



# **Probing Electronic Interactions in Graphene by Optical Spectroscopy**

**Tony F. Heinz**  
**Columbia University. New York, NY**

**KITP Meeting**

# Topics

- 1. Electron-electron interactions in single-layer graphene**
- 2. Interlayer stacking effects in few-layer graphene**

**ABA and ABC stacking**

# Thanks to

**Fai Mak**

**Joshua Lui**

**Zhiqiang Li**

**Prof. Jie Shan**

**(Case Western Reserve U.)**

**Steve Louie (UC Berkeley)**

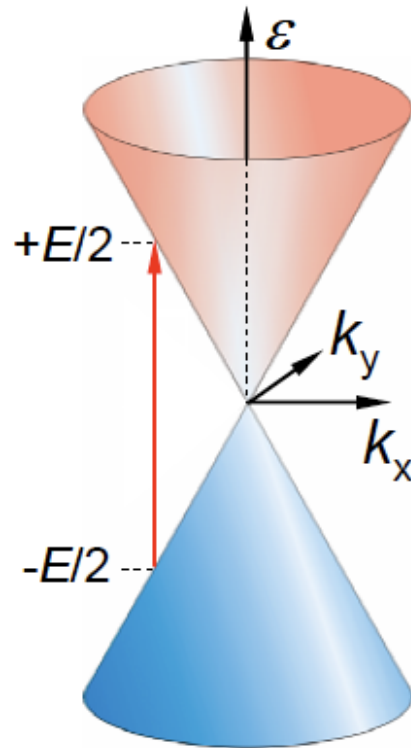
**Theory: e-e interactions in SLG**

**Emmanuele Cappelluti**

**(Inst de Ciencia de Materiales, Madrid, Spain)**

**Theory: interlayer interactions**

# Interband Transitions: Optical Conductivity



**Interband transitions for ideal linearly dispersing bands**

**Optical (sheet) conductivity:**

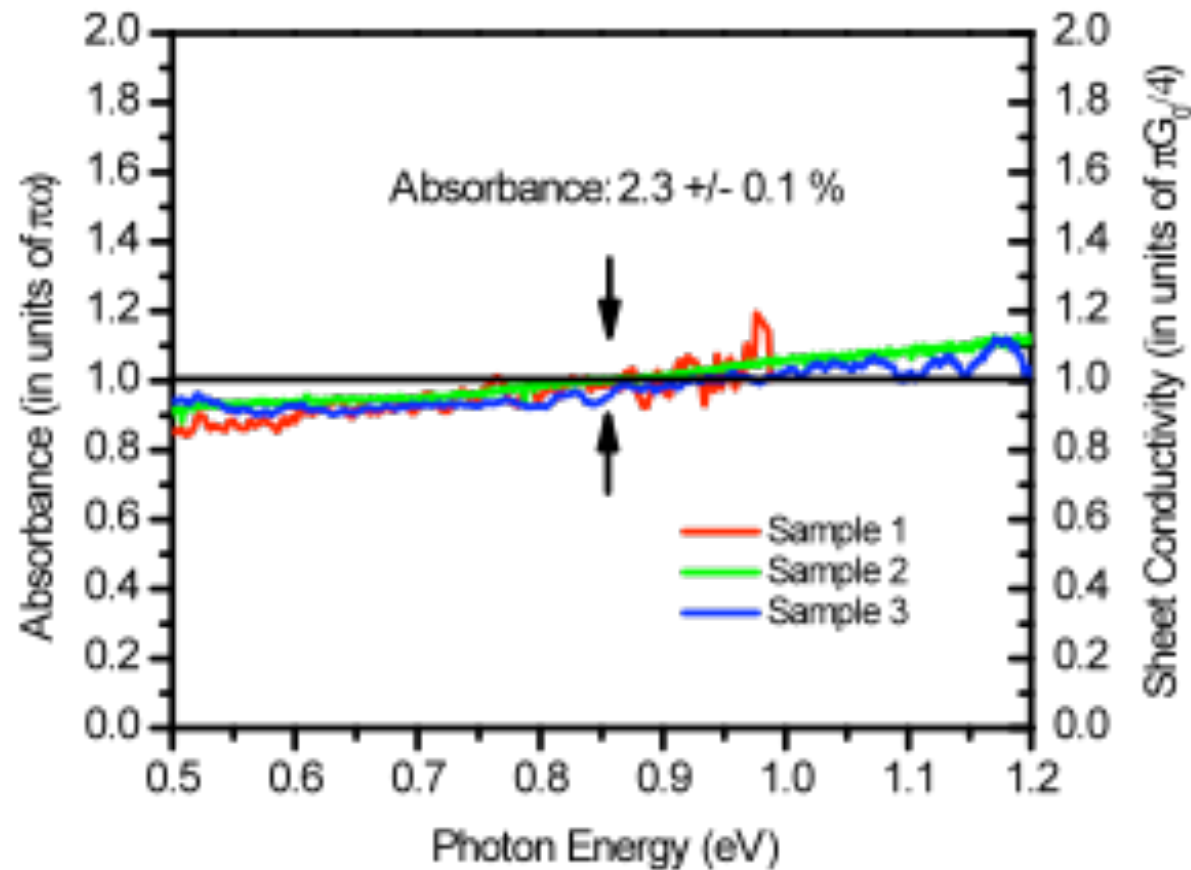
$$\sigma^{(1)}(\omega) = \frac{\pi e^2}{2h} = (\pi/4) G_0$$

**Optical absorption:**

$$A(\omega) = \frac{\pi e^2}{\hbar c} = \pi\alpha = \frac{\pi}{137} = 2.3\%$$

Ando et al. J Phys. Soc. Jpn 71, 1310 (2002)  
Gusynin et al., PRL 96, 256802 (2006)  
Ryu et al., PRB 75, 205344 (2007)  
Abergel et al., PRB 75, 155430 (2007)

# Graphene Optical Absorption/Conductivity



*Universal behavior*

Also Manchester group  
[Science 320, 5881 (2008)]

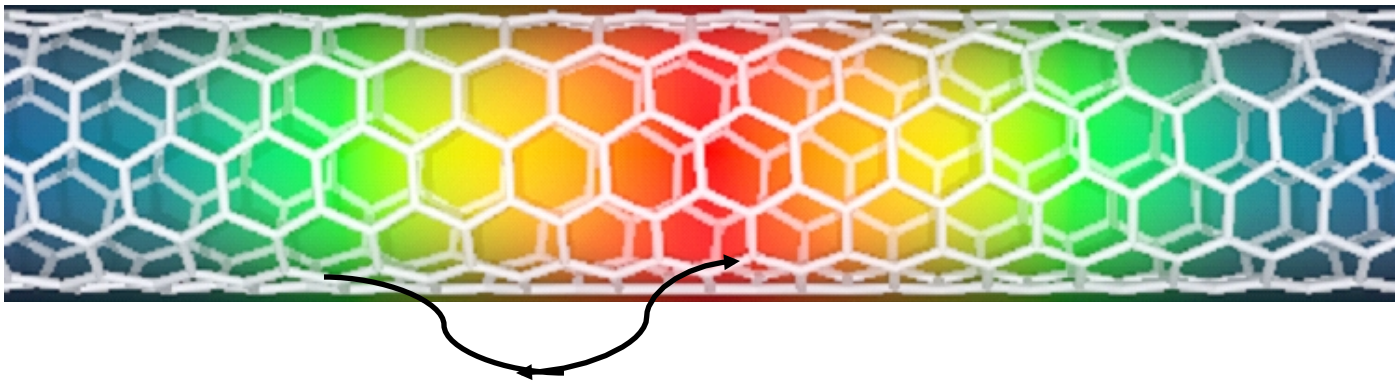
[Columbia grp, PRL 101, 196405 (2008)]

# Role of Many-Body Effects

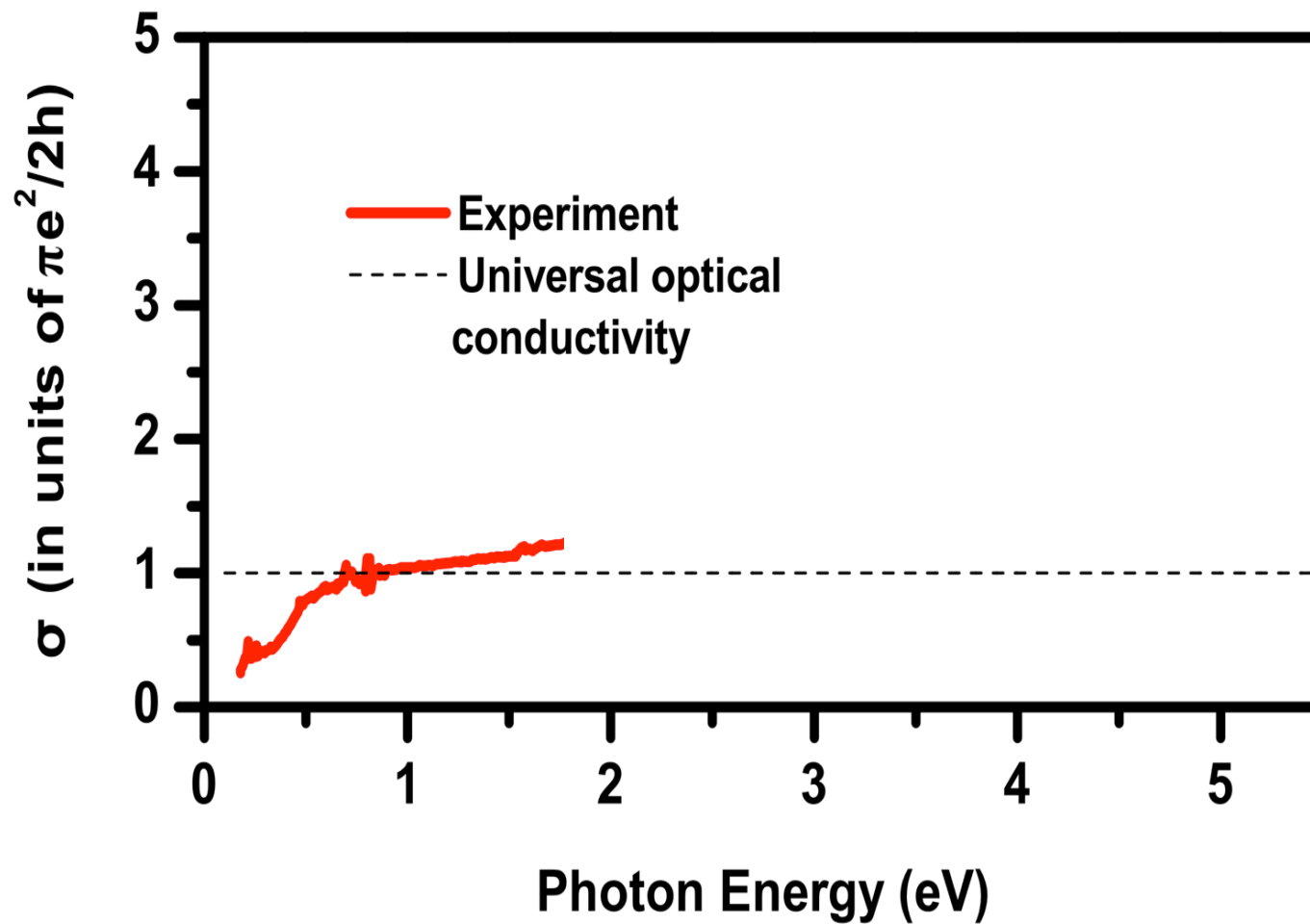
*All optical processes involve electron and hole:  
Exciton formation?*

**Dominant in semiconducting carbon nanotube**

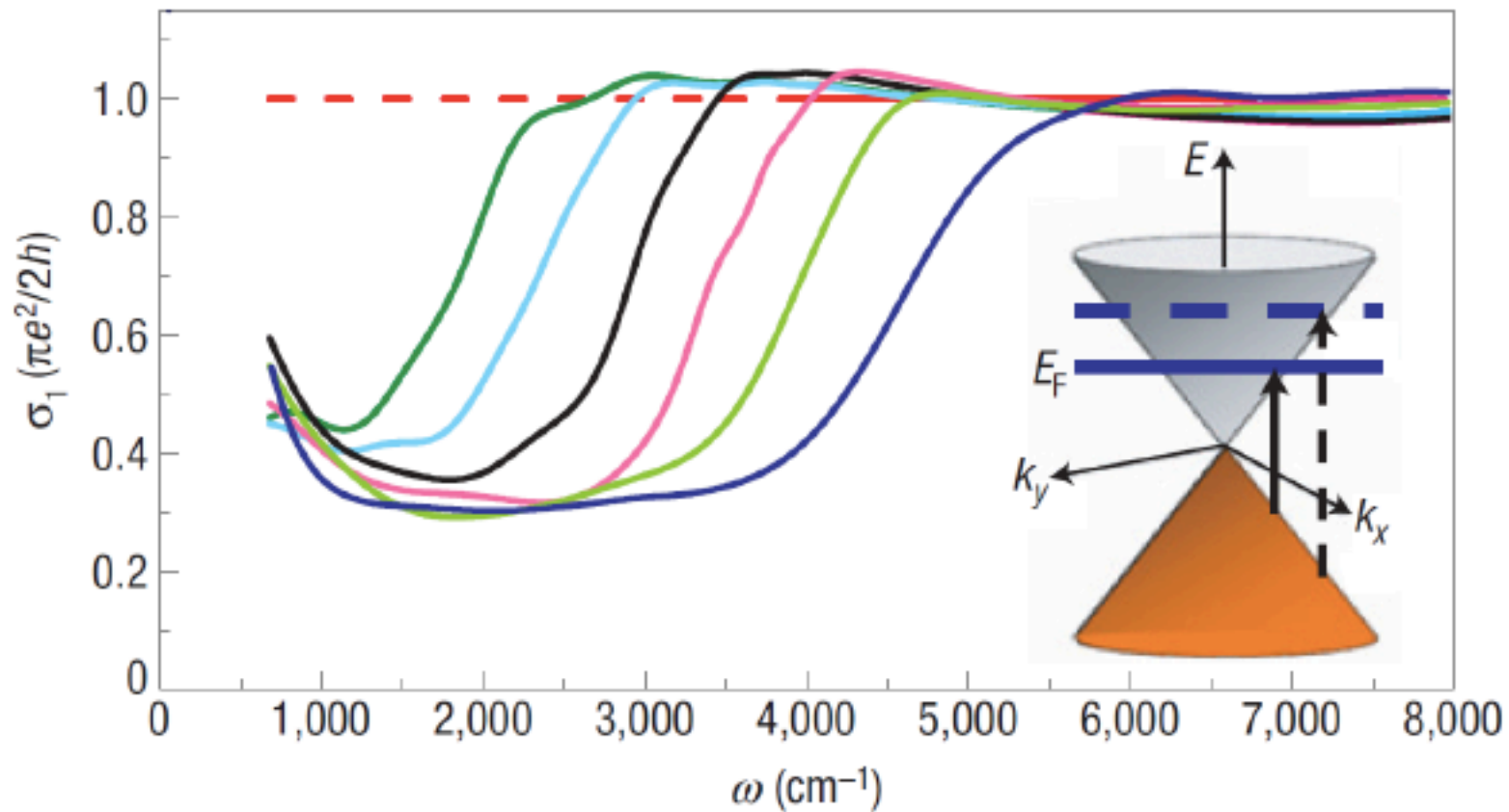
**Significant even in metallic nanotubes**



# Graphene Absorption Spectrum



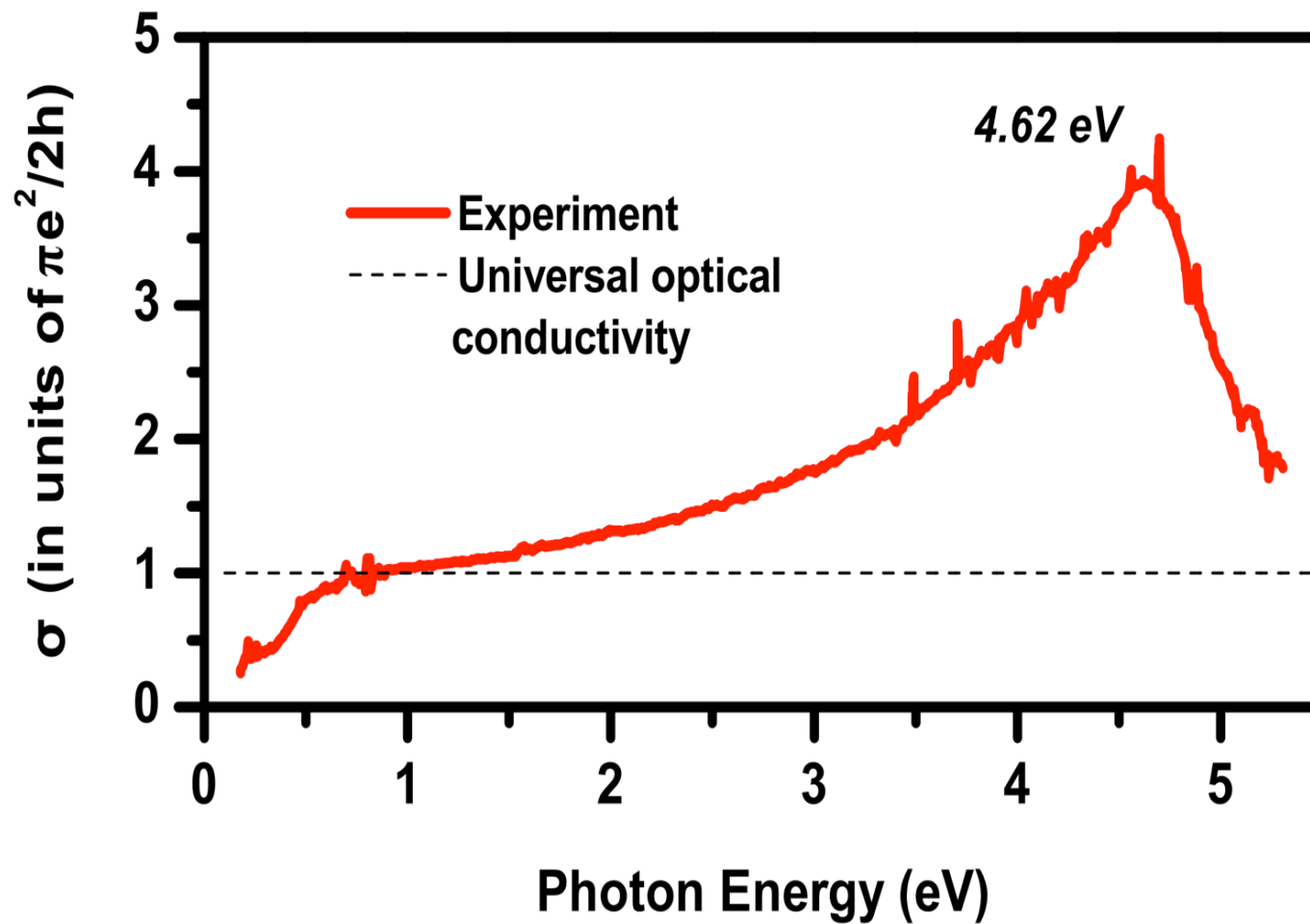
# Tunable Graphene Absorption by Electrostatic Gating



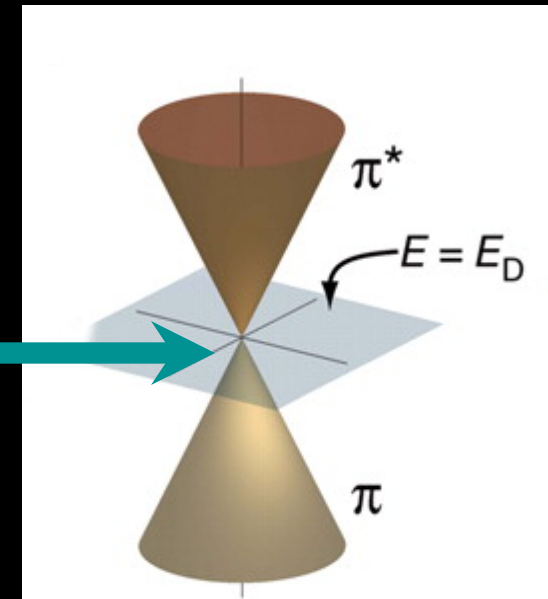
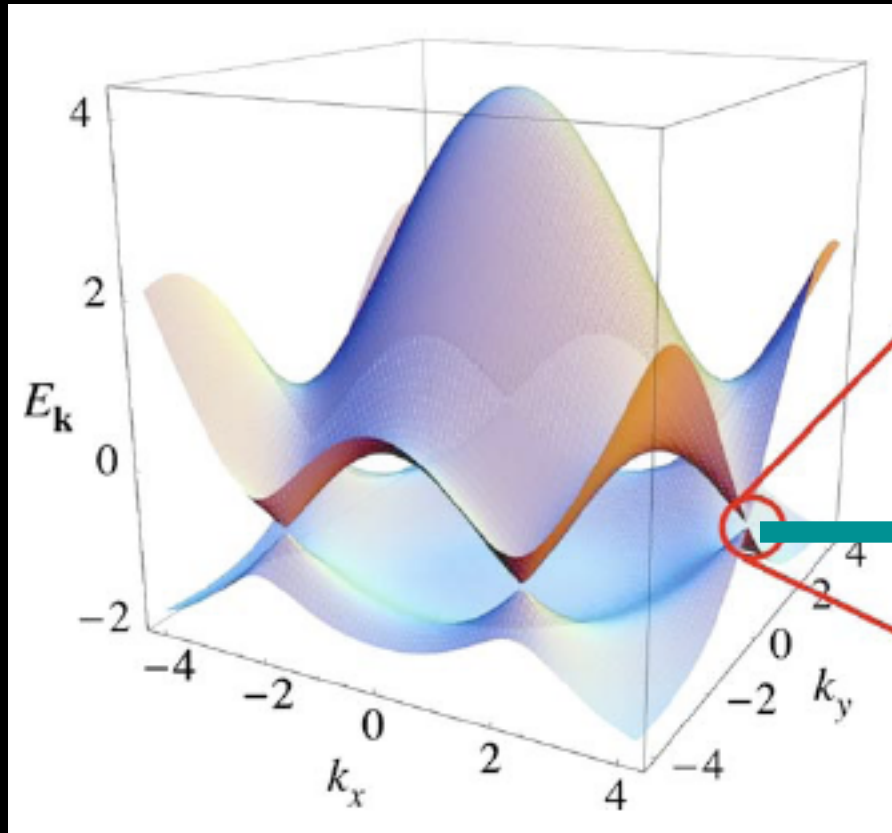
D. Basov et al., UC San Diego  
Also: Feng Wang, UC Berkeley

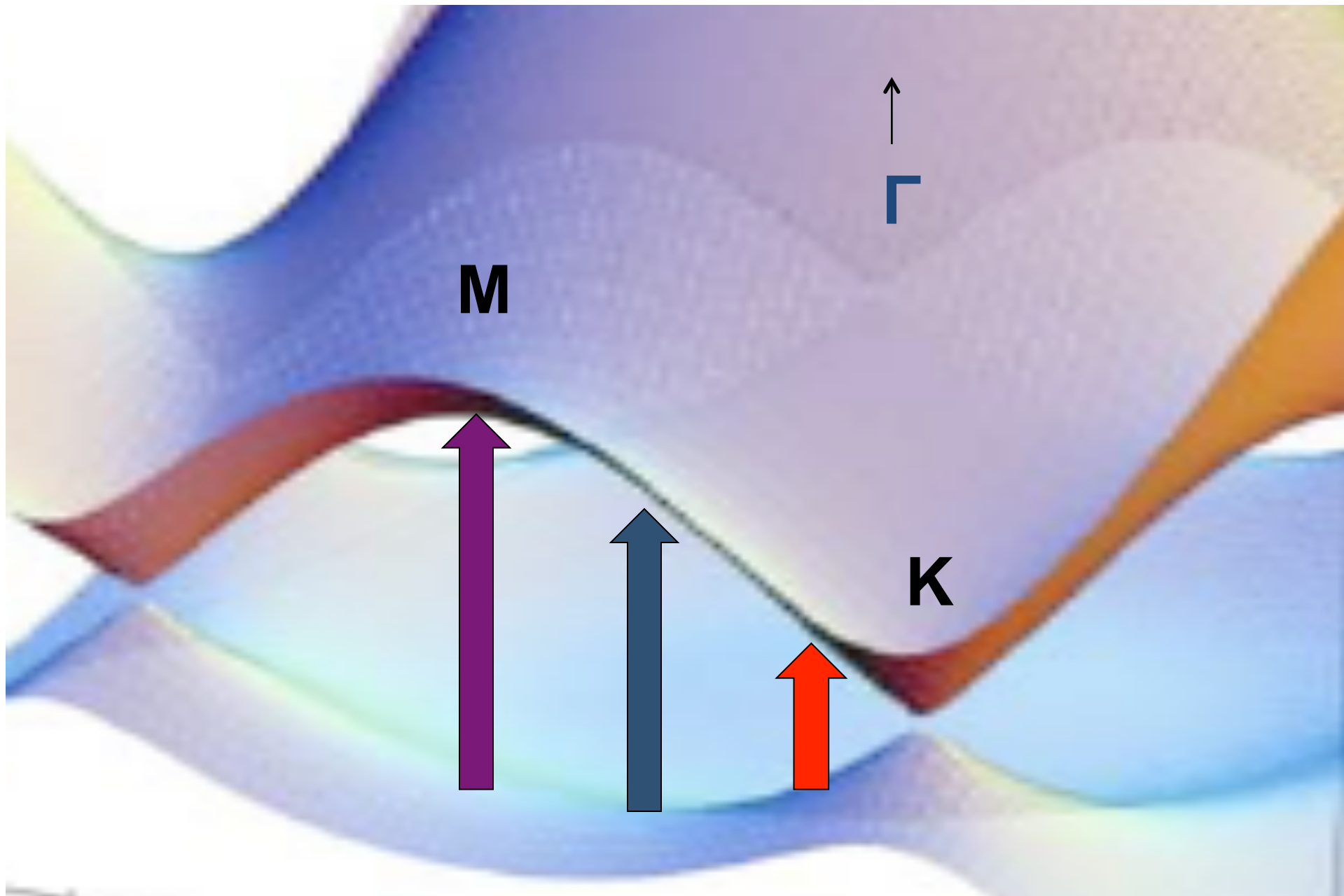


# Graphene Absorption Spectrum

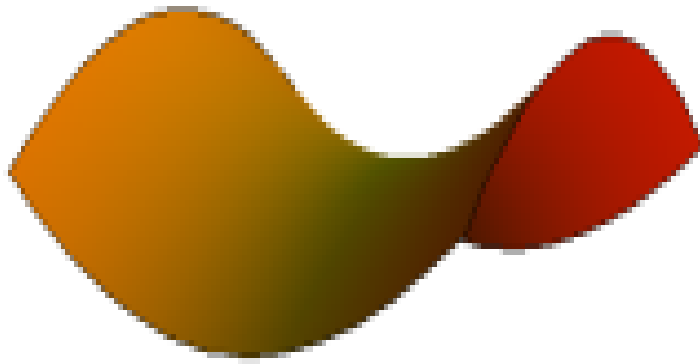


# Graphene Electronic Structure

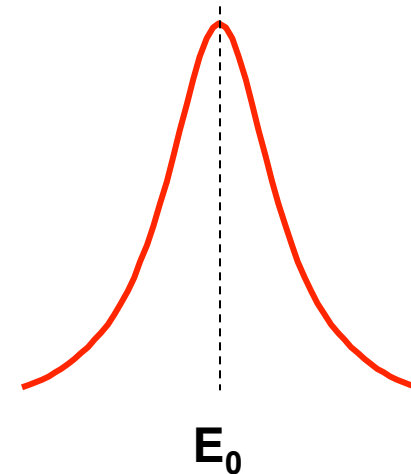




# Absorption at Saddle Point (no e-h interactions)

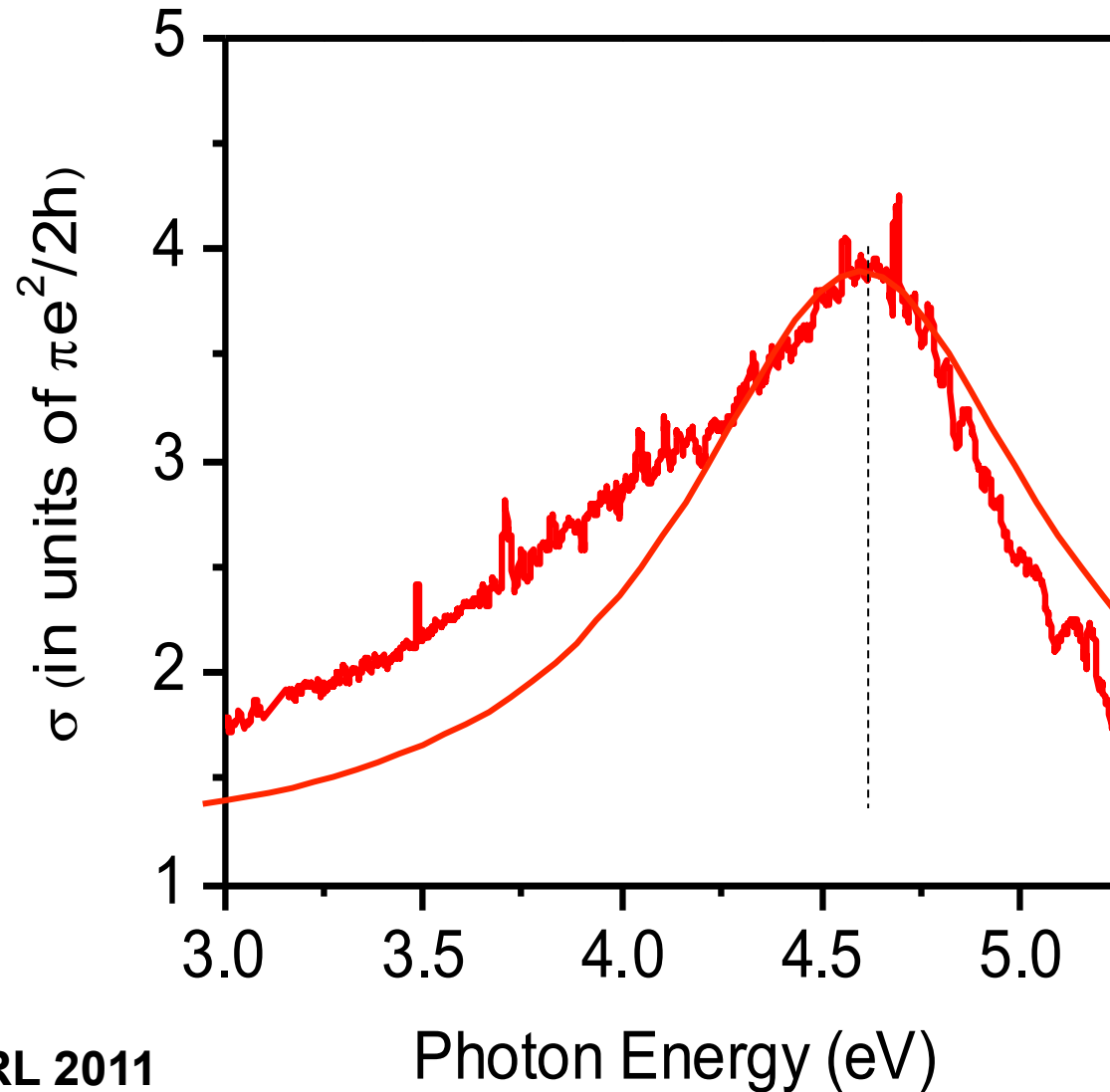


$$DOS_{SP}^{2D}(\omega) \propto -\ln \left| 1 - \frac{\omega}{E_0} \right|$$



Symmetric line shape  
near the saddle point

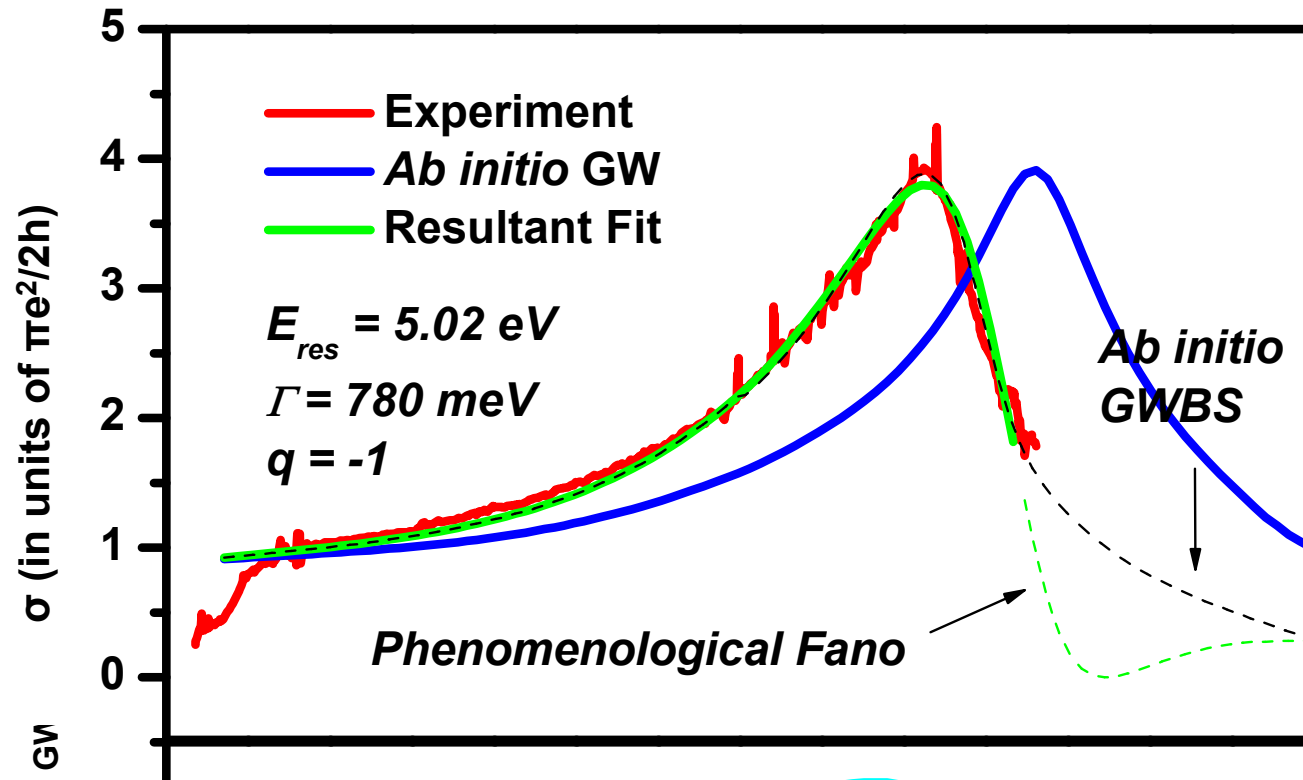
# Absorption Peak in Graphene



Heinz group, PRL 2011

Also Manchester, Stuttgart groups

# Excitonic Effects at the Saddle Point



Yang et al. PRL  
103, 186802 (2009)

Mak et al. PRL 106,  
046401 (2011)

Existence of strong e-h interactions

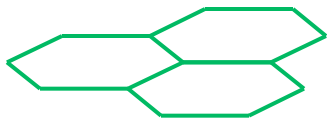
Quasiparticle lifetime near the M-point ~ **10 fs**

# Summary 1

## **SINGLE-LAYER GRAPHENE: e-e interactions**

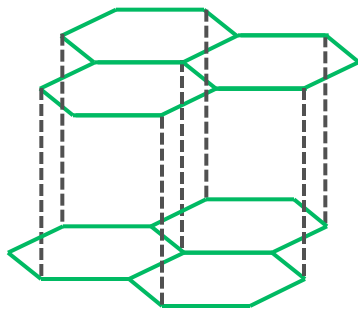
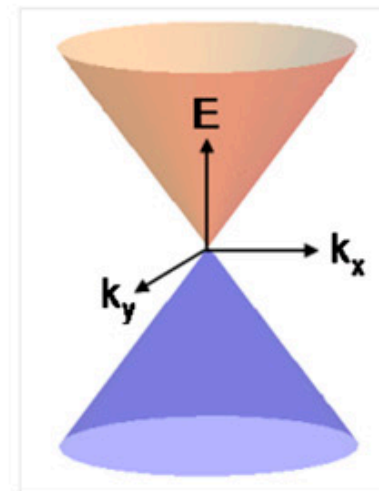
- Major increase in absorption above  $\pi\alpha$  for higher photon energies, rising to close to 10% at 4.6 eV
- Peak is associated with saddle-point at M-point in BZ.
- *Position and asymmetry lineshape require strong excitonic correlations:  
Saddle-point exciton -- discrete state embedded in continuum  
Fano absorption profile*

# Changing the Low-Energy Band Structure by Layer Stacking



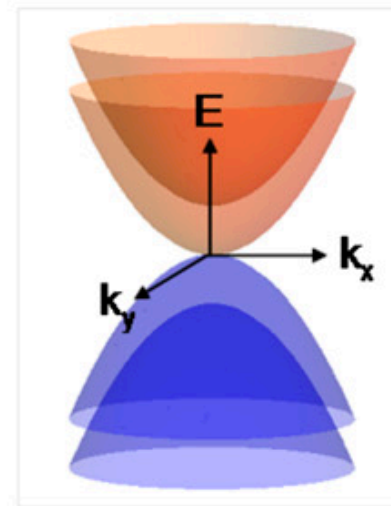
**Graphene Monolayer**

Chiral massless fermions



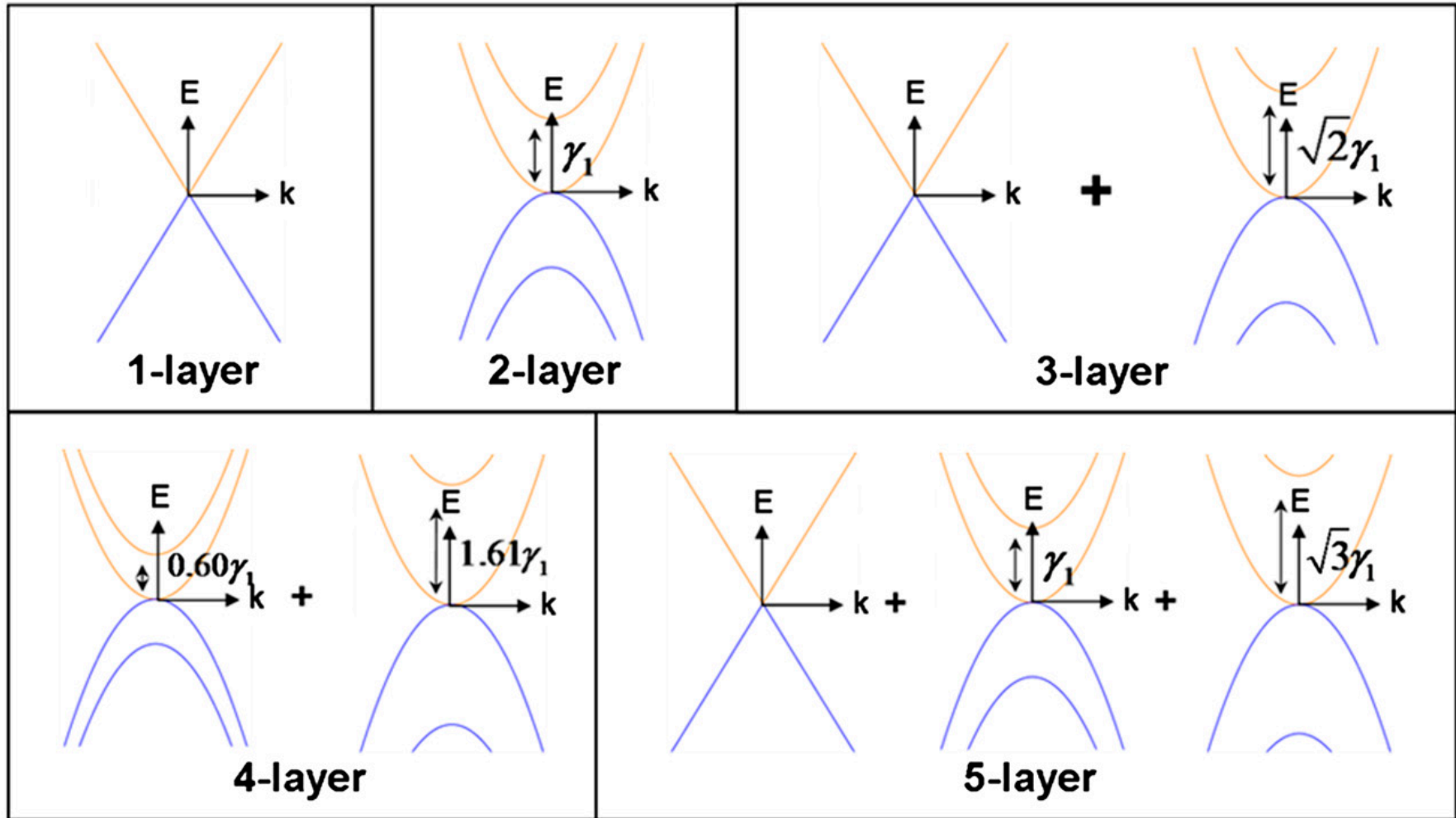
**Graphene AB Bilayer**

Chiral massive fermions

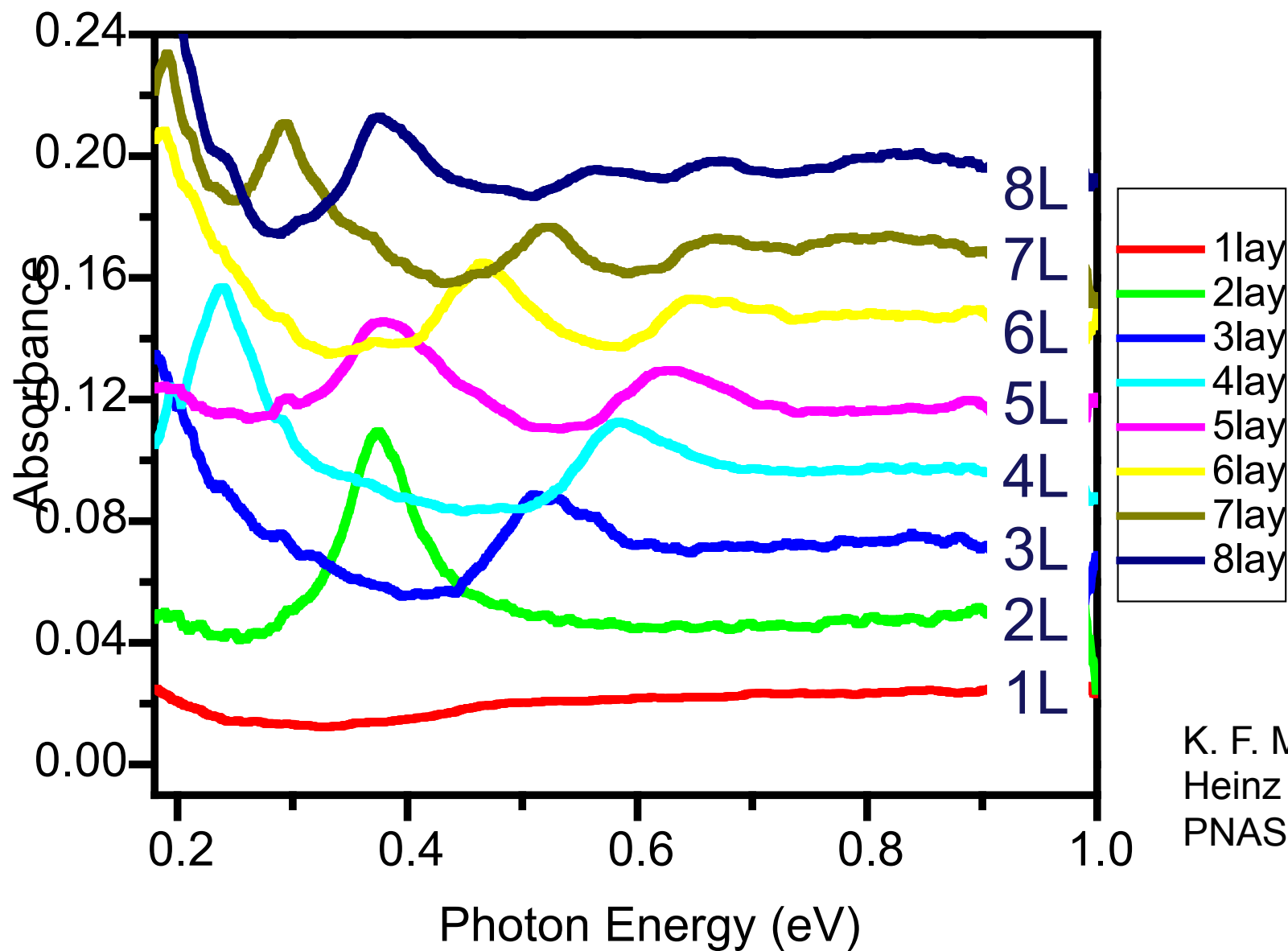




# Few-layer Bernal-stacked graphene

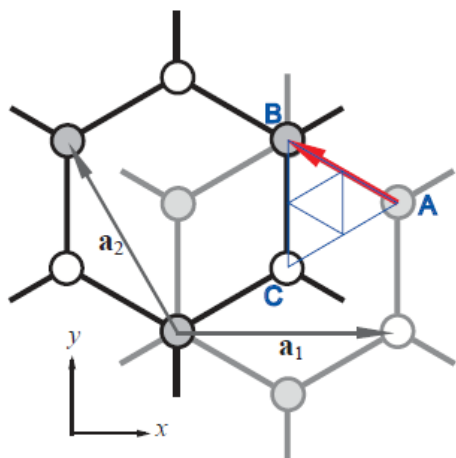


# Few-Layer Graphene Electronic Absorption Spectra



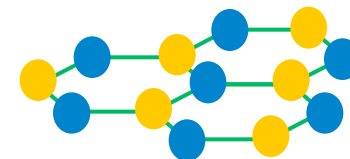
K. F. Mak,  
Heinz group  
PNAS (2010)

# Stacking order in few-layer graphene

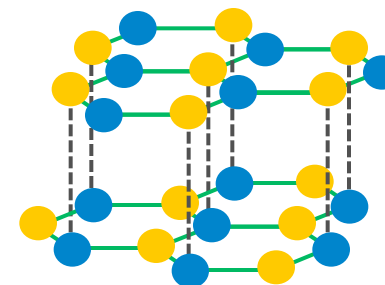


$AB = AC$

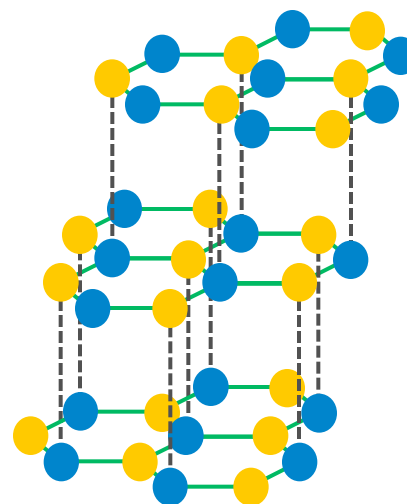
**1-Layer**



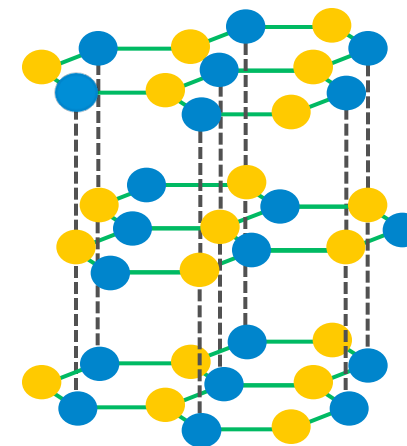
**2-Layer**



**3-Layer**



**ABC**



**ABA**

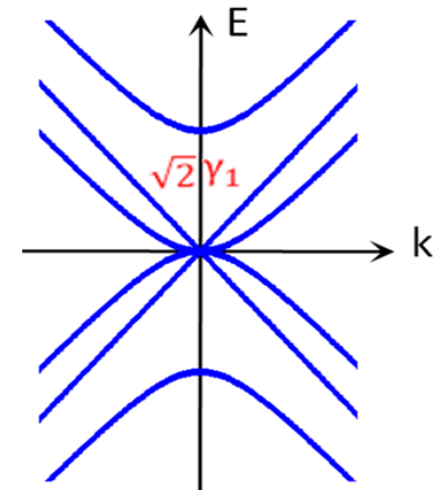
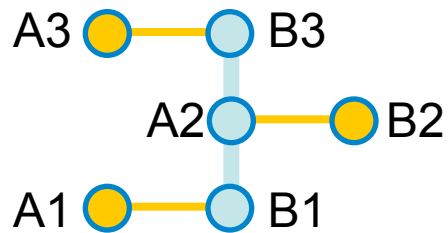
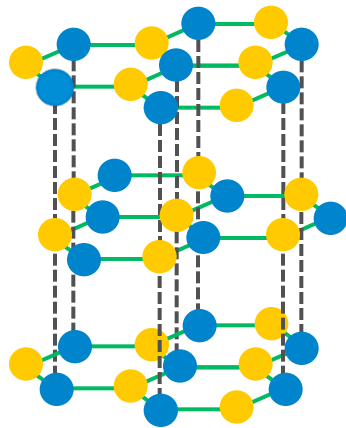
S. Latil and L. henrard, PRL 036803 (2006)

M. Aoki and H. Amawashi, Solid State Commun. 142, 123 (2007)

# Trilayer graphene

**ABA**

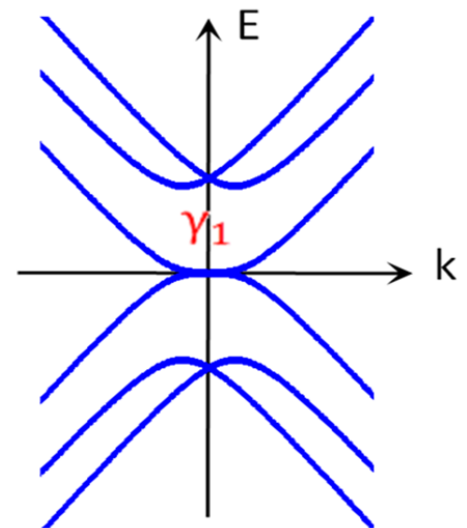
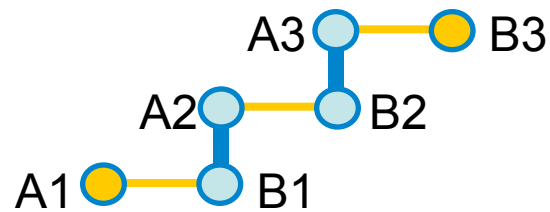
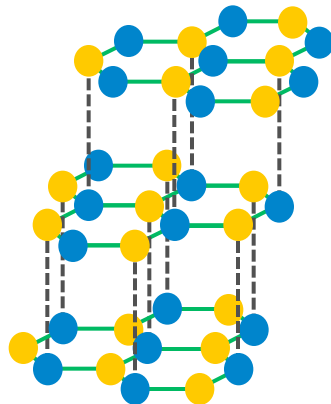
*Mirror symmetry*



(b) ABC

**ABC**

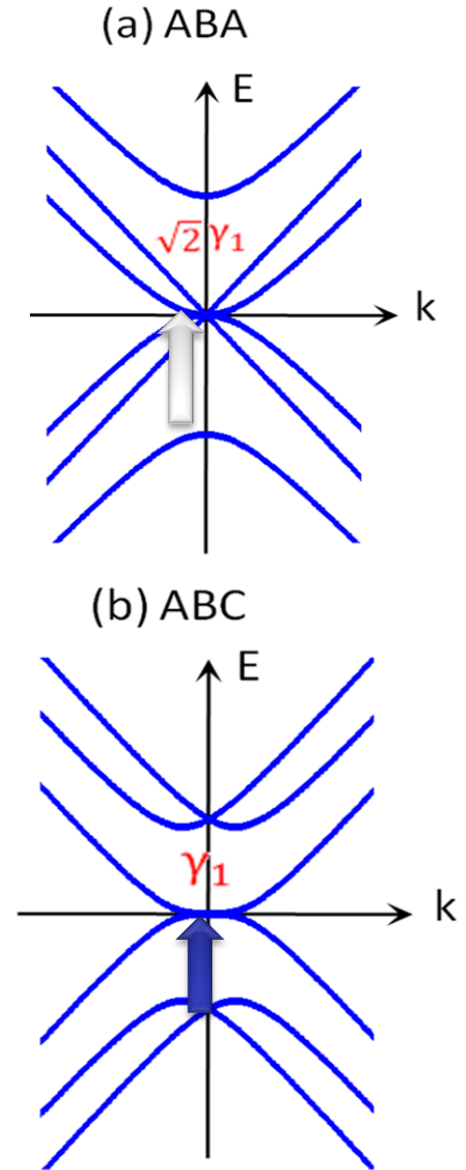
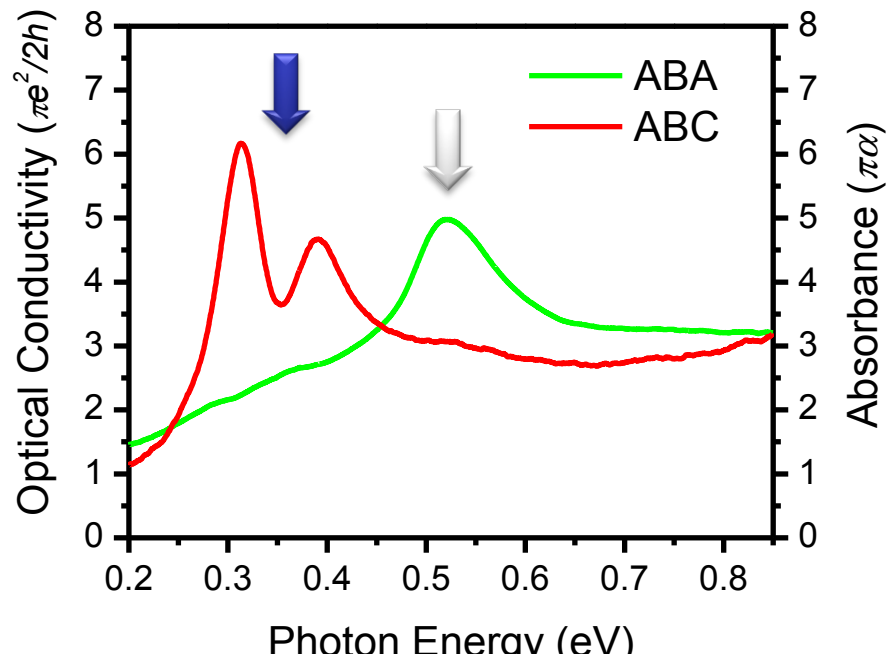
*Inversion symmetry*



# Trilayer graphene

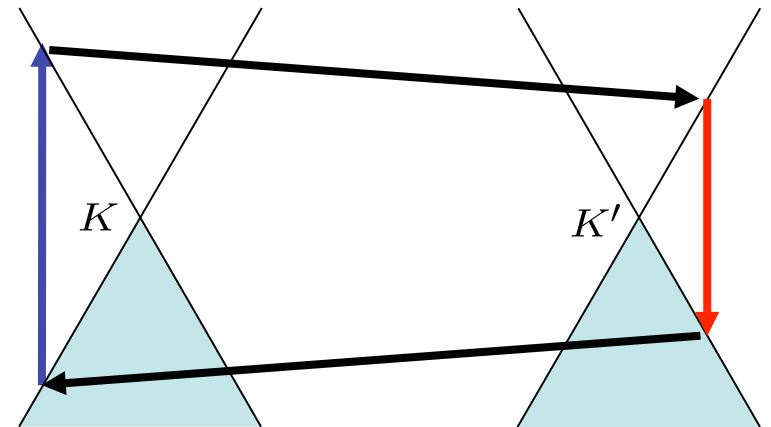
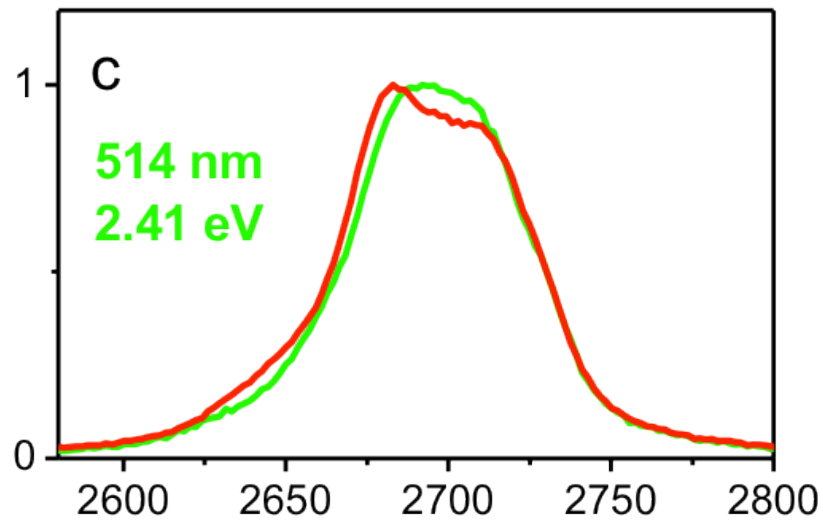
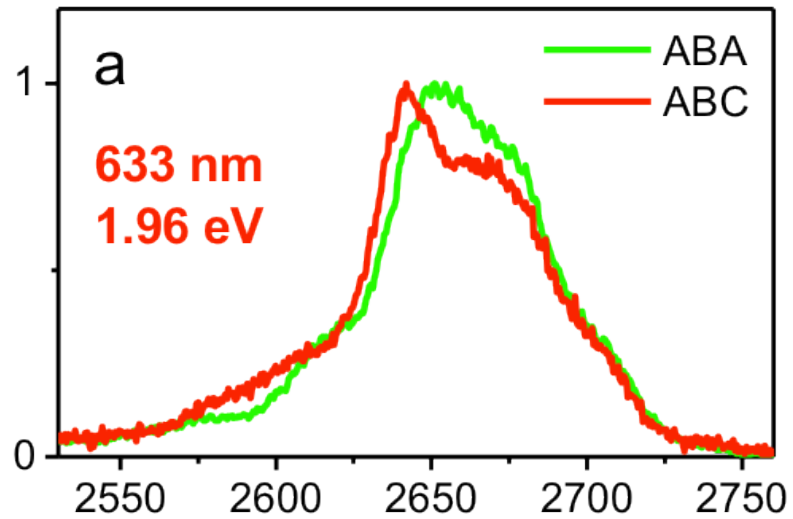
- **Characterization of stacking order by infrared and Raman spectroscopy**
- **Controlling the electronic structure by electrical gating – inducing a band gap**

# Infrared absorption of trilayer graphene



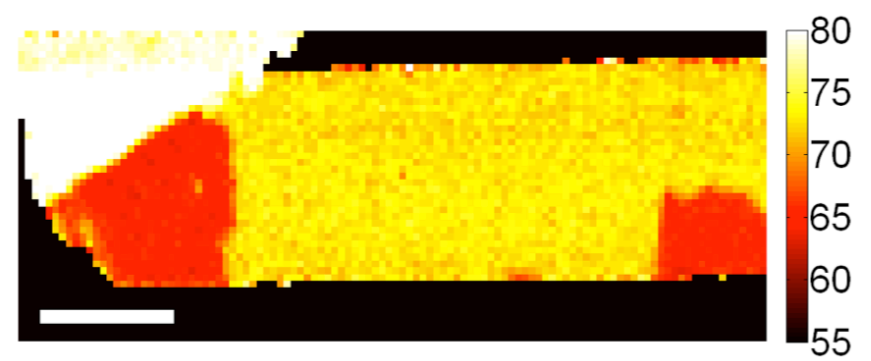
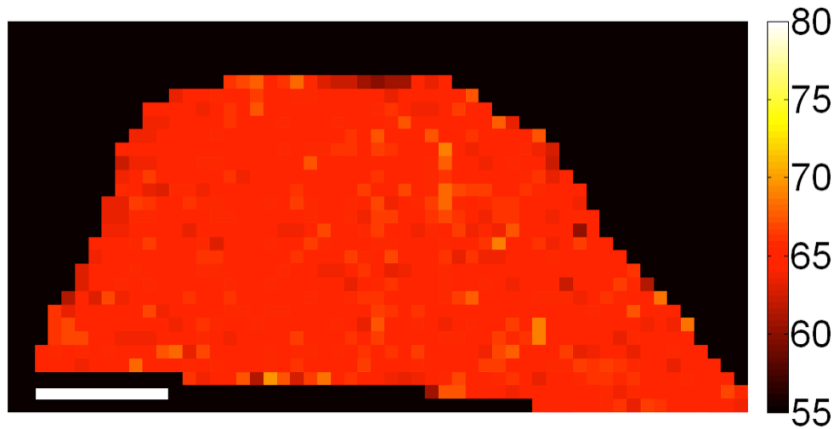
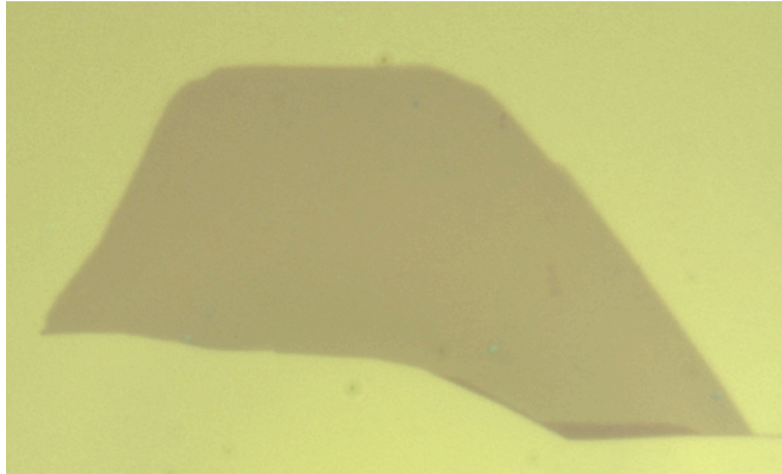
C. H. Lui, TFH *et al*, *Nano Lett.*, 11, 164–169 (2011)

# Raman 2D/G' spectra



C. H. Lui, TFH *et al.*, *Nano Lett.*, 11, 164–169 (2011)

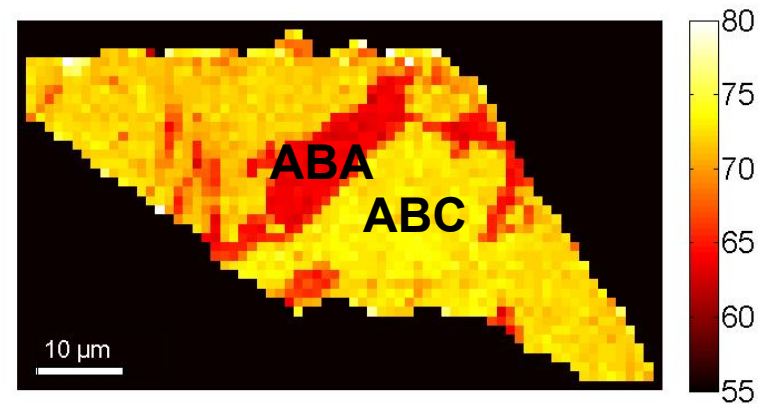
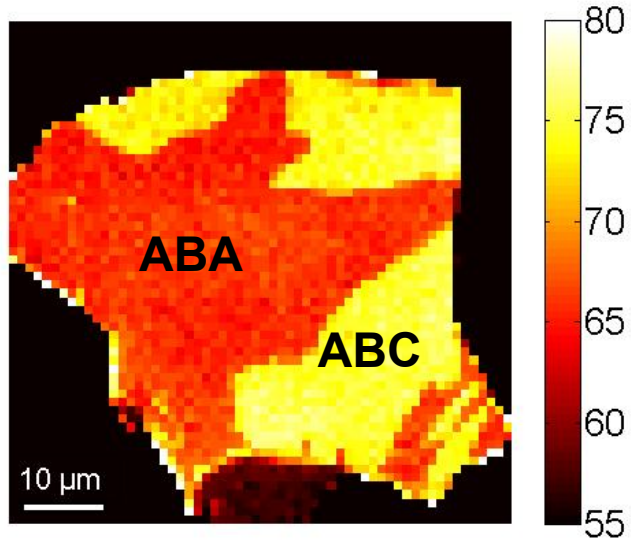
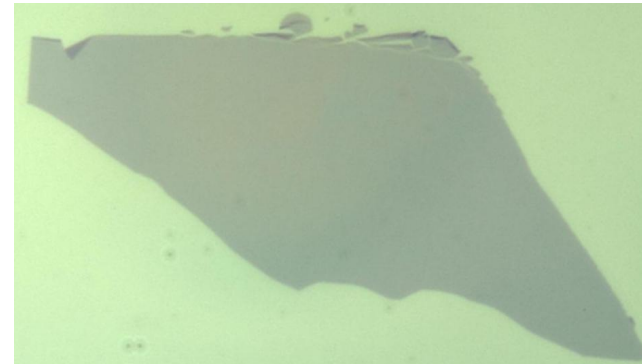
# Raman images of 2D linewidth



C. H. Lui, TFH *et al.*, *Nano Lett.*, 11, 164–169 (2011)



# Raman images of 2D linewidth



C. H. Lui, TFH *et al.*, *Nano Lett.*, 11, 164–169 (2011)

# Statistics

## Trilayer graphene

- total sample number: 45
- Purely ABA samples: 26
- Purely ABC samples: 0
- Mixed-stacking samples: 19
- ABA/ABC area ratio: **85:15**

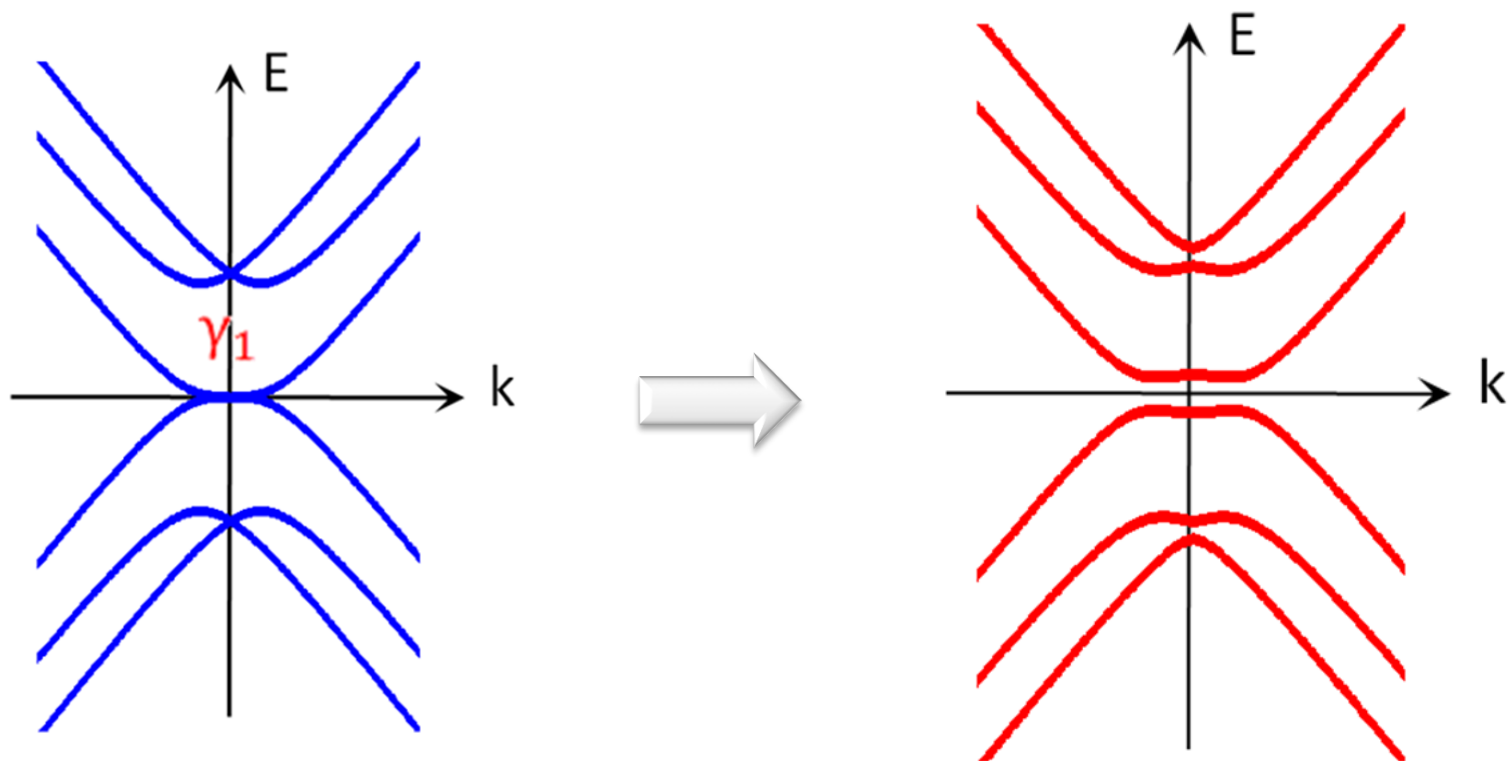
## Graphite (X-ray diffraction studies)

- **14% of rhombohedral (ABC) structure;**
- 6% of disordered structure;
- 80% of Bernal (ABA) structure.

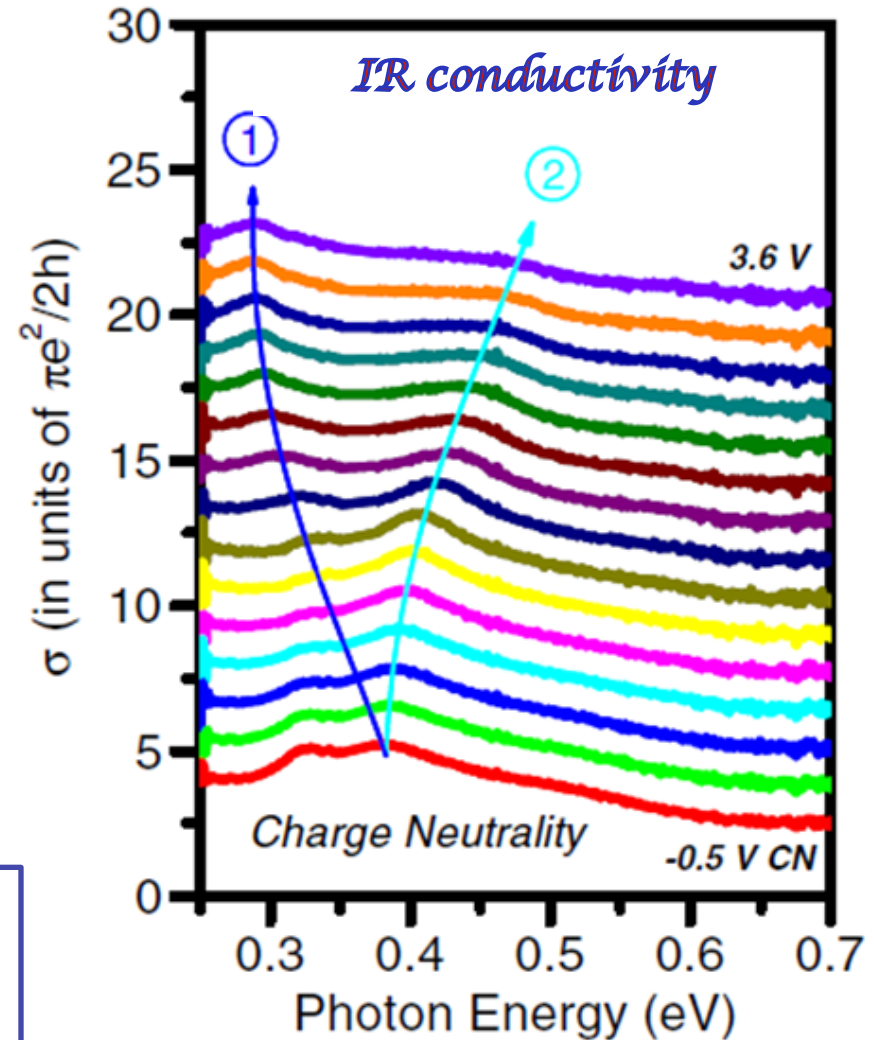
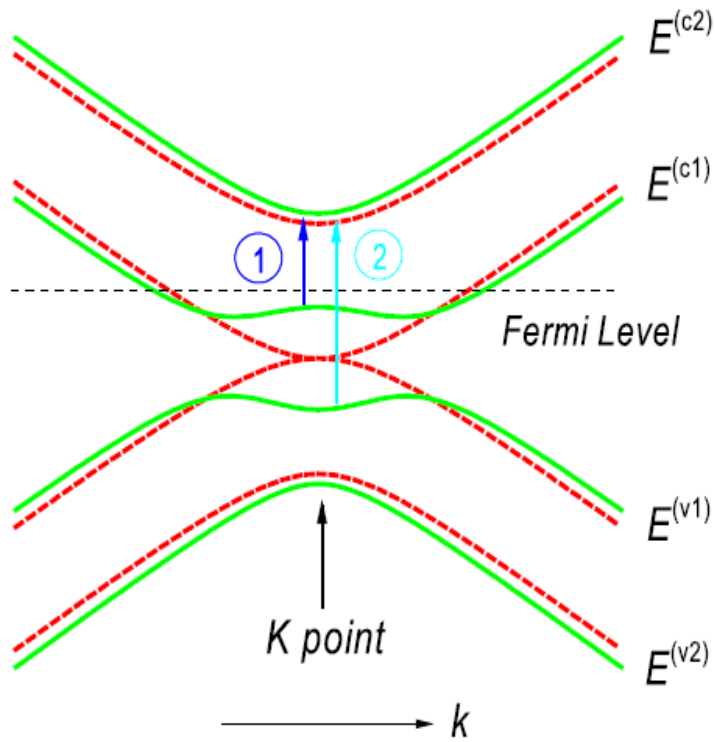
1. Lipson, H., and Stokes, A. R., Proc. Roy. Soc., A, **181**, 101 (1942).
2. Rooksby, H. P. and E. G. Steward, E. G., Nature **159**, 638 (1947)

**Graphene trilayers inherit the structure of graphite.**

# Controlling the Electronic Structure of Trilayer Graphene by Applied E-Fields




# Probing the bilayer band gap by IR



[K. F. Mak *et al*, PRL 102, 256405 (2009).]

[Y. B. Zhang *et al*, Nature 459, 820 (2009)]

[A.B. Kuzmenko *et al*, PRB 80, 165406 (2009).]

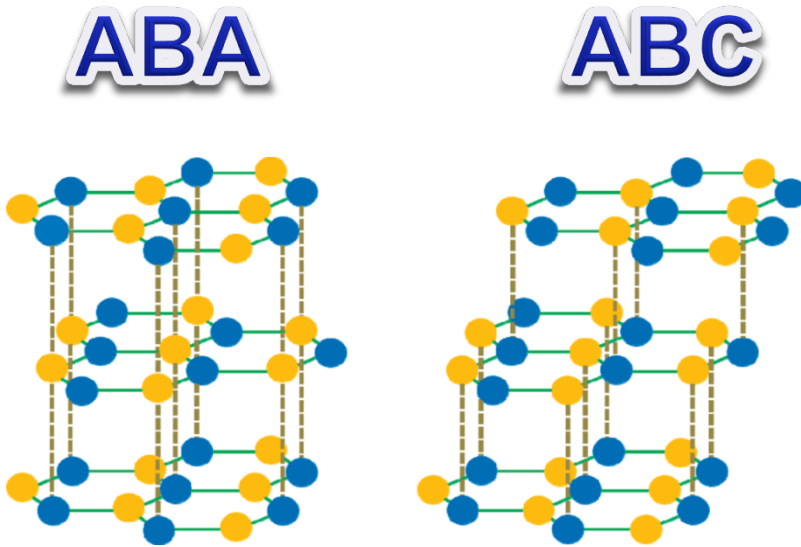


Is the induction of a tunable  
band gap possible in **trilayer**  
graphene?

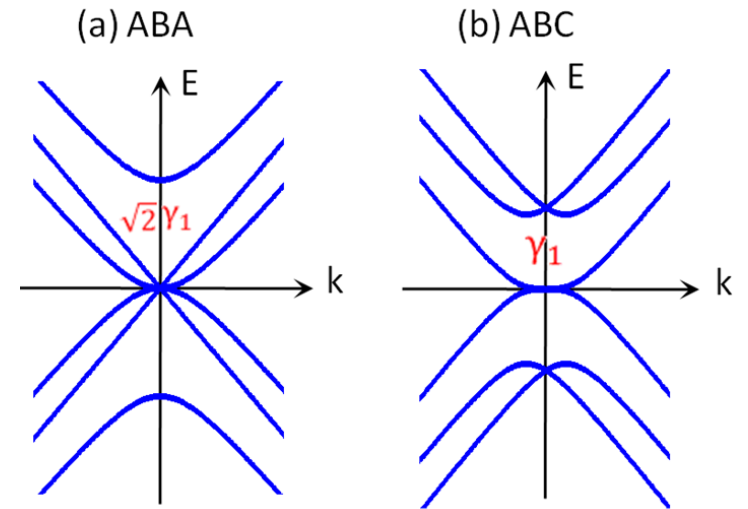
*Yes ! But it depends on  
the stacking order.*

Guinea, Castro-Neto & Peres, Aoki et al., Koshino and McCann, MacDonald, Avetisyan et al,...

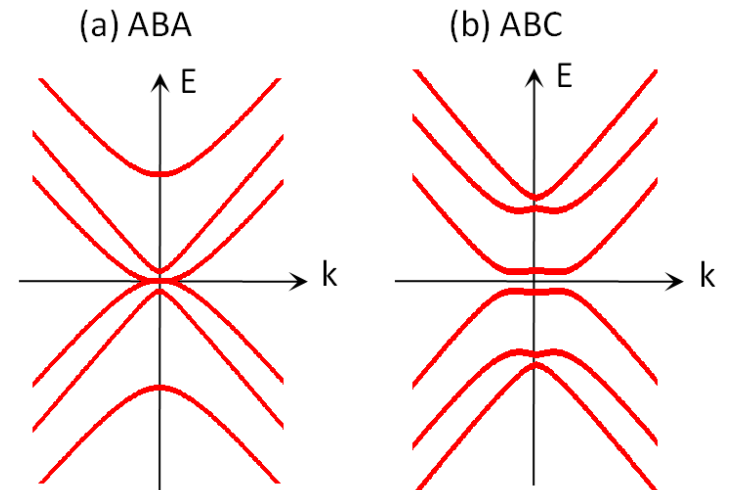
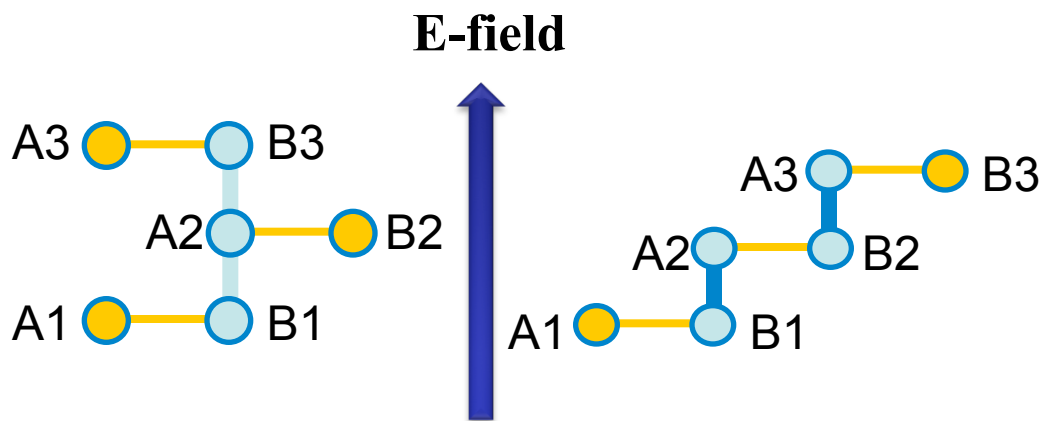
# Electric-field effect in trilayer graphene



**No E-field**



**With E-field**



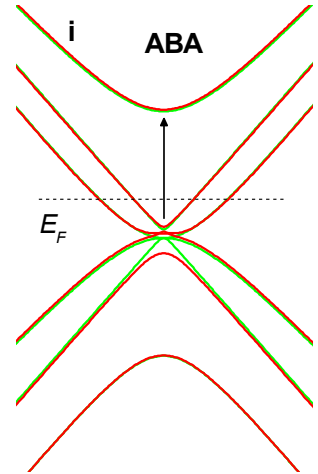
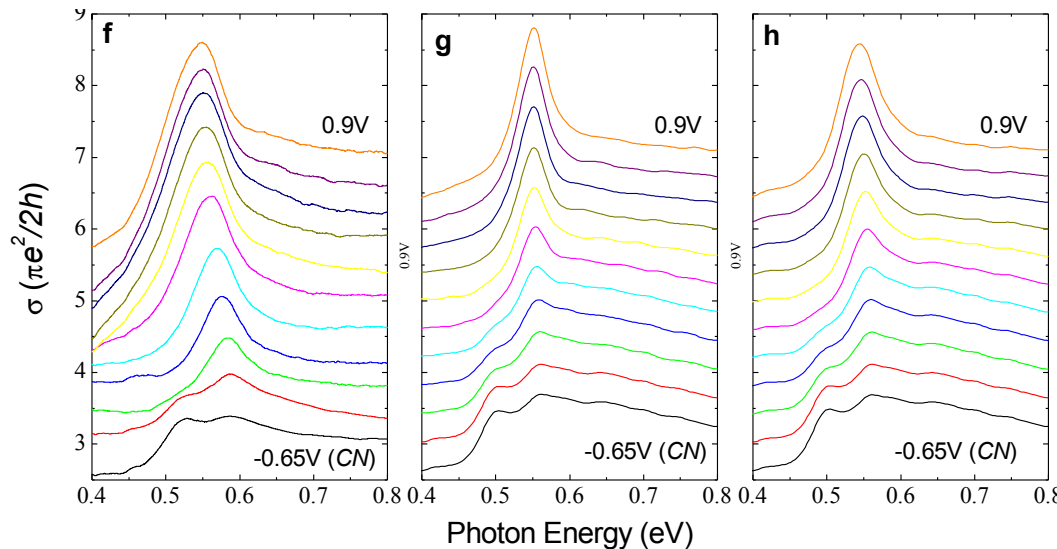
# Electric-field effect in trilayer graphene

Expt.

Field-modified  
band structure

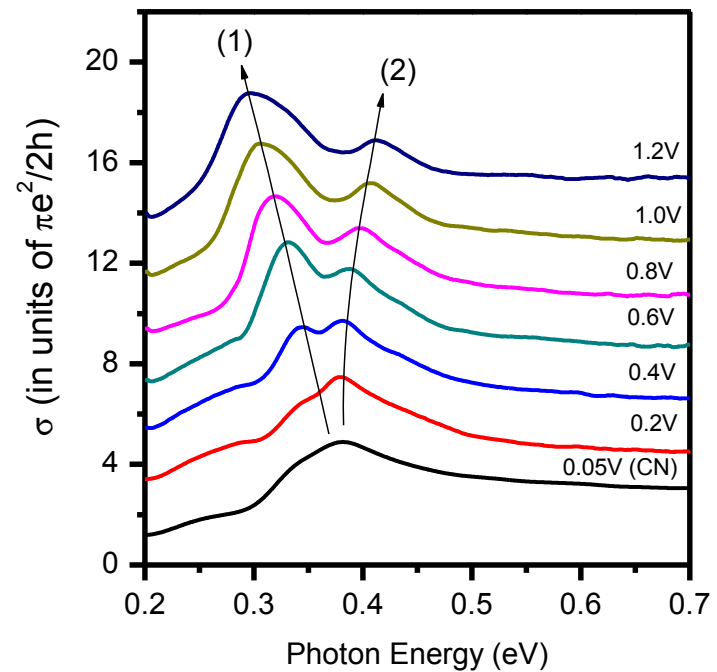
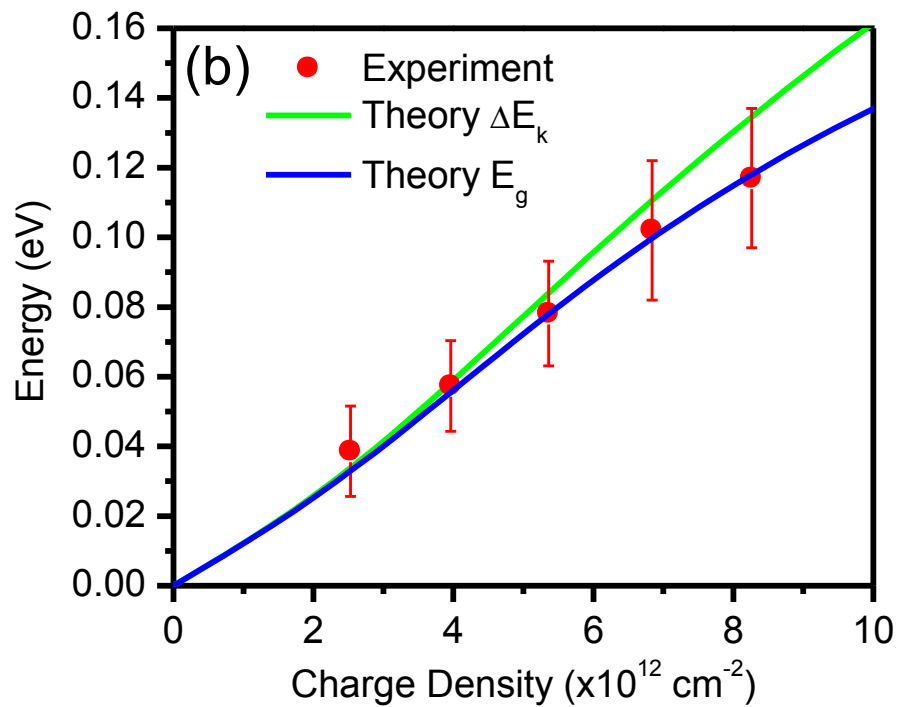
Unchanged  
band structure

ABA



Nature Physics 7, 944-947 (2011)

# Induced band gap in ABC trilayer



*Nature Phys.* **7**, 944-947 (2011)

Also: Related transport measurements: Lau et al., *Nature Phys.* (2011).



# Summary

## **SINGLE-LAYER GRAPHENE: e-e interactions**

- Major increase in absorption above  $\pi\alpha$  for higher photon energies, rising to close to 10% at 4.6 eV
- Peak is associated with saddle-point at M-point in BZ.
- *Position and asymmetry lineshape require strong excitonic correlations: Saddle-point exciton -- discrete state embedded in continuum*  
*Fano absorption profile*

## **TRILAYER GRAPHENE: stacking-dependent interlayer interactions**

- Identification of ABA (Bernal) and ABC (rhombohedral) trilayers
  - IR conductivity
  - Raman 2D/G'
- ABA and ABC trilayers exhibit completely different low-energy band structure, as revealed in IR conductivity
- E-field induced band gap exceeding 100 meV in ABC trilayers; no band gap is found in ABA trilayers.