# Absorbing bosonic dark matter with periodic dielectrics

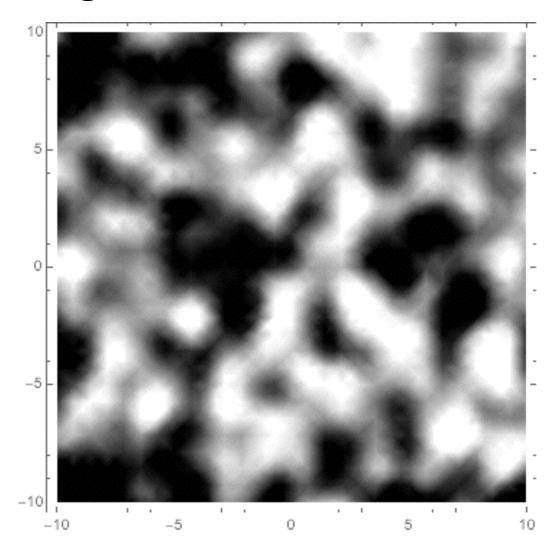
Robert Lasenby, Perimeter Institute KITP, April 5, 2018

## Light bosonic dark matter

- Dark matter mass could be anywhere within  $\sim$  50 orders of magnitude, from  $10^{-22}\,\mathrm{eV}$  to Planck scale
- For masses  $\lesssim 100\,\mathrm{eV}$ , DM must be bosonic (Pauli exclusion), and must be produced non-thermally
- Many such DM candidates, and early-universe production mechanisms, in BSM theories:
  - Axions, hidden photons, light moduli ...
  - Purely gravitational production during inflation, production during phase transitions, ...
- Direct detection experiments very different to WIMPs

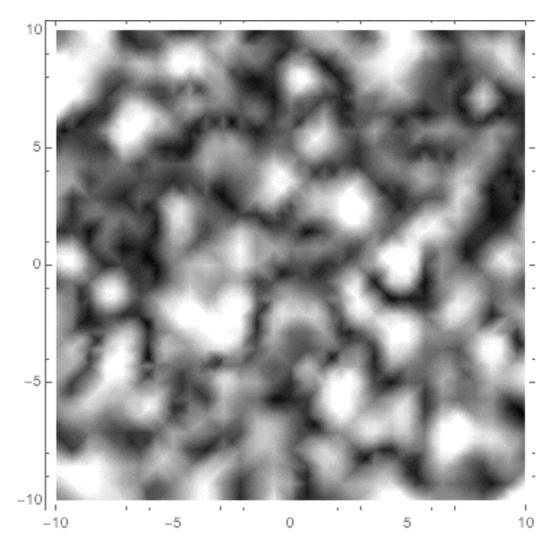
#### Bosonic dark matter fields

- Bosonic DM expected to be coherent, classical-like oscillations of field
- Virialized velocity distribution within galaxies,  $v \sim 10^{-3}$ 
  - Approximately Gaussian random field, with coherence length  $\sim (mv)^{-1}$ , coherence time  $\sim (mv)^{-2}$

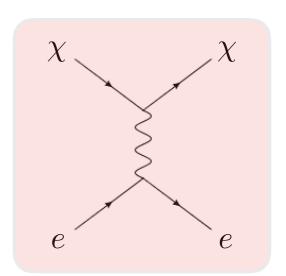


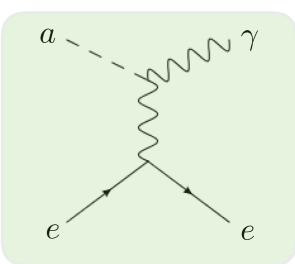
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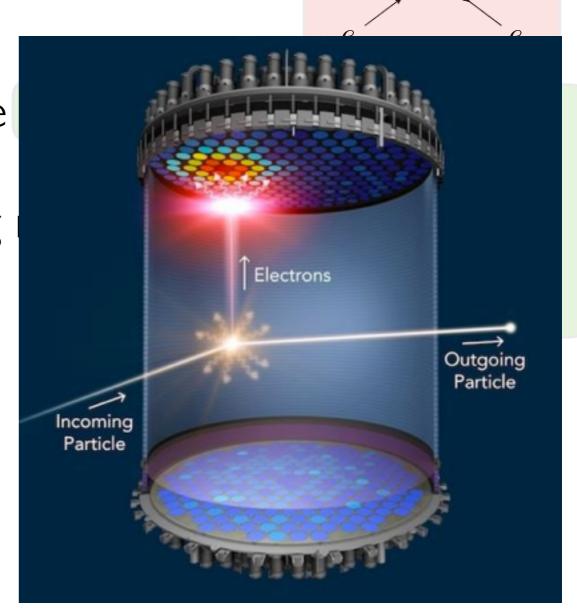
- Detect heavy and/or fermionic DM through scattering
- Many light DM candidates can be absorbed
- Convert whole energy (including rest mass)
   of DM, versus just kinetic energy
- Existing experiments:
   ADMX for axions,
   Xenon for dark photons, ...





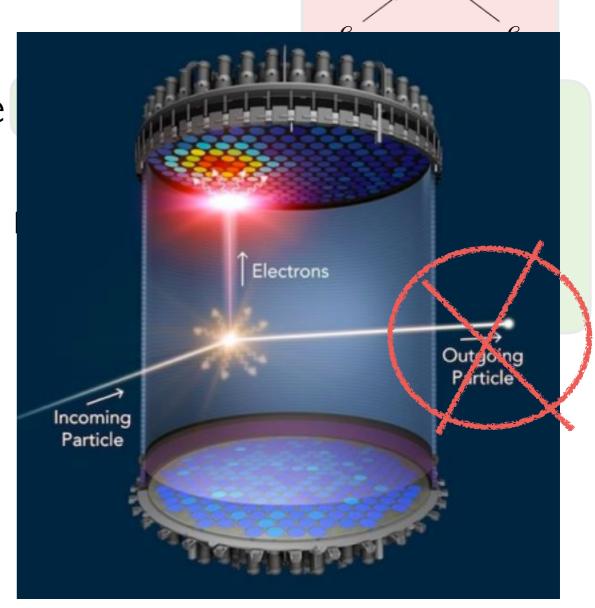
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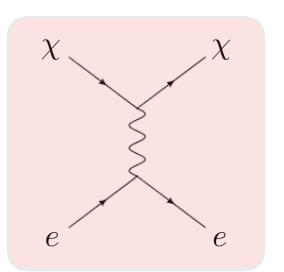


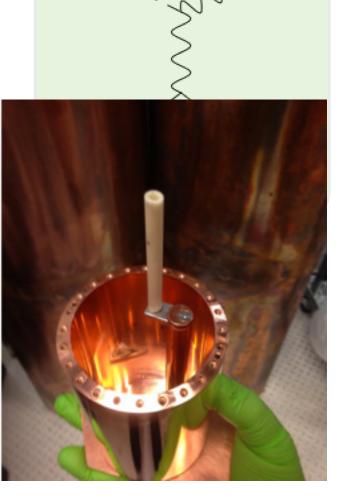
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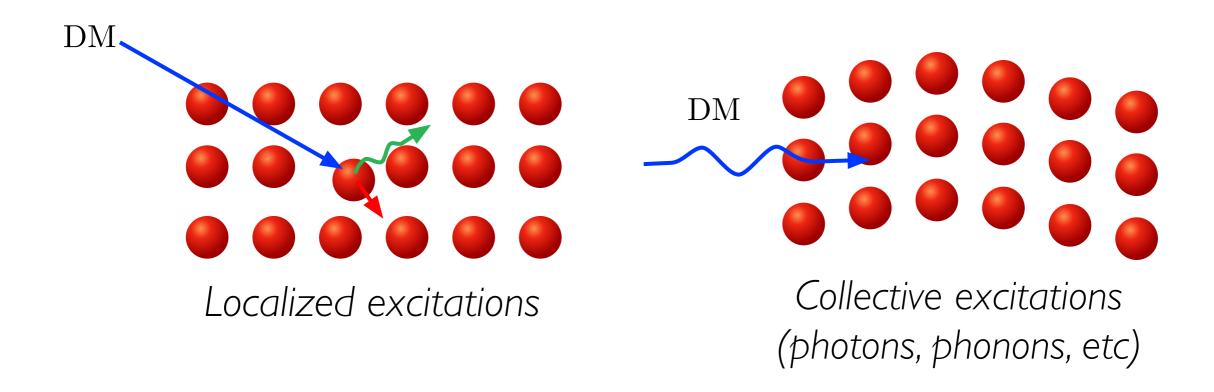
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## Coherent absorption

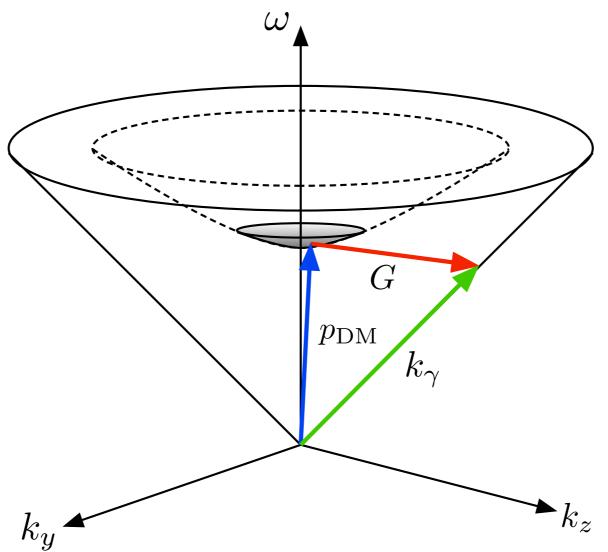
Incoherent vs coherent absorption:



 Coherent absorption can take advantage of large target volume, while still absorbing into specific modes

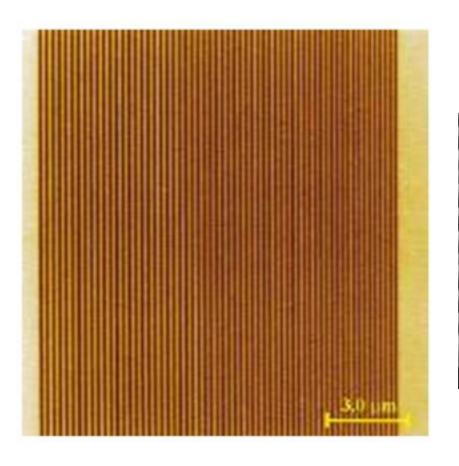
## Coherent absorption

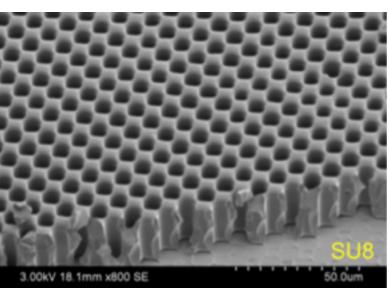
- · Photons often a good signal easily manipulated and detected
- In large target, photons are relativistic momentum mismatch with DM:



#### Photonic materials

Materials with periodic optical properties

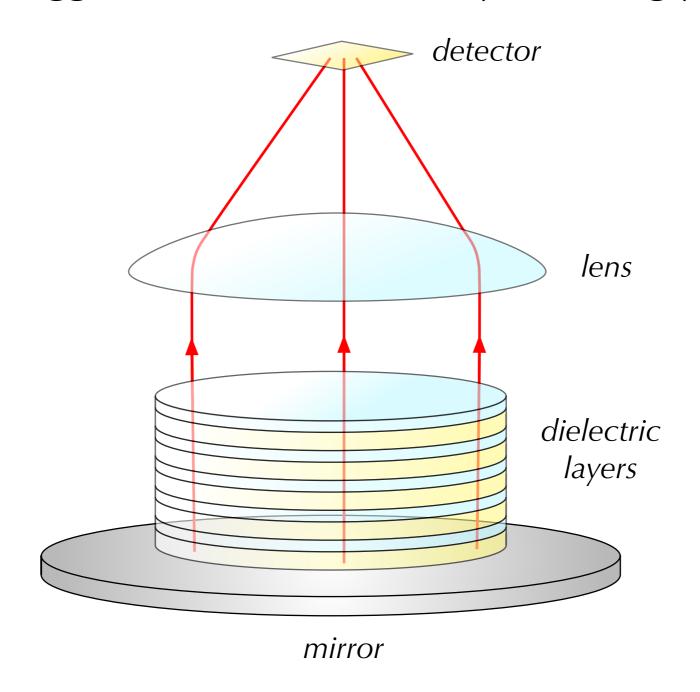






## Dielectric haloscopes

• DM can Bragg-convert in medium, producing photons:



## Axion conversion

Axion-photon coupling

$$\mathcal{L} \supset \frac{1}{2} (\partial_{\mu} a)^{2} - \frac{1}{2} m^{2} a^{2} - \frac{1}{4} g a F_{\mu\nu} \tilde{F}^{\mu\nu}$$

$$= \frac{1}{2} (\partial_{\mu} a)^{2} - \frac{1}{2} m^{2} a^{2} + g a E \cdot B,$$

Modifies Maxwell equations to

$$\nabla \cdot E = \rho - g\nabla a \cdot B \qquad \qquad \nabla \times B = \partial_t E + J + g(\dot{a}B + \nabla a \times E)$$

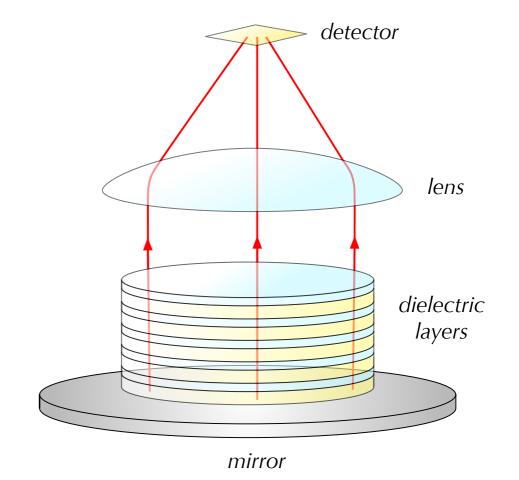
Instantaneous power transfer

$$P_{\mathrm{DM} \to \mathrm{SM}} \simeq \int dV \, E \cdot (g \dot{a} B)$$

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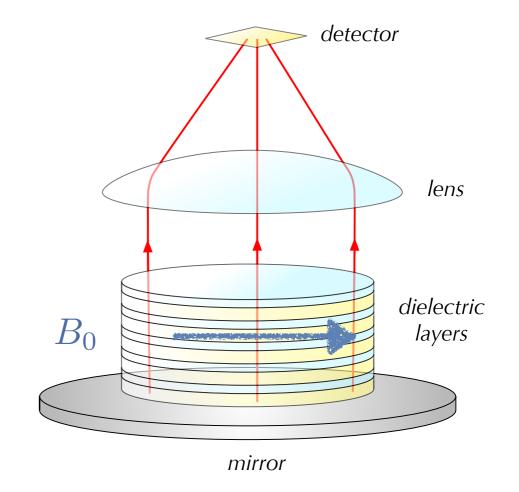
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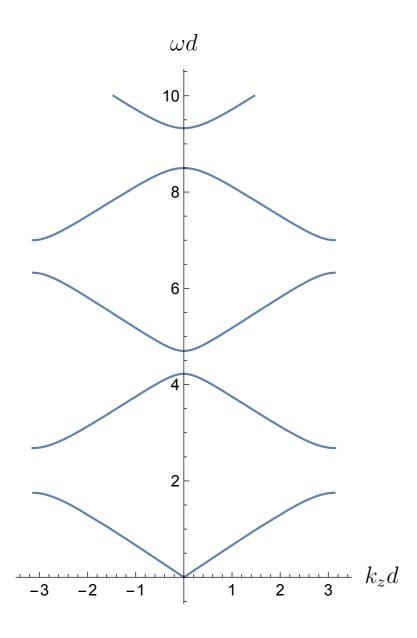
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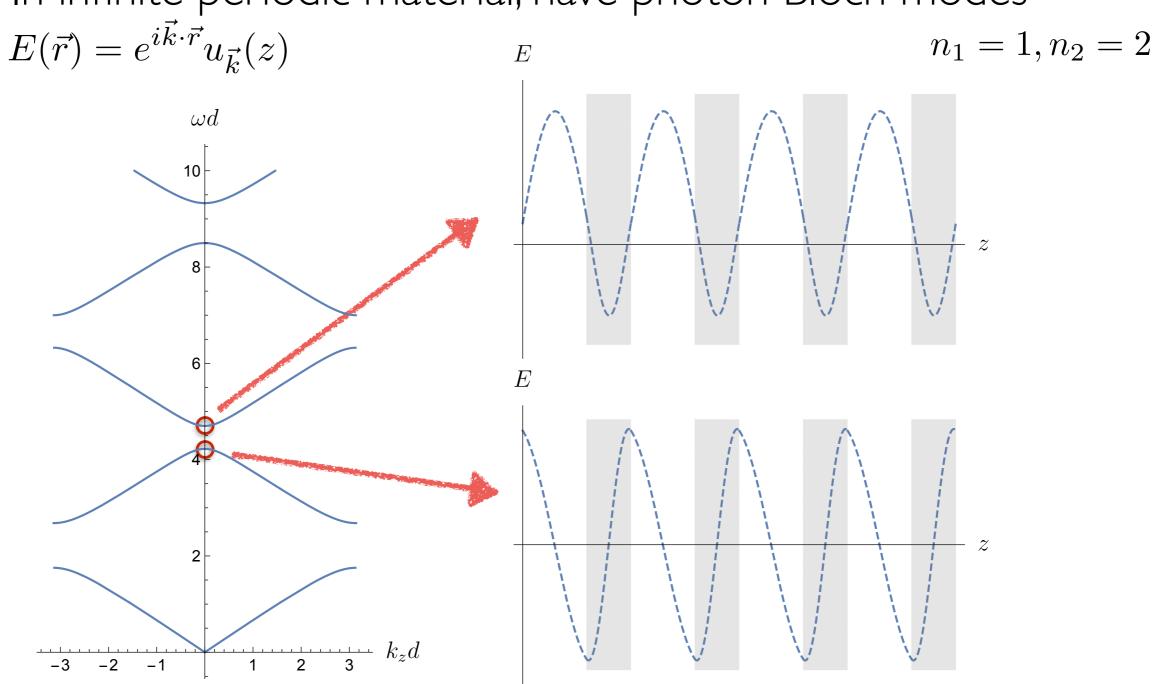
#### Photon modes

• In infinite periodic material, have photon Bloch modes  $E(\vec{r}) = e^{i\vec{k}\cdot\vec{r}}u_{\vec{k}}(z)$ 



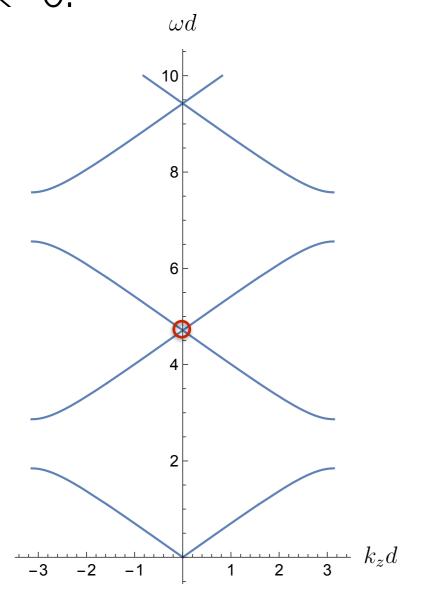
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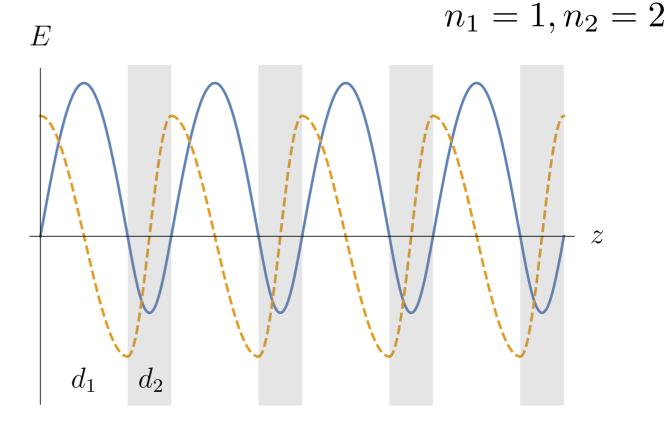
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#### Half-wave stack

• For equal phase depths,  $n_1d_1 = n_2d_2$ , have no bandgaps at k=0:



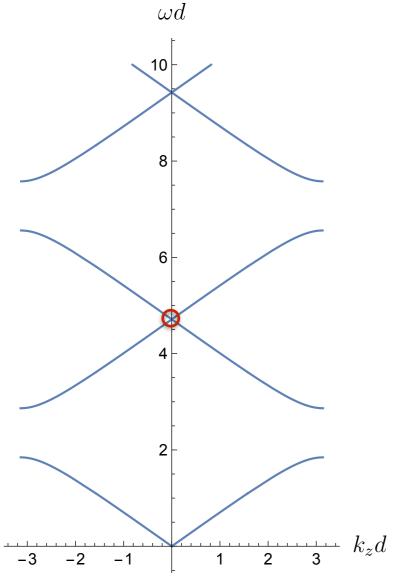


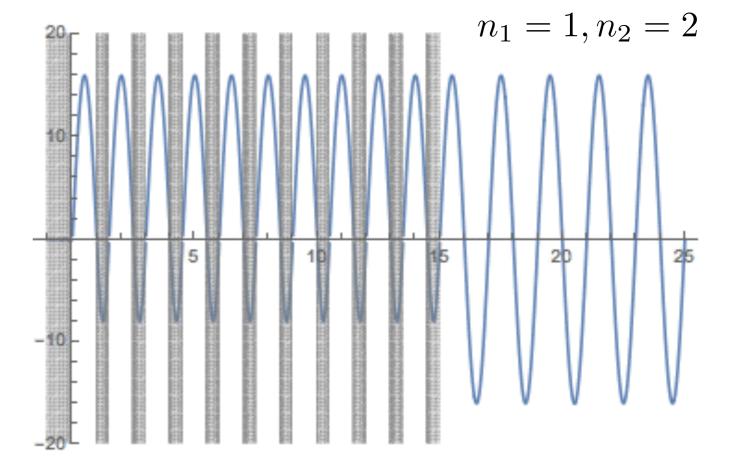
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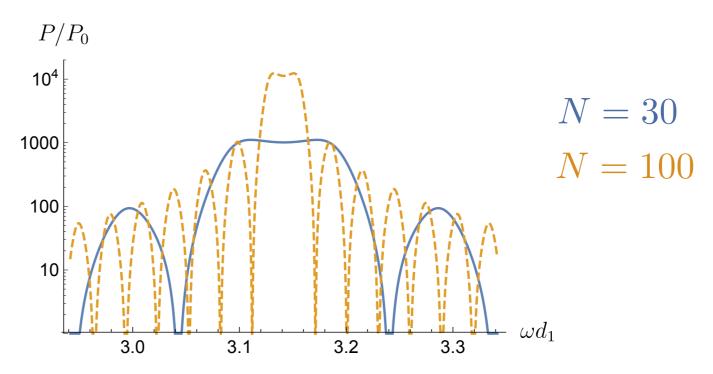
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## Converted power

• For stack of N periods, with area A, converted power from DM at halfwave frequency is

$$P_{\text{abs}} \simeq g^2 B_0^2 \frac{\rho_{\text{DM}}}{m^2} QAN \left(\frac{1}{n_1} + \frac{1}{n_2}\right) \left(\frac{1}{n_2} - \frac{1}{n_1}\right)^2$$

- For ''open cavity'',  $Q \propto N$
- Frequency coverage:



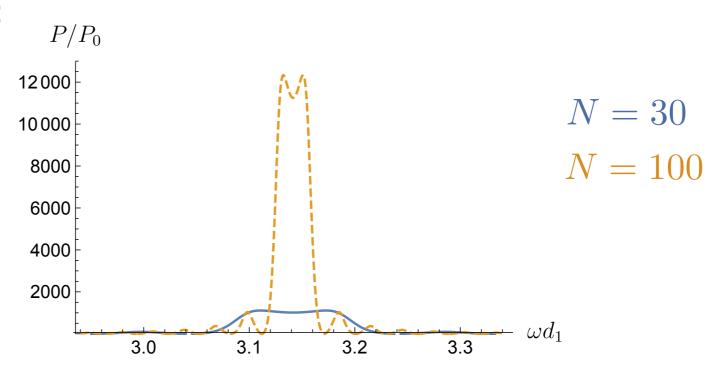
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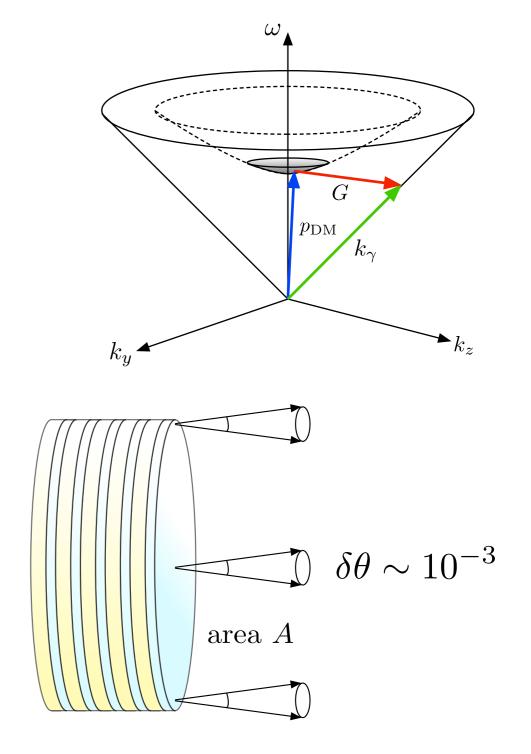


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## Collimated emission

 Material periodicity "donates" momentum in parallel direction, doesn't affect DM momentum in perpendicular directions

- Converted photons emitted in narrow cone around layer normal, opening angle  $\sim v^{-1} \sim 10^{-3}$
- Allows focussing down to area  $\sim 10^{-6} A$



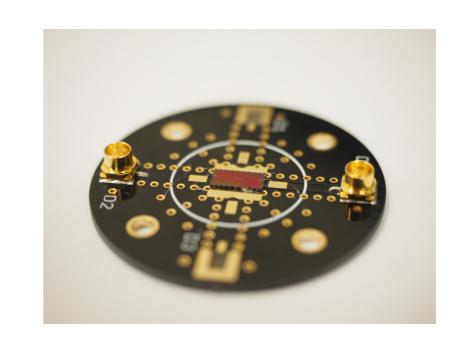
## Optical-frequency absorption

- Analogous scheme proposed at microwave frequencies: MADMAX experiment
- At higher frequencies, photon detection becomes much harder ...
- until we reach near-IR/optical frequencies!
- Experimental challenges:
  - low noise photon detection
  - background suppression (thermal, radioactive, cosmic)
  - fabrication and scanning



#### Photon detection

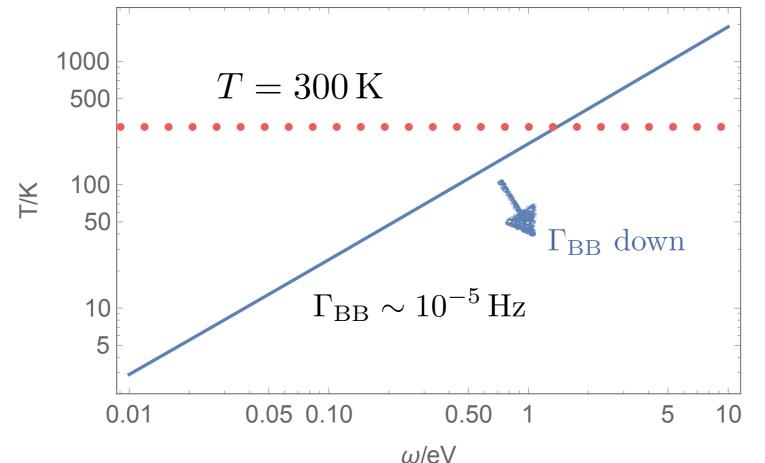
- Collimated emission means that emitted photons can be focused down to area  $\sim 10^{-6}$  of layers' area
  - e.g.  $(100 \, \mu \mathrm{m})^2$  detector for  $(10 \, \mathrm{cm})^2$  layers
- Enables use of small, low-noise detectors
  - Widely-available: PMT, CCD DCR  $\sim 10^{-3}\,\mathrm{Hz}$
  - Lower-noise superconducting detectors: TES, MKID, nanowires  $DCR < 10^{-5} \, Hz$



## Thermal backgrounds

• Blackbody photons: if detector's field of view is at temperature T, number of blackbody photons hitting detector is

$$\Gamma_{\rm BB} \sim \frac{\Delta\omega \,\omega^2}{4\pi^2} A_{\rm det} e^{-\omega/T}$$



$$A_{\rm det} = (100 \, \mu \rm m)^2$$

## Radioactivity / cosmic rays

- Materials of target, shielding, detector etc will contain some radioactive isotopes; unpurified materials could result in  $\sim 100~{\rm decays}~/~{\rm sec}$
- Cosmic ray muons: flux  $\sim 1/(10\,{\rm cm^2\,sec})$ , each deposits energy in target  $\sim 1-100\,{\rm keV}$
- All of these events much more energetic than signal photons, and unless they shower into very many particles, unlikely to hit small detector
- Characterise these backgrounds: active veto / purification / shielding if necessary

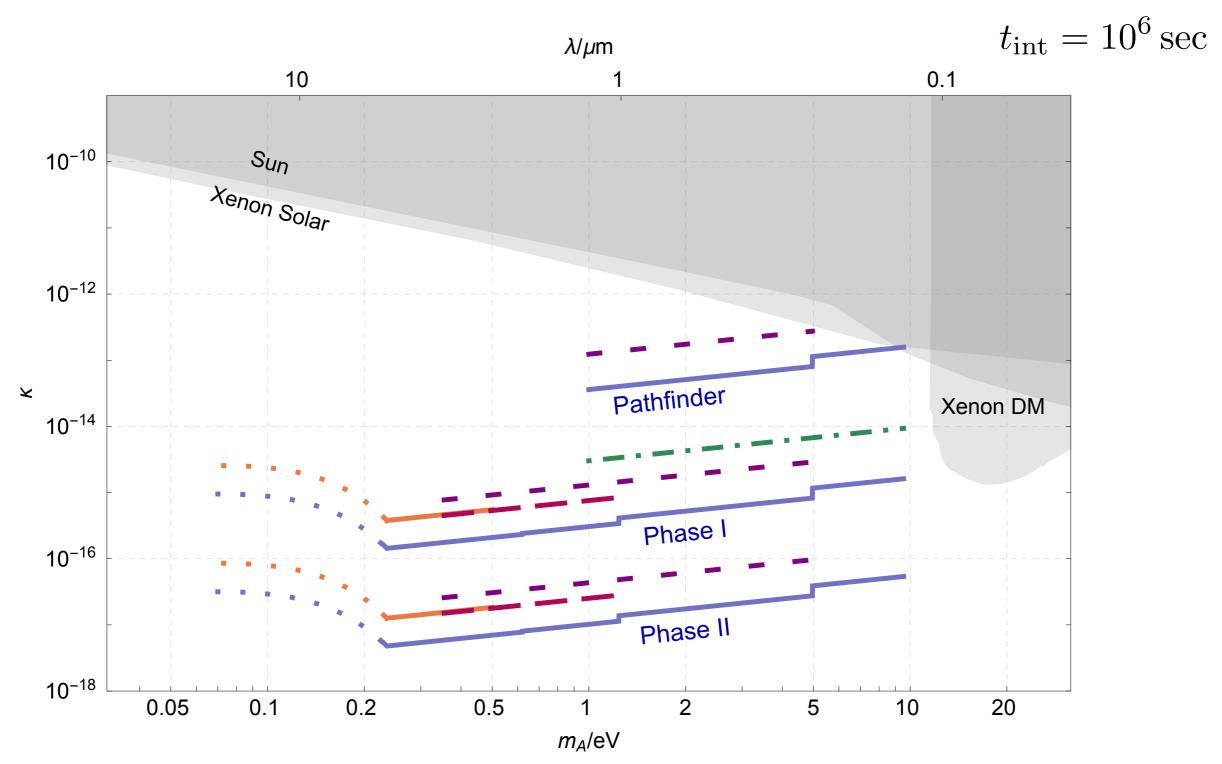
## Dark photon conversion

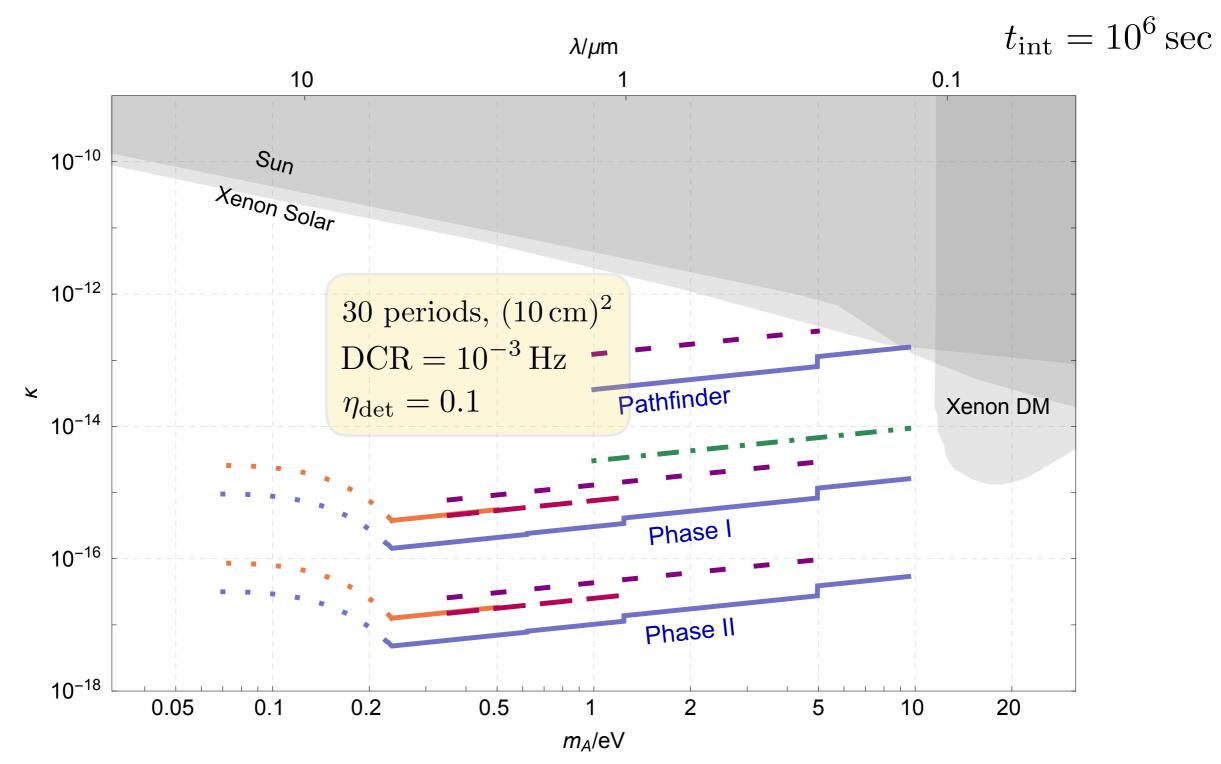
Simplest form of spin-I DM interaction is coupling to EM current:

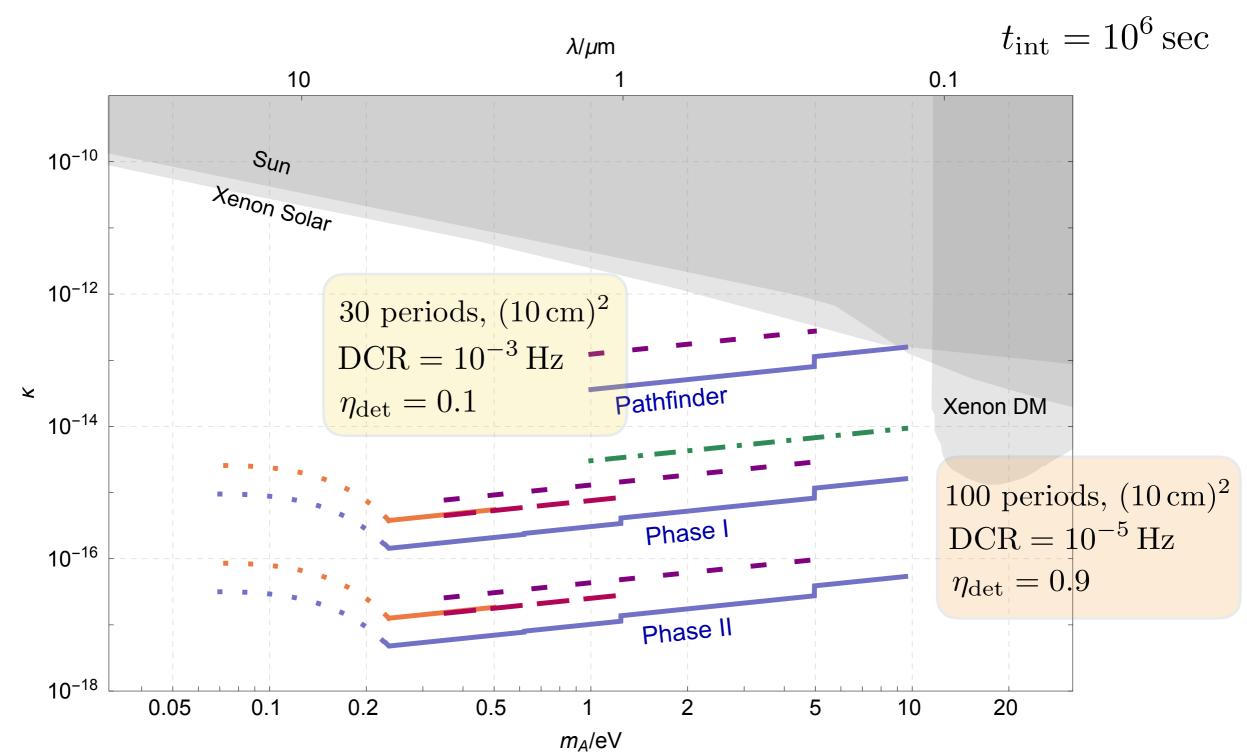
$$\mathcal{L} \supset -\frac{1}{4} F_{\mu\nu} F^{\mu\nu} - \frac{1}{4} F'_{\mu\nu} F'^{\mu\nu} + \frac{1}{2} m^2 A'^2 + J_{\text{EM}} (A + \kappa A')$$

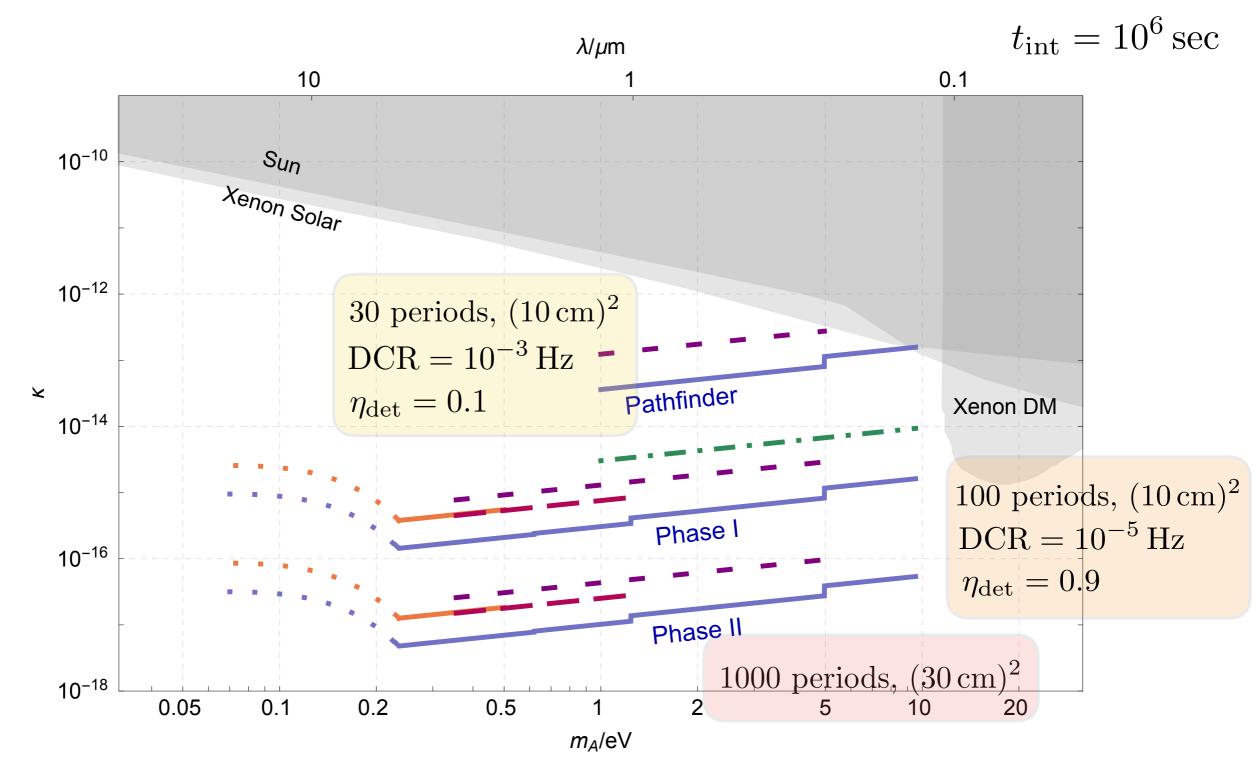
- Also least constrained by current experiments, because of mixing with photon
- Non-relativistic dark photon DM oscillation acts like effective current density,  $J_{A'} \simeq \kappa m \partial_t A'$
- Comparing to "axion current"  $J_a \simeq g\dot{a}B_0$ , dark photons convert to photons in dielectric layers, even without magnetic field

$$P_{\text{abs}} \simeq \frac{2}{3} \kappa^2 m \rho_{\text{DM}} QAN \left( \frac{1}{n_1} + \frac{1}{n_2} \right) \left( \frac{1}{n_2} - \frac{1}{n_1} \right)^2$$

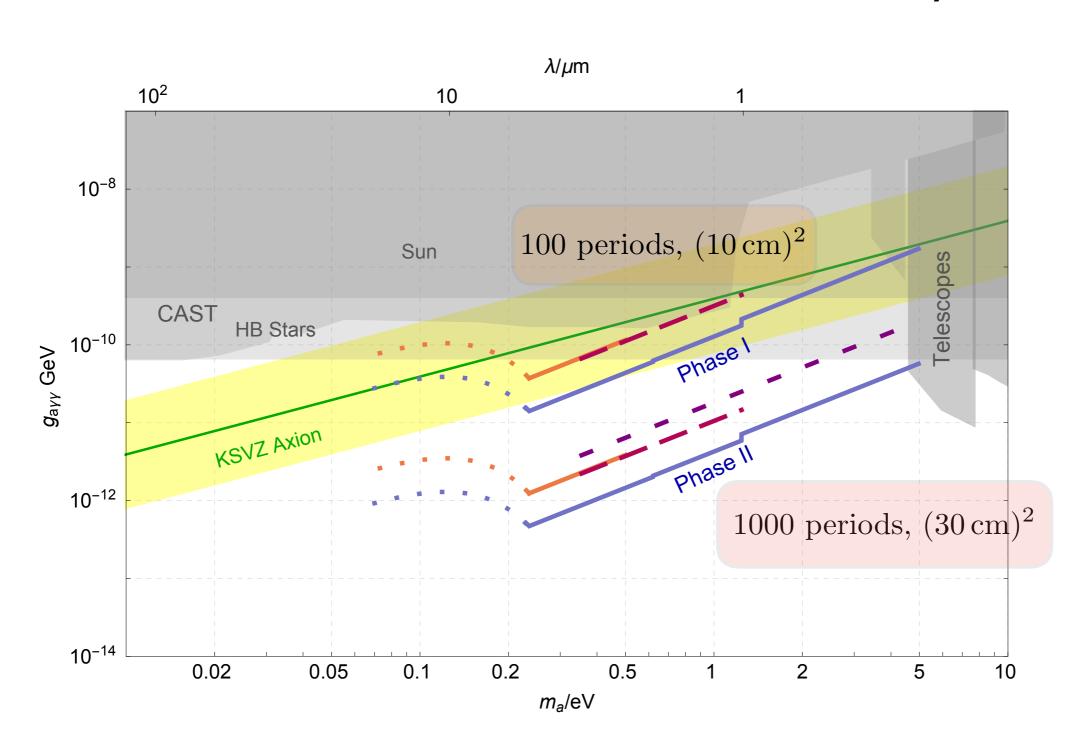








## Axion sensitivity



$$t_{\rm int} = 10^6 \, {\rm sec}$$

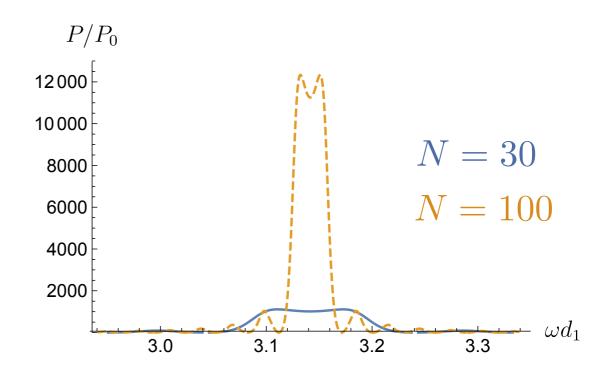
$$B_0 = 10 \,\mathrm{T}$$

$$DCR = 10^{-5} \, Hz$$

$$\eta_{\rm det} = 0.9$$

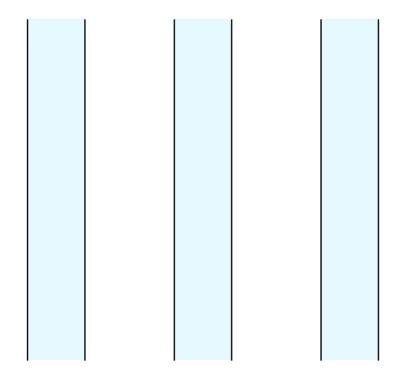
## Scanning

- For half-wave stack,  $P_{\rm abs} \propto N^2$  but bandwidth  $\delta \omega/\omega \sim 1/N$
- Increasing conversion rate requires more layers, but this decreases the mass range covered by a given stack
- What happens for other configurations?



# Frequency-averaged power

• Imagine short "pulse" a(t) of DM field



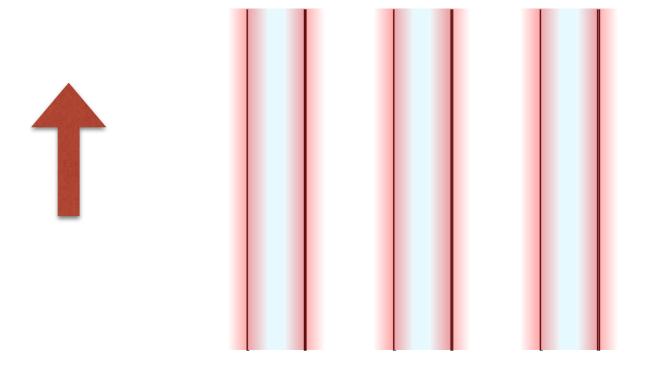
· In general, frequency-averaged power converted is

$$P_{\text{av}} \simeq (ga_0B_0)^2 A \sum_i \left(\frac{1}{n_1} + \frac{1}{n_2}\right) \left(\frac{1}{n_2} - \frac{1}{n_1}\right)^2$$

independent of layer thicknesses and spacings!

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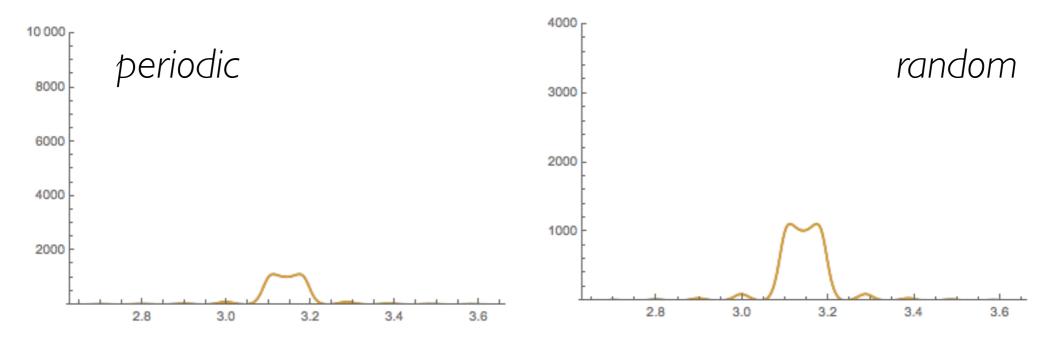
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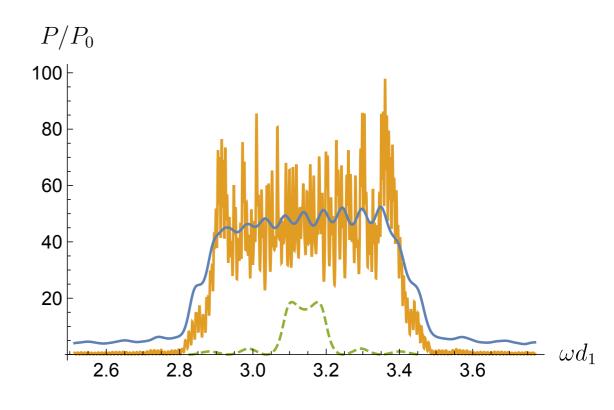
 Converted power as a function of frequency is strongly affected by structure:



- · For periodic layers, half-wave stack has broadest frequency profile
- To increase conversion rate, want more layers, but this tends to decrease bandwidth - need to scan somehow

## Scanning

- If experiment not background-free, signal-to-noise improved by scanning a narrow frequency profile
- At optical frequencies, backgrounds are low bigger issue is expense of fabricating different configurations
- Possibilities:
  - Altering refractive indices
  - Combining stacks of different periodicities



#### Other DM candidates

- To convert spin-0 DM to photons, target must provide "direction" to determine polarization of photon (otherwise rate suppressed by  $v_{\rm DM}^2\sim 10^{-6}$ )
- For  $aE \cdot B$  coupling, magnetic field provides polarization direction
- For other couplings, require directional materials (e.g. spin-polarized for axion-fermion couplings)
- Constraints from existing experiments generally tighter as well: longer-term prospects

## Summary

- Detection of bosonic DM at higher frequencies is an important gap in the experimental program
- Coherent absorption has attractive features; for absorption to photons, it requires wavelength-scale structure in the target
- Layered dielectrics are a simple way to absorb DM candidates with couplings to photons
- Pilot experimental proposals are being worked on!
- Extending downwards to lower frequencies?

## Extending to lower frequencies

- At energies below  $\sim 0.2\,\mathrm{eV}$ , single-photon detection becomes significantly more difficult
- Well-motivated parameter space
  - a generic QCD axion has  $m \lesssim 0.06\,\mathrm{eV}$  from SN1987a bounds
  - post-inflationary QCD axion DM at masses  $\gtrsim 10^{-5}\,\mathrm{eV}$
  - dark photons from higher-scale inflation,  $m \gtrsim 10^{-5} \, \mathrm{eV}$
- Bolometric detectors exist, with NEP  $\sim 10^{-20} \mathrm{W}/\sqrt{\mathrm{Hz}}$
- KSVZ axion gives converted power  $10^{-22}\,\rm W \simeq meV/sec$  from 1000 layers, of area  $(10\,\rm cm)^2$  , in a  $10\,\rm T$  magnetic field
- No known fundamental obstacles to improved superconducting detectors for this frequency range