

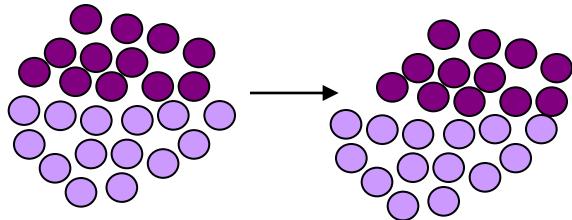
# Deformation of Metallic Glasses: Experimental Puzzles and Theoretical Needs

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Massachusetts Institute of Technology

With special contributions from:  
Eric Homer, David Rodney, Corinne Packard, Naser Al-Aqeeli,  
Oliver Franke

# The prevailing mechanistic view



Shear Transformation Zone (STZ)

Interacting STZs

???

Independent STZs

$$\dot{\gamma} = \alpha_0 v_0 \gamma_0 \cdot \exp\left(-\frac{Q}{kT}\right) \sinh\left(\frac{\tau V}{kT}\right)$$

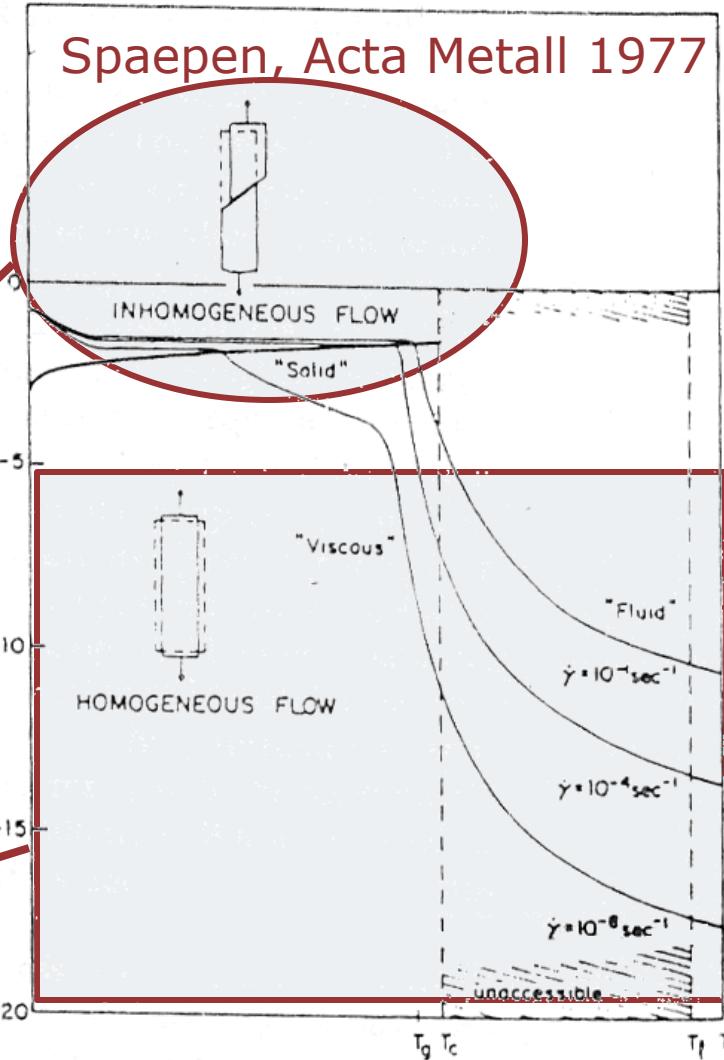
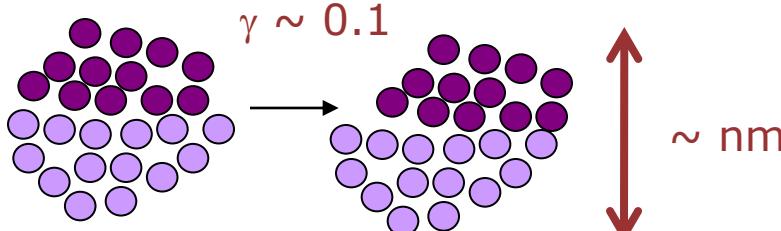
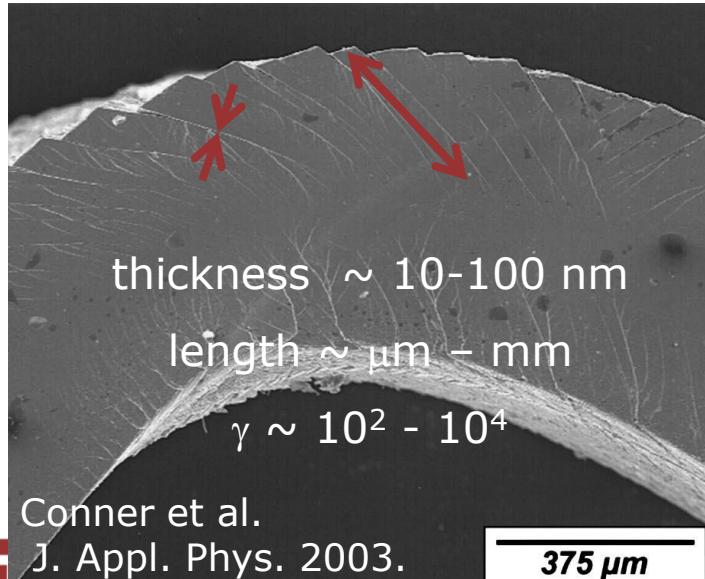
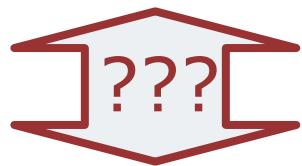


Fig. 2. Schematic deformation map of a metallic glass. The various modes of deformation are indicated.

# Puzzles: the gap between atomic motion and shear bands



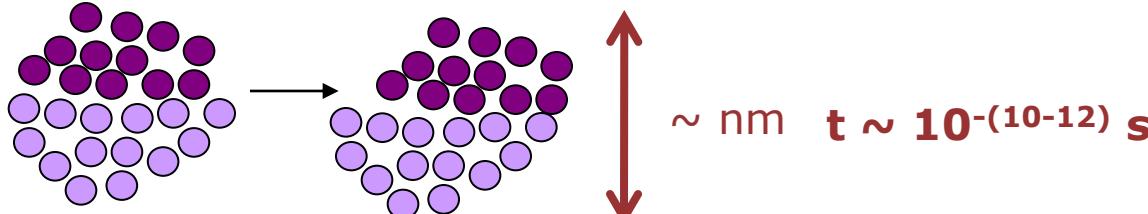
after Argon. Acta Metall. 1979.



- Kinetics
- Behavior in gradients of stress
- Event spectrum

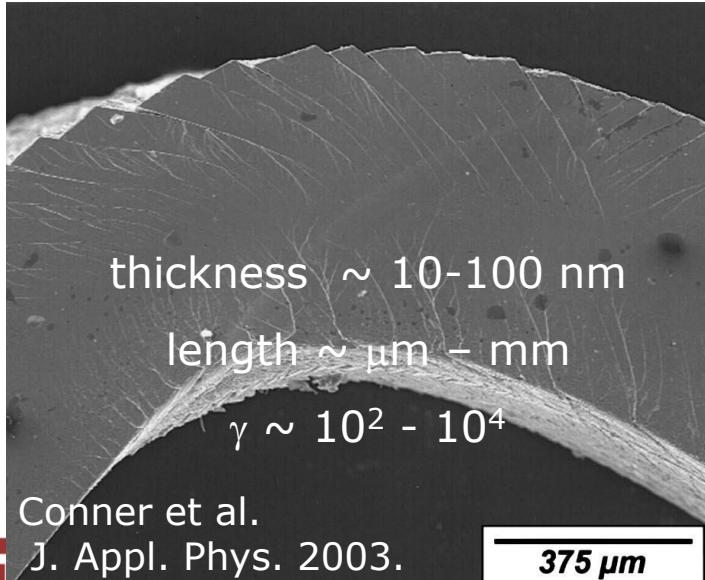
# Kinetics

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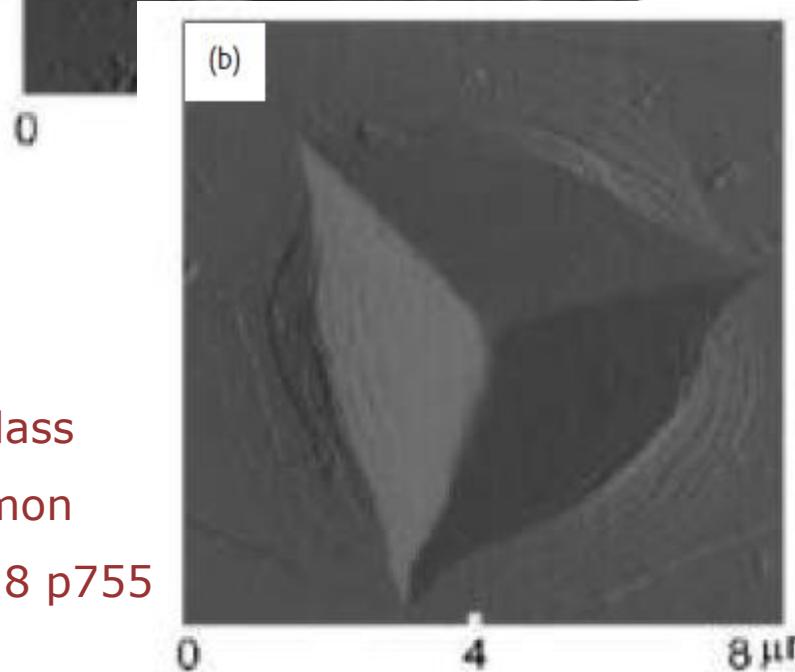
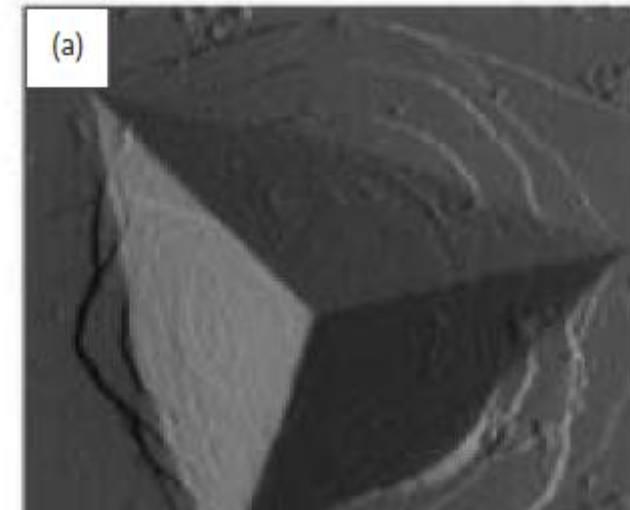
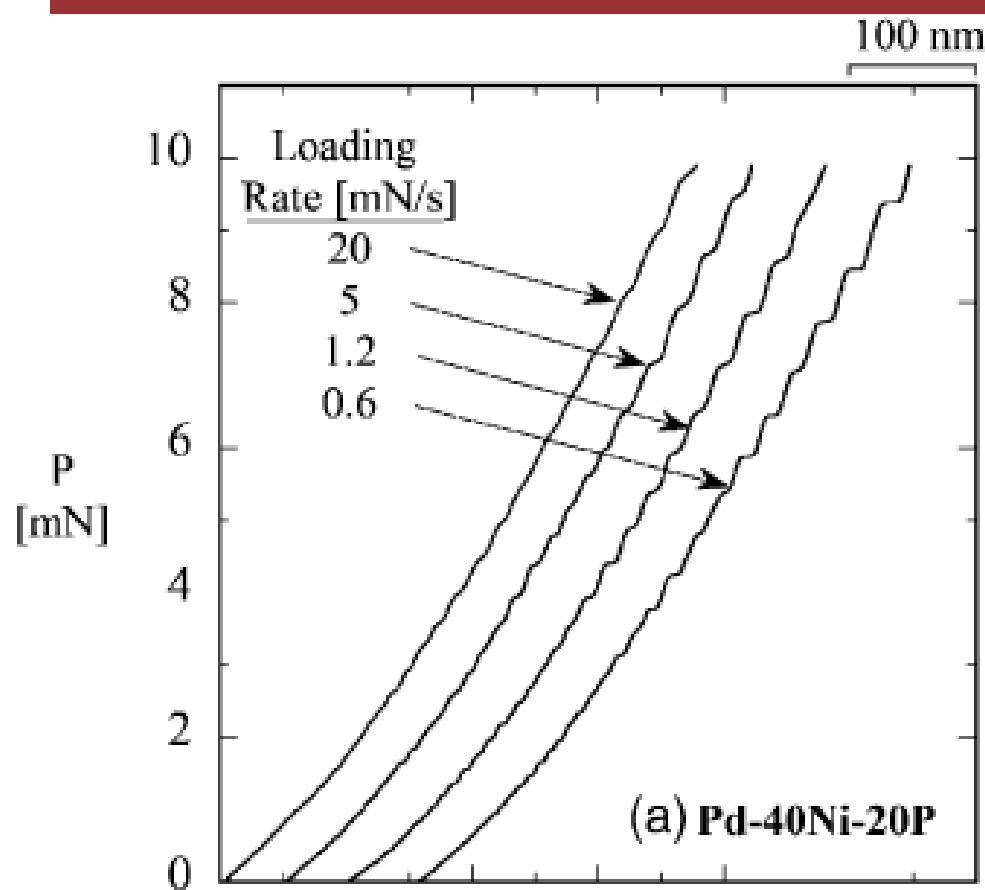
after Argon. Acta Metall. 1979.

$$\sim \text{nm} \quad t \sim 10^{-(10-12)} \text{ s}$$



$$t \sim ???$$

# Timescale for shear bands



Schuh, Nieh

Al based glass

Jiang, Atzmon

JMR (2003) v18 p755

Acta Mater (2003) v51 p87



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# Timescale for shear bands

Critical strain rates:

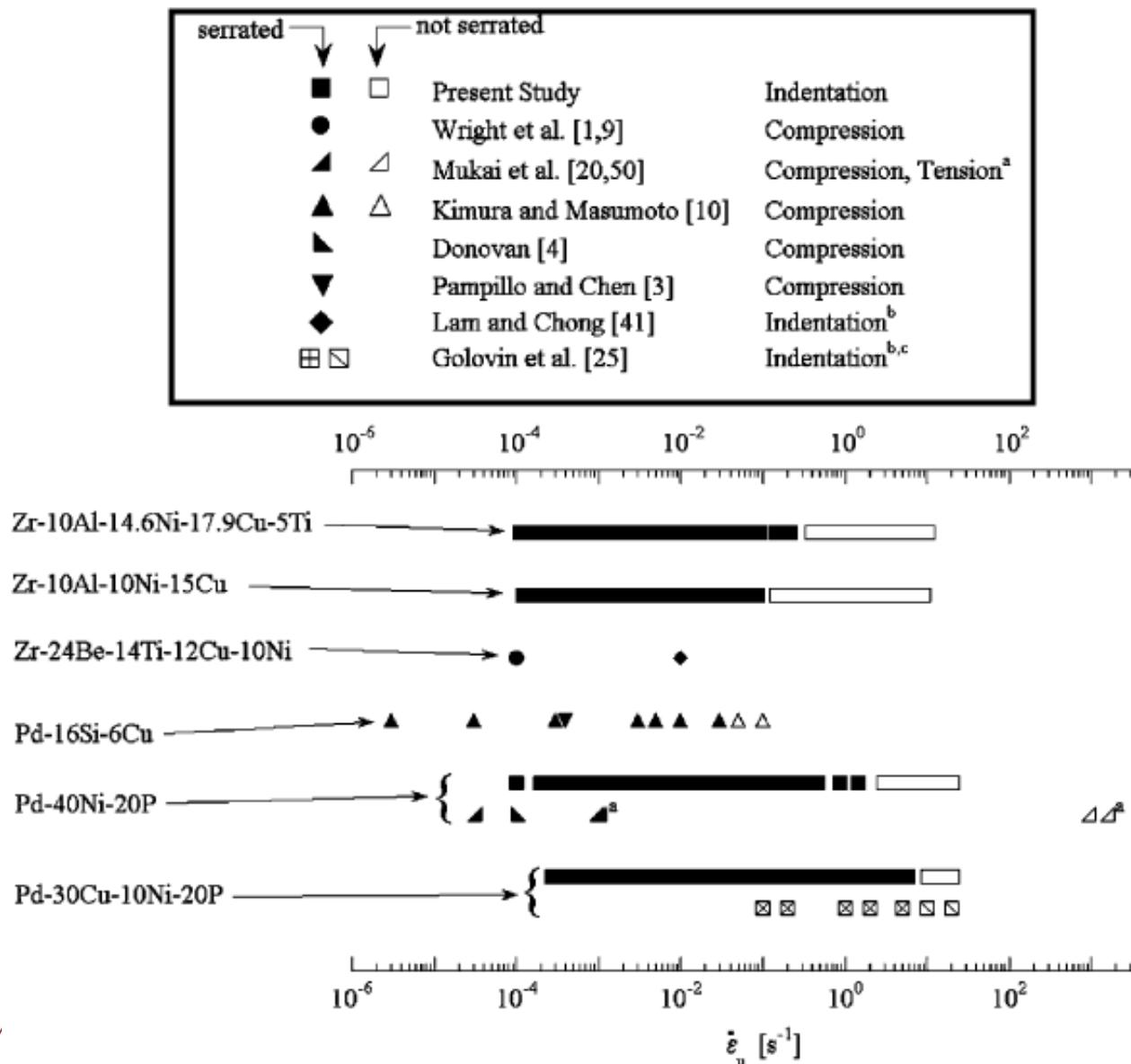
**$10^{-1}$  to  $10^1 \text{ s}^{-1}$**

Strain accommodated:

**.05**

Critical time:

**0.4 to 40 ms**



Schuh, Nieh

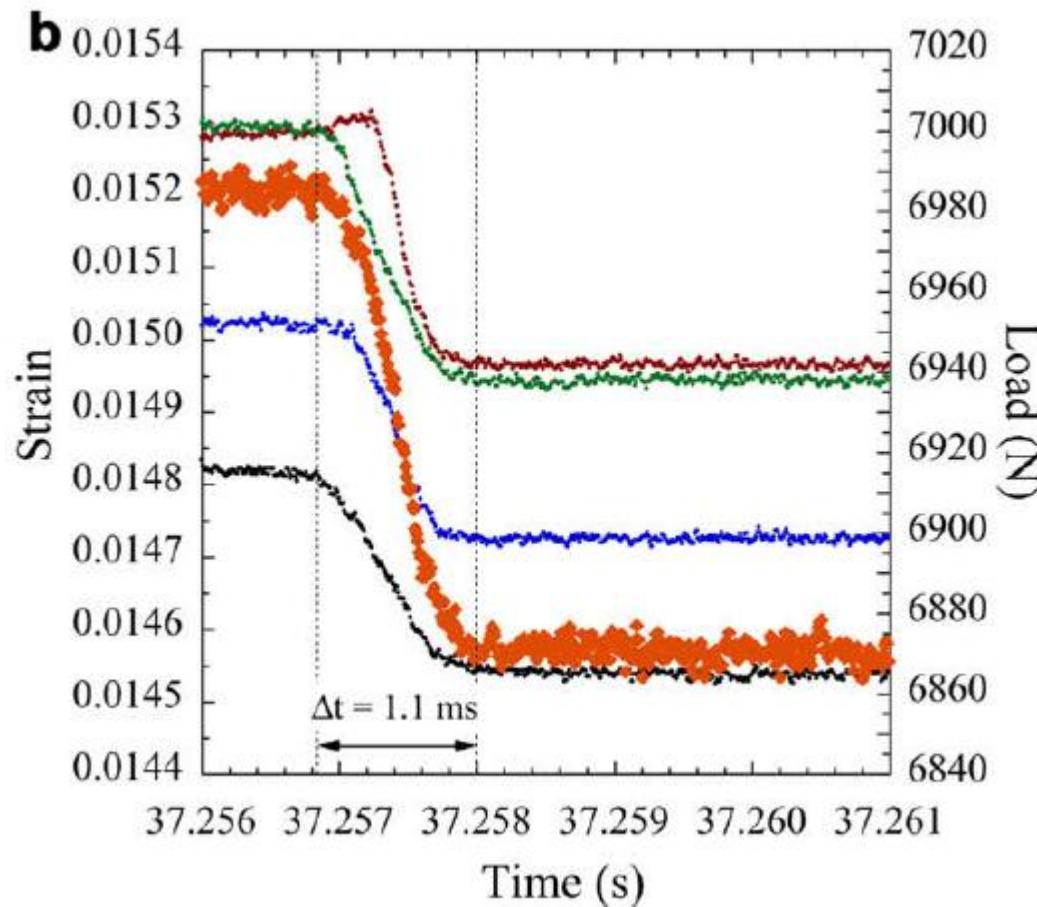
Acta Mater (2003) v51 p87



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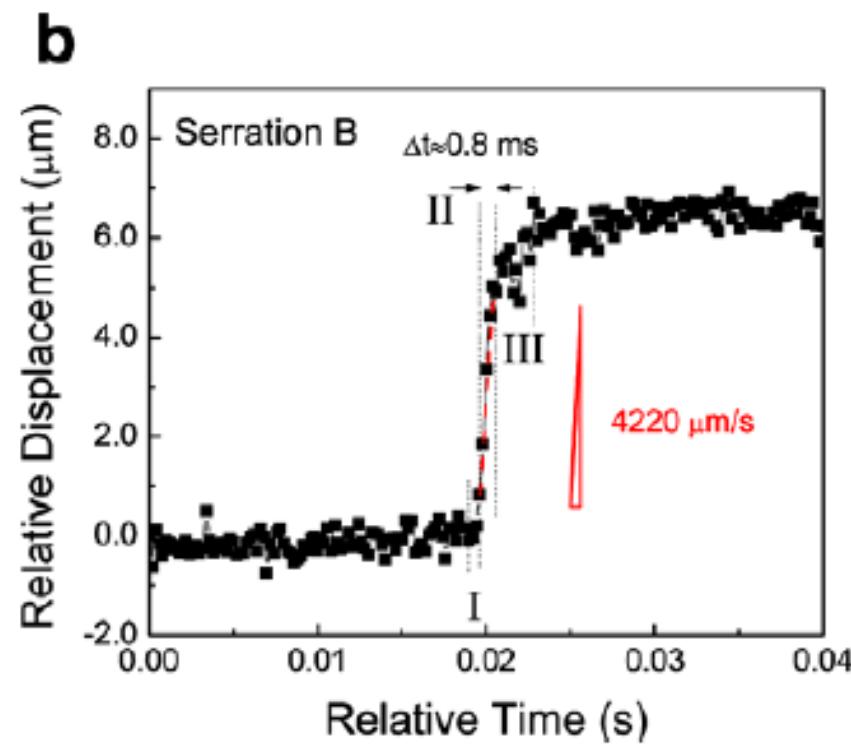
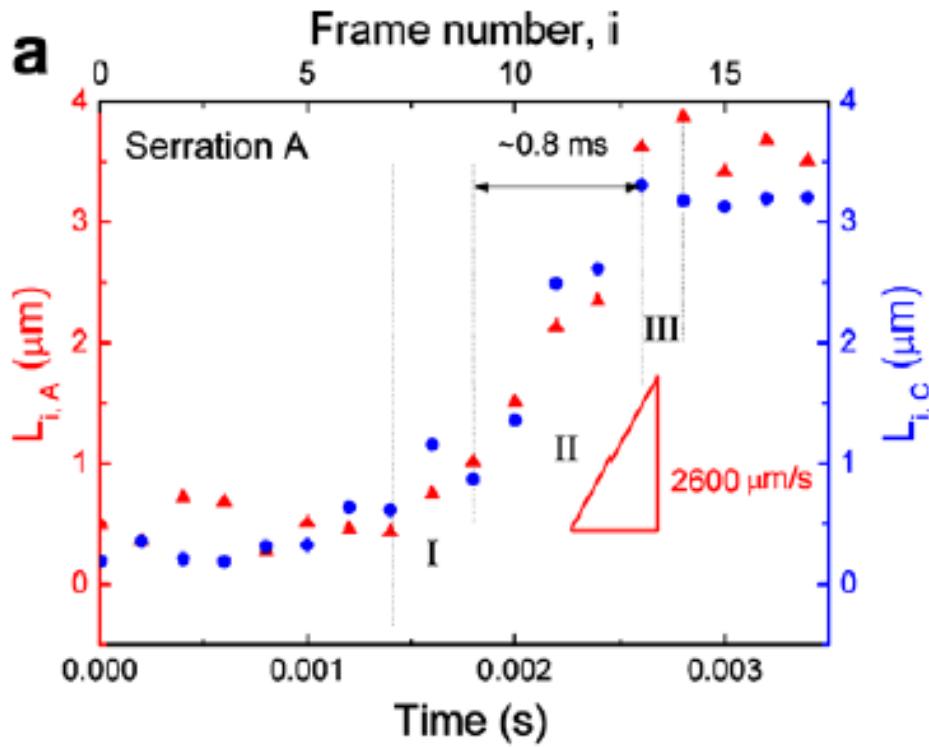
# Strain gauge measurements

Wright et al. Acta Mater (2009) v57 4639

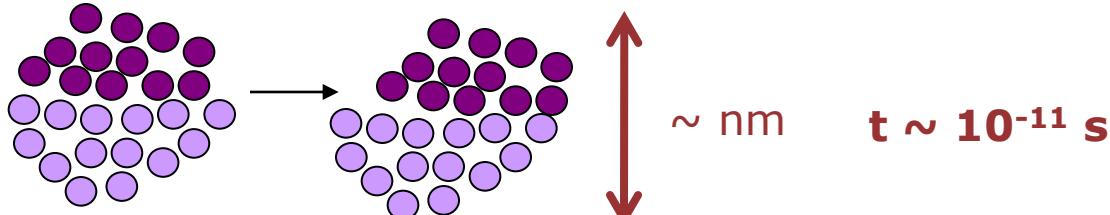


# High speed videography

Song and Nieh (2010) Scripta Mater v62 847

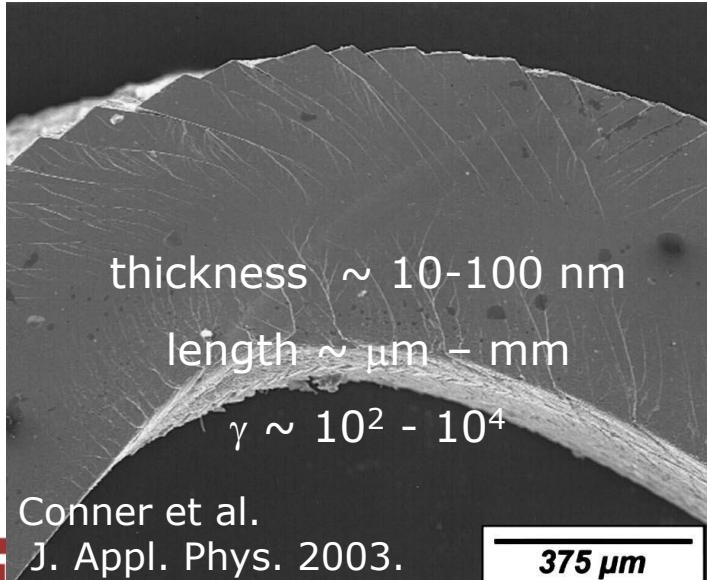


# Kinetics



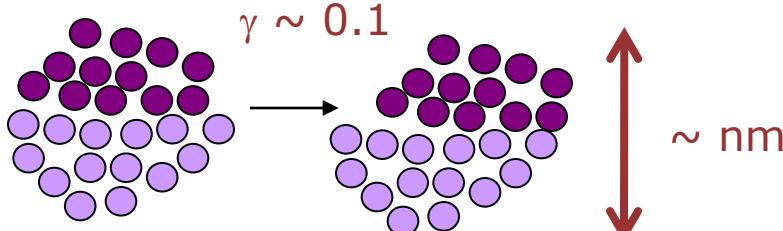
after Argon. Acta Metall. 1979.

**What controls the shear band timescale?**

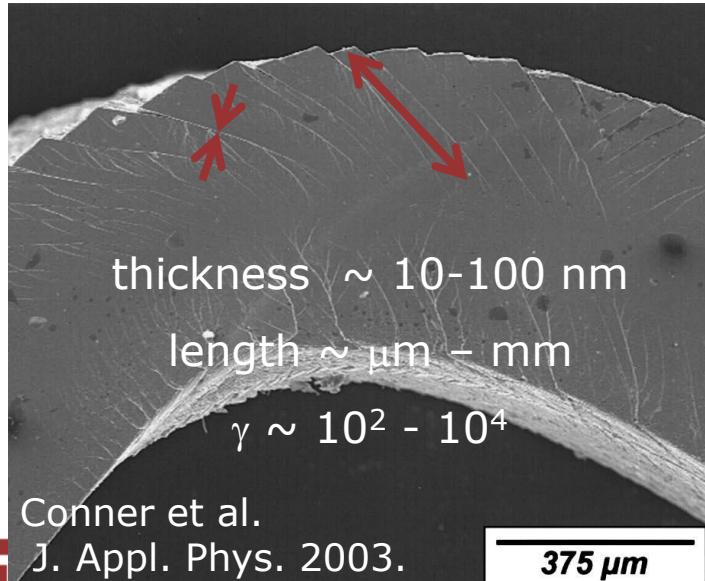
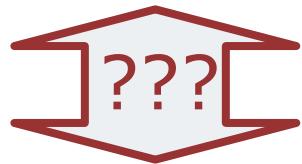


$t \sim 10^{-3} \text{ s}$

# Puzzles: the gap between atomic motion and shear bands



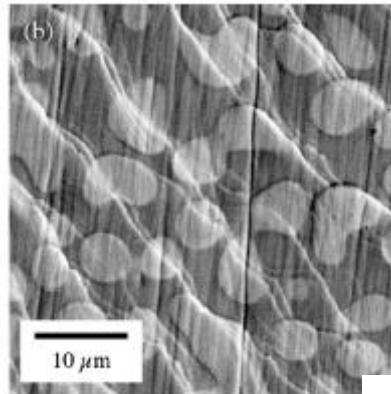
after Argon. Acta Metall. 1979.



- Kinetics
- Behavior in gradients of stress
- Event spectrum

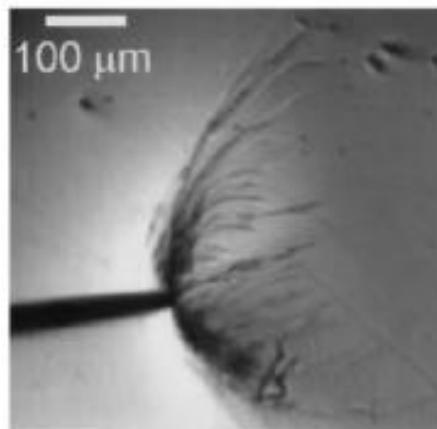
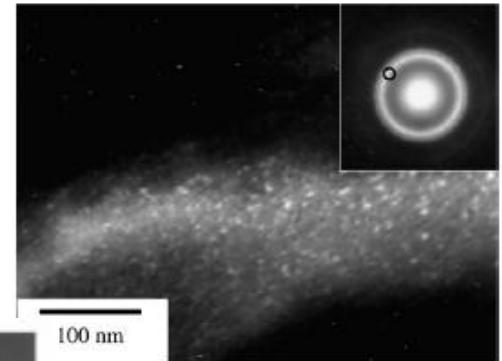
# Shear localization around stress concentrators

- Glass-matrix composites
- Phase transformations during deformation
- Fracture mechanics



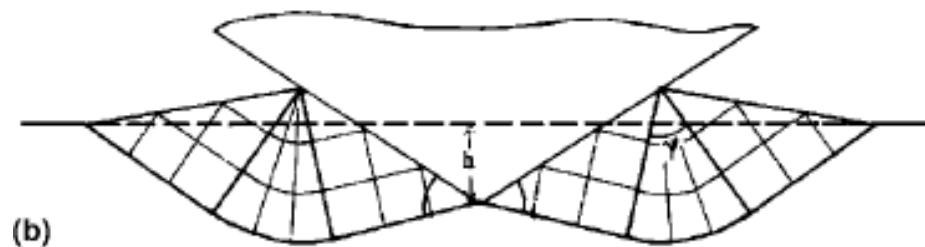
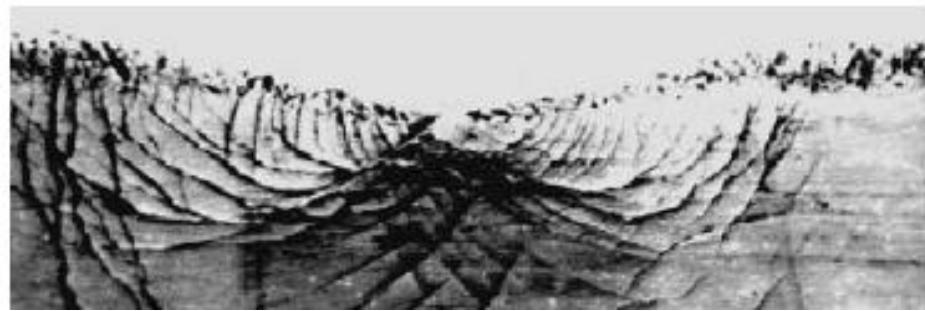
Hays et al.  
PRL (2000)  
v84, 2901

Jiang, Atzmon,  
Acta Mater (2003)  
v51, p4095



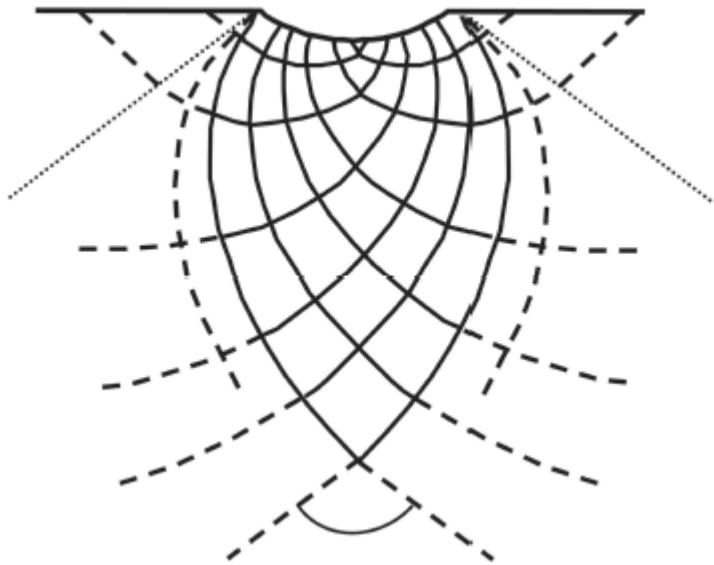
Flores, Dauskardt  
Scripta Mater (1999)  
v41, p937

# Slip line fields

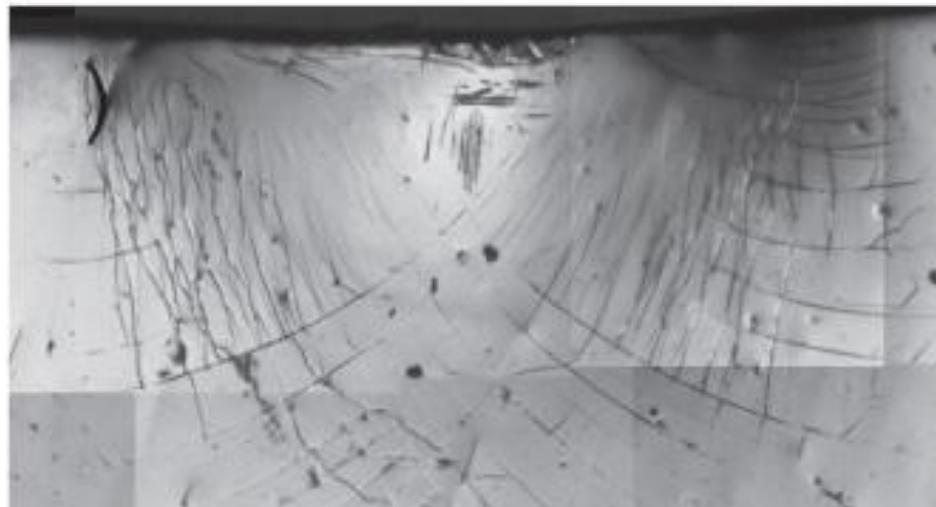


(b)

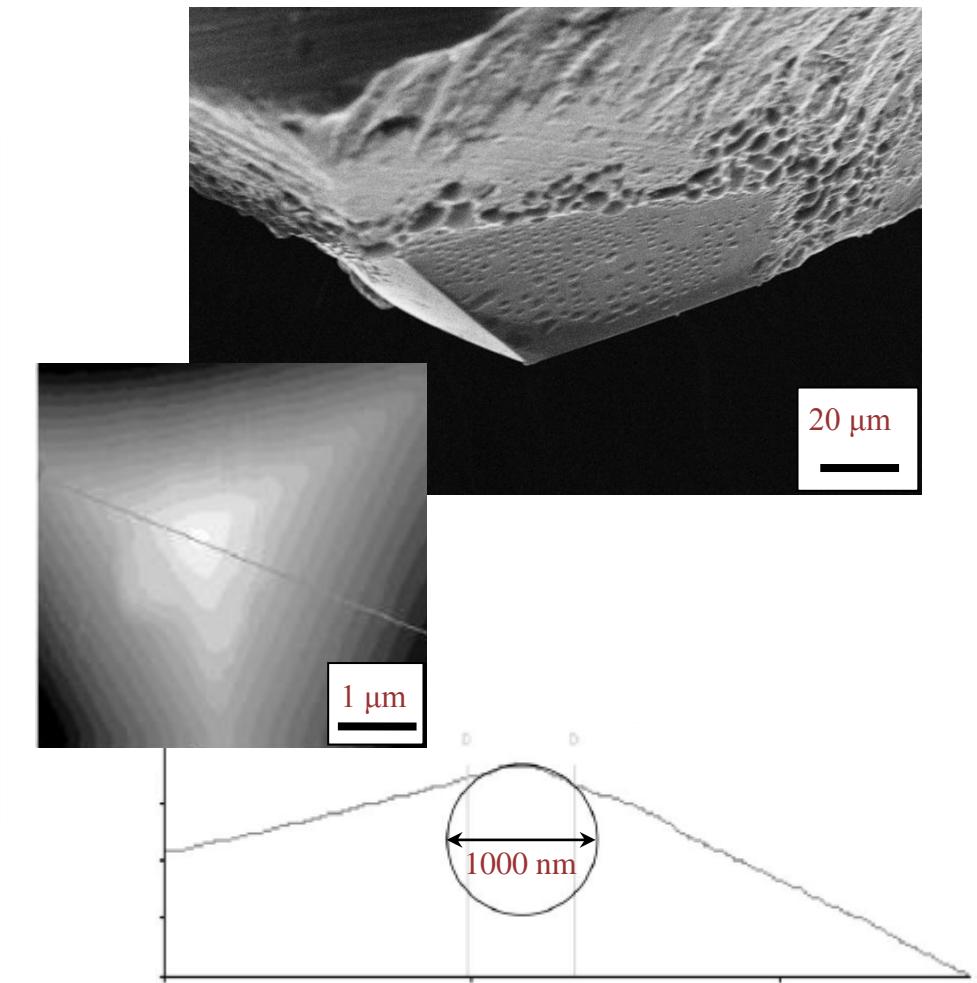
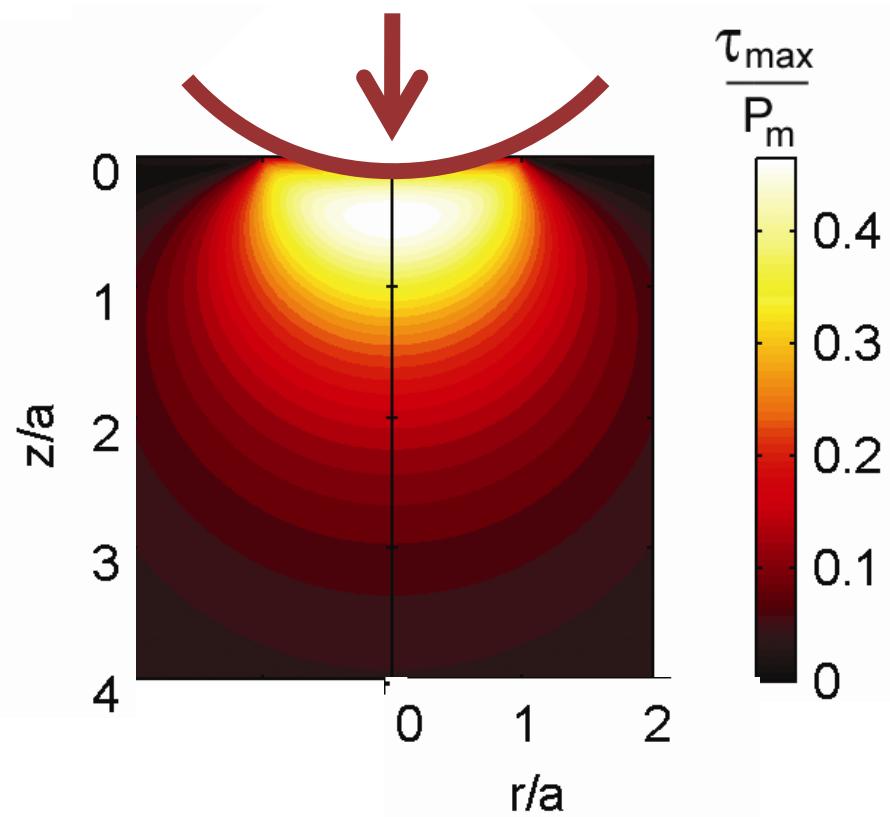
Schuh, Nieh  
JMR (2004) v19 46



Antoniou, JMR (2007) v22 514

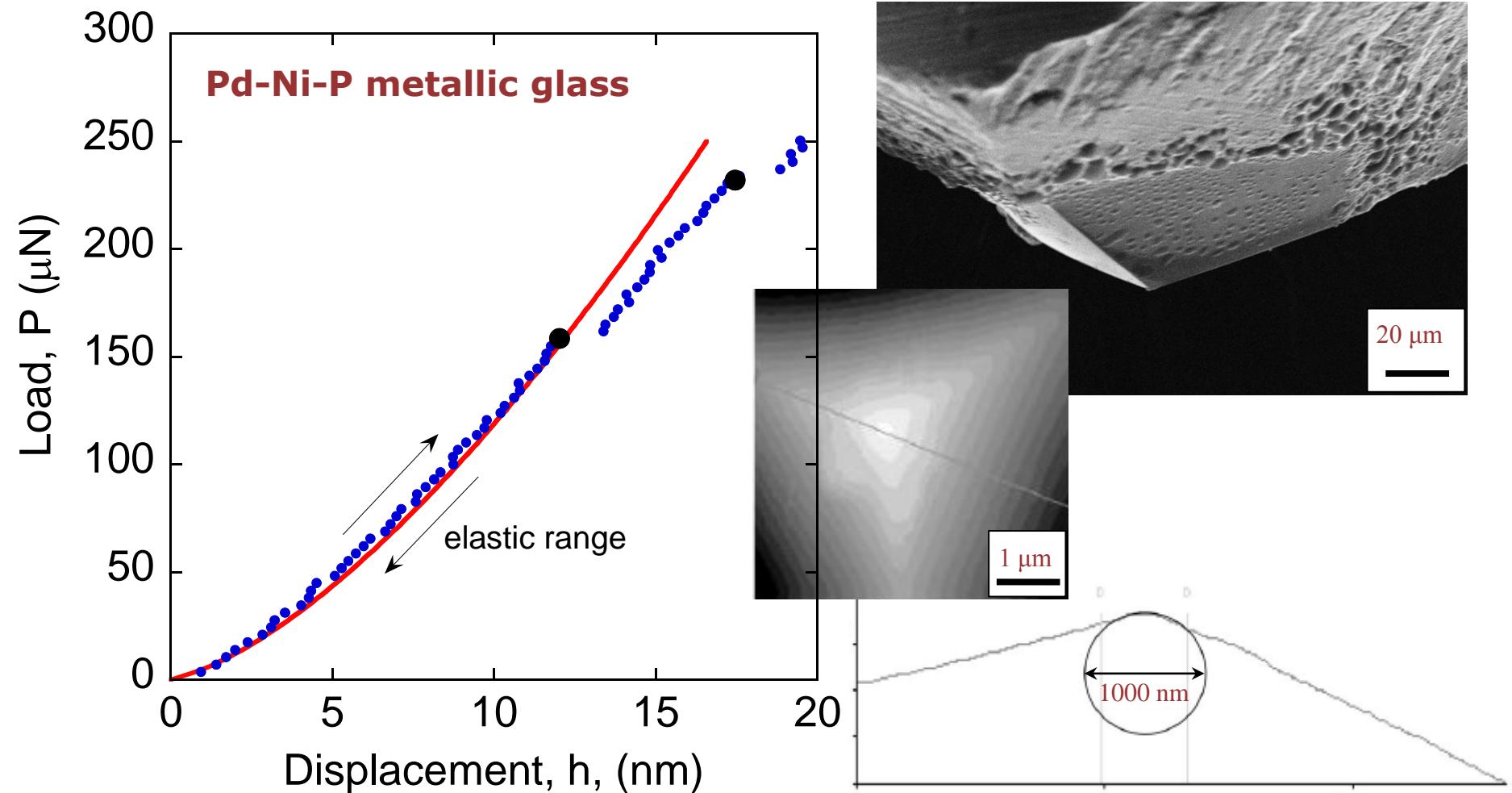


# Nanoindentation measurements



Images from Trelewicz, Packard (MIT)  
as well as Chiu and Ngan, Acta Mater, 2002

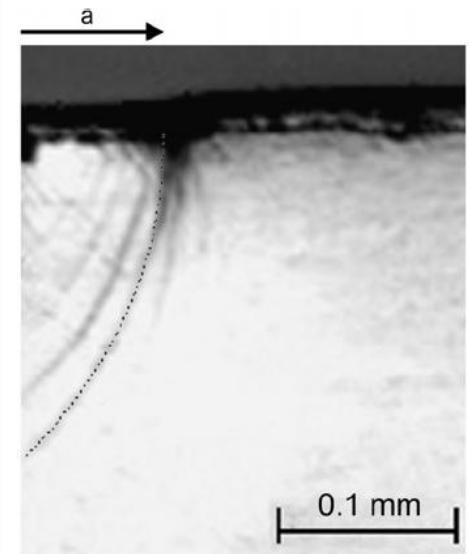
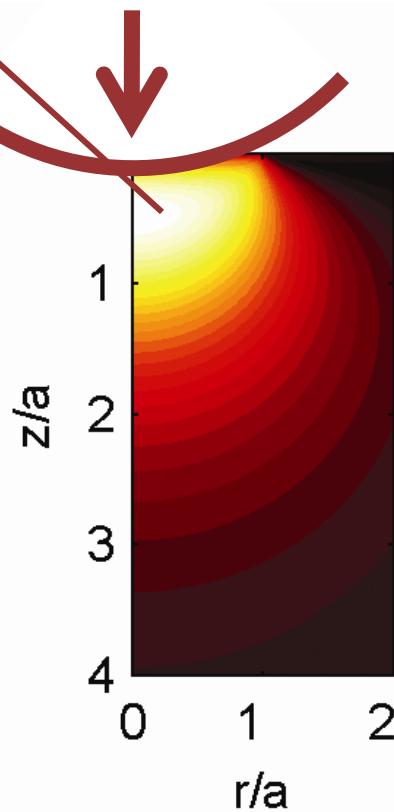
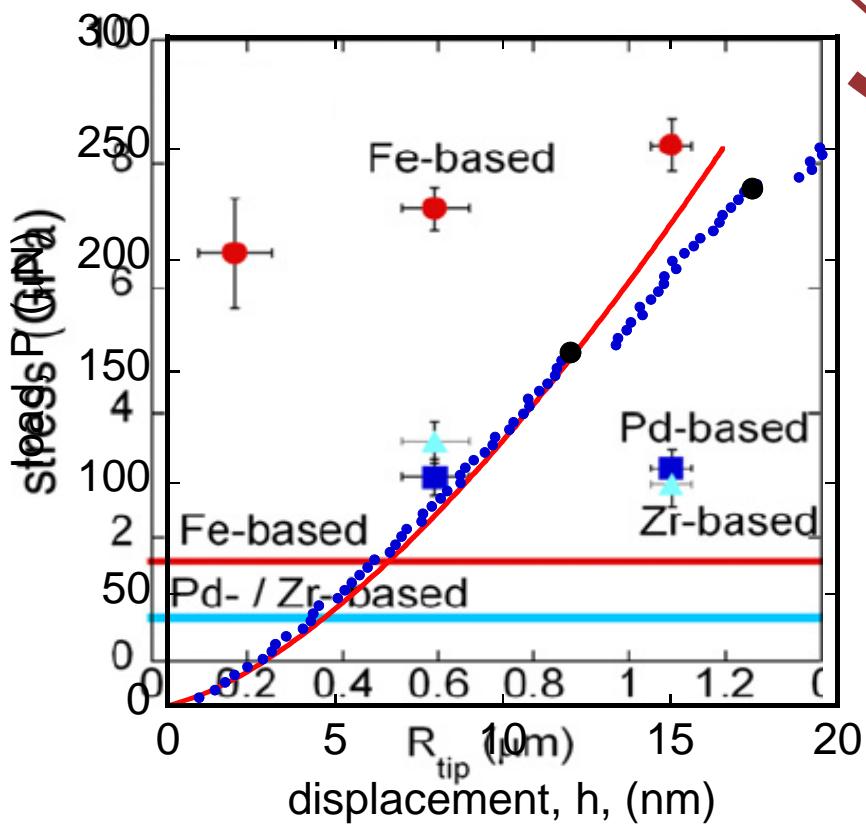
# Nanoindentation measurements



Images from Trelewicz, Packard (MIT)  
as well as Chiu and Ngan, Acta Mater, 2002

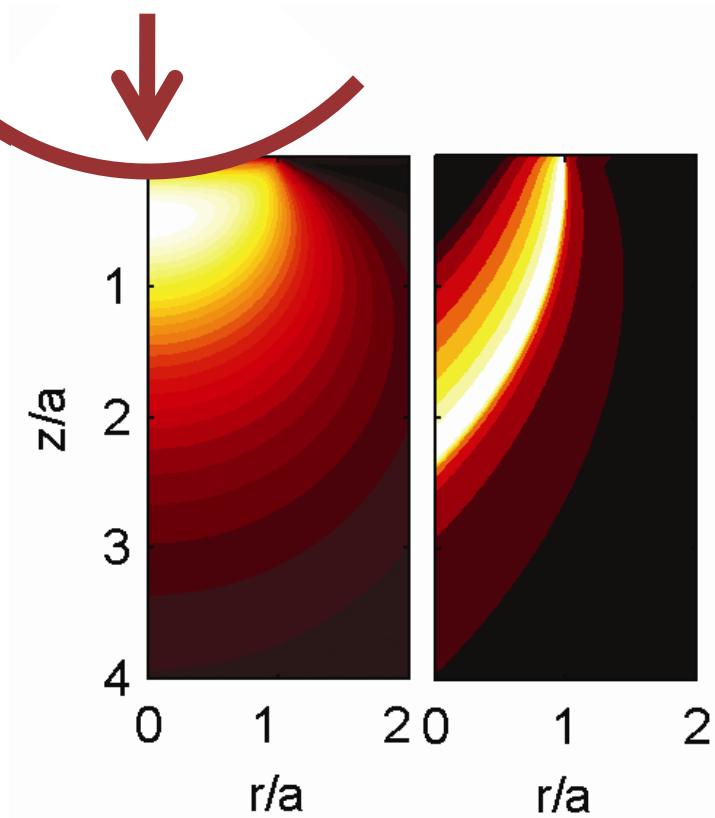
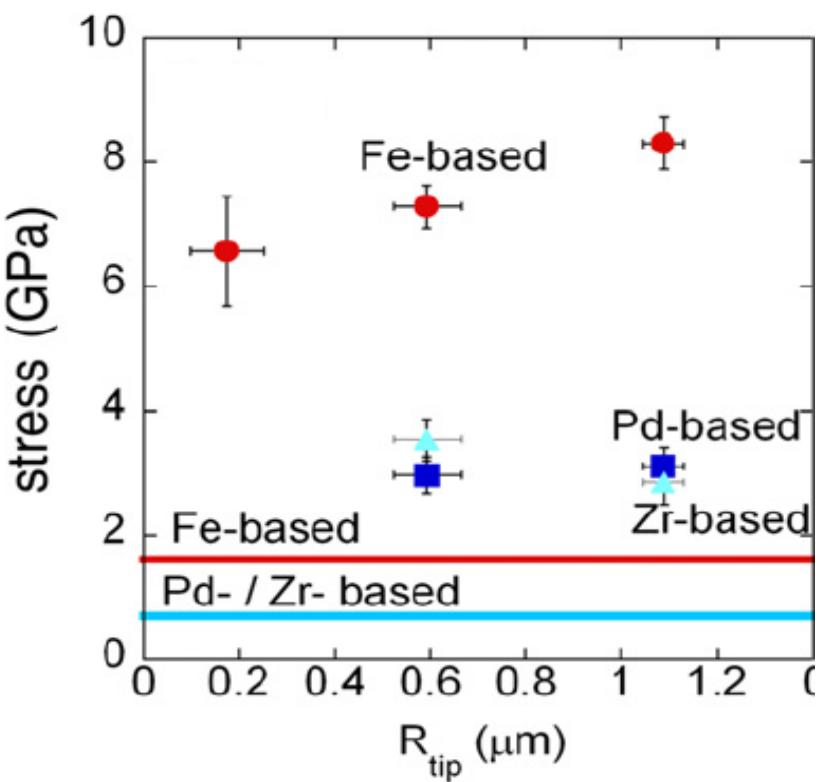
# Metallic glass: yield avoids $\tau_{\max}$

$$\tau_{\max} = \frac{0.47}{\pi} \cdot \left( \frac{4E_R}{3R_{tip}} \right)^{2/3} P^{1/3}$$



Adapted from L. Anand  
J.Mech.Phys.Solids 2005

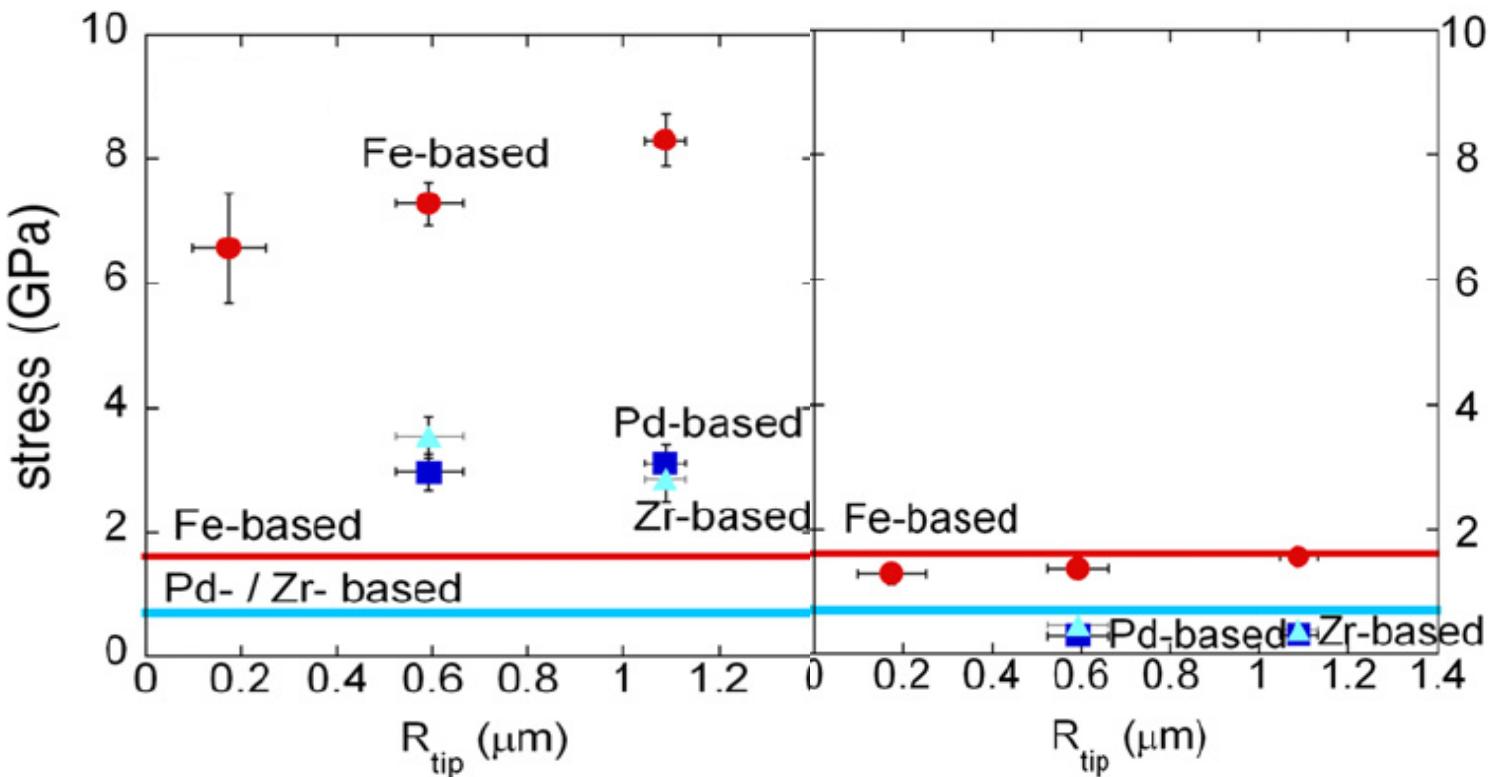
# Metallic glass: yield avoids $\tau_{\max}$



# Metallic glass: yield avoids $\tau_{\max}$

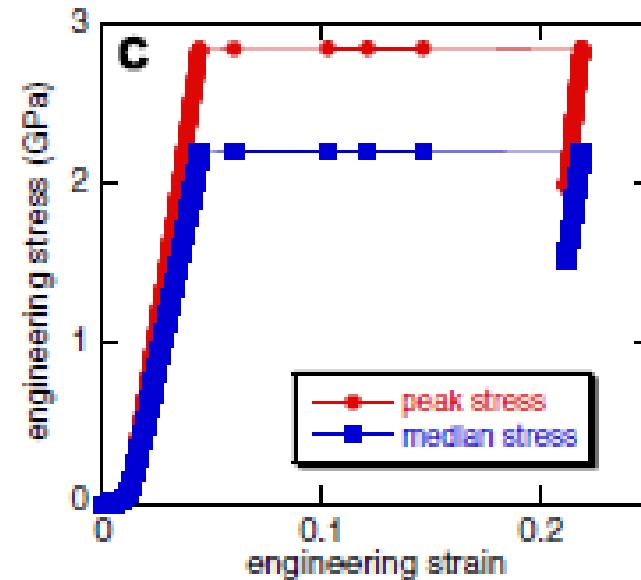
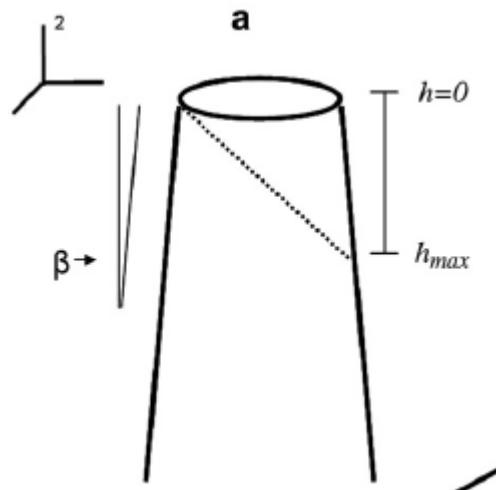
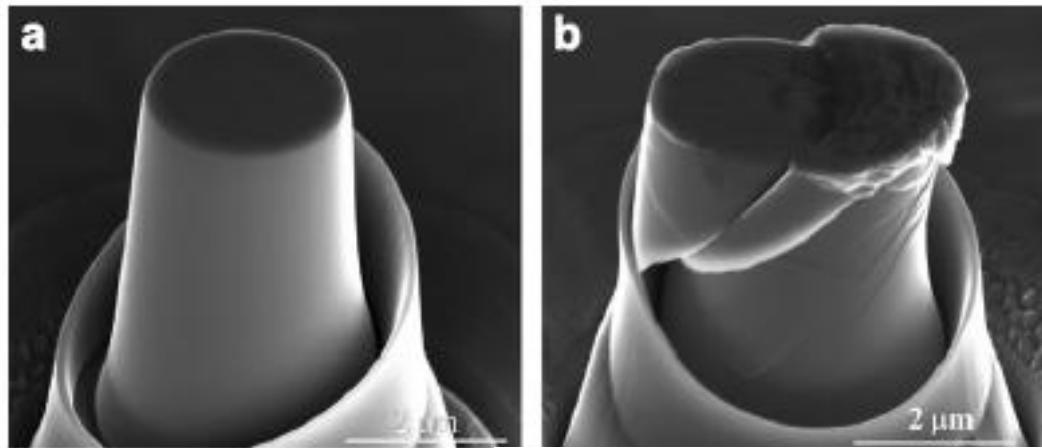
Packard and Schuh

Acta mater. 2007, v55 p5348



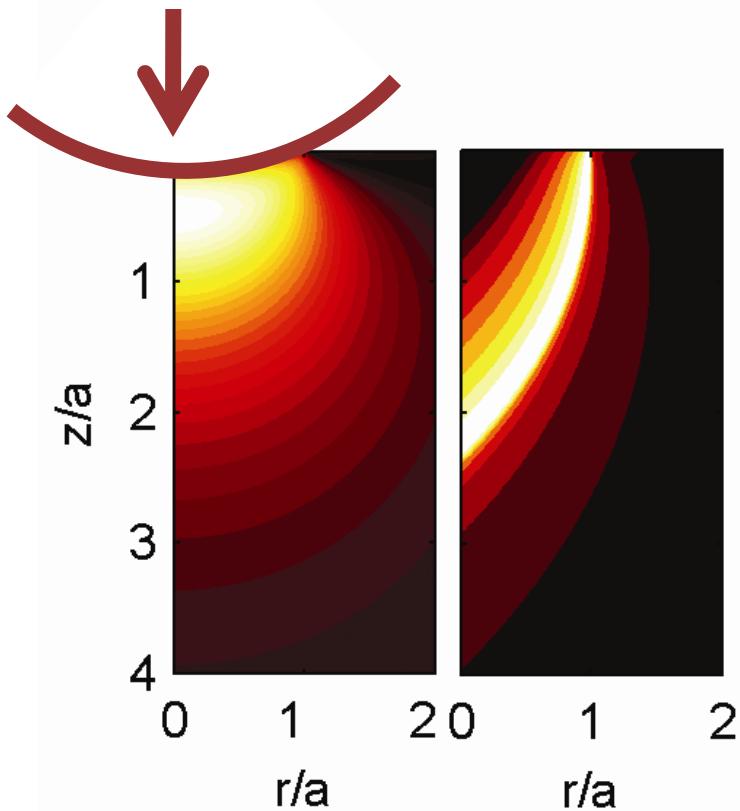
# Tapered microcompression

Schuster et al., Acta Mater (2008) v56, 5091



# Metallic glass: yield avoids $\tau_{\max}$

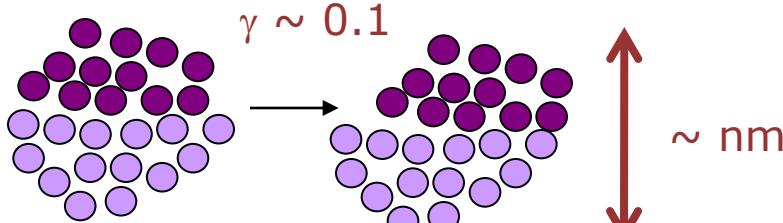
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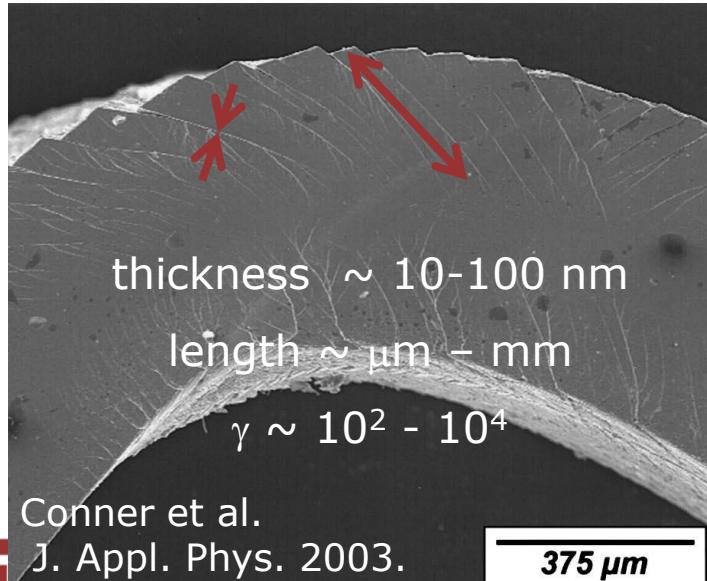
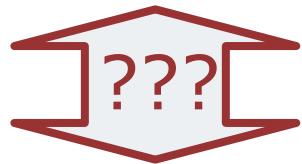
**Yield is controlled by the  
lowest stress point on the  
highest stress shear path!**

**What is the process of STZ assembly that governs the development of the shear plane in a complex stress field?**

# Puzzles: the gap between atomic motion and shear bands

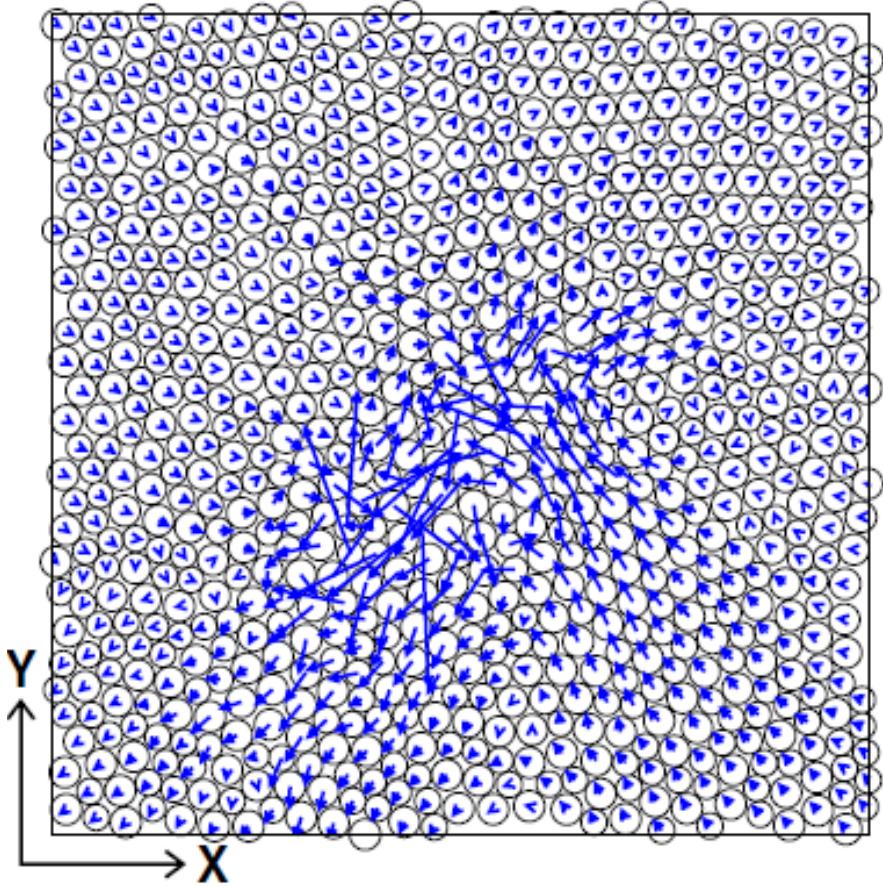
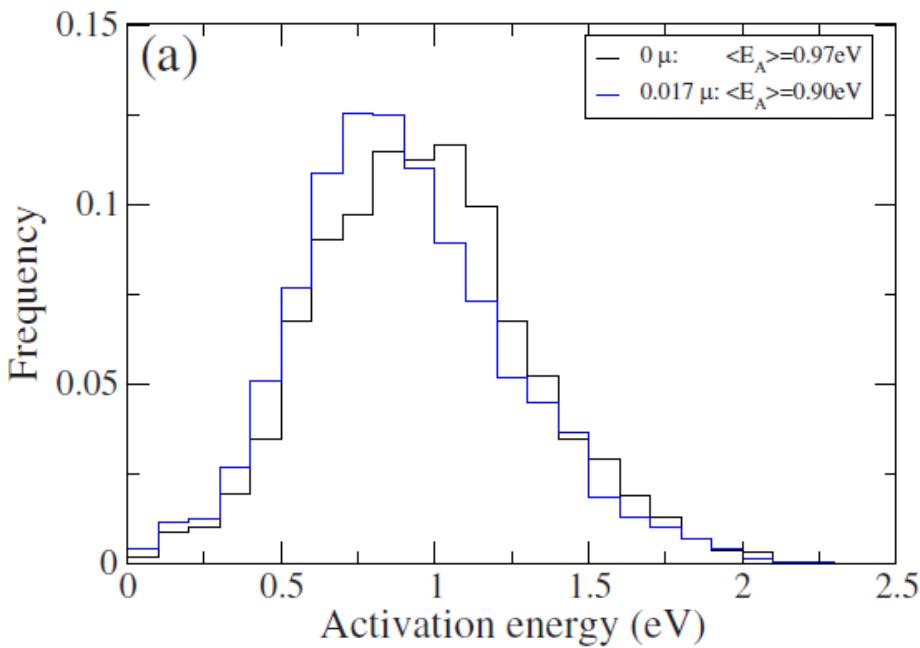


after Argon. Acta Metall. 1979.



- Kinetics
- Behavior in gradients of stress
- Event spectrum

# Event spectrum

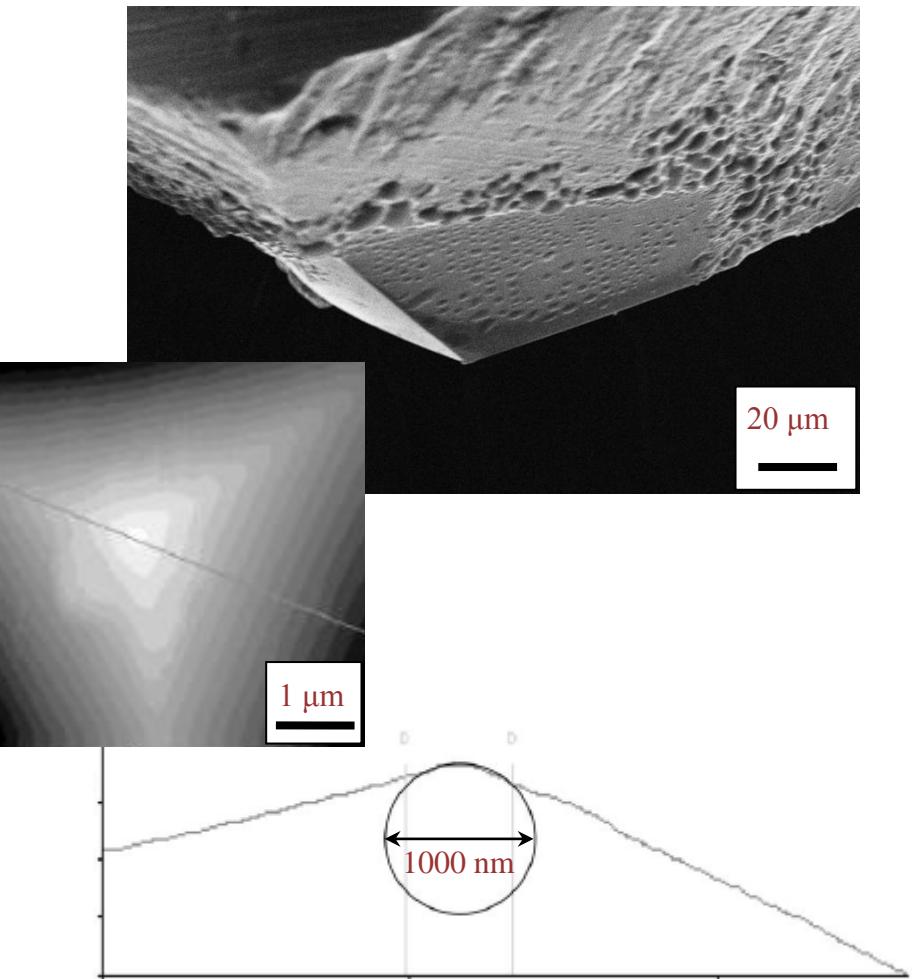
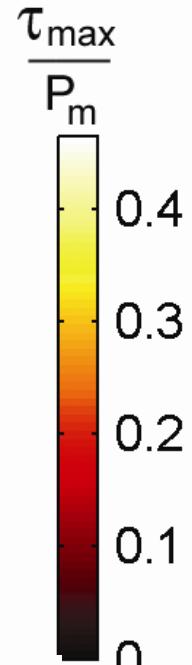
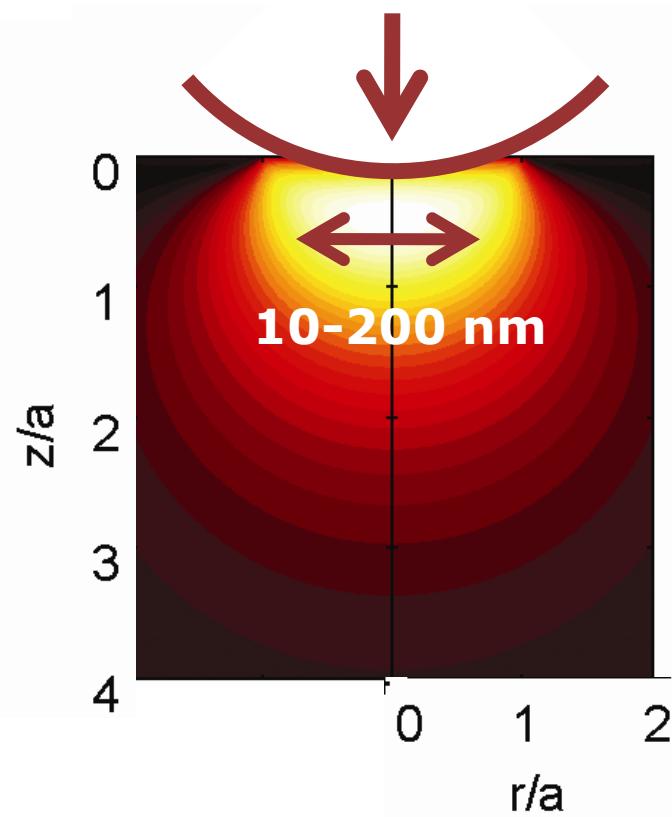


In 'jammed' configuration at  $T = 0 \text{ K}$

D. Rodney: PRL (2009) v102 235503

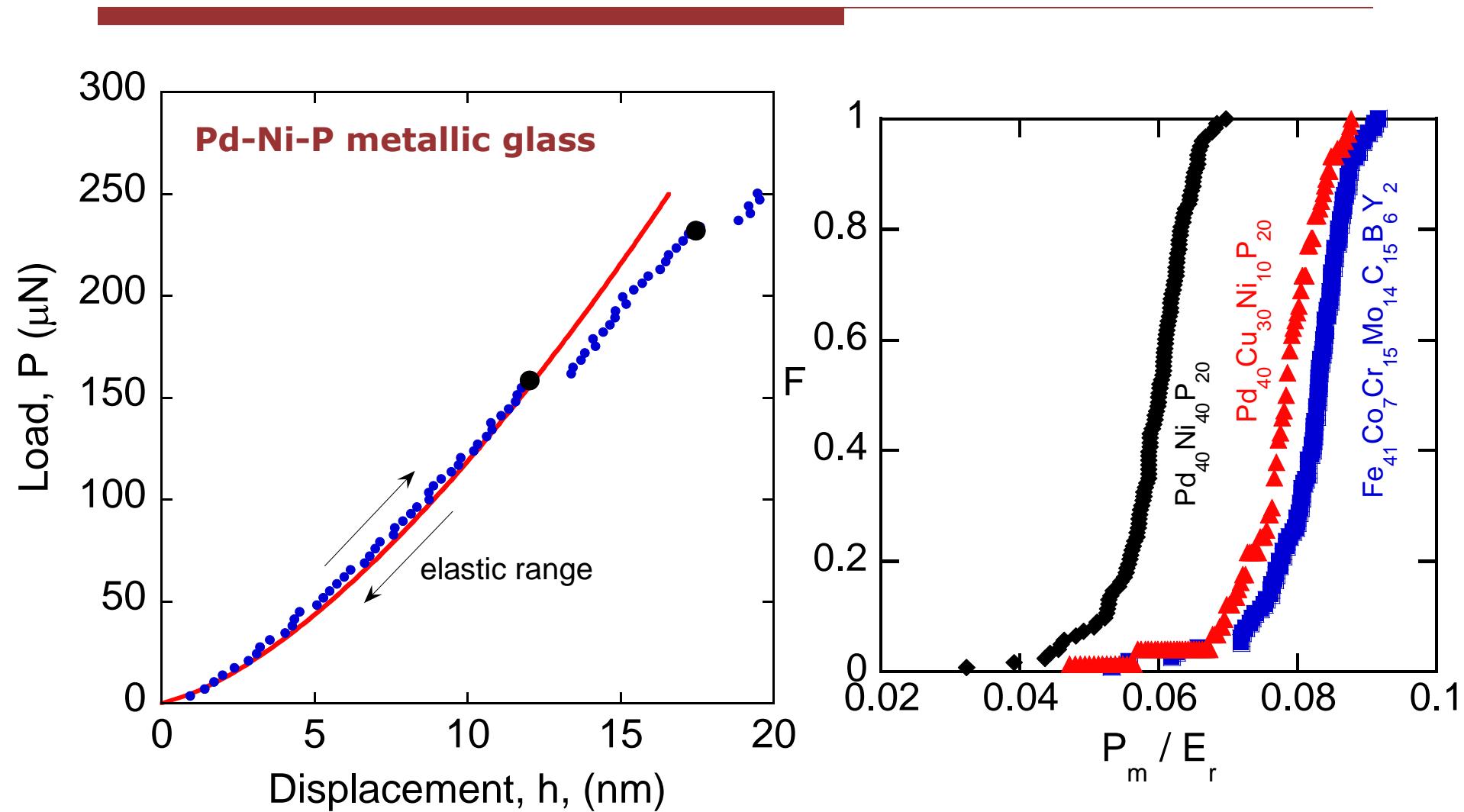
PRB (2009) v80 184203

# Nanoindentation measurements

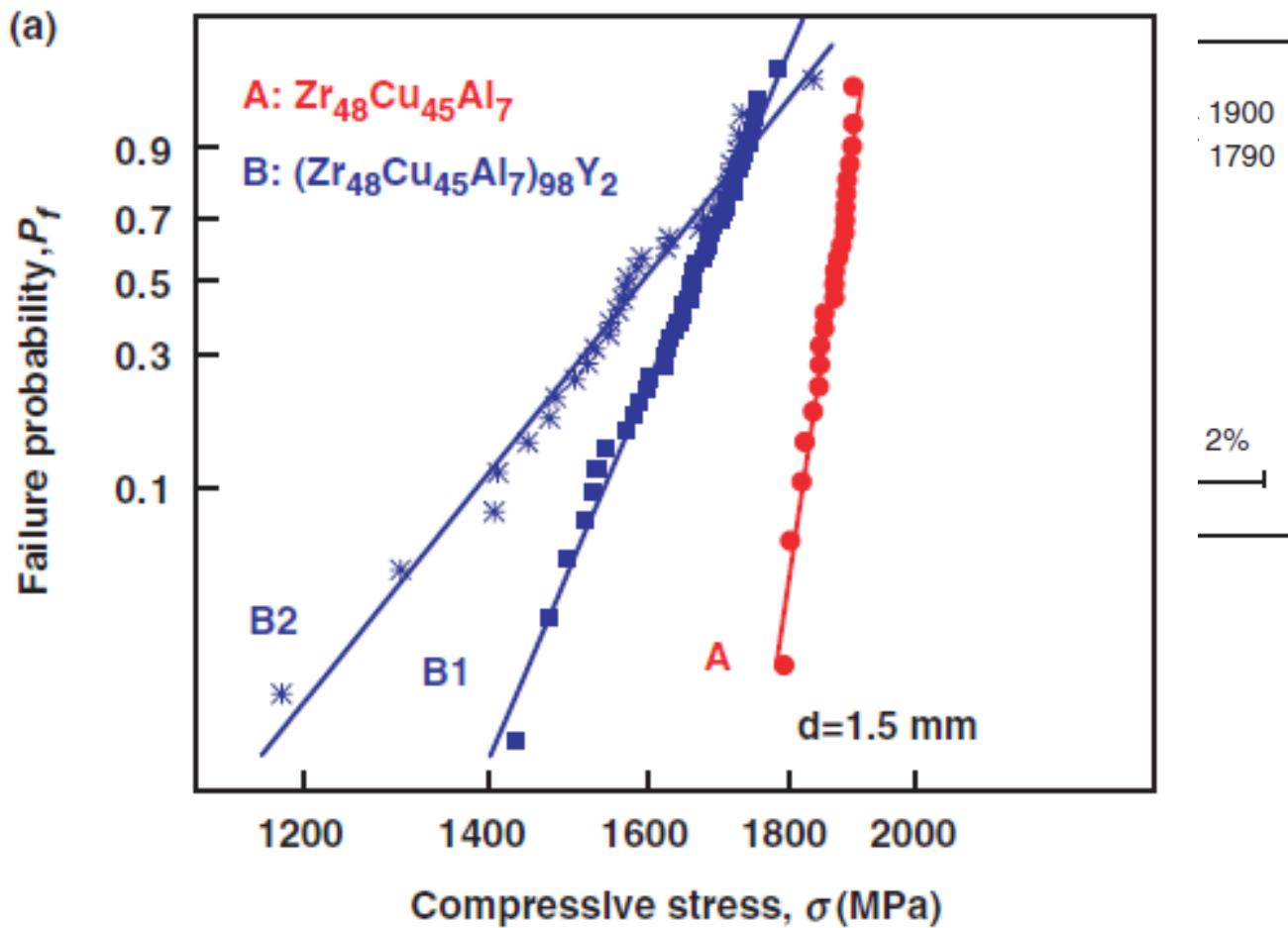


Images from Trelewicz, Packard (MIT)  
as well as Chiu and Ngan, Acta Mater, 2002

# Nanoindentation measurements



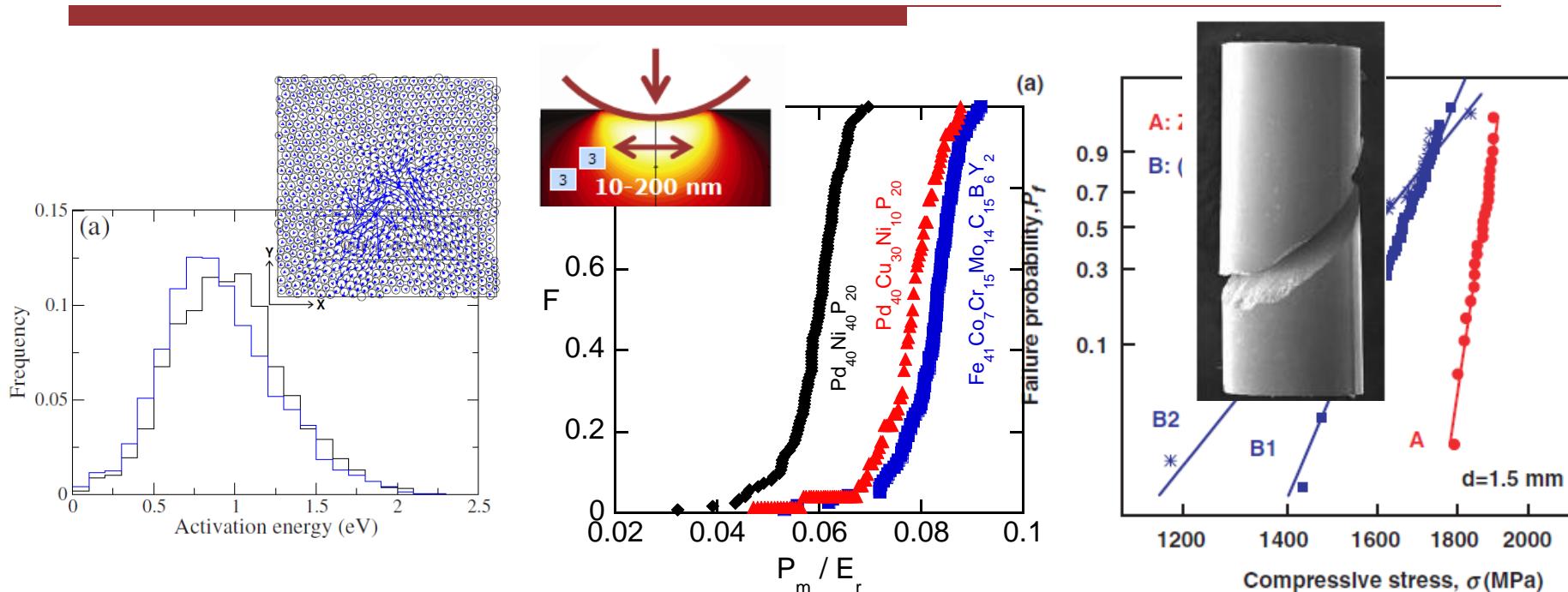
# Event spectrum



W.F. Wu, Y. Li, and C.A. Schuh

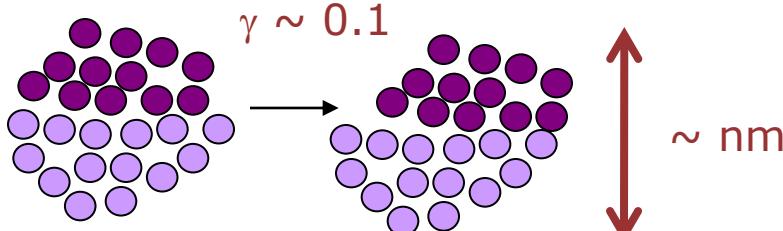
Phil Mag (2008) v88 p71

# Spectra at all scales

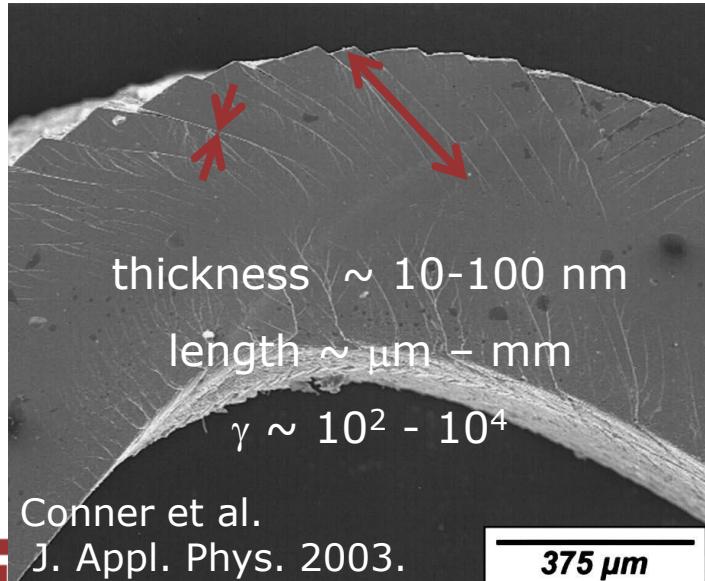
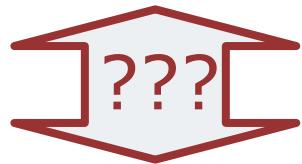


**What is the STZ assembly process that governs strength at larger scales?**

# Puzzles: the gap between atomic motion and shear bands



after Argon. Acta Metall. 1979.

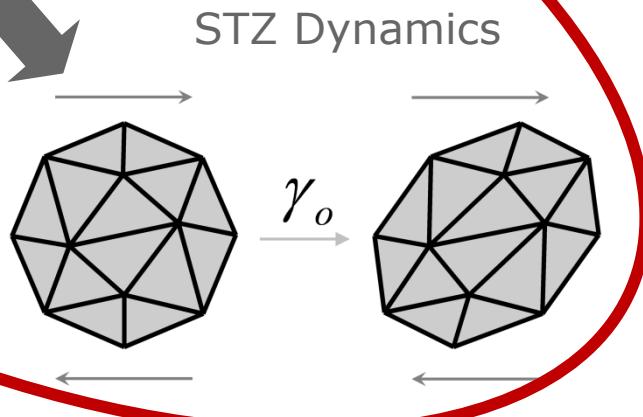
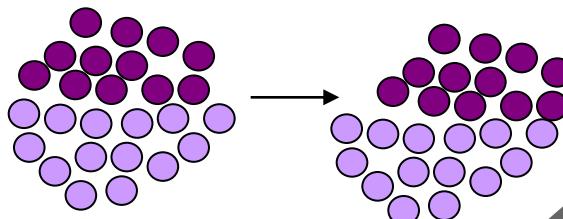
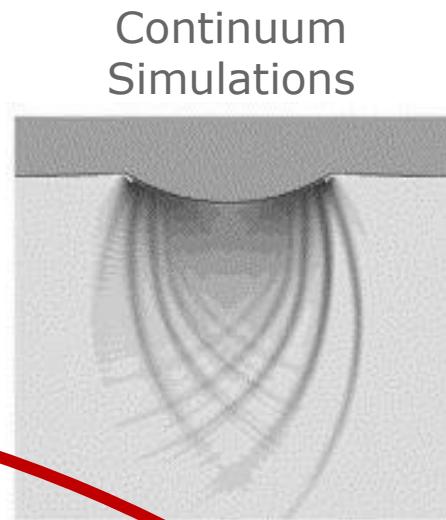
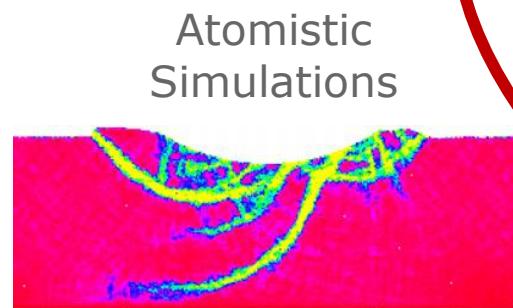


- Kinetics
- Behavior in gradients of stress
- Event spectrum

# STZ Dynamics

- Shear Transformation Zone (STZ)
  - Stochastic stress-biased thermally activated event

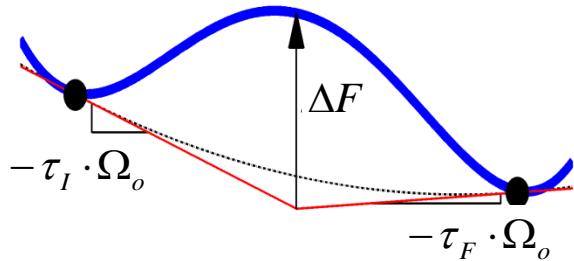
$$\dot{s} = v_o \exp\left(-\frac{\Delta F_o - \tau V^*}{k_B T}\right)$$



# Coarse-graining the shear transformation zone



## Potential Energy Landscape

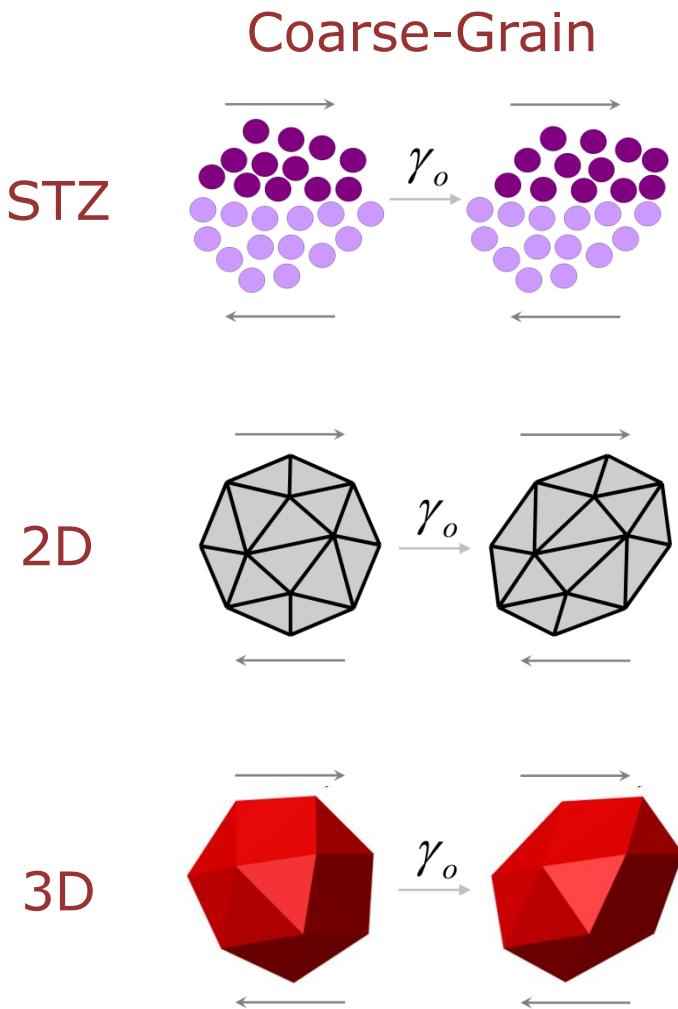


Bulatov, Argon. Model. Simul. Mater. Sci. Eng. 1994.

## Characteristic Attempt Frequency

$$\dot{s} = v_o \cdot \exp\left(-\frac{\Delta F - \frac{1}{2}\tau \cdot \gamma_o \cdot \Omega_o}{kT}\right)$$

# Key elements for a mesoscale model



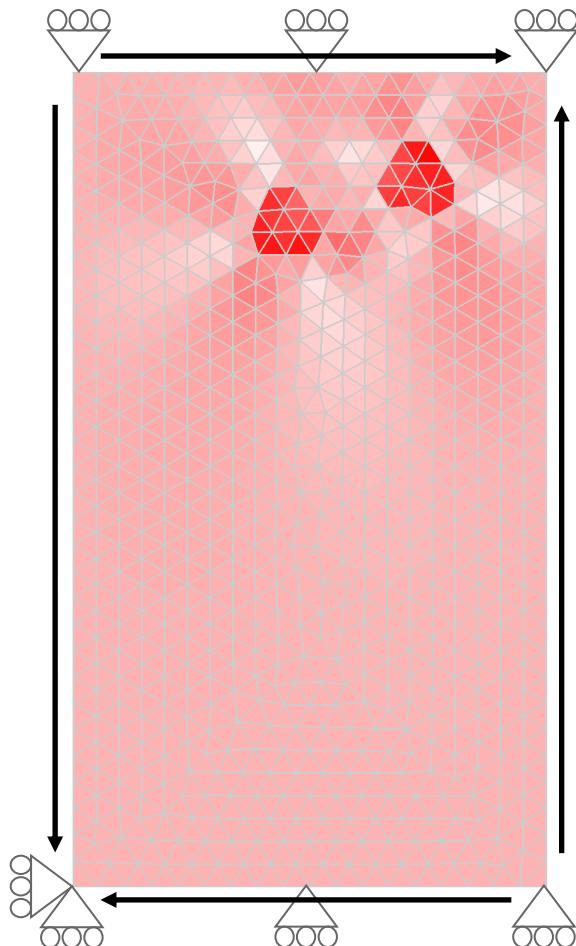
## STZ Activation Rate

$$\dot{s} = v_o \cdot \exp\left(-\frac{\Delta F - \frac{1}{2}\tau \cdot \gamma_o \cdot \Omega_o}{kT}\right)$$

$$\dot{s} = v_o \cdot \exp\left(-\frac{\Delta F}{kT}\right) I_o\left(\frac{\tau_{\max} \cdot \gamma_o \cdot \Omega_o}{2kT}\right)$$

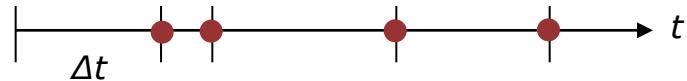
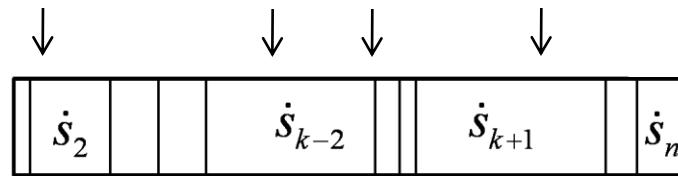
$$\dot{s} = v_o \cdot \exp\left(-\frac{\Delta F}{kT}\right) \iiint_{g \in G} \exp\left(-\frac{\tau(\sigma, g) \cdot \gamma_o \cdot \Omega_o}{2kT}\right) dg$$

# KMC plus FEM



## Kinetic Monte Carlo

$$\dot{s} = v_o \cdot \exp\left(-\frac{\Delta F}{kT}\right) I_o \left( \frac{\tau_{\max} \cdot \gamma_o \cdot \Omega_o}{2kT} \right)$$

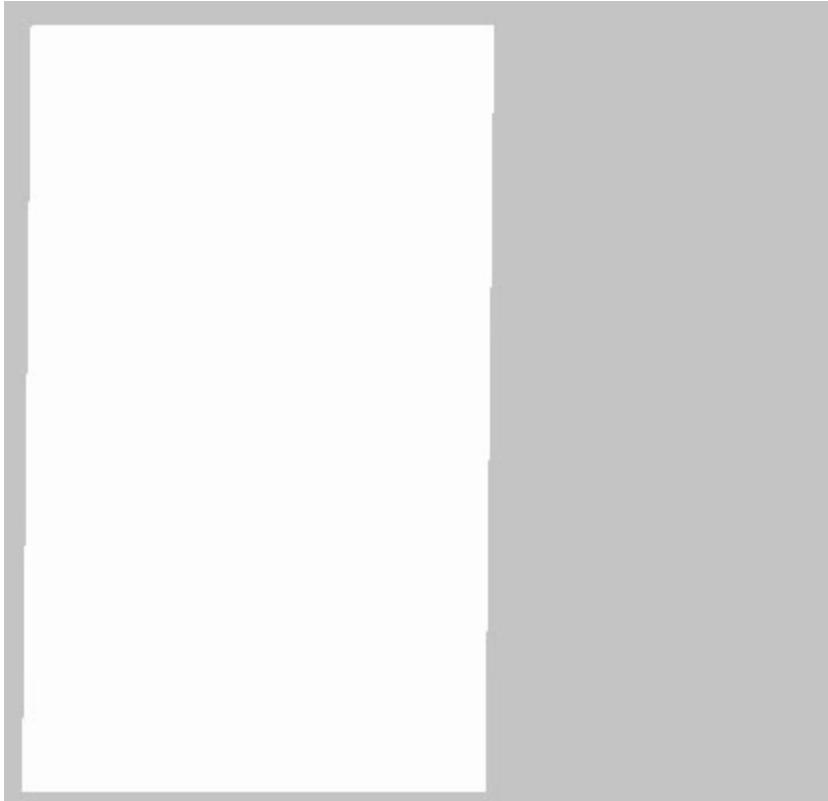


 **ABAQUS**

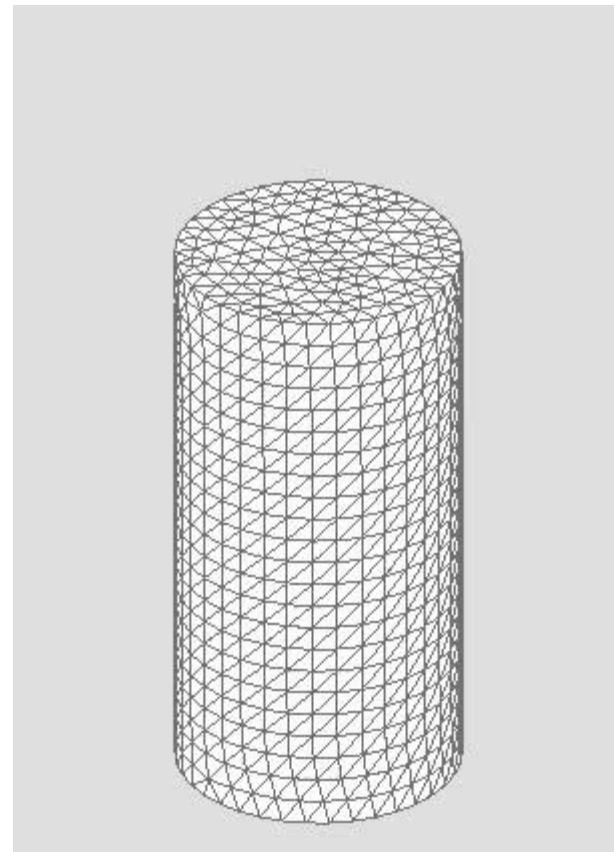
# High temperature

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**2D**



**3D**

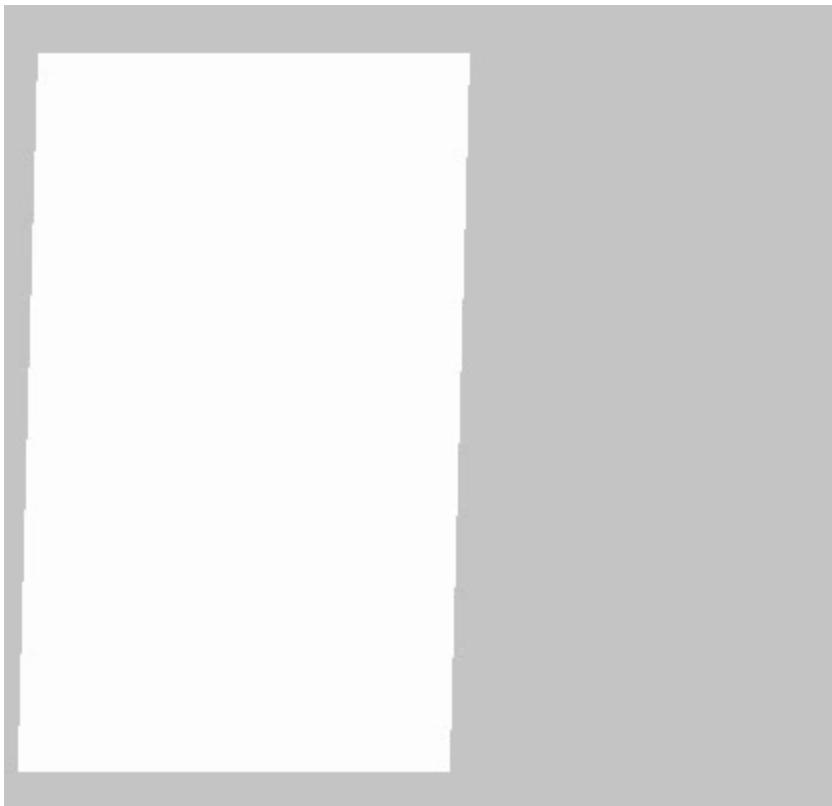


Homer, Schuh. Acta Mat. 2009.

# Low temperature

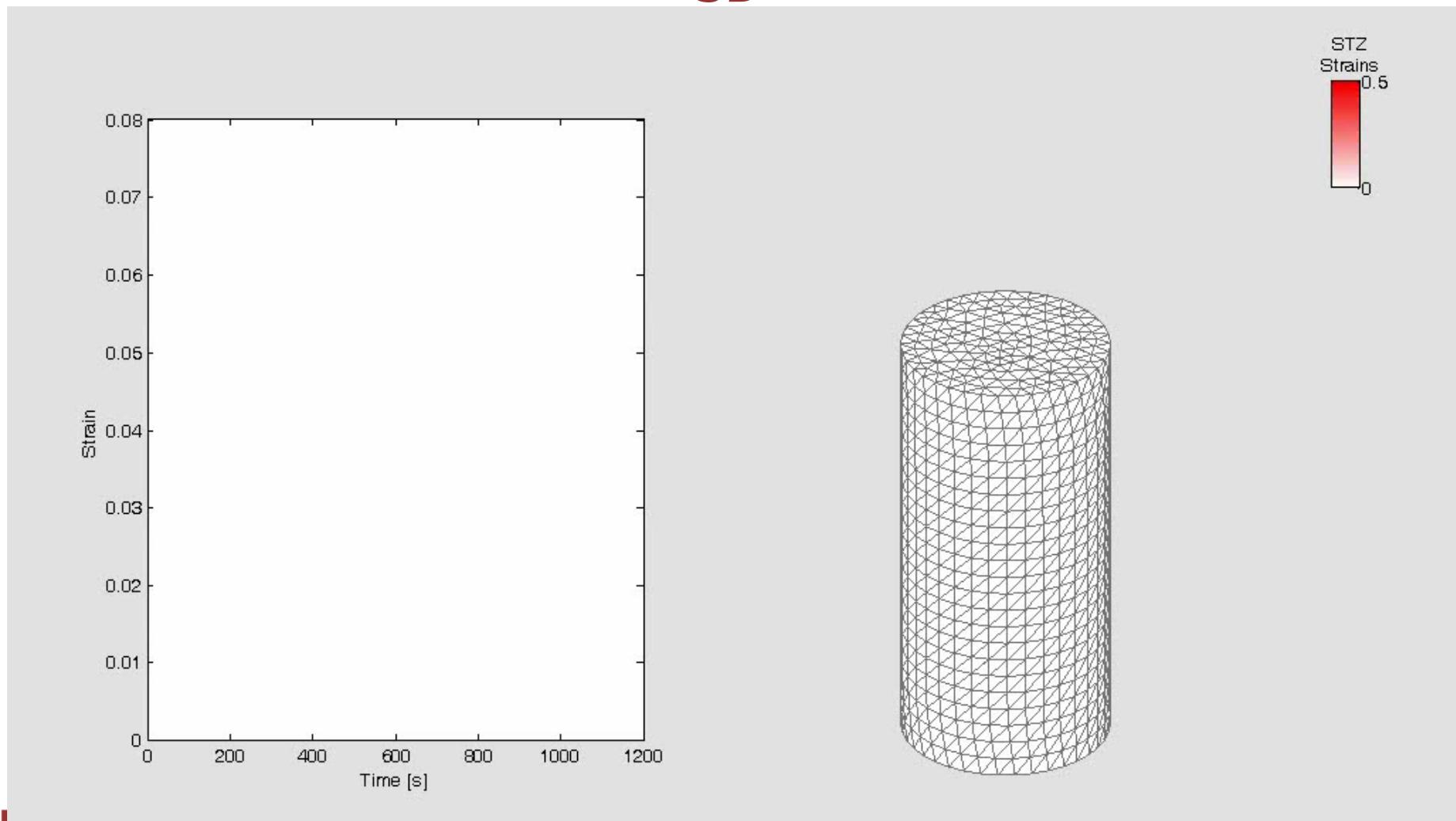
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**2D**

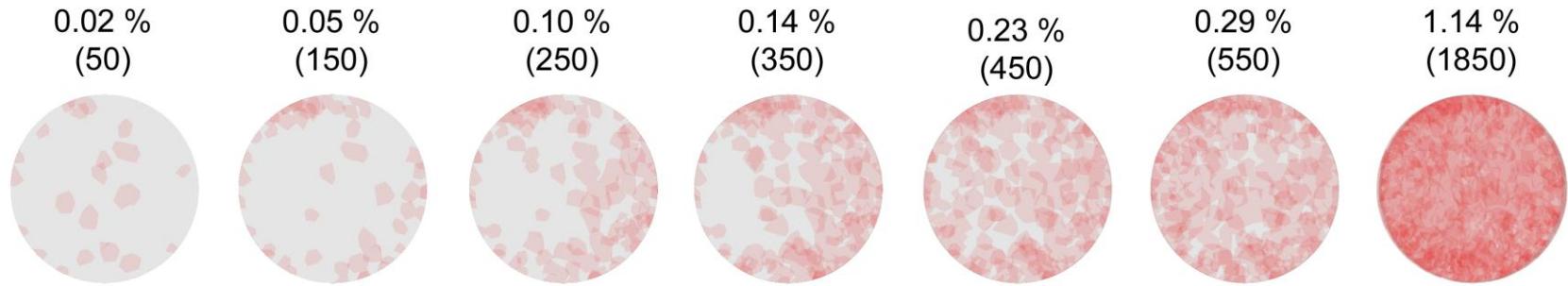


# Low temperature

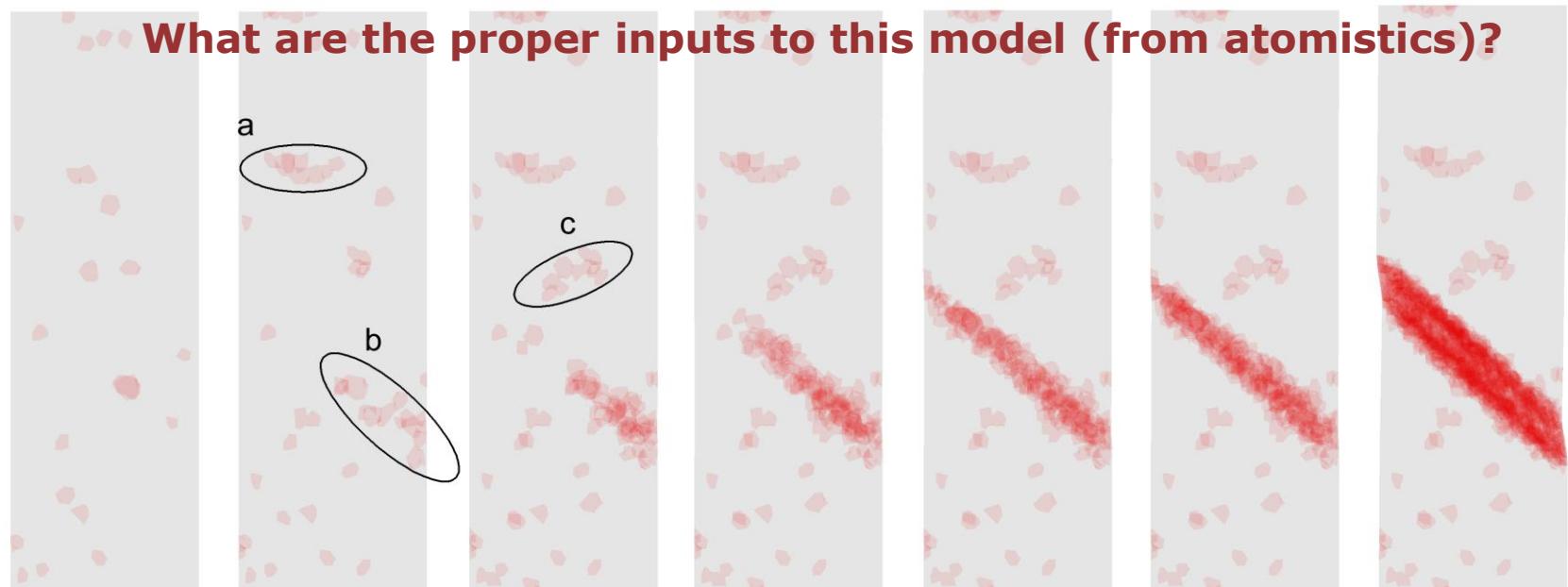
3D



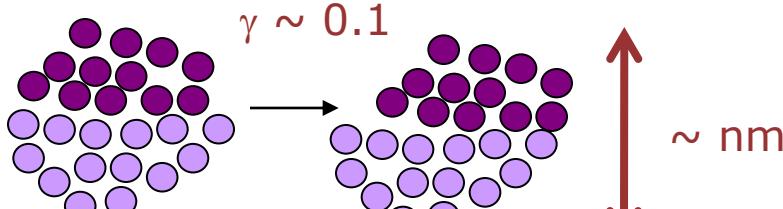
# Shear band formation



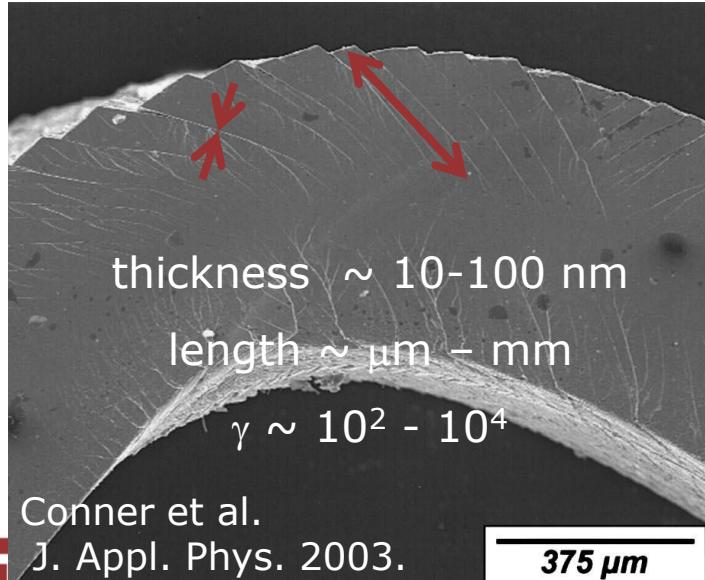
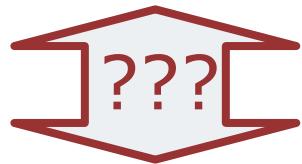
What are the proper inputs to this model (from atomistics)?



# Puzzles: the gap between atomic motion and shear bands



after Argon. Acta Metall. 1979.



- Kinetics
- Behavior in gradients of stress
- Event spectrum