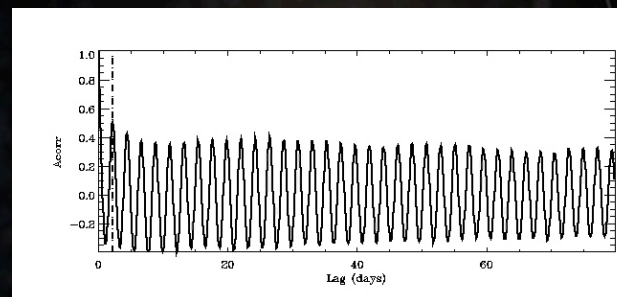


Two close frequencies (5.223 and 5.259  $\mu\text{Hz}$ )

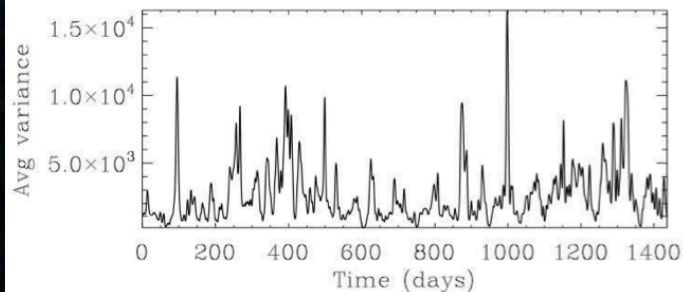
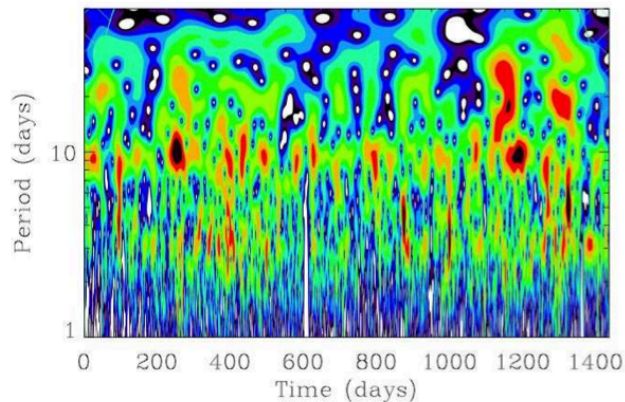
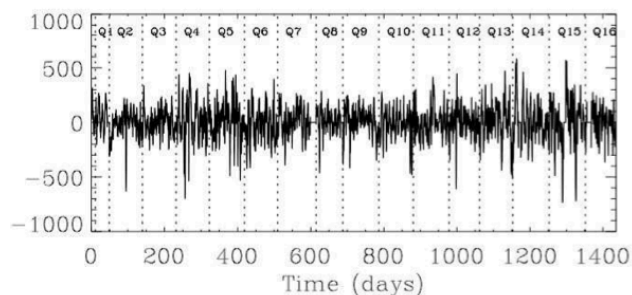
→ Beating effect with a period of  $\sim 540$  days

Not a cycle but signature of long lived magnetic structures:

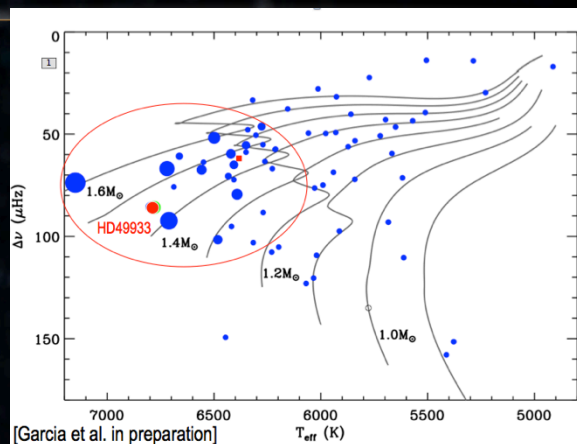
→ Active longitudes



# IV-STELLAR MAGNETIC CYCLES

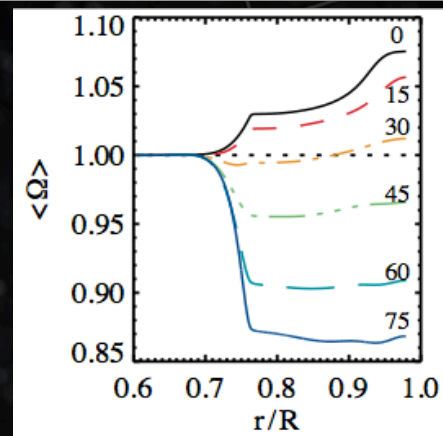
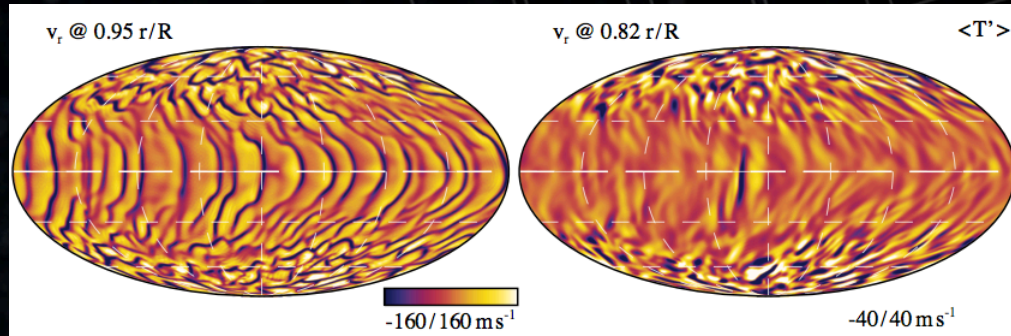


[Mathur, Garcia, et al. ApJ, 2014]



- KIC12009504
- 1D Seismic model
- 3D Model by ASH

Hydrodynamic models

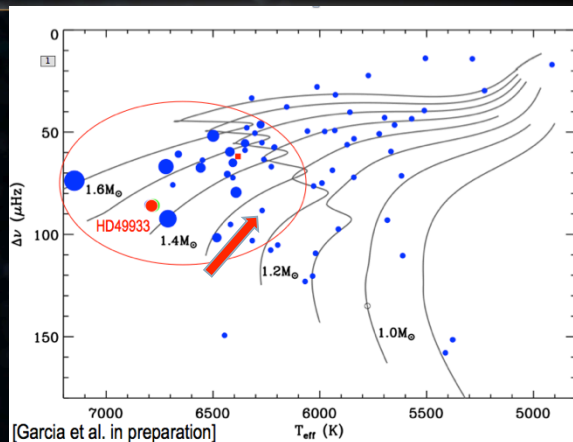
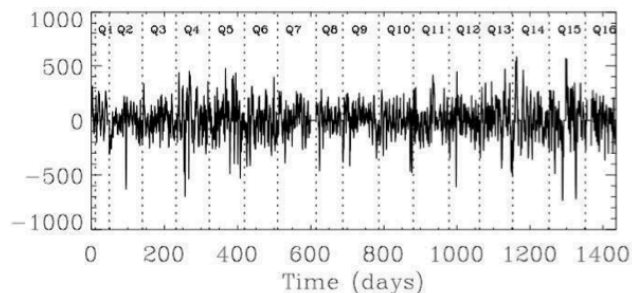


[Augustson, Mathur, Brun et al. in prep.]

$$P_{\text{rot}}=9.5\text{d}; M \sim 1.12M_{\odot}; \langle S_{\text{ph}} \rangle = 167.1 \text{ ppm}; \text{DCZ } 0.8 R$$

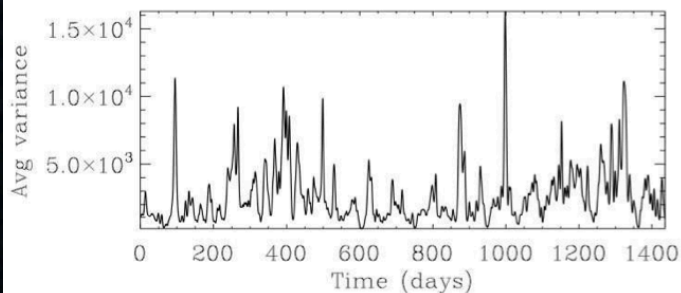
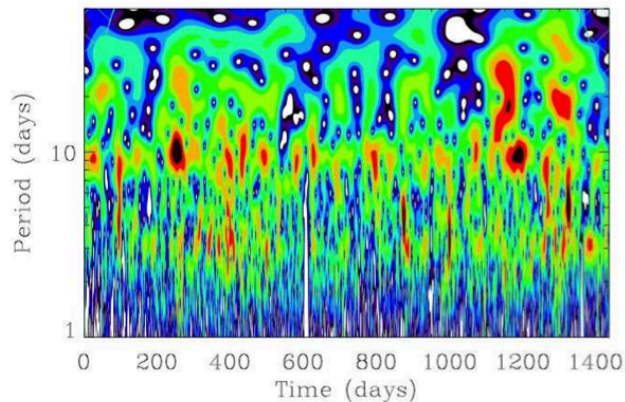


# IV-STELLAR MAGNETIC CYCLES

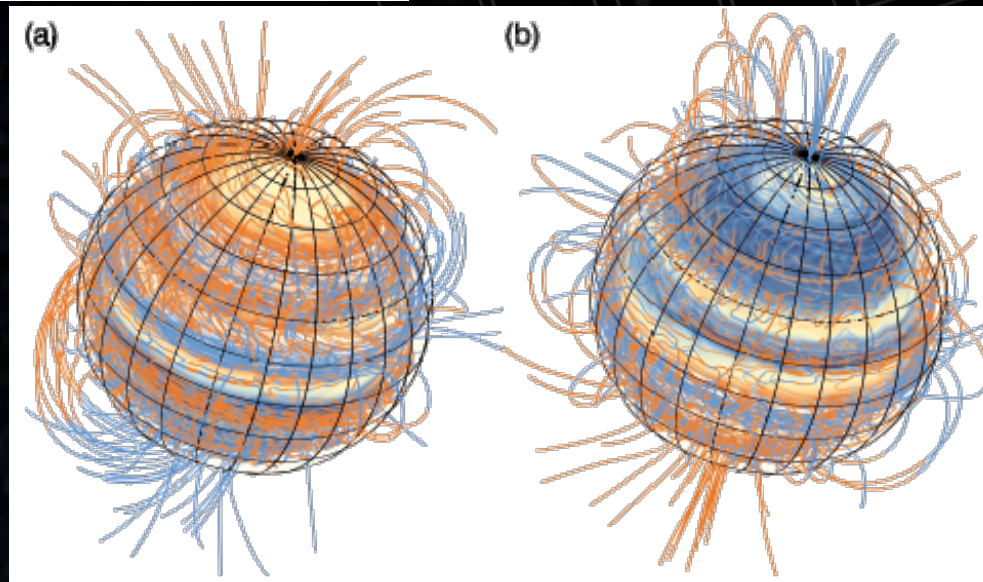


[Garcia et al. in preparation]

- KIC12009504
- 1D Seismic model
- 3D Model by ASH



[Mathur, Garcia, et al. ApJ, 2014]

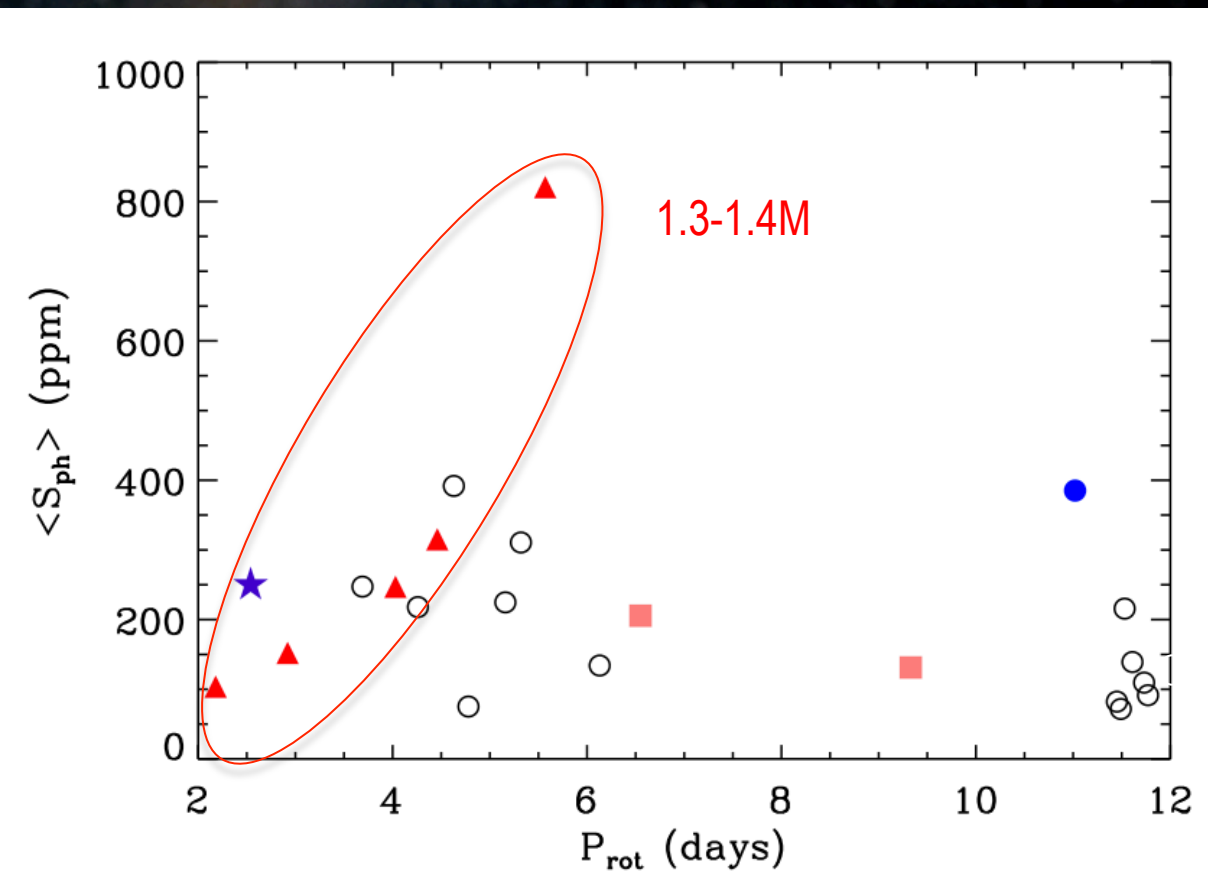


[Augustson, Mathur, Brun et al. in prep.]

$$P_{\text{rot}}=9.5\text{d}; M\sim 1.12M_{\odot}; \langle S_{\text{ph}} \rangle = 167.1 \text{ ppm}; \text{DCZ}\sim 20\%$$



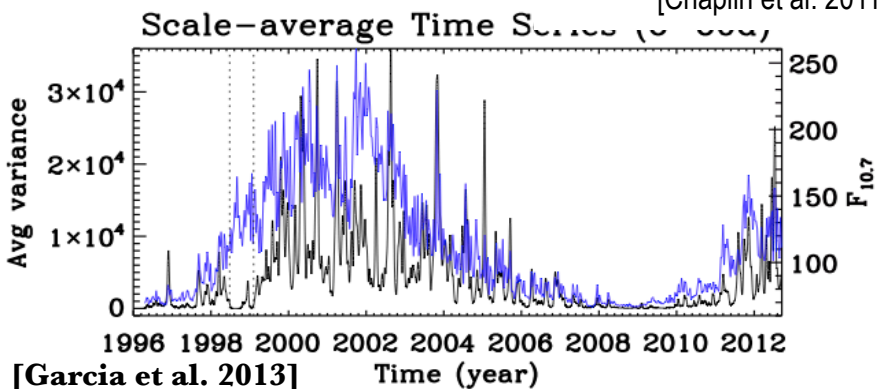
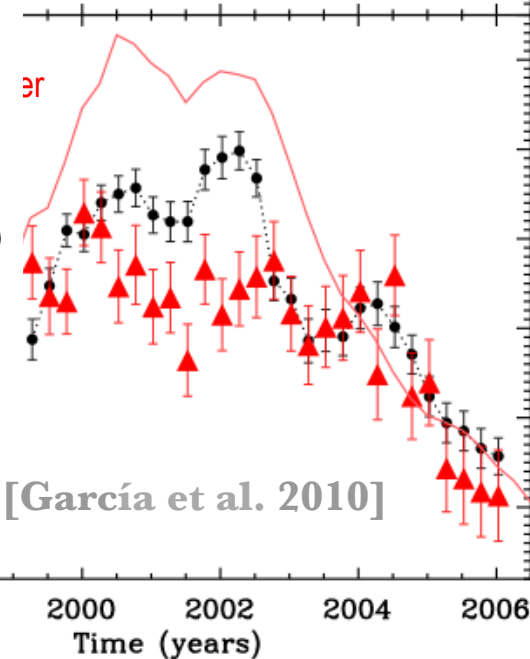
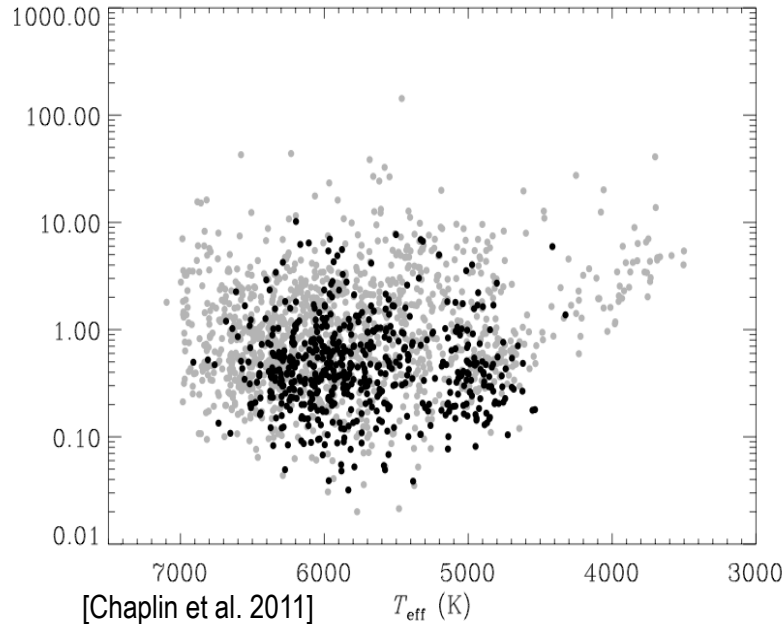
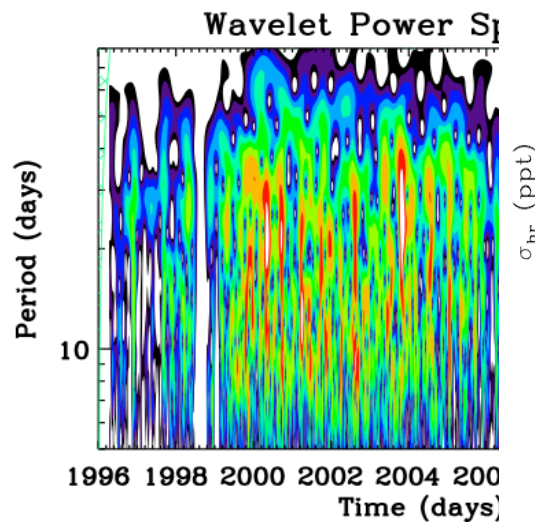
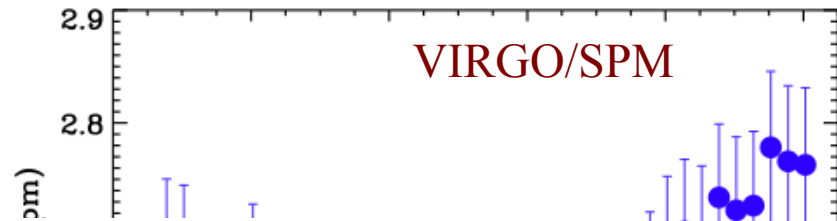
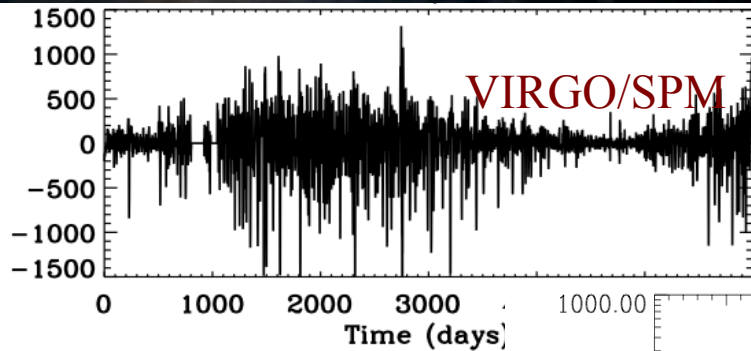
# IV-STELLAR MAGNETIC CYCLES



- ▲ Long-lived active longitudes
- Trends
- Cycle

[Mathur, Garcia, et al. ApJ, 2014]

# IV-MAGNETIC ACTIVITY: SEISMOLOGY

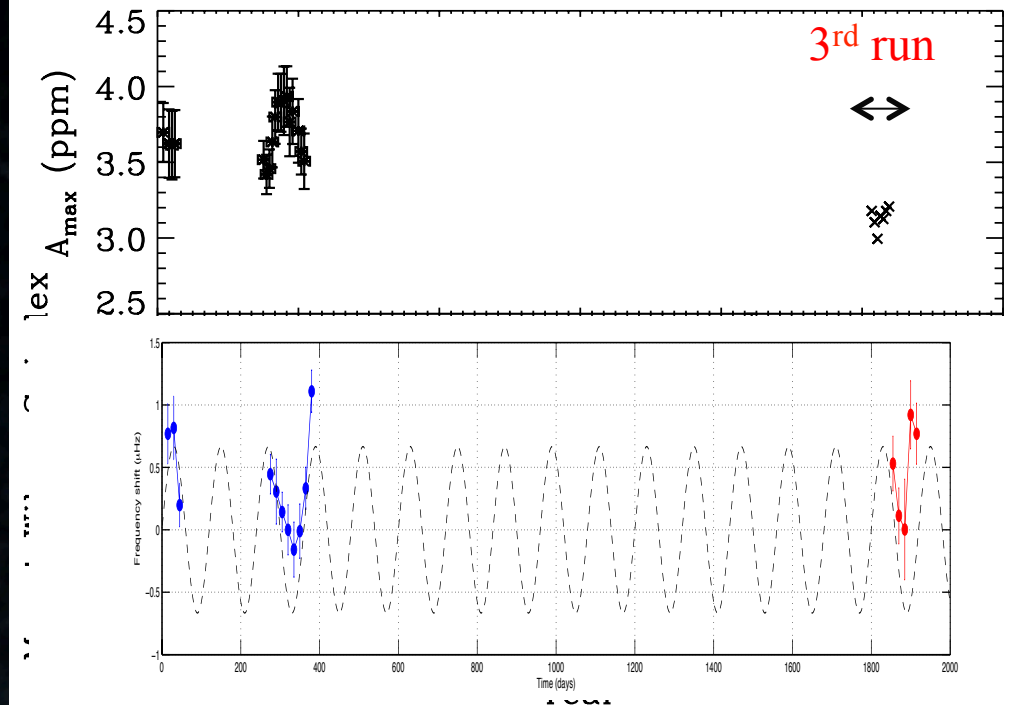
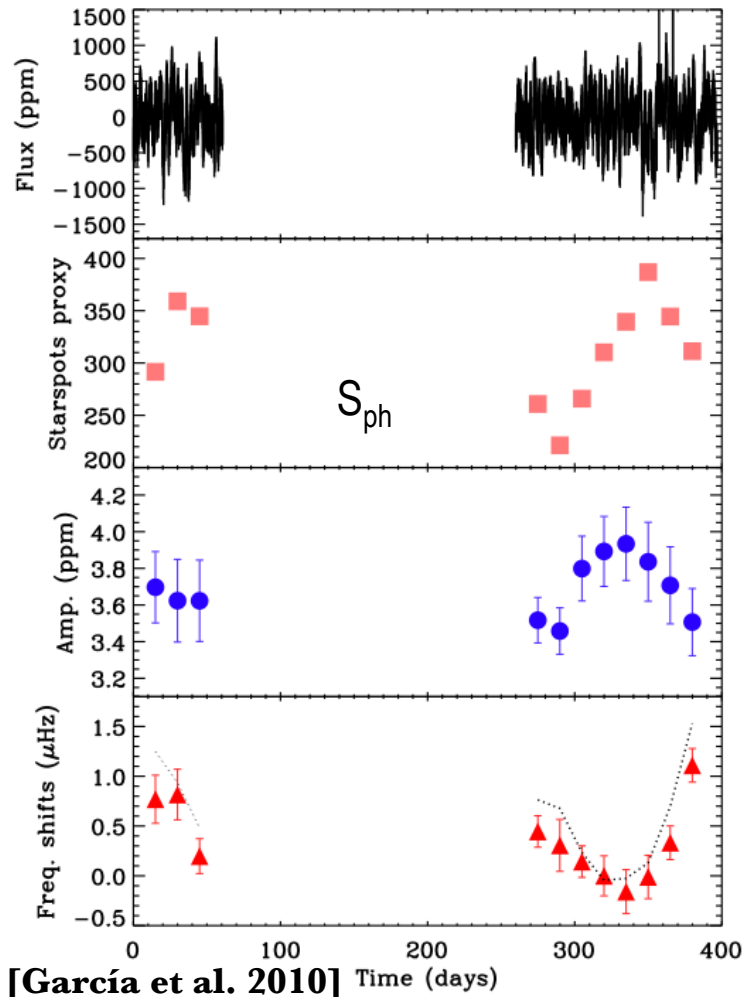


# HINTS OF A MAGNETIC-ACTIVITY CYCLE

*Seismology*

CoRoT

HD49933



- Complementary observations
  - ✓ Ca HK: Mount Wilson index of 0.31
  - Active star

Modified  $S_{ph}$  also used by Chaplin et al. 2011  
Campante et al. 2014

Anticorrelation between amplitude variation and frequency shifts

$P_{cyc} > 120 \text{ days}$



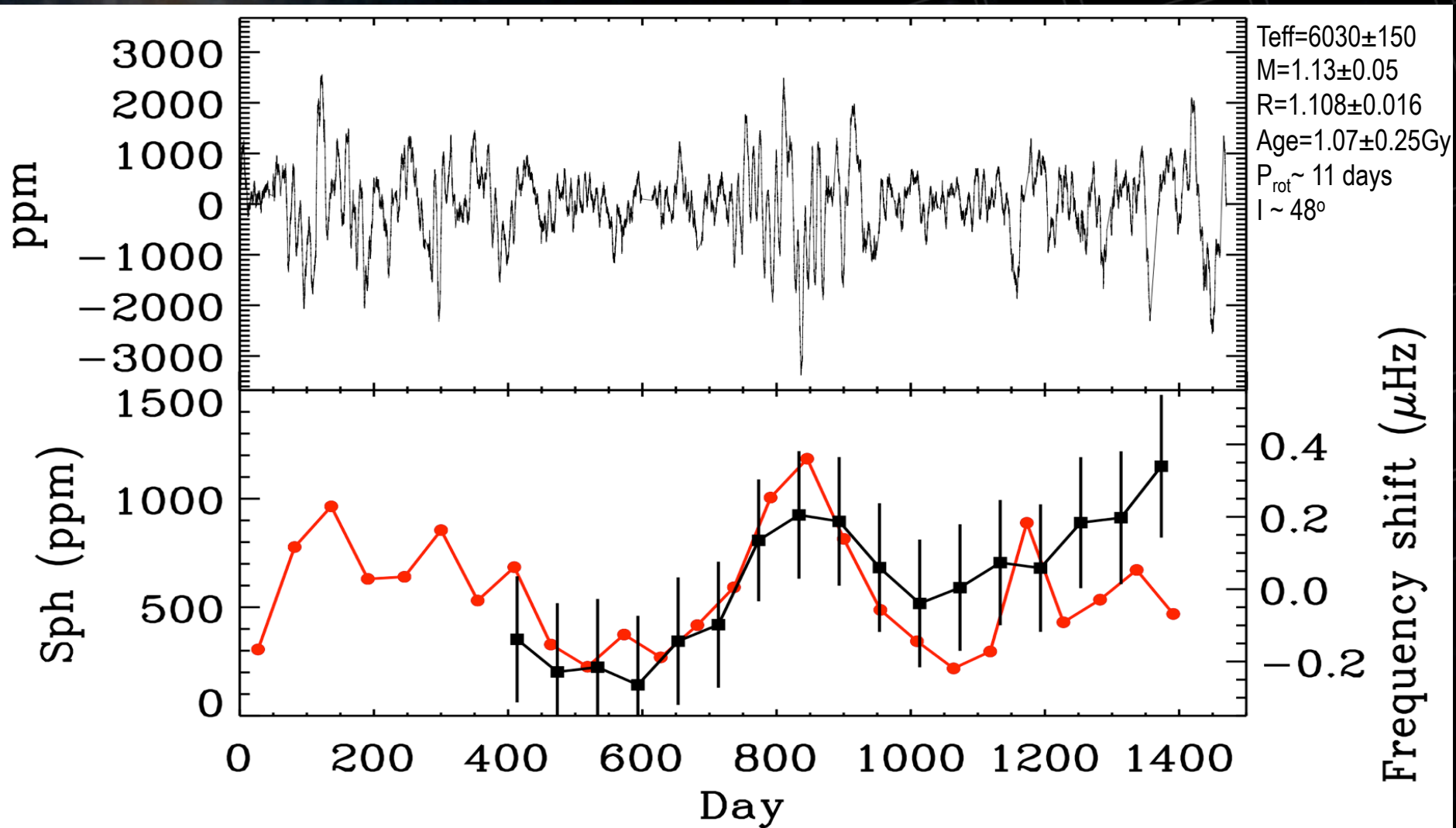
# HINTS OF A MAGNETIC-ACTIVITY CYCLE

➤  $\approx$  Solar analog

*Kepler*

- Correlation between  $S_{ph}$  and p-mode frequency shifts

[Bruntt et al. 2012; Metcalfe et al. 2014; García et al. 2014]



# CONCLUSIONS



*Understand stellar dynamics and magnetism*

*Is required*

*To properly model stellar interiors*

*To better constraint geometry of exoplanetary systems*

*To properly interpret exoplanet atmospheres*

*Characterization of Habitable zones (development of life)*

*Studying many solar-like stars will help  
to better understand The Solar magnetism*

