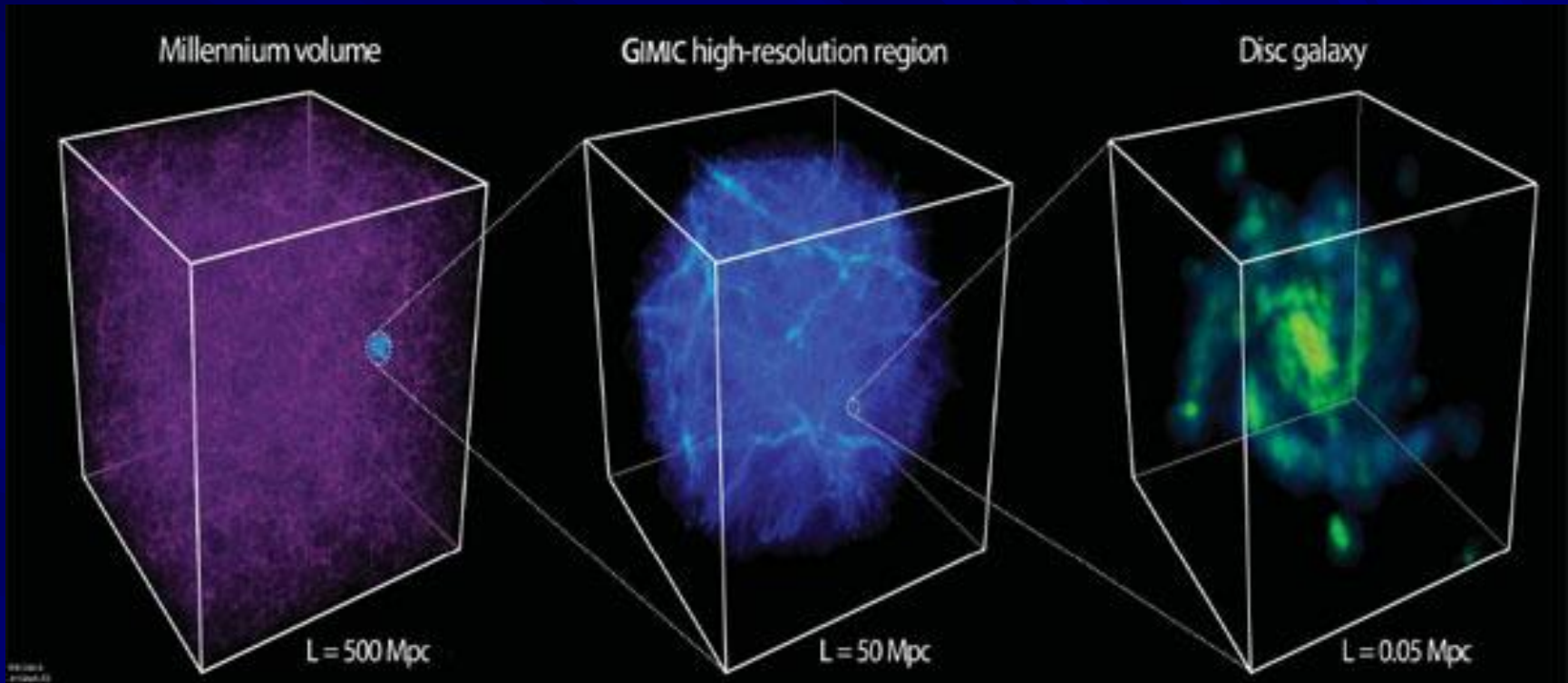


# Measuring Stellar Parameters

Marc Pinsonneault  
Ohio State University

# Galactic Archeology



We can test the formation history of the Milky Way if we can precisely measure stellar ages and abundances.

**PROBLEM:** Are our tools up to the task?

# Overall Picture

- Equations of Stellar Structure
- Mass, Composition, Age (plus rotation and magnetic fields) specify the properties of a star
- Classic Observables:  $L$ ,  $R$ ,  $T_{\text{eff}}$ ,  $\log g$ , kinematics
- New (Seismic) Observables: Core properties; surface CZ depth

# Global Stellar Properties & Their Dynamic Ranges

- Energy output (L) is related to the surface temperature and radius through

$$L = 4\pi R^2 \sigma T_{\text{eff}}^4$$

Where  $T_{\text{eff}}^4$  is the flux per unit area that a blackbody would have

- $L_{\text{sun}} = 3.844 \times 10^{33}$  erg/s
- **For normal stars**  $10^{-4} L_{\text{sun}} < L < 10^6 L_{\text{sun}}$

# Luminosity

## Historical Path

- Measure Fluxes
- Correct for Extinction
- Infer Distance
- *All of these methods scale well to surveys*

## Complications

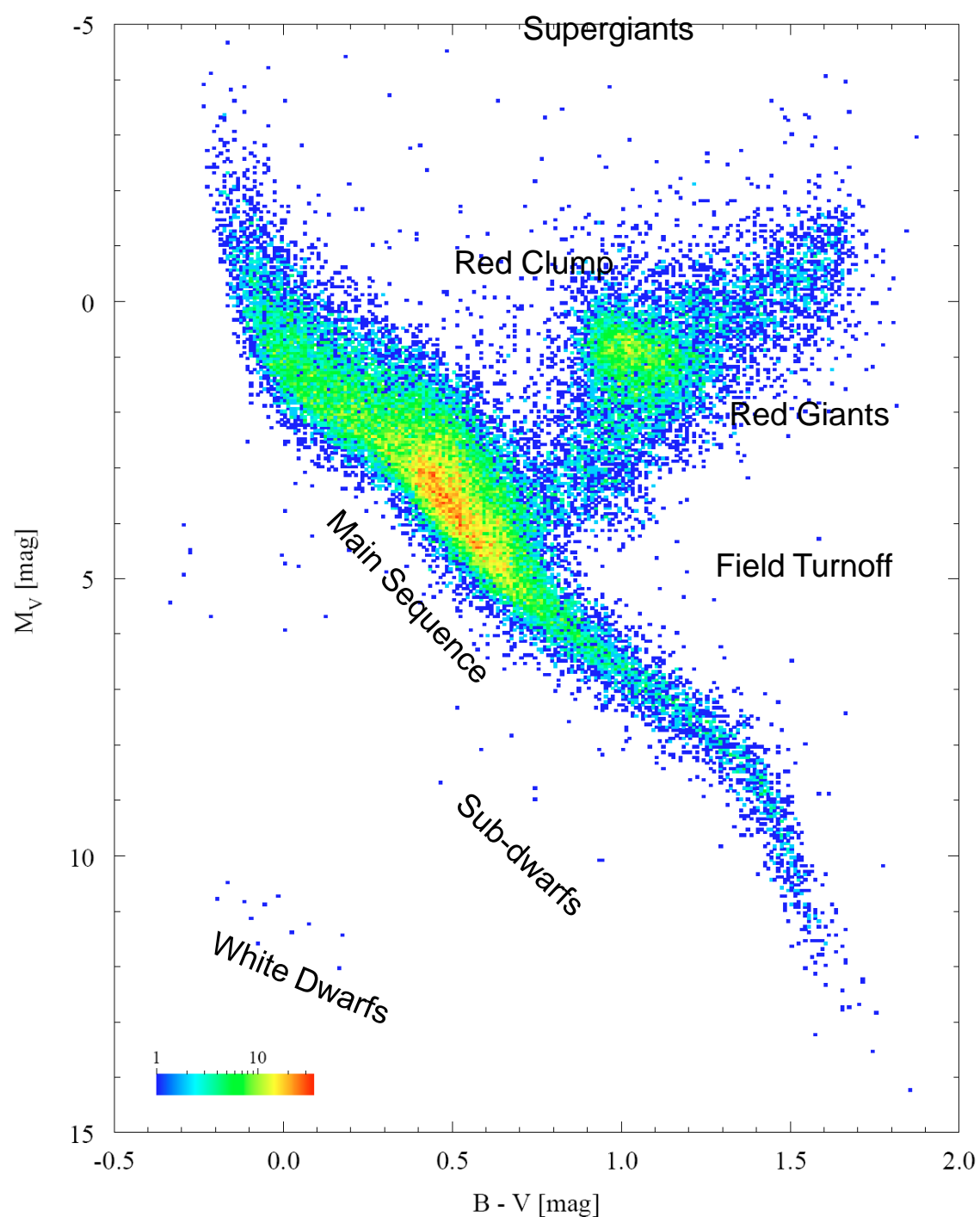
- *Absolute photometry is astonishingly difficult to do well*
- Blends (esp. binaries) affect fluxes and colors
- Reconstructing the SED is quite model dependent
- Extinction is important

**Key Future Development: Gaia**

# The HR Diagram

- Distinct Populations
- Important features give information about galactic populations and relative timescales

Hipparcos  
CMD,  
 $\sigma < 20\%$



# Gaia and Hipparcos

■ Hipparcos:

$10^5$  stars

$\sigma=1$  mas

■ Gaia:

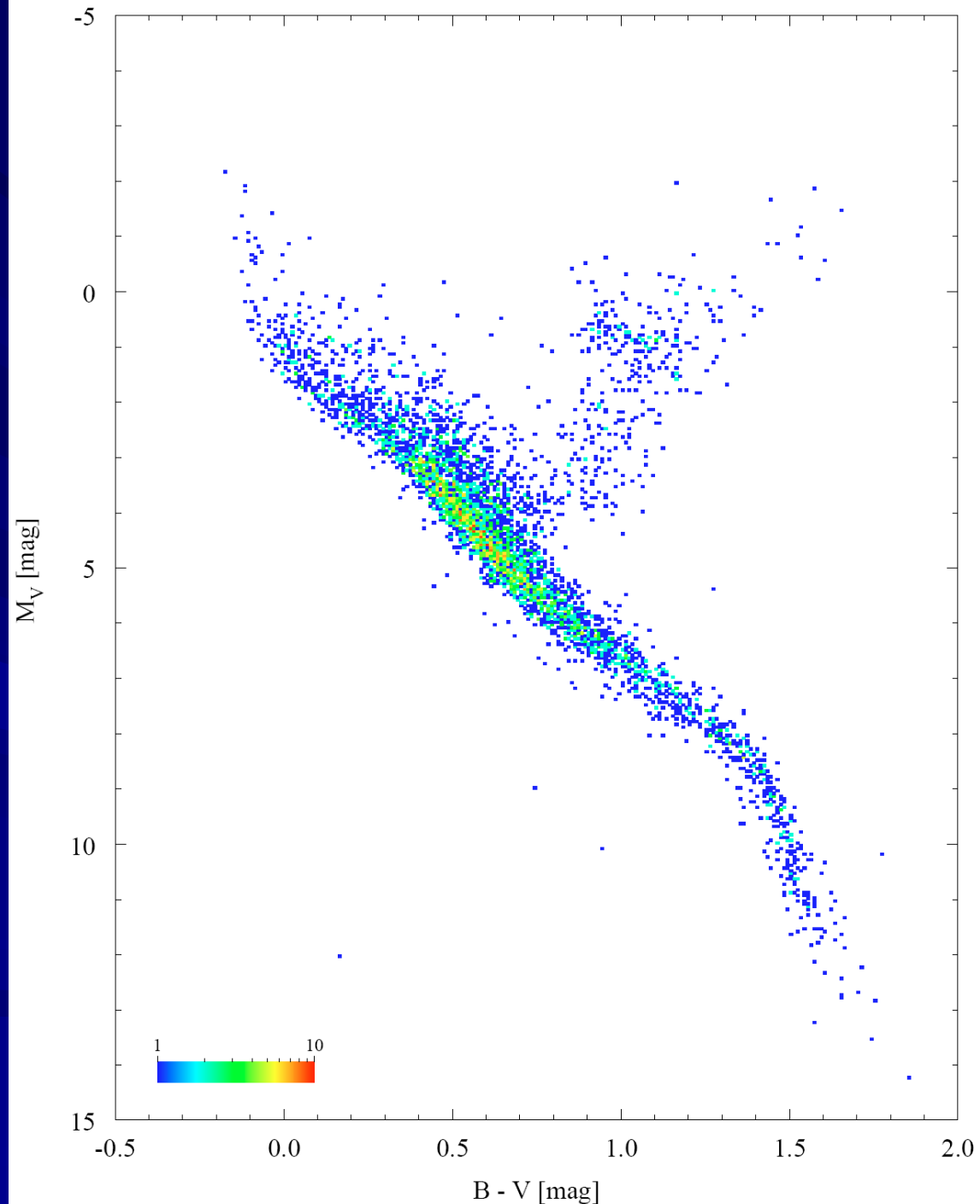
$10^9$  stars

$\sigma=0.003$  mas (12)

$\sigma=0.01$  mas (15)

$\sigma=0.2$  mas (20)

Hipparcos CMD,  $\sigma < 5\%$



# Binaries are Fundamental Astrophysical Calibrators

- EB are efficiently found in time domain surveys
- VB – Gaia!

- Complications:
- Detectability – Visual
- Detectability – Eclipsing
- Labor and Resource Intensive Followup
- Difficult to measure composite properties
- Peculiar Systems

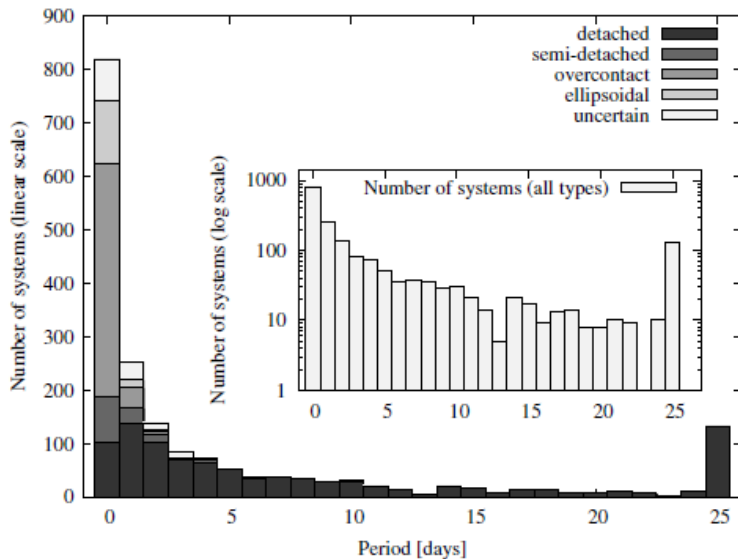


Figure 11. Distribution of periods for all the stars identified as eclipsing binaries in the *Kepler* Q1 data set. The baseline was 34 days (44 with Q0). The bars are stacked by morphology types (detached, semi-detached, overcontact, ellipsoidal, and uncertain). The inset depicts the number of systems in log scale.



# The Binary M-R Relationship

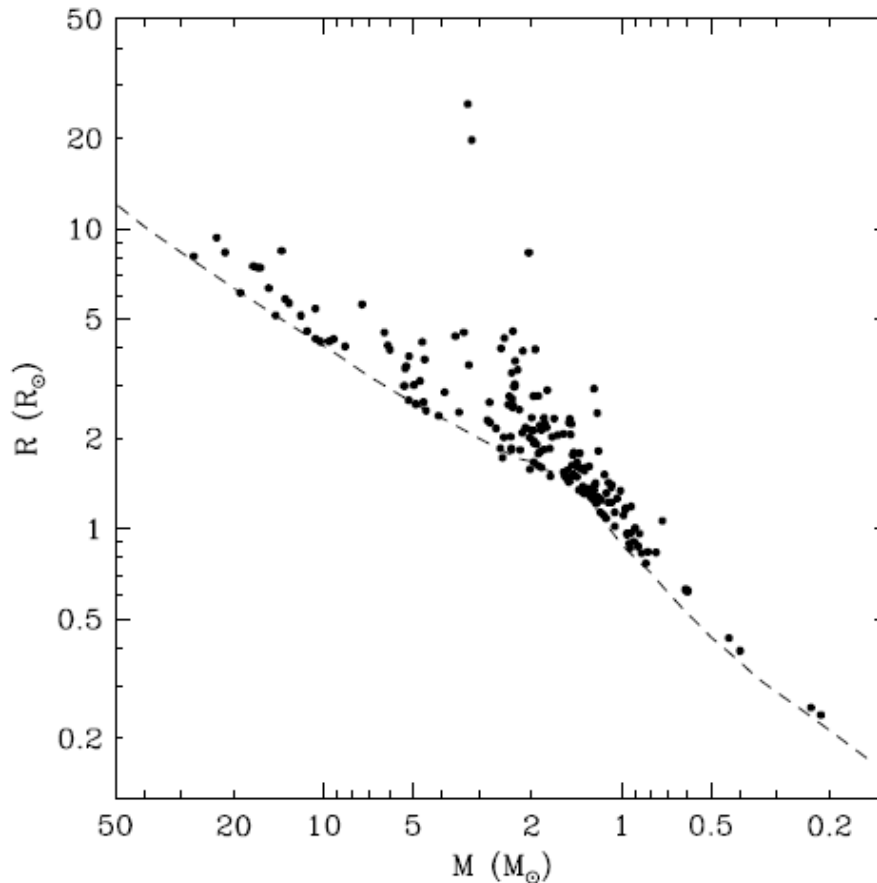
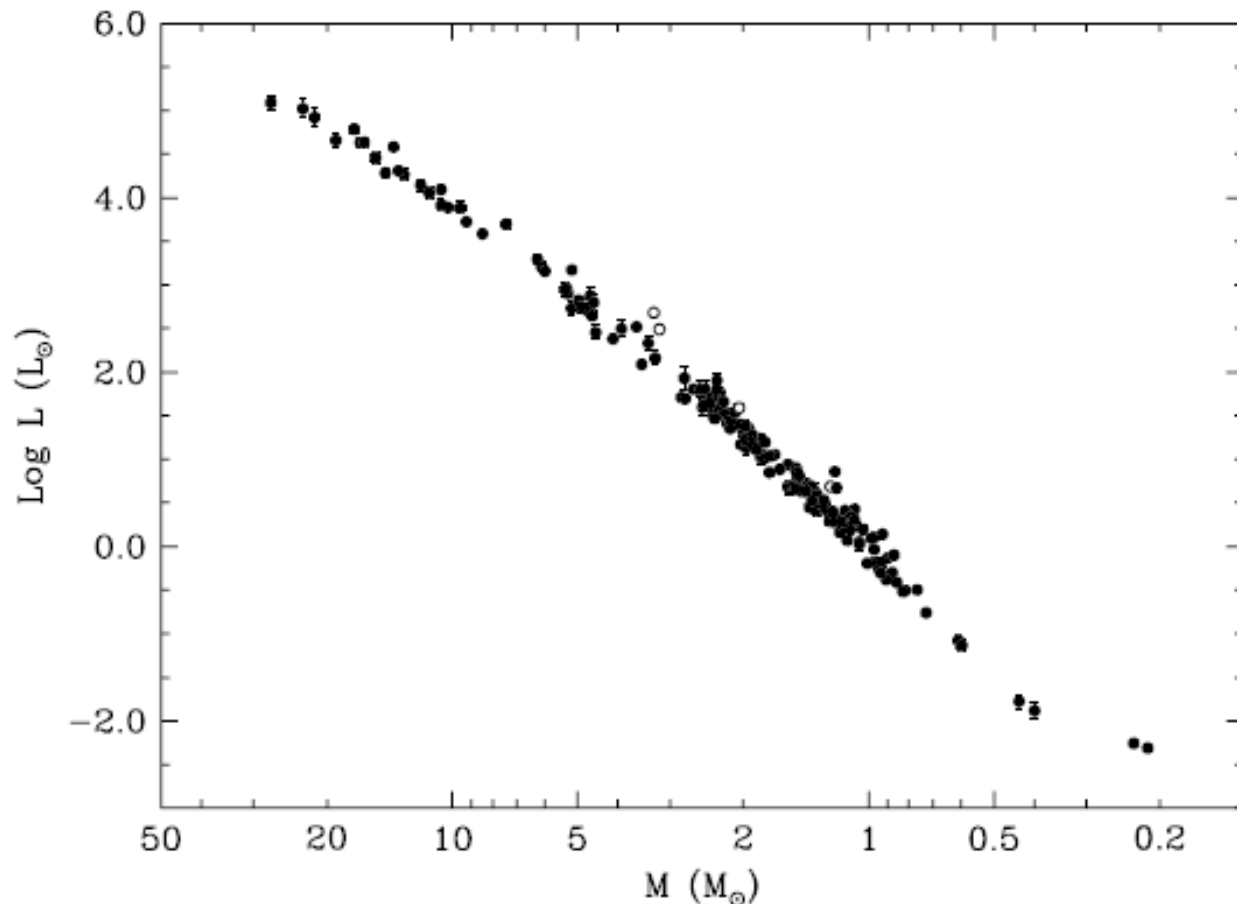


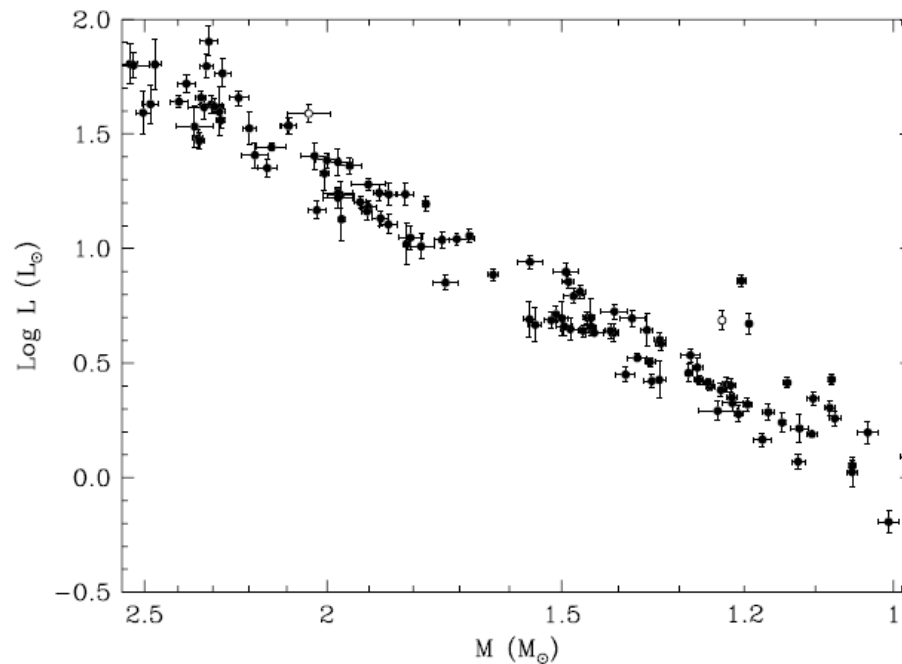
Fig. 2  $R$  vs.  $M$  for the stars in Table 2; error bars are smaller than the plotted symbols. A theoretical zero-age main sequence (ZAMS) for solar metallicity from Girardi et al. (2000) is shown by the dashed line.

# The Fundamental Mass-Luminosity Relationship



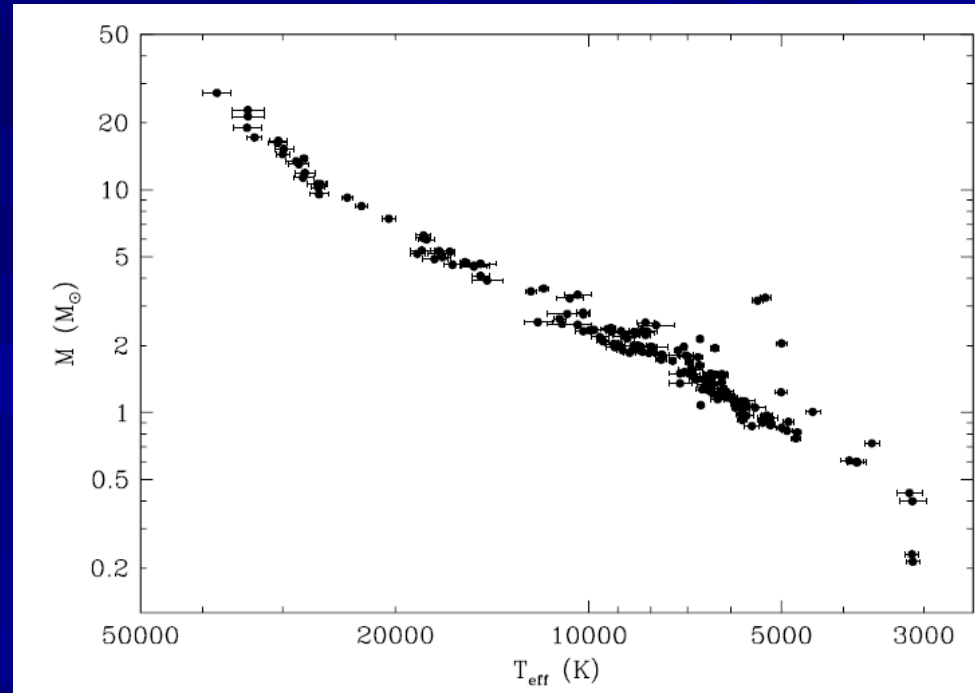
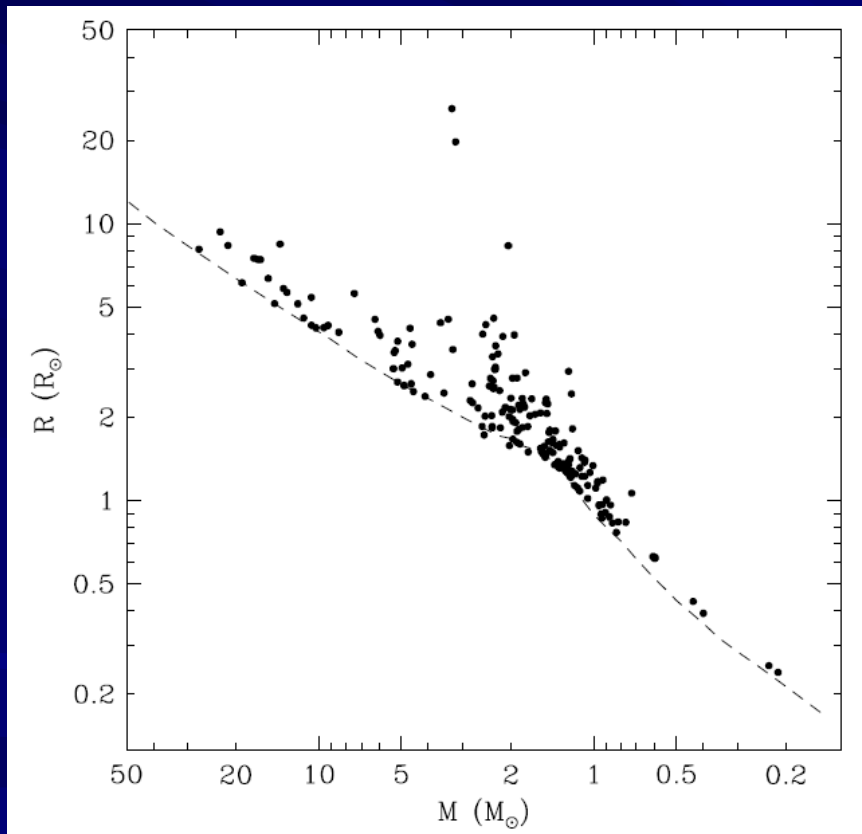
**Fig. 5** The mass-luminosity relation for the stars in Table 2. Error bars are shown, and stars classified as giants are identified by open circles. See Sect. 6 for a discussion of the effects of evolution in this diagram.

# Scatter in the HR Diagram is real and tied to composition



**Fig. 6** Close-up of the 1–2.5  $M_{\odot}$  range of the mass-luminosity relation in Fig. 5. The very significant scatter in  $\log L$  at each mass value is due to the combined effects of stellar evolution and abundance differences (see text). Open circles: stars classified as giants.

# There are also strong M-R and M- $T_{\text{eff}}$ relationships



Note: Radii exhibit evolutionary effects

# Effective Temperature

- $L = 4\pi R^2 \sigma T_{\text{eff}}^4$  **defines** the effective temperature
- The effective temperature scale is defined rigorously only for stars of known R.
- Calibrated relationships that are commonly used:
  - Photometric estimates based on colors (Wien's law) or SED fitting; IRFM
  - Spectroscopic estimates based on stellar absorption lines (Boltzmann/Saha equations)
- Solar  $T_{\text{eff}} = 5,770$  K

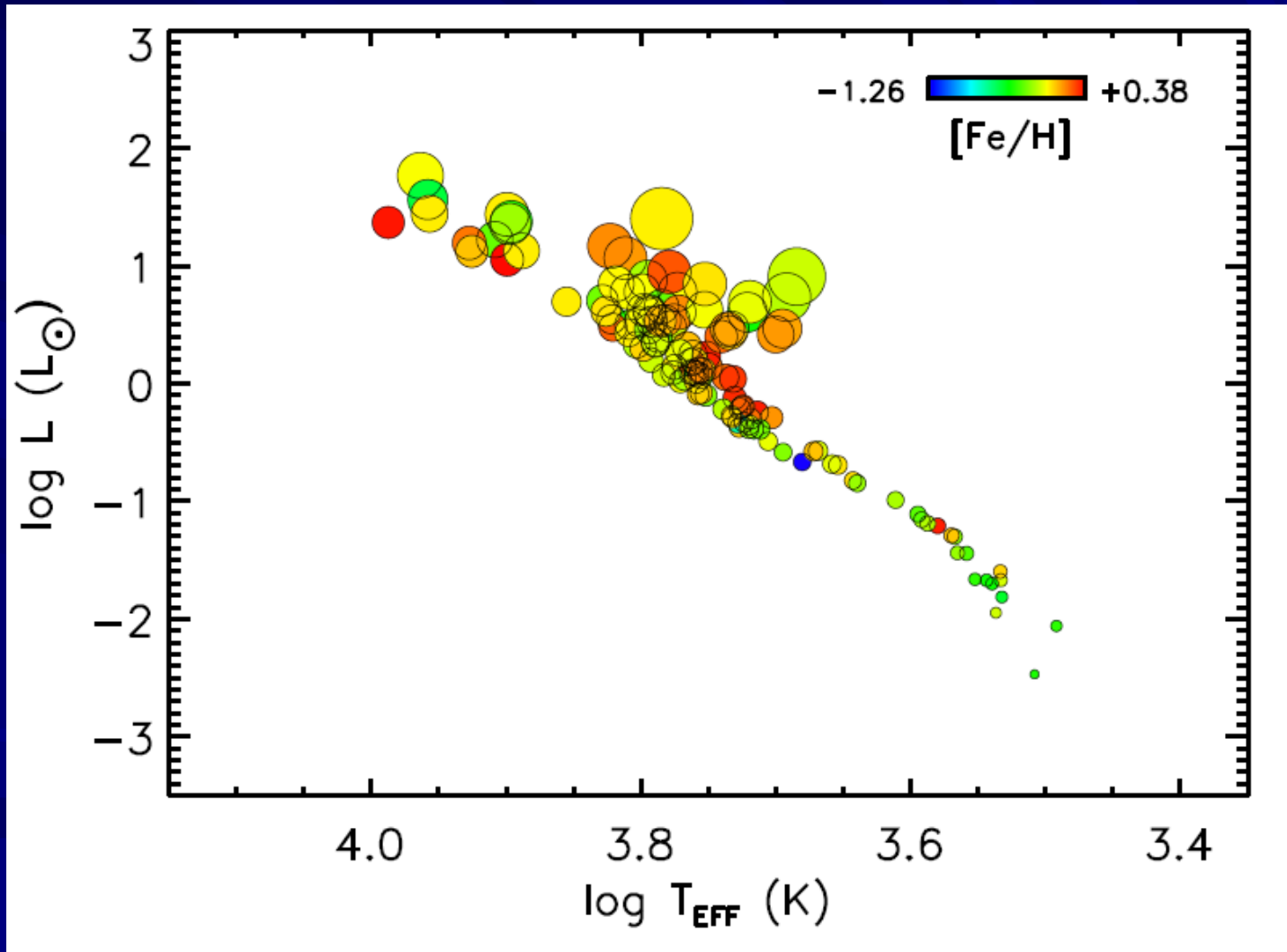
**For normal stars  $3,000$  K  $< T_{\text{eff}} < 50,000$  K**

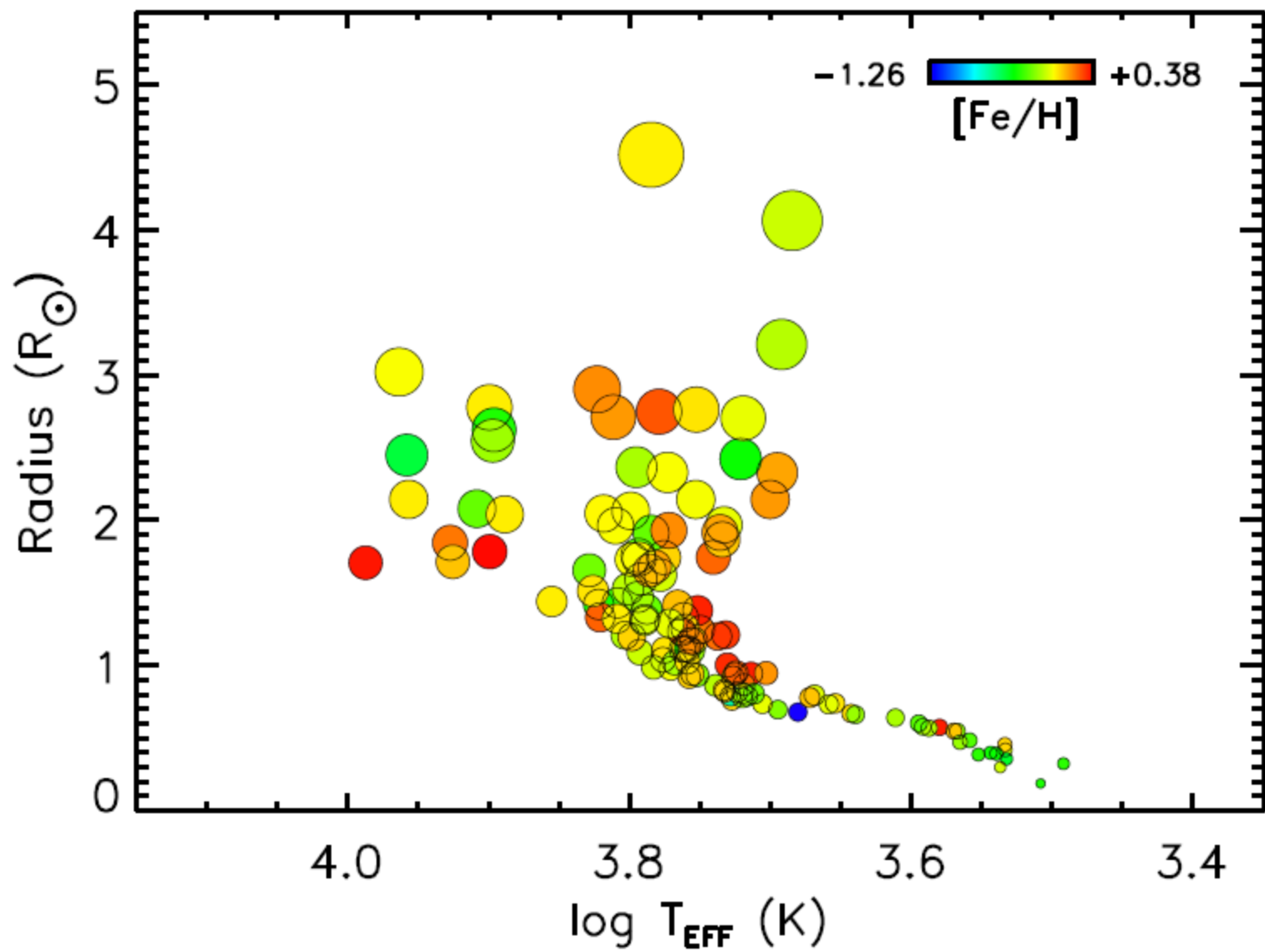
# Interferometry and Radius

- With the advent of optical interferometry we can now measure direct angular diameters with uncertainties  $\sim 0.05$  mas.
- $L + R \Rightarrow T_{\text{eff}}!$



# The Interferometric Sample







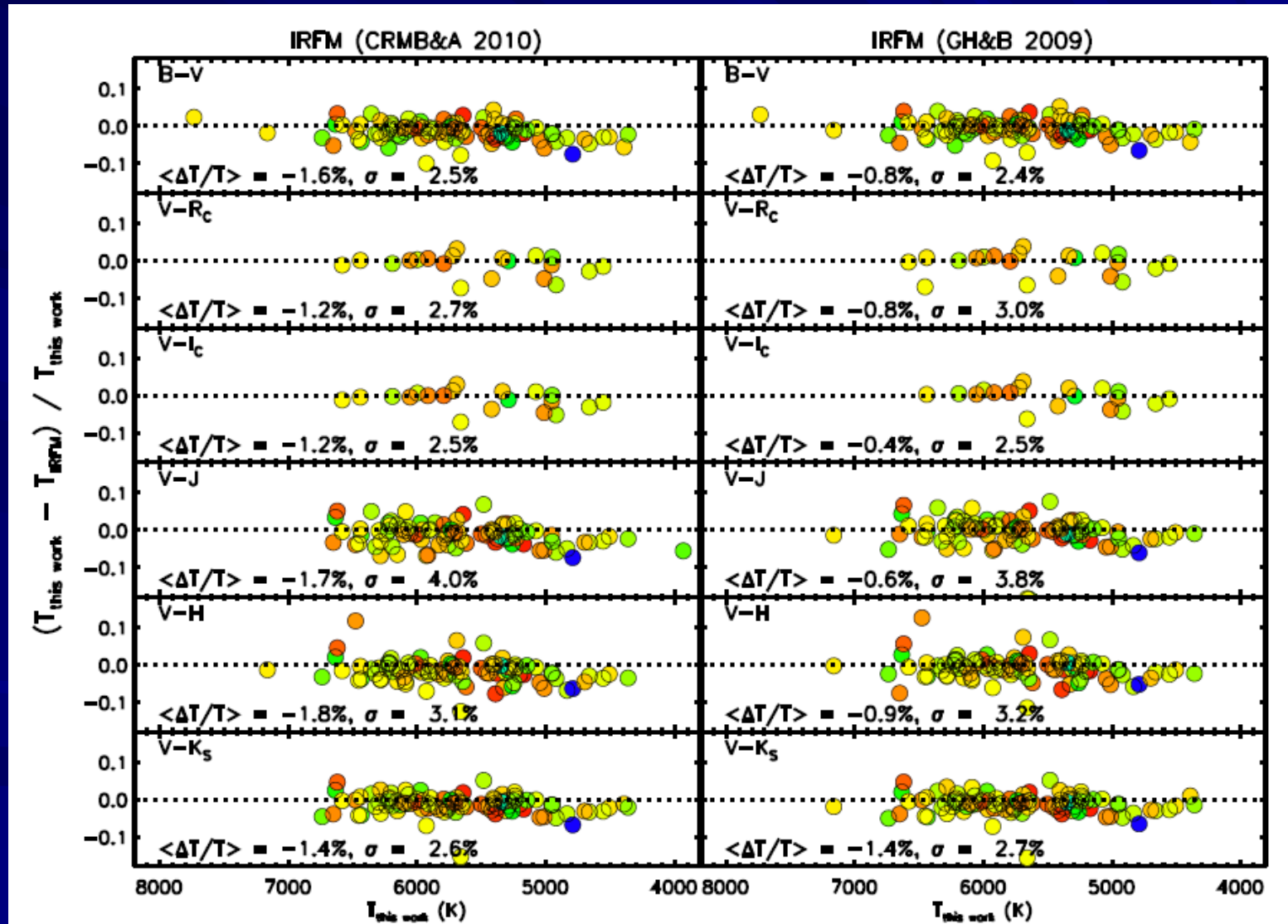
# The Temperature Paradox

- Temperature is the single most important determinant of a stars visible properties
- We have numerous and powerful diagnostics testable with fundamental data

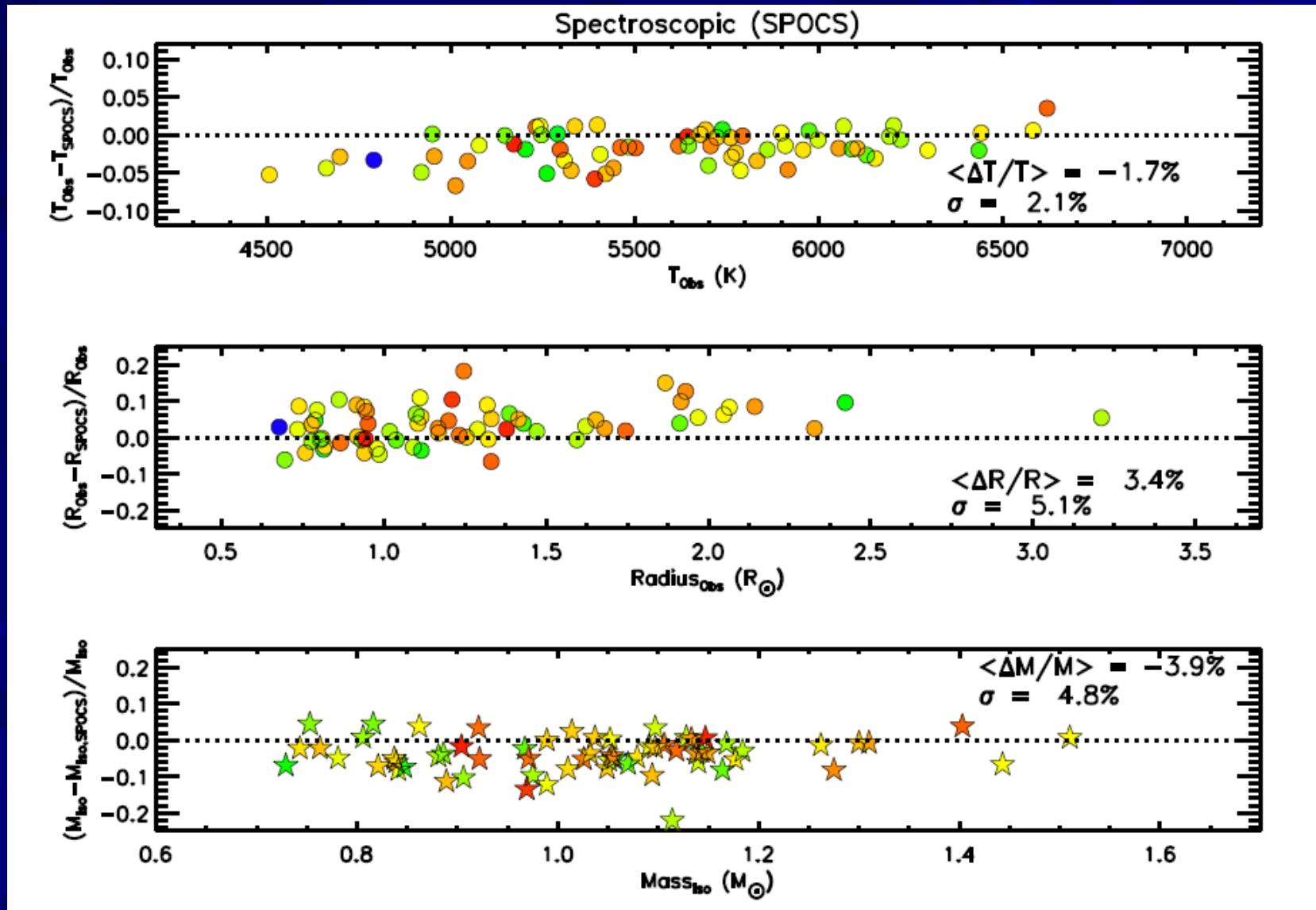
YET

- There are significant disagreements between them that are not resolved

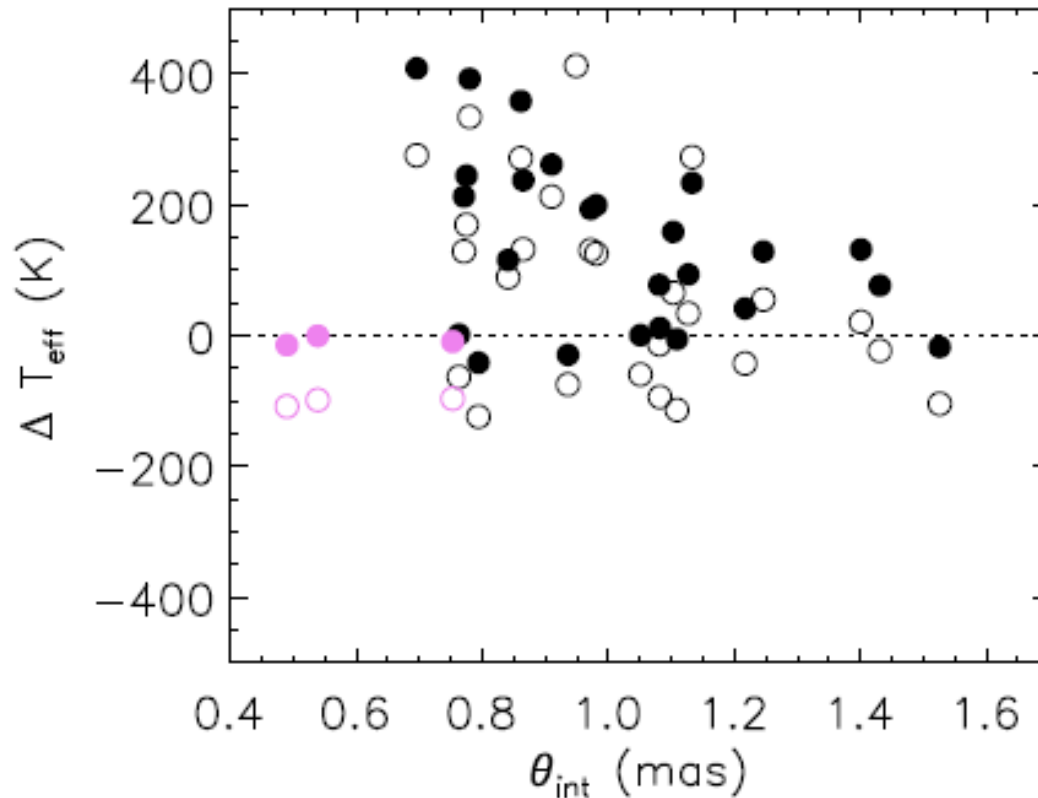
# Interferometry Vs. IRFM/Binaries



# Interferometry Vs. Spectroscopy



# Systematic Errors in Interferometry Data?



Casagrande et al. 2014 (1401.3754)

# The Outer Layers of Cool Stars are Turbulent and Generate Waves

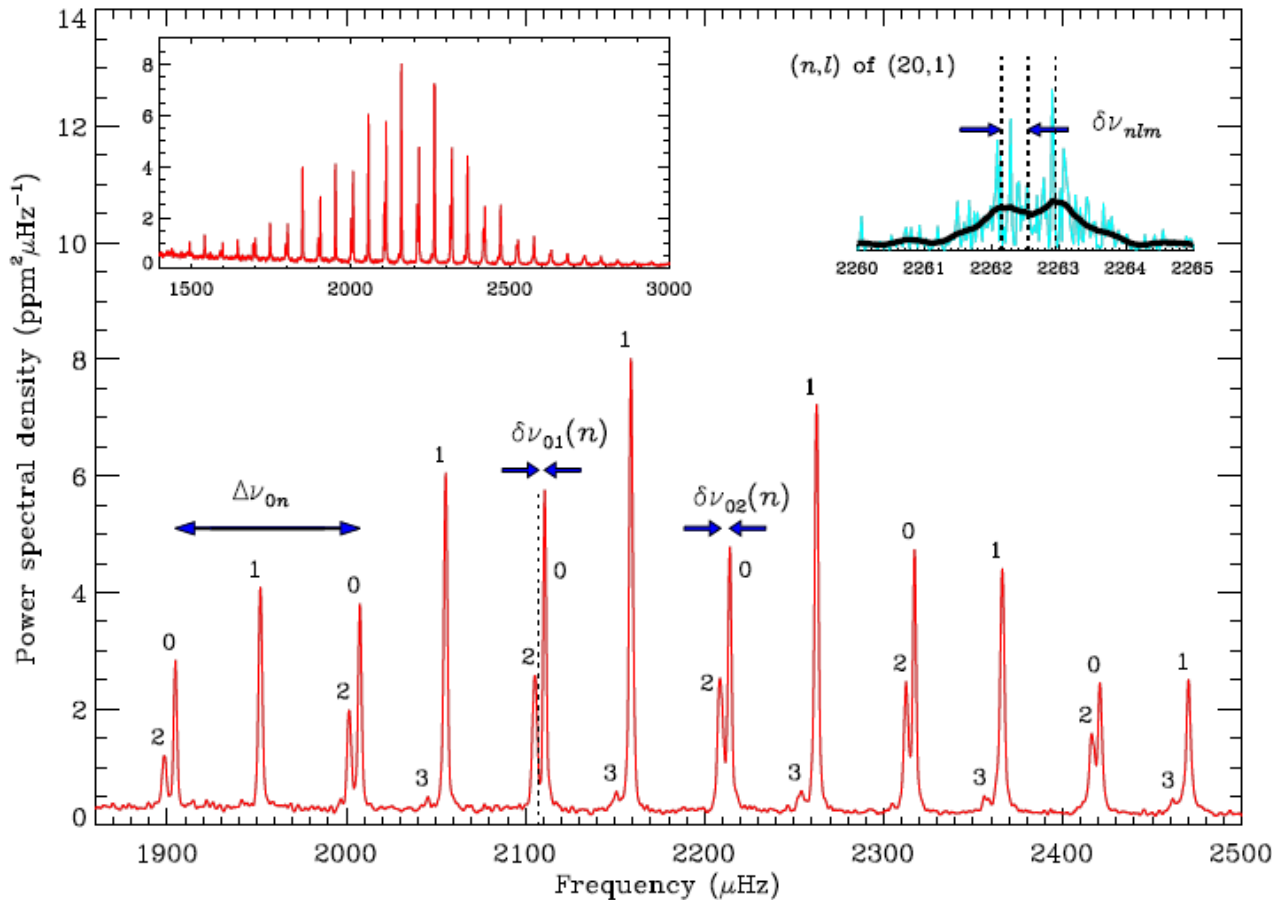
Swedish Solar Telescope

# Solar-like Oscillations in Kepler

$\nu_{\max}$

Rotational Splittings

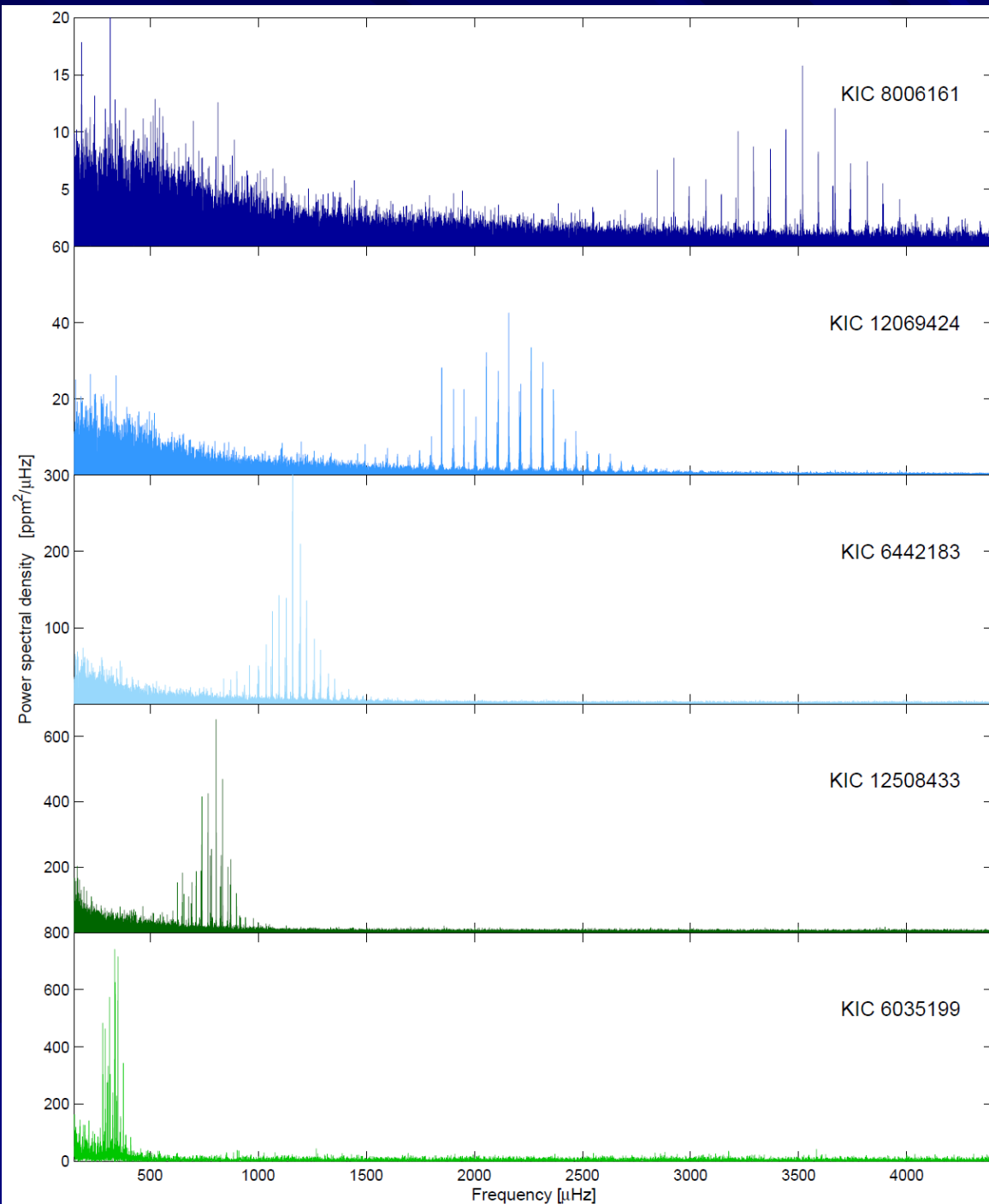
16 Cyg A  
Metcalf et al. 2012



Pure p-mode pattern

# The observed MS pattern is a strong function of $\log g$

From Chaplin & Miglio 2013

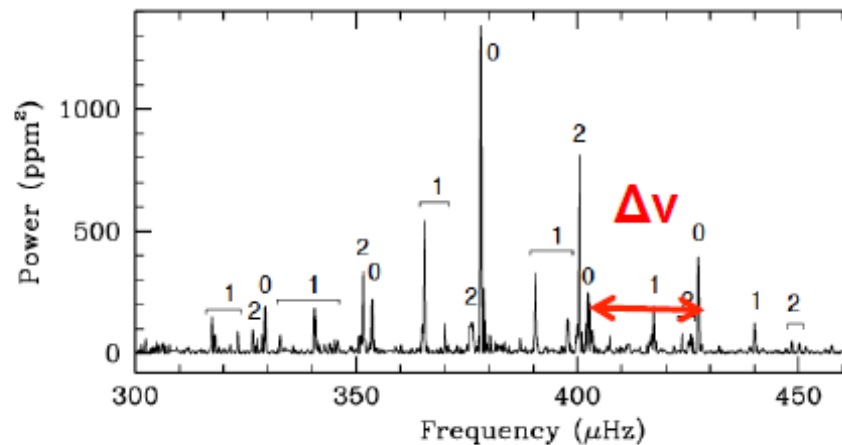
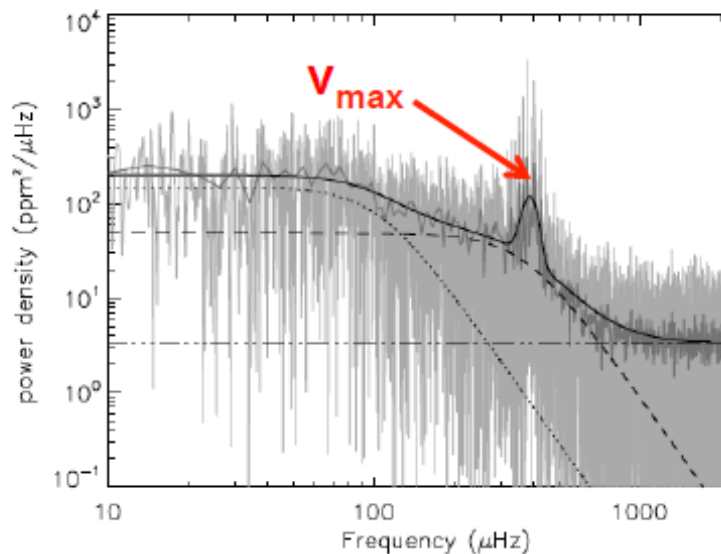


# Interiors: What Do We Learn?

$$\frac{\Delta\nu}{\Delta\nu_{\odot}} = \sqrt{\frac{M/M_{\odot}}{(R/R_{\odot})^3}}$$

$$\frac{\nu_{\max}}{\nu_{\max,\odot}} = \frac{M/M_{\odot}}{(R/R_{\odot})^2 \sqrt{T_{\text{eff}}/T_{\text{eff},\odot}}}$$

Sample power spectrum of red giant KIC4351319 from Di Mauro et al. (2011)



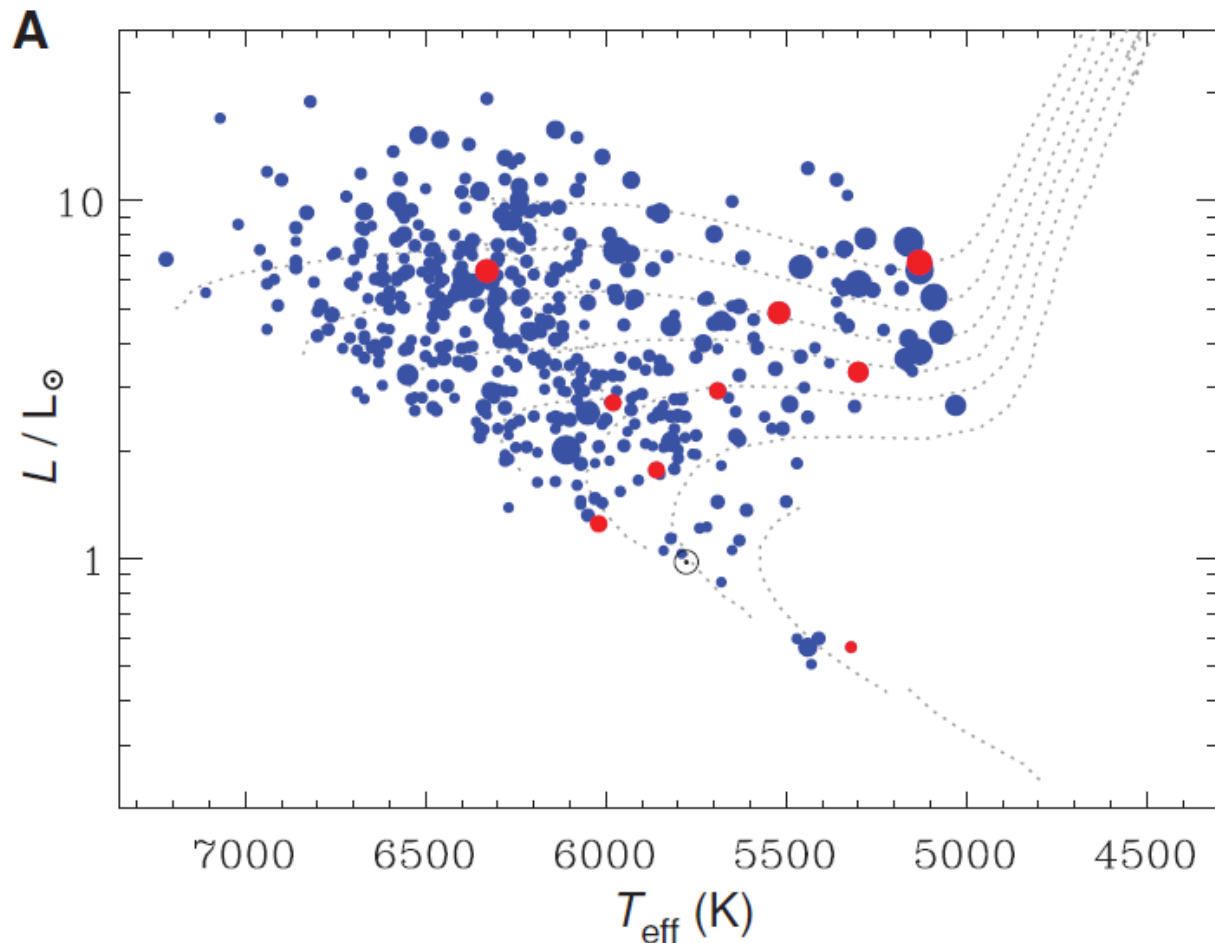


# A Working Tool for Bulk Populations

KASC  
Spectra

Dwarf stars with  
detected sun-like  
oscillations  
from Kepler

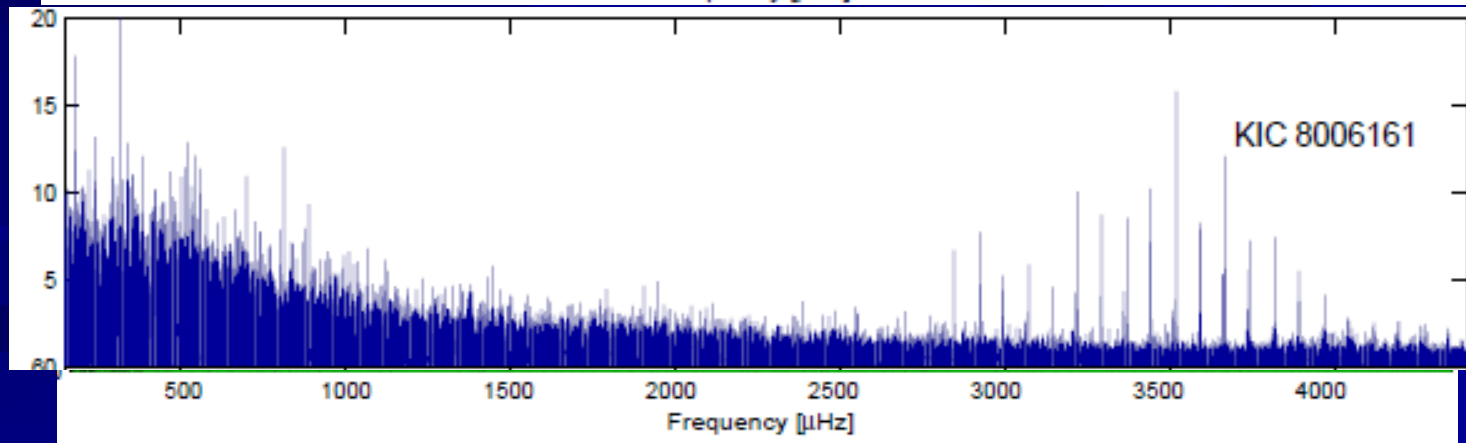
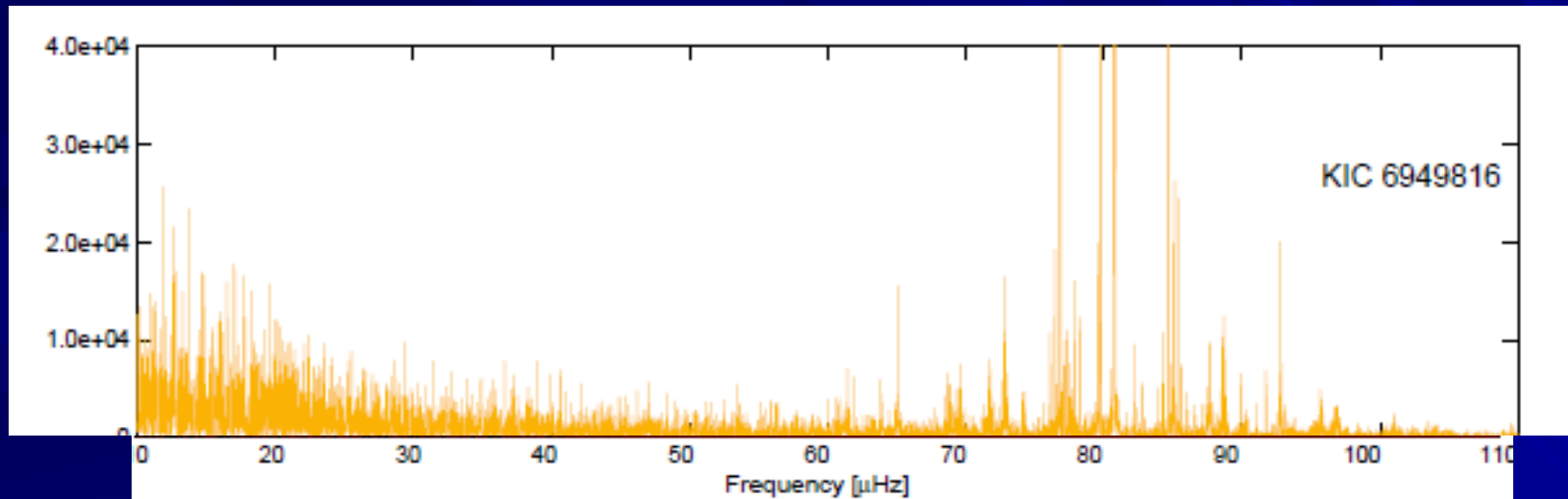
Radius +  
Independent  $T_{\text{eff}}$   
yields distance  
and luminosity  
(Chaplin et al.  
2011, 2013)



# Giants and Kepler

- Giants are high-amplitude pulsators
  - Periods of days to months
- Long period is a huge advantage
  - ⇒ Accessible with 30 minute cadence
  - ⇒ 14,000 stars monitored, essentially all detected (Mosser et al. 2009; Hekker et al. 2010)
- Observed frequency pattern is complex!

# Giant and Dwarf Frequency Patterns Compared



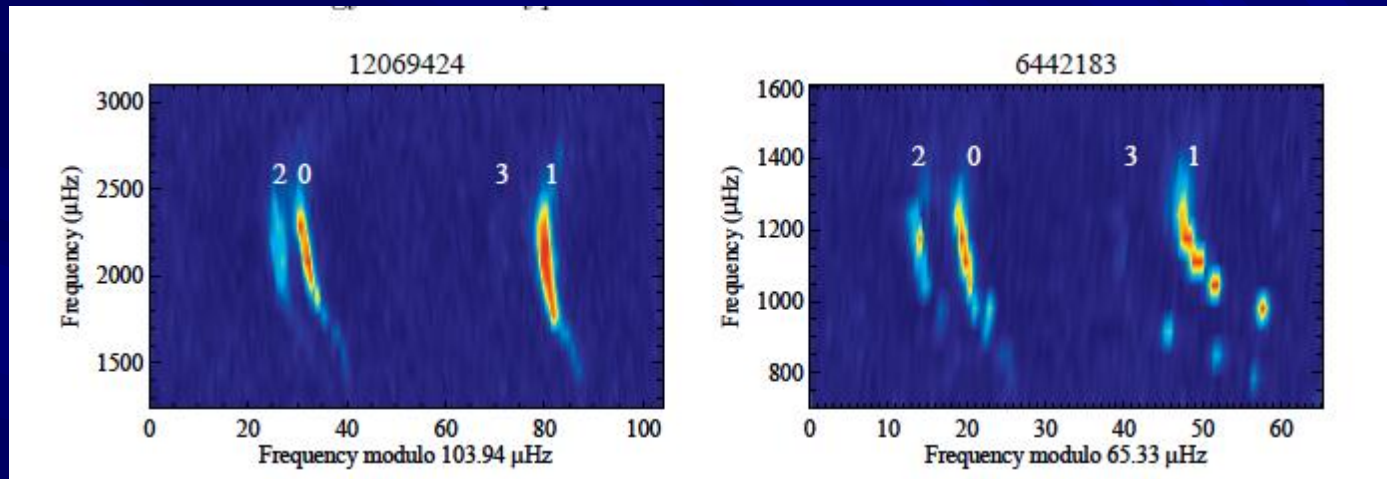
# The Complex Giant Pattern is Explained by Mixed Modes

- Mixed modes propagate as p-modes in the convective envelope and g-modes in the deep core; especially strong impact on  $l=1$
- $l=0$  modes are pure p-modes
- Seen in red giants (Bedding et al. 2010) because the p and g mode frequencies become commensurate
- Comparing the two yields distinct diagnostics of core and envelope properties

# Distinct Patterns in Different Evolutionary States

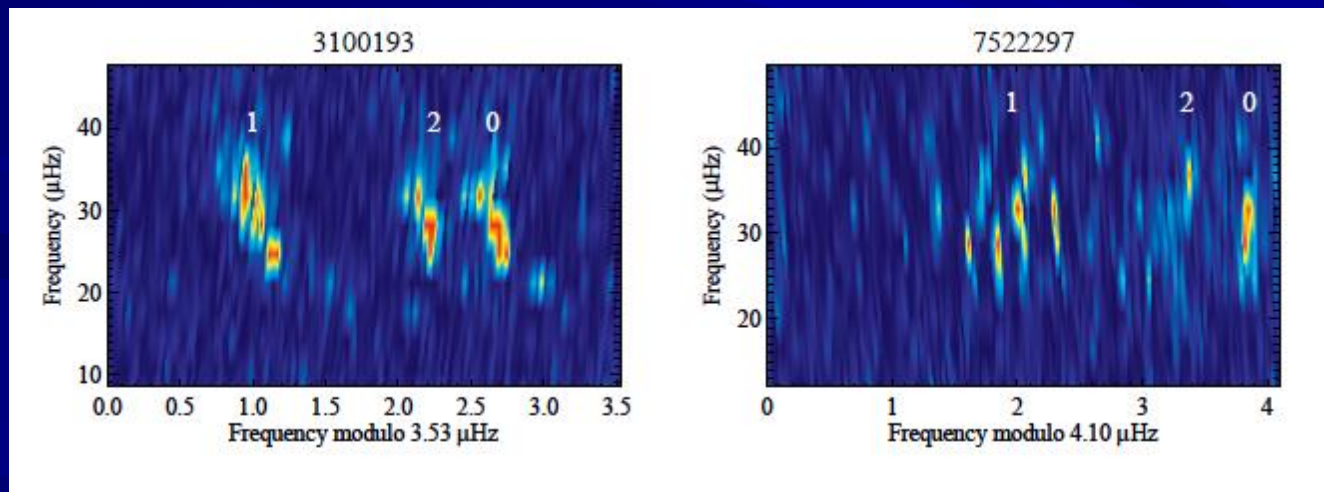
Dwarf

Subgiant



RGB

RC

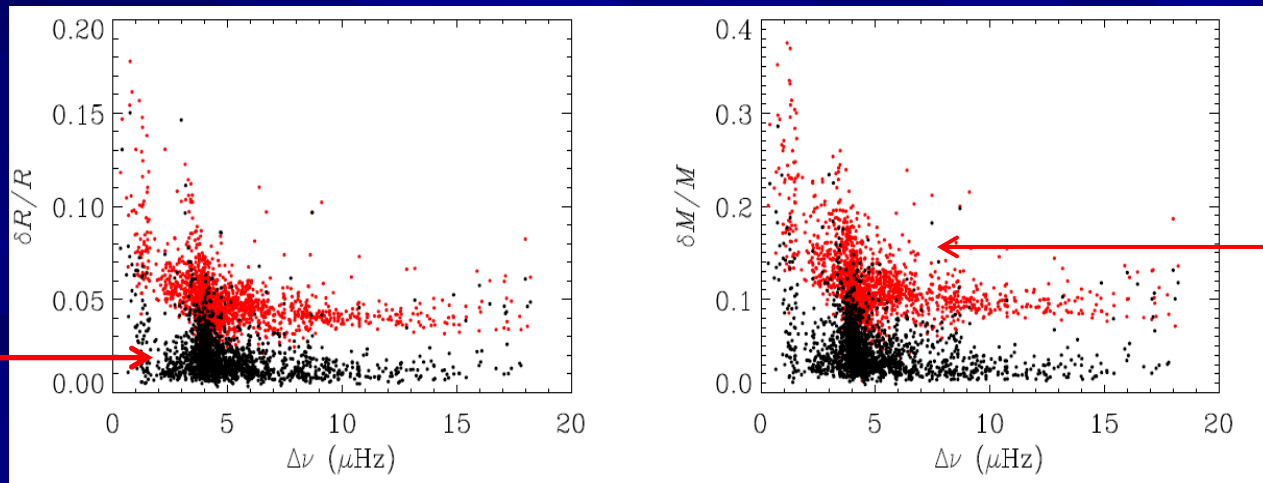


CM  
13

# The APOKASC Approach: DR10

- APOGEE sample: ~2,400 Red Giants
  - 1916 stars that pass quality control checks
- Analyze light curves, extract mean asteroseismic properties ( $\Delta\nu$ ,  $\nu_{\max}$ )
- R+M from Scaling Relations + Grid-based Modeling

Scatter,  
Method  
To Method

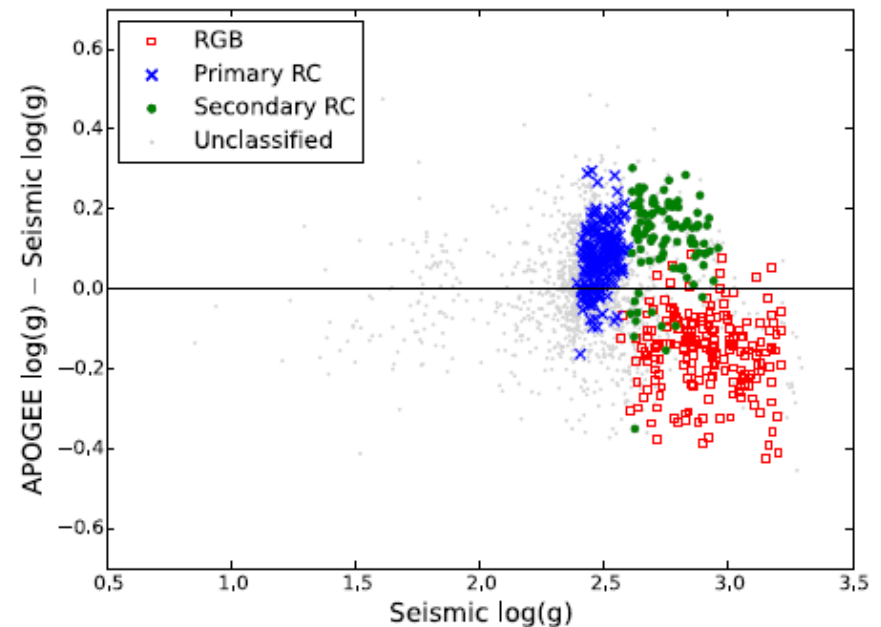
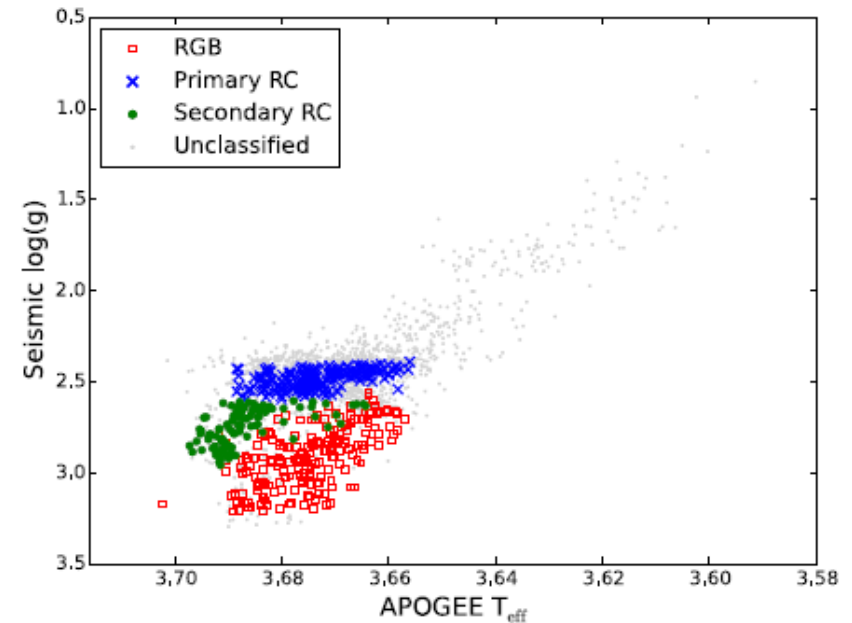


Total  
Error

← Luminosity

# A Test of Atmospheres

- The difference between asteroseismic and spectroscopic  $\log g$  is different for RC, RGB
- Is this an atmospheres or asteroseismic systematic?

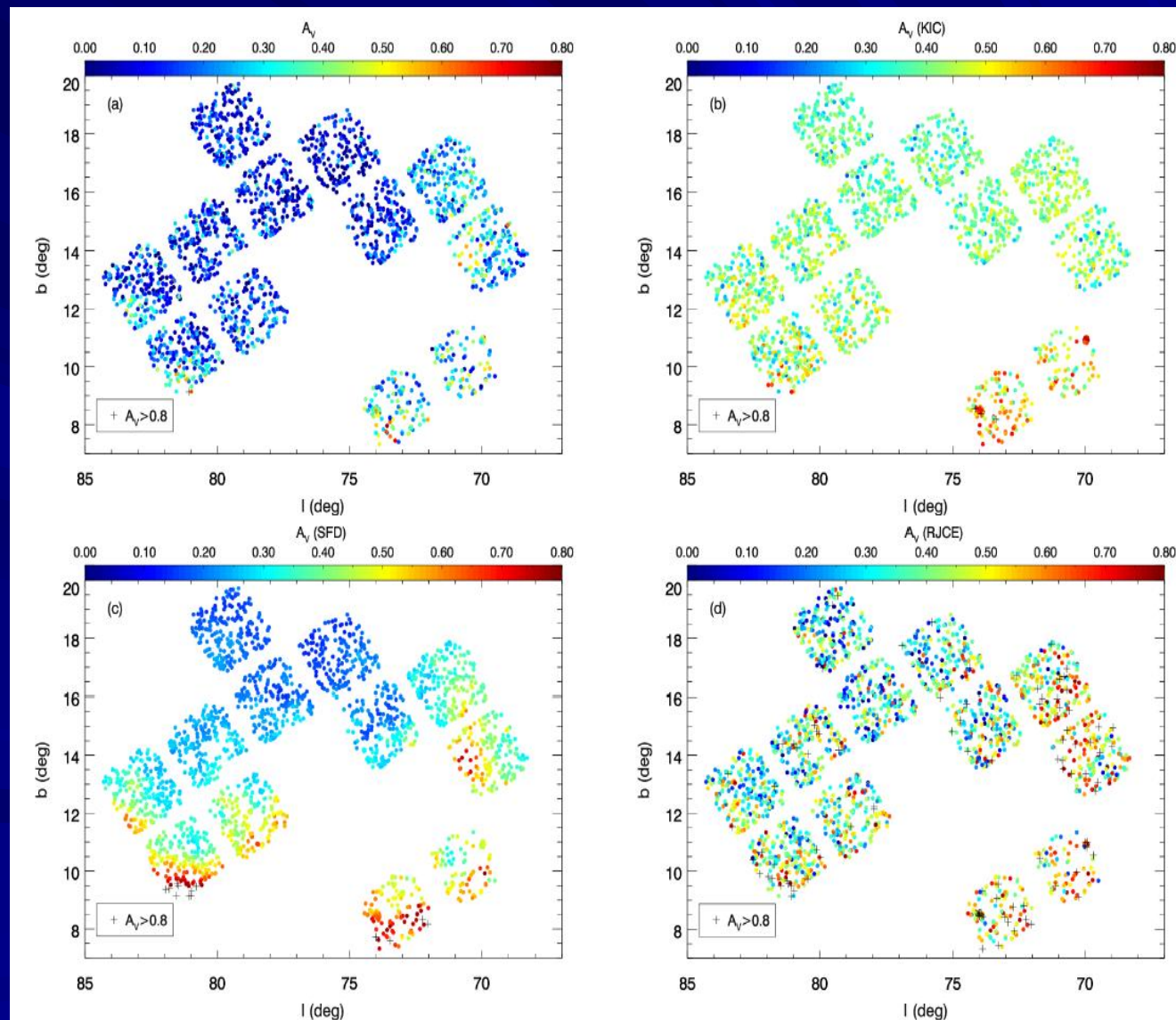


# Rodrigues et al. 2014: SED Fitting and the KIC Extinction

## Rodrigues et al. Extinction Map

## KIC Extinction Map

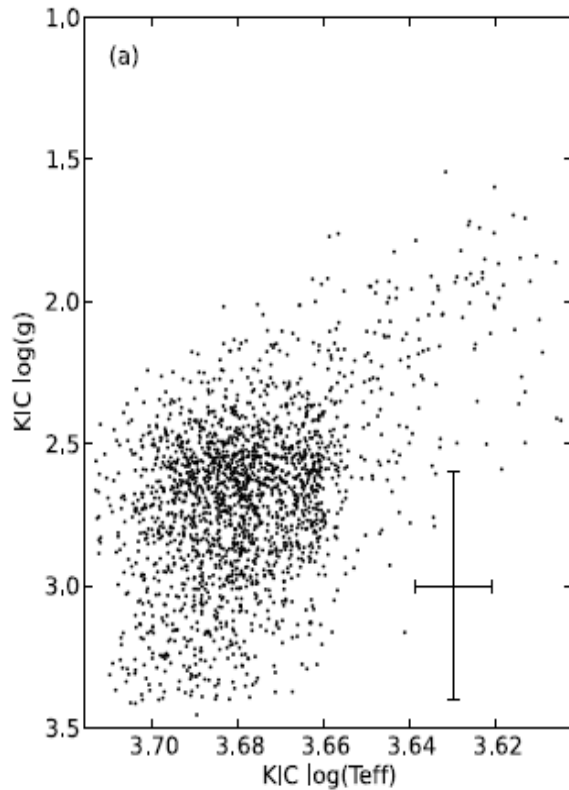
Bottom Line:  
Inferred extinction  
~0.41-0.42 KIC  
(also SAGA)



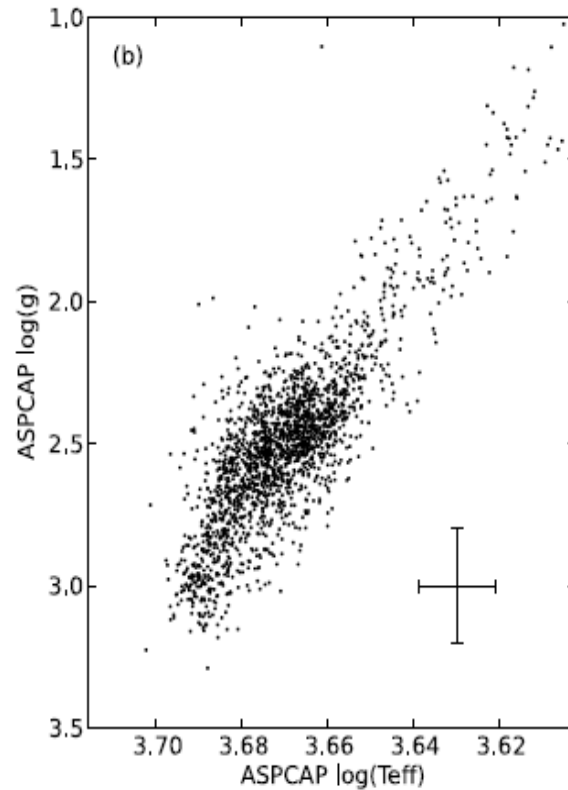
SFD  
(Maximum)  
Extinction  
Map



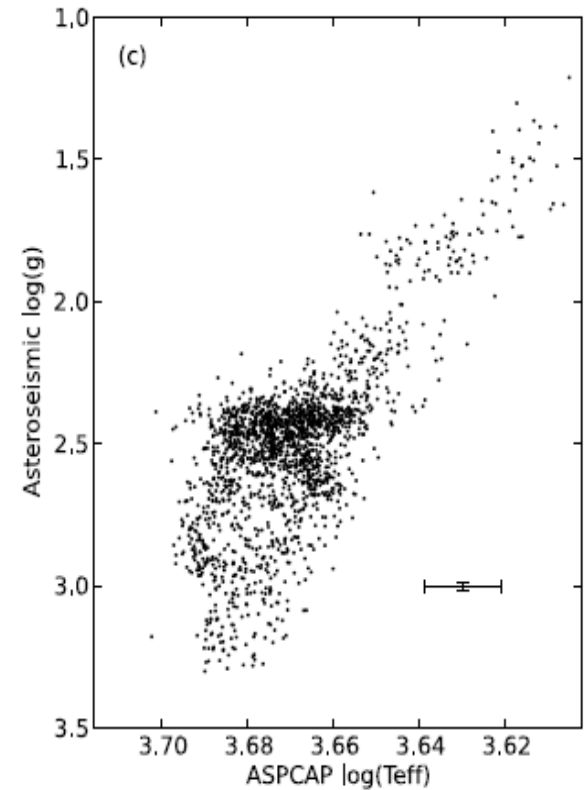
# Results: Snapping Into Focus



Photometry

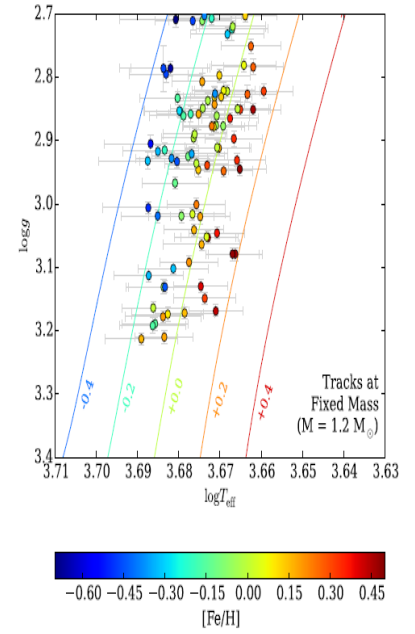
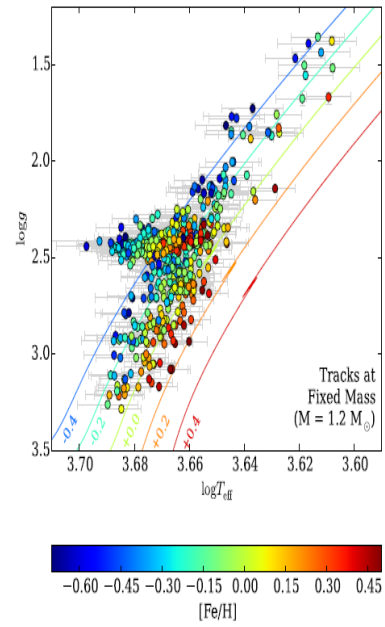
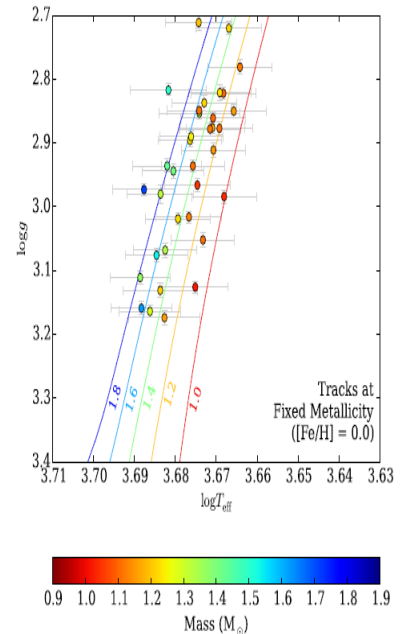
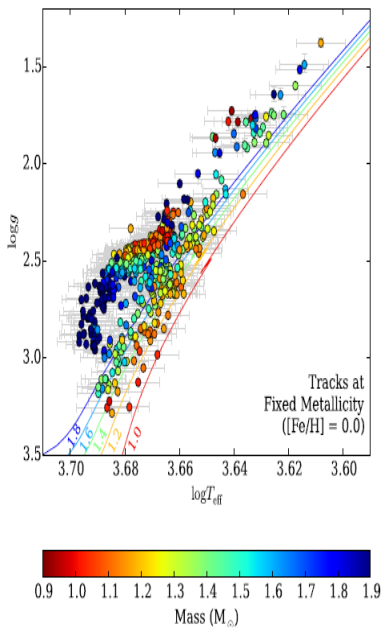


Spectroscopy



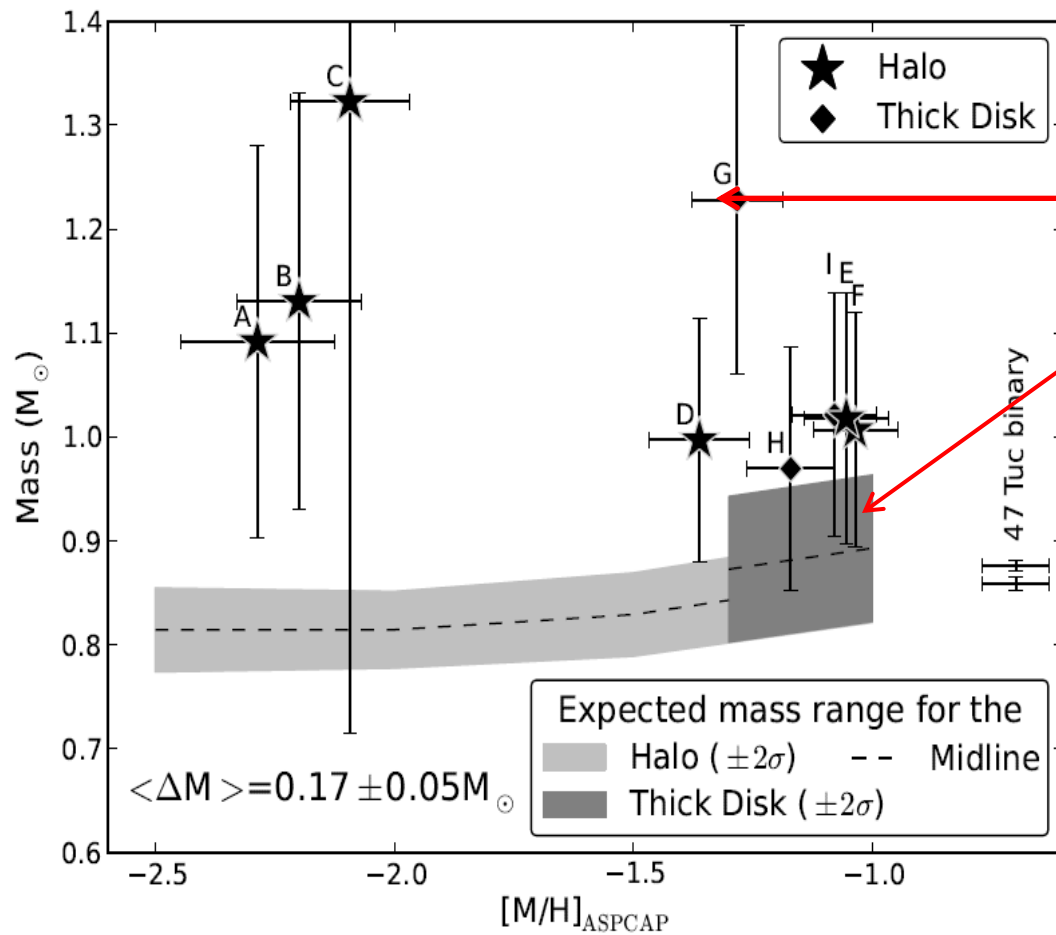
Asteroseismology +  
Spectroscopy

# Mass Trends, Metallicity Trends, Fixed [Fe/H]      Metallicity Trends, Fixed Mass



# Trouble In Halo-Land

Epstein et al. (2014)



Halo Star  
Masses  
From SR  
Are Well  
Above  
Expected  
Values....

# Do We Need to Go Beyond Scaling Relations?

*Calibrate...Correct...OR*

Boutique Modeling:  
Reasonable Mass!

Parallax+  $\Delta\nu$ :  
Reasonable Mass!

