

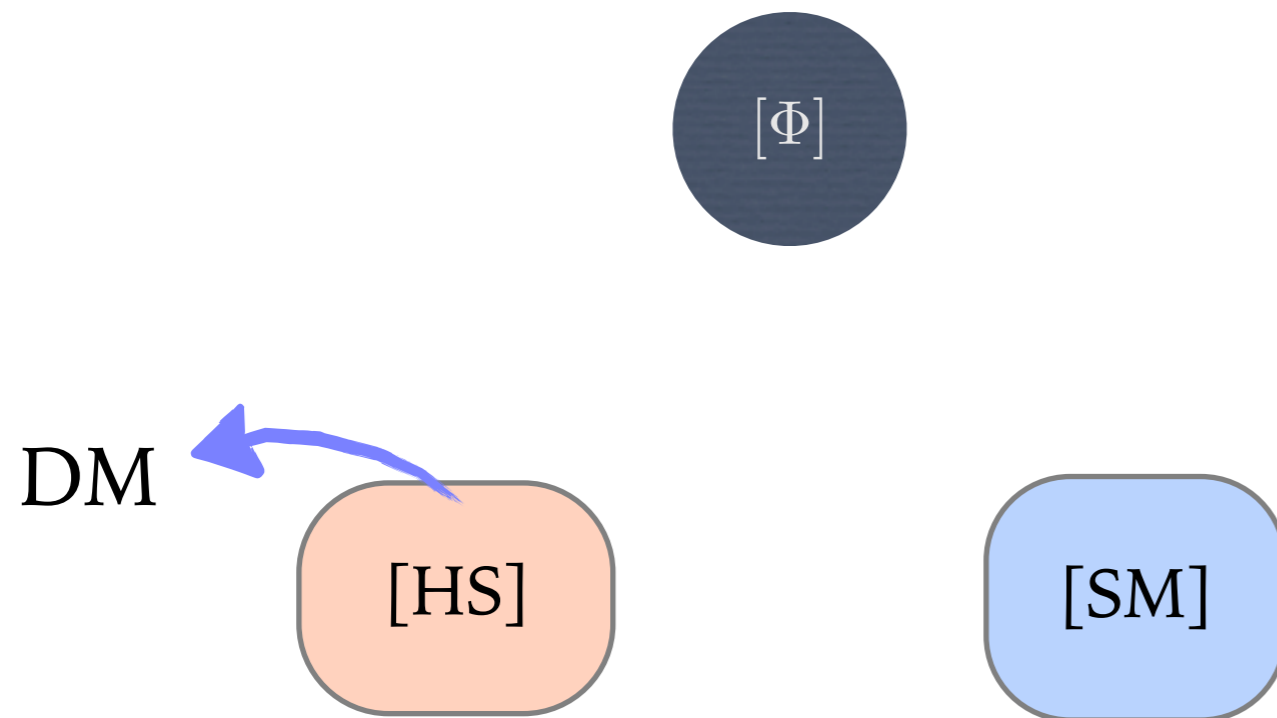


HIDDEN THERMAL HISTORIES

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UIUC

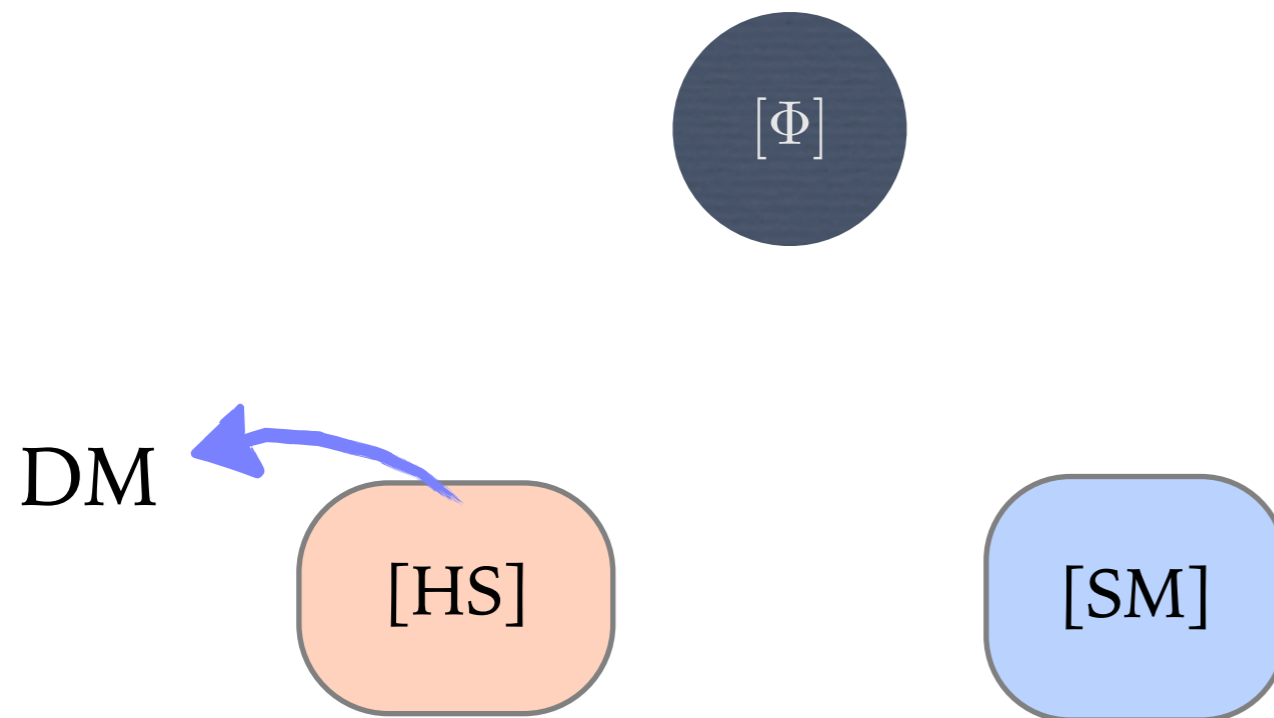
KITP Inflationary Reheating meets Particle Physics Frontier
February 4, 2020

DARK SECTORS



- Why dark sectors?
 - broad, generic class of models
 - many interesting signatures, both celestial and terrestrial

DARK SECTORS

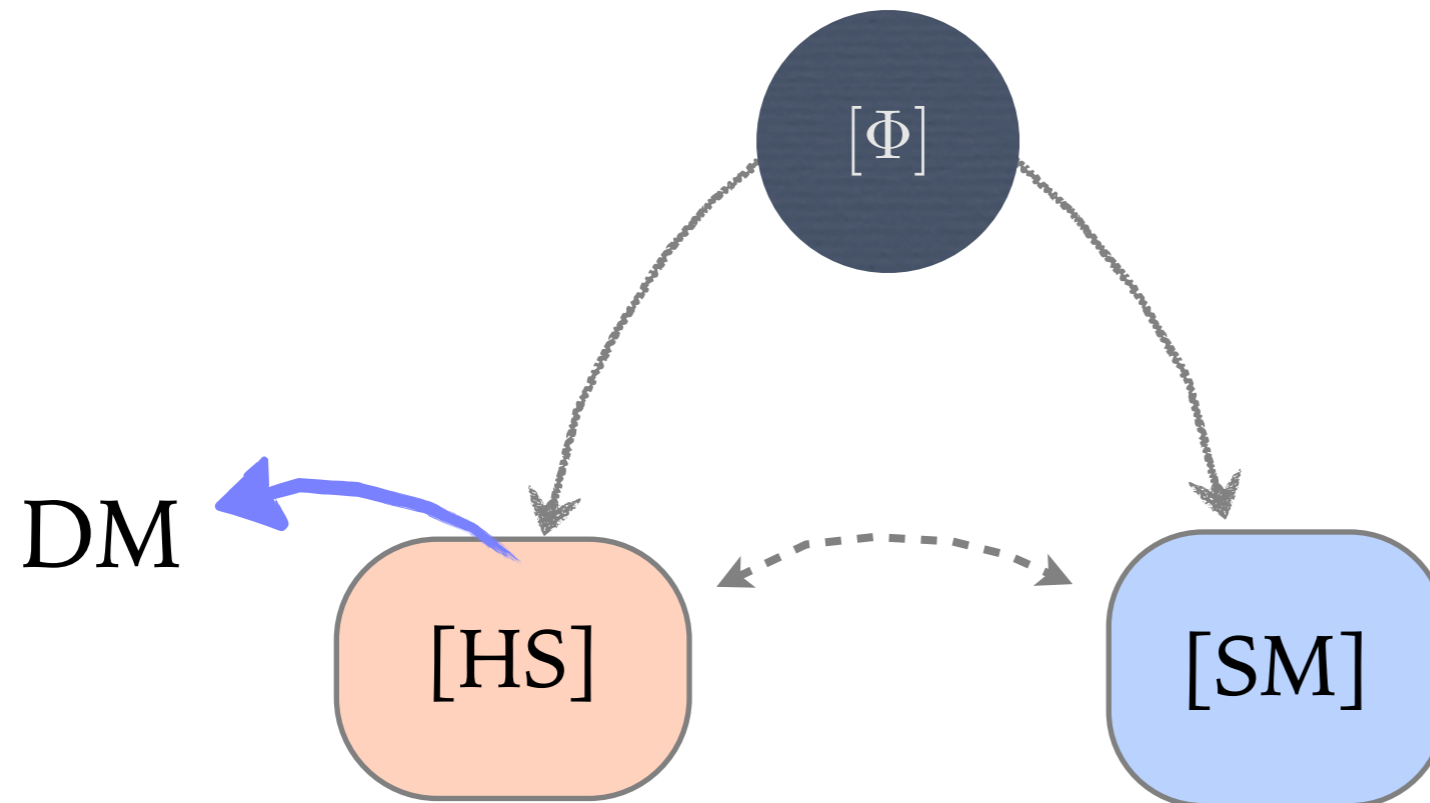


- Why dark sectors?
 - broad, generic class of models
 - many interesting signatures, both celestial and terrestrial

- Dark radiation baths contain a macroscopic amount of **stuff**: energy, entropy
 - must come from somewhere
 - must go somewhere

DARK SECTORS

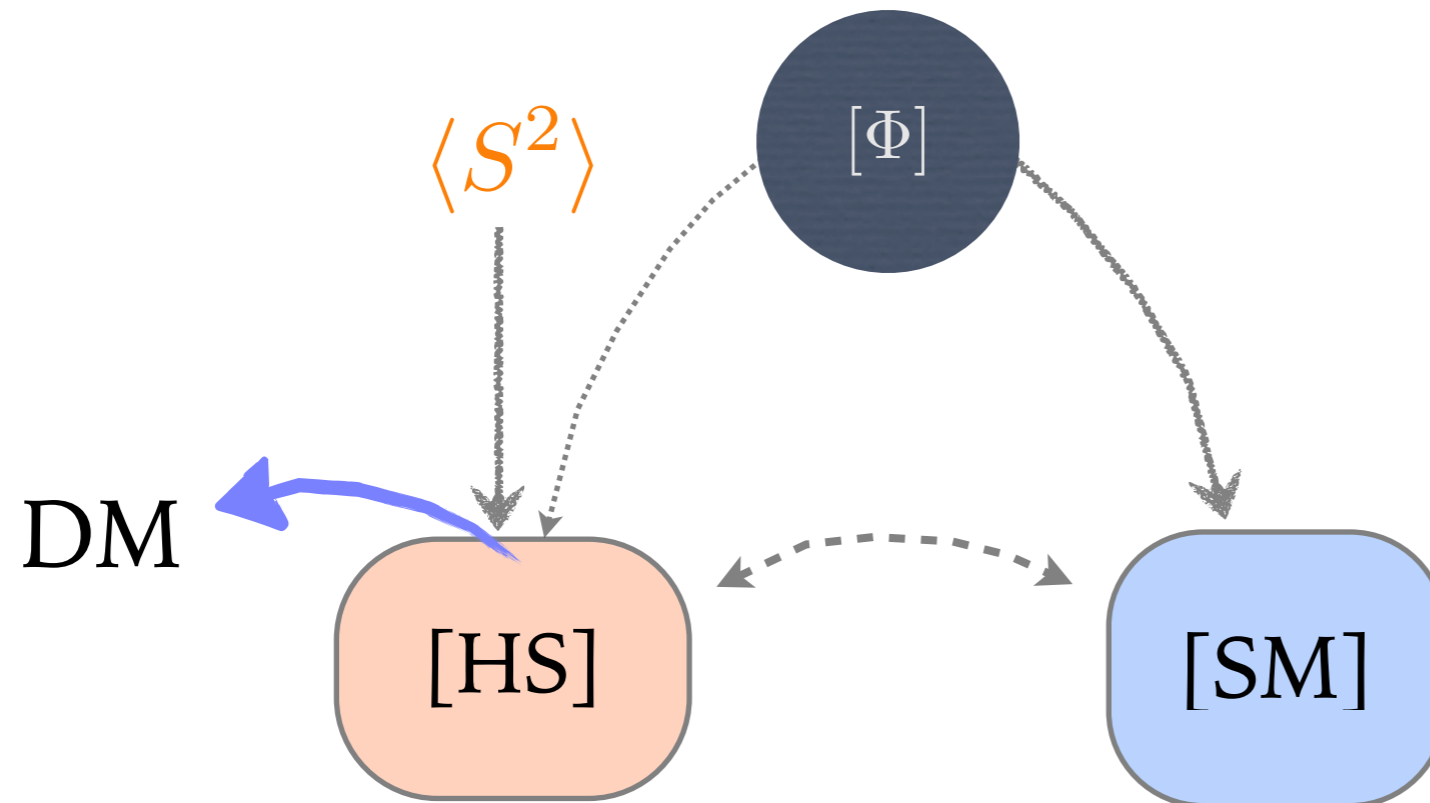
- Minimal cosmologies for dark sectors?



- **asymmetric reheating**: new signatures in decoupled sectors

DARK SECTORS

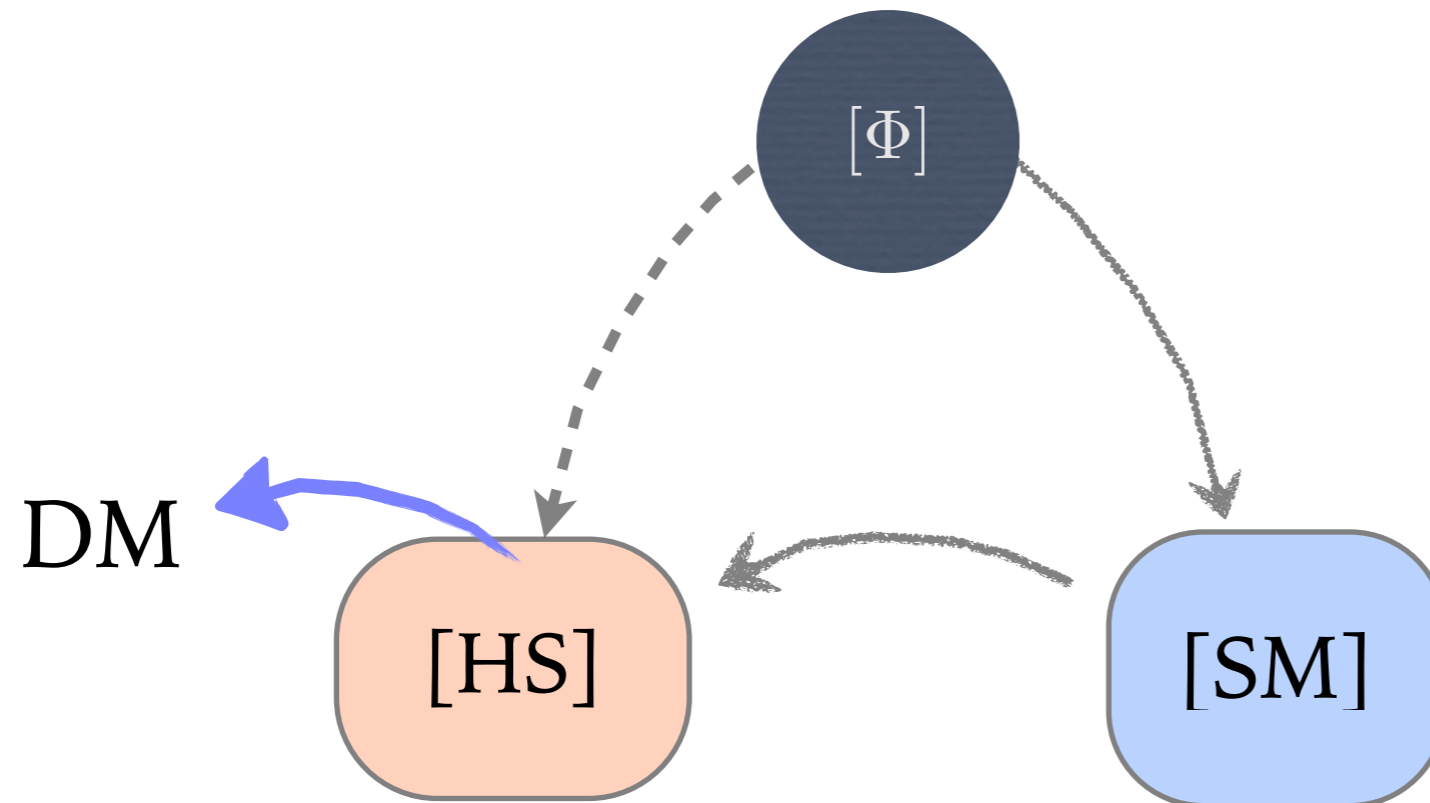
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- **asymmetric reheating**: new signatures in decoupled sectors
- seeded by **stochastic evolution**: isocurvature

DARK SECTORS

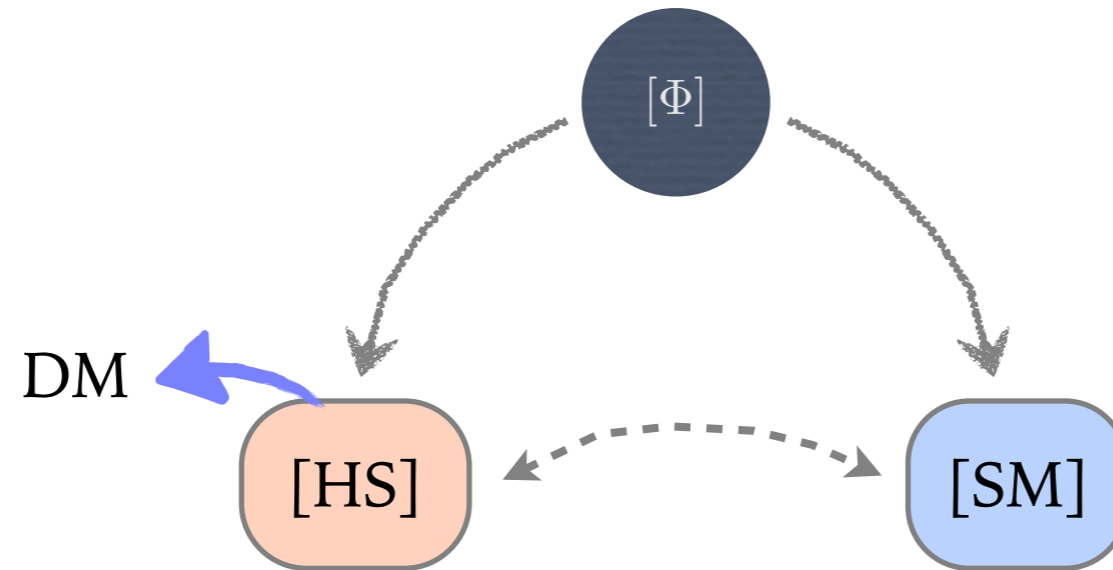
- Minimal cosmologies for dark sectors?



- **asymmetric reheating**: new signatures in decoupled sectors
- seeded by **stochastic evolution**: isocurvature
- **from Standard Model**: predictive; interesting sizes of couplings

MINIMAL COSMOLOGY I: ASYMMETRIC REHEATING

- reheating populates HS, SM directly



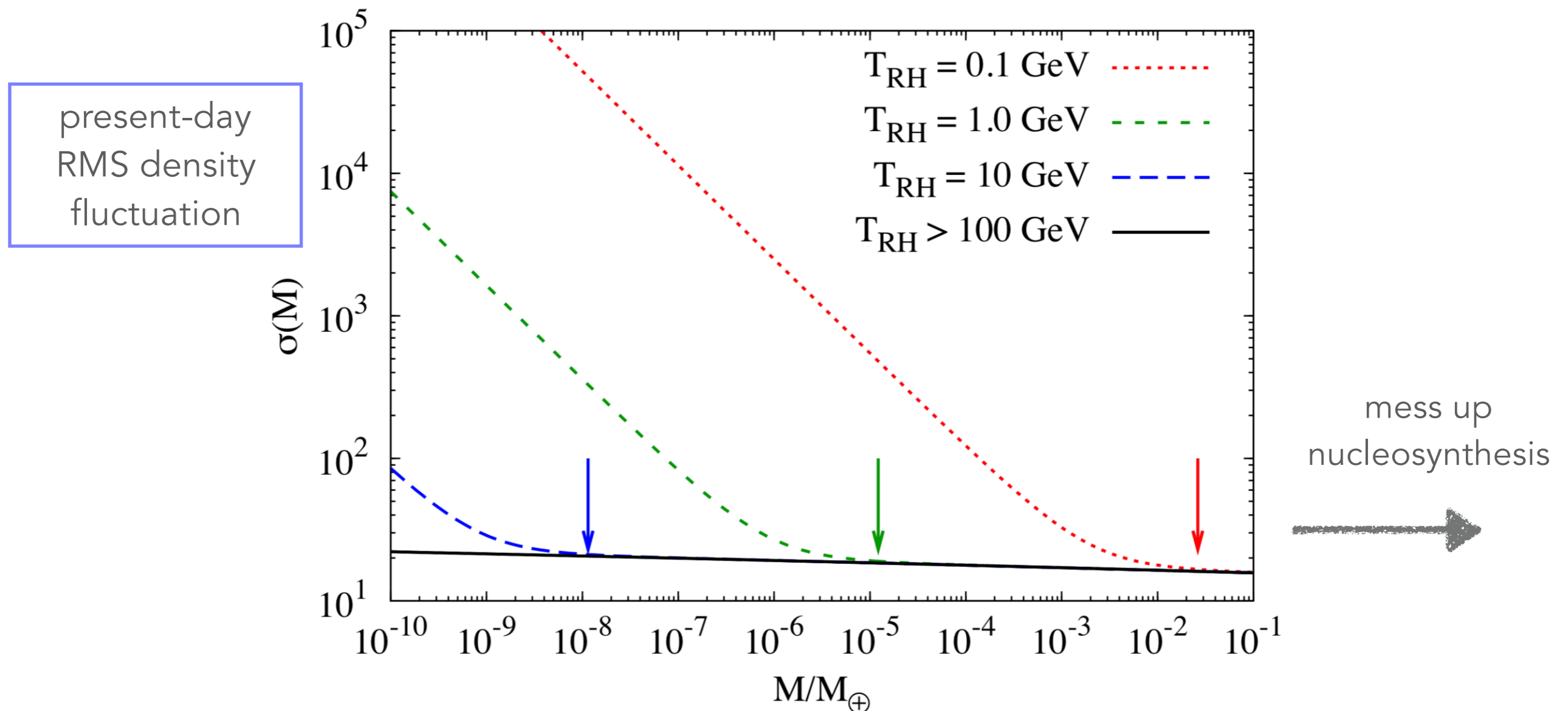
- generally $T_{HS} \neq T_{SM}$
- coupling sectors to same physics in UV necessarily implies interactions
- how important is scattering? Depends on whether m_ϕ is light compared to T_{RH}

FATE OF A DECOUPLED RADIATION BATH

- What happens to the entropy in a dark radiation bath?
 - Cosmologically allowable fates depend on mass of lightest particle(s)
 - if sufficiently light, can be stable: N_{eff}
 - if too massive: must decay
 - BBN or later: signals!
 - pre-BBN? Can easily come to dominate expansion of universe: **early matter-dominated era**

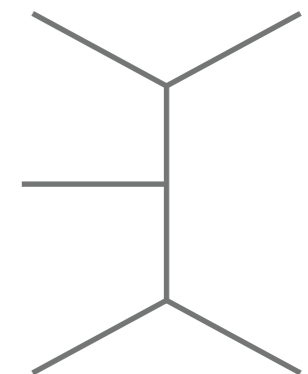
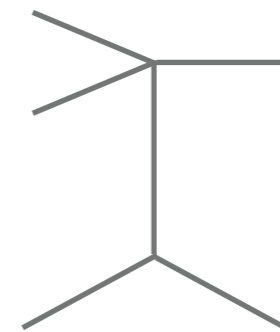
DECOUPLED DARK SECTORS: EARLY MATTER DOMINATION

- Pre-BBN slowdown in expansion rate gives matter a head start on clustering on very small scales:



EARLY CANNIBAL DOMINATION

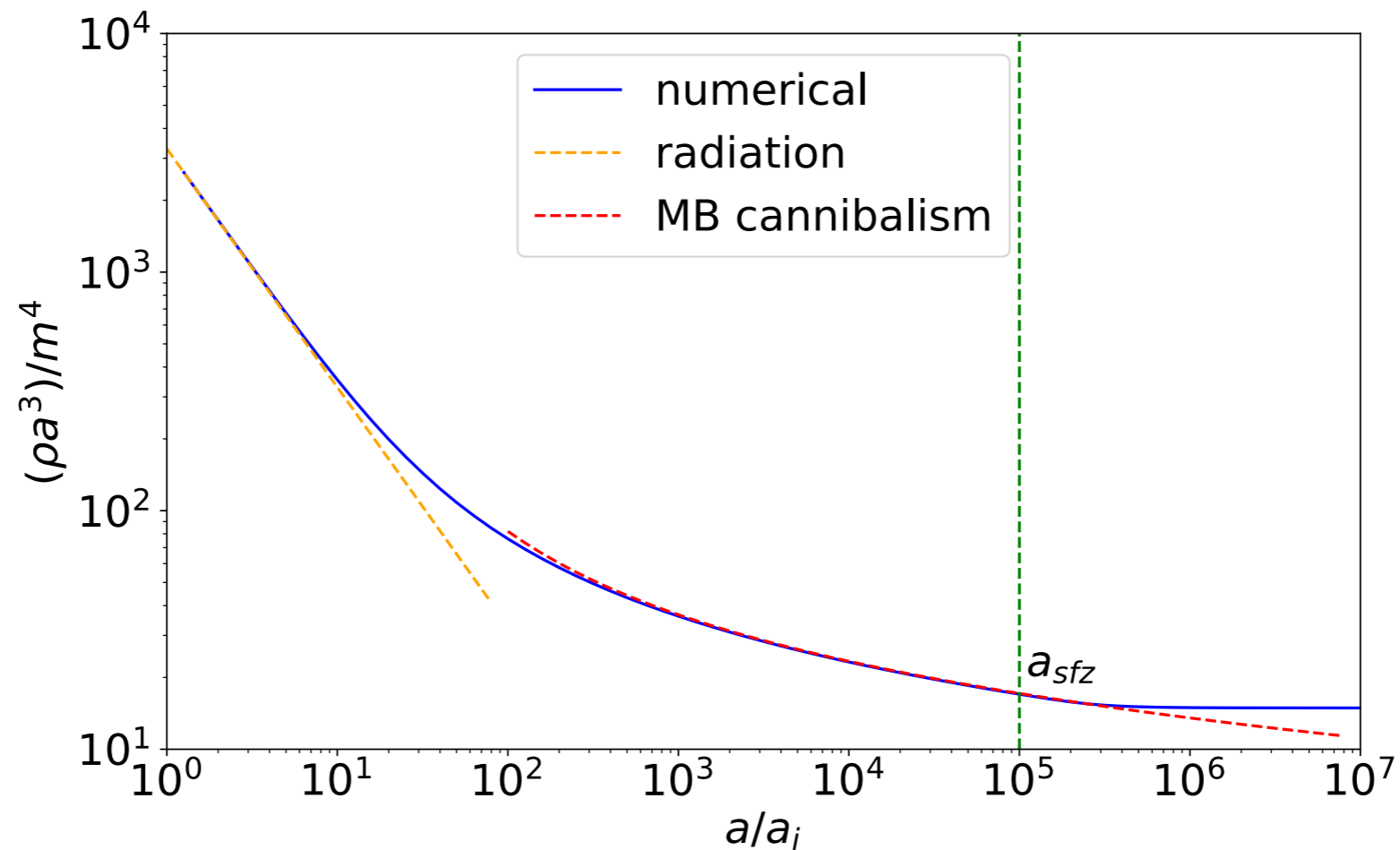
- But relic dark radiation bath might not act as simply matter: may have **interesting self-interactions**
- **Cannibalism**: number-changing self-interactions can keep particle in thermal equilibrium after it becomes non-relativistic
 - ϕ^4 theory exhibits cannibalism
 - hidden glueballs



EARLY CANNIBAL DOMINATION

- Cannibals cool down slowly:

radiation:
 $\rho \sim 1/a^4$



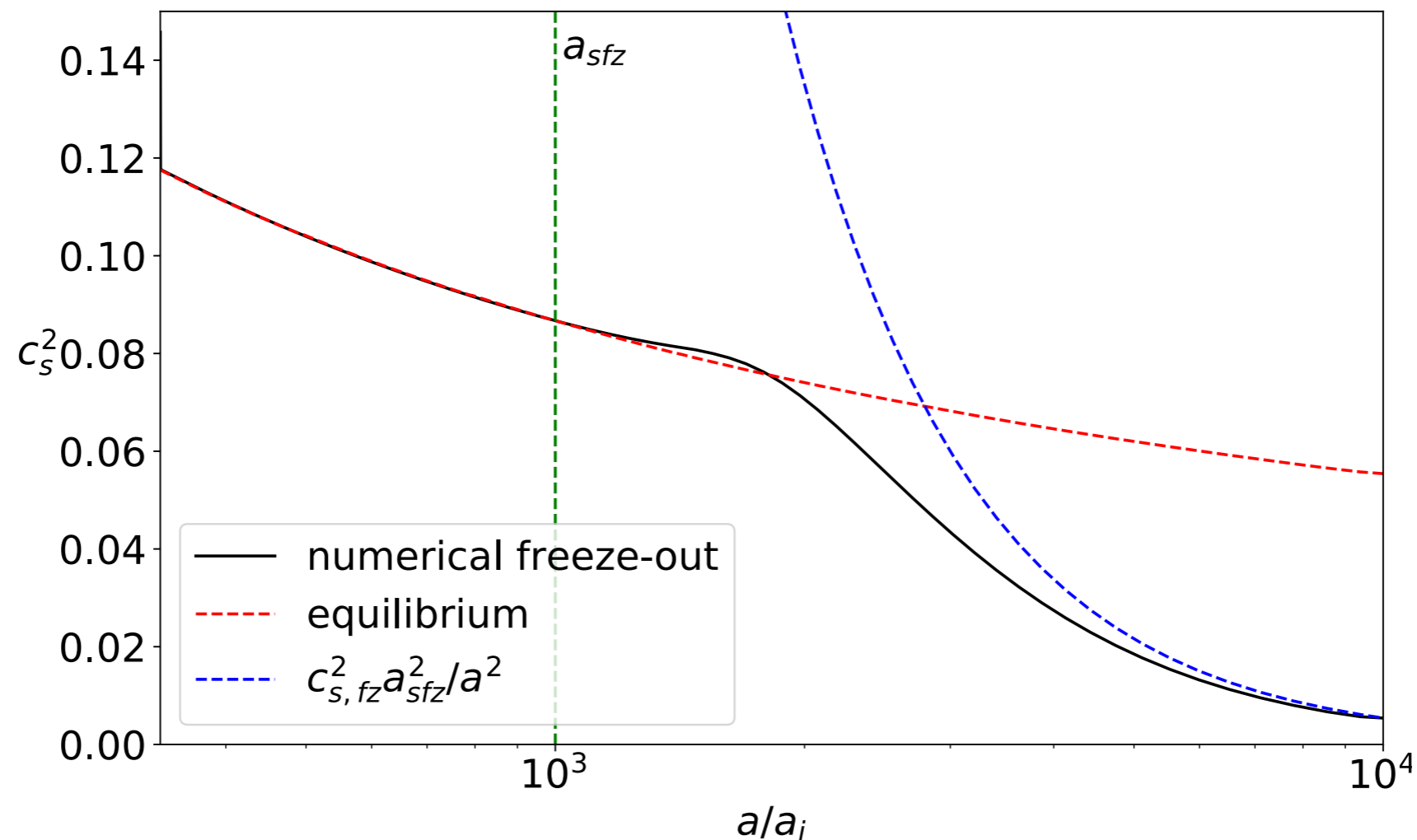
cannibal:
 $\rho \sim 1/(a^3 \ln a)$

matter:
 $\rho \sim 1/a^3$

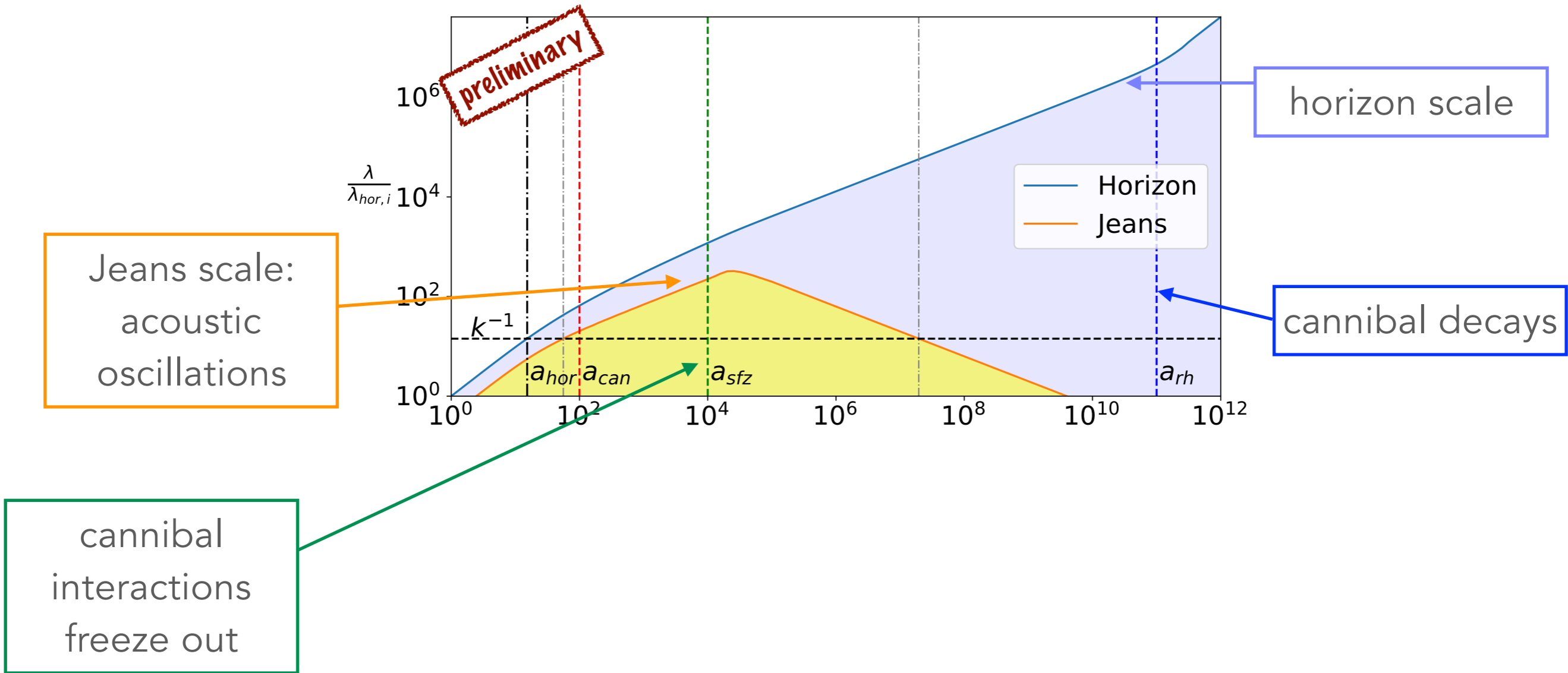
$$\frac{a_{sfz}}{a_{10m}} \sim \text{few} \times 10^4 \alpha_c^{2/3} \left(\frac{\text{GeV}}{m} \right)^{2/9}$$

EARLY CANNIBAL DOMINATION

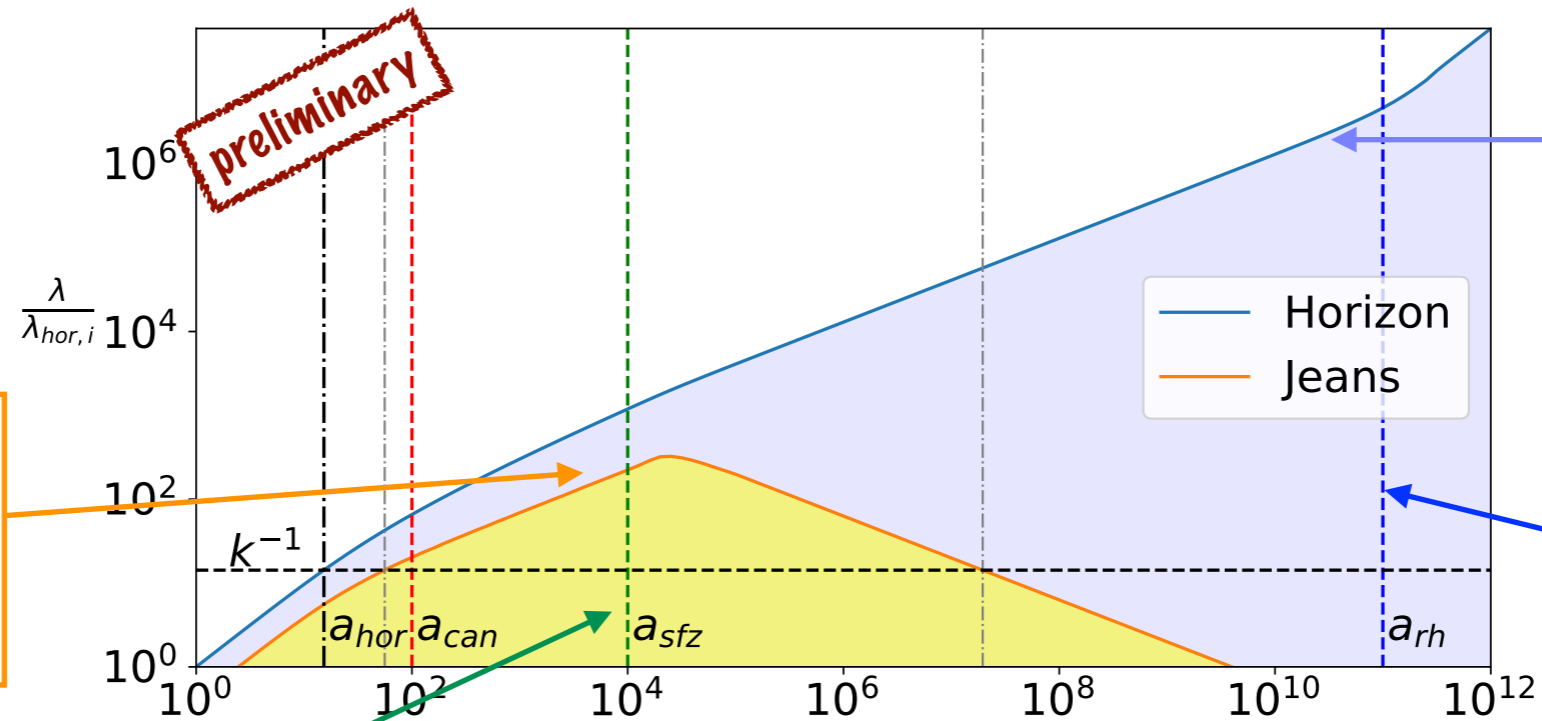
- Imprint of cannibal self-interactions in the distribution of dark matter on very small scales?
- Difficulty cooling → **pressure support**:



EARLY CANNIBAL DOMINATION

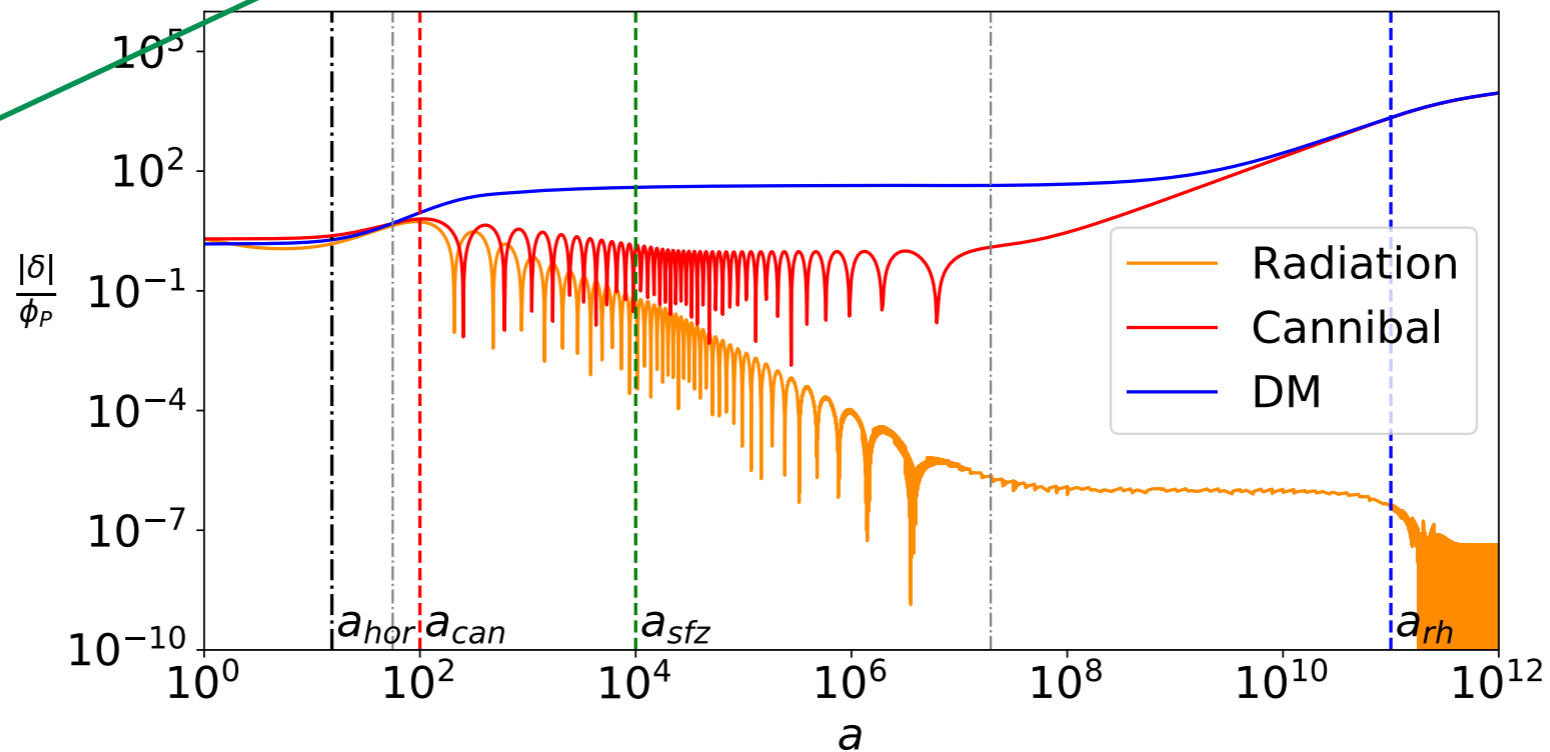


EARLY CANNIBAL DOMINATION

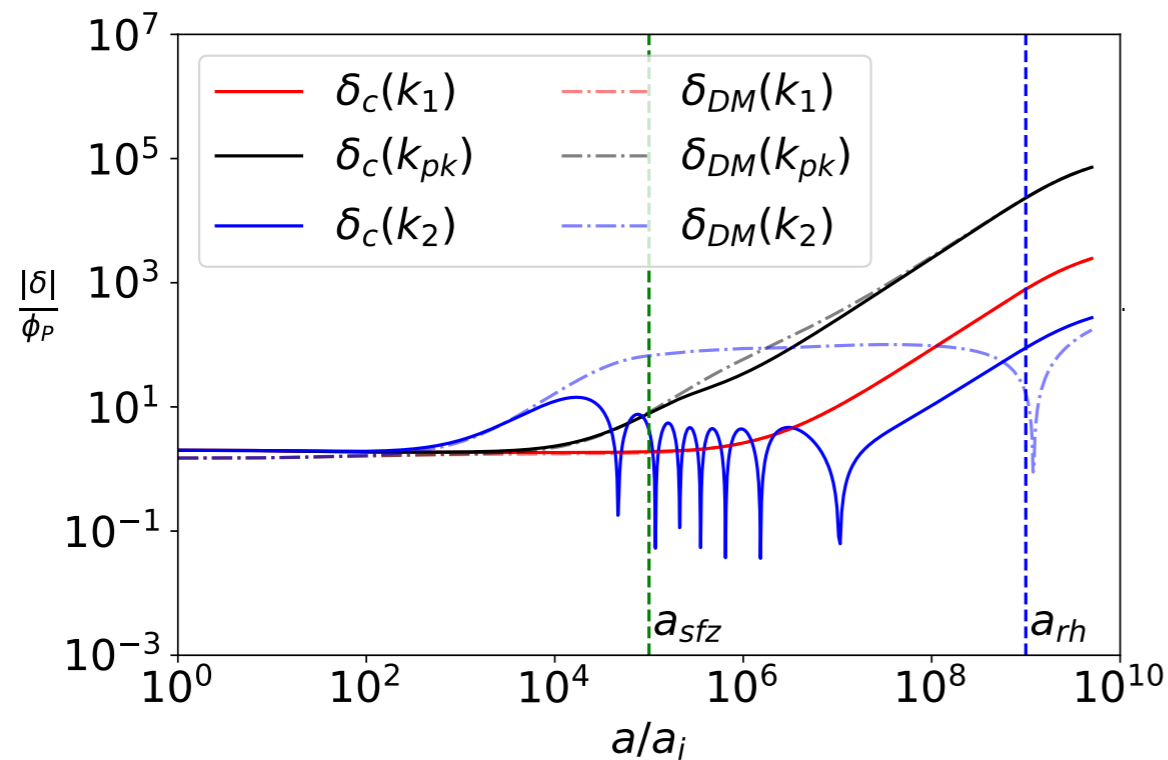
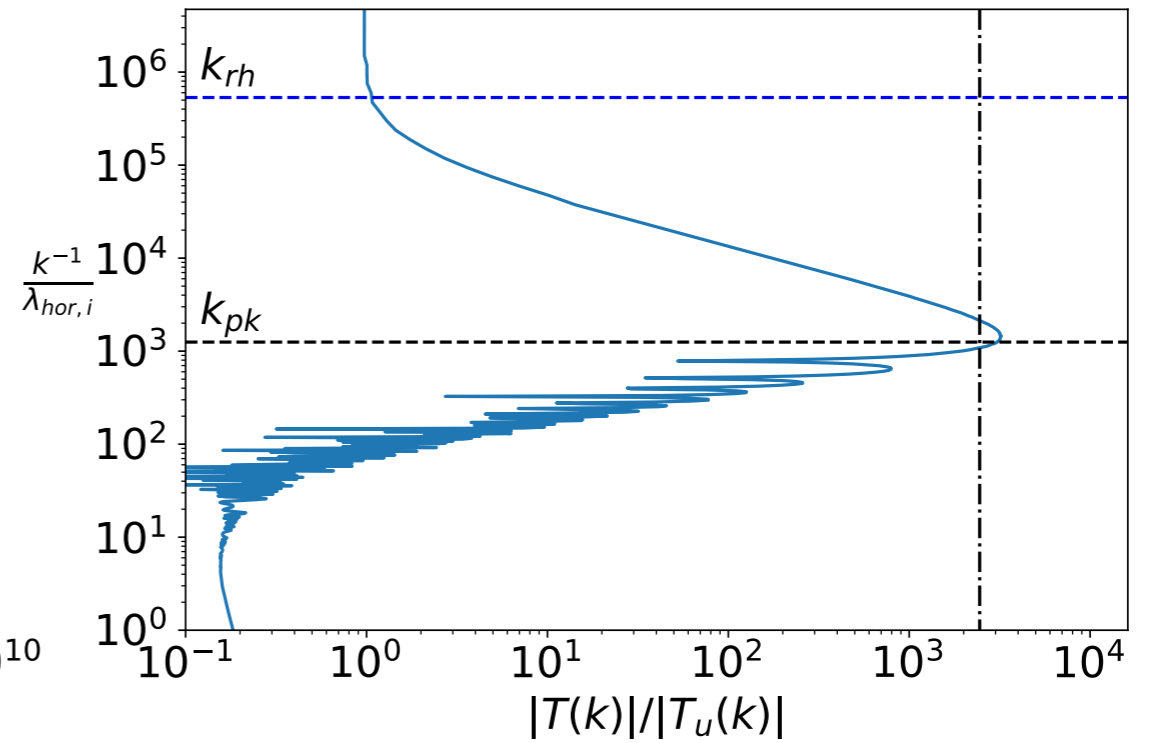
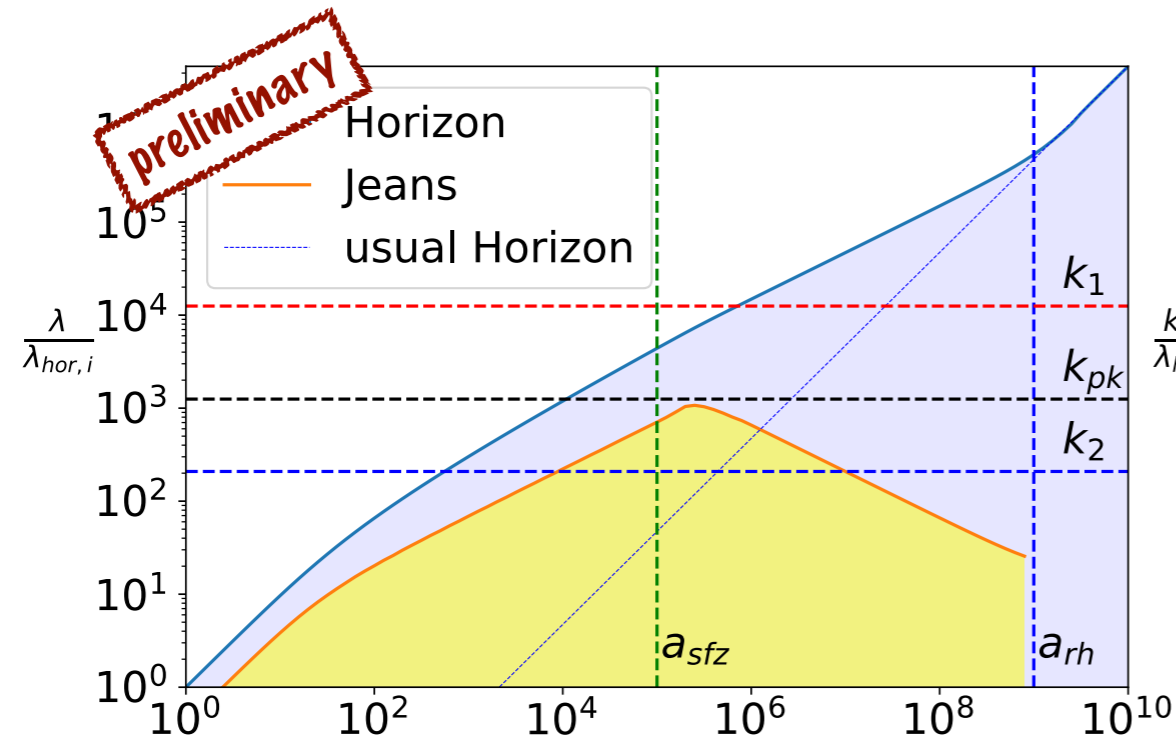


Jeans scale:
acoustic
oscillations

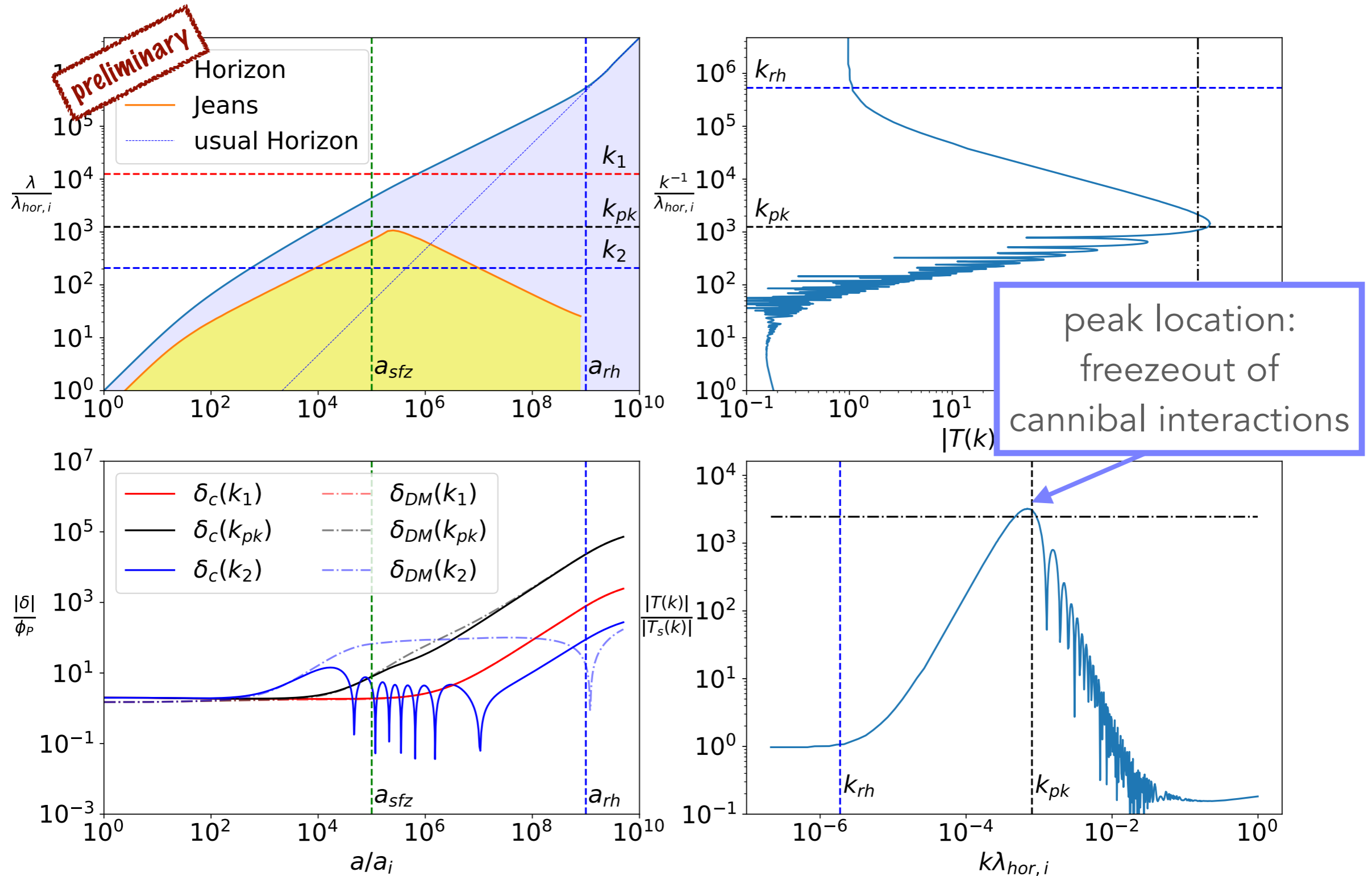
cannibal
interactions
freeze out



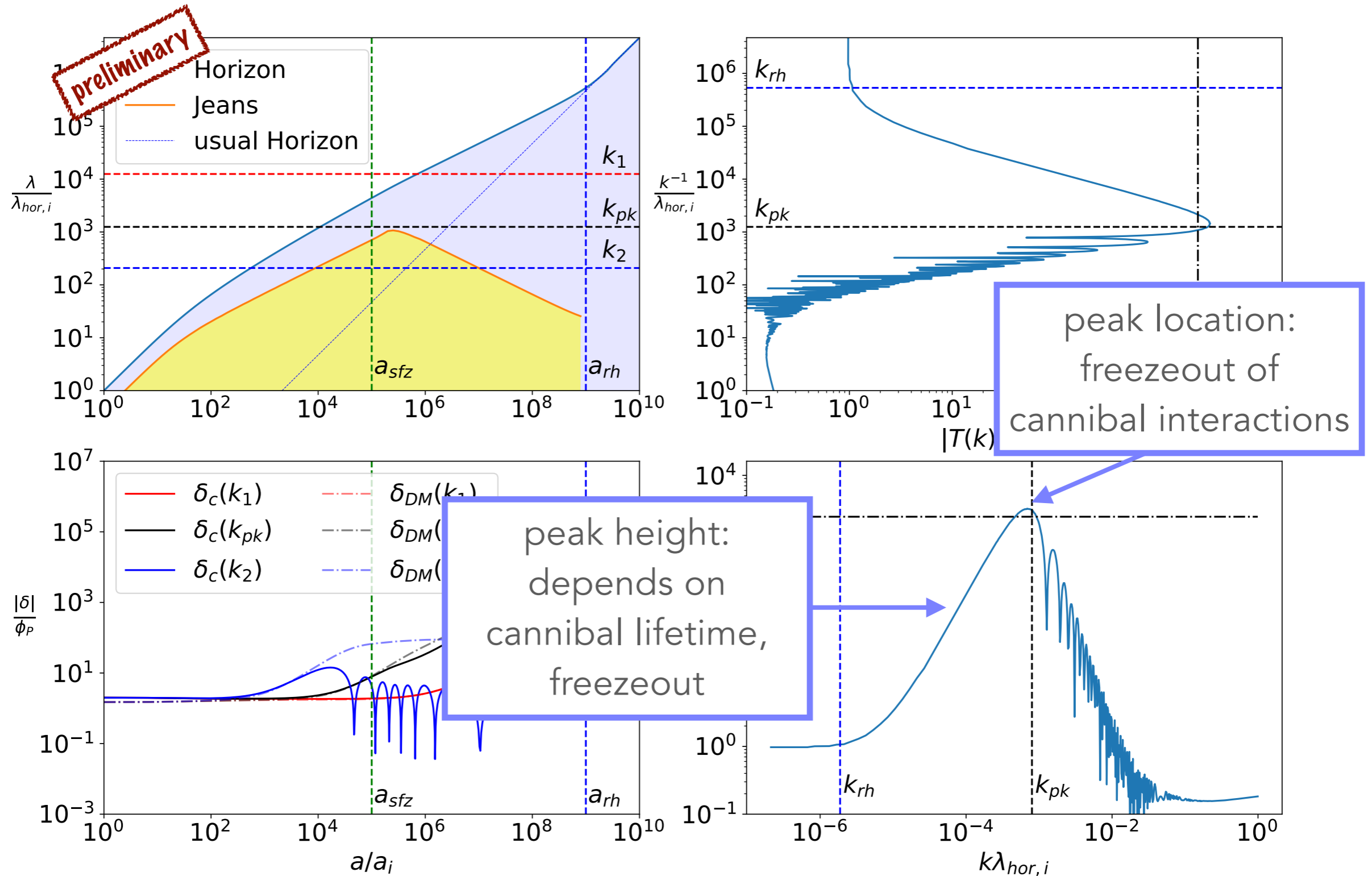
EARLY CANNIBAL DOMINATION



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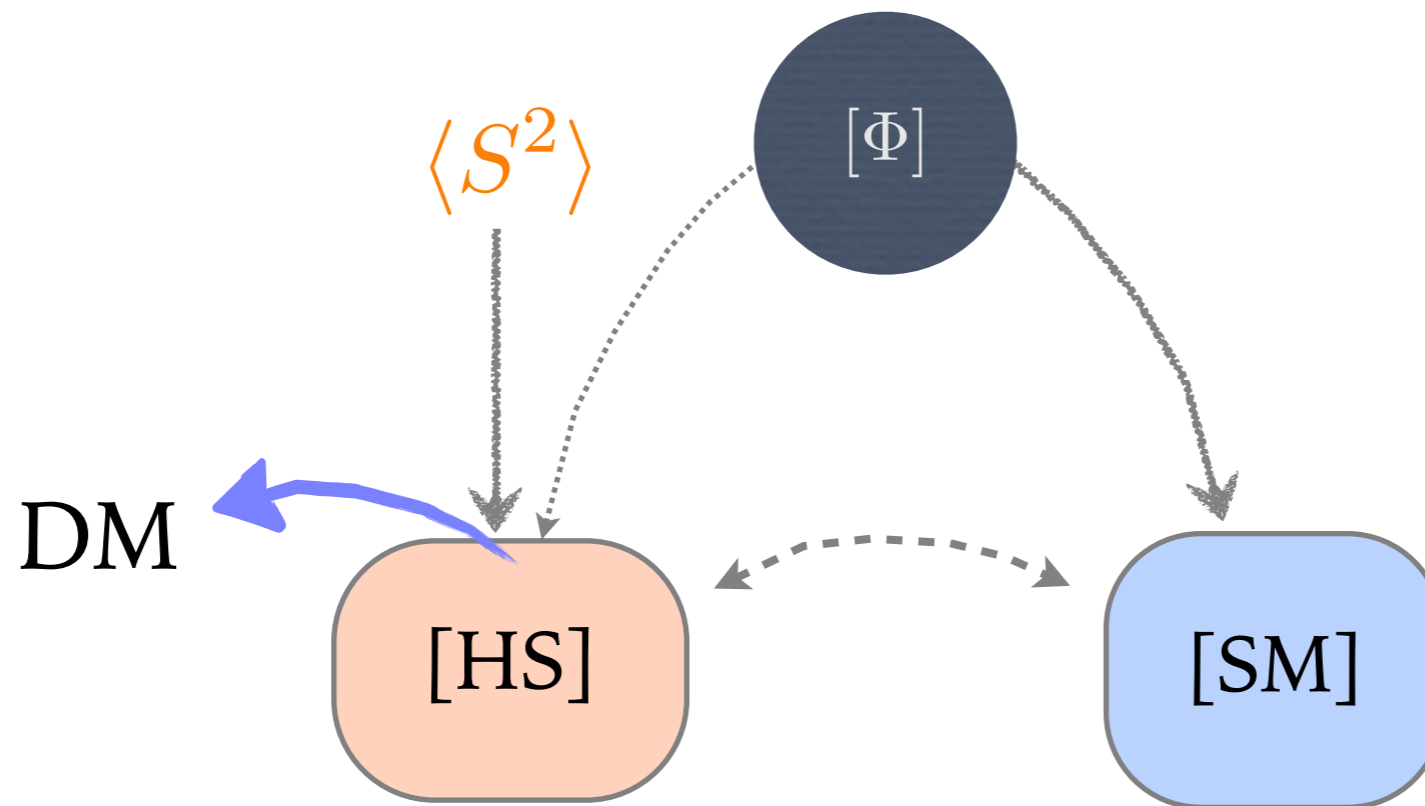


EARLY CANNIBAL DOMINATION



MINIMAL COSMOLOGY II: SPECTATOR DESCENT

- Radiation bath descended from stochastic vev:



- one major motivation for scalars in hidden sectors:
spontaneously break dark gauge groups

SPECTATORS WITH CONTINUOUS SYMMETRIES

- Evolution of scalar vev χ described by Fokker-Planck equation for probability distribution $\rho(\chi)$
- Generalize to field in linear rep of continuous symmetry:

$$\frac{\partial \rho}{\partial t} = \frac{1}{3H} \left[\rho \frac{\partial^2 V}{\partial \chi^2} + \frac{\partial V}{\partial \chi} \frac{\partial \rho}{\partial \chi} \right] + \frac{H^3}{8\pi^2} \frac{\partial^2 \rho}{\partial \chi^2}$$

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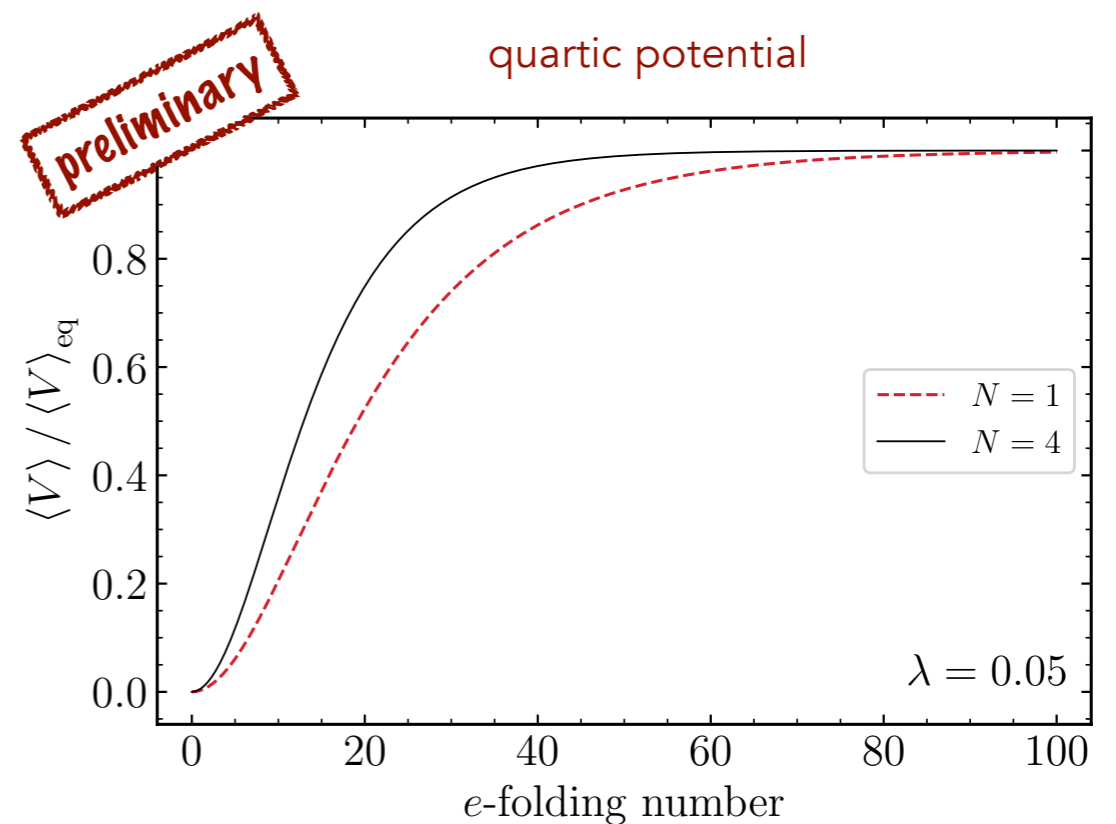
- or in terms of the magnitude of the vev alone:

$$\rho_{\text{eff}}(\chi) \equiv \chi^{N-1} \rho(\chi) \Omega^{N-1}$$

$$\frac{8\pi^2}{H^3} \frac{\partial \rho_{\text{eff}}}{\partial t} = \frac{8\pi^2}{3H^4} \left(\frac{\partial^2 V}{\partial \chi^2} + \frac{(N-1)}{\chi^2} \right) \rho_{\text{eff}} + \frac{8\pi^2}{3H^4} \left(\frac{\partial V}{\partial \chi} - \frac{(N-1)}{\chi} \right) \frac{\partial \rho_{\text{eff}}}{\partial \chi} + \frac{\partial^2 \rho_{\text{eff}}}{\partial \chi^2}$$

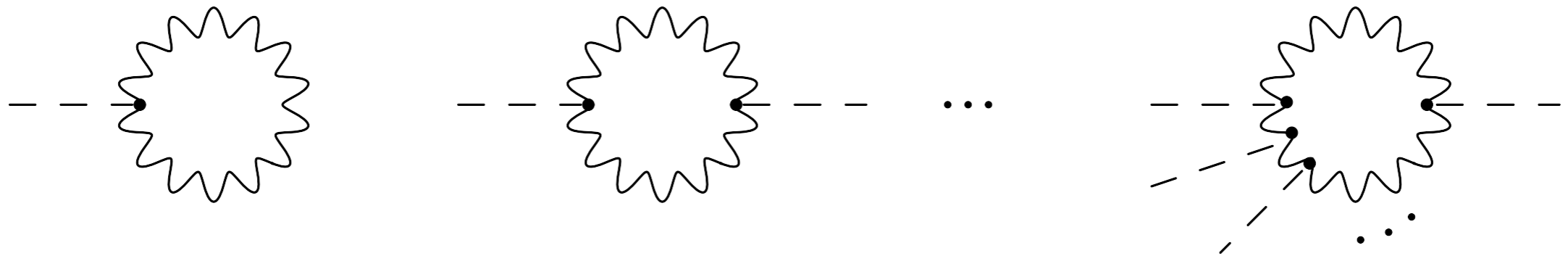
SPECTATORS WITH CONTINUOUS SYMMETRIES

- Consequences of enlarged field space:
 - larger mean vevs, energy densities
 - quartic: $\langle \chi^2 \rangle \sim \sqrt{N} H^2$
 $\langle V \rangle \sim N H^4$
- faster approach to equilibrium distribution



STOCHASTIC SPECTATOR FIELDS

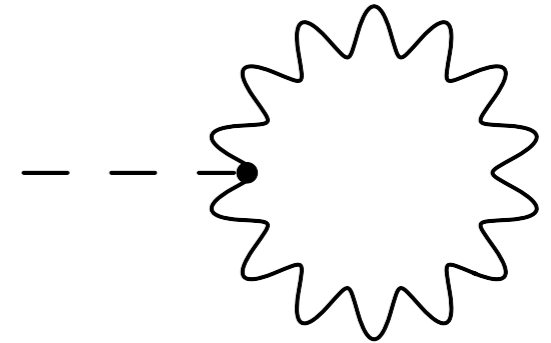
- ▶ What about unitary gauge?
- ▶ New counter-term needed to remove spurious UV divergences:



$$\int \frac{d^4 k}{(2\pi)^4} \frac{k^2}{k^2 - m^2} \sim i\Lambda_{UV}^4 \quad \Rightarrow \quad \mathcal{L}_{ct} = (N - 1)\Lambda_{UV}^4 \ln(\chi)$$

STOCHASTIC SPECTATOR FIELDS

- What happens during inflation?
 - Stochastic approach:



H 

m 


$$\int \frac{d^4 k}{(2\pi)^4} \frac{k^2}{k^2 - m^2} = i\Lambda_{UV}^4 - i\Lambda_{IR}^4$$

canceled by counterterm

finite residual contribution

- with IR cutoff (subhorizon four-volume)⁻¹: $\delta L_{ug} = (N - 1) \frac{3H^4}{8\pi^2} \ln(\chi)$

STOCHASTIC SPECTATOR FIELDS

- This adds new terms to the Fokker-Planck equation:

$$\frac{8\pi^2}{H^3} \frac{\partial \rho_{\text{eff}}}{\partial t} = \frac{8\pi^2}{3H^4} \left(\frac{\partial^2 V}{\partial \chi^2} + \frac{(N-1)}{\chi^2} \right) \rho_{\text{eff}} + \frac{8\pi^2}{3H^4} \left(\frac{\partial V}{\partial \chi} - \frac{(N-1)}{\chi} \right) \frac{\partial \rho_{\text{eff}}}{\partial \chi} + \frac{\partial^2 \rho_{\text{eff}}}{\partial \chi^2}$$

- But this is exactly the Fokker-Planck equation that governs the PDF for the radial mode of an N -dimensional field $\vec{\chi}$
-

STOCHASTIC SPECTATOR FIELDS

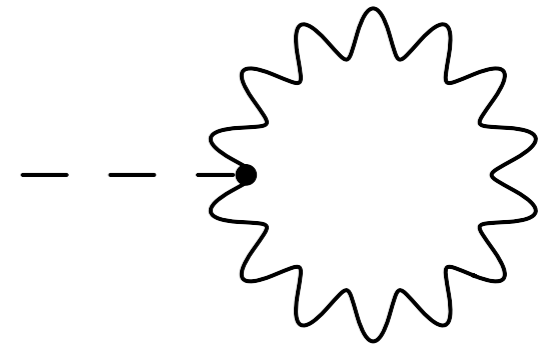
- ▶ As the vev gets larger, so does the mass gap:

m 

H 



$$\int \frac{d^4 k}{(2\pi)^4} \frac{k^2}{k^2 - m^2}$$

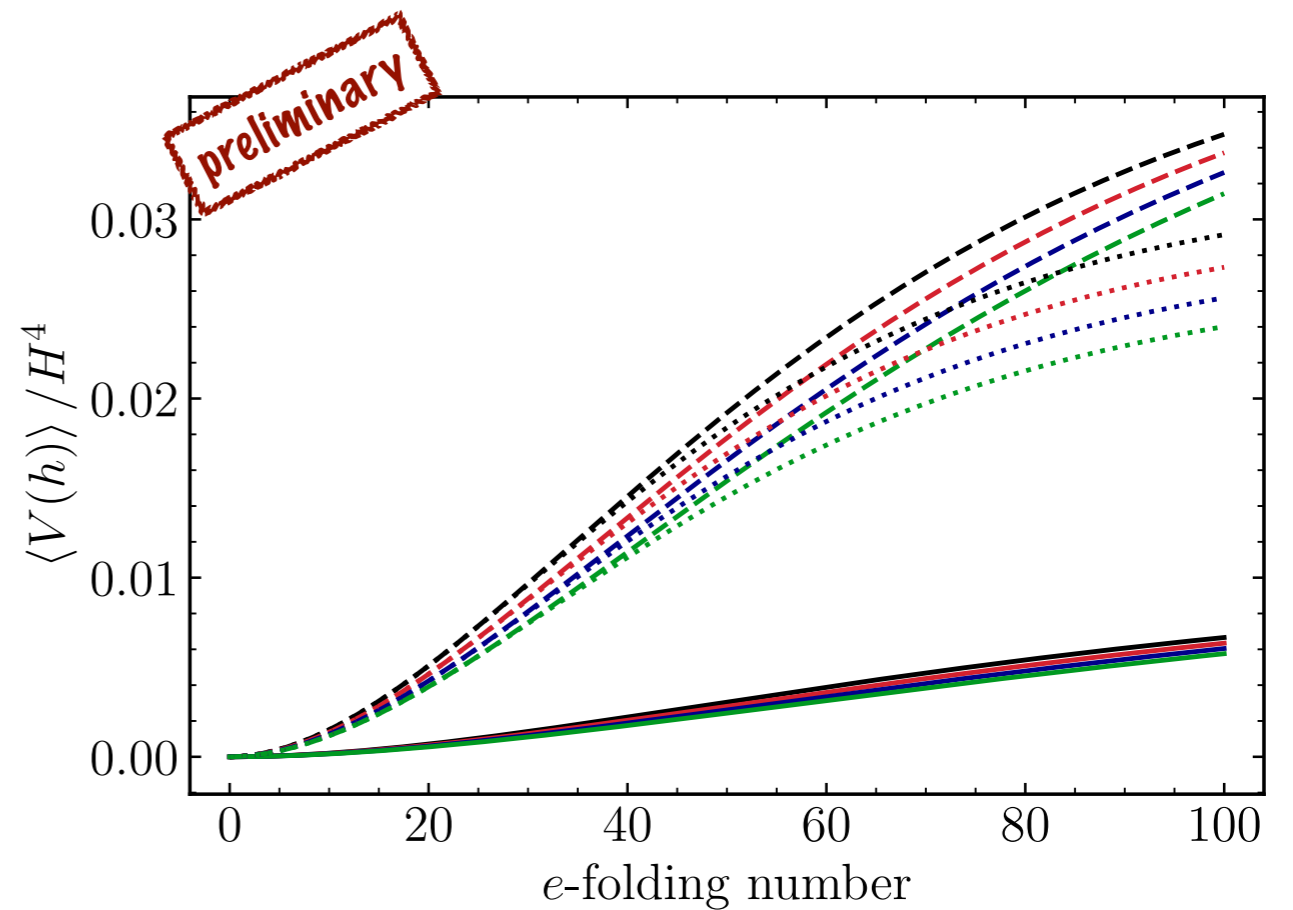
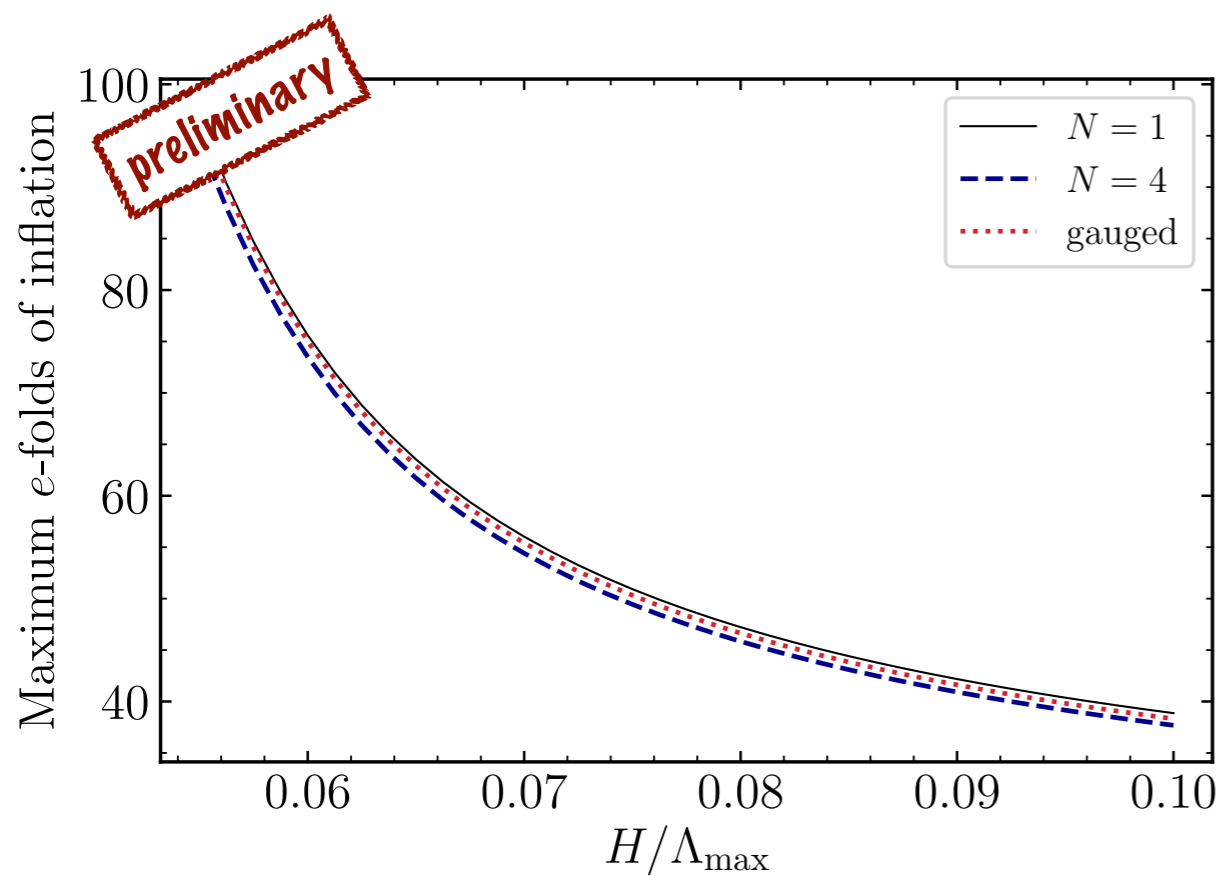


- ▶ \Rightarrow expect spectators with a gauge symmetry to smoothly interpolate from N -d to 1-d

STOCHASTIC SPECTATOR FIELDS

► Apply to SM Higgs:

$$V(h) = -b_0 \ln \left(\frac{H^2 + h^2}{\sqrt{e} \Lambda_{\max}^2} \right) \frac{h^4}{4}$$



SUMMARY AND CONCLUSIONS

- Many possible dark thermal histories
 - most of them do **not** predict terrestrially relevant interaction rates with SM particles
 - look instead to **astrophysics/cosmology** for signals
- **Decoupled dark sectors**
 - minimal population with asymmetric reheating, mild conditions on reheating (T_{RH}/m_ϕ)
 - early cannibal domination: novel imprint of dark particle interactions in small-scale structure
- **Stochastic spectators**
 - stochastic population depends on dimensionality of field space (linear reps)
 - recover in unitary gauge
- **Population from SM:**
 - direct detection now sensitive to **cosmic history**, not just particle content
 - predictive, fun phenomenology: sub-GeV DM, self-interacting DM, ...