# What determines the CD4:CD8 T cell ratio in the immune system ? Insights from genetic and mathematical modelling of thymocyte development

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# Cell of the immune system



# Maintaining homeostasis of the T cell compartment



# Maintaining homeostasis of the T cell compartment



How and why does the thymus make more CD4 than CD8 cells ?



Thymocyte selection - two purposes

# I. Tolerance - delete autoreactive T cells



Thymocyte selection - two purposes

# 2. CD4 vs CD8 lineage specification ensuring TCR-MHC restriction and lineage correlate





CD4 CD8 Double Negative

CD4 CD8 Double Positive



CD4 CD8 Double Negative

CD4 CD8 Double Positive



CD4 CD8 Double Negative

CD4 CD8 Double Positive



CD4 CD8 Double Negative

CD4 CD8 Double Positive



CD4 CD8 Double Negative

CD4 CD8 Double Positive



CD4 CD8 Double Positive

CD4 CD8 Double Negative



CD4 CD8 Double Negative

CD4 CD8 Double Positive



Positive and negative selection - goldilox models



## Lineage commitment - signals instruct fate

# **Kinetic**



# Quantitative instructive

CD4 SP CD4 SP CD4 SP CD4+CD8+ DP CD4+CD8+ DP Veak TCR signals CD8 SP CD8 SP CD8 SP

# Origin of CD4 biased selection

# Thymus



I. Instrinsic differences in Class I and Class II restricted precursors due to TCR repertoire generation 2. Differences in 'efficiency' of selection between CD4 and CD8 lineage cells

# Zap70 deficient mice blocked at double positive stage



MAP Kinases, NF<sub>K</sub>B, Calcium signalling



Role of Zap70 in positive selection :

Conditionally express Zap70

# Conditional Zap70 expression mouse model



huCD2 promotor reverse tetracyclin TransActivator

# Zap70<sup>Tre</sup> rtTA.C<sup>huCD2</sup> Zap70<sup>-/-</sup> Zap70<sup>Tet</sup> mice

# Conditional Zap70 expression mouse model



# Inducible T cell development



# Inducible T cell development



DP thymocytes :



SP thymocytes :



# Establishing precursor-product relationships



Measure relative recovery

MoFlo XDP

# Establishing precursor-product relationships - I

# DPI



# Establishing precursor-product relationships - II

d3

36

13

5.7

23

d4

30

7.1

12

25.

55

Capage &

82



# Temporal dynamics of positive selection



# Temporal regulation of thymic selection





# Mathematical description of development





**Population dynamics** 

$$\begin{aligned} \frac{\mathrm{d}x_1}{\mathrm{d}t} &= \lambda - (\delta_1 + \mu_{12})x_1[t] \\ \frac{\mathrm{d}x_2}{\mathrm{d}t} &= \mu_{12}x_1[t] - (\delta_2 + \mu_{23} + \mu_{24})x_2[t] \\ \frac{\mathrm{d}x_3}{\mathrm{d}t} &= \mu_{23}x_2[t] - (\delta_3 + \mu_{38})x_3[t] \\ \frac{\mathrm{d}y_4}{\mathrm{d}t} &= \mu_{24}x_2[t] - \nu_4 y_4[t] \\ \frac{\mathrm{d}y_8}{\mathrm{d}t} &= \mu_{38}x_3[t] - \nu_8 y_8[t] \end{aligned}$$

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# Generating timecourse data of Class I and Class II restricted T cell development



#### Control time course



#### Class I vs Class II resticted T cell development



# Use data to identify parameters of model

Log vs Lin transformed data

Assume SP plateau

#### Parameter estimations by minimising sum of squares residuals (Nelder-Mead algo in R)

MHC I knockout

Estimate

0.08

0.299

0.583

0.012

0.251

0.781

0.317

0.142

95% CI

(0.055, 0.106)

(0.116, 0.482)

(0.473, 0.692)

(-0.027, 0.051)

(0.214, 0.289)

(0.365, 1.197)

(-0.034, 0.669)

(0.058, 0.225)

Rag control

95% CI

27.503

(0.076, 0.106)

(0.234, 0.506)

(0.393, 0.575)

(-0.697, 1.207)

(0.218, 0.281)

(0.441, 0.866)

(-0.884, 1.171)

(0.132, 0.327)

(-3.289, 5.289)

Estimate

0.091

0.37

0.484

0.255

0.249

0.653

0.143

0.23

1

Parameter

λ

 $\mu_{12}$ 

 $\tilde{\mu_{23}}$ 

 $\tilde{\mu_{24}}$ 

 $\mu_{38}$  $\delta_1$ 

 $\delta_2$ 

 $\delta_3$ 

 $\nu 4$ 

 $\nu 8$ 



-O- b2m KO

🛨 Class II KO

					Rag-control	MHC I KO	MHC II KC
			Mean time spent in DP1 (days)	$\frac{1}{\mu_{12}+\delta_1}$	2.94	3.02	3.2
	MHC II knockout		Mean time spent in DP2	$\frac{1}{\mu_{23}+\mu_{24}+\delta_2}$	0.91	0.82	1.01
(2	Estimate 95% CI		Mean time spent in DP3	$\frac{1}{\mu_{38}+\delta_3}$	3.24	3.72	3.03
)	0.061	(0.043, 0.08)	Mean time spent in CD4SP	$\frac{1}{\nu_4}$	6.33	10.11	-
)	0.48 0.012	(0.196, 0.763) (-0.019, 0.043)	Fraction of DP1 that die	$\frac{\delta_1}{\mu_{12}+\delta_1}$	0.69	0.73	0.79
()	0.136	(-0.153, 0.424)	Fraction of DP1 recruited to DP2	$\frac{\mu 12}{\mu_{12}+\delta_1}$	0.31	0.27	0.21
)	0.251 0.792	(0.219, 0.283) (0.427, 1.158)	Fraction of DP2 that die	$\frac{\delta_2}{\mu_{23}+\mu_{24}+\delta_2}$	0.78	0.79	0.9
$\hat{\boldsymbol{y}}$	0.378	(-0.392, 1.149)	Fraction of DP2 recruited to DP3	$\frac{\mu^{23}}{\mu_{23}+\mu_{24}+\delta_2}$	0.1	0.07	0.09
)	- 0.1	- (-0.72, 0.92)	Fraction of DP2 recruited to CD4SP	$\frac{\mu 24}{\mu_{23} + \mu_{24} + \delta_2}$	0.13	0.14	0.003
			Fraction of DP3 that die	$\frac{\delta_3}{\mu_{38}+\delta_3}$	0.78	0.96	0.61
			Fraction of DP3 recruited to CD8SP	$\frac{\mu 38}{\mu_{38}+\delta_3}$	0.22	0.04	0.39

We assumed:

(i) the rate of input into the DP1 compartment of cells (cells/day) (from DNs) was the same in the WT, MHC I KO and MHC II KO mice

(ii) CD4 and CD8 cell numbers are at steady-state (or plateau) from day 7 onwards. We use this assumption to constrain our estimate for the rate of export from the SP compartments. All other parameters were completely free.

The 95% CI come from a bootstrap procedure: I create a new dataset by randomly re-sampling the observations (with replacement) and find new set of parameters to describe this resampled-dataset. I repeat this n=10<sup>4</sup> times. The 2.5 and 97.5 percentiles of the new parameters is used to determine the 95% confidence intervals.







#### **Thymic Develo**







# Cellular fate during development



# Testing for high death rate in DP2 thymocytes



MoFlo XDP



Distinct death rates amongst Class I and Class II restricted DP2s







 Death rate 8s = 0.88 

 Death rate 4s = 0.27 

 Survival 8s/survival 4s 

 Relative survival :  $e^{-0.88}/e^{-0.27} = 0.54$  

 1.73/3.14 = 0.55

# Using lineage specific death rates to quantify lineage efficiencies



# Modeling reveals unexpectedly high CD8 lineage biased death in selection



# Regulation of thymocyte survival



# "Paralogous" switch between BcI-2 and BcI-XI sensitises DP thymocytes to negative selection



Executioners







# Test the impact of apoptosis - introduce apoptotic stress to thymocytes



# Applying apoptotic stress preferentially kills CD8 lineage cells



# CD4:CD8 ratio only affected by Bax during DP2 stage



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> New York Andy Yates, Albert Einstein College of Medicine, NY, US

Thanks to ...

# TetZap70 development vs WT



# Establishing precursor-product relationships



Measure relative recovery

MoFlo XDP