

# *Role of pore pressure gradients in geophysical flows over permeable substrates*

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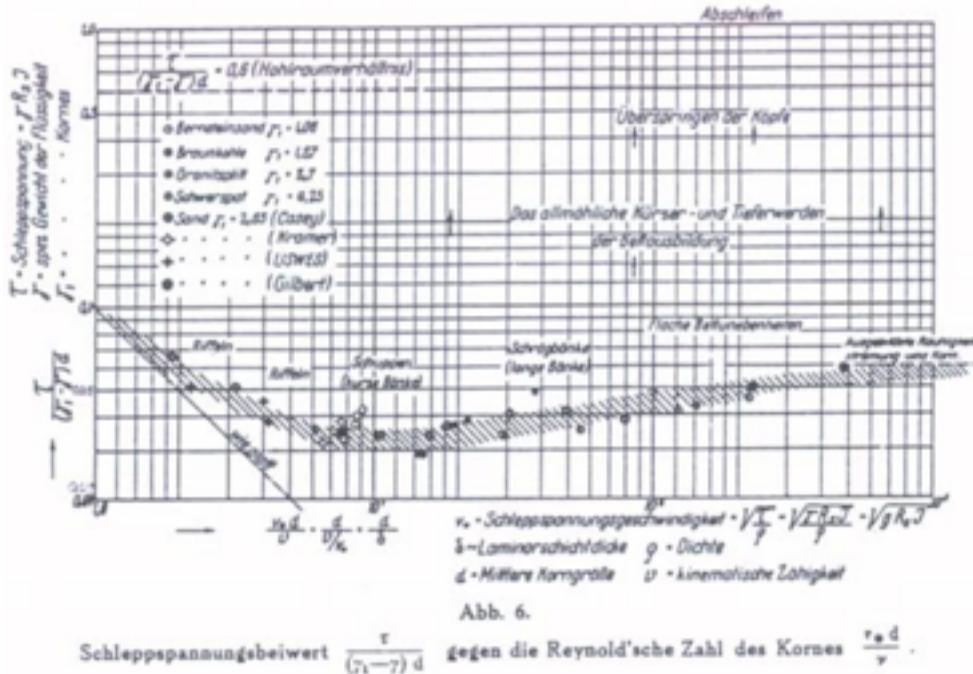


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KITP, December 18, 2013

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## Shields erosion

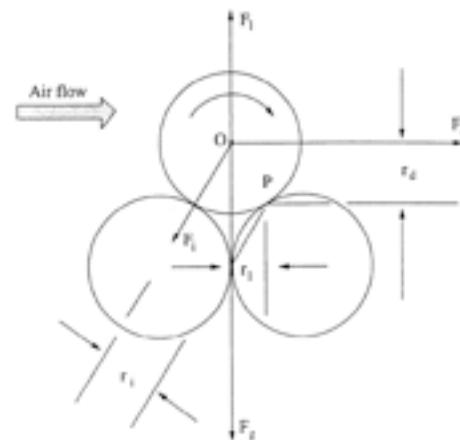


Figure 1. Forces acting on a particle resting on the surface under the influence of an airstream, including the aerodynamic drag  $F_d$ , the aerodynamic lift  $F_l$ , the gravity force  $F_g$ , the moment  $F_m$ , and the cohesive force  $F_c$ ;  $r_d$ ,  $r_l$ ,  $r_m$ , and  $r_c$  are moment arm lengths associated with  $F_d$ ,  $F_l$  and  $F_g$ ,  $F_m$ , and  $F_c$ , respectively. O is the center of gravity of the particle, and P is the pivot point for particle entrainment.

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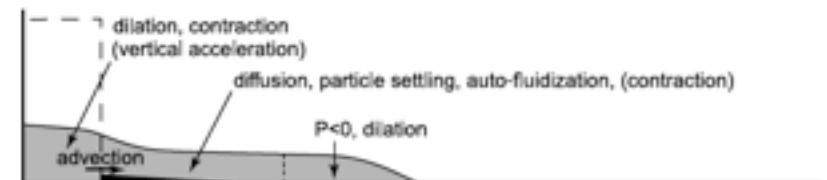


## Flow over porous media

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J. Olsthoorn, M. Stastna, and N. Soontiens, Fluid circulation and seepage in lake sediment due to propagating and trapped internal waves, *Water Resour. Res.* **48**, W11520 (2012).

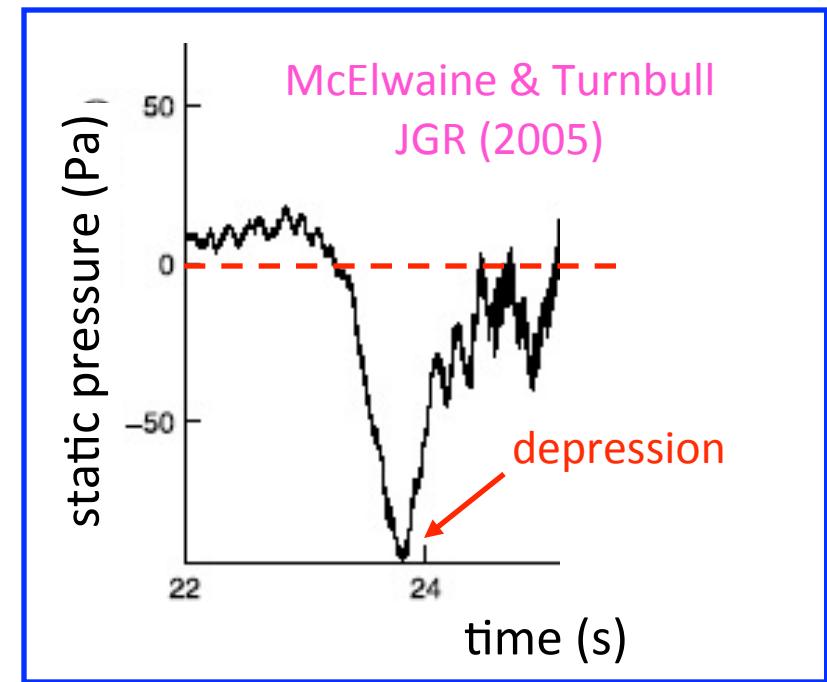
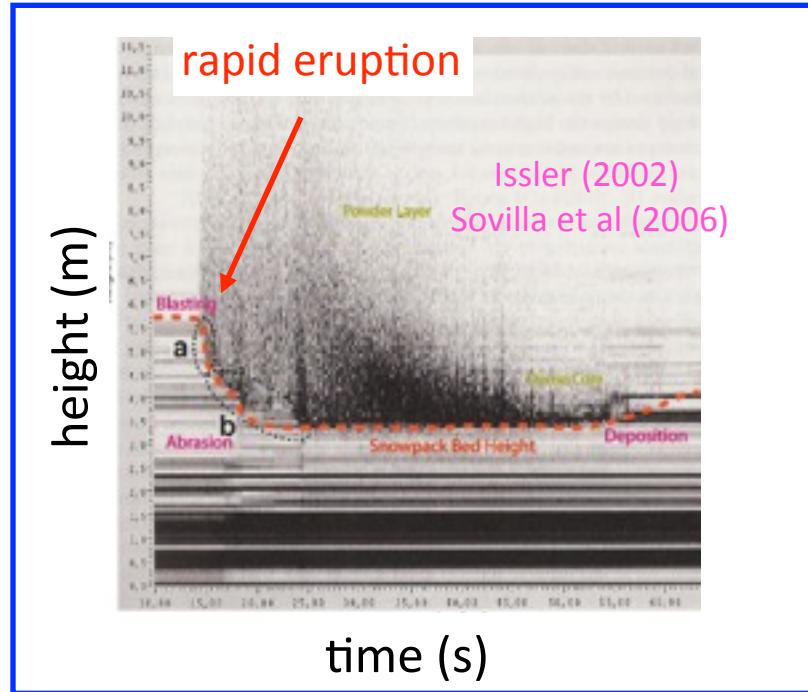
T. Yamamoto, H. L. Koning, H. Sellmeijer, and EP Van Hijum, On the response of a poro-elastic bed to water waves, *J. Fluid Mech.* **87**, 193-206 (1978).

## *Two examples*



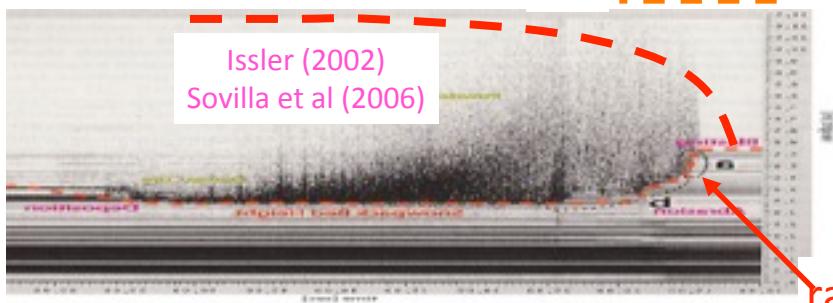
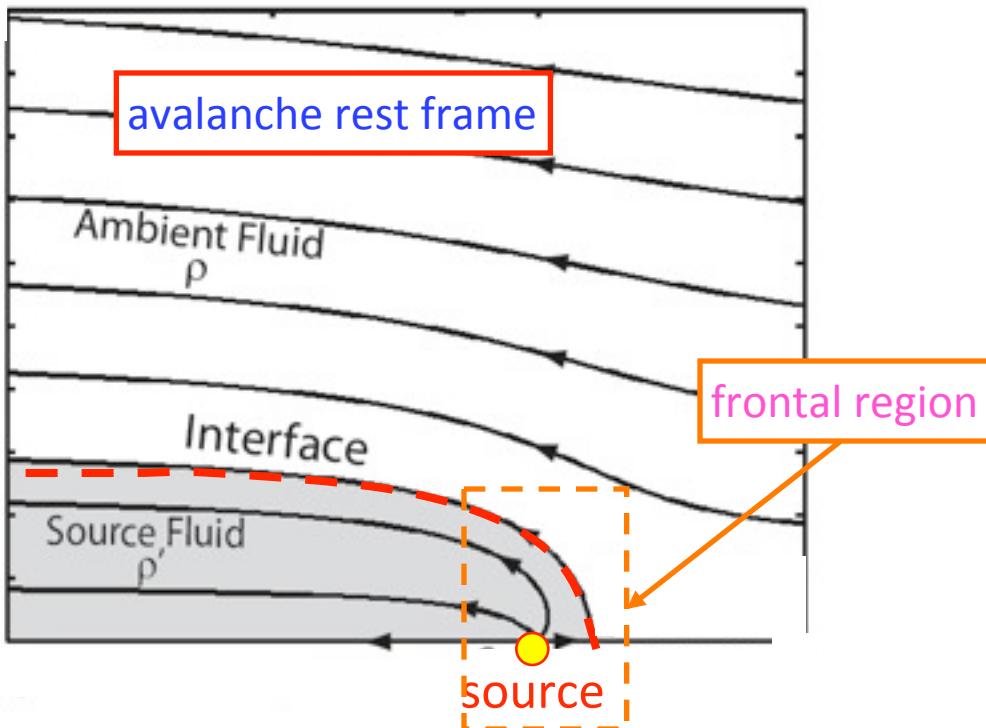
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# Eruption current



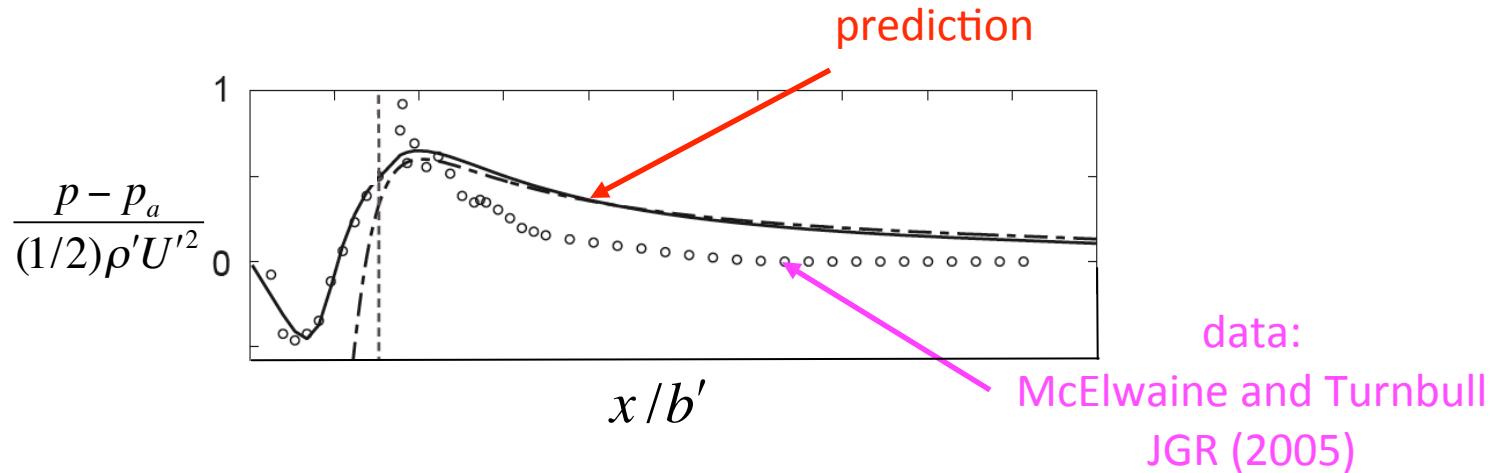
Eruption current =  
a gravity current driven by massive frontal eruption

# Eruption current frontal region



rapid eruption

# Static pressure in the cloud



pressure  $p$ , air density  $\rho$ , cloud density  $\rho'$   
stagnation-source distance  $b'$   
fluidized depth  $h'$

$$\frac{p - p_a}{(1/2)\rho'U'^2} = \frac{2(x/b') - 1}{(x/b')^2 + (h'/b')^2}$$

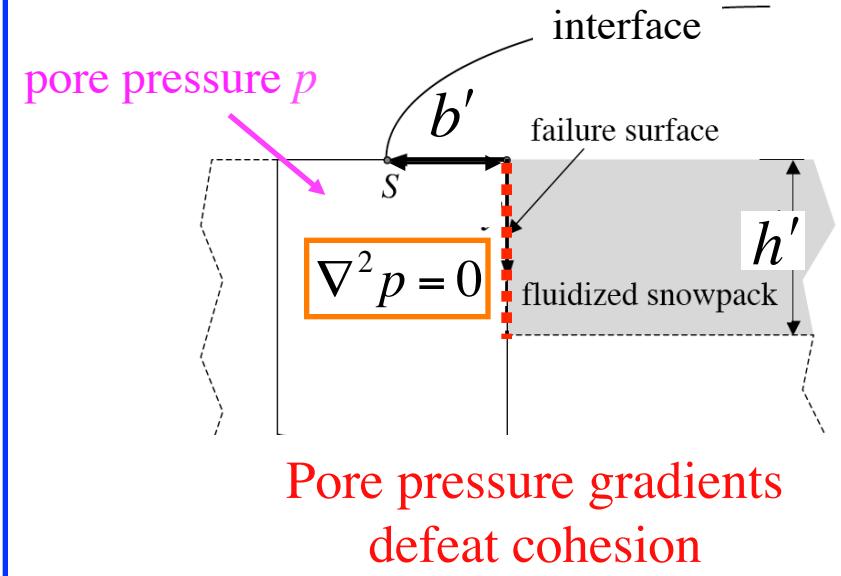
⇒ surface pressure time - history

# Porous snow pack

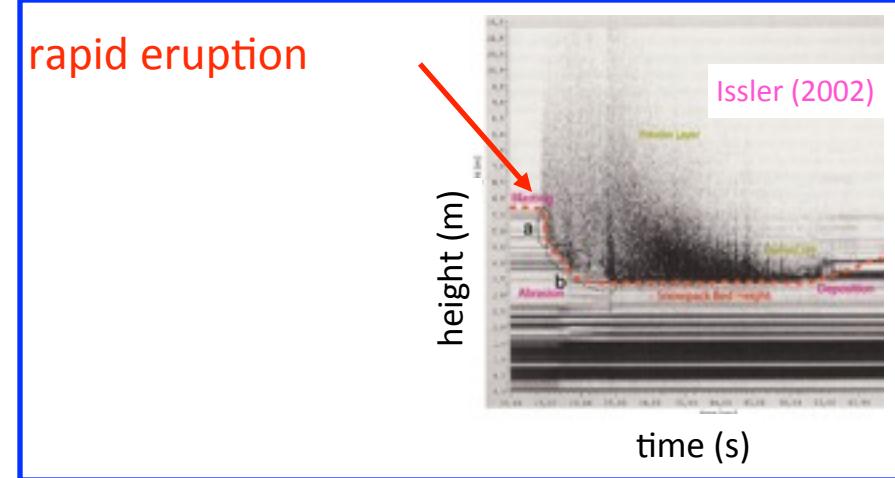
$$u = -\frac{K}{\mu} \nabla p$$

$$\nabla \cdot u = 0$$

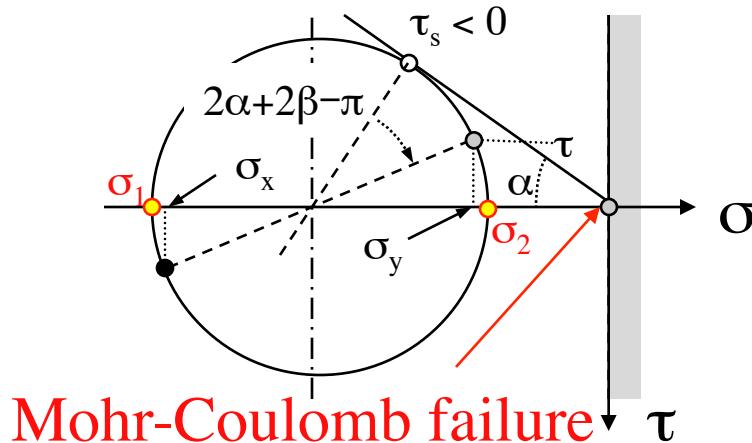
$$\nabla^2 p = 0$$



rapid eruption

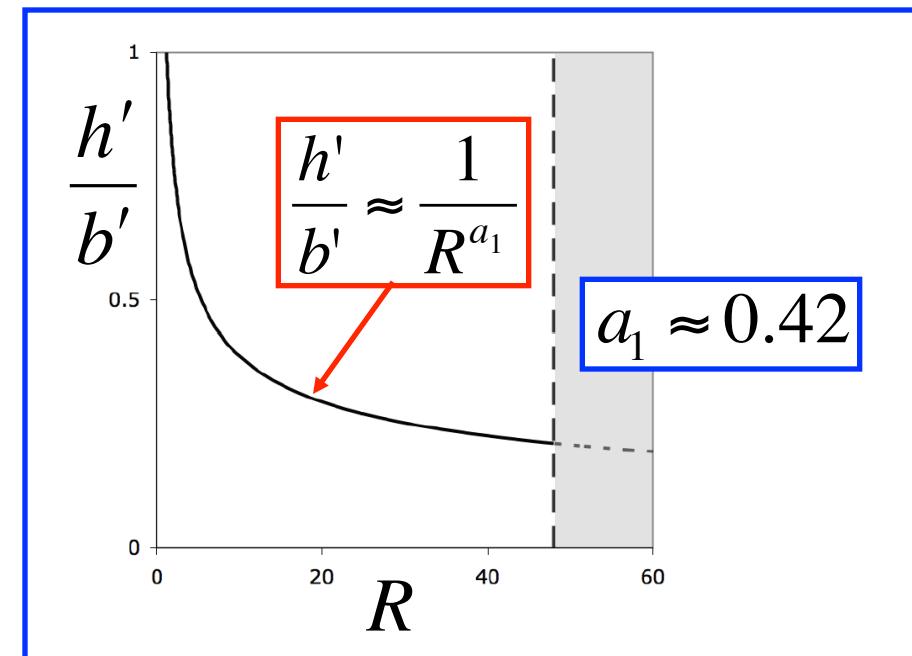
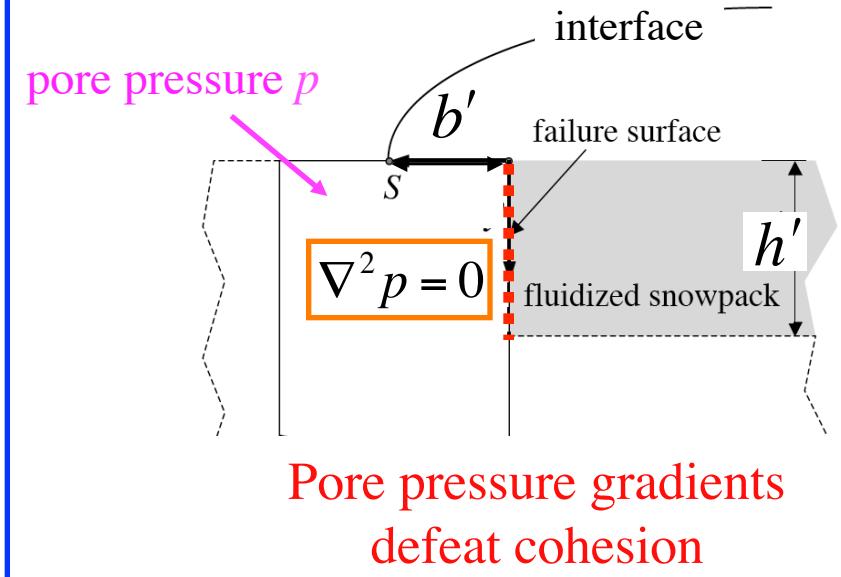


# Fluidization



$$R \equiv \frac{2\rho_c g b' \mu_e}{\rho' U'^2}$$

snowpack density  $\rho_c$ , friction  $\mu_e$



# References

<http://grainflowresearch.mae.cornell.edu>

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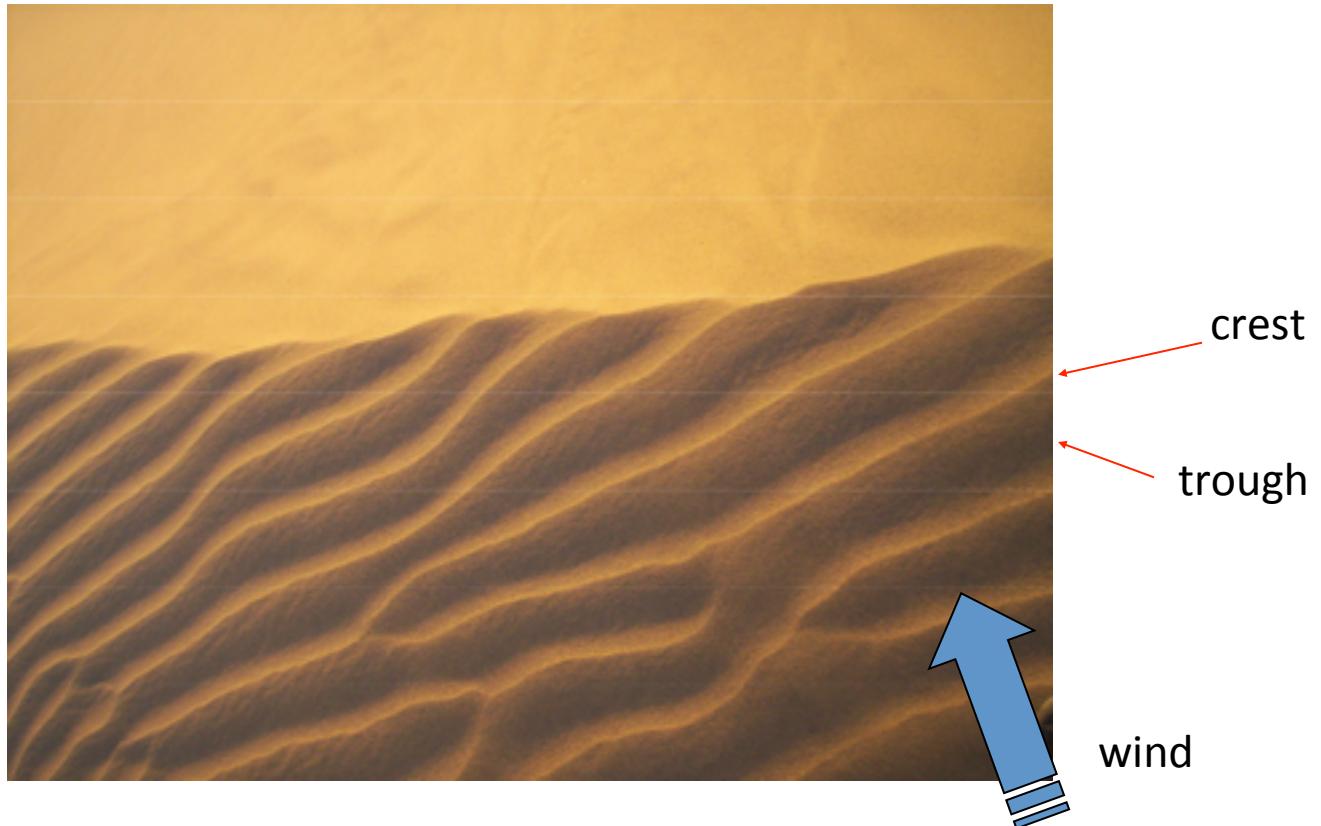
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# Sand ripples



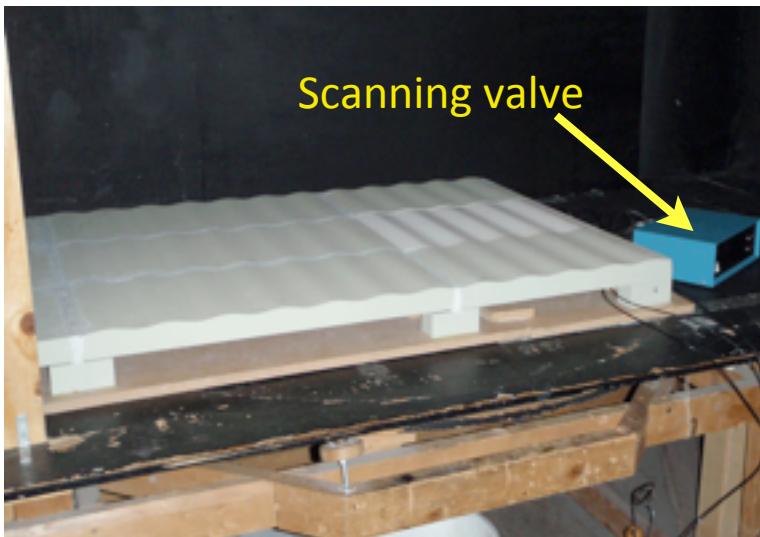
# *Wind tunnel experiments*



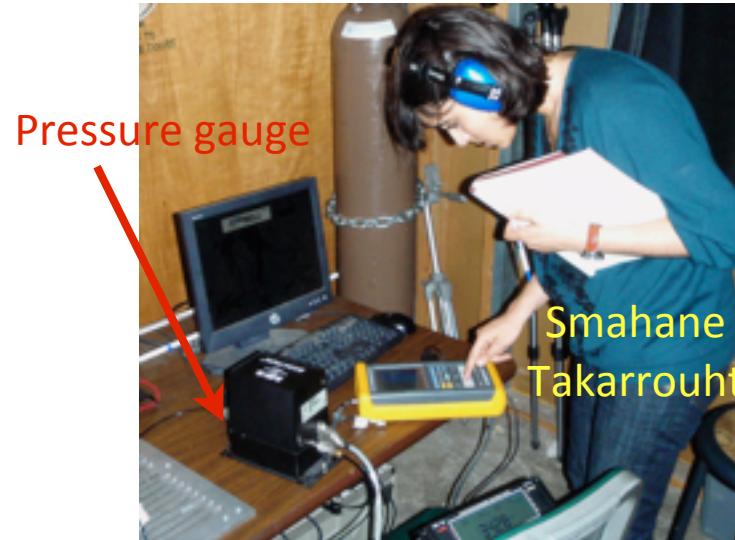
Amin Younes



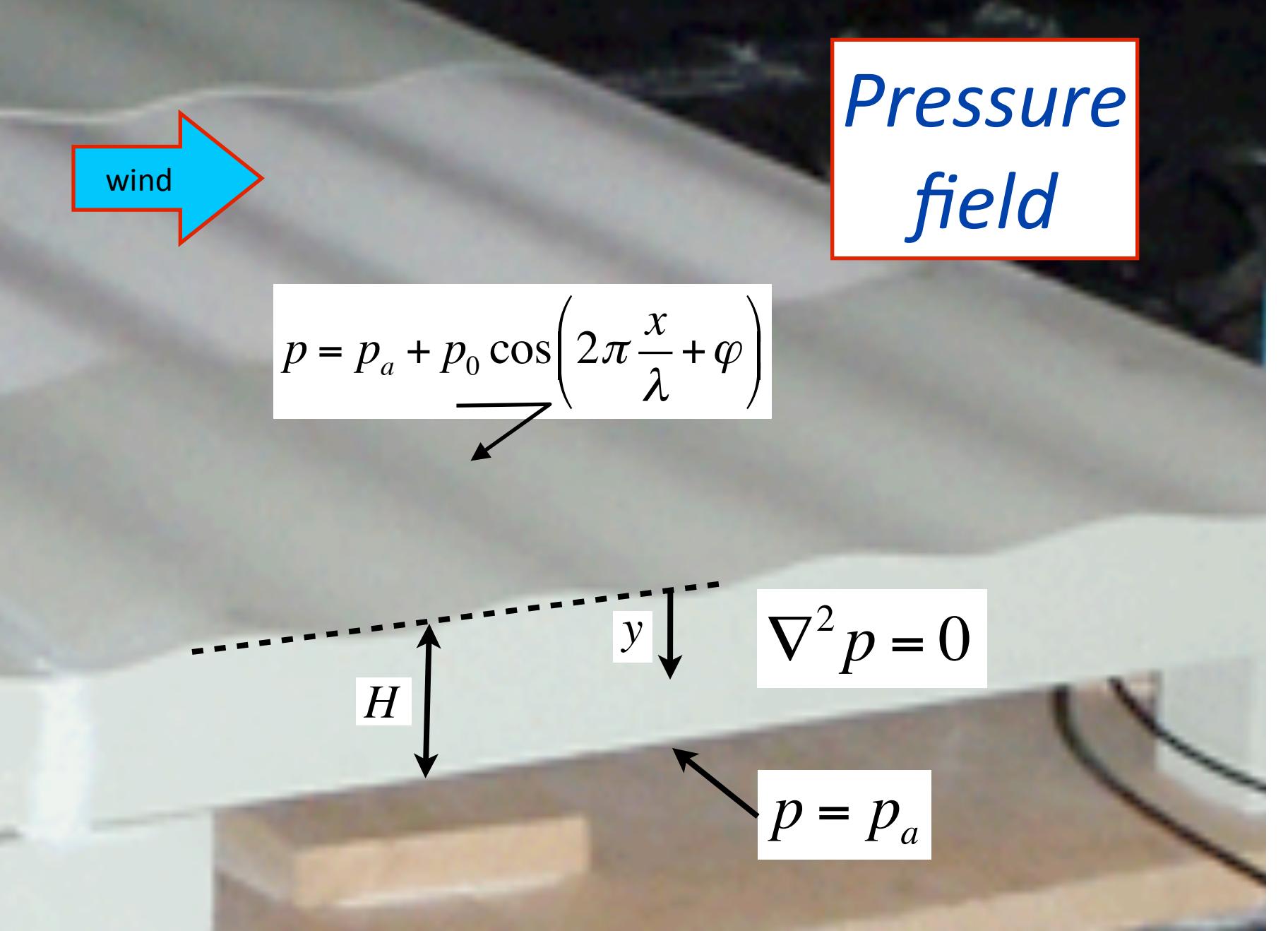
Brian  
Mittereder



Scanning valve

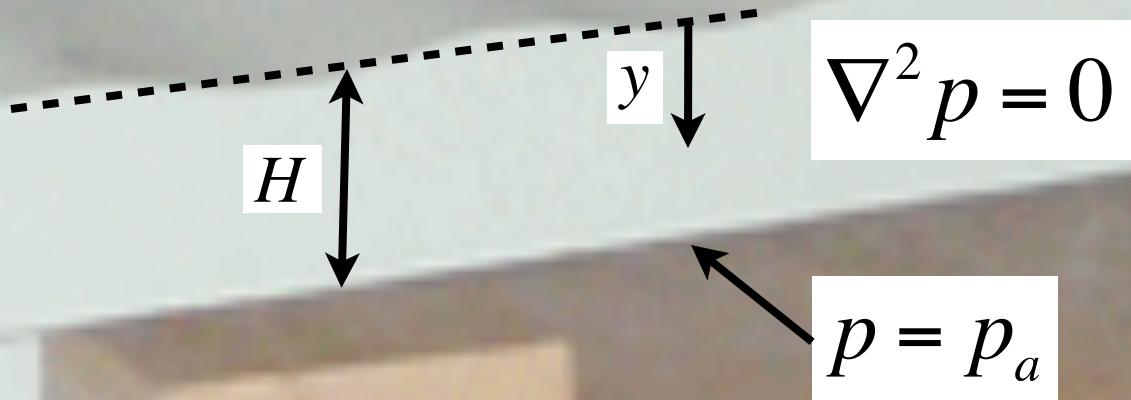


Smahane  
Takarrouht

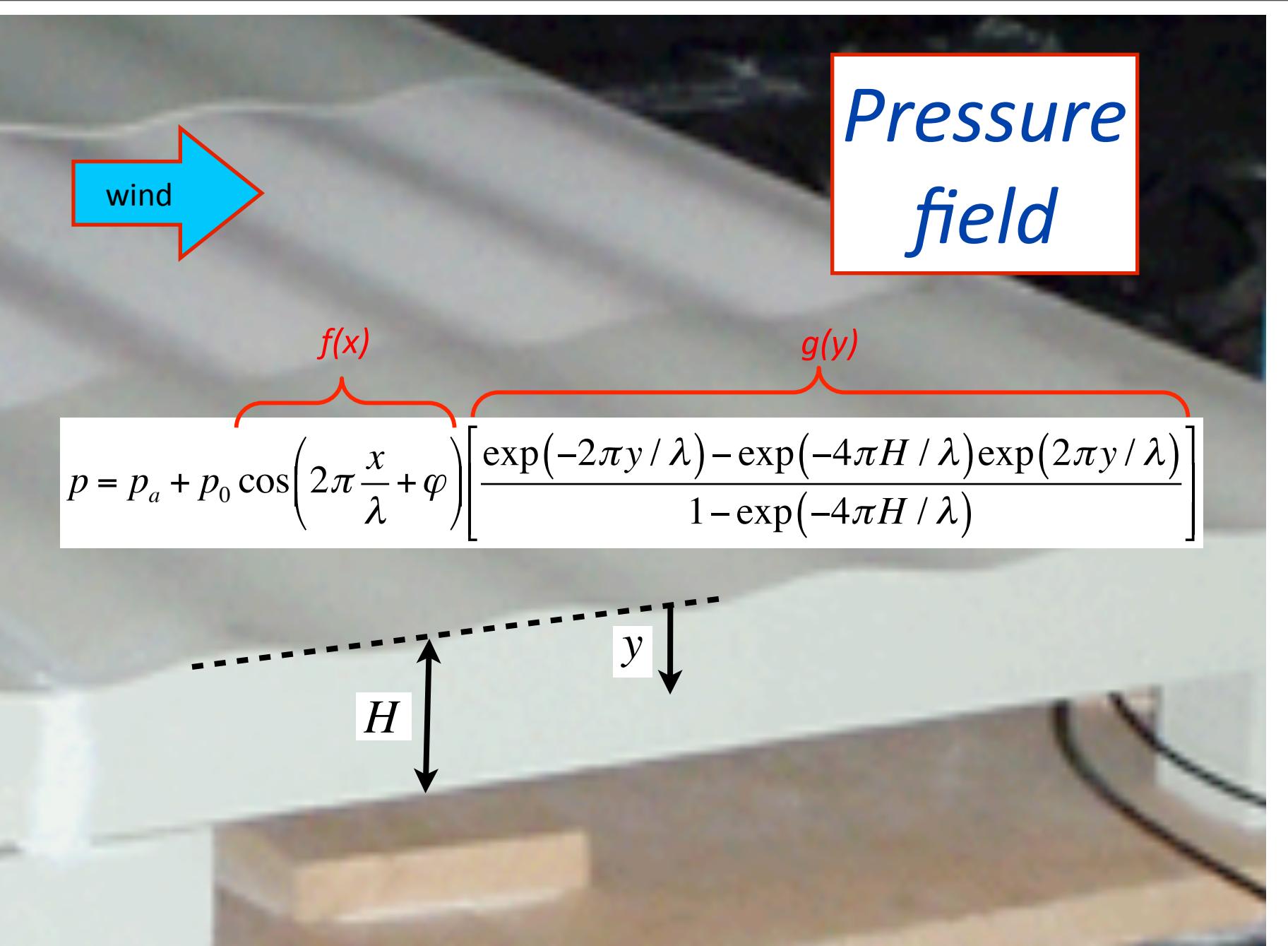


# Pressure field

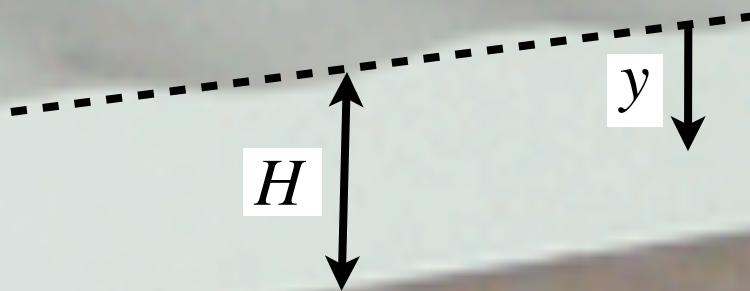
$$p = p_a + p_0 \cos\left(2\pi \frac{x}{\lambda} + \varphi\right)$$



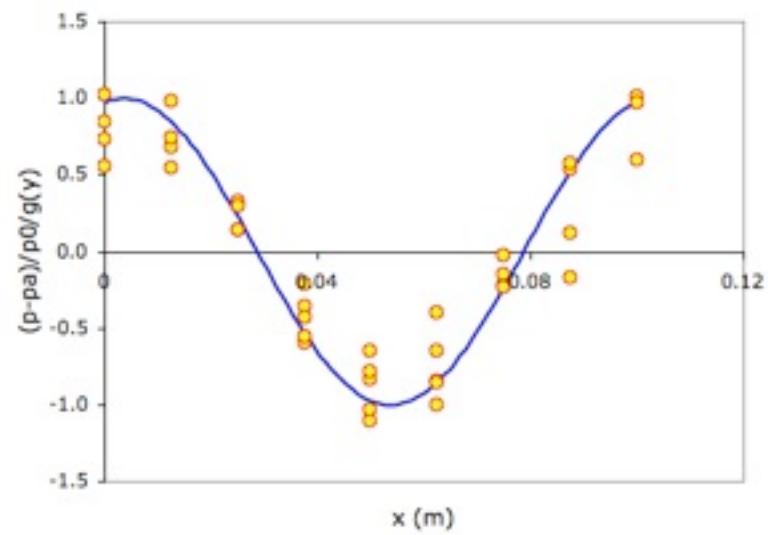
# Pressure field


$$p = p_a + p_0 \cos\left(2\pi \frac{x}{\lambda} + \varphi\right) \left[ \frac{\exp(-2\pi y / \lambda) - \exp(-4\pi H / \lambda) \exp(2\pi y / \lambda)}{1 - \exp(-4\pi H / \lambda)} \right]$$

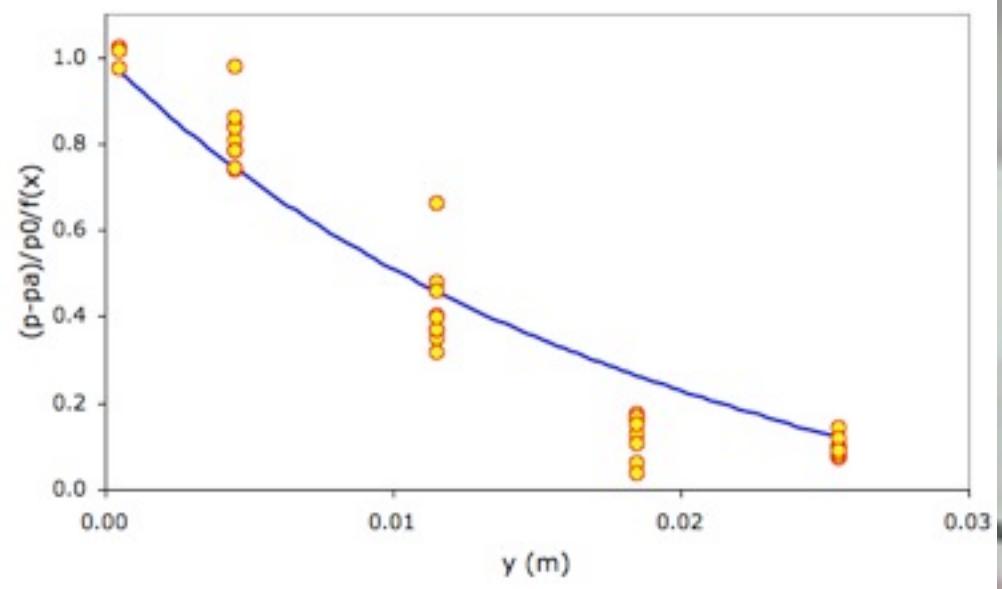
The equation shows the pressure field  $p$  as a function of position  $x$  and  $y$ . It includes a constant atmospheric pressure  $p_a$ , a wind stress coefficient  $p_0$ , a wavelength  $\lambda$ , a phase shift  $\varphi$ , and a height  $H$ . The terms  $f(x)$  and  $g(y)$  are indicated by red brackets above the first and second terms of the equation respectively.



# Pressure field



$$h_0 / \lambda = 3\%$$



# *Toward fluidization*

$$\text{body force} = -\nabla p + \rho_s v g$$

$$\text{fluidization} \Leftrightarrow \frac{\partial p}{\partial y} \geq \rho_s v g$$

$$p^* \equiv \left( \frac{p}{\rho u^2} \right) \left( \frac{\lambda}{h_0} \right)$$

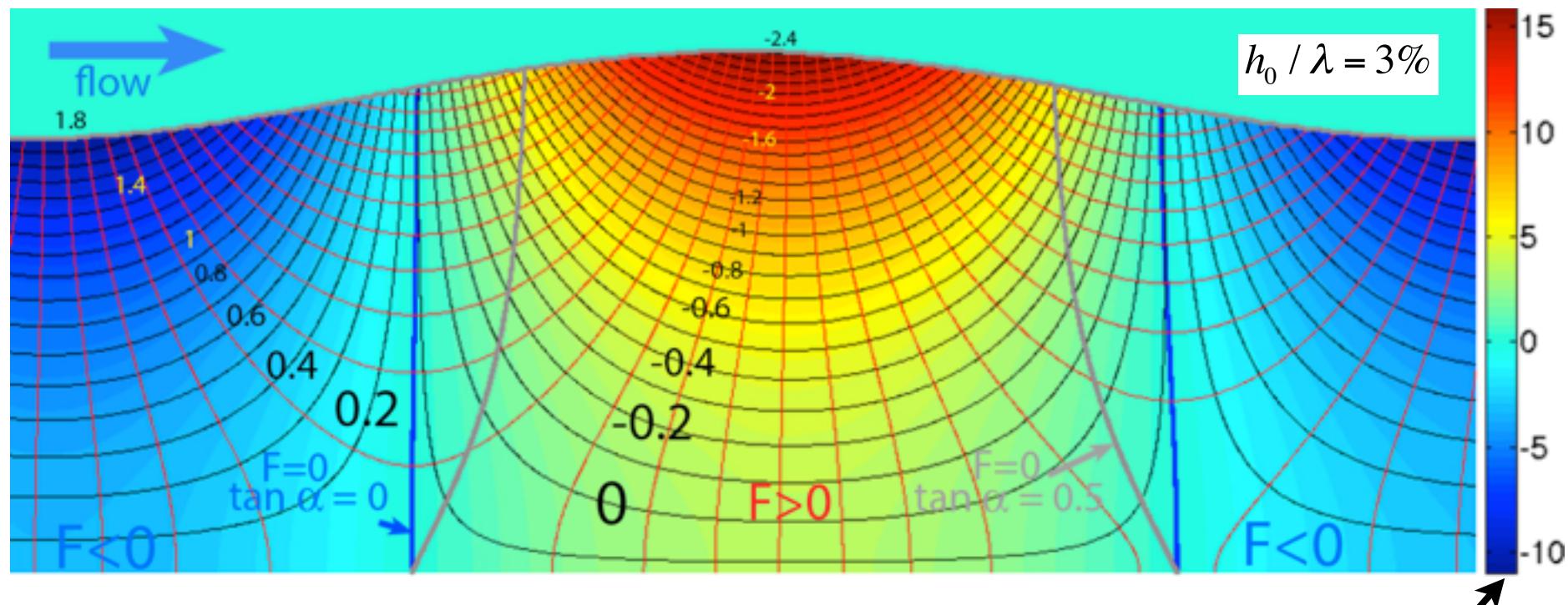
Jackson, P.S., and J.C.R. Hunt, Turbulent  
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Soc. 101, 929-955 (1975).

$$y^* \equiv \frac{y}{\lambda}$$

$$F \equiv \frac{\partial p^*}{\partial y^*} - \tan \alpha \left| \frac{\partial p^*}{\partial x^*} \right| \quad R \equiv \frac{\rho u^2 h_0}{\rho_s v g \lambda^2}$$

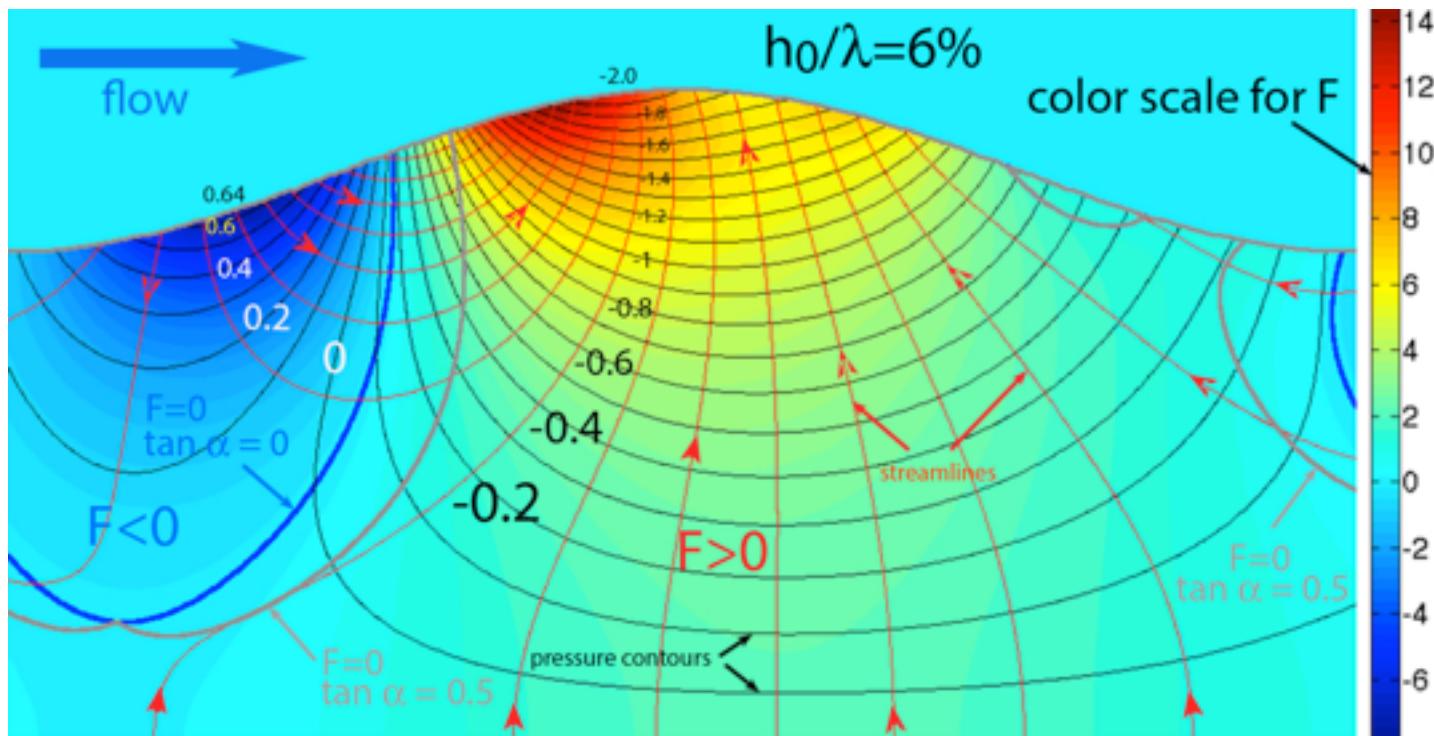
$$\text{fluidization} \Leftrightarrow FR \geq 1$$

# Toward fluidization



$$F \equiv \frac{\partial p^*}{\partial y^*} - \tan \alpha \left| \frac{\partial p^*}{\partial x^*} \right|$$

# Toward fluidization



$$\frac{h_0 d}{\lambda^2} > 0.003 \Rightarrow \nabla p \text{ matters more than Shields}$$



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## *Conclusions*



Flow-induced pressure gradients  
matter to sediment uplift  
over permeable media

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Smahane Takarrouft



Amin Younes



Jin Xu

<http://grainflowresearch.mae.cornell.edu/index.html>