

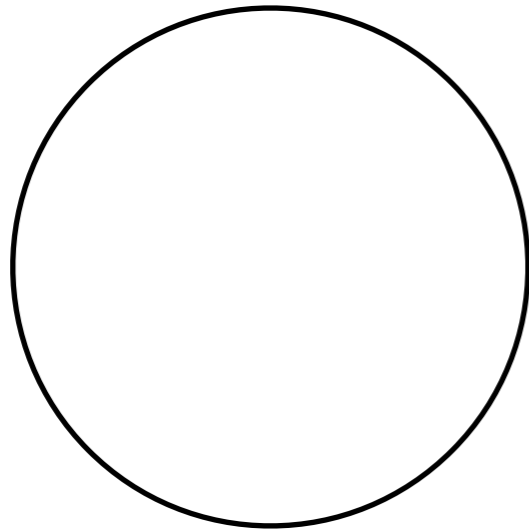
Dynamical environments are interesting III: Can we find them, & making very exotic sources

Richard O'Shaughnessy

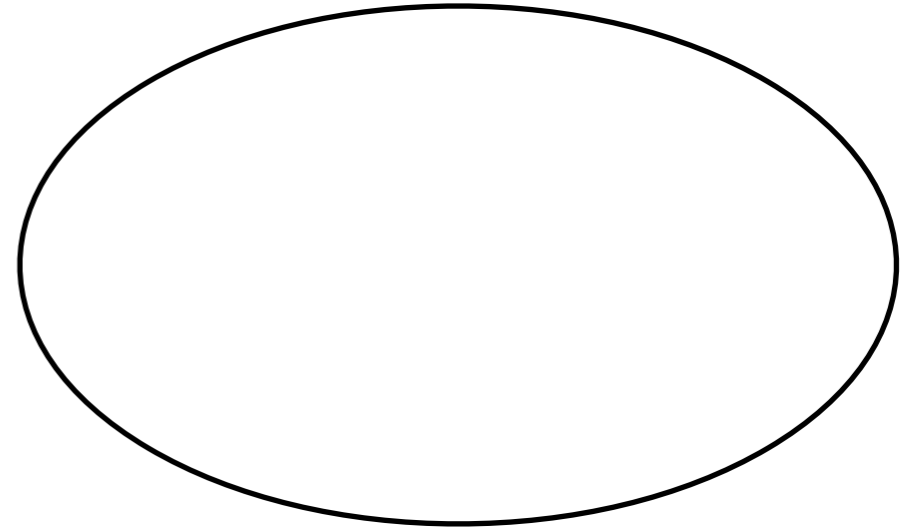
2019-07-16 17 Gravast19

Part 1: Identifying eccentric sources [skip me]

Eccentricity for GW: A review (ground-based IFOs)



More from Alessandra Thursday



- Circular

- Locally constant separation
- Monotonic orbital phase

$$\Phi_{orb} \simeq \omega_{orb} t$$

- Eccentric

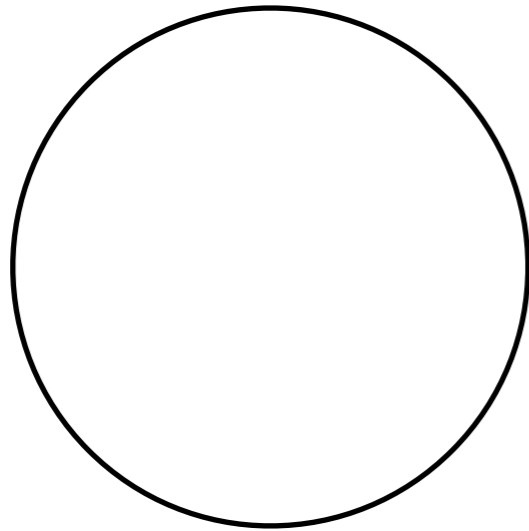
- Time-varying separation
- **Strong field stronger**
- Phase more complex
 - **Multiple harmonics**, impacts detection & PE for band-limited IFOs
 - Technical: tools from dynamics

$$t\omega_{orb} = \psi - e \sin \psi$$

$$\psi = t\omega_{orb} + \sum_{n=1}^{\infty} \frac{2}{n} \sum J_n(ne) \sin n t \omega_{orb}$$

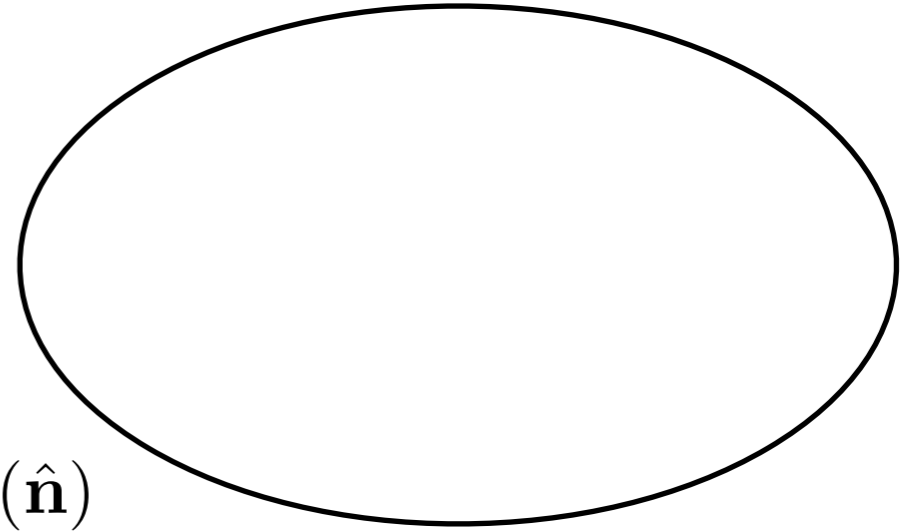
$$r/a = 1 + e^2/2 - \sum_{n=1}^{\infty} \frac{2e}{n} J'_n(ne) \cos n t \omega_{orb}$$

Eccentricity for GW: A review (ground-based IFOs)



More from Alessandra Thursday

$$h = \sum_{lm} h_{lm}^{(-2)} Y_{lm}(\hat{\mathbf{n}})$$



- Circular

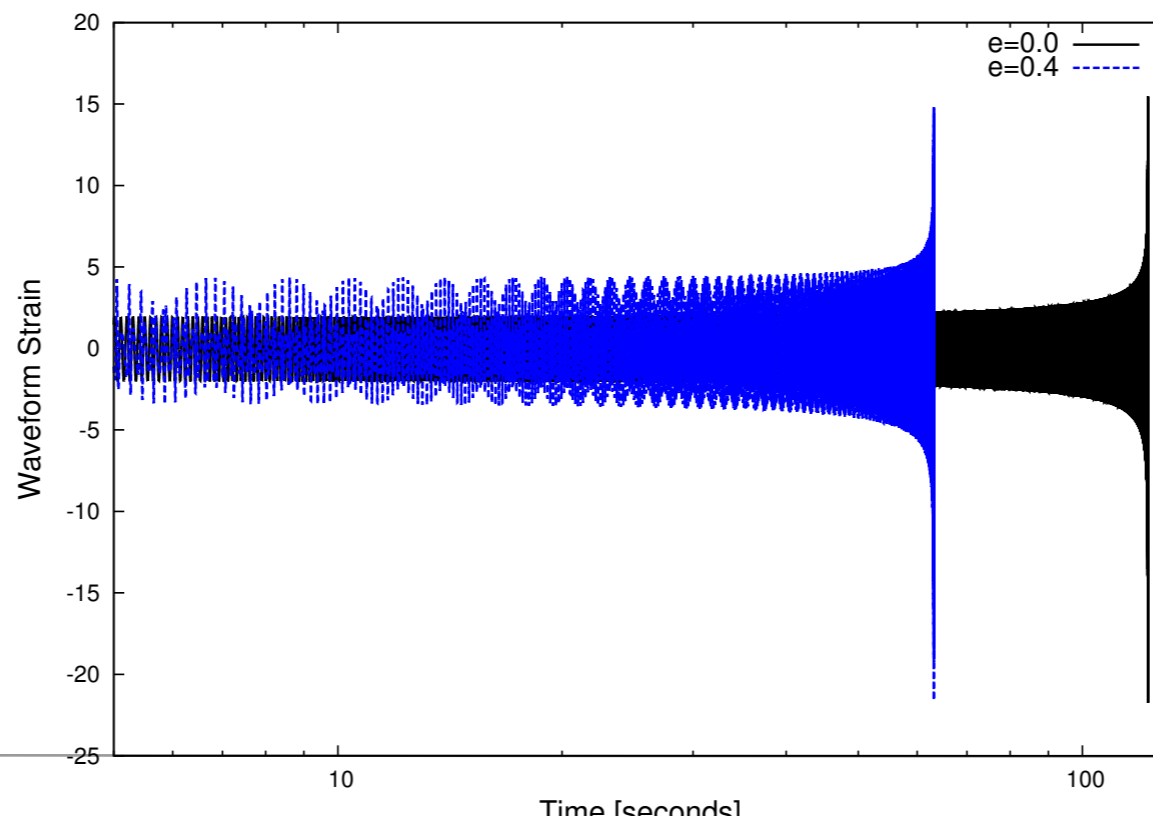
- Without precession, simple

$$h_{lm} = A_{lm} e^{-im\Phi_{orb}}$$

- Eccentric

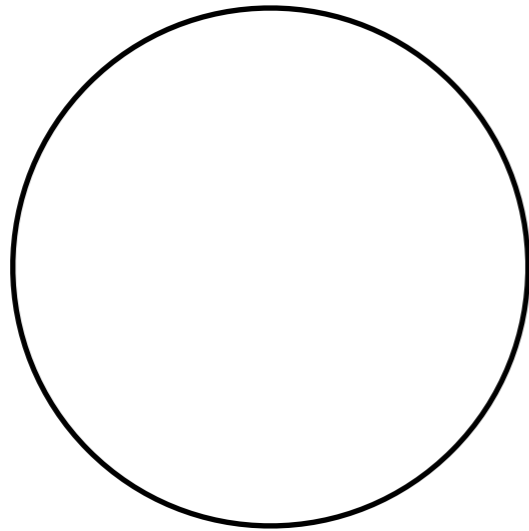
- Strongly modulated, $e \sim 1/f$ late

$$h_{lm} = \sum_k A_{lmk} e^{-ik\Phi_{orb}}$$

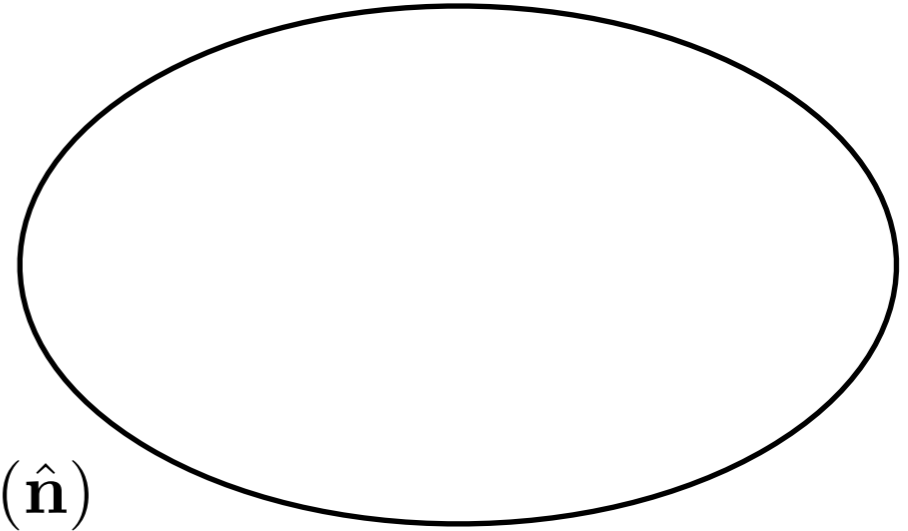


Huerta et al 1408.3406

Eccentricity for GW: A review (ground-based IFOs)



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$$h = \sum_{lm} h_{lm}^{(-2)} Y_{lm}(\hat{\mathbf{n}})$$

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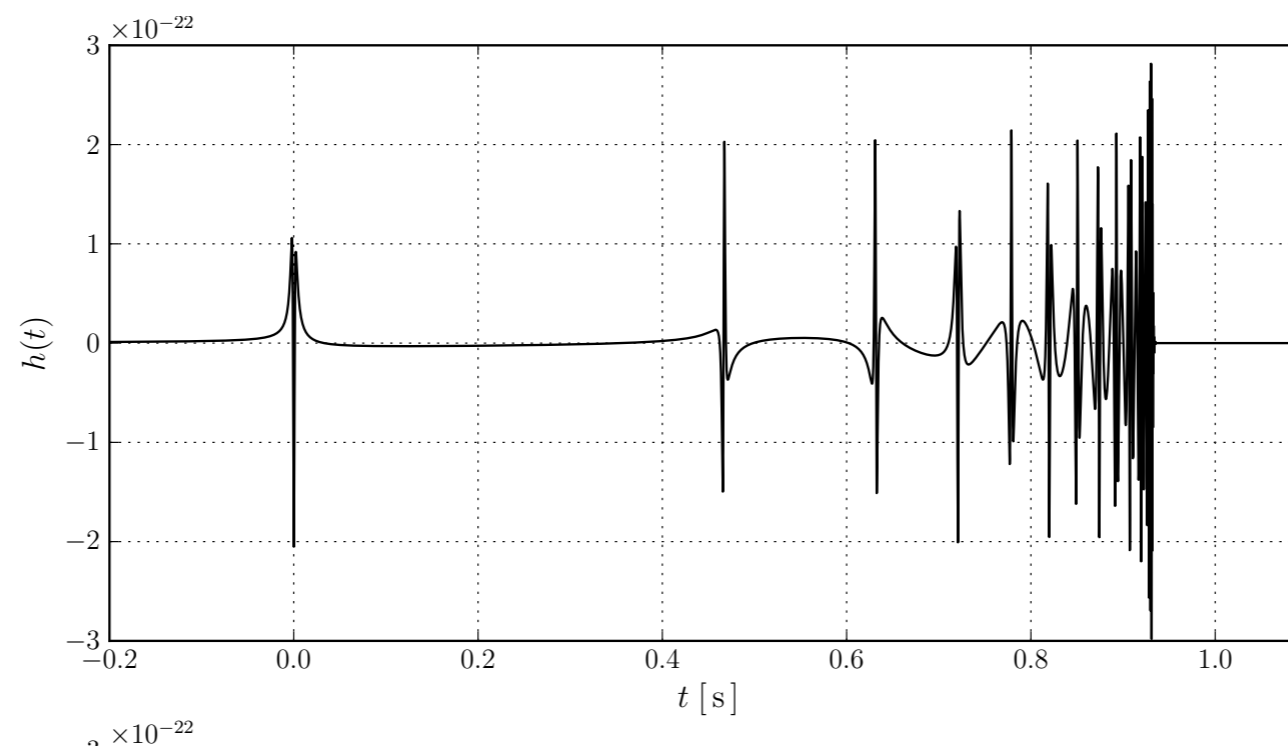
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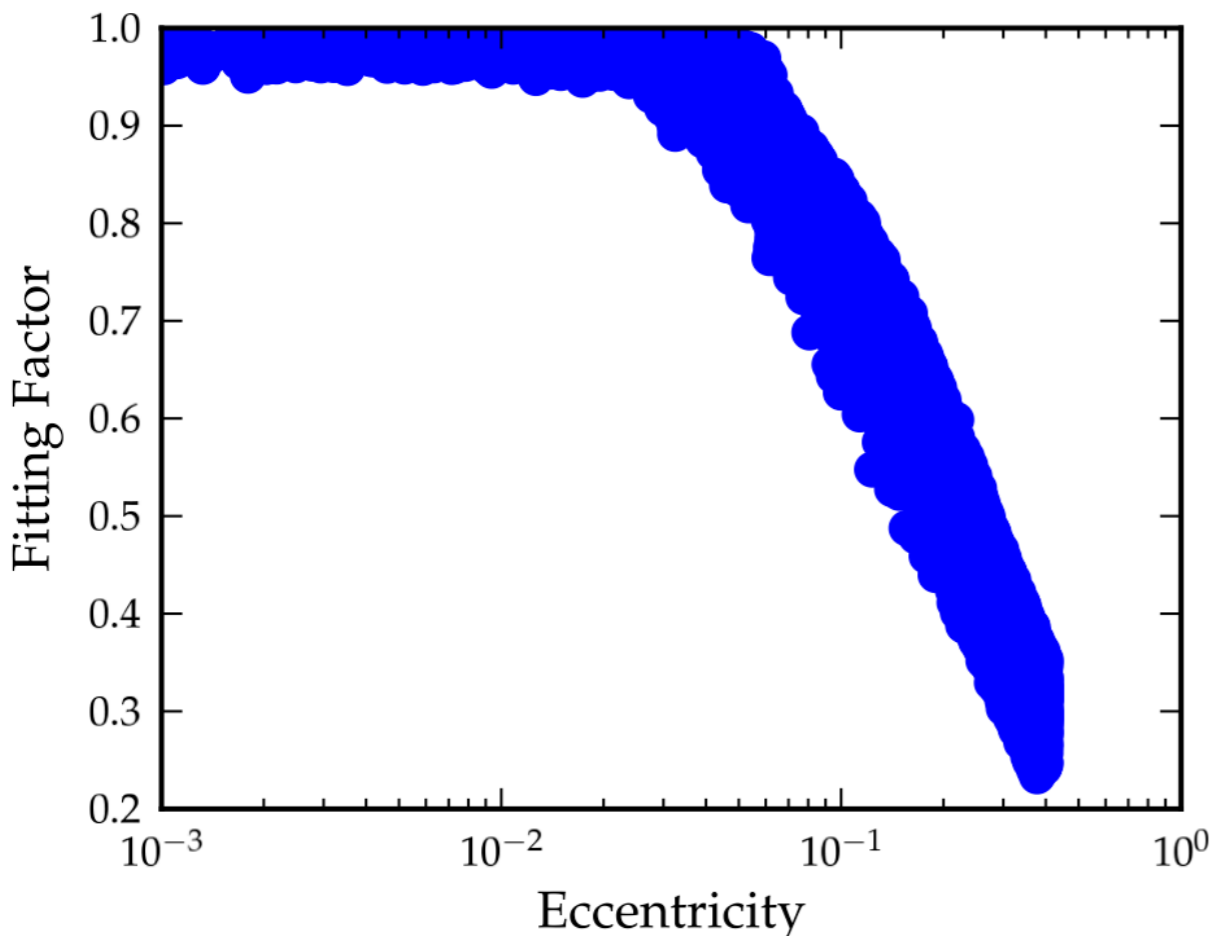
Tai et al 2014

Impact of eccentricity on searches

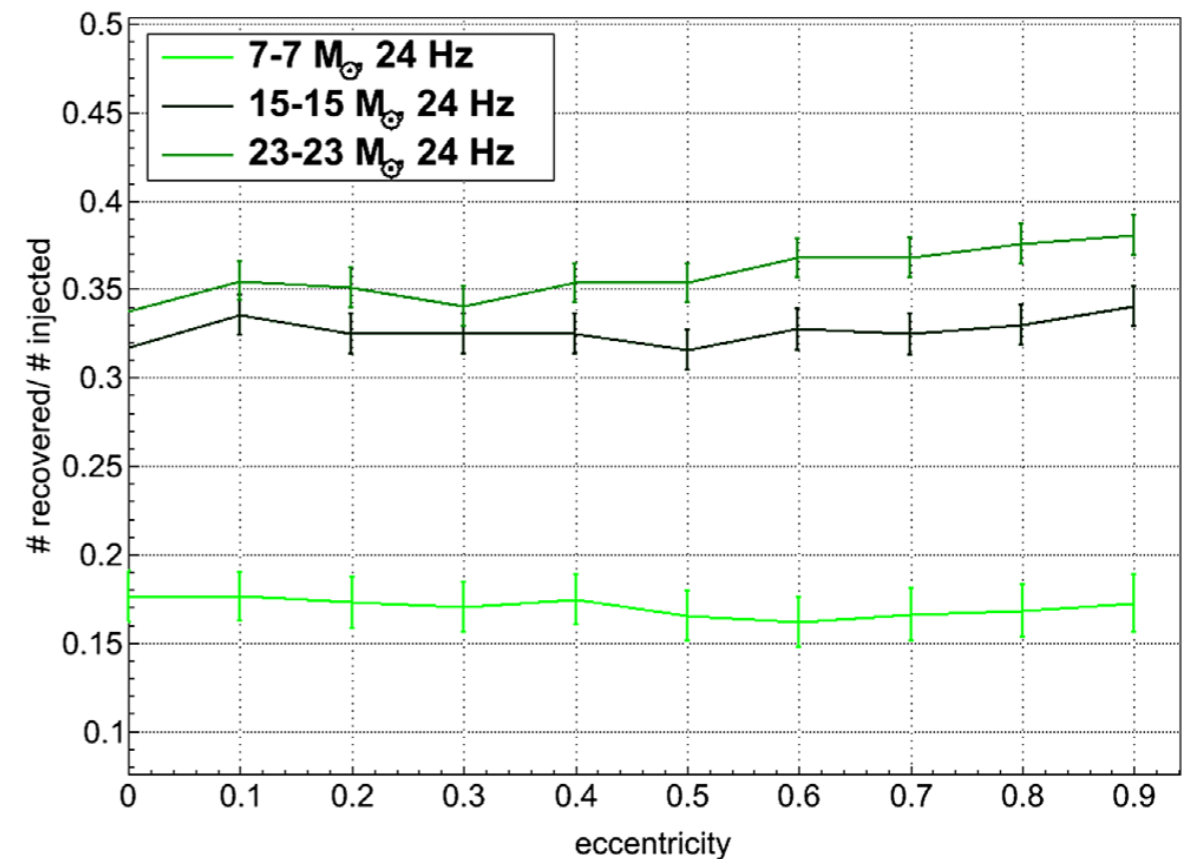
- Rules of thumb:

- Binary highly circular, unless large eccentricity at f_{\min}
- Small phase deviations can be captured by search templates
- Large eccentricity ... work in progress [Tai et al 1403.7754, Tiwari et al 2016 PRD, Thrane & Coughlin; Abbott et al 2019; ...]

Huerta and Brown (1301.1895) templates
[neutron stars, e_0 at 15 Hz in aLIGO]



Tiwari et al PRD 2016 burst search
[O2, e_0 at 24 Hz]

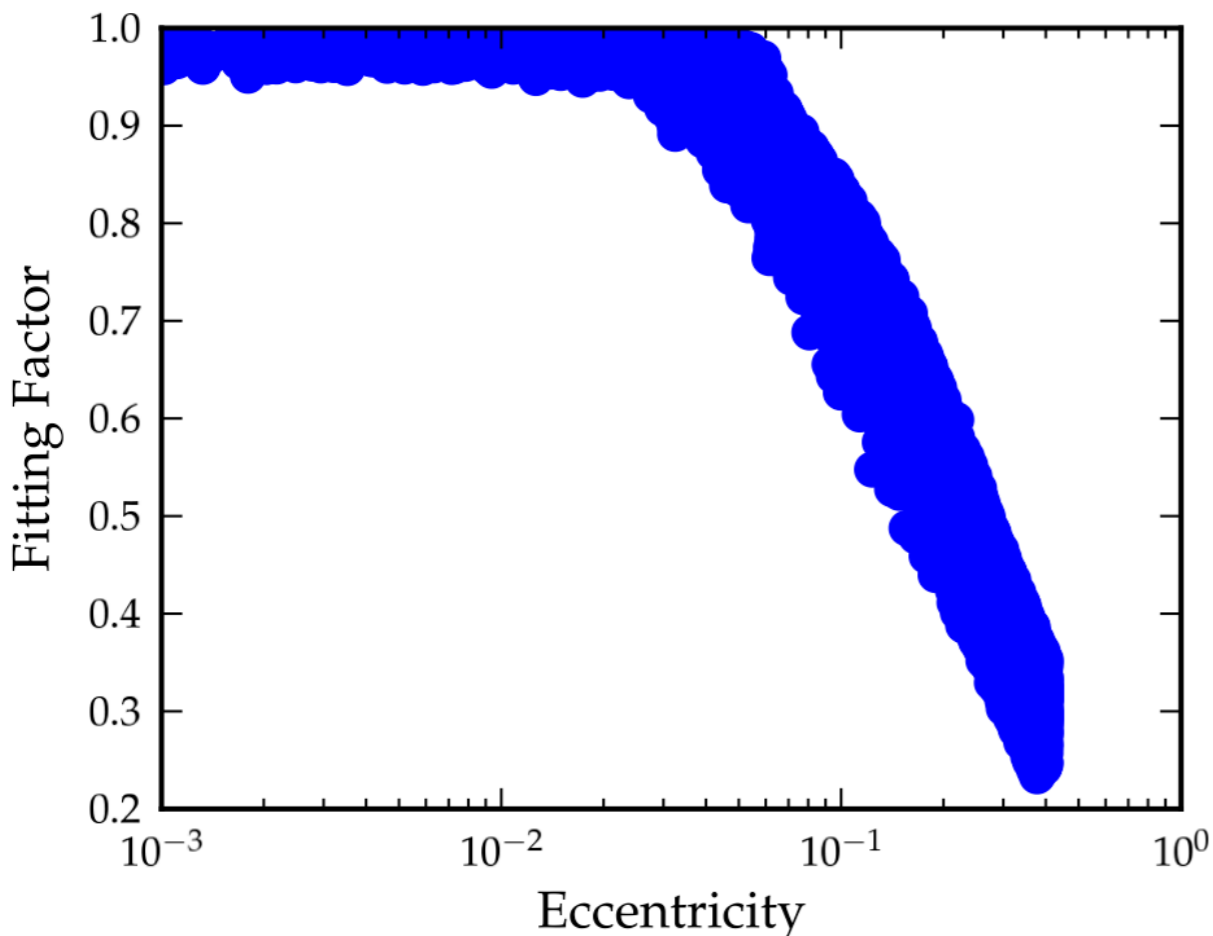


Impact of eccentricity on searches

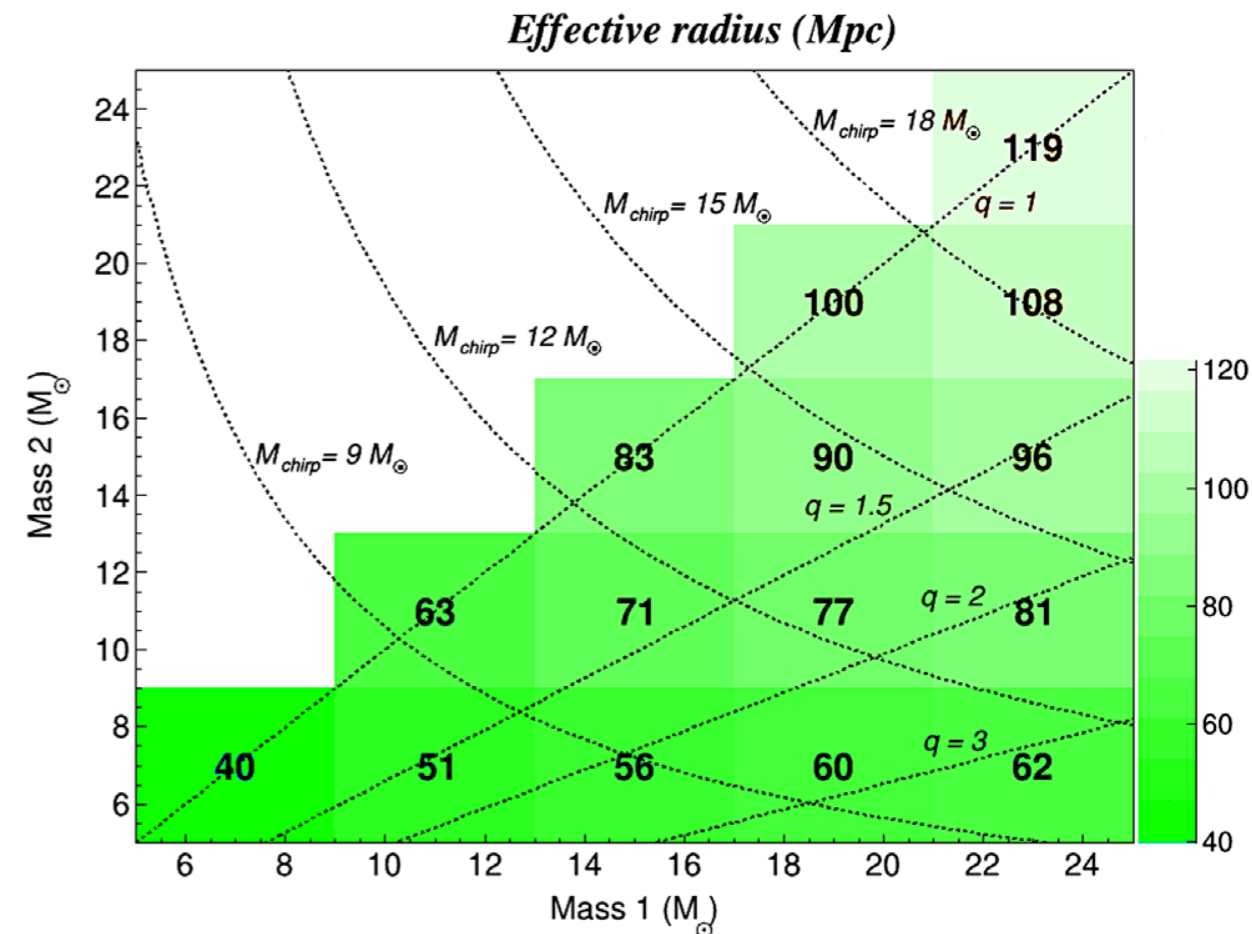
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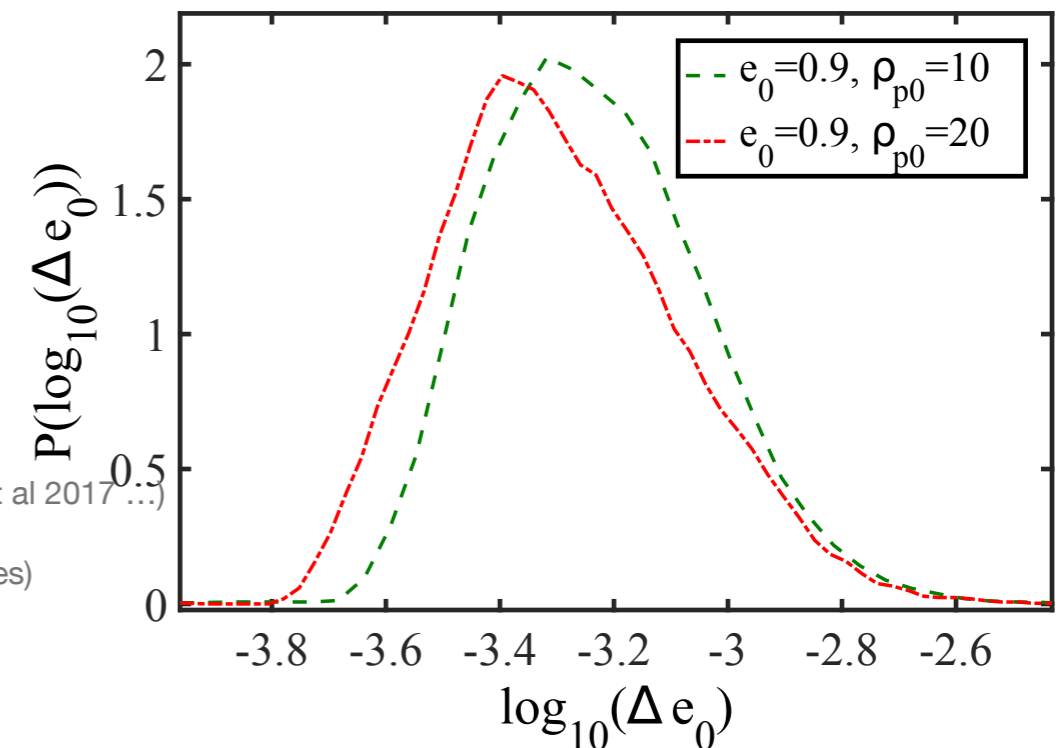


Tiwari et al PRD 2016 burst search
[O2]



Accessing eccentricity?

- **Eccentricity decreases rapidly, but we can form \sim in band**
 - Eccentricity and precession usually expected simultaneously (ouch!)
- Modest eccentricity: **Very accessible observationally (LIGO)**
 - Example (Lower et al 2018): GW150914-like event, full eccentric PE .. $e > 0.05$ fine!
 - Example (George/Huerta, PhysLett B 2018): Machine learning for point estimates
 - Example (Gondan et al ApJ 2018): Fisher estimate (below), for high-SNR systems
 - This case: $d = 100$ Mpc , $30 + 30$ Msun,
 - Using inspiral-only model
 - similar to “phase-connected bursts”
 - See also previous mismatch and PE studies (e.g., J. Henry 2014; Sun et al 2015; Ma et al 2017 ...)
 - Measurement accuracy explored thoroughly in LISA context (e.g., Cornish/Lang/Hughes)
- Main limitation: Reliable models (for search or training) for **massive BBH**
 - ...in progress (e.g., NCSA group and others)

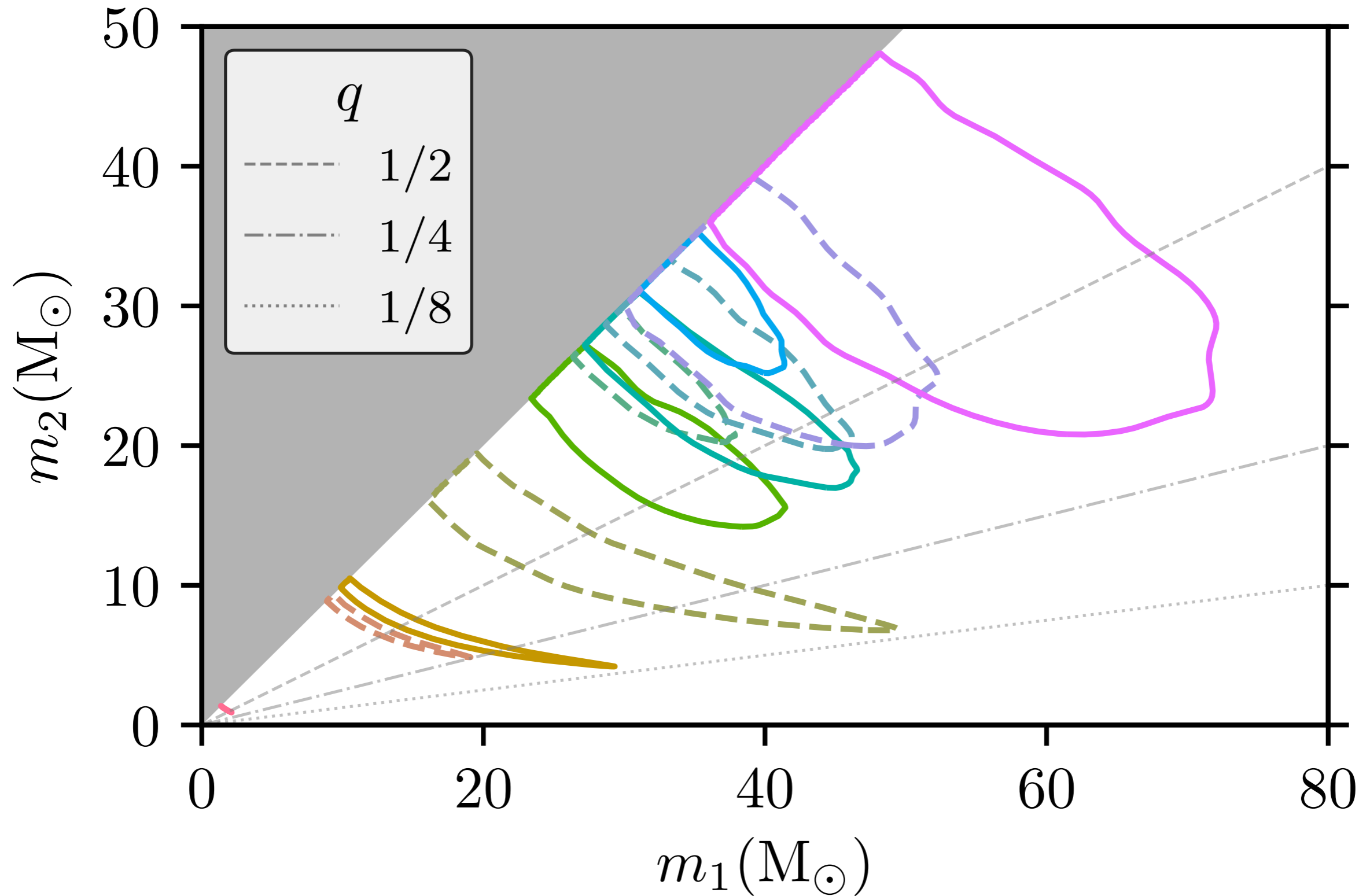


Part 2: Contribution from AGN disks

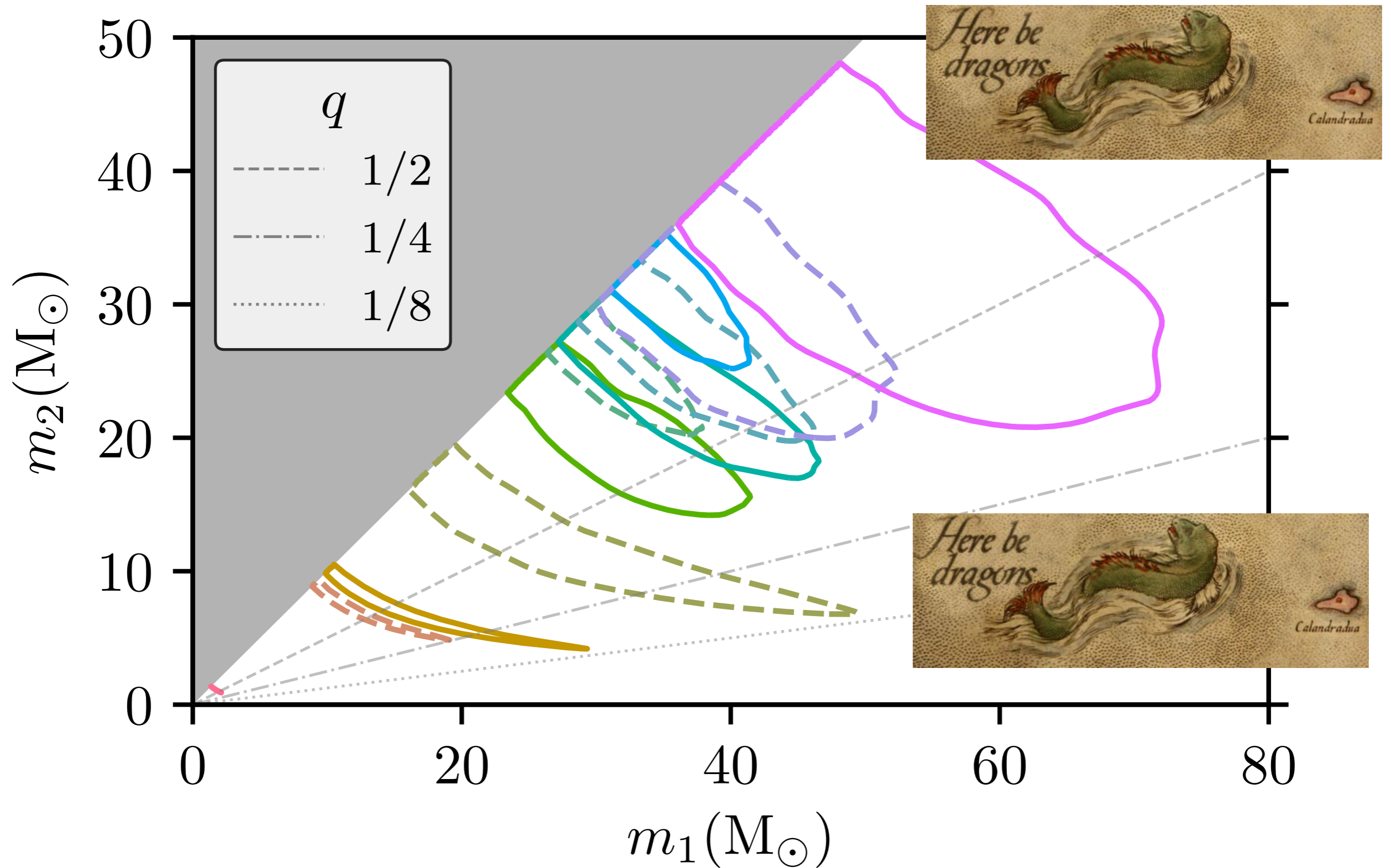
McKernan, Ford, ROS, Wysocki 2019 ([1907.04356](#))

Yang, Bartos et al ([1906.09281](#))

Mass & event rate: where we are now



Mass & event rate: where we are now



...but where did they come from?

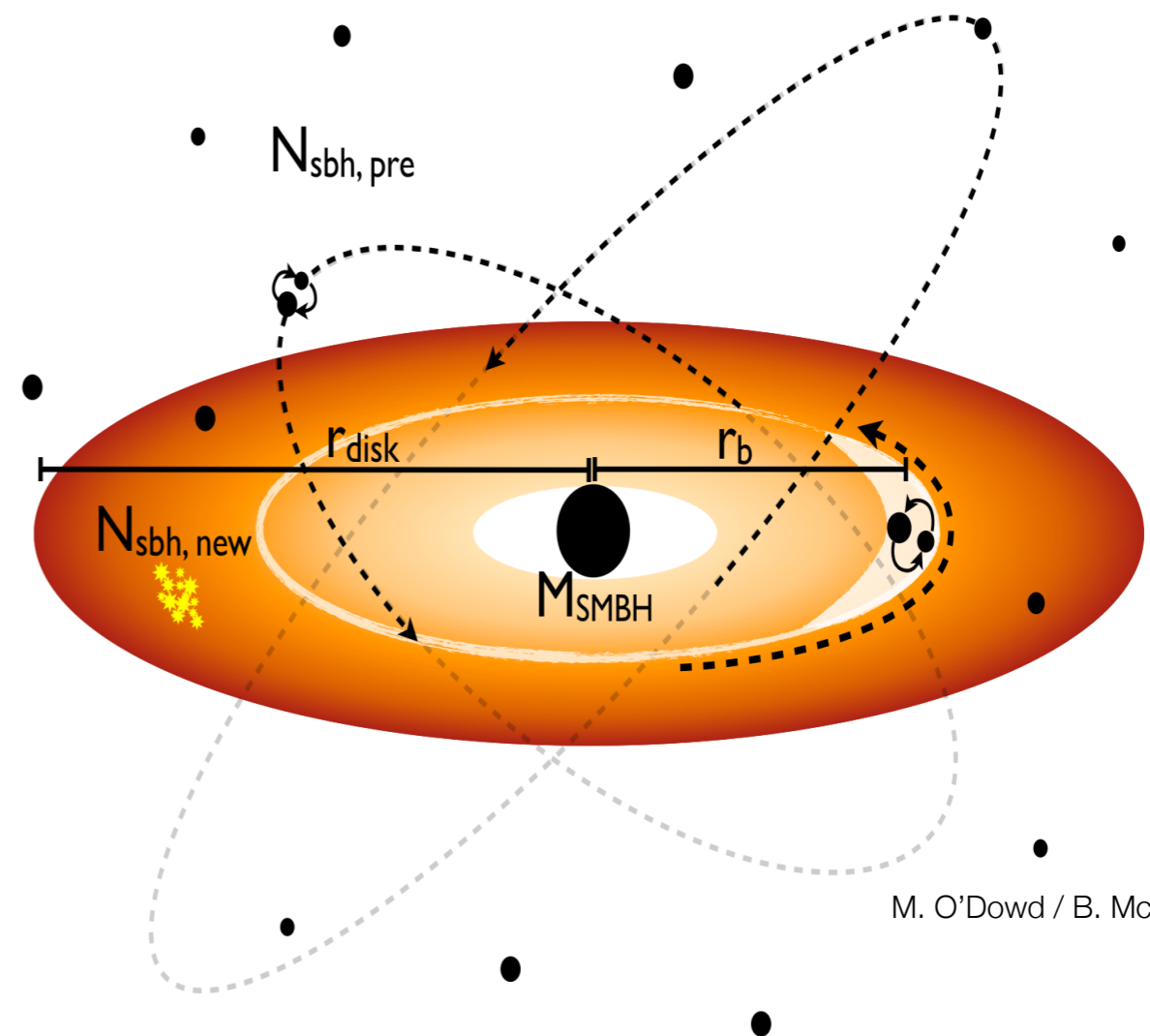
- Conventional [cluster,field], or
- Primordial?
- **Near supermassive BHs?**

brief but **efficient** mechanism

McKernan 2012,2014; Bartos 2017,McKernan 2018, Secunda 2018 ...

See also **McKernan, Ford, ROS, Wysocki 2019 (1907.04356)**

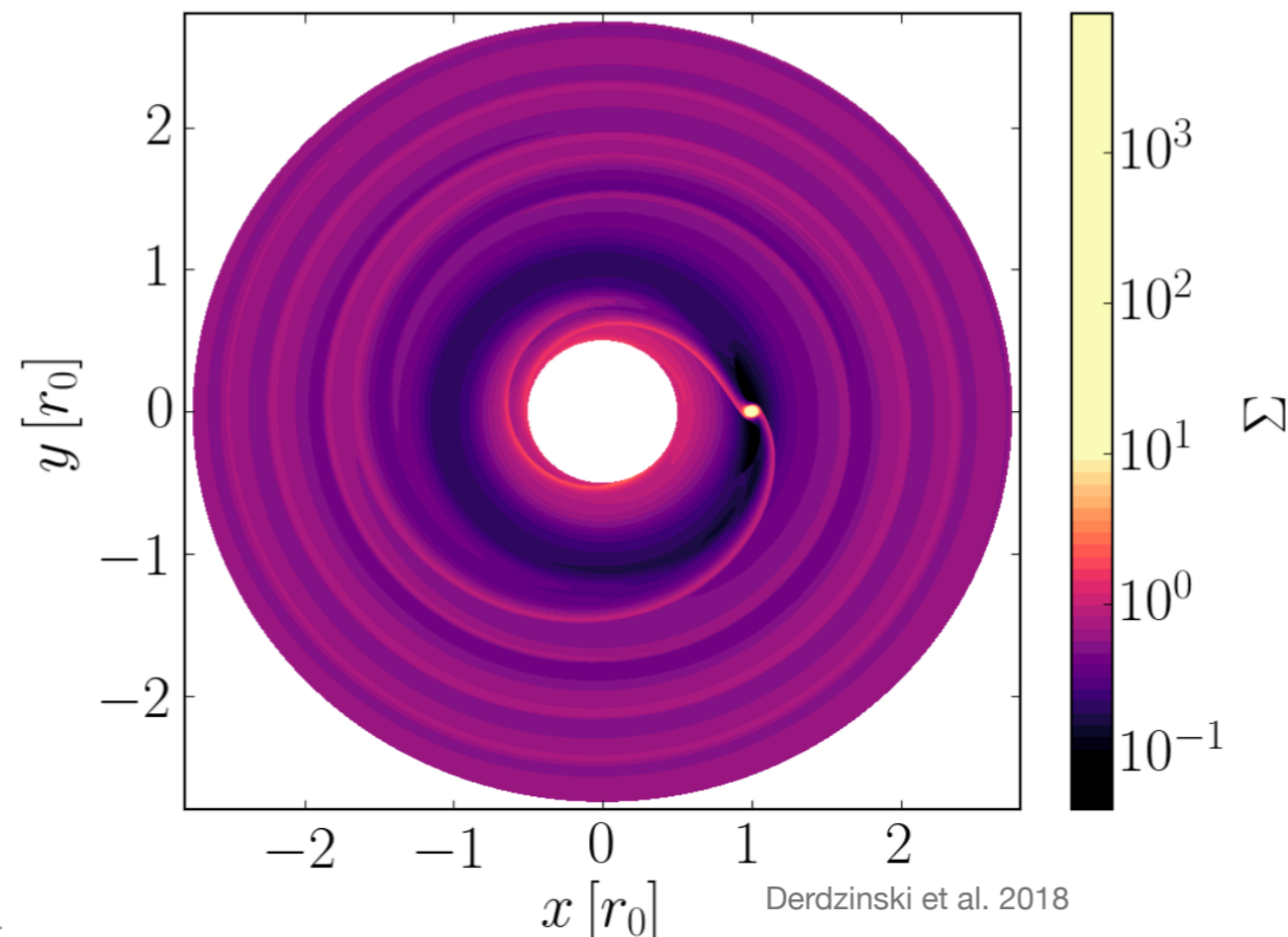
- ...outliers and exotic products as signatures?



M. O'Dowd / B. McKernan

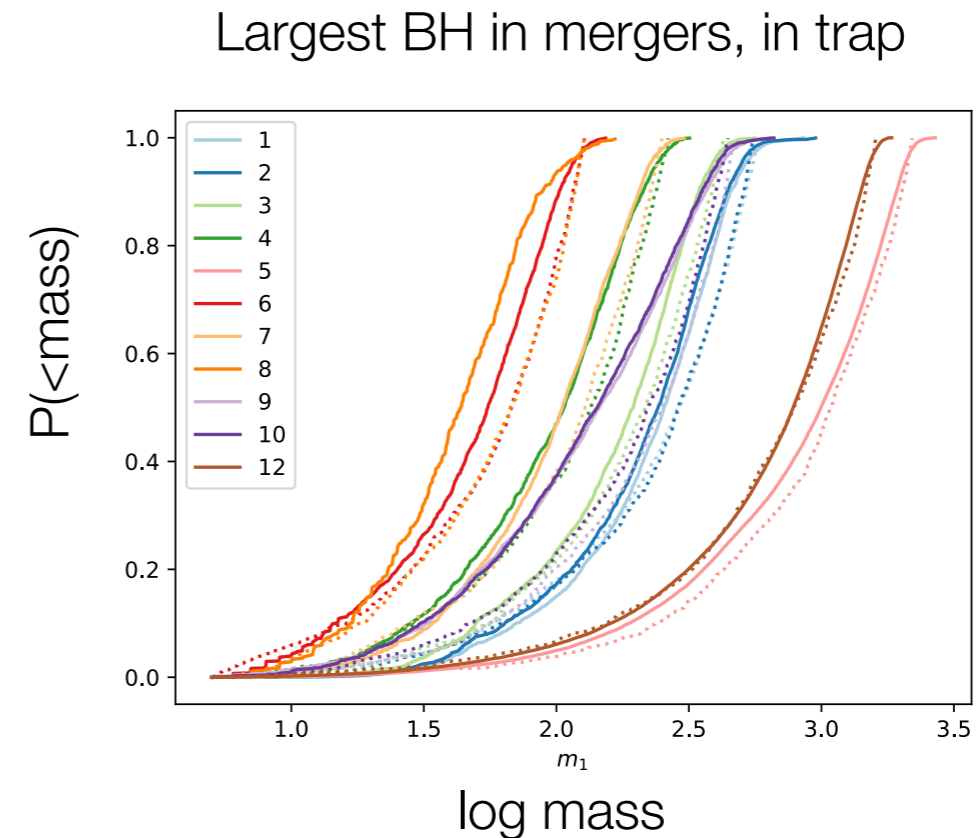
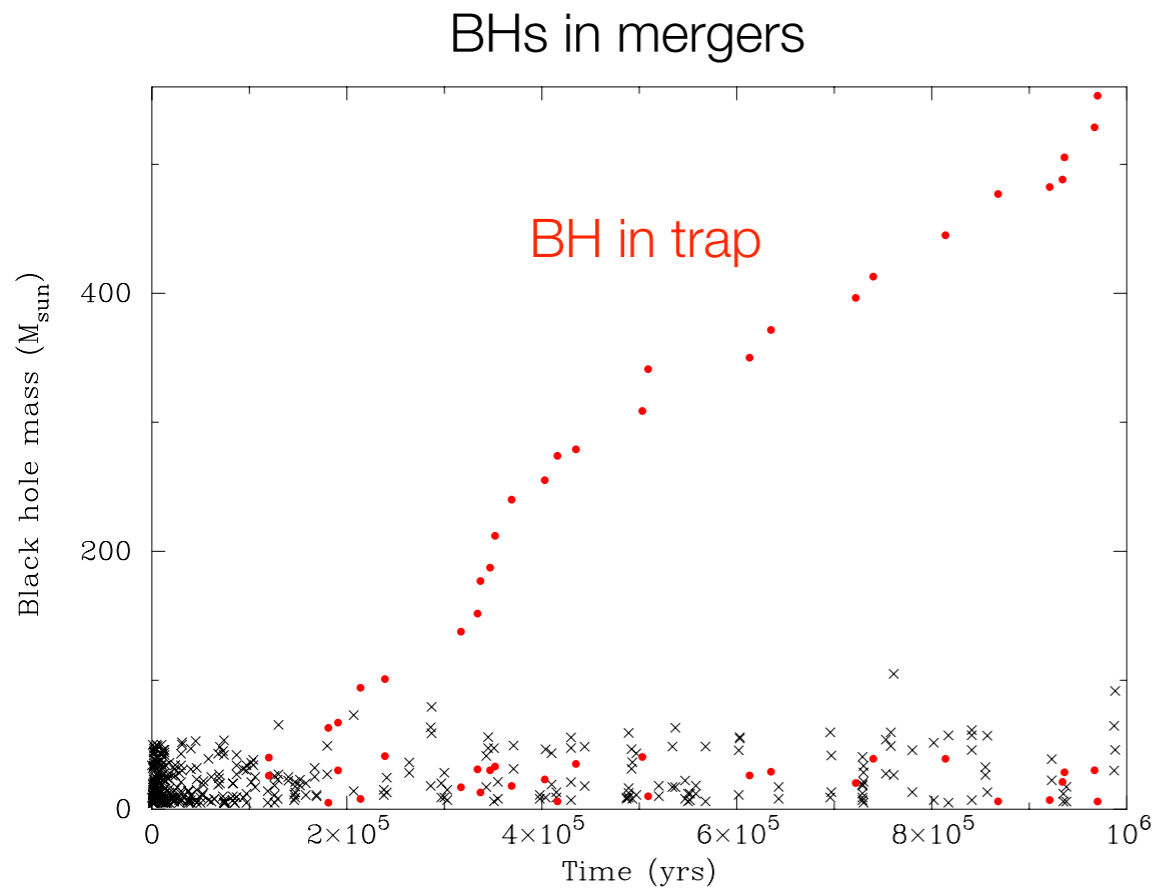
AGN disks: making high mass & high-q binaries

- Many BHs near galactic nucleus
- During active phase, disk can capture them ... brief but **efficient**
- BHs migrate through the disk
 - Bigger go faster
 - “Migration trap” $\sim 100 M$: balanced torques Bellovary et al 2016



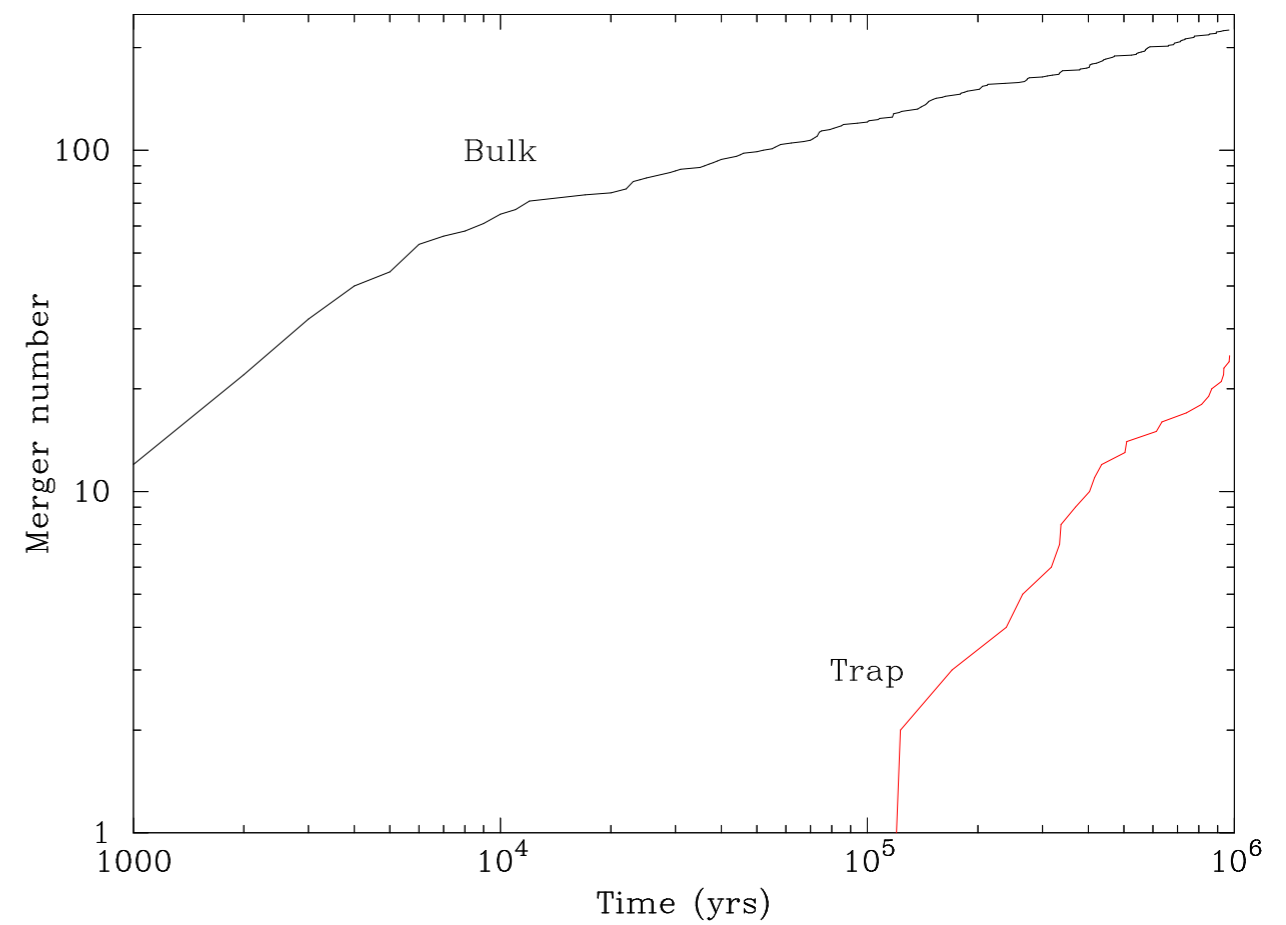
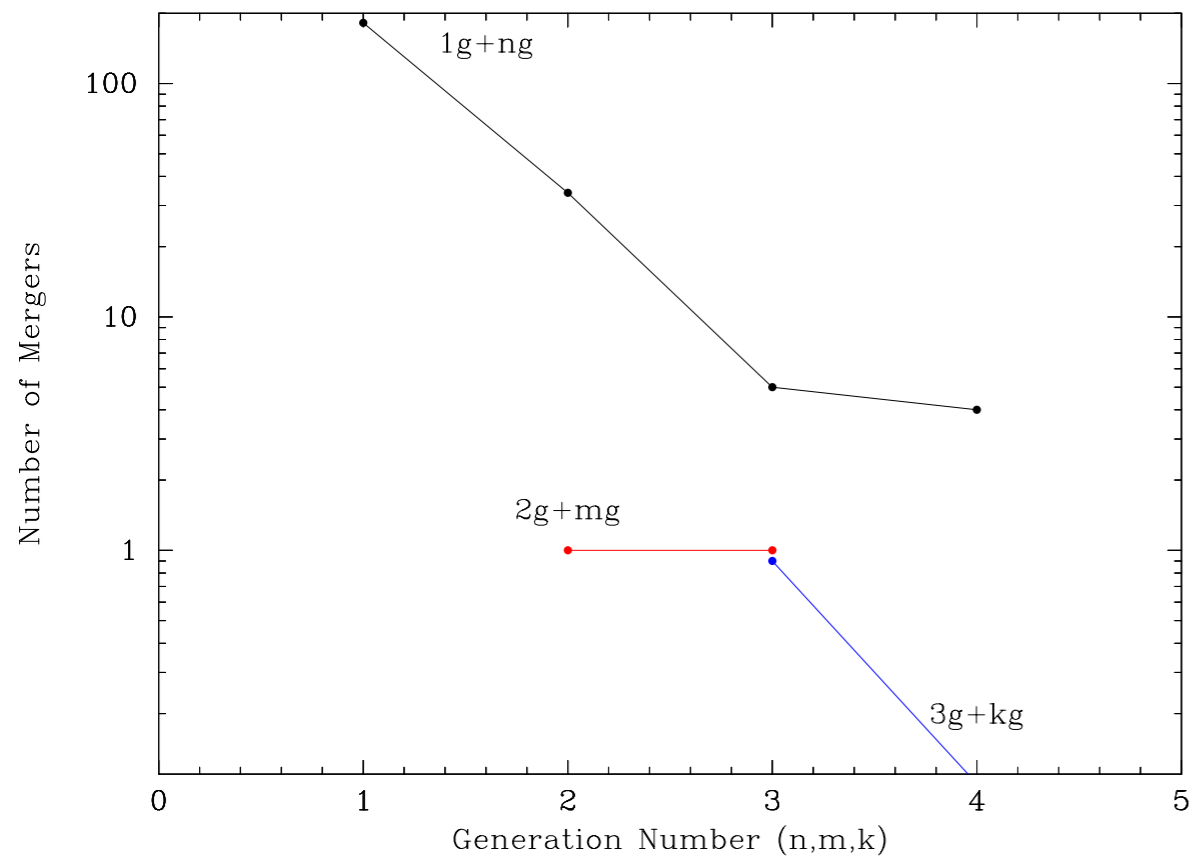
With migration and “grind-in” : high-q, high-M

- Simulate this a lot, see what masses/spins of BBHs form, how often, & why
 - Two-component phenomenology (time-averaged): “trap” and bulk
 - Trap: Builds up $\sim \mathbf{O(1)}$ IMBH at a time, linearly



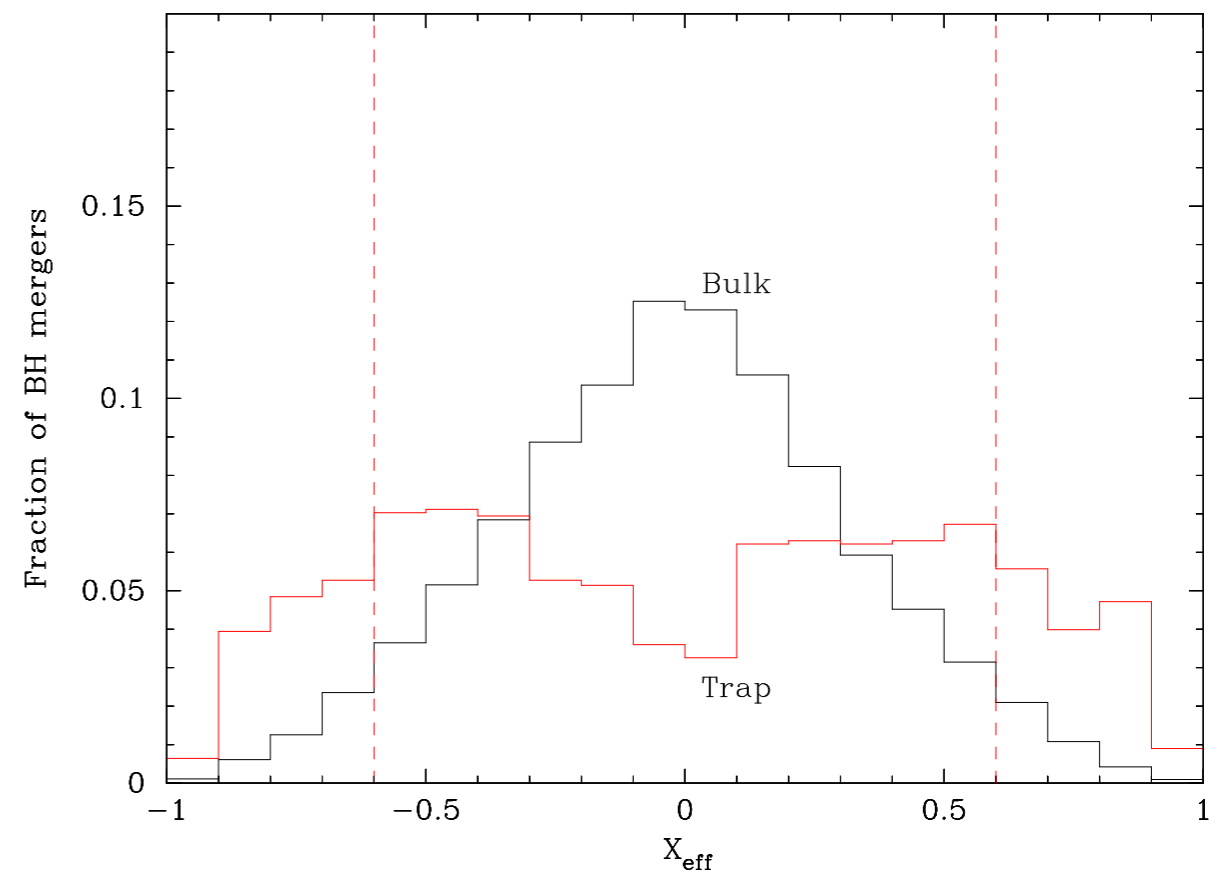
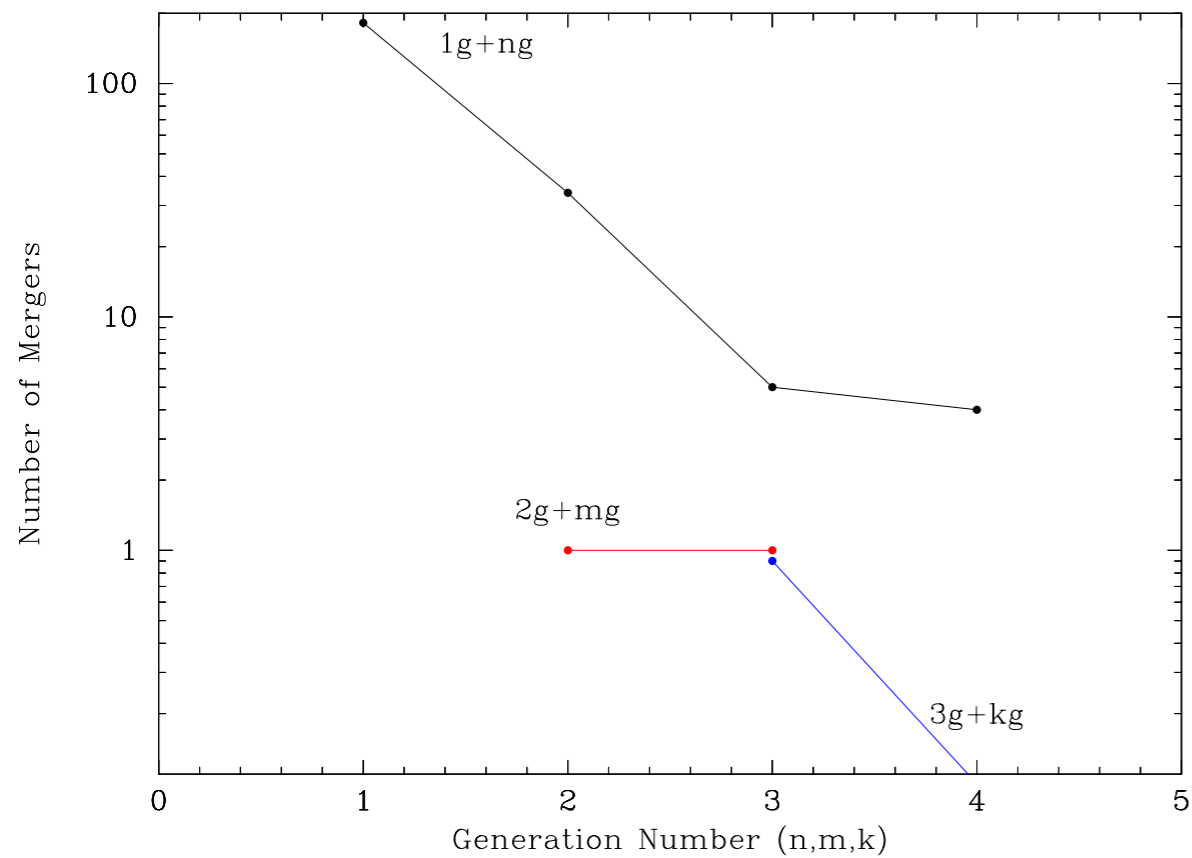
AGN disk growth of BHs

- Most mergers in “bulk”, similar to input population
 - Build up (hierarchical) IMBHs



AGN disk growth of BHs

- Most mergers in “bulk”, similar to input population
- Hierarchical spins (χ_{eff}) are bimodal



Some context: Rates?

- Examples of recent estimates: McKernan ApJ 2018; Stone et al 2017 MNRAS; Ford & McKernan 2019

- “AGN” volume density:

- Best estimate: Current galaxy/SMBH density $2 \times 10^{-5} M_{\odot} / \text{Mpc}^3$ mod lifetime/duty cycle: $\sim 10^{-3} \text{Mpc}^{-3}$
[X-ray bg (Cowie et al 2003, ...); X-ray selected AGN surveys; cosmo sims matching AGN LF (e.g., Hirschmann 2013)]. Rate vs redshift similar to SFR (/1000)

- Integrated disk masses: Very large — lazy estimate

$$\dot{M}_{\text{edd}} \tau_{\text{AGN}} \simeq 2 \times 10^6 M_{\odot} \frac{\tau}{10 \text{Myr}} \frac{M}{10^8 M_{\odot}}$$

- Expect many BHs formed in flow [e.g., Stone et al 2017] ...implies **lower limit** on BH merger rate
- Disk strongly impacts BH binary formation, evolution [migration, binaries]
- Many BHs near SMBH due to mass segregation / cusp [e.g., our GC $\sim 10^4$, review Amaro-Seoane et al 2007]
 - Accretion flow & stellar dynamics advect/segregate BHs into AGN disk
 - Must also get “ground” into disk plane [e.g., McKernan et al 2014 and refs therein]
 - Assume O(1000) BH initially, O(100/Myr) advected

Some context: Rates?

- Examples of recent estimates: McKernan *ApJ* 2018; Stone et al 2017 *MNRAS*; Ford & McKernan 2019

$$\mathcal{R} \simeq n_{gn} \frac{(N_{bh} f_d) f_{AGN} f_b}{\tau_{AGN}}$$
$$\simeq 10^3 \frac{N_{bh} f_d}{10^4} \frac{10 Myr}{\tau_{AGN}} f_{AGN} f_b$$

simplified version of McKernan 2018

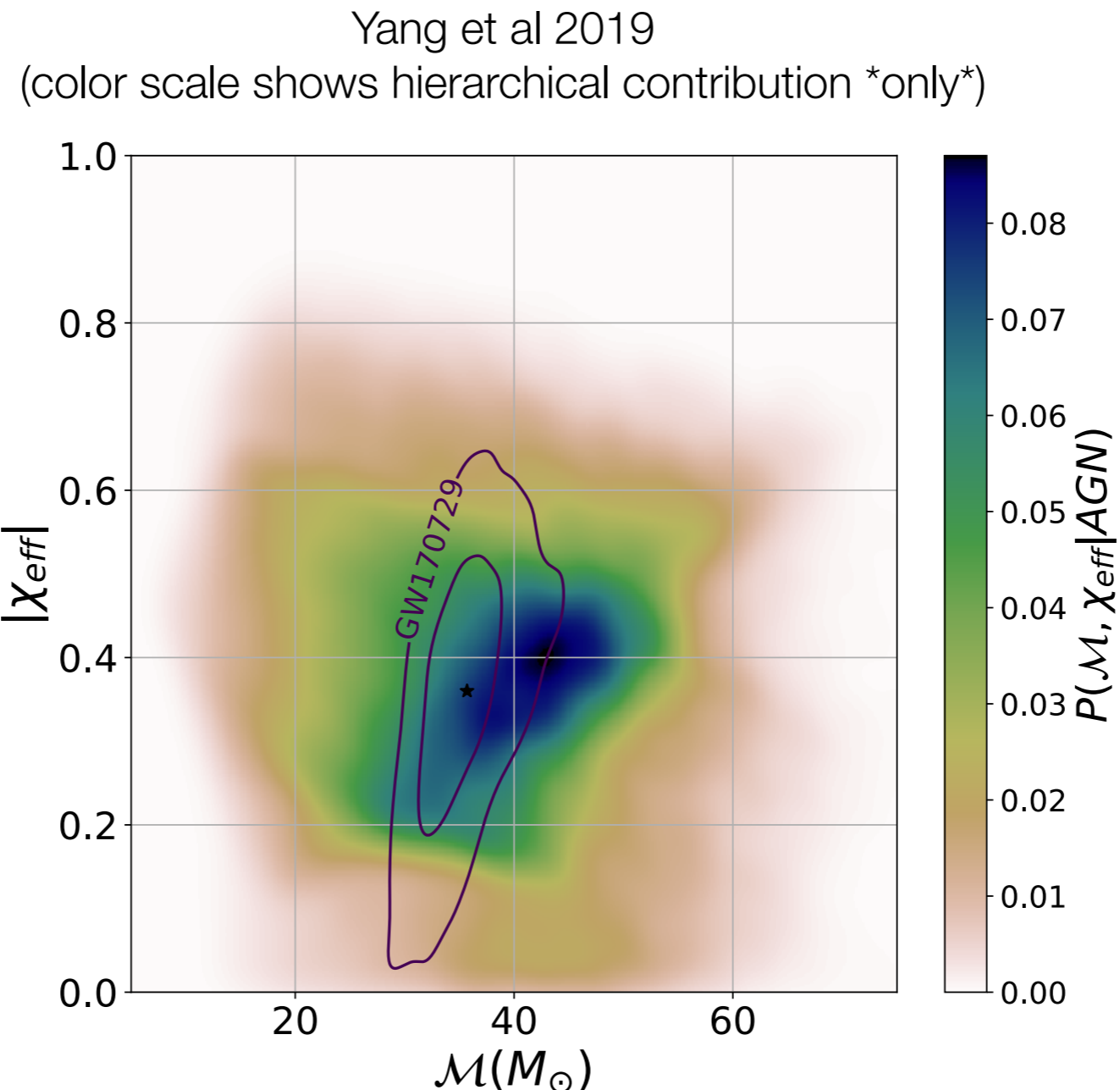
f_{AGN} fraction of GN that are merger sites

f_b fraction of BHs that form binaries (some left behind,...)

$N_{bh} f_b$ number of BH that enter disk

Comparing with observations?

- Consistent with spin, q for 170729, given a plausible seed population (BF ~ 1)
- Similarly: No compelling evidence favoring a hierarchical scenario in some earlier work (without, with HM : Kimball et al arxiv:1903.07813 [Chatziouannou et al 1903.06742](#))



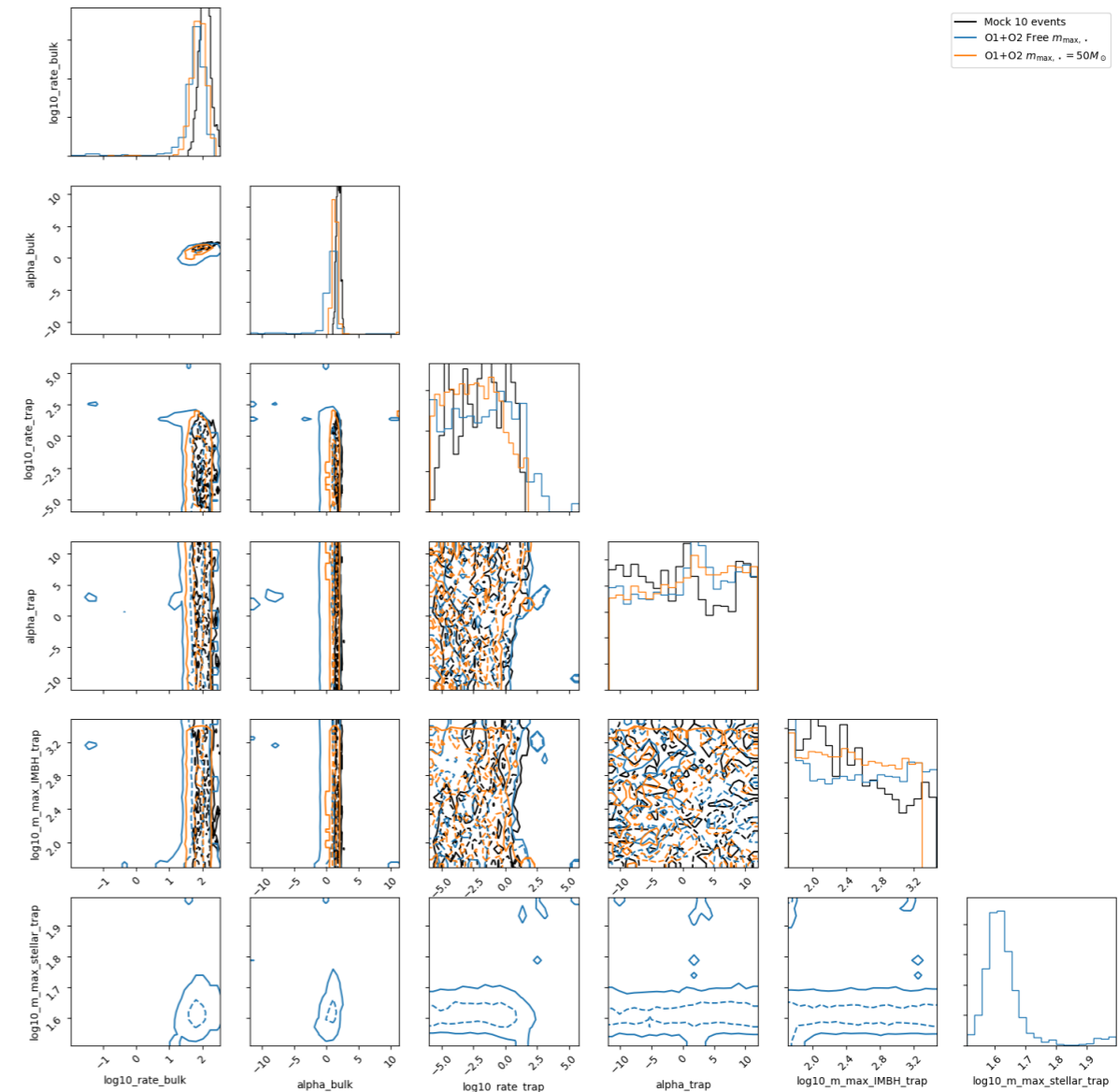
Comparing with observations?

- AGN constraints are **already interesting**

- Limits parameter space of possible AGN
e.g., Ford & McKernan 2019

- Example: Merger rate limits from AGN disk model (real data & simulated O3, assuming no “trap” signatures)

Model	R_{trap}	α_{trap}	R_{bulk}	α_{bulk}
Fixed	0.00	10.82	-10.56	10.92
Free	0.00	161.14	-10.72	10.84



Bonus slides

- Run parameter table

Run	N_{BH}	N_{gr} (/Myr)	γ	M_{Lower} (M_{\odot})	M_{Upper} (M_{\odot})	τ_{AGN} (Myr)	a	trap (r_{g})	disk	t_{-}/t_{+}
R1	869	10^2	1	5	50	1	u	$700r_{\text{g}}$	SG	5
R2	869	10^2	1	5	50	1	u	$700r_{\text{g}}$	SG	1
R3	100	10^2	1	5	50	1	u	$700r_{\text{g}}$	SG	5
R4	851	10^2	2	5	50	1	u	$700r_{\text{g}}$	SG	5
R5	851	10^2	2	5	50	5	u	$700r_{\text{g}}$	SG	5
R6	851	10^2	2	5	15	1	u	$700r_{\text{g}}$	SG	5
R7	851	10^2	2	5	50	1	(1-a)	$700r_{\text{g}}$	SG	5
R8	851	0	2	5	50	1	u	$700r_{\text{g}}$	SG	5
R9	851	0	2	5	50	5	u	$700r_{\text{g}}$	SG	5
R10	851	0	2	5	50	5	u	$700r_{\text{g}}$	SG	1
R11	851	10^2	2	5	50	1	u	none	SG	5
R12	851	10^2	2	5	50	1	u	$500r_{\text{g}}$	TQM	5