

# Buoyancy-driven currents and sediment transport in the ocean

Ben Kneller (University of Aberdeen)

Mohamad Nasr Azadani (UCSB)

With Eckart Meiburg, Brendon Hall, Vineet Birman (UCSB)

Rolf Henniger (ETH)

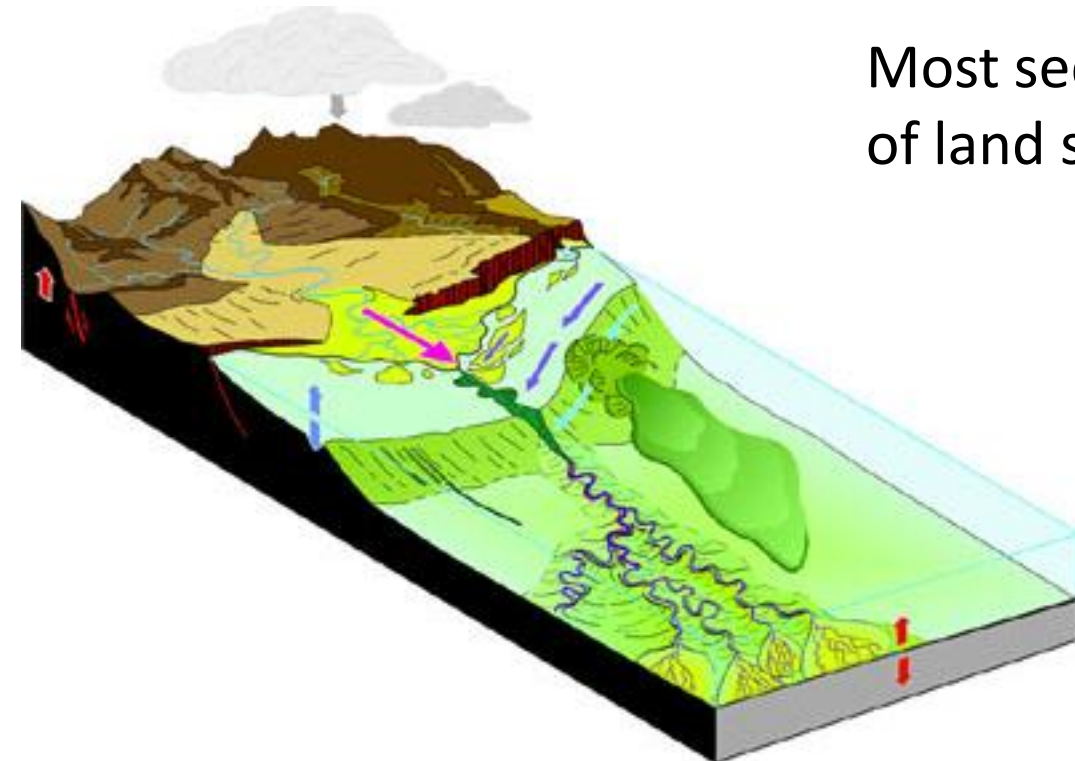
Carolina Boffo, Rafael Manica, (IPH, Federal University of Rio Grande do Sul, Brazil)

Thang Tat Nguyen (University of Aberdeen)

# Context



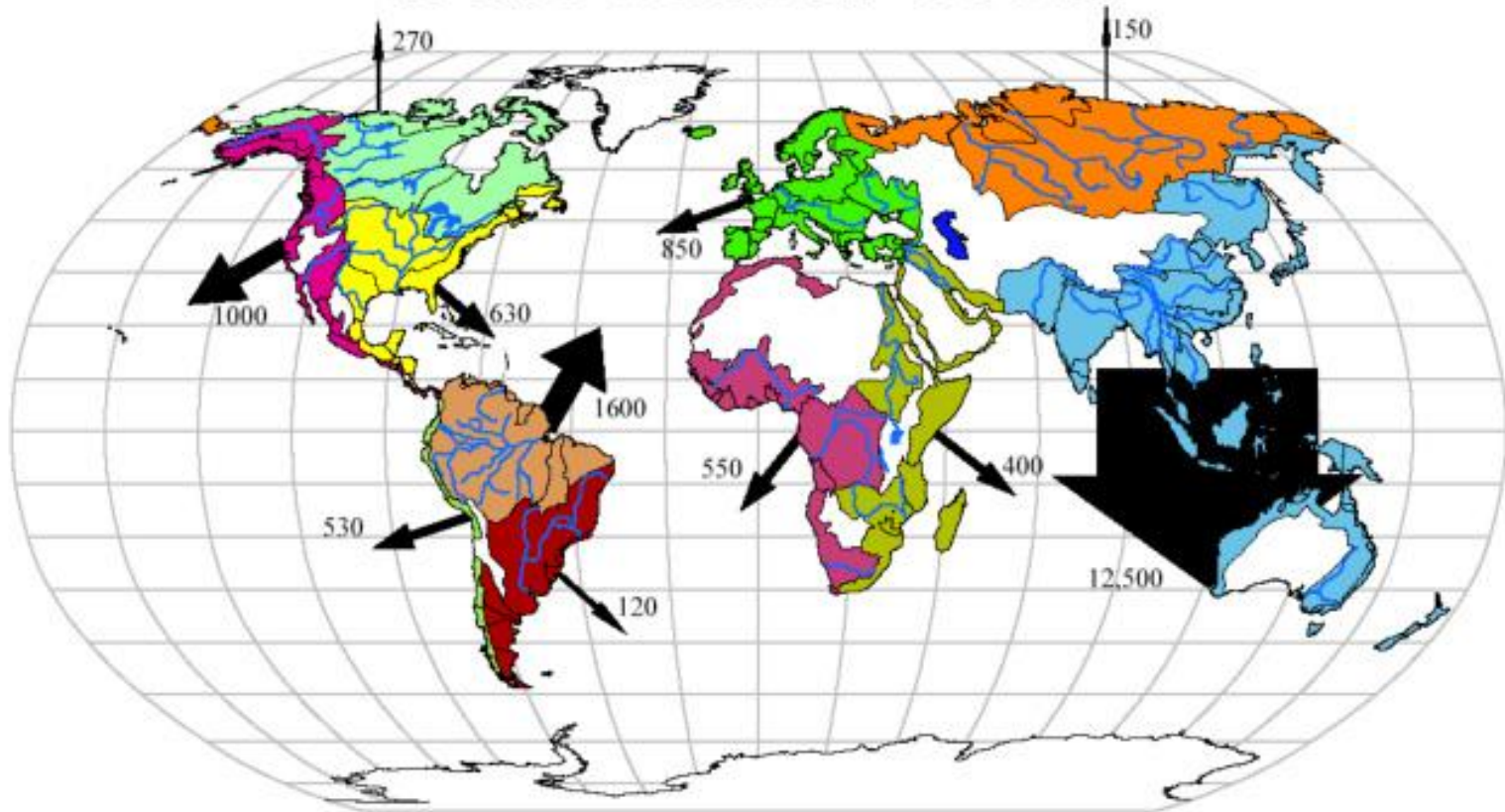
Most sediments derived from erosion of land surfaces reach the ocean





# Context

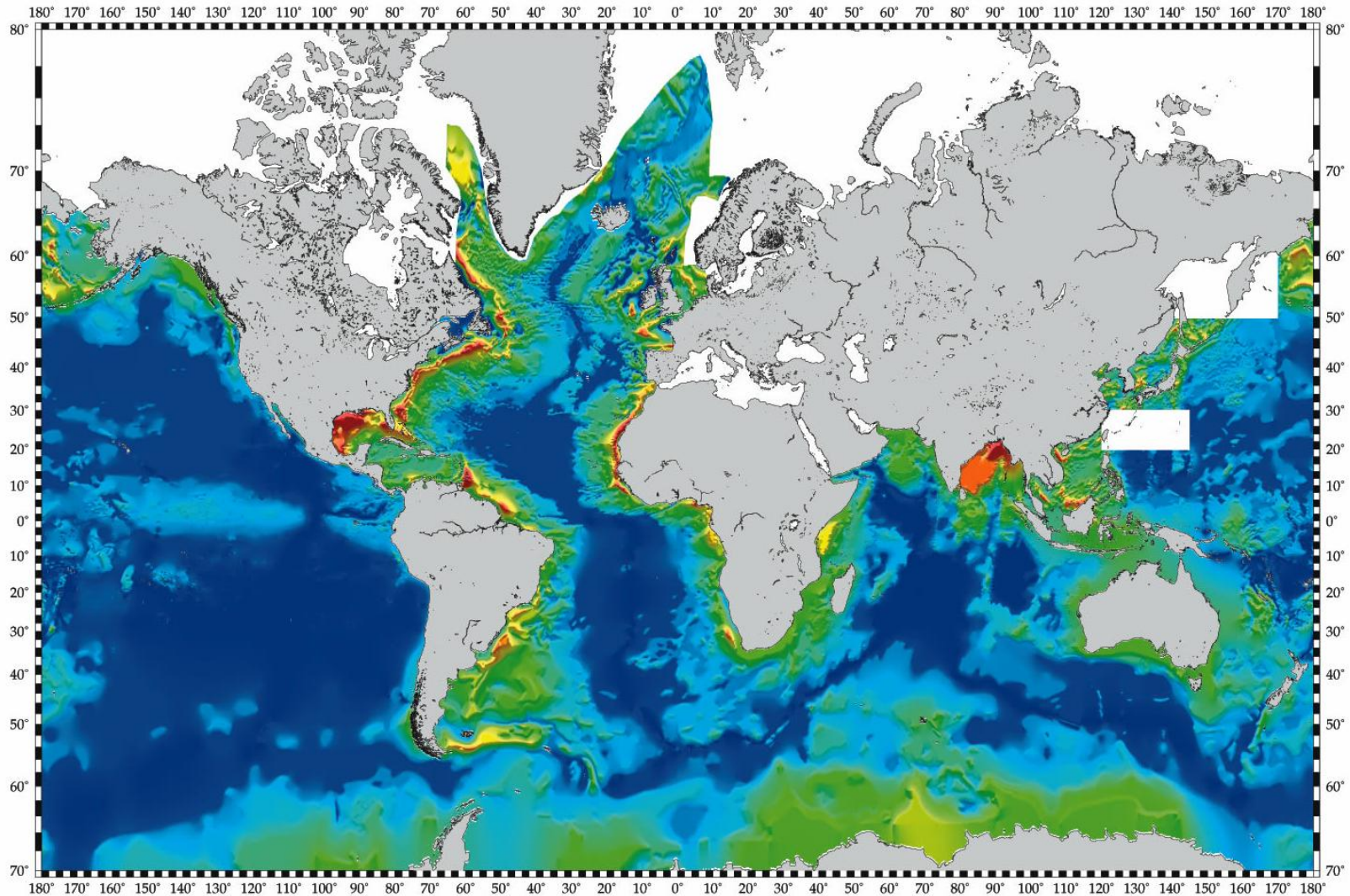
## Fluvial Discharge of Suspended Sediment to the Coastal Ocean



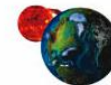
Total =  $19 \times 10^9$  tonnes per year (Milliman and Farnsworth, 2011)

# Context

## ***Total Sediment Thickness of the World's Oceans & Marginal Seas***

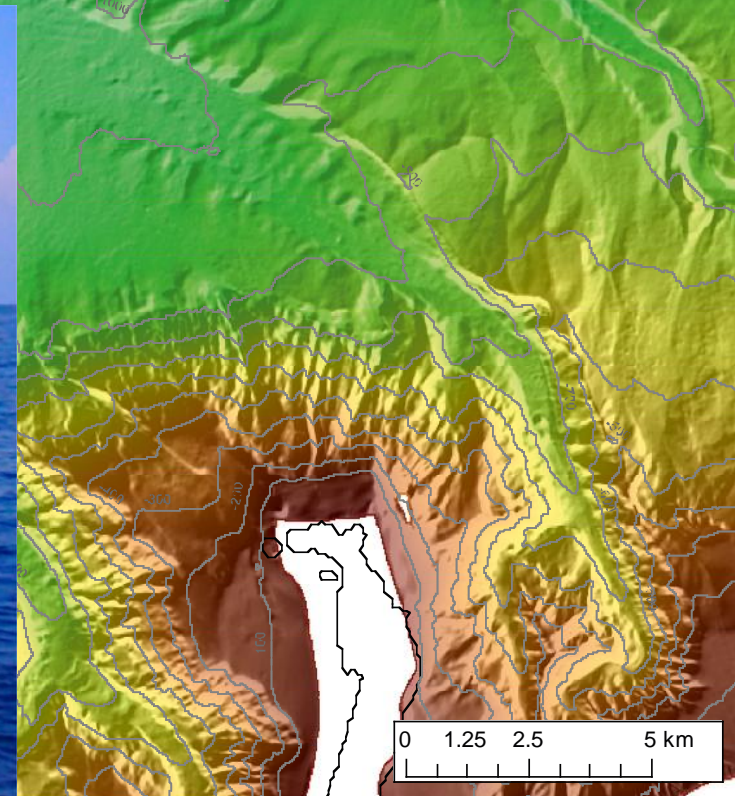
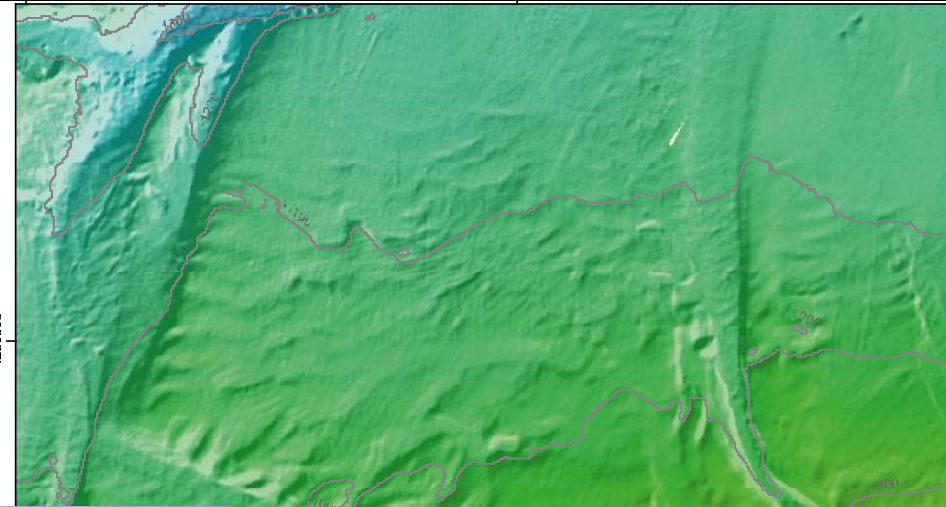


Thickness in Meters



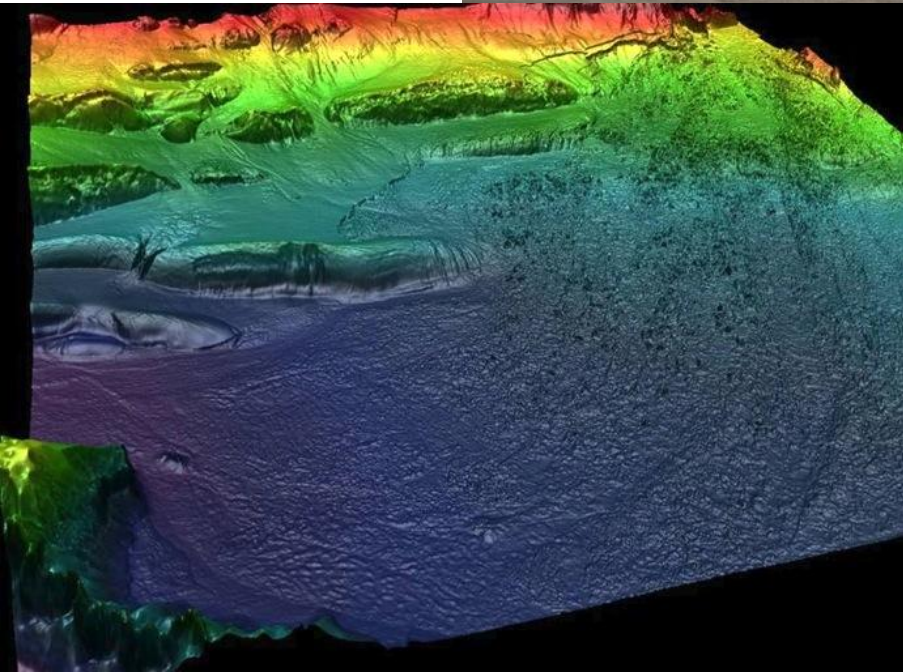


# Context

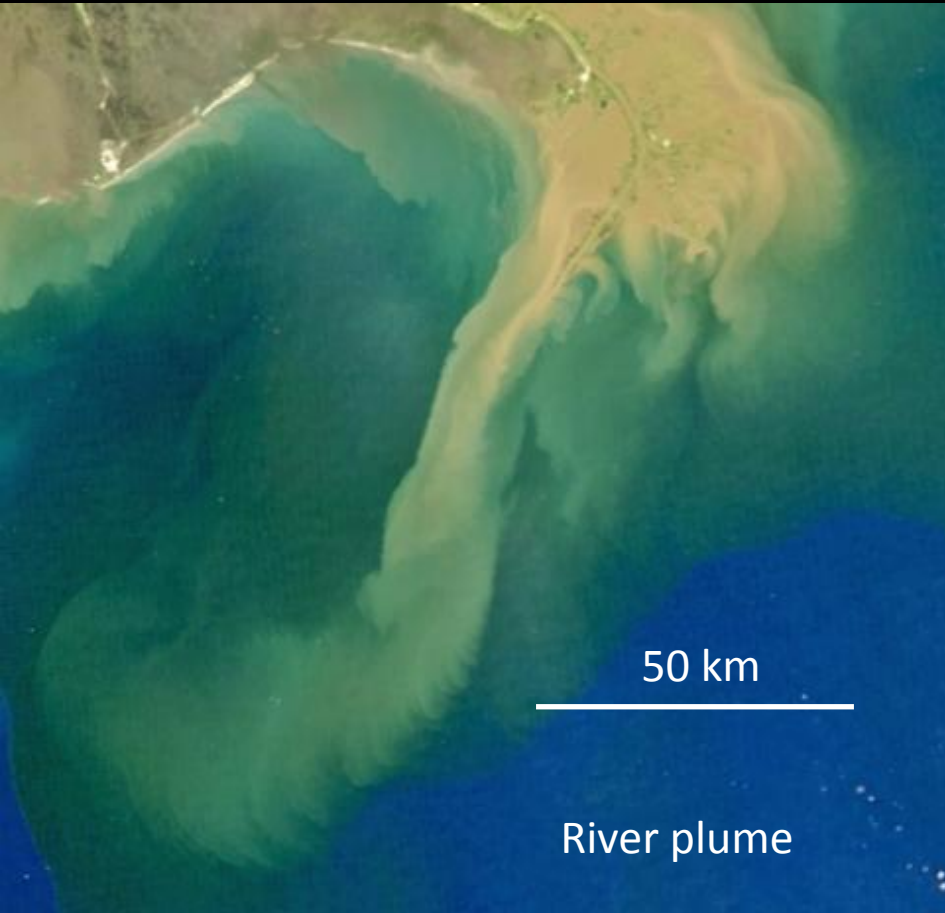




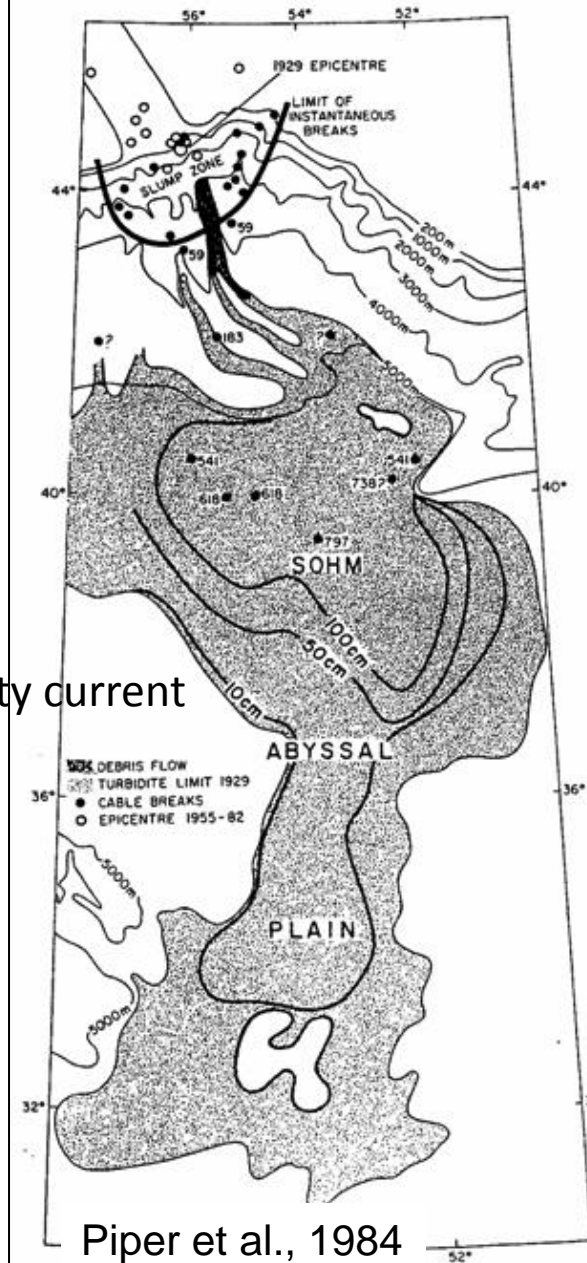
submarine landslides, ice-rafted debris, pelagic settling



# Fluid-mediated transport of sediment to deep water



Turbidity current



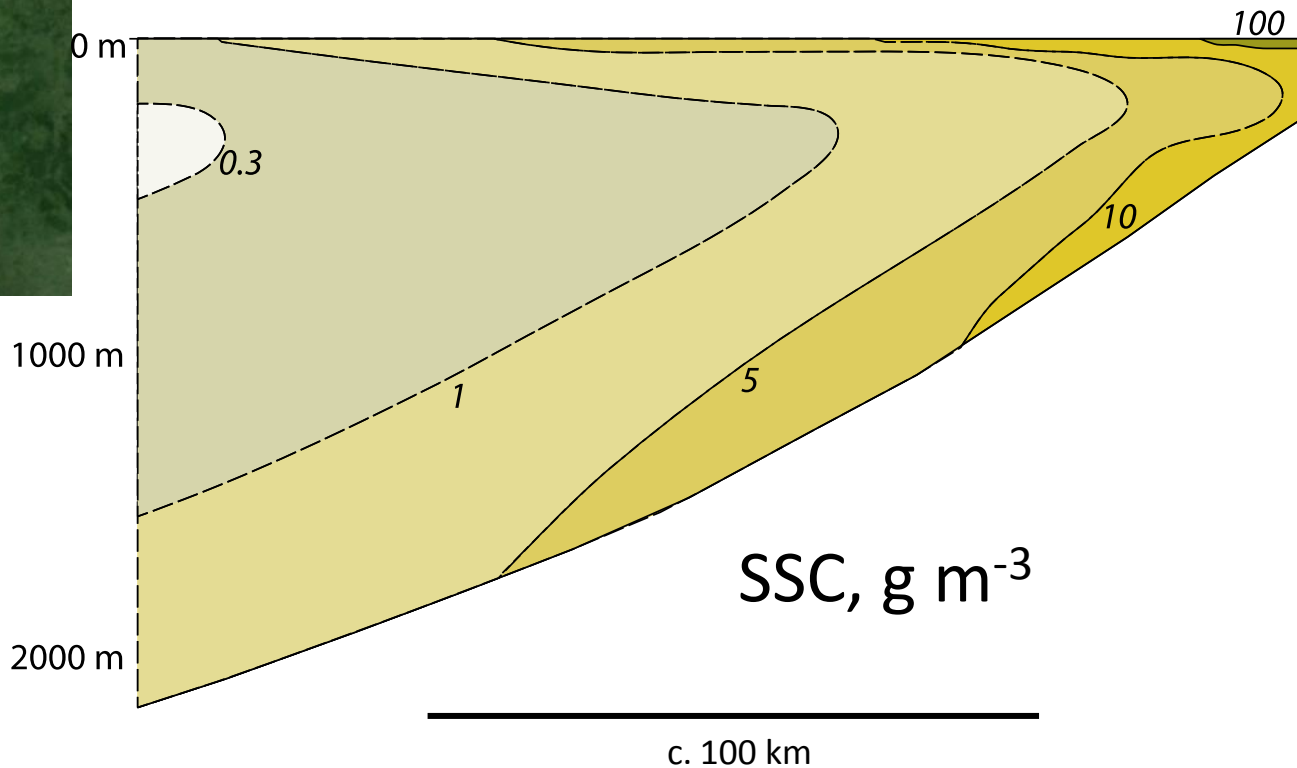
- Both buoyancy-driven
- Turbulence maintains sediment suspension, affecting buoyancy
- Between them these two processes account for most of the sediment in the deep sea



# River plumes

How do they go so far?

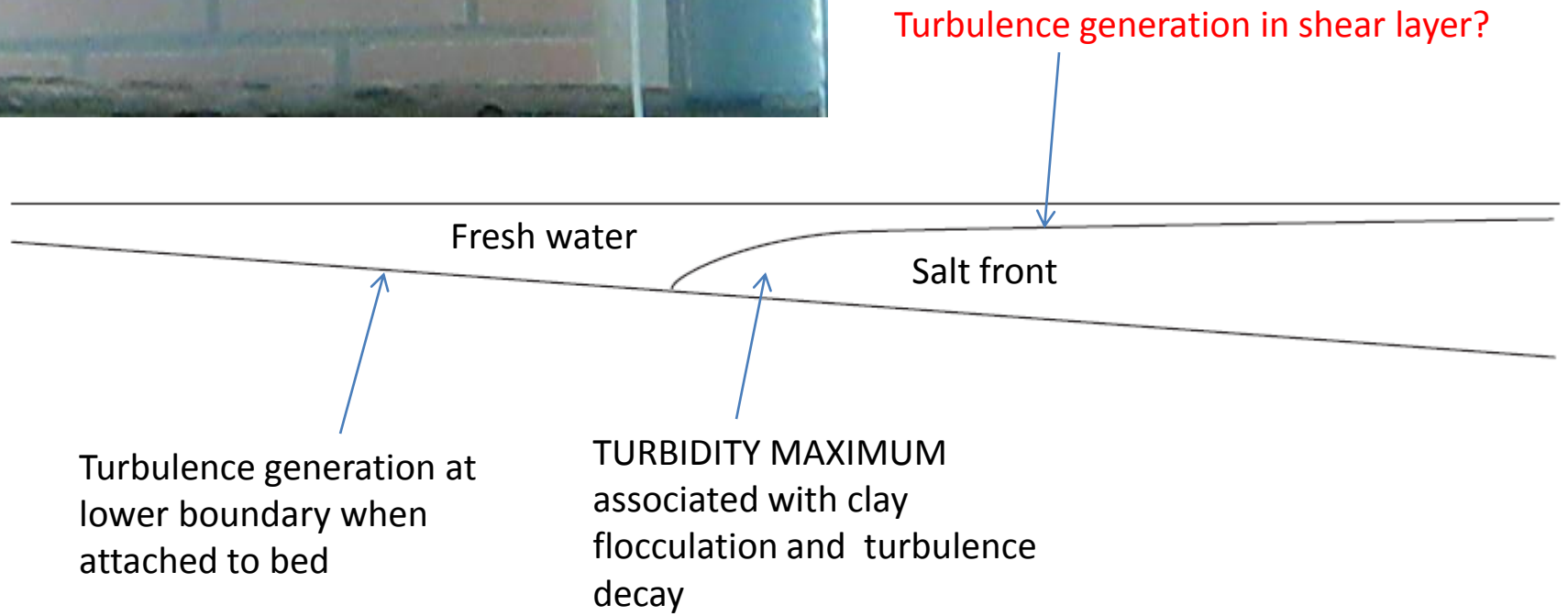
What maintains suspension?



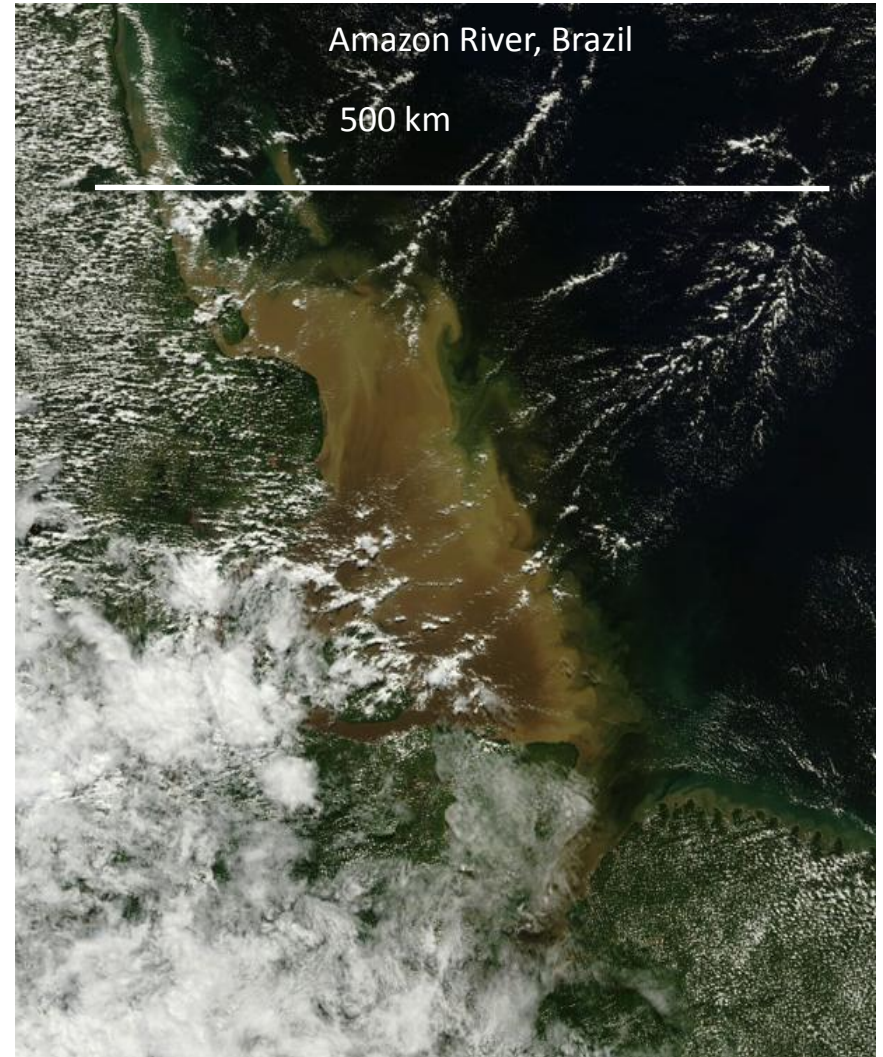
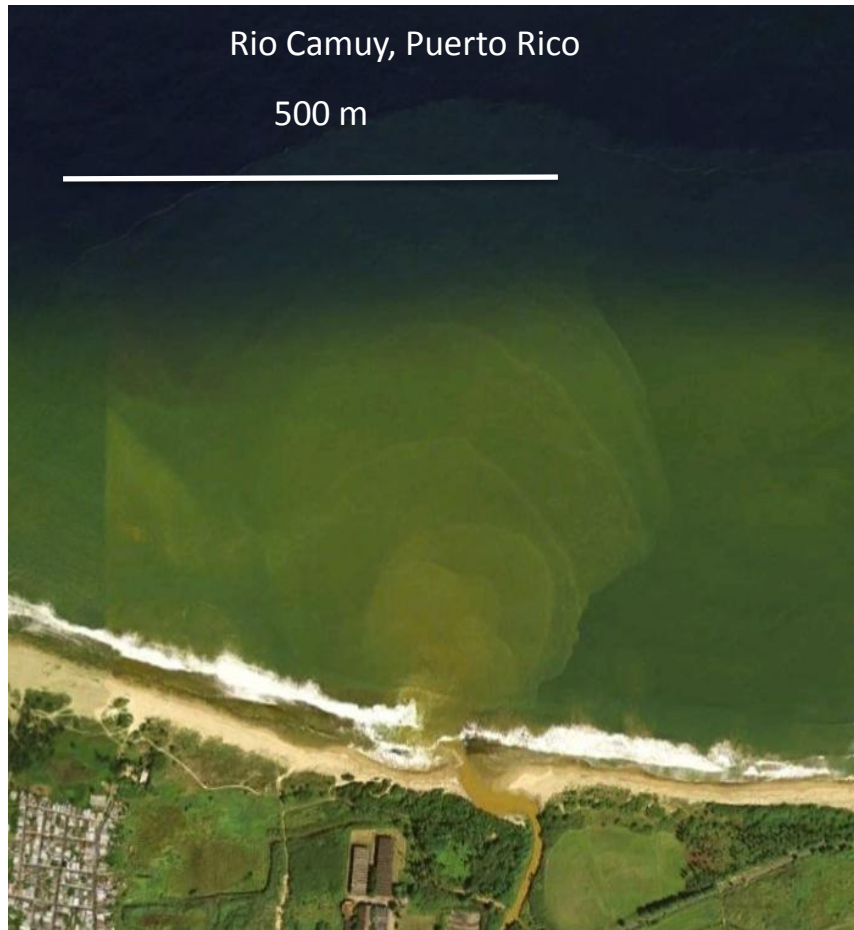
Particulate matter  $>5 \mu\text{m}$  in Congo River plume.  
Eisma & Kalf, 1984



# Positively buoyant surface plume



# River plumes



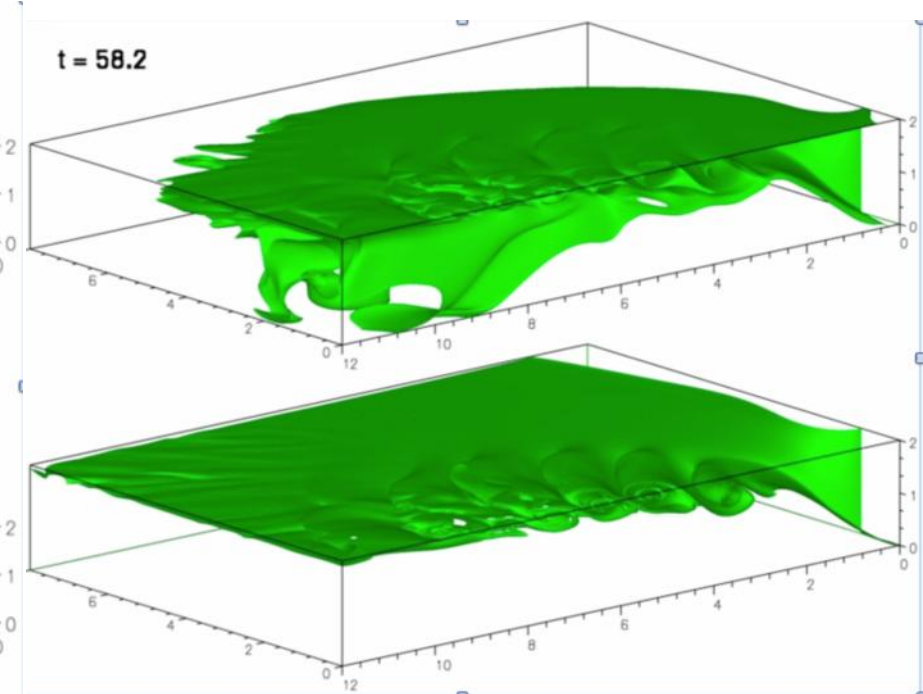
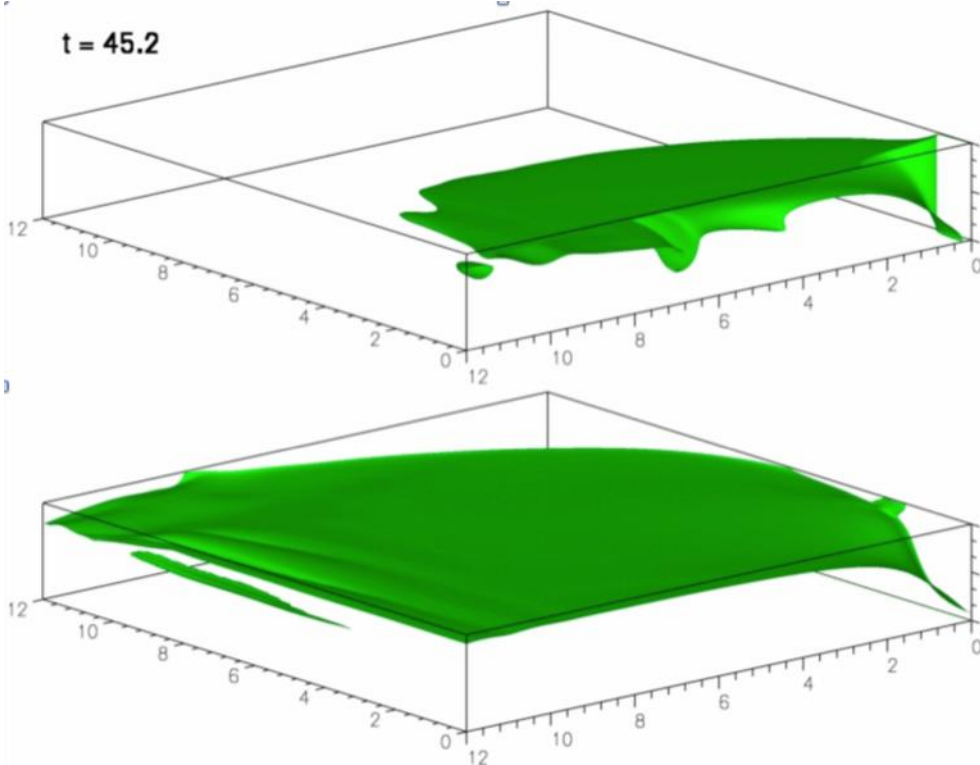


# Plume lower boundary stability – numerical simulation

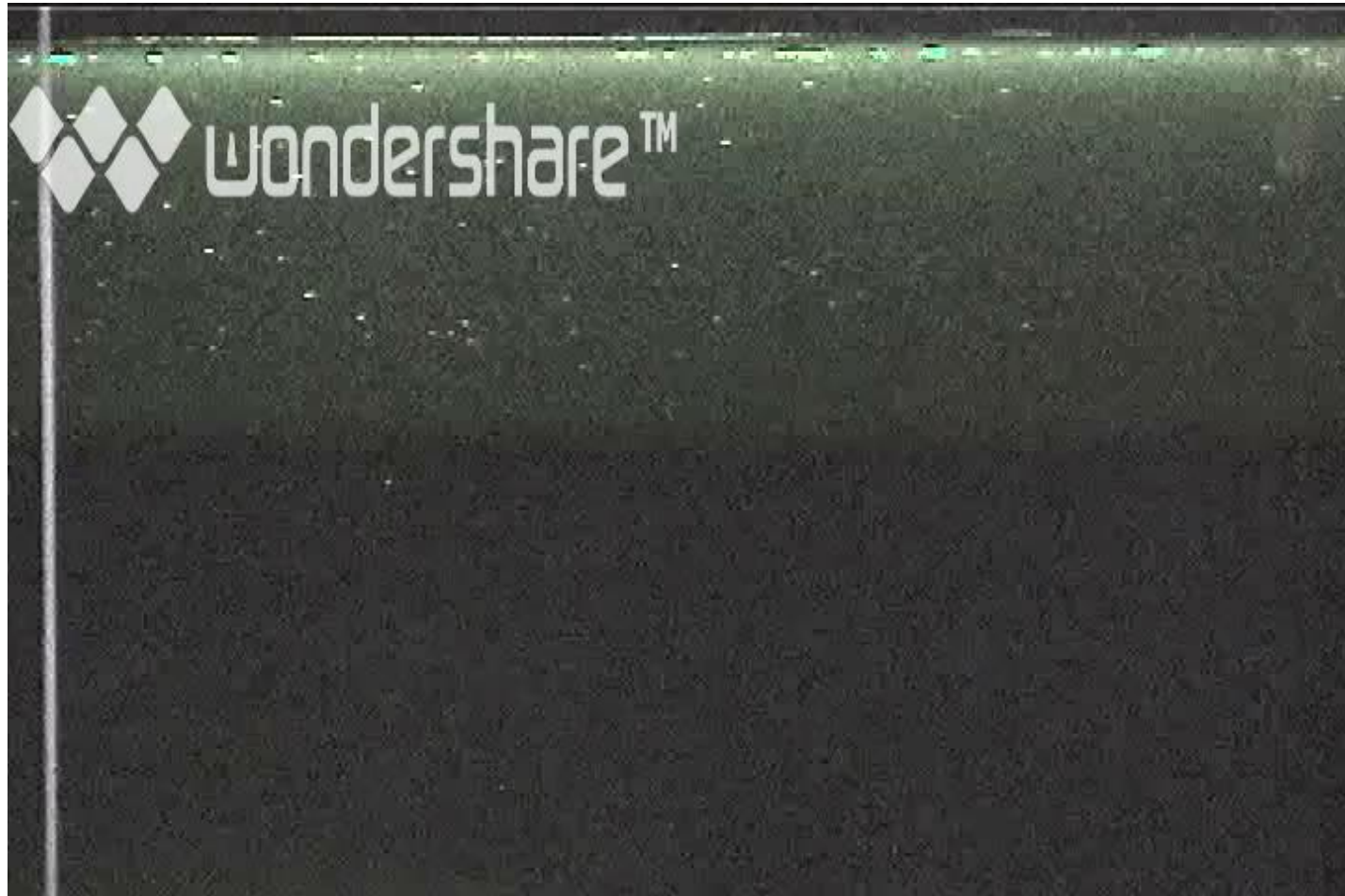
Stability of lower boundary is given by a gradient Richardson number  $Ri_g$ .

Typically the stratification is stable for  $Ri_g > 0.25$ .

$$Ri_g = \frac{\left( g \frac{\partial \rho / \partial z}{\rho_a} \right)}{(\partial u / \partial z)^2}$$

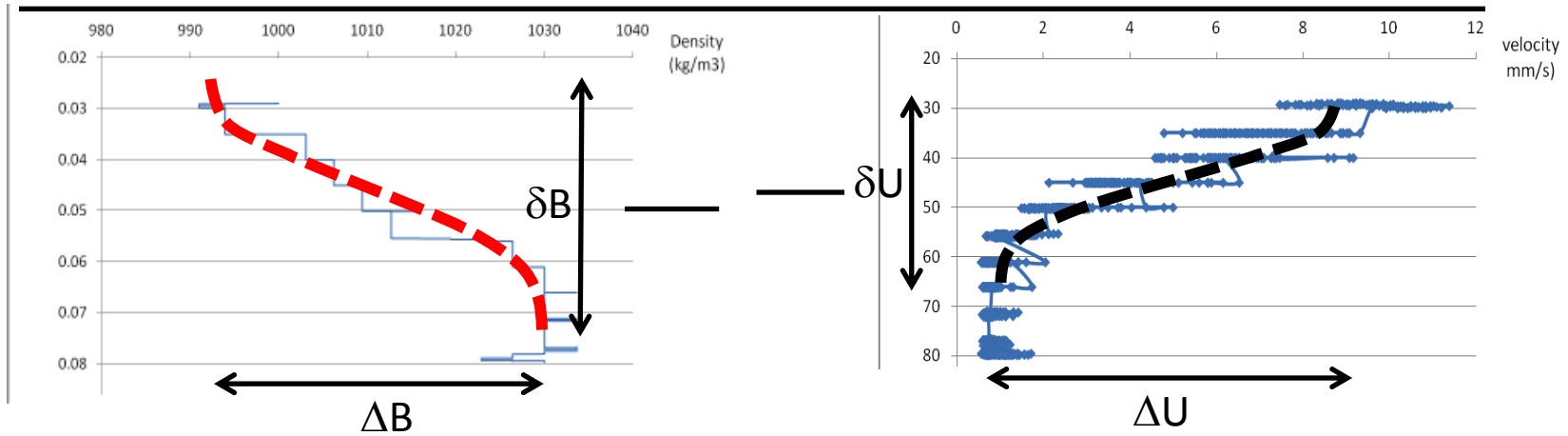


# Plume lower boundary stability – laboratory experiment





# Plume lower boundary stability – laboratory experiment



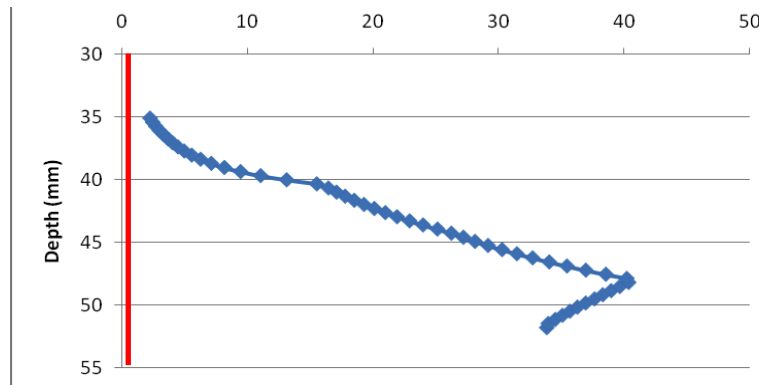
## Density

(calibrated resistivity probe)

## Velocity

(Constant Temperature Anemometry - 'hot wire' probe)

## Gradient Richardson number

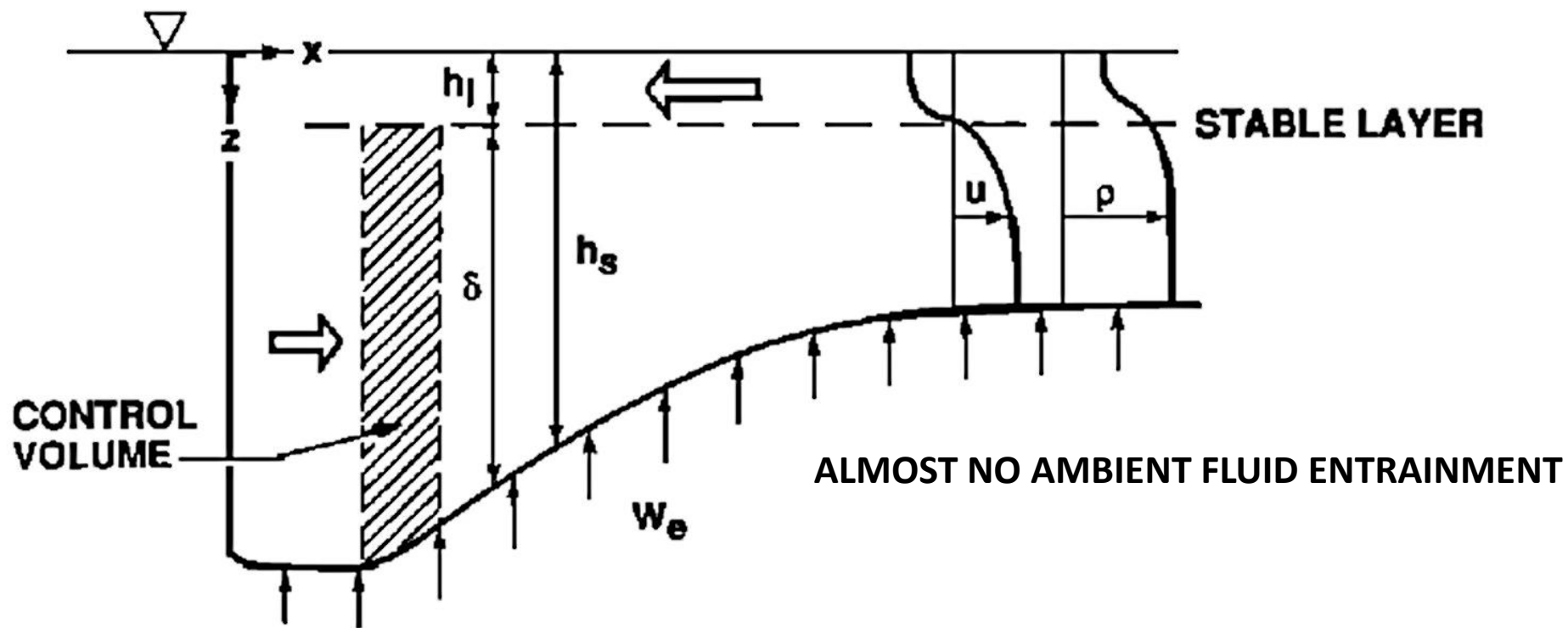


$$Ri_g = \frac{\left( g \frac{\partial \rho / \partial z}{\rho_a} \right)}{(\partial u / \partial z)^2}$$

Stability of stratification suggests that long-range sediment transport by river plumes depends upon wave-generated turbulence

# Plume lower boundary stability – environmental measurement

Leschenault Estuary, Koombana Bay, Western Australia

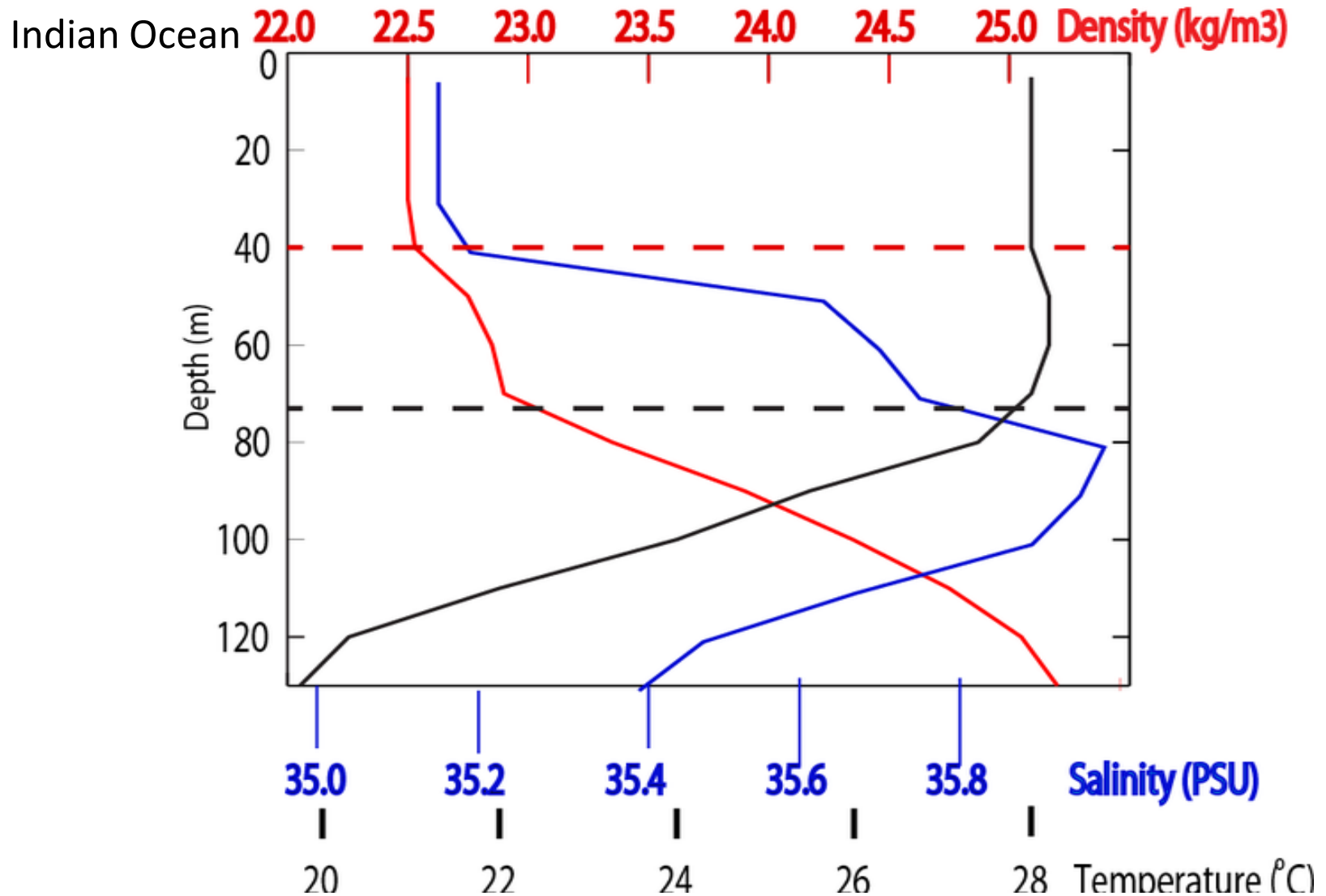


Luketina & Imberger, 1989

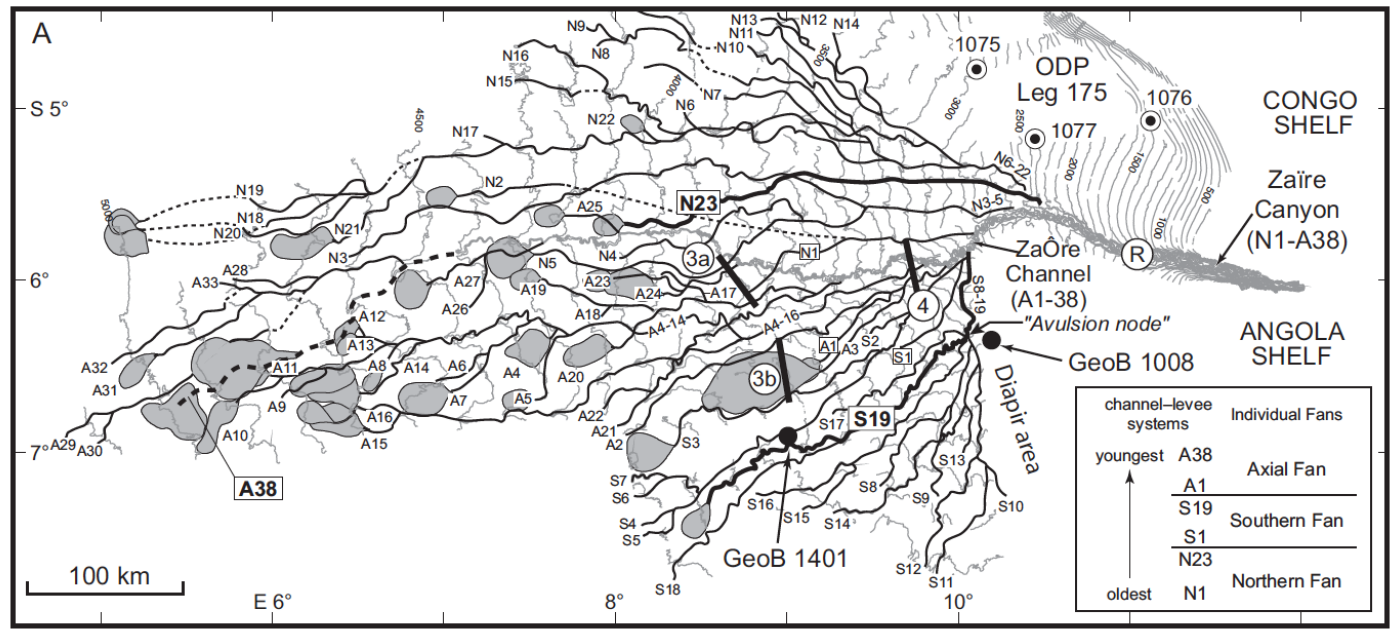


# Ocean mixing layer

Turbulent mixing by surface waves and wind-induced shear

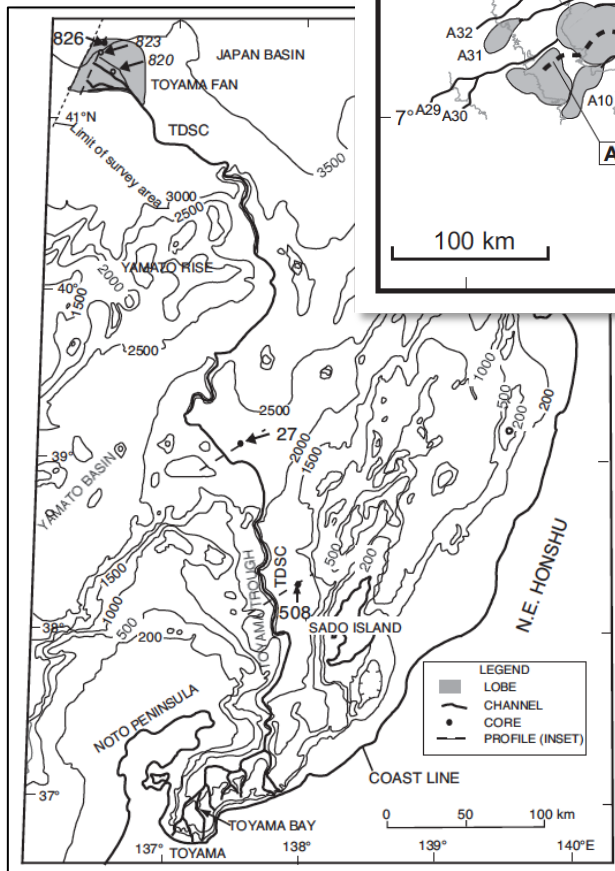


# The problem of large submarine fans



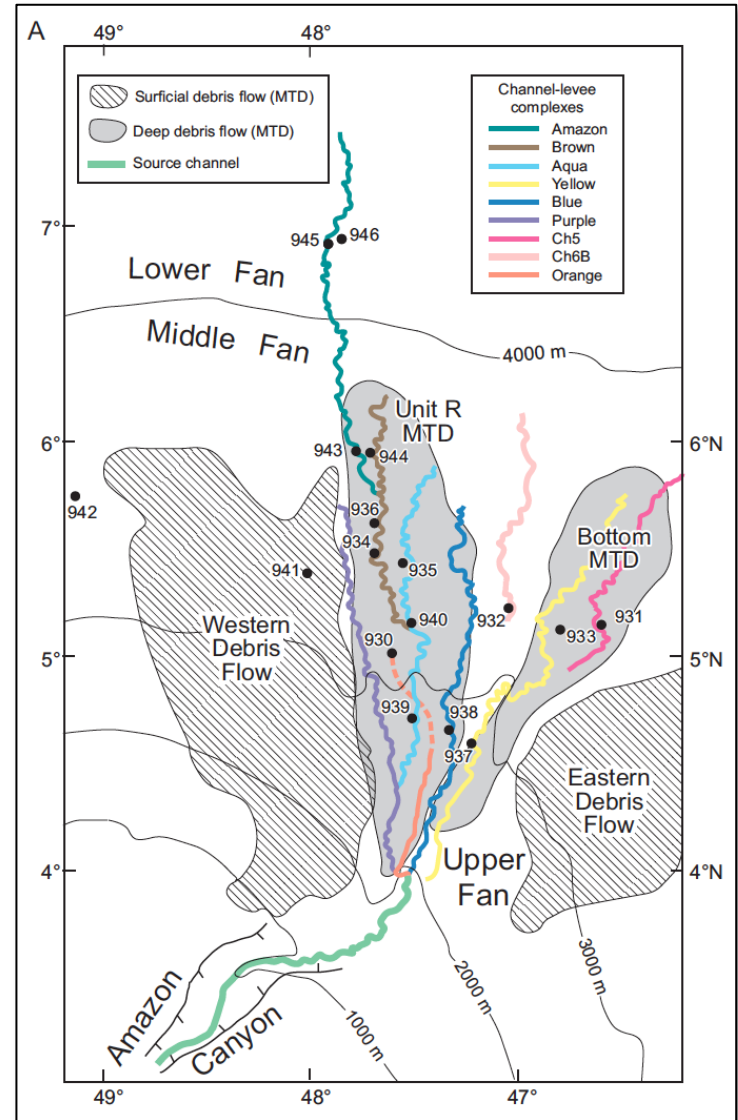
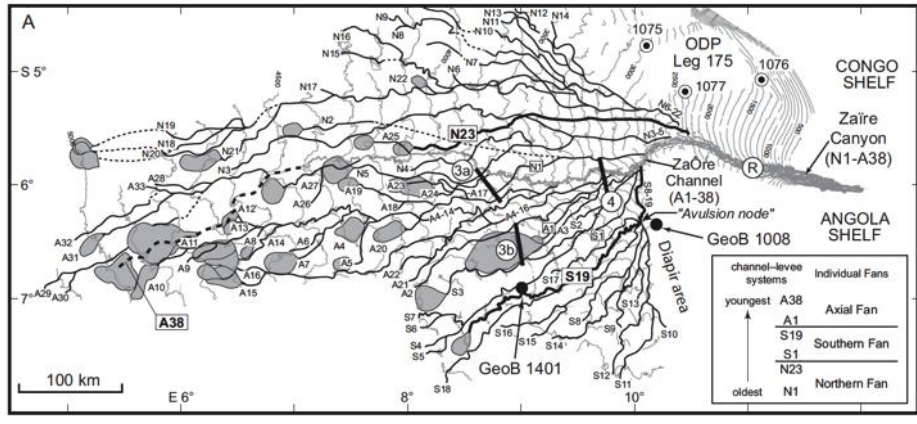
Congo fan. Marsset et al., 2009

Turbidity currents apparently carry sediment in suspension through channels over very low gradients for 500 km...

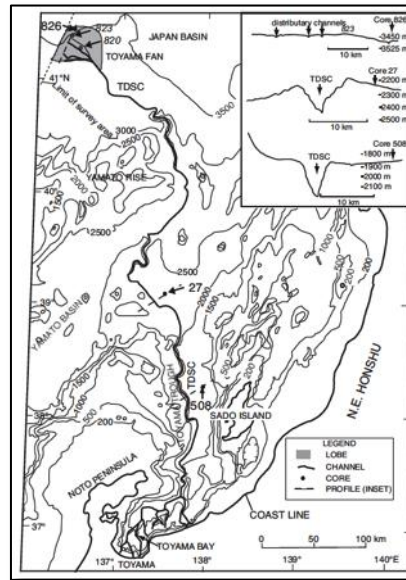


Toyama channel. Nakajima, 2009

# The problem of large submarine fans



...1000 km...



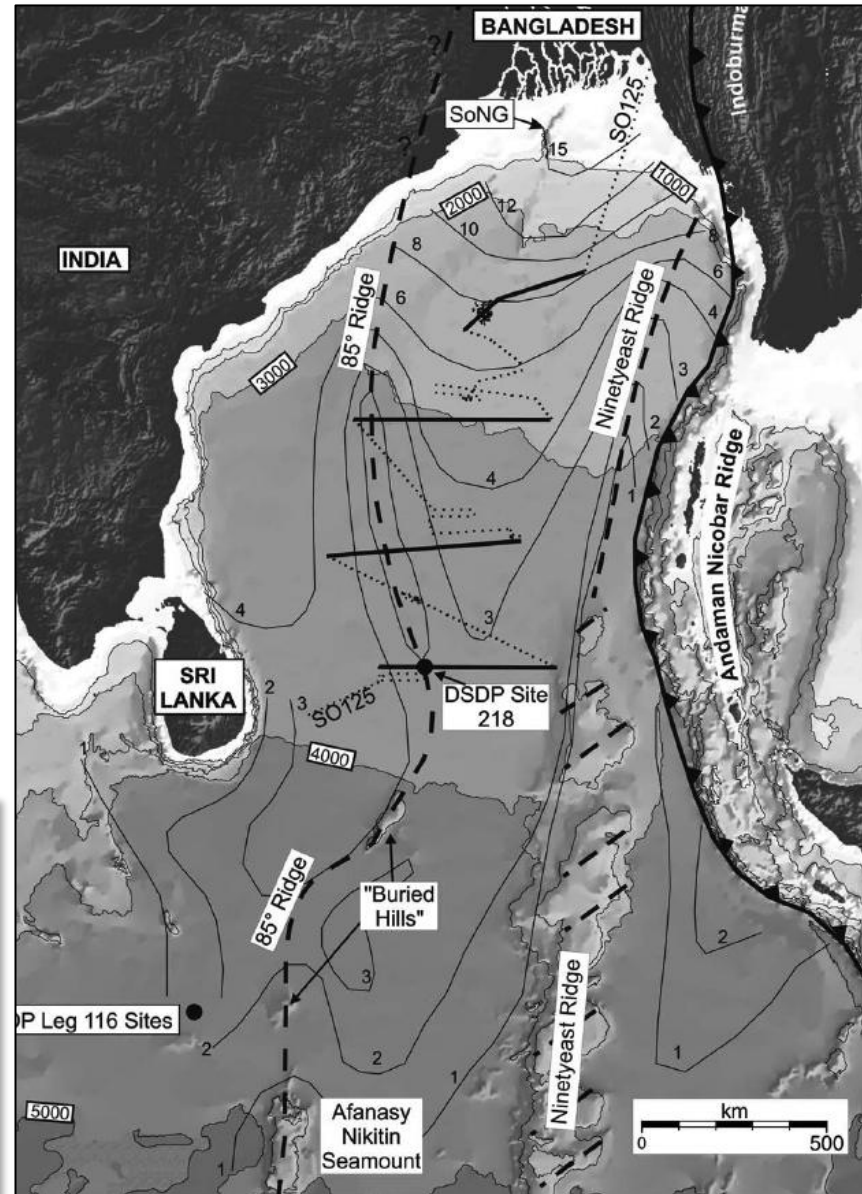
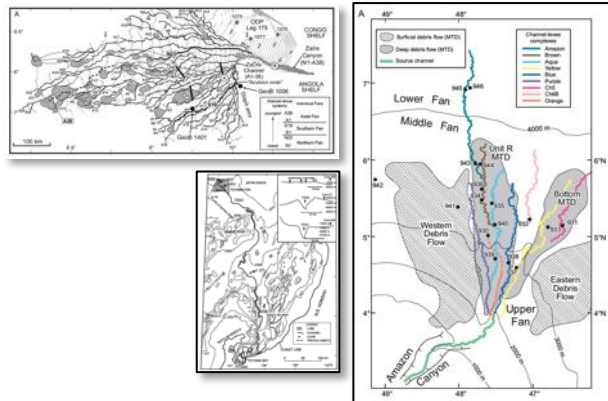
Amazon fan. Maslin, 2009



# The problem of large submarine fans

...even 3000 km

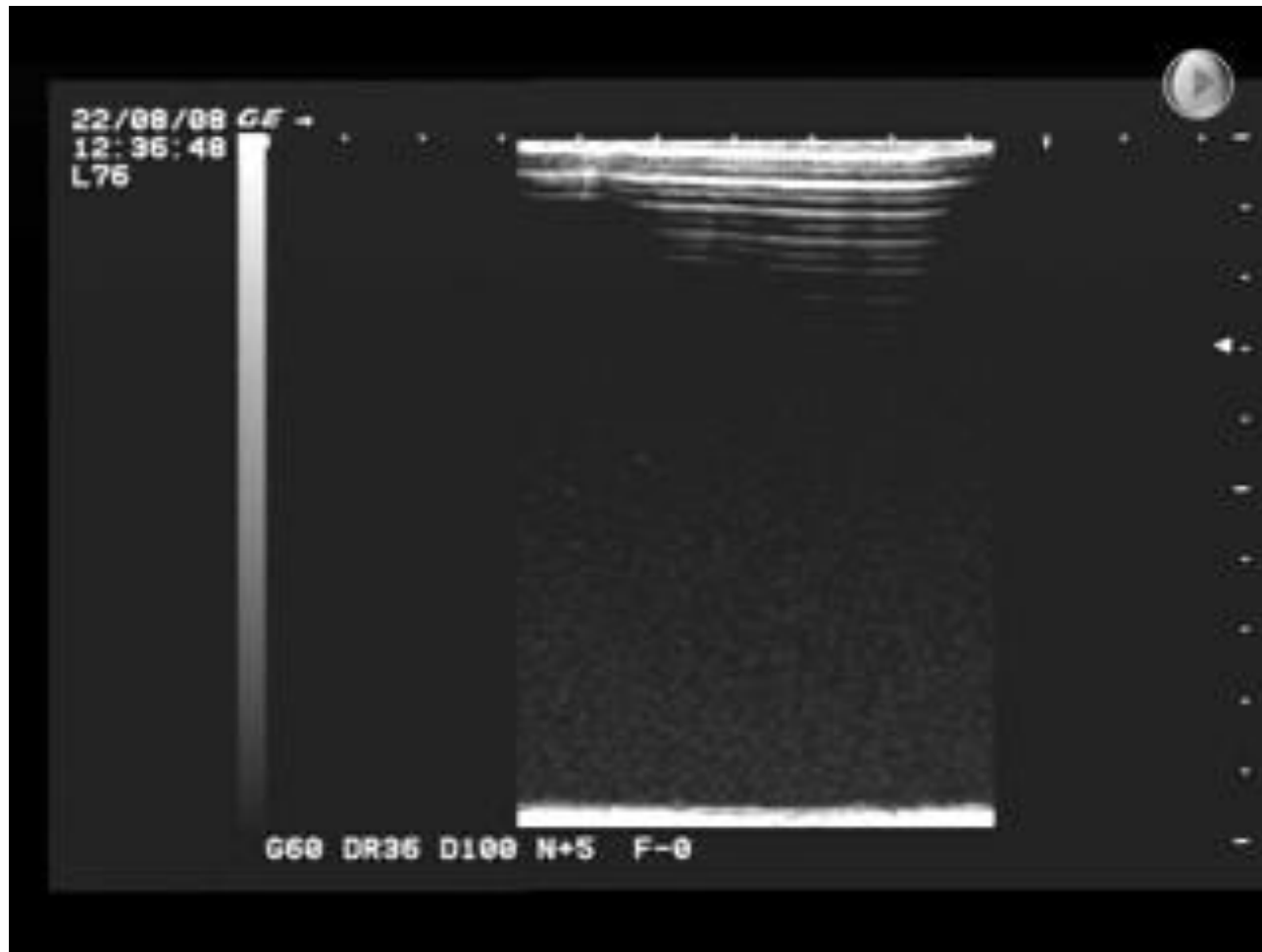
How?



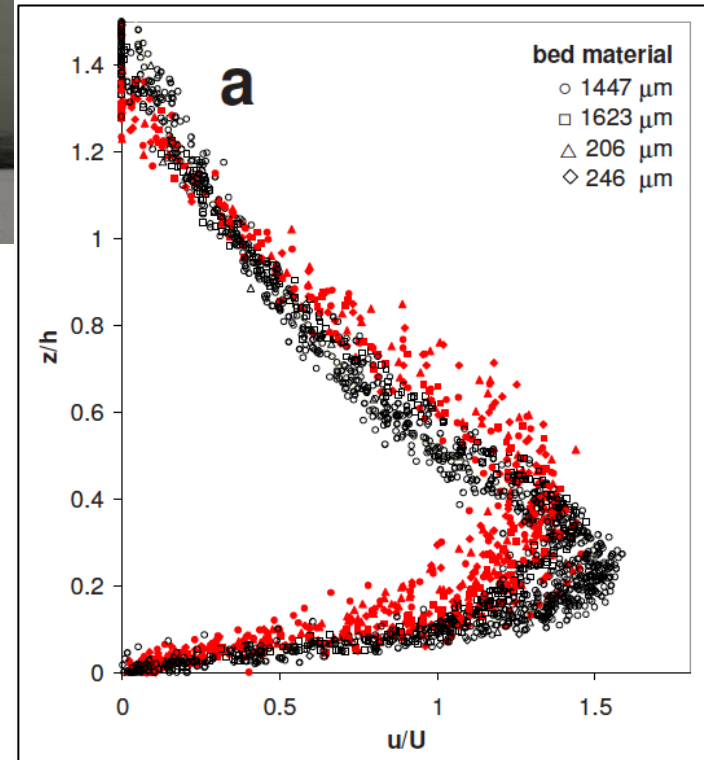
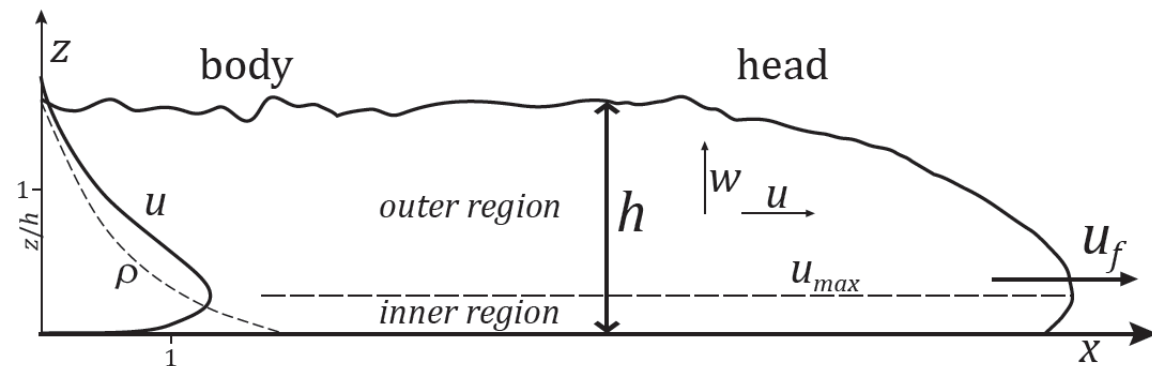
Bengal fan. Schwenk & Spieß, 2009

# Unstable stratification – Kelvin–Helmholtz instabilities

Froude subcritical laboratory turbidity current; crushed coal in water, imaged by medical ultrasound



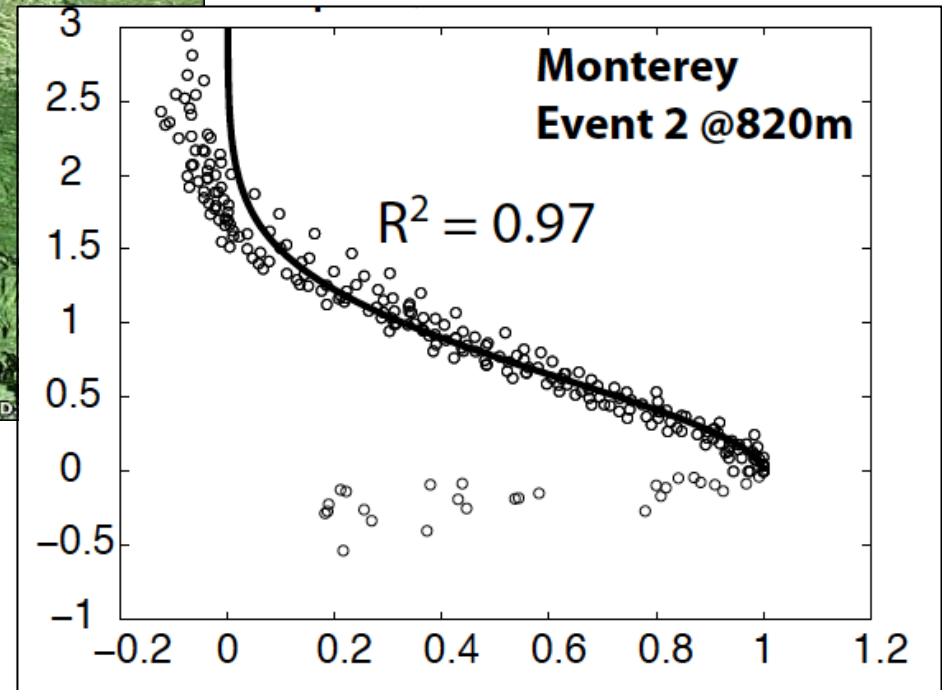
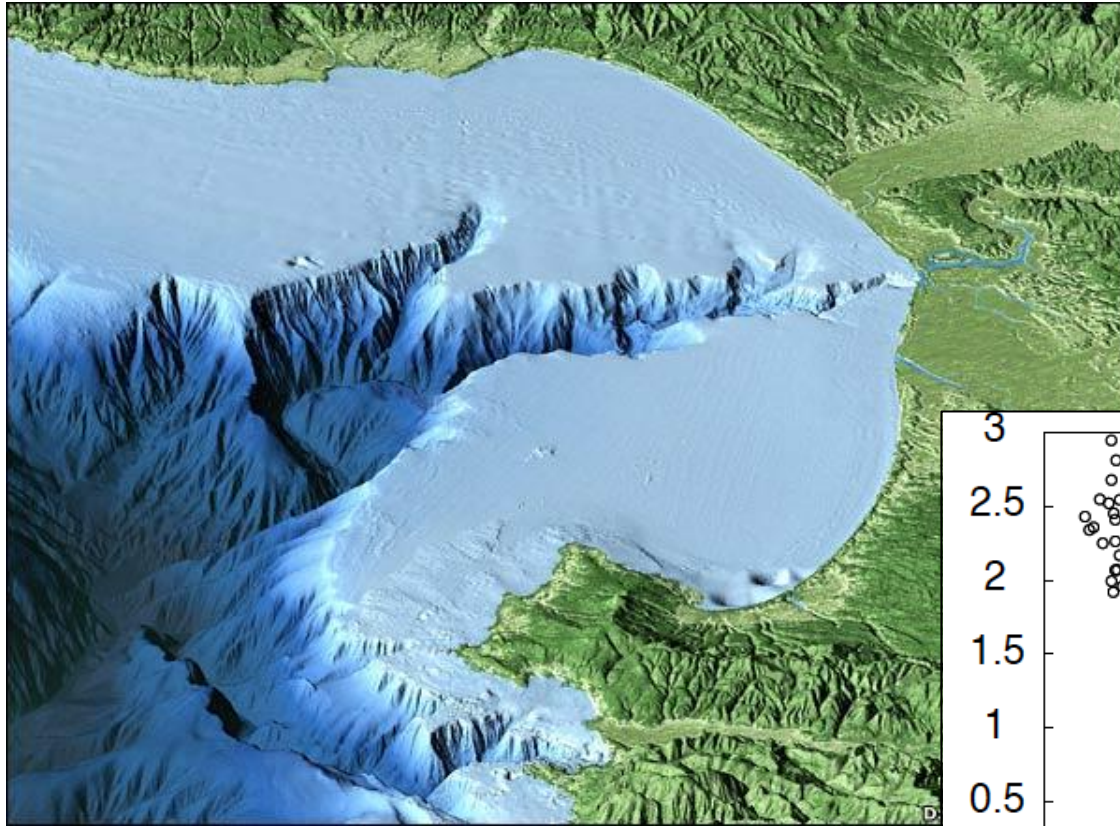
# The classic view – velocity profiles



Experiments on super-critical flows  
Sequeiros et al. 2010

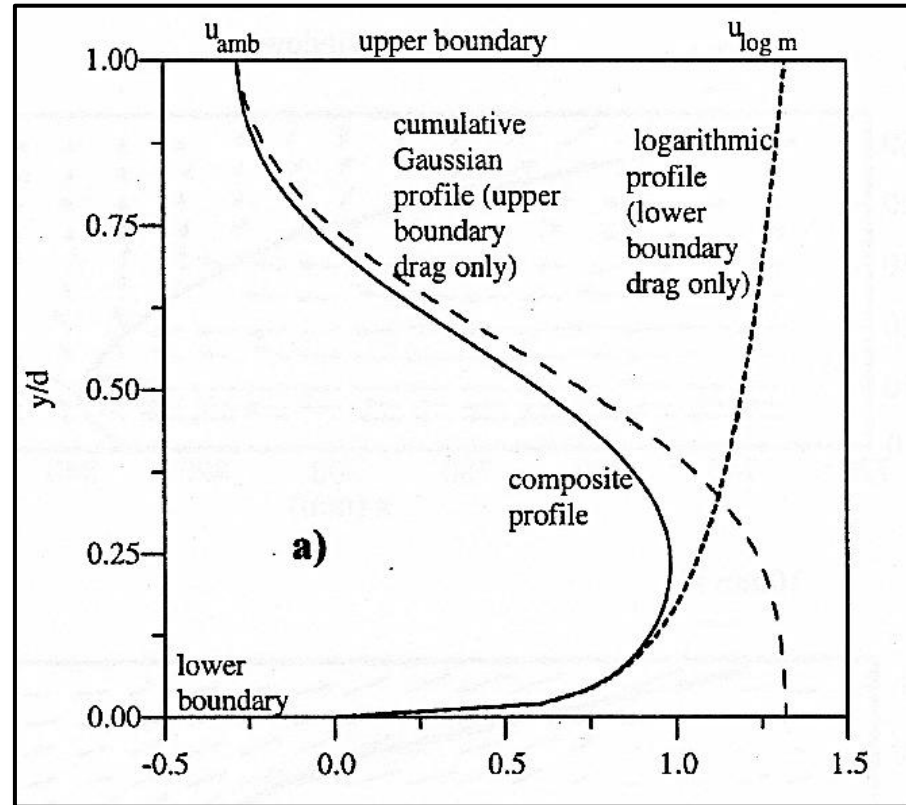


# The classic view – velocity profiles



Natural current  
Xu, 2010

# Origin of the velocity profile



Kneller et al., 1999

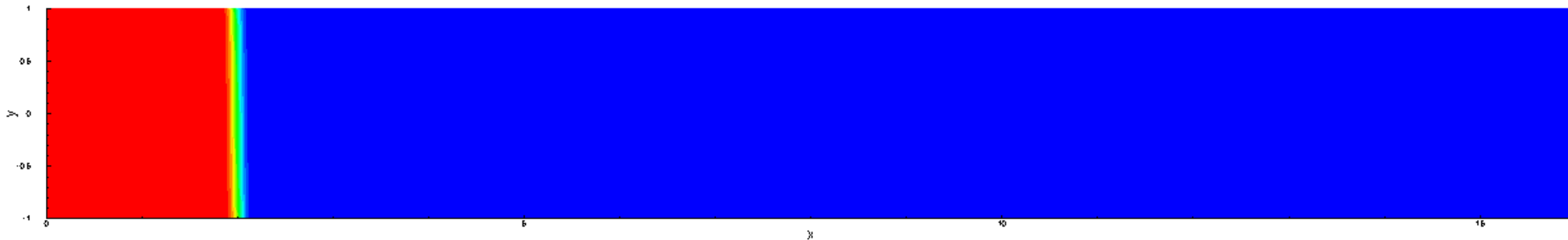
Sum of logarithmic boundary layer profile, and shear layer profile (error function) that extends to the bed where there is high turbulent drag

# Kelvin-Helmholtz instabilities

Kelvin-Helmholtz instabilities generated at upper flow boundary when  $Ri_g < 0.25$

$$Ri_g = \frac{N^2}{(\partial u / \partial z)^2} = \frac{\frac{\partial}{\partial z} \left( \frac{g}{\rho_a} \frac{\partial \rho}{\partial z} \right)}{(\partial u / \partial z)^2}$$

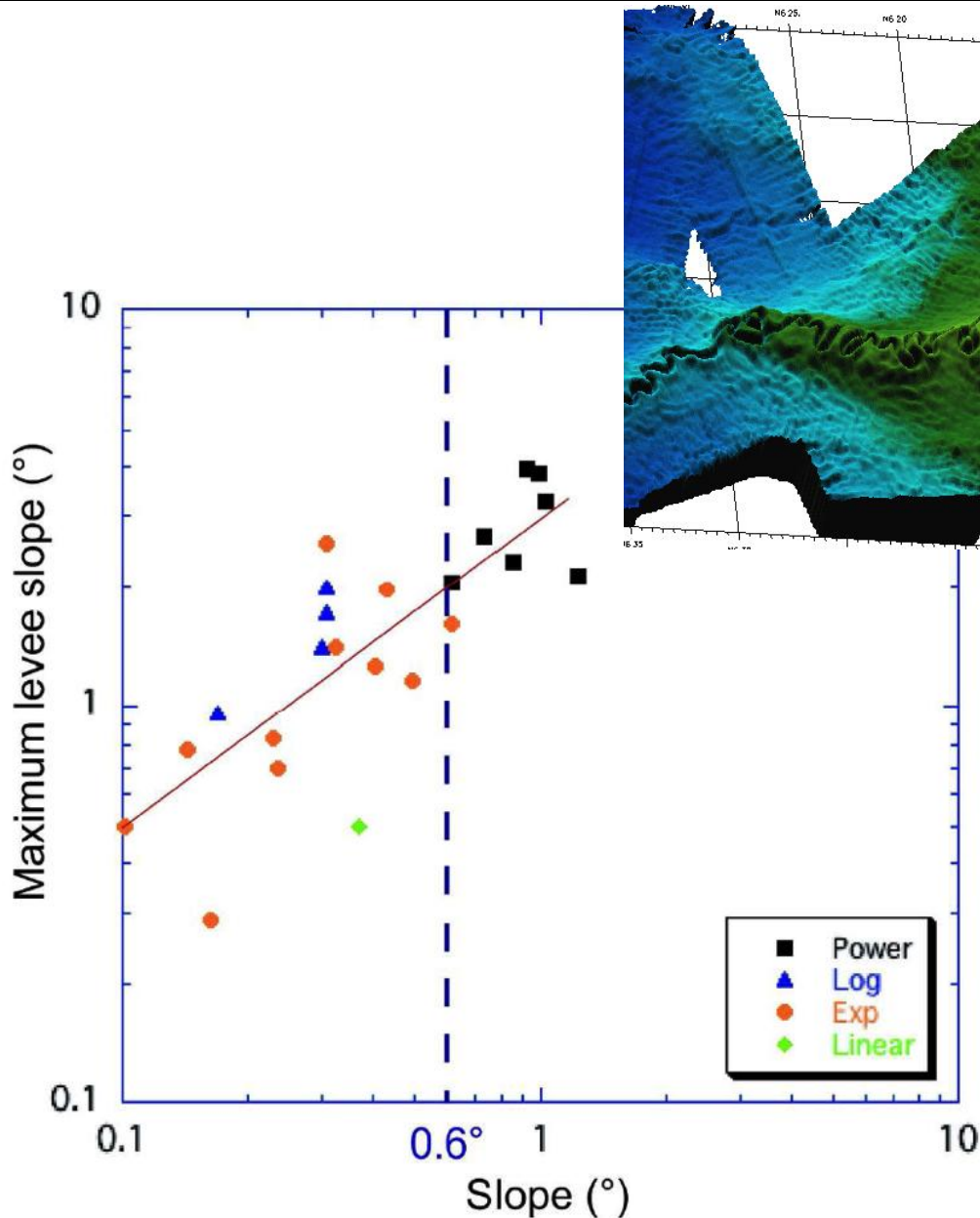
Large eddy simulation of turbidity current,  
Brendon Hall, UCSB



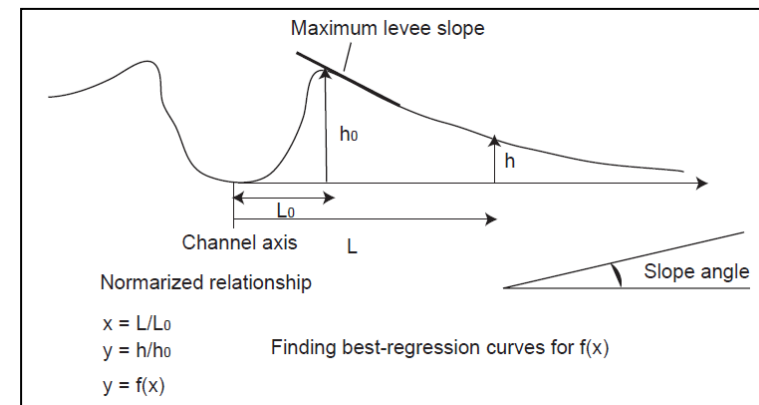
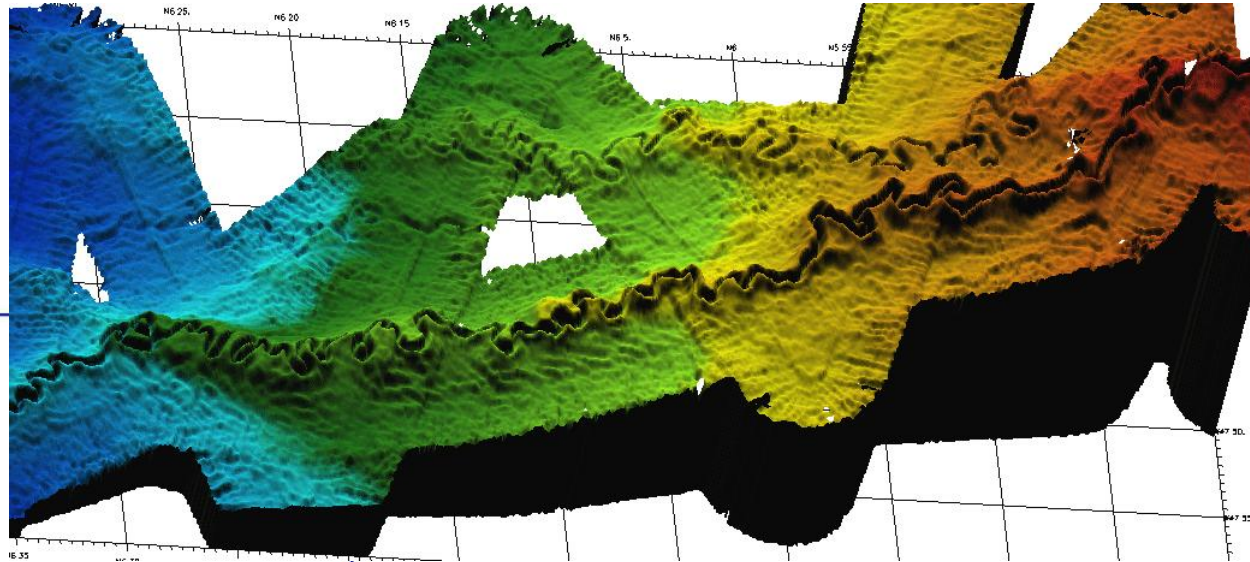
- Turbulent drag largely due to Kelvin-Helmholtz instabilities.
- Entrainment of ambient fluid mainly via KHIs that form when shear dominates and stratification becomes unstable (i.e. when gradient Richardson number is  $< 0.25$ )



# Dependence of levee shape on slope gradient



Nakajima and Kneller, 2013.

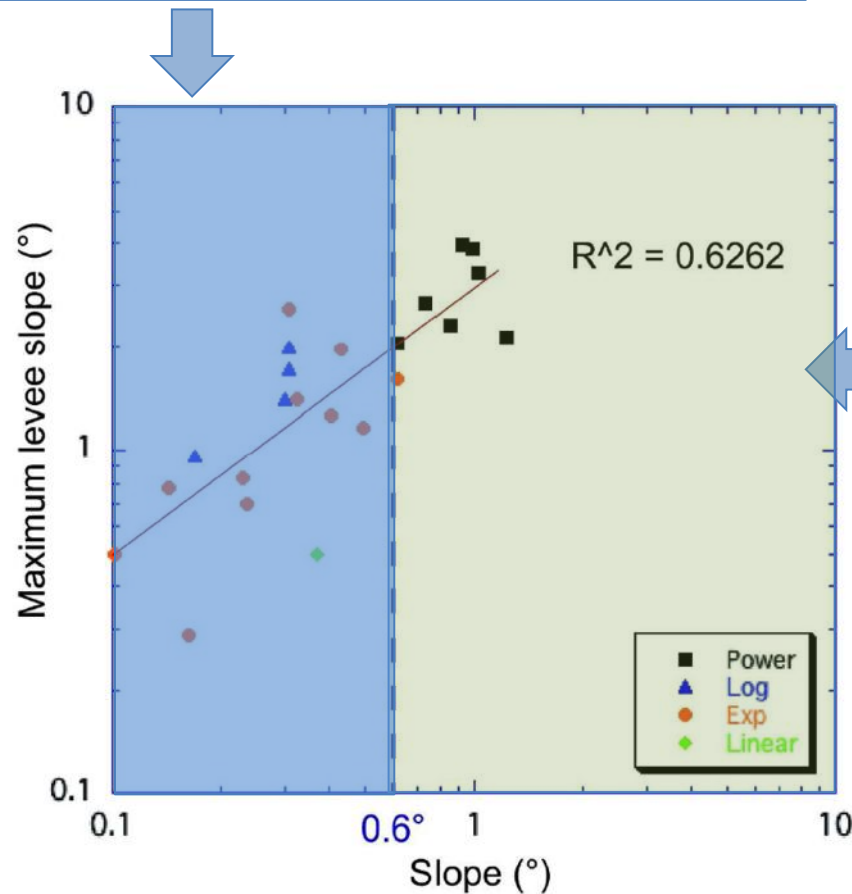


- Gradients of levee scale with regional slope
- Levee decay is power law on slopes  $>0.6^\circ$

$$f(x) = f_0 e^{-\left(\frac{u_s}{uh_0}\right)x}$$

Low gradient,  
exponential decay,  
no entrainment,  
No K-H instabilities

Slope controls presence or  
absence of entrainment

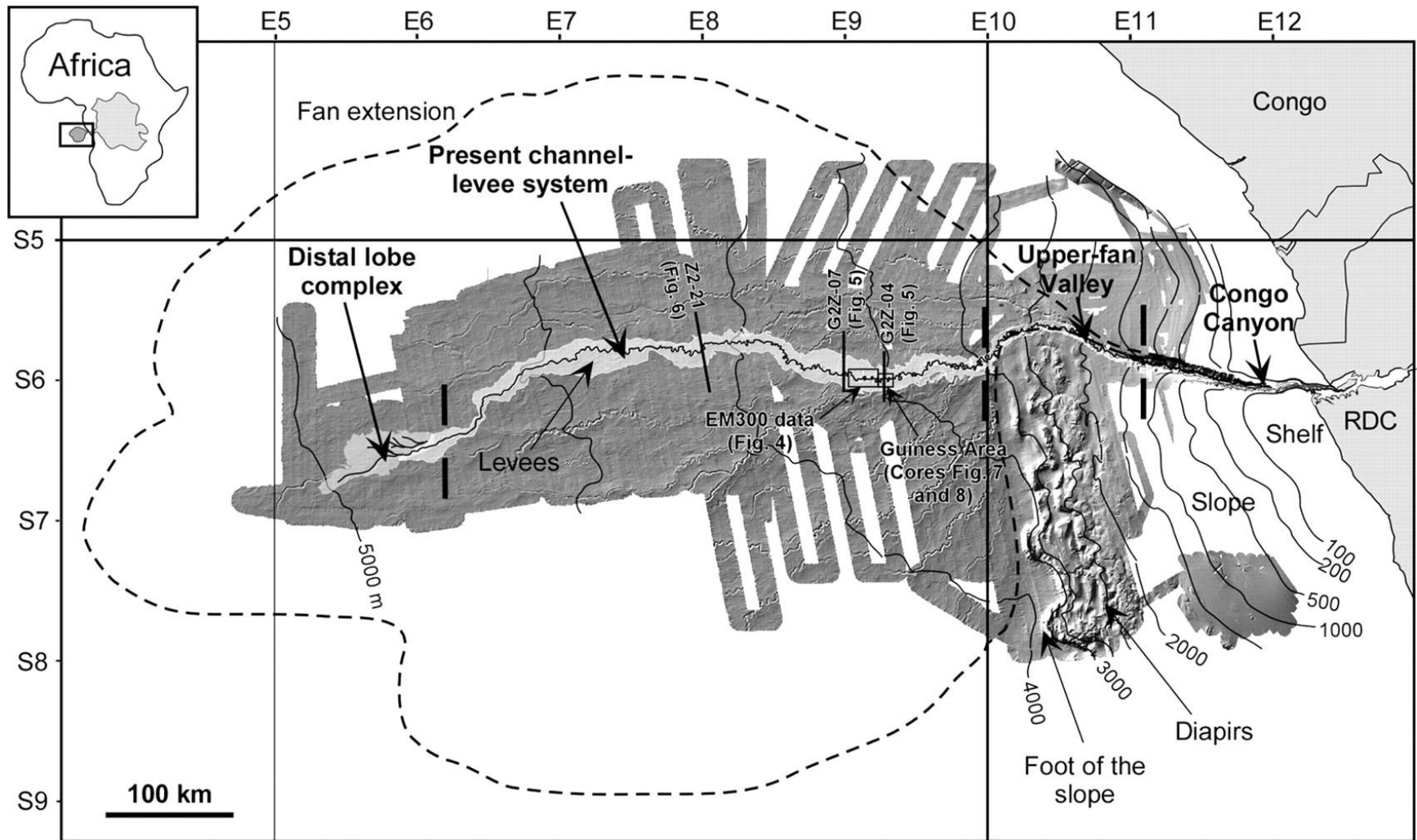


$$f(\hat{x}) = f_0 \left(\frac{uh_0}{\hat{x}}\right)^{\frac{-u_s + E_0}{E_0}}$$

High gradient,  
power law decay,  
entrainment  
via K-H instabilities

Birman et al., 2009

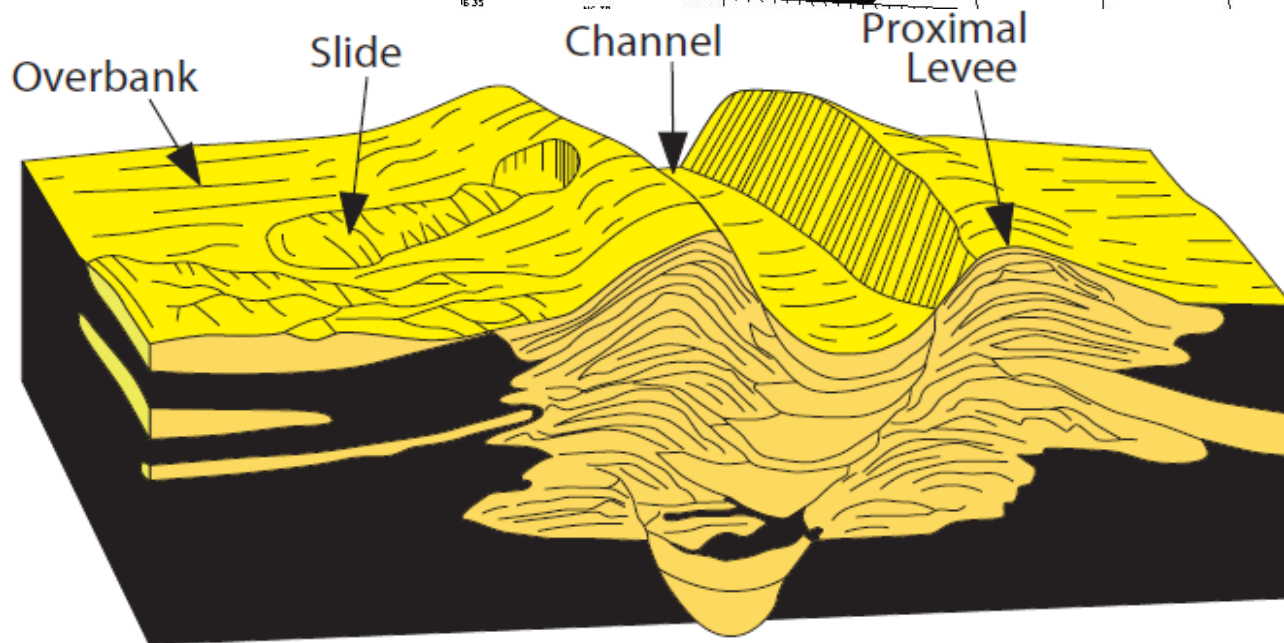
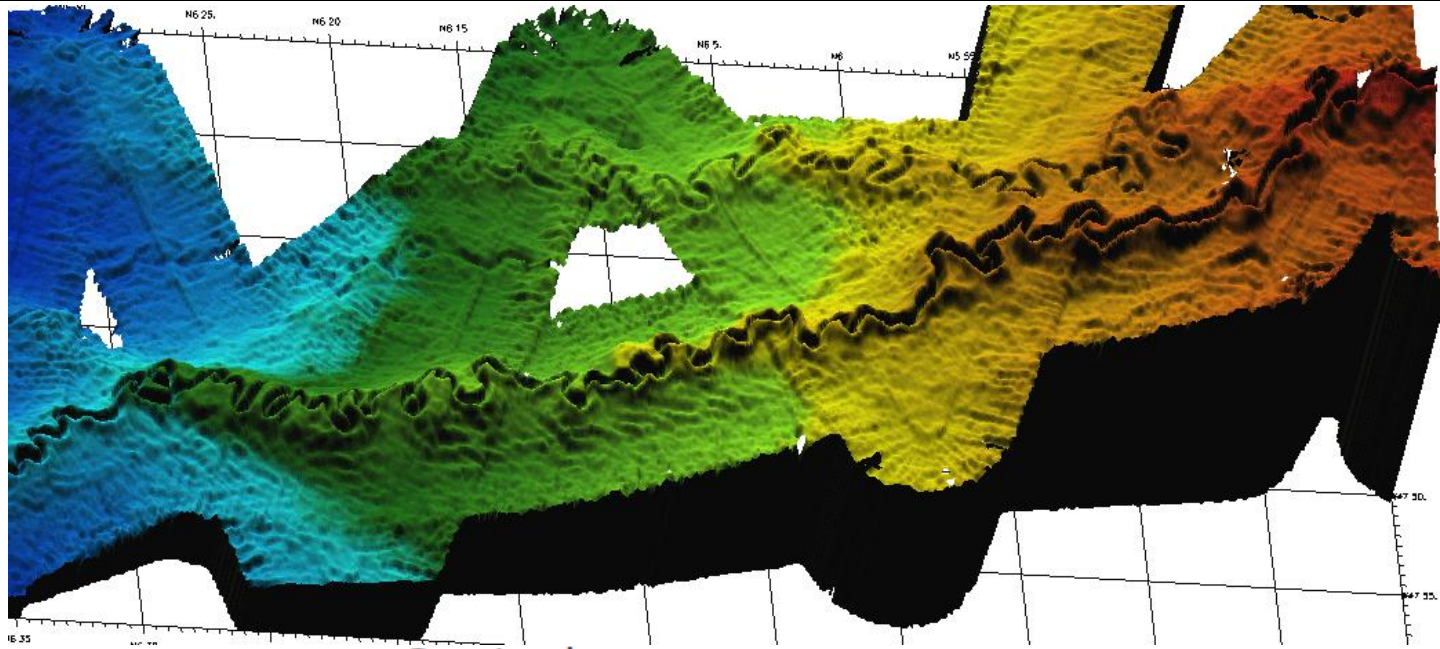
# The problem of large submarine fans



Babonneau et al., 2010



# Characterising flow



# Characterising flow

	<b>Congo</b>	<b>Amazon</b>	<b>Bengal</b>
Gradient of distal channel reaches	0.13°	0.11°	0.05°
Grain-size of lobe sediments ( $u_s$ is proxy for min. shear velocity $u_*$ )	Medium sand	Very fine sand	Silt
Approximate height of distal levees (proxy for flow height)	100m	50m	30m
Velocity	0.7 m s <sup>-1</sup> (Vangriesheim et al., 2009)		
Minimum sediment conc. by volume	≥ 0.1%	≥ 0.01%	≥ 0.003%
Density difference $\Delta\rho$	≥ 1600 g/m <sup>3</sup>	≥ 160 g/m <sup>3</sup>	≥ 50 g/m <sup>3</sup>

$$u_* = \sqrt{g \frac{Dr}{r} h \sin a}$$

## 2D Direct numerical simulation

Continuity equation: Incompressible flow

$$\nabla \cdot \mathbf{u} = 0$$

Conservation of momentum: Navier-Stokes equations in Boussinesq approximations

$$\frac{\partial \mathbf{u}}{\partial t} + \mathbf{u} \cdot \nabla \mathbf{u} = -\nabla p + \frac{1}{Re} \nabla^2 \mathbf{u} + c \mathbf{e}^g$$

Small particle size: neglect inertia

$$\frac{\partial c}{\partial t} + (\mathbf{u} + u_s \mathbf{e}^g) \cdot \nabla c = \frac{1}{ScRe} \nabla^2 c$$



# 2D Direct numerical simulation

Reynolds number

$$Re \circ \frac{\hat{u}_b \hat{H}}{\hat{\eta}} \quad \text{where} \quad \hat{u}_b = \sqrt{\hat{g} \frac{\hat{r}_1 - \hat{r}_0}{\hat{r}_0} \frac{\hat{H}}{2}}$$

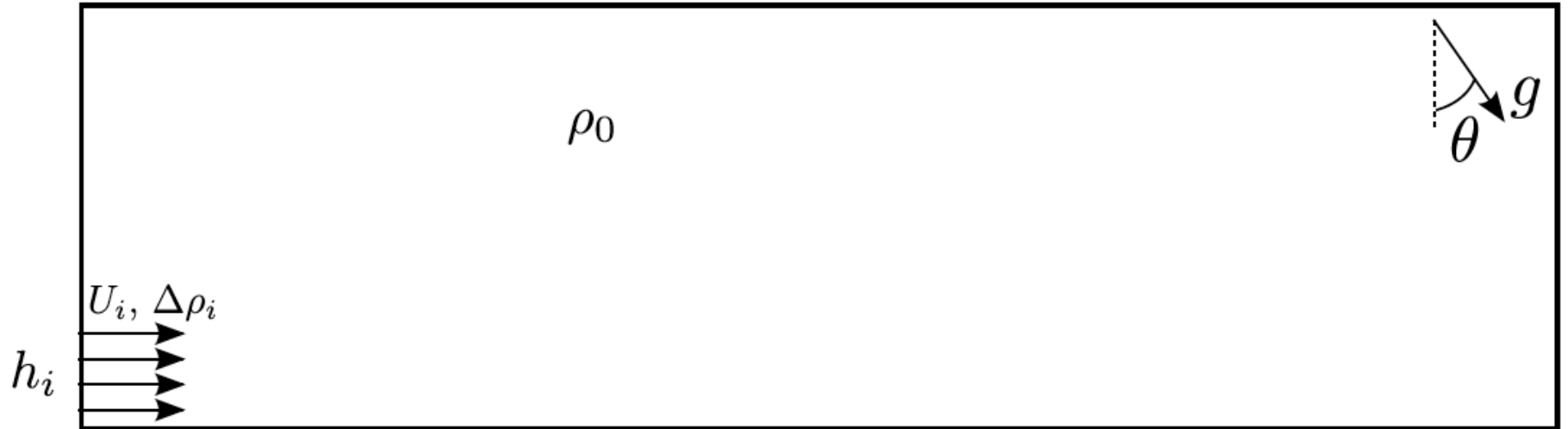
Schmidt number (no significant influence when  $Sc \geq 1$ )

$$Sc \circ \frac{\hat{\eta}}{\hat{K}}$$

Dimensionless particle settling speed

$$u_s \circ \frac{\hat{U}_s}{\hat{u}_b}$$

# 2D Direct numerical simulation



$$Fr_i = \frac{U_i}{u_b}$$

But is a bulk Froude number appropriate in stratified flows?

# 2D Direct numerical simulation; $Re = 4000$

Inlet Froude  
number = 0.78,  
slope = 0.057%

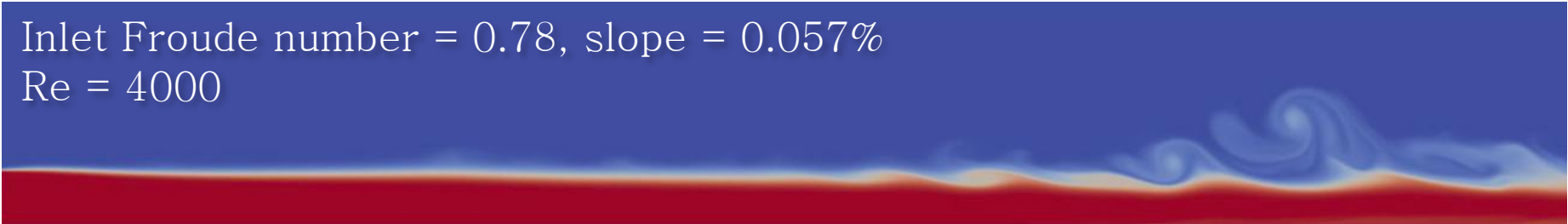
Inlet Froude  
number = 0.9,  
slope = 5%

Inlet Froude  
number = 1.3,  
slope = 5%

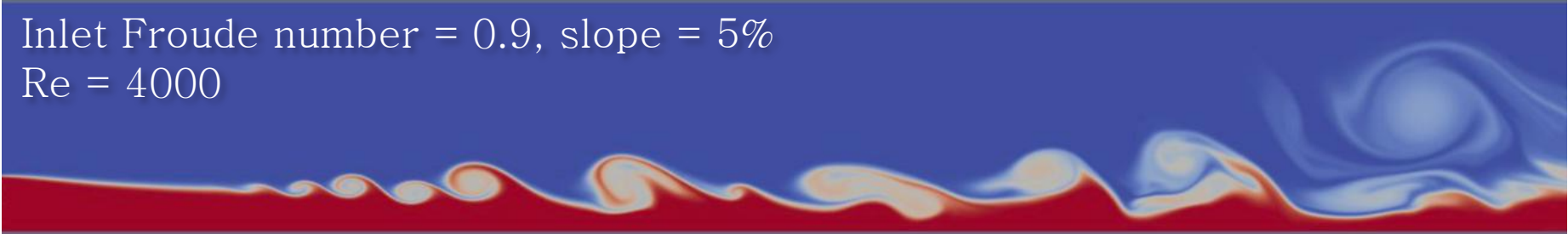


# 2D Direct numerical simulation

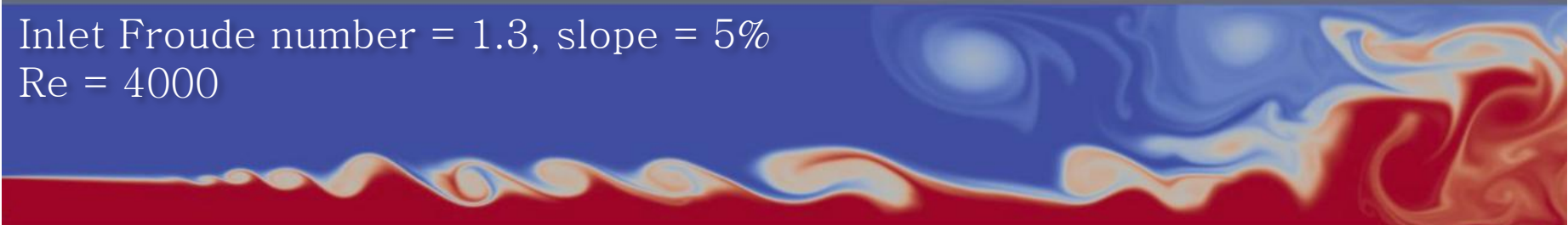
Inlet Froude number = 0.78, slope = 0.057%  
Re = 4000



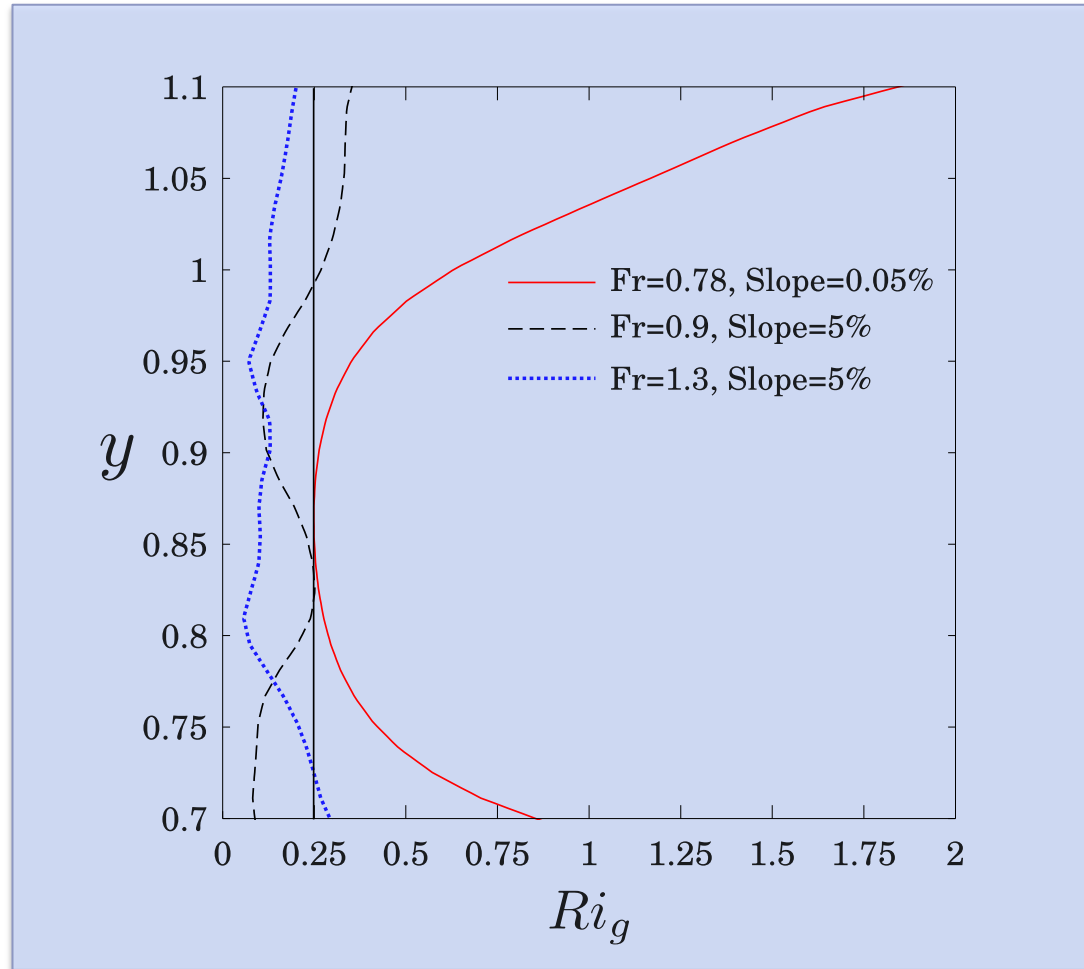
Inlet Froude number = 0.9, slope = 5%  
Re = 4000



Inlet Froude number = 1.3, slope = 5%  
Re = 4000

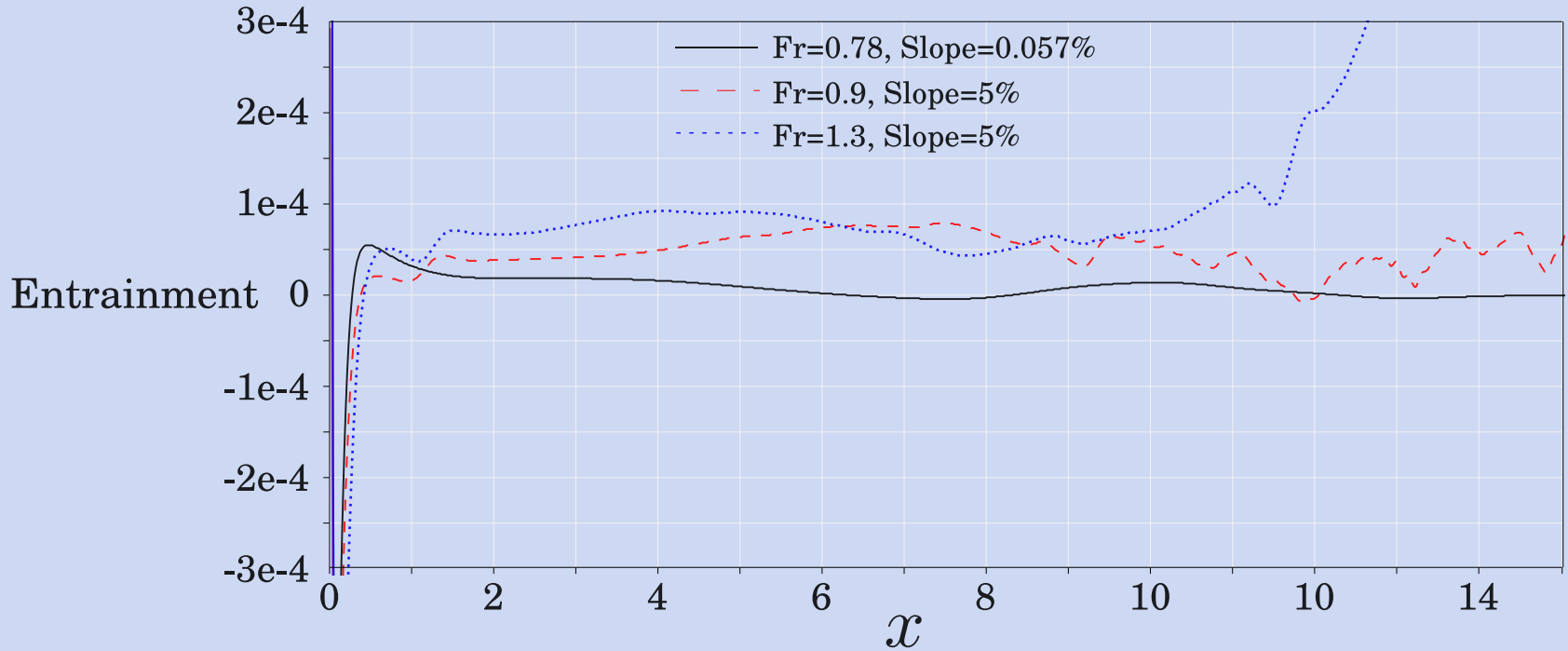


# 2D Direct numerical simulation Gradient Richardson number



Flows on lower gradients (subcritical) have stable stratification

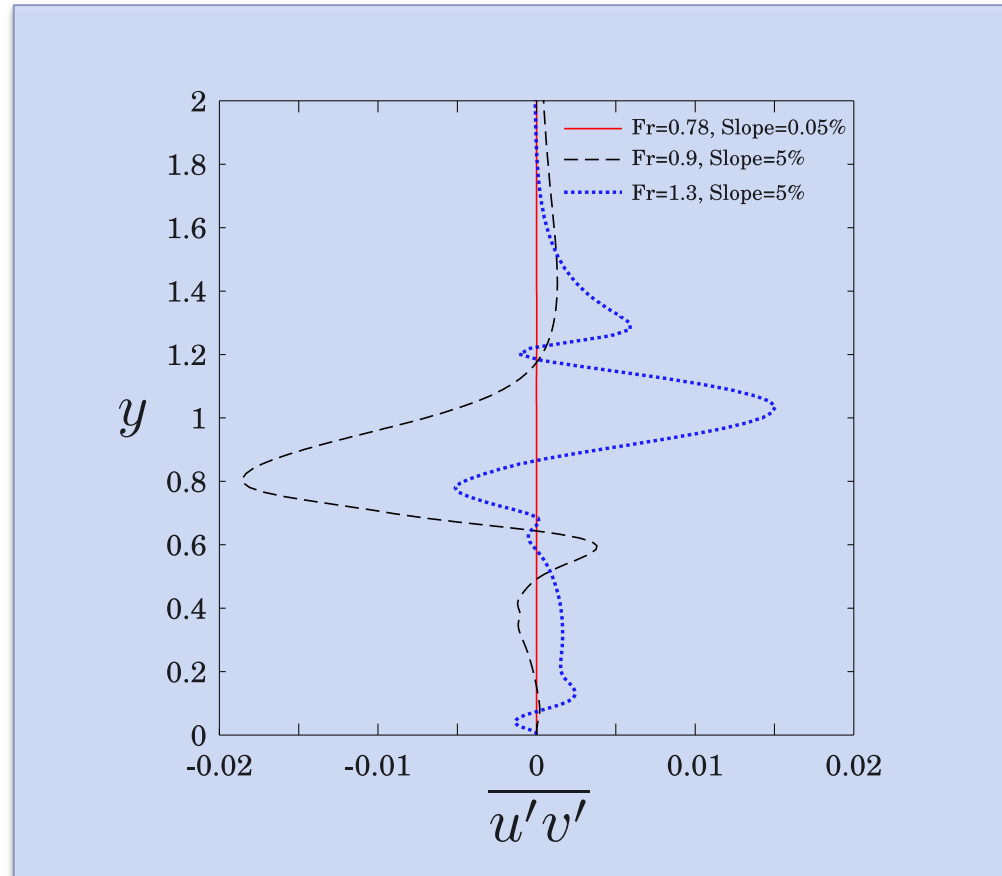
# 2D Direct numerical simulation, entrainment



Flows on lower gradients show minimal entrainment

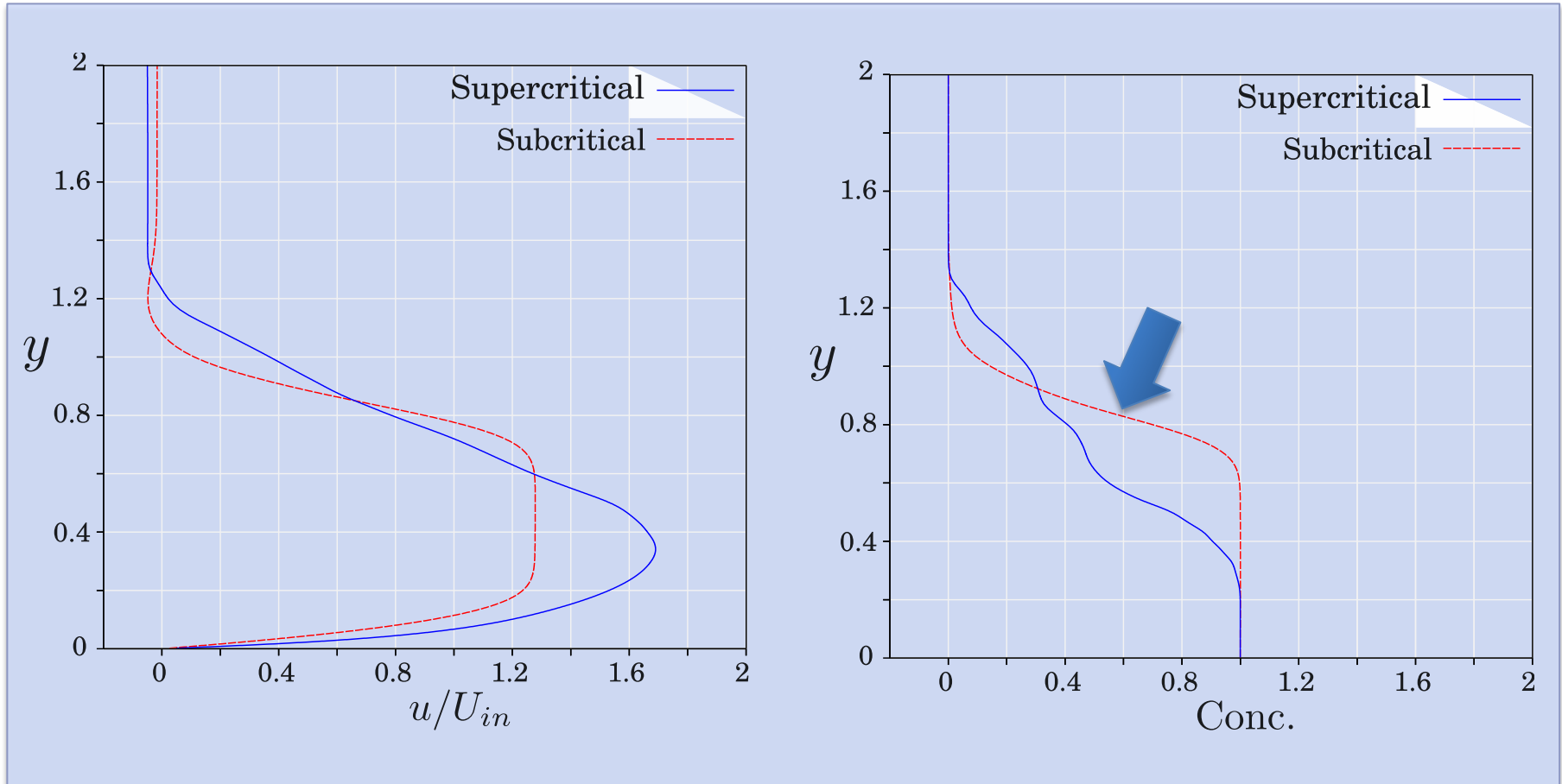


# 2D Direct numerical simulation, 'turbulent' drag



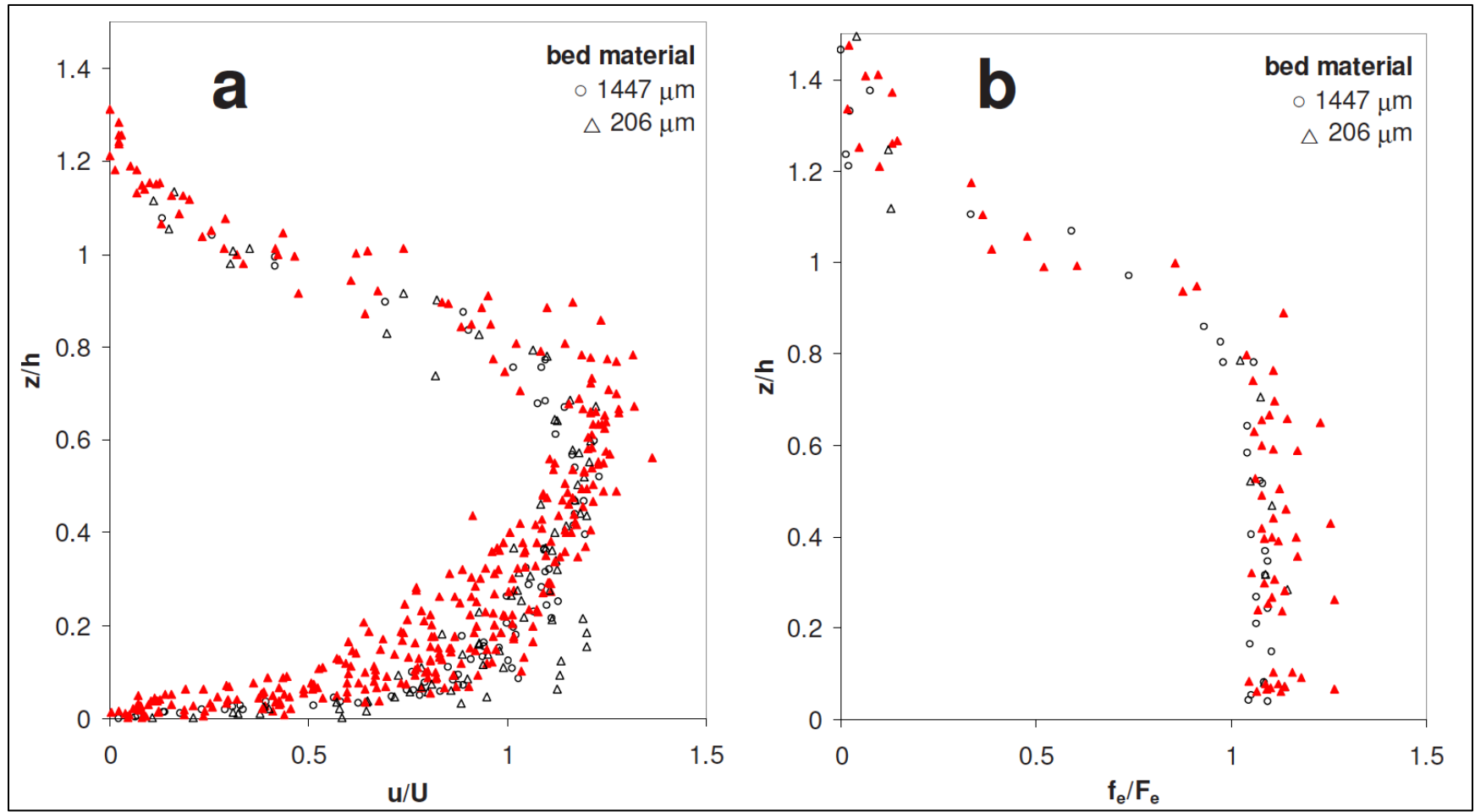
Flows on lower gradients show minimal turbulent drag

# 2D Direct numerical simulation, velocity and density profiles



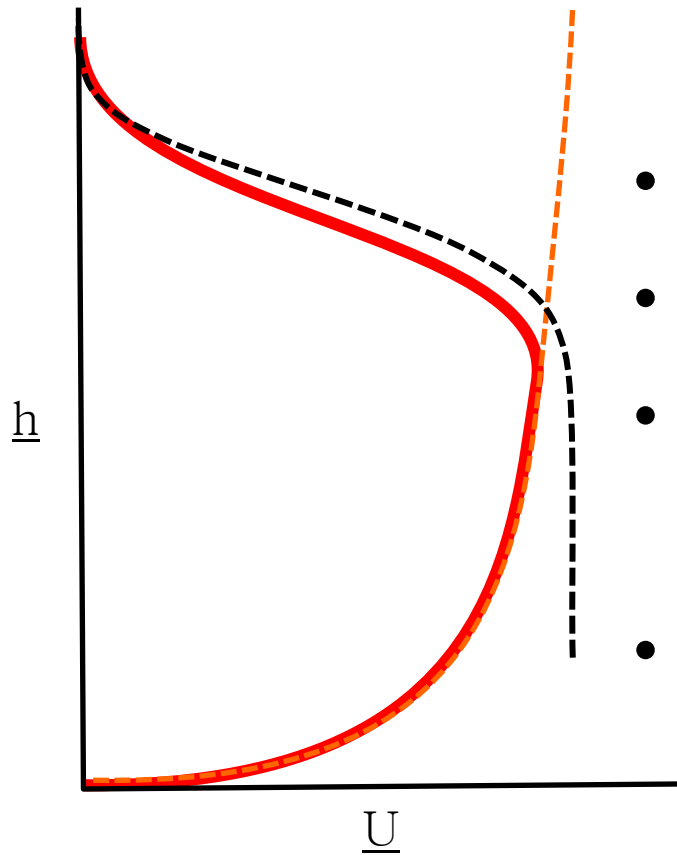
Flows on lower gradients have radically different velocity and density profiles

# Experimental flows show similar behaviour



Sub-critical gravity flows. Sequeiros et al. 2010

# Absence of Kelvin–Helmholtz instabilities...



- Substantially reduced drag
- No ambient fluid entrainment
- Velocity profile dominated by lower boundary
- Weak density stratification



# Influence of settling velocity

$U_s = 0.001$

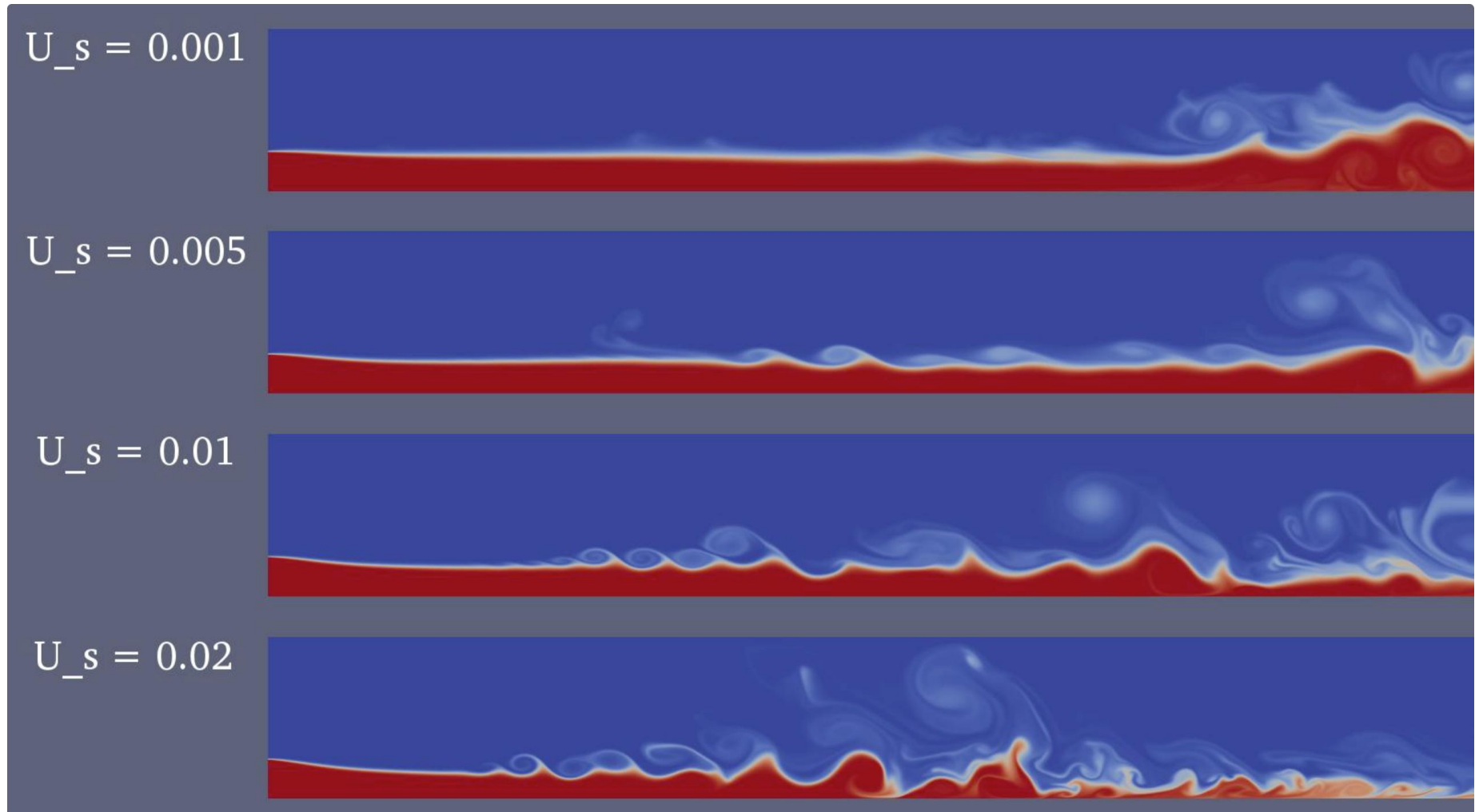
$U_s = 0.005$

$U_s = 0.01$

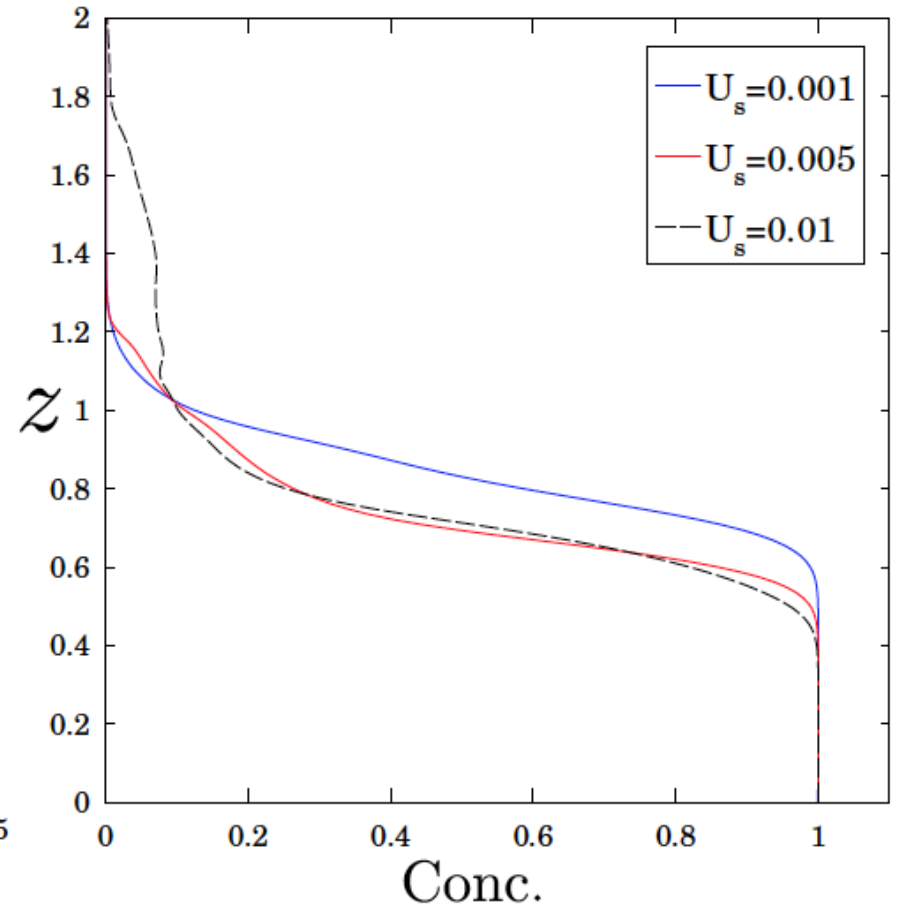
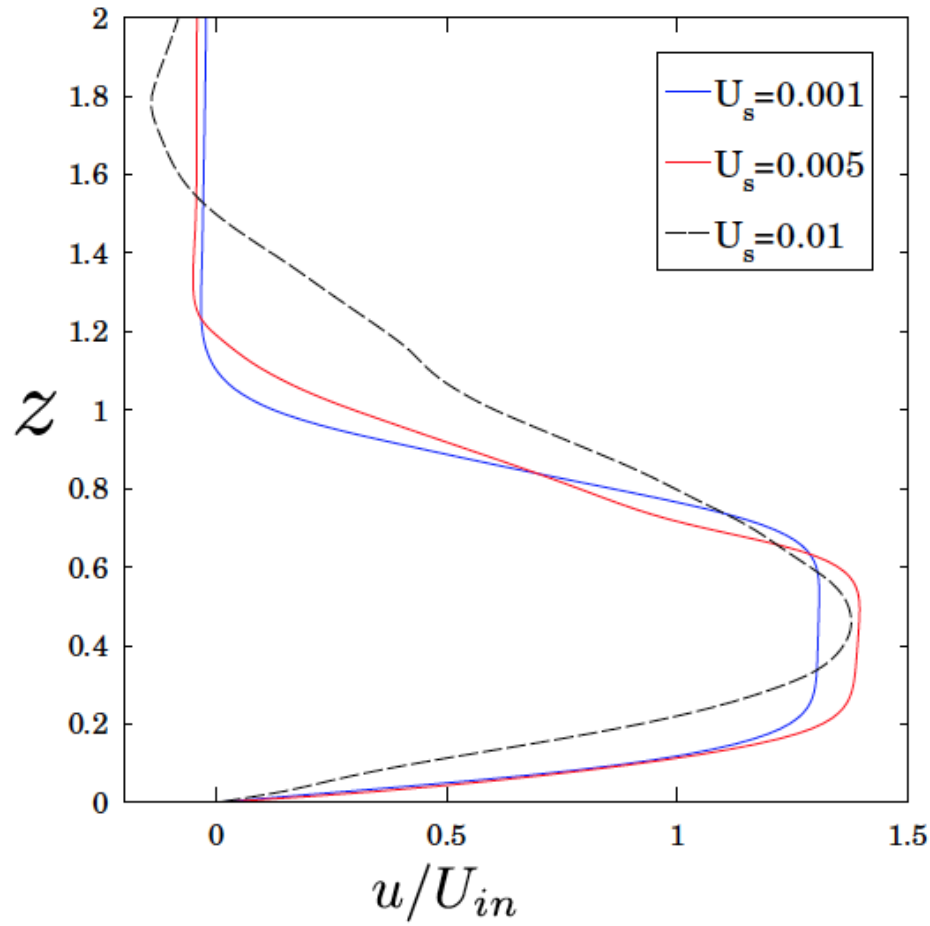
$U_s = 0.02$



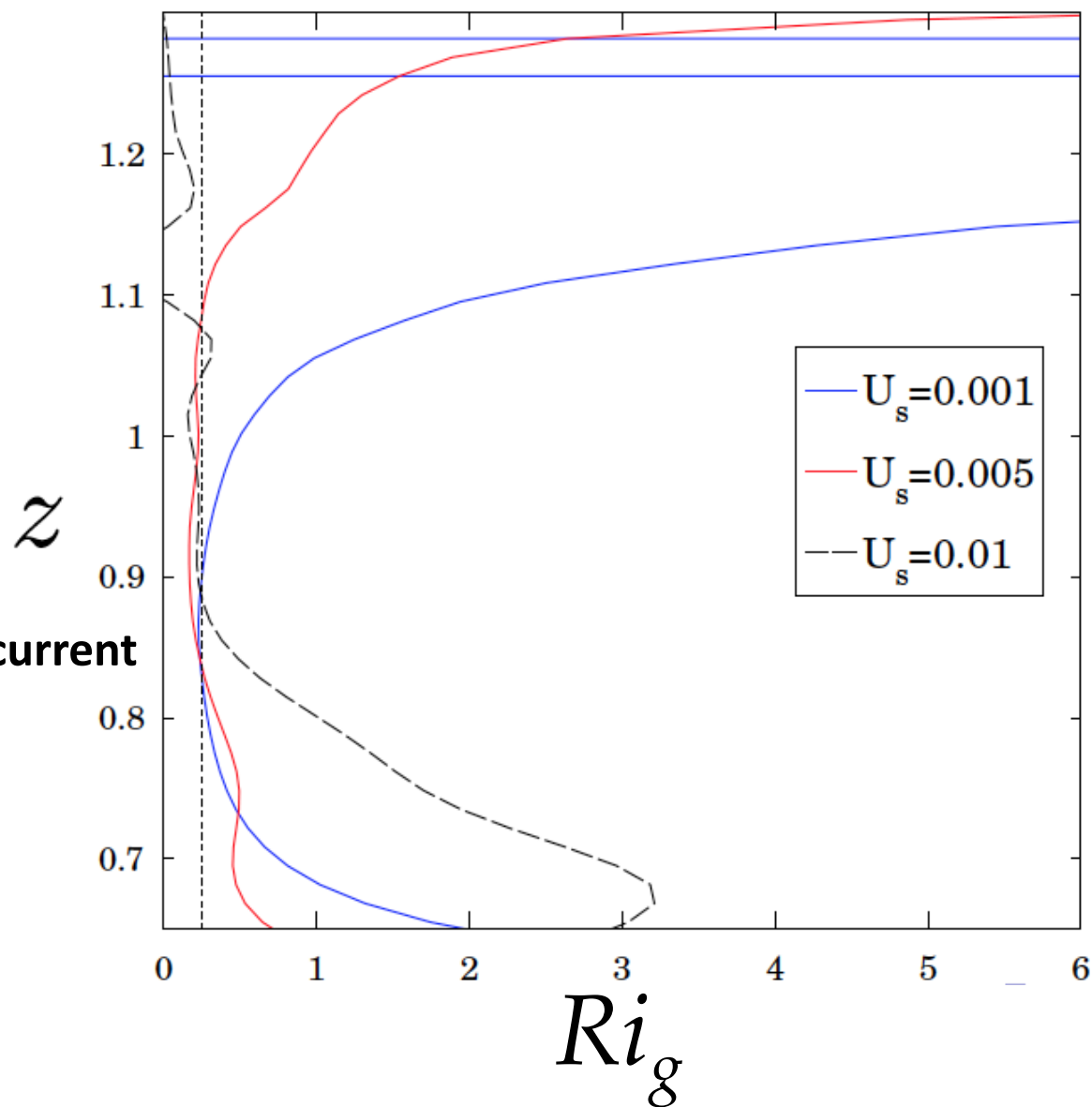
# Influence of settling velocity



# Influence of settling velocity on density and velocity profiles



# Influence of settling velocity on gradient Richardson number





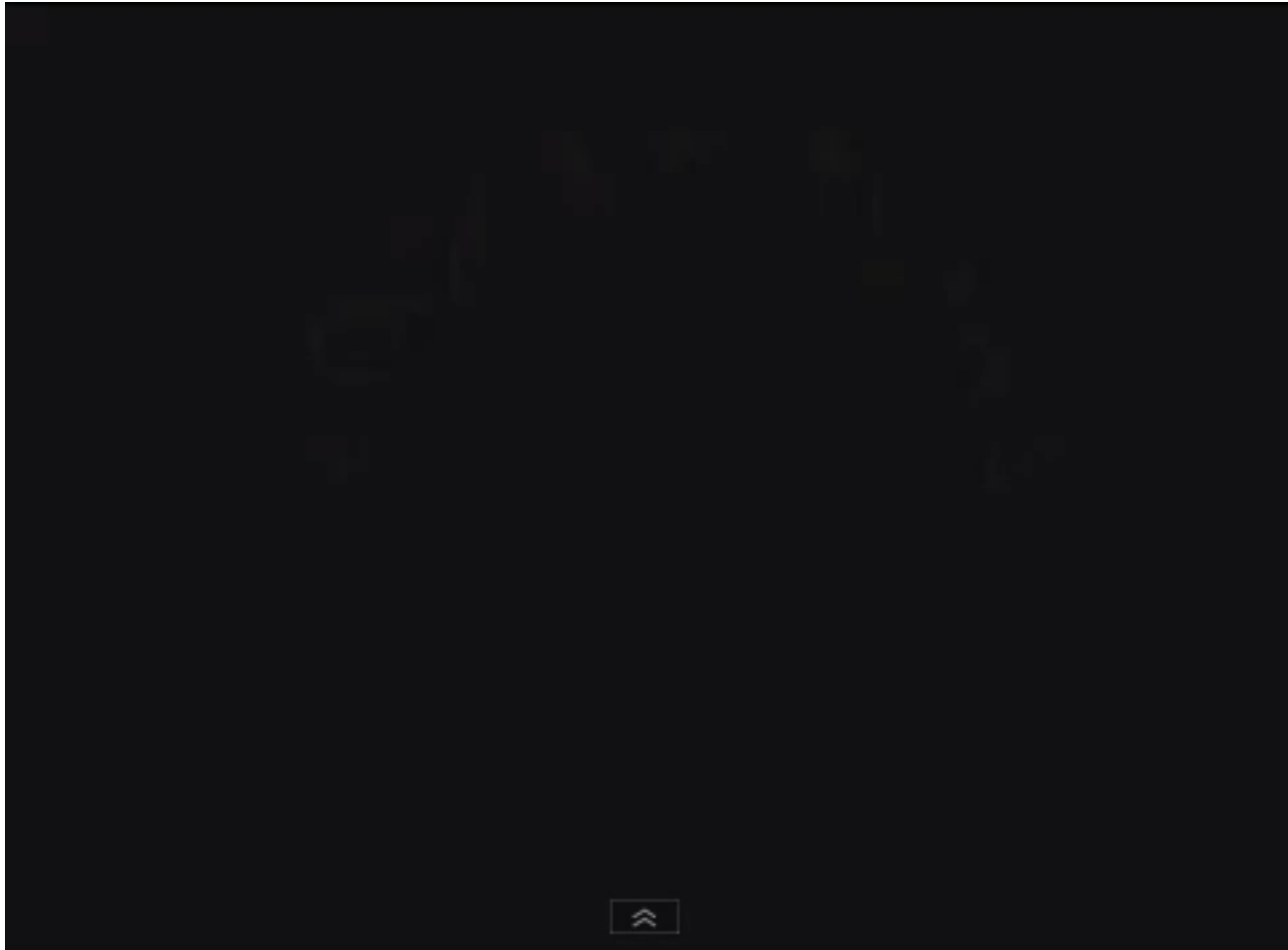
# Constraints on flow parameters

	$u^*$	$U_b$	SSC ( $u^*$ )	SSC ( $U_b$ )
Congo	0.037	0.87	0.03-0.1%	~1%
Amazon	0.012	0.28	0.001-0.01%	~0.50%
Bengal	0.003	0.09	0.0005-0.003%	~0.01%

Is buoyancy velocity the appropriate characteristic velocity with which to scale  $u_s$ ?

# Conclusions

- Turbidity currents on very low gradients probably have stable stratification, do not exhibit Kelvin Helmholtz instabilities, experience **little entrainment** of ambient seawater, and **far lower drag** than flows with Kelvin Helmholtz instabilities
- This accounts for their persistence over enormous distances
- Fundamental difference in character between flows on steep slopes and gentler slopes is driven by change in  $Ri_g$



# Thank you for listening

UCSB

UNIVERSITY OF CALIFORNIA  
SANTA BARBARA



UNIVERSITY  
OF ABERDEEN